



## JRA3-Precision Tests of the Standard Model

Anna Driutti  
(University and INFN Pisa)  
on behalf of JRA3 working group



STRONG-2020 ANNUAL MEETING

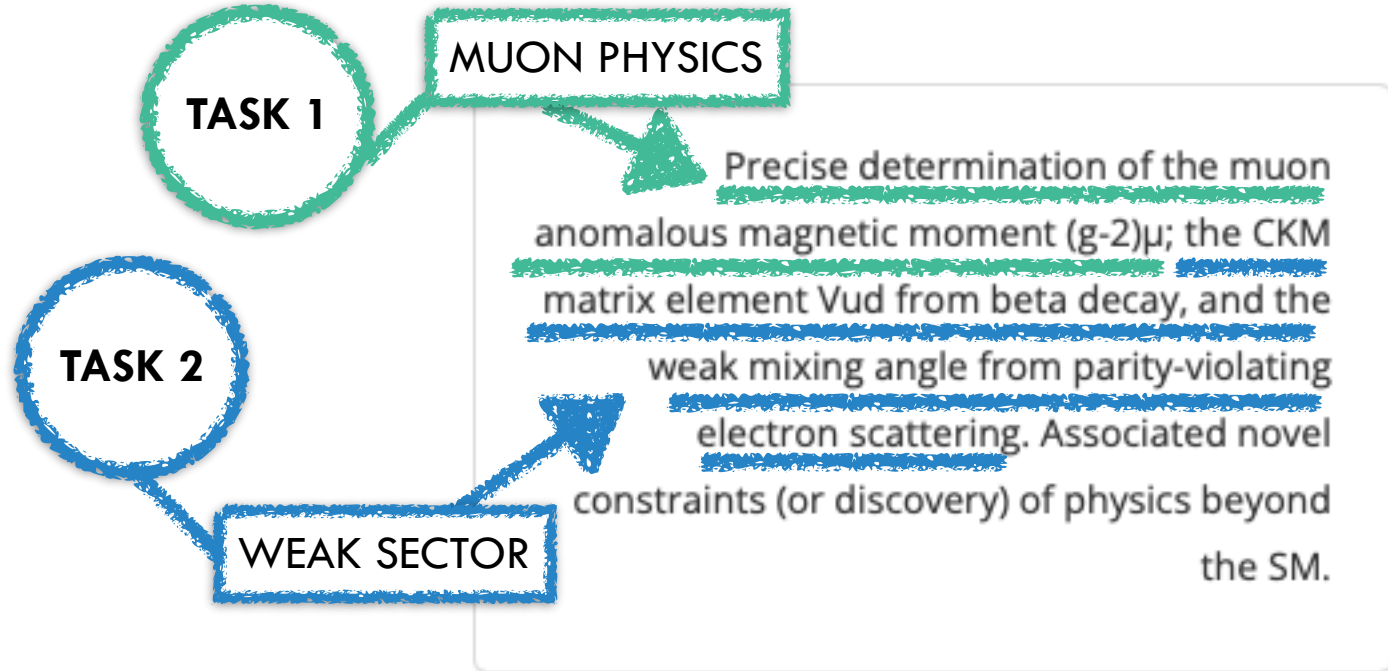
---

17, 18 and 19 October 2022, in Paris, France

# INTRODUCTION

## LOW ENERGY FRONTIER

comprises:



<http://www.strong-2020.eu>

Is part of

**JRA3-PrecisionSM**

Spokespersons:

- Andzrej Kupsc (UU)
- Mikhail Gorshteyn (JGU)
- Graziano Venanzoni (INFN)

Collaborators:

- Muon Sector ~ 20 people
- Weak Sector ~ 15 people

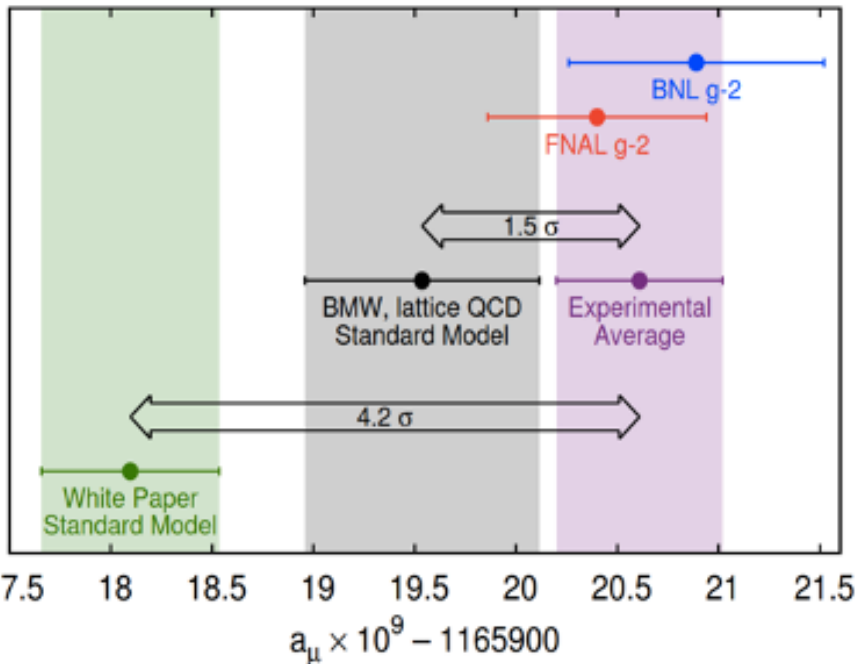
TASK 1

# Muon g-2 anomaly discrepancy

- **Muon:** elementary particle with spin-1/2 and magnetic moment proportional to spin through the **g-factor**:

$$\vec{\mu} = g \frac{q}{2m_{\mu}} \vec{S} \quad \Rightarrow \quad \boxed{a_{\mu} = \frac{g - 2}{2}} \quad \text{muon anomaly}$$

- ➔ Comparison between theoretical value and experimental measurement allows for a precise test of the Standard Model and to look for new physics



- New measurement from FNAL Muon g - 2 Exp. Run-1 data in 2021 confirmed result from BNL:

$$a_{\mu}(\text{FNAL}) = 116592040(54) \cdot 10^{-11} \text{ (460ppb)}$$

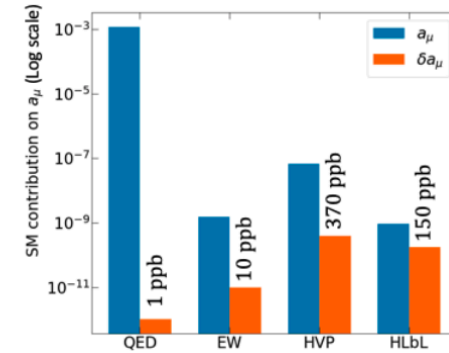
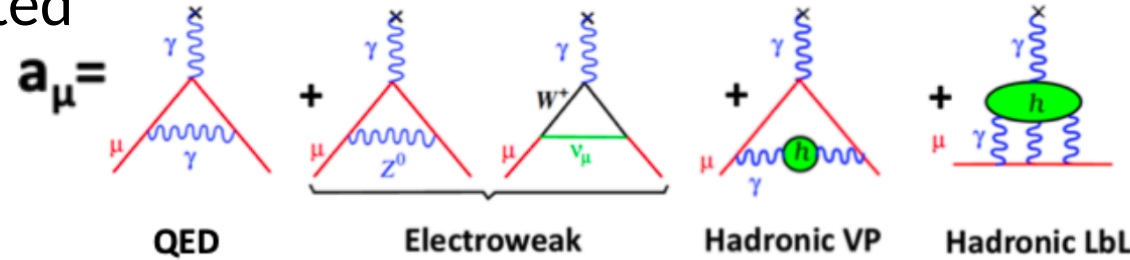
$$a_{\mu}(\text{BNL}) = 116592089(63) \cdot 10^{-11} \text{ (540 ppb)}$$

$$a_{\mu}(\text{Exp}) = 116592061(41) \cdot 10^{-11} \text{ (350 ppb)}$$

- Theory:
  - $a_{\mu}(\text{BMW, SM})$  calculation with LatticeQCD
  - $a_{\mu}(\text{WP, SM})$  calculation recommended by the Theory Initiative based on  $e^+e^-$  data

# Muon g-2 theoretical calculation

- Calculation is continuously updated
- Largest contribution but lowest uncertainty from QED
- EW terms are also well known
- Uncertainty dominated by QCD contributions:



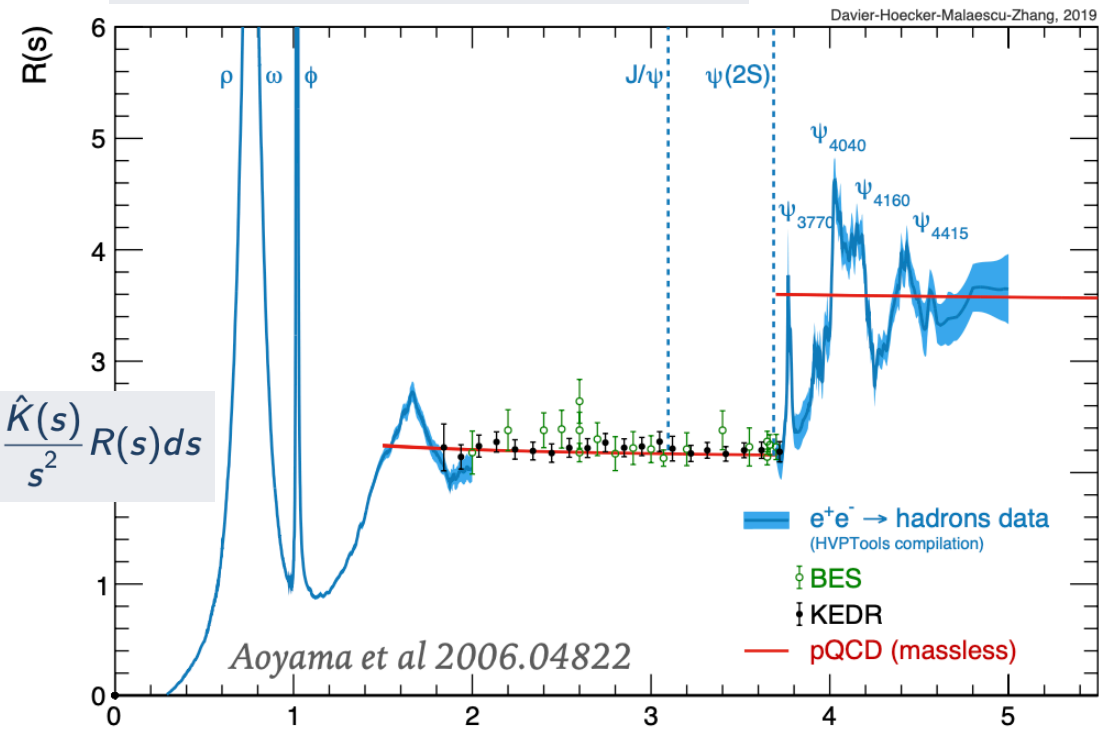
- mainly from **Leading Order Hadronic Vacuum Polarization**: virtual loops with hadrons calculated with two approaches:

- **data-driven**: experimental data plus dispersion theory (used by WP20)

$$a_\mu^{\text{HVP,LO}} = \left(\frac{\alpha m_\mu}{3\pi}\right)^2 \int_{m_\pi^2}^{\infty} \frac{\hat{K}(s)}{s^2} R(s) ds$$

- direct calculation with **latticeQCD**: recent result (BMW20) in tension with data-driven HVP

$$R(s) = \frac{\sigma^0(e^+e^- \rightarrow \text{hadrons}(\gamma))(s)}{\sigma^0(e^+e^- \rightarrow \mu^+\mu^-(\gamma))(s)}$$



# Precision SM Activities for Muon g-2

- **Goal:** compile an annotated database for low-energy hadronic cross sections in  $e^+e^-$  collisions

- **Activities:**

- collect in **HEPDATA** low energy hadronic cross-section measurements

- HEP data public storage web site with well defined submission data format
- Submissions done only by authorized contact persons of collaborations

The screenshot shows the HEPData website interface. The main content area displays a table titled "Table 1" with the following data:

RE	E+ E- -> Pi+ Pi-
SQRT(S)	0.705-0.99 GeV
SQRT(S) [GEV]	SIG [MUB]
0.705	0.77 ±0.08
0.758	1.09 ±0.11
0.7714	1.12 ±0.1
0.7777	1.22 ±0.1
0.784	1.02 ±0.07
0.7903	0.73 ±0.06
0.7967	0.69 ±0.1
0.8099	0.62 ±0.08

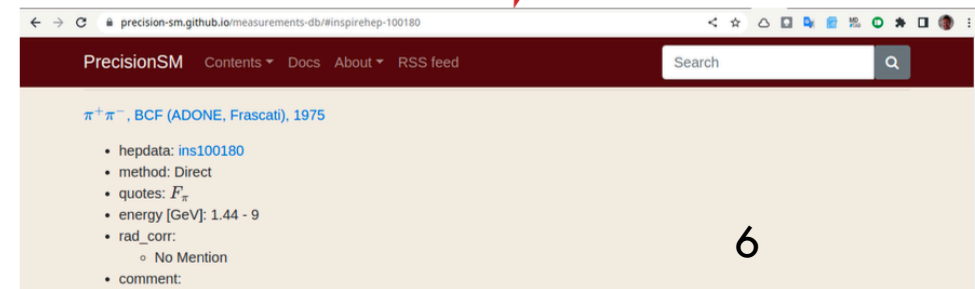
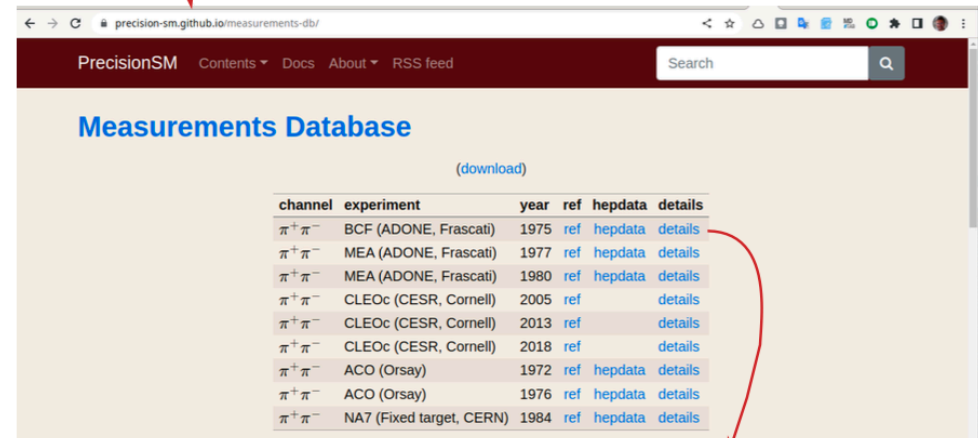
Below the table, there is a "Visualize" section showing a plot of the cross-section data with error bars. The plot title is "Visualize" and the x-axis is labeled "SQRT(S) [GEV]". The y-axis ranges from 0.4 to 1.3. The plot shows a peak around 0.77 GeV. There are also checkboxes for "Sum errors" and "Log Scale (X)".

# Precision SM Activities for Muon g-2

- **Goal:** compile an annotated database for low-energy hadronic cross sections in  $e^+e^-$  collisions

- **Activities:**

- collect in [HEPDATA](#) low energy hadronic cross-section measurements
- maintain annotated database of hadronic cross-section measurements for computation of the LO HVP contribution to  $a_\mu$  on [dedicated web site](#), with hyperlinks



# Precision SM Activities for Muon g-2

- **Goal:** compile an annotated database for low-energy hadronic cross sections in  $e^+e^-$  collisions

- **Activities:**

- collect in [HEPDATA](#) low energy hadronic cross-section measurements
- maintain annotated database of hadronic cross-section measurements for computation of the LO HVP contribution to  $a_\mu$  on dedicated web site, with hyperlinks

- document, with examples, how to use measurements stored in HEPDATA

- responsive plots of measurements of hadronic cross-sections

The screenshot shows a Jupyter Notebook interface with the following content:

**Prepare Root Plot with data from HEPData**  
PrecisionSM Group — 2020-11-21 01:05

get two cross-section measurements from HEPData and plot them

- $e^+e^- \rightarrow \pi^+\pi^-$  BES-III 2016 <https://www.hepdata.net/record/ins1385603>
- $e^+e^- \rightarrow \pi^+\pi^-$  CMD-2 2007 <https://www.hepdata.net/record/ins728302>

```
In [1]: from math import *
import re
from pprint import pprint
import urllib.request
from requests.utils import re
from array import array
import json
import yaml
import itertools
import ROOT
from ROOT import TCanvas, TF1
from ROOT import TGraph, TGraphAsymmErr
from ROOT import gROOT, gBench
```

Welcome to JupyterROOT 6.22/08

```
In [2]: ##
## iterator generator using o
## - first list is inner and
## - also able to return nth
## - iterator never ends
##
class Iterator:
def __init__(self, arr1, arr2):
self.arr1 = arr1
self.arr2 = arr2
def __iter__(self):
self.i1 = 0
self.i2 = 0
return self
```

**Example responsive plot**  
Hovering the cursor above the points reveals the respective x and y values.

The plot shows the squared pion form factor  $|F_\pi|^2$  as a function of the center-of-mass energy  $\sqrt{s}$  in GeV. The x-axis ranges from 0.5 to 1.0 GeV, and the y-axis ranges from 0 to 50. Two data series are plotted: BESIII 2016 (blue circles) and CMD-2 2007 (orange squares). Both series show a prominent resonance peak centered at approximately 0.77 GeV, with a maximum value of about 45. The plot is interactive, allowing users to hover over data points to see their coordinates.



# Status, Next Steps & Workshops

## ● Status:

- Defined procedure and completed infrastructure for the database
- In completion: collection in HEPDATA and annotation on the web site of the  $e^+e^- \rightarrow \pi^+\pi^-$  channel

## ● Next Steps:

- Add the other  $e^+e^- \rightarrow \text{hadrons}$  channels

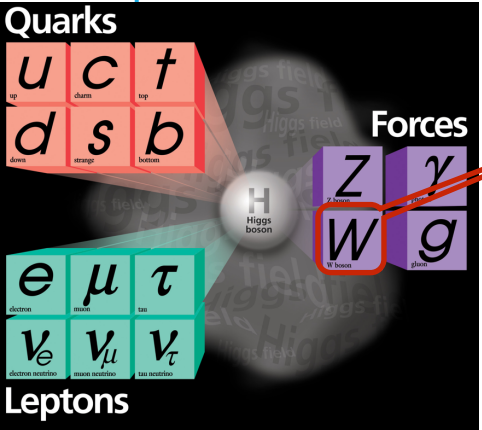
## ● Workshop:

- STRONG 2020 Virtual Workshop on "[Spacelike and Timelike determination of the Hadronic Leading Order contribution to the Muon g-2](#)" [Nov 24 - 27, 2021]
  - book of abstracts submitted to ArXiv [[arXiv:2201.12102](#)]



TASK 2

# Top-Row CKM unitarity anomaly



Charged current interaction -  $\beta$ -decay

$$\mu \rightarrow e + \nu_{\mu} + \bar{\nu}_e, \quad n \rightarrow p + e + \bar{\nu}_e, \quad \pi^{\pm} \rightarrow \mu^{\pm} + \nu_{\mu}/\bar{\nu}_{\mu}$$

Universality of weak interaction:

Same strength in lepton and quark sector

Quark mixing: strength distributed among 3 generations

CKM unitarity - measure of completeness of the

SM:

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix} = V_{CKM} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1$$

**PDG2020: CKM unitarity in the top row**  $|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 0.9985(3)_{V_{ud}}(4)_{V_{us}} - 3\sigma$  deficit

Within this JRA: CKM unitarity anomaly established and sharpened

Methods for new-era high-precision SM calculations developed and applied

# Top-Row CKM unitarity anomaly: Confirmed and Sharpened

Main source: reevaluation of the  $\gamma W$ -box

Bottleneck for precision improvement since 40 years

Major improvement (factor 2) due to new framework

## Dispersion relations (DR) for EW boxes

C-Y Seng, MG et al., Phys.Rev.Lett. 121 (2018) 24, 241804;

C-Y Seng, MG, M.J. Ramsey-Musolf, Phys.Rev. D 100 (2019) 1, 013001

## DR representation of nuclear corrections

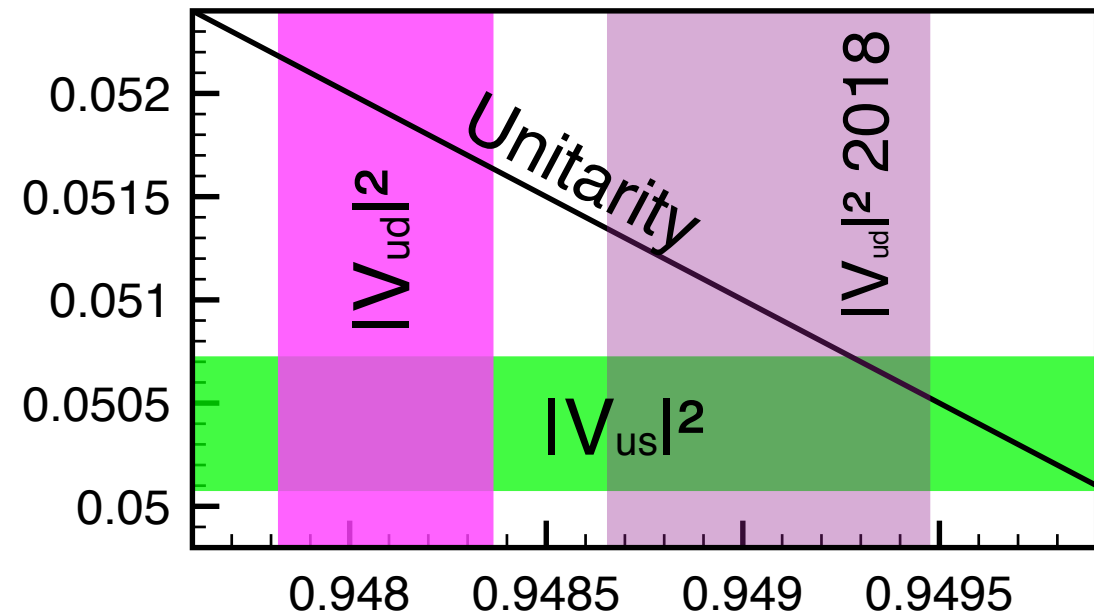
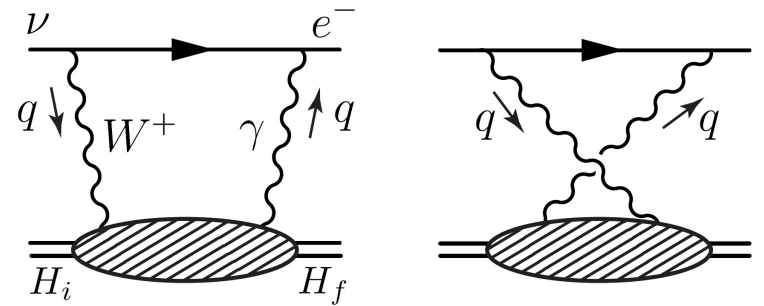
C-Y Seng, MG, M.J. Ramsey-Musolf, Phys.Rev. D 100 (2019) 1, 013001;

MG, Phys.Rev.Lett. 123 (2019) 4, 042503;

## Combined DR + lattice QCD + phenomenology

X. Feng, MG et al, Phys.Rev.Lett. 124 (2020) 19, 192002

C-Y Seng, X. Feng, MG, L-C Jin, Phys.Rev. D 101 (2020) 11, 111301;



# Top-Row CKM unitarity anomaly: Confirmed and Sharpened

The framework further applied to

## Dispersion analysis of radiative corrections to $g_A$ for neutron $\beta$ decay

MG, C-Y Seng, JHEP 10 (2021) 053

Important for: extracting  $V_{ud}$  from neutron decay;  
comparing  $g_A$  from experiment and lattice QCD

## Combined DR + lattice QCD + ChPT for RC to semileptonic kaon decays

C-Y Seng, X. Feng, MG, L-C Jin, U.-G. Meißner, JHEP 10 (2020) 179

P.-X. Ma, X. Feng, MG, L-C Jin, C-Y Seng, PRD 103 (2021) 114503

C-Y Seng, D. Galviz, MG, U.-G. Meißner, PLB 820 (2021) 136522

C-Y Seng, D. Galviz, MG, U.-G. Meißner, 2103.04843

Important for: extracting  $V_{us}$  from  $Kl3$  decays;  
establishing the  $Kl2-Kl3$  discrepancy

**Complete change of landscape in SM tests with CKM unitarity in the past 2 years**

**New method developed; wide range of applications to previously inaccessible corrections**

# Next Steps: Nuclear Corrections

## Dispersion analysis of the nuclear structure correction $\delta_{NS}$ to $V_{ud}$

Collaboration with the group of S. Pastore (Green-Function Monte Carlo ) and P. Navratil (No-Core Shell Model) started

## Data-driven analysis of the isospin-symmetry breaking correction $\delta_C$ to $V_{ud}$

Seng, MG, arXiv: 2208.03037 [nucl-th]

## Proposal for next-generation rare pion decay experiment PIONEER

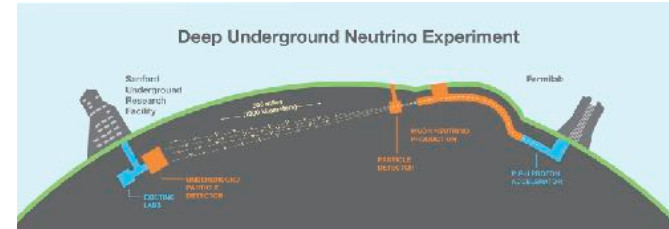
PSI Ring Cyclotron Proposal R-22-01.1 [PIONEER Collaboration] Altmannshofer et al., arXiv: 2203.01981 [hep-ex]

**Full involvement in shaping the future of CKM unitarity**

# WeakMAID: pion production with neutrinos

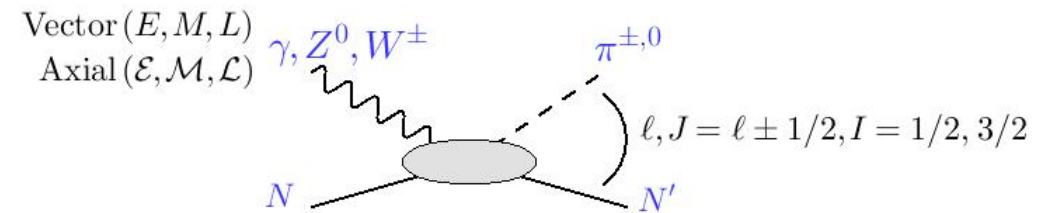
## Motivation:

Neutrino energy reconstruction for neutrino oscillation experiments (DUNE, T2HK)  
 Inelastic neutrino scattering in the near detector, with pion production an important channel, is used as a tool to calibrate the flux of neutrinos in each energy bin to ensure a high-precision determination of neutrino oscillation parameters (masses, angles, phases).



## Method and Background:

Mainz-based partial-wave analysis MAID is a leading player in the field of electromagnetic pion production. MAID is a unitarized isobar model that accounts for all known  $N^*$  and  $\Delta$  resonances. MAID's range of validity  $W \leq 2.5$  GeV needs to be extended to 5-6 GeV to cover DUNE's needs. Axial current contribution has to be added.



## Realization:

WeakMAID is based on the decomposition of scattering amplitudes for weak pion production into multipoles characterized by angular momentum  $l$ , total spin  $J=l\pm 1/2$ , isospin  $I=1/2, 3/2$ , multipolarity (electric E, magnetic M, and longitudinal L) carried by the electroweak probe. Each multipole is unitarized to account for strong rescattering at low energies, and matched with Regge behavior at high energies. **These two features are new among the existing weak pion production models.**

- Home
- Research
- People
- Publications
- Teaching
- Events
- Press and Media



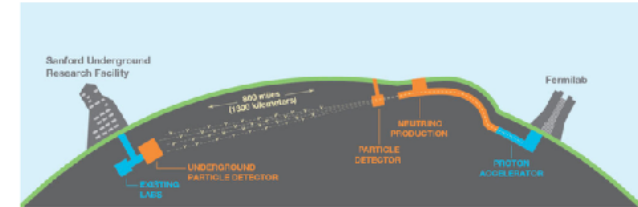
**WeakMAID**

**Dual Unitary Isobar-Regge Model for Pion Neutrino-Production**

Mikhail Gorshteyn, Institut für Kernphysik, Johannes-Gutenberg Universität Mainz

**Motivation**

Long base neutrino oscillation experiments, such as **DUNE**, aim at determining neutrino masses and mixing parameters at an unprecedented level of precision. Born from charged pions decaying in flight, by the time they reach the far detector 1300 km away, the muon neutrinos will oscillate to electron or tau ones. To unravel the oscillation pattern, the energy of the neutrino beam has to be known to a good precision. For this purpose, close enough to the neutrino source - where no oscillation has occurred yet - the near detector is placed to study neutrino interactions with matter. An important mechanism in these interactions is the production of pions. This project is dedicated to developing a state-of-the-art theoretical analysis for weak pion production on the nucleon. Embedded in Monte Carlo simulation codes, it will lead to precise predictions of pion counts in the near detector, resulting in a reliable neutrino energy reconstruction.



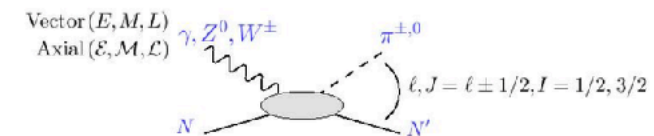
**Method and Background**

Pion production in electromagnetic reactions has a long history. One of the leading efforts is due to the Mainz-based partial wave analysis tool **MAID**, a unitary isobar model that accounts for all known  $N^*$  and  $\Delta$  resonances, single-channel unitarity and over years has proven to be a valuable analysis tool for pion photo- and electroproduction. At present, MAID is further developed by the **Mainz-Tuzla-Zagreb Collaboration**.

MAID approach is suitable for the invariant mass of the  $\pi N$  system  $W < 2$  GeV and moderate photon virtualities. The project WeakMAID builds upon its predecessor while extending it in several ways. Firstly, weak interaction contains the axial current, additionally to the vector current; readily contained in the electromagnetic case. Secondly, the energy spectrum of neutrinos at DUNE extends to 5-6 GeV, so that a connection to high energy such as Regge theory is necessary. This can be correctly done by implementing **unitarity, analyticity and duality constraints**.

**Realization**

As a partial wave analysis (PWA) tool, WeakMAID is based on the decomposition of scattering amplitudes for weak pion production into multipoles characterized by the angular momentum  $l$ , total spin  $J = l \pm 1/2$ , total isospin  $I = 1/2, 3/2$  of the  $\pi N$ -system, as well as the multipolarity (electric  $E$ , magnetic  $M$ , and longitudinal  $L$ ) carried by the electro-weak probe. Two sets of multipoles describe the interaction with the hadronic vector and axial current. Additionally, two sets of invariant amplitudes  $V1-6$  for vector and  $A1-6$  for axial current are introduced, as well as center-of-mass CGLN  $F1-6$  and  $G1-6$ , respectively, and helicity amplitudes  $H1-6$ .



Vector Weak Multipoles ( $E\ell, M\ell, L\ell$ )
Vector Amplitudes ( $F1-6, V1-6, H1-6$ )
Axial Weak Multipoles ( $E\ell, M\ell, L\ell$ )

## Website WeakMAID created

<https://wwwth.kph.uni-mainz.de/weakmaid/>

Users can download tables with multipoles, amplitudes as functions of energy,  $Q^2$ , angle, and integrated cross sections as functions of  $Q^2$ . At present website being tested, journal publication in preparation. As per MAID collaboration policies: once published and tests concluded WeakMAID will be added to official MAID website

## Next Steps

Upon completion of WeakMAID the work on incorporating WeakMAID into MC neutrino events simulators will commence.

## Involvement in shaping DUNE program:

- Two Snowmass White Papers submitted:
- L. Alvarez-Ruso et al, arXiv: 2203.11298 [nucl-ex]
- L. Alvarez-Ruso et al, arXiv: 2203.11319 [physics.ins-det]

# REQUESTED ADJUSTMENTS



## TASK 1

Travels were limited (COVID) for the entire duration of the project

Visits to Fermilab were impossible (COVID) for the entire duration of the project

Until now this impediment was unpleasant but not critical.



## TASK 2

The next step envisions the incorporation of the WeakMAID analysis into MC simulators for which a close collaboration with local researchers at Fermilab is crucial.

**A cost-neutral 1-year extension is desired.**

# CONCLUSIONS

Precision tests of the Standard Model require collection, sophisticated analysis and elaboration of large number measurement:

Within the Strong2020 PrecisionSM project we are:

- assembling an annotated database of hadronic cross-section measurements with a web site that also documents how to use the data
- working on reduce uncertainties on EW boxes calculation for precise calculations of the CKM unitarity
- implementing tools to study the pion production with neutrinos

