

# Enhancing $B_s \rightarrow e^+ e^-$ to an Observable Level

Gilberto Tetlalmatzi-Xolocotzi

*Based on:*

*M. Black, A. Plascencia and GTX, 2208.08995 [hep-ph]*

**CPPS, Theoretische Physik 1,  
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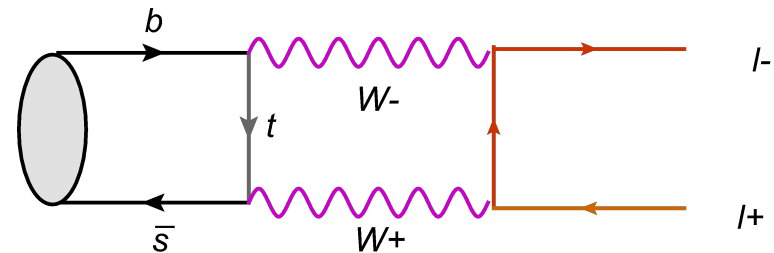
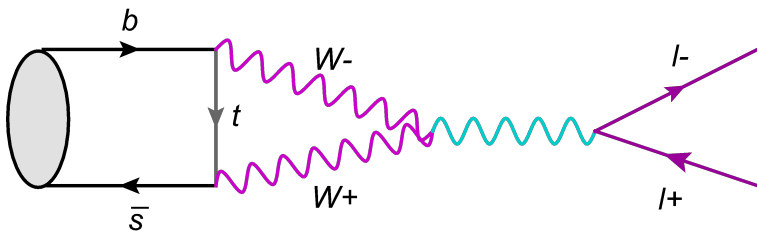
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# $B_s$ meson rare decays properties

In the SM the processes  $B_s \rightarrow l^+ l^-$  are induced **via loops**

$$l = e, \mu, \tau$$



They are **extremely clean**: all the non-perturbative information is encoded in the decay constant of the initial  $B$  meson which is known with a precision of 1%.

$$f_{B_s} = 230.3 \pm 1.3 \text{ MeV}$$

# $B_s$ meson rare decays properties

## Helicity suppression

$$\bar{B}r(B_s \rightarrow l^+ l^-)_{\text{SM}} = \frac{1}{1 - y_s} \frac{G_F^2 \alpha^2}{16\pi^3} \tau_{B_s} |V_{ts} V_{tb}^*|^2 f_{B_s}^2 M_{B_s} m_l^2 \sqrt{1 - 4 \frac{m_l^2}{M_{B_s}^2}} |C_{10}^{\text{SM}}|^2$$

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# Experimental Status

From a weighted average including measurements from LHCb, ATLAS and CMS:

$$\bar{B}r(B_s \rightarrow \mu^+ \mu^-)_{\text{Exp}} = (3.39 \pm 0.29) \times 10^{-9}$$

which is in agreement with the SM result

$$\bar{B}r(B_s \rightarrow \mu^+ \mu^-)_{\text{SM}} = (3.55 \pm 0.10) \times 10^{-9}$$

For pairs of  $\tau$  leptons in the final state

$$\bar{B}r(B_s \rightarrow \tau^+ \tau^-) < 6.8 \times 10^{-3} \quad \text{LHCb [hep-ex/1703.02508]}$$

$$\bar{B}r(B_s \rightarrow \tau^+ \tau^-)_{\text{SM}} = (7.52 \pm 0.20) \times 10^{-7}$$

# Experimental Status

Updated bound from LHCb

$$\bar{B}r(B_s \rightarrow e^+ e^-) < 9.4 \times 10^{-9}$$

LHCb [hep-ex/2003.03999]

$$\bar{B}r(B_s \rightarrow e^+ e^-)_{\text{SM}} = (8.30 \pm 0.22) \times 10^{-14}$$

**5 Orders of magnitude gap** between the experimental bound and the SM

The SM value is out of reach of current or foreseeable experiments

**Any near future observation of  $B_s \rightarrow e^+ e^-$  would be an unambiguous signal of NEW PHYSICS**

# Effective theory treatment

$$\mathcal{H}_{\text{eff}} = -\frac{G_F V_{tb} V_{ts}^* \alpha}{\sqrt{2}\pi} \left[ C_{10}^{\ell\ell} \mathcal{O}_{10}^{\ell\ell} + C_S^{\ell\ell} \mathcal{O}_S^{\ell\ell} + C_P^{\ell\ell} \mathcal{O}_P^{\ell\ell} + C_{10'}^{\ell\ell} \mathcal{O}_{10'}^{\ell\ell} + C_{S'}^{\ell\ell} \mathcal{O}_{S'}^{\ell\ell} + C_{P'}^{\ell\ell} \mathcal{O}_{P'}^{\ell\ell} \right] + \text{h.c.}$$

In the SM the only  $\mathcal{O}_{10}^{\ell\ell} = (\bar{s} \gamma_\mu P_L b) (\bar{\ell} \gamma^\mu \gamma_5 \ell)$  contributes

NP Vector operator  $\longrightarrow \mathcal{O}_{10'}^{\ell\ell} = (\bar{s} \gamma_\mu P_R b) (\bar{\ell} \gamma^\mu \gamma_5 \ell)$

NP Scalar operators  $\longrightarrow \mathcal{O}_S^{\ell\ell} = m_b (\bar{s} P_R b) (\bar{\ell} \ell) \quad \mathcal{O}_{S'}^{\ell\ell} = m_b (\bar{s} P_L b) (\bar{\ell} \ell)$

NP Pseudoscalar operators  $\longrightarrow \mathcal{O}_P^{\ell\ell} = m_b (\bar{s} P_R b) (\bar{\ell} \gamma^5 \ell)$   
 $\longrightarrow \mathcal{O}_{P'}^{\ell\ell} = m_b (\bar{s} P_L b) (\bar{\ell} \gamma^5 \ell)$

# Enhancements on $B_s \rightarrow e^+ e^-$

In the presence of pseudoscalar and scalar particles

$$\bar{B}r(B_s \rightarrow l^+ l^-) = \bar{B}r(B_s \rightarrow l^+ l^-)_{\text{SM}} \times \left[ |P_{\ell\ell}|^2 + \frac{1 - y_s}{1 + y_s} |S_{\ell\ell}|^2 \right]$$

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$$P_{\ell\ell} \equiv \frac{C_{10}^{\ell\ell} - C_{10'}^{\ell\ell}}{C_{10}^{\text{SM}}} + \frac{M_{B_s}^2}{2m_\ell} \left( \frac{m_b}{m_b + m_s} \right) \left[ \frac{C_P^{\ell\ell} - C_{P'}^{\ell\ell}}{C_{10}^{\text{SM}}} \right]$$

$$S_{\ell\ell} \equiv \sqrt{1 - 4 \frac{m_\ell^2}{M_{B_s}^2}} \frac{M_{B_s}^2}{2m_\ell} \left( \frac{m_b}{m_b + m_s} \right) \left[ \frac{C_S^{\ell\ell} - C_{S'}^{\ell\ell}}{C_{10}^{\text{SM}}} \right]$$

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For electrons and muons the factor  
enhances the NP effects

$m_\ell$

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R. Fleischer,  
R. Jaarsma,  
GTX  
[1703.10160]

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For electrons the enhancement effect is maximal.

For the effect to take place the Wilson coefficients should not be proportional to the mass of the final state lepton.



# The THDM and $B_s \rightarrow e^+ e^-$

## The Type III THDM

$$-\mathcal{L} \supset \bar{Q}_L \left( Y_1^u \tilde{H}_1 + Y_2^u \tilde{H}_2 \right) u_R + \bar{Q}_L \left( Y_1^d H_1 + Y_2^d H_2 \right) d_R \\ + \bar{\ell}_L \left( Y_1^e H_1 + Y_2^e H_2 \right) e_R + \text{h.c.},$$

The two doublets are coupled to quarks and leptons

$$H_1^T = (H_1^+, (v_1 + H_1^0 + iA_1^0)/\sqrt{2})$$

$$\tilde{H}_1 = i\sigma_2 H_1^*$$

Rotation to the  
physics basis

$$\begin{pmatrix} H \\ h \end{pmatrix} = \begin{pmatrix} \cos \alpha & \sin \alpha \\ -\sin \alpha & \cos \alpha \end{pmatrix} \begin{pmatrix} H_1^0 \\ H_2^0 \end{pmatrix}$$

$$\begin{pmatrix} G \\ A \end{pmatrix} = \begin{pmatrix} \cos \beta & \sin \beta \\ -\sin \beta & \cos \beta \end{pmatrix} \begin{pmatrix} A_1^0 \\ A_2^0 \end{pmatrix}$$

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SM  
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NP neutral  
scalars

SM  
Higgs

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# The THDM and $B_s \rightarrow e^+ e^-$

The relevant interactions are then

$$-\mathcal{L} \supset y_{ee} \bar{e}eH + y_{bs} \bar{b}sH - i y_{ee} \bar{e}\gamma^5 eA - i y_{bs} \bar{b}\gamma^5 sA$$

leading to the following Wilson coefficients

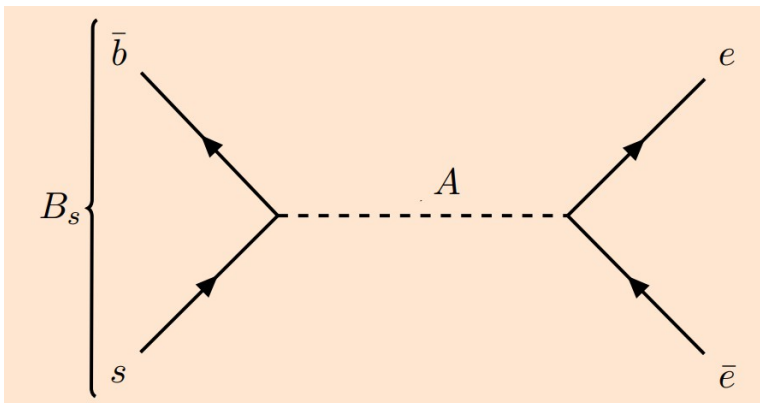
$$C_S^{ee} = \frac{y_{ee}y_{bs}}{M_H^2} \left( \frac{\sqrt{2}\pi}{m_b G_F V_{tb} V_{ts}^* \alpha} \right),$$

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$$C_{S'}^{ee} = C_S^{ee},$$

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← In our model



$$P_{ll} \equiv \frac{C_{10}^{ll} - C_{10'}^{ll}}{C_{10}^{\text{SM}}} + \frac{M_{B_s}^2}{2m_\ell} \left( \frac{m_b}{m_b + m_s} \right) \left[ \frac{C_P^{ll} - C_{P'}^{ll}}{C_{10}^{\text{SM}}} \right]$$

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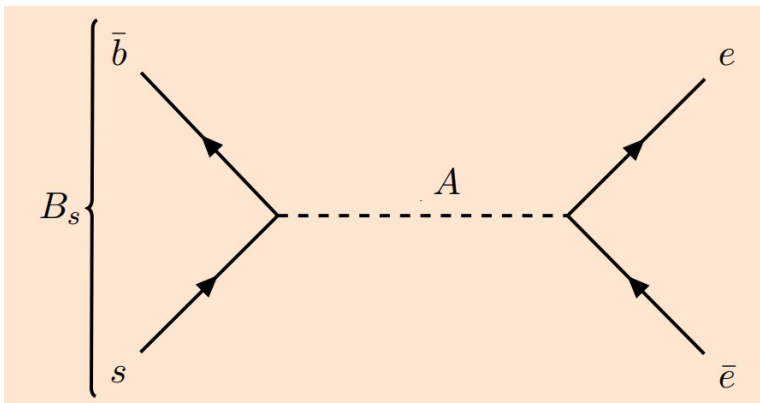
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No contribution from **H** to the branching fraction

# Phenomenological constraints

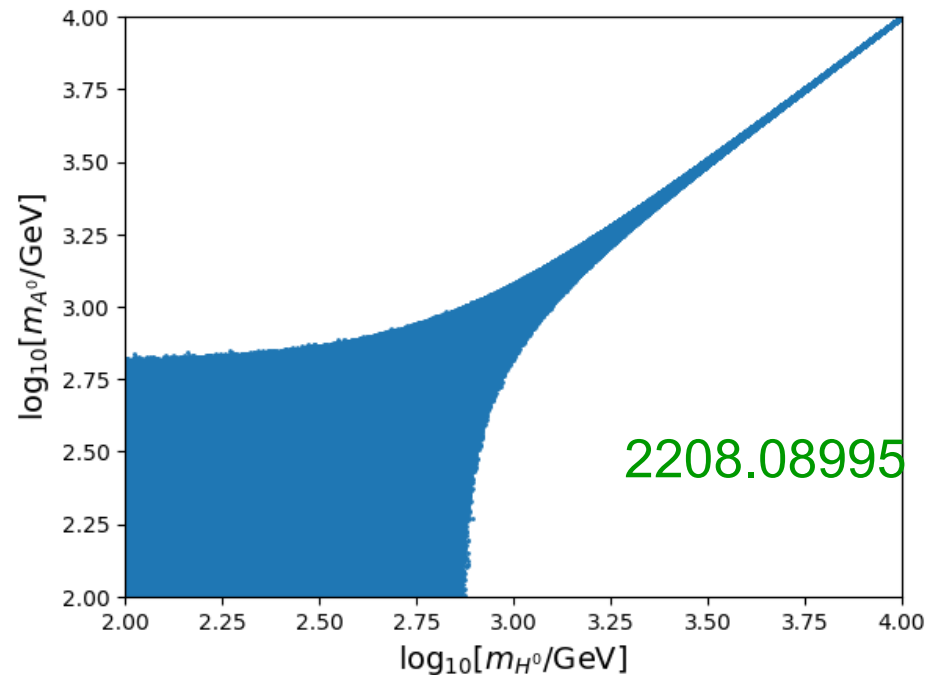
## Scalar potential

$$\begin{aligned} V(H_1, H_2) = & m_{11}^2 H_1^\dagger H_1 + m_{22}^2 H_2^\dagger H_2 - m_{12}^2 \left[ (H_1^\dagger H_2) + \text{h.c.} \right] \\ & + \frac{\lambda_1}{2} (H_1^\dagger H_1)^2 + \frac{\lambda_2}{2} (H_2^\dagger H_2)^2 + \lambda_3 (H_1^\dagger H_1) (H_2^\dagger H_2) + \lambda_4 (H_1^\dagger H_2) (H_2^\dagger H_1) \\ & + \left[ \frac{\lambda_5}{2} (H_1^\dagger H_2)^2 + \lambda_6 (H_1^\dagger H_1) (H_1^\dagger H_2) + \lambda_7 (H_2^\dagger H_2) (H_1^\dagger H_2) + \text{h.c.} \right]. \end{aligned}$$

## Mass constraints

From perturbativity  
and vacuum stability

$$\begin{aligned} 0 < \lambda_{1,2} &< 4 \\ -\sqrt{\lambda_1 \lambda_2} < \lambda_3 &< 4 \\ -4 < \lambda_{4,5,6,7} &< 4 \end{aligned}$$



# Phenomenological constraints

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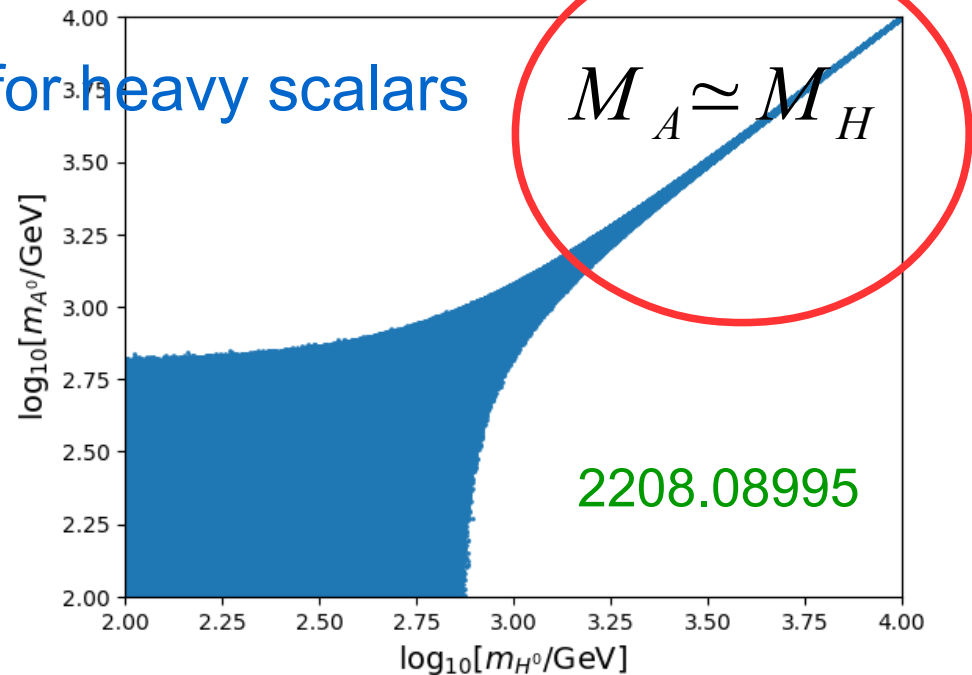
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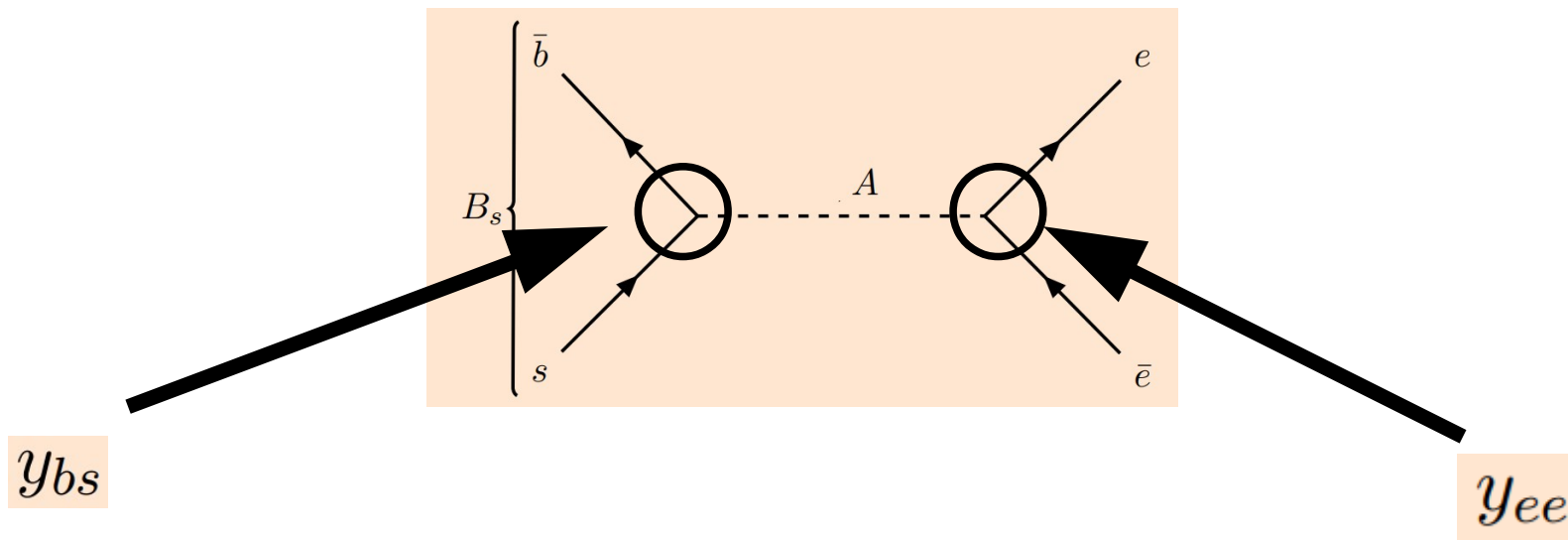
for heavy scalars





# Phenomenological constraints

The possible size of the NP couplings to quarks and leptons has to be determined



Constraints on the leptonic coupling  $y_{ee}$

From  $e^+e^- \rightarrow e^+e^-$  scattering

Constraints derived from  $\rightarrow$  LEP electroweak working group [hep-ex/0612034]

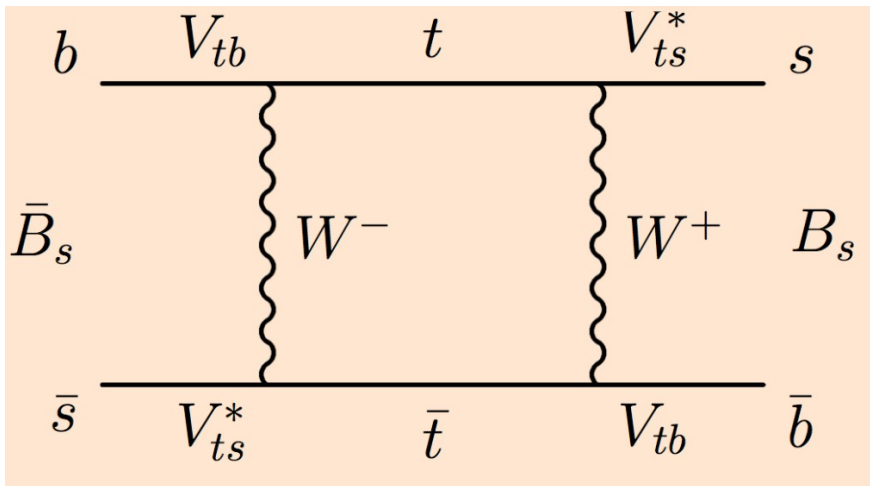
$$\frac{y_{ee}^2}{M_H^2} + \frac{y_{ee}^2}{M_A^2} < \frac{1}{(4 \text{ TeV})^2}$$

# Phenomenological constraints

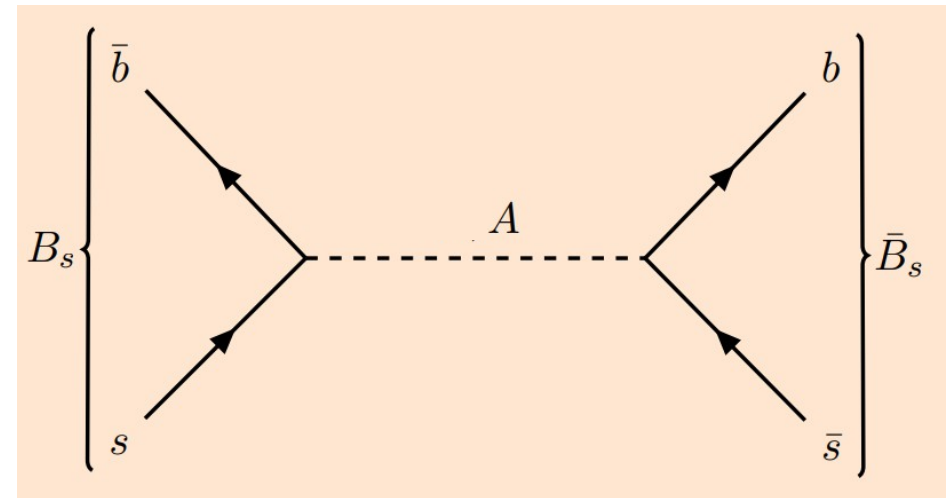
Constraints on the quark coupling  $y_{bs}$

Constraints from neutral B meson mixing

Standard Model



New Physics



$$\Delta M_s^{\text{SM}} = 17.49 \pm 0.64 \text{ ps}^{-1}$$

$$\Delta M_s^{\text{Exp}} = 17.765 \pm 0.006 \text{ ps}^{-1}$$



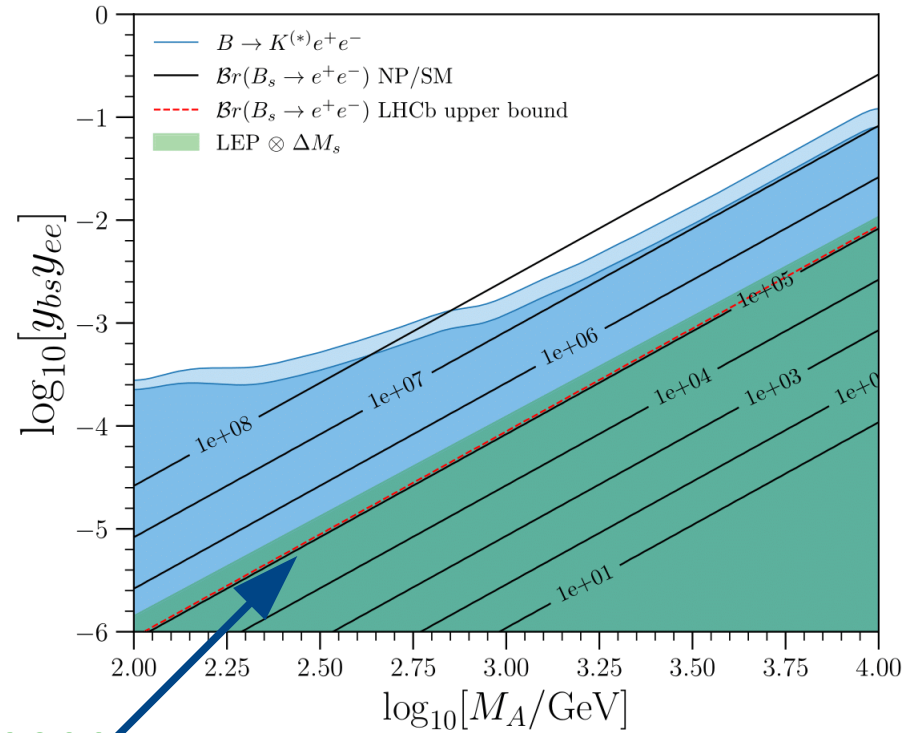
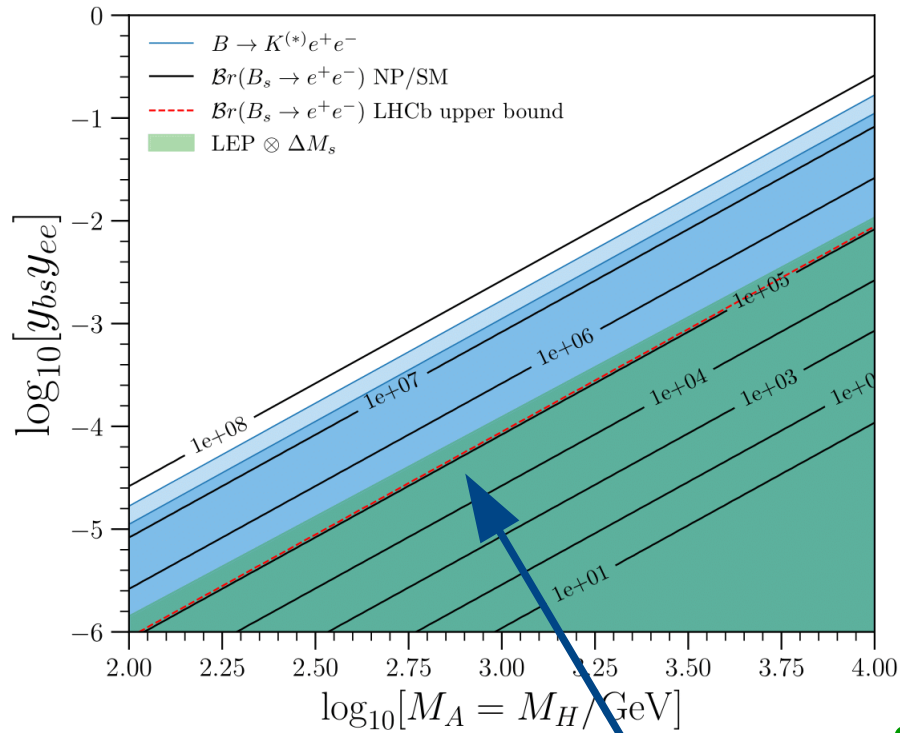
# Phenomenological constraints

Constraints on the product  $y_{ee}y_{bs}$  from  $B \rightarrow K^{(*)}e^+e^-$   
 triggered by  $b \rightarrow se^+e^-$  transitions

Observable	$q^2$ bin (GeV <sup>2</sup> )	Exp. Avg.	SM Pred.
$10^8 \times \frac{\Delta\mathcal{B}}{\Delta q^2}(B^+ \rightarrow K^+e^+e^-)$	[1.0,6.0]	$3.24 \pm 0.65$ [37, 38]	$3.37 \pm 0.56$
	[0.1,4.0]	$4.70 \pm 1.01$ [38]	$3.40 \pm 0.58$
	[4.0,8.12]	$2.36 \pm 0.79$ [38]	$3.31 \pm 0.54$
$10^7 \times \frac{\Delta\mathcal{B}}{\Delta q^2}(B^0 \rightarrow K^{*0}e^+e^-)$	[0.003,1.0]	$3.09 \pm 0.99$ [39]	$2.10 \pm 0.35$
$P'_4(B \rightarrow K^*e^+e^-)$	[1.0,6.0]	$-0.71 \pm 0.40$ [40]	$-0.34 \pm 0.04$
	[14.18,19.0]	$-0.15 \pm 0.41$ [40]	$-0.63 \pm 0.01$
$P'_5(B \rightarrow K^*e^+e^-)$	[1.0,6.0]	$-0.23 \pm 0.41$ [40]	$-0.42 \pm 0.09$
	[14.18,19.0]	$-0.86 \pm 0.34$ [40]	$-0.63 \pm 0.03$

Direct sensitivity to the Wilson coefficients  $C_{S^{(\prime)}, P^{(\prime)}}^{ee}$

# Phenomenological constraints



2208.08995

It is possible to saturate the current experimental bounds while obeying the known constraints

# Generating the NP couplings

## Pati-Salam like model

Consider the model introduced in

P. Fileviez-Perez  
M.B. Wise  
[1307.6213]

based on the symmetry group

$$SU(4)_C \otimes SU(2)_L \otimes U(1)_R$$

SM matter fields  
(leptons are the  
4<sup>th</sup> color of fermions)

$$F_{QL} = \begin{pmatrix} u_r & u_g & u_b & \nu \\ d_r & d_g & d_b & e \end{pmatrix} \sim (4, 2, 0),$$

$$F_u = (u_r^c \ u_g^c \ u_b^c \ \nu^c) \sim (\bar{4}, 1, -1/2),$$

$$F_d = (d_r^c \ d_g^c \ d_b^c \ e^c) \sim (\bar{4}, 1, 1/2).$$

This scenario can be considered a low energy limit of the  
Pati-Salam model

J. C. Pati and  
A. Salam  
Phys. Rev. D 10, 275

Quarks and leptons are unified at low energy

# Generating the NP couplings

## The Yukawa sector

$$-\mathcal{L} = \bar{u}_R \left( Y_1^T \tilde{H}_1 + \frac{1}{2\sqrt{3}} Y_2^T \tilde{H}_2 \right) Q_L + \bar{N}_R \left( Y_1^T \tilde{H}_1 - \frac{\sqrt{3}}{2} Y_2^T \tilde{H}_2 \right) \ell_L \\ + \bar{d}_R \left( Y_3^T H_1^\dagger + \frac{1}{2\sqrt{3}} Y_4^T H_2^\dagger \right) Q_L + \bar{e}_R \left( Y_3^T H_1^\dagger - \frac{\sqrt{3}}{2} Y_4^T H_2^\dagger \right) \ell_L + \text{h.c.}$$

## Type III THDM with 4 Yukawa matrices

$$\tilde{Y}^\ell = (\tan \beta - 3 \cot \beta) \frac{M_{\text{diag}}^E}{4v} + 3 (\tan \beta + \cot \beta) \frac{V_c^T M_{\text{diag}}^D V}{4v},$$

$$\tilde{Y}^d = (3 \tan \beta - \cot \beta) \frac{M_{\text{diag}}^D}{4v} + (\tan \beta + \cot \beta) \frac{V_c^* M_{\text{diag}}^E V^\dagger}{4v},$$



Physical matrices

# Generating the NP couplings

Rotation matrix

$$V = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13} & c_{12}c_{23} - s_{12}s_{23}s_{13} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13} & -c_{12}s_{23} - s_{12}c_{23}s_{13} & c_{23}c_{13} \end{pmatrix}$$

For  $\tan \beta \gg 1$   $s_{ij} \rightarrow 1$   $s'_{ij} \rightarrow 1$

$$\tilde{Y}^{\ell} = \frac{\tan \beta}{4v} \begin{pmatrix} m_e + 3m_b & \varepsilon & \varepsilon \\ \varepsilon & m_{\mu} + 3m_s & \varepsilon \\ \varepsilon & \varepsilon & m_{\tau} + 3m_d \end{pmatrix}$$

$$y_{ee} \gg y_{\mu\mu}, y_{\tau\tau}$$

$$\tilde{Y}^d = \frac{\tan \beta}{4v} \begin{pmatrix} 3m_d + m_{\tau} & \varepsilon & \varepsilon \\ \varepsilon & 3m_s + m_{\mu} & \varepsilon \\ \varepsilon & \varepsilon & 3m_b + m_e \end{pmatrix}$$

$$y_{dd} \simeq y_{bb} \gg y_{ss}$$



# Generating the NP couplings

$$\mathcal{H}_{\text{eff}} \supset -\frac{y_{ee}y_{\mu\tau}}{M_H^2}(\bar{\tau}\mu)(\bar{e}e) - \frac{y_{\tau\tau}y_{\mu\tau}}{M_H^2}(\bar{\tau}\mu)(\bar{\tau}\tau) \\ + \frac{y_{ee}y_{\mu\tau}}{M_A^2}(\bar{\tau}\gamma^5\mu)(\bar{e}\gamma^5e) + \frac{y_{\tau\tau}y_{\mu\tau}}{M_A^2}(\bar{\tau}\gamma^5\mu)(\bar{\tau}\gamma^5\tau)$$

$$\mathcal{O}_{LL}^{ee} = \bar{\tau}(1 - \gamma_5)\mu \bar{e}(1 - \gamma_5)e,$$

$$\mathcal{O}_{RR}^{ee} = \bar{\tau}(1 + \gamma_5)\mu \bar{e}(1 + \gamma_5)e,$$

$$\mathcal{O}_{LR}^{ee} = \bar{\tau}(1 - \gamma_5)\mu \bar{e}(1 + \gamma_5)e,$$

$$\mathcal{O}_{RL}^{ee} = \bar{\tau}(1 + \gamma_5)\mu \bar{e}(1 - \gamma_5)e,$$

$$C_{LL}^{ee} = C_{RR}^{ee} = \frac{y_{ee}y_{\mu\tau}}{4} \left[ \frac{1}{M_H^2} - \frac{1}{M_A^2} \right], \quad C_{LR}^{ee} = C_{RL}^{ee} = \frac{y_{ee}y_{\mu\tau}}{4} \left[ \frac{1}{M_H^2} + \frac{1}{M_A^2} \right]$$

the model implies effects on the channels

$$\tau^- \rightarrow \mu^- e^+ e^-$$

$$\tau \rightarrow \mu\gamma$$

## Experimental bounds

$$\text{Br}(\tau^- \rightarrow \mu^- e^+ e^-) < 1.8 \times 10^{-8}$$

$$\text{Br}(\tau \rightarrow \mu\gamma) < 4.4 \times 10^{-8}$$

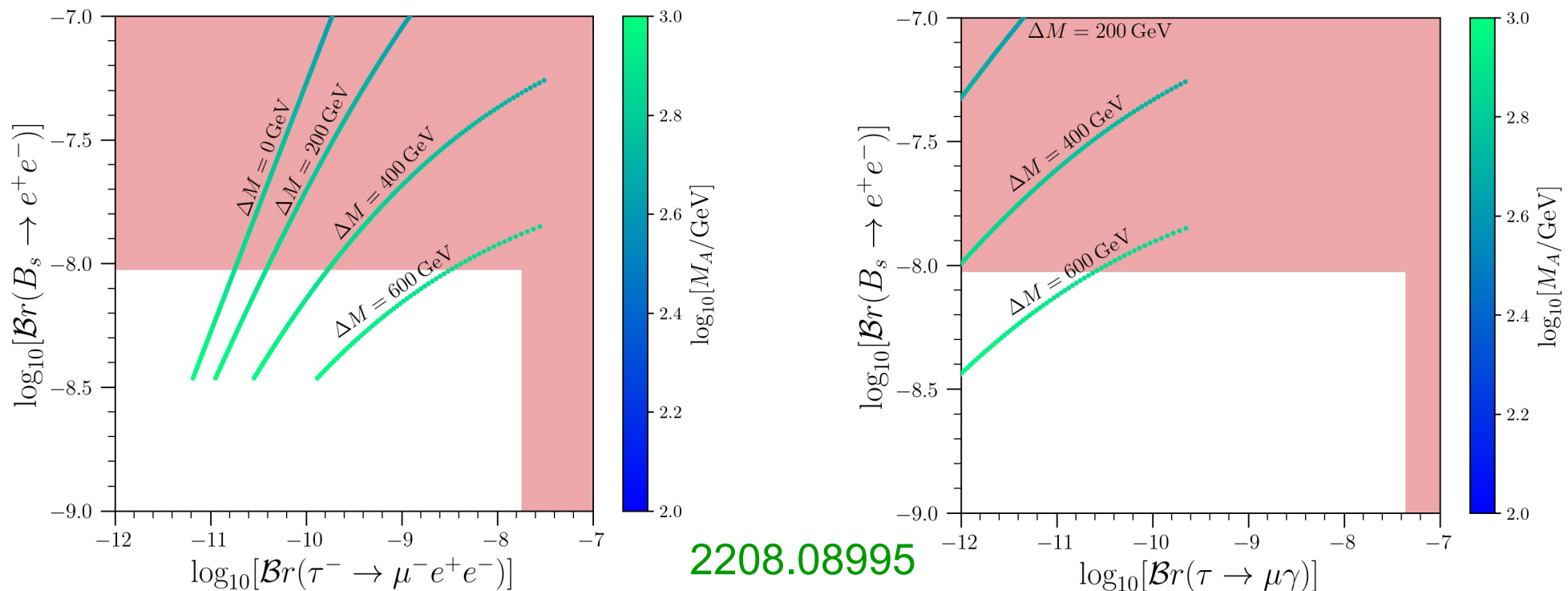
*Babar*  
[hep-ex/0908.2381]

*Belle*  
[hep-ex/1001.3221]

# Generating the NP couplings

## Phenomenological correlations

$$\Delta M = M_A - M_H$$



Since  $y_{\mu\mu} \ll y_{ee}$  we can obey the known results for

$$\bar{\mathcal{B}}r(B_s \rightarrow \mu^+\mu^-)$$

within  $2\sigma$

# Conclusions

- Scalars and pseudoscalar particles can enhance dramatically the branching fraction  $Br(B_s \rightarrow e^+ e^-)$ .
- One of the conditions for the enhancement is that the New Physics couplings should not be proportional to  $m_e$ .
- The type III THDM allows to fulfill this criteria while satisfying the known phenomenological constraints.
- The required conditions can be accomplished within the Low energy limit of the Pati Salam model.



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# Phenomenological constraints

## Relevant Operators

$$\mathcal{O}_V^{\Delta B=2} = \bar{s}_i \gamma^\mu (1 - \gamma_5) b_i \bar{s}_j \gamma_\mu (1 - \gamma_5) b_j, \quad \mathcal{O}_{LL}^{\Delta B=2} = \bar{s}_i (1 - \gamma_5) b_i \bar{s}_j (1 - \gamma_5) b_j$$

$$\mathcal{O}_{RR}^{\Delta B=2} = \bar{s}_i (1 + \gamma_5) b_i \bar{s}_j (1 + \gamma_5) b_j, \quad \mathcal{O}_{LR}^{\Delta B=2} = \bar{s}_i (1 - \gamma_5) b_i \bar{s}_j (1 + \gamma_5) b_j$$

## Standard Model

$$C_{RR}^{\Delta B=2} = \frac{y_{bs}^2}{4} \left[ \frac{1}{m_H^2} - \frac{1}{m_A^2} \right], \quad C_{RR}^{\Delta B=2} = C_{LL}^{\Delta B=2}, \quad C_{LR}^{\Delta B=2} = \frac{y_{bs}^2}{2} \left[ \frac{1}{m_H^2} + \frac{1}{m_A^2} \right]$$

$$\Delta M_s = 2 |M_{12}^s|$$

$$M_{12}^s = \frac{G_F^2}{12\pi^2} \lambda_t^2 M_W^2 S_0(x_t) \hat{\eta}_B f_{B_s}^2 M_{B_s} B_1 + \frac{1}{2M_{B_s}} \left[ 2C_{RR}^{\Delta B=2} \langle \mathcal{O}_{RR}^{\Delta B=2} \rangle + C_{LR}^{\Delta B=2} \langle \mathcal{O}_{LR}^{\Delta B=2} \rangle \right]$$

# The THDM and $B_s \rightarrow e^+ e^-$

## Non-diagonal mass matrices

$$m^i = Y_1^i \frac{v_1}{\sqrt{2}} + Y_2^i \frac{v_2}{\sqrt{2}}$$

## After transforming to the physical basis for fermions

$$-\mathcal{L} \supset \bar{f}_L^i \left[ \frac{M_{\text{diag}}^i}{v} h + \left( -\cot \beta \frac{M_{\text{diag}}^i}{v} + \frac{\Omega^i}{\sqrt{2}s_\beta} \right) (H \pm iA) \right] f_R^i + \text{h.c.}$$

$$\tilde{Y}^\ell = -\cot \beta \frac{M_{\text{diag}}^E}{v} + \frac{\Omega^\ell}{\sqrt{2}s_\beta} = \begin{pmatrix} y_{ee} & \varepsilon & \varepsilon \\ \varepsilon & y_{\mu\mu} & \varepsilon \\ \varepsilon & \varepsilon & y_{\tau\tau} \end{pmatrix}$$

To enhance decays  
into pairs of electrons

$$y_{\mu\mu} \ll y_{ee}$$

$$\tilde{Y}^d = -\cot \beta \frac{M_{\text{diag}}^D}{v} + \frac{\Omega^d}{\sqrt{2}s_\beta} = \begin{pmatrix} y_{dd} & \varepsilon & \varepsilon \\ \varepsilon & y_{ss} & y_{bs}/2 \\ \varepsilon & y_{bs}/2 & y_{bb} \end{pmatrix}$$

To avoid sizeable  
lepton flavour  
violation, and  
bounds from  
kaon-mixing

$$\varepsilon \ll y_{ij}$$

# Generating the NP couplings

For the off-diagonal couplings we have

$$\begin{aligned}\tilde{Y}_{sb}^d &= \frac{1}{4v} (\tan \beta + \cot \beta) (m_\mu s'_{23} c_{23} - m_e s_{23} c'_{23}), \\ \tilde{Y}_{bs}^d &= \frac{1}{4v} (\tan \beta + \cot \beta) (m_\mu s_{23} c'_{23} - m_e s'_{23} c_{23}), \\ \tilde{Y}_{\mu\tau}^\ell &= \frac{3}{4v} (\tan \beta + \cot \beta) (m_s s'_{23} c_{23} - m_d s_{23} c'_{23}), \\ \tilde{Y}_{\tau\mu}^\ell &= \frac{3}{4v} (\tan \beta + \cot \beta) (m_s s_{23} c'_{23} - m_d s'_{23} c_{23}),\end{aligned}$$

where  $s_{ij} \rightarrow 1$   $s'_{ij} \rightarrow 1$  but for  $s_{23}$  and  $s'_{23}$

when

$$s_{23} = s'_{23}$$



$$\tilde{Y}_{sb}^d = \tilde{Y}_{bs}^d = y_{bs}/2$$

$$\tilde{Y}_{\mu\tau}^\ell = \tilde{Y}_{\tau\mu}^\ell = y_{\tau\mu}/2$$