

# CP violation and (heavy) Neutrinos

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CP2023 12.02. – 17.02.

# Flavour violation in SM

## Flavour and CP violation: SM

Flavour in the **Standard Model**: interactions (and transitions) between **fermion families**

$$\begin{aligned} \mathcal{L} = & -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} \\ & + i \bar{F} \not{D} \gamma + h.c. \\ & + \bar{\chi}_i Y_{ij} \chi_j \phi + h.c. \\ & + |\not{D}_\mu \phi|^2 - V(\phi) \end{aligned}$$

Gauge interactions are **flavour universal**

Yukawas  $Y_{ij}^u$ ,  $Y_{ij}^d$  and  $Y_{ij}^\ell$  encode all **flavour dynamics**

(Masses, mixings and **CP violation**)

**SM quark sector:**

6 massive states

flavour violated in charged current interactions  $V_{CKM}^{ij} W^\pm \bar{q}_i q_j$

total **baryon number** is conserved in SM interactions

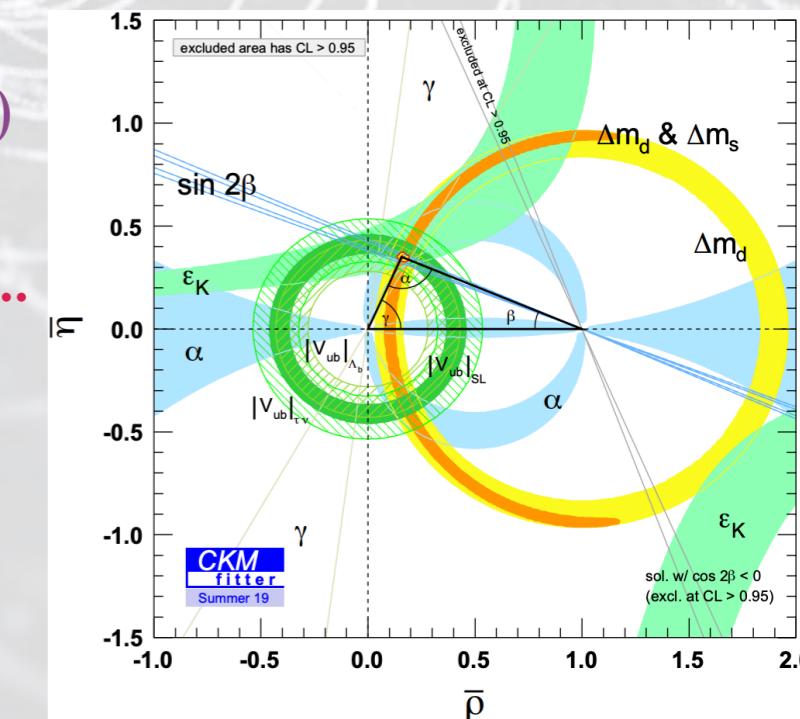
CP violation:  $\delta_{CKM}$  and  $\theta_{QCD}$

(not enough to explain BAU from baryogenesis)

**CKM paradigm** extensively probed:

Meson oscillations & decays,  $\beta$  decays, **CP violation...**

Few tensions, CAA,  $V_{cb}$ ,  $V_{ub}$ , ...



See talks by Stéphane,  
Francesca and Radek

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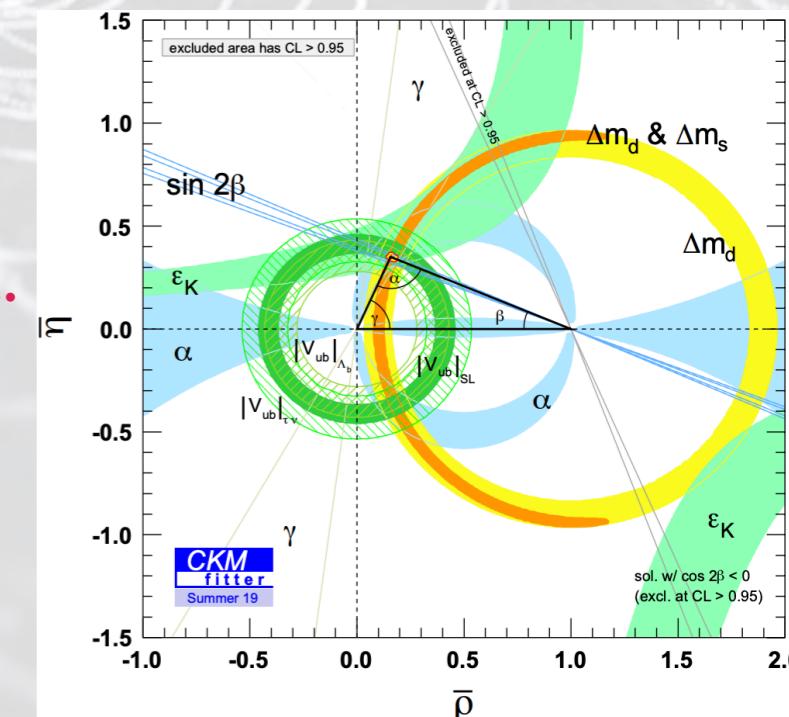
**CKM paradigm** extensively probed:

Meson oscillations & decays,  $\beta$  decays, **CP violation...**

Few tensions, CAA,  $V_{cb}$ ,  $V_{ub}$ , ...

**SM lepton sector:** neutrinos are strictly massless

- ▶ Conservation of (total) **lepton number** and **lepton flavour**
- ▶ **Lepton flavour universality** only broken by Yukawas
- ▶ No intrinsic **CPV sources** – (tiny) lepton **EDMs** @ 4-loop



See talks by Stéphane,  
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# Flavours: beyond SM

Strong arguments in **f(l)avour** of New Physics!

Observations **unaccounted** for in SM:  $\nu$ -oscillations, Dark matter,

baryon asymmetry of the Universe

(also some theoretical caveats...)

How to unveil the NP model at work?

⇒ Test SM **symmetries** with flavour observables:

(c)LFV, lepton flavour universality violation, ...

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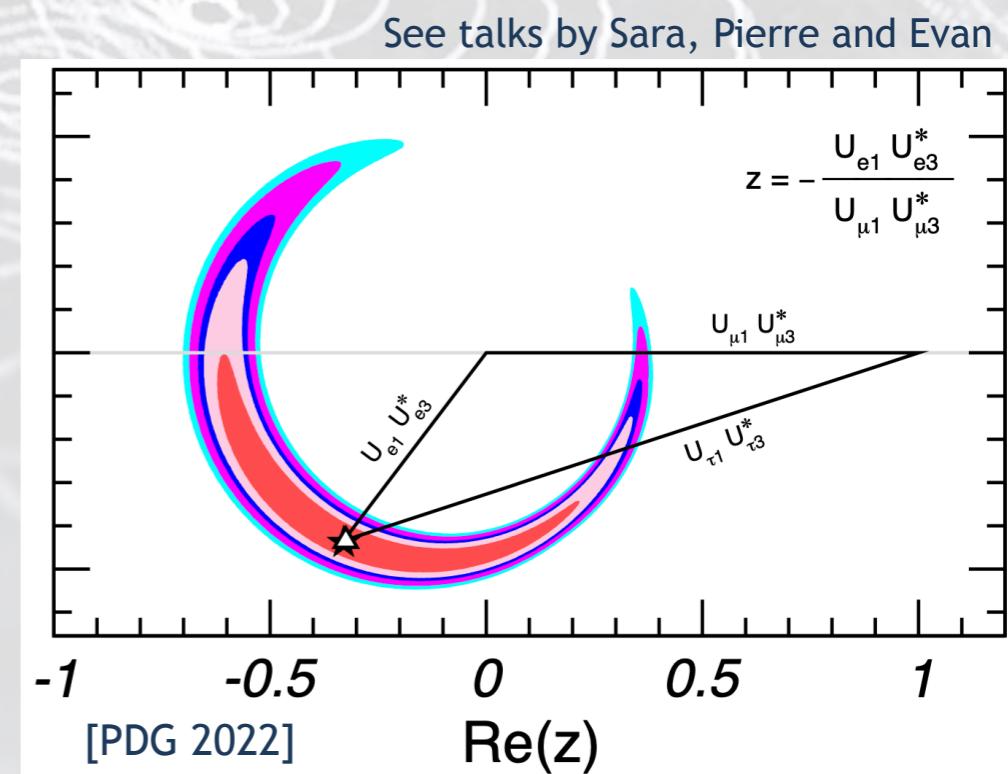
(c)LFV, lepton flavour universality violation, ...

$\nu$ -oscillations 1st laboratory **evidence** of New Physics!

- ▶ New mechanism of mass generation? Majorana fields?
- ▶ New sources of CP violation?

Several puzzles remain:

- ▶ Absolute mass scale?
- ▶ Mass ordering? (NO vs IO)
- ▶ CP violation maximal?



## Lepton flavour probes of New Physics

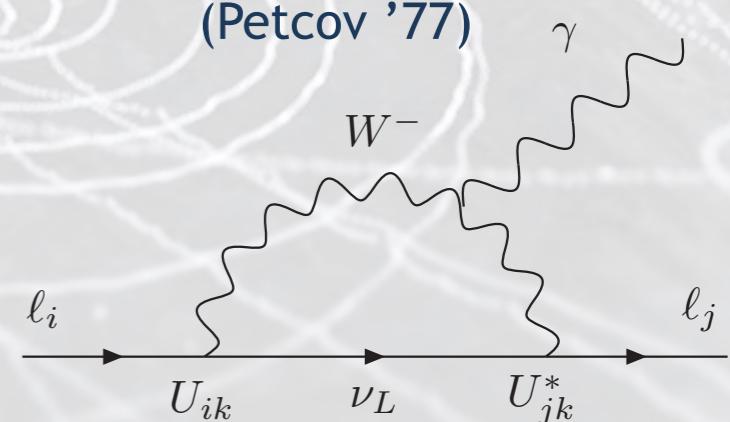
Neutrinos oscillate  $\Rightarrow$  neutral lepton flavour violated, neutrinos are massive,  
new sources of CPV?

Extend SM to accommodate  $\nu_\alpha \leftrightarrow \nu_\beta$ : ad-hoc 3  $\nu_R \Rightarrow$  Dirac masses, “ $\text{SM}_{m_\nu}$ ”,  $U_{\text{PMNS}}$

In  $\text{SM}_{m_\nu}$ : flavour-universal lepton couplings, lepton number conserved

cLFV possible ... but not observable!  $\text{BR}(\mu \rightarrow e\gamma) \propto |\sum U_{\mu i}^* U_{ei} m_{\nu_i}^2 / m_W^2| \simeq 10^{-54}$   
(Petcov '77)

EDMs still tiny... (2-loop from  $\delta_{CP}$ ,  $|d_\ell| \sim 10^{-35} \text{ ecm}$ )



$\Rightarrow$  any cLFV signal would imply non-minimal New Physics!  
(Not necessarily related to  $m_\nu$  generation)

Lepton flavours offer a plethora of observables and probes of New Physics

$\Rightarrow$  Negative search results: allow to place tight bounds on New Physics

# Neutrino mass generation

Mechanisms of  $m_\nu$  generation: account for **oscillation data**

and ideally address **SM issues** – BAU (leptogenesis), DM candidates, ...

Many well motivated possibilities, featuring distinct **NP states** (singlets, triplets)

Realised at **very different scales**  $\Lambda_{\text{EW}} \sim \Lambda_{\text{GUT}}$

⇒ Expect **very different phenomenological impact**

Compare “vanilla” type I seesaw vs. **low-scale seesaw**:

---

**High scale:**  $\mathcal{O}(10^{10-15} \text{ GeV})$

Theoretically “**natural**”  $Y^\nu \sim 1$

“Vanilla” leptogenesis

Decoupled new states

**Low scale:**  $\mathcal{O}(\text{MeV - TeV})$

Finetuning of  $Y^\nu$  (or approximate LN conservation)

Leptogenesis possible (resonant, ...)

New states **within experimental reach!**

**Collider, high-intensities (“leptonic observables”)**

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⇒ **low-scale seesaws** (and variants): non-decoupled states, **modified lepton currents!**

⇒ rich phenomenology at **colliders, high intensities and low energies**

(Also expect tight constraints)

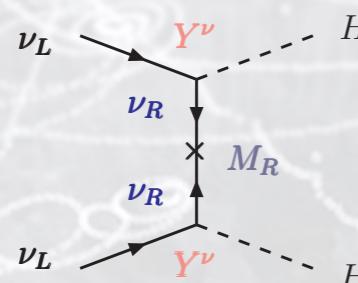
testability!!

## Disentangle seesaw mass models – more correlations

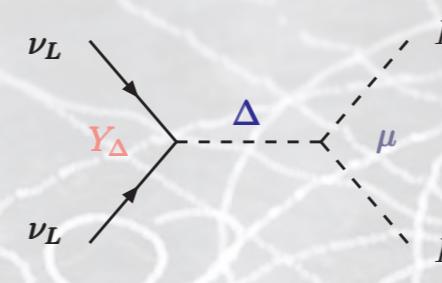
► Models of  $m_\nu$  (and leptonic LFV) predict/accommodate extensive ranges for cLFV...

In the absence of direct NP discovery - correlations might allow to disentangle models and provide important complementary information to direct searches!

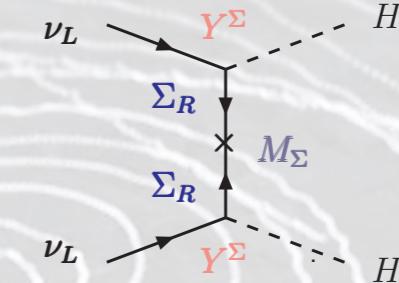
► Seesaw realisations: distinctive signatures for numerous cLFV observables ratios of observables to identify seesaw mediators & constrain their masses!



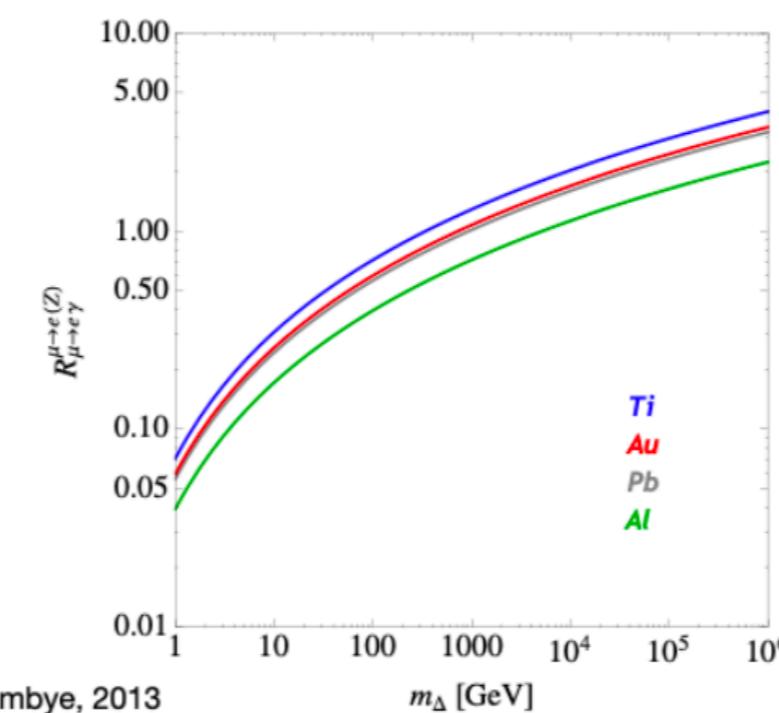
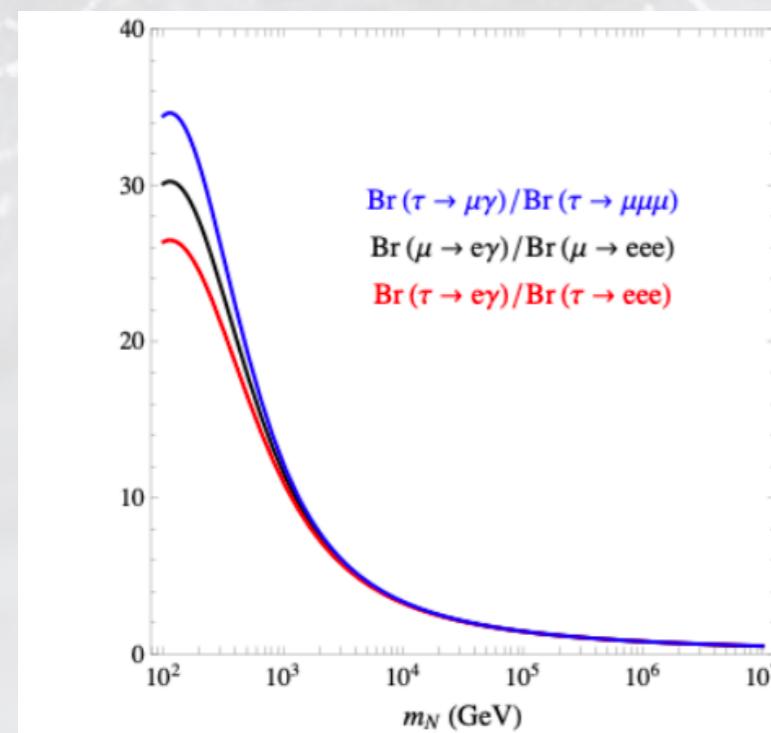
Type I (fermion singlet)



Type II (scalar triplet)



Type III (fermion triplet)



$$\frac{\text{BR}(\mu \rightarrow e\gamma)}{\text{BR}(\mu \rightarrow 3e)} = 1.3 \times 10^{-3}$$

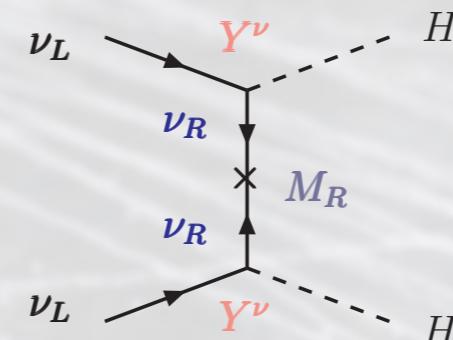
$$\frac{\text{BR}(\tau \rightarrow \mu\gamma)}{\text{BR}(\tau \rightarrow 3\mu)} = 1.3 \times 10^{-3}$$

$$\frac{\text{BR}(\mu \rightarrow e\gamma)}{\text{CR}(e-\mu, \text{Ti})} = 3.1 \times 10^{-4}$$

# Type I seesaw

(Heavy) right-handed **Majorana** neutrinos coupled via Higgs to SM-like neutrinos

$$M_\nu = \begin{pmatrix} 0 & v Y_\nu \\ v Y_\nu^T & M_N \end{pmatrix}$$



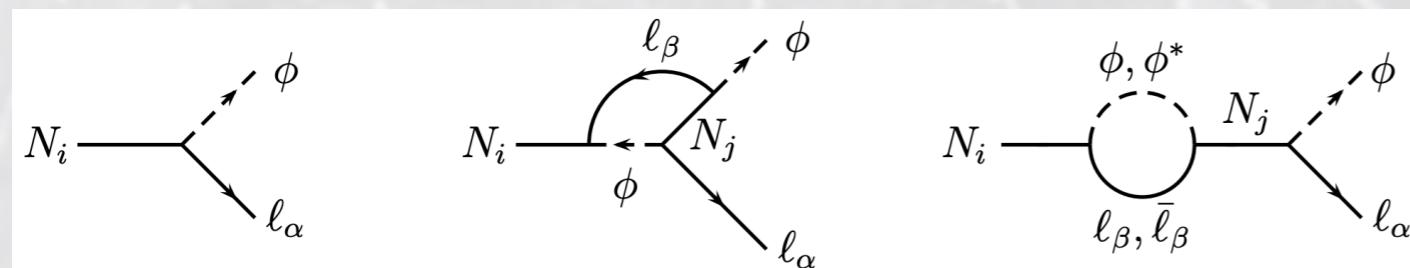
Generate “naturally” small masses of the active neutrinos

Masses and mixings:  $\mathbf{m}_\nu \simeq -v^2 Y_\nu^T \mathbf{M}_N^{-1} Y_\nu$ ,  $\mathbf{U}^T \mathcal{M}_\nu^{6 \times 6} \mathbf{U} = \text{diag}(m_i)$

$$U_{\nu N} \simeq v Y_\nu^* M_N^{-1\dagger} \quad \mathbf{U} = \begin{pmatrix} \mathbf{U}_{\nu\nu} & U_{\nu N} \\ U_{N\nu} & U_{NN} \end{pmatrix}, \quad \mathbf{U}_{\nu\nu} \simeq (1 - \eta) \mathbf{U}_{\text{PMNS}}$$

**Leptogenesis in a nutshell:** generate lepton asymmetry  $\Rightarrow$  convert into baryon asymmetry  
 (See talk by Stéphane Lavignac and lectures by Julia Harz)

**CP-violating** out of equilibrium decay  $\Rightarrow$  create lepton asymmetry (at a high scale)



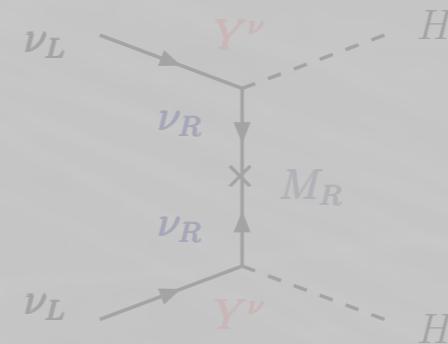
**Interference** of tree & loop diagrams

$$\epsilon_i^\alpha \equiv \frac{\Gamma(N_i \rightarrow \phi \ell_\alpha) - \Gamma(N_i \rightarrow \phi^\dagger \bar{\ell}_\alpha)}{\sum_\beta [\Gamma(N_i \rightarrow \phi \ell_\beta) + \Gamma(N_i \rightarrow \phi^\dagger \bar{\ell}_\beta)]} \propto \sum_{j \neq i} \text{Im}[Y_{\alpha i}^* (Y^{\nu\dagger} Y^\nu)_{ij} Y_{\alpha j}^\nu]$$

# Type I seesaw

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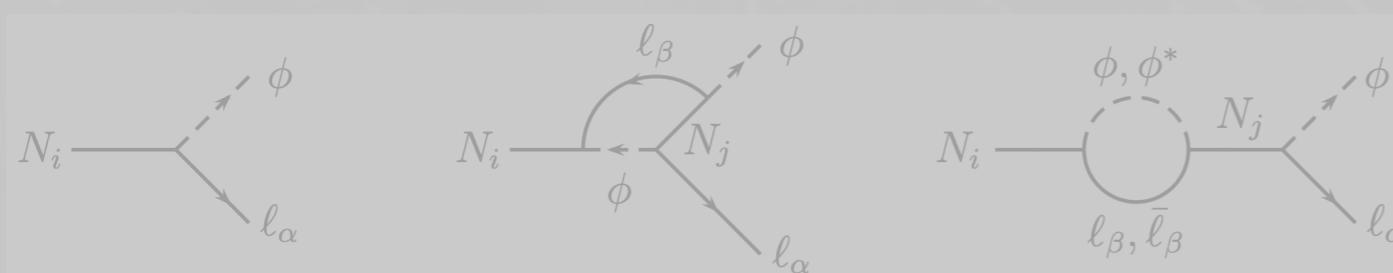
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## What is the phenomenological impact of these phases?

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# LNV and CP violation

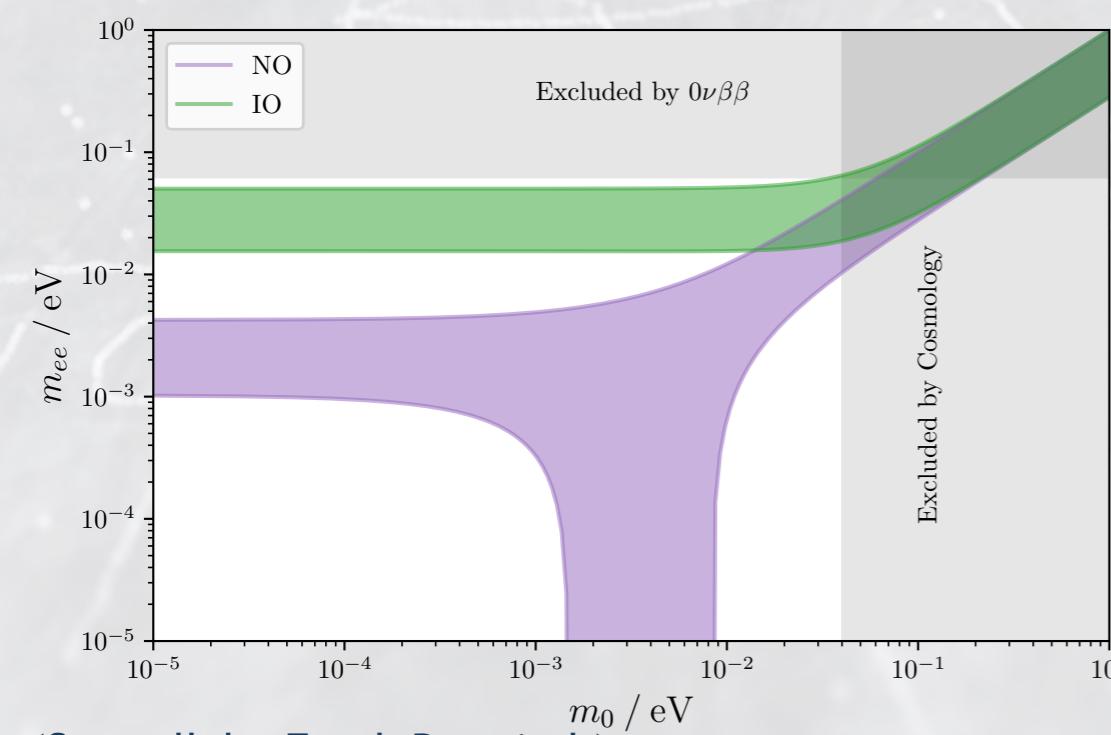
## CPV phases and LNV

If neutrinos are **Majorana**, total **lepton number** is violated @ tree-level

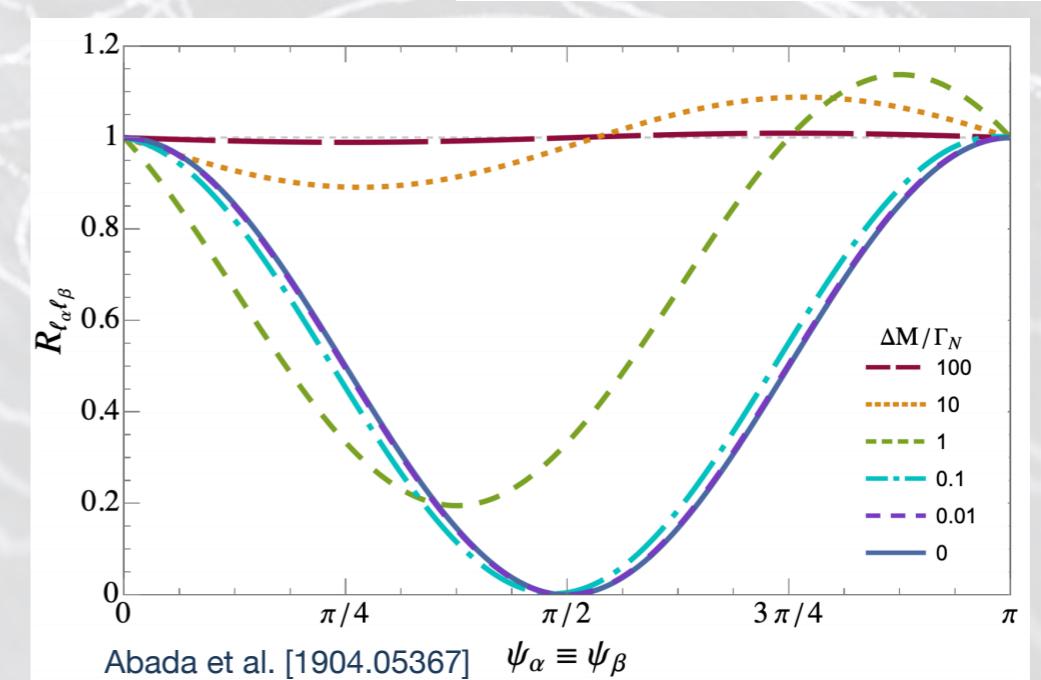
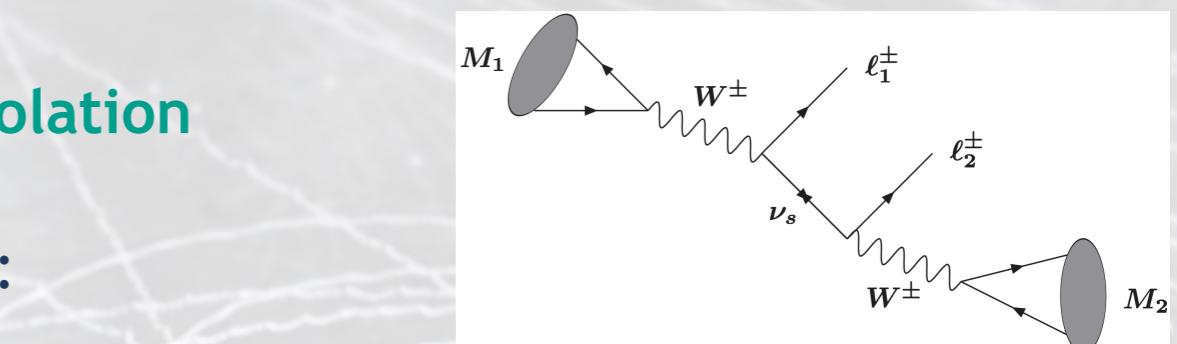
⇒ Expect  $0\nu\beta\beta$ , **LNV meson decays**, SS di-lepton tails, ...

**Massive** (and mixing) neutrinos: new sources of **CP violation**

**CP violating** phases are known to play a crucial role:



(See talk by Frank Deppisch)



Abada et al. [1904.05367]

PMNS phases lead to “neck” in  $0\nu\beta\beta$ , sterile states can interfere in **LNV meson decays**

(Similar interference effects in SS vs OS di-lepton production)

e.g. Abada et al. [2208.13882]

# LNV and CP violation

## CPV phases and LNV

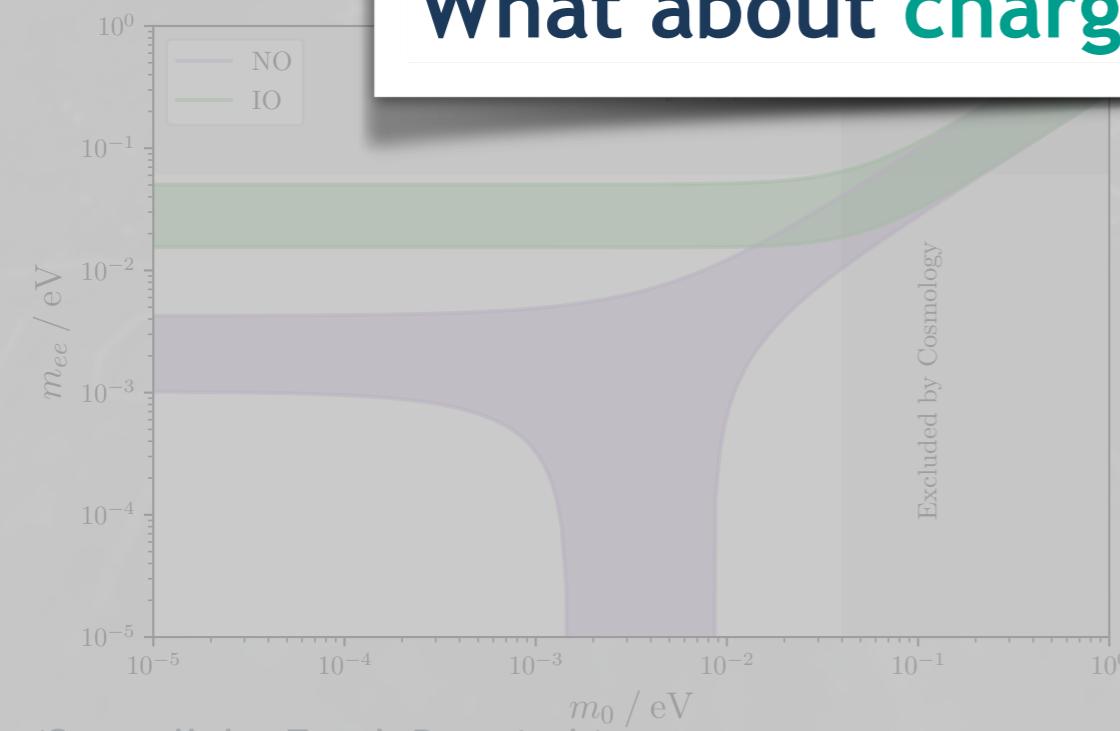
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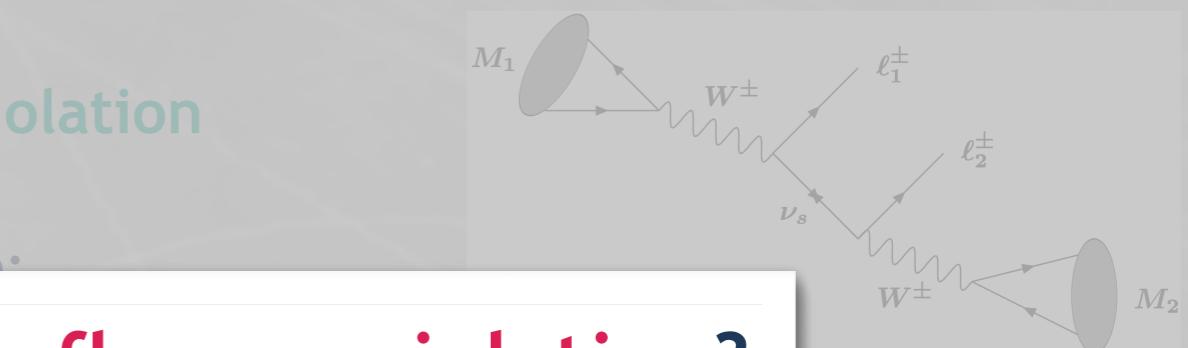
**Massive** (and mixing) neutrinos: new sources of **CP violation**

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**What about charged lepton flavour violation?**



(See talk by Frank Deppisch)



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# A “3+2” neutrino toy model

Simplified "toy models" for phenomenological analyses: SM +  $\nu_s$

► Ad-hoc (low-energy) constructions: SM extended via  $n_S$  Majorana massive states

No assumption on mechanism of mass generation

Well-defined interactions in physical basis

*Phenomenological low-energy limit of complete constructions (type I seesaw, ISS, ...)*

Hypotheses: 3 active neutrinos + 2 sterile states

interaction basis  $\leftrightarrow$  physical basis

Left-handed lepton mixing  $\tilde{U}_{\text{PMNS}}$

3 × 3 sub-block, non-unitary!

Active-sterile mixing  $U_{\alpha i}$

3 × 5 rectangular matrix

$$n_L = (\nu_{L e}, \nu_{L \mu}, \nu_{L \tau}, \nu_s^c, \nu_{s'}^c)^T$$

$$|n_L\rangle = \mathcal{U}_{5 \times 5} |\nu_i\rangle$$

$$\mathcal{U}_{5 \times 5} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} & U_{e4} & U_{e5} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} & U_{\mu 4} & U_{\mu 5} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} & U_{\tau 4} & U_{\tau 5} \\ U_{s1} & U_{s2} & U_{s3} & U_{s4} & U_{s5} \\ U_{s'1} & U_{s'2} & U_{s'3} & U_{s'4} & U_{s'5} \end{pmatrix}$$

$$\mathcal{U} = R_{45} R_{35} R_{25} R_{15} R_{34} R_{24} R_{14} R_{23} R_{13} R_{12} \times \text{diag}(1, e^{i\varphi_2}, e^{i\varphi_3}, e^{i\varphi_4}, e^{i\varphi_5})$$

Would-be PMNS no longer unitary, leptonic W and Z vertices modified

► Physical parameters: 5 masses [3 light (mostly active) & 2 heavier (mostly sterile) states]

10 mixing angles, 10 CPV phases (6 Dirac  $\delta_{ij}$ , 4 Majorana  $\varphi_i$ )

# The impact of CP violating phases

cLFV processes mediated by HNL at loop-level

Consider "3+2" toy model (addition of 2 heavy sterile states; leptonic mixing  $\mathcal{U}_{5 \times 5}$ , CPV phases)

► Radiative decays:  $\text{BR}(\mu \rightarrow e\gamma) \propto |G_\gamma^{\mu e}|^2$

$$G_\gamma^{\mu e} = \sum_{i=4,5} \mathcal{U}_{ei} \mathcal{U}_{\mu i}^* G_\gamma \left( \frac{m_{N_i}^2}{m_W^2} \right)$$



Assume (for *simplicity & illustrative purposes*):  $m_4 \approx m_5$  and  $\sin \theta_{\alpha 4} \approx \sin \theta_{\alpha 5} \ll 1$

$$|G_\gamma^{\mu e}|^2 \approx 4 \sin^2 \theta_{e4} \sin^2 \theta_{\mu 4} \cos^2 \left( \frac{\delta_{14} + \delta_{25} - \delta_{15} - \delta_{24}}{2} \right) G_\gamma \left( \frac{m_{N_i}^2}{m_W^2} \right)$$

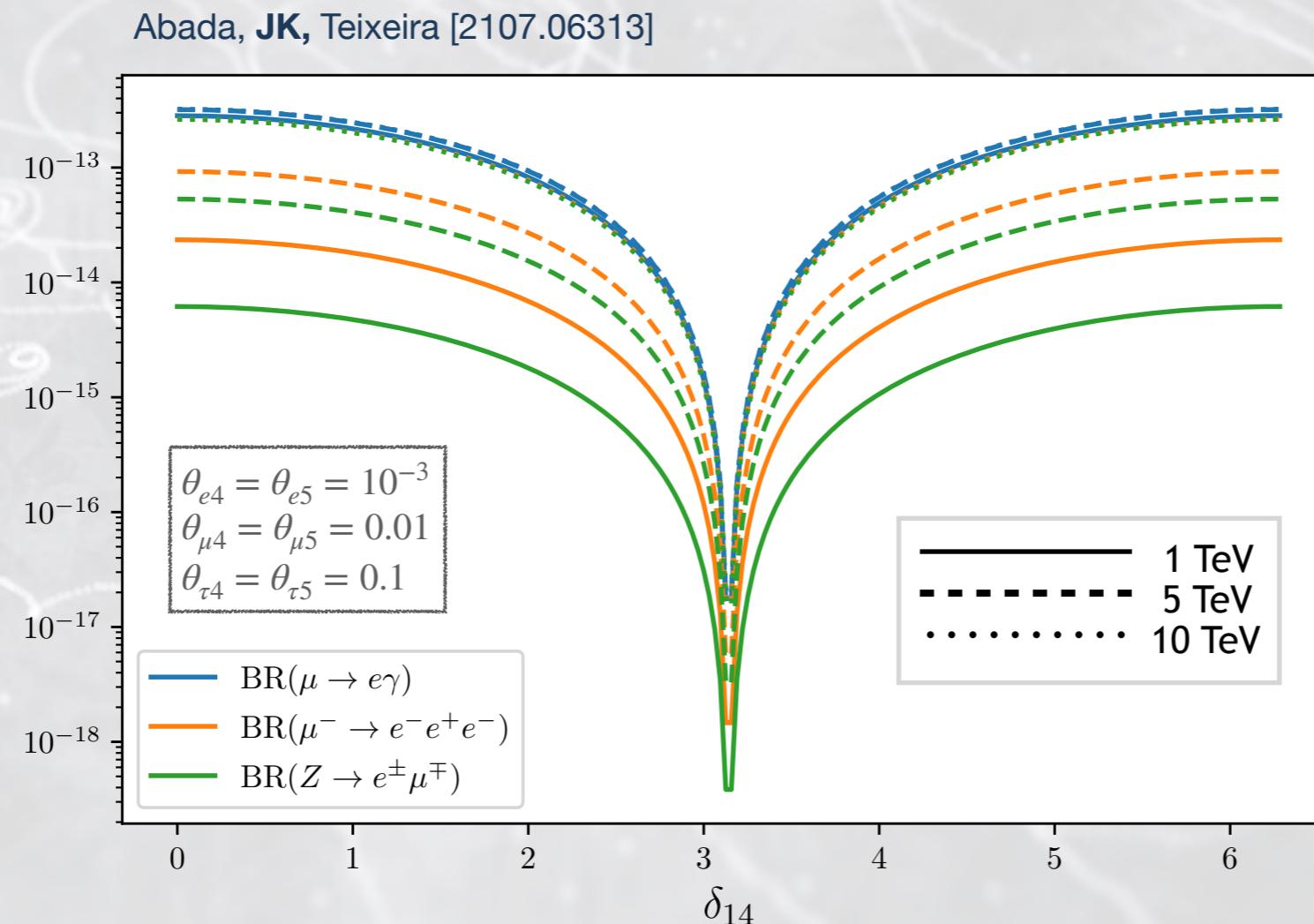
⇒ Radiative decays: rate depends **only on Dirac phases**; full cancellation for  $\Sigma \delta = \pi$

(Other form factors - more involved expressions, depend also on Majorana phases  $\varphi_{4,5}$ )

# The impact of CP violating phases: Dirac

cLFV processes mediated by HNL at loop-level

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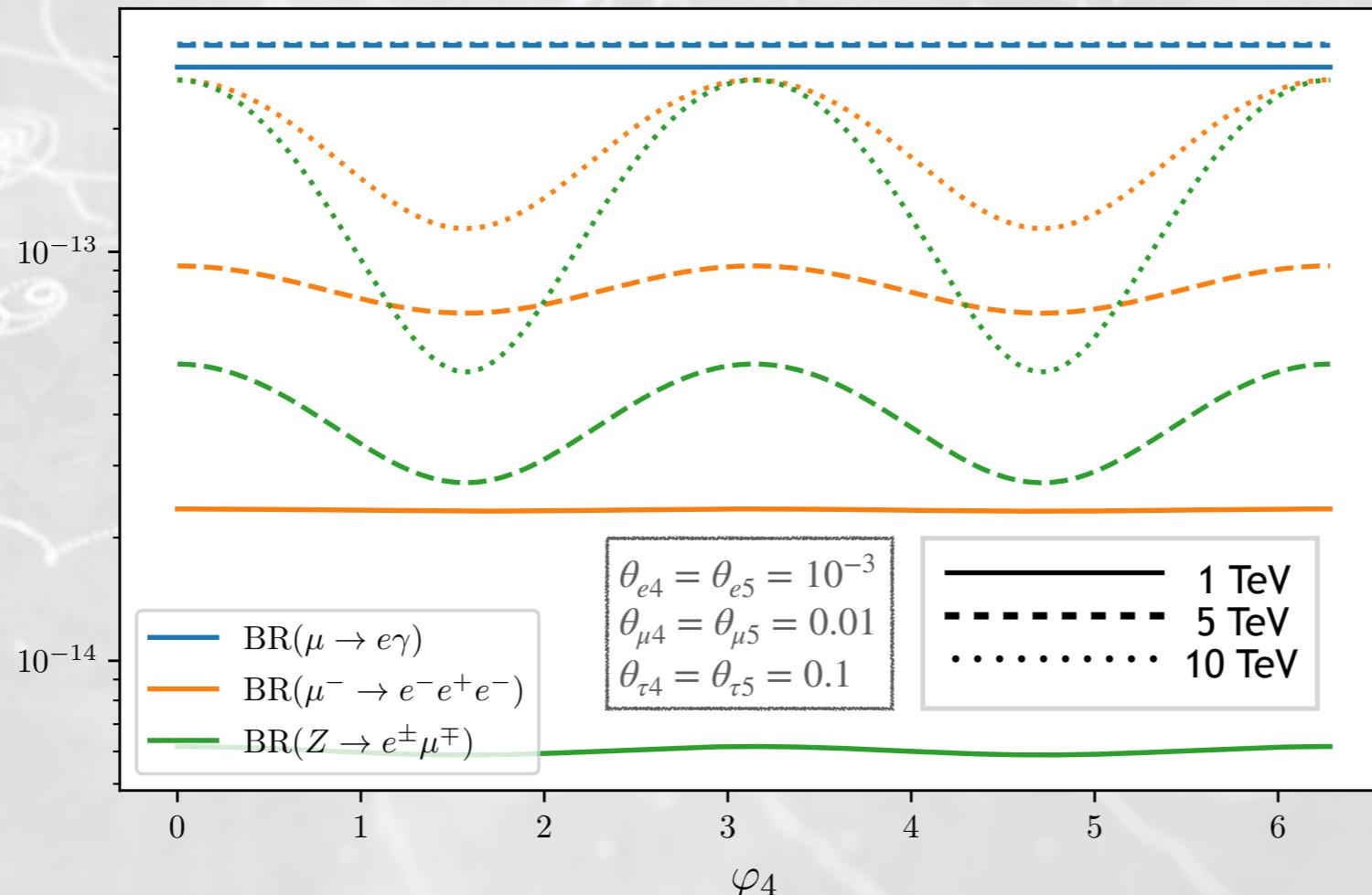
⇒ Full cancellation of the rates for  $\delta_{14} = \pi$ , similar results for other (Dirac) phases

# The impact of CP violating phases: Majorana

cLFV processes mediated by HNL at loop-level

Consider "3+2" toy model (addition of 2 heavy sterile states; leptonic mixing  $\mathcal{U}_{5\times 5}$ , CPV phases)

Abada, JK, Teixeira [2107.06313]



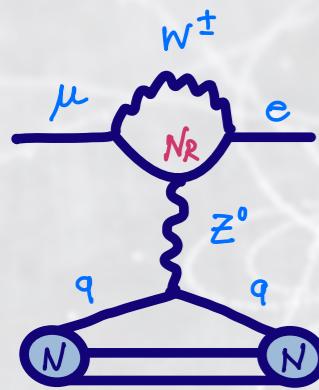
⇒ Milder dependence,  $\gamma$ -penguin independent of Majorana phases

# The impact of CP violating phases – breaking correlations

cLFV signatures: ratios of observables to identify mediators & constrain their masses!

But - CP violating phases do matter! And *impact naïve expectations...*

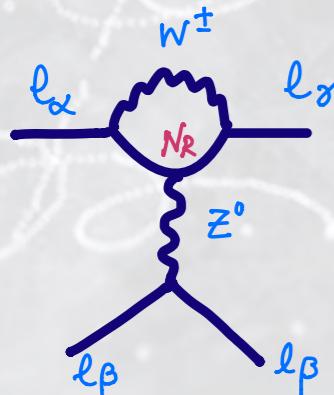
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Observables dominated by common topology: Z-penguins

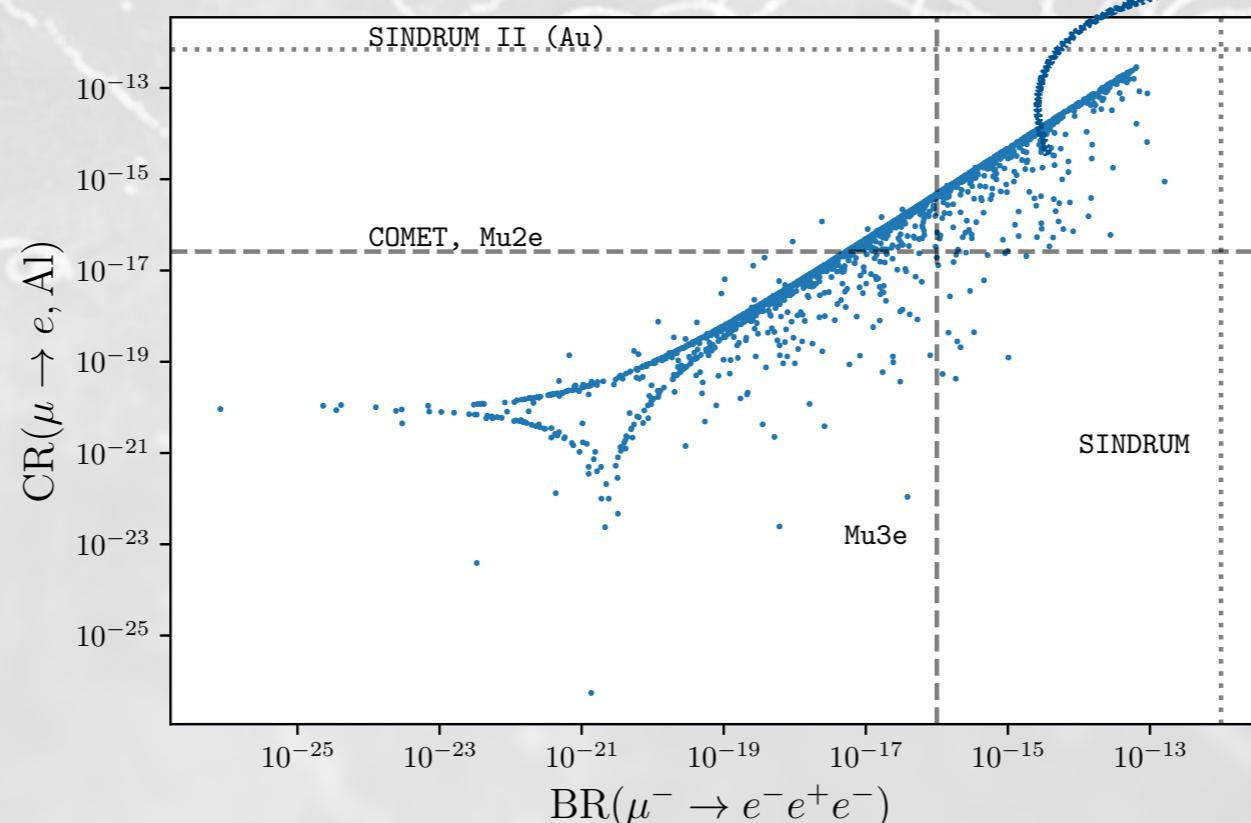
$\mu - e$  conversion in nuclei

3-body muon decays ( $\mu \rightarrow 3e$ )



$$m_4 = m_5 = 1 \text{ TeV}$$

- CP conserving



Abada, JK, Teixeira [2107.06313]

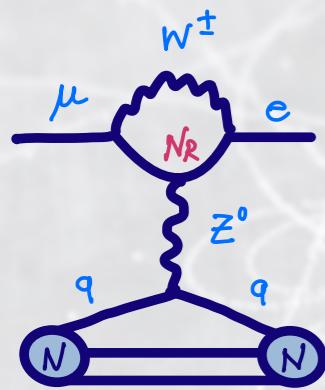
**Observation of  $\mu \rightarrow 3e$**   
 $\Rightarrow$  observation of  
 $\mu - e$  conversion

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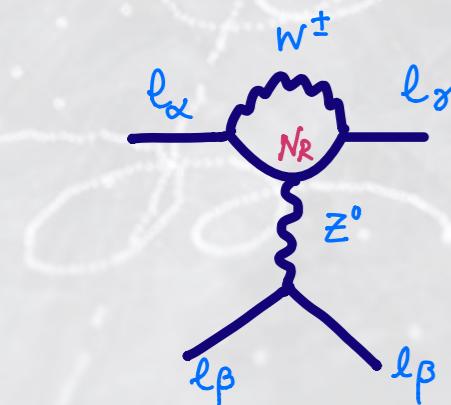
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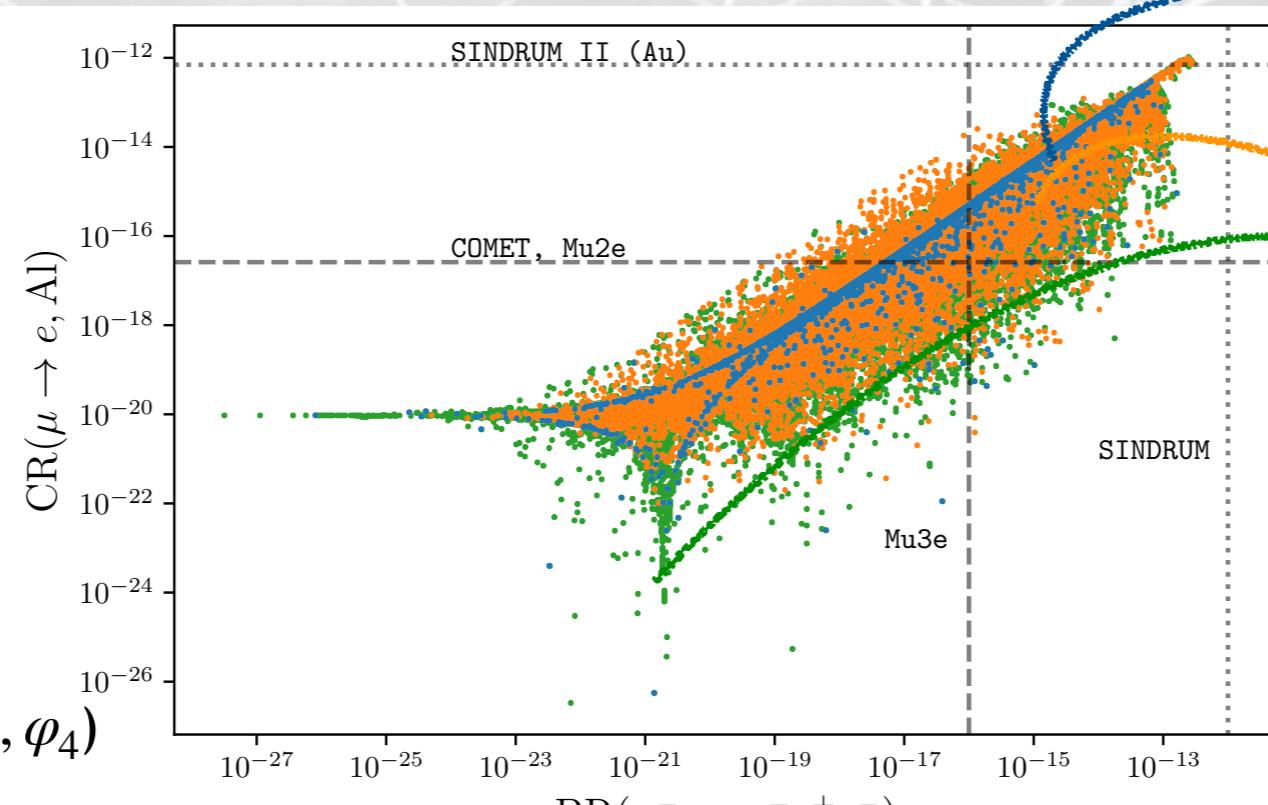
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- CP conserving
- CPV phases (random  $\delta_{\alpha 4}, \varphi_4$ )
- CPV phases (grid  $n\pi/4$ )



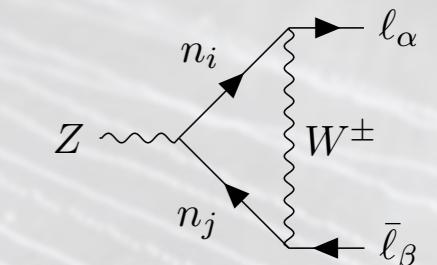
Abada, JK, Teixeira [2107.06313]

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**↗ observation of**  
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## CP-asymmetries

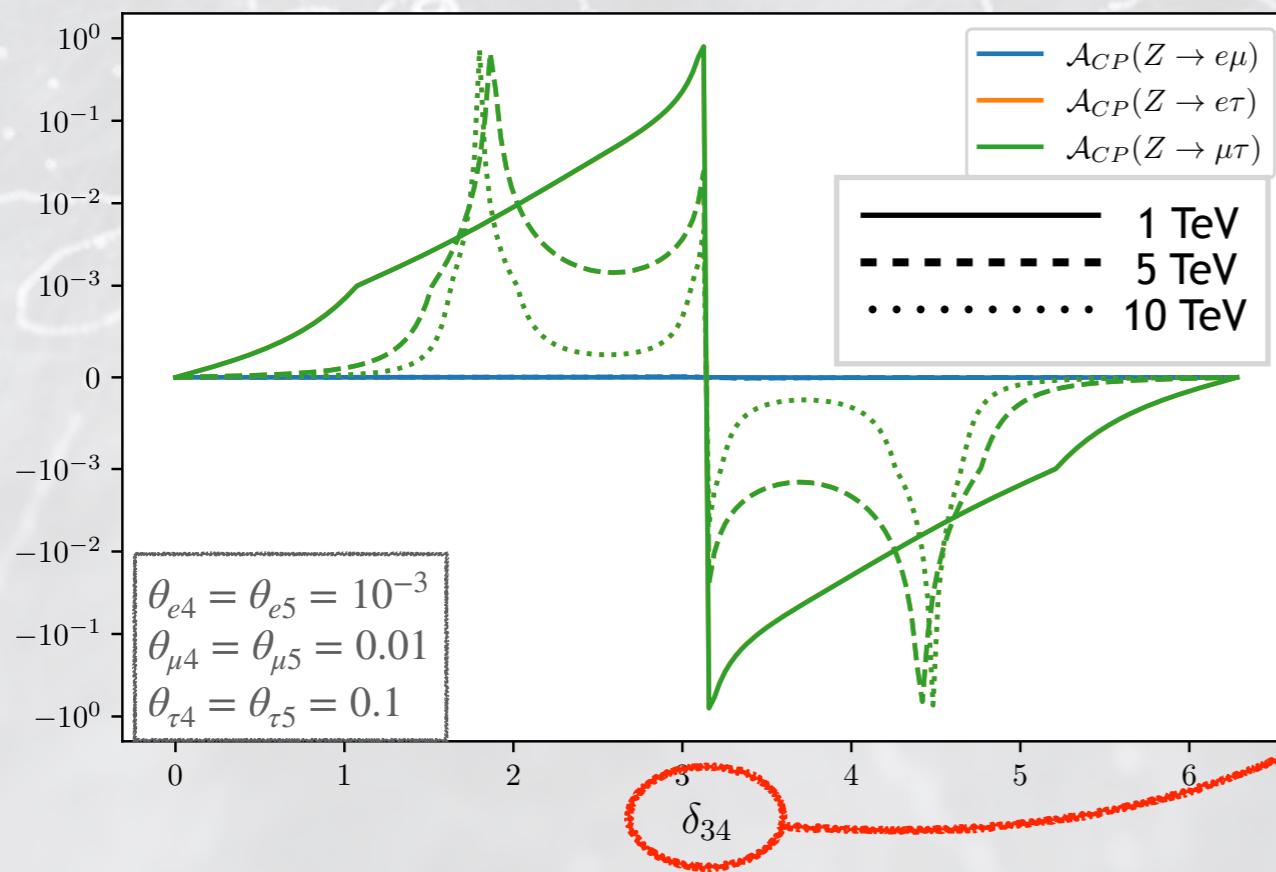
Correlations broken, large mixing angles still possible, how do we “tag” the presence of **CPV**?

Introduce **CP**-asymmetries:  $\mathcal{A}_{CP}(Z \rightarrow \ell_\alpha \ell_\beta) = \frac{\Gamma(Z \rightarrow \ell_\alpha^+ \ell_\beta^-) - \Gamma(Z \rightarrow \ell_\alpha^- \ell_\beta^+)}{\Gamma(Z \rightarrow \ell_\alpha^+ \ell_\beta^-) + \Gamma(Z \rightarrow \ell_\alpha^- \ell_\beta^+)}$



Consider "3+2" toy model (addition of **2 heavy sterile states**; leptonic mixing  $\mathcal{U}_{5 \times 5}$ , **CPV phases**)

**Simplified approach:**  $\sin \theta_{\alpha 4} = \sin \theta_{\alpha 5}$  ;  $m_4 = m_5 = (1, 5, 10)$  TeV



Abada, JK, Pinsard, Rosauro, Teixeira [2207.10109]

- ▶ Impact of **Majorana** CPV phases (per mile - per cent effect)
- ▶ **Dirac:** sensitivity of  $\mathcal{A}_{CP}$  to **all phases**
- $\delta_{34}$  - at the source of very large  $\mathcal{A}_{CP}(Z \rightarrow \mu\tau)$   
⇒ amplified with **increasing  $m_{4,5}$**   
(Higgs decay asymmetries accidentally negligible)

## CP-asymmetries

Correlations broken, large mixing angles still possible, how do we “tag” the presence of **CPV**?

Benchmark points (with different mixing)

$P_1$  (**CP-conserving**),  $P_2$  (**CP-violating**)  
lead to identical **cLFV predictions!**

Observable	$\mu \rightarrow eee$	$\mu - e$ (Al)	$\tau \rightarrow \mu\mu\mu$	$Z \rightarrow \mu\tau$
$P_{1,2}$ prediction	$2 \times 10^{-15}$	$5 \times 10^{-14}$	$1 \times 10^{-10}$	$2 \times 10^{-10}$

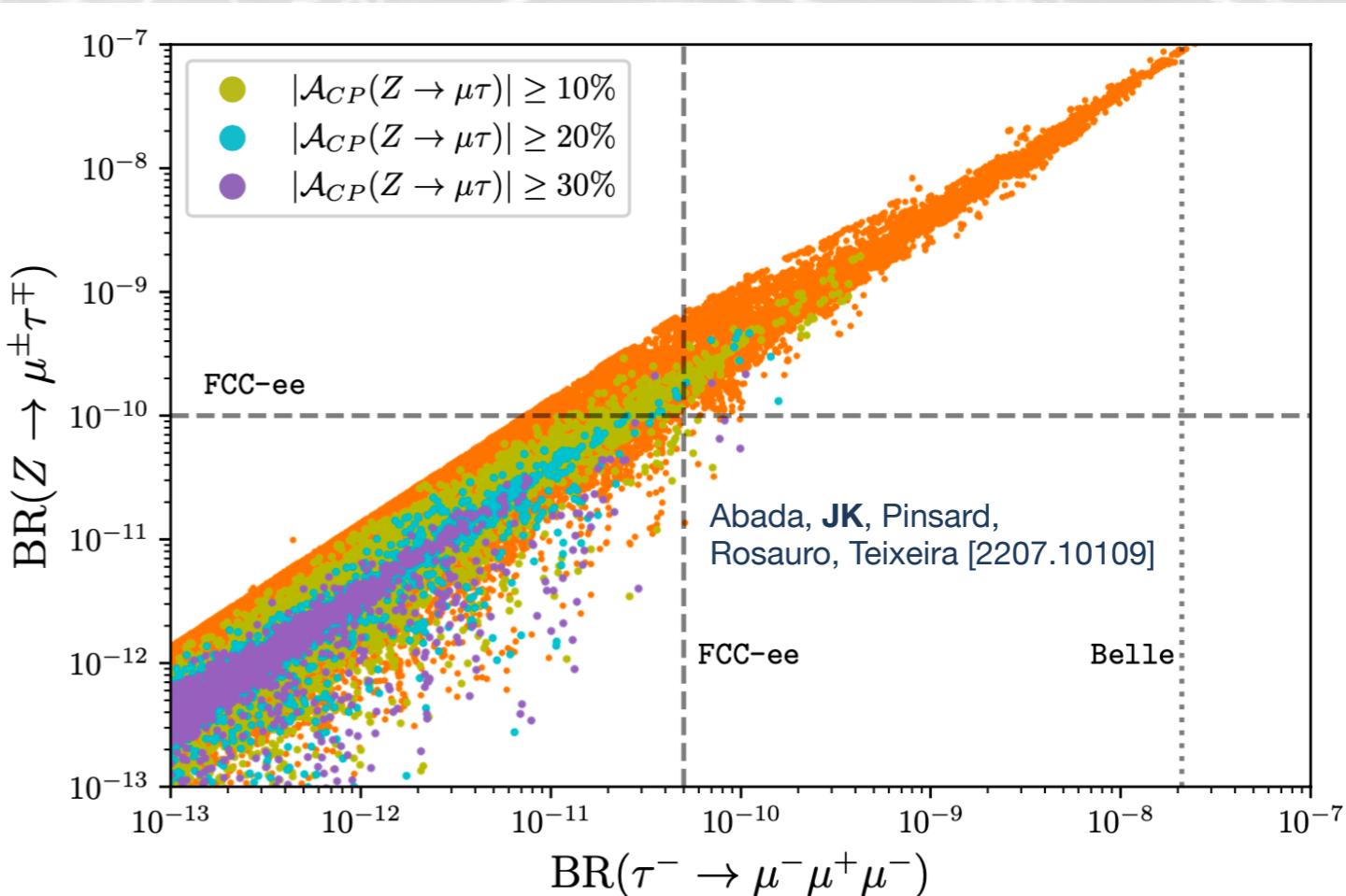
Abada, JK, Pinsard,  
Rosauro, Teixeira [2207.10109]

$$\text{Consider CP-asymmetries: } \mathcal{A}_{CP}(Z \rightarrow \ell_\alpha^+ \ell_\beta^-) = \frac{\Gamma(Z \rightarrow \ell_\alpha^+ \ell_\beta^-) - \Gamma(Z \rightarrow \ell_\alpha^- \ell_\beta^+)}{\Gamma(Z \rightarrow \ell_\alpha^+ \ell_\beta^-) + \Gamma(Z \rightarrow \ell_\alpha^- \ell_\beta^+)}$$

$\Rightarrow P_2: \mathcal{A}_{CP}(Z \rightarrow \mu\tau) \simeq 30\% !$

Measuring **CP-asymmetries**, i.e. searching  
for  $Z \rightarrow \ell_\alpha^+ \ell_\beta^-$  and  $Z \rightarrow \ell_\alpha^- \ell_\beta^+$  independently  
might allow to constrain **CPV phases**  
and can help to identify the **source of cLFV!**

**CP (T)-asymmetries** have also been considered in  
angular distributions of  $\mu \rightarrow eee$   
(see Bolton & Petcov [2204.03468])



## Conclusion

Neutrino oscillations are the 1st **laboratory evidence** of **New Physics!**

⇒ massive and oscillating neutrinos open the door to **LFV** and  
new sources of **CPV**

New **CPV phases** from **HNL** play a crucial role in **LNV** and **cLFV** processes:

- ⇒ **Interference effects** can enhance or suppress rates
- ⇒ Correlations between observables can be broken

Strong phenomenological impact!

**CP violating phases** need to be consistently taken into account in  
analyses of **HNL** models

See also Ema's poster :)



## Conclusion

Neutrino oscillations are the 1st **laboratory evidence** of **New Physics!**

⇒ massive and oscillating neutrinos open the door to **LFV** and

new sources of **CPV**

New **CPV phases** from **HNL** play a crucial role in analyses:

⇒ Interactions can be broken  
"You cannot spell **flavour** without **CP Violation**"  
**Phases do really matter!**

Strong phenomenological impact!

**CP violating phases** need to be consistently taken into account in analyses of **HNL** models



# Backup



# cLFV observables across all sectors and energies

Any **cLFV** signal necessarily implies the presence of **New Physics!**

- ▶ “Purely” leptonic cLFV observables:  $\ell_\beta \rightarrow \ell_\alpha \gamma, \ell_\beta \rightarrow \ell_\alpha \ell_\gamma \ell_{\gamma'}$   
 Most stringent exp. bounds:  $\text{BR}(\mu \rightarrow e\gamma) \lesssim 4.2 \times 10^{-13}, \text{BR}(\mu \rightarrow eee) \lesssim 10^{-12}$
- ▶ Muonic atoms (and bound states): many “nuclear-assisted” cLFV observables  
 e.g. neutrinoless  $\mu - e$  conversion ( $\mu^- N \rightarrow e^- N$ ) :  $\text{CR}(\mu - e, \text{Au}) \lesssim 7 \times 10^{-13}$
- ▶ Semi-leptonic cLFV  $\tau$  decays:  $\tau \rightarrow P\ell', \tau \rightarrow V\ell'$ ;  $\text{BR}(\tau \rightarrow \phi\mu) \lesssim 8.4 \times 10^{-8}$
- ▶ (Semi-) leptonic cLFV meson decays:  $M \rightarrow \ell_\alpha^\pm \ell_\beta^\mp, M \rightarrow M' \ell_\alpha^\pm \ell_\beta^\mp$ ;  
 $\text{BR}(K_L \rightarrow \mu^\pm e^\mp) \lesssim 4.7 \times 10^{-12}, \text{BR}(B_{(s)} \rightarrow \ell_\alpha^\pm \ell_\beta^\mp) \lesssim \mathcal{O}(10^{-5})$
- ▶ cLFV @ higher energies:  $Z \rightarrow \ell_\alpha^\pm \ell_\beta^\mp, H \rightarrow \ell_\alpha^\pm \ell_\beta^\mp$ , high- $p_T$  di-lepton tails  $pp \rightarrow \ell_\alpha^\pm \ell_\beta^\mp$ ,  
 $\text{BR}(Z \rightarrow \ell_\alpha^\pm \ell_\beta^\mp) \lesssim \mathcal{O}(10^{-6})$

# cLFV observables across all sectors and energies

Any cLFV signal

► “Purely”

Mos

► Muonic

e.g. neutrino

► Semi-lept

(Semi-)

► cLFV @  
BR

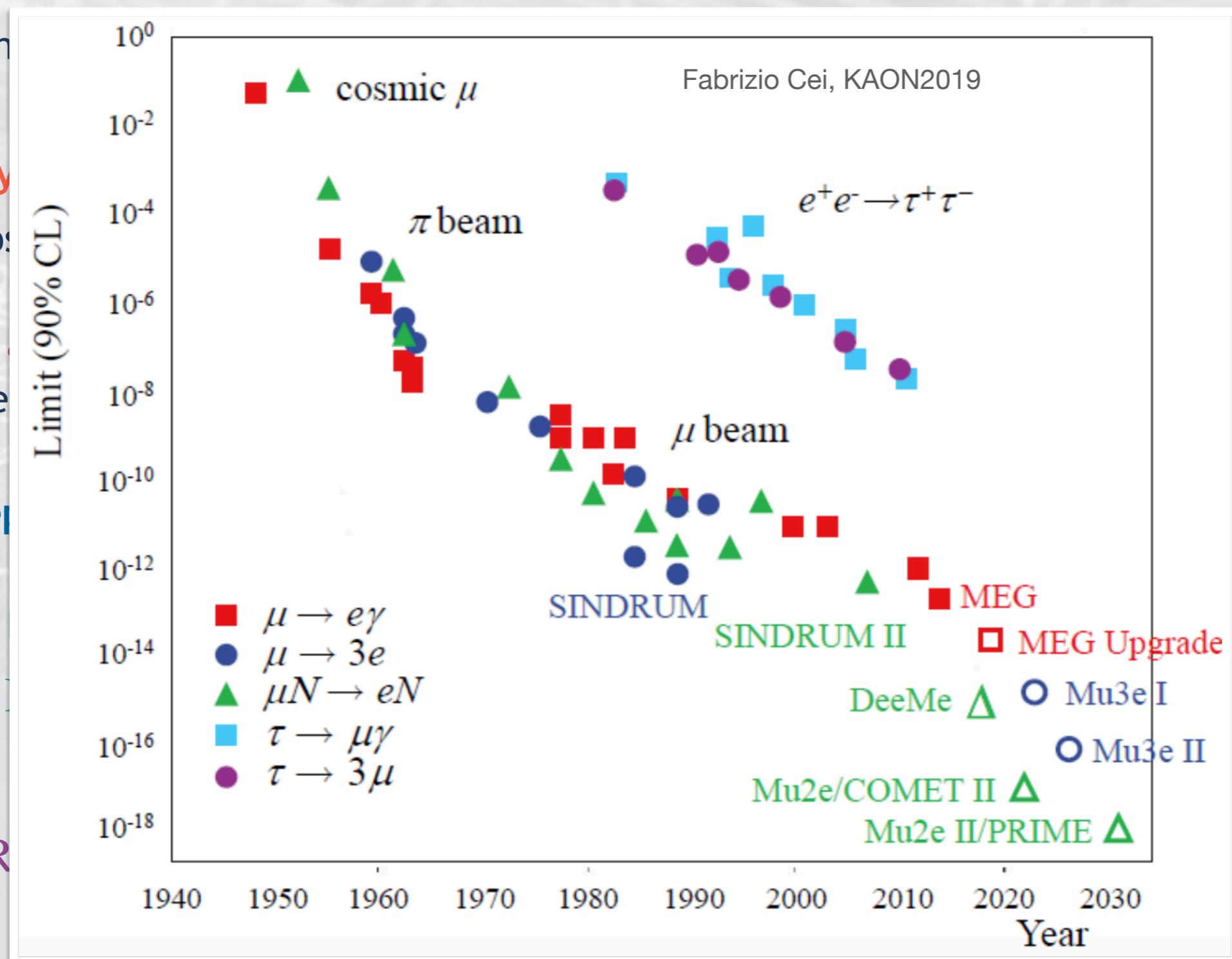
$e) \lesssim 10^{-12}$

es

$10^{-13}$

$10^{-8}$

$p \rightarrow \ell_\alpha^\pm \ell_\beta^\mp,$



# Low-scale seesaw

## Low-scale type I seesaw

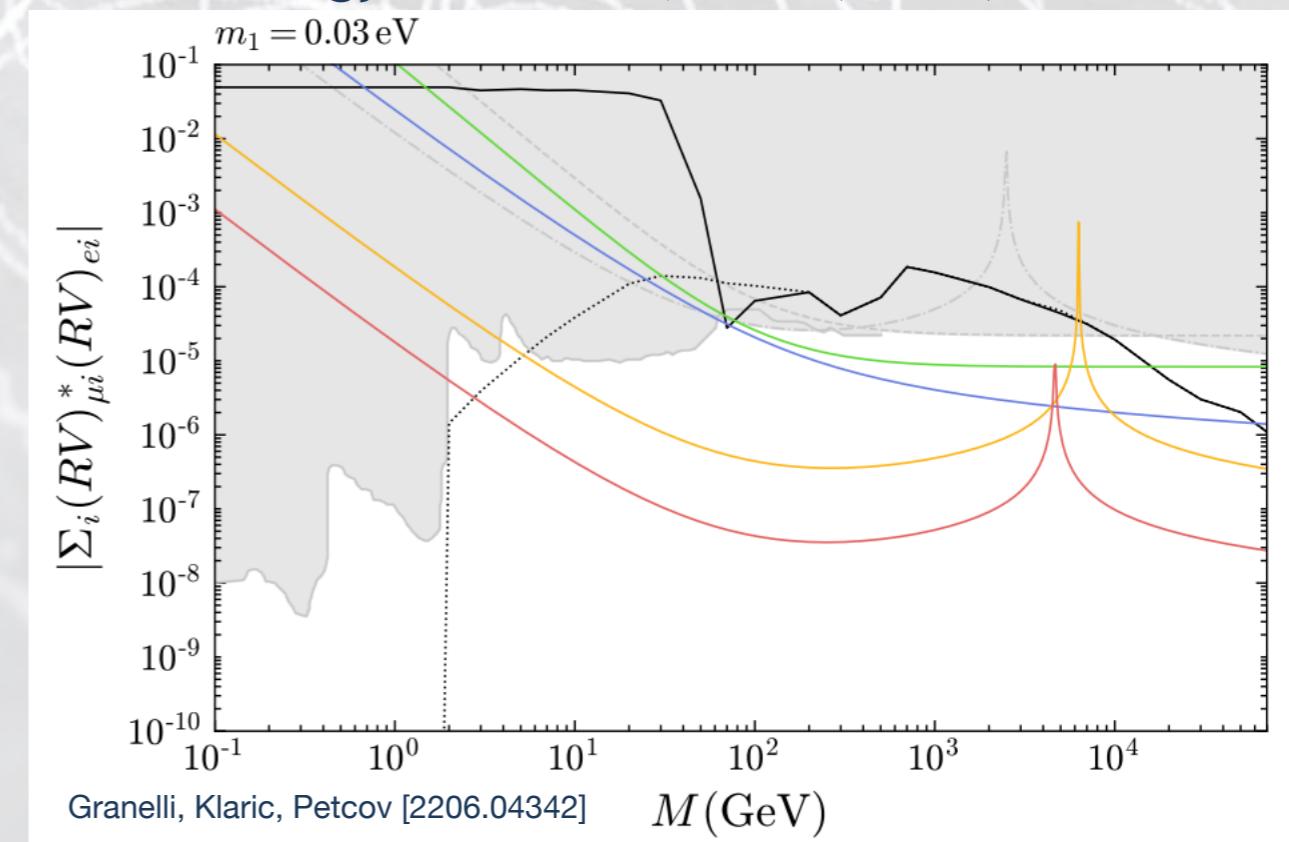
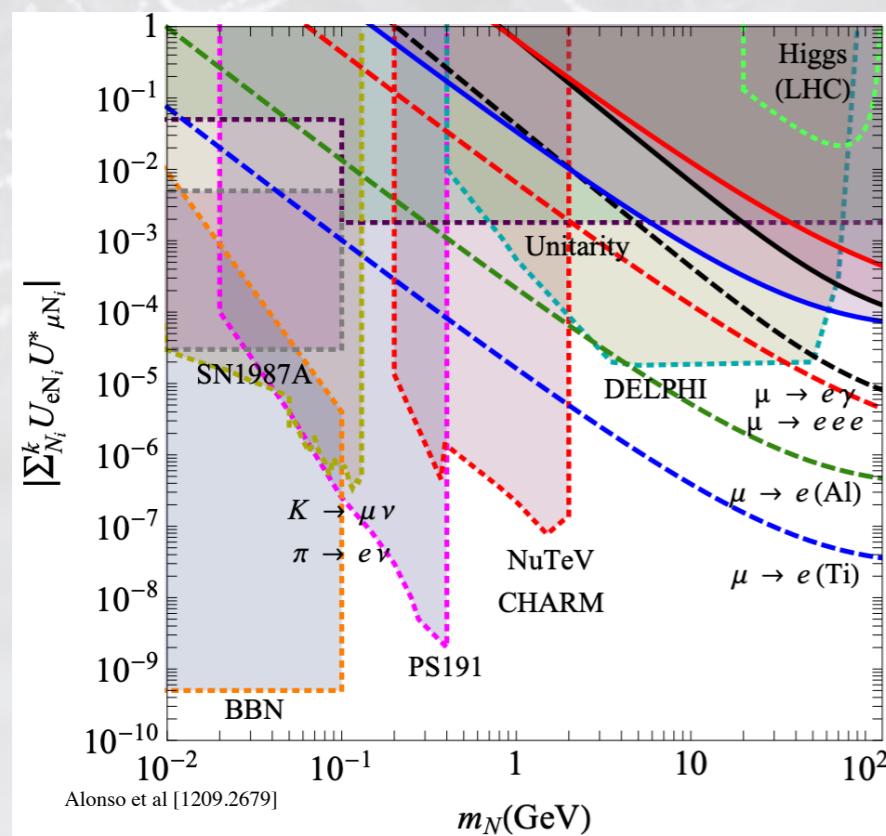
Extend SM with 3 “heavy” RH Majorana neutrinos:  $\text{MeV} \lesssim m_{N_i} \lesssim 1 - 100 \text{TeV}$

Masses and mixings:  $\mathbf{m}_\nu \simeq -v^2 Y_\nu^T \mathbf{M}_N^{-1} Y_\nu$ ,  $\mathcal{U}^T \mathcal{M}_\nu^{6 \times 6} \mathcal{U} = \text{diag}(m_i)$

$$U_{\nu N} \simeq Y_\nu^\dagger M_N^{-1} \quad \mathcal{U} = \begin{pmatrix} \mathbf{U}_{\nu\nu} & U_{\nu N} \\ U_{N\nu} & U_{NN} \end{pmatrix}, \quad \mathbf{U}_{\nu\nu} \simeq (1 - \eta) \mathbf{U}_{\text{PMNS}}$$

Heavy states not decoupled  $\Rightarrow$  neutral and charged lepton currents modified

$\Rightarrow$  very rich phenomenology: colliders, CLFV, LNV, ...

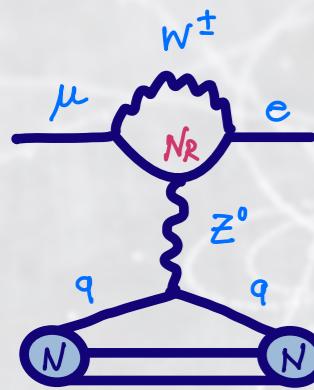


# The impact of CP violating phases – no more correlations

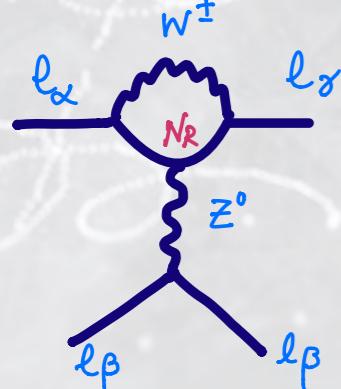
cLFV signatures: ratios of observables to identify mediators & constrain their masses!

But - CP violating phases do matter! And impact naïve expectations...

Consider "3+2" toy model (addition of 2 heavy sterile states; leptonic mixing  $\mathcal{U}_{5 \times 5}$ , CPV phases)

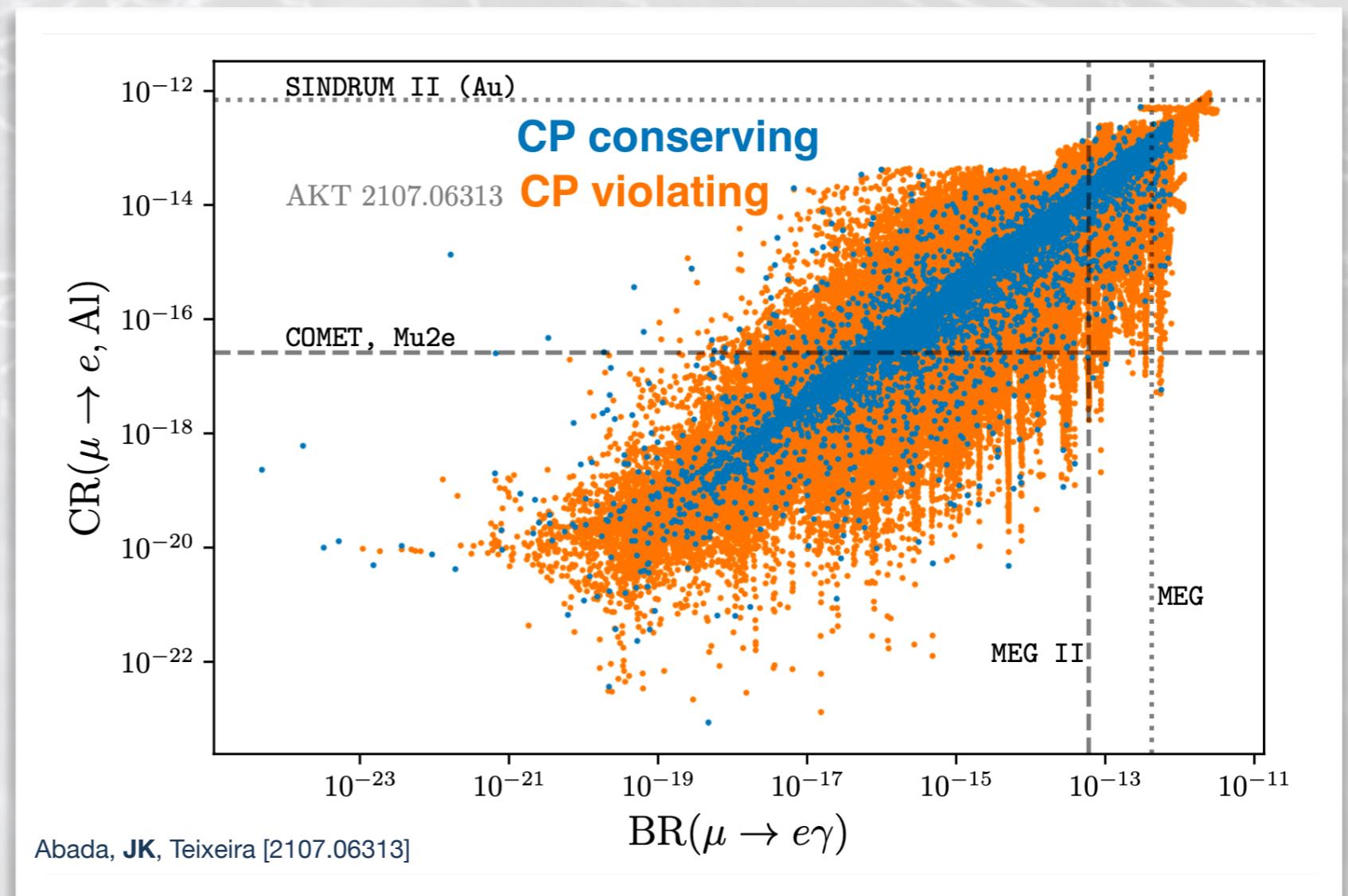


Observables dominated by common topology: Z-penguins



Also vary mass splitting,  
all angles/phases independently

⇒ Generic effect of CPV phases!

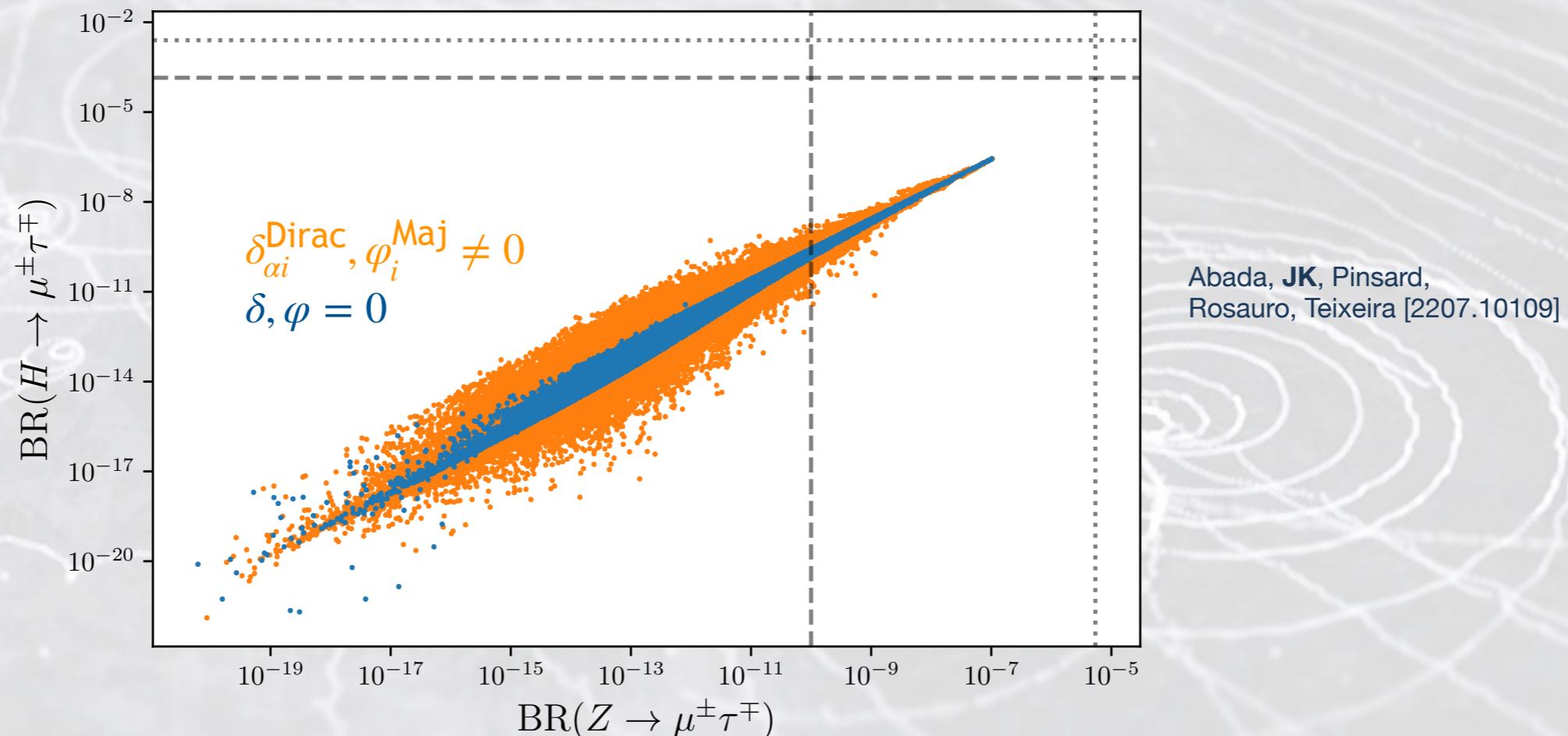


# cLFV: Z and Higgs

**cLFV processes:**  $H \rightarrow \ell_\alpha \ell_\beta$ ,  $Z \rightarrow \ell_\alpha \ell_\beta$  and **CPV Dirac / Majorana phases**

Consider "3+2" toy model (addition of 2 heavy sterile states; leptonic mixing  $\mathcal{U}_{5 \times 5}$ , **CPV phases**)

All angles & **CPV phases** randomly (independently) varied; non-degenerate heavy states (TeV)



→ Important contributions of **sterile fermions** to cLFV **Higgs** and **Z** decays!

( $H \rightarrow \mu\tau$  most promising, but still beyond "observation", even FCC-ee...)

→ Effect of **Majorana** and **Dirac** phases on cLFV rates: *constructive and destructive interferences*

Milder loss of correlation with respect to CP conserving case than **cLFV leptonic decays**

# The impact of CP violating phases – no more correlations

cLFV signatures: ratios of observables to identify mediators & constrain their masses!

But - CP violating phases do matter! And impact naïve expectations...

Some *illustrative benchmark points* - CP conserving ( $P_i$ ) and CPV variants ( $P'_i$ )

	BR( $\mu \rightarrow e\gamma$ )	BR( $\mu \rightarrow 3e$ )	CR( $\mu - e$ , Al)	BR( $\tau \rightarrow 3\mu$ )	BR( $Z \rightarrow \mu\tau$ )
$P_1$	$3 \times 10^{-16}$ ○	$1 \times 10^{-15}$ ✓	$9 \times 10^{-15}$ ✓	$2 \times 10^{-13}$ ○	$3 \times 10^{-12}$ ○
$P'_1$	$1 \times 10^{-13}$ ✓	$2 \times 10^{-14}$ ✓	$1 \times 10^{-16}$ ✓	$1 \times 10^{-10}$ ✓	$2 \times 10^{-9}$ ✓
$P_2$	$2 \times 10^{-23}$ ○	$2 \times 10^{-20}$ ○	$2 \times 10^{-19}$ ○	$1 \times 10^{-10}$ ✓	$3 \times 10^{-9}$ ✓
$P'_2$	$6 \times 10^{-14}$ ✓	$4 \times 10^{-14}$ ✓	$9 \times 10^{-14}$ ✓	$8 \times 10^{-11}$ ✓	$1 \times 10^{-9}$ ✓
$P_3$	$2 \times 10^{-11}$ ✗	$3 \times 10^{-10}$ ✗	$3 \times 10^{-9}$ ✗	$2 \times 10^{-8}$ ✓	$8 \times 10^{-7}$ ✓
$P'_3$	$8 \times 10^{-15}$ ○	$1 \times 10^{-14}$ ✓	$6 \times 10^{-14}$ ✓	$2 \times 10^{-9}$ ✓	$1 \times 10^{-8}$ ✓

Abada, JK, Teixeira [2107.06313]

→  $P_3$ : only cLFV  $\tau$  decays in allowed region; cLFV  $\mu$  transitions already experimentally disfavoured  
Regime of large mixing angles excluded?

$P'_3$ : all considered cLFV transitions currently allowed,  $\mu \rightarrow e\gamma$  beyond sensitivity!

(Non)-observation of cLFV observable(s) ⇒ not necessarily disfavour HNL extension!