

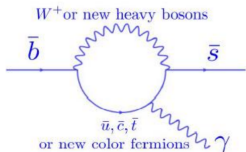
GDR-InF Meeting, Lyon

Measuring time-dependent CP asymmetry of
 $B^0 \rightarrow K_S^0 \pi^+ \pi^- \gamma$ at Belle/Belle II.

Varghese Babu,
on behalf of the IPHC group.

November 2, 2022





- Time-dependent CP -asymmetry of $B^0 \rightarrow K_{res}\gamma \rightarrow K_S^0\pi^+\pi^-\gamma$ is sensitive to photon polarization of quark-level process $b \rightarrow s\gamma$
- The polarization is predominantly left-handed in the Standard Model (SM), but new physics contributions may modify this.
 - Atwood et al., Phys. Rev. Lett. 79, 185
 - E. Kou et al., JHEP 12 (2013) 102 [1305.3173]
 - N. Haba et al., JHEP 03 (2015) 160 [1501.00668]

$$\mathcal{M} \simeq -\frac{4G_F}{\sqrt{2}} V_{ts}^* V_{tb} \left[(C_{7\gamma}^{SM} + C_{7\gamma}^{NP}) \langle \mathcal{O}_{7\gamma} \rangle + C_{7\gamma}'^{NP} \langle \mathcal{O}'_{7\gamma} \rangle \right] \quad (1)$$

$$A_{CP}(\Delta t) = \frac{\Gamma(B_{\text{tag}=B^0}(\Delta t) \rightarrow f_{CP}) - \Gamma(B_{\text{tag}=\bar{B}^0}(\Delta t) \rightarrow f_{CP})}{\Gamma(B_{\text{tag}=B^0}(\Delta t) \rightarrow f_{CP}) + \Gamma(B_{\text{tag}=\bar{B}^0}(\Delta t) \rightarrow f_{CP})} = S \sin(\Delta m \Delta t) + A \cos(\Delta m \Delta t) \quad (2)$$

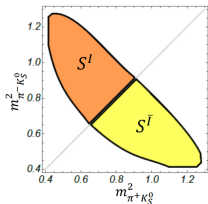
- $A \simeq 0$ for the B_d system
- Previous measurements of S for this mode:
 - **BaBar PRD93 (2015)**: $S_{K_S^0 \pi^+ \pi^- \gamma} = 0.14 \pm 0.25 \pm 0.03$ (full stat : $471 \times 10^6 B\bar{B}$)
 - **Belle PRL101 (2008)**: $S_{K_S^0 \pi^+ \pi^- \gamma} = 0.11 \pm 0.33 \pm 0.07$ ($657 \times 10^6 B\bar{B}$)
- We plan to do a combined measurement with Belle and current Belle II data.
- We are interested in the S_{CP} measurement of the CP -eigenstate $B^0 \rightarrow K_{res} \gamma \rightarrow \rho^0 K_S^0 \gamma \rightarrow K_S^0 \pi^+ \pi^- \gamma$
- Therefore non- CP -eigenstates should be appropriately dealt with by considering a dilution factor

$$D = \frac{S_{K_S^0 \pi^+ \pi^- \gamma}}{S_{K_S^0 \rho^0 \gamma}} \quad (3)$$

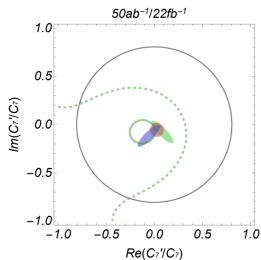
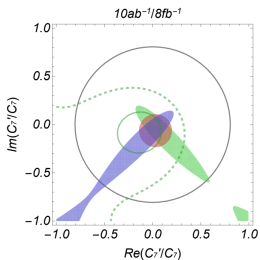
Introduction

- Recent work by *S. Akar, et al.*, proposes new observables by dividing the dataset in the dalitz-plane. The two new observables will provide orthogonal constraints to the real and imaginary parts of C_7'/C_7 in the complex plane.

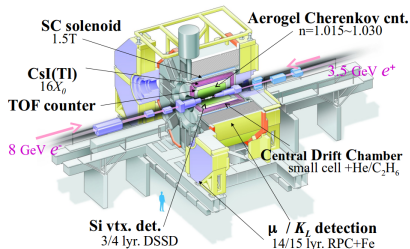
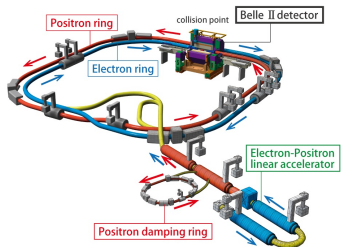
[S. Akar et al., JHEP 09 \(2019\) 034](#)



- New observables :
 $S_{K_S^0 \rho^0 \gamma}^+ = S^I + S^{\bar{I}}$,
 $S_{K_S^0 \rho^0 \gamma}^- = S^I - S^{\bar{I}}$

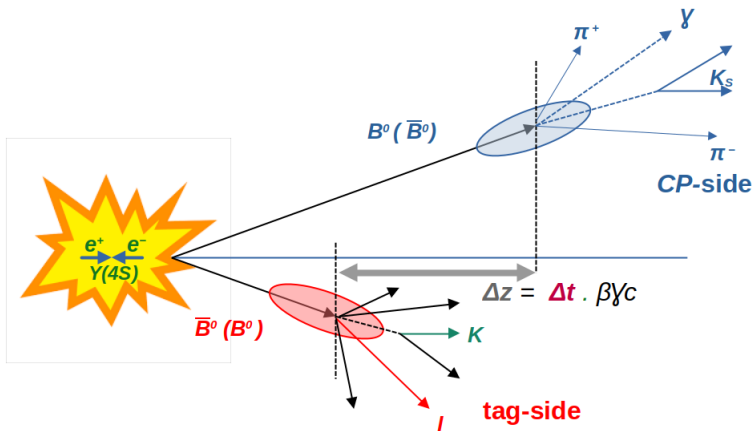


Belle experiment



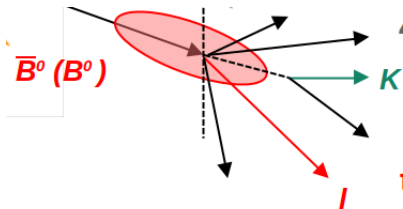
- Experiment with highest instantaneous luminosity in its own time : $2.11 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$
- 711 fb^{-1} of integrated luminosity at the $\Upsilon(4S)$ resonance
- Asymmetric e^+ (3.5 GeV) - e^- (8 GeV) collider, allowing for measurement of proper decay time difference between B -meson pair
- Relatively clean background environment with excellent particle identification capability

Event reconstruction



- After the CP -side B candidate is reconstructed and vertexed, the tracks from the rest of the event are vertexed for the tag-vertex.
- The flavour tagging algorithm is run on the rest of the event.

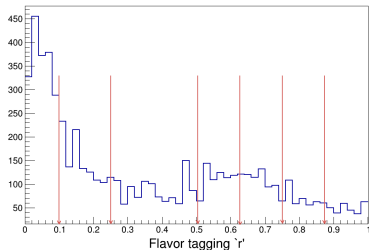
Flavour Tagging



The flavour tagger outputs a tag-flavour and a dilution-factor 'r'.

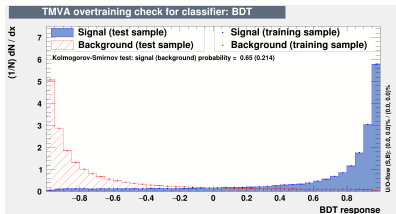
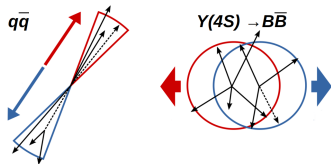
H. Kakuno, et. al., Neutral B flavor tagging for the measurement of mixing-induced CP violation at Belle, NIM A: Vol 533, Issue 3, 2004

- (1) high-momentum leptons from $B^0 \rightarrow X\ell^+\nu$ decays,
- (2) kaons, since the majority of them originate from $B^0 \rightarrow K^+X$ decays through the cascade transition $\bar{b} \rightarrow \bar{c} \rightarrow \bar{s}$,
- (3) intermediate momentum leptons from $\bar{b} \rightarrow \bar{c} \rightarrow \bar{s}\ell^-\bar{\nu}$ decays,
- (4) high momentum pions coming from $B^0 \rightarrow D^{(*)}\pi^+X$ decays,
- (5) slow pions from $B^0 \rightarrow D^{*+}X, D^{*-} \rightarrow \bar{D}^0\pi^-$ decays, and
- (6) $\bar{\Lambda}$ baryons from the cascade decay $\bar{b} \rightarrow \bar{c} \rightarrow \bar{s}$.



r-bin	w	Δw
0	0.5	0.0
1	0.418826	-0.00877001
2	0.319303	0.0103515
3	0.222948	-0.0109253
4	0.163191	-0.0186365
5	0.104085	0.00168037
6	0.0251454	-0.0036441

Event selection - continuum suppression



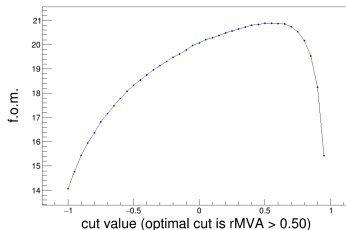
- We build a BDT-classifier based on event-shape variables that discriminate between continuum and resonant events using

- Cosine of the thrust axes of the event,
- Cosine of the B -momentum polar angle and
- Fox-Wolfram moments. G. C. Fox and S. Wolfram, Phys. Rev. Lett. 41, 1581 (1978).

$$H_l = \sum_{i,j} \frac{|p_i||p_j|}{E_{event}^2} P_l(\cos \theta_{i,j}) \quad (4)$$

- The dominant background comes from the non-resonant $e^+e^- \rightarrow q\bar{q}$ $q \in \{u, d, s, c\}$. Has a jet-like event topology as opposed to a more spherically symmetric topology of $\Upsilon(4S) \rightarrow B\bar{B}$ events

Figure-of-merit vs ROOT CS-MVA cut



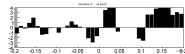
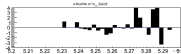
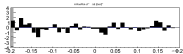
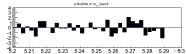
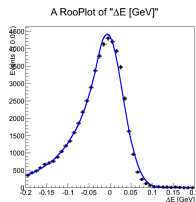
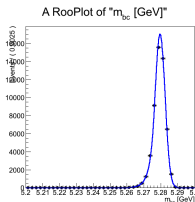
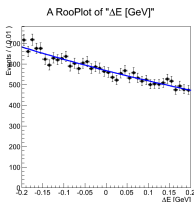
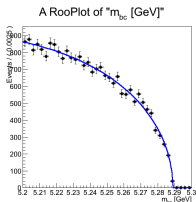
Selection criteria

Selection	Remark
MVA-classifier > 0.5	To suppress continuum events (optimized)
π^0 -veto < 0.2, η -veto < 0.25'	To suppress photon pollution from $\pi^0 \rightarrow \gamma\gamma$ and $\eta \rightarrow \gamma\gamma$ decays
Multivariate standard Belle K_S^0 selection	
e9/e25(γ) > 0.95	Avoid merged π^0 ECL clusters
$\cos(\theta)_\gamma$ [-0.65 - 0.86]	To avoid pollution from low-energy photons from beam background
E_γ [1.5 - 3.5 GeV]	To select ρ^0 resonance
$M_{\pi^+\pi^-}$ [0.6 - 0.9 GeV]	To avoid kaon pollution
kaon-ID(π^+ , π^-) < 0.25	To avoid electron pollution
electron-ID(π^+ , π^-) < 0.25	To choose appropriate K_{res} resonances
$M_{K_S\pi\pi}$ < 1.8 GeV	For both, CP and tag-vertices
Vertex fits converged	
$\chi^2/N.D.F$ < 50	

Single candidate selection: If there are multiple B_{CP} candidates, the one with the best CP-side vertex C.L. is chosen.

Measurement strategy

- We do a 3-D fit of M_{bc} , ΔE and Δt simultaneously in 7 flavour tagging r-bins .
- 5 fit components : signal, cross-feed, continuum-background, rare-MC background and $B\bar{B}$ background.
- 3D p.d.f.'s are modelled as the product of 1-D p.d.f.'s.
- The shape parameters in M_{bc} and ΔE are fixed for all the five fit components



Continuum background:

M_{bc} : Argus
 ΔE : Exponential

Signal :

M_{bc} : Crystal-ball
 ΔE : Crystal-ball

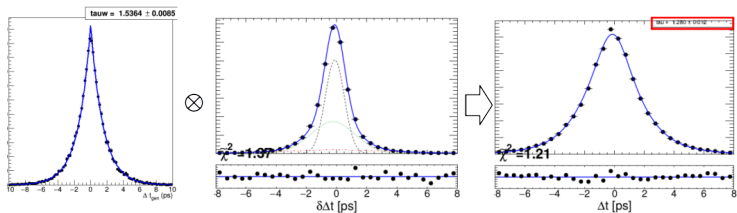
Δt resolution function

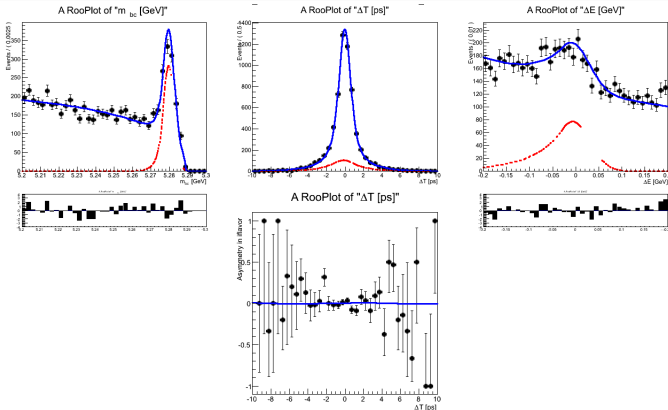
- In Δt , the signal p.d.f. can be written as

$$\mathcal{P}(\Delta t, q = \pm 1) = \frac{e^{-|\Delta t|/\tau_{B^0}}}{4\tau_{B^0}} \{1 - q\Delta w + q(1 - 2w)[S \sin(\Delta m \Delta t) + A \cos(\Delta m \Delta t)]\} \otimes R_{det} \quad (5)$$

- $R_{det}(\cos\theta_B, E_{CMS}, N_{tracks}^{CP}, \sigma_Z^{CP}, \chi^2, CP, N.D.F.^{CP}, N_{tracks}^{tag}, \sigma_Z^{tag}, \chi^2, tag, N.D.F.^{tag})$ is the Δt resolution function that arises from the finite resolution of the CP and tag-side vertices, together with the kinematic approximation that $\Delta z \simeq \Delta t \cdot \beta\gamma c$.
- This has already been calibrated for Belle in the 'tatami' Δt fit-framework.

H. Tajima, et. al., Proper-time resolution function for measurement of time evolution of B mesons at the KEK B-Factory, NIM A: Vol533, Issue 3, 2004





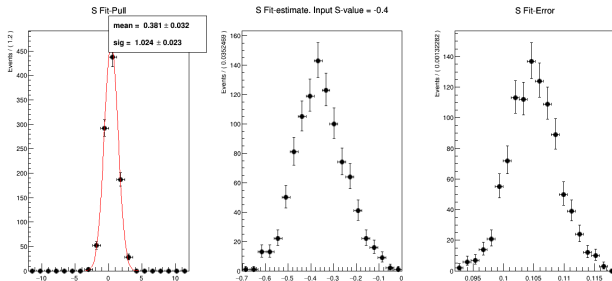
- Full fit on an MC cocktail after selections and single-candidate selection. The cocktail reflects nominal signal and background yields in 1 equivalent Belle dataset.

- Overall $N_{\text{signal}+C.F.}$ and $N_{3\text{-component background}}$ are floated along with S and A
- $$S = 0.04 \pm 0.11 \quad (6)$$

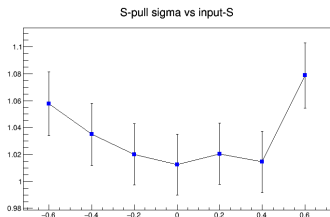
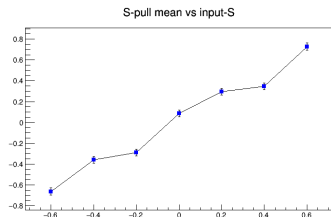
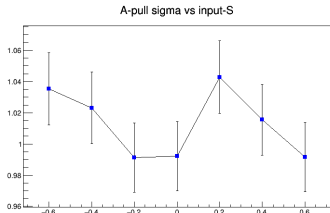
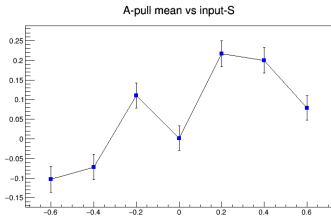
$$A = 0.04 \pm 0.08 \quad (7)$$

Linearity study with ensemble-fits

- We generate 1 million events with $A = 0$ and $S = [-0.6, -0.4, -0.2, 0.0, 0.2, 0.4, 0.6]$ using the minimal CP model PHSP_CP (implemented in Belle software).
- We make 1000 bootstrapped datasets for each input value of S with signal and all background components in the correct proportions.
- Perform ensemble fits to study the relationship between input and estimated values of A and S



Behaviour of A and S pull-distribution mean and width



- Some bias observed in the mean of S pull distribution means. S seems to be overestimated on average by a factor $\sim 14\%$
- The source of this bias is not yet known. Could live with it, by assigning an appropriate correction and associated systematic error(?).

Status and plans

- Plan to start estimating systematic errors from various sources.
- We intend to combine the measurement for Belle and Belle II. Petros has newly joined the group as a Ph.D. student and will start developing the fit strategy for Belle II data.
- Work has already begun on calibrating the Δt resolution function, and the flavour tagging mistag metrics.

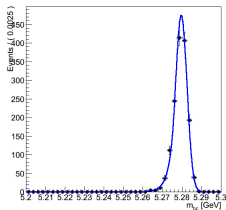
Connected talk (next)

- This physics channel is a good mode to benchmark the performance of the proposed vertex detector upgrade of Belle II. Petros will present his work on this topic.

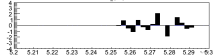
Thank you

Backup : Signal shape

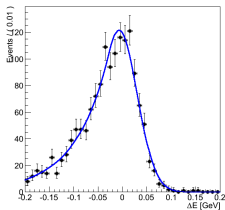
A RooPlot of " m_{bc} [GeV]"



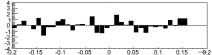
#Histogram: m_bc [GeV]



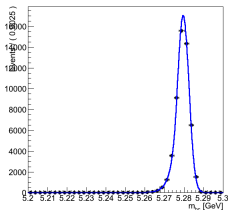
A RooPlot of " ΔE [GeV]"



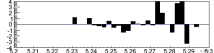
#Histogram: Delta E [GeV]



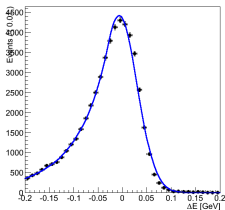
A RooPlot of " m_{bc} [GeV]"



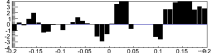
#Histogram: m_bc [GeV]



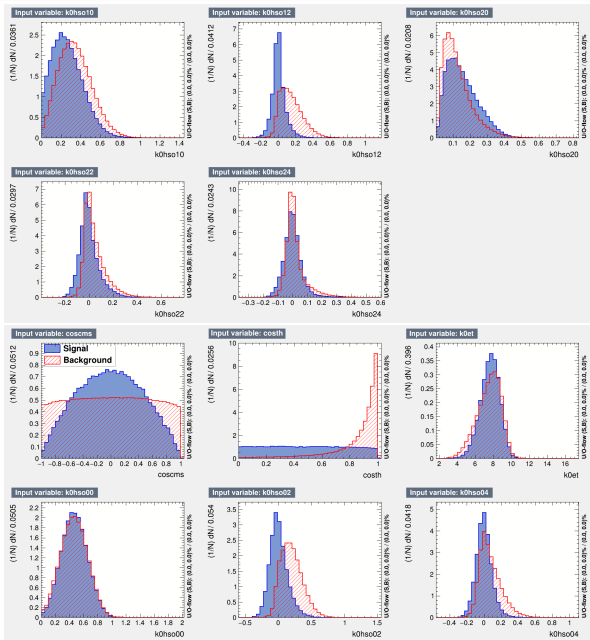
A RooPlot of " ΔE [GeV]"



#Histogram: Delta E [GeV]



Backup : continuum suppression variables



Backup : continuum suppression optimization

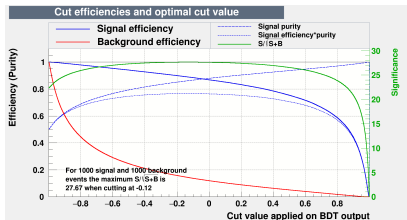
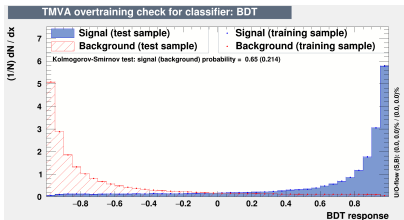
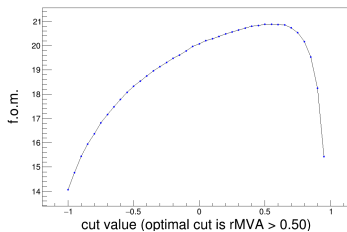
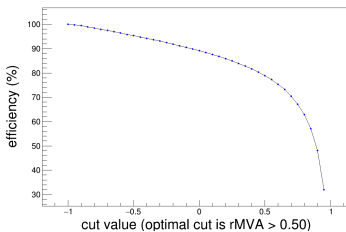


Figure-of-merit vs ROOT CS-MVA cut



Signal efficiency vs ROOT CS-MVA cut



Backup : π^0, η vetoes

Each veto pairs candidate photon (high-energy) with other low-energy photons in the event and calculates the maximum likelihood of it having come from an η or π^0

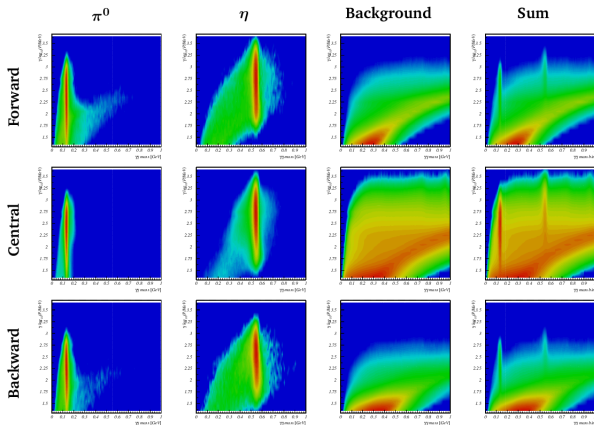
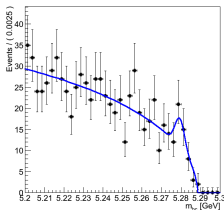


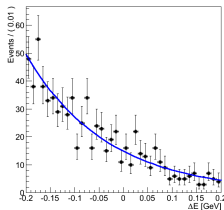
Figure 2: From left to right, MC probability densities in the $\log_{10}(E_{\gamma_2}/\text{MeV})$ versus $m_{\gamma_1\gamma_2}$ plane for true π^0 , η , random combinations and the sum, for three calorimeter zones.

Backup : Background component shapes

A RooPlot of " m_{bc} [GeV]"

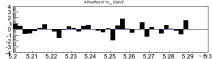


A RooPlot of " ΔE [GeV]"

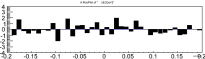


$B\bar{B}$ background:
 M_{bc} : Gaussian + Argus
 ΔE : Exponential

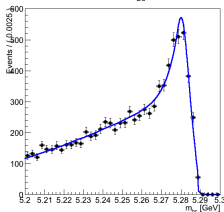
RooPlot of "m_bc [GeV]"



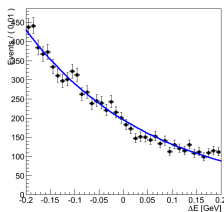
RooPlot of "Delta E [GeV]"



A RooPlot of " m_{bc} [GeV]"

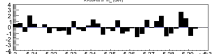


A RooPlot of " ΔE [GeV]"

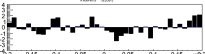


Rare MC background :
 M_{bc} : Crystal-ball + Argus
 ΔE : Exponential

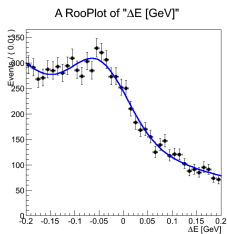
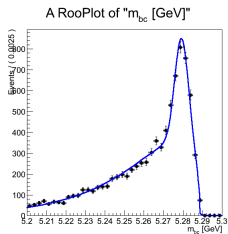
RooPlot of "m_bc [GeV]"



RooPlot of "Delta E [GeV]"



Backup :cross-feed shape



Cross-feed :
 M_{bc} : Crystal-ball + Argus
 ΔE : Exponential

