

Particle physics with muons

with my personal bias...

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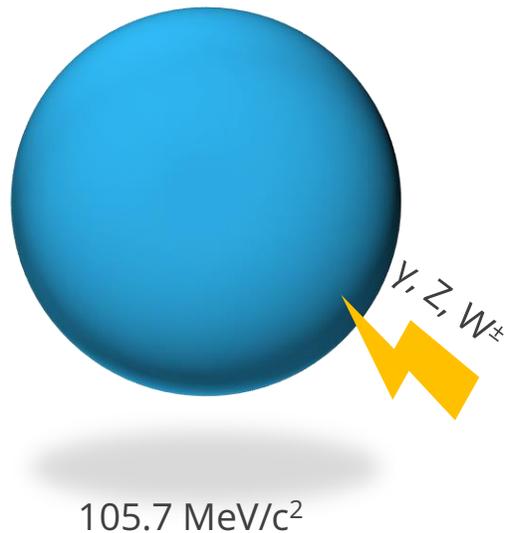
Int. Conf. on the Physics of the Two Infinities

March 30, 2023

@ Kyoto University



The Muon



2nd-gen. charged lepton

Replica of electron but with 200 times larger mass

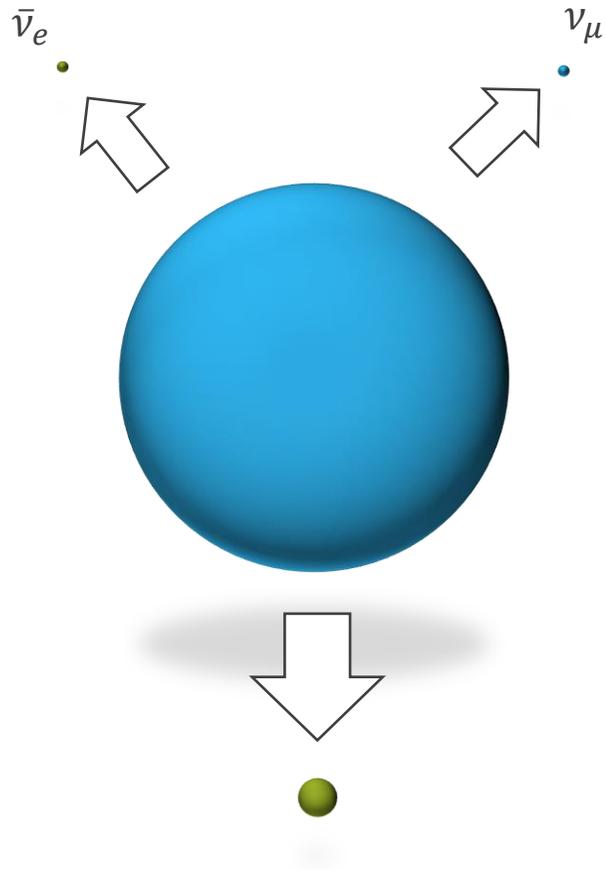
Only Higgs Yukawa coupling distinguishes e/μ.

- Gauge interactions don't (Gauge symmetry)
- [Lepton Flavor Universality](#)

We still don't know why it exists

- after 86 years from the discovery.
- *"Who ordered that?"* (Rabi)

Muons decay weakly



The first unstable elementary particle

- ▣ The beginning of **flavor physics**

Muons decay only via **weak interaction**

Lifetime: **$2.2 \mu\text{s}$**

- ▣ Long enough to manipulate and make beam

Determines Fermi constant (G_F)

- ▣ One of the most fundamental parameters of SM
- ▣ MuLan experiment @ PSI (2013) **510 ppb**

Discovery of the muon opened modern particle physics.

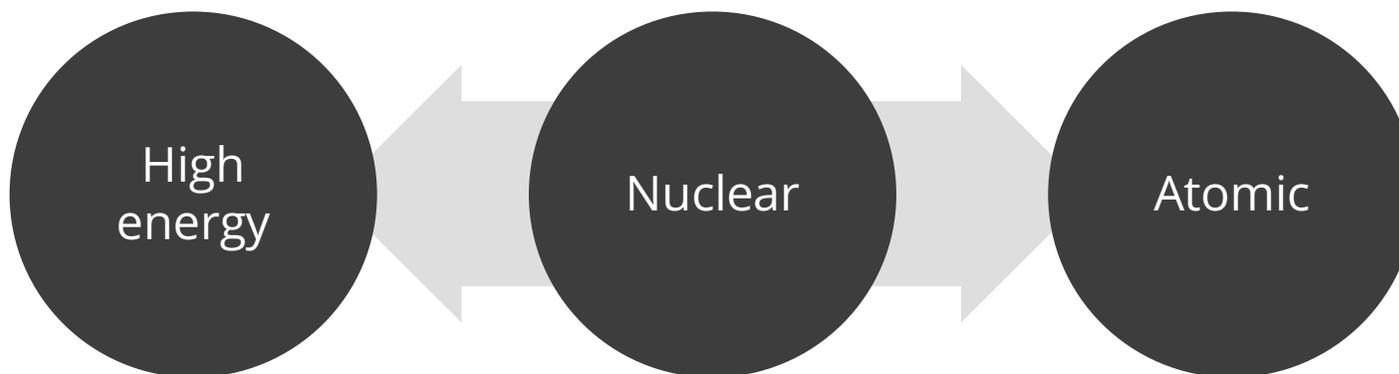
Studies of its properties played an essential role to establish SM.

Is it a legacy physics?

— No. It's still active, even **hottest** now!

Particle physics with muons

Synergies in physics & experimental techniques



Three keywords

High precision
measurements
Fight against systematics

Rare process searches
Fight with backgrounds

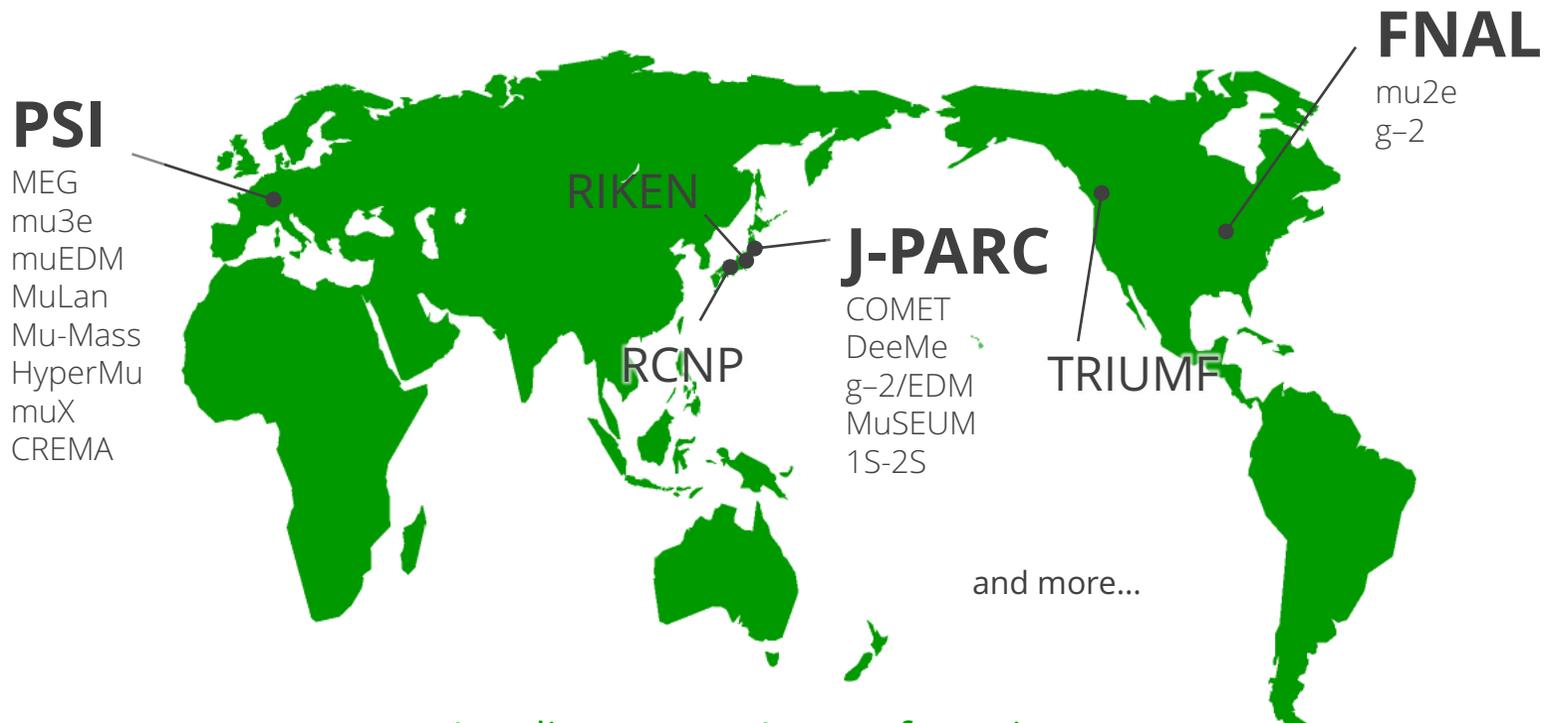
High intensity muon beams

Muon sources in the world

μ^\pm are produced from π^\pm decay

π^\pm are produced by hitting protons to a target, so μ^\pm are tertiary beam.
Therefore, **high-power proton accelerators** become muon factories.

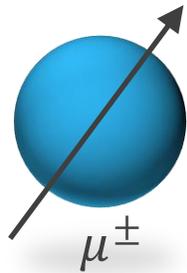
Maximum intensity: 10^8 s^{-1} (now) $\rightarrow 10^{10-11} \text{ s}^{-1}$ (in near future)



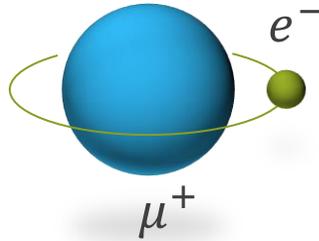
Leading meson/muon factories

Unique experimental systems

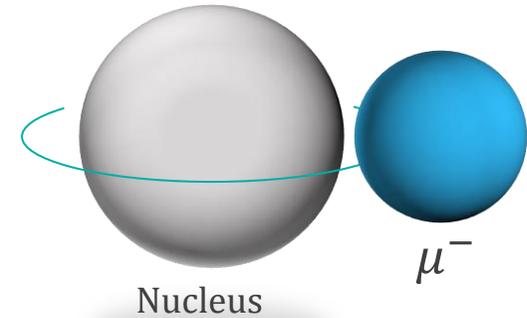
Free muon



Muonium
(Mu)



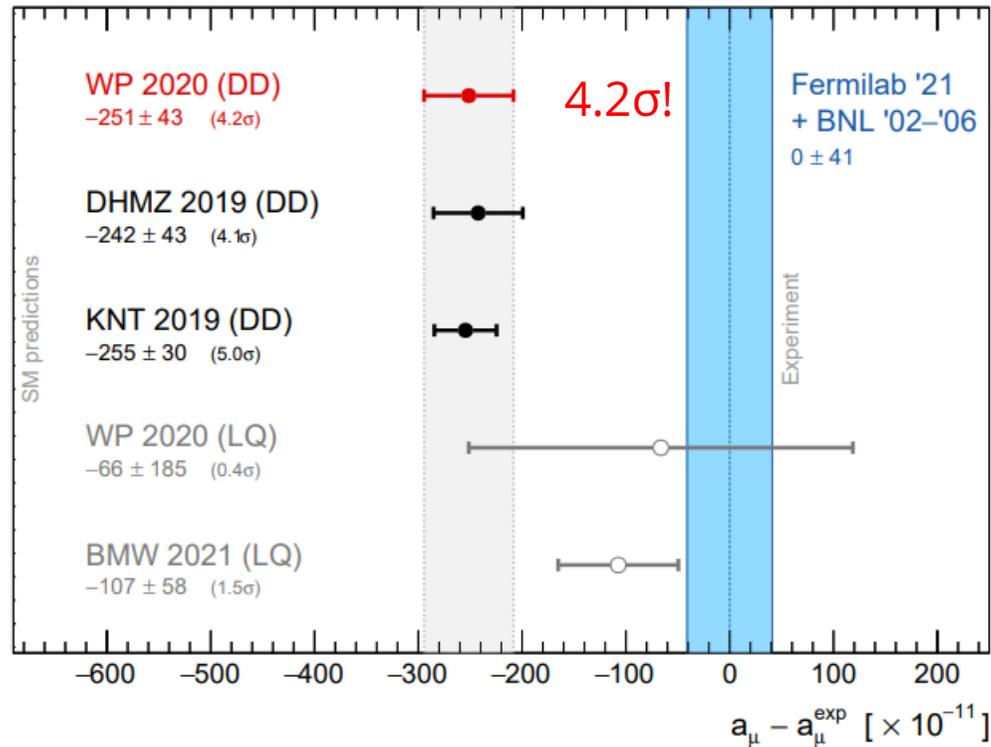
Muonic atom



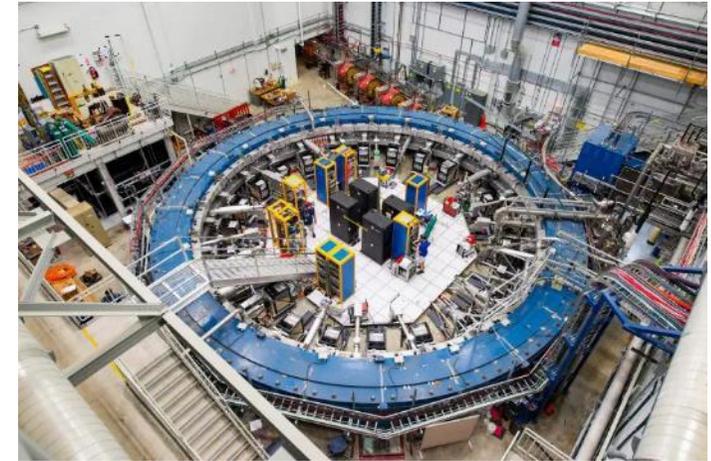
Exotic "hydrogens/atoms"

Anomaly in anomaly: $g_\mu - 2$

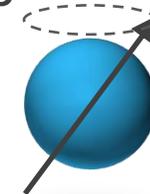
20-year long outstanding anomaly



New experiment @ FNAL confirmed the previous experimental result (2021). **350 ppb**



Measure spin precession frequency in a B field: ω_a



$$\vec{\omega} = -\frac{e}{m} \left[a_\mu \vec{B} - \left(a_\mu - \frac{1}{\gamma^2 - 1} \right) \frac{\vec{\beta} \times \vec{E}}{c} + \frac{\eta}{2} \left(\vec{\beta} \times \vec{B} + \frac{\vec{E}}{c} \right) \right]$$

We are not confident that the anomaly is a signature of NP.

- ❑ Theoretical uncertainties (hadronic), especially in view of recent lattice results.
- ❑ Unknown experimental systematic errors.

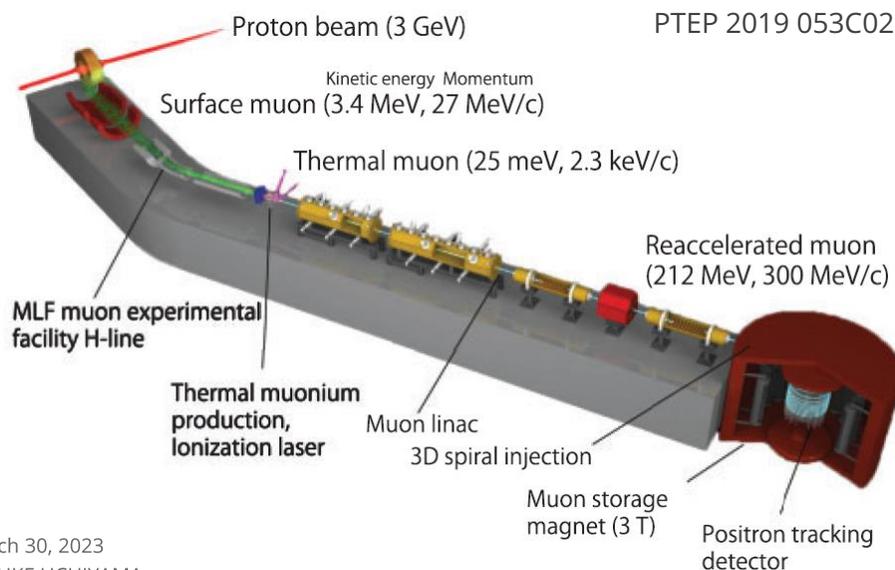
Crosscheck by independent experiments is necessary

- ❑ with different technique.
- ❑ → a new experiment at J-PARC (muon g-2/EDM), starting from 2028.

It is important to conclude even if it ends with systematic error

- ❑ because it has been a **strong guidance** for both theoretical and experimental research.

Will we be confident if it is confirmed?

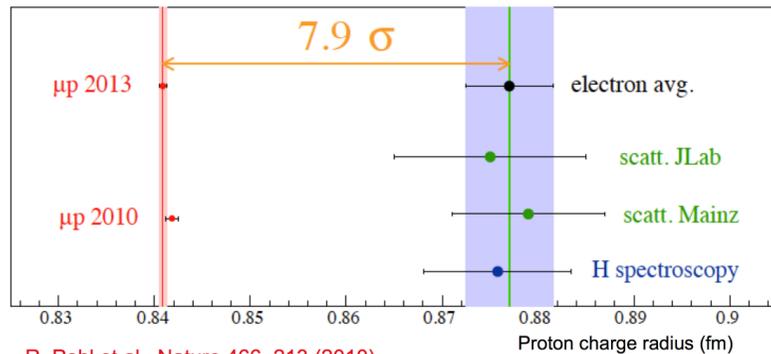
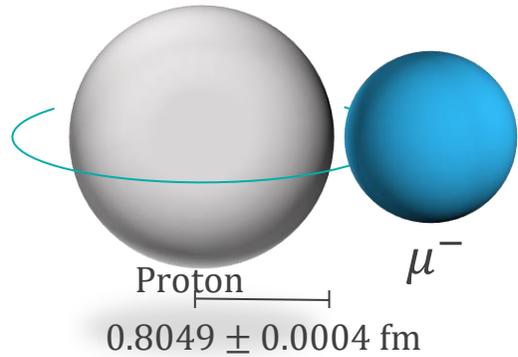


$$\vec{\omega} = -\frac{e}{m} \left[a_{\mu} \vec{B} - \left(a_{\mu} - \frac{1}{\gamma^2 - 1} \right) \frac{\vec{\beta} \times \vec{E}}{c} + \frac{\eta}{2} \left(\vec{\beta} \times \vec{B} + \frac{\vec{E}}{c} \right) \right]$$

- Low emittance μ^+ beam
- with muon cooling by muonium laser-ionization
- and muon acceleration.
- No need of electric field, avoid magic momentum.
- Measure EDM at the same time.

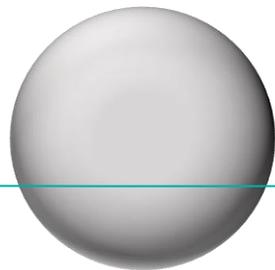
Goal: 450 ppb (stat.) + 70 ppb (sys.)

Muonic atom



R. Pohl et al., Nature 466, 213 (2010)
A. Antognini et al., Science 339, 417 (2013)

M. Kohl



Precise measurements of energy levels in muonic hydrogen

- Strict test of QED.
- 200 heavier → orbit much closer to nucleus.

Proton charge radius

- Hydrogen spectroscopy (atomic phys) + e-p scattering (nuclear/particle phys)
- New measurements with **Lamb shift ($2S-2P$) in muonic hydrogen** at PSI.
- Much more precise & accurate than with e.

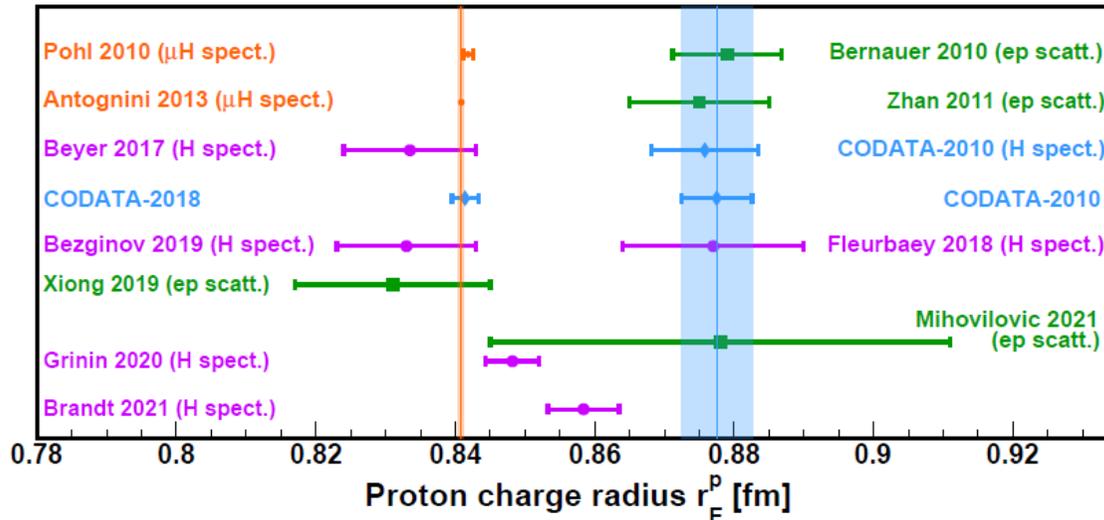
Bohr radius **200** times smaller,
200³ times sensitive to p radius!

Big surprise!



Recent status

W. Xiong, C. Peng, arXiv:2302.1381



PDG 2022

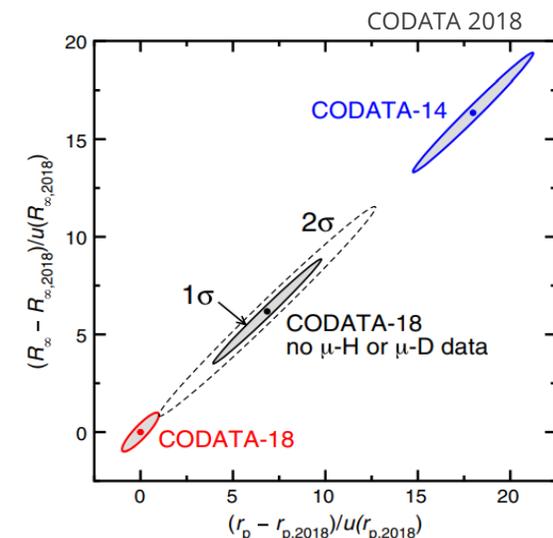
However, reflecting the new electronic measurements, the 2018 CODATA, TIESINGA 21, recommended value is 0.8414(19) fm, and the puzzle appears to be resolved.

Experts don't consider it fully resolved until they understand how and where these differences come from.

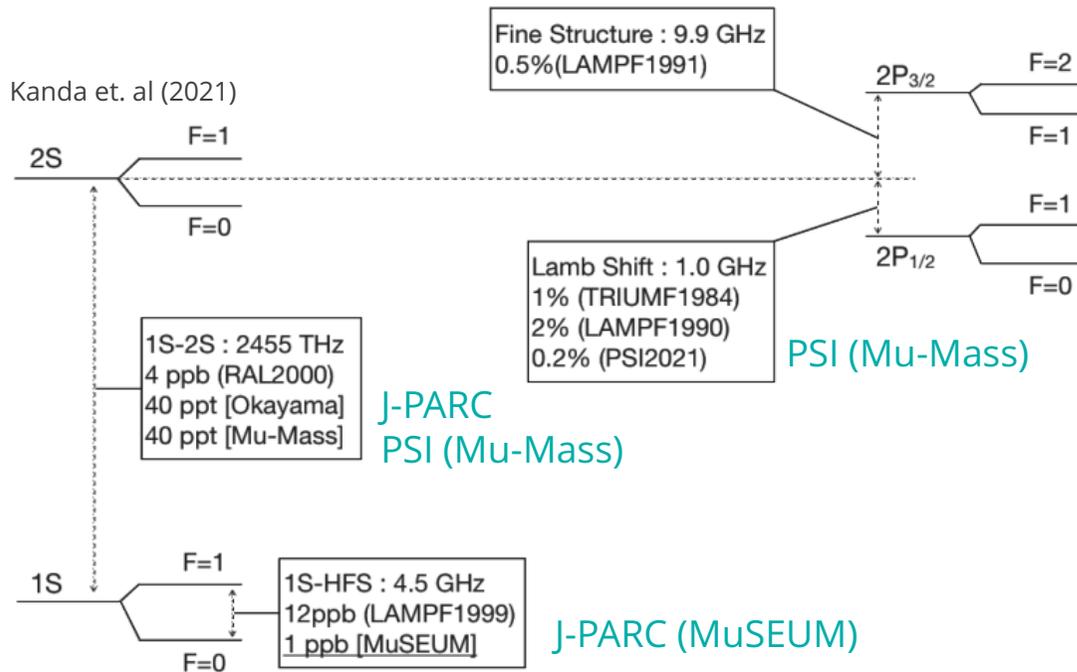
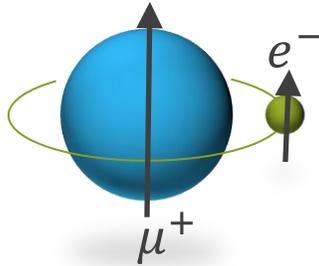
Proton radius puzzle is now somehow solved.

- New experiments & analyses reproduced the results with muonic hydrogen.
- Remind us the importance of experiments with different system.
- Input to the determination of Rydberg constant (R_∞),
- which is now the 2nd most precise constant to date.

1.9×10^{-3} ppb



Muonium



Pure leptonic “hydrogen”

- Enable precise test of electro-weak.
- Free from form factor (finite size) of proton.
- Measure energy levels
- with laser spectroscopy developed in atomic physics.

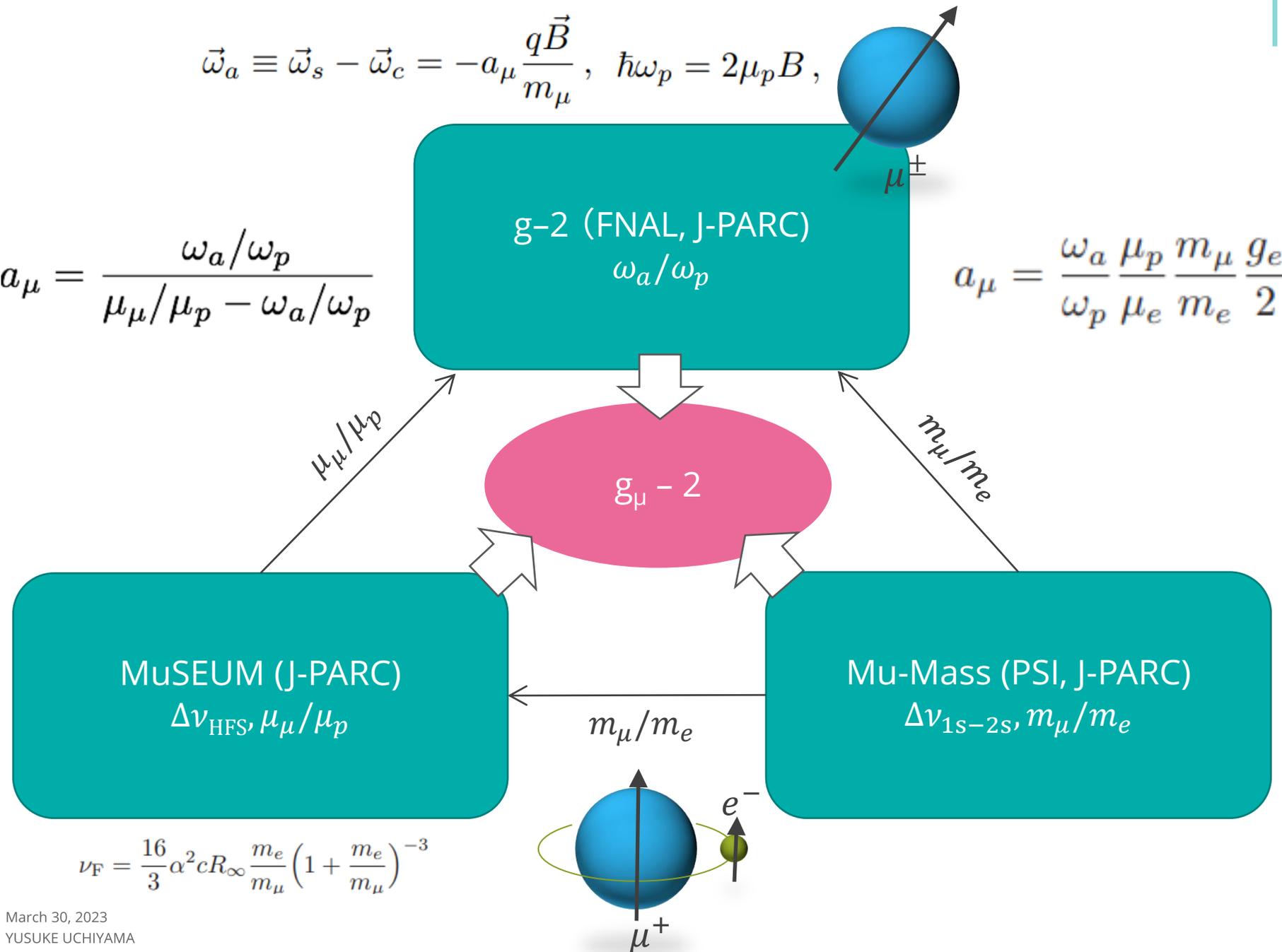
High precision measurements are now possible

- with high-intensity muon beams
- and advanced laser technologies.
- (Alternative) determination of fundamental physics constants: α, R_∞, m_μ
- Precise test of QED.

$$\vec{\omega}_a \equiv \vec{\omega}_s - \vec{\omega}_c = -a_\mu \frac{q\vec{B}}{m_\mu}, \quad \hbar\omega_p = 2\mu_p B,$$

$$a_\mu = \frac{\omega_a/\omega_p}{\mu_\mu/\mu_p - \omega_a/\omega_p}$$

$$a_\mu = \frac{\omega_a \mu_p m_\mu g_e}{\omega_p \mu_e m_e 2}$$



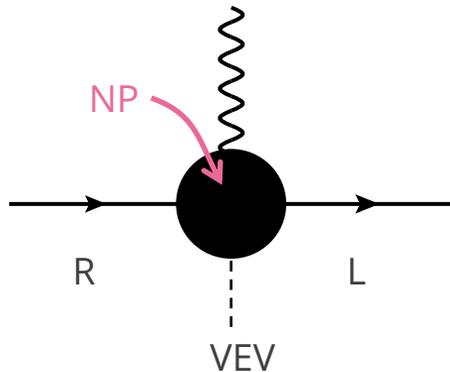
$$\nu_F = \frac{16}{3} \alpha^2 c R_\infty \frac{m_e}{m_\mu} \left(1 + \frac{m_e}{m_\mu}\right)^{-3}$$

Relation b/w $g-2$, EDM, & $\mu \rightarrow e\gamma$

Interaction of muon with photon

In effective field theory, new physics contributes model independently via Dim.6 dipole operator

modifies dipole moments

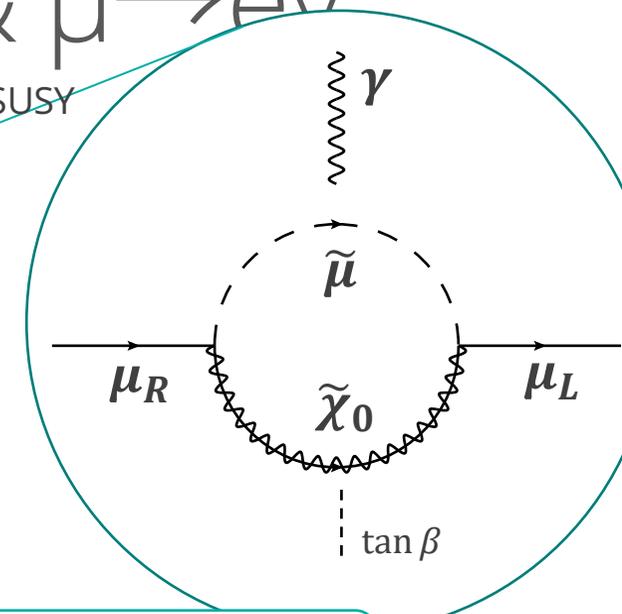


Relation b/w g-2, EDM, & $\mu \rightarrow e\gamma$

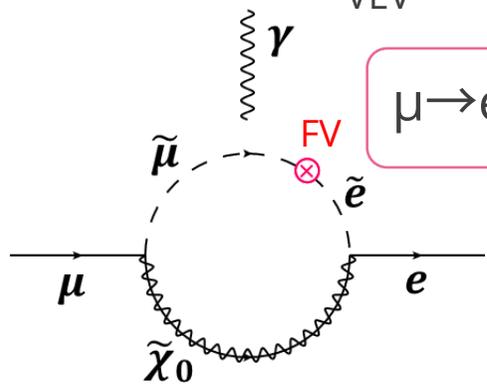
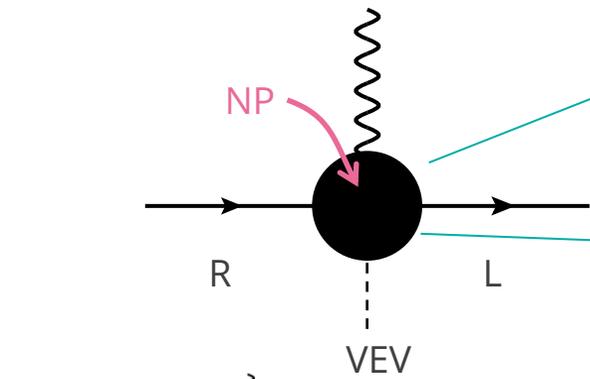
e.g. SUSY

Interaction of muon with photon

In effective field theory, new physics contributes model independently via Dim.6 dipole operator modifies dipole moments

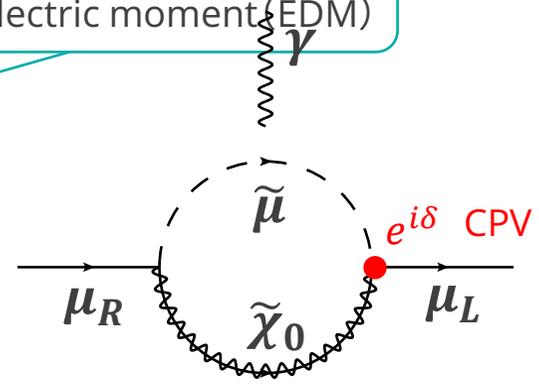


Real: magnetic moment (g-2)
Imaginary: electric moment (EDM)



$\mu \rightarrow e\gamma$

$$\begin{pmatrix} m_{\tilde{e}\tilde{e}} & m_{\tilde{e}\tilde{\mu}} & m_{\tilde{e}\tilde{\tau}} \\ m_{\tilde{\mu}\tilde{e}} & m_{\tilde{\mu}\tilde{\mu}} & m_{\tilde{\mu}\tilde{\tau}} \\ m_{\tilde{\tau}\tilde{e}} & m_{\tilde{\tau}\tilde{\mu}} & m_{\tilde{\tau}\tilde{\tau}} \end{pmatrix}$$

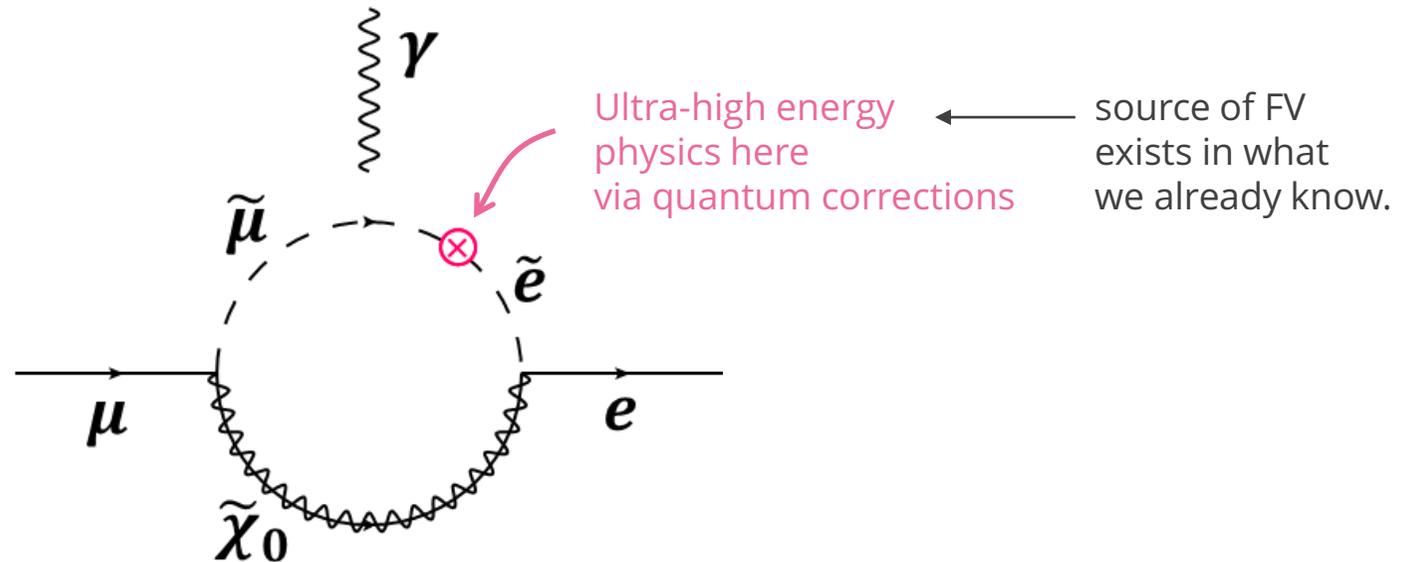


Slepton mass-matrix is in general not diagonalized together with that for leptons

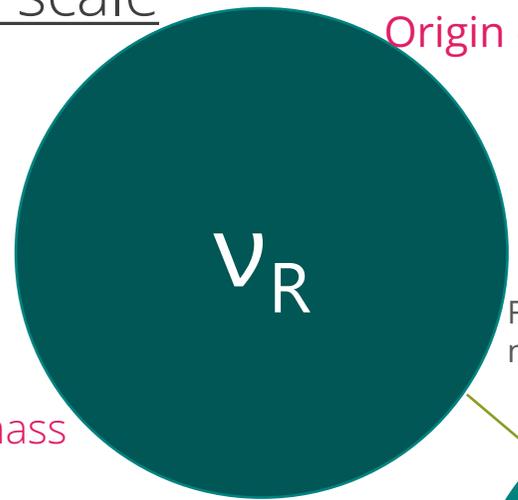
Flavor violating processes are of particular interesting.

Why?

1. provides definitive evidence for NP when discovered (unlike $g-2$) via “forbidden” decay searches
2. connects to ultra-high energy physics



Ultra-high scale
~10¹⁶ GeV



Neutrino mass

Origin of matter

Inflation



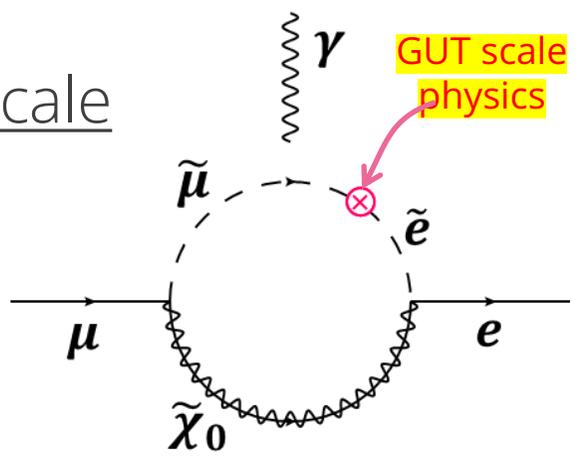
GUT

Force unification
Matter unification
Charge quantization

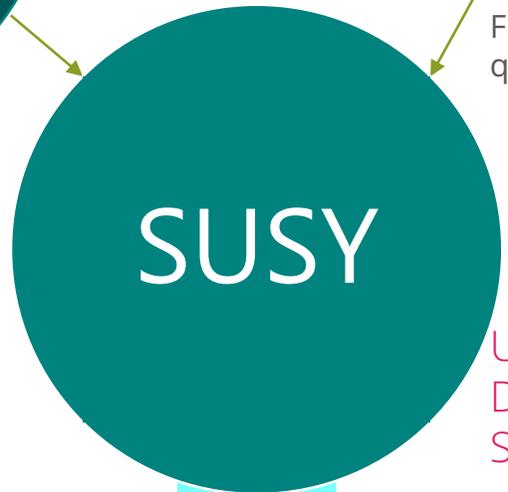
Flavor violation from neutrino Yukawa

Flavor violation from quark Yukawa

TeV scale



GUT scale physics



SUSY

Unify symmetries in space-time & internal
Dark matter
Solve hierarchy problem

Low scale

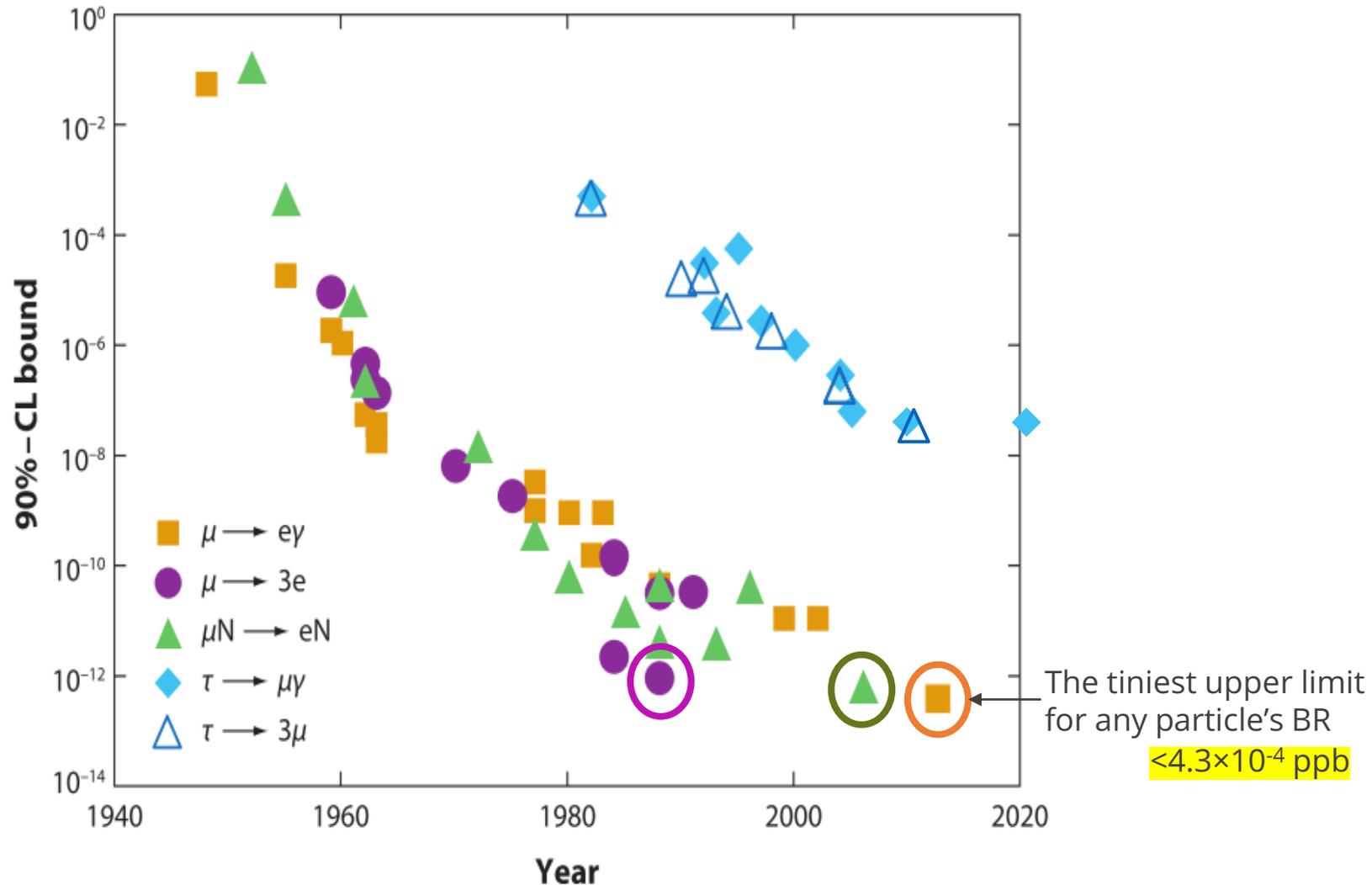


CLFV

$B(\mu \rightarrow e\gamma) \sim 10^{-12} - 10^{-15}$

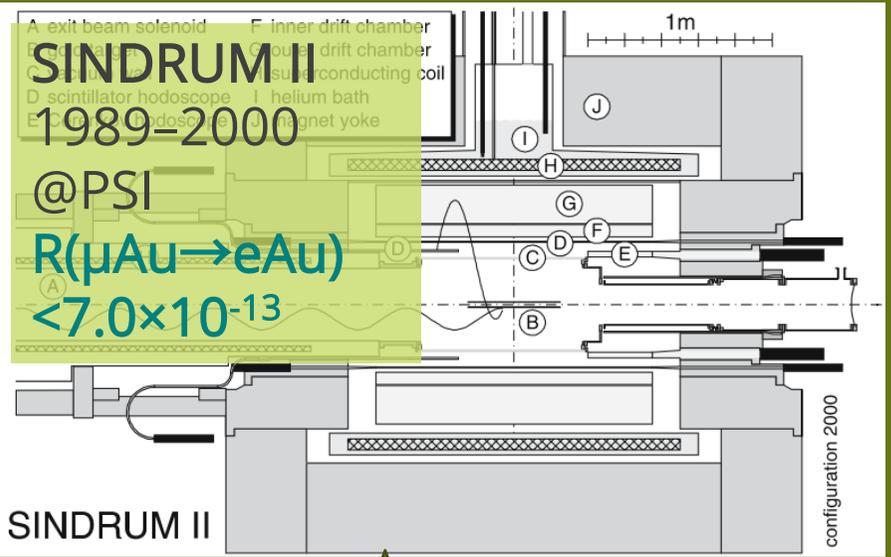
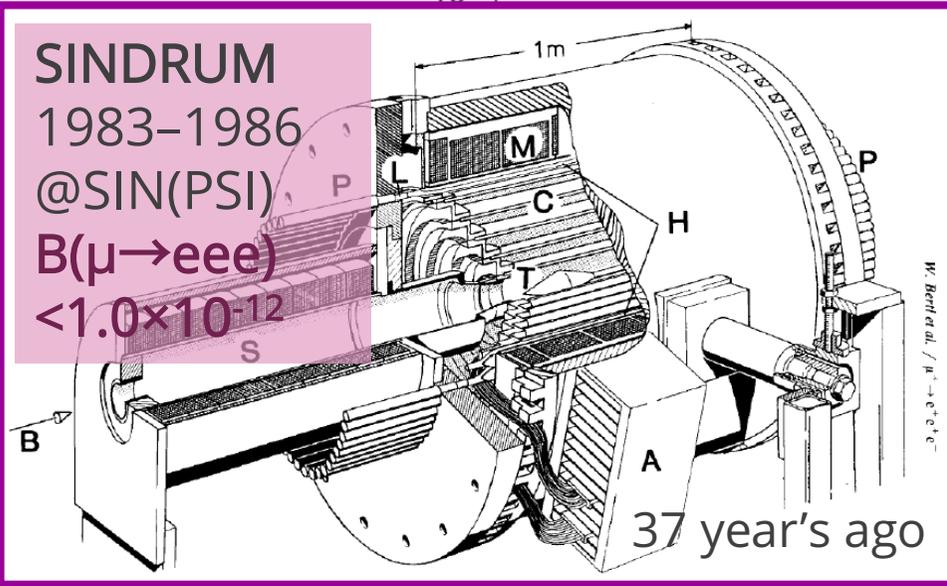
Create a new vision of "elementary particle & Universe" with muon decays

CLFV search history



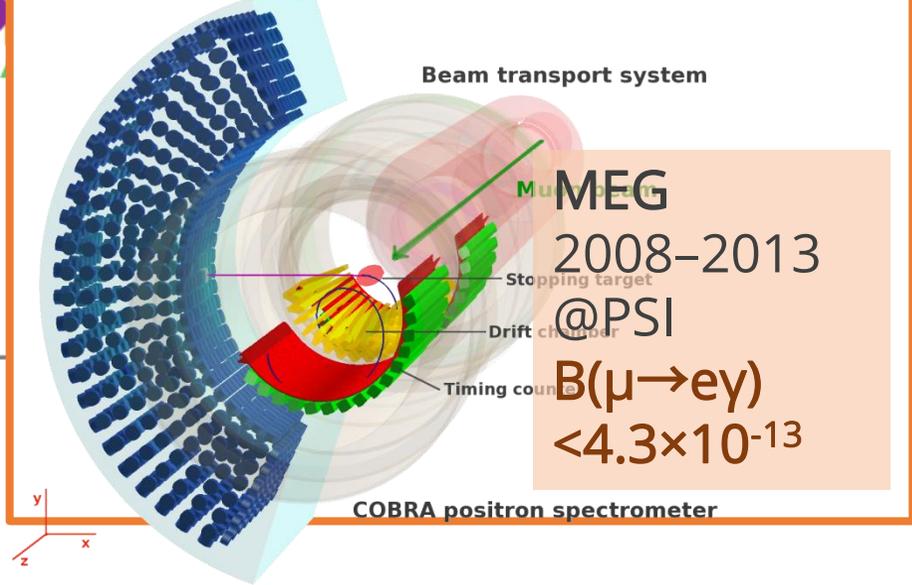
CLFV search history

SINDRUM
 1983-1986
 @SIN(PSI)
 $B(\mu \rightarrow eee)$
 $< 1.0 \times 10^{-12}$



SINDRUM II
 1989-2000
 @PSI
 $R(\mu Au \rightarrow e Au)$
 $< 7.0 \times 10^{-13}$

Liquid xenon gamma-ray detector

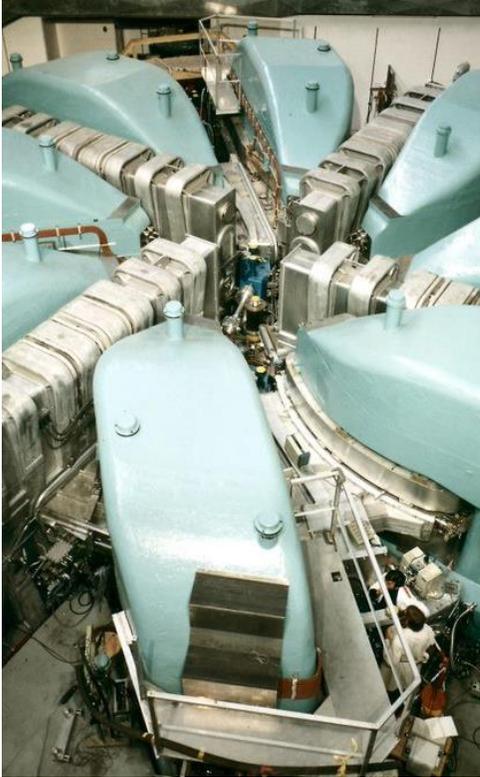


MEG
 2008-2013
 @PSI
 $B(\mu \rightarrow e\gamma)$
 $< 4.3 \times 10^{-13}$

μ LFV \rightarrow
PSI!!

The MEG II experiment

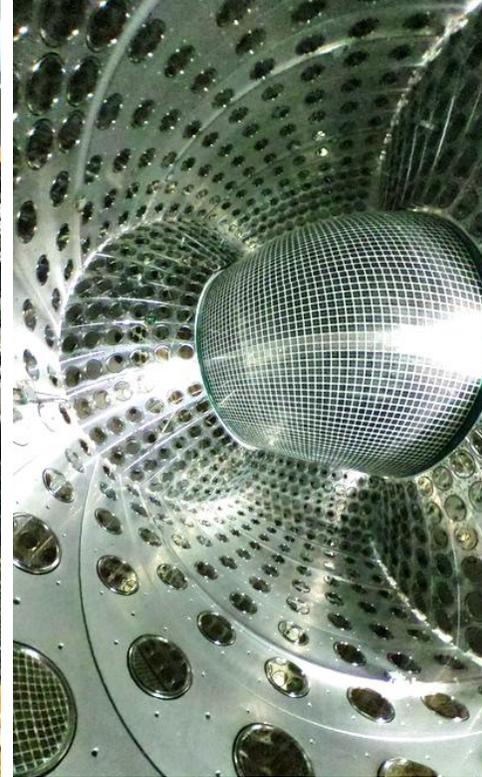
the only ongoing μ LFV experiment now



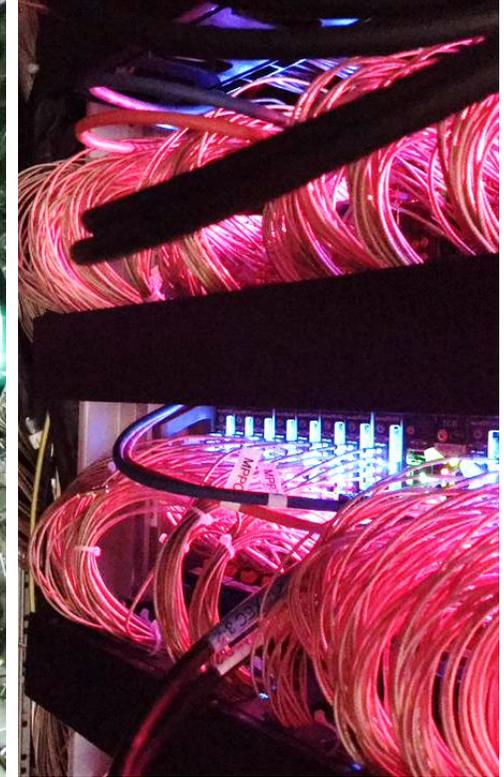
1.4 MW 590-MeV proton ring cyclotron, providing world's most intense DC muon beam



10^8 s^{-1} beamline, gradient field SC solenoid, high-rate capable low-mass e^+ detectors

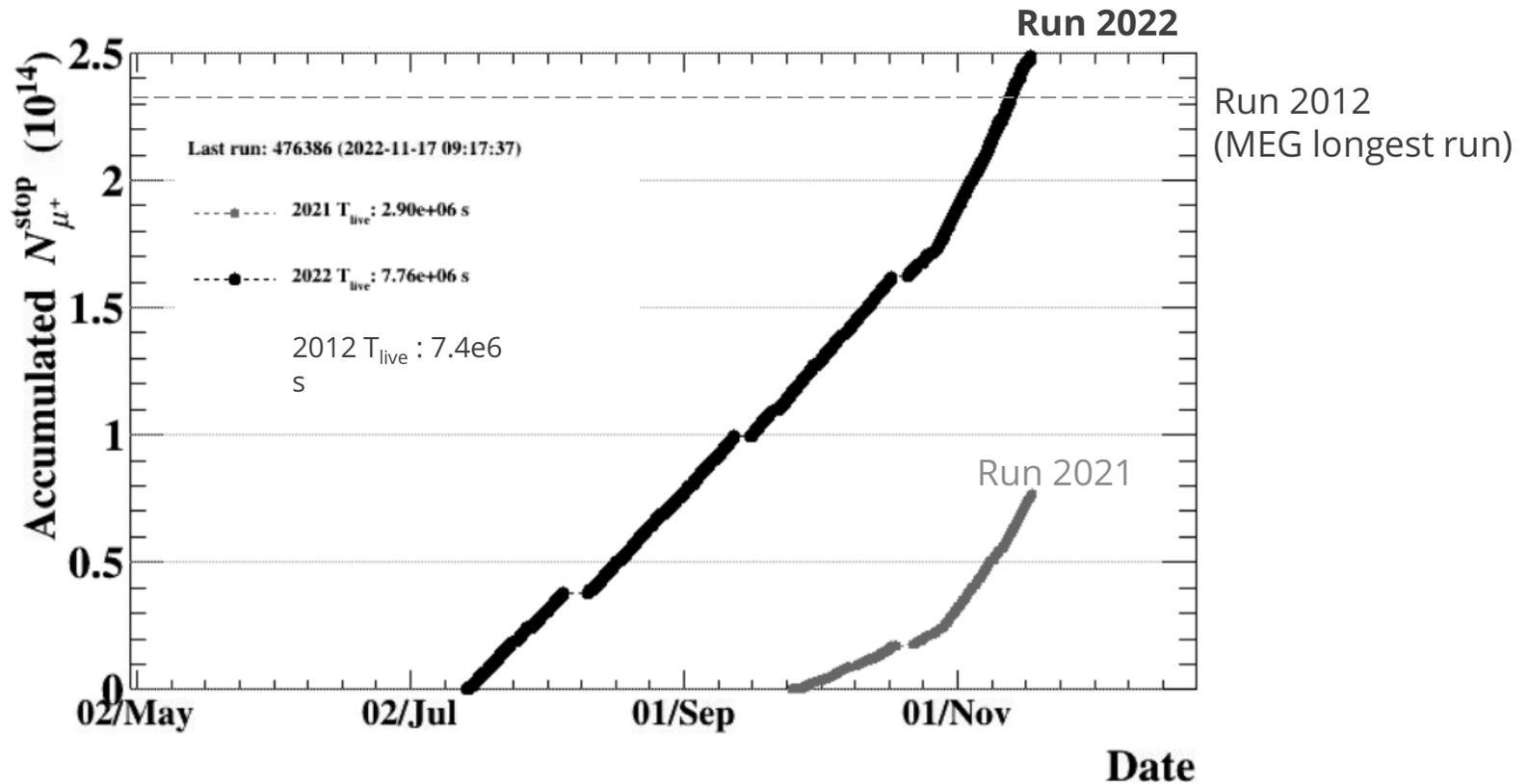


LXe scintillation photon detector with VUV sensitive photo-sensors, a pioneer work of LXe detectors



Integrated trigger & DAQ system to record waveform data @ 1.4 GSPS, with trigger rate of $<30 \text{ Hz}$.

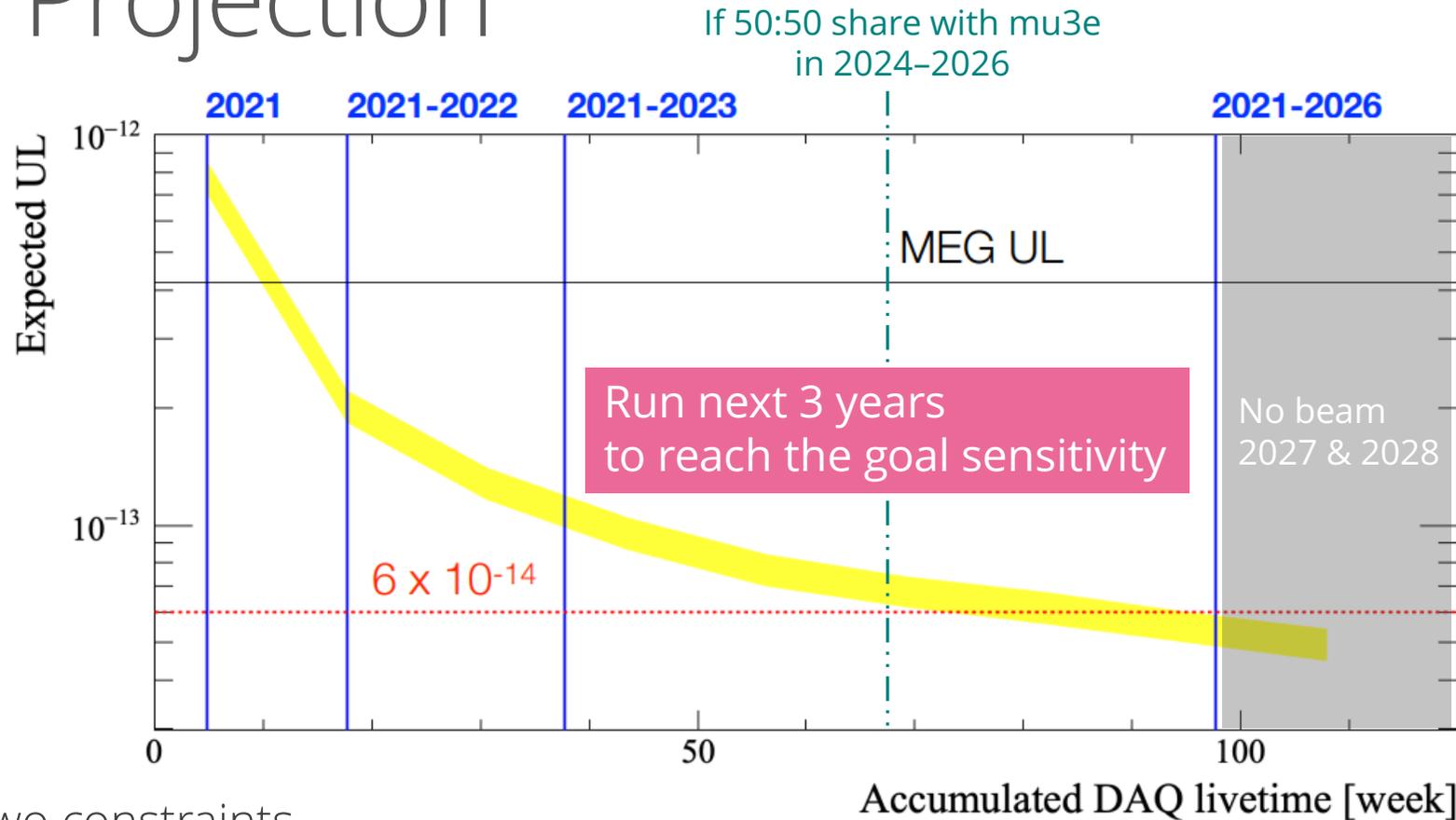
MEG II started in 2021



2021: pilot run → 1st result foreseen in this summer.

2022: 1st long production run → ×2.5 better sensitivity than MEG

Projection

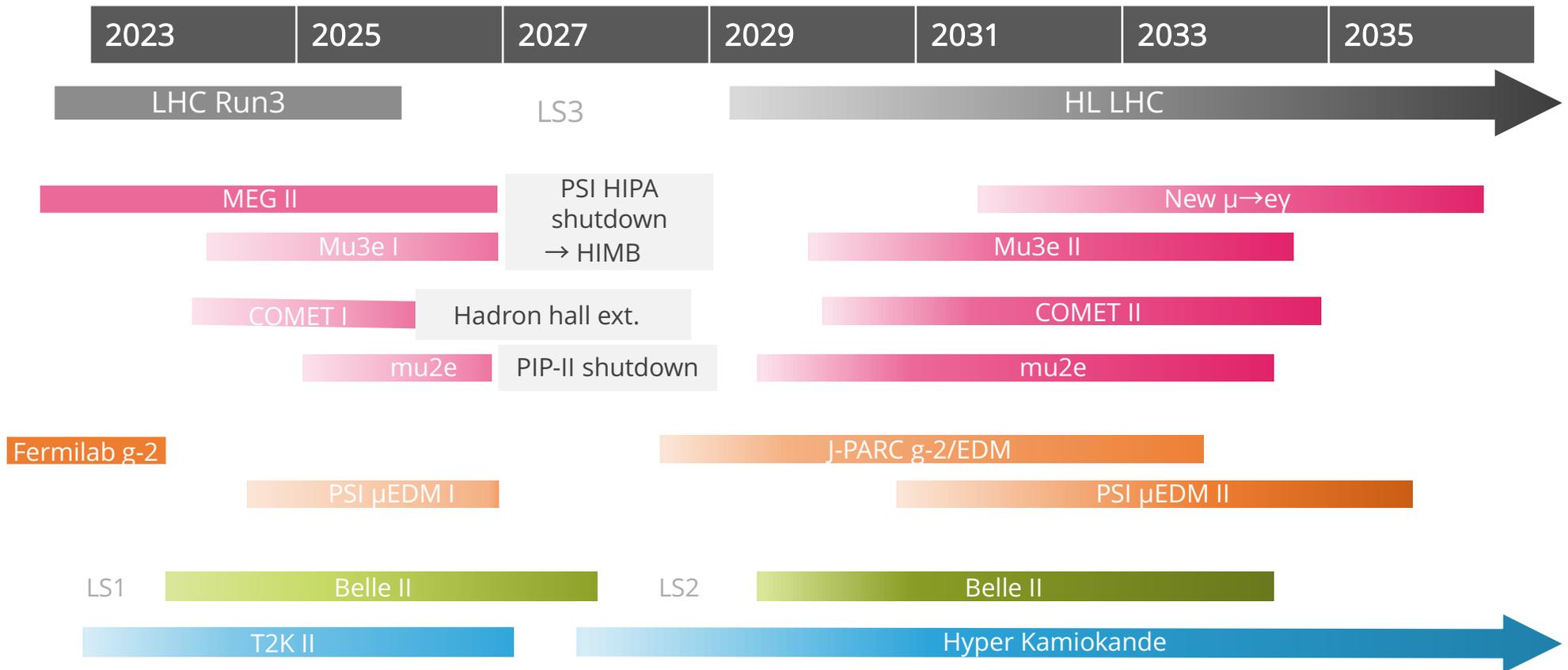


Two constraints

1. Long shutdown in 2027–2028 planned to build a new high-intensity muon beamline (10^{10} s^{-1})
2. Share $\pi E5$ beamline with mu3e once they get ready. They also conduct phase I experiment before the shutdown...

Next decade

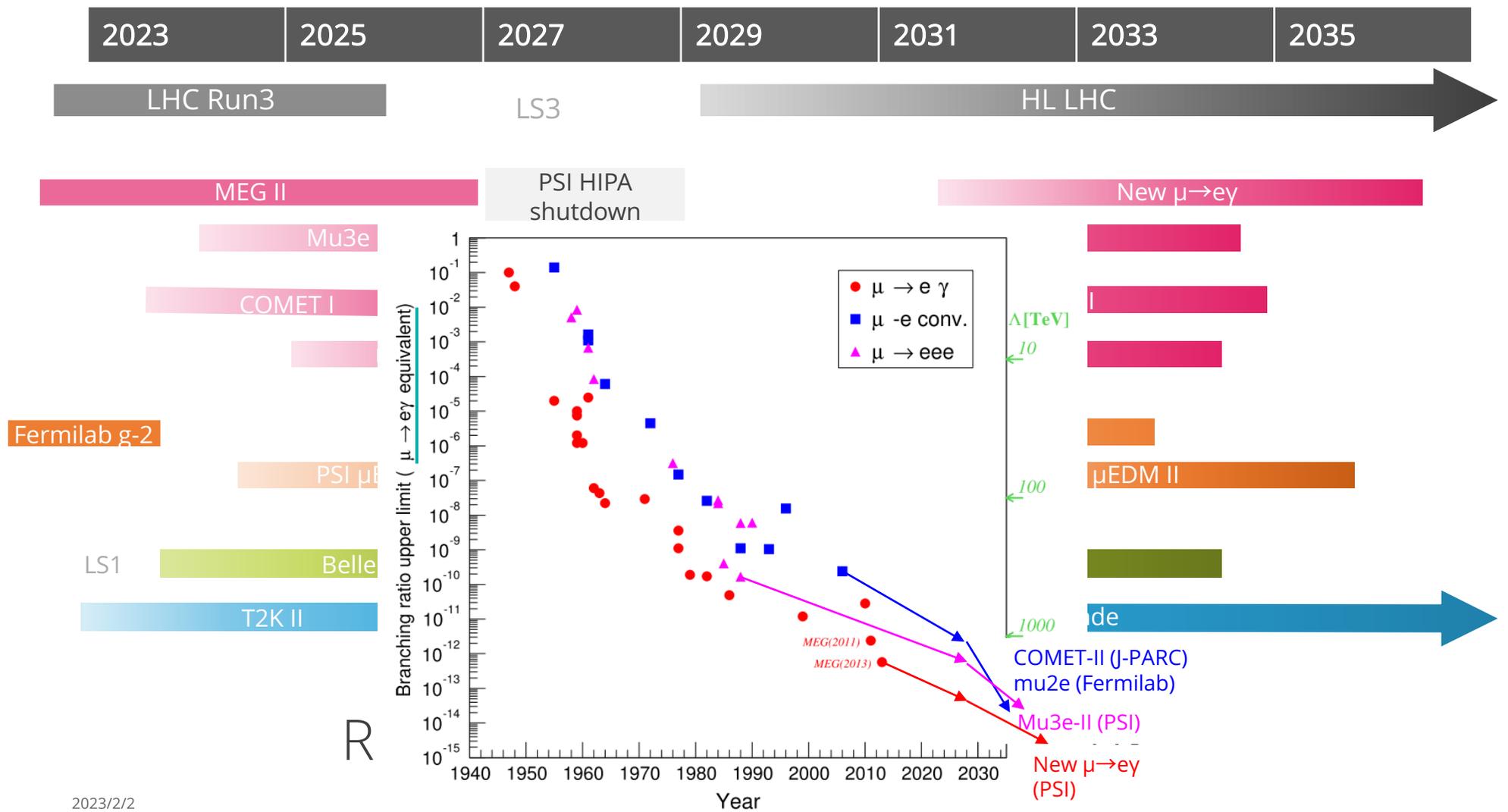
Include my perspective



Rich programs in 2020s – 2030s

Next decade

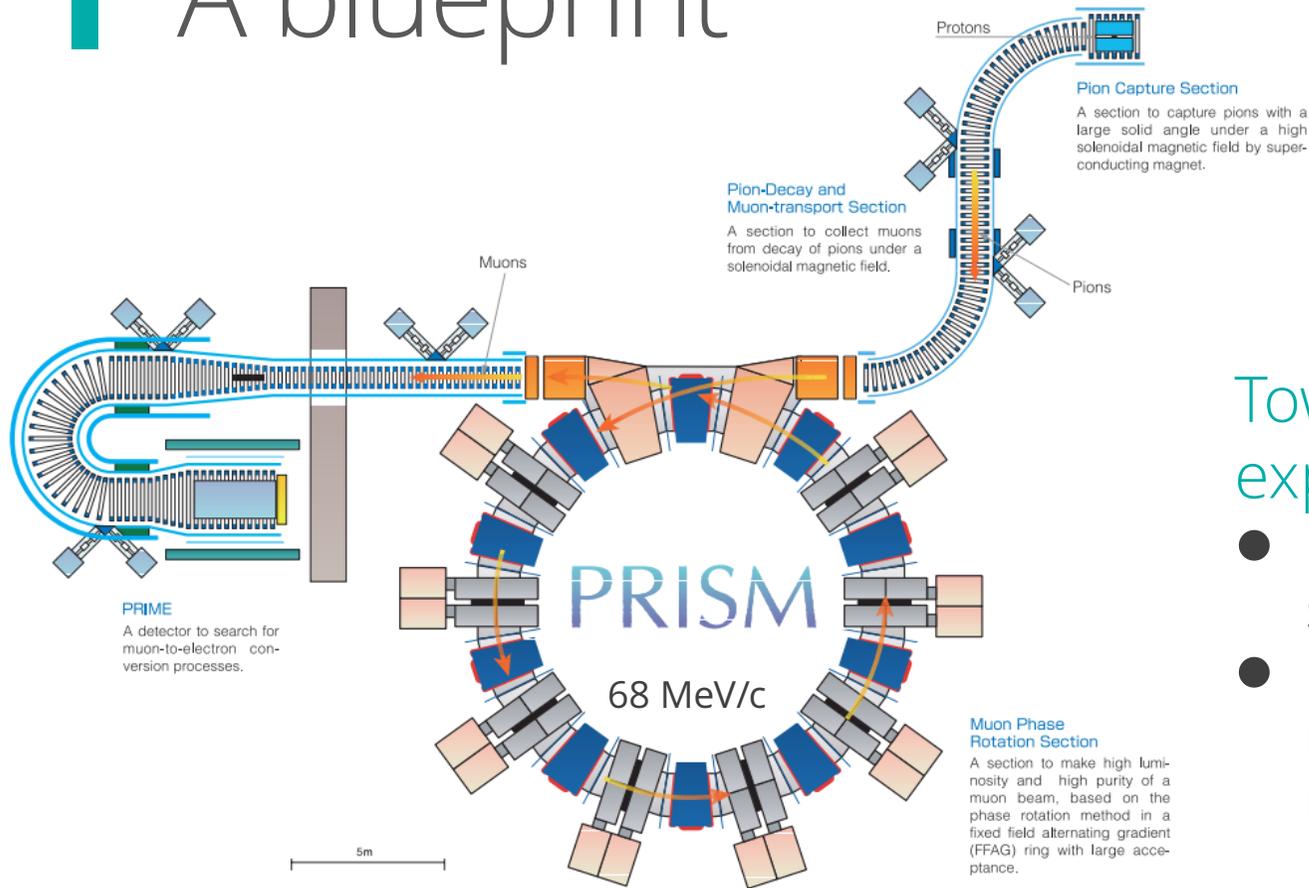
Include my perspective



■ What about far future?

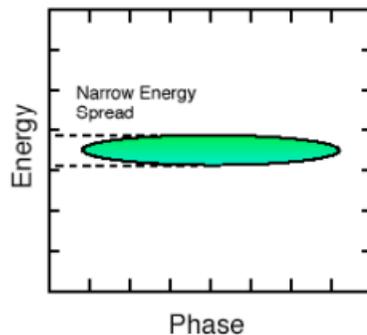
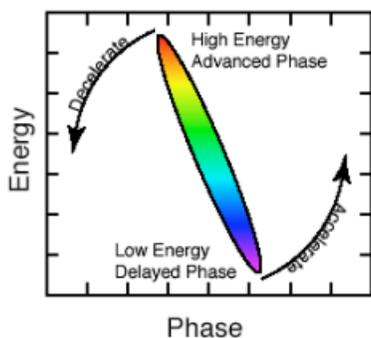
Manipulation of muons will be a key in 2040s particle physics

personal A blueprint

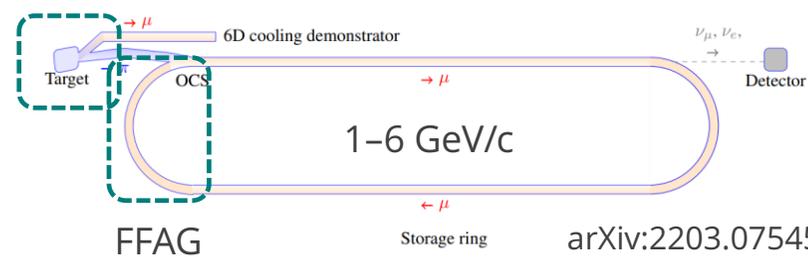


Towards an ultimate CLFV experiment $O(10^{-18})$

- FFAG-based phase rotating storage ring
- High intensity (10^{12} s^{-1}), monochromatic, high purity muon beam



Technical synergy with vSTORM



personal A blueprint

Towards colliders with muons

Worldwide interest and efforts for muon colliders

- ❑ However, technically not mature.
- ❑ Japanese contribution to MC is behind, but we have advanced technologies
 - High-power proton driver (J-PARC)
 - COMET will establish pion capture technique → 10^{11} s^{-1} beam
 - g-2/EDM will establish low emittance μ^+ beam with muonium-ionization cooling and muon acceleration for the first time in the world
 - FFAG technologies may fit to fast acceleration

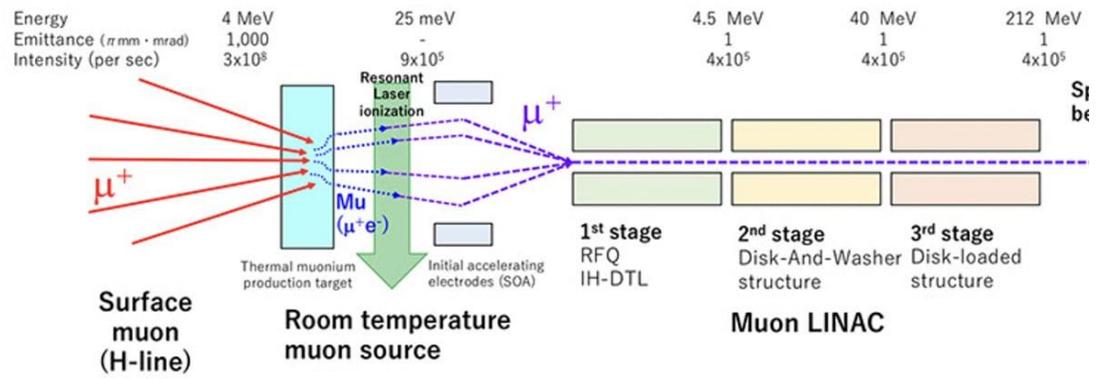


collider with μ^+

Y. Fukao



H. Inuma



PTEP 2022 053B02

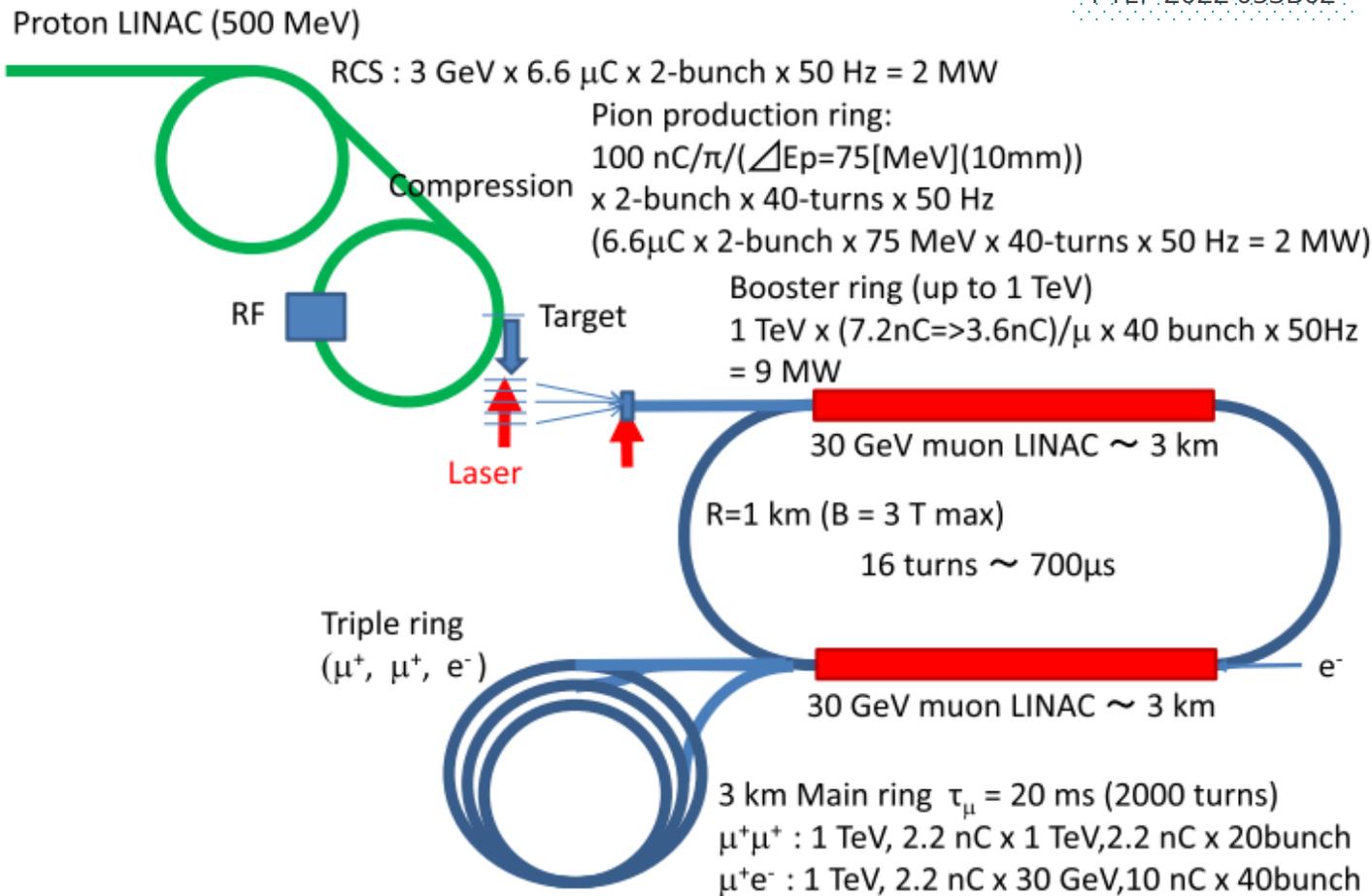


Fig. 1. Conceptual design of the $\mu^+e^-/\mu^+\mu^+$ collider.

A new idea of μ^+e^- collider: μ TRISTAN

- as a Higgs factory
 $\sqrt{s} = 346$ GeV
- a realistic design
- earlier realization than $\mu^+\mu^-$

As a pre step, start with
v-factory (only ν_e & $\bar{\nu}_\mu$) with 5 GeV?

Conclusions

Muons have played an essential role in modern physics (SM) in its 86-year history

Providing the most fundamental (G_F) & most precise (R_∞) parameters in SM.

Today & next decade would be the **hottest period** of particle physics with muons

New experiments in J-Parc (& lattice QCD) will conclude the $g - 2$ anomaly.

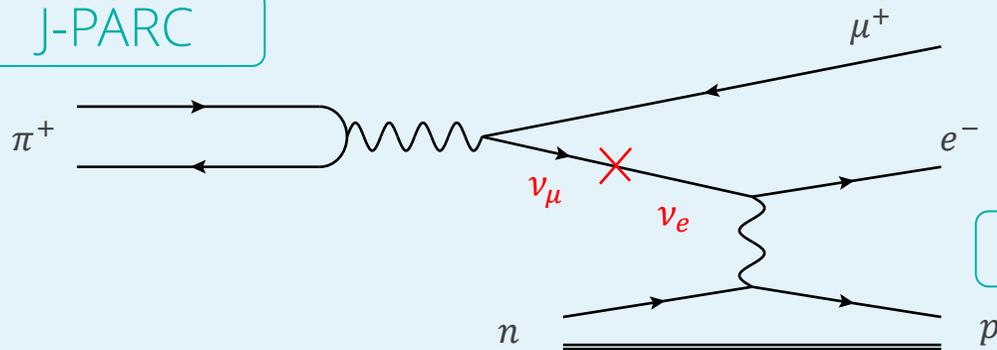
New **CLFV** experiments in the world would discover evidence for NP.

So, **CLFV** & **LFUV** would be key probes for NP.

New **technologies to manipulate muons** would be the key of high-energy & particle physics in 2040s (or even earlier)

CLFV processes in SM

J-PARC



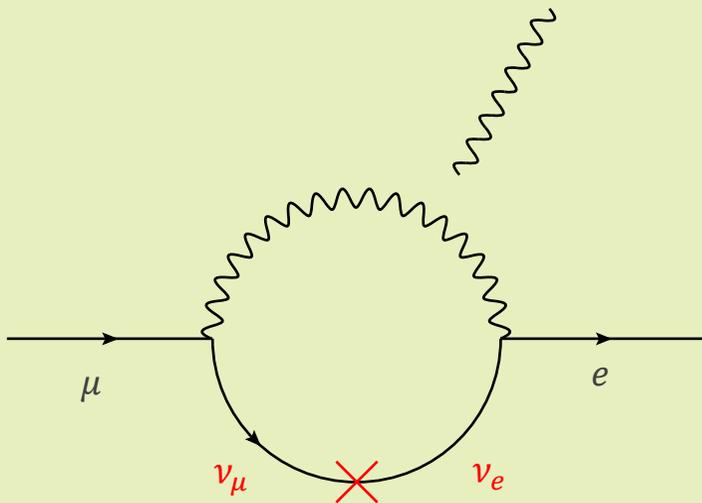
SK

$$\pi^+ n \rightarrow \mu^+ e^- p$$

$$L_e = 0 \\ L_\mu = 0$$

$$L_e = 1 \\ L_\mu = -1$$

CLFV!!



$$\mu \rightarrow e \gamma$$

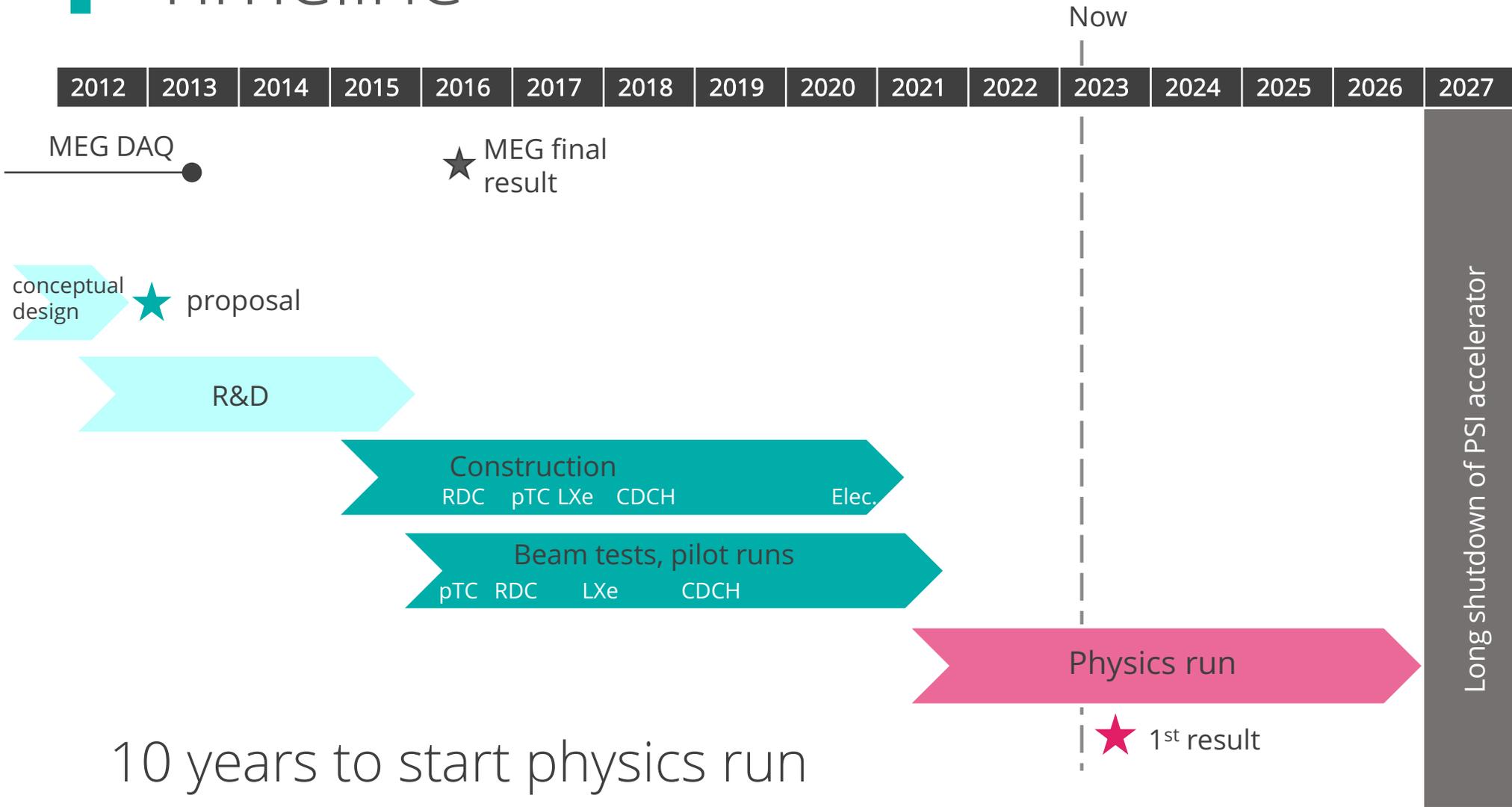
$$L_e = 0 \quad L_e = 1 \\ L_\mu = 1 \quad L_\mu = 0$$

$$\frac{3\alpha}{32\pi} \left| \sum_{i=2,3} U_{\mu i}^* U_{e i} \frac{\Delta m_{i1}^2}{M_W^2} \right|^2 < 10^{-54}$$

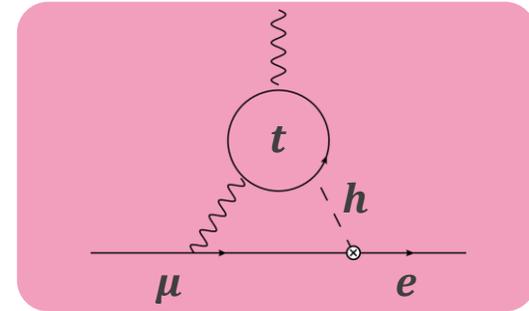
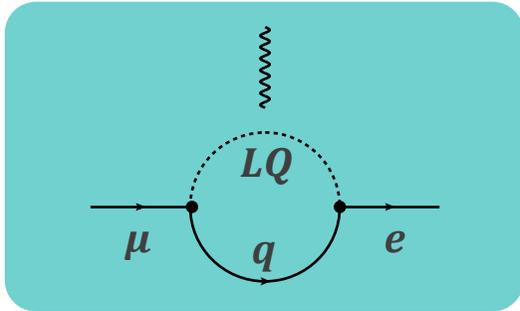
Just too small probability
due to mysteriously tiny neutrino masses

Impossible to be observed
If observed, **definitive evidence for NP**

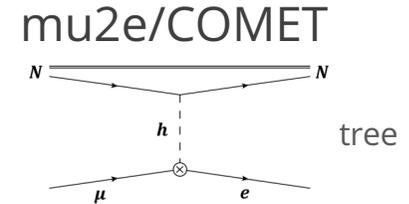
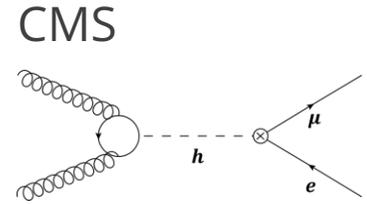
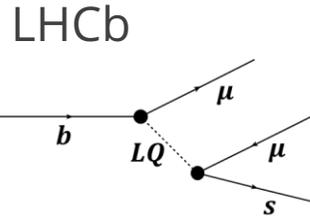
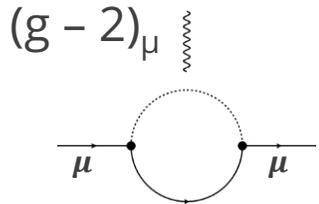
Timeline



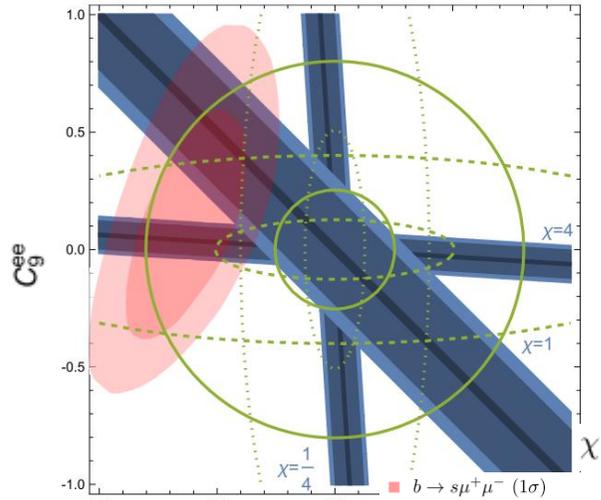
Other reasons



two-loop

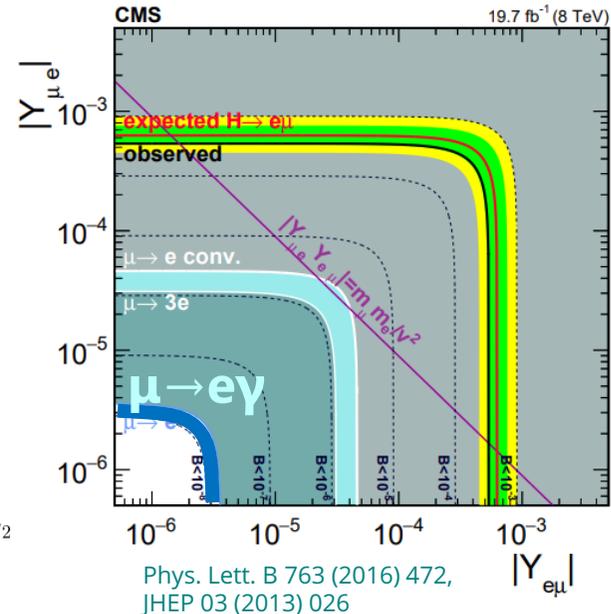


tree



Strong correlation b/w observed anomalies.
If new particle couples to both muon and electron it induces sizable $\mu \rightarrow e\gamma$.

- $b \rightarrow s\mu^+\mu^-$ (1σ)
- $\text{Br}[\mu \rightarrow e\gamma] < 4.2 \cdot 10^{-13}$ with Φ_3
- $\text{Br}[\mu \rightarrow e\gamma] < 4.2 \cdot 10^{-13}$ with V_1^μ
- $\text{Br}[\mu \rightarrow e\gamma] < 4.2 \cdot 10^{-13}$ with V_3^μ
- $b \rightarrow s\mu^+\mu^-$ (2σ)
- $\text{Br}[B \rightarrow K\mu^\pm e^\mp]$ with $\gamma = 1/2$
- $\text{Br}[B \rightarrow K\mu^\pm e^\mp]$ with $\gamma = 1$
- $\text{Br}[B \rightarrow K\mu^\pm e^\mp]$ with $\gamma = 2$

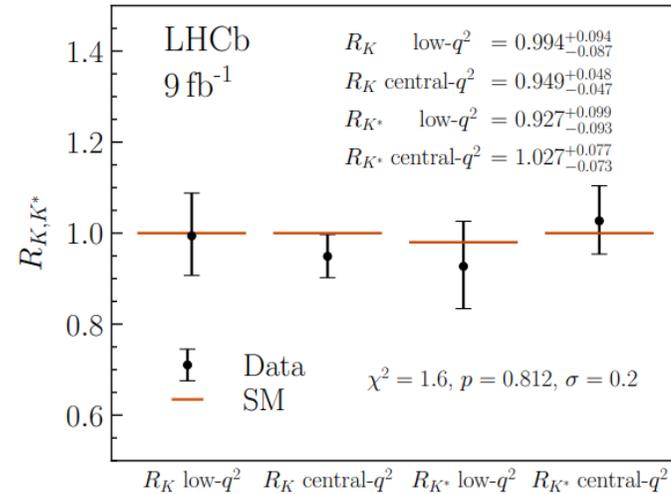
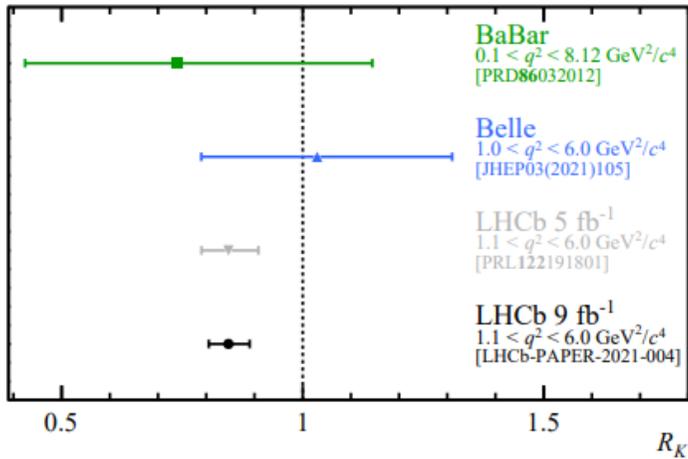


Limit on $\mu \rightarrow e\gamma$ provides the most stringent limit on the LFV Higgs decay
 $\text{BR}(h \rightarrow \mu e) \lesssim 10^{-8}$
(CMS limit:
 $\text{BR}(h \rightarrow \mu e) < 3.5 \times 10^{-4}$)

Phys. Lett. B 763 (2016) 472,
JHEP 03 (2013) 026

Recent news

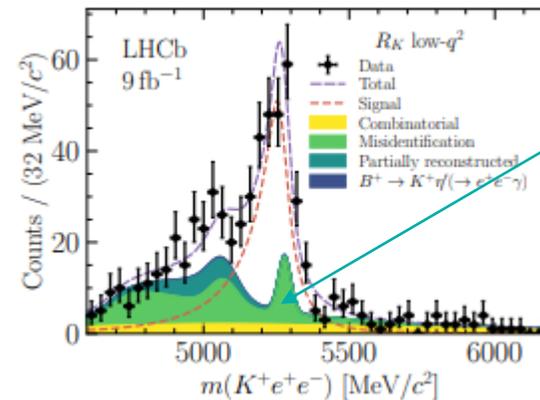
> 3σ discrepancy found !!!!



[arXiv:2212.09153](https://arxiv.org/abs/2212.09153)

Nature Physics 18, (2022) 277-282
 545 citations (← many theories to explain this anomaly)

Surely it is the way for science to go, but
Flavor physics is now put to test.
 (Lots of “anomalies” appeared and disappeared not only in flavor physics.)



Peaking BG
 unconsidered
 in the old
 analysis

We need conclusive experiments

Different processes

Why search different channels

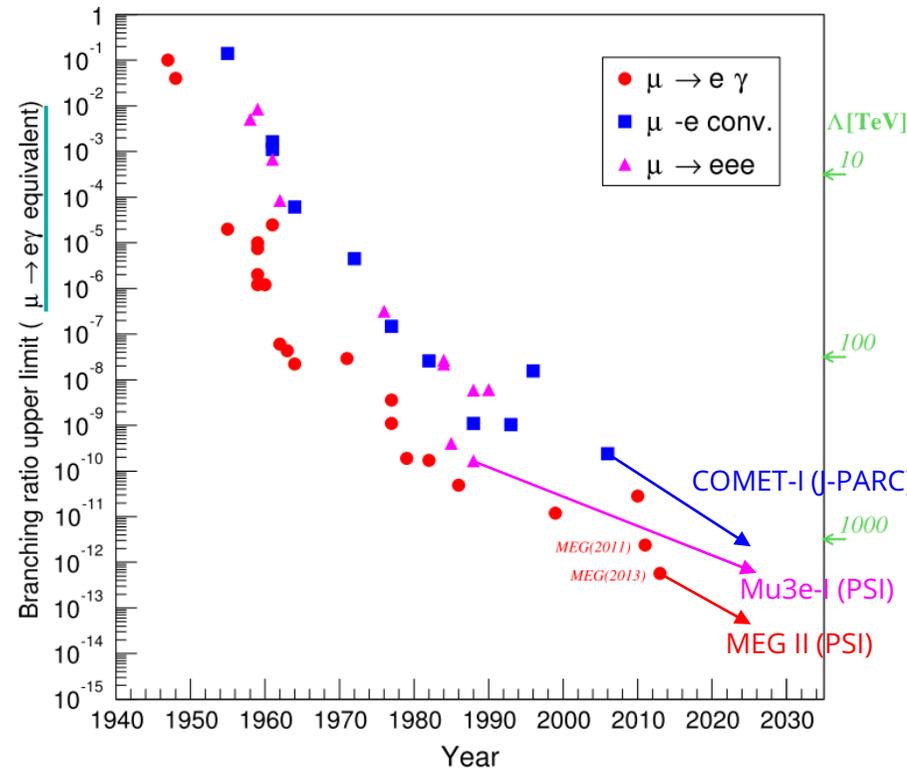
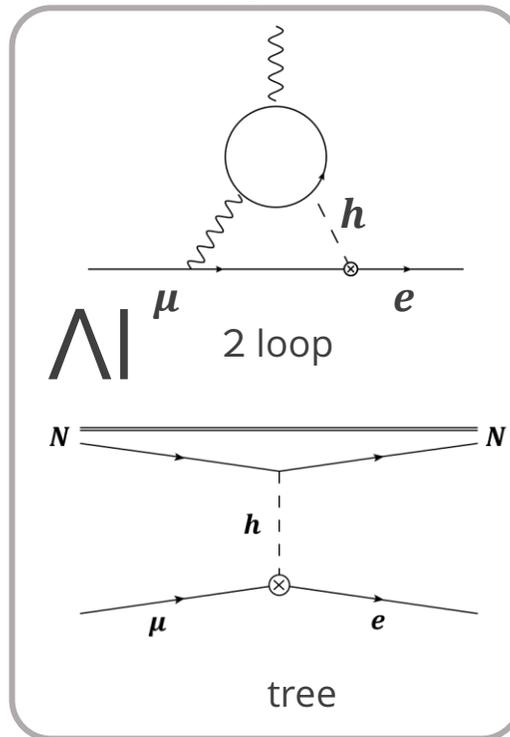
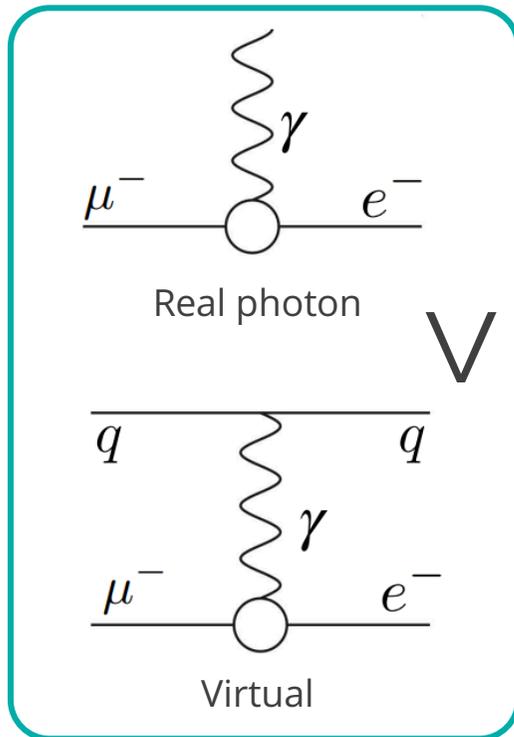
- ❑ Sensitive to different physics behind
- ❑ Different requirements for experiments
- ❑ Test/confirmation for the other experiments
- ❑ Identify physics once discovered in a channel
- ❑ Competition

What are you interested in?
 What are available technologies?

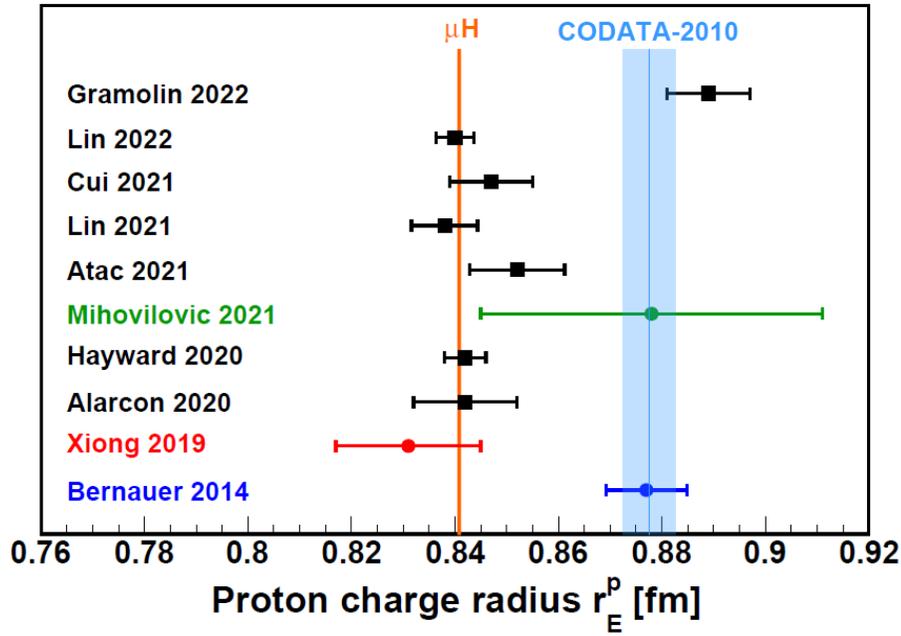
So far, $\mu \rightarrow e\gamma$ has always leded.

SUSY-GUT case

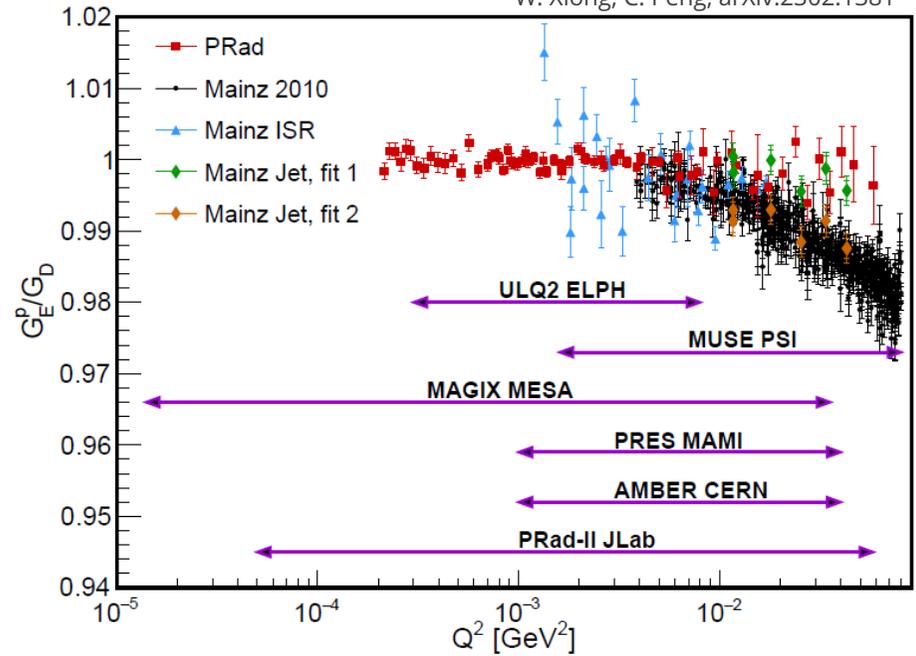
Higgs case



W. Xiong, C. Peng, arXiv:2302.1381



W. Xiong, C. Peng, arXiv:2302.1381



Neutrino Factory : FFAG based

