## Overview of Theory / deliverables for the FCC Feasibility Study

## Fulvio Piccinini

INFN, Sezione di Pavia

November 21, 2022



Joint FCC-France & Italy 2022 Workshop in Lyon, Lyon, 21 – 22 November 2022

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## SM tested up to $\sim 200~\text{GeV}$ with $e^+e^-$ colliders



LEP EWWG, SLD WG, ALEPH, DELPHI, L3, OPAL, Phys. Rept. 427 (2006) 257

- precision  $\mathcal{O}(0.1\%)$  measurements of the processes  $e^+e^- \rightarrow f\bar{f}$
- $\mathcal{O}(1\%)$  for the processes  $e^+e^- \rightarrow WW/ZZ \rightarrow 4$  fermions

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## LEP/SLC legacy at the Z pole



LEP EWWG, SLD WG, ALEPH, DELPHI, L3, OPAL, Phys. Rept. 427 (2006) 257

## 2012 $\rightarrow$ Higgs boson @LHC: mass and width



ATLAS-CONF-2020-005



T.B. Ta, La Thuile 2022

- $\sim 0.1\%$  precision on Higgs mass
- Width (SM  $\sim 4$  MeV)
  - $\Gamma < 14.4 \text{ MeV} (\text{ATLAS 36 fb}^{-1})$
  - $\Gamma < 3.2^{+2.4}_{-1.7}$  MeV (CMS)

## $2012 \rightarrow Higgs$ boson @LHC

Production

- production (and decay) measured in several channels
- for some channel th. uncertainties of same order of exp systematics



Decay

ATLAS Coll., Nature 607 (2022) 7917

### agreement with th. predictions

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## 2022: Higgs @LHC

• coupling strengths in the "k" framework



### · agreement with th. predictions

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## 2022: Higgs @LHC



 $x_F \frac{m_F}{\sqrt{W_V}}$  or  $\sqrt{K_V} \frac{m_V}{\sqrt{W_V}}$ ATLAS Run 2  $\mathbf{\overline{\Phi}} \kappa_c = \kappa_r$ κ. is a free parameter SM prediction 10-2 10-3 a н 10-4  $\kappa_F$  or  $\kappa_V$ 1.4 1.2 0.8 10-1 10<sup>2</sup> 10 1 Particle mass [GeV]

CMS Coll., Nature 607 (2022) 7917

ATLAS Coll., Nature 607 (2022) 7917

## Higgs self-coupling: sensitivity through

double Higgs production (at NLO or LO in associated production)

Borowka et al., arXiv:1604.06447; Grazzini et al., arXiv:1803.02463



• single Higgs production (at NNLO or NLO in associated production) and decay (at NLO or NNLO for  $H \rightarrow \gamma \gamma$ )



EW precision observables at two loops

Degrassi et al., arXiv:1702.01737; Kribs et al., arXiv:1702.07678



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## Present sensitivity to $\mathbf{k}_{\lambda}$

•  $k_{\lambda} = \lambda_{HHH} / \lambda_{HHH}^{SM}$ 





ATLAS, arXiv:2211.01216

- HH driven constraining power
- $-1.4 < k_{\lambda} < 6.1$  @95% CL

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ATLAS, arXiv:2211.01216

- HH driven constraining power
- $-1.4 < k_{\lambda} < 6.1$  @95% CL
- additional constraining power also from EWPO  $M_W$  and  $\sin^2 \vartheta_{eff}^{\ell}$ , in particular in view of future FCC precision

Degrassi et al., arXiv:2102.07651

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- hardly constrained SM Higgs self-coupling
- negative searches of New Physics at high energy

## From low energy...: Muon g - 2 recent result



B. Abi et al., Phys. Rev. Lett. 126 (2021) 14, 141801 [arXiv:2104.03281[hep-ex]]

- Increased experimental precision expected soon
- puzzle of SM prediction based on LQCD

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## LFU @LHC from *B* meson decays

## Tensions in measurements involving the transitions

• 
$$\mathbf{\bar{b}} \to \mathbf{\bar{c}}\ell^+ \nu_{\ell} (\mathbf{R}_D, \mathbf{R}_{D^*})$$

•  $\bar{\mathbf{b}} \to \bar{\mathbf{s}}\ell^+\ell^ (\ell = \mu, e)$ 



#### e.g.

$$R_{K} = \frac{\frac{\mathcal{B}(B^{+} \to K^{+} \mu^{+} \mu^{-})}{\mathcal{B}(B^{+} \to J/\psi(\to \mu^{+} \mu^{-})K^{+} \mu^{+} \mu^{-})}}{\frac{\mathcal{B}(B^{+} \to K^{+} e^{+} e^{-})}{\mathcal{B}(B^{+} \to J/\psi(\to e^{+} e^{-})K^{+} e^{+} e^{-})}}}$$
$$R_{K^{*}} = \dots$$
$$R_{K^{0}_{S}} = \dots$$

G.M. Ciezarek, LHC Seminar, CERN 18/10/2022



R. Aaij et al. (LHCb Coll.), arXiv:2103.11769

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 $\sim 3~\sigma$ Joint FCC-France & Italy 2022

## Exotic hadron spectroscopy



F. Blanc (LHCb Coll.), ICHEP 2022

### Challenge for QCD in the non-perturbative regime

## In addition to unanswered questions, e.g.

- Nature of EWSB
- Neutrino masses
- Higgs and Flavour
- Dark Matter
- Baryon asymmetry in the Universe
- Gravity

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### connections with Higgs in the following picture

#### What is the origin of the vast range of quark and lepton masses in the Standard Model?

- Are there modified interactions to the Higgs boson and known particles?
- Does the Higgs decay into pairs of quarks and leptons with distinct flavours (for example, H → μ<sup>+</sup>τ)?

#### What is dark matter?

- Can the Higgs provide a portal to dark matter or a dark sector?
- Is the Higgs lifetime consistent with the Standard Model?
- Are there new decay modes of the Higgs?

## What is the origin of the early-universe inflation?

- Is the Higgs connected to the mechanism that drives inflation?
- Are there any imprints in cosmological observations?



# Why is the electroweak interaction so much stronger than gravity?

- Are there new particles close to the mass of the Higgs boson?
- Is the Higgs boson elementary or made of other particles?
- Are there anomalies in the interactions of the Higgs with the W and Z?

# Why is there more matter than antimatter in the universe?

- Are there charge-parity violating Higgs decays?
- Are there anomalies in the Higgs self-coupling that would imply a strong firstorder early-universe electroweak phase transition?
- Are there multiple Higgs sectors?

G.P. Salam, L.-T. Wang, G. Zanderighi, Nature 607 (2022) 7917



J. de Blas et al., (Azzi, Farry, Nason, Tricoli, Zeppenfeld Eds.)

CERN-LPCC-2018-03, arXiv:1902.04070

not including the latest CDF  $M_W$  measurement

## Prospects for HL-LHC: Higgs and global analysis



- few % uncertainty for signal strengths
- foreseen th. uncertainty dominant

in the SMEFT approach





J. de Blas et al., (Azzi, Farry, Nason, Tricoli,

Zeppenfeld Eds.) arXiv:1902.04070

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With no clearcut compelling direction for an extension of the SM, a future machine with very broad physics potential is necessary to advance our knowledge

# FCC is an ideal machine allowing to investigate at a never explored level both the intensity and the energy frontier

in the following some considerations on the first stage, FCC-ee

### revisit LEP physics with much larger statistics

- at Z pole (~ 0.1% at LEP1)
- at WW threshold (~ 1% at LEP2)

- explore for the first time at a leptonic collider
  - *ZH* threshold
  - $t\bar{t}$  threshold

## Cross sections and event numbers





G. Bernardi et al., arXiv:2203.06520[hep-ex]

- Z-pole, 3 points:  $5 \times 10^{12} Z$
- *WW* threshold, 2 points: 10<sup>8</sup> *W* pairs
- *HZ* threshold:  $10^6 HZ$ +  $2.5 \times 10^4 WW \rightarrow H$
- $t\bar{t}$  threshold, 3 points:  $10^6 t\bar{t} + 2 \times 10^5 HZ$  $+5 \times 10^4 WW \rightarrow H$

## Higgs@FCCee



P. Azzurri et al., arXiv:2106.15438

### key feature: model-independent measurement of g<sub>HZZ</sub>

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Collider	HL-LHC	$FCC-ee_{240\rightarrow 365}$	FCC-ee	FCC-INT	FCC-INT
			+ HL-LHC		+ HL-LHC
Int. Lumi $(ab^{-1})$	3	5 + 0.2 + 1.5	-	30	-
Years	10	3 + 1 + 4	-	25	-
$g_{\rm HZZ}$ (%)	1.5	0.18	0.17	0.17	0.16
$g_{\rm HWW}$ (%)	1.7	0.44	0.41	0.20	0.19
$g_{\rm Hbb}~(\%)$	5.1	0.69	0.64	0.48	0.48
$g_{\rm Hcc}$ (%)	SM	1.3	1.3	0.96	0.96
$g_{\mathrm{Hgg}}$ (%)	2.5	1.0	0.89	0.52	0.5
$g_{\mathrm{H}\tau\tau}$ (%)	1.9	0.74	0.66	0.49	0.46
$g_{\mathrm{H}\mu\mu}$ (%)	4.4	8.9	3.9	0.43	0.43
$g_{\rm H\gamma\gamma}$ (%)	1.8	3.9	1.3	0.32	0.32
$g_{\mathrm{HZ}\gamma}$ (%)	11.	_	10.	0.71	0.7
$g_{\rm Htt}$ (%)	3.4	-	3.1	1.0	0.95
$g_{\rm HHH}$ (%)	50.	44.	33.	3-4	3-4
$\Gamma_{\rm H}$ (%)	SM	1.1	1.1	0.91	0.91

G. Bernardi et al., arXiv:2203.06520[hep-ex]

Observable	Present	FCC-ee	FCC-ee	Comment and dominant exp. error
	value $\pm$ error	Stat.	Syst.	
$m_{\rm Z} ~({\rm keV})$	$91,186,700\pm 2200$	4	100	From Z lineshape scan; beam energy calibration
$\Gamma_Z$ (keV)	$2,495,200 \pm 2300$	4	25	From Z lineshape scan; beam energy calibration
$R_{\ell}^{Z}$ (×10 <sup>3</sup> )	$20,767 \pm 25$	0.06	0.2 - 1.0	Ratio of hadrons to leptons; acceptance for letpons
$\alpha_{S}(m_{Z}^{2})$ (×10 <sup>4</sup> )	$1,196 \pm 30$	0.1	0.4 - 1.6	From $R_{\ell}^{\mathbb{Z}}$ above
$R_b \ (\times 10^6)$	$216,290 \pm 660$	0.3	< 60	Ratio of $b\overline{b}$ to hadrons; stat. extrapol. from SLD
$\sigma_{\rm had}^0 \ (\times 10^3) \ ({\rm nb})$	$41,541 \pm 37$	0.1	4	Peak hadronic cross section; luminosity measurement
$N_{\nu}$ (×10 <sup>3</sup> )	$2,996 \pm 7$	0.005	1	Z peak cross sections; luminosity measurement
$sin^2 \theta_W^{eff}$ (×10 <sup>6</sup> )	$231,480\pm160$	1.4	1.4	From $A_{FB}^{\mu\mu}$ at Z peak; beam energy calibration
$1/\alpha_{QED}(m_Z^2)$ (×10 <sup>3</sup> )	$128,952\pm14$	3.8	1.2	From $A_{FB}^{\mu\mu}$ off peak
$A_{FB}^{b,0}$ (×10 <sup>4</sup> )	$992 \pm 16$	0.02	1.3	b-quark asymmetry at Z pole; from jet charge
$A_{e} (\times 10^{4})$	$1,498\pm49$	0.07	0.2	from $A_{FB}^{\text{pol},\tau}$ ; systematics from non- $\tau$ backgrounds
$m_W$ (MeV)	$80,350 \pm 15$	0.25	0.3	From WW threshold scan; beam energy calibration
$\Gamma_W$ (MeV)	$2,085 \pm 42$	1.2	0.3	From WW threshold scan; beam energy calibration
$N_{\nu}$ (×10 <sup>3</sup> )	$2,920 \pm 50$	0.8	Small	Ratio of invis. to leptonic in radiative Z returns
$\alpha_S(m_W^2)$ (×10 <sup>4</sup> )	$1,170\pm420$	3	Small	From $R^W_\ell$

G. Bernardi et al., arXiv:2203.06520[hep-ex]

## Global EW fit@FCC-ee

• through oblique *S*, *T*, *U* parameters



### • in the SMEFT approach



G. Bernardi et al., arXiv:2203.06520[hep-ex]

## Two directions for theoretical studies towards FCC

### analysis of presently conceivable and/or new scenarios of BSM physics

- study of potential FCC sensitivity to new heavy degrees of freedom through EFT approaches
- investigation of light new degrees of freedom through classes of models

 $\implies$  this will be discussed within the Theory session of tomorrow

		Flavour anomalies	Aoife Bharucha
Models of Composite Higgs at FCG		Room 2	11:15 - 11:40
Aldo Deandrea et al.		Axion-like particles Dr Jérémie	at FCC
Room 2	09:15 - 09:40	Quevillon	
Dark Matter: status and FCC Dario Buttazzo.	prospect at	Room 2	11:40 - 12:05
		Light composite sca	alars at FCC-ee
Status and prospects o Mark Goodsell	fSUSY	and FCC-hh Leonard Schwarze et al.	
Room 2	10:15 - 10:40	Discussion / potenti	al synergies
Piccinini (INFN)	Joint FCC-Fra	ance & Italy 2022	November 21, 2

## Two directions for theoretical studies towards FCC

 development of theoretical calculations necessary to satisfy the unprecedented precision requirements of FCC

 $\implies$  some example concerning FCC-ee in the following slides

### Challenges for theory: an example, Z pole



LEP EWWG, SLD WG, ALEPH, DELPHI, L3, OPAL, Phys. Rept. 427 (2006) 257

FCC-ee will require pushing th. uncertainty down by at least a factor of 10 on cross sections and even more on  $A_{FB}$  w.r.t LEP What changed from LEP era in the field of theory predictions?

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Impressive development during LHC era

### Impressive development during LHC era

reality: automatic codes for event generation at NLO (QCD and EW) precision matched to all order resummation of logarithmic enhanced corrections

- $2 \rightarrow 2$ @NNLO QCD perturbative accuracy for all processes
- $2 \rightarrow 3 @\mathsf{NNLO} \ \mathsf{QCD} \ \mathsf{accuracy} \ \mathsf{becoming} \ \mathsf{available} \ \mathsf{for} \ \mathsf{selected} \ \mathsf{processes}$
- N3LO QCD calculations for Higgs and DY production
- different approaches for matching NNLO calculation and resummation of logs

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N3LO QCD calculations for Higgs and DY production

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### not enough for FCC-ee

• Workshop "Precision calculations for future  $e^+e^-$  colliders: targets and tools", CERN, 7-17 June 2022

https://indico.cern.ch/event/1140580/

- improved description of ISR QED radiation and IF interference (non-factorizable effects larger than the required precision, contrary to LEP precision), together with a sensible procedure for extracting EWPO in presence of higher order corrections (beyond one loop)
- some progress already achieved and future paths identified

Blondel, Gluza, Jadach, Janot, Riemann (Eds), CERN-2019-003

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Blondel, Gluza, Jadach, Janot, Riemann (Eds), CERN-2019-003

- at least complete NNLO accuracy in  $e^+e^- \rightarrow f\bar{f}$
- expansion of the amplitude for  $e^+e^-\to f\bar{f}$  around the complex pole  $s_0=M_Z^2-i\Gamma_Z M_Z$

$$\mathcal{M} = \frac{R}{s - s_0} + S + S'(s - s_0)$$

$$R \rightarrow \text{known@NNLO} + \text{leading higher orders}$$

$$S \rightarrow \text{known@NLO}$$

$$S' \rightarrow \text{known@(N)LO}$$

• EWPO extraction:  $\rightarrow Z f \bar{f}$  vertex at N3LO and leading N4LO

A. Freitas

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A. Freitas

- The above two items are beyond present knowledge
- progress needed on the study of the mathematical structure of scattering amplitudes
- as well as seminumerical approaches to Feynman diagram

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- Also new MC generators will be necessary to keep under control the theoretical precision at the few  $10^{-5}$  level
  - through matching between fixed order perturbative corrections and (exclusive) resummation
  - different groups already started, e.g. MG5\_aMC@NLO, Whizard, Sherpa, Herwig7, Pythia8, KKmc, BhLumi, BabaYaga

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• Luminosity requires control of QED corrections (and had vacuum polarization) for Bhabha scattering with one order of magnitude better than for LEP  $\sim 0.06\%$  (recently revisited at  $\sim 0.04\%$ )

P. Janot and S. Jadach, arXiv:1912.02067

- beam-beam interaction effects have to be considered
  - e.g. tiny shift on luminosity ( $\sim 0.05\%$ ) which contributes to remove the LEP tension in the number of light neutrinos

 $N_{\nu} = 2.9840 \pm 0.0082 \implies N_{\nu} = 2.9963 \pm 0.0074$ 

P. Janot and S. Jadach, arXiv:1912.02067; Voutsinas, Perez, Dam, Janot, arXiv:1908.01704

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- for hadronic final states (  $\to A^0_{FB},\,\alpha_s(Q^2)$  from event shape variables,  $\tau^+\tau^-)$ 
  - parton shower precision, non perturbative QCD corrections
  - quark and gluon fragmentation
  - jet substructure

P. Nason, D. D'Enterria, G. Soyez

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- Improvements in QED corrections crucial also for Flavour physics
  - two rare decays  $B^0 \to K^* \tau^+ \tau^-$  and  $B^+ \to \pi \tau^+ \nu_{\tau}$  (n.a. at LHC and BELLEII) will allow to perform strong checks of LFU
  - while QCD effects cancel in the ratio of BRs, QED do not (because of the different leptonic masses)
  - Workshop "FCC Flavour Physics Programme", CERN, 12-13 Sept. 2022

https://indico.cern.ch/event/1186057

## Another example, WW threshold: $e^+e^- ightarrow 4$ fermions



- first NLO exact calculation completed in 2005 for  $WW \rightarrow 4f$ 
  - th. accuracy  $\lesssim 1\%$  A. Denner et al., PLB612 (2005) 223; NPB 724 (2005) 247
- at present  $e^+e^- \rightarrow 4f$  cross sections @NLO accuracy can be calculated with automated tools
- NNLO enhanced contributions because of Coulomb photon effects calculated by means of EFT methods

M. Beneke et al., NPB 792 (2008) 89; S. Actis et al., NPB807 (2009) 1

• th. accuracy  $\sim 0.5\%$   $\Delta M_W \sim 3 \text{ MeV}$ 

## WW threshold: future prospects

- Having in mind a target precision  $\Delta M_W \sim 1$  MeV we would need
  - an improved treatment of EFT, which requires
    - NNLO corrections to  $e^+e^- \rightarrow WW$  in NWA
    - NNLO accuracy in the W decay
  - improved treatment of ISR including the partonic structure of the electron up to NLL

S. Frixione, Bertone, Cacciari, Stagnitto, Zaro, Zhao

## $t\bar{t}$ threshold (from M. Beneke)

- I  $e^+e^- \rightarrow t\bar{t}X$  cross section near threshold now computed at NNNLO in (PNR)QCD + top-Yukawa effects
  - Sizeable 3rd order corrections and reduction of theoretical uncertainty to about ±3%.
- II Realistic predictions for  $e^+e^- \rightarrow W^+W^-b\bar{b}$  near top-pair threshold
  - NNLO available, including cuts invariant mass cuts.
- III Parameter dependences  $(m_t, \Gamma_t, y_t, \alpha_s)$  can be studied.
  - $(m_t, \Gamma_t)$  with unrivaled accuracy.
  - yt with 20% accuracy from threshold already challenging.
- IV Further requirements:
  - ISR / QED PDF's for  $x \rightarrow 1$  with NLL evolution
  - N4LO QCD would be reassuring, but appears prohibitive.

https://www.hepforge.org/downloads/qqbarthreshold/

M. Beneke (TU München)		CERN, 08 June 2022	25 / 25
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## Summary and outlook

FCC colliders necessary to improve our knowledge of Nature

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- exciting challenges for model building looking for the "right" extension of the SM using data from colliders, GW, cosmological surveys, expts from space, neutrino expts, DM passive searches

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- FCC-ee needs a very big jump in the accuracy of theoretical predictions
  - according to LEP and LHC experience, we had an enormous progress in the calculation techniques and development of new Monte Carlo generators, but

**progress requires coherent efforts in a long range** in order to avoid as much as possible the systematics being dominated by theoretical uncertainty