

# De la dynamique galactique à la formation stellaire : comment est régulé le taux de formation d'étoiles ?

*From galactic dynamics to star formation, what sets the star formation rate?*

in collaboration with Patrick Hennebelle, Frédéric Bournaud, Tine Colman, Simon Iteanu et Corentin le Yhuellic

Journées du labex P2IO, 1/11/2022

# Stars shape the universe.

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Processing: Robert Eder

- ▶ Stars represents only a few % of the mass of a galaxy
- ▶ But they play a key role in the galactic ecosystem
  - ▶ gravitational potential
  - ▶ injection of energy via feedback
  - ▶ metal enrichment



Image Credit: NASA, ESA, CSA, STScI; Processing Copyright: Robert Eder

# Stars form out of the dense gas of the InterStellar Medium



Image Credit: NASA, ESA, CSA, STScI, Webb ERO Production Team

# Stars form out of the dense gas of the InterStellar Medium

## What is the **ISM**?

Space between the stars

- ▶ ~ 99 % gas (by mass)  
(H/HII/H<sub>2</sub> 70 %, He 28 %)
- ▶ ~ 1 % dust grains

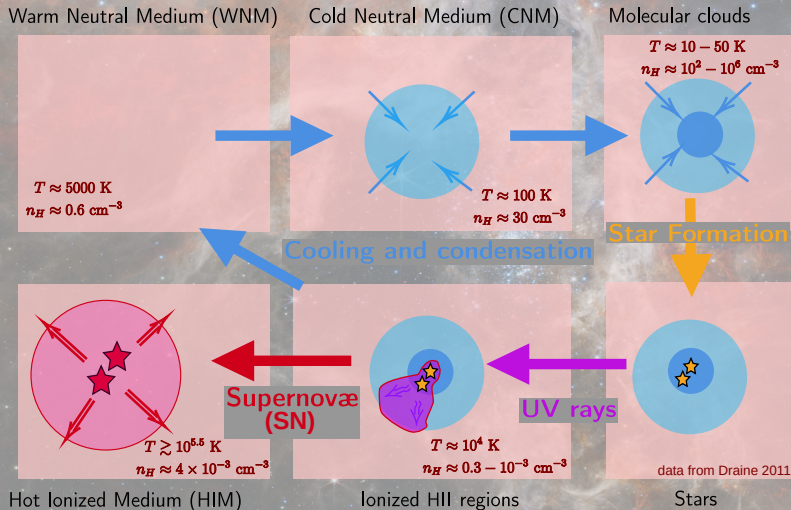
Main drivers of the ISM

- ▶ Hydrodynamics
- ▶ Gravity
- ▶ Cooling/Heating
- ▶ Chemistry
- ▶ Magnetic field (MHD)
- ▶ Stars



Image Credit: NASA, ESA, CSA, STScI, Webb ERO Production Team

# The matter cycle in the ISM

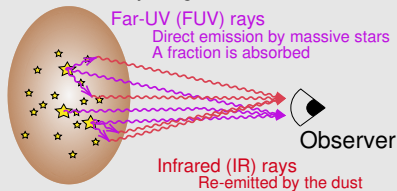


# The star formation rate (SFR)

Mass of star formed by unit of time

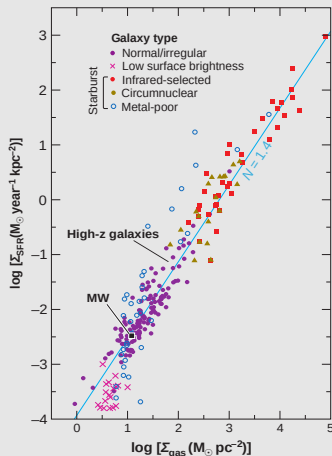
## Observation of the SFR

① Measuring the light emission let us know the mass of young massive stars



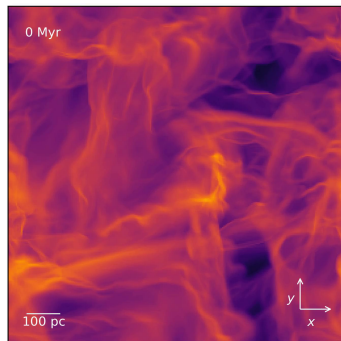
② The initial mass function enables to recover the total SFR

## The Schmidt-Kennicutt law relation (SK)



# What triggers stops star formation?

because gravity would consume all the gas quickly

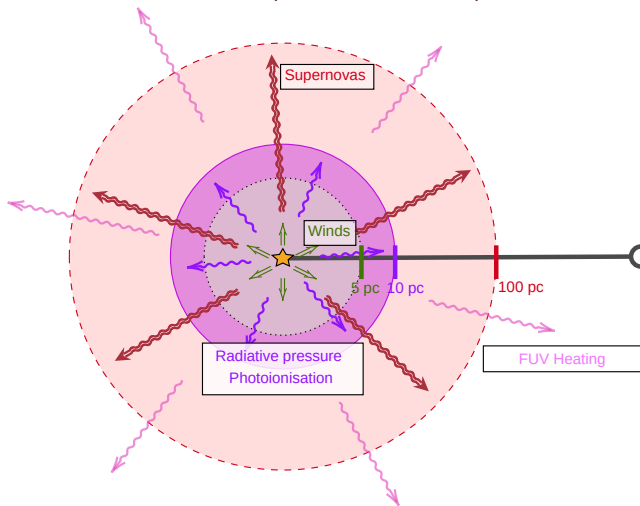


$$SFR_{\text{grav}} \approx \frac{M_{\text{dense}}}{t_{\text{free-fall}}} \approx 460 M_{\odot} \cdot \text{yr}^{-1}$$

$$\gg SFR_{\text{obs}} \approx 2 M_{\odot} \cdot \text{yr}^{-1}$$

# What stops star formation?

A natural candidate: stars themselves! (via stellar feedback)



More stars  $\rightarrow$  more feedback  $\rightarrow$  less star formation. Self-regulation?



# What stops star formation?

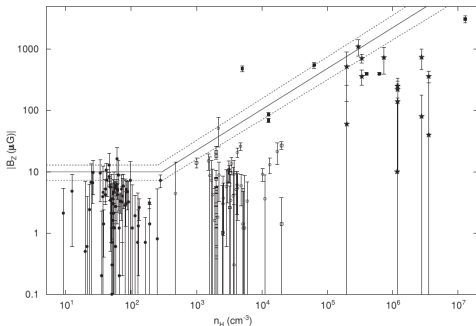
Magnetic field

- ▶ Magnetic pressure

$$P_{\text{mag}} = \frac{B^2}{8\pi}$$

- ▶ Magnetic tension

$$\mathcal{T}_{\text{mag}} = \frac{(\mathbf{B} \cdot \nabla) \mathbf{B}}{4\pi}$$

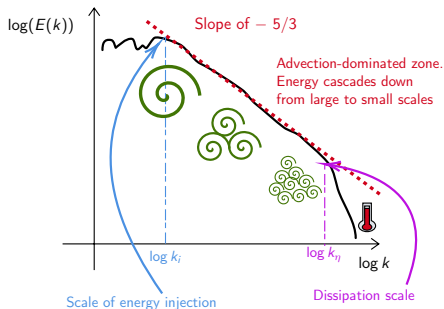


Crutcher et al.

Equipartition:  $E_{\text{magnetic}} \sim E_{\text{turbulent}} \sim E_{\text{thermal}} \sim E_{\text{starlight}} \sim E_{\text{dust emission}}$

# What stops star formation?

## Turbulence

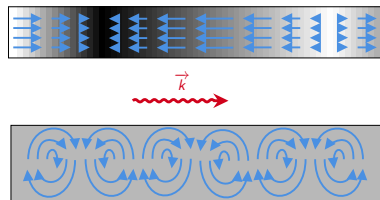


## Richardson cascade for incompressible turbulence

Characterized by its strength  $\sigma$  and compressibility  $\chi$

## Turbulence can be composed of

- compressive modes



- or solenoidal modes

# Goals

- ▶ What is the more efficient process that quenches star formation?
- ▶ What regulates star formation?
- ▶ It is the same for all galaxies?

## Outline

- I - Introduction
  - A - Star Formation
  - B - Quenching of star formation
- II - Kiloparsec simulations
  - A - Stellar feedback
  - B - Large scale turbulence
- III - Full galactic simulations
- IV - Conclusions

# Physics

Hydrodynamics

Gas gravity

Stars and dark matter gravity

Star formation

Stellar feedback

SN

HII

FUV

Magnetic field

Turbulence

 $\sigma$  $\chi$ 

# Scale

Small:  $< 10$  pc

- Atoms:  $10^{-25}$  pc
- ★ Stars:  $10^{-8}$  to  $10^{-5}$  pc
- ✧ Protoplanetary disks:  $10^{-4}$  pc
- Star clusters: 1 pc

Medium: 1 pc to 1 kpc

- ⊗ HII regions: 10 pc
- ⊛ SN shells: 100 pc
- ☁ Molecular clouds: 100 pc

Large: 100 pc to 20 kpc

- ♪ Galaxy : 10 kpc

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 $\sigma$  $\chi$ 

Focus

Included

Not included

# Scale

Small: ~~< 10 pc~~

Medium: 1 pc to 1 kpc

Large: ~~100 pc to 20 kpc~~

## Outline

I - Introduction

II - Kiloparsec simulations

III - Disk simulations

IV - Conclusions

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## Outline

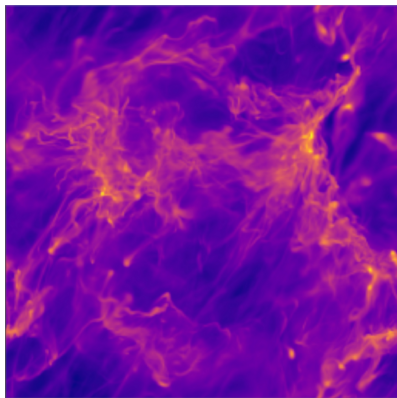
I - Introduction

II - Kiloparsec simulations

III - **Disk simulations**

IV - Conclusions

## II - Kiloparsec simulations



Brucy+ 2020,  
Brucy+ 2022 (subm), with a  
glimpse of Brucy & Hennebelle,  
2023 (in prep.)

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I - Introduction

A - Star Formation

B - Quenching of star  
formation

II - Kiloparsec simulations

A - Stellar feedback

B - Large scale turbulence

III - Full galactic simulations

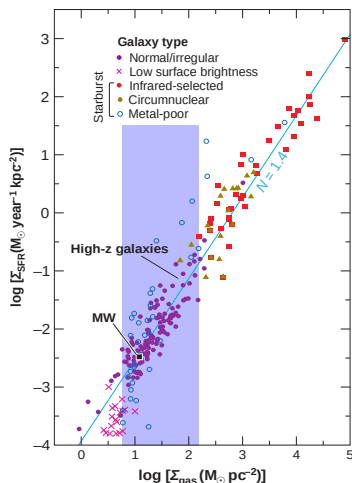
IV - Conclusions

# Kiloparsec simulations

**Goals** We focus what quenches the SFR in dense environments, and in particular

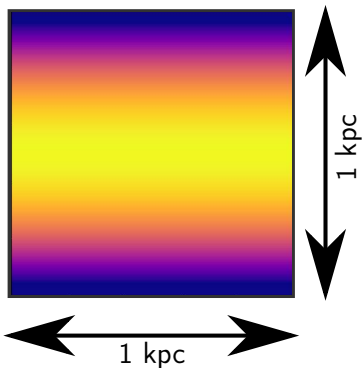
- ★ Role of stellar feedback
- 🌀 Role of large scale turbulence
- U Role of magnetic field

Can these processes explain the observed SFR from the Schmidt-Kennicutt (SK) relation?





## Main simulation setup



Roughly similar setup:  
FRIGG, TIGRESS, SILCC.

### MHD simulations with Ramses

- ▶ MHD equations + cooling
- ▶ Star formation and feedback
- ▶ **No** very hot gas ( $> 10^6$  K)

### Initial conditions

- ▶  $\rho(z) = n_0 \exp\left(-\frac{1}{2} \left(\frac{z}{z_0}\right)^2\right)$
- ▶ Stellar and dark matter potential
- ▶  $B_x(z) = B_0 \exp\left(-\frac{1}{2} \left(\frac{z}{z_0}\right)^2\right)$

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## Outline

II - Kiloparsec simulations

A - Stellar feedback

B - Large scale turbulence

Focus

Included

Not included

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## Outline

II - Kiloparsec simulations

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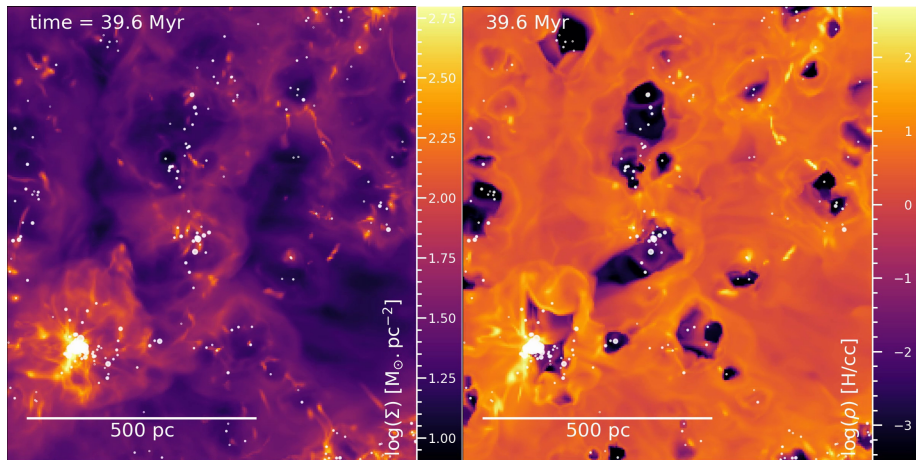
Focus

Included

Not included

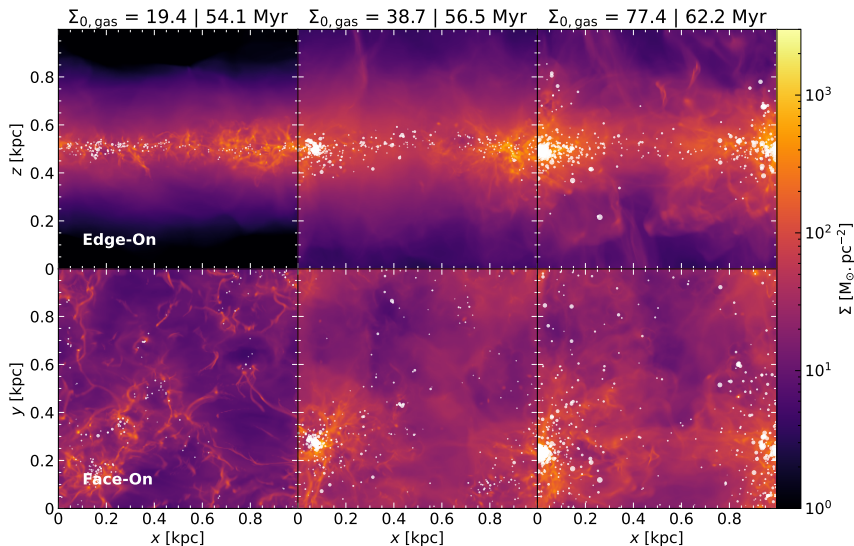
## A - With only stellar feedbacks

$\Sigma = 38.7 M_{\odot} \cdot \text{pc}^{-2}$ . Face on views of column density (left) and midplane density (right).

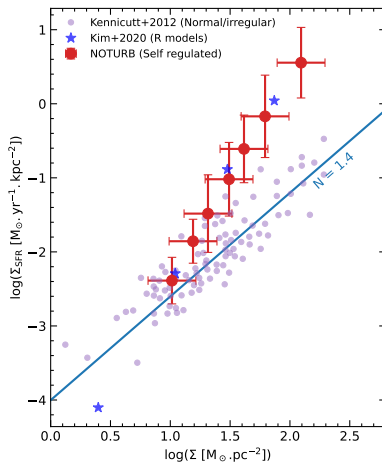


## A - With only stellar feedbacks

## Column density maps



## A - With only stellar feedbacks



**Stellar feedback is sufficient in Milky-Way like galaxies ... BUT is too weak in high-z galaxies.**

## B - The influence of larger-scale dynamics: turbulent driving



## Turbulence from galactic dynamics

- ▶ Spirals, mass transfert → turbulence (eg. Krumholz+ 2018)

## B - The influence of larger-scale dynamics: turbulent driving



$$\mathbf{f}(\mathbf{x}, t) = f_{\text{rms}} \times \int \hat{\mathbf{f}}(\mathbf{k}, t) e^{i\mathbf{k} \cdot \mathbf{x}} d^3\mathbf{k}$$

## Turbulence from galactic dynamics

- ▶ Spirals, mass transfert → turbulence (eg. Krumholz+ 2018)
- ▶ Expected injected power:  
 $P_{\text{LS}} \propto \Sigma_g^4$  or  $P_{\text{LS}} \propto \Sigma_g^{2.5}$

## Model

An extra 2D force is added to generate random motion at scales between 300 and 1000 pc.



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II - Kiloparsec simulations

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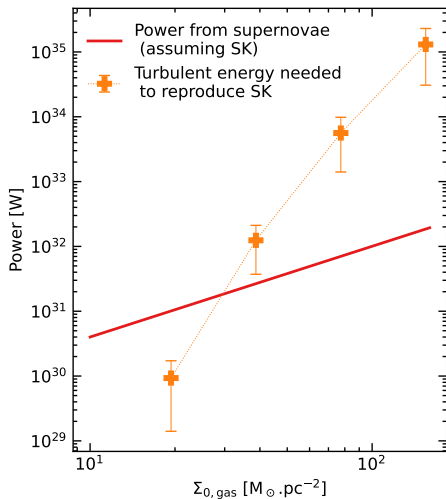
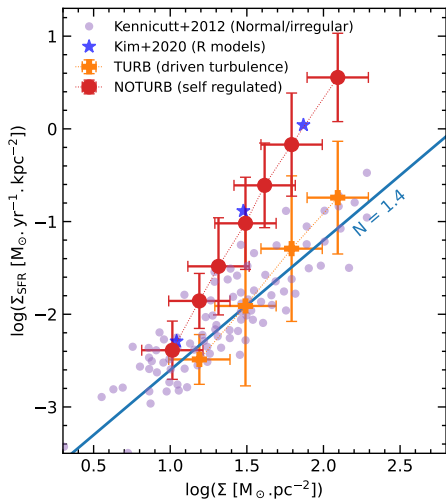
## Outline

II - Kiloparsec simulations

A - Stellar feedback

B - Large scale turbulence

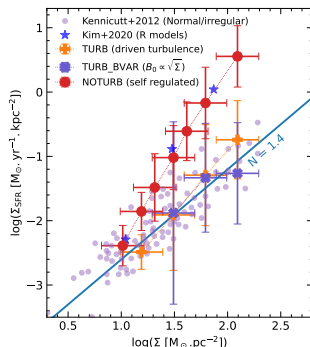
# Power needed to retrieve the Schmidt-Kennicutt relation



**Stellar feedback is not powerful enough to quench star formation.**

# Conclusion of part II

- ★ Role of stellar feedback.
  - ★ Not **powerful** enough to quench star formation in gas-rich galaxies
- ⌚ Role of large scale turbulence.
  - ⌚ A suitable candidate for gas-rich galaxies
  - ⌚ Increase **speed dispersion** and **anisotropy**
  - ⌚ **Solenoidal** driving 10x more **efficient**



## IV - Full galactic simulations



### Outline

#### I - Introduction

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A - Stellar feedback

B - Large scale turbulence

#### III - Full galactic simulations

#### IV - Conclusions

## Constraining the turbulent driving

Is the turbulence we inject realistic ?

What would be a realistic turbulent driving at these scales for gas-rich galaxies?

- ▶ analytical models (gravoturbulence (Nusser+2022), radials motions (Krumholtz+2018), accretion from outside the galaxy (Forbes+2022))
- ▶ observational constraints (PHANGS, Sun+2022),
- ▶ galactic scale simulations.

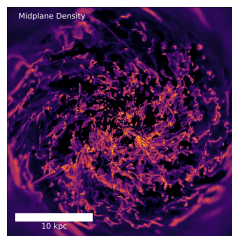
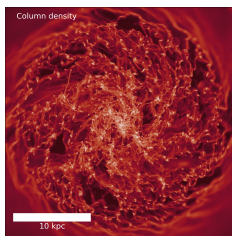
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- ▶ observational constraints (PHANGS, Sun+2022),
- ▶ **galactic scale simulations.**

**Work in progress: galactic scale simulations and measure turbulence**



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 $\sigma$  $\chi$ 

# Scale

Small: &lt; 10 pc

Medium: 1 pc-1 kpc

Large: 100 pc to 20 kpc

## Outline

III - Full galactic simulations

Focus

Included

Not included



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# Scale

Small: ~~< 10 pc~~

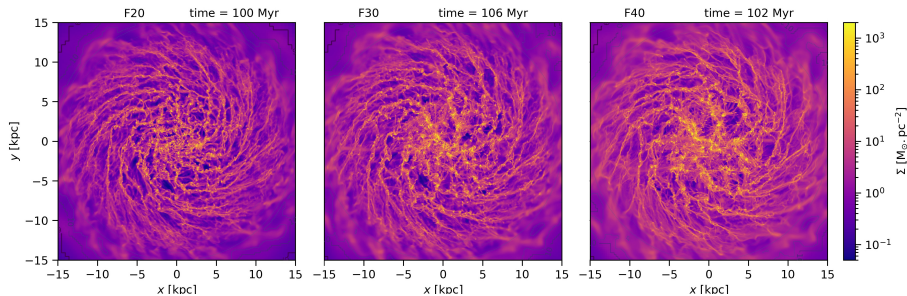
Medium: 1 pc to 1 kpc

Large: 100 pc to 20 kpc

## Outline

III - Full galactic simulations

# Column density maps



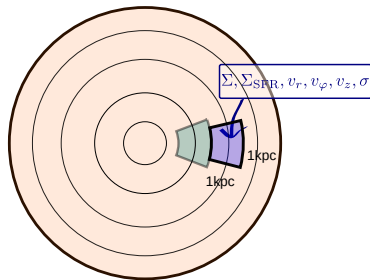
Gas Fraction: 20 %

30%

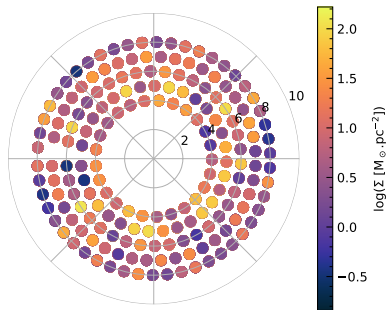
40%

# First insights

## Sectors extraction

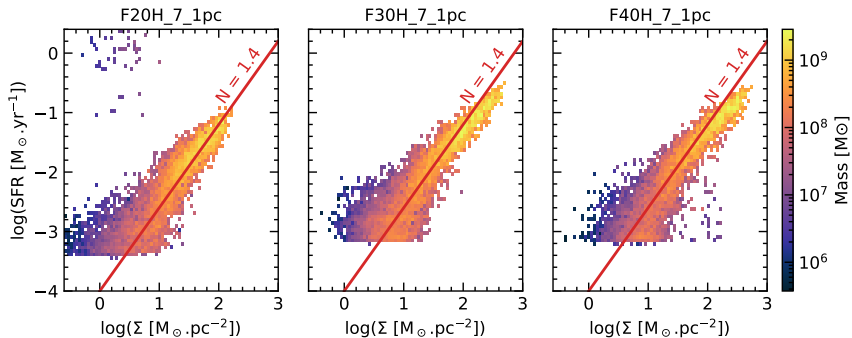


Sector extraction



Position of the extracted sectors

## SFR and Schmidt-Kennicutt law



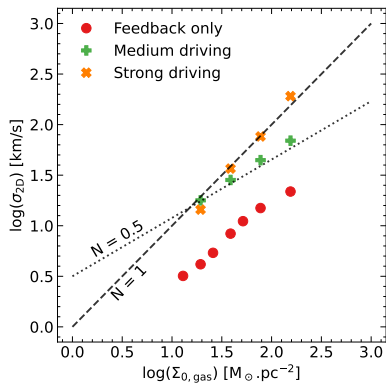
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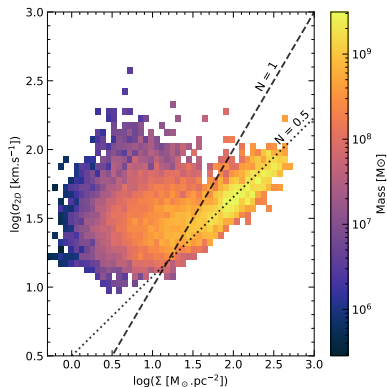
40%

# Comparison between kpc boxes and full galaxy simulations

Preliminary results on velocity dispersion for a galaxy with 30 % gas fraction



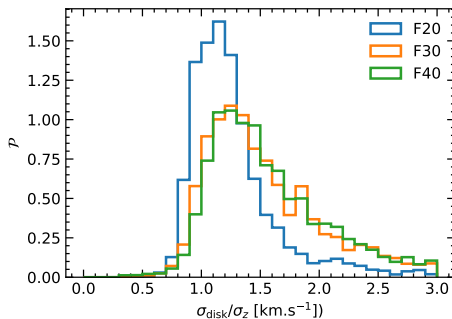
Box simulations



Galactic simulation

# Comparison between kpc boxes and full galaxy simulations

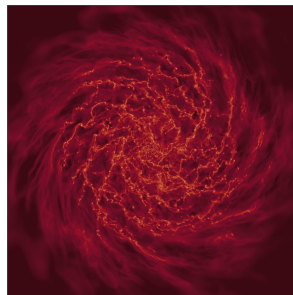
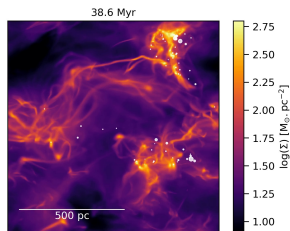
Preliminary results on velocity dispersion for a galaxy with 30 % gas fraction



**Turbulence is less strong and anisotropic than our requirements in kpc simulations**

# Summary

- ▶ Feedback regulation is suitable in Milky-way like galaxies but not in higher column density environments,
- ▶ The turbulence from large scale motions in the galaxy interacts
- ▶ Galactic simulations can be used to constrain turbulent driving at the kiloparsec scale.



# Perspective

- ▶ Completion of the parameter study at the kiloparsec scale
- ▶ **Better understanding of the turbulence injection**
  - ▶ Fourier analysis of the galactic scale simulation
  - ▶ Tracking where the turbulent energy come from
  - ▶ Add magnetic field
- ▶ How much the SFR is quenched? (this work) → How?
  - ▶ Work on the link between SFR and turbulence
  - ▶ Similar work on feedback



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# Appendix

Turbox

Galturb

Fragdisk

Model for radial profiles

Q

Numerical turbulence

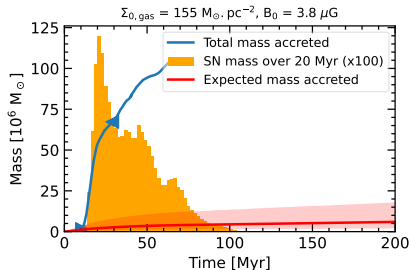
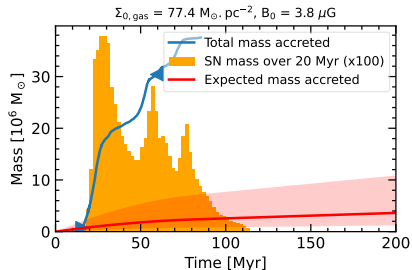
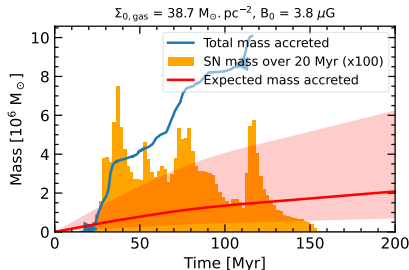
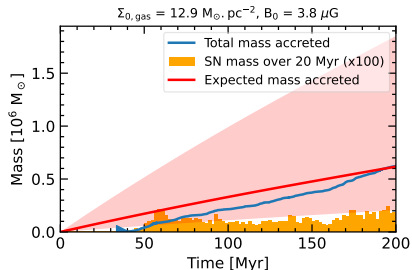
Equations

Initial conditions

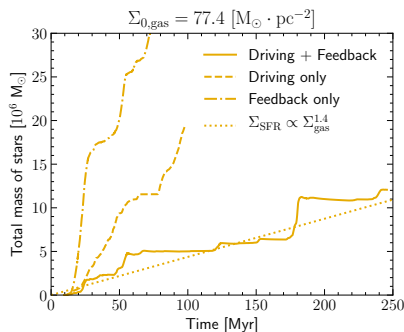
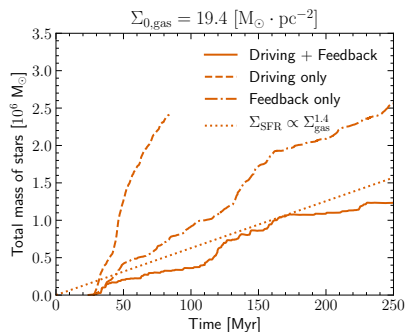
Context & SOA

More results

# With only stellar feedbacks



## Is stellar feedback needed ?



Stellar feedback is necessary, but its importance decreases as the gas column density increases.

# The influence of larger-scale dynamics: turbulent driving



## Turbulence from galactic dynamics

- ▶ Spirals, mass transfert → turbulence (eg. Krumholz+ 2018)

# The influence of larger-scale dynamics: turbulent driving

$\epsilon$  specific power injected

$v_l$  typical speed at a scale  $l$

$\sigma_g$  speed dispersion of the gas

$$\epsilon \sim \frac{v_l^3}{l}, \quad (1)$$

## Turbulence from galactic dynamics

- ▶ Spirals, mass transfert  $\rightarrow$  turbulence (eg. Krumholz+ 2018)
- ▶ Expected injected power:  
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# The influence of larger-scale dynamics: turbulent driving

$$\epsilon \sim \frac{v_l^3}{l} \propto \sigma_g^3, \quad (1)$$

$Q$  Toomre parameter  
 $\kappa$  epicyclic frequency  
 $\Sigma_g$  gas column density  
 $G$  gravitational constant

$$Q = \frac{\sigma_g \kappa}{\pi \Sigma_g G} \propto \frac{\sigma_g \kappa}{\Sigma_g} \sim 1, \quad (2)$$

## Turbulence from galactic dynamics

- ▶ Spirals, mass transfer  $\rightarrow$  turbulence (eg. Krumholz+ 2018)
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2 cases:  $\kappa \propto \sigma_g$  or constant  $\kappa$

$$\sigma_g \propto \Sigma_g^{0.5} \text{ or } \sigma_g \propto \Sigma_g, \quad (3)$$

$$\epsilon \propto \Sigma_g^{1.5} \text{ or } \epsilon \propto \Sigma_g^3, \quad (4)$$

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2 cases:  $\kappa \propto \sigma_g$  or constant  $\kappa$

$$\sigma_g \propto \Sigma_g^{0.5} \text{ or } \sigma_g \propto \Sigma_g, \quad (3)$$

$$\epsilon \propto \Sigma_g^{1.5} \text{ or } \epsilon \propto \Sigma_g^3, \quad (4)$$

$$P_{\text{LS}} \propto \Sigma_g^{2.5} \text{ or } P_{\text{LS}} \propto \Sigma_g^4. \quad (5)$$

with  $P_{\text{LS}}$  the total power injected.

## Turbulence from galactic dynamics

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$$\mathbf{f}(\mathbf{x}, t) = f_{\text{rms}} \times \int \hat{\mathbf{f}}(\mathbf{k}, t) e^{i\mathbf{k} \cdot \mathbf{x}} d^3\mathbf{k}$$

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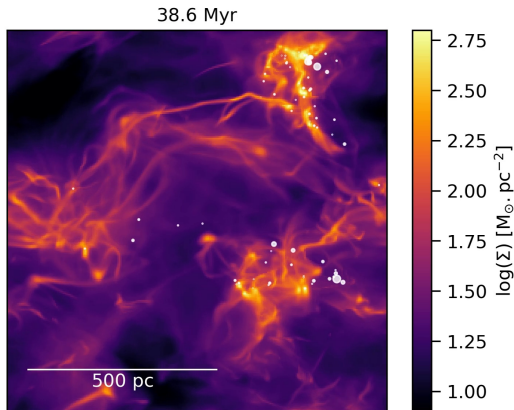
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## Model

An extra 2D force is added to generate random motion at scales between 300 and 1000 pc.

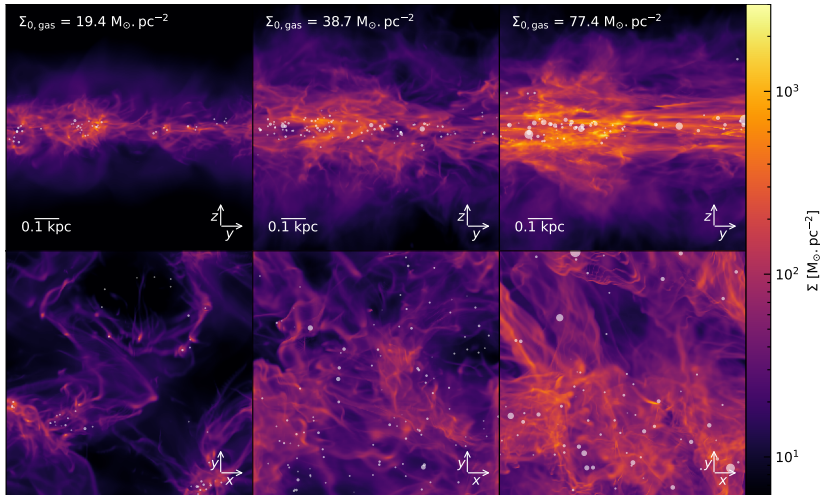
# With large-scale turbulence driving

$\Sigma = 38.7 M_{\odot} \cdot \text{pc}^{-2}$ , strong driving. Face on views of column density

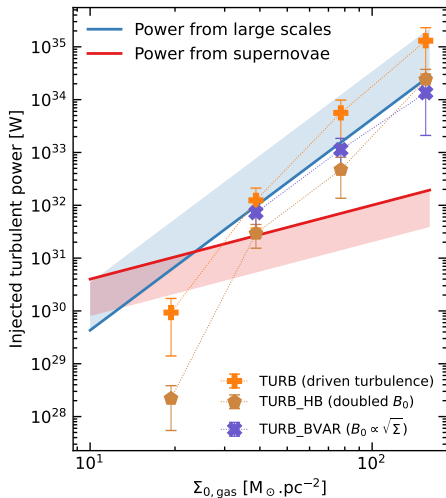
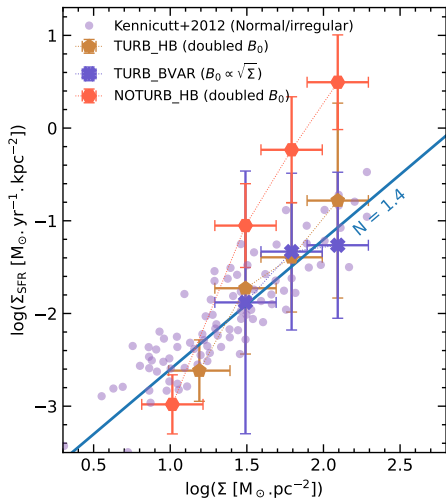


# Can we reproduce Schmidt-Kennicutt with turbulence driving?

Column density maps

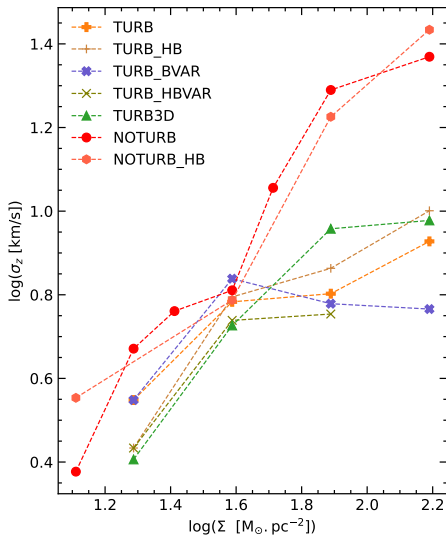
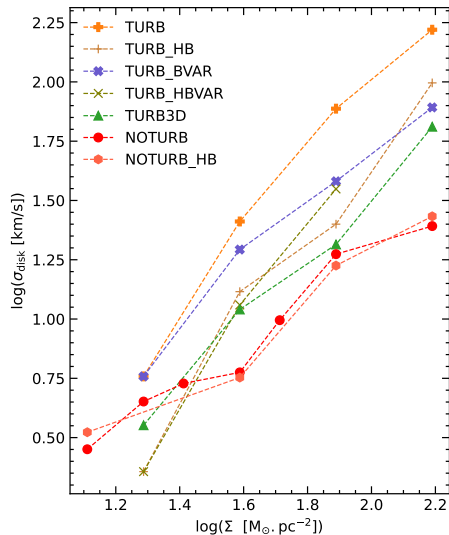


## High magnetic field

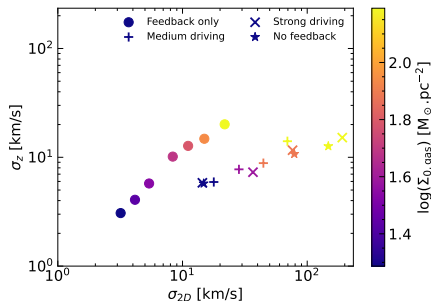
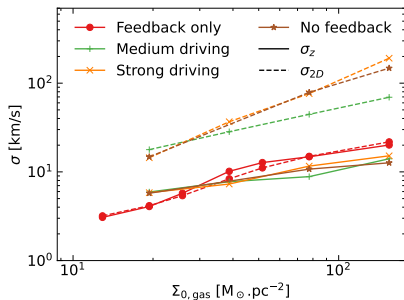


Even with higher B field, we cannot reproduce SK without injecting turbulence

## Velocity dispersion



# A word about velocity dispersion



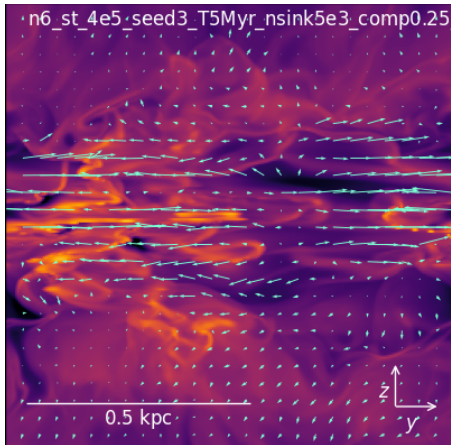
Velocity dispersion measured in the simulations, where

$$\sigma_{2D} = \sqrt{\sigma_x^2 + \sigma_y^2} / \sqrt{2}.$$

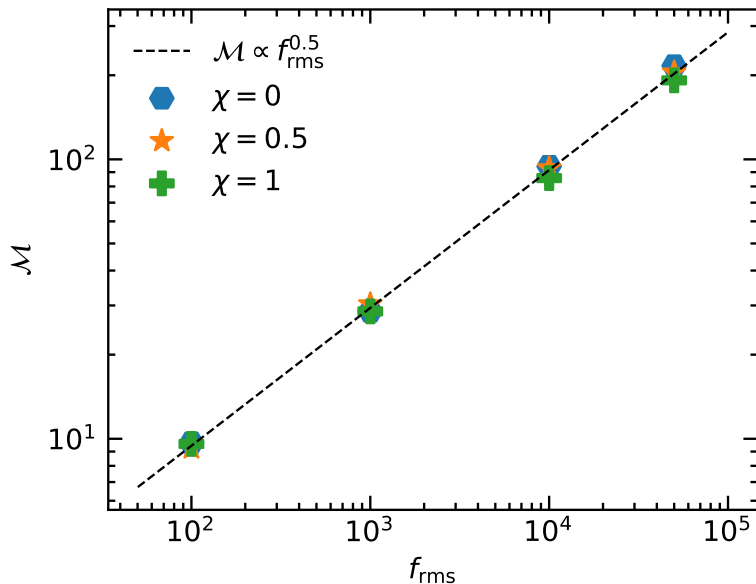
The simulations with high 2D turbulent driving show a high anisotropy, while simulations without driving are almost isotropic.



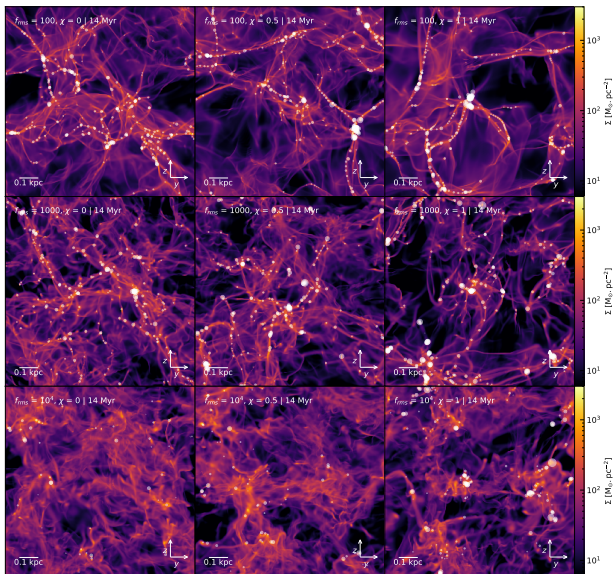
# Apodized Driving



## Further study (WIP): Link between SFR and turbulence

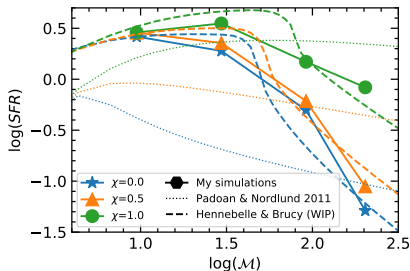
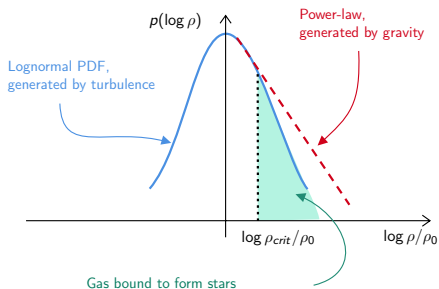


## Further study (WIP): Link between SFR and turbulence



# Further study (WIP): Link between SFR and turbulence

Using an idealized turbulent box

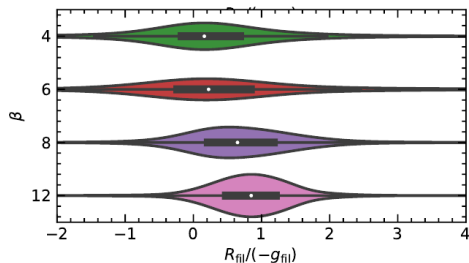


- Goal: improve existing analytical SFR models for higher Mach number.

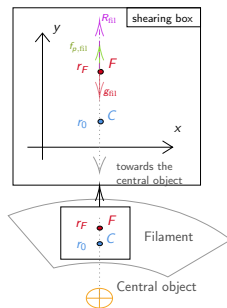
## Analytical model for filaments

- ▶ First try : pure hydrostatic model
- ▶ only self-gravity and pressure.
- ▶ We solved the Lane-Emden equations for a cylindrical distribution.
- ▶ Does not convincingly match the simulations

# Analytical model for filaments



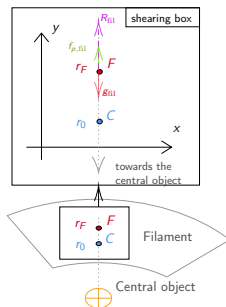
Support due to differential rotation plays a role !



# Analytical model for filaments

Simplifying assumptions:

1. shearing box approximation,
2. mechanical equilibrium,
3. gas is locally isothermal,
4. filaments are thin.



# Analytical model for filaments

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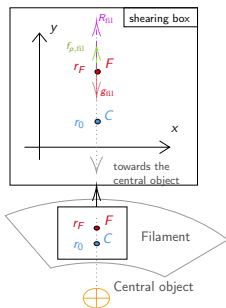
1. shearing box approximation,
2. mechanical equilibrium,
3. gas is locally isothermal,
4. filaments are thin.

We end up with a integro-differential equation for the normalized column density  $\tilde{\Sigma}$  in the filament.

$$\frac{\partial_{\tilde{y}} \tilde{\Sigma}}{\tilde{\Sigma}} = \int_0^{\tilde{\Lambda}} \tilde{\Sigma}(0, y') D(y', \tilde{y}, \varepsilon) dy' + \tilde{y}. \quad (1)$$

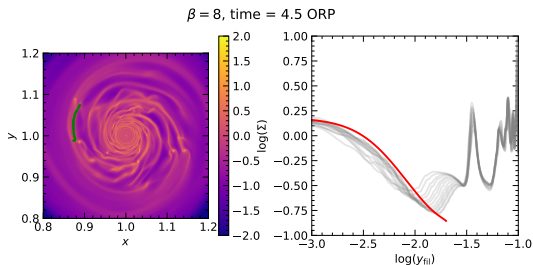
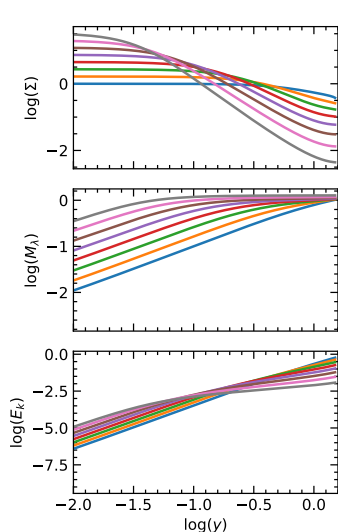
where

$$D(y, y', \varepsilon) = \frac{y' - y}{(y - y')^2 + \varepsilon^2} - \frac{y' + y}{(y' + y)^2 + \varepsilon^2} \quad (2)$$



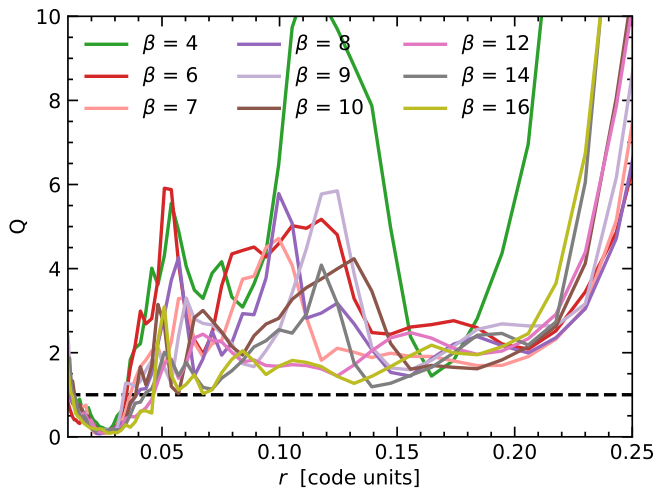


# Analytical model for filaments

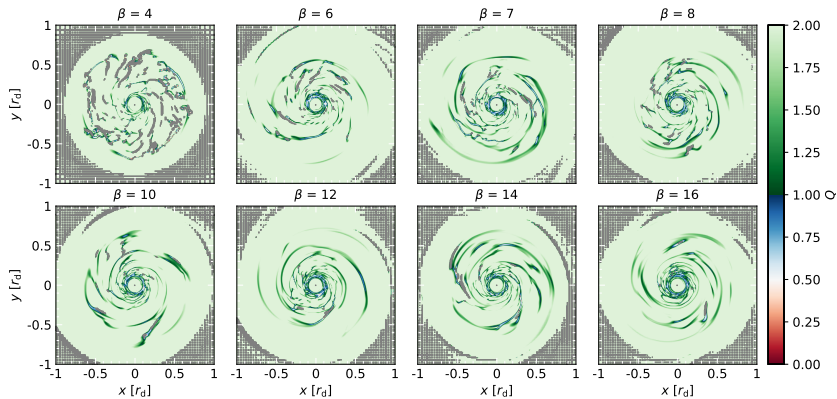


- ▶ The model enables to build a sequence of equilibrium (left)
- ▶ The model can be fitted to actual filaments in the simulation (top)
- ▶ BUT the model cannot explain the slope of the  $\Sigma$ -PDF (profile too stiff, PDF too flat).

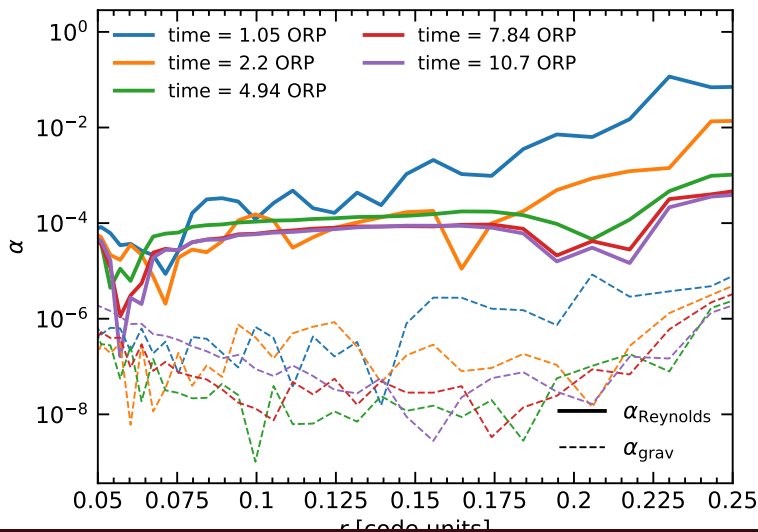
Q



Q



## Alpha - Q = 3



## HD equations

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{u}) = 0, \quad (3)$$

$$\frac{\partial \mathbf{u}}{\partial t} + \mathbf{u} \cdot \nabla \mathbf{u} + \frac{1}{\rho} \nabla P = -\frac{GM}{r^2 + z^2} (\cos(\theta) \mathbf{e}_r + \sin(\theta) \mathbf{e}_z) \quad (4)$$

$$\frac{\partial E}{\partial t} + \nabla \cdot ((E + P) \mathbf{u}) = 0 \quad (5)$$

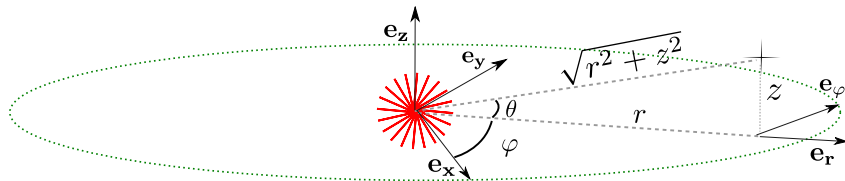


Figure: Coordinate system.

## Self-gravity

New source term in Euler equation. Poisson potential:

$$\Delta\phi = -4\pi G\rho$$

## Cooling

New source term in energy equation:

$$\frac{\partial E}{\partial t} + \nabla \cdot ((E + P) \mathbf{u}) = -\frac{E_{int}}{t_{cool}}$$

where  $E_{int} = E - E_c$  is the internal energy and  $E_c = \frac{1}{2}\rho\mathbf{u}^2$  is the kinetic energy.

Cooling time  $t_{cool} = \beta\Omega^{-1}$

# Initial conditions

## Vertical equilibrium

$$\frac{1}{\rho} \frac{\partial P}{\partial z} + \frac{GM \sin(\theta)}{r^2 + z^2} = 0$$

$$\rho(r, z) = \rho_c(r) \exp \left( \frac{GM}{c_s^2} \left( \frac{1}{\sqrt{r^2 + z^2}} \right) - \frac{1}{r} \right)$$

where  $\rho_c(r)$  is a free parameter chosen so that  $\Sigma \propto r^{-1}$

## Initial conditions

## Radial equilibrium

$$\frac{u_\varphi^2}{r} = \frac{1}{\rho} \frac{\partial(c_s^2 \rho)}{\partial r} + r \frac{GM}{(r^2 + z^2)^{3/2}}$$

$$\Omega^2 = \frac{1}{\rho r} \frac{\partial(c_s^2 \rho)}{\partial r} + \frac{GM}{(r^2 + z^2)^{3/2}}$$

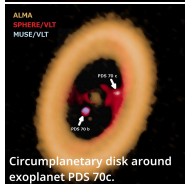
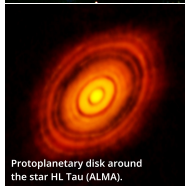
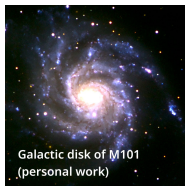
$$\Omega^2(r \leq r_{in}) = \frac{GM}{r^3} - \frac{5}{2} \frac{c_s^2}{r^2}$$

$$\Omega^2(r > r_{in}) = \frac{GM}{r^2 \sqrt{r^2 + z^2}} - \frac{7}{2} \frac{c_s^2}{r^2}$$

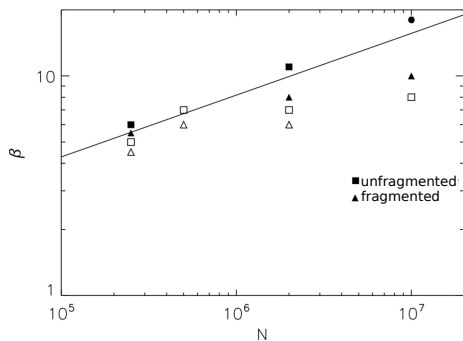


# Fragmentation of self-gravitating disks

- ▶ Self-gravitating disks: disks massive enough so that their own gravity plays an significant role.
- ▶ Can be found around black holes (galaxies), stars (protoplanetary disks) or planets (circumplanetary disks).
- ▶ Fragmentation, when the gas collapse under is own gravity is important for star, planet and moon formation.

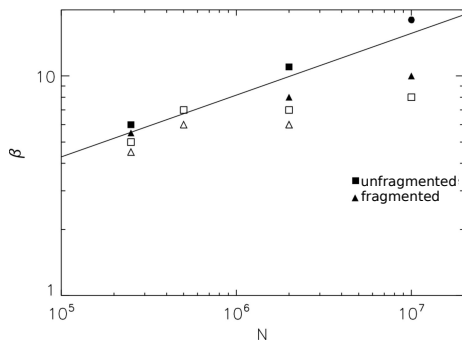


# Non-convergence of the stability limit



Critical value for  $\beta$  as a function of resolution, Meru & Bate 2012 and Rice et al. 2014.

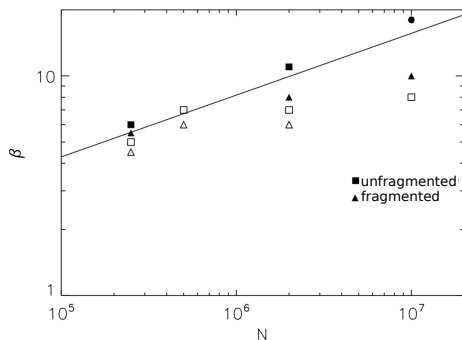
# Non-convergence of the stability limit



Paardekooper 2012, Hopkins 2013:  
Stochastic aspects

Critical value for  $\beta$  as a function of resolution, Meru & Bate 2012 and Rice et al. 2014.

# Non-convergence of the stability limit



Critical value for  $\beta$  as a function of resolution, Meru & Bate 2012 and Rice et al. 2014.

Paardekooper 2012, Hopkins 2013:  
Stochastic aspects

The simulations are mainly SPH or on 2D fixed-size grid.

*"It would be interesting to try to understand the convergence problem with a Godunov scheme"*

Meru & Bate 2012

## Description of the simulations

### Code: Ramses

- ▶ Finite volumes over a 3D grid.
- ▶ Conservative scheme (Godunov).
- ▶ Adaptive Mesh refinement.

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- ▶  $M_{\text{disk}} = M_{\star}/10$ .
- ▶ Equilibrium:  $Q(t = 0) \geq 2$ .
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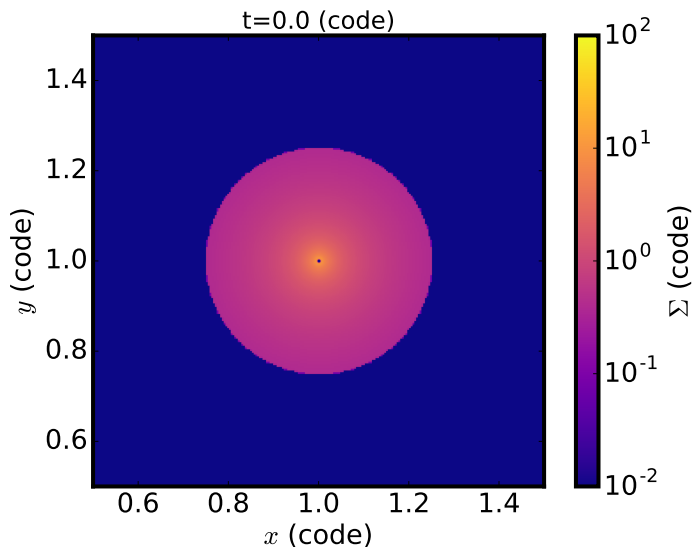
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## Resolution

Size of a cell  $dx = 2^{-l}$  where  $l$  is the level of refinement.

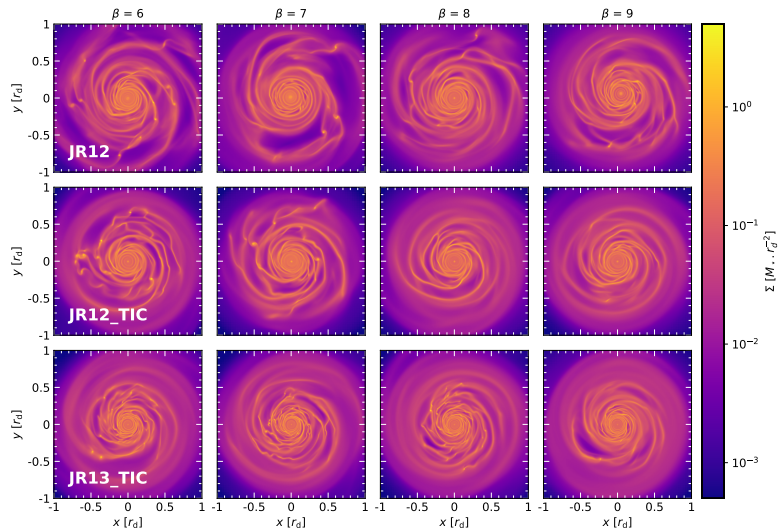
Grid at  $l = 6$  (box) and  $l = 10$  (disk, on  $256^3$  cells) + extra refinement based on jeans length  $\lambda_J$ . Cell refined if  $l < l_{\text{max}}$  and  $dx > 20\lambda_J$ .

Group	$l_{\text{max}}$	Initial cond.
JR11	11	smooth
JR12	12	smooth
JR12_TIC	12	turbulent
JR13_TIC	13	turbulent

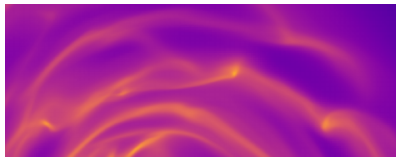
Results: movie for  $\beta = 7$  (group JR12)



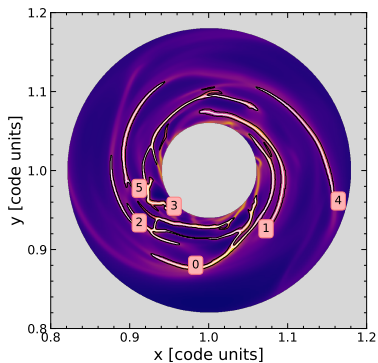
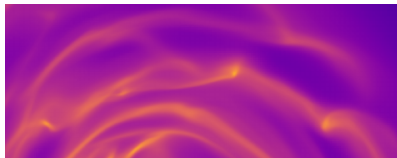
## Results: Column density maps



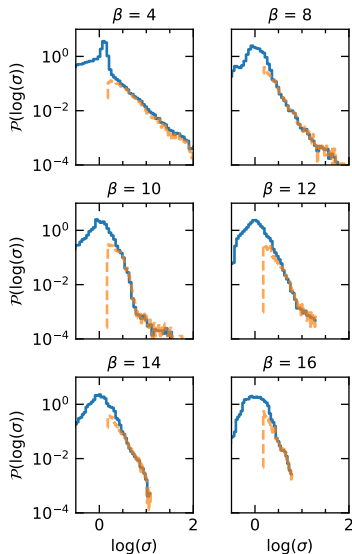
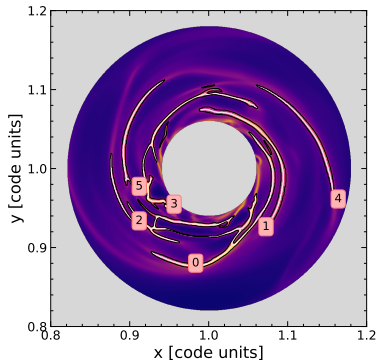
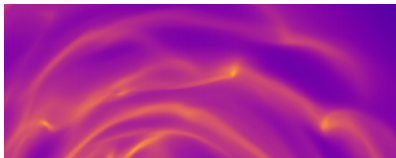
# What shapes the PDF ?



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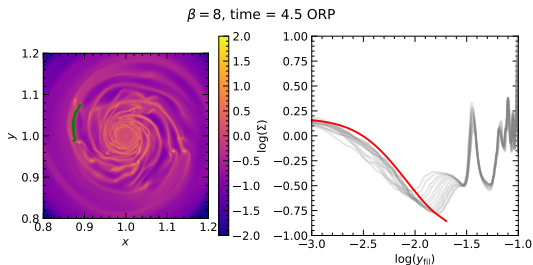
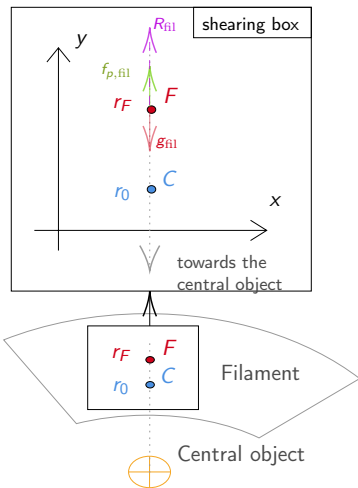


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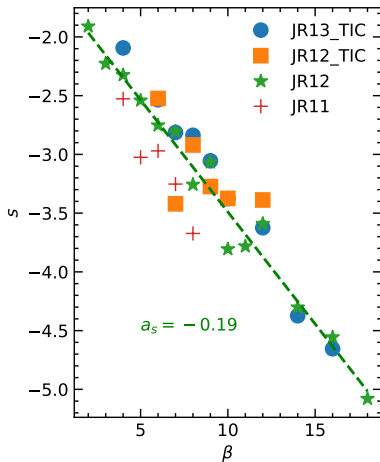
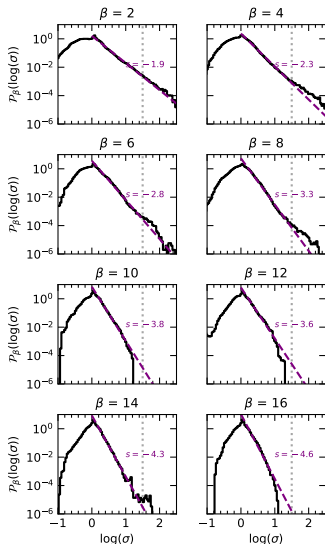


— disk    - - - filaments

# Analytical model for the radial profile of filaments

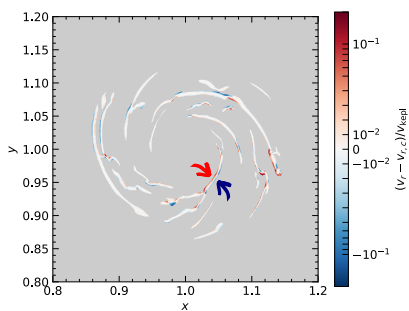


- Model of an infinite filament undergoing **pressure**, **tidal forces** and **self gravity**.
- The model can be fitted to actual filaments in the simulation (top)
- But the radial profile of filaments is not enough to understand the PDF

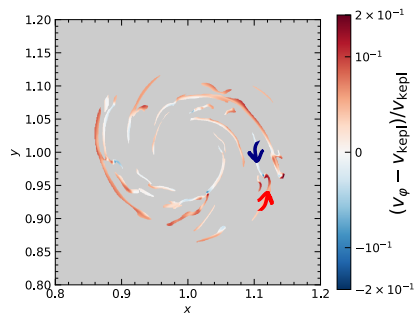
How to explain the  $s - \beta$  correlation ?

$$s = -0.2\beta - 1.6, \quad R^2 = 0.97$$

# The PDF is not built radially but alongside filaments



Radial collapse



Azimuthal collapse

Filaments are collapsing in the azimuthal direction.

## How to explain the $s - \beta$ correlation ?

Heating by gravitational instabilities in ring of mean column density  $\bar{\Sigma}$ , height  $h$ , and volume  $V$ .

$$\alpha_{\text{grav}} = \frac{2}{3} \frac{1}{4\pi G} \frac{2h}{\bar{\Sigma} c_s^2 V} \int_V g_r g_\varphi dV. \quad (6)$$



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$$\text{PDF}(\Sigma) = \frac{P_0}{\sigma_0 \bar{\Sigma}} \left( \frac{\Sigma}{\sigma_0 \bar{\Sigma}} \right)^{s-1}. \quad (7)$$

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we can write

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## How to explain the $s - \beta$ correlation ?

If self-gravity dominates, we can approximate

$$g_r \simeq \varepsilon_r 2\pi G \Sigma \text{ and } g_\varphi \simeq \varepsilon_\varphi 2\pi G \Sigma \quad (9)$$

where  $\varepsilon_r$  and  $\varepsilon_\varphi$  are unknown efficiencies.

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$$\alpha_{\text{grav}} = -\frac{2}{3} \frac{2\pi G \bar{\Sigma} h \varepsilon_r \varepsilon_\varphi}{c_s^2} \frac{\sigma_0^2 P_0}{s + 2}. \quad (10)$$

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Finally, we retrieve a linear relationship between  $s$  and  $\beta$ :

$$s = -\frac{10}{3} \varepsilon_r \varepsilon_\varphi \sigma_0^2 P_0 \beta - 2. \quad (12)$$

