Nuclear Physics at the Edge of Stability

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October 28, 2022





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Introduction

What is the Drip Line?



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Introduction





Shell model

The nuclear Shell Model (SM) is used to describe the atomic nuclei. It divides the nuclei in:

- Inert core
- Valence space.
- This is a closed quantum system (CQS) and thus we can't describe
 - Reactions
 - Decay
 - Resonances.



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Shell model

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- Inert core
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This is a closed quantum system (CQS) and thus we can't describe

- Reactions
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- Resonances.

A solution is to extend the SM to an open quantum system (OQS).



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Berggren basis



$$\int_0^\infty f(r)dr = \int_0^R f(r)dr + \int_0^\infty f(R + x \cdot e^{i\theta})e^{i\theta}dx$$

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Why use the Berggren basis?





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Berggren basis

We generate a Berggren basis by solving the Schrödinger equation:

$$u_\ell''(r) = \left[rac{\ell(\ell+1)}{r^2} + v_\ell(r) - k^2
ight] u_\ell(r), \quad k^2 \in \mathbb{C}$$

Different inner product in the vector space. Time conjugate + Hermitian conjugate

$$\langle \tilde{\Psi} | \Phi
angle = \int dx \, \tilde{\Psi}^*(x) \Phi(x) o \langle \mathcal{O}
angle \in \mathbb{C}$$

But $N^2 = \int_0^\infty u^2(r) dr$ diverges! We use complex scaling to regularize:

$$N^{2} = \int_{0}^{R} u^{2}(r)dr + \int_{0}^{\infty} u^{2}(R + x \cdot e^{i\theta})e^{i\theta}dx$$

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Gamow Shell Model (GSM)

Practical applications:

$$\int_{L^+} u_k(r) u_k(r') \approx \sum_i^{N_d} u_i(r) u_i(r')$$

Discretized contour in k-plane

Normalized discrete single particle Berggren basis $\{\phi_{\ell,\eta}\}$, which can be used to build a many-body basis

$$\sum_{n} |SD_{n}\rangle \langle \widetilde{SD_{n}}| \approx 1 \qquad |SD\rangle = |\phi_{1}\phi_{2}...\phi_{M}\rangle$$
Many-body completeness relation
N. Michel et al., Phys.Rev.Lett. 89, 042502 (2002)

$$H|\Psi\rangle = E|\Psi\rangle \quad |\Psi\rangle = \sum_{n} c_{n}|SD\rangle$$

Individual reaction channels cannot be defined in the Slater determinant representation of GSM.

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Coupled channel formulation of GSM (GSM-CC)

The channel wave-function is defined as

$$|(c,r)\rangle = \mathcal{A} \left\{ |\Psi_T^{J_T}\rangle \otimes |\Psi_P^{J_P}\rangle \right\}_{M_A}^{J_A}.$$

$$\square = \sum_m c_m |SD_m\rangle \text{ from GSM}$$
The quantum number $c \to \{Z - z, N - n, J^T; z, n, \ell, J_{int}, J_P\}.$
One can define entrance and exit channels with correct asymptotics.
The wave functions are

$$|\Psi_{M_A}^{J_A}\rangle = \sum_c \int_0^\infty \left(\frac{u_c(r)}{r}\right) |(c,r)\rangle r^2 dr.$$

The Schrödinger equation becomes the coupled-channel equation

$$\sum_{c} \int_{0}^{\infty} dr \, r^{2} (H_{cc'}(r,r') - EN_{cc'}(r,r')) \frac{u_{c}(r)}{r} = 0.$$

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Methodology

- Model space: inert core + valence particles ⇒ studies of heavier systems are possible.
- Calculations in cluster orbital shell model coordinates.

Y Suzuki and K Ikeda, Phys.Rev.C 38, 410 (1988)

 Two-body part: FHT interaction + Coulomb.

H. Furutani et al., Prog. Theor. Phys. 62, 981 (1979)

• Cluster part with a N³LO chiral effective interaction.





Structure of ⁷Be and ⁴He(³He,³He) cross-section



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Structure of ⁷Be and ⁶Li(p,p) cross-section



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Structure of ⁷Li and ⁴He(³H,³H) cross-section



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Near threshold effects in the spectroscopic factors and energies



- Interference phenomenon between resonant and non-resonant states.
- Spectroscopic factor (SF) \rightarrow measure of the occupancy of a single particle shell.

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Multichannel threshold effects $[^{7}Li (5/2_{1}^{-})]$



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Multichannel threshold effects $[^{7}Li (5/2_{1}^{-})]$



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Multichannel threshold effects $[^{7}Be(3/2_{2}^{-})]$



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Multichannel threshold effects $[^{7}Be(3/2_{2}^{-})]$



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Multichannel threshold effects



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Is this nonsense?



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Conclusions

- GSM-CC provides the microscopic open quantum system description of spectra and reactions in multichannel and multiple mass partition framework.
- First applications of GSM-CC in multichannel calculations with different mass partitions:

• ⁸Be (⁴He + ⁴He, ⁷Li + p, ⁷Be + n)

Outlook:

- Calculations for heavier systems with different cores like ⁴⁰Ca.
- Radiative capture reactions with cluster projectiles.
- Transfer and knockout reactions.

Conclusions

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Outlook:

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Thank you for your attention!

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Back up

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The overlap method

Why Lanczos doesn't work?

- Resonant A-body states are surrounded by many scattering A-body states.
- One cannot differentiate between resonant and scattering states given by the Lanczos method.

The overlap method consist of two steps:

- $\label{eq:Fully diagonalize with an incomplete basis of bound and resonant pole states. From this we extract a pivot <math display="inline">|\Psi_0\rangle.$
- 2 Using the full Berggren basis, find $|\Psi\rangle$ that optimizes the overlap $|\langle \Psi_0 | \Psi \rangle|$.



Coupled channel formulation of GSM (GSM-CC)

One separates the Hamiltonian as

Normalizing $\langle \Psi_{p}^{J_{p}} | \Psi_{p}^{J_{p}} \rangle = \delta(\mathcal{K}_{CM} - \mathcal{K}'_{CM})$ is difficult.

$$|\Psi_{p}^{J_{p}}
angle^{HO} = \sum_{N} C_{N}^{HO} |SD_{N}
angle^{HO} = \sum_{n} C_{n} |SD_{n}
angle_{N}$$

Target SD generated by GSM

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Old solution

We begin by tranforming the problem to a standard eigenvalue problem

- In matrix form: $\mathcal{HU} = \mathcal{EOU}$.
- If we do the substitutions $\mathcal{W} = \mathcal{O}^{1/2}\mathcal{U}$ and $\mathcal{H}_m = \mathcal{O}^{-1/2}\mathcal{H}\mathcal{O}^{-1/2}$.
- the CC equation becomes $\mathcal{H}_m \mathcal{W} = E \mathcal{W}$. The CC-equation to solve becomes:

$$\left[\frac{\hbar^2}{2\mu_c}\left(-\frac{d^2}{dr^2}+\frac{l_c(l_c+1)}{r^2}\right)+V_c^{loc}(r)\right]w_c(r)+\sum_{c'}\int_0^{\infty}V_{cc'}^{non-loc}w_c'(r)dr'=(E-E_{T_c})w_c(r),$$

with

$$u_c(r) = w_c(r) + \sum_{c'} \int_0^\infty r'^2 [\mathcal{O}^{1/2}(\mathcal{O}-1)\mathcal{O}^{1/2}]_{cc'}(r,r') \frac{w_{c'}(r')}{r'}.$$

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To tolve the CC-equation we use the method of modified equivalent potential.

$$W''(r) = M^{eq}(r)W(r) + S^{eq}(r)$$

where

•
$$M_{cc'}^{eq} \rightarrow M_{cc'}^{eq}(V_{cc'}^{loc}, V_{cc'}^{non-loc})$$

• $S_{cc'}^{eq} \rightarrow S_{cc'}^{eq}(V_{cc'}^{non-loc})$

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Solution via Green Functions.

For $\hat{H}|\Psi\rangle = E|\Psi\rangle$ we make the ansatz: • $\hat{H} = \hat{H}^{(0)} + \hat{H}_{rest}$ • $|\Psi\rangle = |\Psi^{(0)}\rangle + |\Psi_{rest}\rangle$ • $\hat{H}^{(0)}|\Psi^{(0)}\rangle = E|\Psi^{(0)}\rangle$

We end up with

$$(\hat{H} - E) |\Psi_{rest}\rangle = -\hat{H}_{rest} |\Psi^{(0)}\rangle \rightarrow M_E |\Psi_{rest}\rangle = |S\rangle.$$

Generating a Berggren basis $\{|n, c\rangle\}$:

•
$$(\Psi_{rest})_{n,c} = \langle n, c | \Psi_{rest} \rangle$$

• $(M_E)_{n',c',n,c} = \langle n', c' | (\hat{H} - E) | n, c \rangle$
• $S_{n'.c'} = \langle n', c' | S \rangle$

We now solve $\Psi_{rest} = M_E^{-1}S$

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Interaction

The GSM Hamiltonian is:

$$H = \sum_{i} \left[\frac{p_i^2}{2m} + V_{WS}(r_i) + V_C(r_i) \right] + V_{res,12}.$$

The Woods-Saxon (WS) potential given by

$$V(r) = -V_{WS}\dot{f}(r) - 4V_{so}(\vec{l}\cdot\vec{s})\frac{1}{r}\left|\frac{df(r)}{dr}\right|,$$

and the WS form factor

$$f(r) = \left[1 + \exp\left(\frac{r-R_0}{d}\right)\right]^{-1}.$$

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Interaction

The FHT H. Furutani et al., Prog. Theor. Phys. 62, 981 (1979) interaction is written in terms of spin-isospin operators Π_{ST} A. DeShalit and H. Feshbach, (1974):

$$V_c(r) = \sum_{S,T=0,1} V_c^{ST} f_c^{ST}(r) \Pi_{ST}$$

$$V_{LS}(r) = (\vec{L} \cdot \vec{S}) V_{LS}^{11} f_{LS}^{11}(r) \Pi_{11}$$
$$V_{T}(r) = S_{ij} \sum_{T=0,1} V_{T}^{1T} f_{T}^{1T}(r) \Pi_{1T},$$

where $S_{ij} = 3(\vec{\sigma}_i \cdot \hat{r})(\vec{\sigma}_j \cdot \hat{r}) - \vec{\sigma}_i \cdot \vec{\sigma}_j$, $f_i^{ST}(r)$ are radial form factors and V_i^{ST} are parameters to be optimized.

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We can use the standard cross-section formulas. The channel wave-function has the asymptotic behavior

$$\mu_c^{eJ_A^{\pi}}(r) \stackrel{r o \infty}{ o} \delta_{ce} F_{\ell_e \eta_e}(k_e r) - T_{ec}^{J_A} H^+_{\ell_c \eta_c}(k_c r)$$

The cross-section is

$$\frac{d\sigma_{\tilde{e}\to\tilde{c}}}{d\Omega}(\theta) = \frac{1}{(2J_{int}+1)(2J_T^{\tilde{e}}+1)} \sum_{M_{\rho}^{\tilde{e}}M_t^{\tilde{e}}M_t^{\tilde{e}}M_{\rho}^{\tilde{c}}M_t^{\tilde{c}}} \frac{K_{CM}^{\tilde{c}}}{K_{CM}^{\tilde{e}}} \left| f_{\tilde{e}M_{\rho}^{\tilde{e}}M_t^{\tilde{e}}\to\tilde{c}M_{\rho}^{\tilde{e}}M_t^{\tilde{c}}}(\theta) \right|^2$$

where the form factor is obtained from the T-matrix.

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Previous studies using GSM-CC

What has been achieved so far with the channel representation:

• ¹⁸Ne(p, p')

Y Jaganathen et al., Phys.Rev.C 89, 034624 (2014)

• $^7Be(p,\gamma)^8B$

K Fossez et al., Phys.Rev.C 91, 034609 (2015)

• ${}^{4}He(d,d)$

A Mercenne et al., Phys.Rev.C 99, 044606 (2019)



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Previous studies using GSM-CC

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1.6• ${}^{18}Ne(p, p')$ 1.4 1.2 $S (10^2 \text{ barn eV})$ 1.0 • $^7Be(p,\gamma)^8B$ 0.8K Fossez et al., Phys.Rev.C 91, 034609 (2015) 0.60.4• ${}^{4}He(d,d)$ 0.20.0 2.5 3.0 1.01.5

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 $E_{\rm c.m.}$ (MeV)

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Previous studies using GSM-CC

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A Mercenne et al., Phys.Rev.C 99, 044606 (2019)

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