

Rare, radiative and semi-leptonic B decays; Charm and Kaon Physics

Overview and Challenges

C. Agapopoulou (LPNHE), J. Cerasoli (IPHC), N. Mahmoudi (IP2I), O. Sumensari (IJCLab)

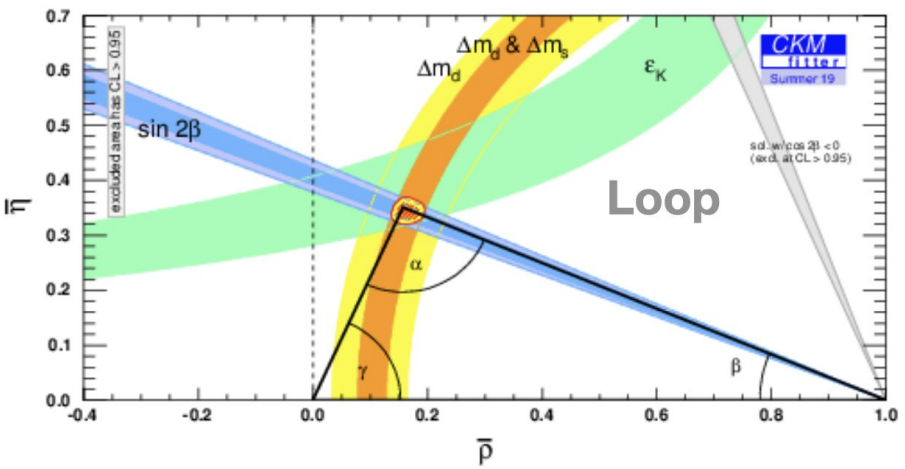
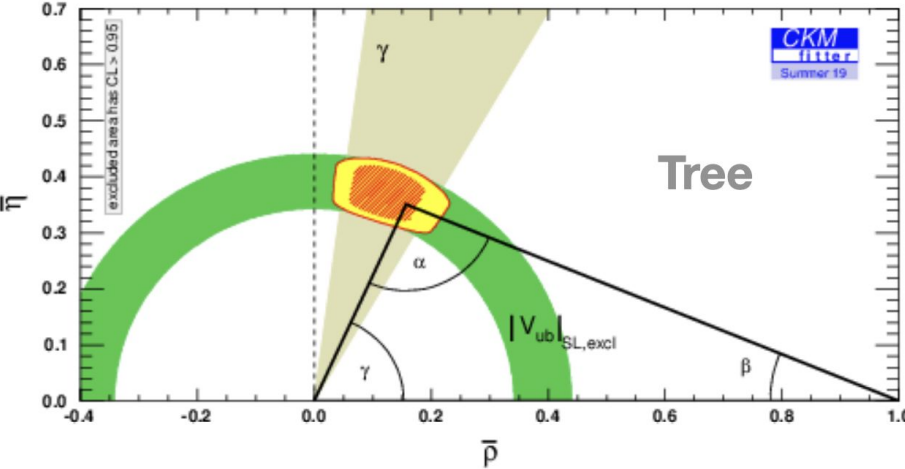
GDR-InF annual meeting, Lyon, 03/11

Brief theory overview / challenges

CKM-ology

$$V_{\text{CKM}} = \begin{pmatrix} d & s & b \\ \bullet & \bullet & \bullet \\ \bullet & \bullet & \bullet \\ \bullet & \bullet & \bullet \end{pmatrix} \begin{matrix} u \\ c \\ t \end{matrix}$$

Fix the CKM matrix entries through *tree-level* decays and over-constrain *loop-induced* ones (progress through th. and exp. precision):

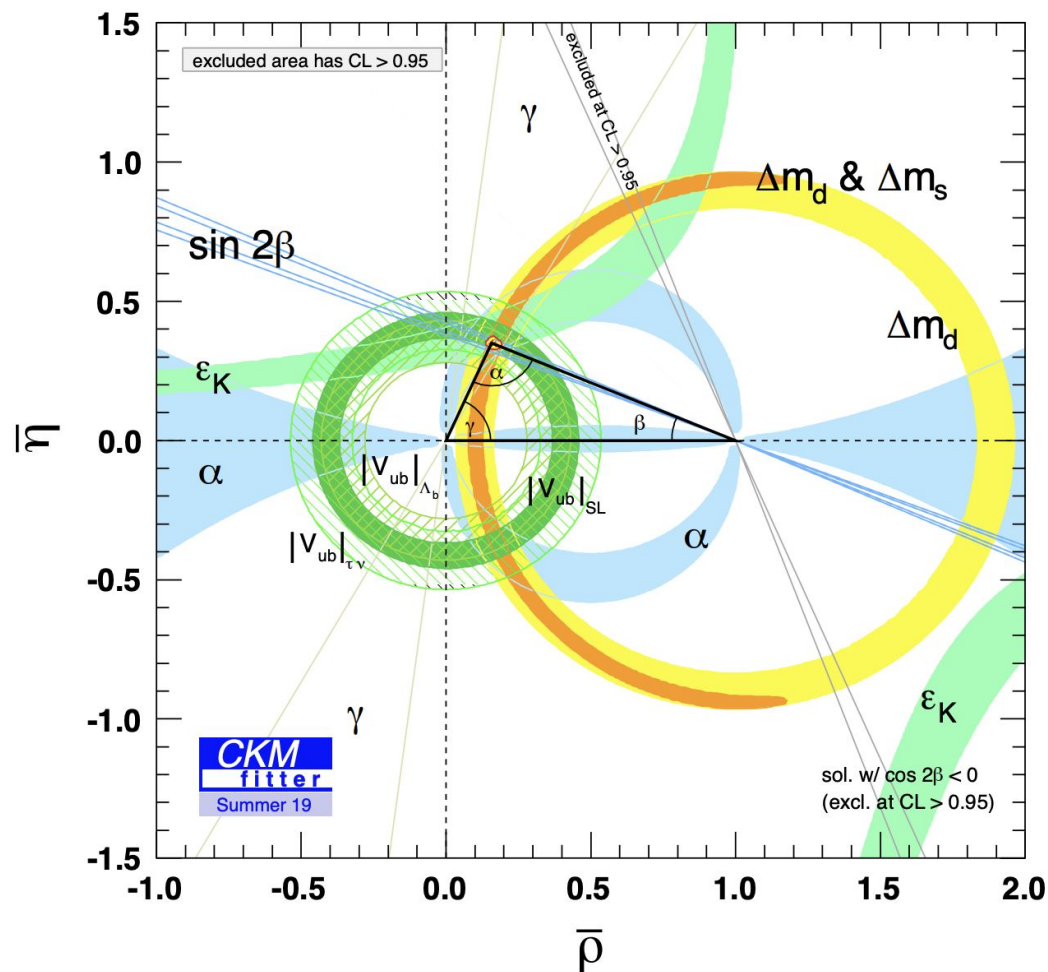


See talk by Vincent Tisserand

CKM-ology

Open questions:

- Exclusive vs. inclusive V_{cb} and V_{ub} .
- Is V_{ud} under control?
- What about V_{us} ($K_{\mu 2}$ vs. K_{l3})?

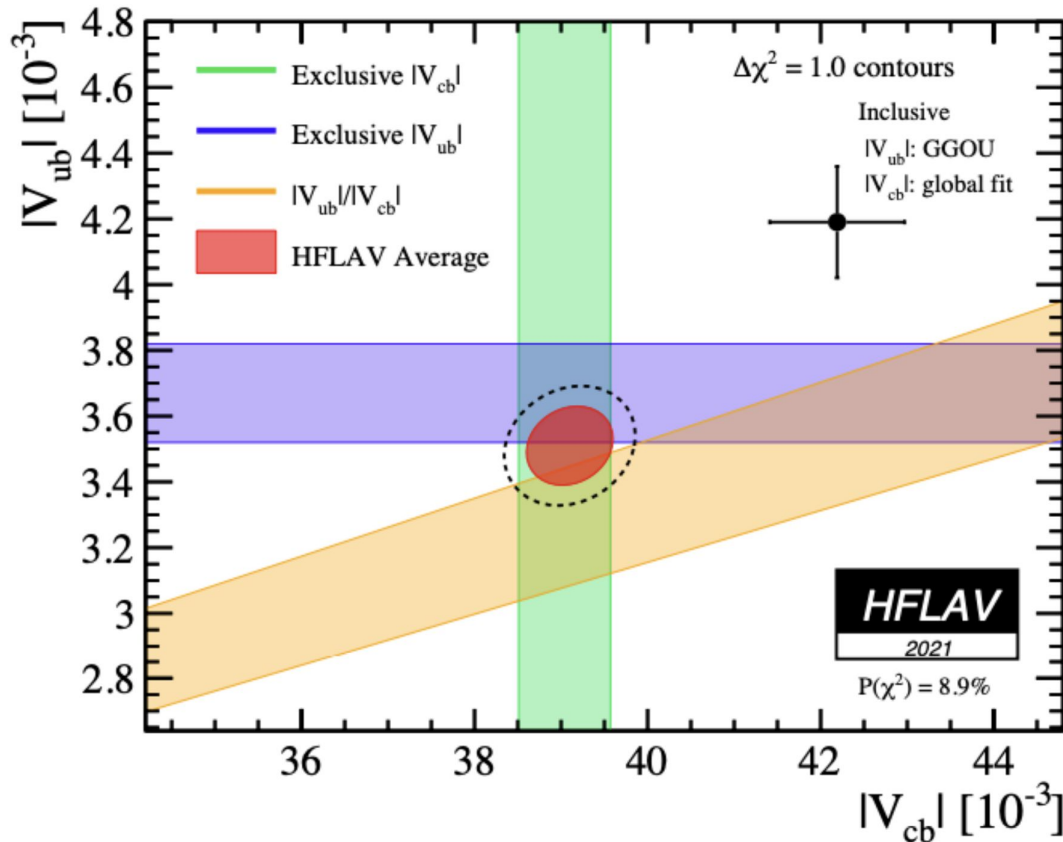


Many questions to be clarified...

Inclusive vs. exclusive: V_{ub} and V_{cb}

Still an open issue...

[2206.07501]



- Long-standing discrepancy...
- V_{cb} plays an **important role** in the predictions of **FCNC**:

$$|V_{tb}V_{ts}|^2 \simeq |V_{cb}|^2 [1 + \mathcal{O}(\lambda^2)]$$



NB. Introduces an *ambiguity* ($\approx 10\%$) in the SM prediction of *FCNC* processes such as $B(B \rightarrow K^{(*)} \nu \nu)$.

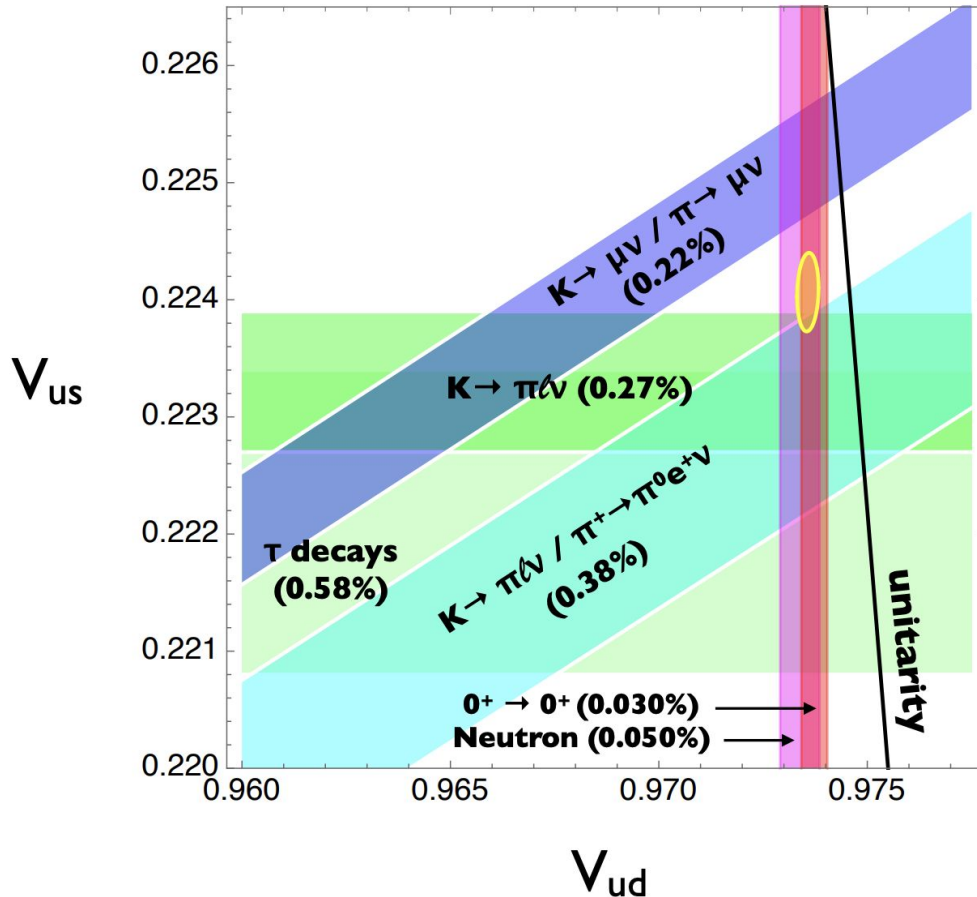
See talk by Ludovico Vittorio

First-row CKM unitarity

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1$$

≈ 0

[2111.05338]



- Significant discrepancies between nuclear β -decays and (semi)leptonic kaon decays:

→ Are nuclear effects under control?

- Mild deviation from unitarity also in $K_{\mu 2}/\pi_{\mu 2}$ vs. $K_{l 3}$.

→ Need to control radiative corrections! LQCD simulations can already account for QED effects in leptonic π and K decays!

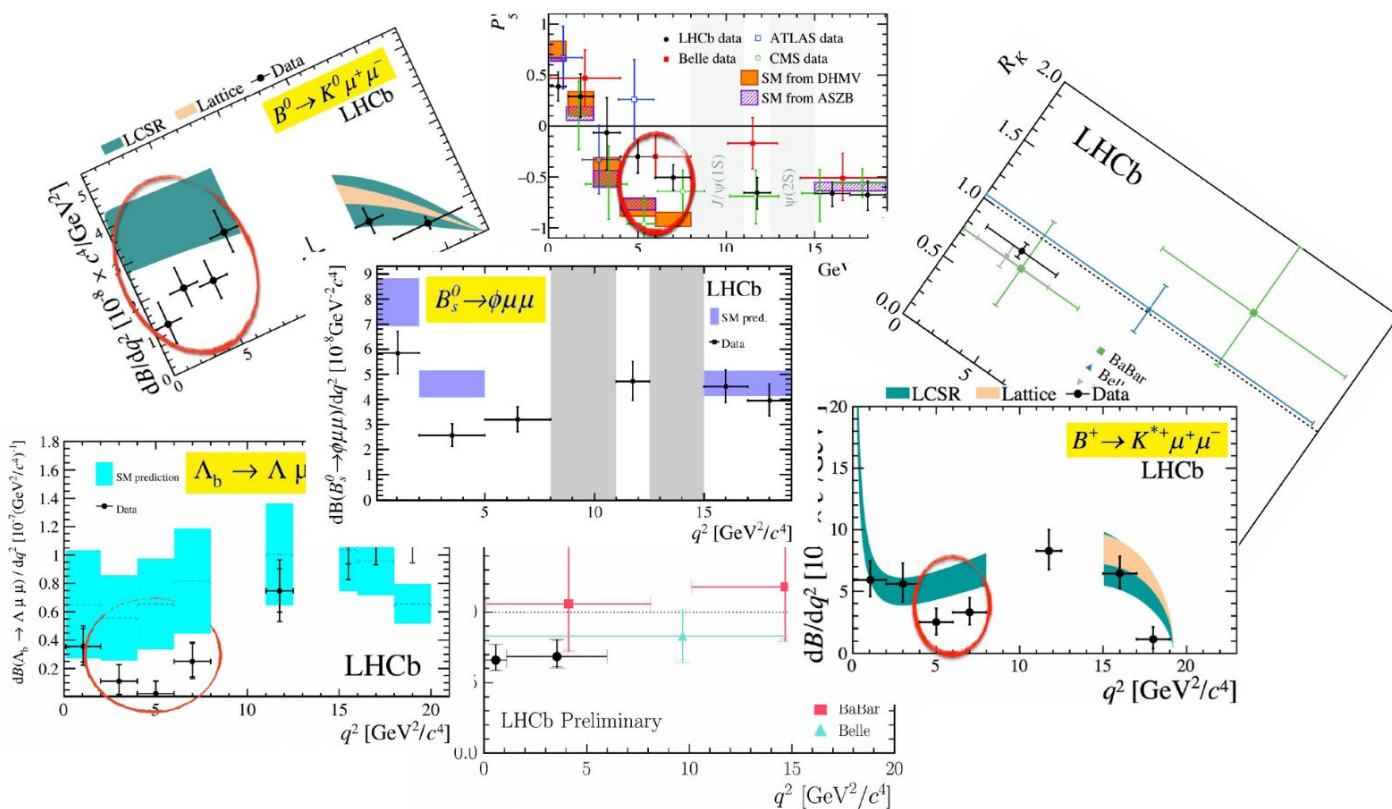
[1711.06537]

More information (exp. and th.) needed to solve this issue

Seeking New Physics with rare B -decays

Impressive effort in studying $b \rightarrow sll$ transitions at LHCb, but also ATLAS, CMS and Belle, with the measurement of a large number of independent branching ratios and angular observables, ratios,...

$B \rightarrow K\mu^+\mu^-$, $B \rightarrow K^+e^+e^-$, $B \rightarrow K^*\mu^+\mu^-$ (F_L , A_{FB} , S_i , P_i), $B_s \rightarrow \phi\mu^+\mu^-$, ...



Several small deviations from the SM predictions...

Theoretical Framework: $b \rightarrow s \ell \bar{\ell}$

Effective Hamiltonian has two parts: $\mathcal{H}_{\text{eff}} = \mathcal{H}_{\text{eff}}^{\text{sl}} + \mathcal{H}_{\text{eff}}^{\text{had}}$

$$\mathcal{H}_{\text{eff}}^{\text{sl}} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \left[\sum_{i=7,9,10,S,P} C_i^{(\prime)} \mathcal{O}_i^{(\prime)} \right]$$



$$\langle M \ell \bar{\ell} | \mathcal{H}_{\text{eff}}^{\text{sl}} | B \rangle \propto \mathcal{A}_V^\mu \bar{u}_\ell \gamma_\mu v_\ell + \mathcal{A}_A^\mu \bar{u}_\ell \gamma_\mu \gamma_5 v_\ell + \mathcal{A}_S \bar{u}_\ell v_\ell + \mathcal{A}_P \bar{u}_\ell \gamma_5 v_\ell$$

local contributions:

$$\mathcal{A}_V^\mu = -\frac{2im_b}{q^2} C_7 \langle M | \bar{s} \sigma^{\mu\nu} q_\nu P_R b | B \rangle + C_9 \langle M | \bar{s} \gamma^\mu P_L b | B \rangle$$

$$\mathcal{A}_A^\mu = C_{10} \langle M | \bar{s} \gamma^\mu P_L b | B \rangle$$

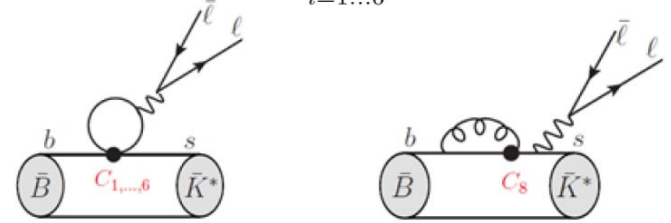
$$\mathcal{A}_{S,P} = C_{S,P} \langle M | \bar{s} P_{R,L} b | B \rangle$$

- 3 form factors for final state $M = K$
- 7 form factors for final state $M = K^*, \phi$

Determined by **Lattice QCD** (high q^2), **Light-Cone Sum Rules** (low q^2) and **combined fit of LCSR + Lattice** (low + high q^2)

Ball et al '04; Khodjamirian et al. '10; HPQCD '13; Altmannshofer et al. '14; Bharucha et al. '15; MILC '15; Horgan et al. '15; Gubernari et al. '18

$$\mathcal{H}_{\text{eff}}^{\text{had}} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \left[\sum_{i=1\dots 6} C_i^{(\prime)} \mathcal{O}_i^{(\prime)} + C_8 \mathcal{O}_8 \right]$$



$$\langle M \ell \bar{\ell} | \mathcal{H}_{\text{eff}}^{\text{had}} | B \rangle \propto \mathcal{N}^\mu \bar{u}_\ell \gamma_\mu v_\ell$$

non-local contributions:

$$\mathcal{H}^\mu = \frac{-16i\pi^2}{q^2} \sum_{i=1,\dots,6,8} C_i \int dx^4 e^{iq \cdot x} \langle M | T \{ j_{\text{em}}^\mu(x), \mathcal{O}_i(0) \} | B \rangle$$

$$j_{\text{em}}^\mu = \sum_q Q_q \bar{q} \gamma^\mu q$$

Calculated for low q^2 at LO in QCD factorization (QCdf)
Beneke et al '01 and '04

higher powers not fully known ("guesstimated")

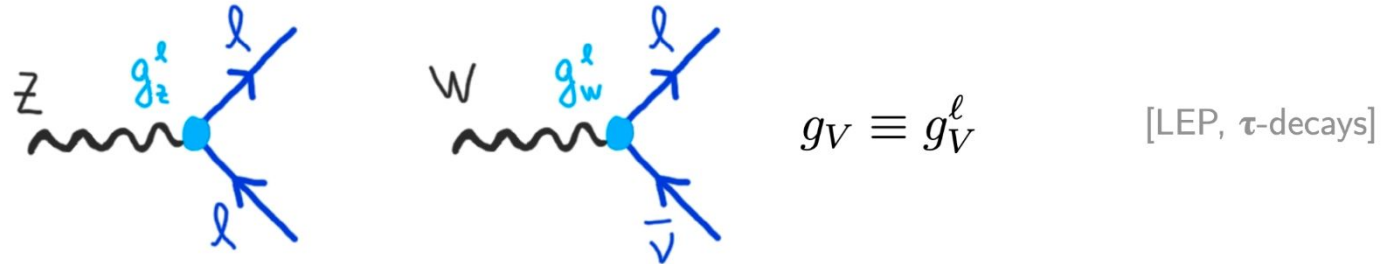
↪ recent progress using **analyticity + experimental data on $b \rightarrow s c \bar{c}$** show these corrections should be small

Bobeth et al. '17, Gubernari, et al. '20 and '22

See talks by Meril Reboud and Aleks Smolkovic

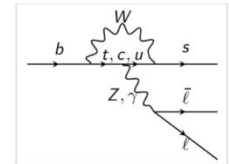
Lepton Flavor Universality Violation?

- Well-tested property of the SM gauge sector, which is broken by Yukawas:

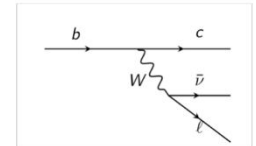


- Several discrepancies have been observed in **b-hadron** decays:

$$R_{K^{(*)}} = \frac{\mathcal{B}(B \rightarrow K^{(*)} \mu\mu)}{\mathcal{B}(B \rightarrow K^{(*)} ee)} \Big|_{q^2 \in [q_{\min}^2, q_{\max}^2]} \quad \& \quad R_{K^{(*)}}^{\text{exp}} < R_{K^{(*)}}^{\text{SM}}$$



$$R_{D^{(*)}} = \frac{\mathcal{B}(B \rightarrow D^{(*)} \tau\bar{\nu})}{\mathcal{B}(B \rightarrow D^{(*)} \ell\bar{\nu})} \Big|_{\ell \in (e, \mu)} \quad \& \quad R_{D^{(*)}}^{\text{exp}} > R_{D^{(*)}}^{\text{SM}}$$

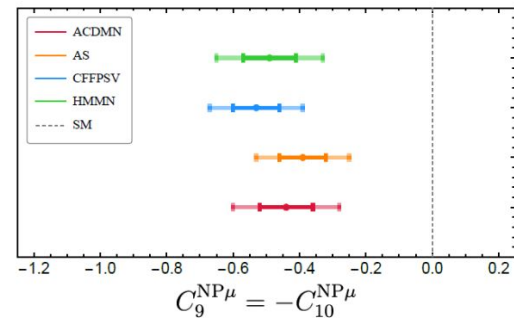
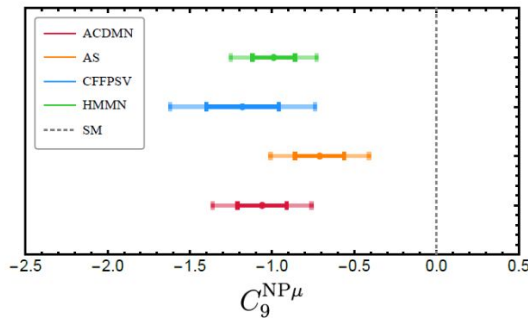


[LHCb, B-factories]

Theoretically clean observables! See talk by Saad Nabeebaccus
Needs clarification (Belle-II and LHCb run-II)

Global $b \rightarrow s\ell\ell$ fits

One dimensional fits:



ACDMN: M. Algueró, B. Capdevila, S. Descotes-Genon, J. Matias, M. Novoa-Brunet

arXiv:2104.08921

AS: W. Altmannshofer, P. Stangl

arXiv:2103.13370

CFFPSV: M. Ciuchini, M. Fedele, E. Franco, A. Paul, L. Silvestrini, M. Valli

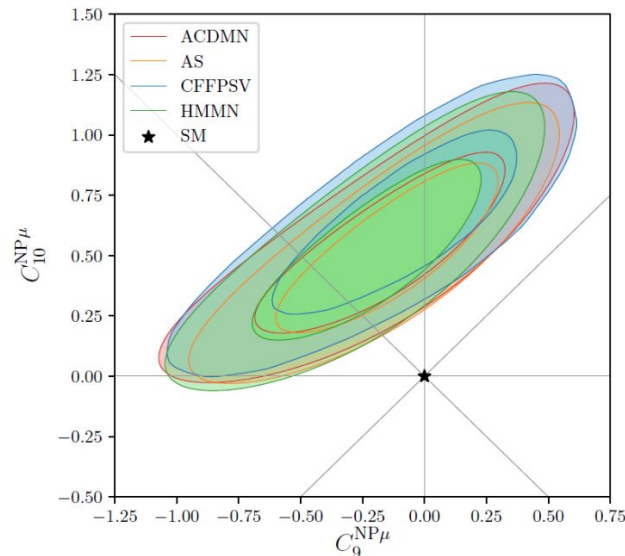
arXiv:2011.01212

HMMN: T. Hurth, F. Mahmoudi, D. Martínez-Santos, S. Neshatpour

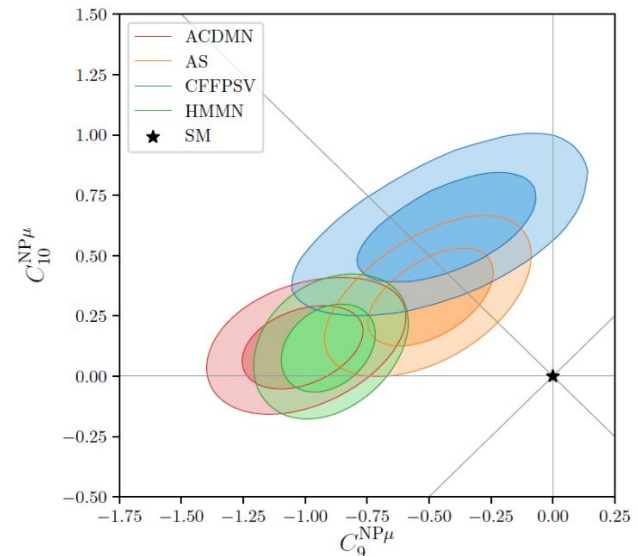
arXiv:2104.10058

Two dimensional fits:

Clean observables



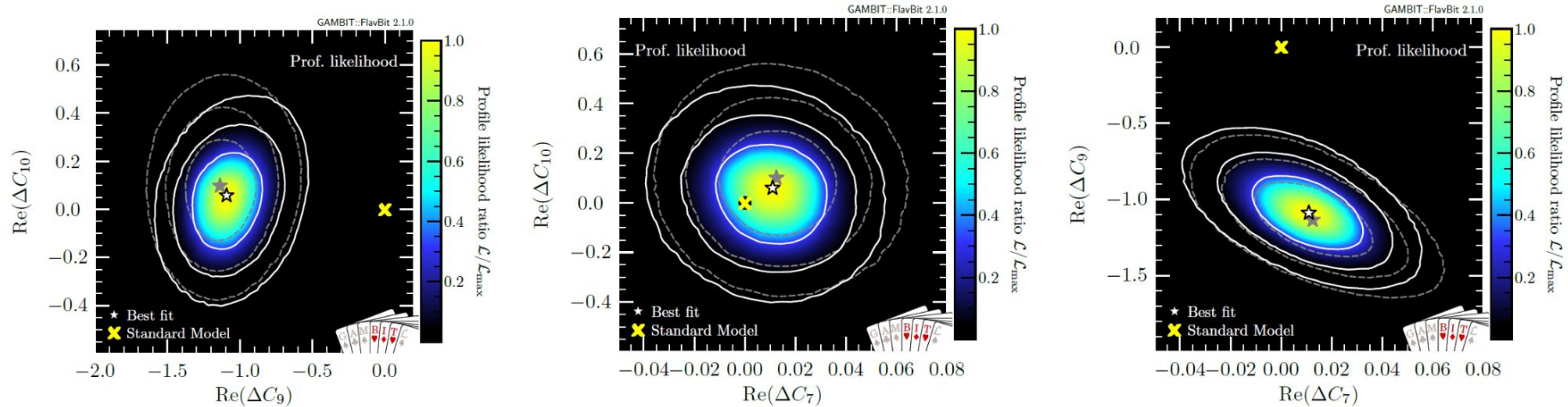
All observables



Global $b \rightarrow s \ell \ell$ fits

2D fits to angular observables and branching ratios (No LFUV ratios):

with the assumption of 10% power corrections



GAMBIT, J. Bhom et al., Eur.Phys.J.C 81 (2021) 12, 1076

- Contour lines: 1, 2 and 3 σ confidence regions.
- SM prediction: yellow cross.
- Grey contours: when the theory covariance is approximated by its value in the SM, across the entire parameter space.

Large negative contributions to C_9 are favoured

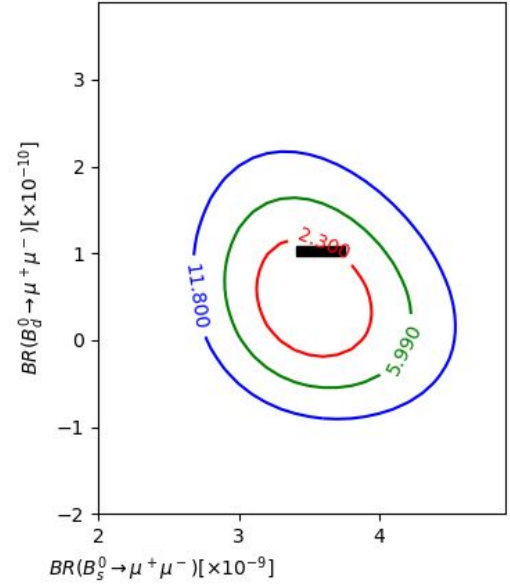
[NEW] $B_s \rightarrow \mu\mu$ and $b \rightarrow s\ell\ell$ fits

SM prediction: $\text{BR}(B_s \rightarrow \mu^+\mu^-) = (3.61 \pm 0.17) \times 10^{-9}$

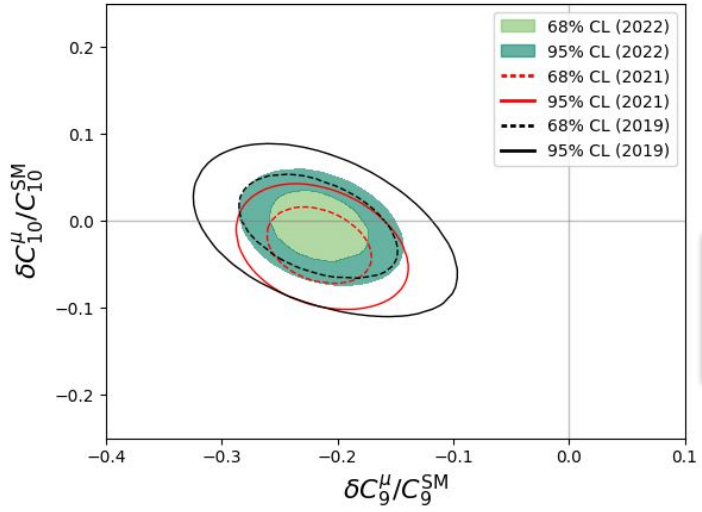
CMS, July 2022 (CMS-PAS-BPH-21-006)

$$\text{BR}(B_s \rightarrow \mu^+\mu^-)^{\text{CMS}} = (3.95^{+0.39+0.27+0.21}_{-0.37-0.22-0.19}) \times 10^{-9}$$

combination using the latest measurements:
 $\text{BR}(B_s \rightarrow \mu^+\mu^-) = 3.52^{+0.32}_{-0.30} \times 10^{-9}$



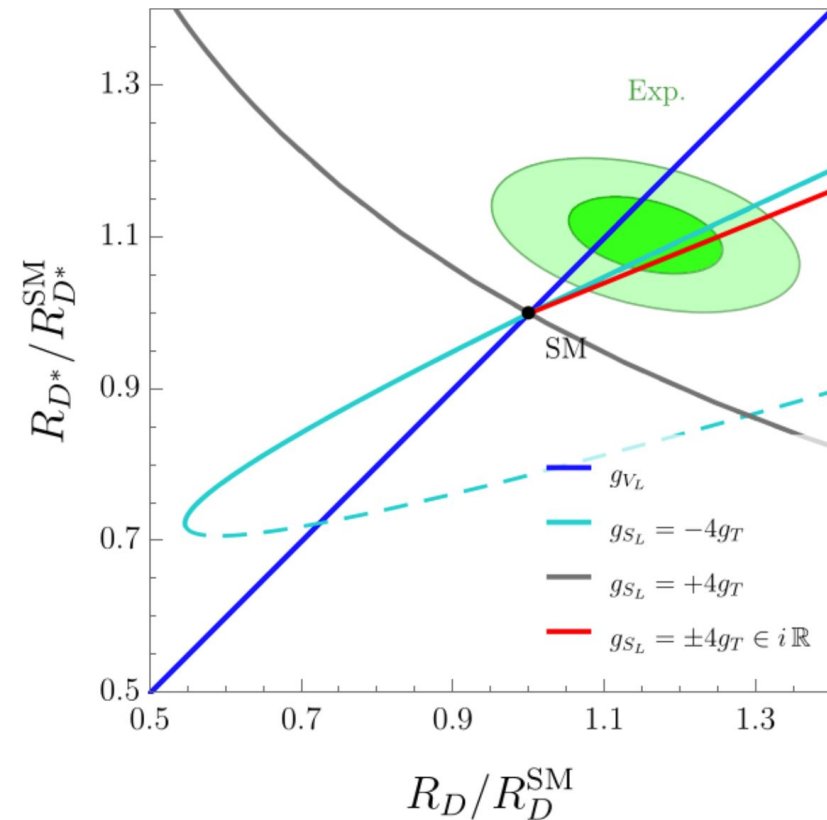
2210.07221



2019: Run I results
2021: (partial) Run II updates, mainly for $B \rightarrow K^*\mu^+\mu^-$, R_K and $B_s \rightarrow \mu^+\mu^-$ (LHCb)
2022: current situation
 (partial) Run II updates, mainly for $B_s \rightarrow \mu^+\mu^-$ (CMS), $R_{K^{*+}}$, $R_{K_S^0}$ and $B_s \rightarrow \phi\mu^+\mu^-$

LFU violation in $b \rightarrow c \tau \nu$

$$\mathcal{L}_{\text{eff}} = -2\sqrt{2}G_F V_{cb} \left[(1 + g_{V_L})(\bar{c}_L \gamma_\mu b_L)(\bar{\ell}_L \gamma_\mu \nu_L) + g_{V_R}(\bar{c}_R \gamma_\mu b_R)(\bar{\ell}_L \gamma_\mu \nu_L) \right. \\ \left. + g_{S_R}(\bar{c}_L b_R)(\bar{\ell}_R \nu_L) + g_{S_L}(\bar{c}_R b_L)(\bar{\ell}_R \nu_L) + g_T(\bar{c}_R \sigma_{\mu\nu} b_L)(\bar{\ell}_R \sigma_{\mu\nu} \nu_L) \right] + \text{h.c.}$$



- Several scenarios can accommodate data:
 \Rightarrow e.g., g_{V_L} and $g_{S_L} = \pm 4g_T$ (at $\mu \approx 1$ TeV).

- More **exp. information** is **needed!**

i) e.g., many angular observables:

$$B \rightarrow D \tau \bar{\nu}$$

$$B \rightarrow D^*(D\pi)\tau \bar{\nu}$$

$$\Lambda_b \rightarrow \Lambda_c(\rightarrow \Lambda\pi)\tau \bar{\nu}$$

ii) Other LFU ratios:

$$R_{D_s^{(*)}}, R_{\eta_c}, R_{J/\psi}, R_{\Lambda_c}, \dots$$

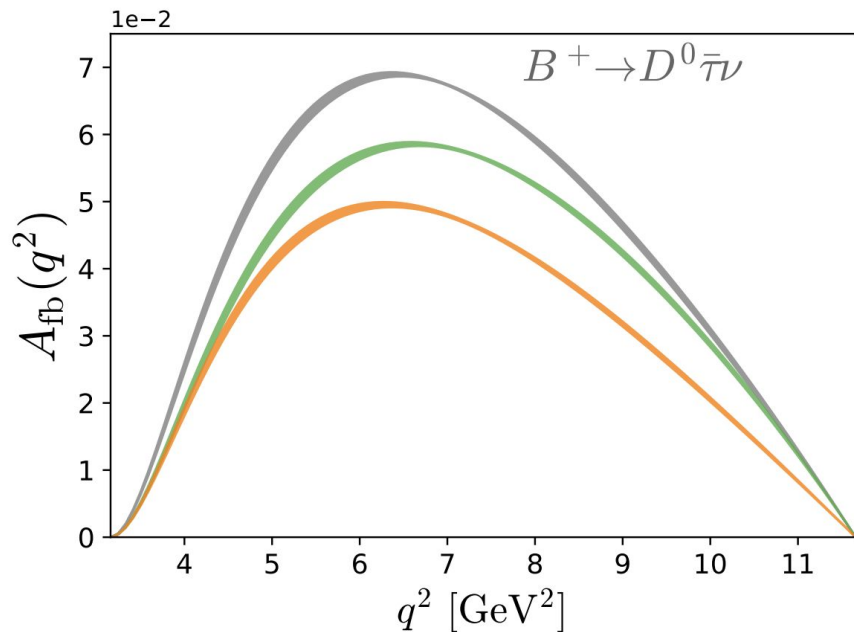
see e.g. [2103.12504]

Angular observables - $b \rightarrow c \tau \bar{\nu}$

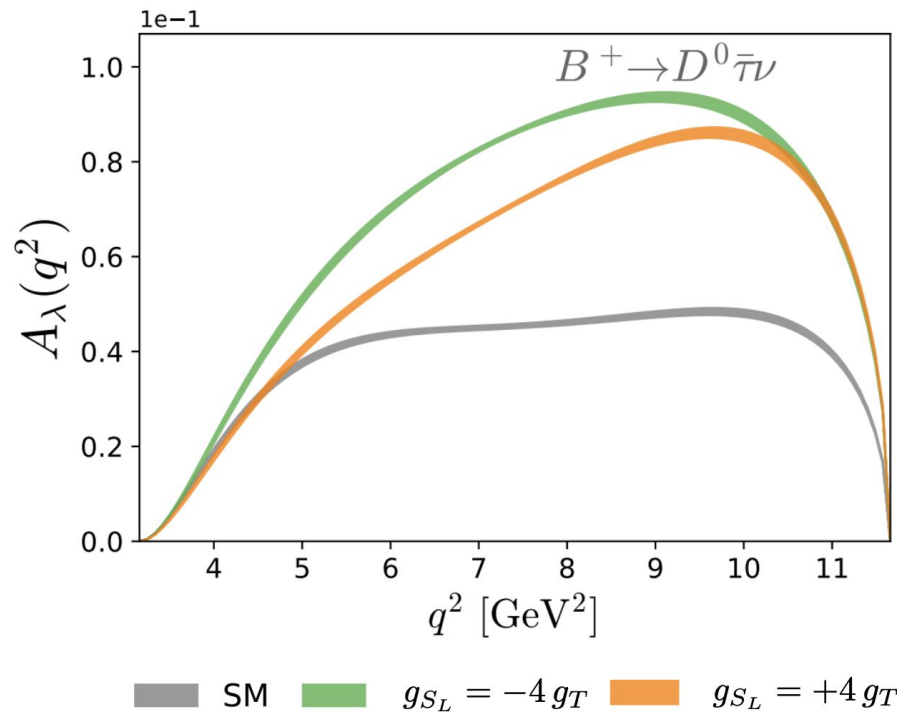
Example: $B \rightarrow D \tau \bar{\nu}$

[2012.09872]

Forward-backward asymmetry



Lepton-polarization asymmetry



Many more opportunities in other modes:

$$B \rightarrow D^*(\rightarrow D\pi)\tau\bar{\nu}$$

$$\Lambda_b \rightarrow \Lambda_c(\rightarrow \Lambda\pi)\tau\bar{\nu}$$

[1602.03030, 1907.02257, 2104.02094...]

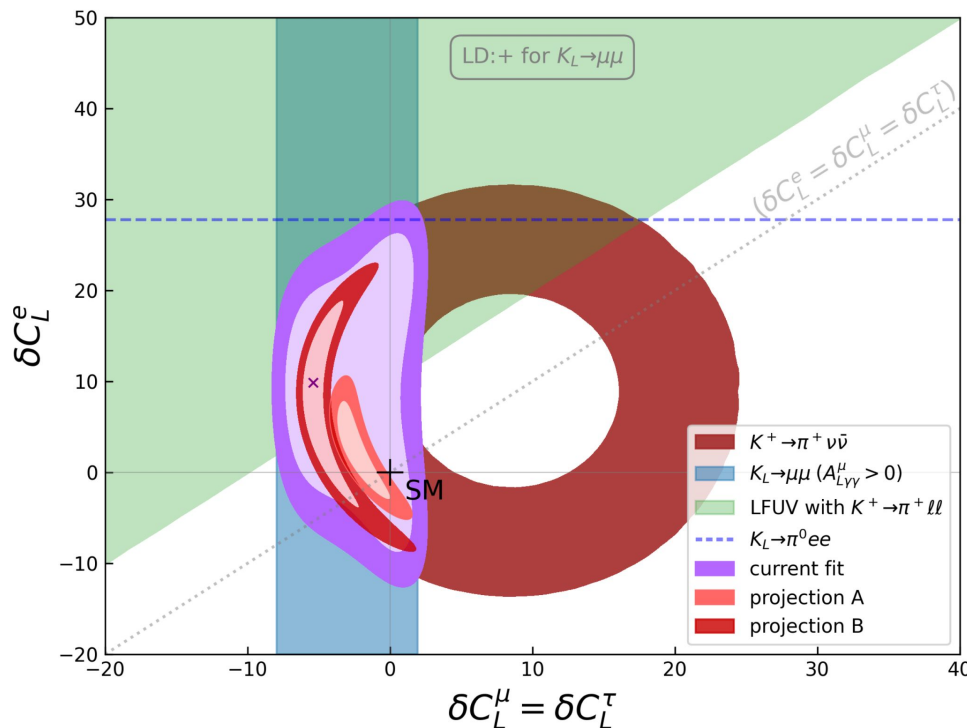
[1907.12554, 2209.13409]

From B -physics to kaons

It is natural to expect that the NP effects in B -meson decays would also impact operators contributing to kaon decays. [1705.10729, 1802.00786, 2005.03734, 2206.14748]...

Global picture:

[2206.14748]



Relevant operators:

$$O_9^\ell = (\bar{s}\gamma_\mu P_L d) (\bar{\ell}\gamma^\mu \ell)$$

$$O_{10}^\ell = (\bar{s}\gamma_\mu P_L d) (\bar{\ell}\gamma^\mu \gamma_5 \ell)$$

$$O_L^\ell = (\bar{s}\gamma_\mu P_L d) (\bar{\nu}_\ell \gamma^\mu (1 - \gamma_5) \nu_\ell)$$

Projection A: Assuming SM as the central values

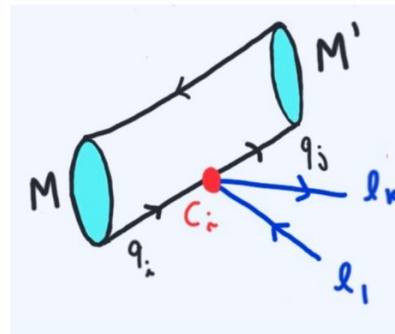
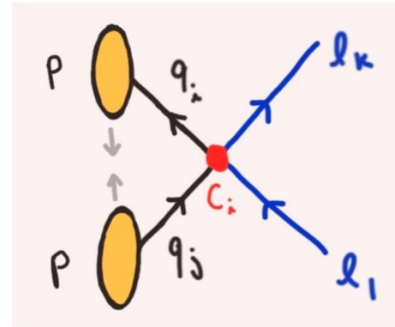
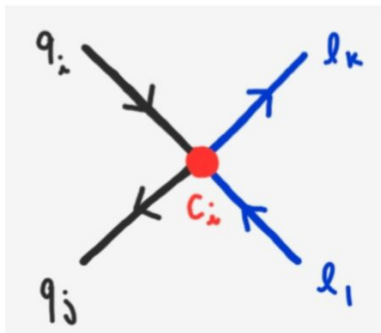
Projection B: Assuming the best-fit values from the current fits as the central values

→ **Effective probe of NP in the muon sector!**

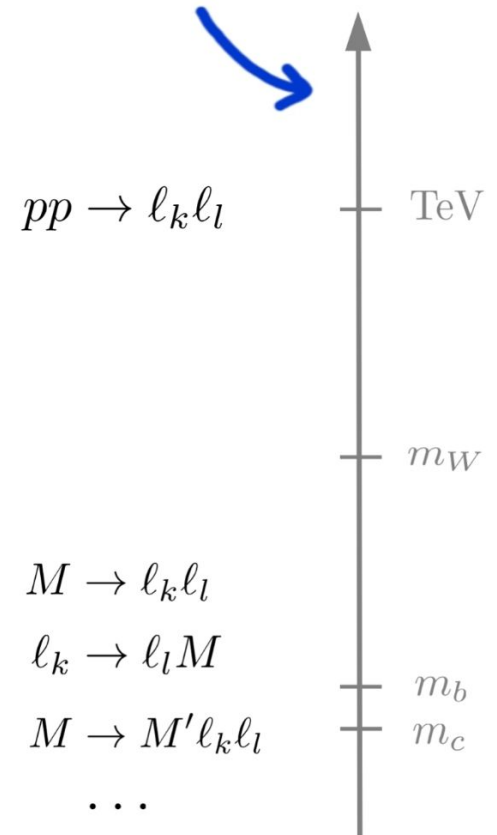
Need to achieve a better accuracy in the theoretical computation of $K_L \rightarrow \mu\mu$

Flavor physics at high- p_T

LHC is also a flavor experiment!



Flavorful New Physics?

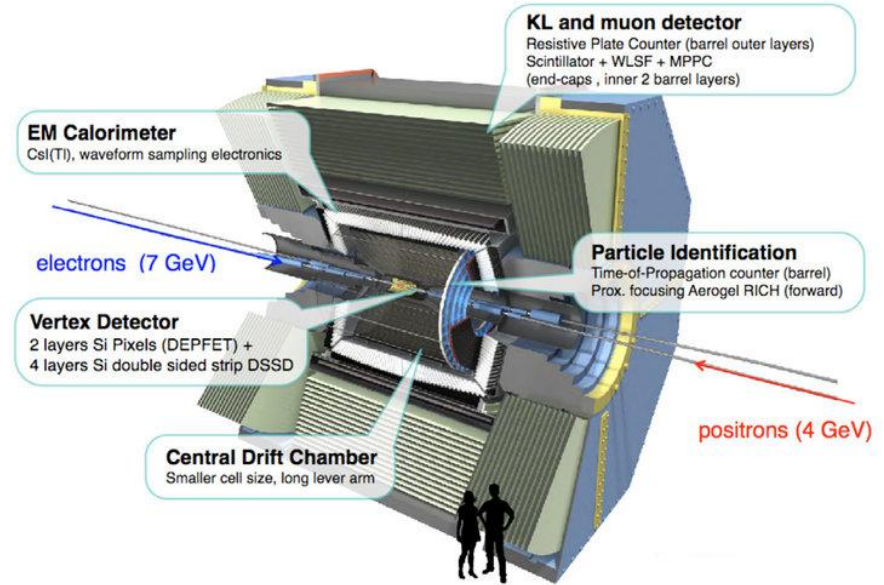
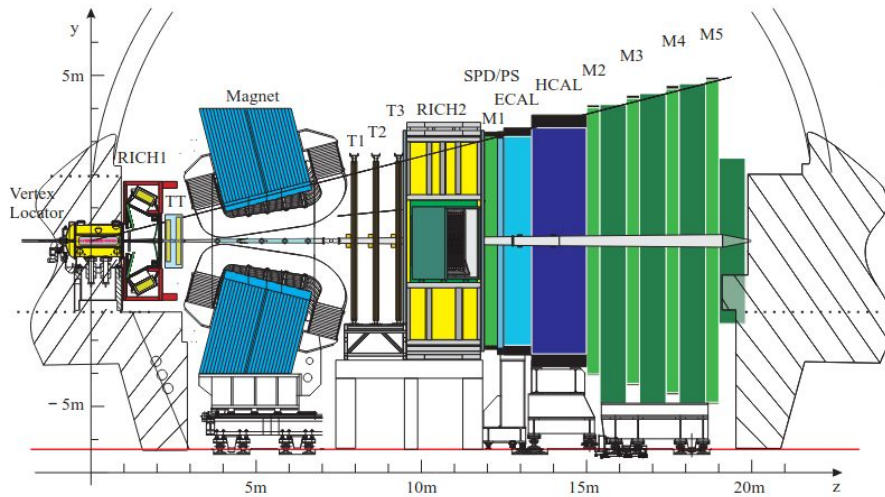


High- p_T searches (CMS and ATLAS) can probe the same operators constrained by flavor-physics experiments (NA62, KOTO, BES-III, LHCb, Belle-II...).

See talk by Felix Wilsch!

Experimental challenges and new results

LHCb vs Belle II



- $\sigma (pp \rightarrow bb) \sim 144 \mu\text{b}$ (13 TeV) in $2 < \eta < 5$
- 3 fb^{-1} at 7 TeV + 6 fb^{-1} at 13 TeV

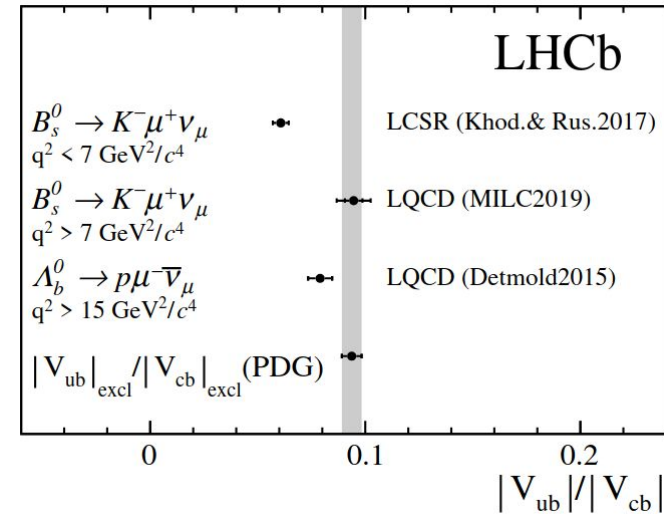
- High vertex resolution (VELO)
- Good PID capabilities (RICH, Calo, Muon)
- Hadronic environment, low trigger efficiency
- Forward detector, no hermiticity

- e^+e^- collisions at 10.58 GeV ($Y(4S)$ resonance)
- $\sim 430 \text{ fb}^{-1}$ collected

- Clean environment, high trigger efficiency
- Hermetic detector, missing energy recovered
- World-record luminosity ($4.7 \cdot 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$)
- Lower production cross-section $\sigma(e^+e^- \rightarrow Y(4S)) \sim 1 \text{ nb}$

Recent results and prospects for V_{ub} and V_{cb}

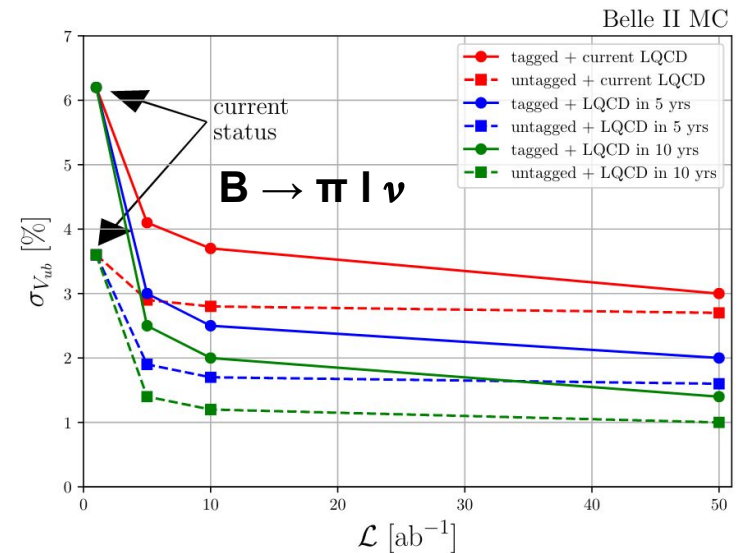
- LHCb measured the ratio $|V_{ub}|/|V_{cb}|$ [[arXiv:2012.05143](#)]
 - Exclusive $B_s^0 \rightarrow K^- \mu^+ \nu$ and $\Lambda_b^0 \rightarrow p \mu^- \nu$
 - Expected **precision of $\lesssim 1\%$** with full LHCb dataset (300 fb⁻¹) [[arXiv:1808.08865](#)]



- ... and $|V_{cb}|$ with exclusive $B_s^0 \rightarrow D^{(*)-} \mu^+ \nu$ [[arXiv:2001.03225](#)]
 - $|V_{cb}|_{\text{CLN}} = (41.4 \pm 0.6 \pm 0.9 \pm 1.2) \cdot 10^{-3}$
 - $|V_{cb}|_{\text{BGL}} = (42.3 \pm 0.8 \pm 0.9 \pm 1.2) \cdot 10^{-3}$

- Recent [measurements](#) also by Belle II:
 - $|V_{ub}|$ from $B \rightarrow \pi e \nu$: $|V_{ub}| = (3.88 \pm 0.45) \times 10^{-3}$
 - $|V_{cb}|$ from $B \rightarrow D^* l \nu$: $|V_{cb}| = (37.9 \pm 2.7) \times 10^{-3}$
 - $|V_{cb}|$ from $B \rightarrow X_c l \nu$: $|V_{cb}| = (41.69 \pm 0.63) \times 10^{-3}$

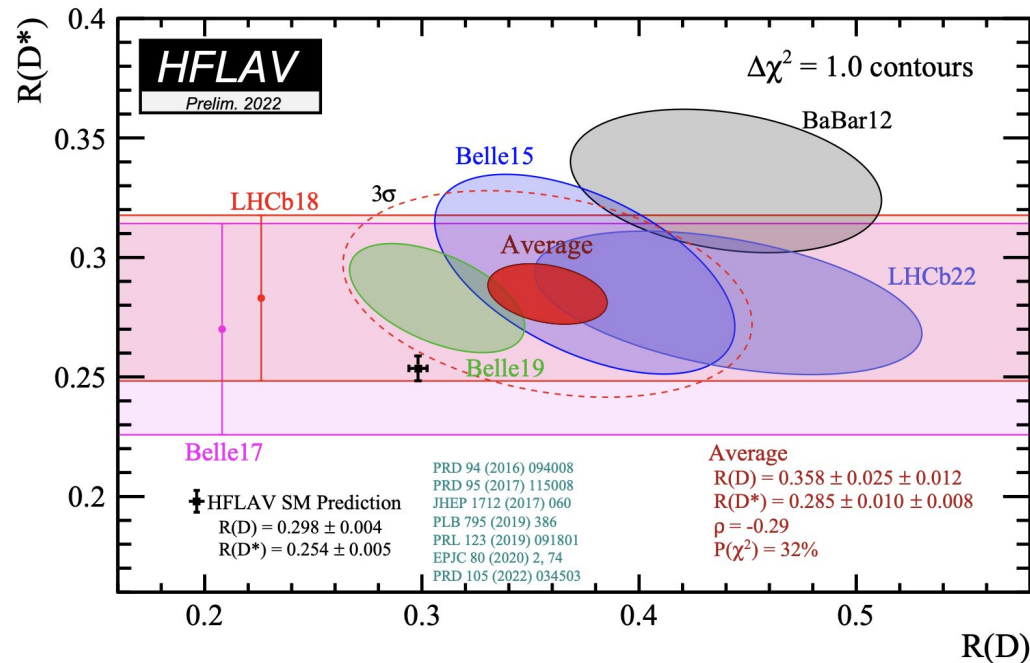
- Expected **precision of $O(1\%)$** with full Belle II dataset (50 ab⁻¹)



[[arXiv:1808.10567](#)]

R(D) and R(D*) measurement at LHCb

- First R(D) and R(D*) combined measurement at a hadronic machine (3 fb^{-1})
- Main challenges:
 - Missing energy from neutrinos, no narrow peak \rightarrow three-dimensional fit in E_μ , m_{missing}^2 , q^2
 - Background from partially reconstructed and misidentified B decays
 - Generation and validation of simulated samples
- **1.9 (3.2) σ agreement** between this measurement (new average) and SM prediction



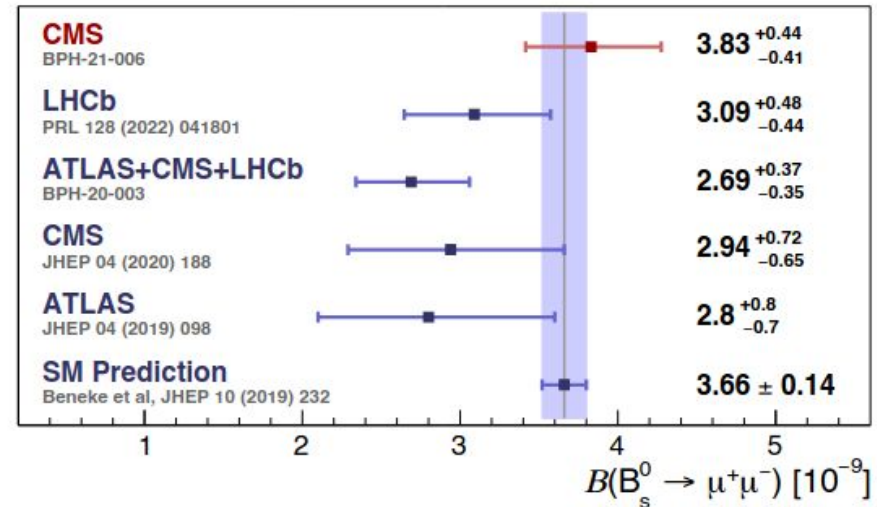
- Run 2 measurement ongoing in this and other channels
- **See talk by Gaya Benane!**

$B^0_{(s)} \rightarrow l^+ l^- (\gamma)$

- Recent updates from LHCb and CMS on

$$B^0_{(s)} \rightarrow \mu^+ \mu^- (\gamma)$$

- See talk by Camille Normand!**



- Upper limits on $B^0_{(s)} \rightarrow e^+ e^-$ and $B^0_{(s)} \rightarrow \tau^+ \tau^-$ provided by LHCb

$$\bar{B}(B^0 \rightarrow e^- e^+) < 3.0 \cdot 10^{-9} \text{ at 95\% CL,}$$

$$\bar{B}(B^0_s \rightarrow e^- e^+) < 11.2 \cdot 10^{-9} \text{ at 95\% CL.}$$

[\[arXiv:2003.03999\]](https://arxiv.org/abs/2003.03999)

$$\bar{B}(B^0 \rightarrow \tau^+ \tau^-) < 2.1 \cdot 10^{-3} \text{ at 95\% CL,}$$

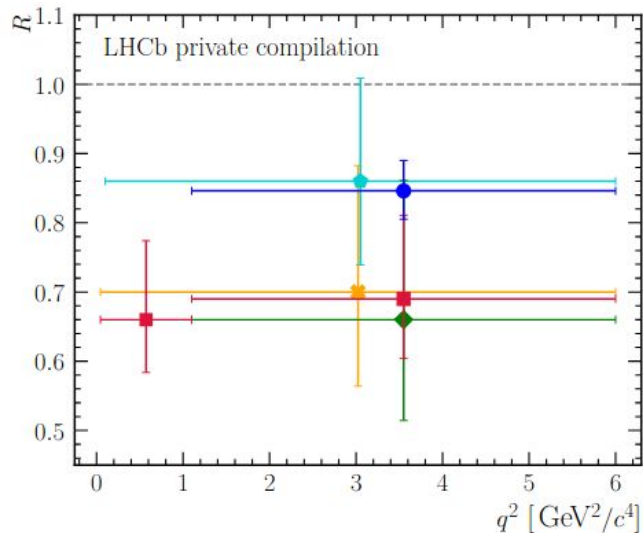
$$\bar{B}(B^0_s \rightarrow \tau^+ \tau^-) < 6.8 \cdot 10^{-3} \text{ at 95\% CL.}$$

[\[arXiv:1703.02508\]](https://arxiv.org/abs/1703.02508)

- See talk by Gilberto Tetlalmatzi-Xolocotzi!**

LFU tests in rare decays

- Several LFU tests in b-hadron decays performed at LHCb
- $R(K)$ shows **3.1 σ discrepancy w.r.t. SM** predictions
- Overall trend observed in LFU ratios, *updated measurements ongoing*



R_K [Nat. Phys. 18, 277–282 (2022)]
 $R_{K_S^0}$ [PRL 128, No. 19]
 $R_{K^{*+}}$ [PRL 128, No. 19]

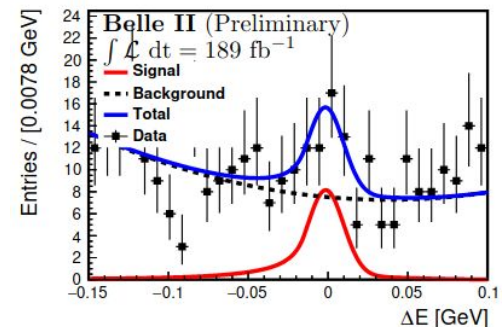
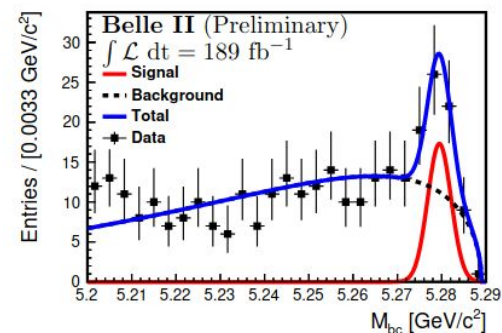
R_{pK} [JHEP 05 (2020) 040]
 $R_{K^{*0}}$ [JHEP 08 (2017) 055]

- First measurement of $B \rightarrow K^* l^+ l^-$ branching ratios at Belle II
- Results in agreement with world average, *updates ongoing*

$$\mathcal{B}(B \rightarrow K^*(892)\mu^+\mu^-) = (1.19 \pm 0.31 \pm_{-0.07}^{+0.08}) \times 10^{-6},$$

$$\mathcal{B}(B \rightarrow K^*(892)e^+e^-) = (1.42 \pm 0.48 \pm 0.09) \times 10^{-6},$$

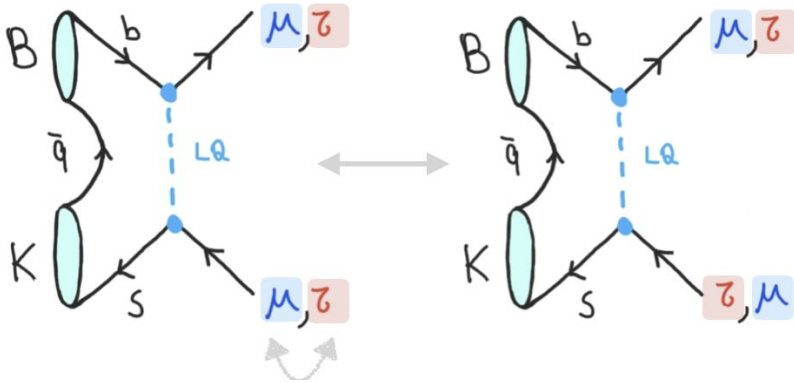
$$\mathcal{B}(B \rightarrow K^*(892)l^+l^-) = (1.25 \pm 0.30 \pm_{-0.07}^{+0.08}) \times 10^{-6},$$



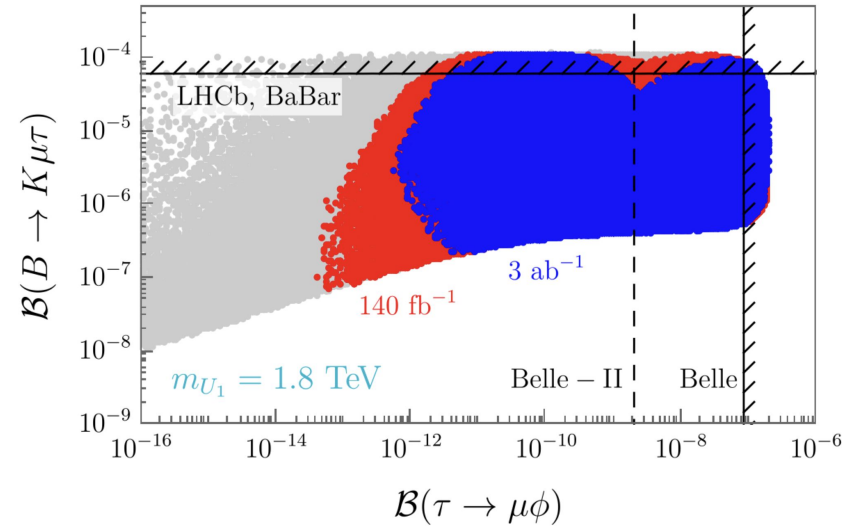
Lepton Flavor Violation

Example: $U_1 \sim (3, 1, 2/3)$

- From **LFUV** to **LFV**:



[1411.0565, 1602.00881...]



[2103.12504]

- New **limits on LFV modes** @ 90 % (95 %) CL:

$$B_s^0 \rightarrow \phi \mu e$$

$$\mathcal{B}(B_s^0 \rightarrow \phi \mu^\pm e^\mp) < 16.0 \times 10^{-9} \quad (19.8 \times 10^{-9})$$

[arXiv:2207.04005]

$$B^0 \rightarrow K^{*0} \mu e$$

$$\mathcal{B}(B^0 \rightarrow K^{*0} \mu^\pm e^\mp) < 10.1 \times 10^{-9} \quad (11.7 \times 10^{-9}),$$

[arXiv:2209.09846]

$$B^0 \rightarrow K^{*0} \tau \mu$$

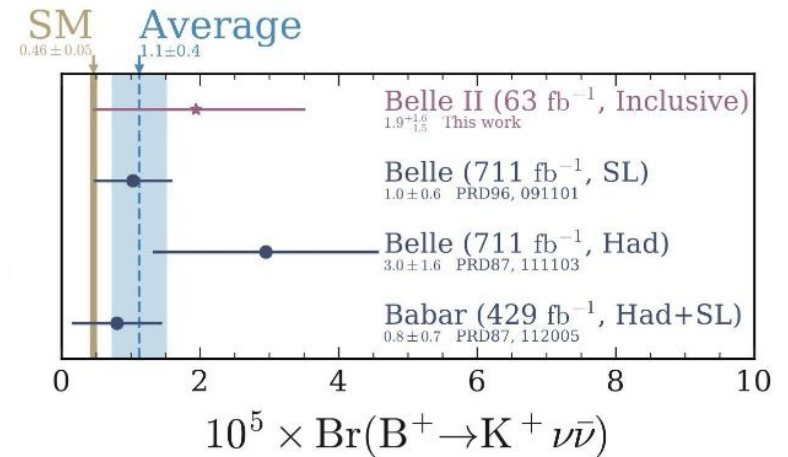
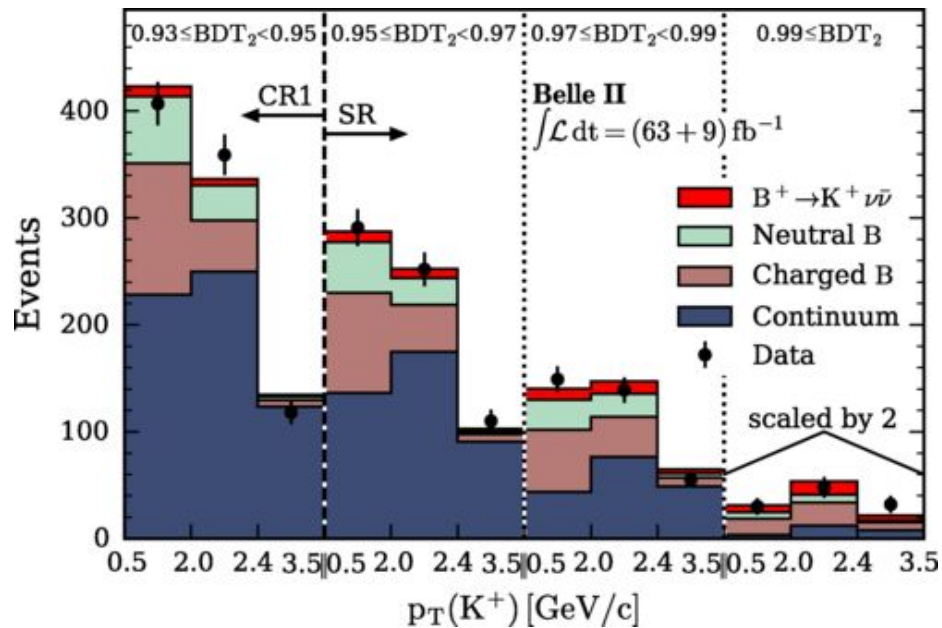
$$\begin{aligned} \mathcal{B}(B^0 \rightarrow K^{*0} \tau^+ \mu^-) &< 1.0 \quad (1.2) \times 10^{-5} \\ \mathcal{B}(B^0 \rightarrow K^{*0} \tau^- \mu^+) &< 8.2 \quad (9.8) \times 10^{-6} \end{aligned}$$

- No sign of LFV yet, we keep searching!

Search for the $B \rightarrow K \nu \nu$ decay

[arXiv:2104.12624]

- Crucial **complementarity to $b \rightarrow s l^+ l^-$** searches
- **Golden channel** for Belle II:
 - Missing energy from neutrinos \rightarrow full reconstruction of the event needed
 - Expected **$\mathcal{O}(10\%)$ uncertainty with 50 ab^{-1}** \rightarrow **Approaching precision regime!**

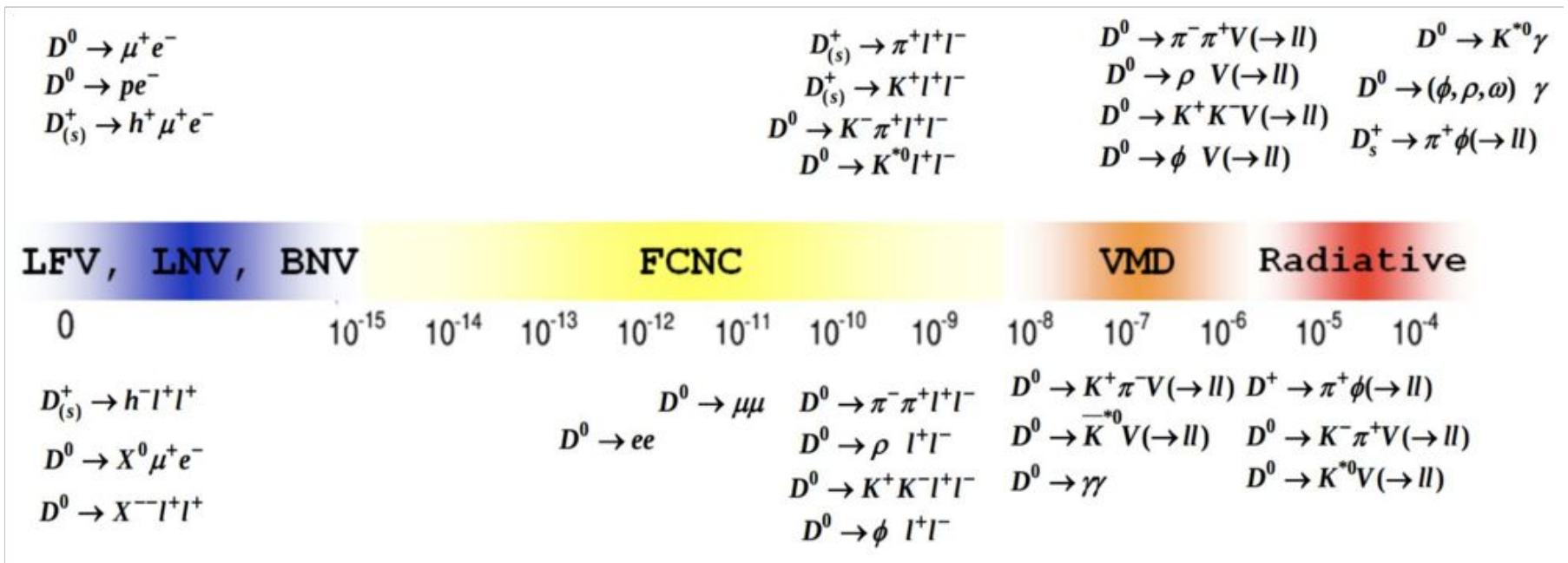


$\mathfrak{B}(B^+ \rightarrow K^+ \nu \nu) < 4.1 \times 10^{-5}$ @ 90 % CL

- Updated measurements ongoing in several channels!
- **See talk by Lucas Martel and Jacopo Cerasoli!**

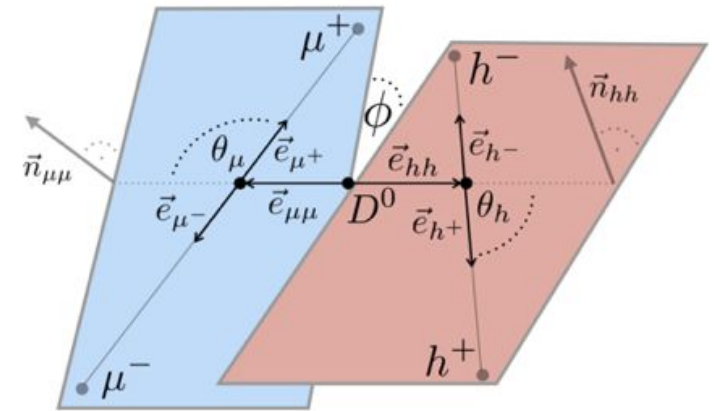
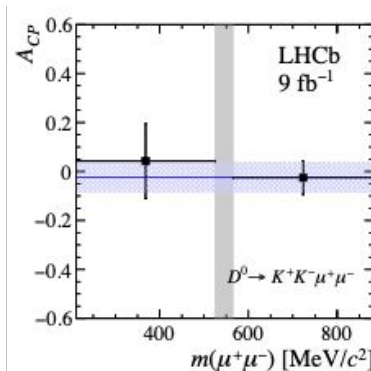
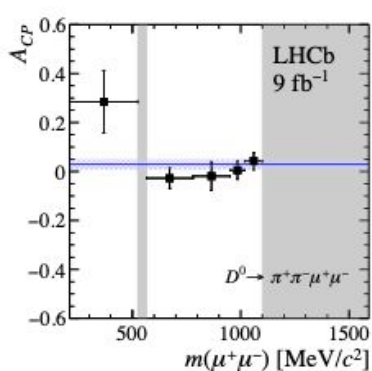
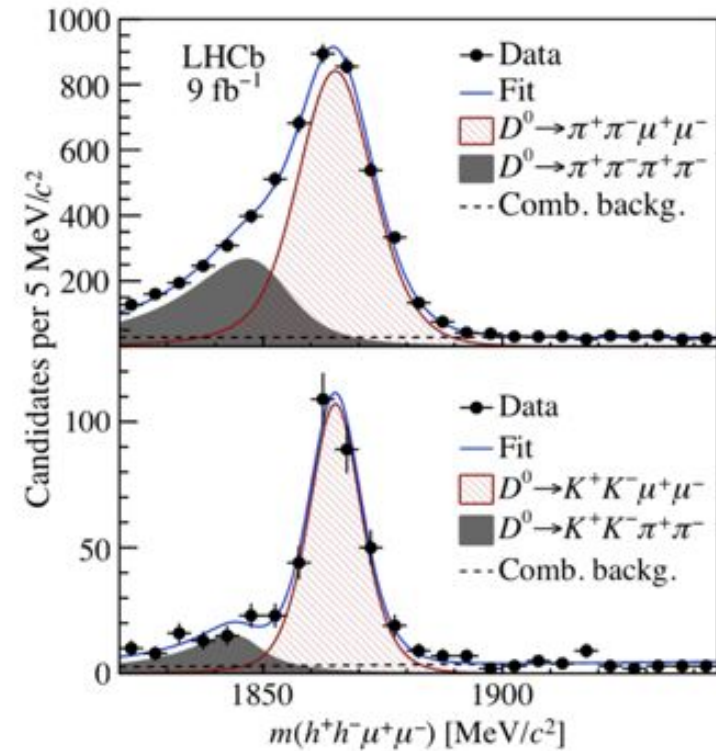
Rare charm decays

- Probing $c \rightarrow u$ type FCNC - **complementarity to B physics!**
- Charm scale not too far from Λ_{QCD} & resonant D contributions
 - Accurate theoretical predictions are challenging
 - Test SM consistency / search for NP through clean observables & null tests
- Very suppressed in the SM due to GIM and CKM suppressions
 - Rich spectrum of channels from forbidden and ultra-rare to less rare / resonant



Rare charm decays

- **Complementarity with $b \rightarrow s l^+ l^-$ searches**
- LHCb has produced world leading measurements in muon modes:
- First observation ($h=\pi, K$) with 2012 data (2 fb^{-1}) [[Phys. Rev. Lett. 119, 181805](#)]
- Measurement of selected angular and CP asymmetries with Run 1 + 2016 data (5 fb^{-1}) [[Phys. Rev. Lett. 121, 091801](#)]
- And first full angular analysis of a rare charm decay \rightarrow search for CP violation! [[Phys.Rev.Lett. 128 \(2022\) 22, 221801](#)]



- **What about electron channels? \rightarrow See talk by Alessandro Scarabotto!**

Summary

- **Rare, radiative and semi-leptonic B decays are rich channels**
- **Charm and Kaon physics offer important complementarity**
- **Rich phenomenology, from MeV to TeV range**
- **Exciting experimental results coming out!**

Thank you!