

Towards a complete L0-L2 pipeline

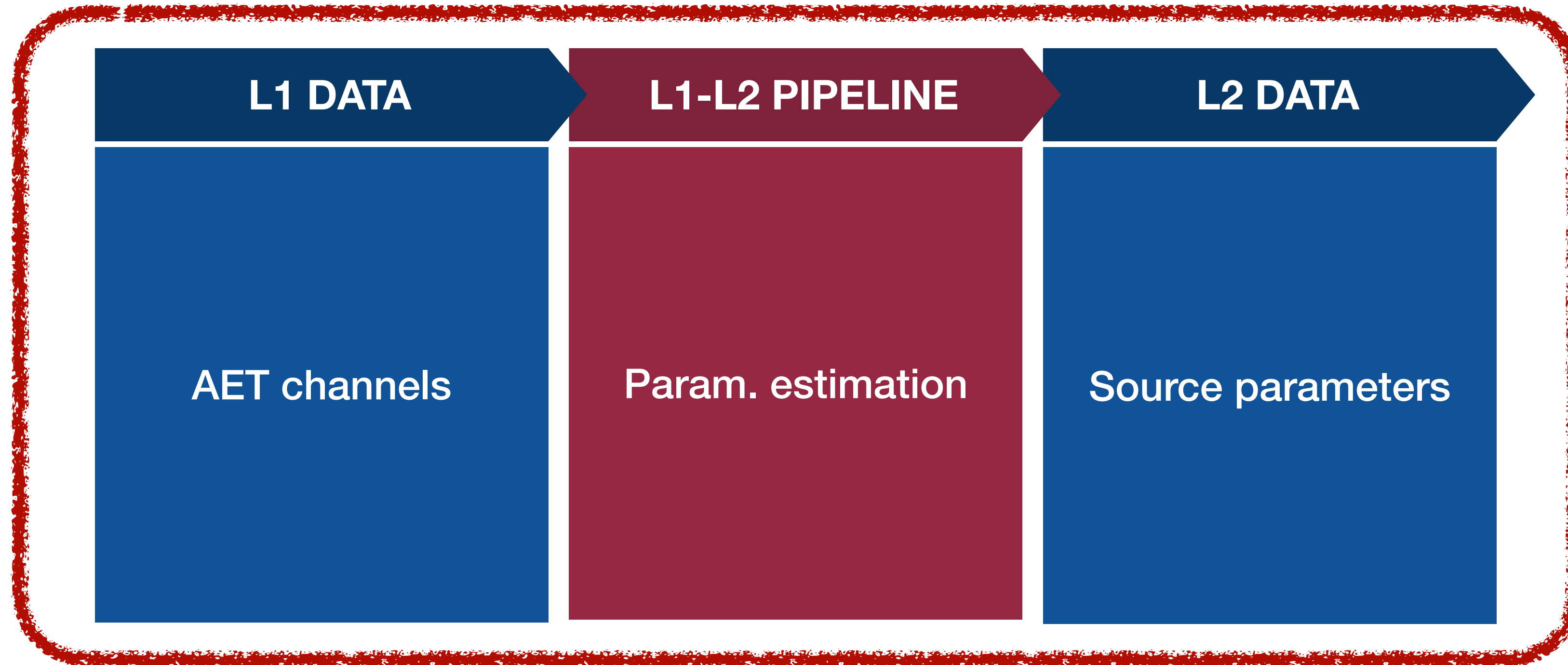
Progress in simulation, processing and analysis

SYRTE |  Observatoire
de Paris | PSL 

 University
of Glasgow

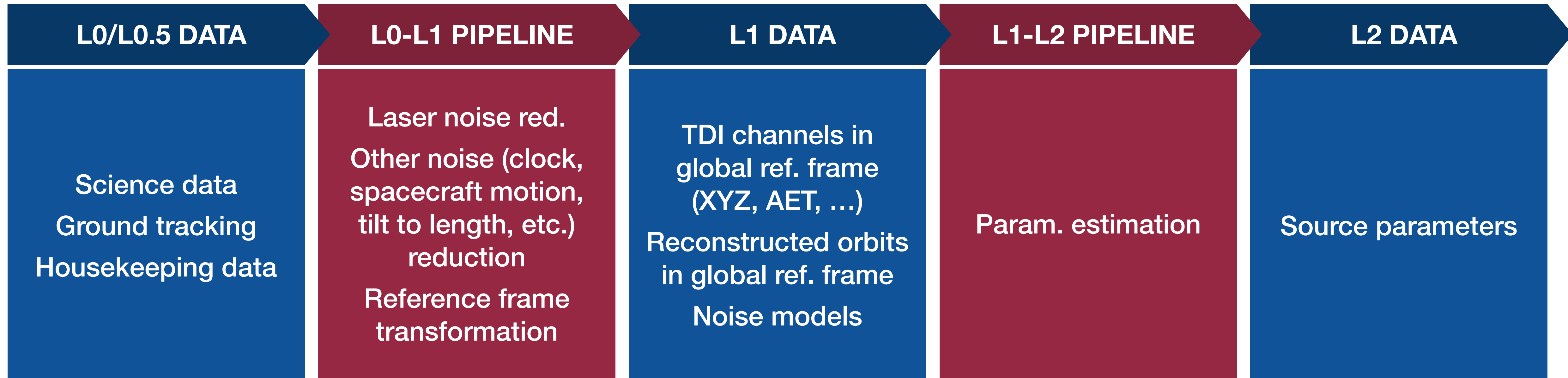
Jean-Baptiste Bayle and Olaf Hartwig – 2022 LIDA (Toulouse)

LISA Data Analysis Pipeline

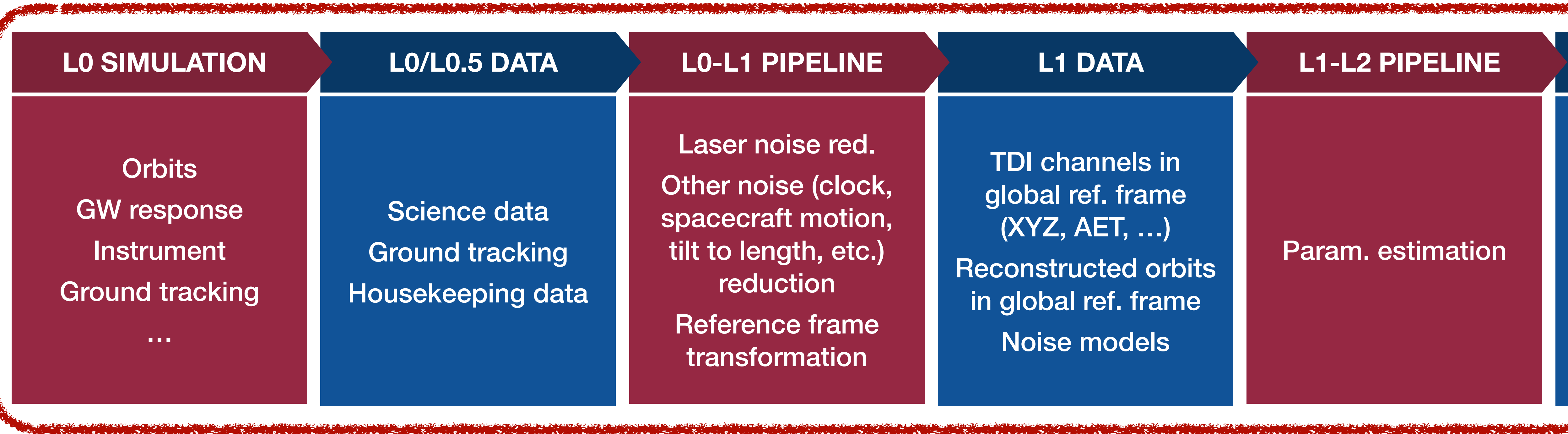


LDC

LISA Data Analysis Pipeline



LISA Data Analysis Pipeline



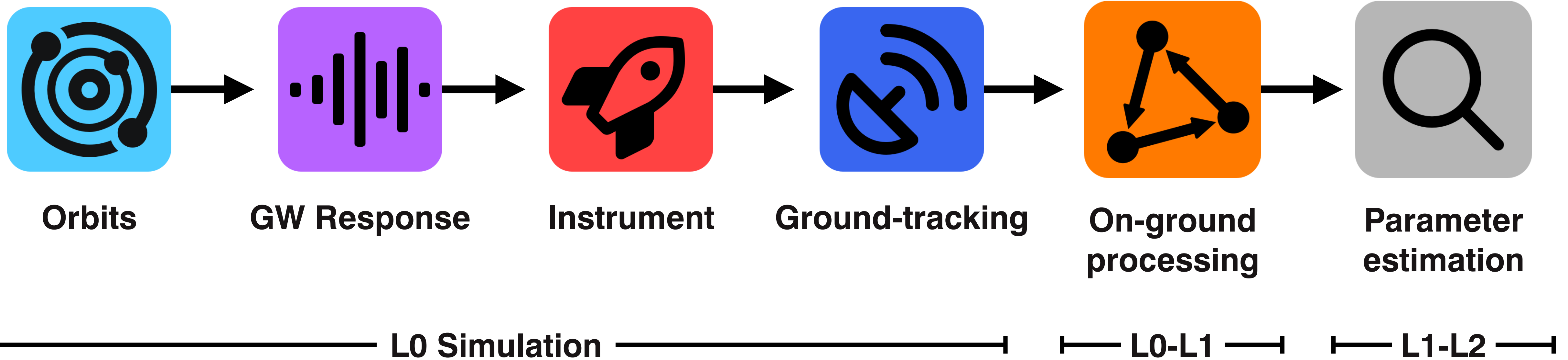
L0-L2 DEMONSTRATION PIPELINE

Context

- **Activity requested by ESA & LISA Consortium**
 - FMT Task 4.5 started only a few months ago
 - Preparation for mission adoption over summer 2023
 - Deliverables are a demonstration pipeline and some figures of merits (Before june?)
- **Participants**
 - University of Glasgow (Jean-Baptiste Bayle, Christian Chapman-Bird, Graham Wohlan)
 - SYRTE (Olaf Hartwig, Aurelien Hees, Marc Lilley, Peter Wolf)

Method

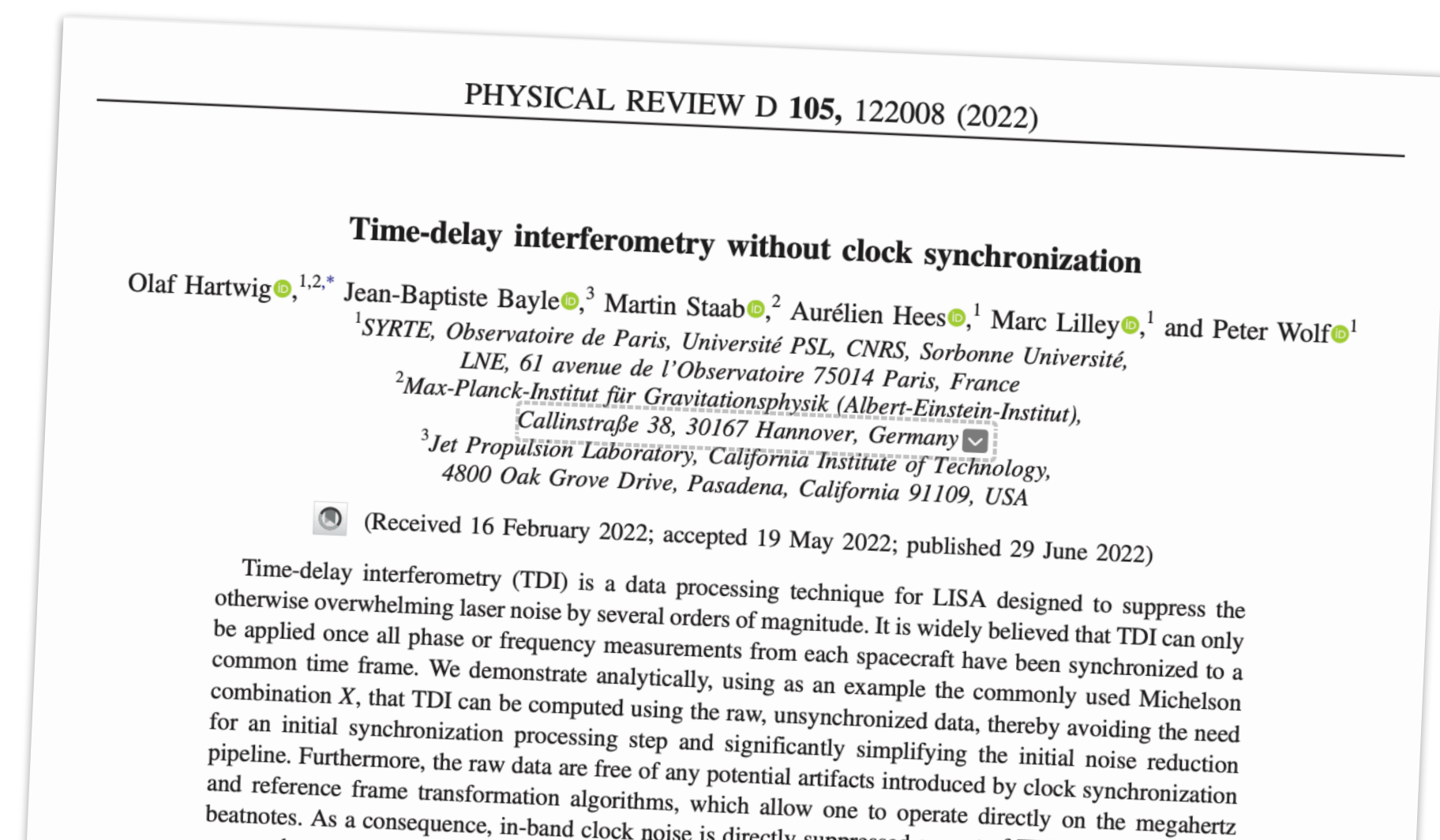
- Build a pipeline with various processing blocks



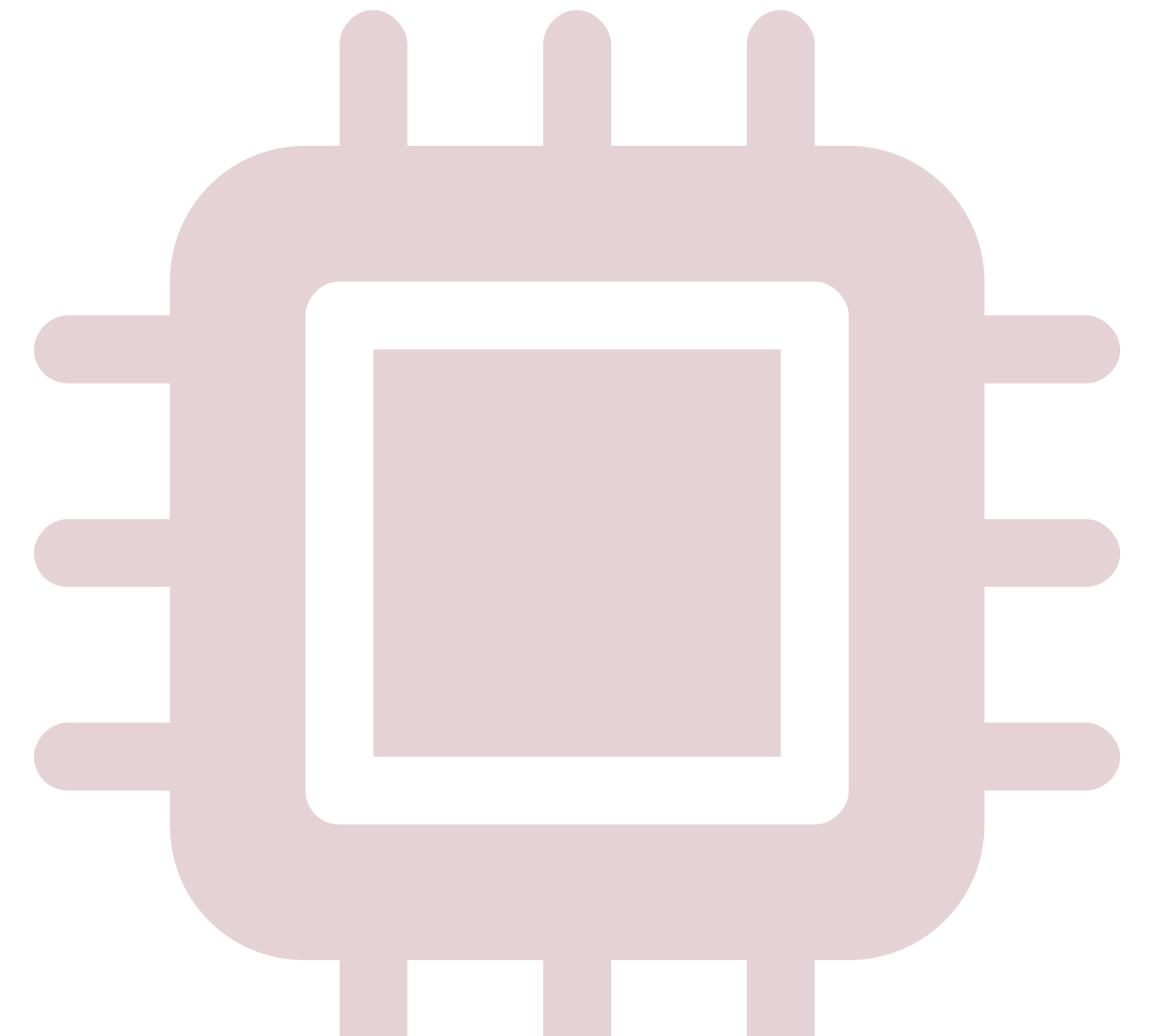
- Assemble the blocks and builds performance metrics

Method

- Processing blocks exist in multiple versions (various configurations)
 - Start with simplified configurations
 - Increase model faithfulness (and processing accordingly) and assess metric variations
- Short timeframe, so restrict the activity to
 - Rather simple target configuration
 - ▶ Well separated loud Galactic binary sources
 - ▶ Current best simulation model of the instrument
 - ▶ Processing derived from [10.1103/PhysRevD.105.122008](https://arxiv.org/abs/10.1103/PhysRevD.105.122008)
 - ▶ Parameter estimation based on LDC
 - Identify impactful effects (and try to mitigate them?)

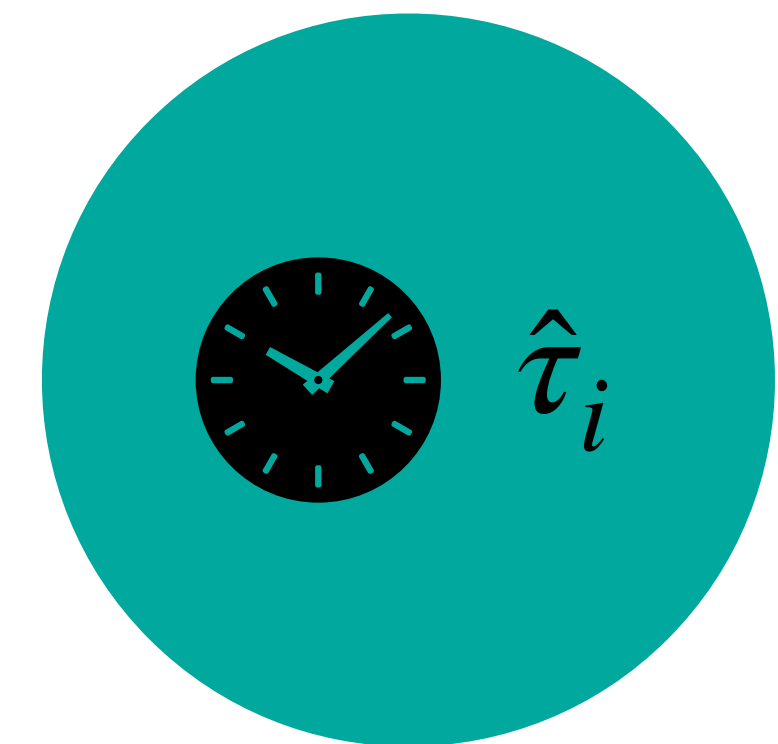
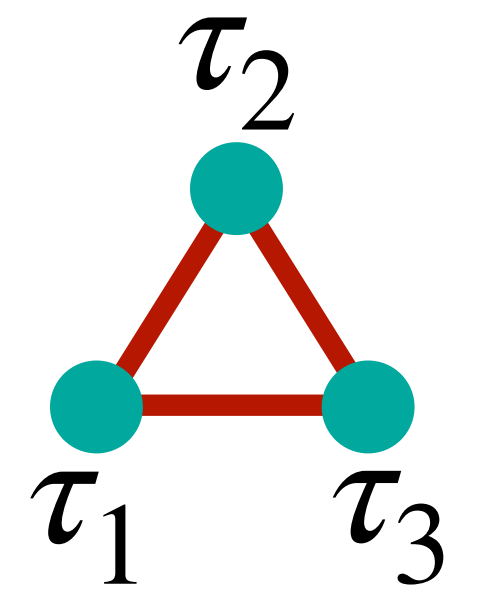
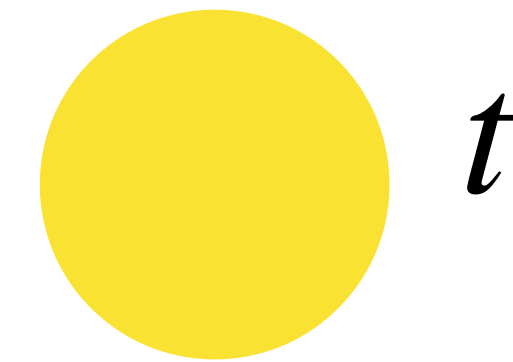


L0 Simulation



Timescales

- **Global TCB time t**
 - Defined as time shown of a perfect clock sitting at Solar system barycenter
 - Global timescale, used for orbits and GW strain
- **One proper time τ_i for each spacecraft i ($i = 1,2,3$)**
 - Defined as time shown by a *perfect* clock sitting in spacecraft i
 - Related to t (and each other) by General Relativity
 - Used to describe physics inside one spacecraft
- **One onboard clock time $\hat{\tau}_i$ for each spacecraft i ($i = 1,2,3$)**
 - Defined as time shown by the *actual* clock sitting in spacecraft
 - Differs from τ_i by instrumental imperfections
 - Only timescales directly accessible by the satellites

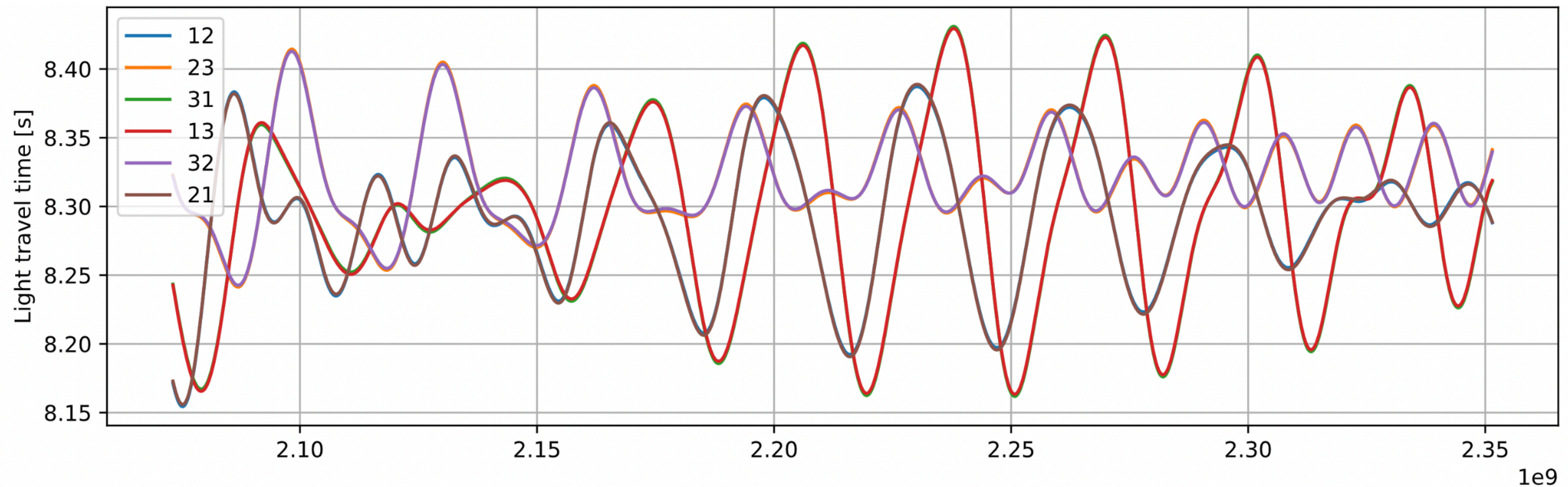


Orbits

- Use ESA numerically optimized orbits
- Interpolate spacecraft state vectors and compute necessary quantities (e.g., light travel times and relativistic relationships between reference frames) with



Bayle, Jean-Baptiste, Hees, Aurélien, Lilley, Marc, & Le Poncin-Lafitte, Christophe. (2022). LISA Orbits (2.0). Zenodo. <https://doi.org/10.5281/zenodo.6412992>



GW Response

- Compute frequency shift due to gravitational waves measured on each optical bench (link responses) in the spacecraft proper time frames with



Bayle, Jean-Baptiste, Baghi, Quentin, Renzini, Arianna, & Le Jeune, Maude. (2022). LISA GW Response (1.1). Zenodo. <https://doi.org/10.5281/zenodo.6423436>

- Model fully described in documentation

- Deformation induced on link 12 is $H_{12}(t) = h_{+}^{\text{SSB}}(t)\xi_{+}(\hat{\mathbf{u}}, \hat{\mathbf{v}}, \hat{\mathbf{n}}_{12}) + h_{\times}^{\text{SSB}}(t)\xi_{\times}(\hat{\mathbf{u}}, \hat{\mathbf{v}}, \hat{\mathbf{n}}_{12})$
- Reception time t_1 of a photon emitted at t_2 is $t_1 \approx t_2 + \frac{L_{12}}{c} - \frac{1}{2c} \int_0^{L_{12}} H_{12}(\mathbf{x}(\lambda), t(\lambda)) d\lambda$
- We substitute and differentiate to obtain the frequency shift

$$y_{12}(t_1) \approx \frac{1}{2(1 - \hat{\mathbf{k}} \cdot \hat{\mathbf{n}}_{12}(t_1))} \left[H_{12} \left(t_1 - \frac{L_{12}(t_1)}{c} - \frac{\hat{\mathbf{k}} \cdot \mathbf{x}_2(t_1)}{c} \right) - H_{12} \left(t_1 - \frac{\hat{\mathbf{k}} \cdot \mathbf{x}_1(t_1)}{c} \right) \right]$$

- Resample to proper times $\hat{\tau}_1(t)$ using orbits

Instrument Simulation

- Simulation model available in a paper *in prep.* and the LISA Instrument Simulation Model document ([available here](#) for the consortium members)



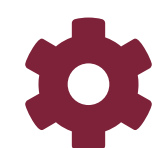
Bayle, Jean-Baptiste, Hartwig, Olaf, & Staab, Martin. (2022).

LISA Instrument (1.1.1). Zenodo. <https://doi.org/10.5281/zenodo.7071251>

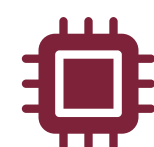
- Instrumental simulation includes



Optics (modulation and propagation of laser beams, main interferometric measurements and auxiliary measurements)



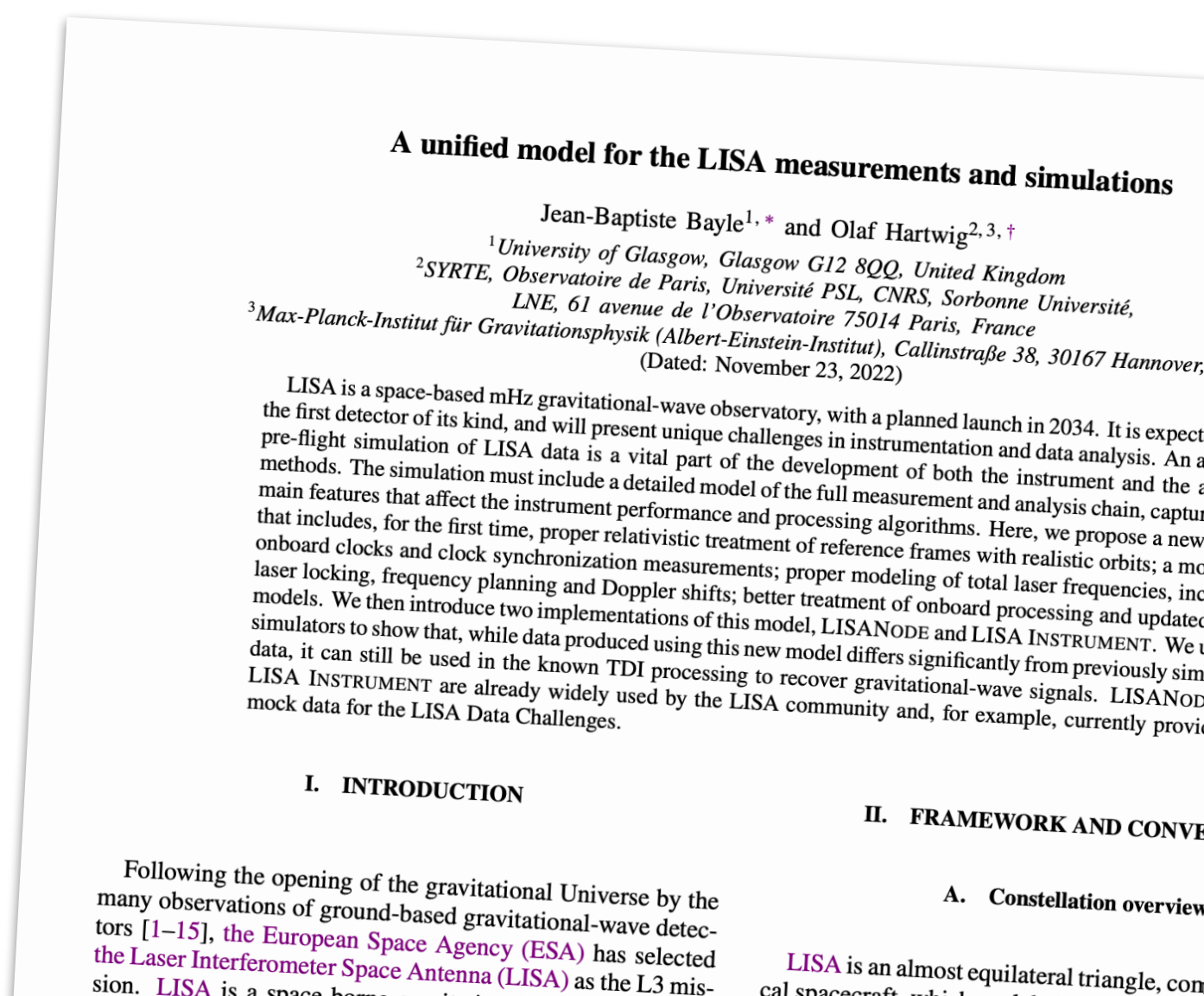
Dynamics (motion of spacecraft and test masses) – currently limited



Onboard processing (digital sampling, filtering and downsampling)

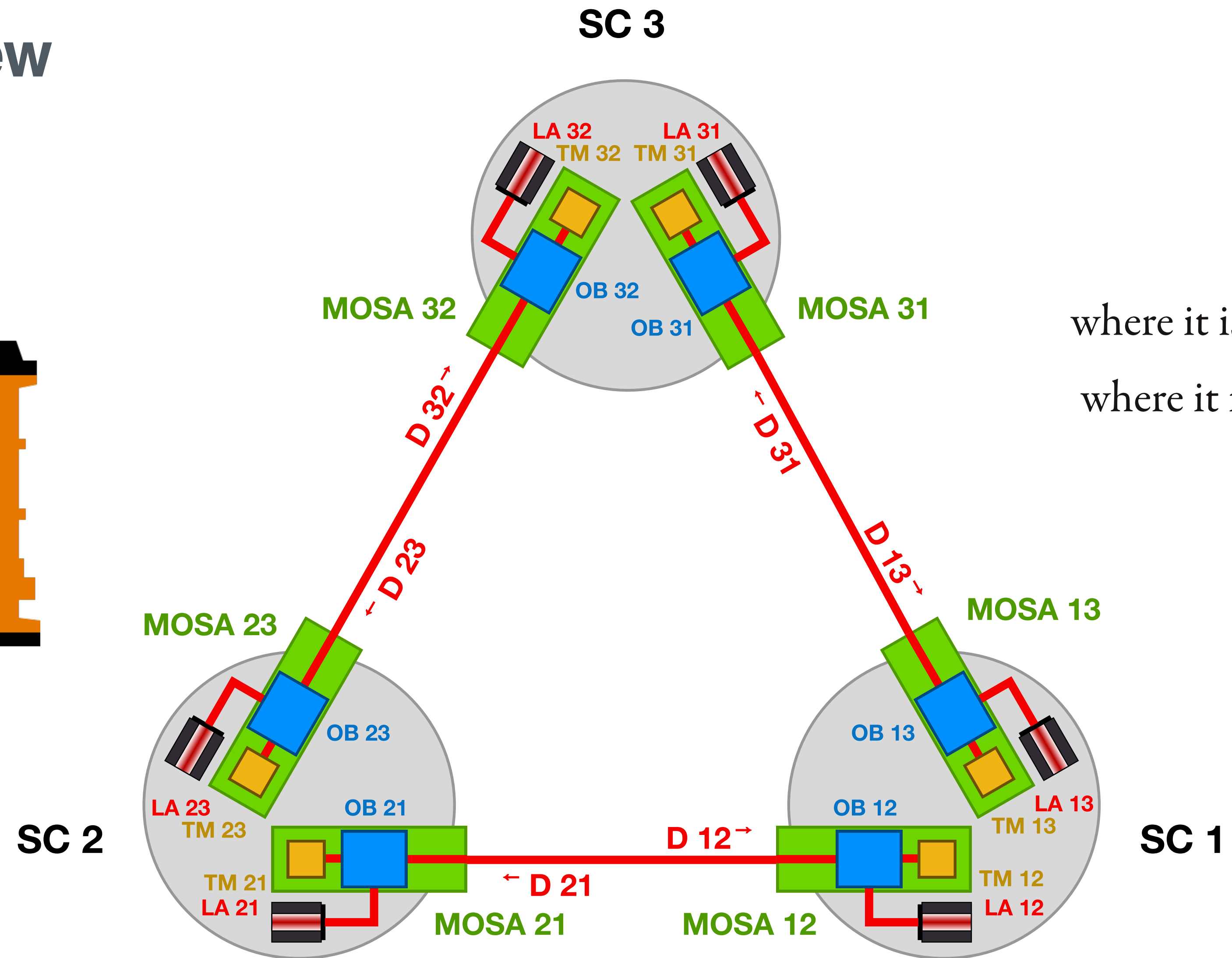
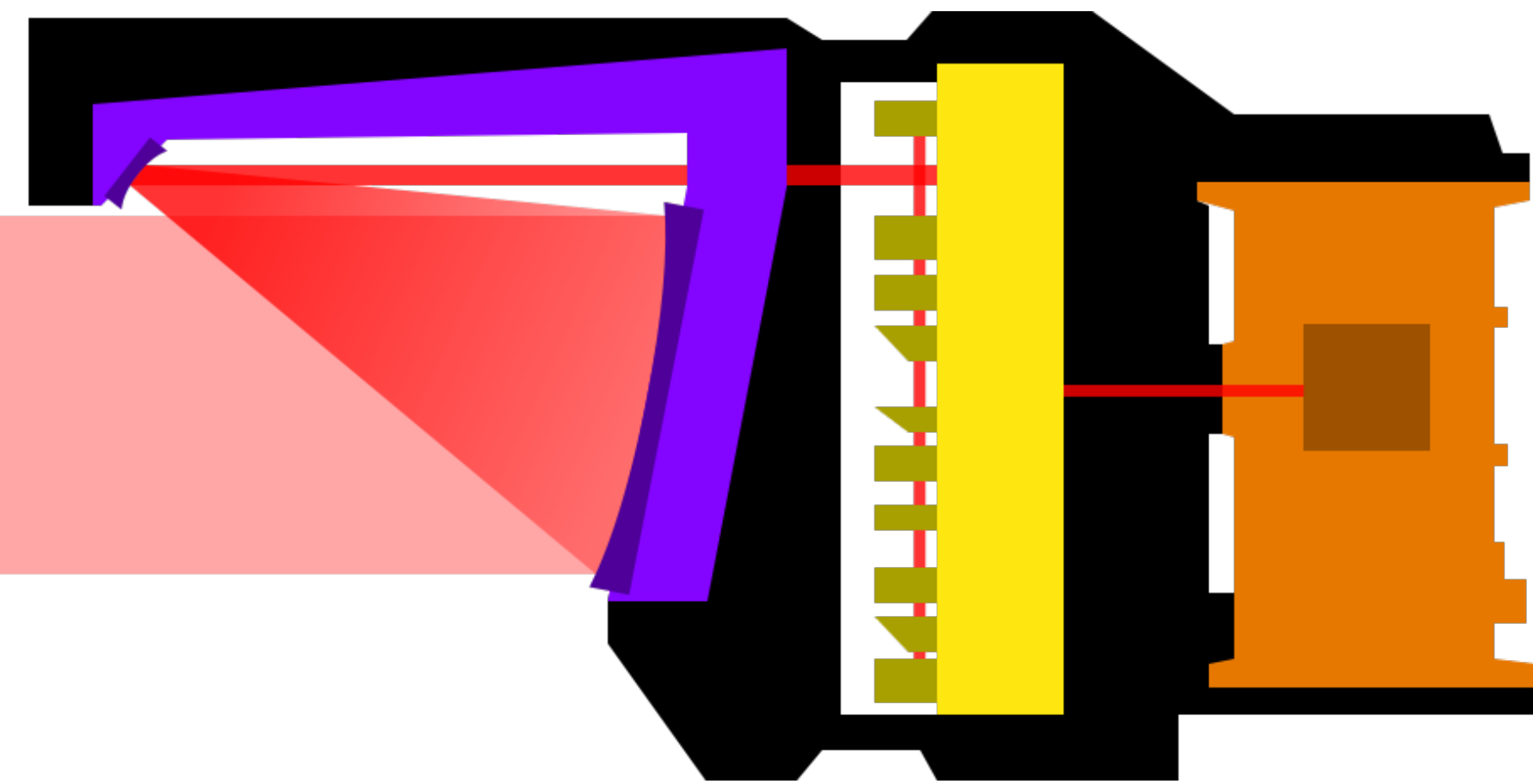
- Two sampling rates

- Measurements telemetered at 4 Hz
- Physics simulated at 16 Hz (inputs upsampled during simulation)



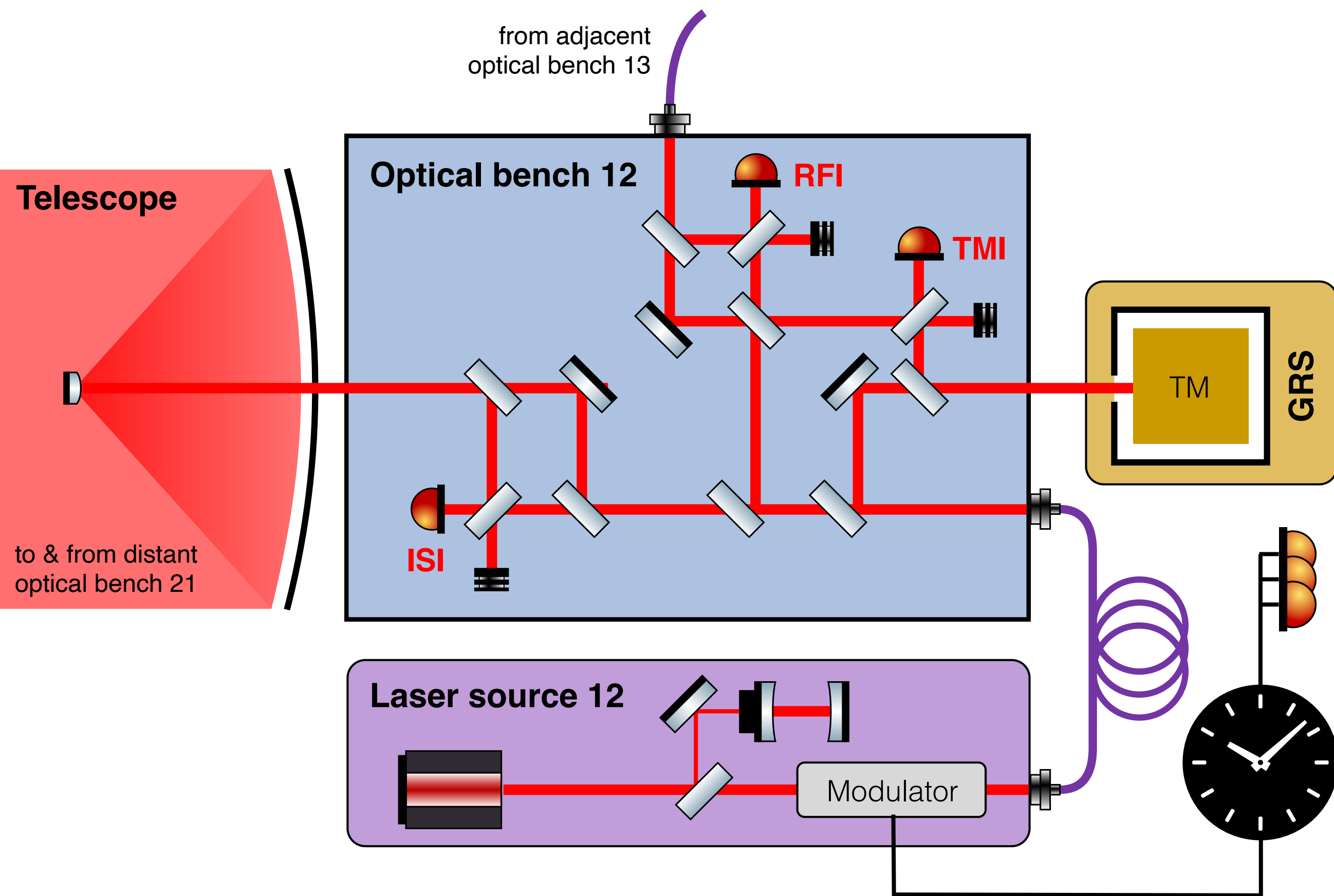
Instrument Simulation

Constellation Overview



Instrument Simulation

Optical Bench Overview



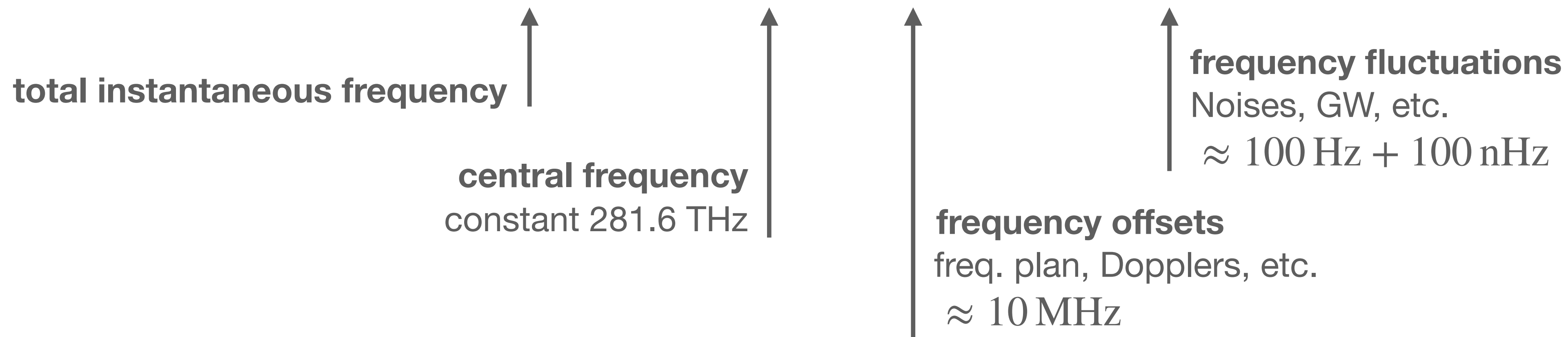
- 3 main interferometric signals recorded on each optical bench
 - **Inter-spacecraft interferometer (ISI)**
 - **Reference interferometer (RFI)**
 - **Testmass interferometer (TMI)**
- Interferometer data sampled according to onboard clock
- Modulate laser beams using clock signal to correct for sampling errors during L0-L1 processing

Instrument Simulation

Laser Beams

- Electromagnetic field $E(\tau) = E_0(\tau)\cos(2\pi\Phi(\tau))$
- GW signals encoded in the oscillating part of the field
- Simulate total frequencies $\nu(\tau) = \dot{\Phi}(\tau)/2\pi$ – *not just strain!*

$$\nu(\tau) = \nu_0 + \nu^o(\tau) + \nu^\epsilon(\tau)$$



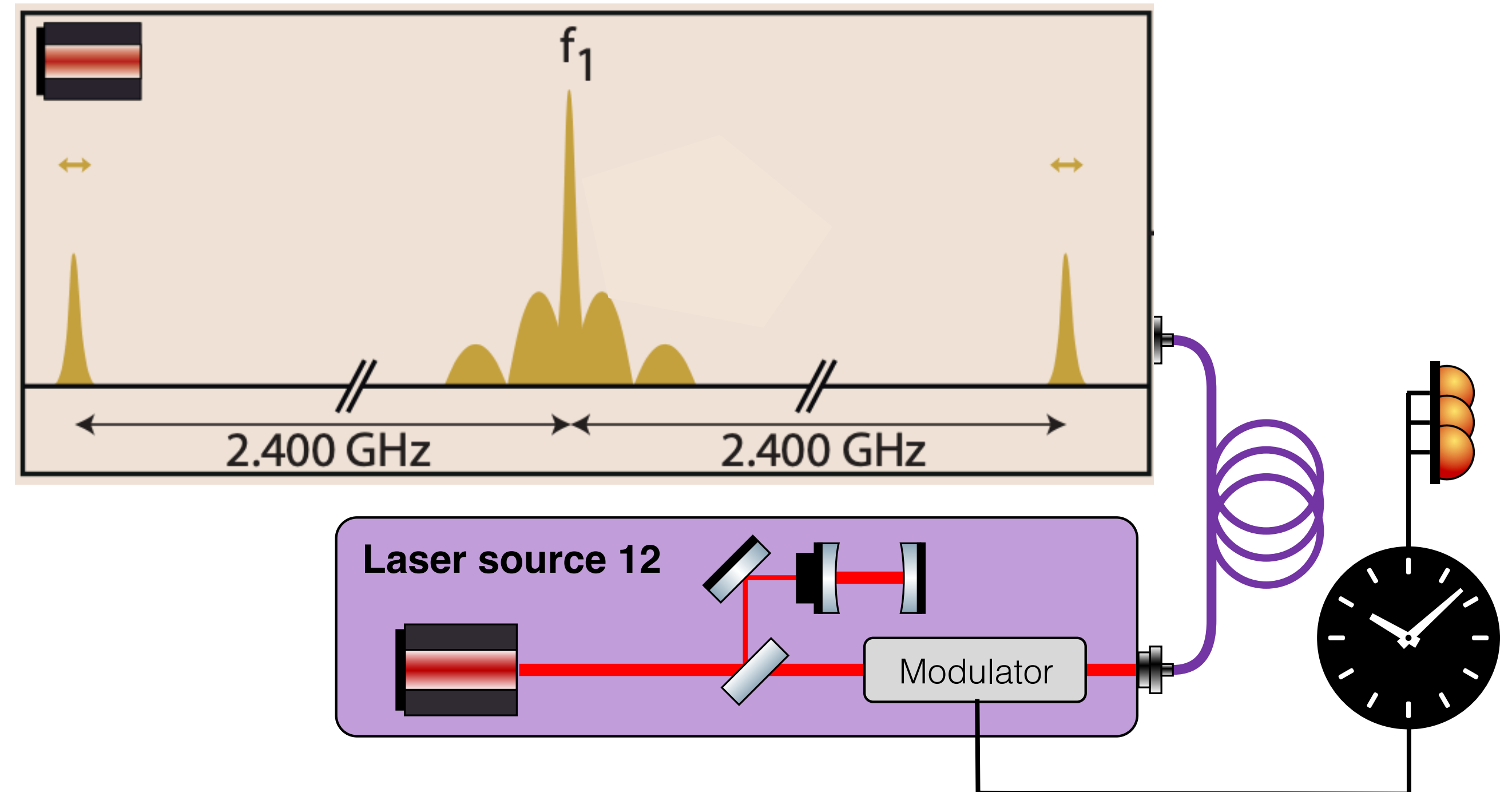
Instrument Simulation

Beam Modulation

- Onboard clocks used to sample data, therefore contribute to *phase errors*
- Phase modulation used to measure the in-band part of this clock noise

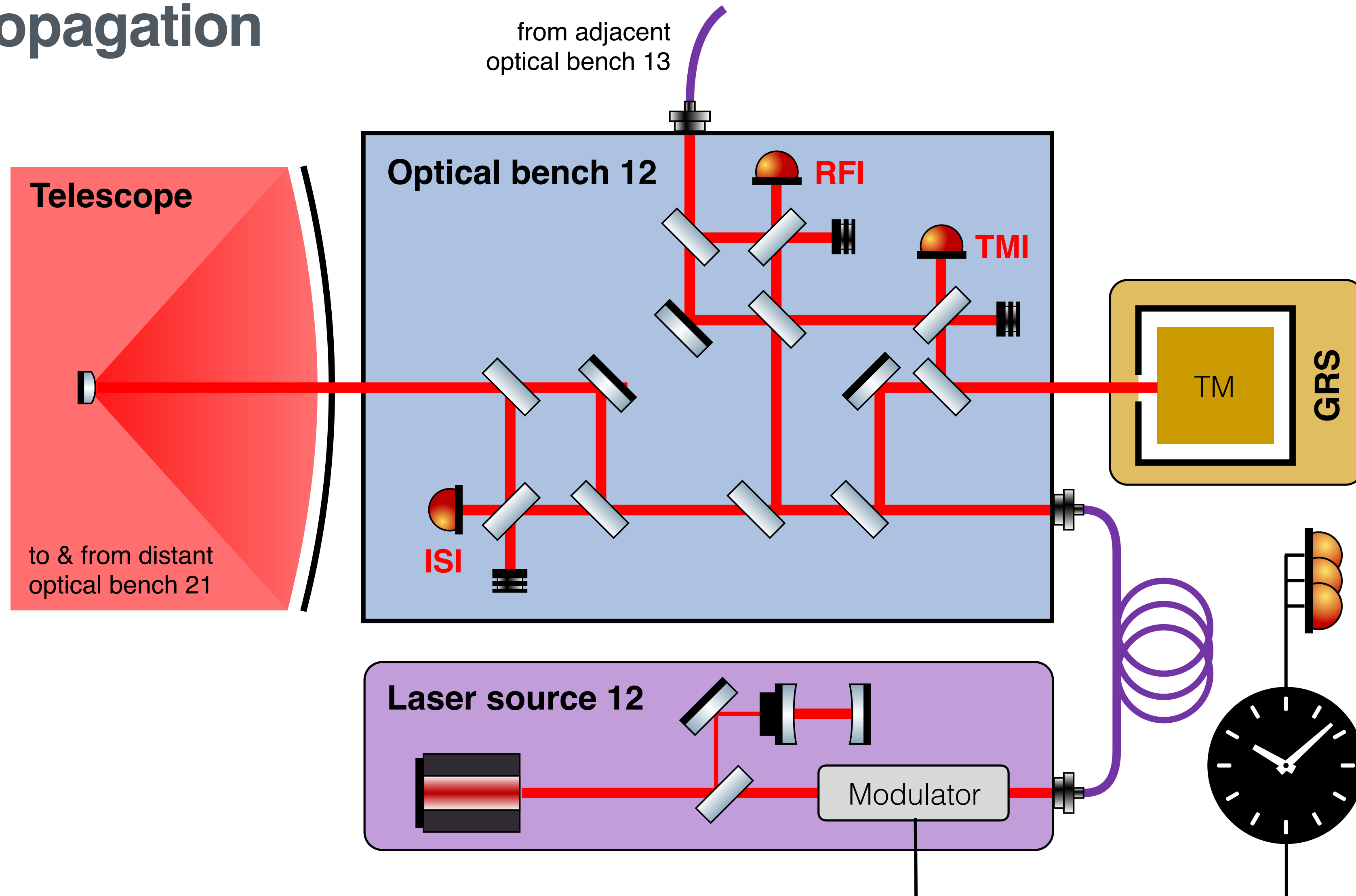
$$E(\tau) = E_0 e^{j2\pi(\Phi_c(\tau) + m\Phi_m(\tau))}$$

- Modeled as “independent” sideband beams (expansion with Bessel functions)



Instrument Simulation

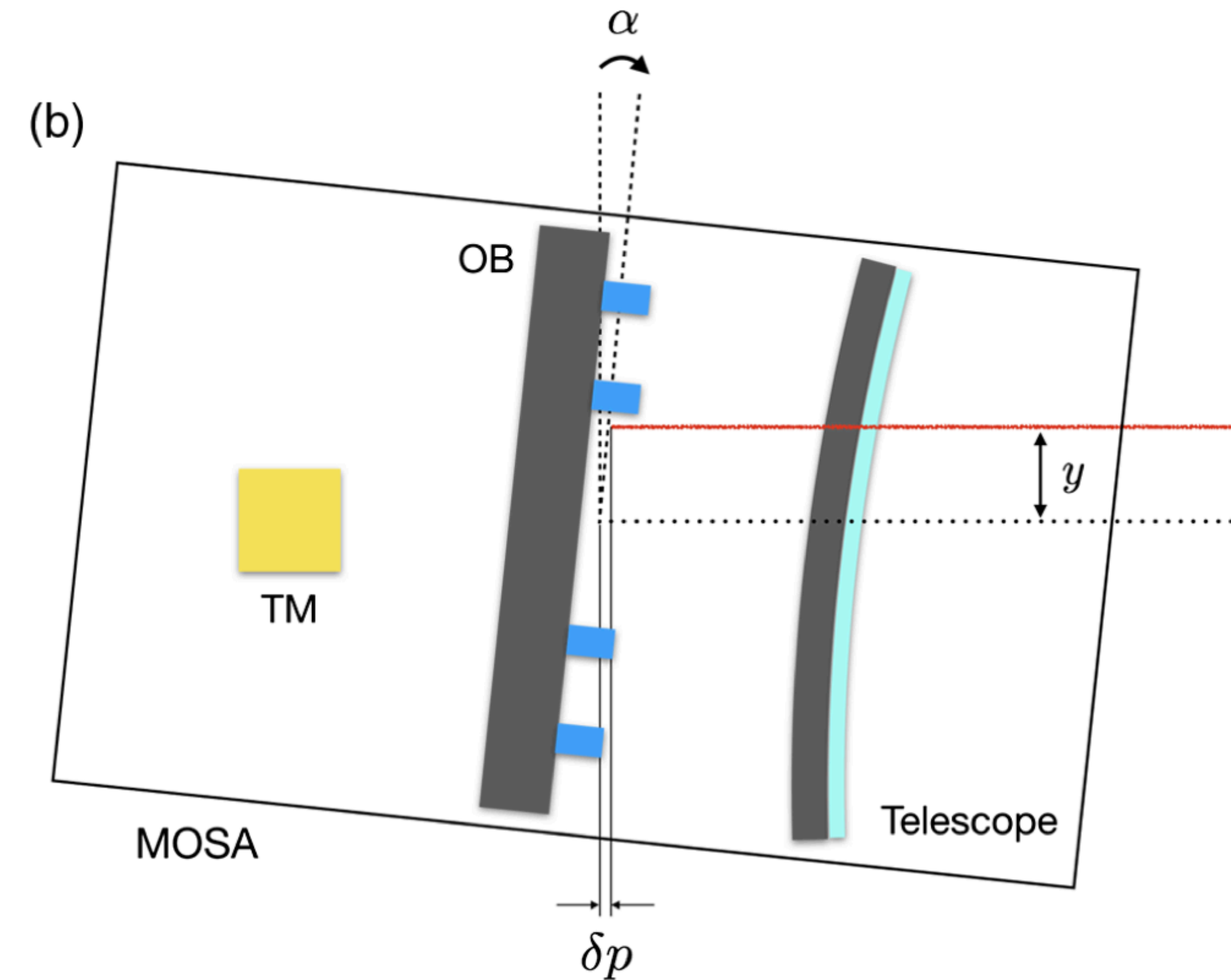
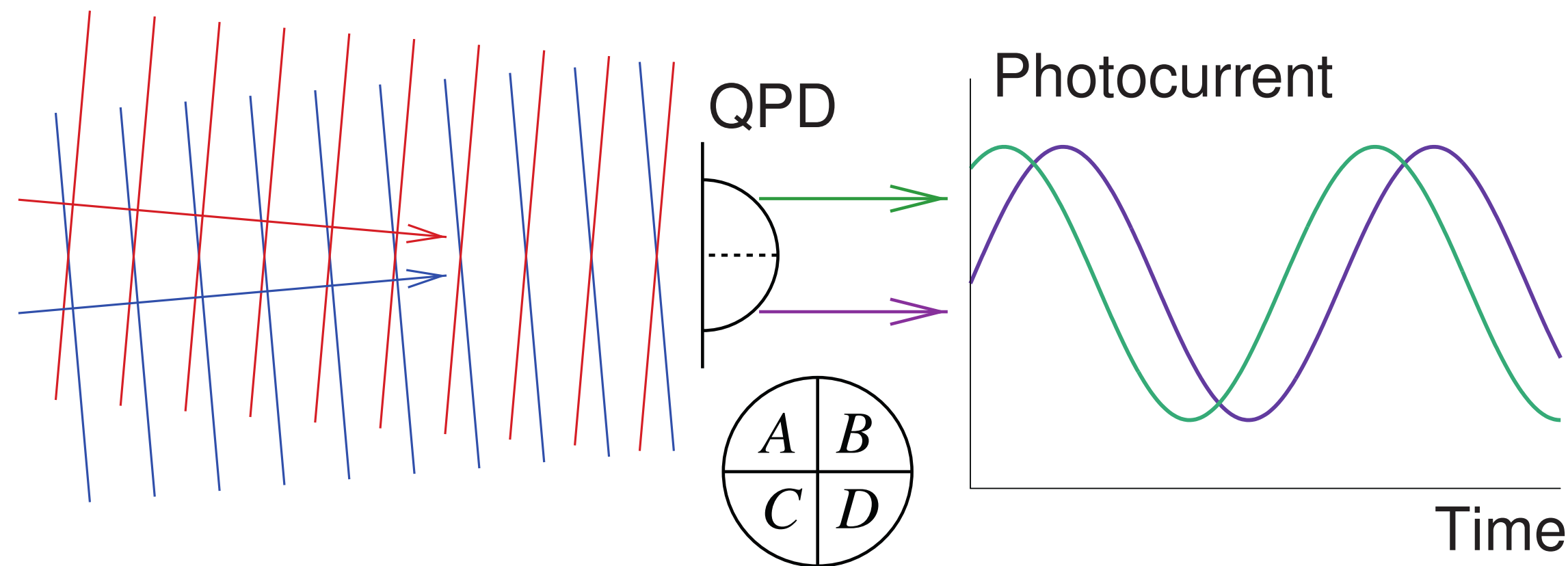
Beam Propagation



Instrument Simulation

Tilt to Length (TTL)

- Tilt to length couples beam tilts and optical element misalignment to pathlength changes
- Linear model with a set of 24 coefficients relating tilt angles to pathlength changes
- DWS allows to measure angular tilts of 2 beams by combining outputs of a quadrant photodiode



Paczkowski et al. (2022). 10.1103/PhysRevD.106.042005

Instrument Simulation

Inter-spacecraft Propagation

- Phase is a frame invariant quantity, so total phase is equal at reception and emission
- Signals propagated between spacecraft using **proper pseudoranges (PPRs)**, which include **light travel times** and conversion factor between spacecraft proper times
- In addition,
 - GWs cause a tiny ($\approx 10^{-20}$ s) additional modulation of the PPR
 - Additional Doppler shifts with frequency data

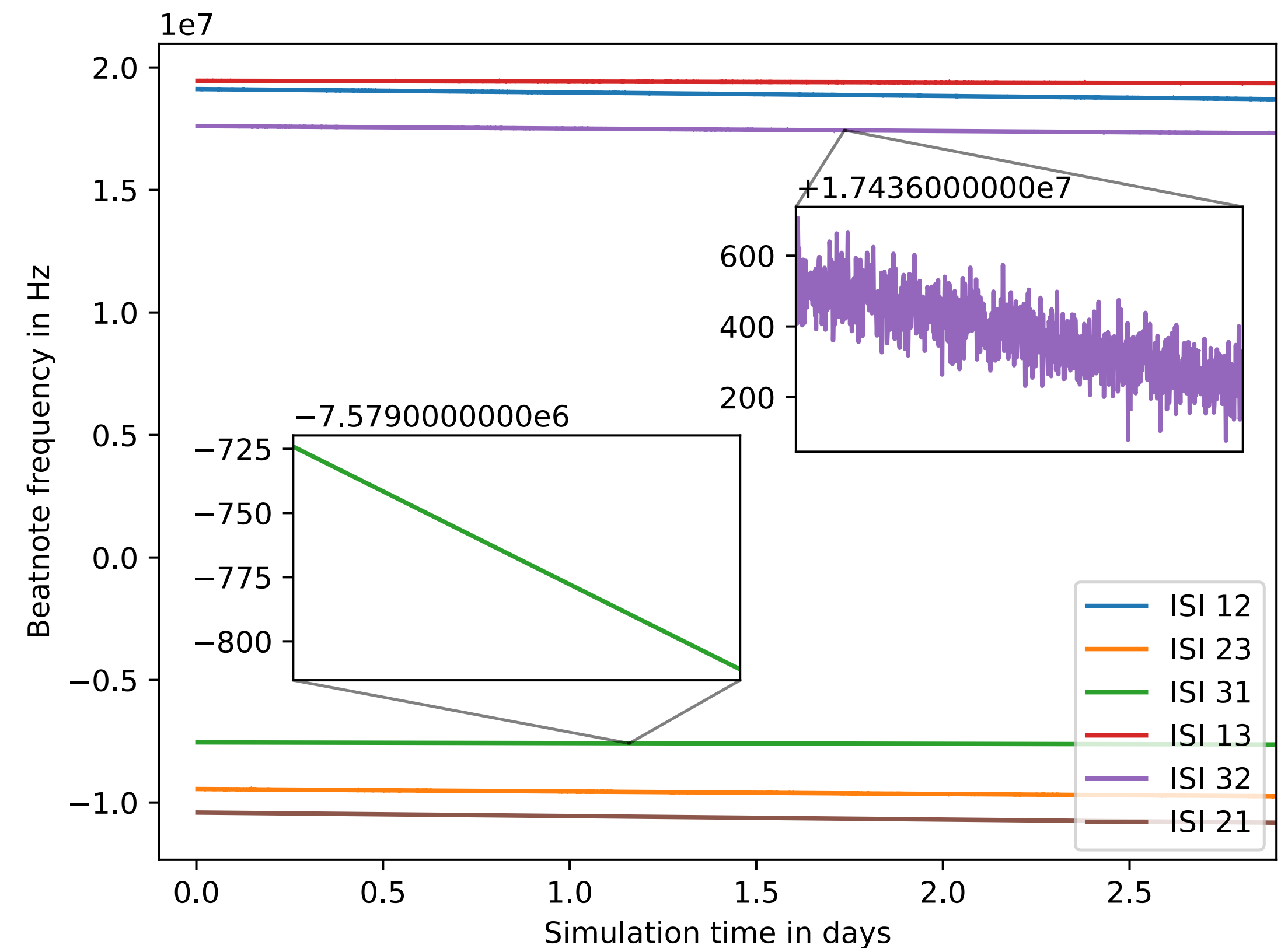
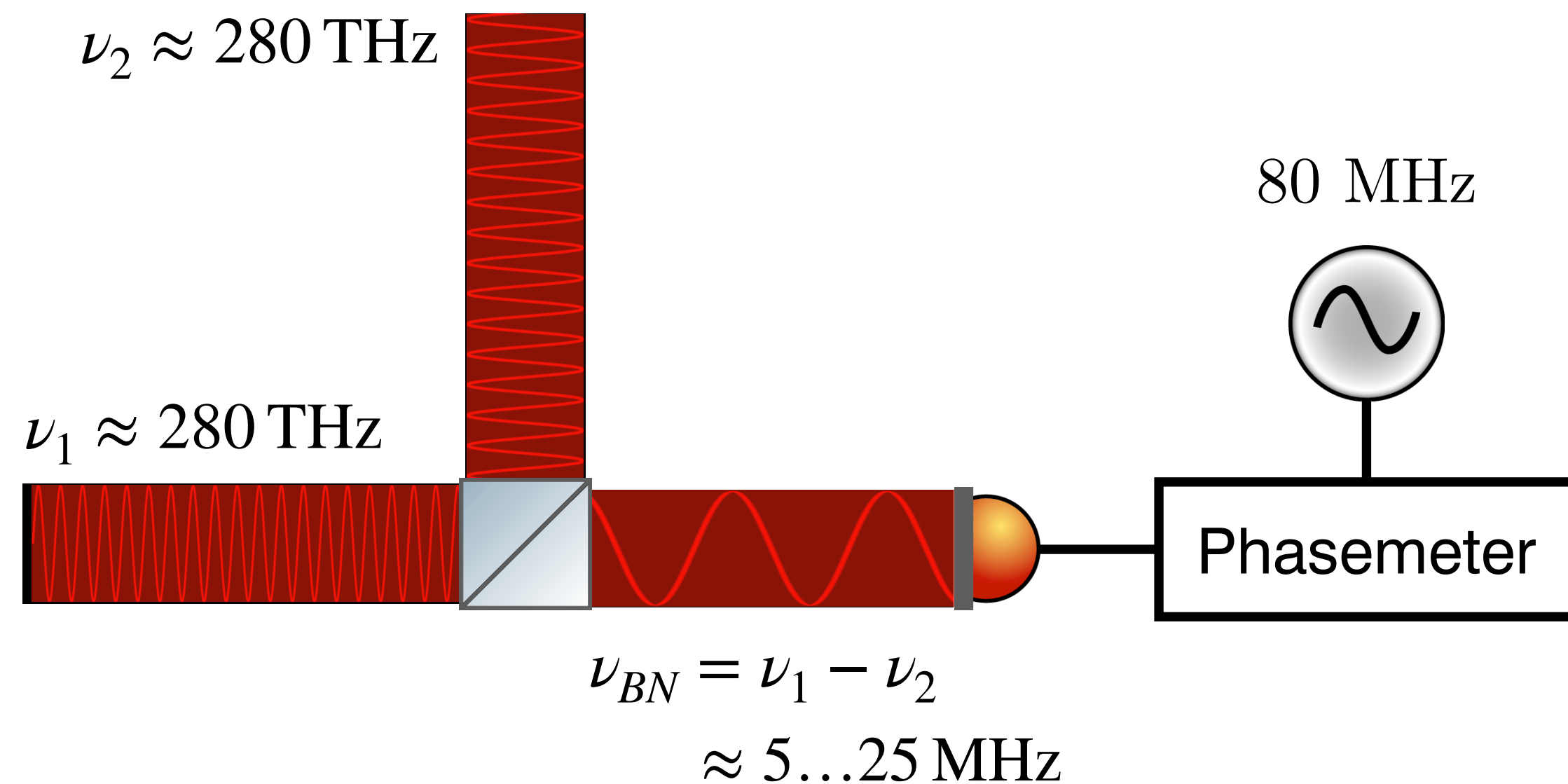
$$\nu_{ij \leftarrow ji}(\tau) = \frac{d}{d\tau} \Phi_{ji}(\tau - d_{ij}(\tau) - H_{ij}(\tau)) = (1 - \dot{d}_{ij}(\tau) - \dot{H}_{ij}(t)) \nu_{ji}(\tau - d_{ij}(\tau))$$

PPRs ↑
total instantaneous frequency ↑
Doppler shift ↑

Instrument Simulation

Interferometry & Readout

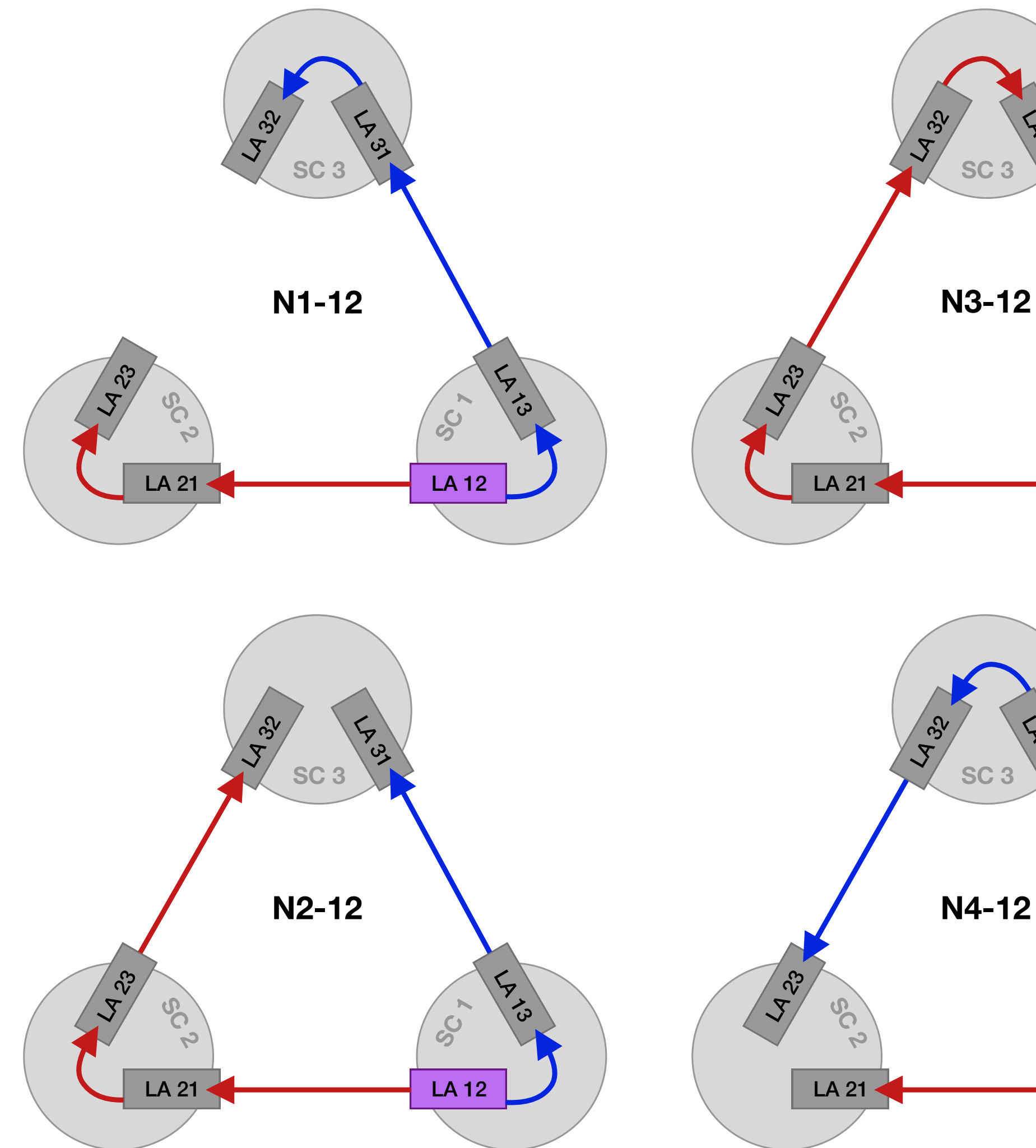
- LISA uses heterodyne interferometry and GW is encoded as μ -cycle phase fluctuation in MHz beatnotes (in frequency)
- Beatnotes recorded according to local clock



Instrument Simulation

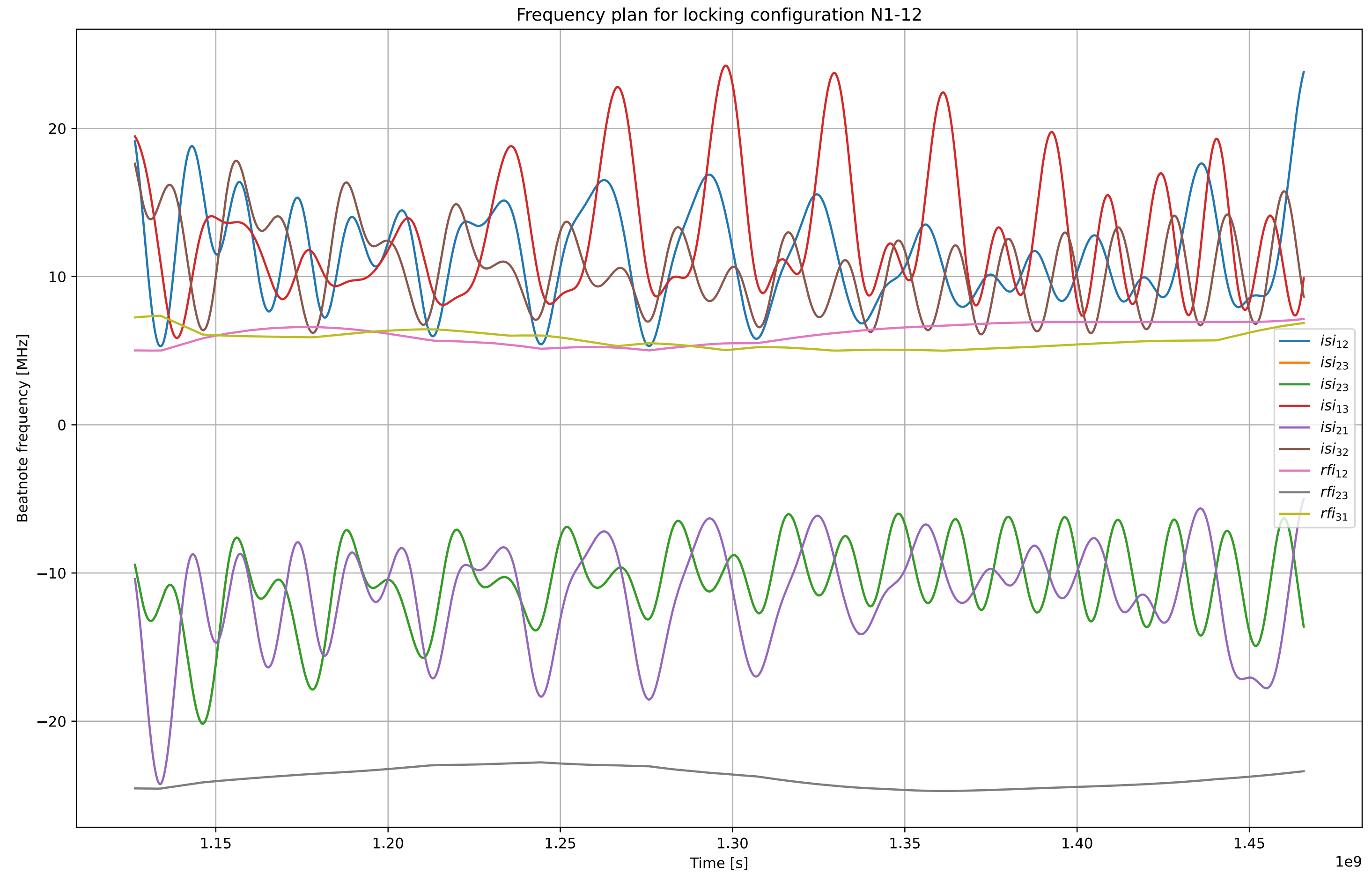
Laser Locking & Frequency Plan

- All beatnotes should fall into the phasemeter validity frequency range (5 to 25 MHz)
 - Doppler shifts frequencies by 10s of MHz
 - Solution: lock lasers (many configurations possible) with an optimized precomputed frequency plan
- Frequency plan optimized numerically by G. Heinzel
- As a consequence, noises are distributed over different beatnotes



Instrument Simulation

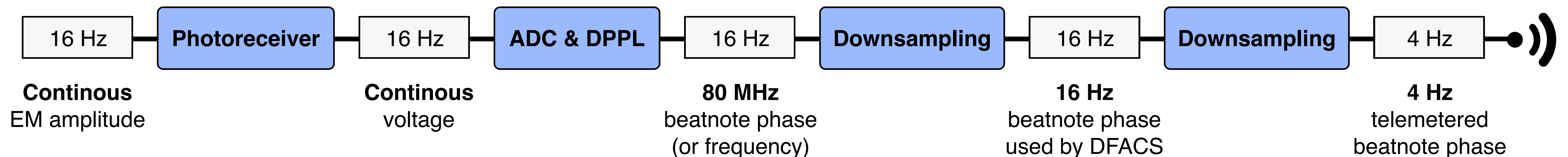
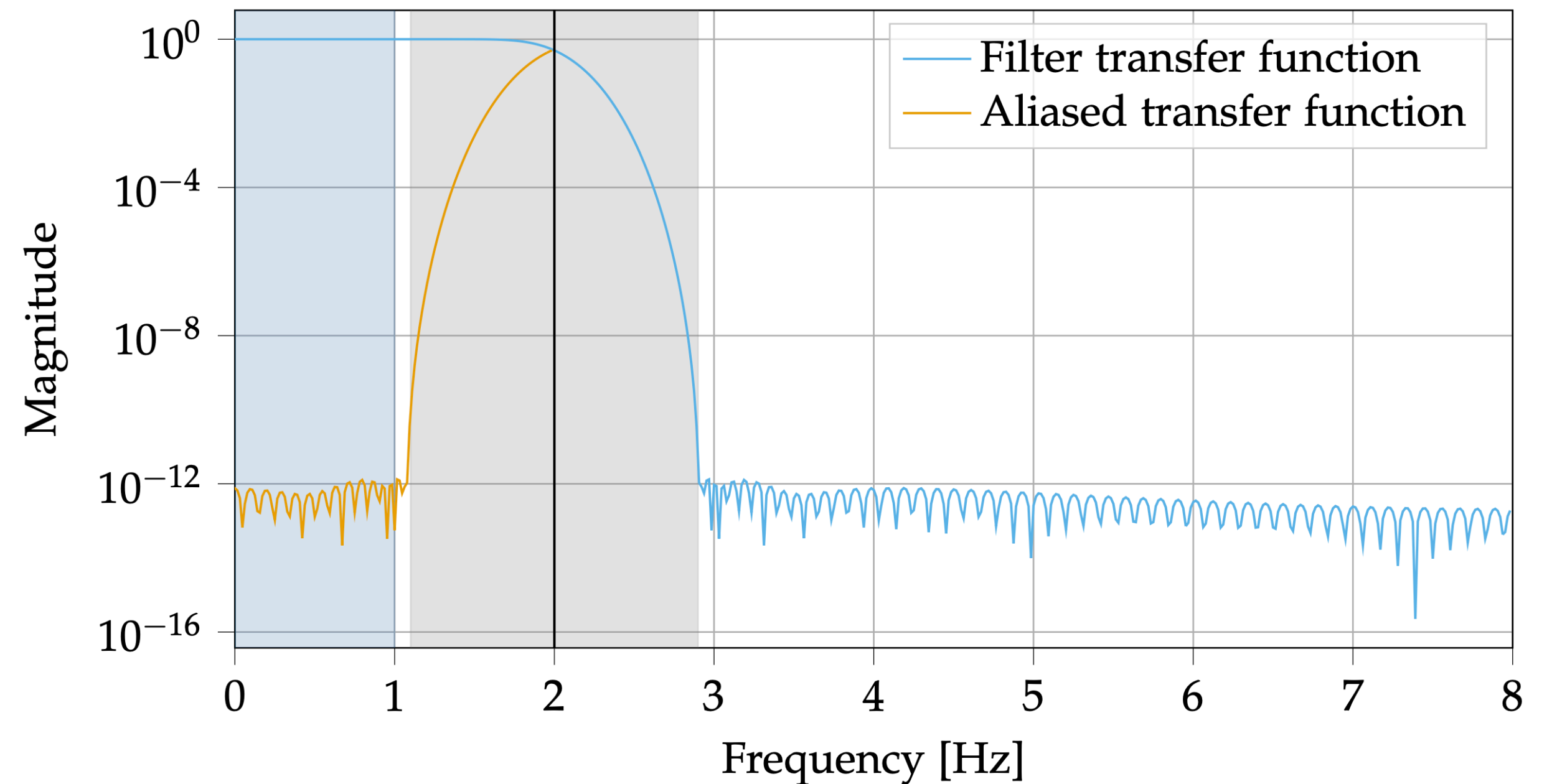
Laser Locking & Frequency Plan



Instrument Simulation

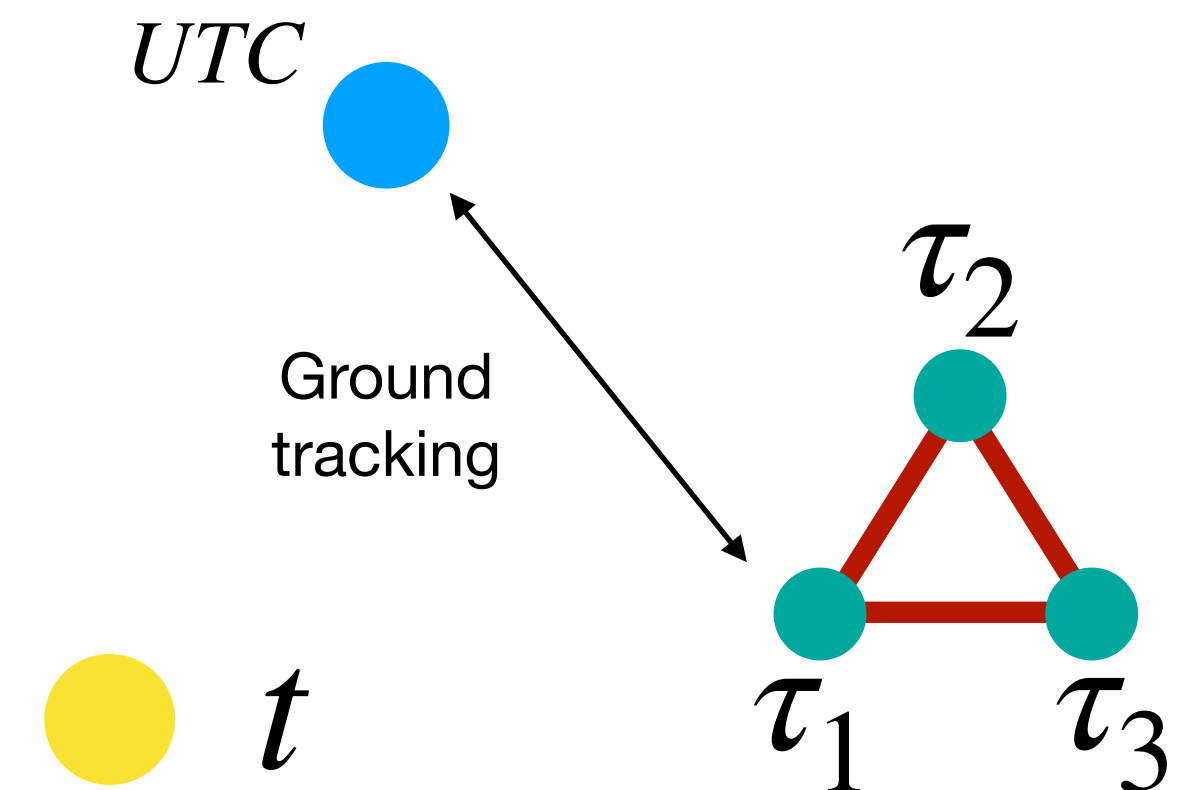
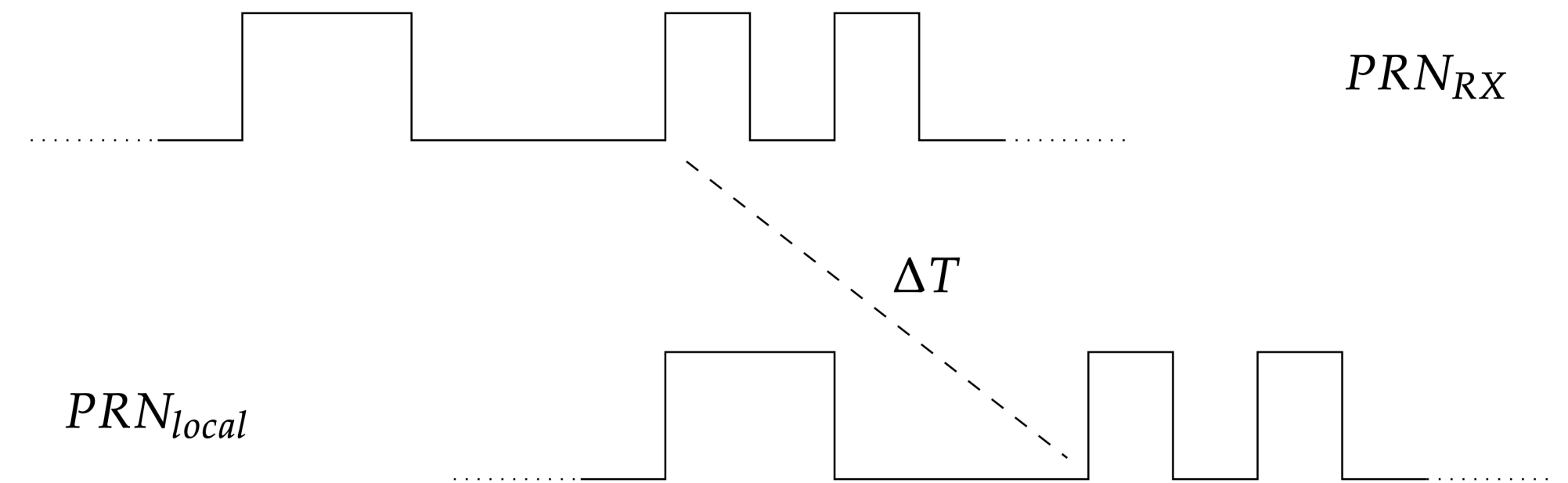
Onboard Processing

- In reality
 - Phasemeter runs at 80 MHz
 - Filtered and downsampled in several steps to final 4 Hz telemetry
- In simulation
 - Physics and phasemeter at 16 Hz
 - Single filter and decimation step to 4 Hz



MPR & Ground Tracking

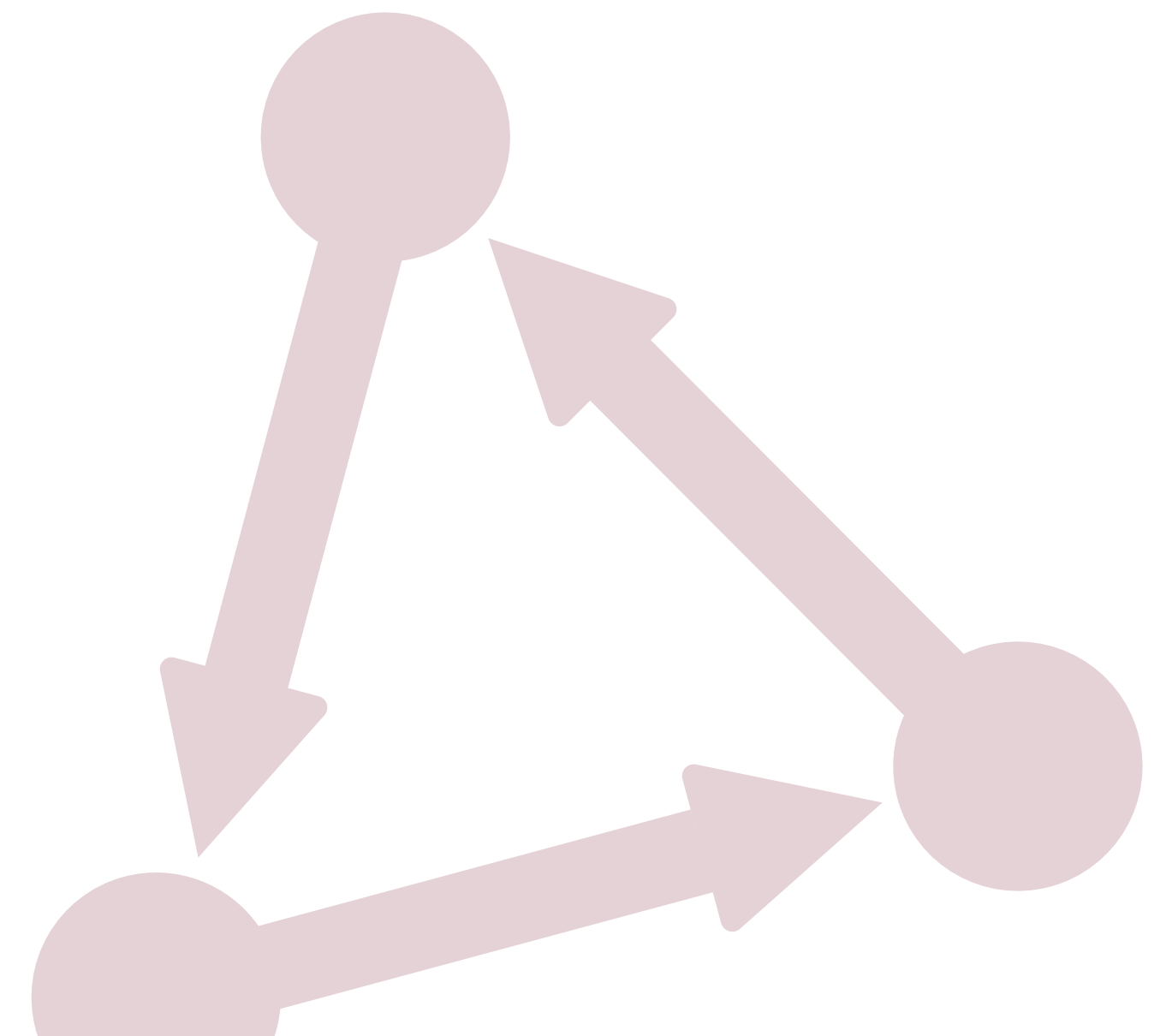
- Measured pseudoranges (MPRs)
 - Correlate signals from two distant clocks
 - Include photon light travel time and transformation between clock times $\Delta T = \hat{\tau}_i - \hat{\tau}_j$ (and any correlation errors)
- Ground tracking provides estimates of
 - Spacecraft positions with 2-50 km accuracy (direction dependent) and spacecraft velocities with 10 cm/s accuracy
 - Time correlations between clocks and a global time frame (here UTC) better than ms accuracy



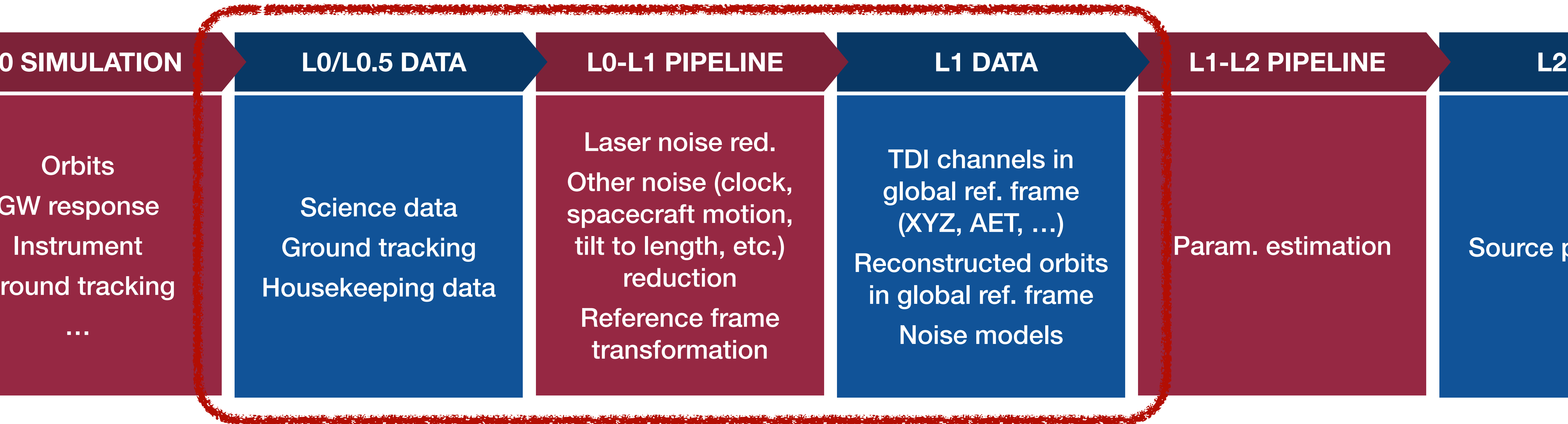
L0 Data Overview

- Science data
 - 3 interferometer data (carrier and sideband) on the 6 optical benches
 - Measured pseudoranges (MPRs)
 - Differential waveform sensor (DWS) measurements
 - Other quantities not simulated currently (GRS, etc).
- Ground-tracking
 - Reconstructed orbits
 - Time correlations (clock times as a function of a global reference frame)
- Housekeeping and calibration stuff (lots of 'em)

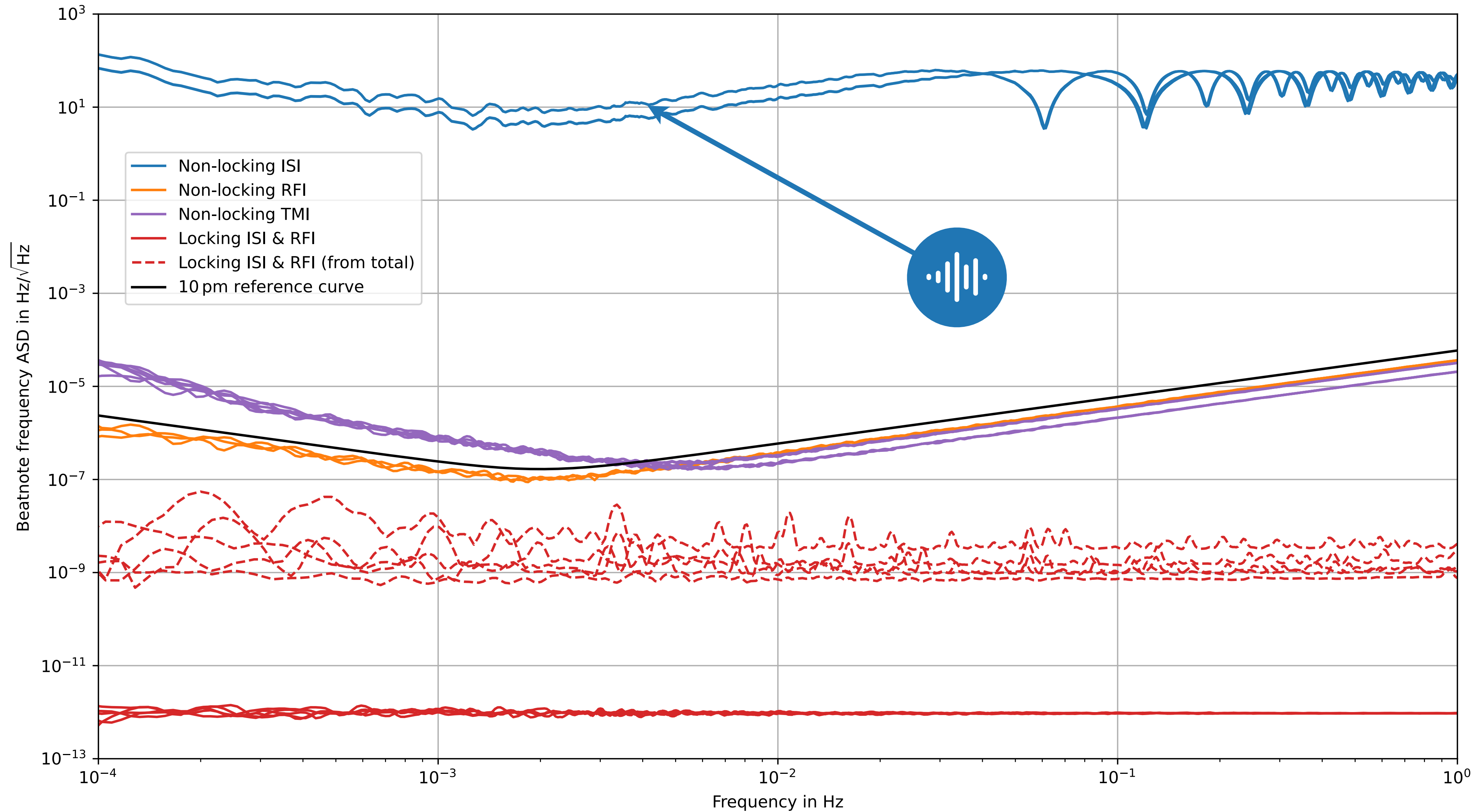
L0-L1 Processing



LISA Data Analysis Pipeline



L0 Data Overview



One Recipe (Amongst Others)

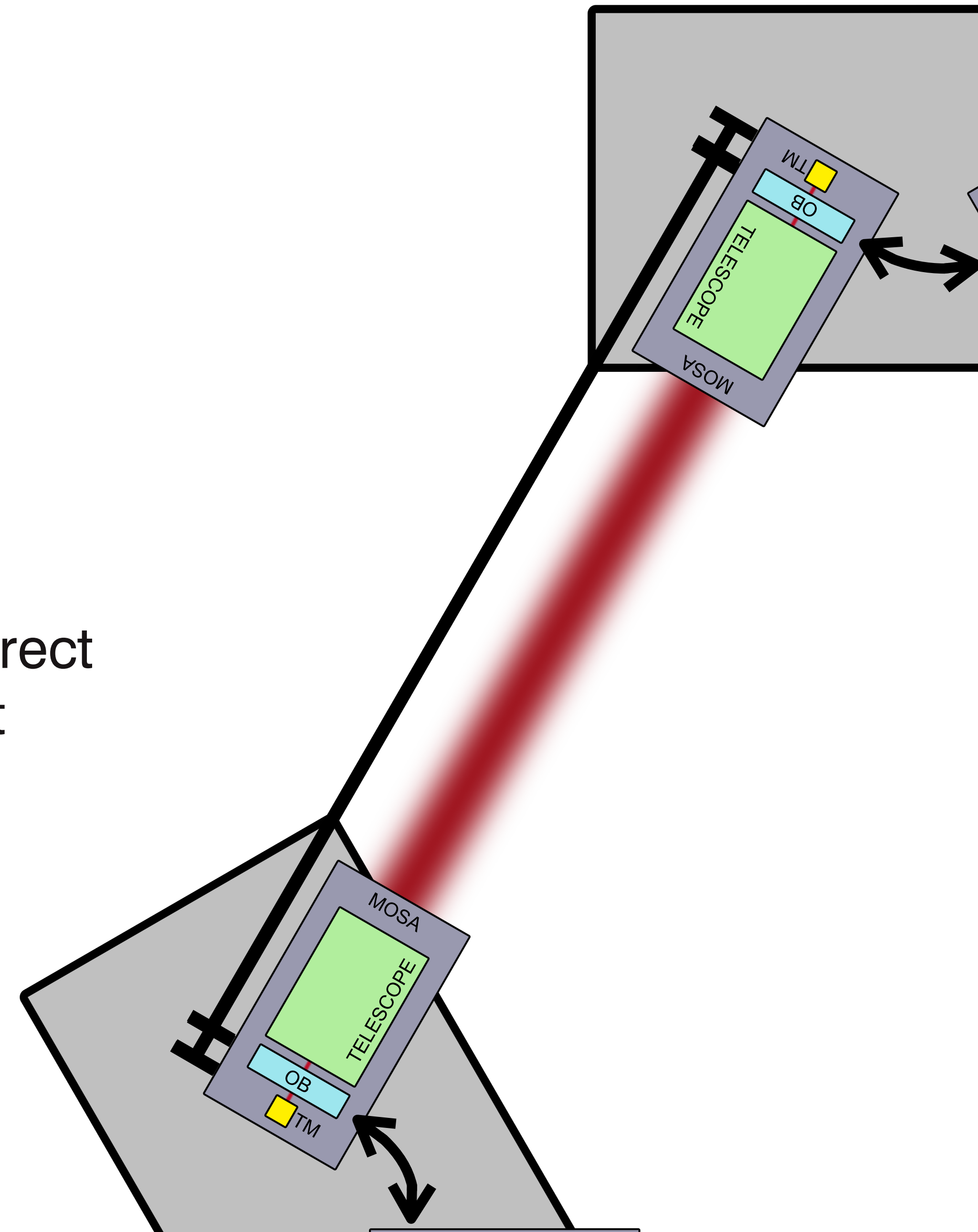
Here, L0-L1 pipeline for total frequency

Phase data will also be available, TBD if we gain anything in PE from using it...

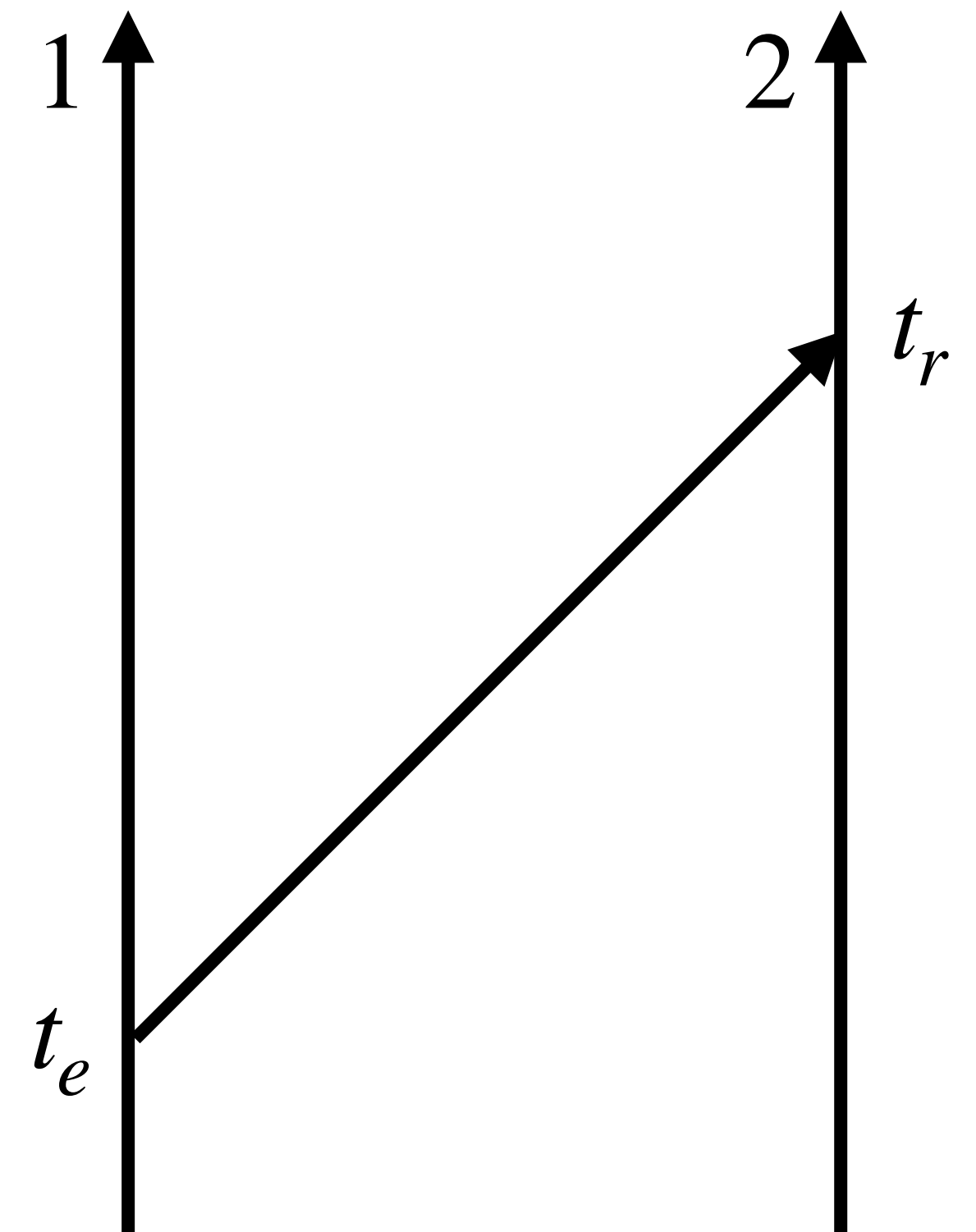
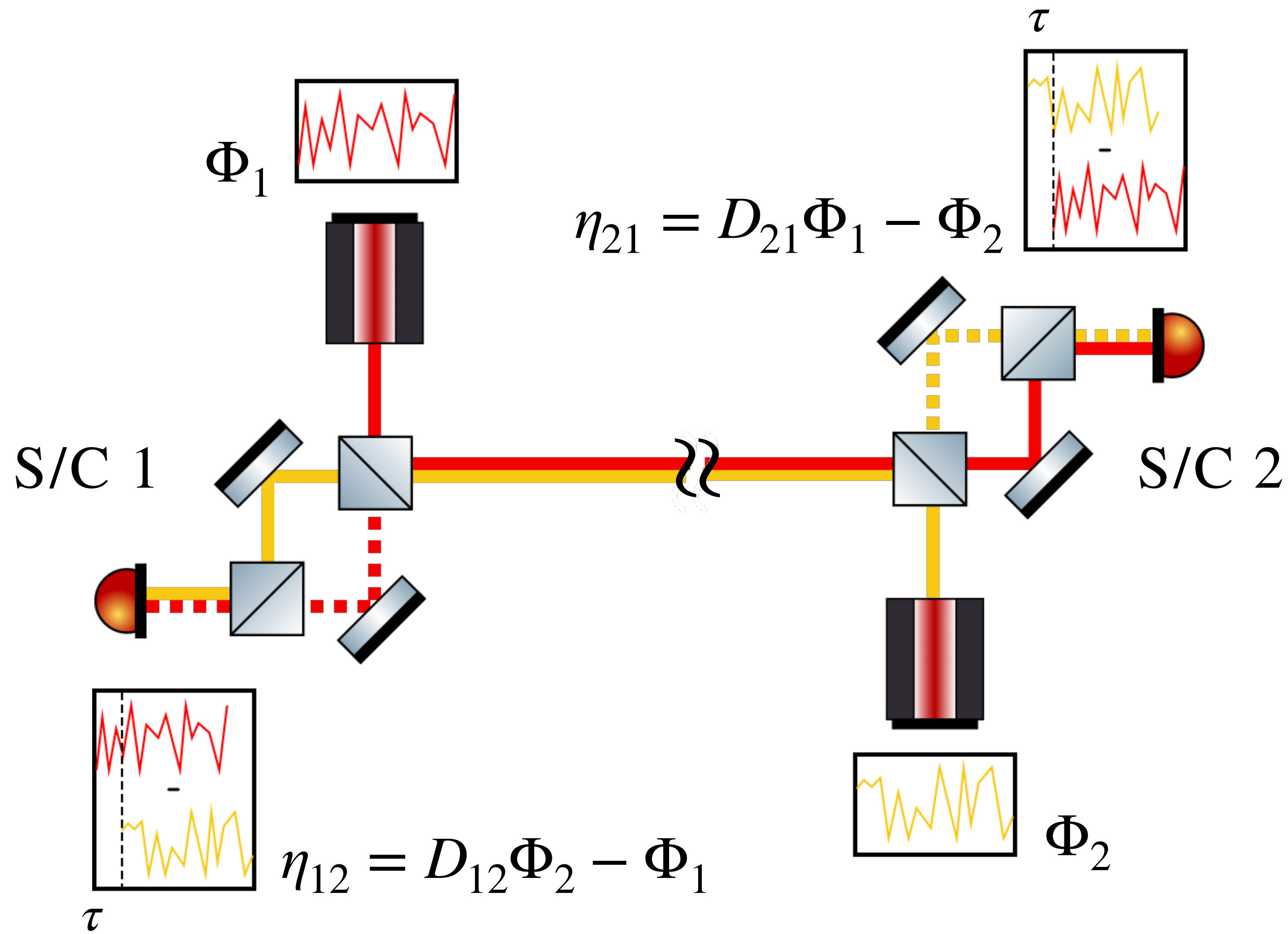
1. Accurate estimation of the pseudoranges
 - Merge ground-tracking, MPRs and sidebands to provide accurate and low-noise estimates
 - Compute light travel times for response function
2. Construct test-mass-to-test-mass measurements to reduce spacecraft motion
3. Reduce tilt-to-length using DWS measurements
4. Correct for laser and clock noise using TDI
5. Synchronize TDI variable to a global reference frame using time correlations
6. Compute AET channels (if actually useful for PE)

Single-Link Corrections

- **We want to monitor the TM-to-TM measurement**
- 3 Interferometers on each optical bench
 - Inter-spacecraft interferometer (ISI)
 - Test-mass interferometer (TMI)
 - Reference(interferometer (RFI)
- Combined in early processing step to synthesize direct TM-to-TM measurement, with 1 laser per spacecraft
- Then subtract TTL via DWS measurements
 - Coupling coefficients are estimated using dedicated calibration experiments (under investigation)

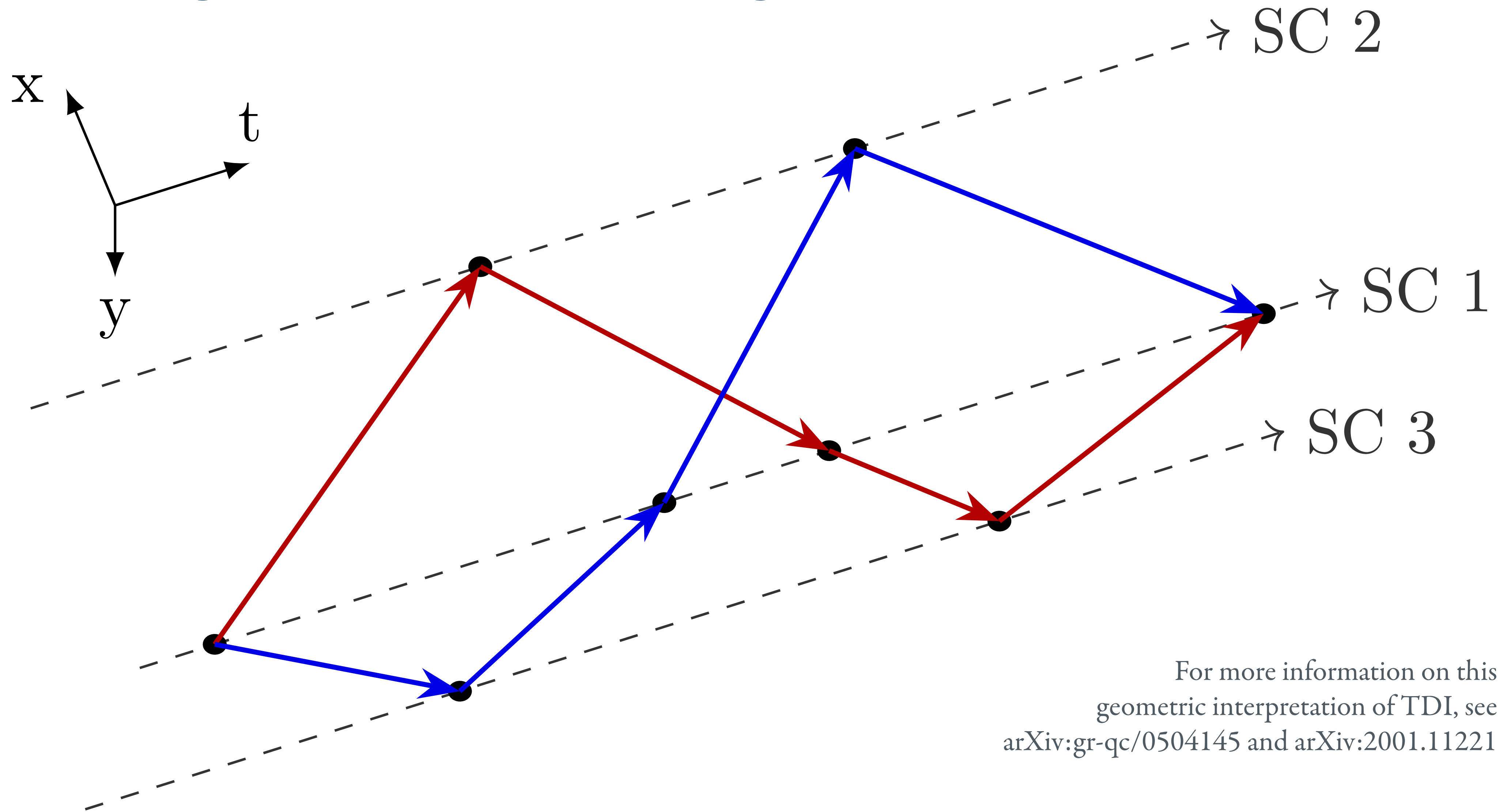


Simplified LISA Link



$$\begin{aligned} \Phi_1(t_e) &\equiv D_{21}\Phi_1(t_r) \\ &= \Phi_1(t_r - d_{21}(t_r)) \end{aligned}$$

Time-Delay Interferometry



For more information on this
geometric interpretation of TDI, see
[arXiv:gr-qc/0504145](https://arxiv.org/abs/gr-qc/0504145) and [arXiv:2001.11221](https://arxiv.org/abs/2001.11221)

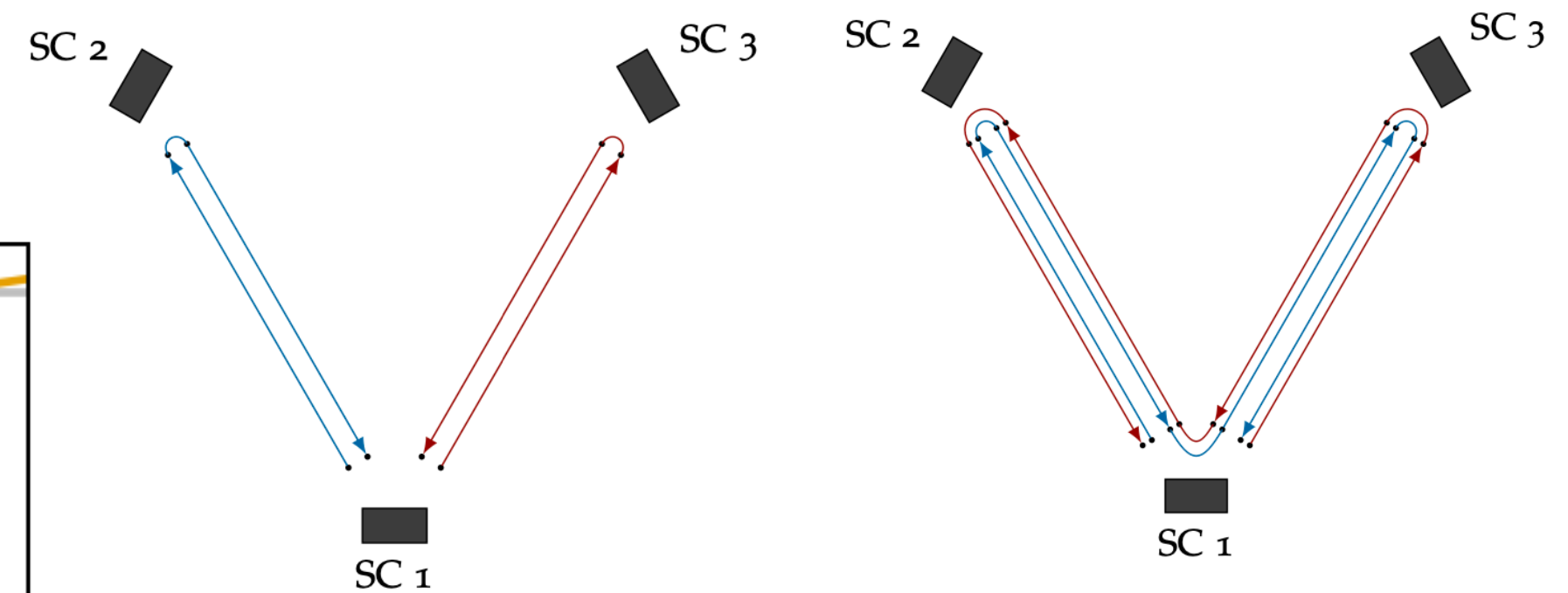
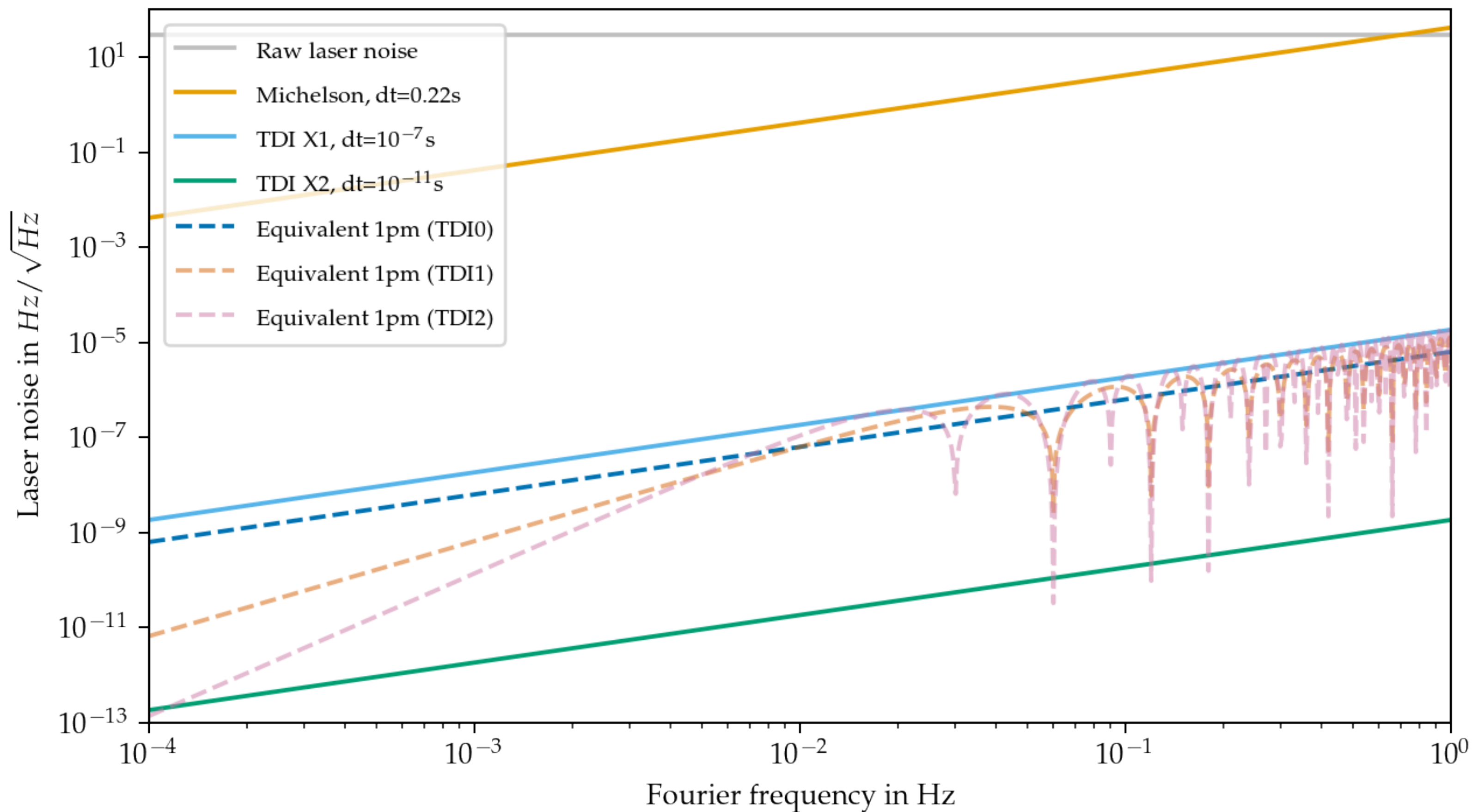
Laser Noise Residual

... Assuming Realistic Orbits

Average light travel times with ESA orbits: $d_A \approx 8.3\text{ s}$, $\dot{d}_A \approx 10^{-9}$ and $\ddot{d}_A \approx 10^{-15}\text{ s}^{-1}$

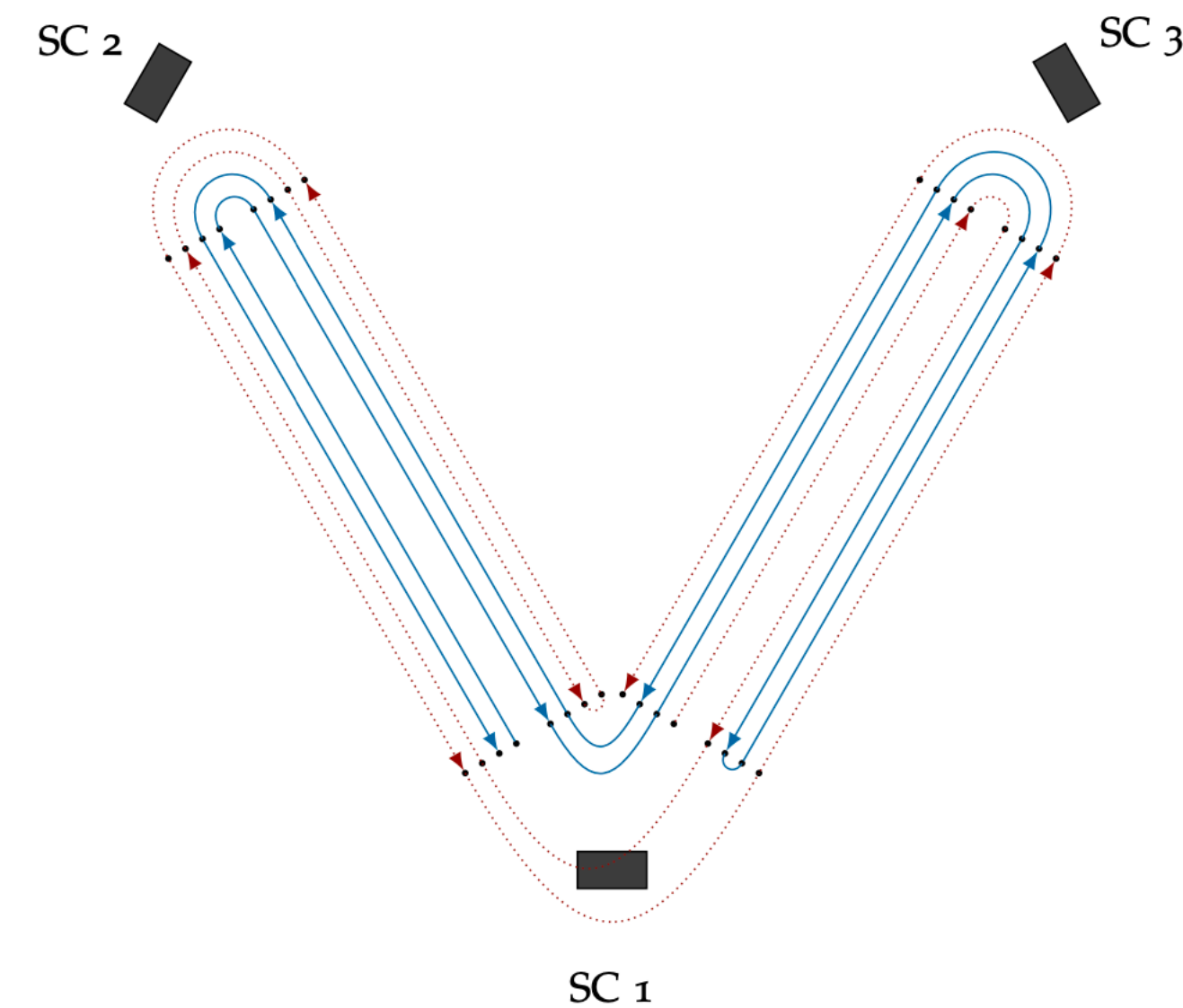
$$S_{\Phi, \text{TDI}} \approx (2\pi f)^2 \delta t^2 S_{\Phi}$$

Residual laser noise



$$\Delta\tau_0 \approx 2(d_{12} - d_{13})$$

$$\Delta\tau_1 \approx 4d(\dot{d}_{31} - \dot{d}_{12})$$



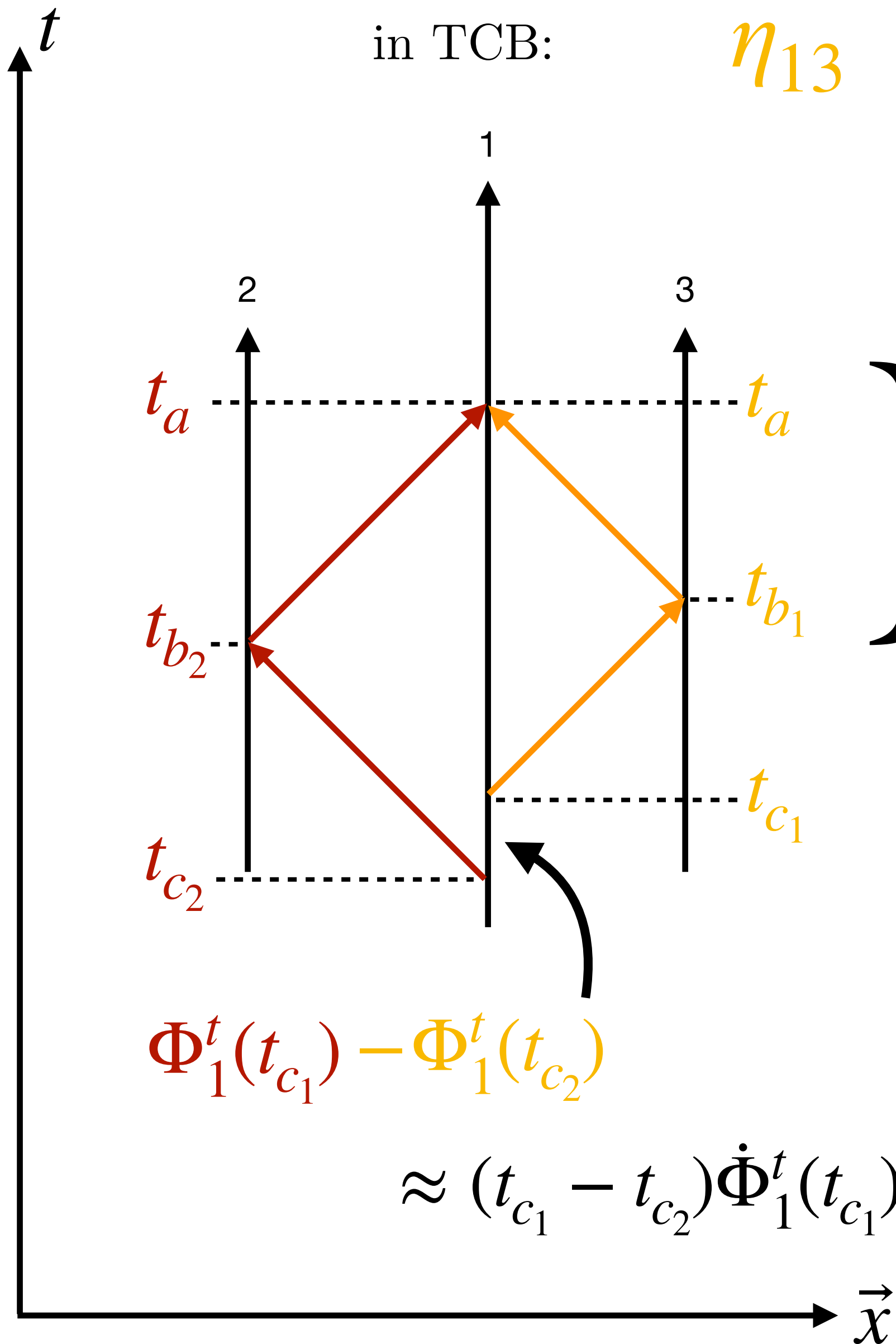
$$\Delta\tau_2 = \approx t[(\dot{d}_{12}^2 - \dot{d}_{31}^2) - 2d(\ddot{d}_{12} - \ddot{d}_{31})]$$

TDI with desynchronized clocks

Geometric TDI with Clock Times

Measurements
in TCB:

$$\eta_{13} - \eta_{12} + D_{13}\eta_{31} - D_{12}\eta_{21}$$



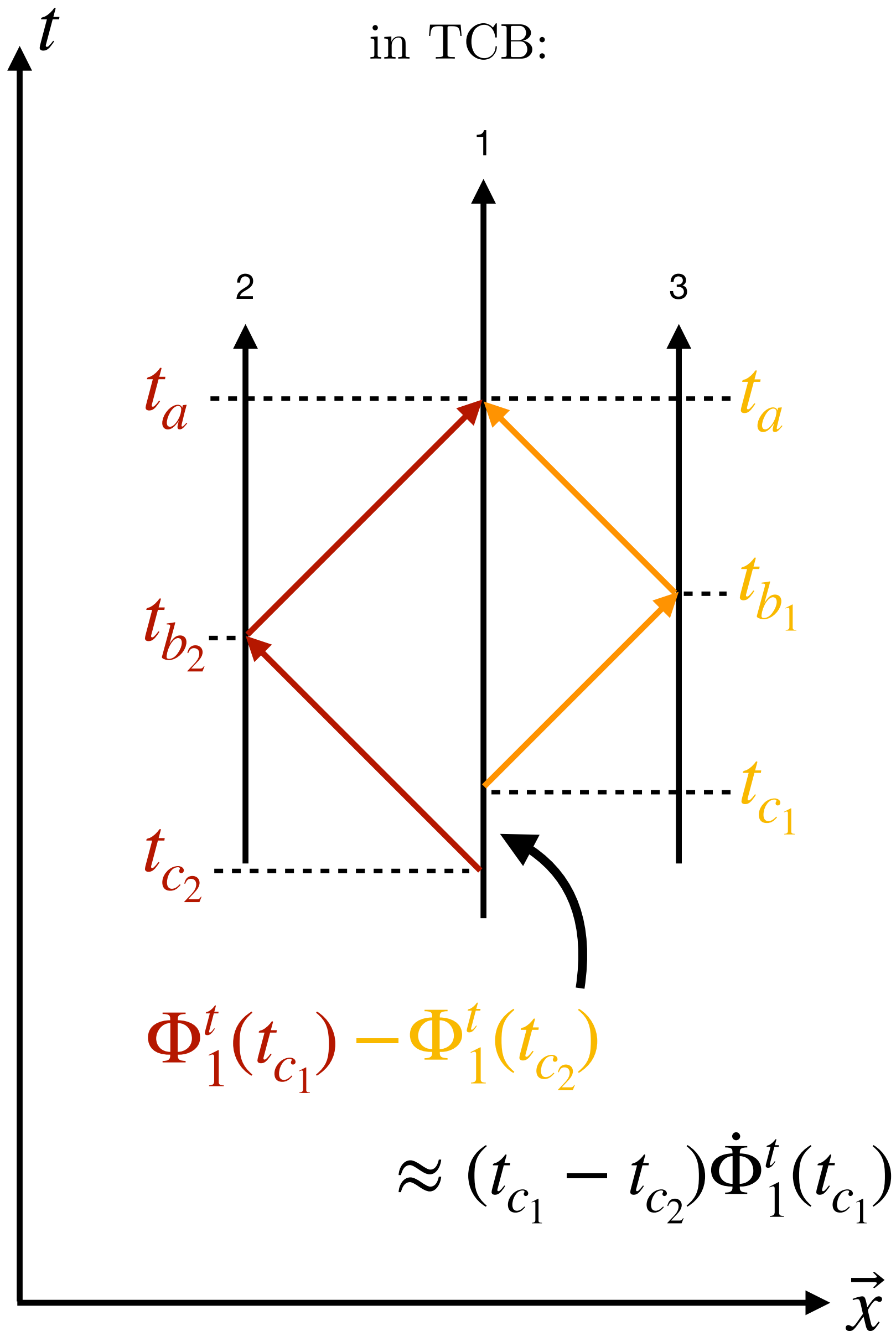
Light travel time in TCB,
Computed from S/C position
estimates

$$\Phi_1^t(t_{c_1}) - \Phi_1^t(t_{c_2})$$

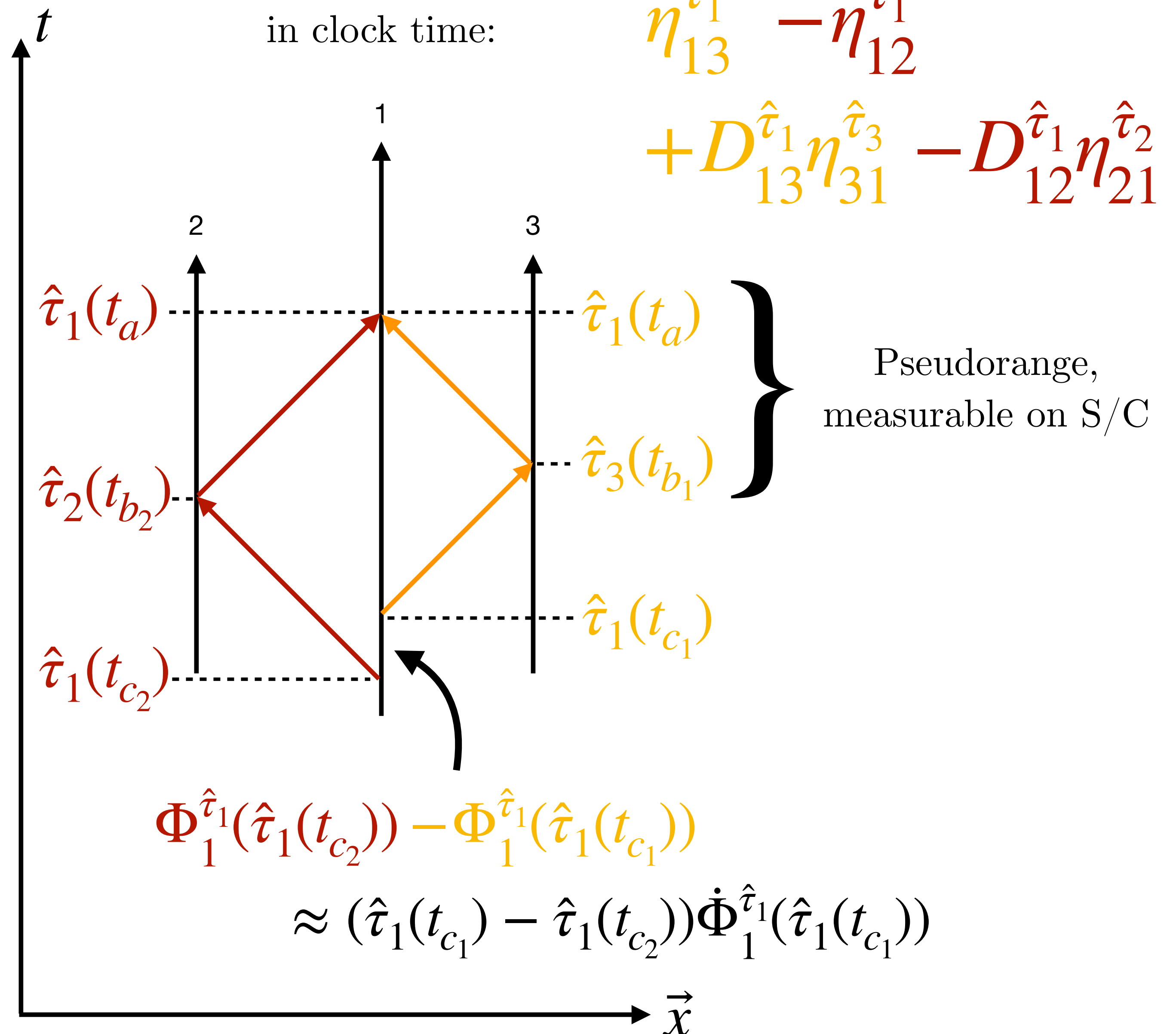
$$\approx (t_{c_1} - t_{c_2}) \dot{\Phi}_1^t(t_{c_1})$$

Geometric TDI with Clock Times

Measurements
in TCB:



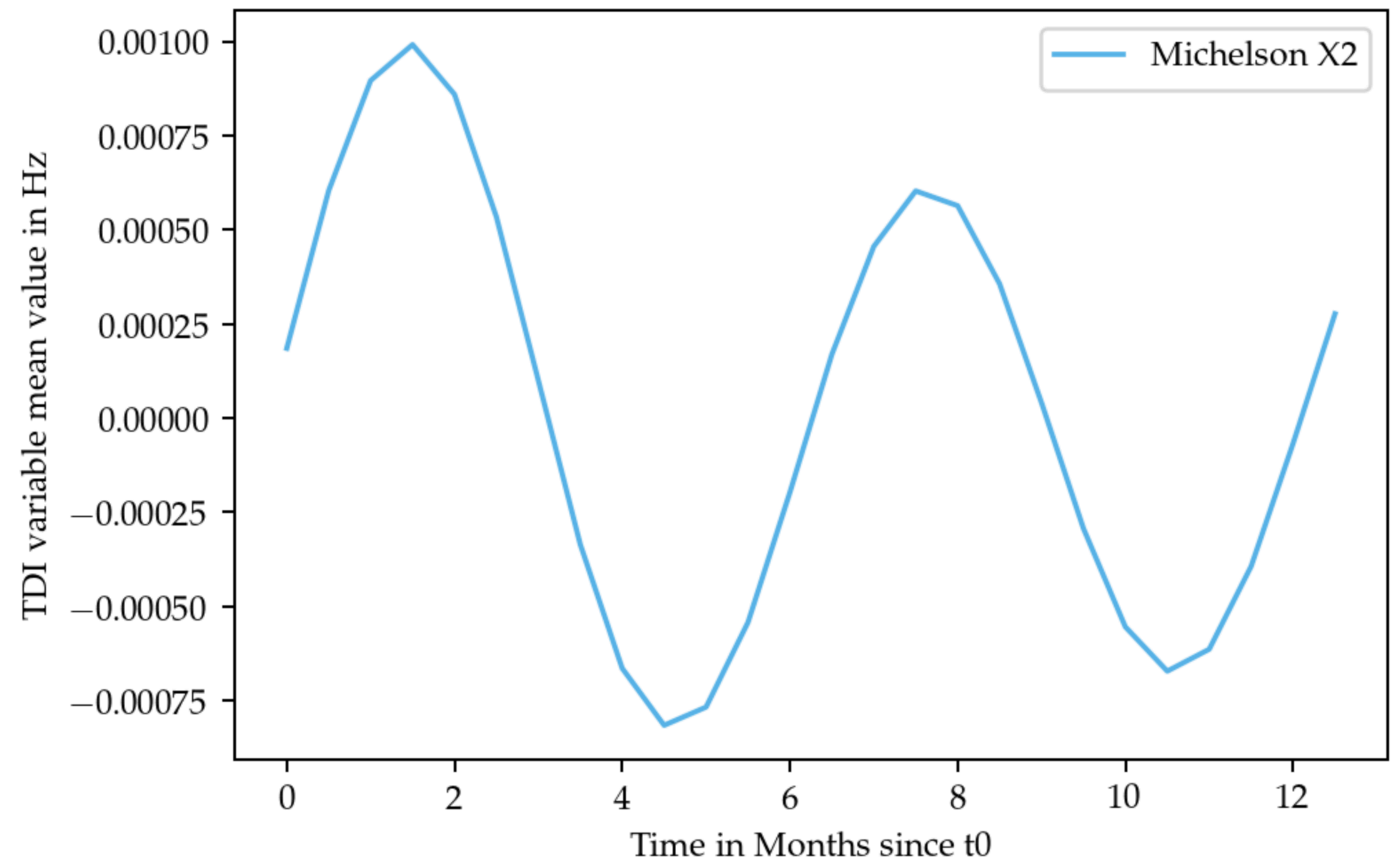
Measurements
in clock time:



Clock Noise

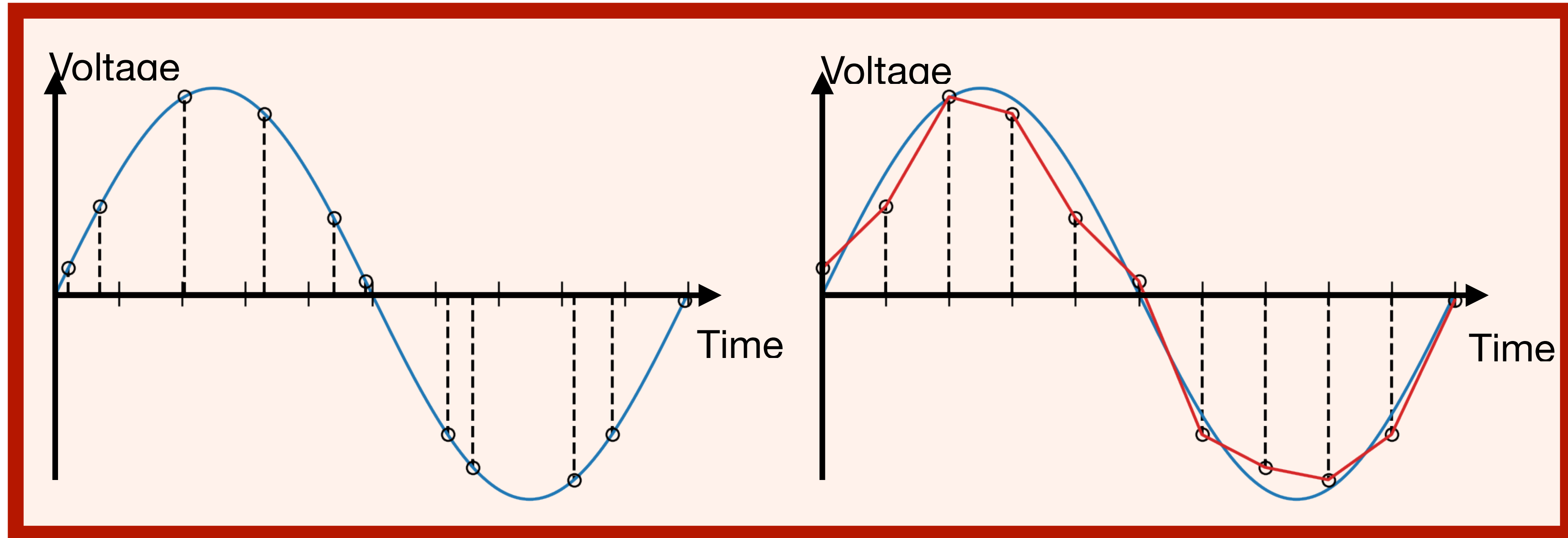
... with Perfect Pseudoranges

- We can show that we get $X^{\hat{\tau}_1}(\tau) = X^t(\tau - \delta\hat{\tau}_1(\tau)) \approx X^t(\tau) - \dot{X}^t(\tau)\delta\hat{\tau}_1(\tau)$
- The mean value of $\dot{X}^t(\tau)$ varies between ± 1 mHz, with a period of 2/year
- This is 10 orders of magnitude below the previous coupling to 10 MHz beatnotes!
- Remark: noise-free variables still need to be sync. to TCB
- Remark 2: large drift can be subtracted — should we?



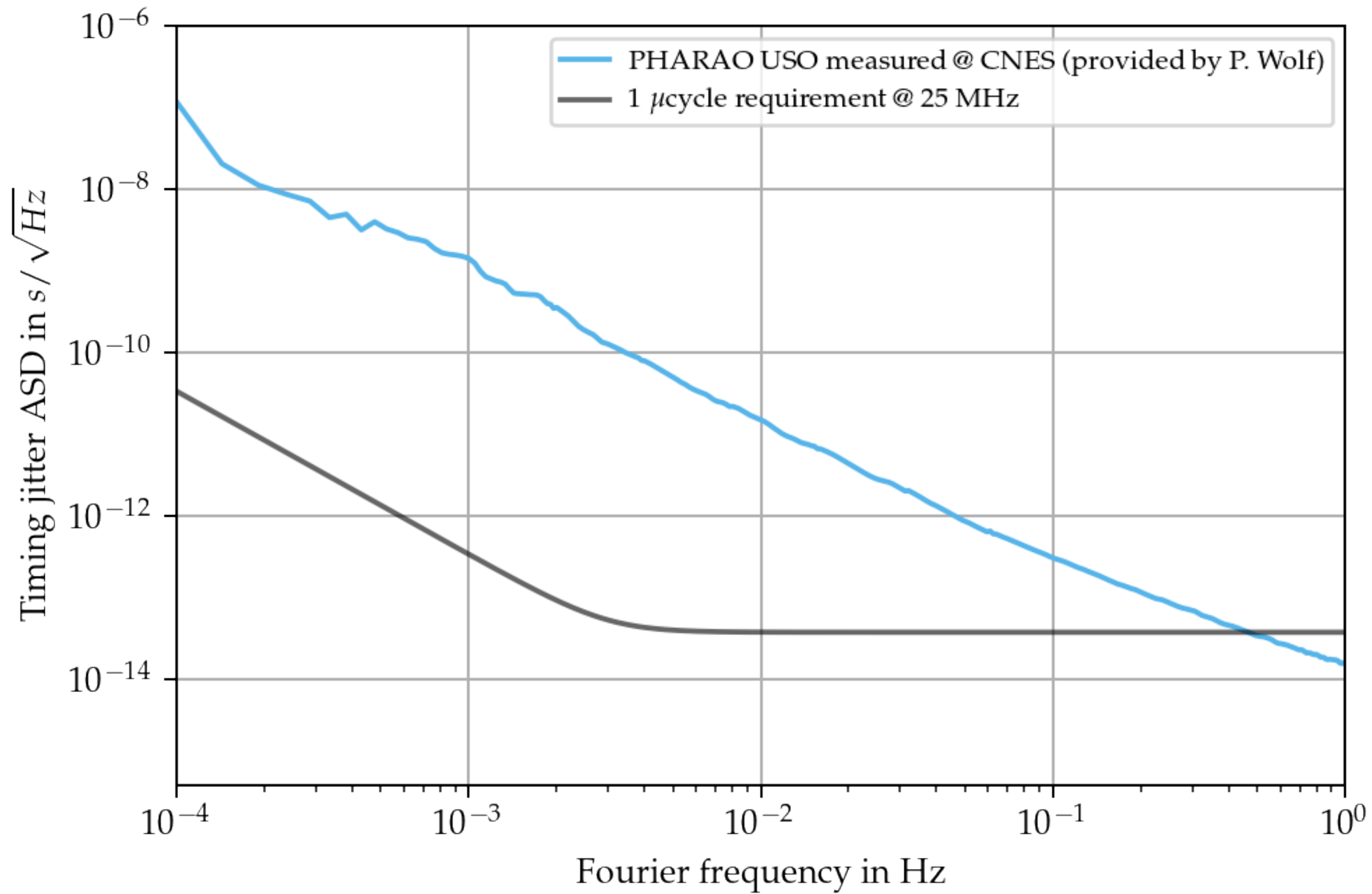
Clock Noise

... With Imperfect Pseudorange



- 25 MHz beatnotes require 40 fs/sqHz timing precision for μ cycle signals: clocks not good enough!
- Correct clock noise alongside laser noise by properly time-shifting each individual sample
- Any time shift applied in TDI inherits same timing requirement, if applied to total phase/frequency

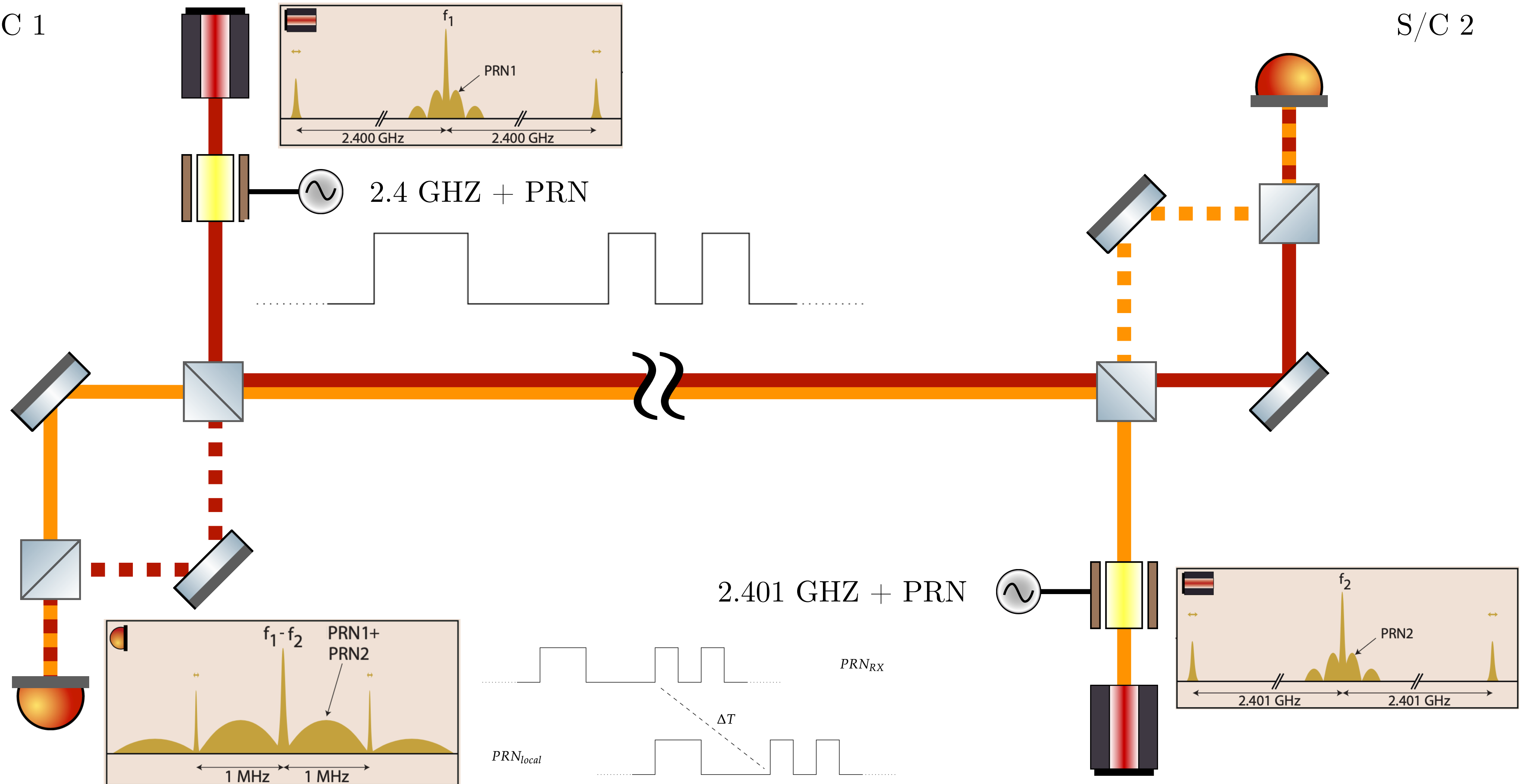
Clock comparison performance



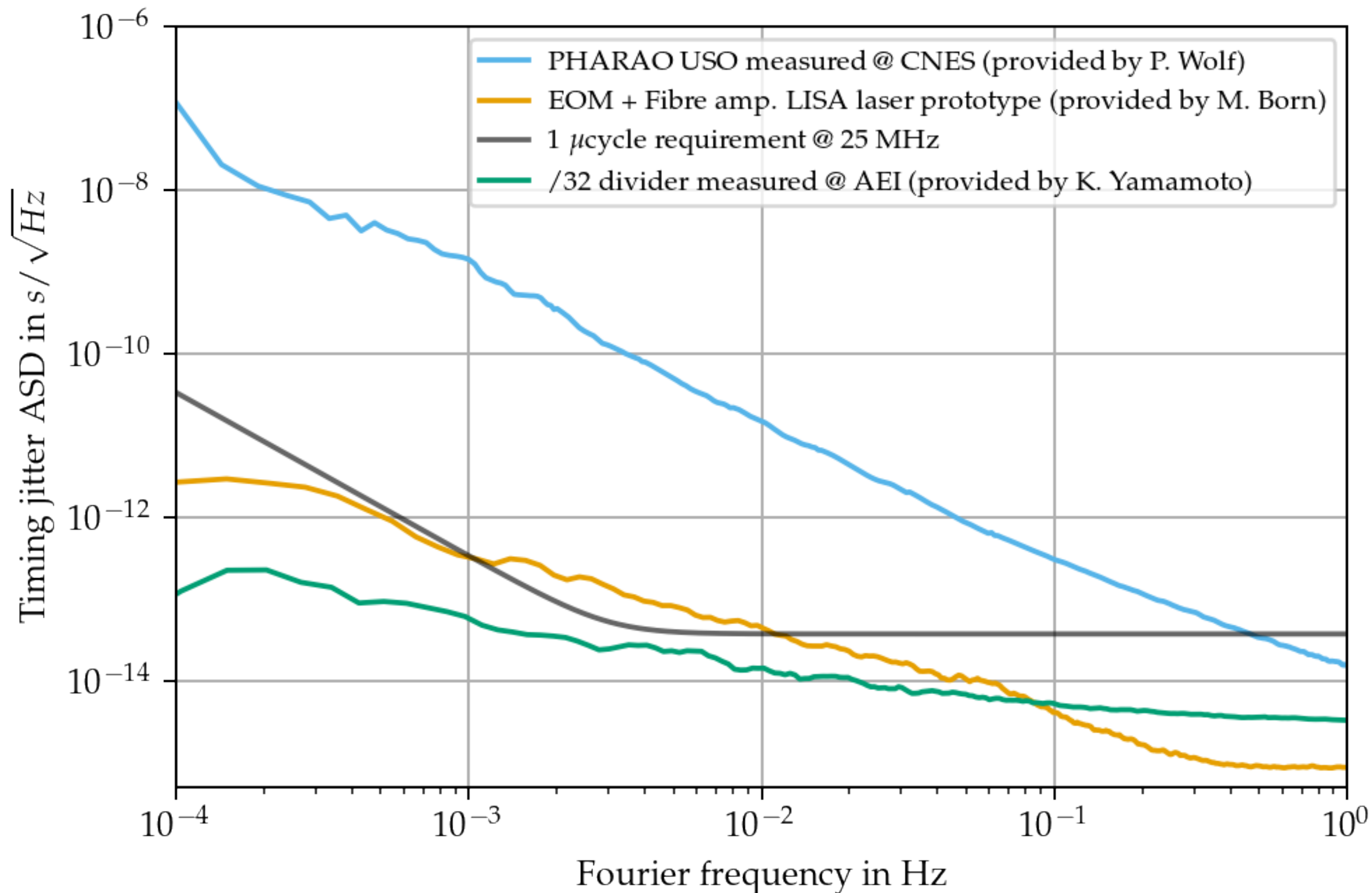
Sideband & PRN Modulation

S/C 1

S/C 2



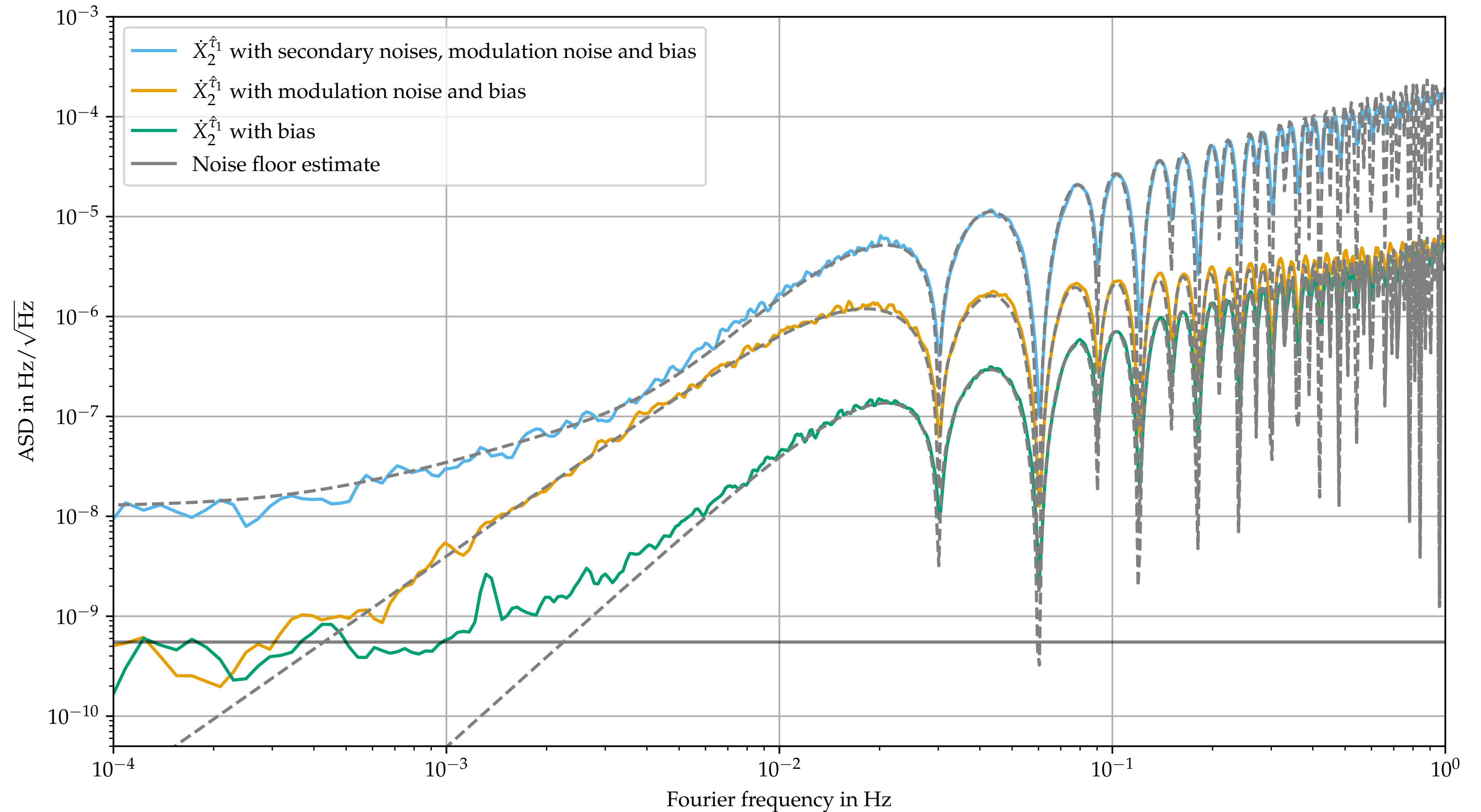
Clock Compared Performance



- PRN and sidebands allow measurement of pseudorange at $40 \text{ fs Hz}^{-0.5}$ level
- Absolute value of pseudorange accurate to $\approx 3 \text{ ns}$ (1 m)
- Clock synchronisation to globale frame accurate to $\approx 0.1 \text{ ms}$ (30 km)

TDI Performance

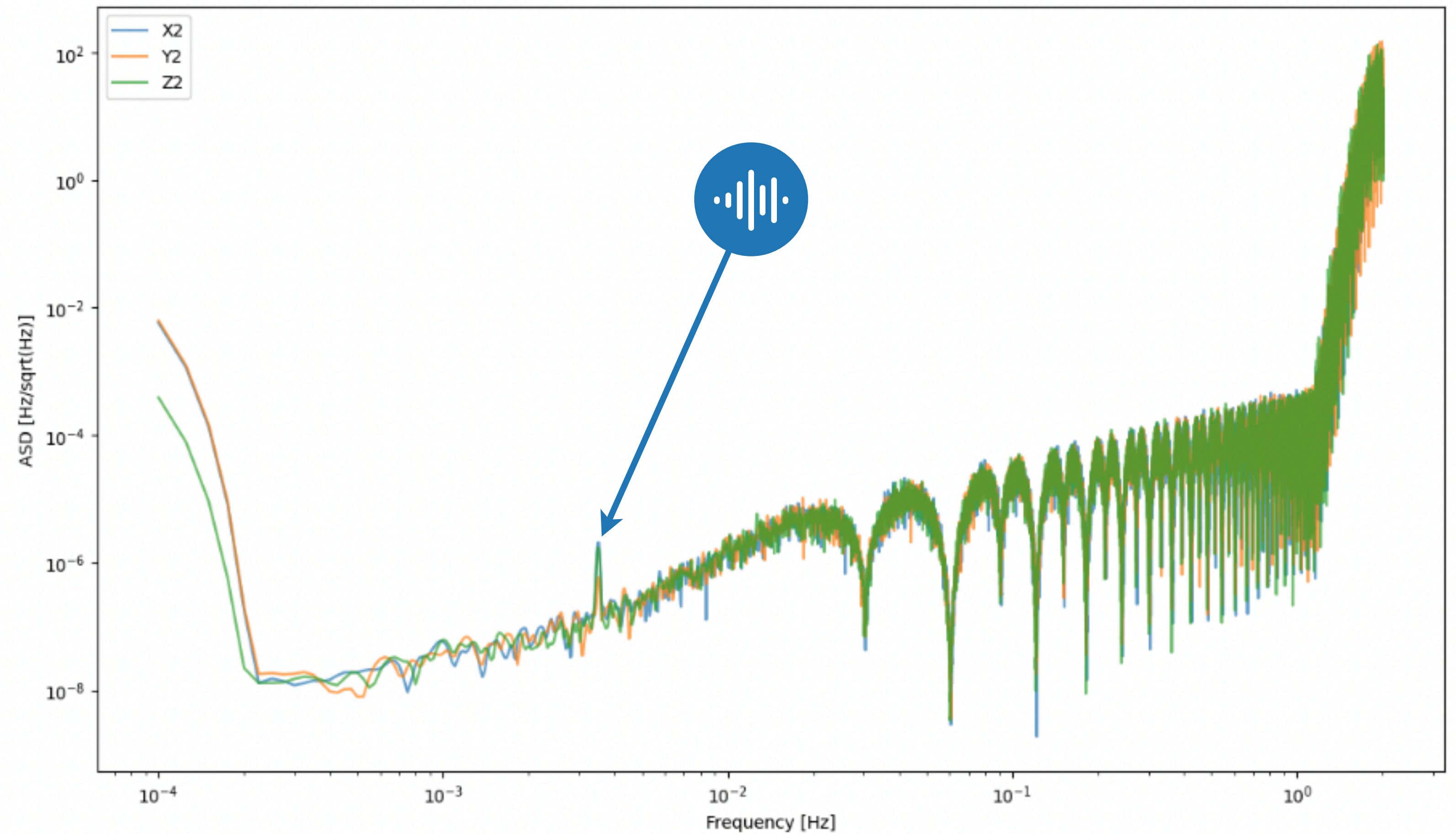
- Perform simulation with
 - Realistic orbits
 - Realistic laser, clock, sideband, PRN noises
 - Ultimately limiting secondary noises
- Performance is unaffected by large clock drifts and offsets
- Noise due to clock correction depends on the beatnote frequency and is nonstationary



Time delay interferometry without clock synchronisation,
O. Hartwig, J.-B. Bayle, M. Staab, A. Hees, M. Lilley, P. Wolf. arXiv:2202.01124

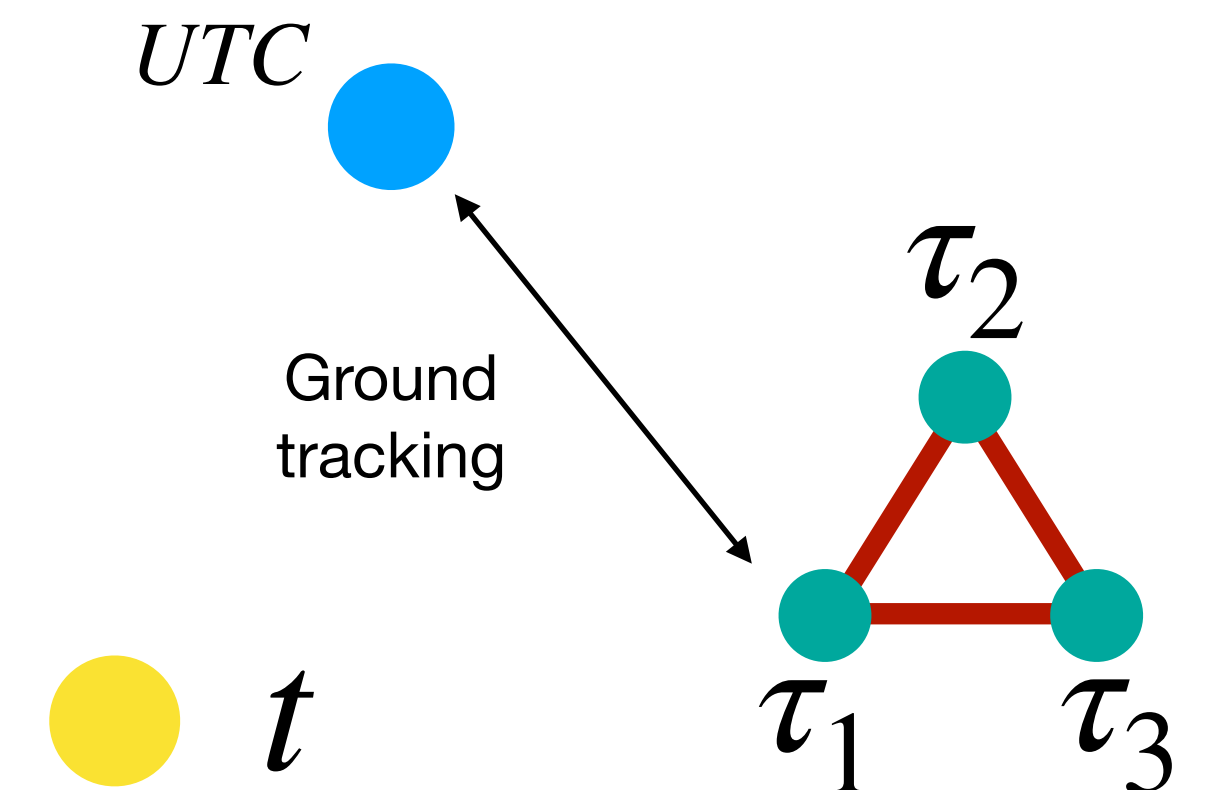
Current Outputs

- As first step, we consider a single verification binary
- Amplitude is boosted to give 4 year SNR in just 3 days
- Signal is clearly visible in TDI data



Time Synchronisation & Orbit Calculation

- After noise reduction, still need to synchronize resulting TDI channels to a global time frame at about 1ms accuracy
 - Use directly clock information from ground tracking
- For the parameter estimation, we need estimates of the orbits and light travel times to compute the response function
 - First try: directly feed-forward reconstructed orbits provided by MOC
 - Also compute LTTs directly from MOC orbits (≈ 1 ms accuracy)
- Impact of these procedures is one output of this study



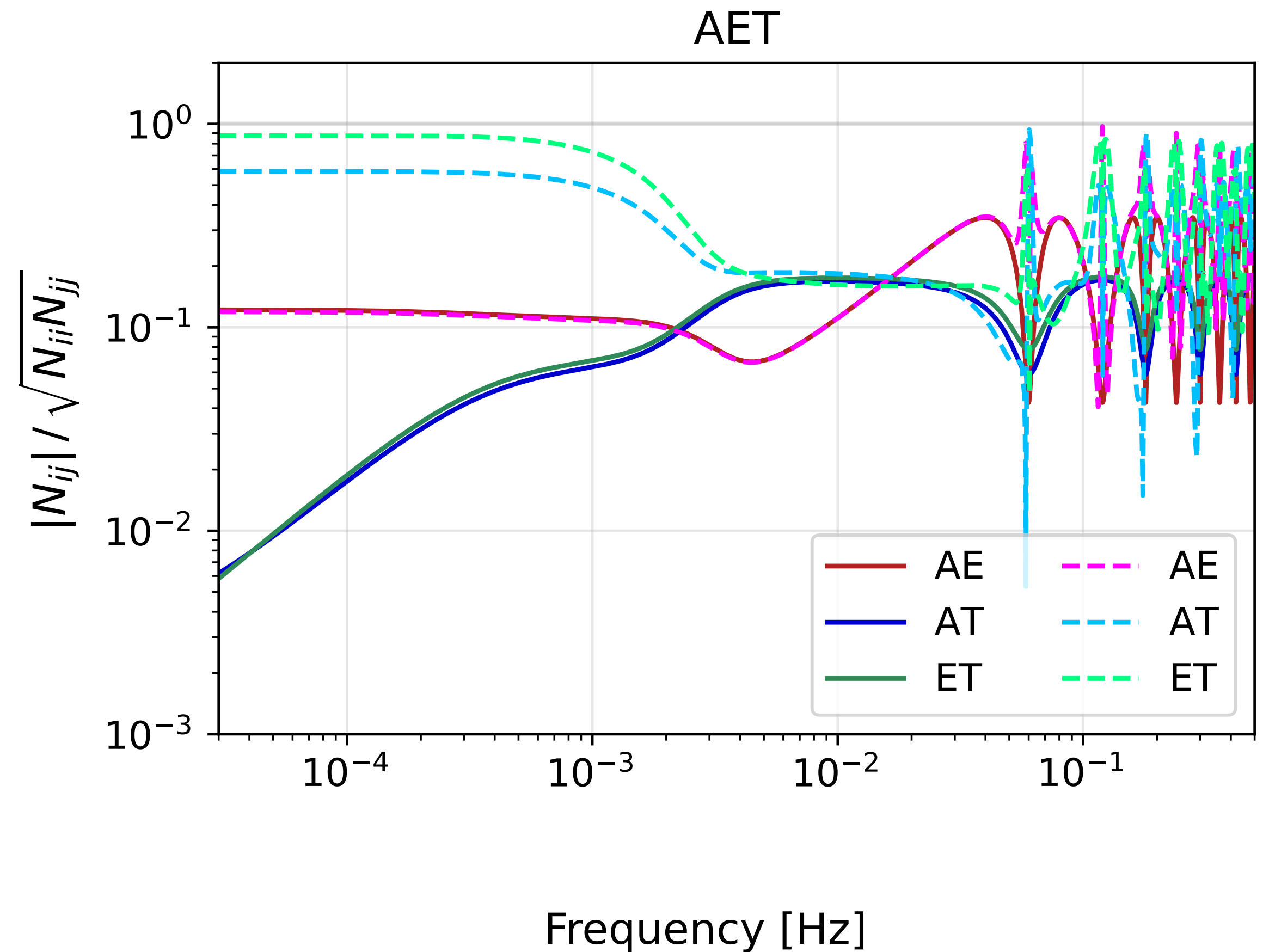
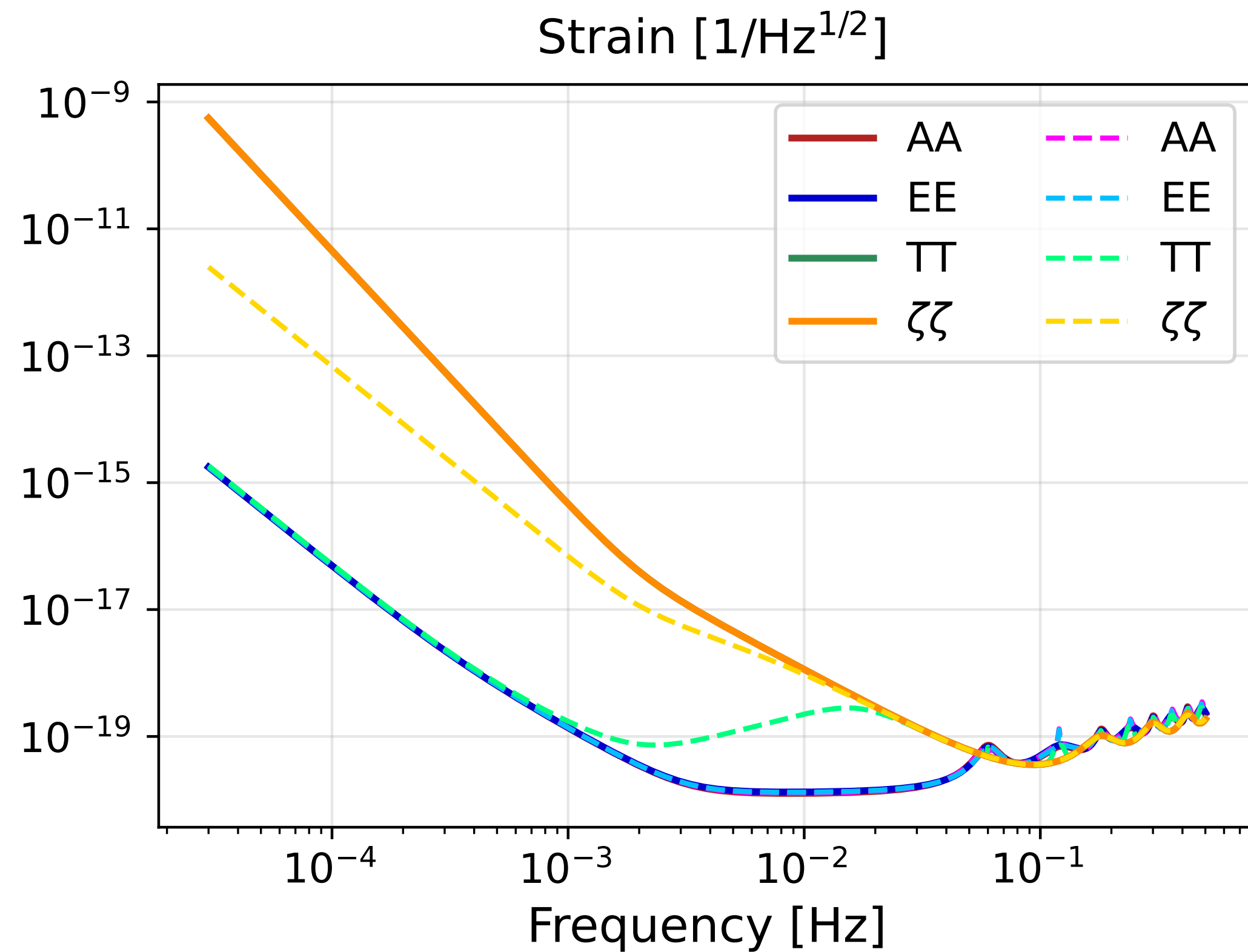
Orthogonal Channels

- Once synchronized, we can combine multiple channels to construct quasi-orthogonal channels. For example,

$$A = \frac{Z - X}{\sqrt{2}}, \quad E = \frac{X - 2Y + Z}{\sqrt{6}}, \quad T = \frac{X + Y + Z}{\sqrt{3}}$$

- **Warning: these are not orthogonal in realistic scenarios!**
 - Arm lengths and individual noise levels not equal
- Impact under investigation...
- Could use other base channels, better orthogonalization, or skip *AET* and use the full covariance matrix

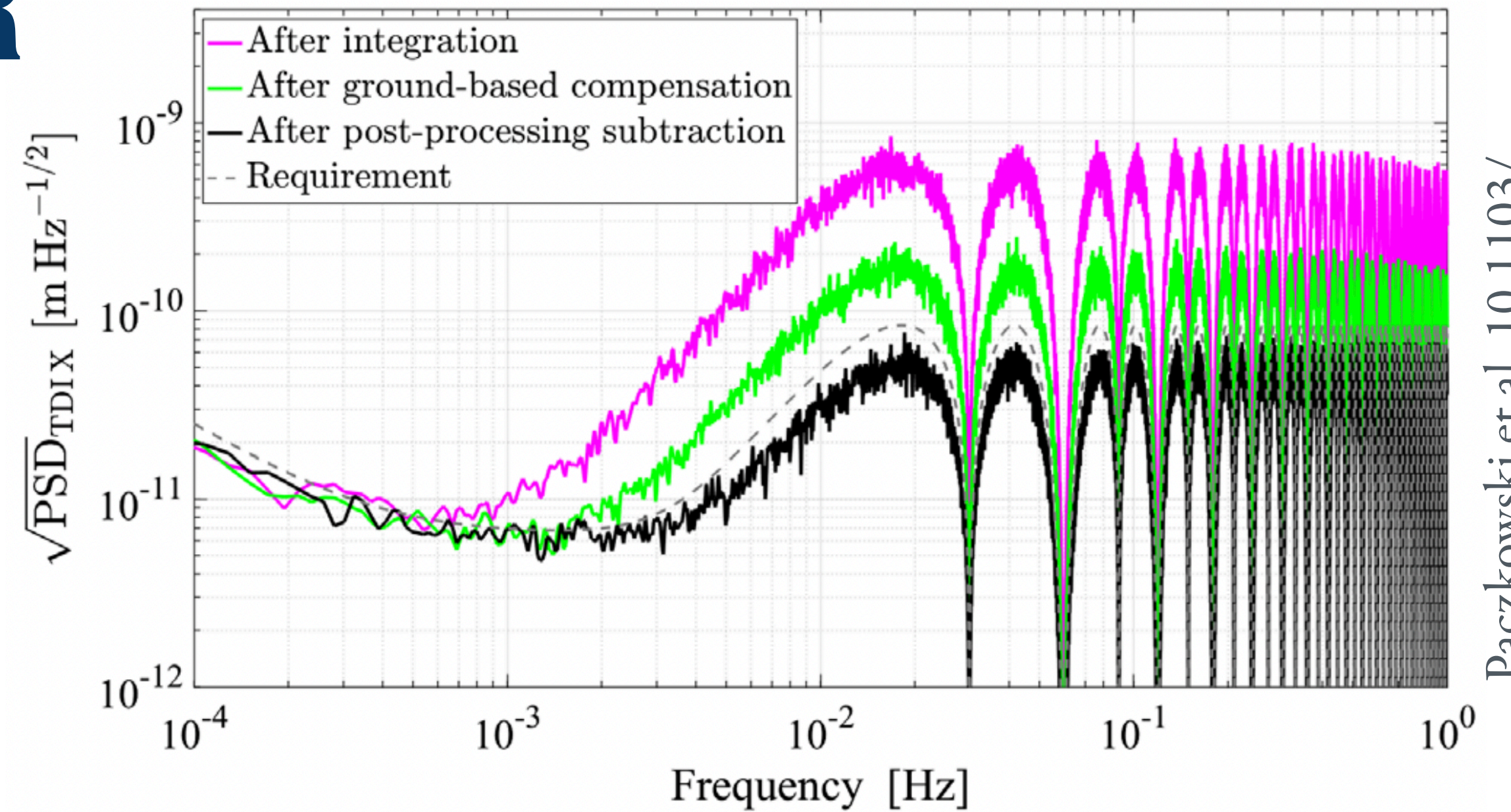
Analytical Michelson



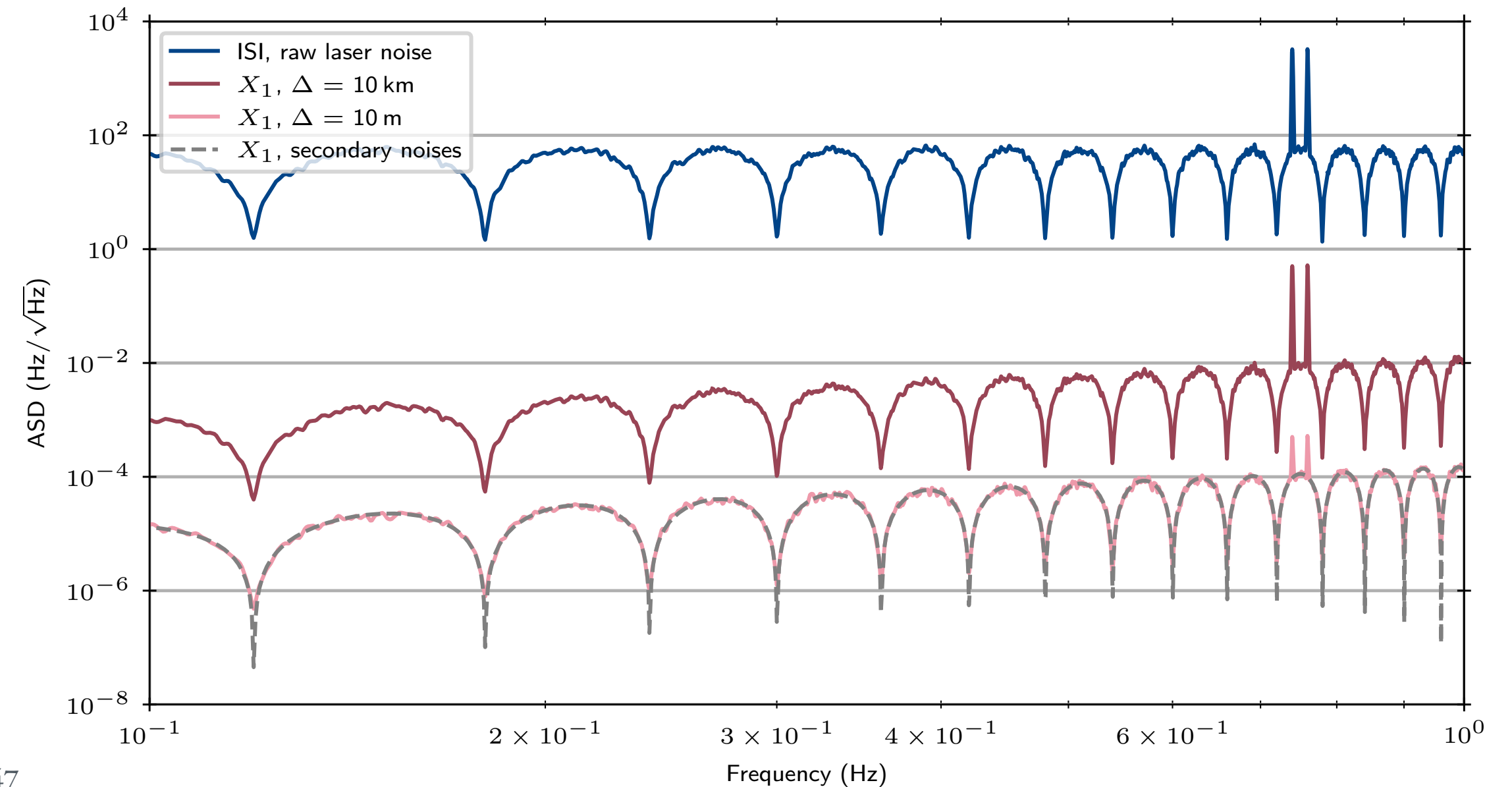
- Assume realistic (but static) arm length mismatches
- Assume noise levels drawn from normal distribution with $\sigma = 0.2$

A Word on TTL & TDIR

- Some processing steps envisioned as part of L0-L1 will require to fit some parameters to the data
- TTL coefficients are not known sufficiently well a-priori
 - Fit DWS measurement coupling factors by minimizing the noise
- Pseudorange measurements might contain additional unmodeled biases
 - Fit ranging bias by minimizing noise in TDI combinations



Paczkowski et al. 10.1103/PhysRevD.106.042005



Staab et al., in prep.

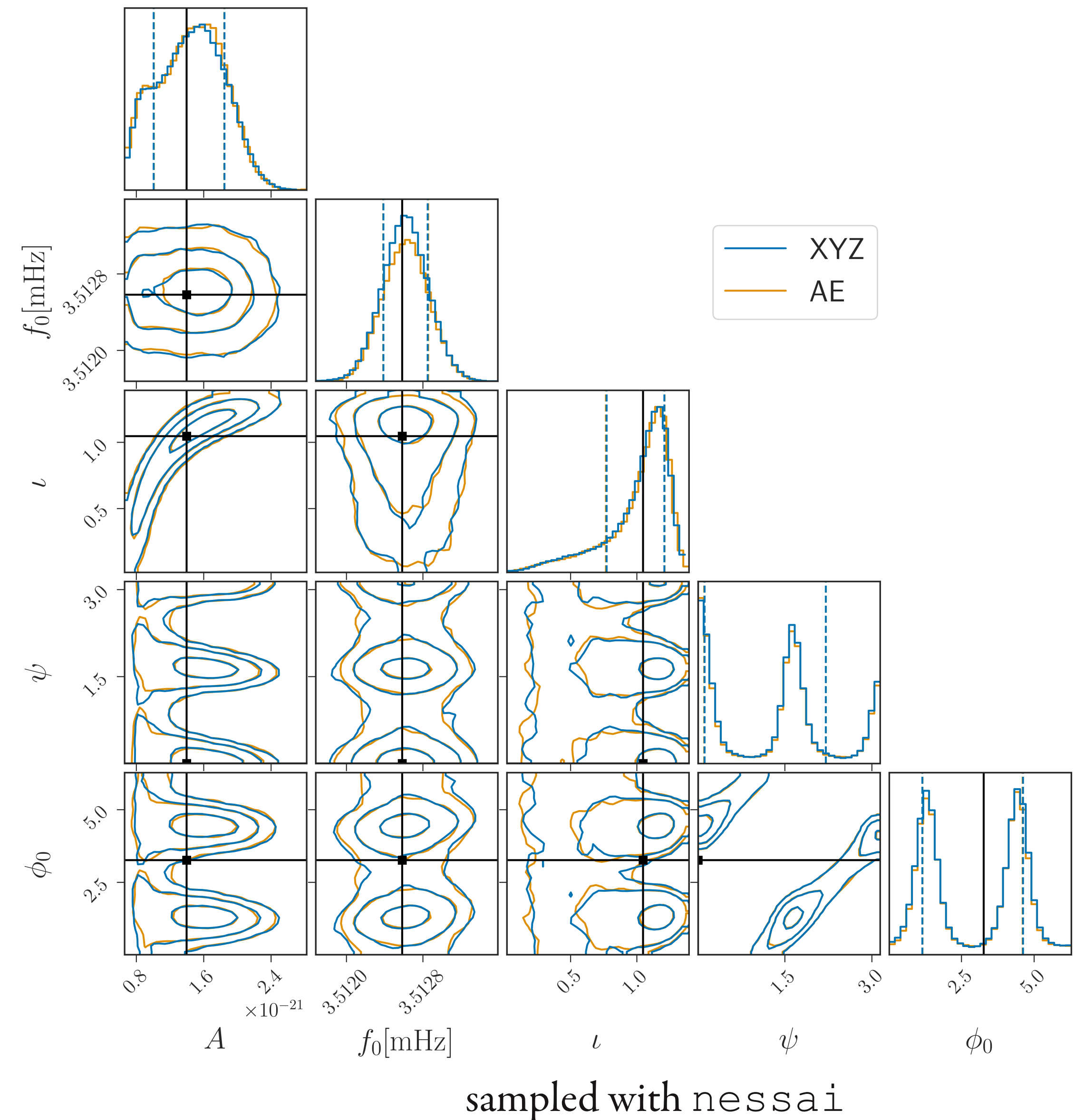
L1-L2 Parameter Estimation

Thanks Christian Chapman-Bird!



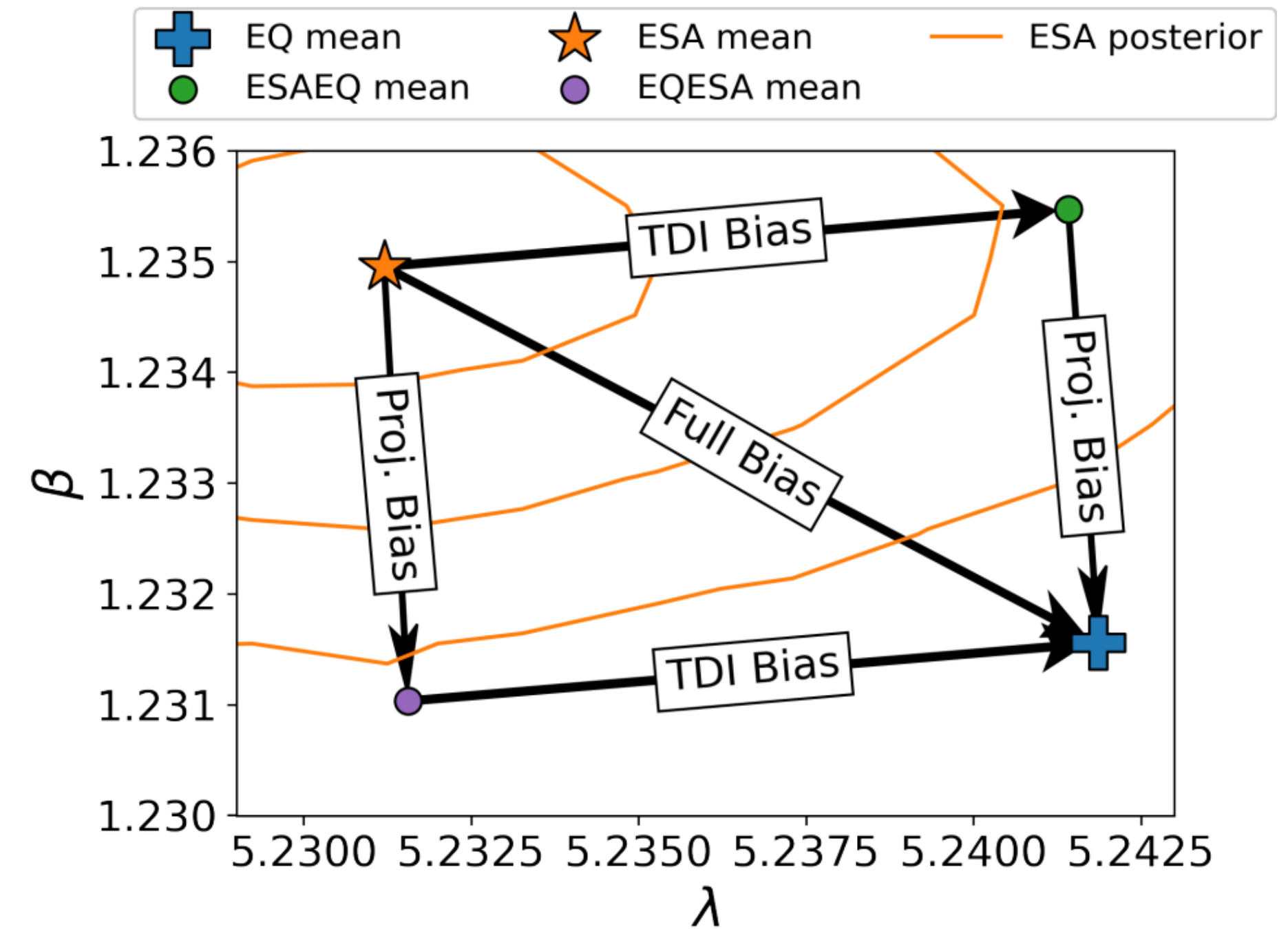
Current Progress

- Single galactic binary with optimal SNR of 100 for a 4-year dataset
 - For ease of testing, reduce to 3 days of data and rescale amplitude
 - Sky position fixed: "verification binary"
 - Equal-armlength orbits and aforementioned primary/secondary noise sources enabled
- Parameters are recovered well (except phase, likely an error with epochs somewhere!)
- We see good agreement between working in 2nd-generation $AE(T)$ or XYZ , but for more realistic orbits we expect biases to emerge if diagonal covariance matrix is assumed



Next Steps

- Adapt the FastGB waveform model to incorporate
 - More realistic orbits, including unequal and time-varying armlengths
 - Use of orbital information obtained from ground tracking, instead of evolving a dynamical model
 - Eventually, merge these changes with existing GBGPU waveform model
- Extend simulation duration to 4 years and enable further noise sources
 - Verify that sky localisation and frequency derivative inference are performed successfully
- Experiment with various noise sources to probe the resulting impact on parameter estimation
 - Explore under which scenarios parameter estimation will incur biases



Conclusion & Outlook



Conclusion & Outlook

- Many analysis methods to extract source parameters under development
- These methods often rely on simplifying assumptions, not necessarily reflecting the full complexity of the LISA data
- We work on checking (some of) these assumptions by building a (more) realistic simulation-processing-analysis pipeline
- We go from simple configurations (close to current LDC) and slowly add realistic features and processing elements to check that they do not break anything
- Activity started by defining the target configuration and run the pipeline with a simple configuration – PE works (mostly) as expected!