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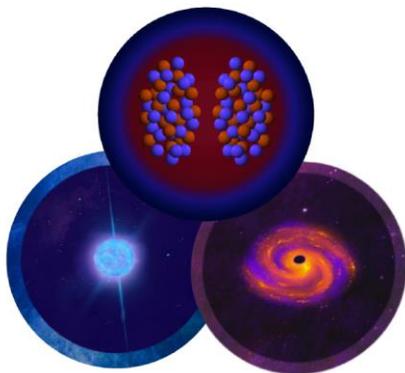
**DAAD**

**STRONG**  
2020

# Strangeness in Nuclear Matter

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(SUBATECH, Nantes)



**Second DMLab Meeting**  
12-13 December 2022 (DESY)



# Strangeness in Universe

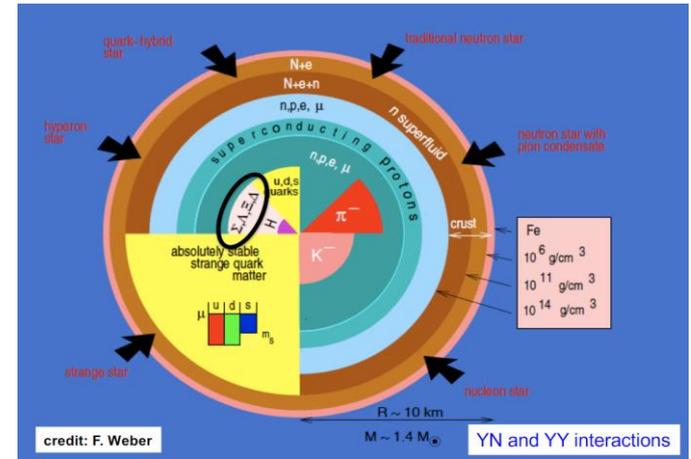
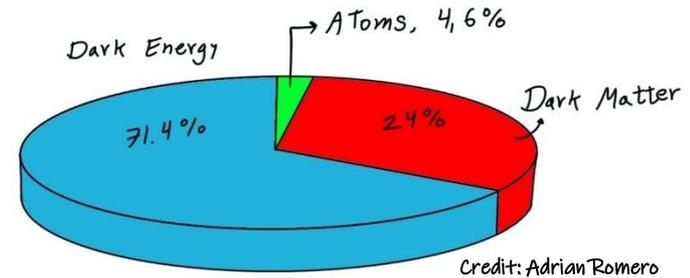
**Nuclear matter** is strangeness neutral

→ built of u,d quarks

**Strangeness conservation:** s-sbar quarks are produced in pairs only

**Strangeness in Universe:**  
in the core of neutron stars

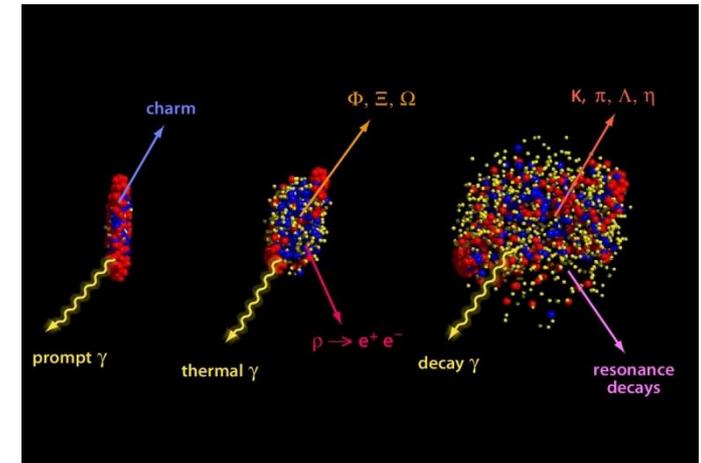
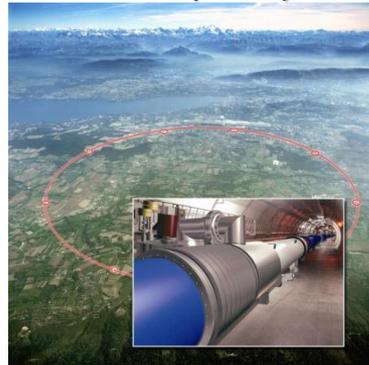
**Strangeness in Laboratory:**  
produced in heavy-ion experiments



SIS & FAIR (GSI)

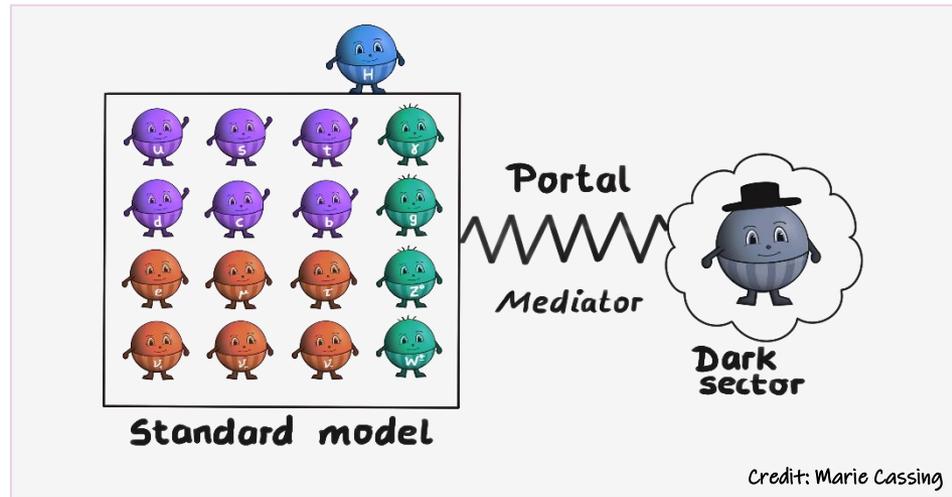


LHC (CERN)



# ,Strangeness' in DMLab

**DMLab:** search for **non-gravitational dark matter (DM)** interactions with normal matter, i.e. with **standard model (SM)** particles



**Strange particles** are important probes of the **properties of ,standard' matter:**

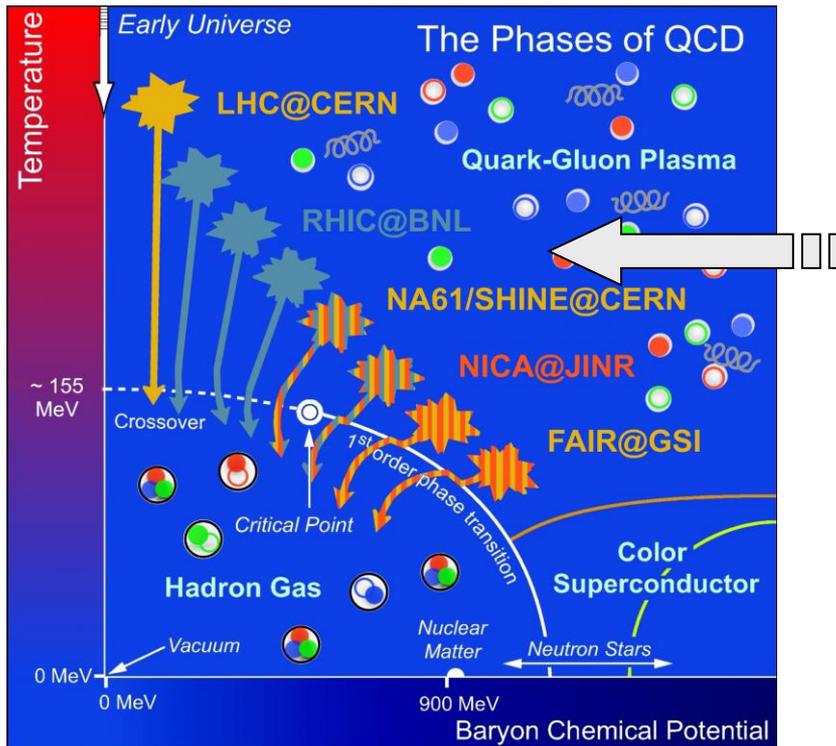
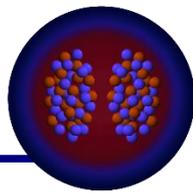
- Equation-of-State (EoS)**
- medium modification** of hadron properties in dense and hot matter and chiral symmetry restoration
- formation of the quark-gluon plasma (**QGP**) at high  $T$  and  $\mu_B$
- formation of **hypernuclei**
- strangeness in **neutron stars**

**Strange particles** can couple to **DM particles**

→ search for DM candidates in heavy-ion experiments



# Heavy-ion physics:



## The phase diagram of QCD:

- **Equation-of-State** of hot and dense matter?
- Study of the **phase transition** from hadronic to partonic matter – **Quark-Gluon-Plasma**
- Search for possible **critical point**
- Search for signatures of **chiral symmetry restoration**
- Study of the **in-medium properties of hadrons** (including strange mesons and baryons) at high baryon density and temperature

**Our goal:** to study the properties and dynamics of strongly interacting matter created in heavy-ion collisions on a **microscopic basis**

**Theory:** QCD + many body theory + microscopic transport theory

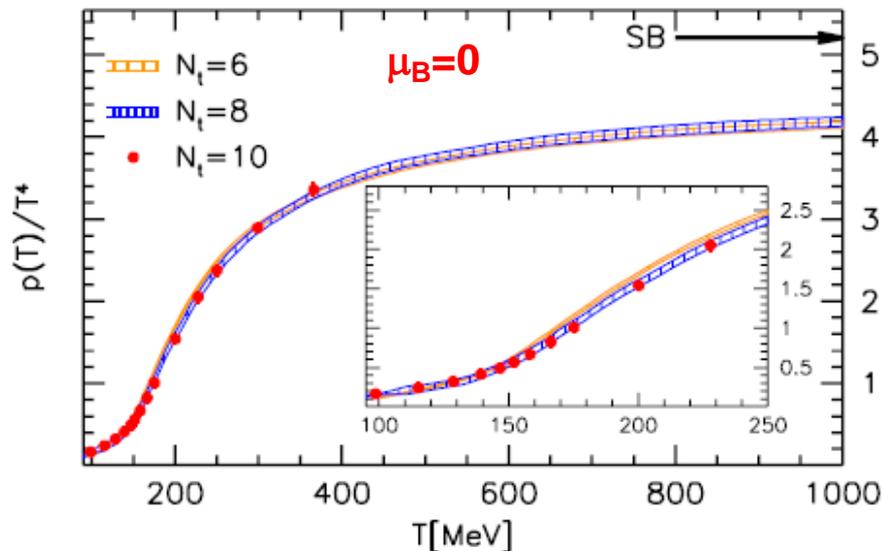
**Realization:** dynamical transport approaches → **PHSD** & **PHQMD**



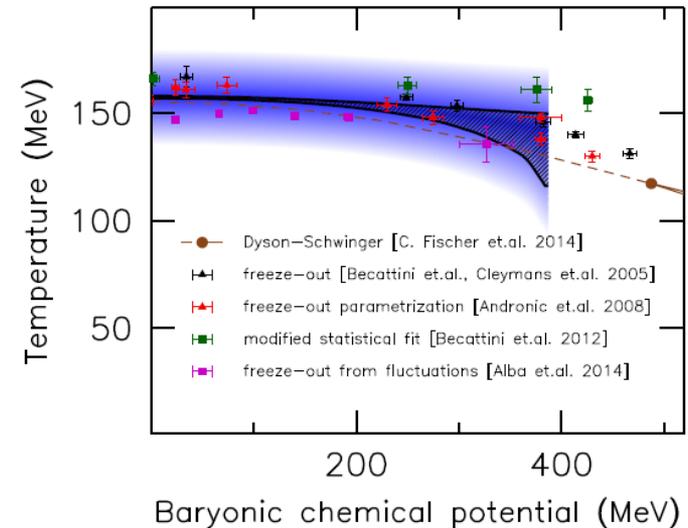
# Thermodynamics of QCD at finite $T$ and $\mu_B$

- For the **microscopic transport description** of the system one needs to know all degrees of freedom (hadronic and partonic) as well as their properties and interactions!

Thermal properties of QCD in  $(T, \mu_B)$  plane  
 → **lattice QCD** – limited to the low  $\mu_B < 400$  MeV



IQCD: J. Guenther et al.,  
 Nucl. Phys. A 967 (2017) 720



Lattice QCD results up to  $\mu_B < 400$  MeV:

**Crossover:** hadron gas → QGP

How to learn about the EoS and degrees-of-freedom of the matter from HICs?

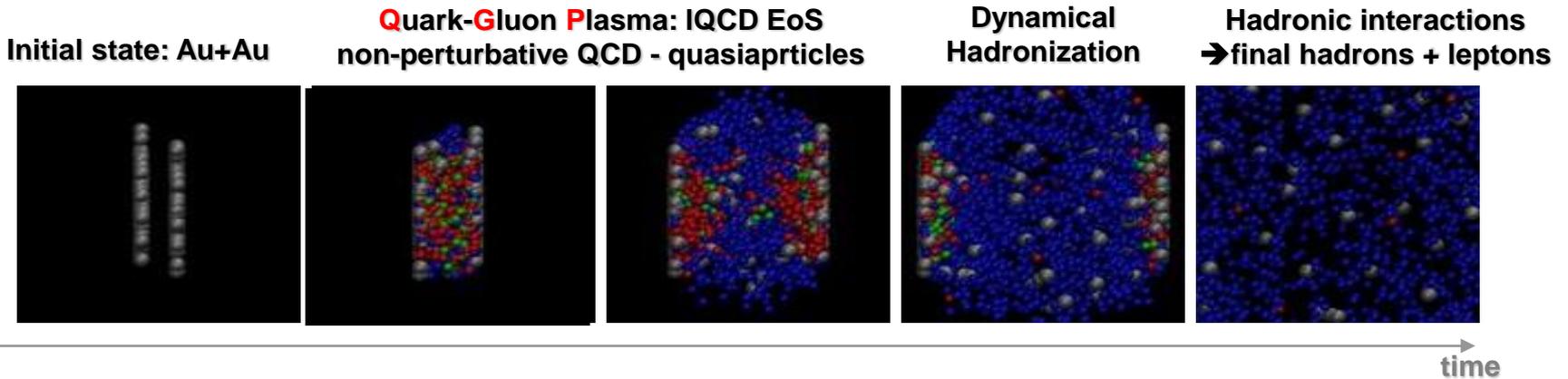
→ **microscopic transport approaches** → comparison to HIC experiments



# Dynamical modeling of heavy-ion collisions - PHSD

**Parton-Hadron-String Dynamics (PHSD)** is a **non-equilibrium microscopic transport approach** for the description of dynamics of strongly-interacting hadronic and partonic matter created in heavy-ion collisions

**Dynamics:** based on the solution of generalized off-shell transport equations derived from Kadanoff-Baym many-body theory (beyond semi-classical BUU)



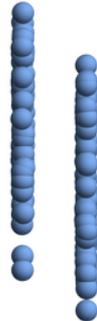
→ PHSD provides a good description of ‘bulk’ hadronic and electromagnetic observables from SIS to LHC energies

→ PHSD can be used for the theoretical **study of the DM production in HICs:** cf. recent extension beyond SM sector: dark photon production in HICs



# Stages of a collision in PHSD

$t = 0.05 \text{ fm}/c$



$\text{Au} + \text{Au} \sqrt{s_{\text{NN}}} = 200 \text{ GeV}$

$b = 2.2 \text{ fm}$  – Section view

-  Baryons (394)
-  Antibaryons ( 0)
-  Mesons ( 0)
-  Quarks ( 0)
-  Gluons ( 0)

# Stages of a collision in PHSD

$t = 1.6512 \text{ fm}/c$



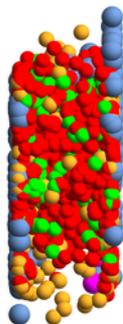
$\text{Au} + \text{Au} \sqrt{s_{\text{NN}}} = 200 \text{ GeV}$

$b = 2.2 \text{ fm}$  – Section view

-  Baryons (394)
-  Antibaryons ( 0)
-  Mesons (1523)
-  Quarks (4553)
-  Gluons (368)

# Stages of a collision in PHSD

$t = 3.91921 \text{ fm}/c$



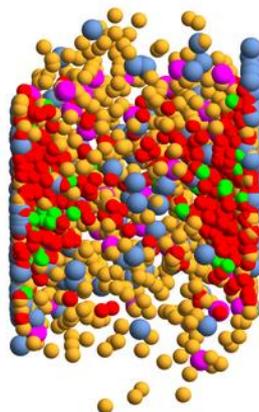
$\text{Au} + \text{Au} \sqrt{s_{\text{NN}}} = 200 \text{ GeV}$

$b = 2.2 \text{ fm}$  – Section view

-  Baryons (426)
-  Antibaryons ( 29)
-  Mesons (1189)
-  Quarks (4459)
-  Gluons (783)

# Stages of a collision in PHSD

$t = 7.31921 \text{ fm}/c$



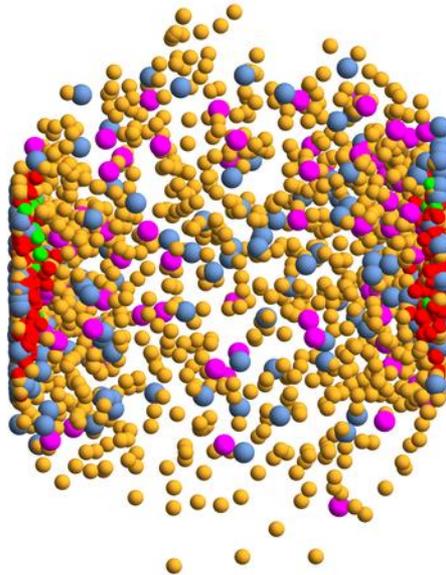
$\text{Au} + \text{Au} \sqrt{s_{\text{NN}}} = 200 \text{ GeV}$

$b = 2.2 \text{ fm}$  – Section view

-  Baryons (540)
-  Antibaryons (120)
-  Mesons (2481)
-  Quarks (2901)
-  Gluons (492)

# Stages of a collision in PHSD

$t = 12.0192 \text{ fm}/c$



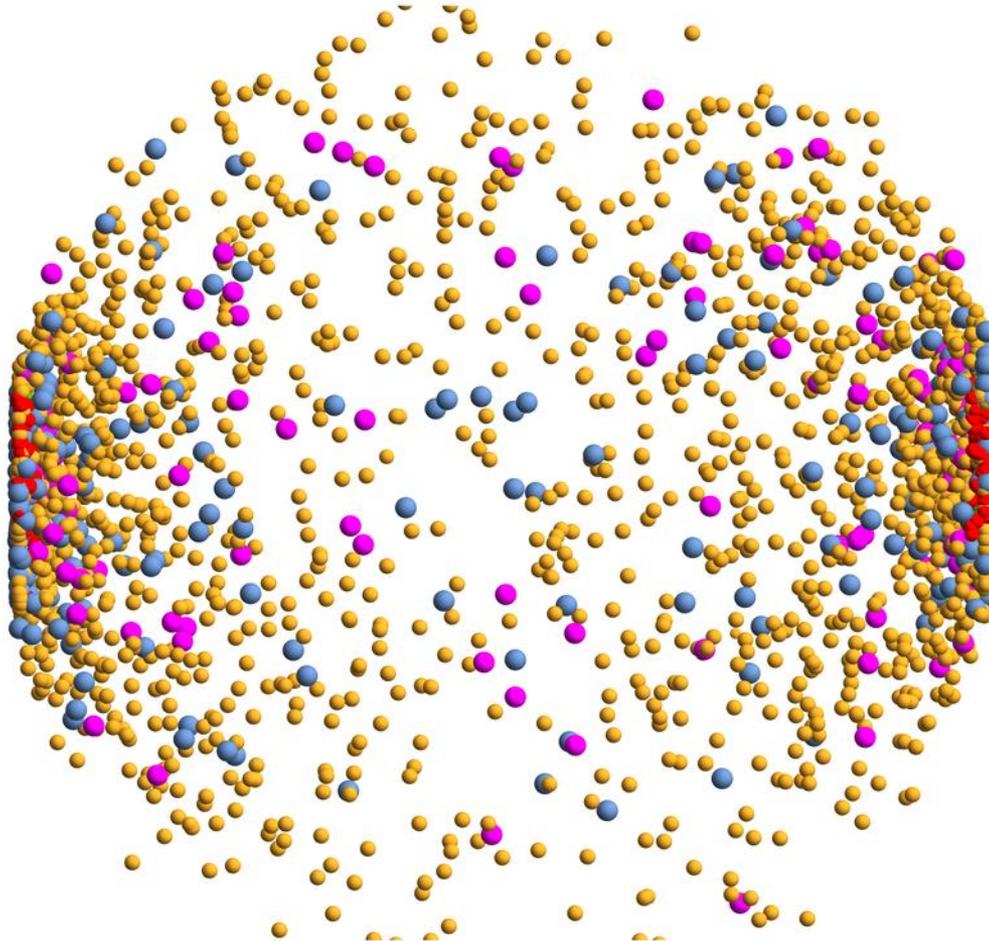
$\text{Au} + \text{Au} \sqrt{s_{\text{NN}}} = 200 \text{ GeV}$

$b = 2.2 \text{ fm}$  - Section view

-  Baryons (626)
-  Antibaryons (202)
-  Mesons (3357)
-  Quarks (1835)
-  Gluons (269)

# Stages of a collision in PHSD

$t = 25.5191 \text{ fm}/c$



$\text{Au} + \text{Au} \sqrt{s_{\text{NN}}} = 200 \text{ GeV}$

$b = 2.2 \text{ fm}$  - Section view

 Baryons (710)

 Antibaryons (272)

 Mesons (4343)

 Quarks ( 899)

 Gluons ( 46)

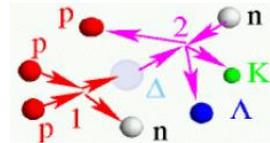
# Strangeness production in HICs

**GSI:** study strange meson (K, Kbar) production in A+A at (sub-)threshold energies

□ experimental observation of  $K^+$ ,  $K^-$  production below the NN-threshold

## I. Strangeness production channels at low energies

• baryon-baryon collisions:  $K = (K, K^0)$



Strange quark exchange between  $K^-$  and hyperons  $Y=(\Lambda, \Sigma)$

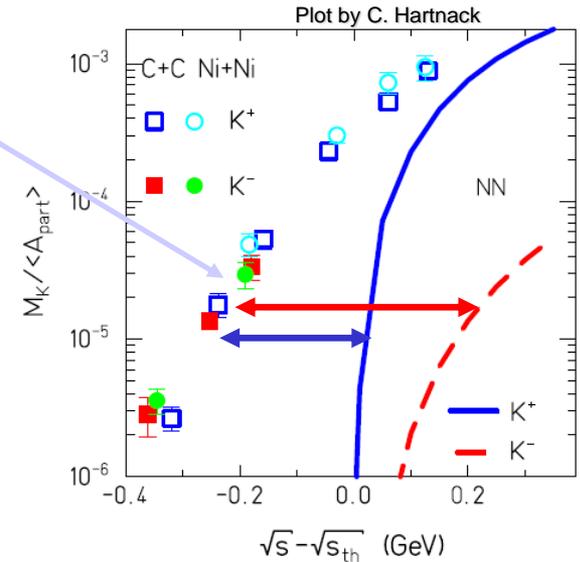
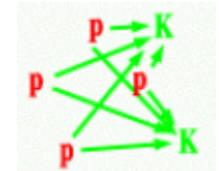
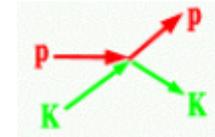
• meson-baryon collisions:  
dominant channel for low energy  $K^-$  production

• meson-meson collisions:  $\pi + \pi \rightarrow K + \bar{K}$

• resonance decays:  $\phi \rightarrow K + \bar{K}$

## II. Strangeness rescattering

= (quasi-)elastic scattering with baryons and mesons



The production cross sections and self-energies of K, Kbar are **modified in the nuclear medium** !

# In-medium effects for strange mesons

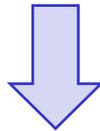
The hadrons - in particular **strange mesons (K, Kbar and K\*)** - modify their properties in the dense and hot nuclear medium due to the strong interaction with the environment

... long history ...

## Models:

□ chiral SU(3) model, chiral perturbation theory, relativistic mean-field models: KN-potential → **dropping' of K<sup>-</sup> mass and enhancement' of K<sup>+</sup> mass**

Kaplan and Nelson, PLB 175 (1986) 57;  
Weise, Brown, Schaffner, Krippa, Oset, Lutz, Mishra, ... et al.



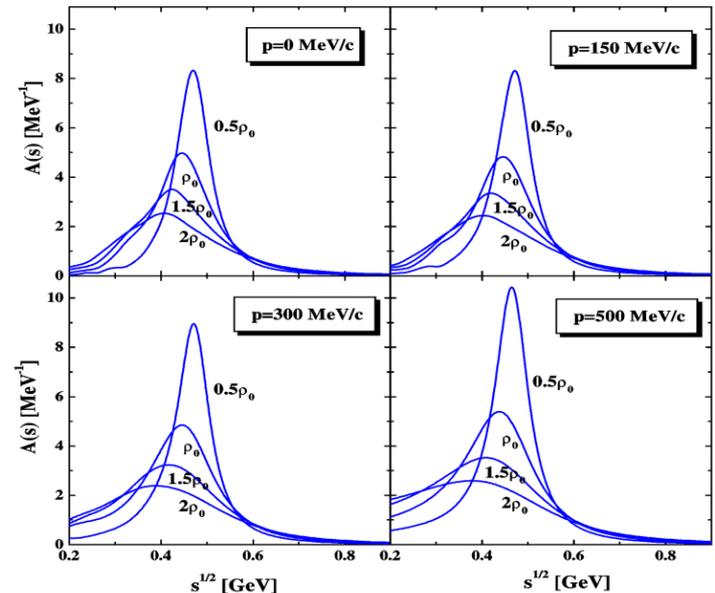
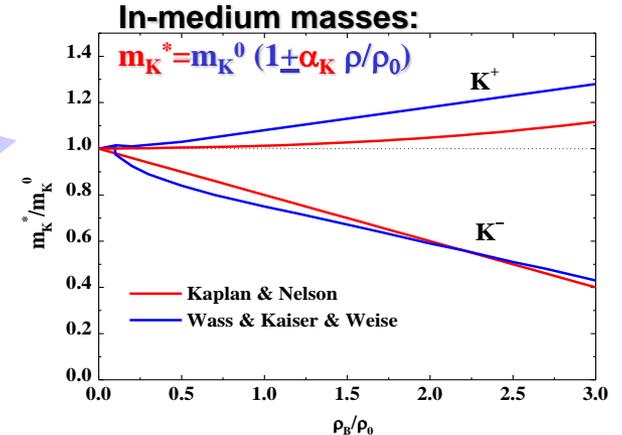
□ **self-consistent coupled-channel approach**  
- **G-matrix:**

→ momentum, density and temperature dependent **spectral function of antikaons A(p<sub>K</sub>, ρ, T):**  
in-medium modification of the real and imaginary part of the **self-energy Σ** (mass and width)

L. Tolos et al., NPA 690 (2001) 547

→ off-shell HSD: W. Cassing et al., Nucl.Phys.A 727 (2003) 59

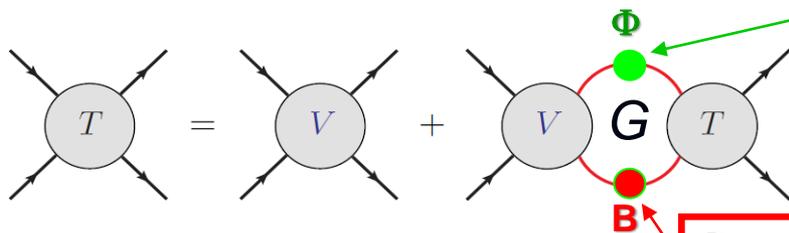
Cf. review: C. Hartnack et al., Phys.Rept. 510 (2012) 119



# The coupled-channel G-matrix approach

Solution of the **Bethe-Salpeter** equation in coupled channels:

**Medium:**



Meson selfenergy and spectral function

Baryons: Pauli blocking and potential dressing

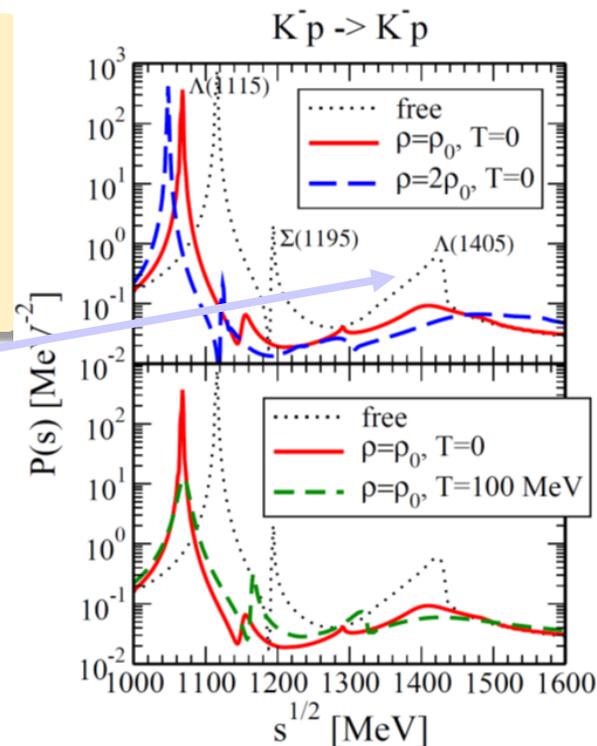
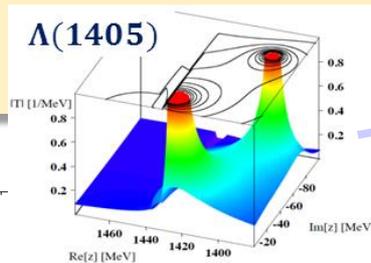
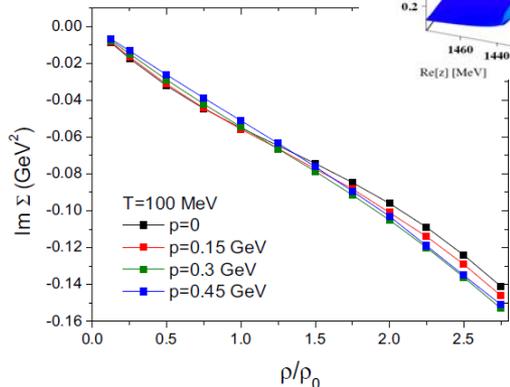
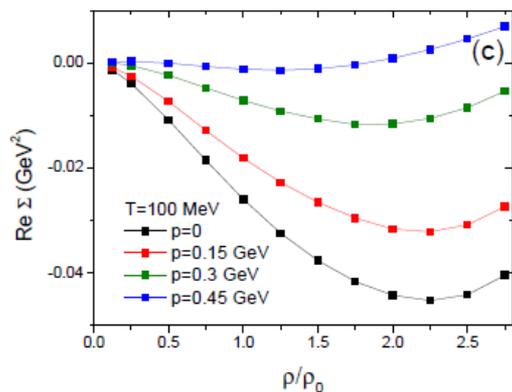
$$T_{ij}(\rho, T) = V_{ij} + V_{il} G_l(\rho, T) T_{lj}(\rho, T)$$

$$P \propto |T|^2$$

Coupled-channels [full  $SU(3)$  basis, isospin  $I = 0, 1$ ]

- $S = -1$ :  $K^-p, \bar{K}^0n, \pi^0\Lambda, \pi^0\Sigma^0, \eta\Lambda, \eta\Sigma^0, \pi^+\Sigma^-, \pi^-\Sigma^+, K^+\Xi^-, K^0\Xi^0, K^-n, \pi^0\Sigma^-, \pi^-\Sigma^0, \pi^-\Lambda, \eta\Sigma^-, K^0\Xi^-$
- $S = +1$ :  $K^+p; K^+n, K^0p$

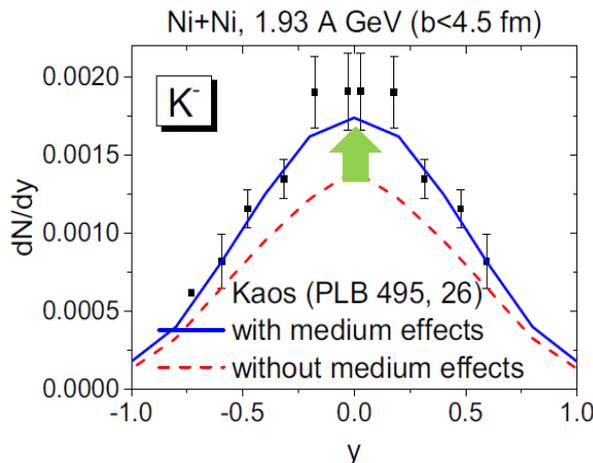
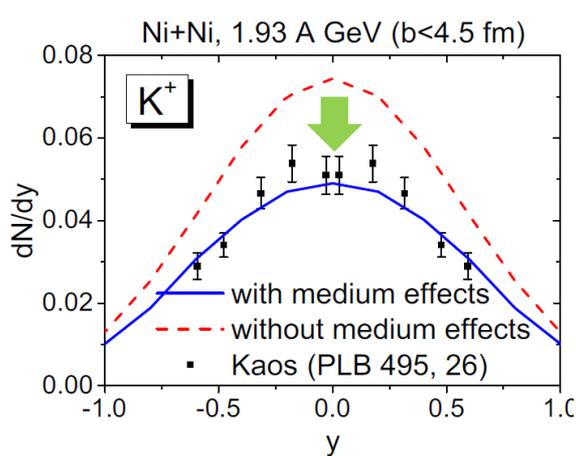
In-medium  $K^-$  self-energy:  $\Sigma = \text{Re}\Sigma + i \text{Im}\Sigma$



**G-matrix** (based on the Jülich meson-exchange model): L. Tolos et al., NPA 690 (2001) 547

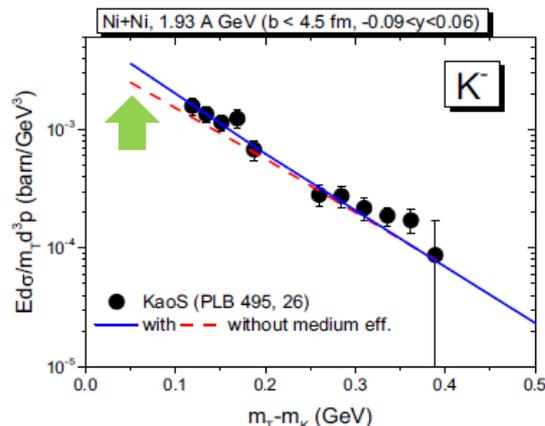
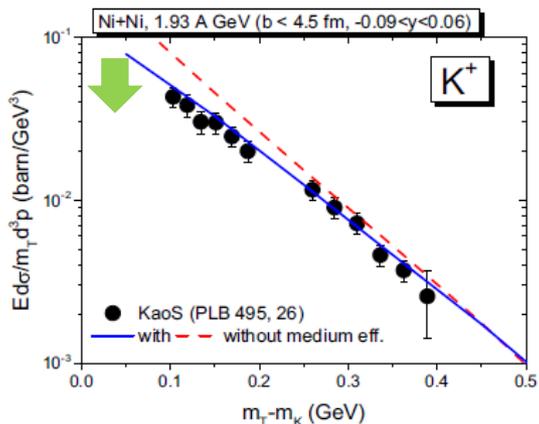
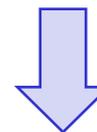
**Improved** (based on  $SU(3)$  mB chiral Lagrangian): D. Cabrera, L. Tolos, J. Aichelin, E.B., PRC90 (2014) 055207

# y- and $m_T$ spectra of (anti)kaons in central Ni+Ni collisions at 1.93 A GeV



## In-medium effects :

- suppresses kaon production
- hardens kaon spectrum
- enhances antikaon production
- softens antikaon spectrum

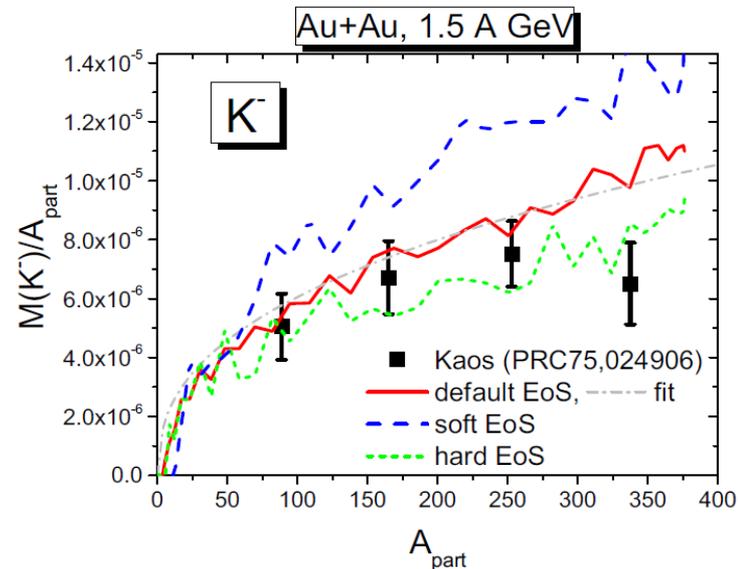
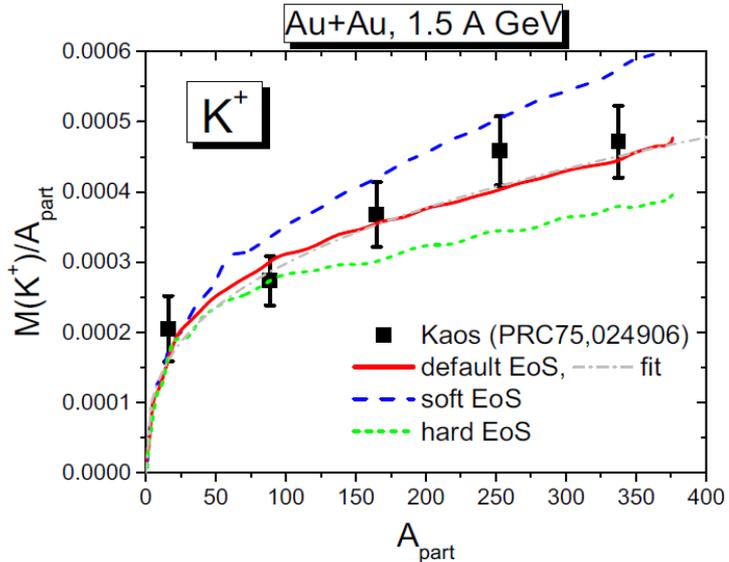


## Heavy-ion experiments at SIS energies (FOPI, KaoS, HADES):

Observables: invariant yield, rapidity spectra, ratios, flow, angular distributions →

- Moderate **repulsive** potential for  $K^+$
- Stronger **attractive** potential for  $K^-$
- $K^+$  and  $K^-$  exhibit different freeze-out conditions

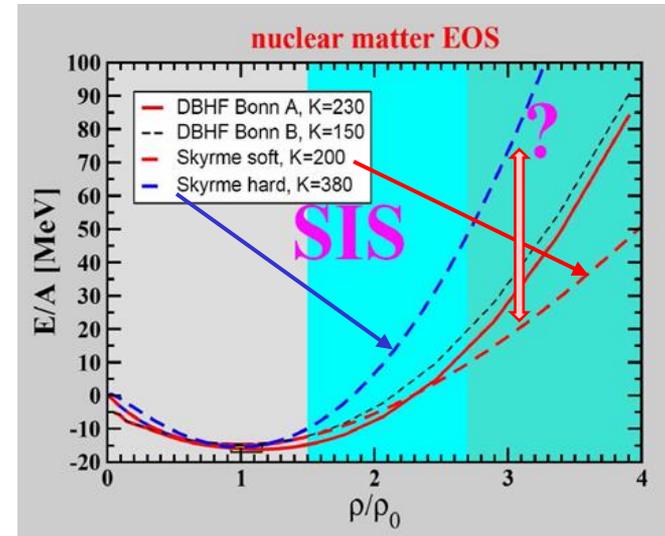
# Probing of EoS with strangeness



**Skyrme potential:**  $U(\rho) = a\left(\frac{\rho}{\rho_0}\right) + b\left(\frac{\rho}{\rho_0}\right)^\gamma$

where  $a = -153 \text{ MeV}$ ,  $b = 98.8 \text{ MeV}$ ,  $\gamma = 1.63$ .

**Compression modulus K:**  $K = -V \frac{dP}{dV} = 9\rho^2 \frac{\partial^2(E/A)}{\partial \rho^2} \Big|_{\rho_0}$



DBHF model: Dirak-Brückner-Hartree-Fock G-matrix – density and momentum dependent potential

## Sensitivity to EoS:

**Hard EoS:**  $K=380 \text{ MeV}$  → hard to be compressed, less NN collisions to produce (anti)kaons

**Default EoS:**  $K=300 \text{ MeV}$

**Soft EoS:**  $K=210 \text{ MeV}$  → easy to be compressed, more NN collisions to produce (anti)kaons

# From kaons in HICs ... to stars

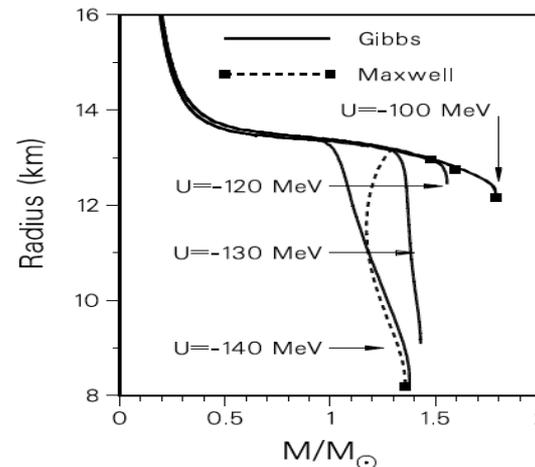
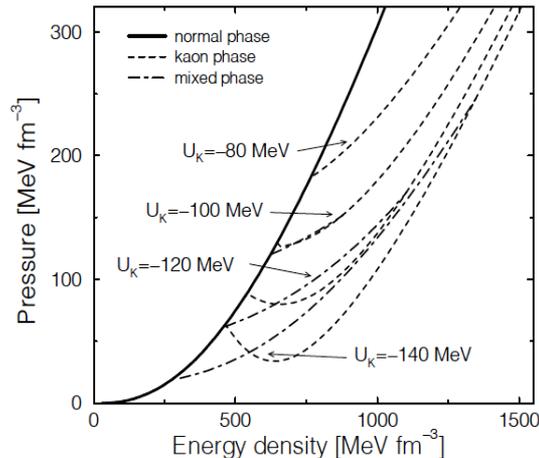
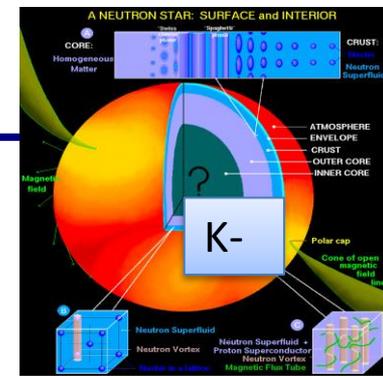
## Kaon condensation in neutron stars ?

\* Kaplan and Nelson '86 :

In-medium effects on (anti)kaons can be pronounced so as to have kaon condensation

\* Glendenning and Schaffner-Bielich '99 :

Antikaon potential at saturation density is deeper than -120 MeV



EoS is softened due to kaon condensation

The maximum star mass is lowered with increasing attractive K-N potential

## Constraints from theory and HICs:

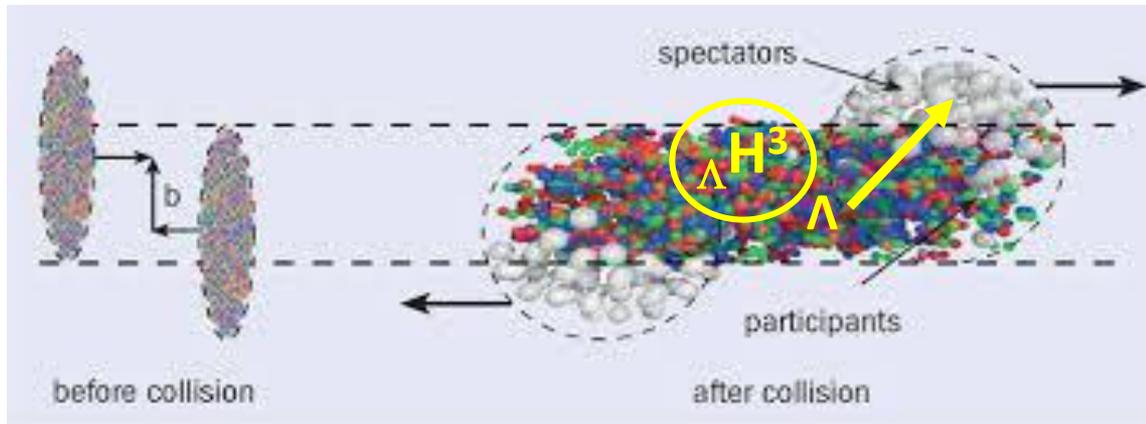
\* Tolos, Polls, Ramos '01; Cabrera, Tolos, Aichelin and E.B.'14; Song et al.'21

G-matrix unitarized scheme based on meson-exchange models or chiral Lagrangians predicts a moderate attraction in nuclear matter ← consistent with heavy-ion results!

→ kaon condensation in neutron stars seems very unlikely according to G-matrix model

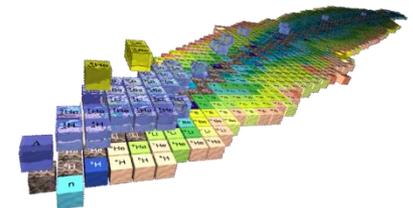
# Why do we study hypermatter production?

**Hyperons  $Y=(\Lambda, \Sigma)$**  are produced by elementary reactions during the heavy-ion collisions in the middle of the fireball and traverse to the target/projectile region by interactions with nuclear matter. They can form hypernuclei.



## Hypernuclei as bound objects:

- give information on **hyperon-nucleon (YN) and hyperon-hyperon (YY) interactions**
- **EoS** including strangeness
- give access to the **third dimension** of the nuclear chart (strangeness)
- important for **neutron stars** (production of hypermatter at high density and low temperature)
- new field of hyperon spectroscopy





**PHQMD:** a unified n-body microscopic transport approach for the description of heavy-ion collisions and **dynamical cluster formation** from low to ultra-relativistic energies

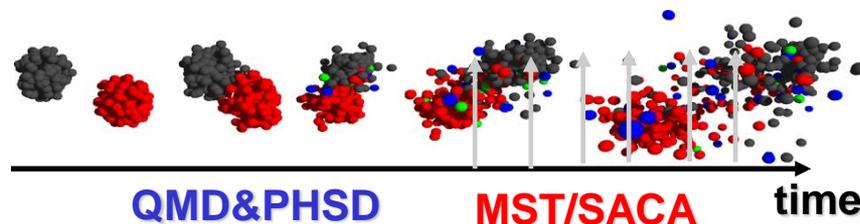
**Realization:** combined model **PHQMD = (PHSD & QMD) & (MST/SACA)**

## Parton-Hadron-Quantum-Molecular Dynamics

Initialization → propagation of baryons:  
**QMD (Quantum-Molecular Dynamics)**

Propagation of partons (quarks, gluons) and mesons  
+ **collision integral** = interactions of hadrons and partons (QGP)  
from **PHSD (Parton-Hadron-String Dynamics)**

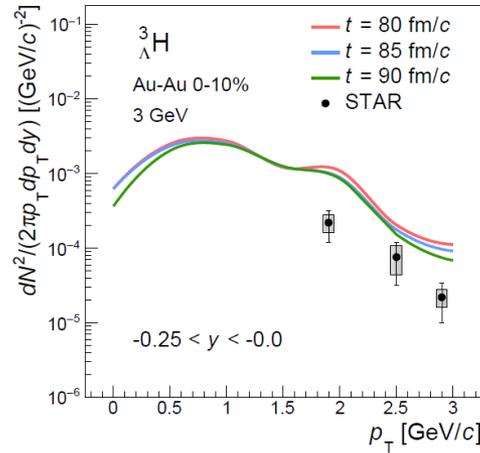
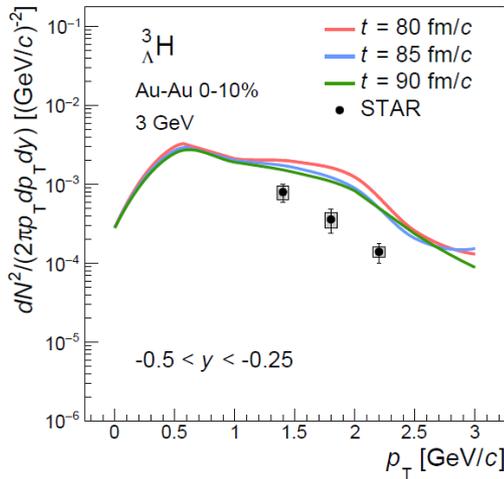
Cluster recognition:  
**SACA (Simulated Annealing Clusterization Algorithm)**  
or **MST (Minimum Spanning Tree)**



# Hypernuclei production at $s^{1/2} = 3$ GeV

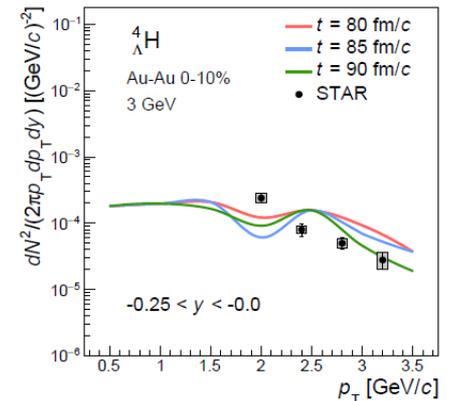
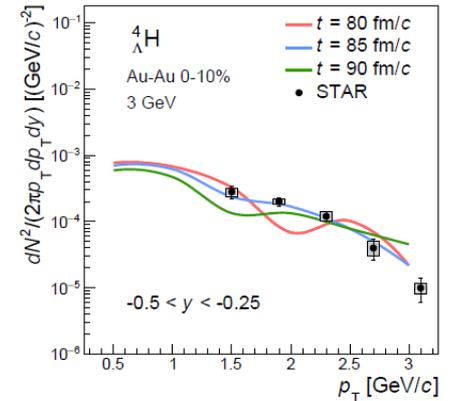
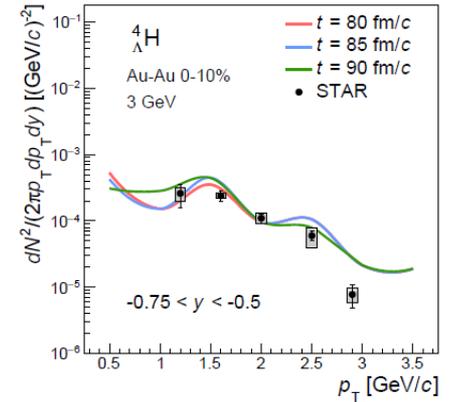
The PHQMD comparison with most recent STAR fixed target distribution of  ${}^3\text{H}_\Lambda$ ,  ${}^4\text{H}_\Lambda$  from Au+Au central collisions at  $\sqrt{s} = 3$  GeV

- Assumption for nucleon-hyperon potential:  $V_{N\Lambda} = 2/3 V_{NN}$



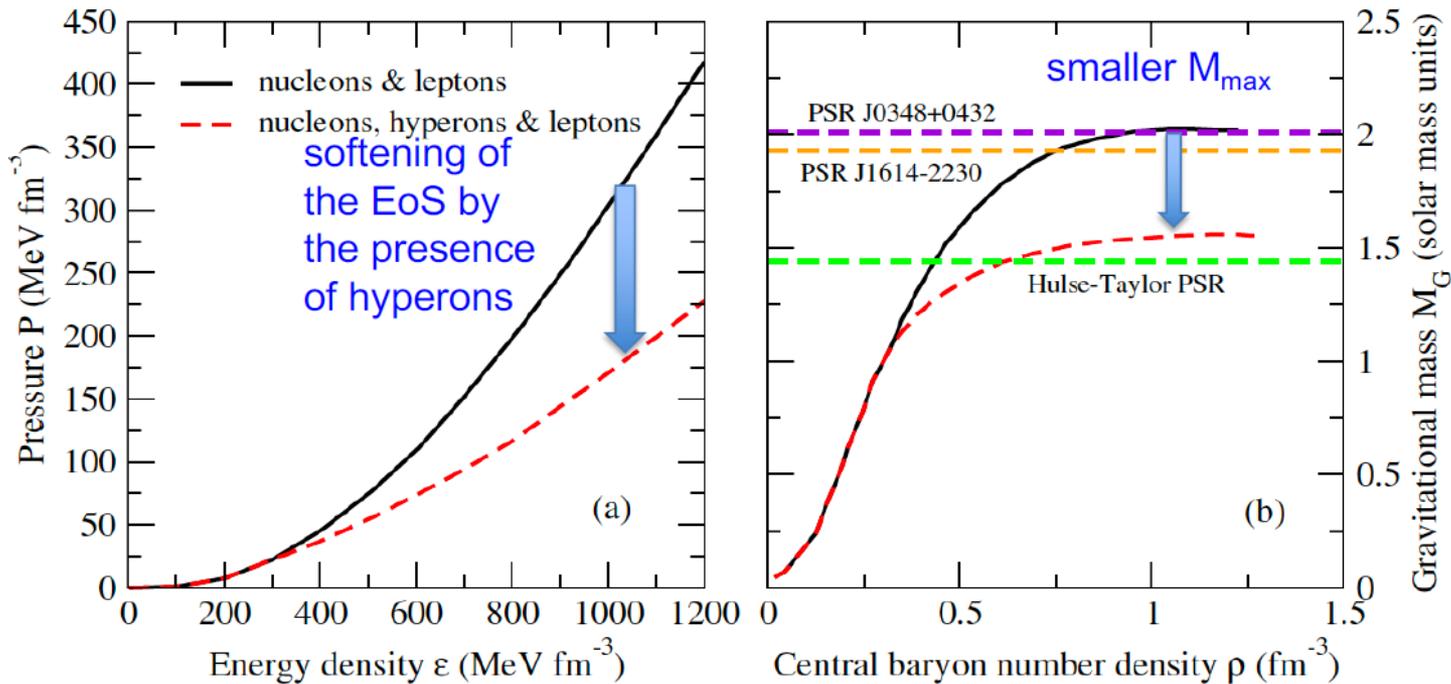
➔ Reasonable description of hypernuclei production

- PHQMD predicts the **dynamical formation of clusters** from low to ultra-relativistic energies due to the interactions
- Cluster formation is sensitive to the YN and NN potential  
➔ **sensitivity to EoS**

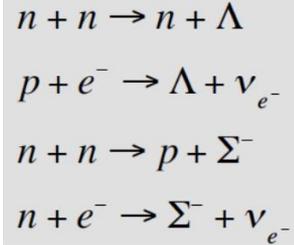


# Neutron stars with hyperons

The presence of hyperons in neutron stars  
 → softening of EoS:



$\beta$ -stable  
hyperonic matter:



Chatterjee and Vidana '16;  
 Vidana '18  
 Credit: Laura Tolos

**'Hyperon puzzle'**: induces a strong softening of the EoS  
 that leads to  $M_{\max} < 2M_{\odot}$

– possible solution of 'hyperon puzzle': **dark matter inside stars** →

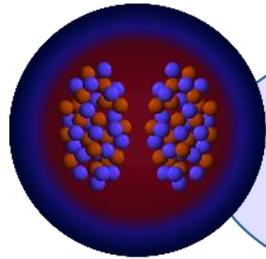


# Search for DM particles: DMLab theory

DM ,candidate'



**Heavy-ion physics**

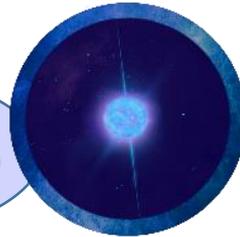


- Search for DM particles in HIC based on SM-DM interactions via possible portals:

$$\mathcal{L} \supset \begin{cases} -\frac{\epsilon}{2 \cos \theta_W} B_{\mu\nu} F'^{\mu\nu}, & \text{vector portal} \\ (\mu\phi + \lambda\phi^2) H^\dagger H, & \text{Higgs portal} \\ y_n L H N, & \text{neutrino portal} \\ \frac{a}{f_a} F_{\mu\nu} \tilde{F}^{\mu\nu}, & \text{axion portal.} \end{cases}$$

→ Constraints on masses and coupling constants of DM candidates by comparison of theory results with experimental data

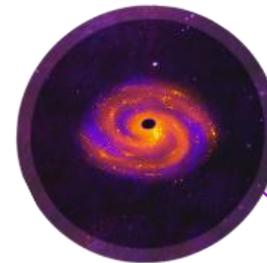
**Astrophysics**



→ Constraints from astrophysical observations: masses, radii of stars, star cooling (e.g.  $\Lambda \rightarrow \pi^0 + X^0$ ), gravitational waves

Camalich et al., PRD 103 (2021) L12301

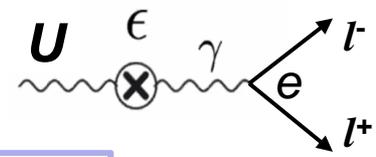
**Cosmology**



→ Constraints from cosmological observations: evolution of Universe, matter density, cosmic microwave background, rotation of galaxis

The '**vector**' portal : existence of a **U(1)-U(1)'** gauge symmetry group mixing

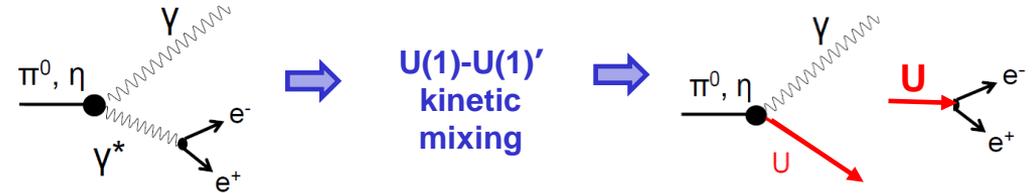
$$\mathcal{L}_{A'} = -\frac{1}{4}F'^{\mu\nu}F'_{\mu\nu} + \frac{1}{2} \frac{\epsilon}{\cos\theta_W} B^{\mu\nu}F'_{\mu\nu} - \frac{1}{2}m_{A'}^2 A'^{\mu}A'_{\mu}$$



Notation for 'dark photon': A' or U- boson

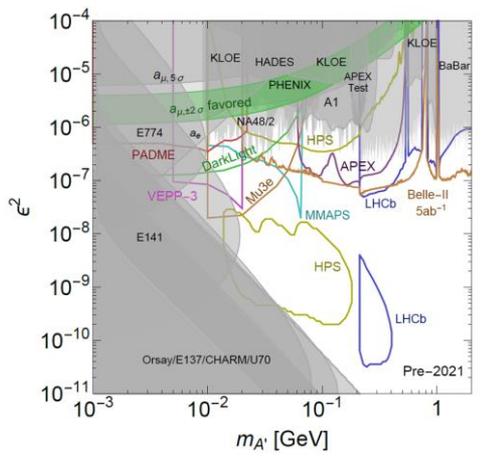
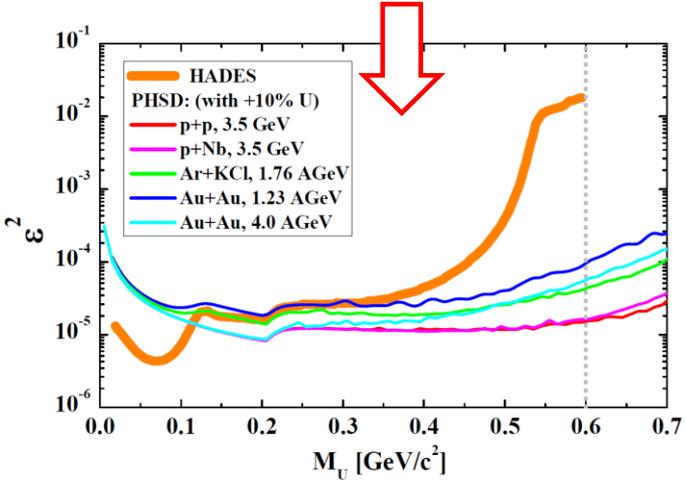
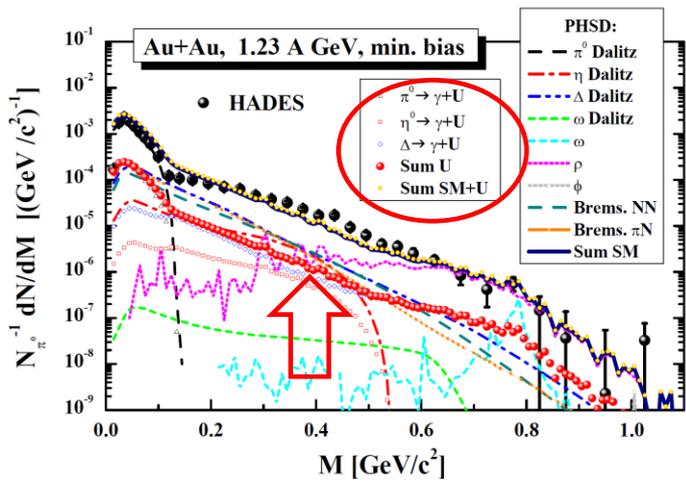
**Unknown: kinetic mixing parameter  $\epsilon$  and mass  $M_U$**

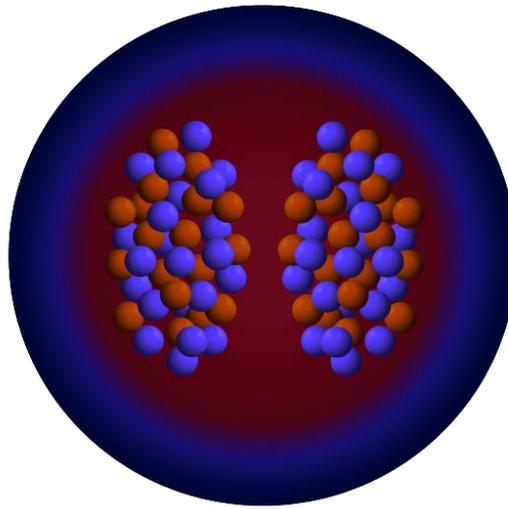
B. Holdom, PL B 166, 196 (1986)  
B. Batell et al., PRD 80, 095024 (2009)



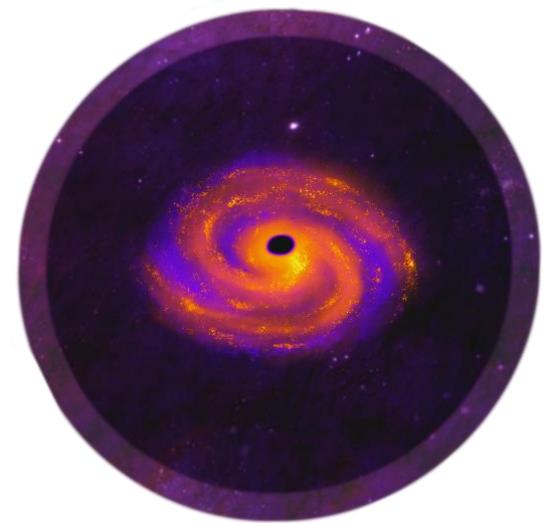
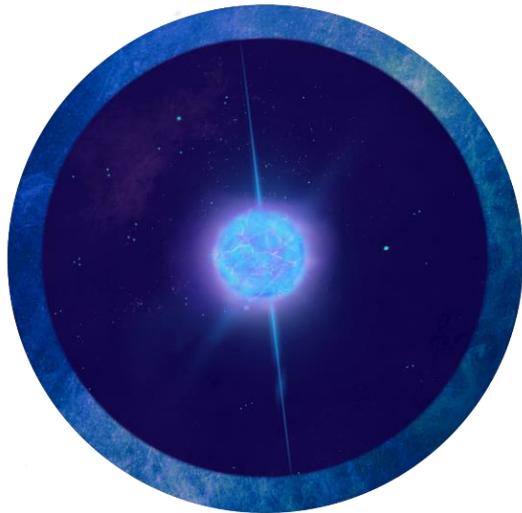
$\pi^0 \rightarrow \gamma + U$ ,  
 $\eta \rightarrow \gamma + U$ ,  $U \rightarrow e^+e^-$   
 $\Delta \rightarrow N + U$

The **upper limit for the kinetic mixing parameter  $\epsilon^2(M_U)$**  of light dark photons extracted from the **PHSD** dilepton spectra - with 10% allowed surplus of the total SM yield by an additional **DM** yield at given M:





**Thank you for your attention !**



*Credit: Marie Cassing*