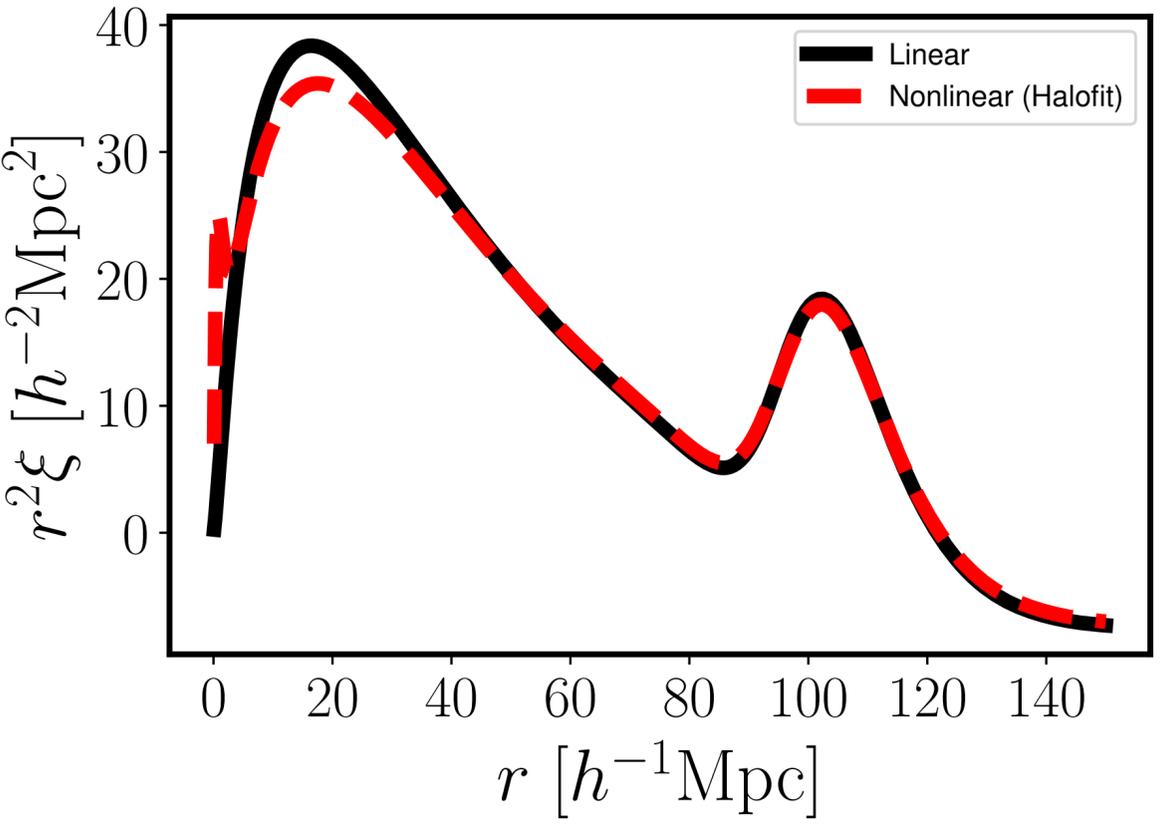
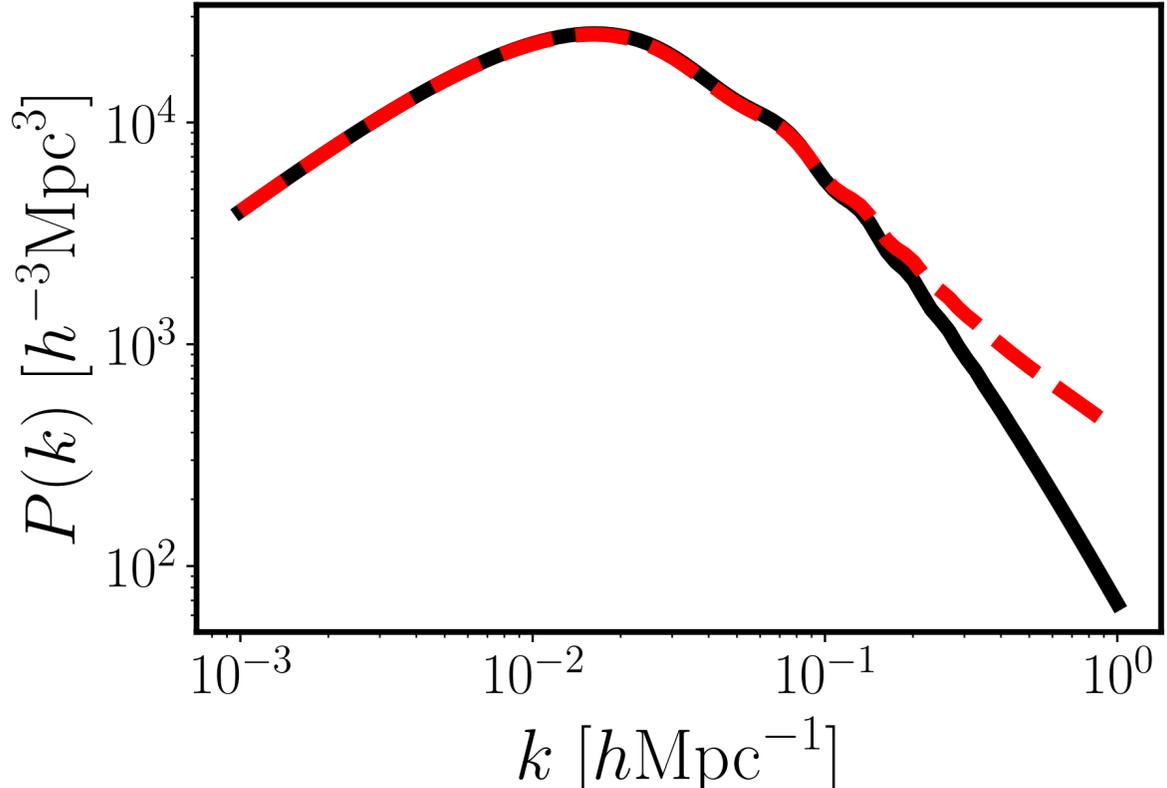
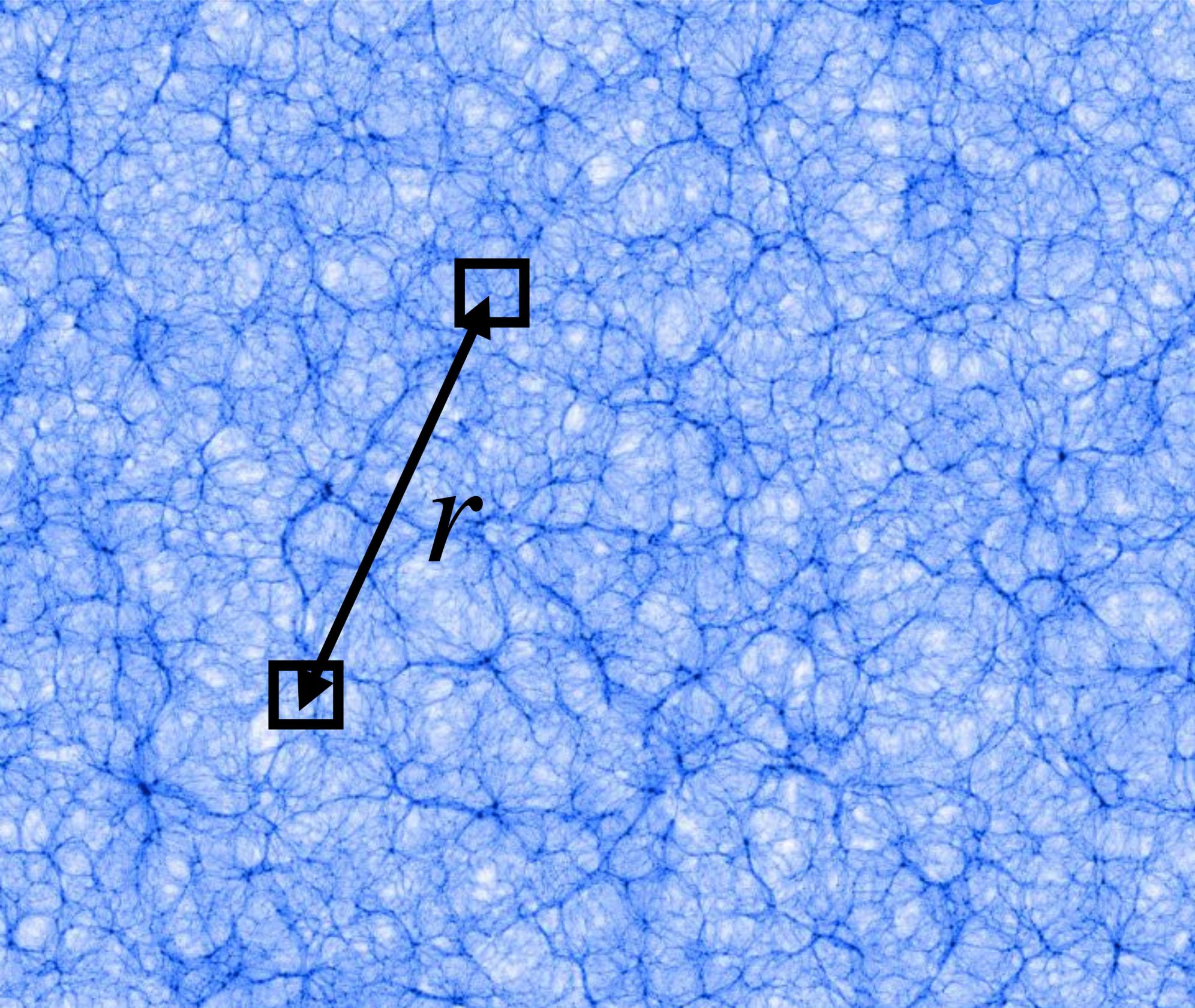
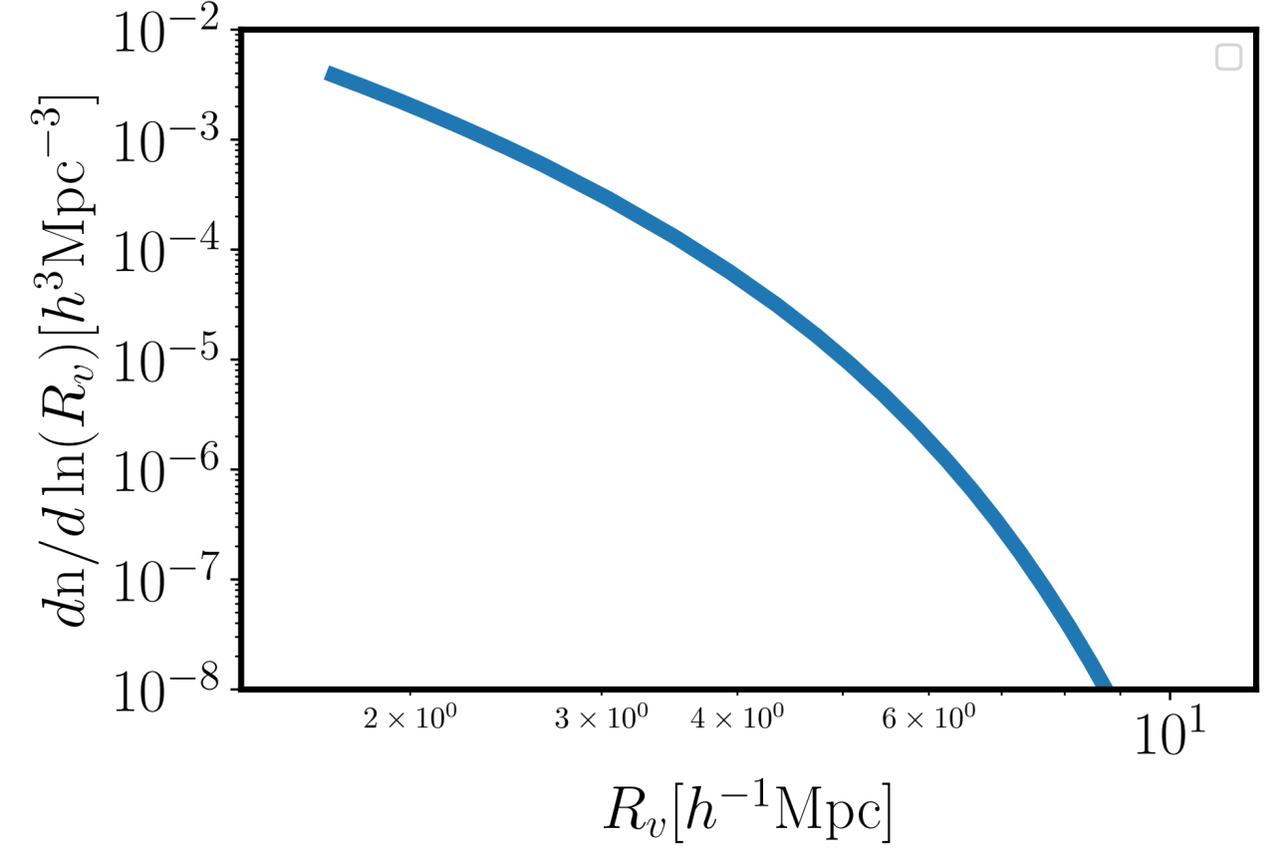
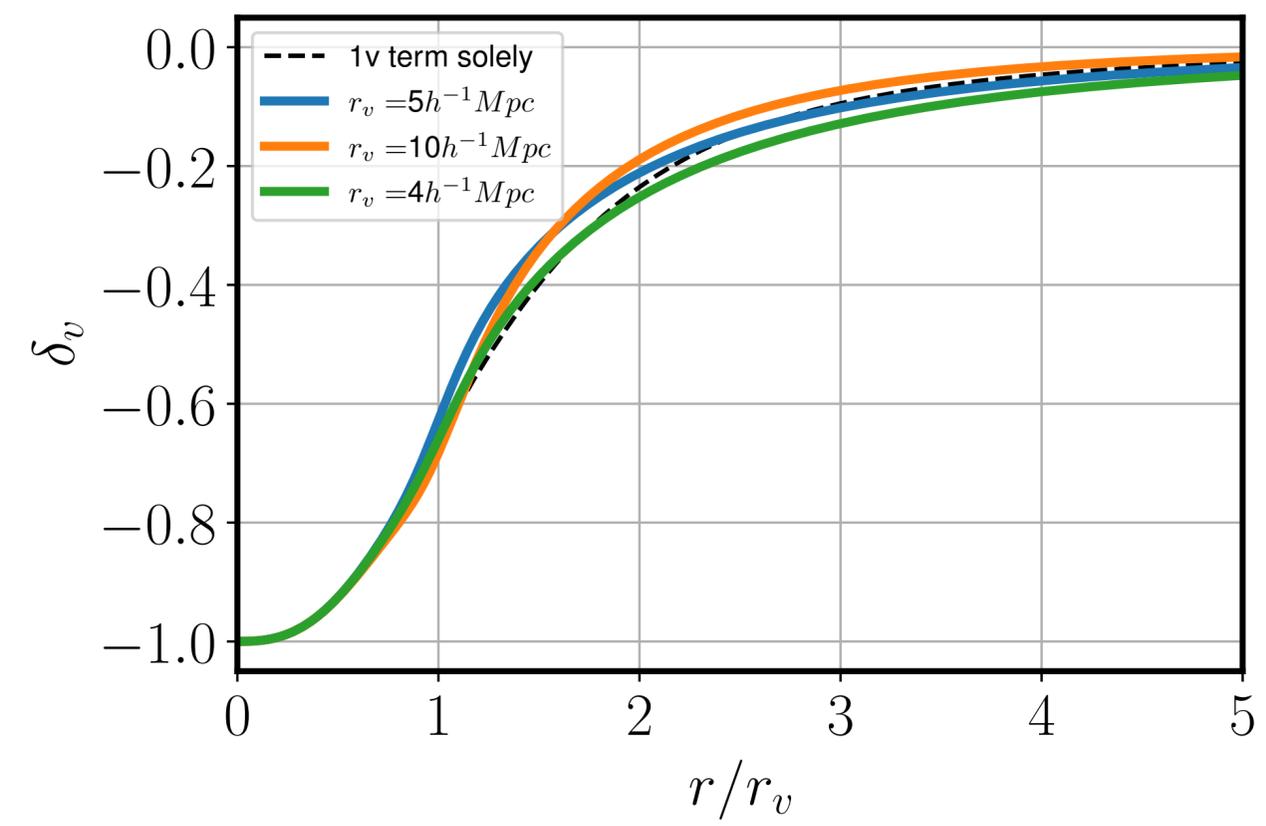
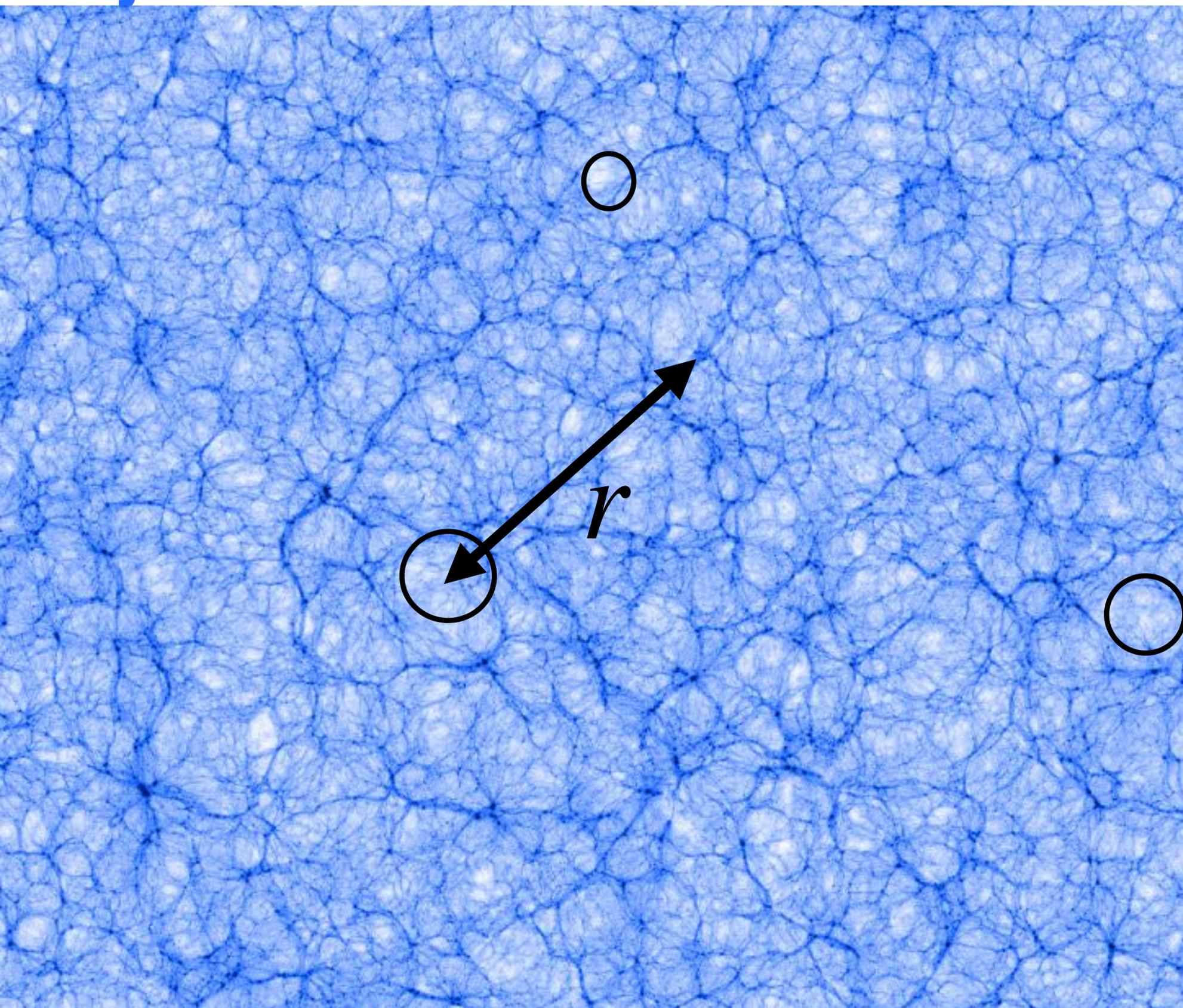


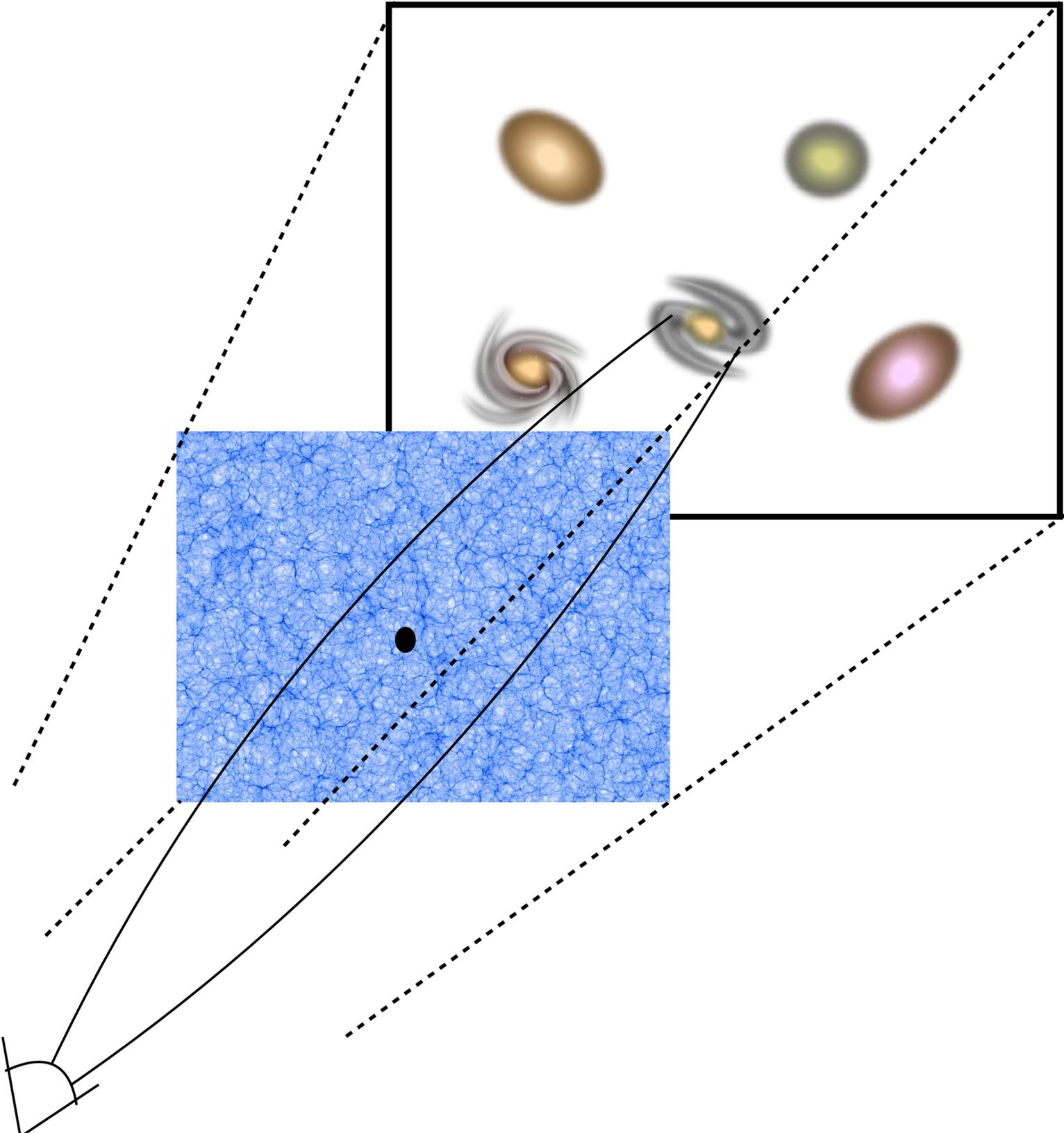
How To Extract Information From Large Scale Structure?



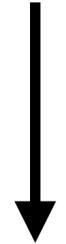
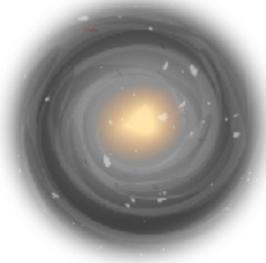
Why Voids?



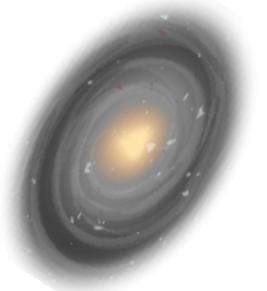
Why Weak Lensing?



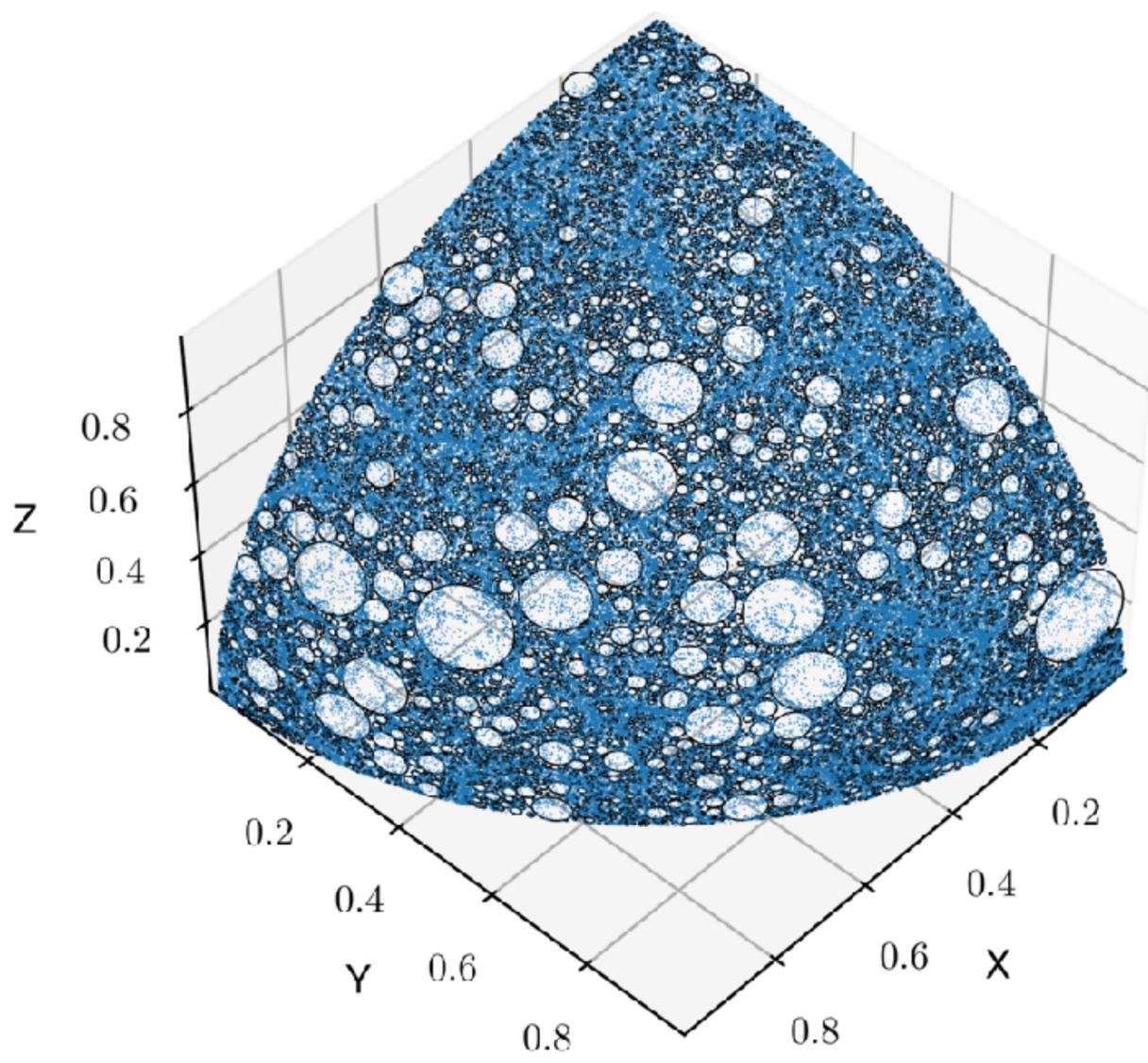
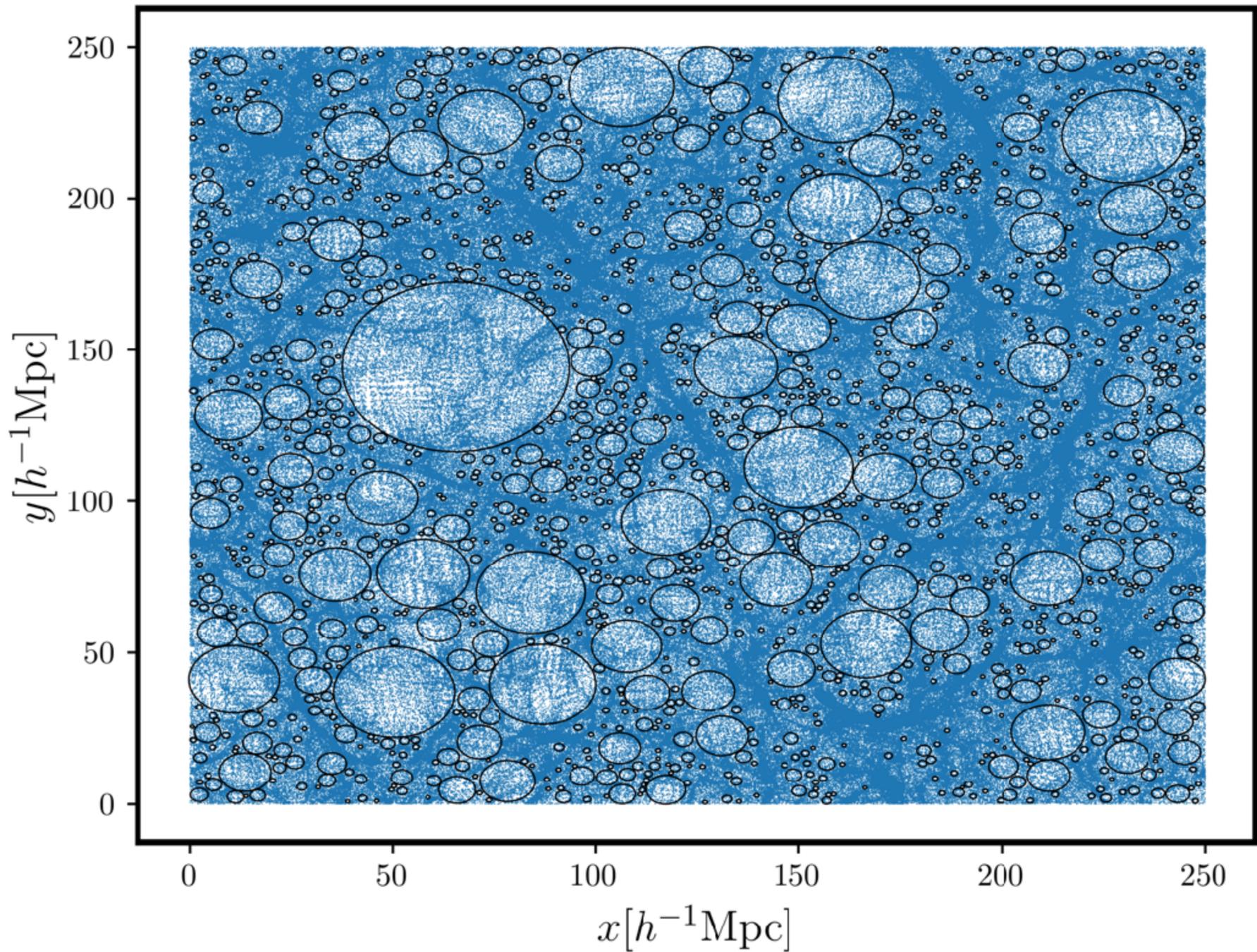
NL



L

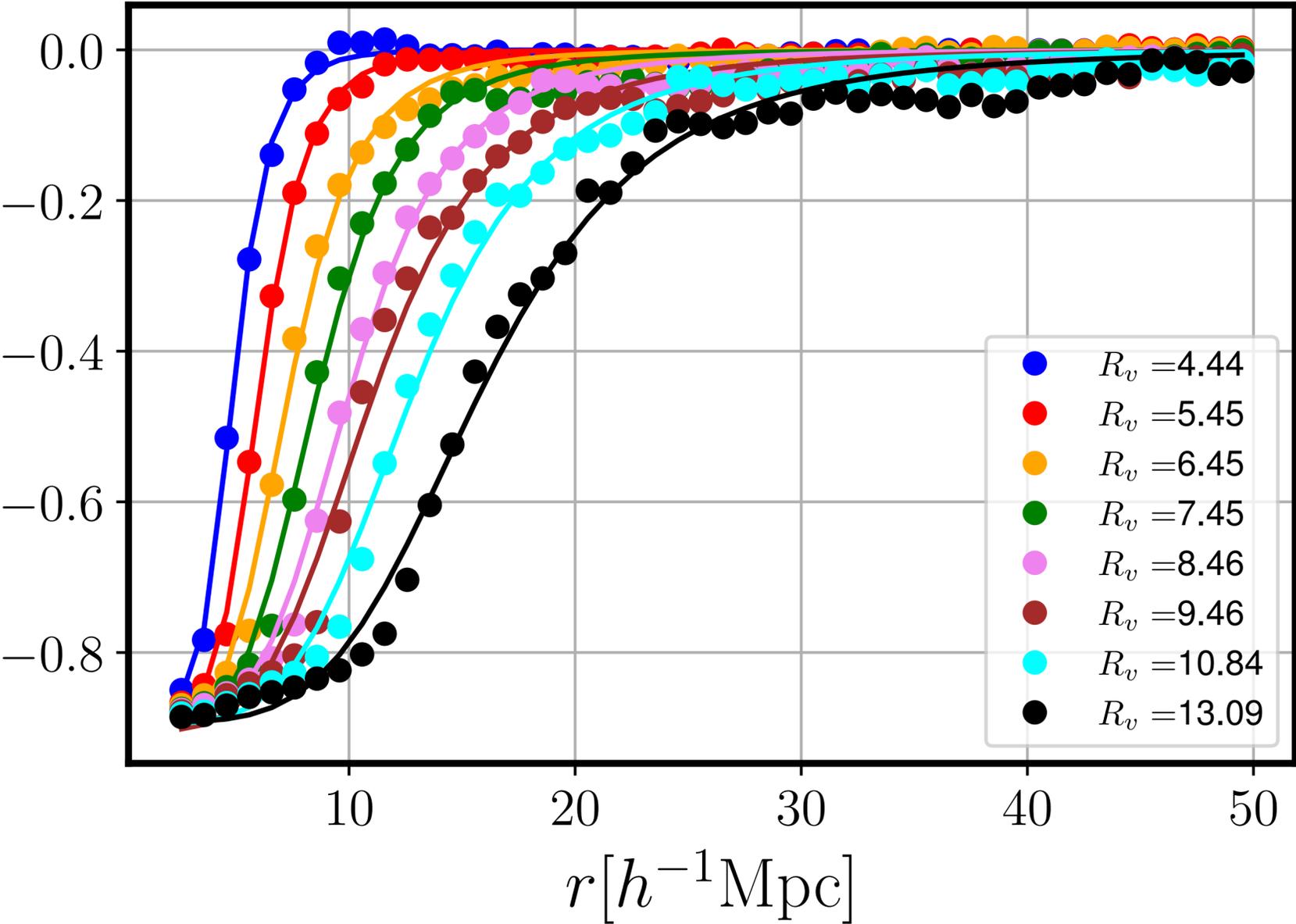


Optimum Centering Void Finder

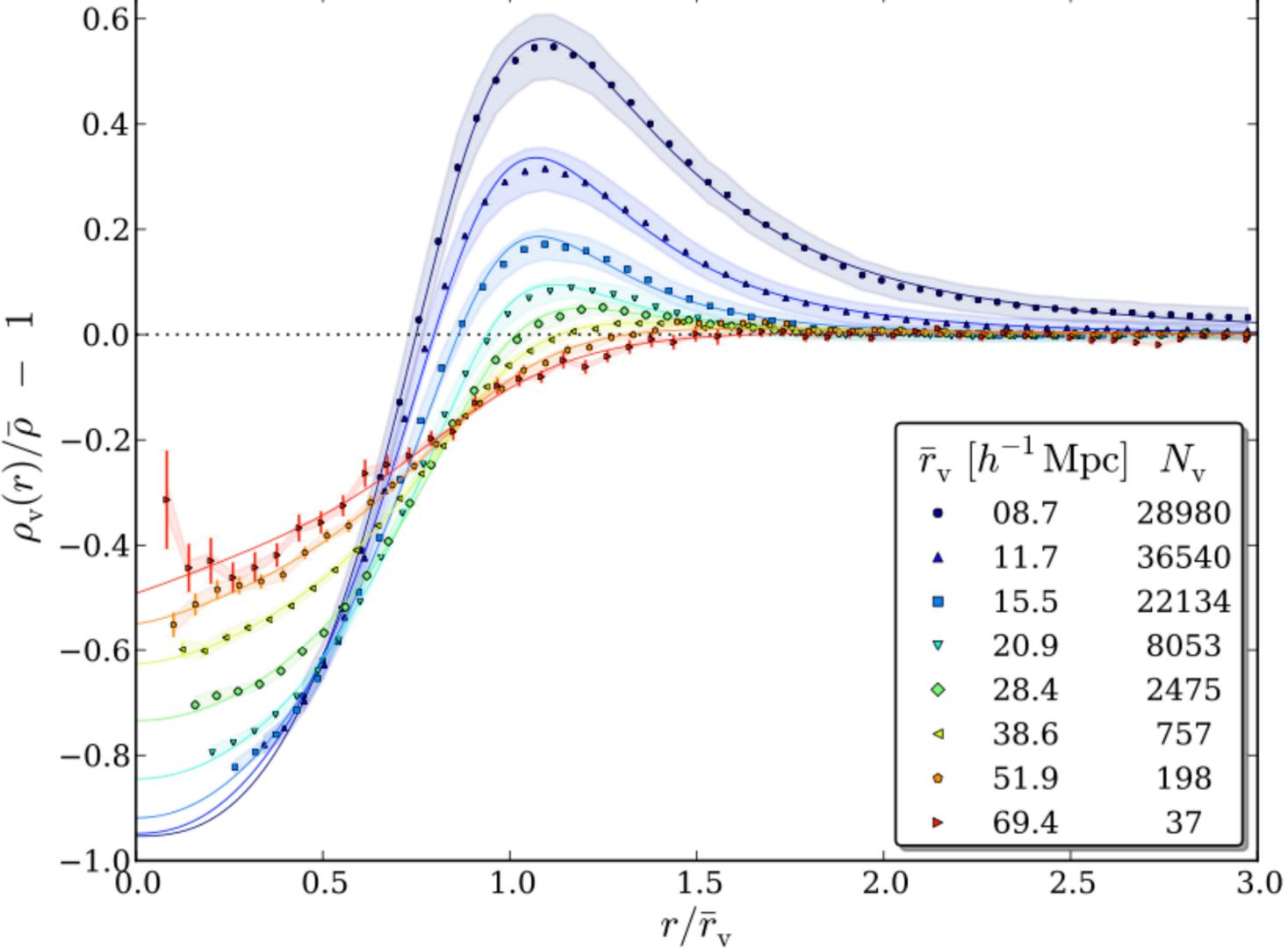


Comparison With Literature

OCVF

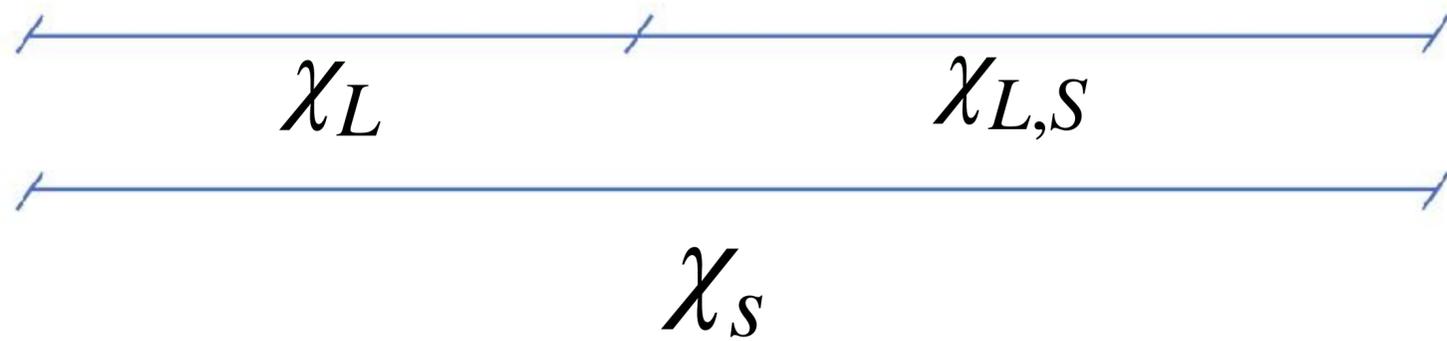
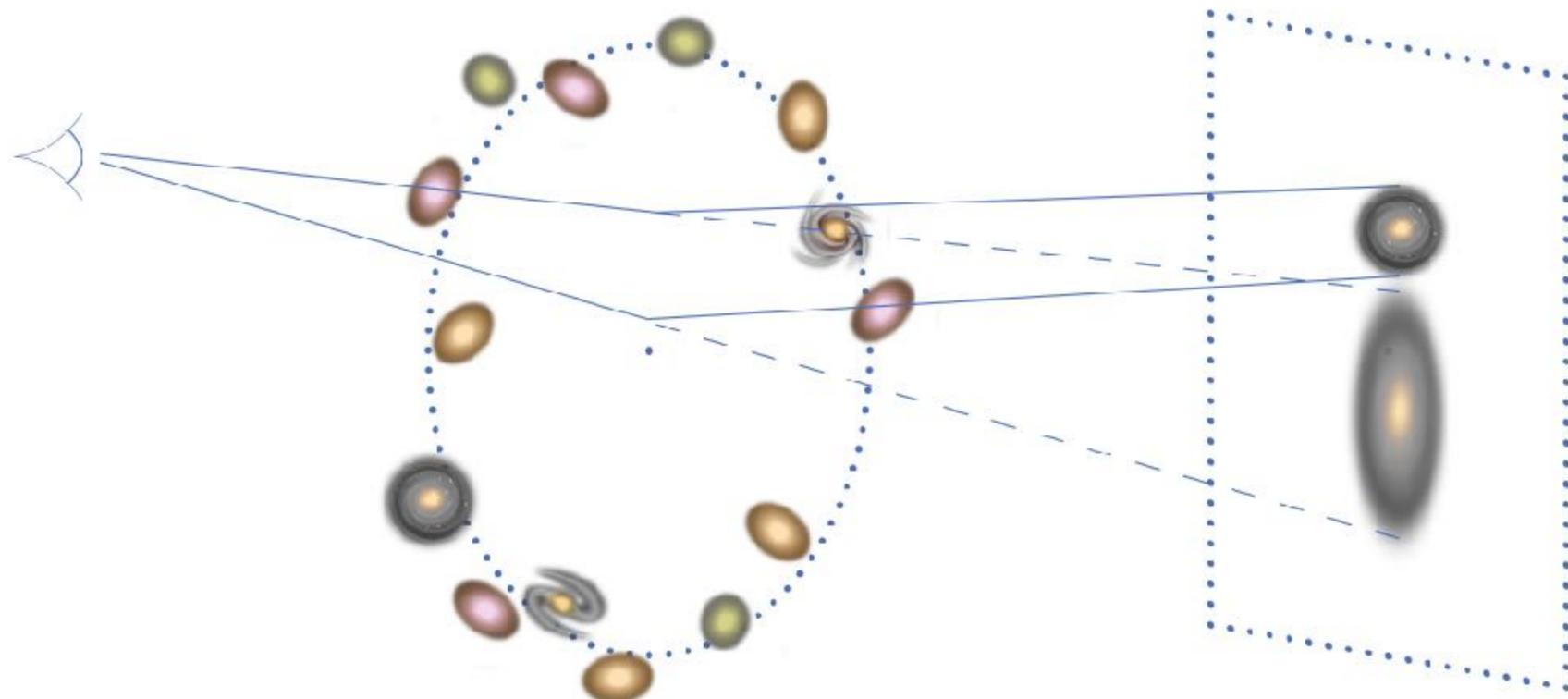


ZOBOV



Hamaus et al (2014)

WL Voids



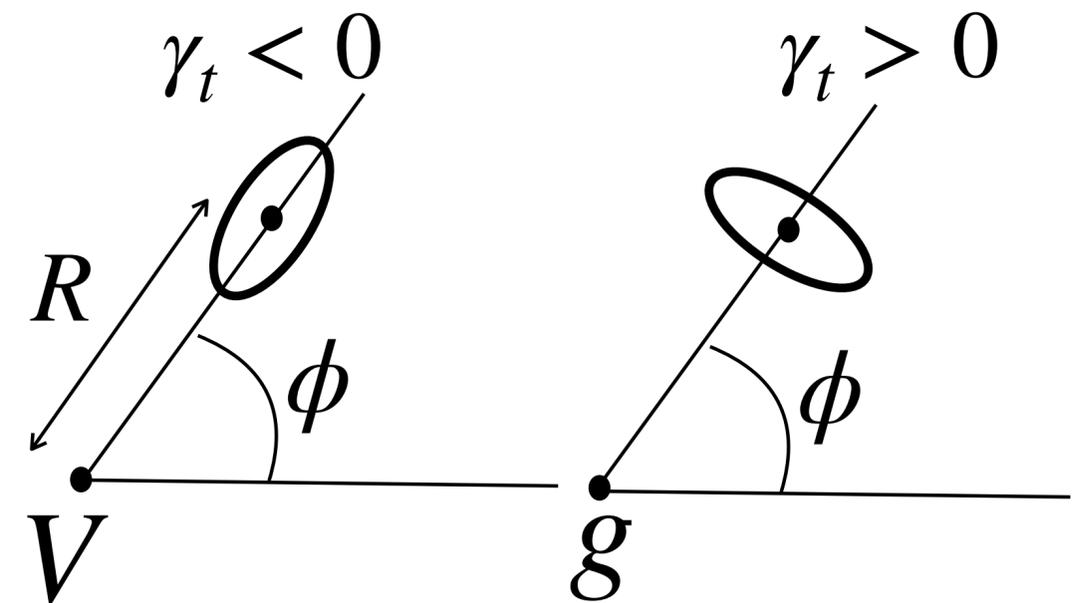
Differential surface mass density:

$$\Delta\Sigma(R, z_L) = \Sigma_{crit}(\bar{\kappa}(< R) - \kappa(R))$$

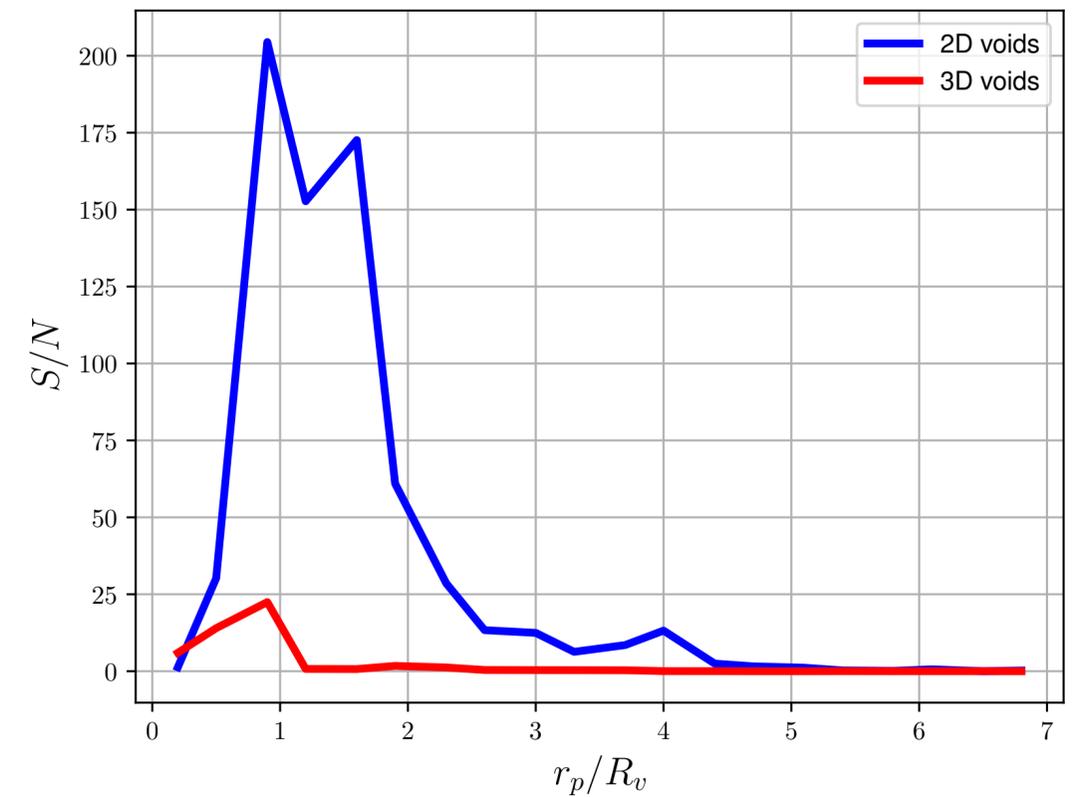
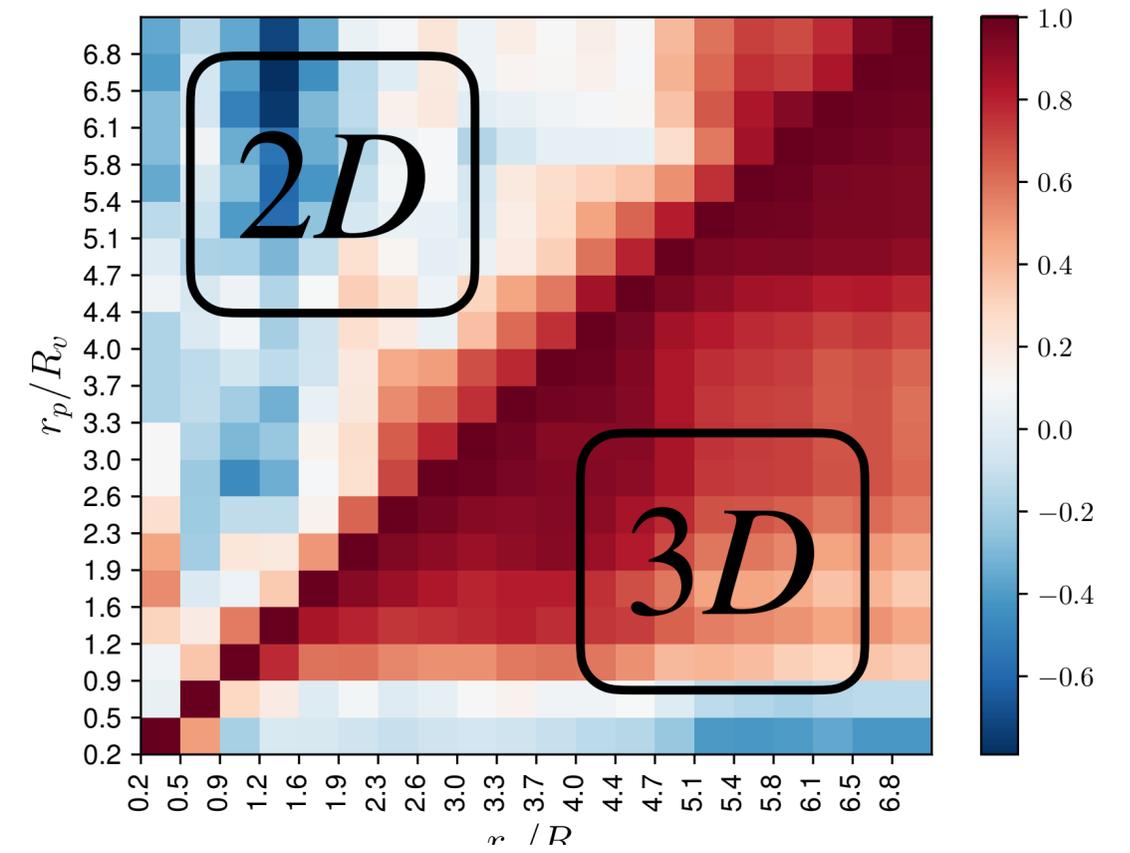
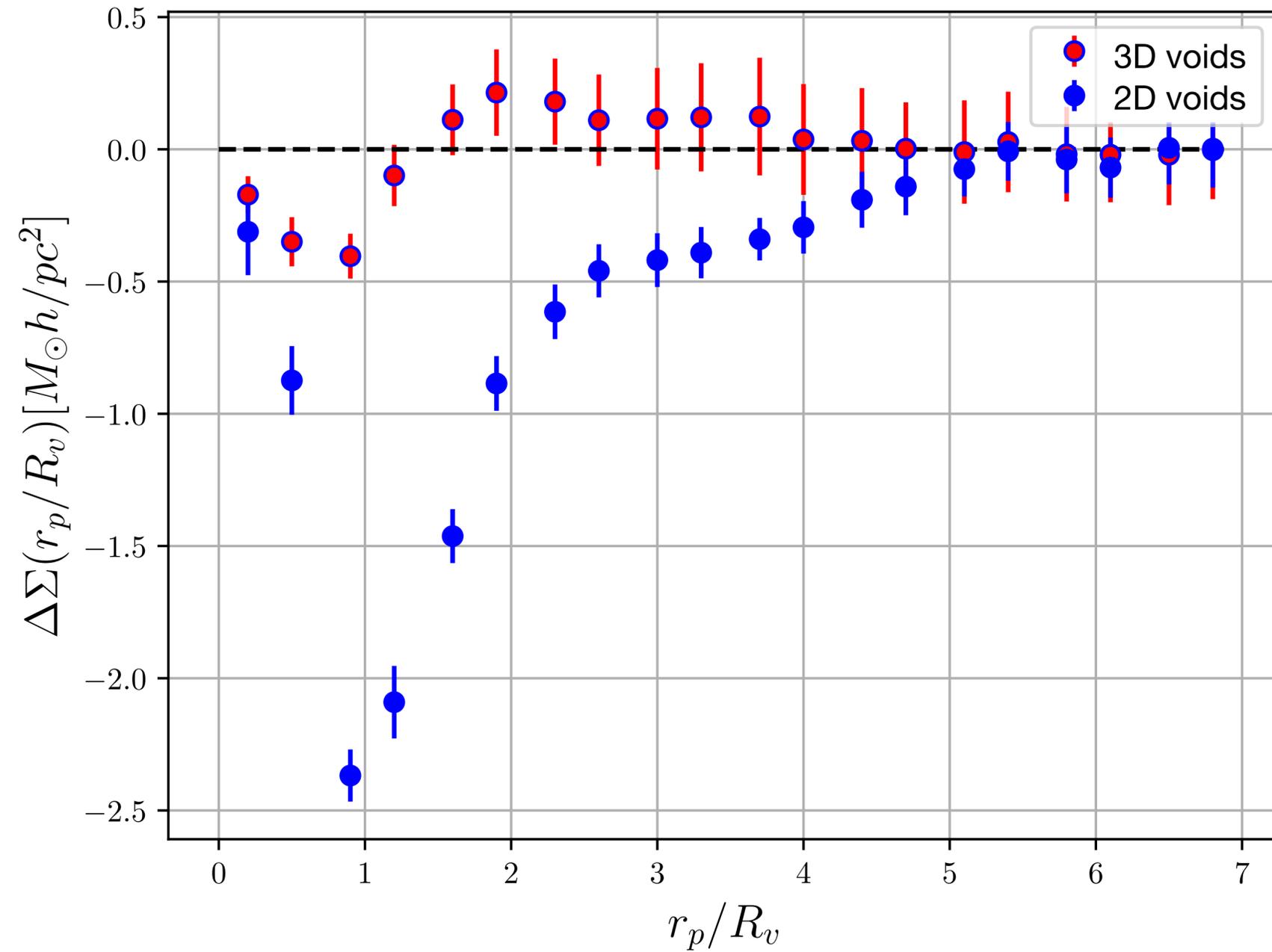
$$= \Sigma_{crit} \times \gamma_t(R)$$

$$\kappa(R) = \int d\chi \Sigma_{crit}^{-1} \bar{\rho} \delta(\chi, R) \equiv \Sigma_{crit}^{-1} \Sigma(R)$$

$$\Rightarrow \Delta\Sigma(R) = \bar{\Sigma}(< R) - \Sigma(R)$$

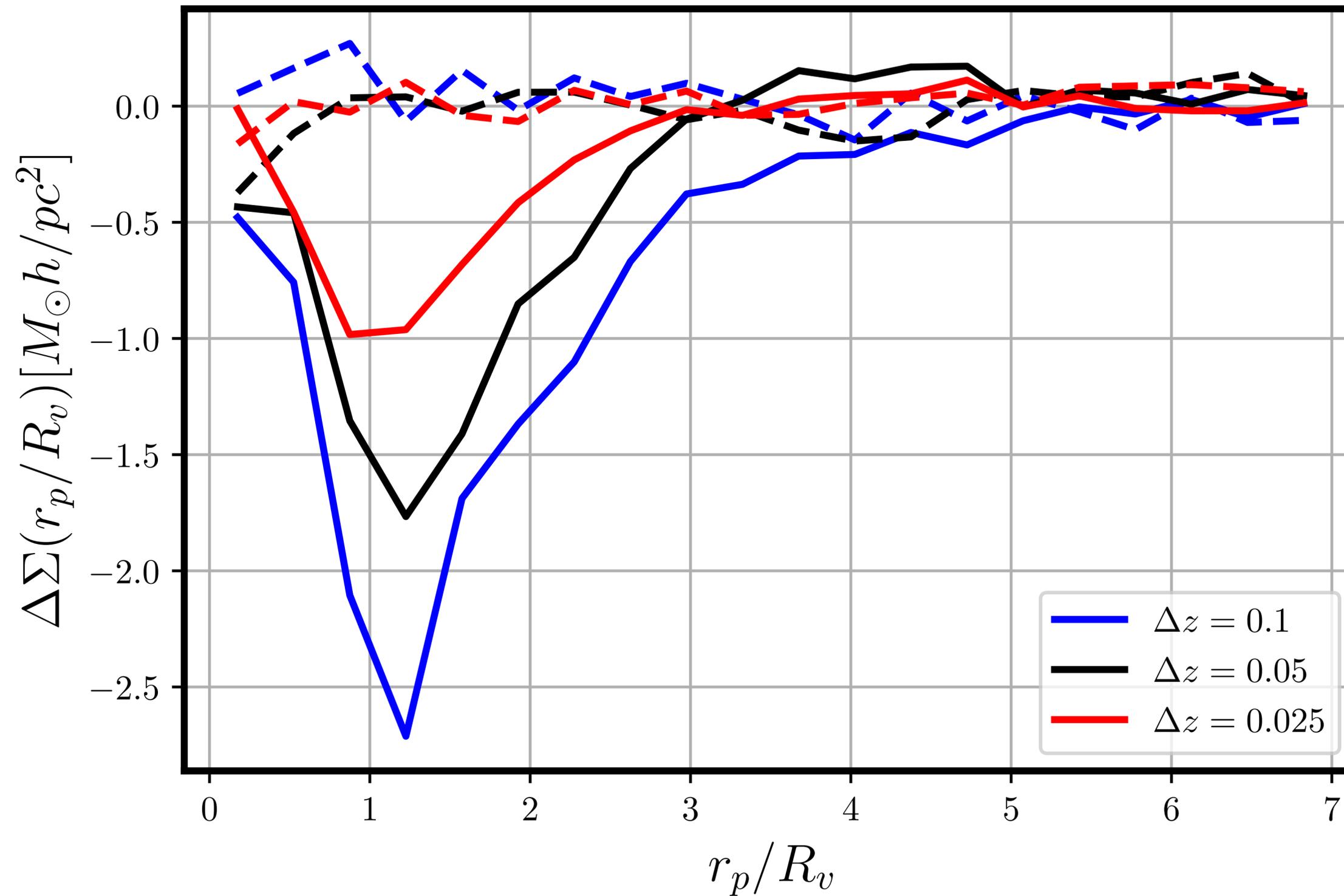


How To Optimize VL Measurement?



The Role of Bin Size

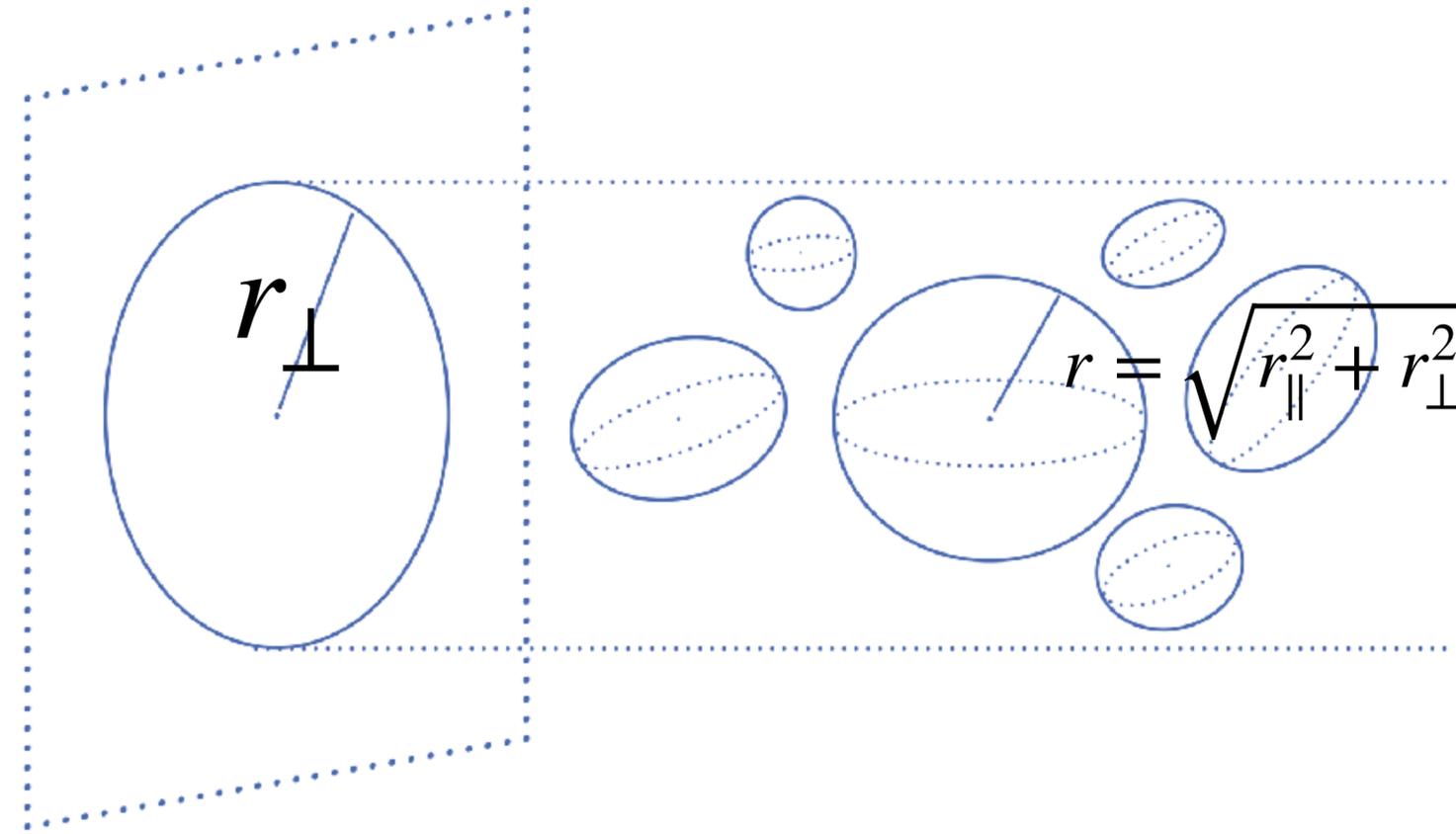
BGS $0.1 < z < 0.5$



The Void-Lensing Model

Projected field

3D field



$$\delta_{2D}(r_{\perp} | R_{2D}, \Delta_{2D}) = \int dR_{3D} \frac{dn_v}{dR_{3D}}(R_{3D} | \Delta_{3D}) \int dx_{\perp} dx_{\parallel} d\alpha P(x_{\perp}, x_{\parallel}, \alpha | R_{3D}, R_{2D}, \Delta_{3D}, \Delta_{2D}) \int dr_{\parallel} \delta_{3D}(r_{\perp} - x_{\perp}, r_{\parallel} - x_{\parallel} | \alpha, R_{3D}, \Delta_{3D})$$

The Void-Lensing Model

$$\delta_{2D}(r_{\perp} | R_{2D}, \Delta_{2D}) = \int dR_{3D} \frac{dn_v}{dR_{3D}}(R_{3D} | \Delta_{3D}) \int dx_{\perp} dx_{\parallel} d\alpha P(x_{\perp}, x_{\parallel}, \alpha | R_{3D}, R_{2D}, \Delta_{3D}, \Delta_{2D}) \int dr_{\parallel} \delta_{3D}(r_{\perp} - x_{\perp}, r_{\parallel} - x_{\parallel} | \alpha, R_{3D}, \Delta_{3D})$$

\simeq

$$\delta_{2D}(r_{\perp} | M_{2D}) = \int d \ln R_{3D} \frac{dn_v}{d \ln R_{3D}} \int dx_{\perp} (1 + \xi(x_{\perp})) \int dr_{\parallel} \delta_{3D}(r_{\perp}, r_{\parallel} | \alpha, R_{3D})$$

$$= \int dr_{\parallel} \delta^{eff}(r_{\perp}, r_{\parallel} | \alpha, R_{3D})$$

$$\Rightarrow \Delta\Sigma(r_{\perp}) = \bar{\delta}_{2D}(< r_{\perp}) - \delta_{2D}(r_{\perp})$$

The Void-Lensing Model

$$\delta_{2D}(r_{\perp} | R_{2D}, \Delta_{2D}) = \int dR_{3D} \frac{dn_v}{dR_{3D}}(R_{3D} | \Delta_{3D}) \int dx_{\perp} dx_{\parallel} d\alpha P(x_{\perp}, x_{\parallel}, \alpha | R_{3D}, R_{2D}, \Delta_{3D}, \Delta_{2D}) \int dr_{\parallel} \delta_{3D}(r_{\perp} - x_{\perp}, r_{\parallel} - x_{\parallel} | \alpha, R_{3D}, \Delta_{3D})$$

$$\approx$$

$$\delta_{2D}(r_{\perp} | M_{2D}) = \int d \ln R_{3D} \boxed{\frac{dn_v}{d \ln R_{3D}}} \int dx_{\perp} (1 + \xi(x_{\perp})) \int dr_{\parallel} \delta_{3D}(r_{\perp}, r_{\parallel} | \alpha, R_{3D})$$

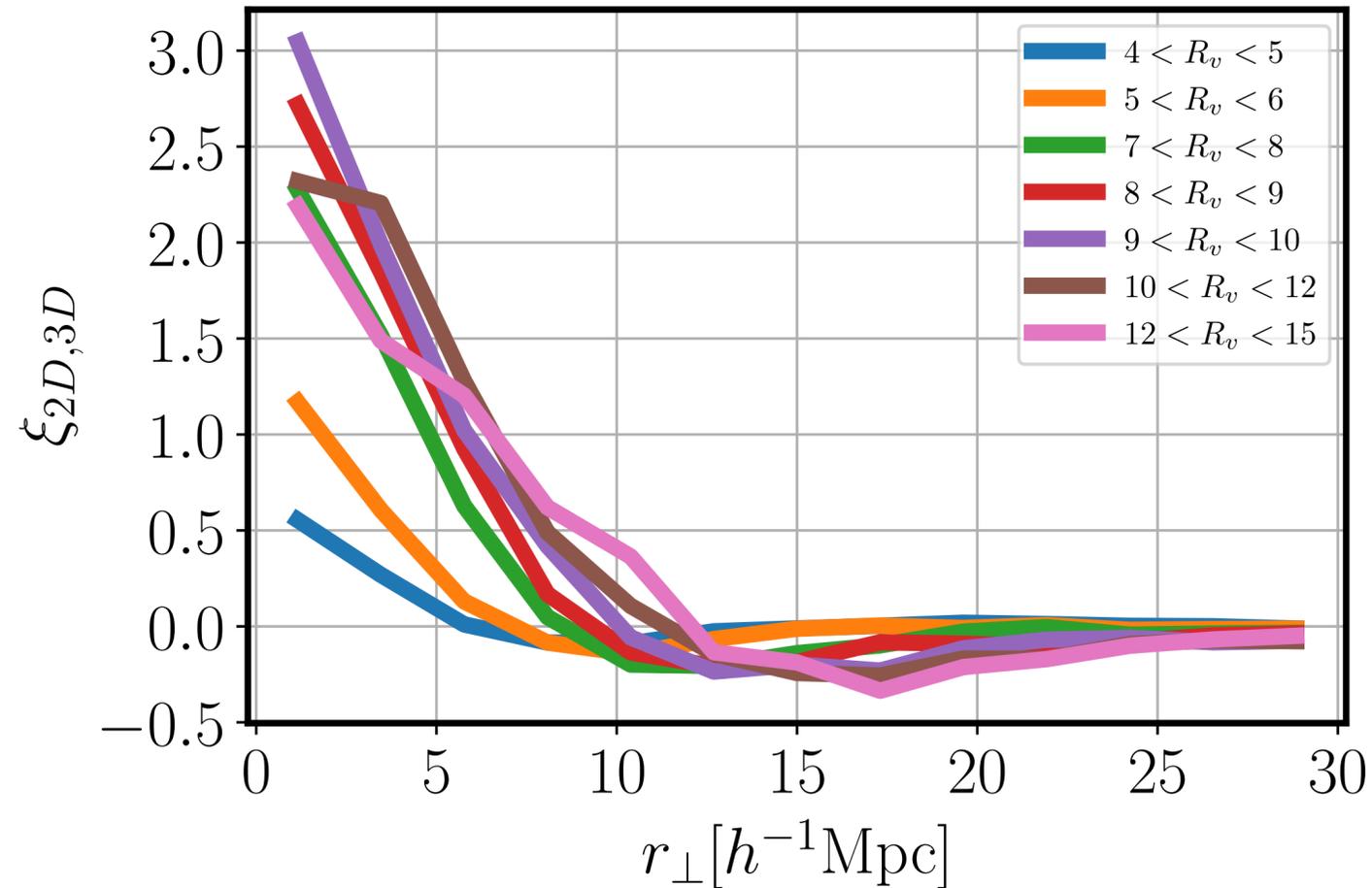
$$\frac{dn_v}{d \ln R} = \frac{f(\sigma)}{V(R)} \frac{d \ln \sigma^{-1}}{d \ln R} \quad , \text{ where} \quad \sigma^2(R) \equiv \int \frac{dk}{2\pi^2} k^2 P_{mm}^L(k) | \tilde{W}(k | R) |^2$$

The Void-Lensing Model

$$\delta_{2D}(r_{\perp} | R_{2D}, \Delta_{2D}) = \int dR_{3D} \frac{dn_v}{dR_{3D}}(R_{3D} | \Delta_{3D}) \int dx_{\perp} dx_{\parallel} d\alpha P(x_{\perp}, x_{\parallel}, \alpha | R_{3D}, R_{2D}, \Delta_{3D}, \Delta_{2D}) \int dr_{\parallel} \rho_{3D}(r_{\perp} - x_{\perp}, r_{\parallel} - x_{\parallel} | \alpha, R_{3D}, \Delta_{3D})$$

$$\delta_{2D}(r_{\perp} | M_{2D}) = \int d \ln R_{3D} \frac{dn_v}{d \ln R_{3D}} \int dx_{\perp} (1 + \xi(x_{\perp})) \int dr_{\parallel} \delta_{3D}(r_{\perp}, r_{\parallel} | \alpha, R_{3D})$$

$$5 < R_v^{2D} < 15$$

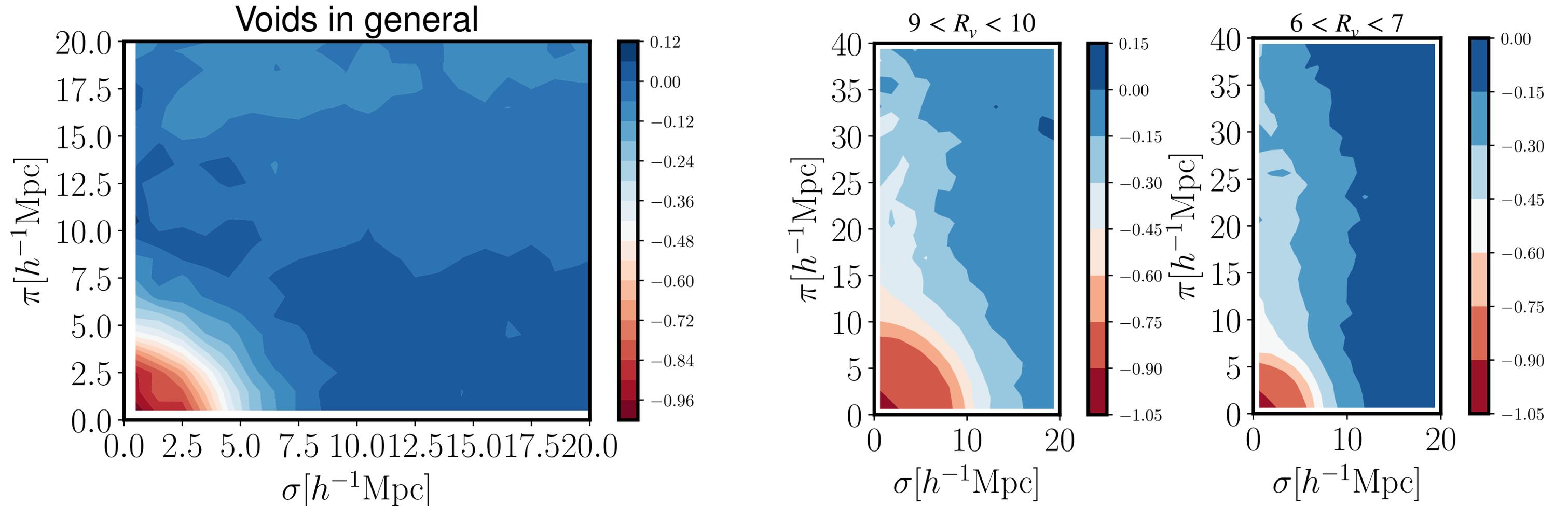


The Void-Lensing Model

$$\delta_{2D}(r_{\perp} | R_{2D}, \Delta_{2D}) = \int dR_{3D} \frac{dn_v}{dR_{3D}}(R_{3D} | \Delta_{3D}) \int dx_{\perp} dx_{\parallel} d\alpha P(x_{\perp}, x_{\parallel}, \alpha | R_{3D}, R_{2D}, \Delta_{3D}, \Delta_{2D}) \int dr_{\parallel} \delta_{3D}(r_{\perp} - x_{\perp}, r_{\parallel} - x_{\parallel} | \alpha, R_{3D}, \Delta_{3D})$$

\approx

$$\delta_{2D}(r_{\perp} | M_{2D}) = \int d \ln R_{3D} \frac{dn_v}{d \ln R_{3D}} \int dx_{\perp} (1 + \xi(x_{\perp})) \int dr_{\parallel} \delta_{3D}(r_{\perp}, r_{\parallel} | \alpha, R_{3D})$$

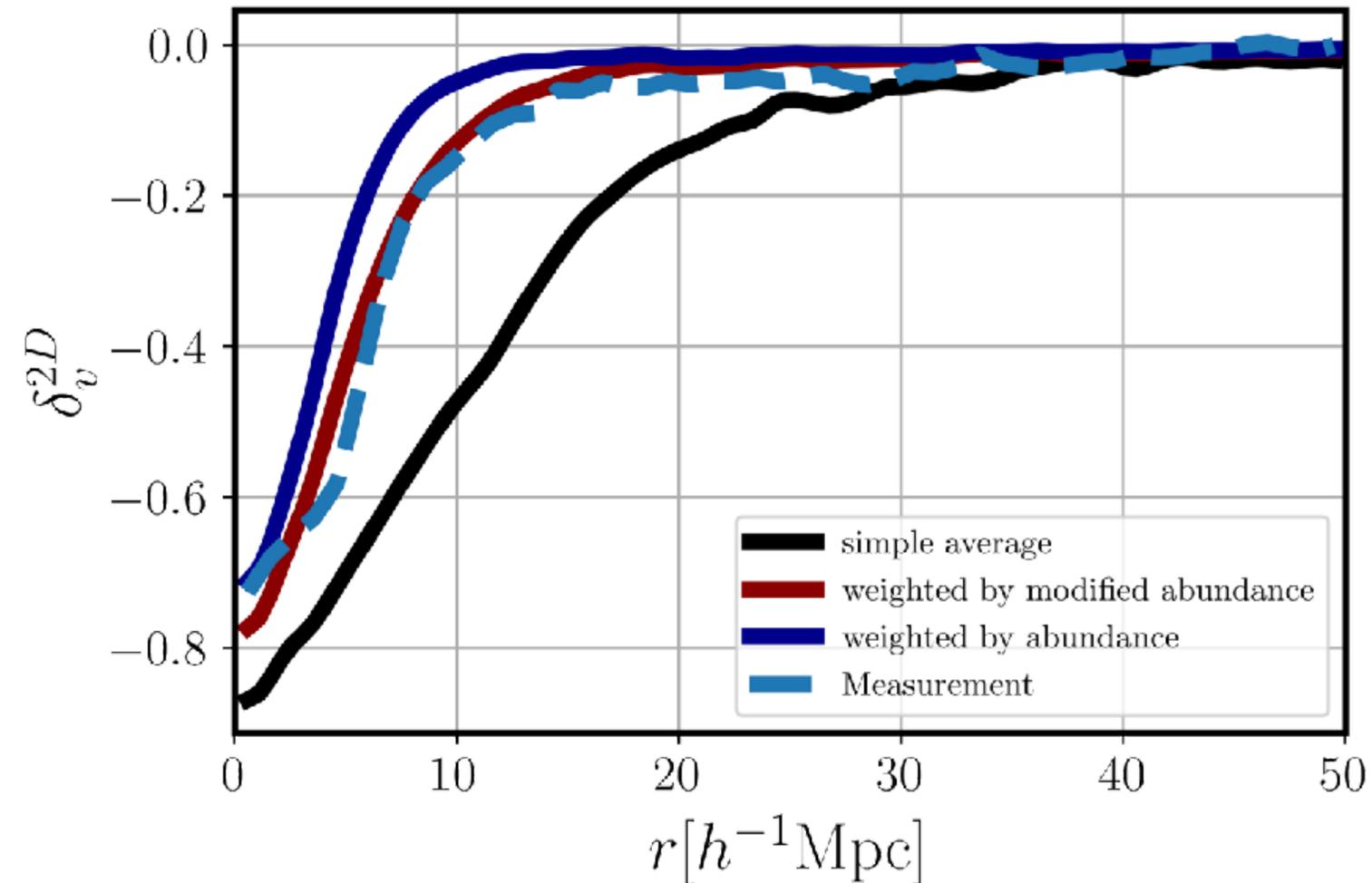


Preliminary Result

$$\delta_{2D}(r_{\perp} | R_{2D}, \Delta_{2D}) = \int dR_{3D} \frac{dn_{\nu}}{dR_{3D}}(R_{3D} | \Delta_{3D}) \int dx_{\perp} dx_{\parallel} d\alpha P(x_{\perp}, x_{\parallel}, \alpha | R_{3D}, R_{2D}, \Delta_{3D}, \Delta_{2D}) \int dr_{\parallel} \delta_{3D}(r_{\perp} - x_{\perp}, r_{\parallel} - x_{\parallel} | \alpha, R_{3D}, \Delta_{3D})$$

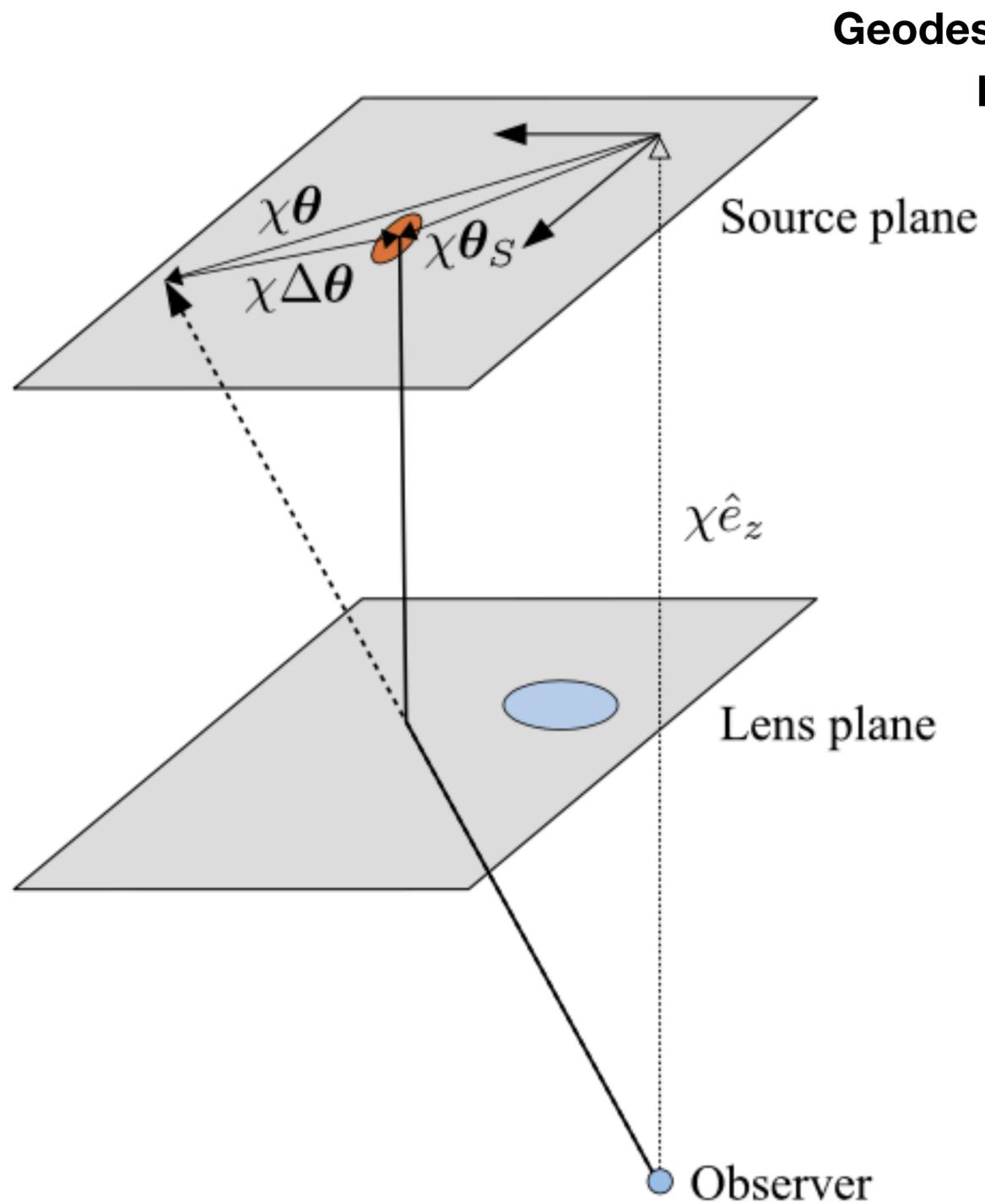
$$\approx$$

$$\delta_{2D}(r_{\perp} | M_{2D}) = \int d \ln R_{3D} \frac{dn_{\nu}}{d \ln R_{3D}} \int dx_{\perp} (1 + \xi(x_{\perp})) \int dr_{\parallel} \delta_{3D}(r_{\perp}, r_{\parallel} | \alpha, R_{3D})$$



Conclusions and Prospects

- Our method is capable of measuring $\Delta\Sigma$ with high S/N
- Apply this method to real DESI data
- Promising results in relating 3D and 2D underdensities
- Open questions: (i) How much we can reconstruct from the DM field using 2D underdensities? (ii) Is the Void intrinsic alignment sensitive to cosmology, modifications to gravity or neutrinos?
- Future: Apply the pipe line to the real data and perform cosmological analysis for the first time



Geodesic equation + scalar perturbations \Rightarrow

$$\theta^i = \theta_s^i + \Delta\theta^i$$

$$\Delta\theta^i(\boldsymbol{\theta}) = \frac{2}{c^2} \int_0^\chi d\chi' \Phi_{,i}(\mathbf{x}(\boldsymbol{\theta}, \chi')) \chi' \left(1 - \frac{\chi'}{\chi}\right)$$

$$\psi_{ij} \equiv \frac{\partial \Delta\theta^i}{\partial \theta^j} = \frac{\partial^2}{\partial \theta^i \partial \theta^j} \phi_L(\boldsymbol{\theta}) = \frac{2}{c^2} \int_0^\chi d\chi' \Phi_{,ij}(\mathbf{x}(\boldsymbol{\theta}, \chi')) \chi' \left(1 - \frac{\chi'}{\chi}\right)$$

$$A_{ij} \equiv \frac{\partial \theta_S^i}{\partial \theta^j} = \begin{pmatrix} 1 - \kappa - \gamma_1 & -\gamma_2 \\ -\gamma_2 & 1 - \kappa + \gamma_1 \end{pmatrix}$$

$$A_{ij} = \delta_{ij} + \psi_{ij}$$

$$\kappa = \psi_{11} + \psi_{22} = \frac{2}{c^2} \int_0^\chi d\chi' \nabla^2 \Phi(\mathbf{x}(\boldsymbol{\theta}, \chi')) \chi' \left(1 - \frac{\chi'}{\chi}\right)$$

$$\gamma_1 = -\frac{\psi_{11} - \psi_{22}}{2} \qquad \gamma_2 = -\psi_{12}$$