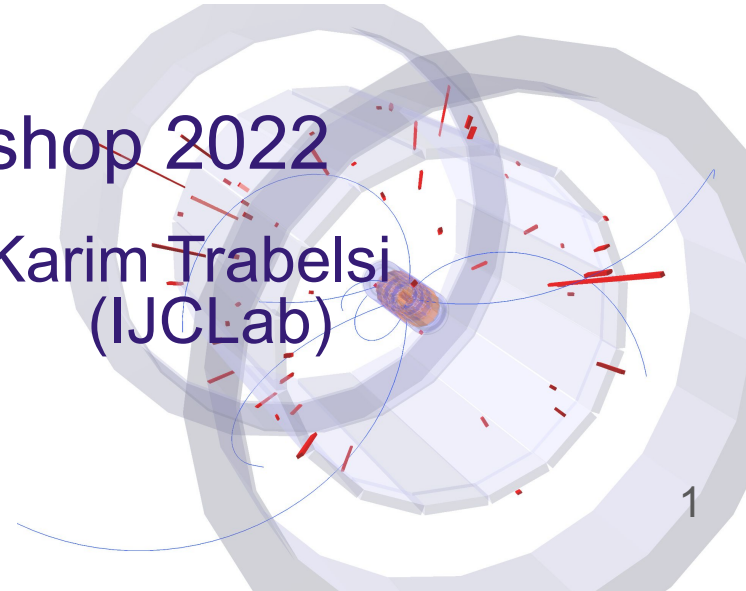


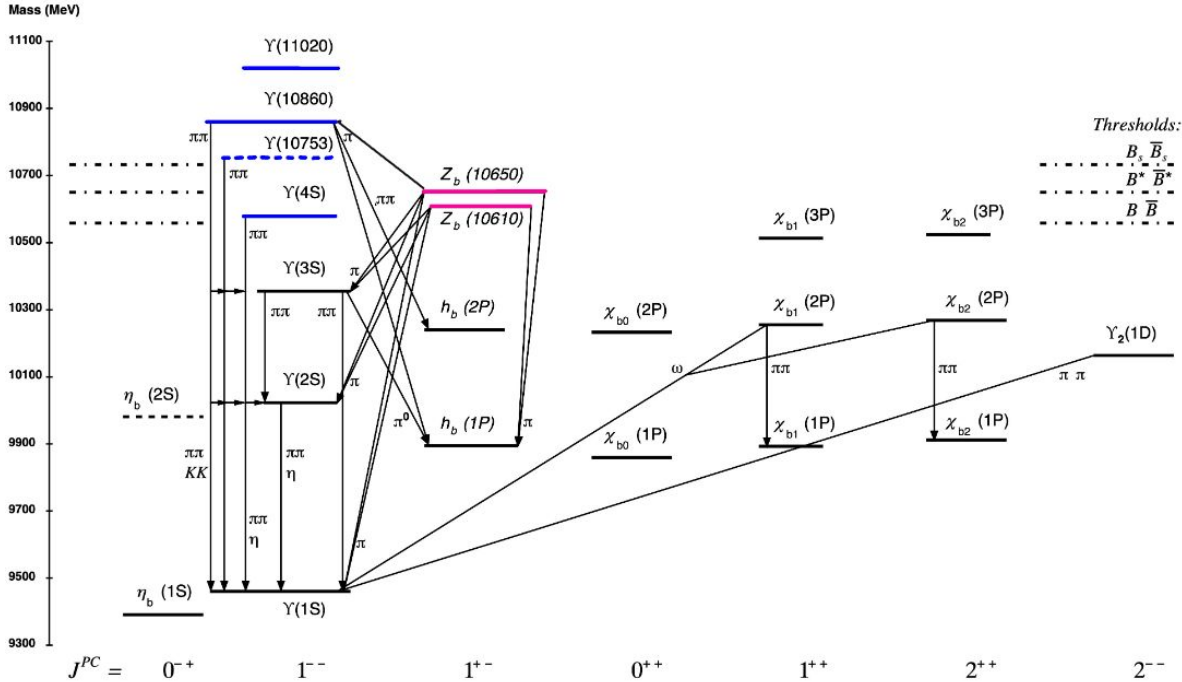
# Bottomonium spectroscopy at Belle/Belle II

GDR-InF Annual Workshop 2022

Pavel Oskin, Roman Mizuk, Karim Trabelsi  
(IJCLab) (HSE) (IJCLab)



# Bottomonium



non-relativistic system ( $v/c \sim 0.06$ )

The spectroscopy is similar to a hydrogen atom and we use the same notation.

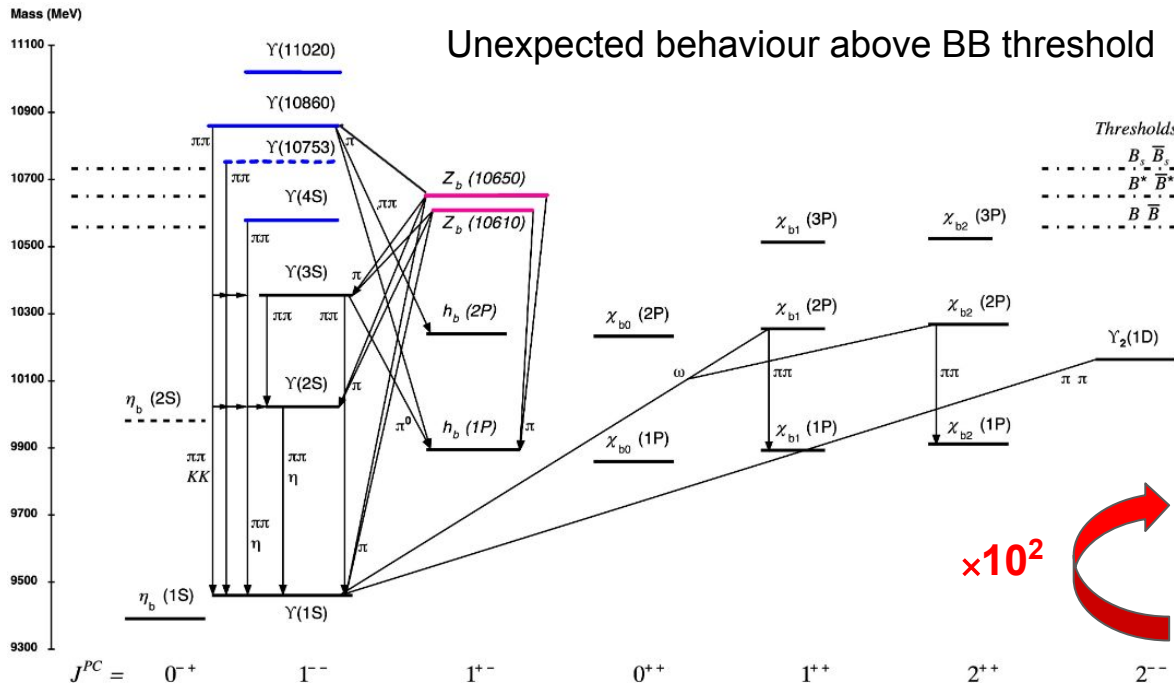
We have two type of states:

- Below BB threshold
- Above BB threshold

The states below BB mesons threshold are well described by the potential models.

Conventional bottomonium (pure bb states)  
 Bottomonium-like states (mixture of bb and BB)  
 Purely exotic states

# Bottomonium



Process	$\Gamma$ , MeV
$\Upsilon(5S) \rightarrow \Upsilon(1S)\eta$	$0.039 \pm 0.011$
$\Upsilon(5S) \rightarrow \Upsilon(2S)\eta$	$0.204 \pm 0.44$
$\Upsilon(4S) \rightarrow \Upsilon(1S)\eta$	$0.004 \pm 0.0008$
$\Upsilon(4S) \rightarrow h_b(1P)\eta$	$0.045 \pm 0.007$
$\Upsilon(3S) \rightarrow \Upsilon(1S)\eta$	$< 0.002 \cdot 10^{-3}$
$\Upsilon(2S) \rightarrow \Upsilon(1S)\eta$	$(0.0093 \pm 0.0015) \cdot 10^{-3}$

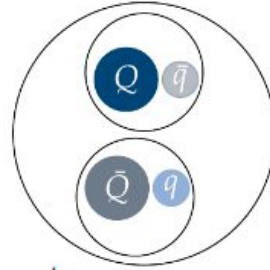
Process	$\Gamma$ , MeV
$\Upsilon(5S) \rightarrow \Upsilon(1S)\pi^+\pi^-$	$0.59 \pm 0.04 \pm 0.09$
$\Upsilon(5S) \rightarrow \Upsilon(2S)\pi^+\pi^-$	$0.85 \pm 0.07 \pm 0.16$
$\Upsilon(5S) \rightarrow \Upsilon(3S)\pi^+\pi^-$	$0.52^{+0.20}_{-0.17} \pm 0.10$
$\Upsilon(2S) \rightarrow \Upsilon(1S)\pi^+\pi^-$	$0.0060 \pm 0.0005$
$\Upsilon(3S) \rightarrow \Upsilon(1S)\pi^+\pi^-$	$0.0009 \pm 0.00008$
$\Upsilon(4S) \rightarrow \Upsilon(1S)\pi^+\pi^-$	$0.0019 \pm 0.0002$

Conventional bottomonium (pure bb states)  
 Bottomonium-like states (mixture of bb and BB)  
 Purely exotic states

PRL 100, 112001 (2008)

## Hadronic molecule

Compound state of two hadrons. The most promising model. The bottomonium-like states can be described as a mixture of pure bottomonium and a molecular component:



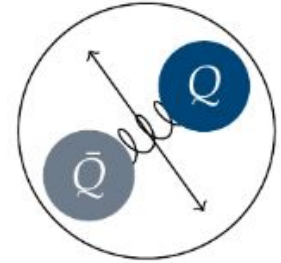
$$Y(4S, 5S) = C_1 \cdot |bb\rangle + C_2 \cdot |B_{(s)}^{((*)*)} B_{(s)}^{((*)*)}\rangle$$

$Z_b$ decay mode	Branching fraction
$Z_b^+(10610) \rightarrow \Upsilon(nS)/h_b(mP)\pi^+$	$14.4_{-1.9}^{+2.5}\%$
$Z_b^+(10610) \rightarrow B^+ \bar{B}^{*0}/B^+ \bar{B}^0$	$85.6_{-2.9}^{+2.1}\%$
$Z_b^+(10650) \rightarrow \Upsilon(nS)/h_b(mP)\pi^+$	$26.6_{-4.7}^{+5.0}\%$
$Z_b^+(10650) \rightarrow B^{*+} \bar{B}^{*0}$	$74_{-6}^{+4}\%$

PRL, 108, 122001 (2012)

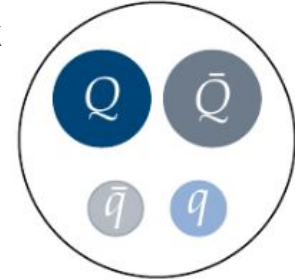
## Hybrid

Conventional quark-antiquark mesons with excited gluon degrees of freedom.



## Compact tetraquark

States containing four constituent quarks irrespective of their clustering.

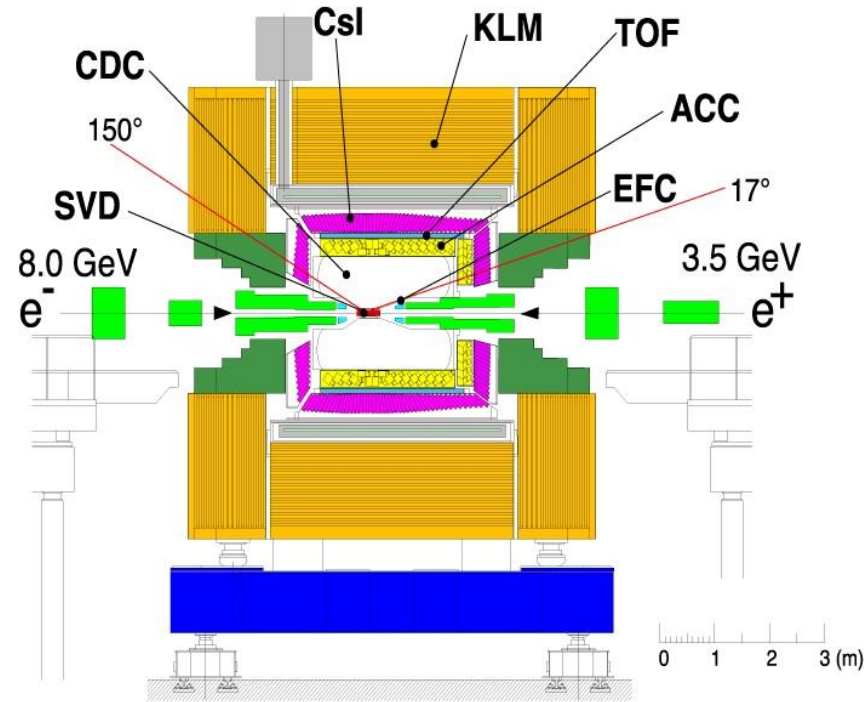


## Hadroquarkonium

Compact quarkonium core surrounded by an excited light-quark cloud.



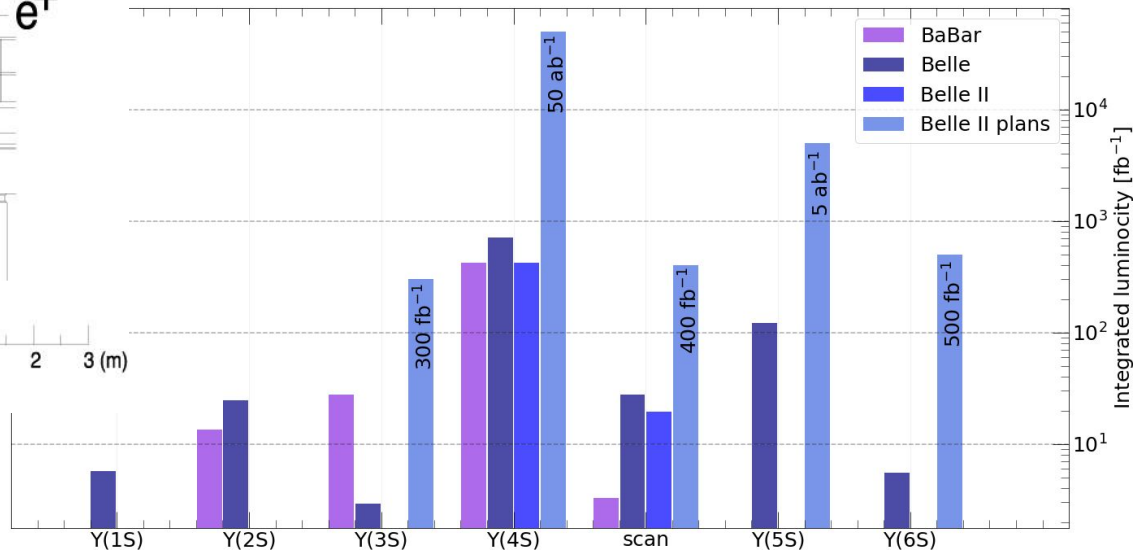
# KEKB and Belle



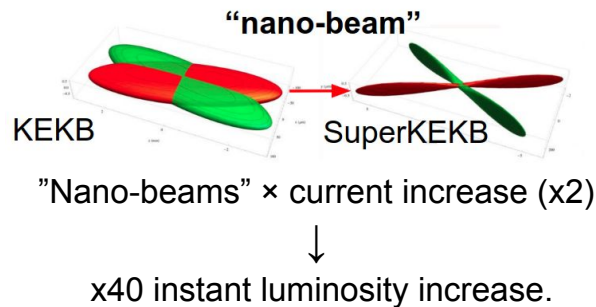
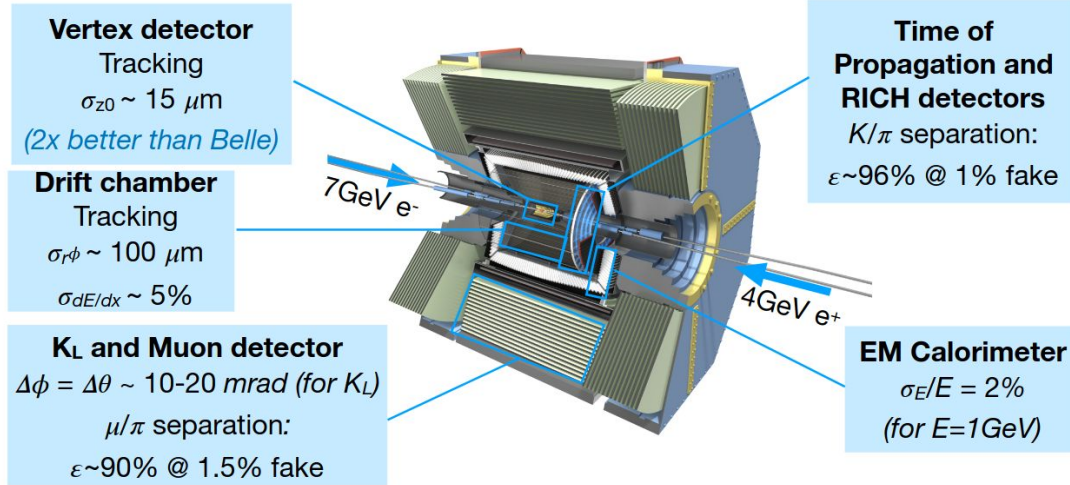
EPJ C 74, 3026 (2014)

Collected data:

- 121 fb<sup>-1</sup> at Y(5S)  $\sim 7.11 \times 10^6 B_s B_s$
- 711 fb<sup>-1</sup> at Y(4S)  $\sim 771 \times 10^6 BB$
- 3 fb<sup>-1</sup> at Y(3S)
- 24 fb<sup>-1</sup> at Y(2S)
- 6 fb<sup>-1</sup> at Y(1S)
- 26 fb<sup>-1</sup> scan above Y(4S)



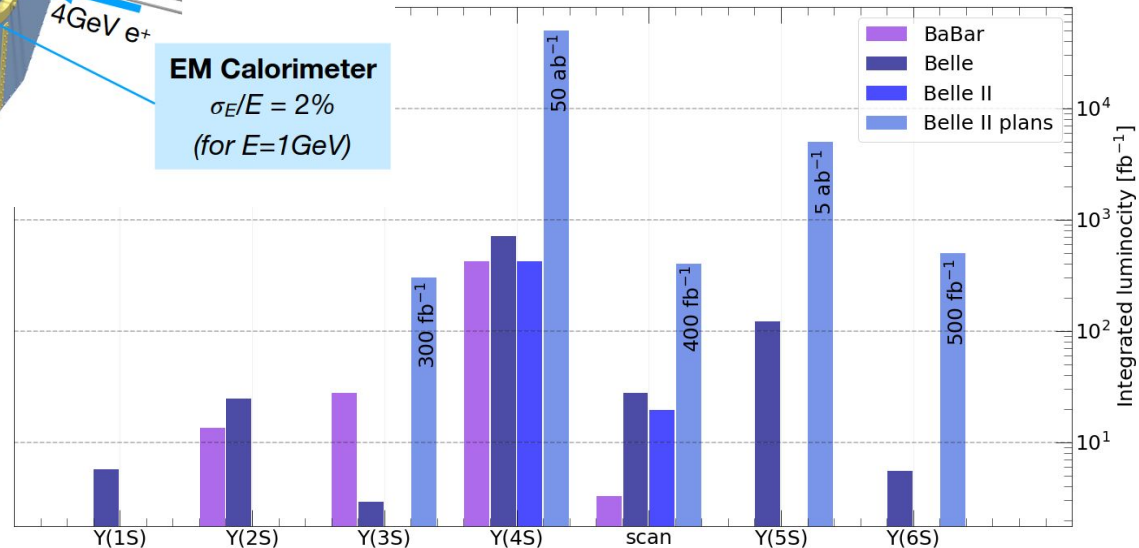
# SuperKEKB and Belle II



Collected data:

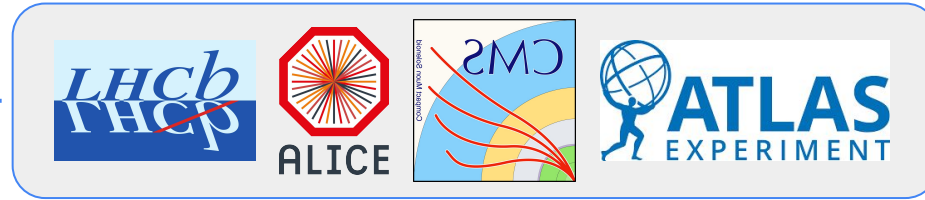
- 424  $\text{fb}^{-1}$  at Y(4S)
- 19  $\text{fb}^{-1}$  scan above Y(4S)

Improved detector and software performance.  
The main goal is to increase statistics!



# Bottomonium production

Prompt production

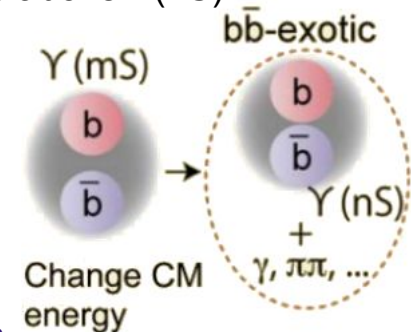


Direct production in  $e^+e^-$  collisions



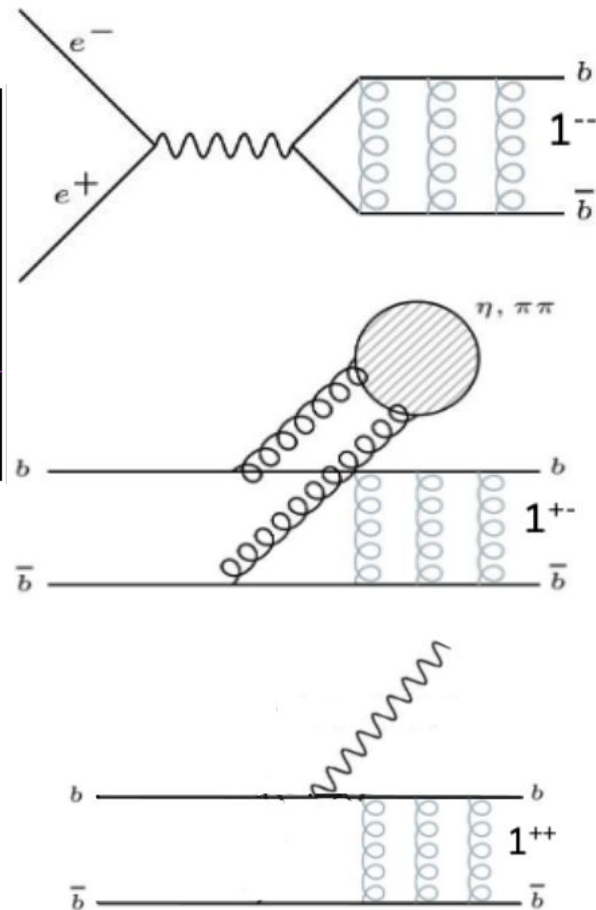
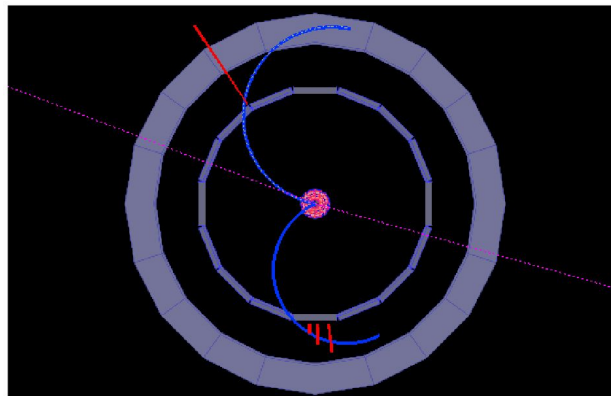
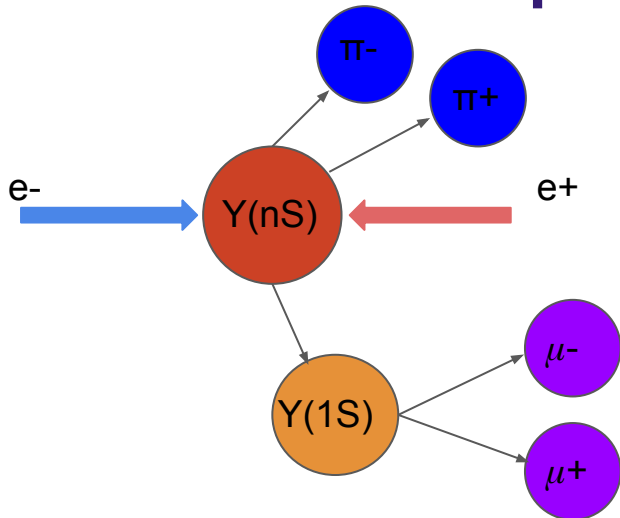
- Provides a unique clean environment (we have only bottomonium in the event);
- Precise measurement of the beam energy gives access to “unreconstructable” particles and decay modes;
- Allows tuning CM energy
- Only  $Y(nS)$  states can be produced with quantum numbers of the photon  $1^-$
- Other quantum numbers can be obtained via hadronic or radiative transitions from  $1^-$  states;

gives access to exotic states above  $Y(4S)$





# Bottomonium production



- Provides a unique clean environment (we have only bottomonium in the event);
- Precise measurement of the beam energy gives access to “unreconstructable” particles and decay modes;
- Allows tuning CM energy
- Only  $Y(nS)$  states can be produced with quantum numbers of the photon  $1^{--}$
- Other quantum numbers can be obtained via hadronic or radiative transitions from  $1^{--}$  states;

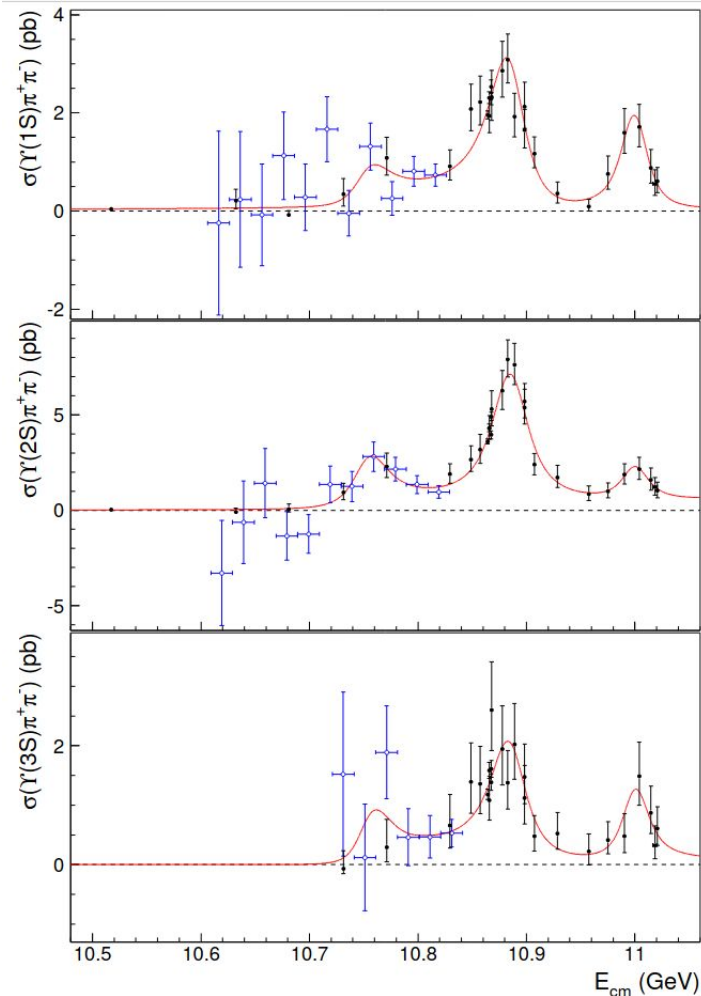
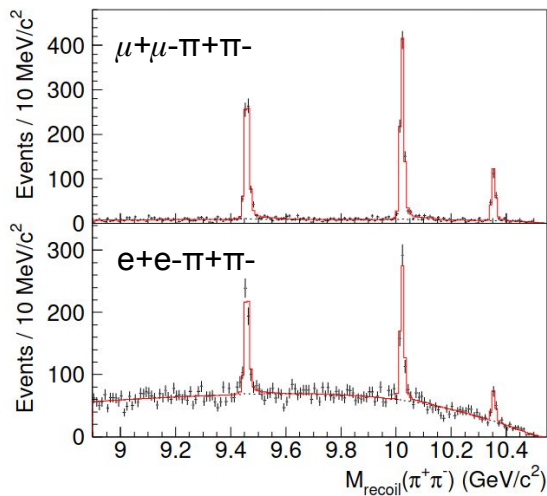
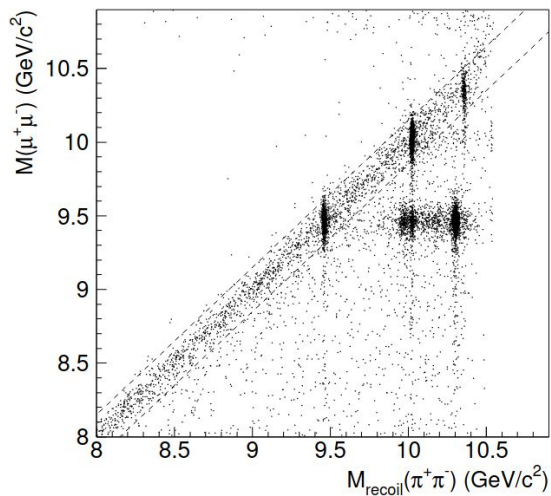


# Discovery of the $Y(10753)$

$Y(10753)$  state was observed in the  $e^+ e^- \rightarrow Y(nS) \pi^+ \pi^-$  ( $n = 1, 2, 3$ ) cross section energy dependence.

JHEP 10 (2019) 220

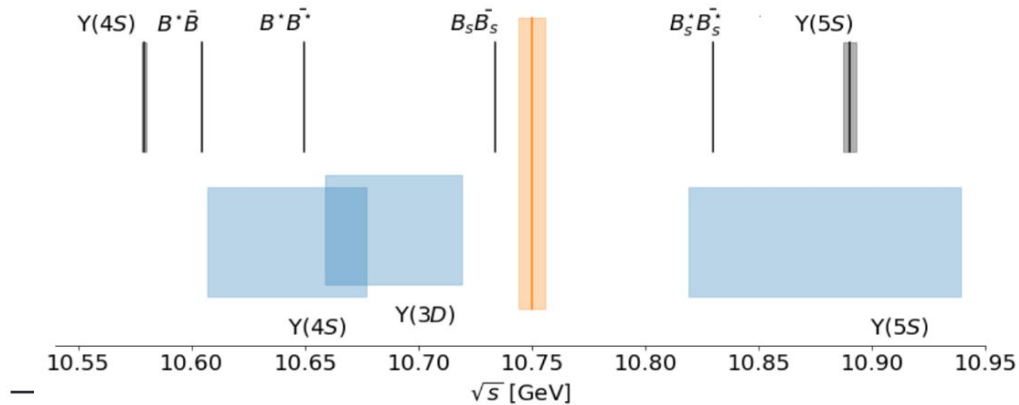
$\sqrt{s} = 10.864 \text{ GeV}$     $L = 47.647 \text{ fb}^{-1}$



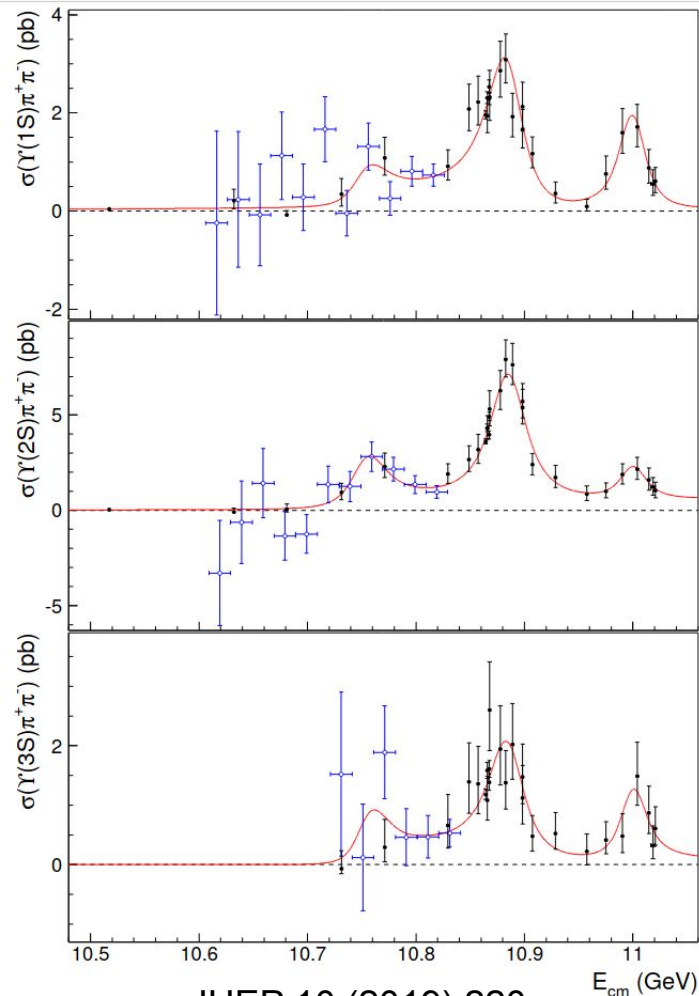
# Discovery of the $\Upsilon(10753)$

$\Upsilon(10753)$  was observed in the  $e^+ e^- \rightarrow \Upsilon(nS) \pi^+ \pi^-$  ( $n = 1, 2, 3$ ) cross section energy dependence.

- Molecular state? Does not coincide with a threshold.
- No obvious conventional bottomonium interpretation.



	$\Upsilon(10860)$	$\Upsilon(11020)$	New structure
$M$ (MeV/ $c^2$ )	$10885.3 \pm 1.5^{+2.2}_{-0.9}$	$11000.0^{+4.0}_{-4.5} {}^{+1.0}_{-1.3}$	$10752.7 \pm 5.9^{+0.7}_{-1.1}$
$\Gamma$ (MeV)	$36.6^{+4.5}_{-3.9} {}^{+0.5}_{-1.1}$	$23.8^{+8.0}_{-6.8} {}^{+0.7}_{-1.8}$	$35.5^{+17.6}_{-11.3} {}^{+3.9}_{-3.3}$

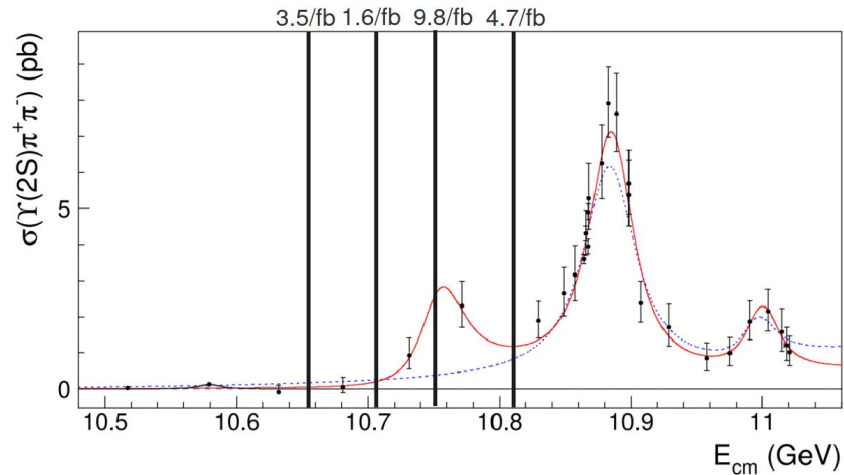
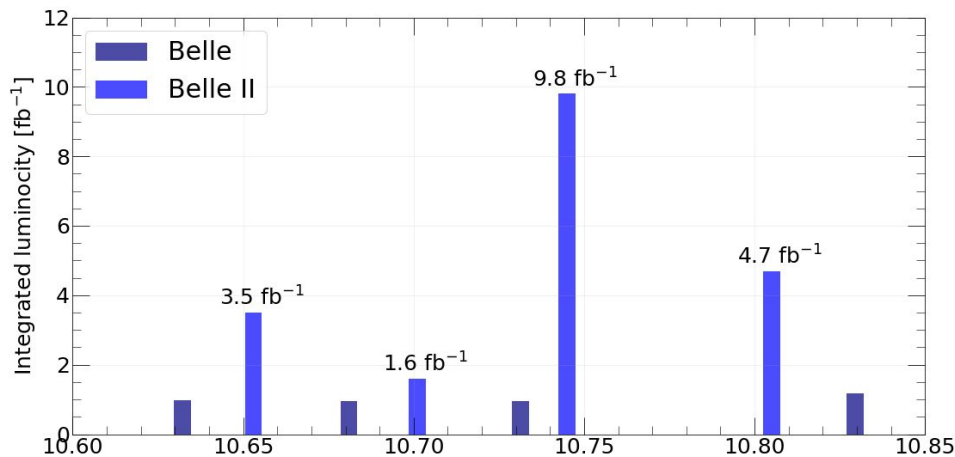


**JHEP 10 (2019) 220**

$E_{cm}$  (GeV)  
10

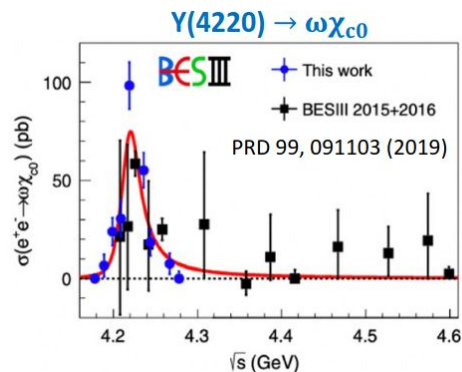
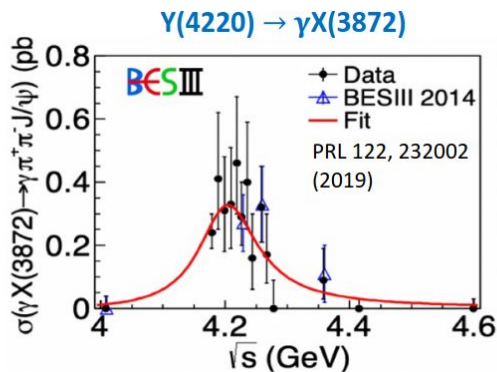
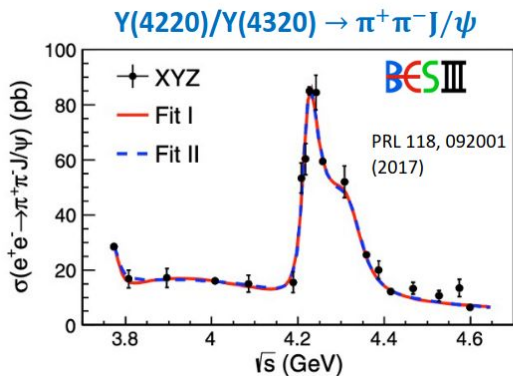
# Belle II energy scan above Y(4S)

- Unique data provide an opportunity to study Y(10753) in different final states and understand its nature.
- Scan above Y(4S) has a good potential for early physics impact by Belle II even with small statistics.

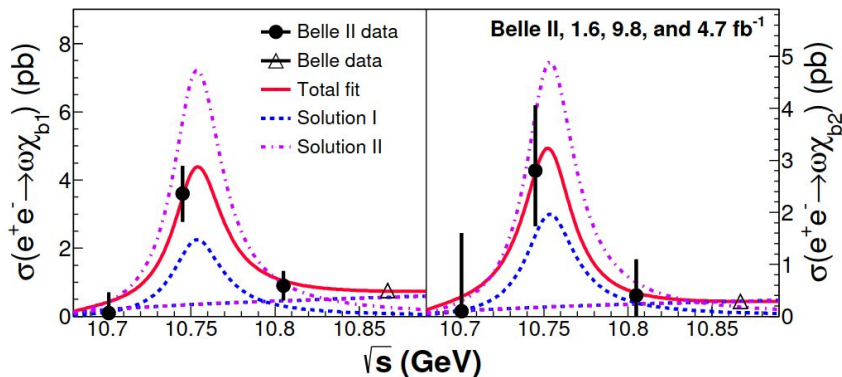


# Observation of $e^+e^- \rightarrow \omega\chi_{bJ}(1P)$ at $\sqrt{s} = 10.745$ GeV

- Similar to Y(10753) structure named Y(4220) was observed in  $e^+e^- \rightarrow J/\psi \pi^+\pi^-$  cross section dependence by BES III (PRL 118, 092001 (2017)).
- BES III also observed the Y(4220) peak in  $\gamma X(3872)$  and  $\omega\chi_{c0}$  final states (PRL, 122, 232002 (2019), PRD 99, 091103(R) (2019)).
- $\omega\chi_{b1,2}$  production was found to be enhanced near Y(5S) (PRL 113, 142001 (2014)).
- We expect Y(10753) to decay into  $\gamma[X_b \rightarrow \omega Y(1S)]$  and  $\omega\chi_{bJ}$  final states.



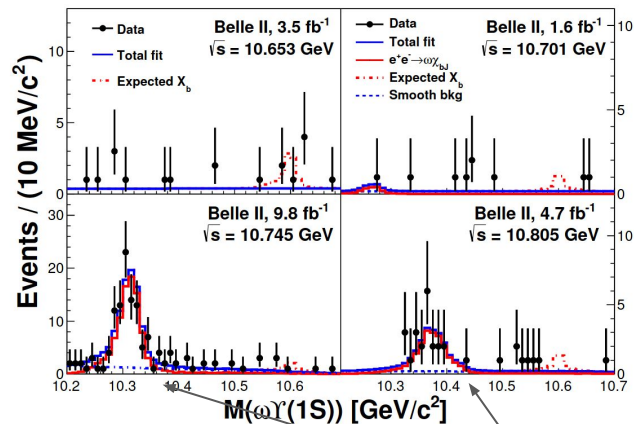
# Observation of $e^+e^- \rightarrow \omega\chi_{bJ}(1P)$ at $\sqrt{s} = 10.745$ GeV



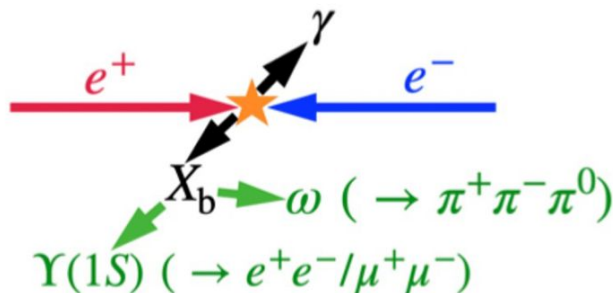
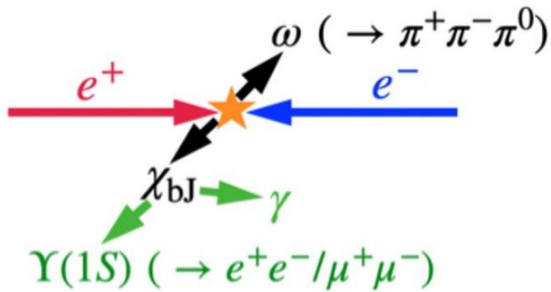
Strongly enhanced at 10.745 GeV.

$$\sigma(e^+e^- \rightarrow \omega\chi_{b1}) = 3.6 \pm 0.7 \pm 0.5 \text{ pb}$$

$$\sigma(e^+e^- \rightarrow \omega\chi_{b2}) = 2.8_{-1.0}^{+1.2} \pm 0.4 \text{ pb}$$



No evidence of  $X_b$  state. These are reflections of  $\omega\chi_{bJ}(1P)$ .



arXiv:2208.13189

# Search for $e^+e^- \rightarrow \eta_b(1S)\omega$ at $\sqrt{s} = 10.745$ GeV

There is tetraquark interpretation (Chin Phys. C 43 123102 (2019)) of  $Y(10753)$  state, which predicts enhancement of the  $Y(10753) \rightarrow \eta_b(1S)\omega$  transition:

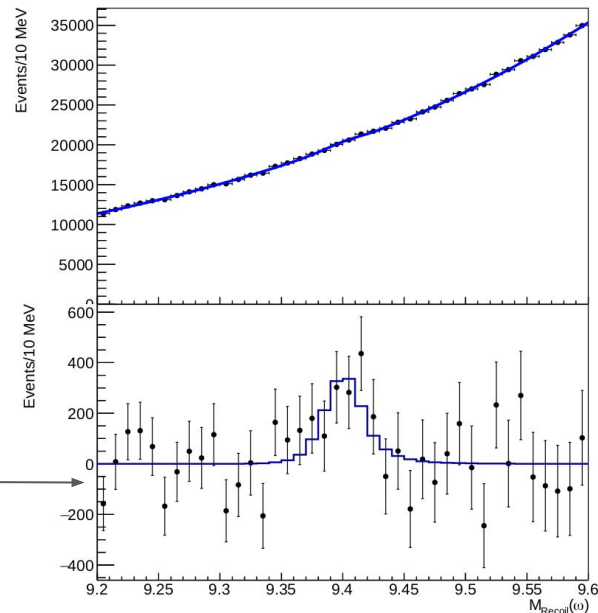
$$\frac{\Gamma(\eta_b \omega)}{\Gamma(\Upsilon \pi^+ \pi^-)} \sim 30$$

We reconstruct only  $\omega \rightarrow \pi^+ \pi^- \pi^0$  and use the recoil mass to identify signal.

$$M_{\text{recoil}}(\omega) = \sqrt{(\sqrt{s} - E_{\omega}^*)^2 - (p_{\omega}^*)^2}$$

Assuming the cross section of this transition is the same as  $\omega\chi_{b1}(1P)$ , we expect to have enough sensitivity to see the signal.

Belle II MC study



Also we search for  $e^+e^- \rightarrow \omega\chi_{bJ}(1P)$  ( $J = 0,1,2$ ) which are found to be enhanced at the scan energies

# BB decomposition with B-tagging

Study the energy dependence of the BB pairs production.

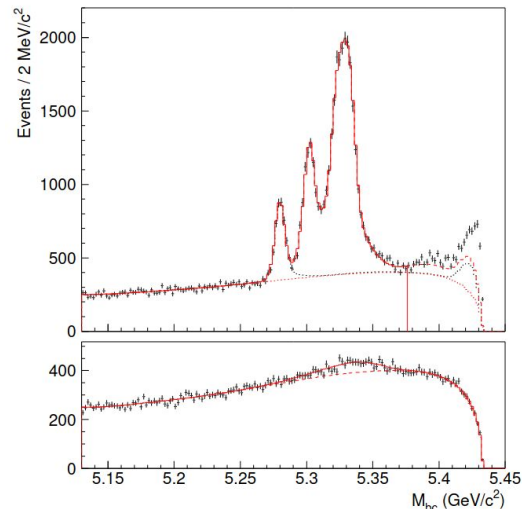
B-tagging can be used to measure the  $B_{(s)}^{(*)} B_{(s)}^{(*)}$  cross section energy dependence.

Yet another unique way to study bottomonium at Belle / Belle II.

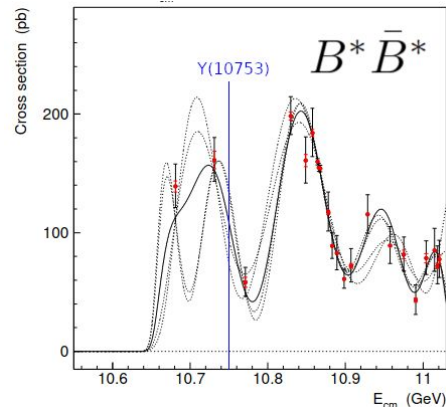
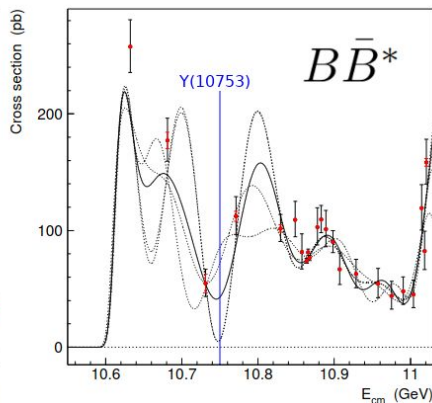
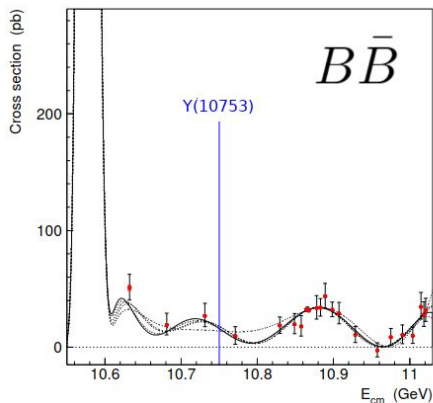
A good probe for bottomonium models (especially the molecular model)

Improving FEI performance could affect bottomonium studies.

JHEP 06 (2021) 137



$$M_{bc} = \sqrt{(E_{cm}/2)^2 - p_B^2}$$





# Belle II potential

Scan above Y(4S) gives an opportunity for a lot of unique studies:

- Y(10753) decays to different exclusive and inclusive final states. Study of its properties;
- Energy dependence of the various final state cross sections;
- BB decomposition and its cross section dependence on CM energy;

Wide range of long-term non-Y(4S) possibilities:

- Increase the above-Y(4S) scan statistics;
- Y(6S) region study with high statistics after accelerator upgrade;
- LFV / LFU / spectroscopy with Y(2S,3S) decays;

## Golden Modes

$$e^+e^- \rightarrow \pi^+\pi^-\Upsilon(pS)(\rightarrow \ell^+\ell^-)$$

$B\bar{B}$  decomposition

$$\pi^+\pi^-\text{ Dalitz}$$

$$Y_b \rightarrow \omega\eta_b(1S)$$

$$Y_b \rightarrow \omega\chi_{bJ}(1P)$$

## Silver Modes

$$Y_b \rightarrow \pi^+\pi^-X \text{ (inclusive)}$$

$$Y_b \rightarrow \eta X \text{ (inclusive)}$$

$$Y_b \rightarrow \eta\Upsilon(1S, 2S)(\rightarrow \ell^+\ell^-)$$

$$Y_b \rightarrow \eta'\Upsilon(1S)(\rightarrow \ell^+\ell^-)$$

$$Y_b \rightarrow \Upsilon(1S) \text{ (inclusive)}$$

## Bronze Modes

$$Y_b \rightarrow \gamma X_b$$

$$Y_b \rightarrow \pi^0\pi^0\Upsilon(pS)(\rightarrow \ell^+\ell^-)$$

$$Y_b \rightarrow KK(\phi)\Upsilon(pS)(\rightarrow \ell^+\ell^-)$$

$$Y_b \rightarrow \pi^0\pi^0X \text{ (inclusive)}$$

$$Y_b \rightarrow \pi^0X \text{ (incl. or excl.)}$$

...

# Summary

Belle and Belle II are unique devices for bottomonium studies:

- Tunable CM energy;
- Production in  $e^+ e^-$  collisions provides a low background environment;
- Precisely measured CM energy allows the studying of inclusive modes using the missing mass technique.

First results with above- $Y(4S)$  scan data:

- Successful runs above  $Y(4S)$ ;
- First observation of  $Y(10753) \rightarrow \chi_{bJ}(1P)\omega$ ;
- No evidence for  $X_b$  (bottomonium analog of  $X(3872)$ ) at  $\sqrt{s} = 10.745$  GeV;

Thank you for attention!

# Backup

# Backup

# LFV search in bottomonium decays

- $Y(1S) \rightarrow l^\pm l^\mp$  : Two-body vector meson CLFV process  $\rightarrow$  probing the vector and tensor operators of the effective Lagrangian for NP;
- $Y(1S) \rightarrow \gamma l^\pm l^\mp$  First study of three-body radiative CLFV (complementary access to NP);

PRD 94, 074023 (2016)

PRD 91, 113013 (2015)

- $Y(2S) \rightarrow Y(1S)\pi\pi$  is preferred over  $Y(1S)$

## PROS

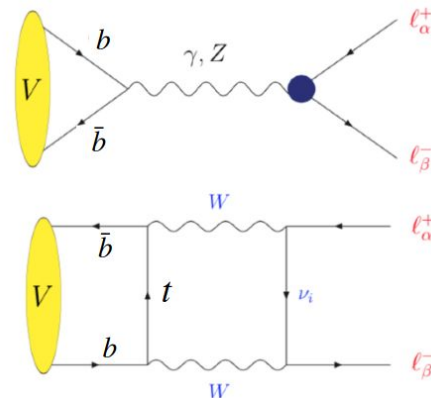
- higher trigger efficiency (two more tracks in the event);
- easier QED background suppression;
- $\pi\pi$  recoil mass has a better resolution;

## CONS

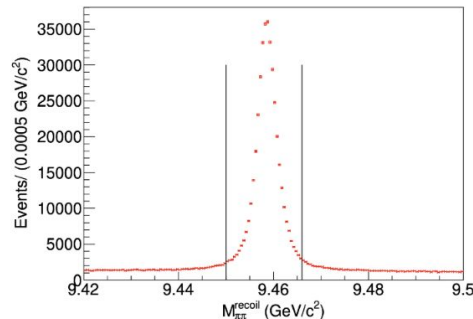
- Smaller statistics (26M vs 119M) due to  $\text{BF}[Y(1S) \rightarrow Y(1S)\pi\pi] \sim 18\%$ ;

- Background is studied on off-resonance data at 10.52 GeV;

JHEP 05 2022, 095



$\pi\pi$  recoil consistent with  $Y(1S)$  mass



$$M_{\pi\pi}^{\text{recoil}} = \sqrt{(E_{e^+e^-} - E_{\pi\pi})^2 - |\vec{p}_{\pi\pi}|^2}$$

$$M_{\pi\pi}^{\text{recoil}} \in (9.45, 9.466) \text{ GeV}/c^2$$

# LFV search in bottomonium decays

JHEP 05 2022, 095

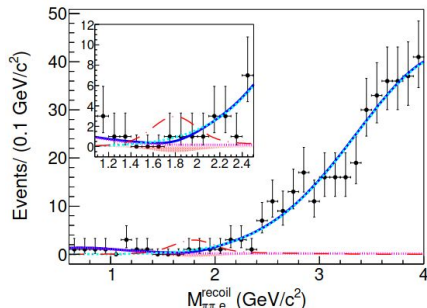
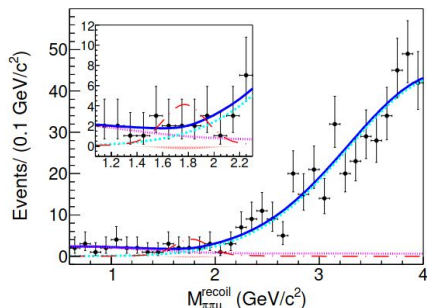
## $e\mu$ case

LFC decays are used for calibration

The b.r.'s are compared to world average

Expected  $\sim 9$  events from  $e/\mu$  mis-ID

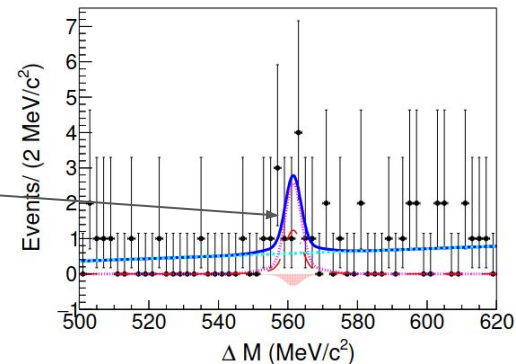
$$\Delta M = M(Y(2S)) - M(Y(1S)) = M(\pi\pi(\gamma)\Pi) \sim 560 \text{ MeV}$$



## $e\tau$ case

Background from  $\tau \rightarrow e(\mu)\nu(3\pi\nu)$  decays

Expected peak at  $\tau$  mass



Decay	$\epsilon$ (%)	$N_{\text{sig}}^{\text{fit}}$	$N_{\text{sig}}^{\text{UL}}$	$\mathcal{B}^{\text{UL}}$	PDG result
$\Upsilon(1S) \rightarrow e^\pm \mu^\mp$	32.5	$-1.3 \pm 3.7$	3.6	$3.9 \times 10^{-7}$	—
$\Upsilon(1S) \rightarrow \mu^\pm \tau^\mp$	8.8	$-1.5 \pm 4.3$	6.8	$2.7 \times 10^{-6}$	$6.0 \times 10^{-6}$
$\Upsilon(1S) \rightarrow e^\pm \tau^\mp$	7.1	$-3.5 \pm 2.7$	5.3	$2.7 \times 10^{-6}$	—
$\Upsilon(1S) \rightarrow \gamma e^\pm \mu^\mp$	24.6	$+0.8 \pm 1.5$	2.9	$4.2 \times 10^{-7}$	—
$\Upsilon(1S) \rightarrow \gamma \mu^\pm \tau^\mp$	5.8	$+2.1 \pm 5.9$	10.0	$6.1 \times 10^{-6}$	—
$\Upsilon(1S) \rightarrow \gamma e^\pm \tau^\mp$	5.0	$-9.5 \pm 6.3$	9.1	$6.5 \times 10^{-6}$	—