

Towards new approaches to cluster detection for cosmology

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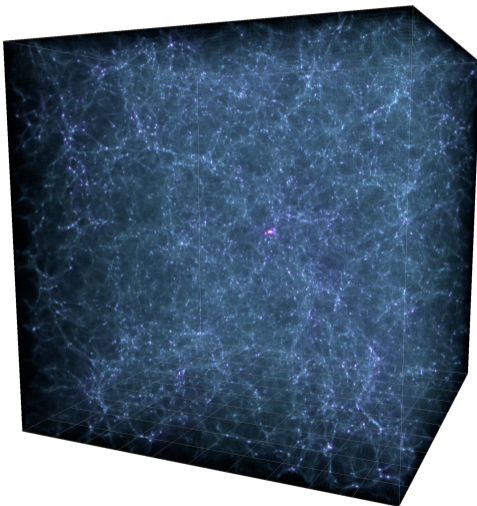
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- 3 Game trees
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- 5 A clustering game
- 6 Conclusions

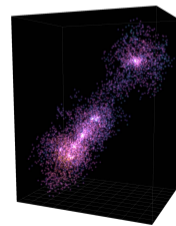
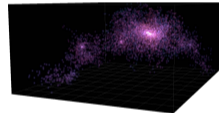
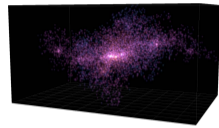
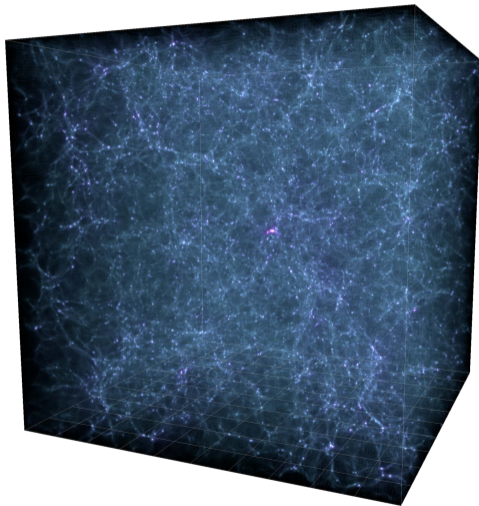
Galaxy clusters

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Halos in simulations



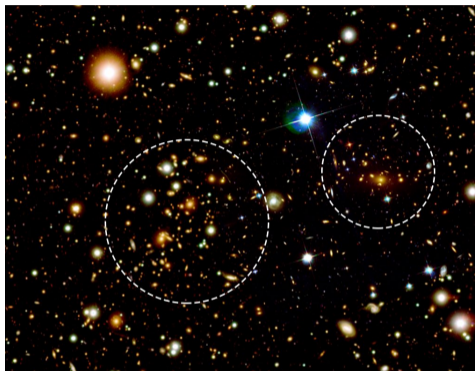
Halos in simulations



Galaxy clusters in observations



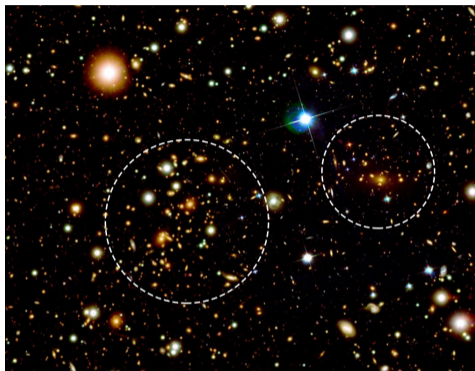
Galaxy clusters in observations



Observational cosmology using galaxy clusters

Galaxy clusters as building blocks of cosmological analyses.

Galaxy clusters in observations



Observational cosmology using galaxy clusters

Galaxy clusters as building blocks of cosmological analyses.

Main problem of this presentation in the context of LSST

How to detect galaxy clusters?

Galaxy cluster detection

Clusters in simulations

- Input: particles

Simulation cluster detectors

- Spherical Over Density (SOD)
- Friends-of-Friends (FoF)
- ...

Clusters in observations

- Input: sources/galaxies

Observational cluster detectors for LSST

- redMaPPer (Rykoff et al. 2013)
- WaZP (Benoist 2014)
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Improving cluster detection for observational cosmology

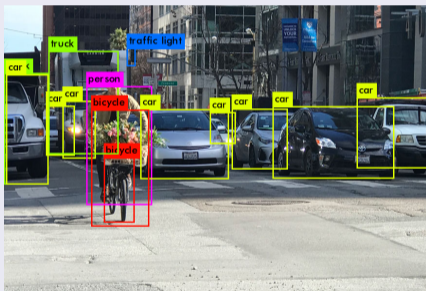
Can we use machine-learning to improve cluster detection for observational cosmology?

Clusters and computers

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Using deep neural networks to detect galaxy clusters

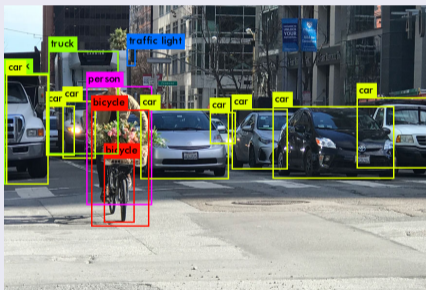
Idea: try to adapt YOLO



You Only Look Once (Redmon et al. 2015)

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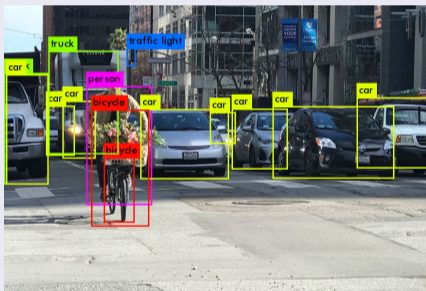
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Technical problems

- Ultra large images
- More than 3 colors

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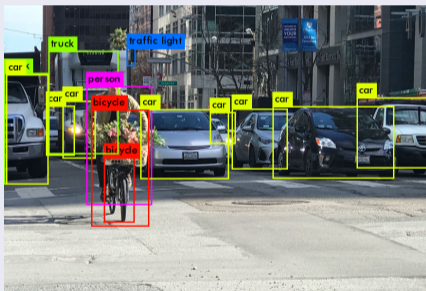
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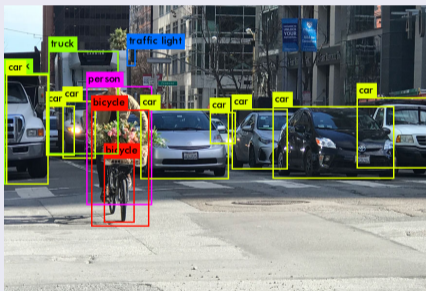
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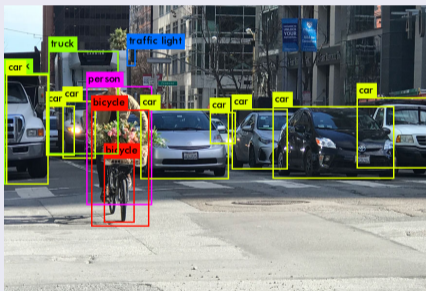
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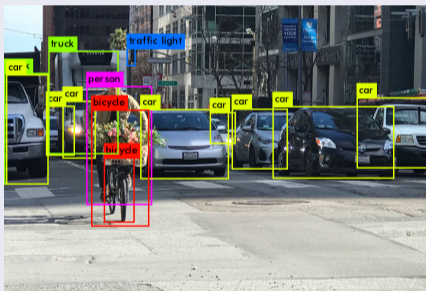
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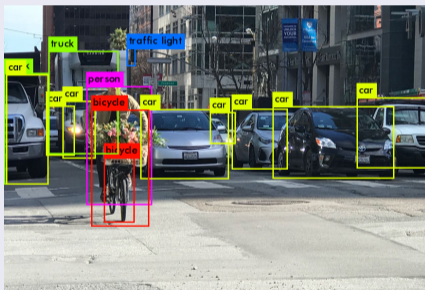
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Direction of investigation

Physics-guided machine-learning?

A problem of definition

The fundamental problem of clusters

- No universal definition: many definitions and parameterization across simulations and observations
- Computers require definitions: implicit or explicit parameterization in algorithms
- Algorithms \Leftrightarrow Definitions

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Physics-based definitions

- Physical distance
- Gravitational potential
- Virialized structures
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A problem of definition

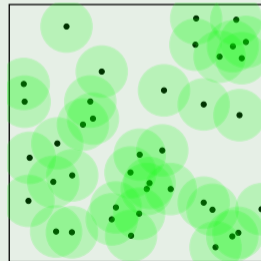
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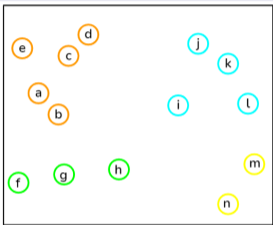
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Example of FoF: linking-length

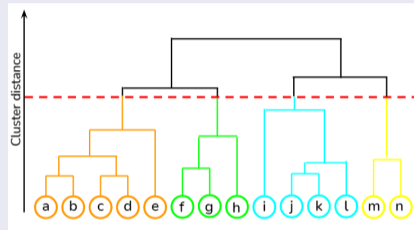


Trees as a universal representation for clustering results

Hierarchical clustering

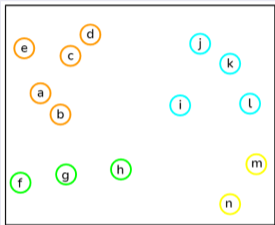


Cluster dendrograms

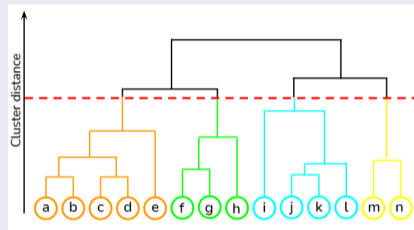


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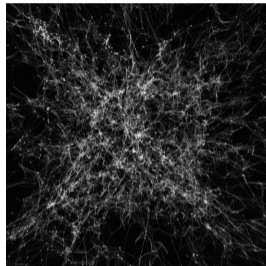
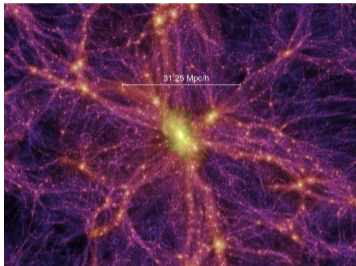
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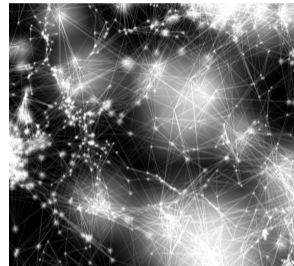
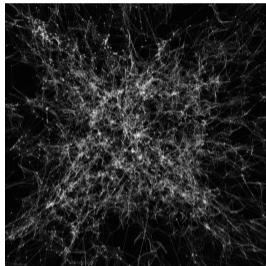
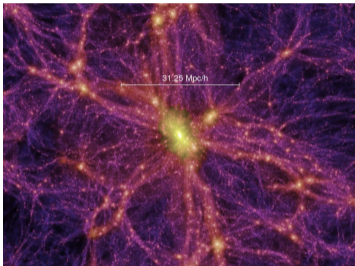
A universal representation

- Traditional galaxy cluster finders \Rightarrow 3-level trees (root/clusters/sources)
- With subhalo finders \Rightarrow 4-level trees (root/clusters/subclusters/sources)
- Hierarchical finders \Rightarrow N -level trees (root/supersuperclusters/superclusters/.../sources)

Graph as a numerical representation of the cosmic web



Graph as a numerical representation of the cosmic web



Representing the cosmic web as a graph

- Vertices: particles, sources
- Edges: physical parameterization (physical distance. . .)
- Going beyond: fuzzy graphs to take into account error bars

A computer science perspective on galaxy clustering: graphs and trees

Reframing of the galaxy clustering problem

- Cosmic web \Leftrightarrow Graph
- Galaxy clustering \Leftrightarrow Trees

A computer science perspective on galaxy clustering: graphs and trees

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Computer science perspective

Galaxy clustering problem \Leftrightarrow Computing Trees on Graphs

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Discrete vs continuous mathematics

- Comparison of galaxy clustering algorithms \Rightarrow comparison of trees
- Computer science related problem: tree metric and distances

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Research direction

Playing games on the cosmic web: computing galaxy clustering trees on the cosmic web graph

- Well-framed computer science problem
- Bridge between numerical cosmology, computer science, and discrete mathematics
- Computer science tools available

Game trees

- 1 Galaxy clusters
- 2 Clusters and computers
- 3 **Game trees**
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Game trees: starting with Tic-Tac-Toe



Game trees

A universal way to represent sequential N -player(s) games with perfect information.

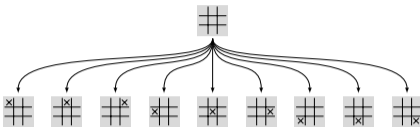
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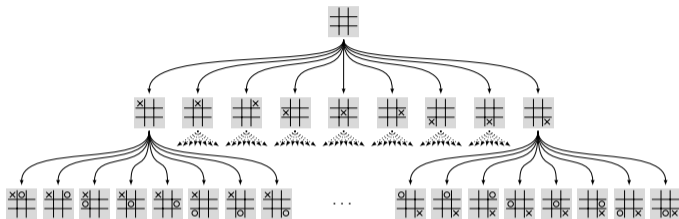
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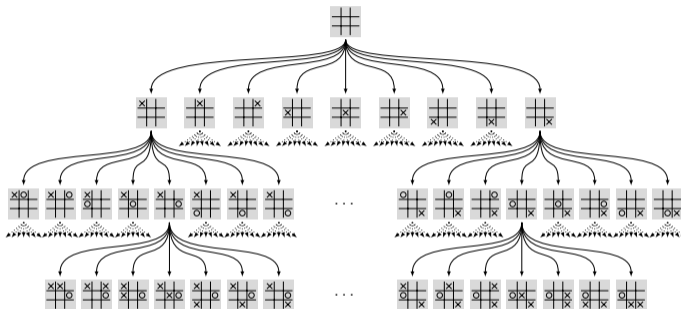
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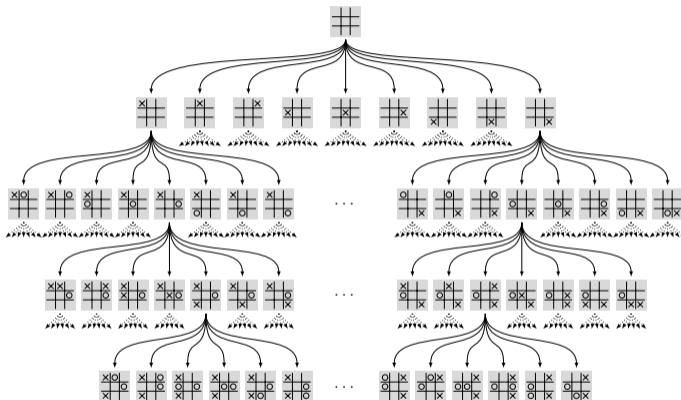
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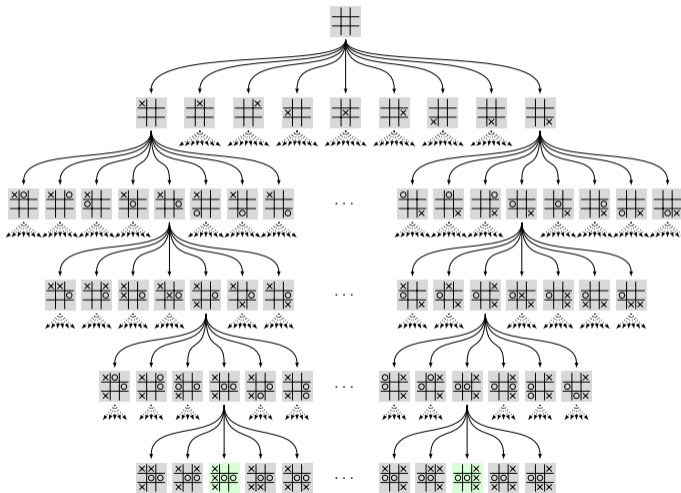
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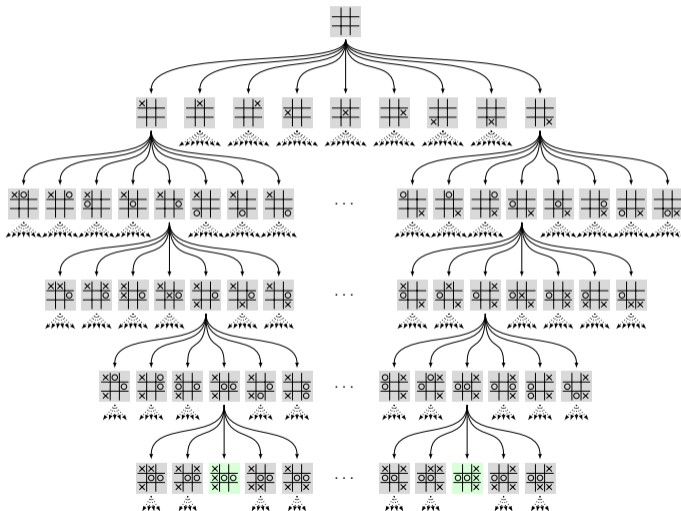
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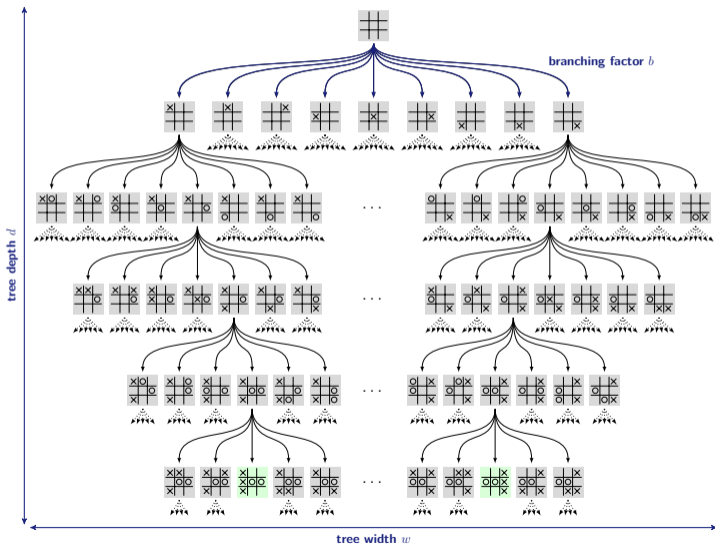
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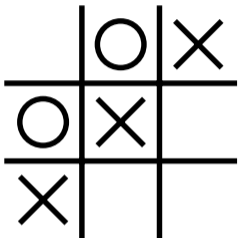
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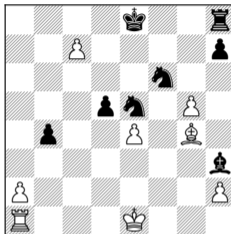
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Game complexity



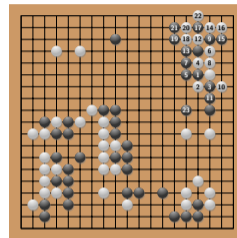
Tic-Tac-Toe

- Board size $\Rightarrow 3^2 = 9$
- Average game length $\Rightarrow 9$
- Average branching factor $\Rightarrow 4$
- Number of games $\Rightarrow 255\,168$



Chess

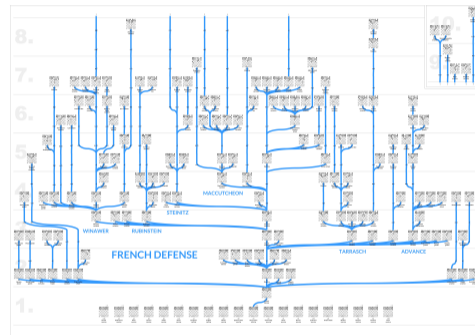
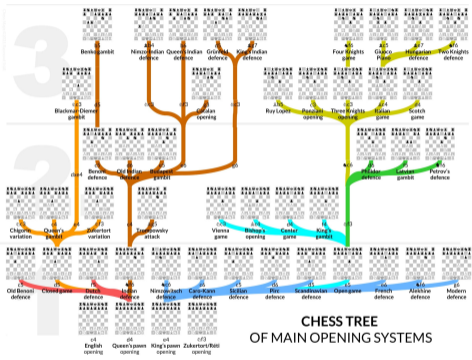
- Board size $\Rightarrow 8^2 = 64$
- Average game length $\Rightarrow 70$
- Average branching factor $\Rightarrow 35$
- Complexity $\Rightarrow 35^{70} \approx 10^{64}$



Go

- Board size $\Rightarrow 19^2 = 361$
- Average game length $\Rightarrow 150$
- Average branching factor $\Rightarrow 250$
- Complexity $\Rightarrow 250^{150} \approx 10^{360}$

Playing chess algorithmically



Brute-forcing

Game tree still tractable: average depth $d = 70$, average branching factor $b = 35$

The problem with the game of Go

Intractability

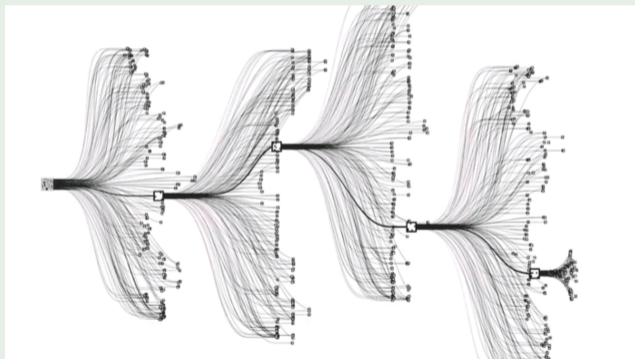
Go's game tree average depth $d = 150$, average branching factor $b = 250$

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Deepmind's AlphaGo/AlphaZero

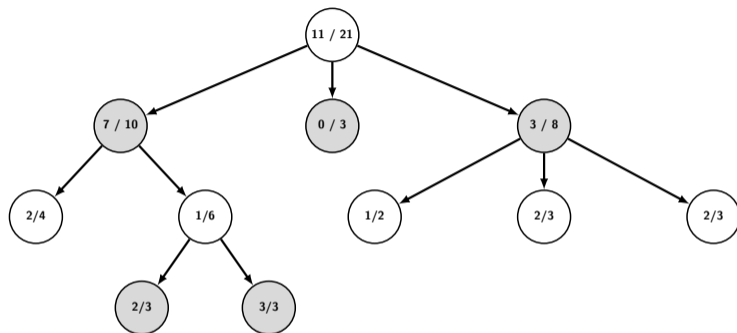


Breakthrough in 2017 (David Silver et al.)

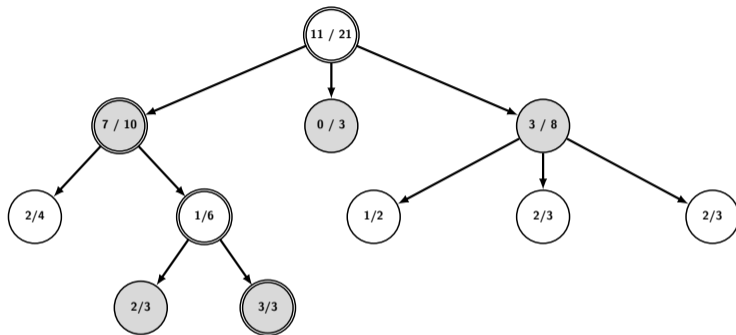
MCTS and AlphaZero

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Monte-Carlo-Tree-Search (MCTS) overview



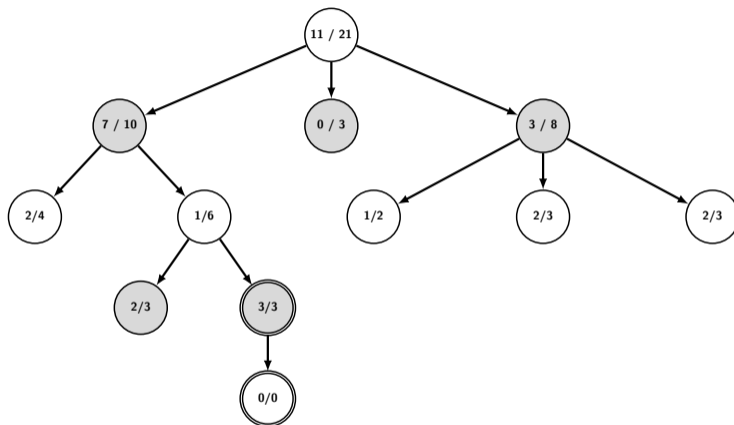
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Selection

Select a leaf node.

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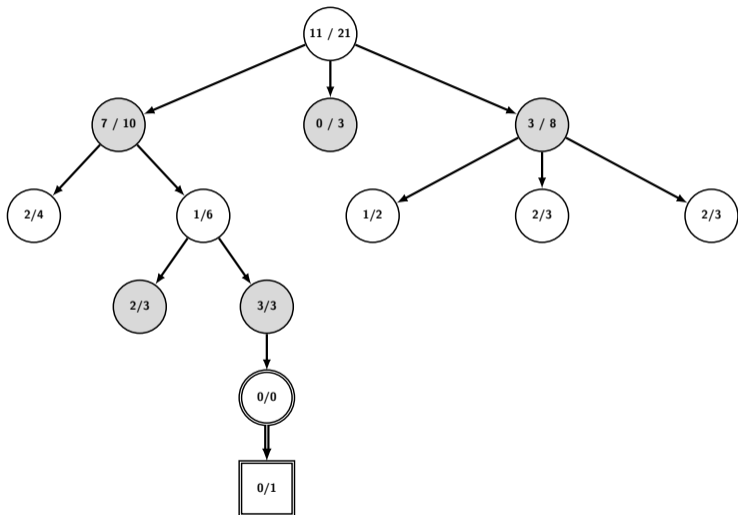
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Create one or more children nodes and select one of them.

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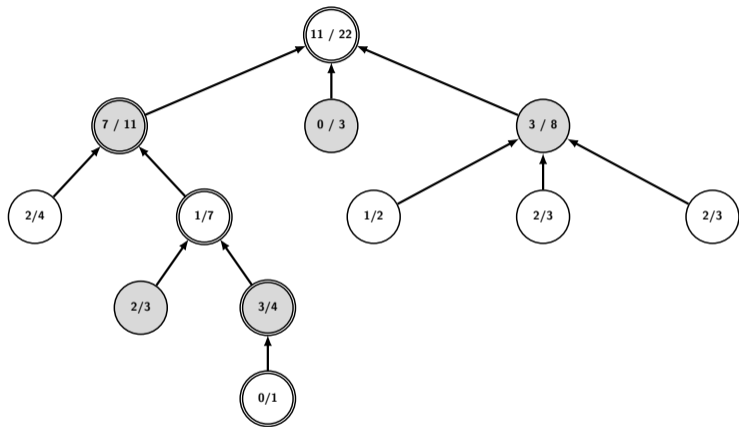
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Complete a full random ployout from the selected child.

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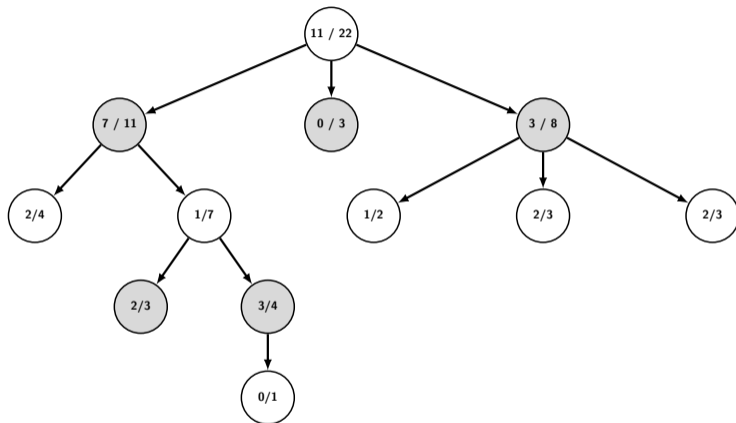
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Backpropagate the result of the simulation back to the root.

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Monte-Carlo-Tree-Search (MCTS) refinements

Simulations

- To get a distribution of results, N_s simulations can be performed at each step
- Simulated playouts can be done in a better way than using random moves

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Selection: exploitation vs exploration

Example of the UCT (Upper Confidence Bound 1 applied to Trees) policy:

$$\max_x \left(\frac{w_i(x)}{n_i(x)} + c \sqrt{\frac{\log(N_i(x))}{n_i(x)}} \right)$$

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- $c \Rightarrow$ exploration coefficient ($c = \sqrt{2}$)

AlphaZero = Monte-Carlo-Tree-Search + Deep Neural Networks

Monte-Carlo-Tree-Search (MCTS)

- Selection
- Expansion
- Simulation
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Policy deep neural network

- Input: s , the current state of the board (+ optionally previous states)
- Output: p , to select the most probable/promising moves
- General idea: reduce the breadth of the tree search

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Value deep neural network

- Input: s , the current state of the board (+ optionally previous states)
- Output: v , the probability to win
- General idea: reduce the depth of the tree search

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- Input: s , the current state of the board (+ optionally previous states)
- Output: p , to select the most probable/promising moves
- General idea: reduce the breadth of the tree search

Value deep neural network

- Input: s , the current state of the board (+ optionally previous states)
- Output: v , the probability to win
- General idea: reduce the depth of the tree search

AlphaZero = MCTS + Policy Net + Value Net

Tree search guided by “intuition” and “expert-knowledge”.

A clustering game

- 1 Galaxy clusters
- 2 Clusters and computers
- 3 Game trees
- 4 MCTS and AlphaZero
- 5 A clustering game
- 6 Conclusions

A clustering game

Game's board

The cosmic-web graph

A clustering game

Game's board

The cosmic-web graph

Game's goal

Extracting a clustering tree from the graph

A clustering game

Game's board

The cosmic-web graph

Game's goal

Extracting a clustering tree from the graph

Game's move

Create a link between a particle and its best neighbouring candidate

Using MCTS and Neural Nets to play the clustering game

Preparation using simulations

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- Compute the cosmic-web graph \mathcal{G}

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Playing phase

- Play the 1-player game using MCTS + Neural Nets on real observations using $\vec{x} = (x_0, x_1, x_2, \dots, x_{n-1})$

Using MCTS and Neural Nets to play the clustering game

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- No need of observational data on ϕ

Combining the best of both worlds

Physics-guided machine-learning approach

- Works for any physics-based criteria ϕ and observational data \vec{x} (including images and error bars)
- Builds an “intuition” on ϕ using simulations ($\phi \Leftrightarrow$ How does the game board looks like?)
- No black-box effect anymore

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Possible cluster definitions based on ϕ

- Physical distance
- Matter density
- Gravitational potential
- Virialization
- Linear combination of all of the above
- ...

Conclusions

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Towards the ultimate definition?

Cluster definition collapse in $t = +\infty$

- In $t = +\infty \Rightarrow$ isolated clusters
- All definitions are equivalent

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Simulating the end of time

- Let simulations run far into the future
- Detect clusters

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Simulating the end of time

- Let simulations run far into the future
- Detect clusters
- Go back in time to $z = 0$ tracking particles

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Analysis

- Play the game using this criterion
- Use computer science and discrete mathematics to compare $\mathcal{T}_i = f(\phi_i)$

Conclusions

Limitations of machine-learning approaches

- Black-box approaches, hard to interpret and adjust in terms of physics
- Risk of circular definitions

Cluster detection as a computer science problem

- Cosmic-web \Leftrightarrow Graph
- Clusters \Leftrightarrow Trees
- Galaxy clustering problem \Leftrightarrow Computing Trees on Graphs

The game of cluster detection

- MCTS + Deep Neural Networks = physics-guided machine-learning approach
- Work with arbitrary physics criterion ϕ and observational data \vec{x}

A starting project!

Reach out if you're interested: vincent.reverdy@lapp.in2p3.fr