



IAS

INSTITUTE FOR
ADVANCED STUDY

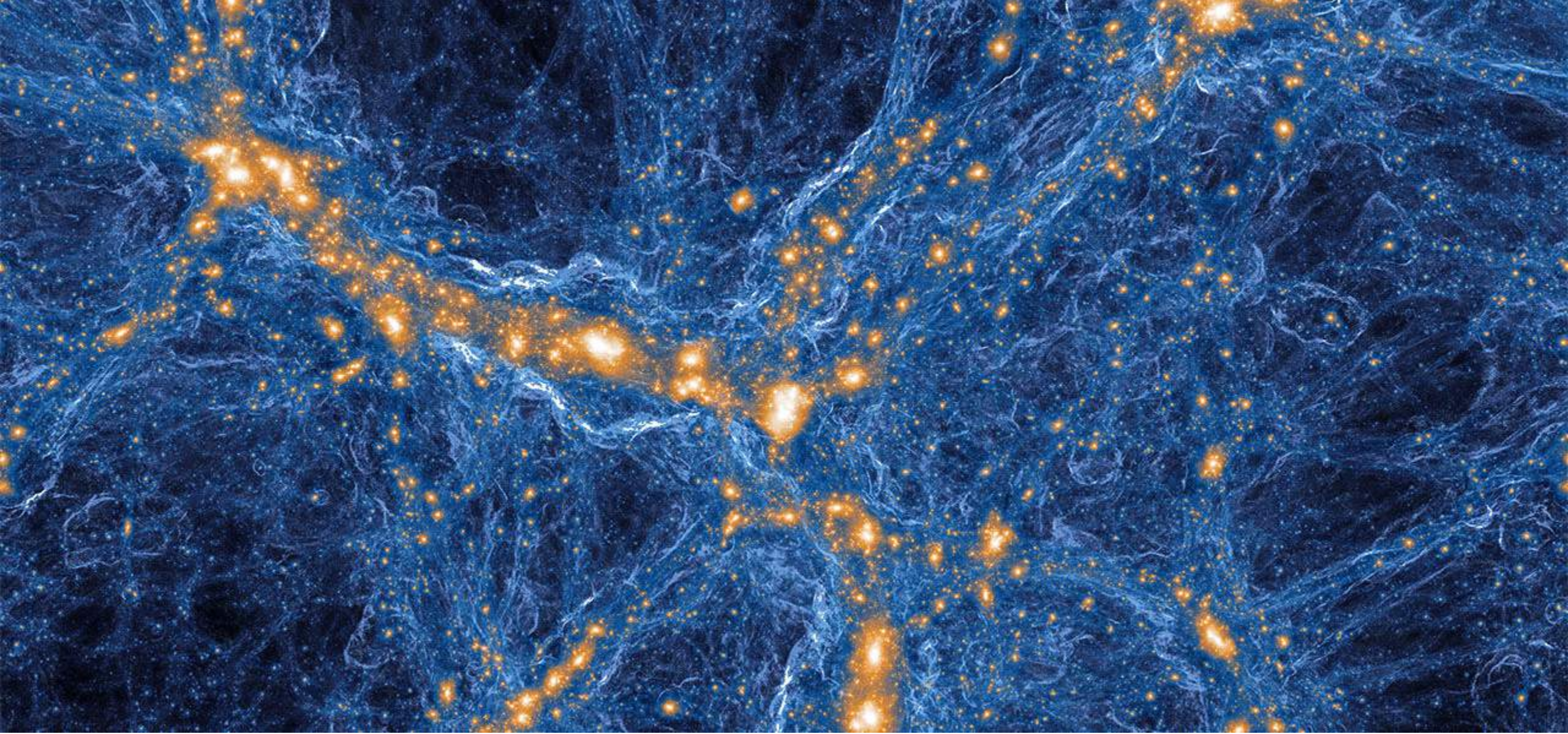


Spectroscopic Surveys: A Precision Probe of Old & New Physics

Oliver Philcox (Princeton / IAS)

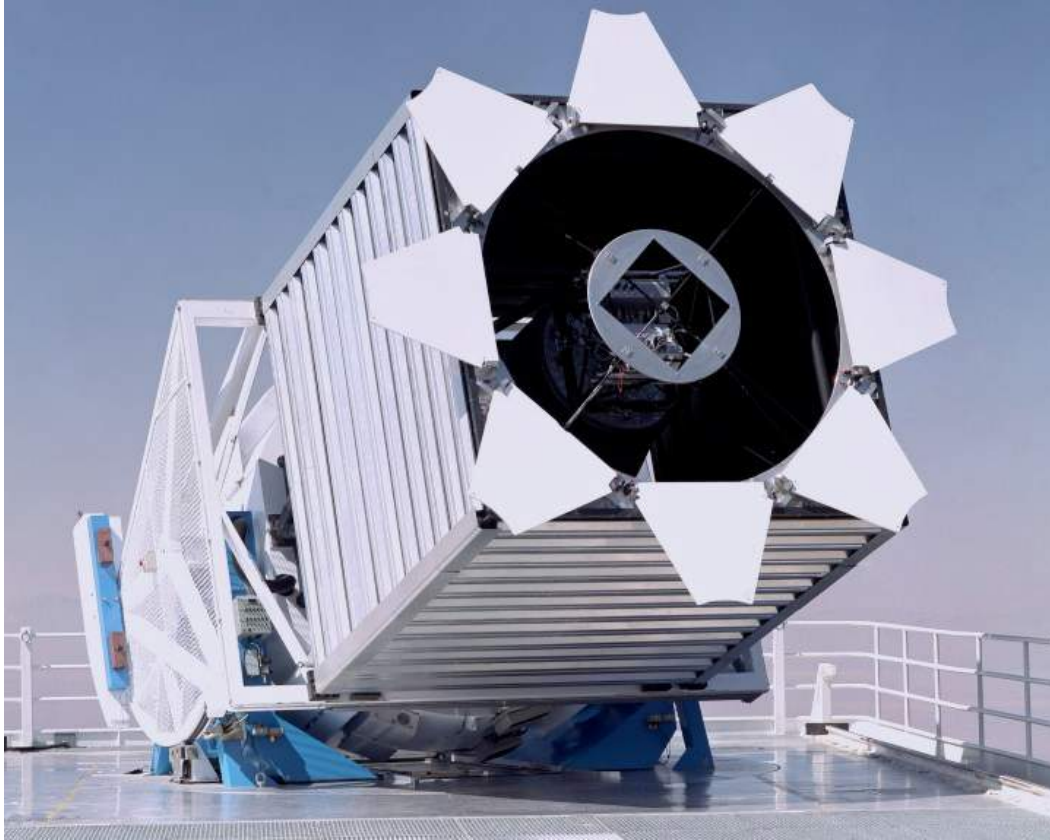
Dark Energy Webinar, May 2022

Collaborators: Mikhail Ivanov, Giovanni Cabass, Marko Simonovic, Matias Zaldarriaga, Takahiro Nishimichi, Masahiro Takada, Blake Sherwin, Gerrit Farren, Eric Baxter, Dillon Brout

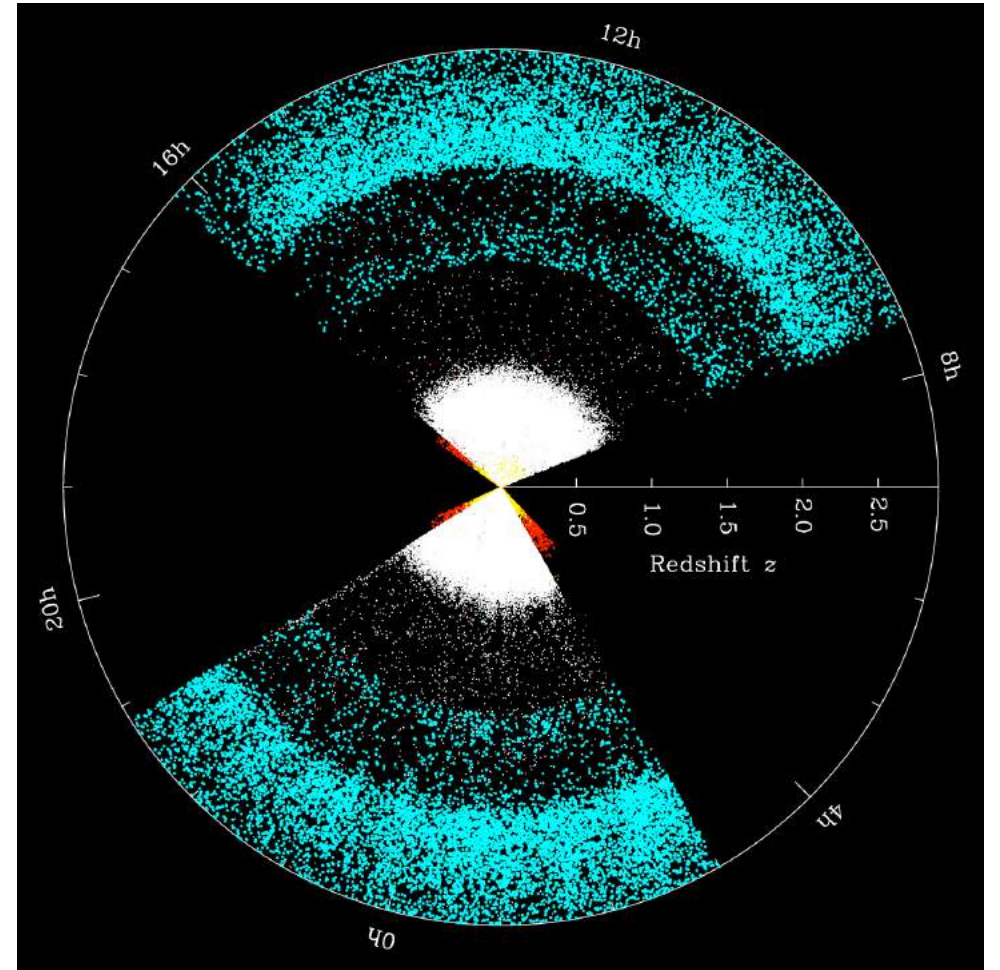
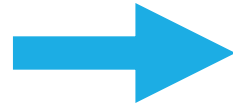


1. What Can We Measure?

COSMOLOGY FROM SPECTROSCOPIC SURVEYS



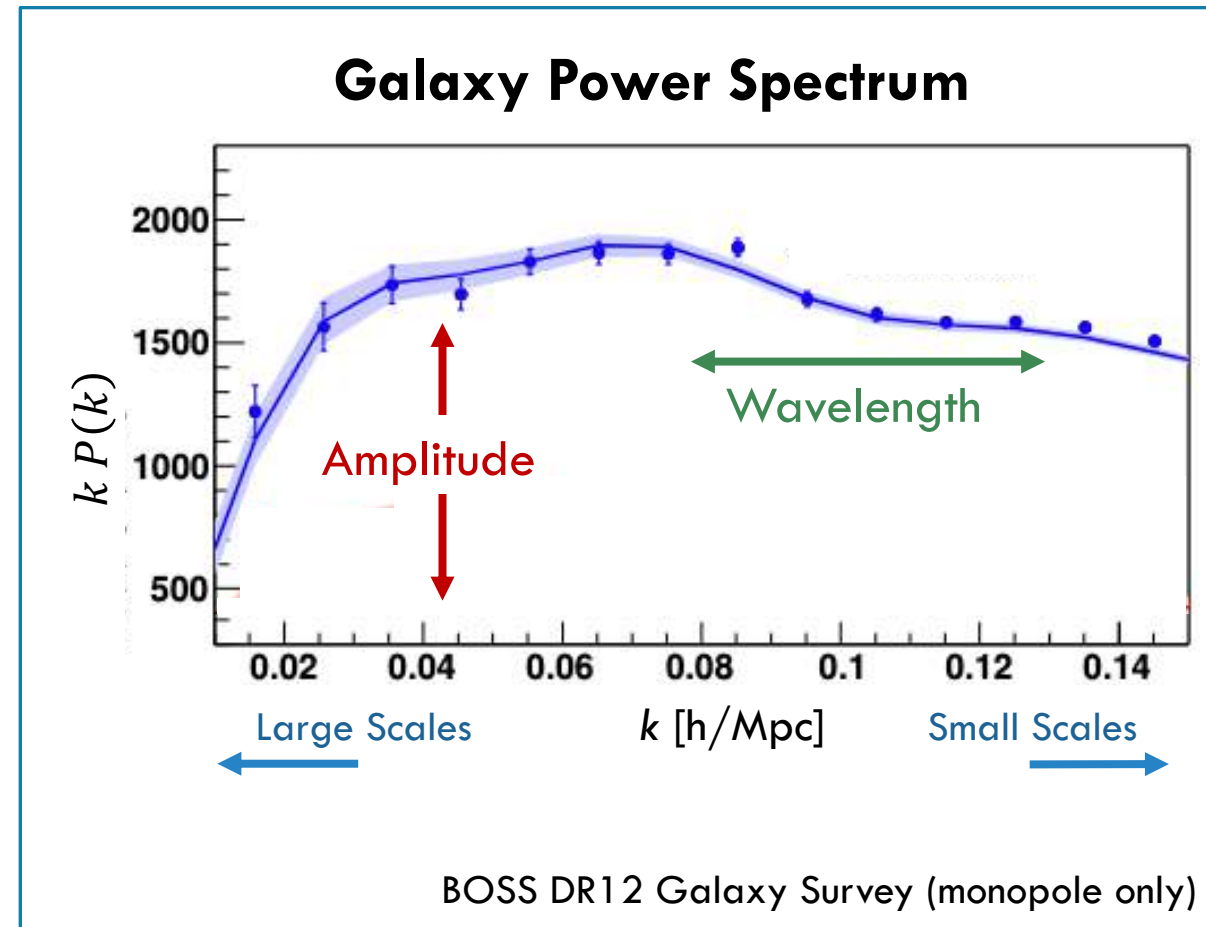
Big Telescope



10^6 Galaxy Positions

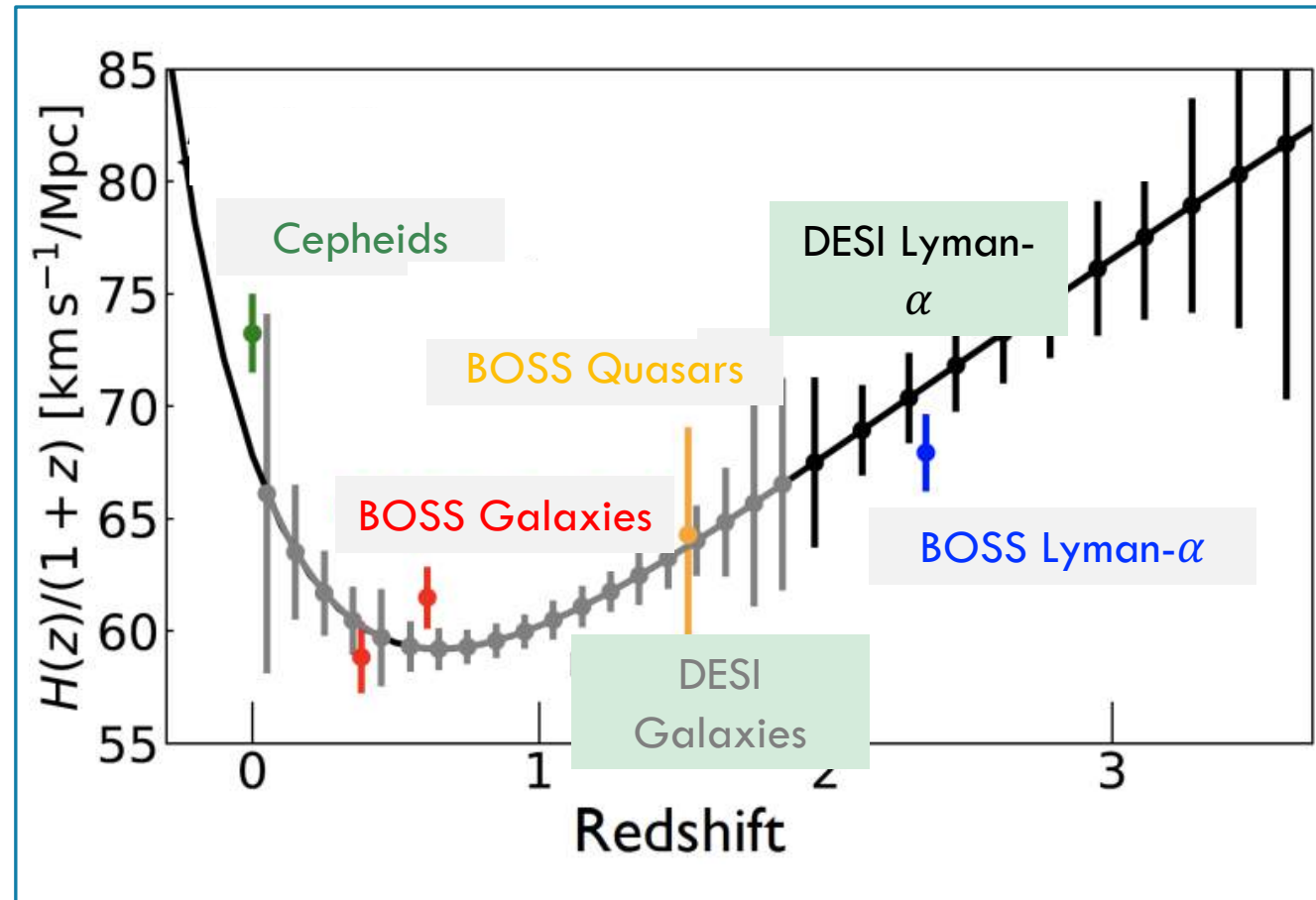
WHAT DO WE DO WITH THE DATA?

- ▶ Compress the 10^6 galaxy positions to a **power spectrum**, $\langle \delta_g(\mathbf{k}) \delta_g^*(\mathbf{k}) \rangle$
- ▶ Use a **scaling analysis** to measure:
 - ▶ Overall **amplitude** (= primordial amplitude)
 - ▶ **Wiggle** positions (= BAO feature)
- ▶ Robust way to constrain **growth rate** $D_A(z)$, and **expansion history** $H(z)$



WHAT DO WE DO WITH THE DATA?

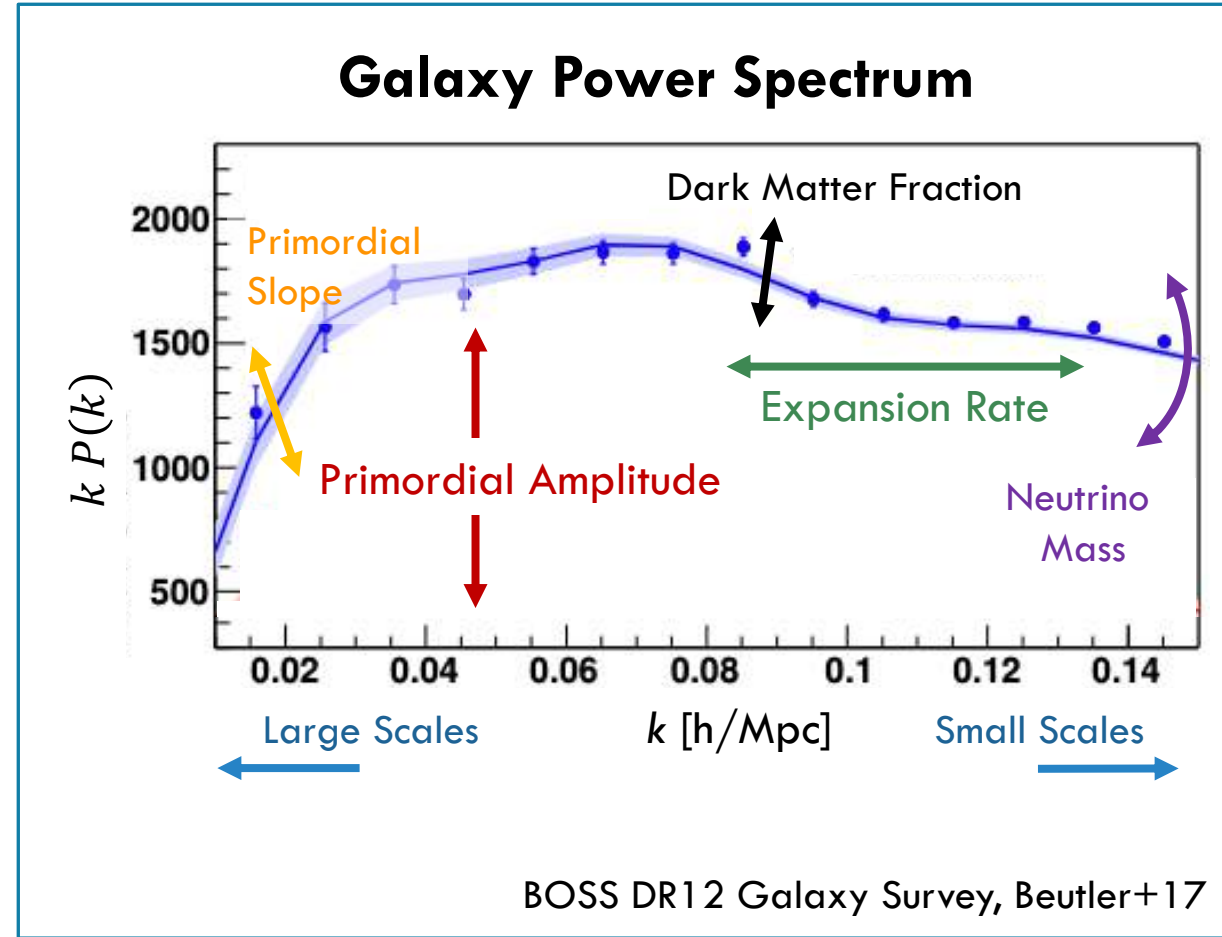
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 - ▶ Overall **amplitude** (= primordial amplitude)
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- ▶ Robust way to constrain **growth rate** $D_A(z)$, and **expansion history** $H(z)$



WHAT COULD WE DO WITH THE DATA?

- ▶ This is *not* all the available information!
- ▶ Measure parameters **directly** from the **full shape** of the galaxy power spectrum
- ▶ This is just like for the CMB!

This needs an accurate theory model...



THE EFFECTIVE FIELD THEORY OF LARGE SCALE STRUCTURE

▷ **Analytic** theory for $\delta(\mathbf{x})$, based on the non-ideal **fluid equations**

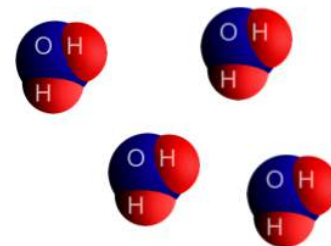
▷ A controlled Taylor series in k/k_{NL}

(or $k\sigma_{\text{FoG}}$, kR_{Halo})

▷ **Major Ingredient:** *Back-reaction* of small-scale physics on large-scale modes

▷ **Also includes:** galaxy bias, long-wavelength displacements, redshift-space distortions, primordial non-Gaussianity, etc.

$$\dot{v}^i + H v^i + v^j \delta_j v^i = \frac{1}{\rho} \delta_j \tau^{ij}$$



large
scales



THE EFFECTIVE FIELD THEORY OF LARGE SCALE STRUCTURE

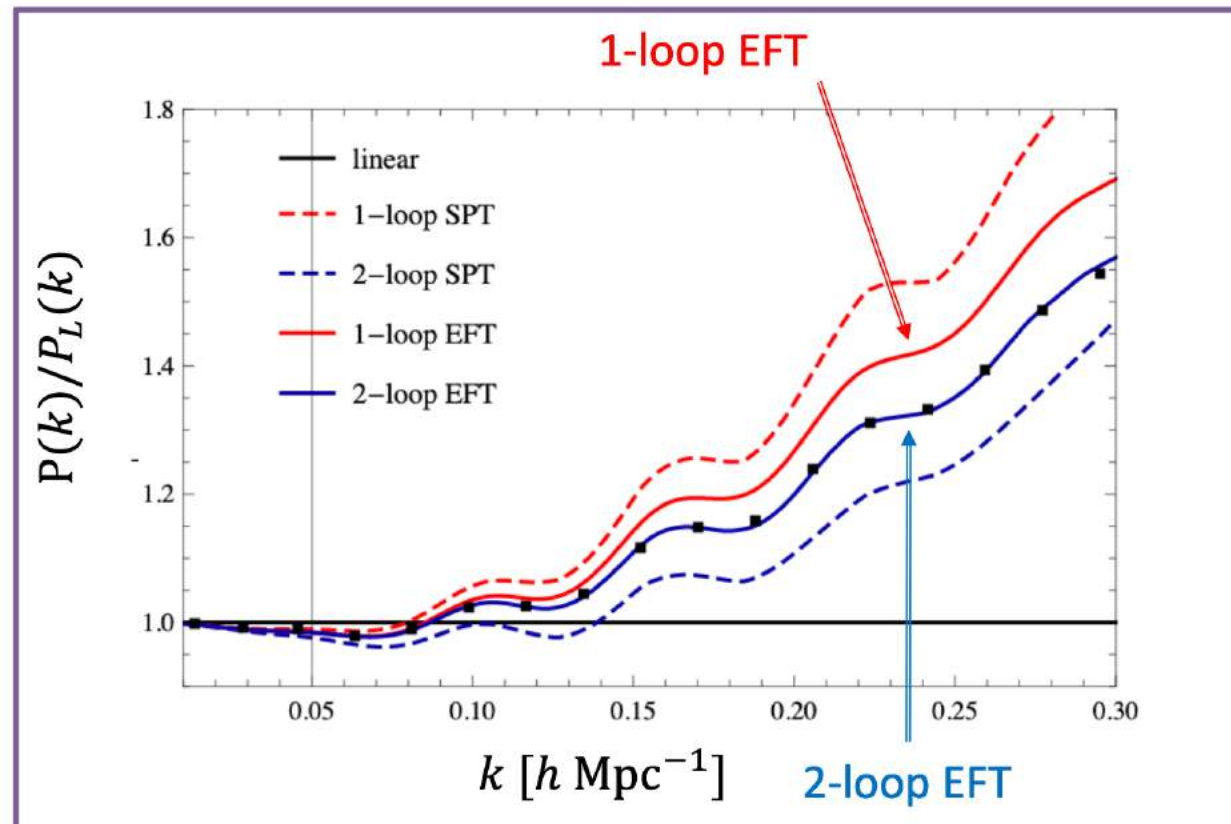
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▷ **Major Ingredient:** *Back-reaction* of small-scale physics on large-scale modes

▷ **Also includes:** galaxy bias, long-wavelength displacements, redshift-space distortions, primordial non-Gaussianity, etc.

Arbitrarily accurate on large scales!



MODEL VALIDATION

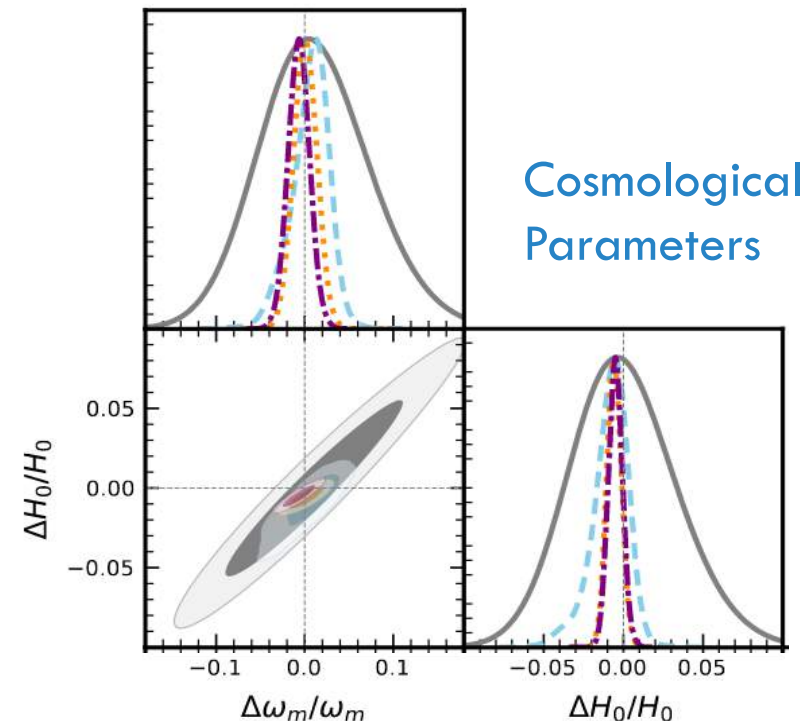
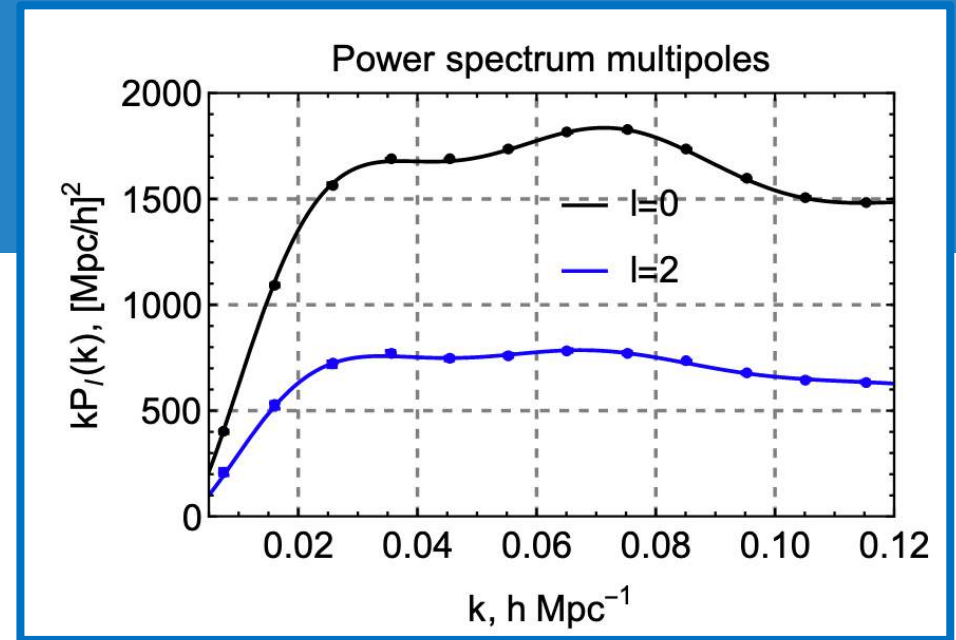
▷ Compare EFTofLSS model to N-body simulations, comparing $P_{gg}(\mathbf{k})$

▷ Total volume: $566 (h^{-1}\text{Gpc})^3$

▷ *Larger than DESI / Euclid!*

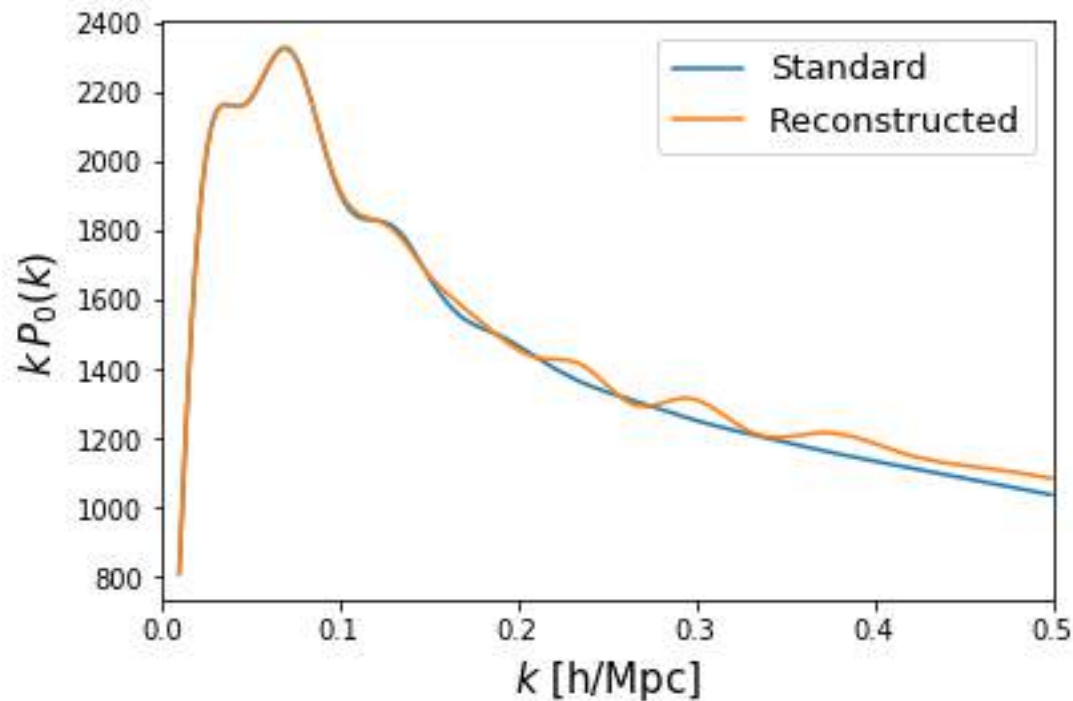
▷ Fully **blind** analysis

▷ **Unbiased cosmological parameters!**

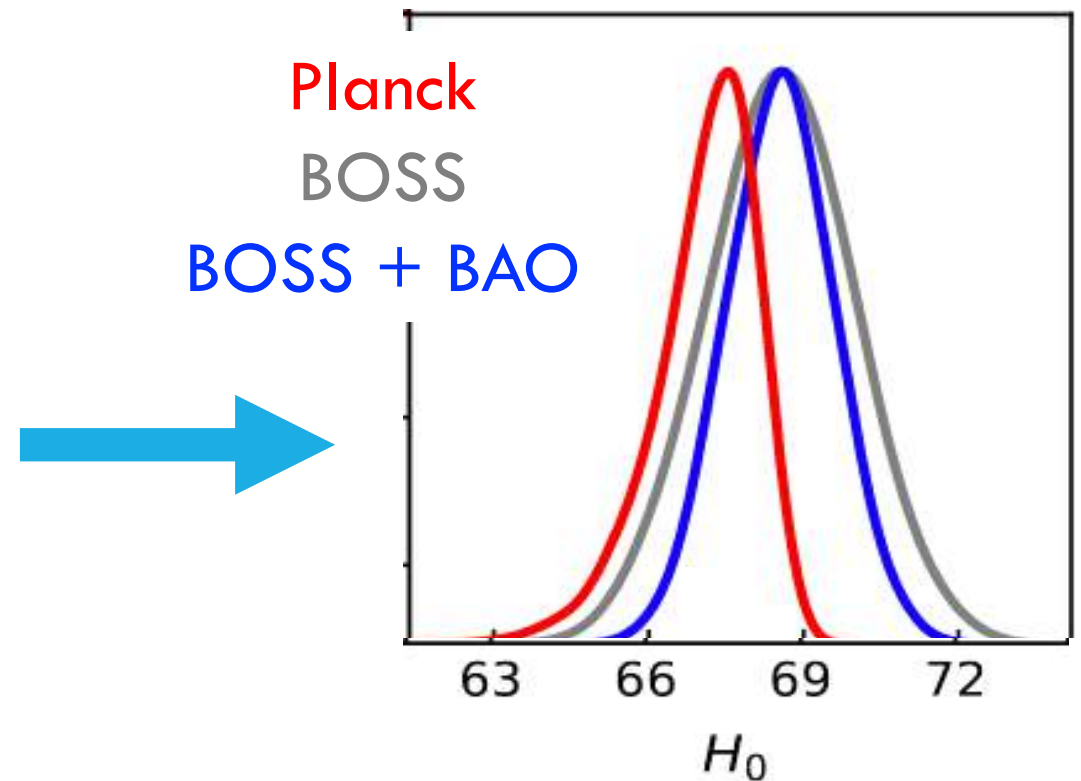


WHAT'S BEYOND THE POWER SPECTRUM? (#1)

Add the **wiggly** information from **baryon acoustic oscillations**

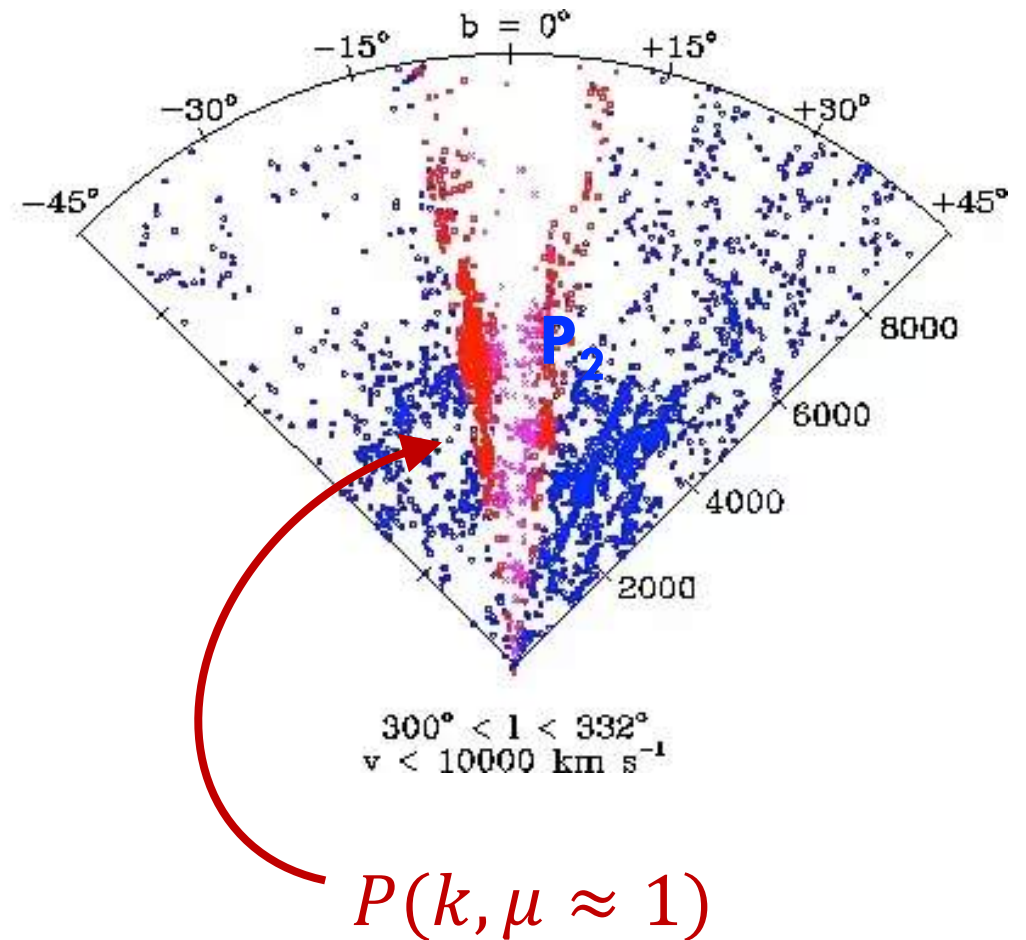


40% better H_0 !



WHAT'S BEYOND THE POWER SPECTRUM? (#2)

- ▷ Fingers-of-God are limiting at high- k
- ▷ k_{\max} is lower for radial modes!
- ▷ Can we compute $P(k, \mu = 0)$?



WHAT'S BEYOND THE POWER SPECTRUM? (#2)

Compute the **real-space** power spectrum

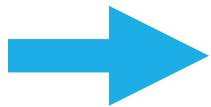
$$P_0(k)$$

+

$$P_2(k)$$

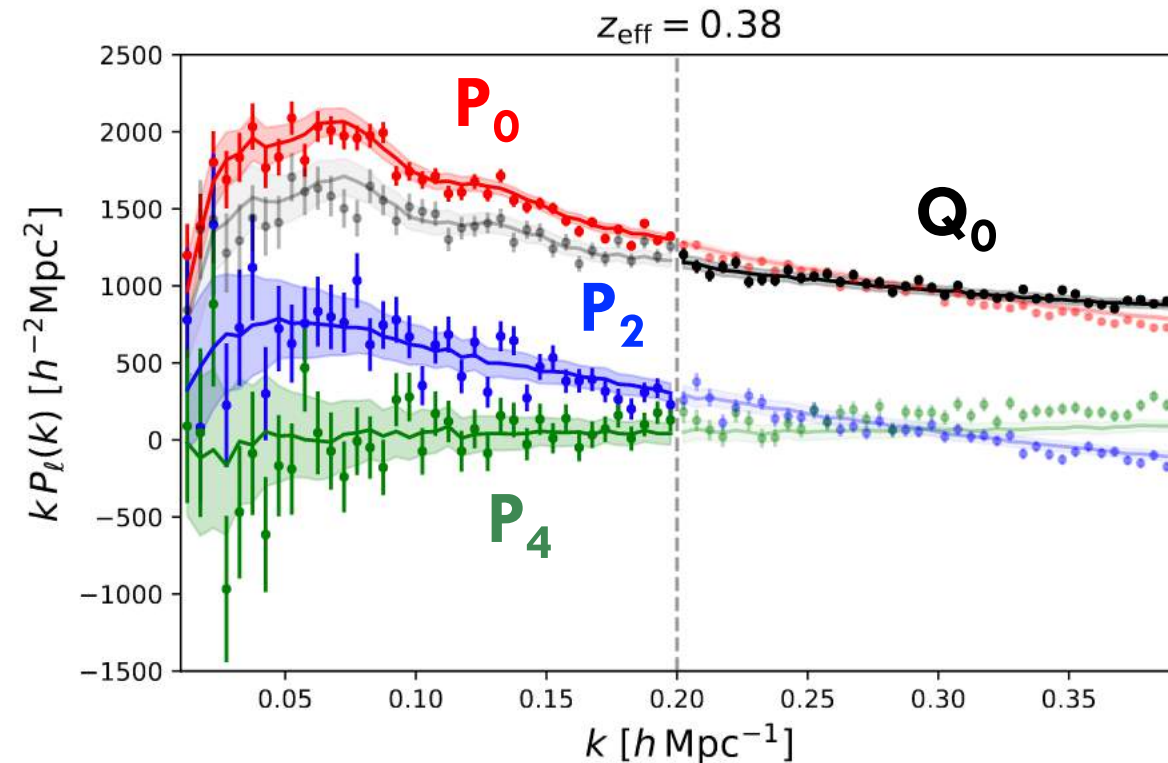
+

$$P_4(k)$$



$$Q_0(k) \approx P(k, \mu = 0)$$

- No Fingers-of-God!
- Push to $k_{\max} = 0.4h/\text{Mpc}$
- Constraints improve by (10 – 100)%



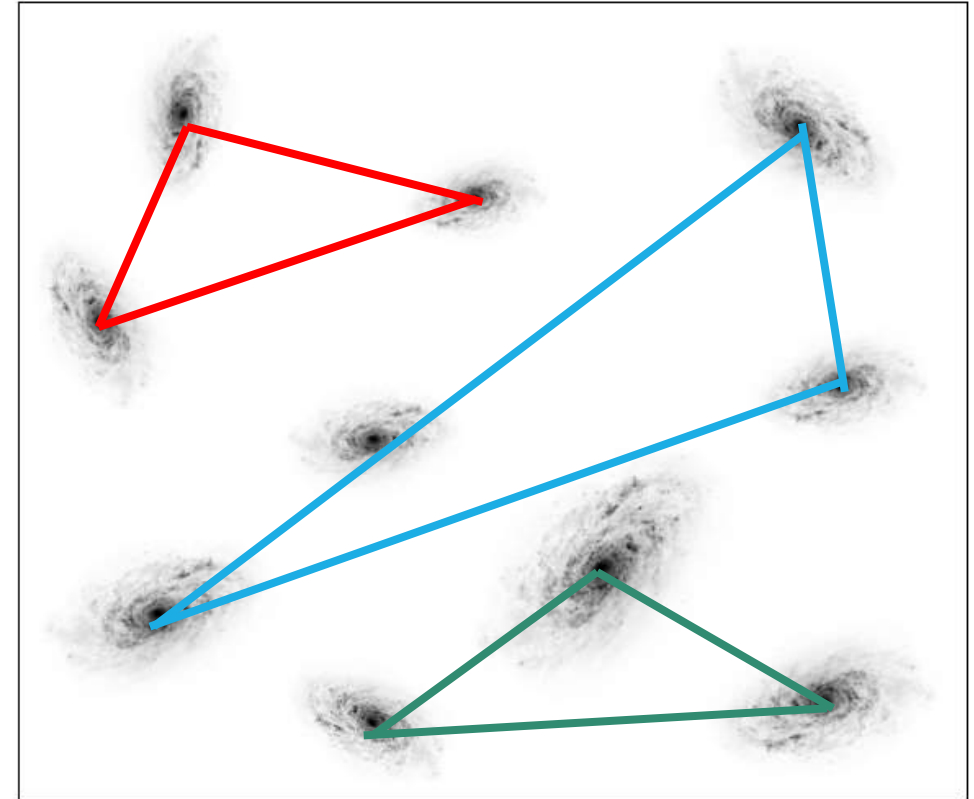
WHAT'S BEYOND THE POWER SPECTRUM? (#3)

Add the **galaxy bispectrum**:

$$B_g(k_1, k_2, k_3) = \langle \delta_g(\mathbf{k}_1) \delta_g(\mathbf{k}_2) \delta_g(\mathbf{k}_3) \rangle'$$

This is hard:

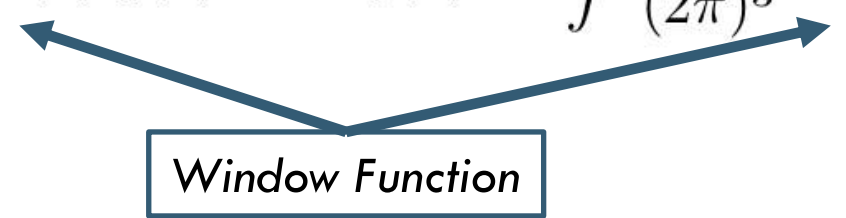
- Window functions
- Theory model



THE MASKED BISPECTRUM

Problem: We don't measure the density field directly.

$$\delta_g(\mathbf{r}) \rightarrow W(\mathbf{r})\delta_g(\mathbf{r}) \quad \delta_g(\mathbf{k}) \rightarrow \int \frac{d\mathbf{p}}{(2\pi)^3} W(\mathbf{k} - \mathbf{p})\delta_g(\mathbf{p})$$


Window Function

The measured bispectrum is a **triple convolution**

$$B_g(\mathbf{k}_1, \mathbf{k}_2) \rightarrow \int_{\mathbf{p}_1 \mathbf{p}_2} W(\mathbf{k}_1 - \mathbf{p}_1)W(\mathbf{k}_2 - \mathbf{p}_2)W(\mathbf{p}_1 + \mathbf{p}_2 - \mathbf{k}_1 - \mathbf{k}_2)B_g(\mathbf{p}_1, \mathbf{p}_2)$$

Solution: Convolve the **theory model** too

This is very expensive!



BISPECTRA WITHOUT WINDOWS

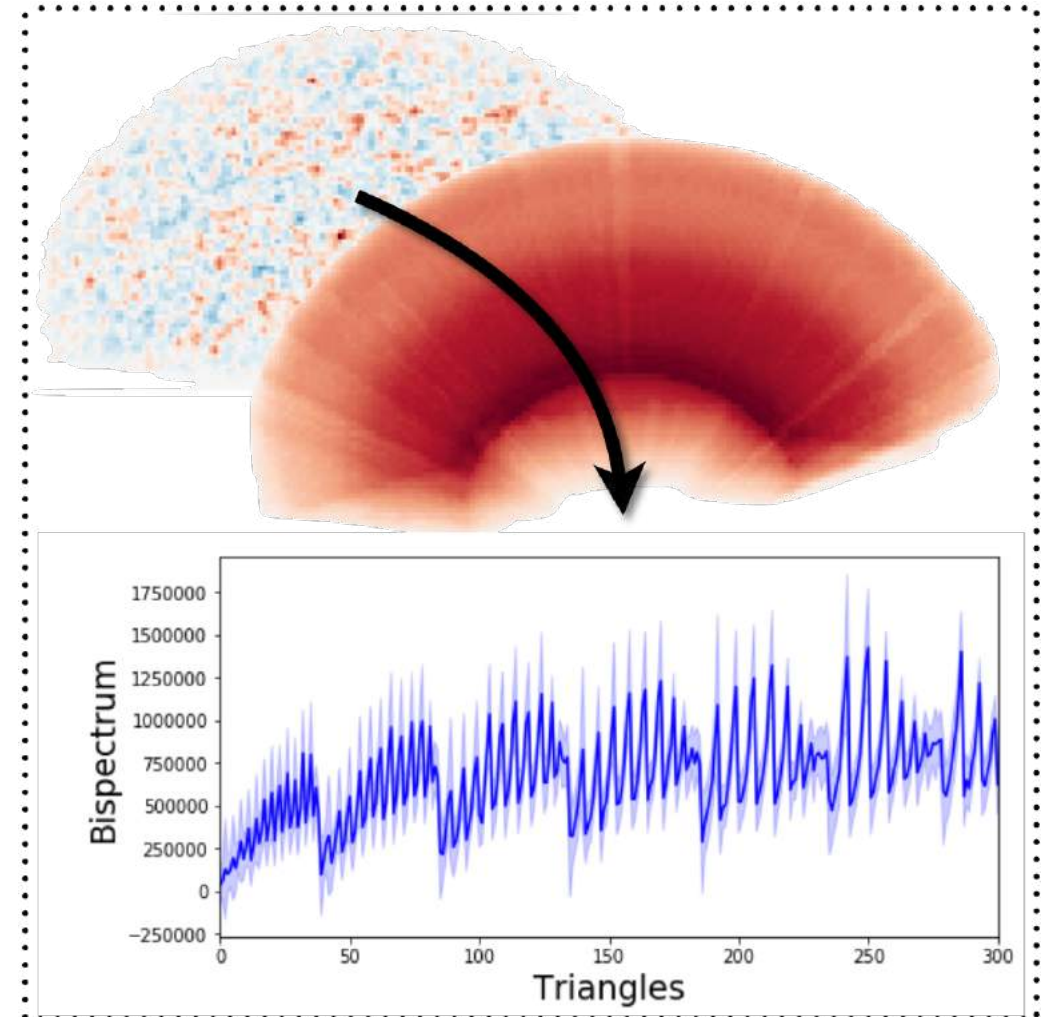
Alternatively: estimate the **unwindowed** bispectrum directly

$$B_g^{\text{win}}(\mathbf{k}_1, \mathbf{k}_2) = \int_{\mathbf{p}_1 \mathbf{p}_2} W(\mathbf{k}_1 - \mathbf{p}_1) W(\mathbf{k}_2 - \mathbf{p}_2) W(\mathbf{p}_1 + \mathbf{p}_2 - \mathbf{k}_1 - \mathbf{k}_2) \boxed{B_g(\mathbf{p}_1, \mathbf{p}_2)}$$

▷ Derive a **maximum-likelihood** estimator for the **true** bispectrum

▷ Effectively **deconvolves** the window

$$\nabla_{B_g} L[\text{data} | B_g] = 0 \quad \Rightarrow \quad \hat{B}_g = \dots$$



MODELLING THE BISPECTRUM

1-loop bispectrum coming soon!

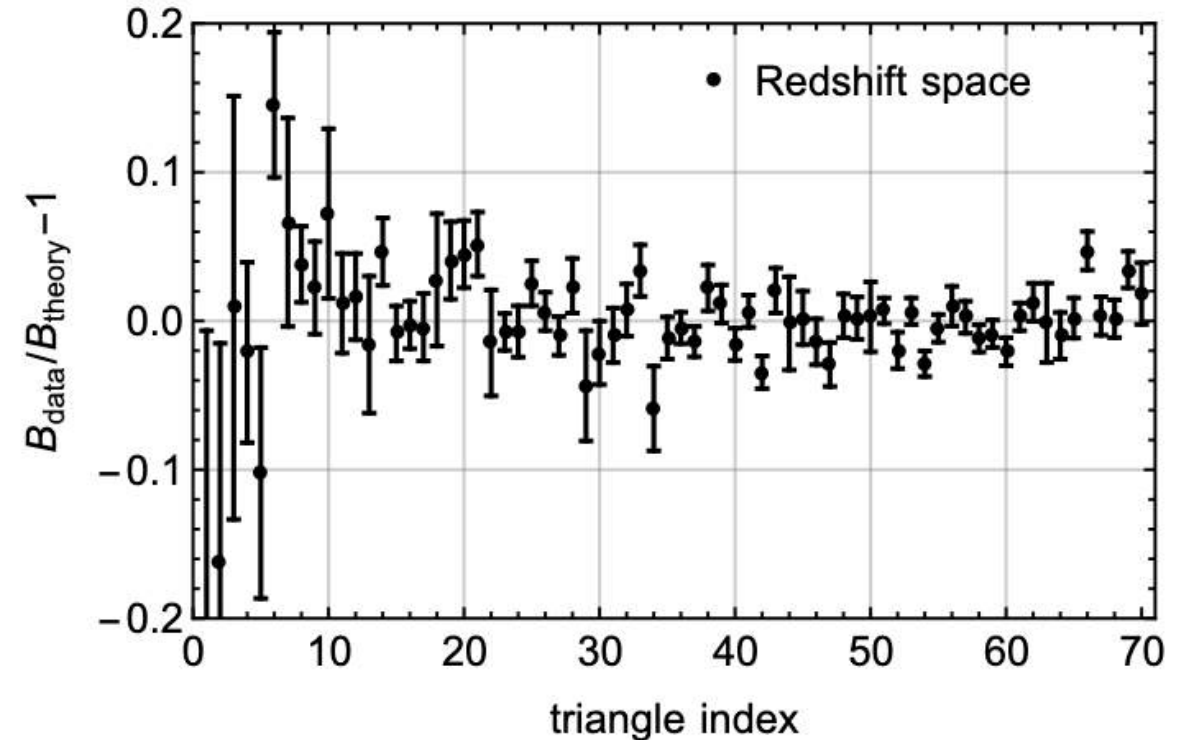
Effective-Field-Theory Model:

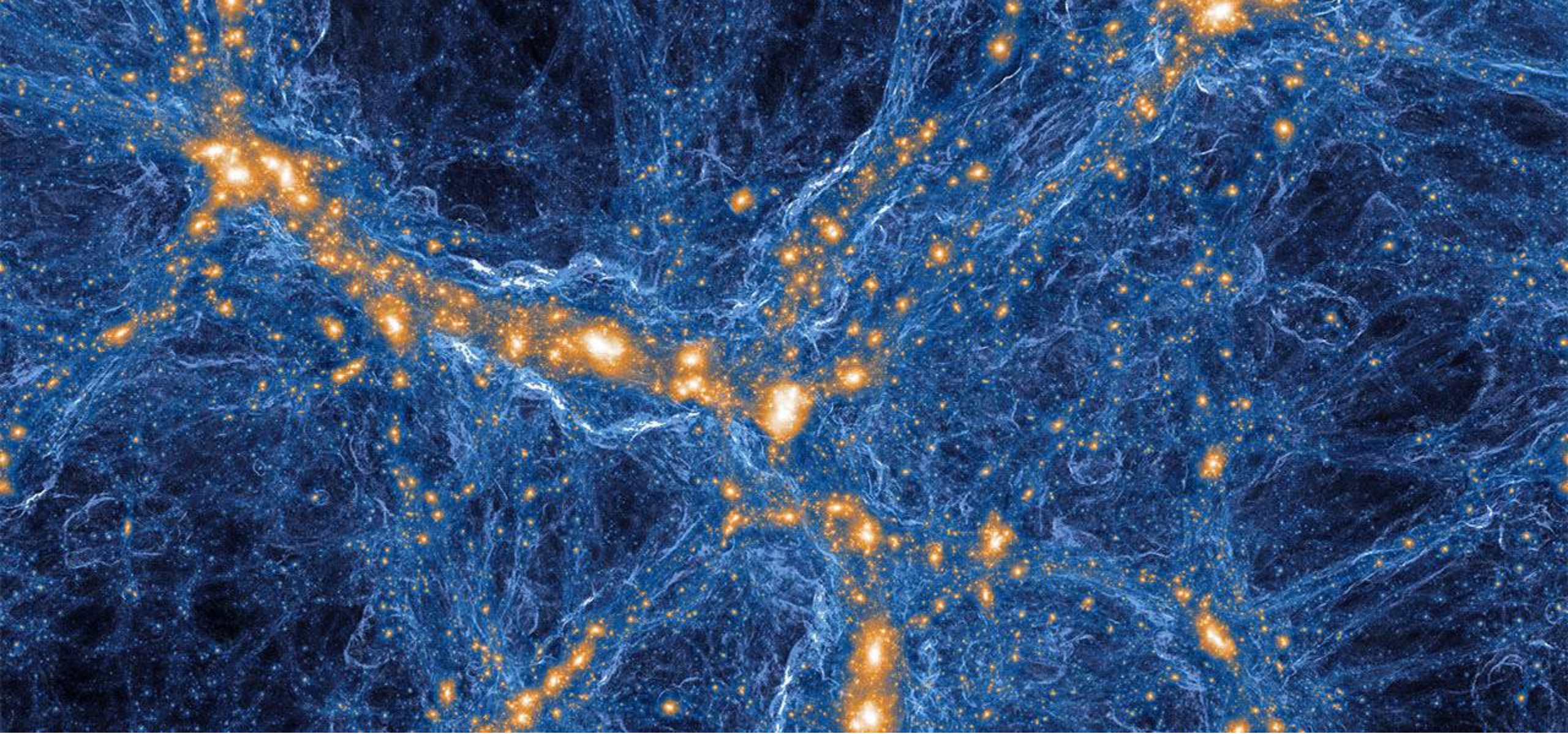
- Tree-level theory
- Second-order galaxy bias
- Large-scale displacements
- Coordinate transformations
- Fingers-of-God

Tested on 566 (Gpc/h)^3 simulations

Accurate up to $k_{max} = 0.08 \text{ h/Mpc}$

Data \div Theory $- 1$

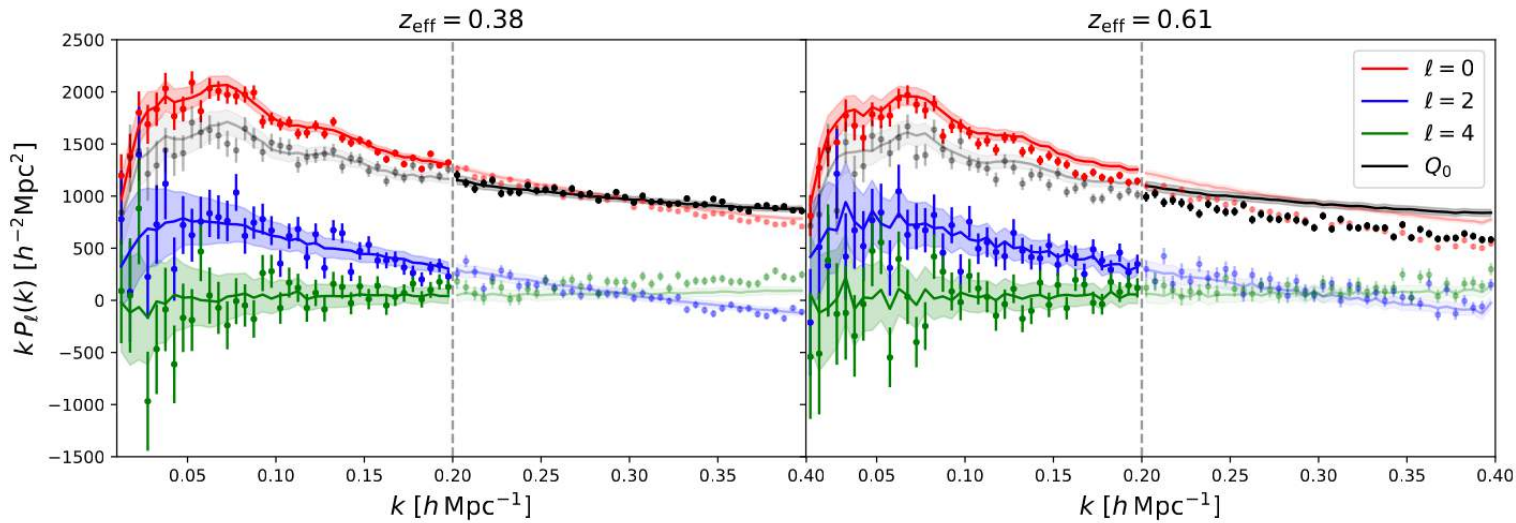




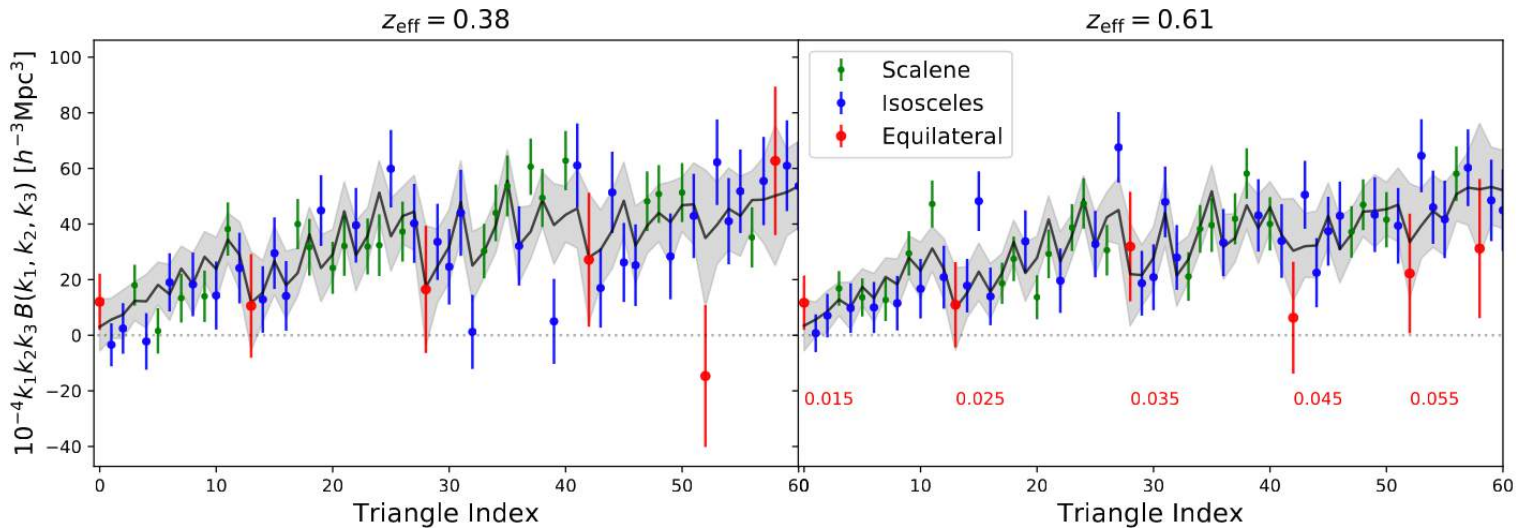
2. What Have We Learnt About Λ CDM?

THE UNOFFICIAL BOSS DR12 ANALYSIS

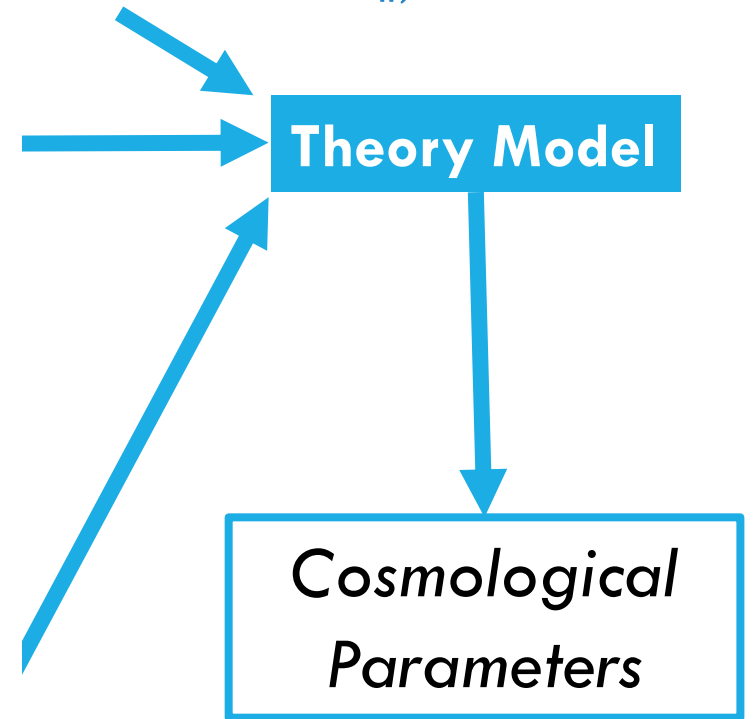
$P_\ell + Q_0$



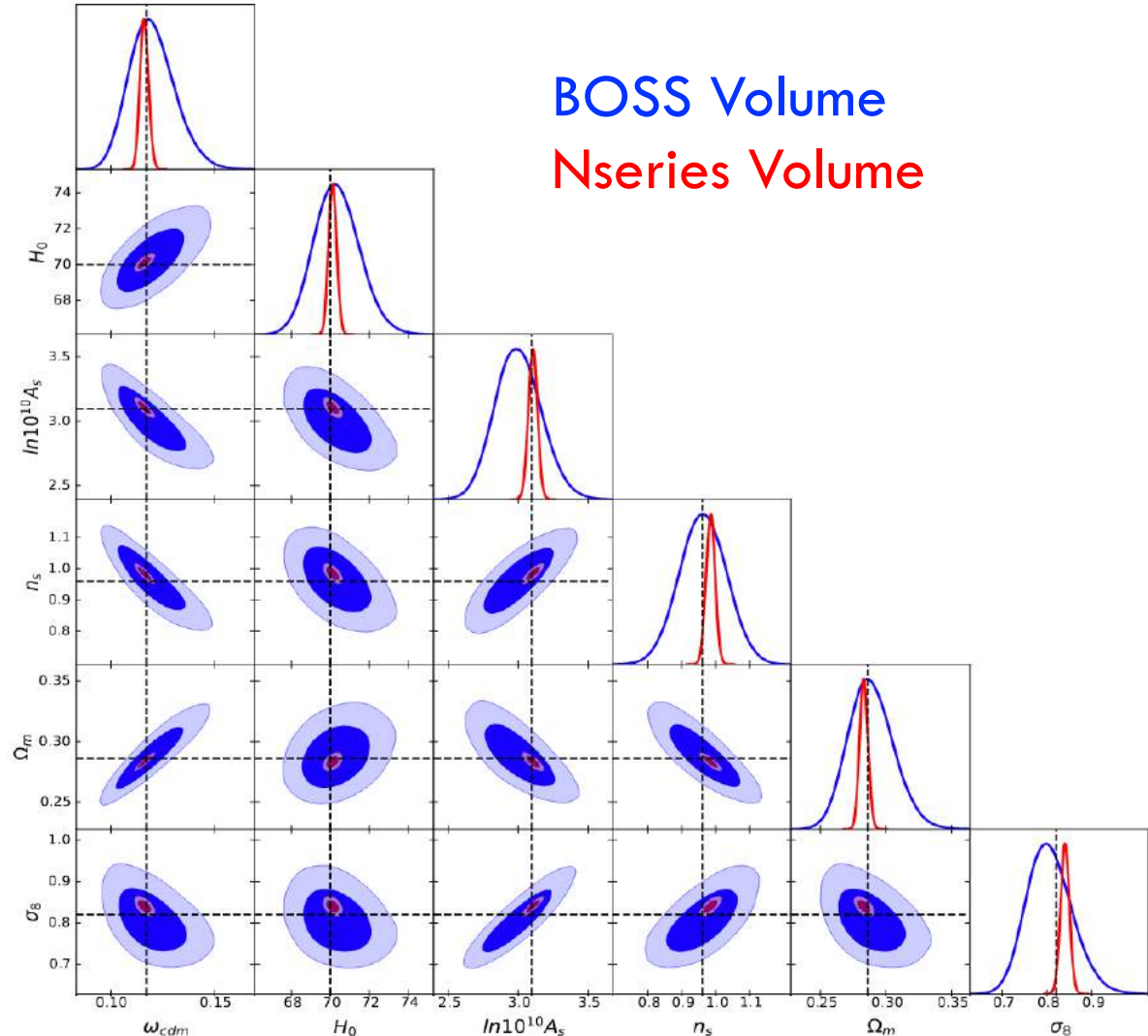
Bispectrum



Wiggles ($\alpha_{\parallel, \perp}$)



THE UNOFFICIAL BOSS DR12 ANALYSIS - TESTING

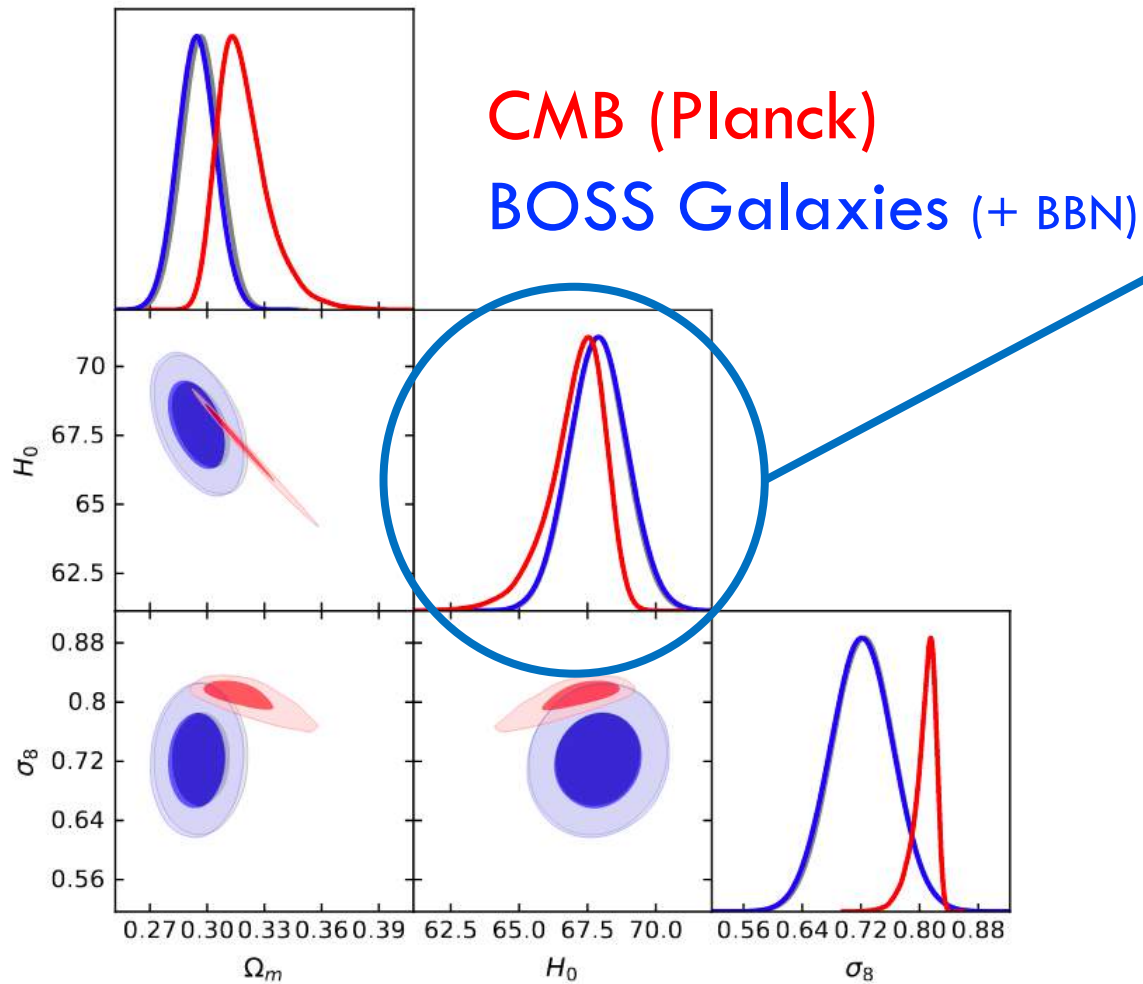


Validate with high-resolution **Nseries** mocks

- All parameters recovered at $\ll 1\sigma$
- Theory model works!
- Window function works!
- Fiber collisions work!

See [GitHub.com/oliverphilcox/full_shape_likelihoods](https://github.com/oliverphilcox/full_shape_likelihoods)

CONSTRAINTS ON H_0



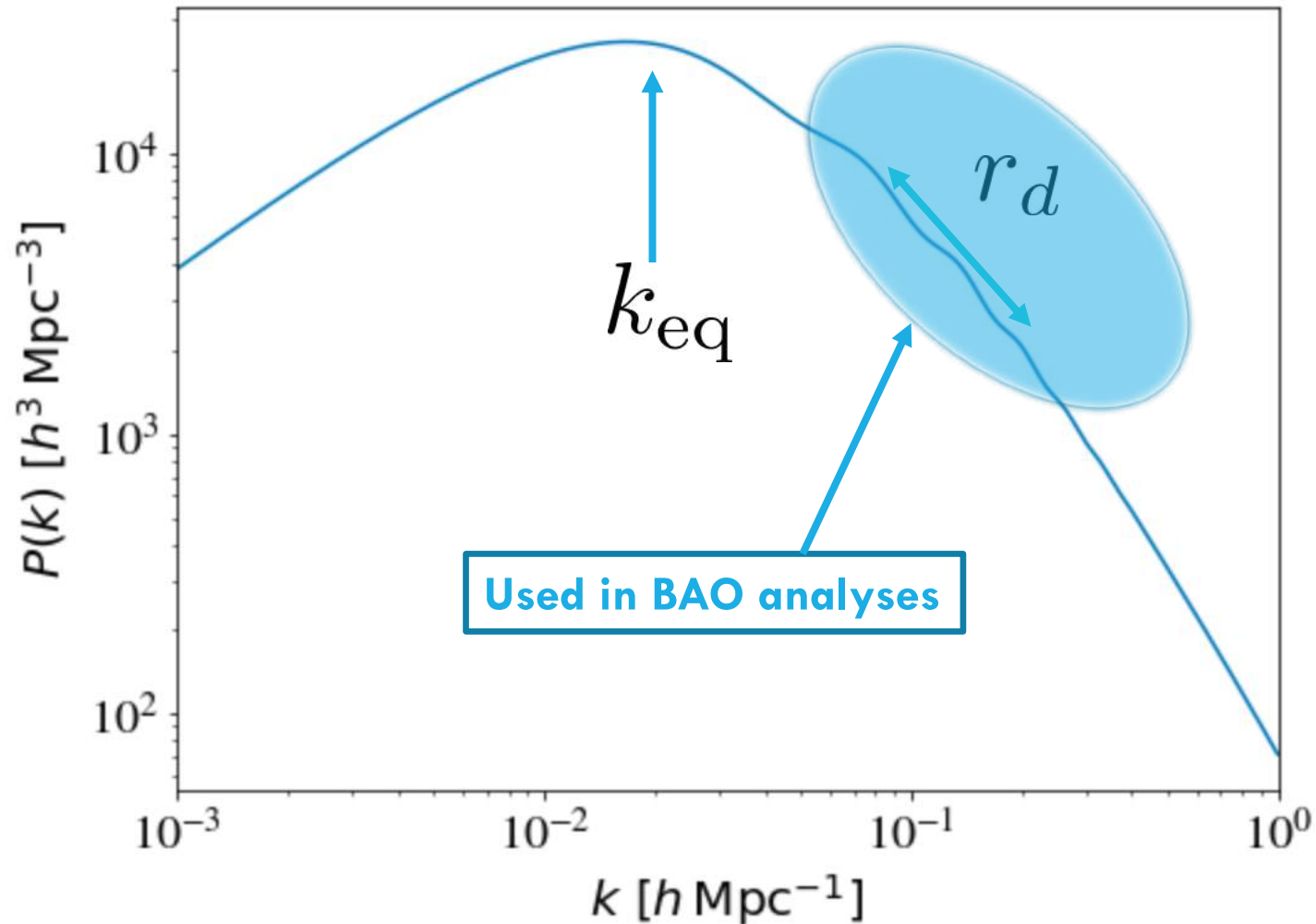
BOSS Power Spectrum + Bispectrum:

$$H_0 = 68.3 \pm 0.8 \text{ km s}^{-1} \text{ Mpc}^{-1}$$

- H_0 agrees with *Planck*
- 3.7σ discrepant with *SHOES*!

Where does this information come from?

TWO STANDARD RULERS FOR H_0



1. The Sound Horizon: r_d

- ▷ The **sound horizon** at baryon drag ($z \sim 1100$)

2. The Equality Scale: k_{eq}^{-1}

- ▷ The **horizon** at radiation-matter equality ($z \sim 3600$)

Both can be used to extract H_0

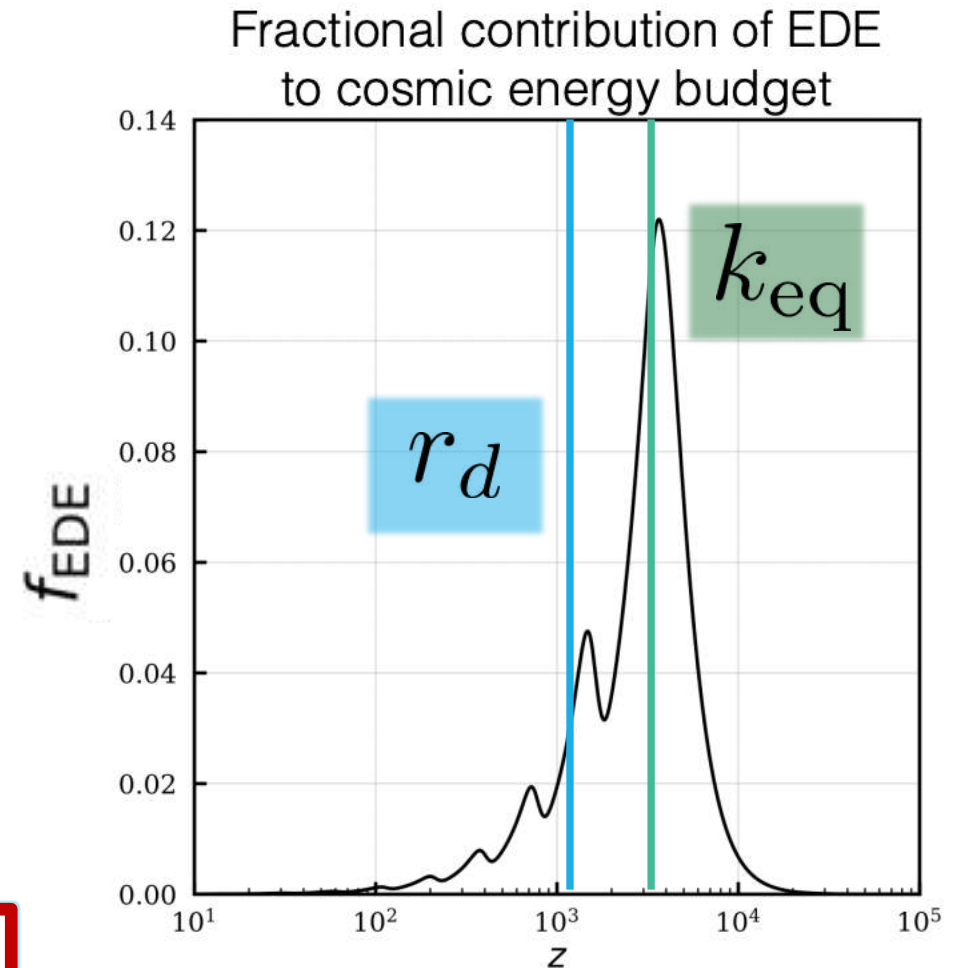
THE EQUALITY SCALE: AN (OLD) PROBE OF H_0 ?

- The **equality scale** contains H_0 information

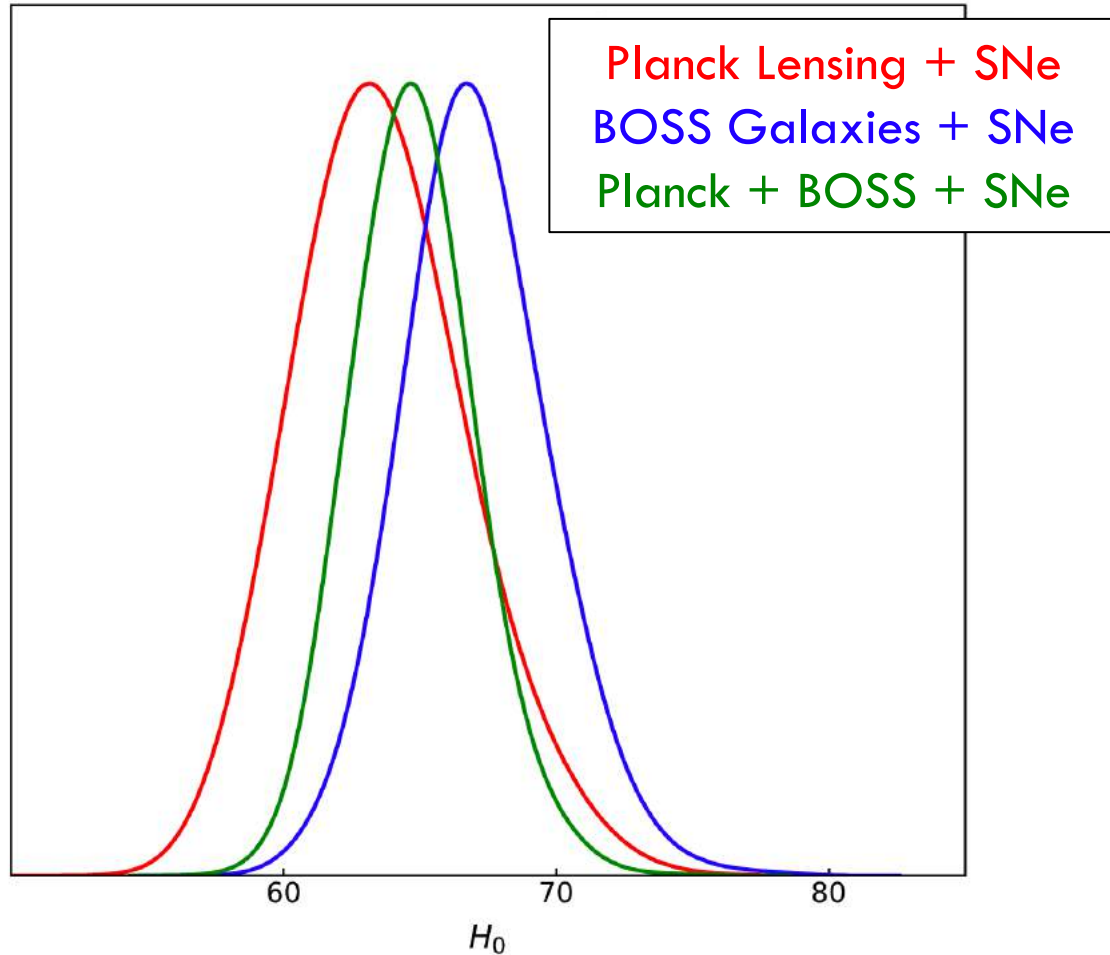
$$\theta_{\text{eq}} \sim k_{\text{eq}} D_A(z) \propto H_0$$

- This is anchored at $z_{\text{eq}} \sim 3600$, **much** before recombination at $z_d \sim 1100$
- New physics at $z \sim 10^3$ should affect **BAO** and **equality** H_0 measurements **differently**

$H_0(z_{\text{eq}}) - H_0(z_d)$ is a consistency test for Λ CDM



CONSTRAINTS ON H_0



Sound-Horizon Independent Constraints

BOSS Full Power Spectrum + Bispectrum:

$$(z \approx 1100) \quad H_0 = 68.3 \pm 0.8 \text{ km s}^{-1} \text{ Mpc}^{-1}$$

BOSS-without-the-sound-horizon:

(using new r_d -marginalized pipeline)

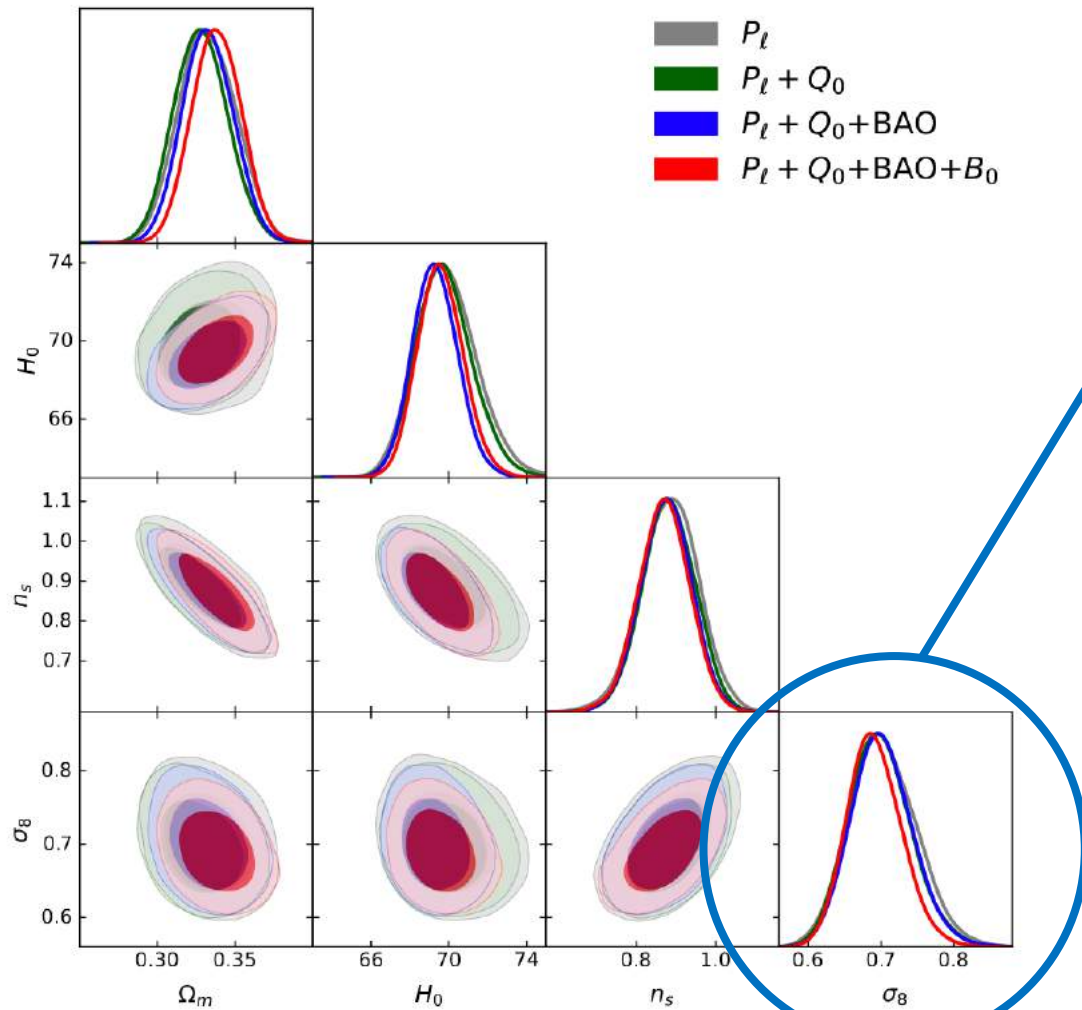
$$(z \approx 3500) \quad H_0 = 67.1 \pm 2.7 \text{ km s}^{-1} \text{ Mpc}^{-1}$$

3.0 σ tension with SHOES!

Measurements will get **much** tighter with Euclid!

CONSTRAINTS ON σ_8

BOSS (+ BBN) Constraints



BOSS Power Spectrum + Bispectrum:

$$\sigma_8 = 0.72 \pm 0.03 \text{ (with Planck } n_s)$$

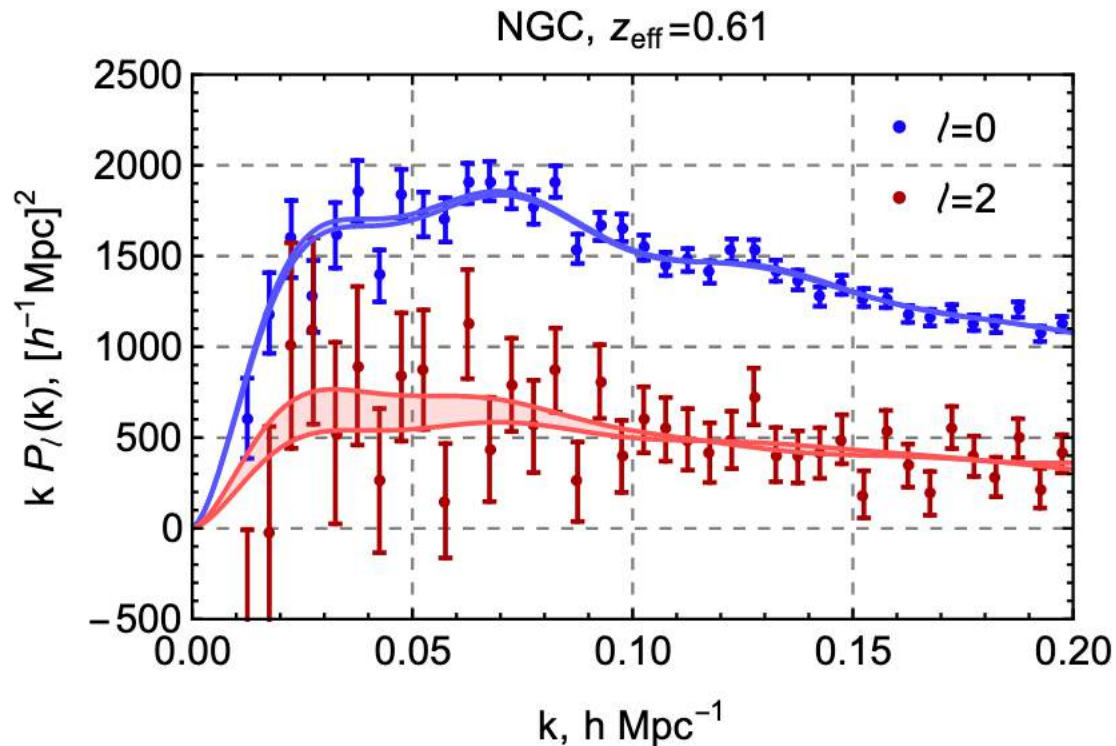
$$\sigma_8 = 0.69 \pm 0.04 \text{ (no Planck)}$$

This is consistent with weak lensing, but somewhat lower than *Planck*:

$$S_8 = 0.73 \pm 0.04 \text{ (BOSS)}$$

$$S_8 = 0.83 \pm 0.01 \text{ (Planck)}$$

WHERE DOES THE σ_8 INFORMATION COME FROM?



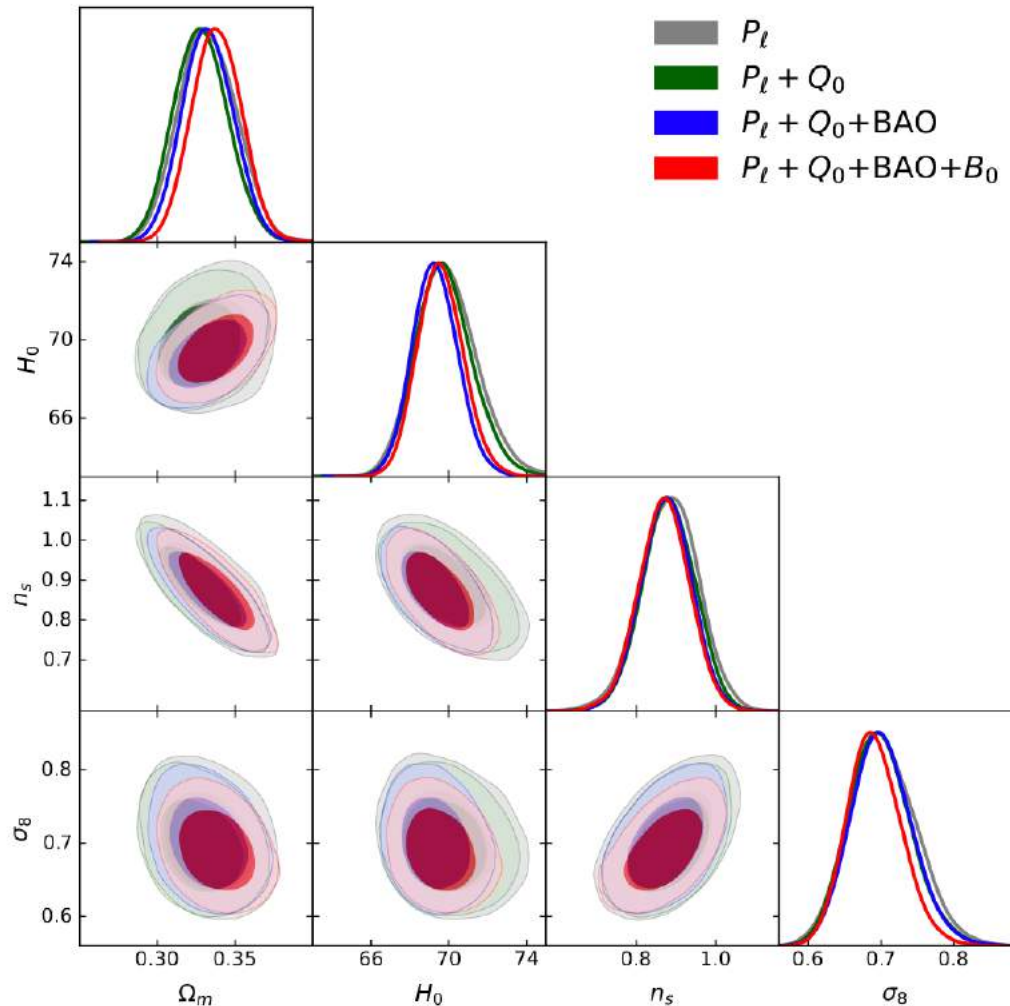
σ_8 is set by the **large-scale** ($k < 0.1 h/\text{Mpc}$) quadrupole

This is hard to change!

- ▶ Mostly linear scales
- ▶ Bias well understood
- ▶ Fingers-of-God suppressed

CONSTRAINTS ON OTHER PARAMETERS

BOSS (+ BBN) Constraints



Matter Density:

$$\Omega_m = 0.34 \pm 0.02$$

Consistent with Pantheon+ supernovae!

Spectral Slope:

$$n_s = 0.87 \pm 0.07$$

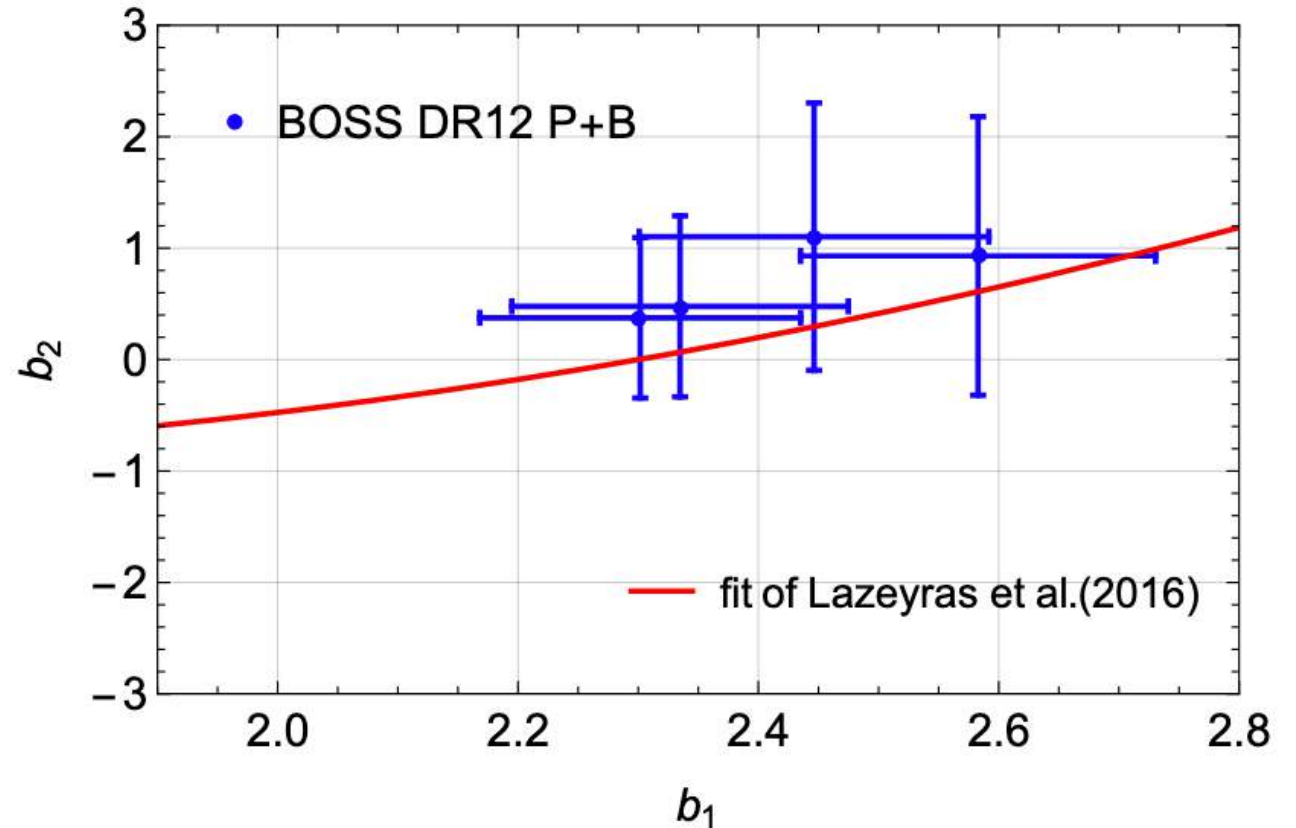
Consistent with *Planck*

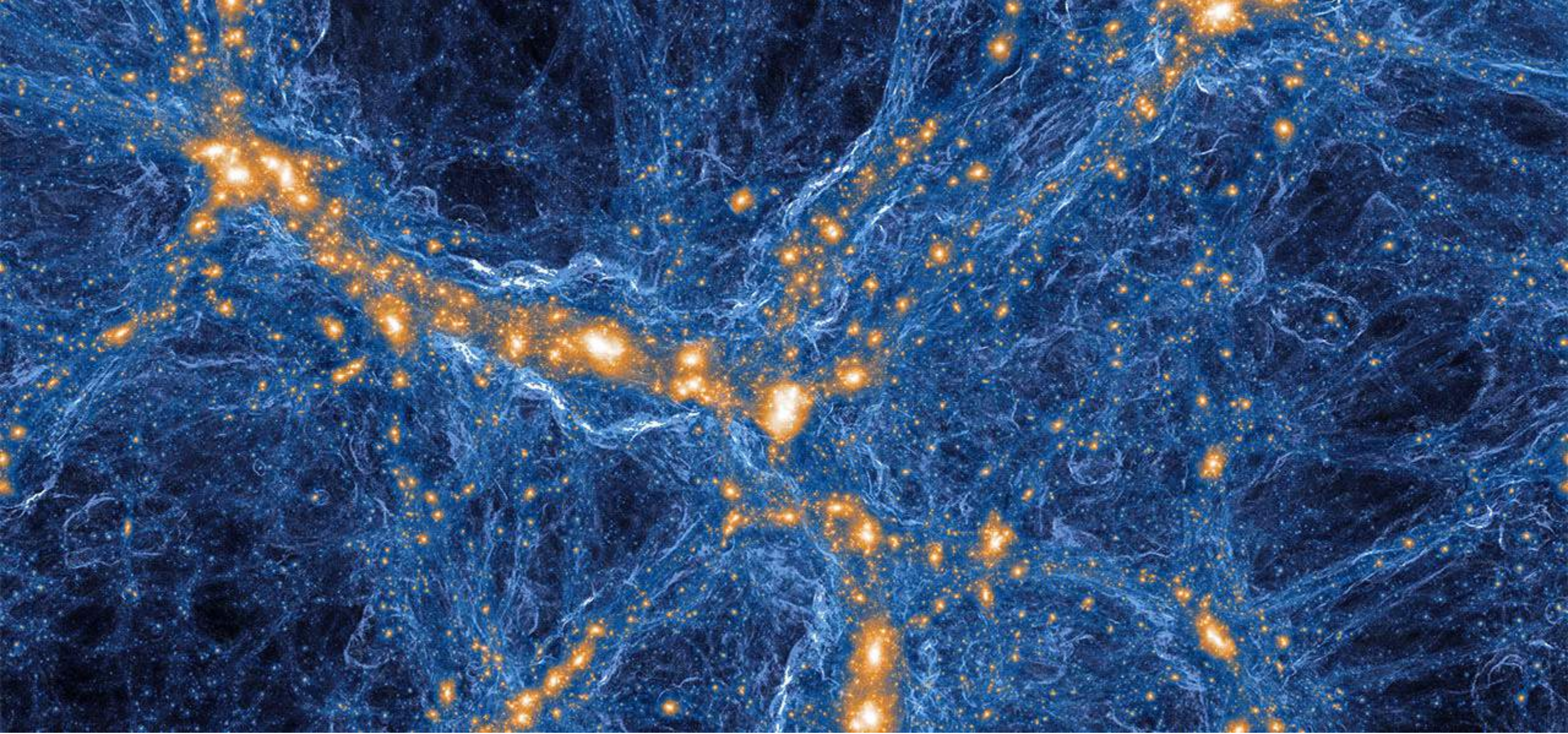
Neutrino Mass:

$$\sum m_\nu < 0.14 \text{ eV (95\% CL)}$$

CONSTRAINTS ON ASTROPHYSICS

- ▷ Analysis also measures **bias parameters** (especially the bispectrum)
- ▷ These encode the physics of galaxy formation
- ▷ Consistent with simulation results!





3. What Have We Learnt Beyond Λ CDM?

NON-GAUSSIAN INFLATION

Are the primordial perturbations **Gaussian** and **adiabatic**?

In Single-Field Slow-Roll Inflation:

$$f_{\text{NL}} \sim (1 - n_s) \ll 1$$

Non-standard inflation can beat this:

- ▷ Multifield Inflation [Local Bispectrum]
- ▷ New Kinetic Terms [Equilateral Bispectrum]
- ▷ New Vacuum States [Folded Bispectrum]

$$B_\zeta(\mathbf{k}_1, \mathbf{k}_2) \approx \frac{6}{5} f_{\text{NL}} P_\zeta(k_1) P_\zeta(k_2) + 2 \text{ perms.}$$

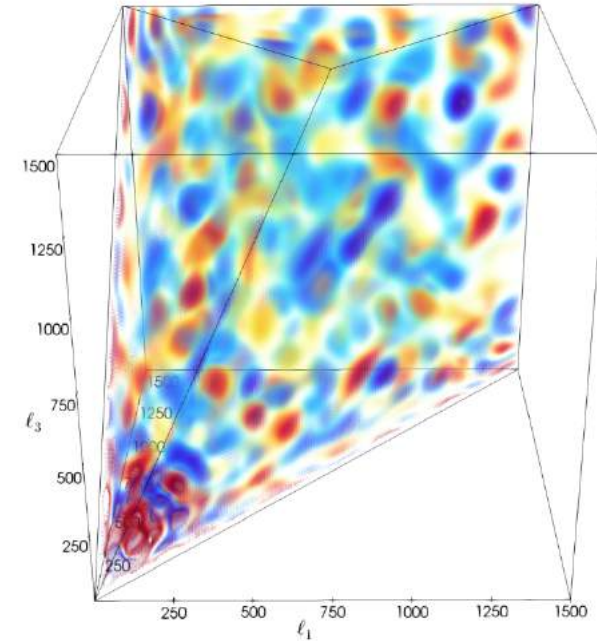
NON-GAUSSIAN INFLATION

$$B_{\zeta}(\mathbf{k}_1, \mathbf{k}_2) \approx \frac{6}{5} f_{\text{NL}} P_{\zeta}(k_1) P_{\zeta}(k_2) + 2 \text{ perms.}$$

How do we measure this?

1. CMB Bispectrum

Planck TTT Bispectrum



$\approx 2\times$ better
with CMB-S4!

f_{NL} Constraints

Local	6.7 ± 5.6
Equilateral	6 ± 66
Orthogonal	-38 ± 36

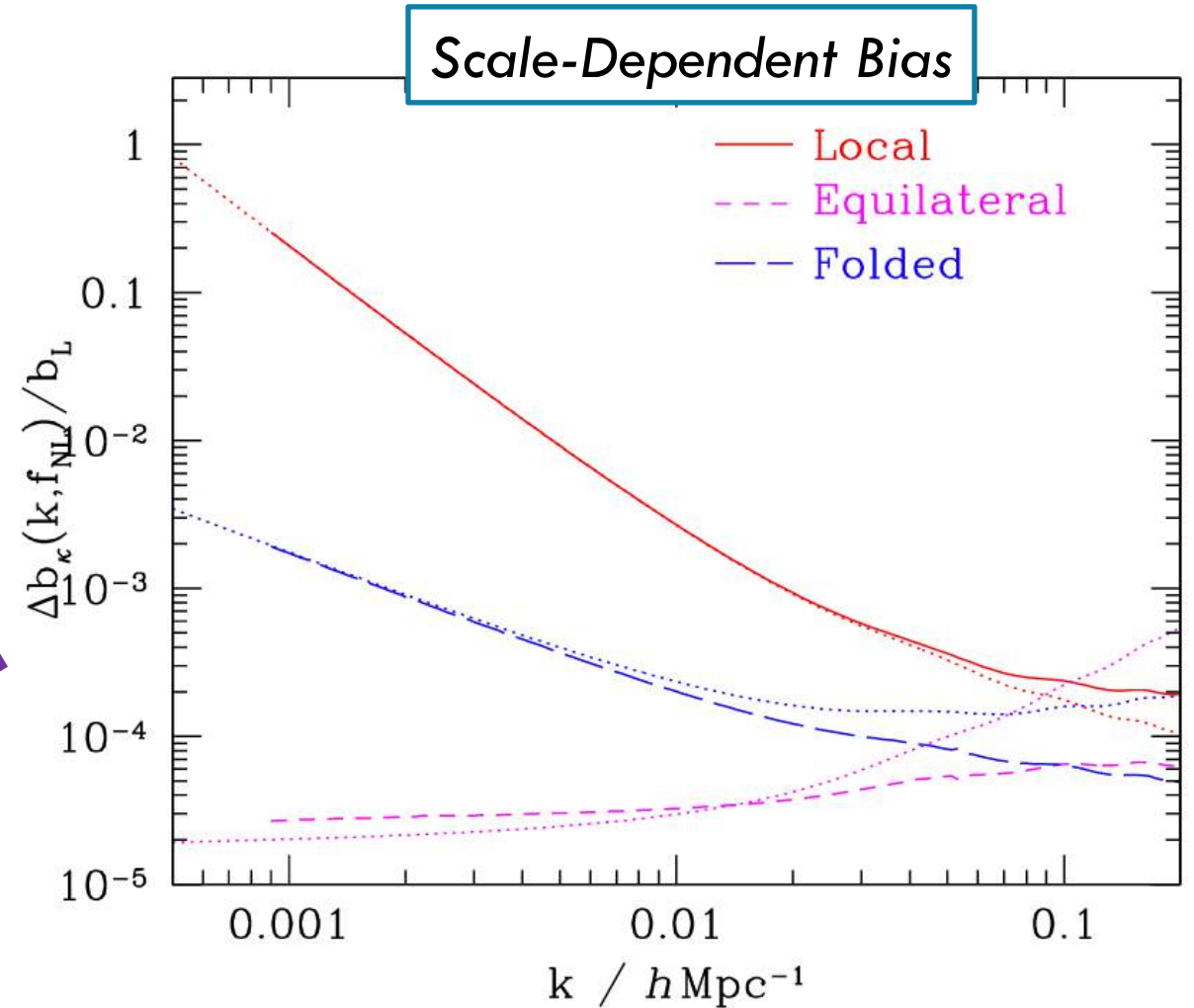
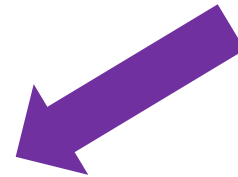
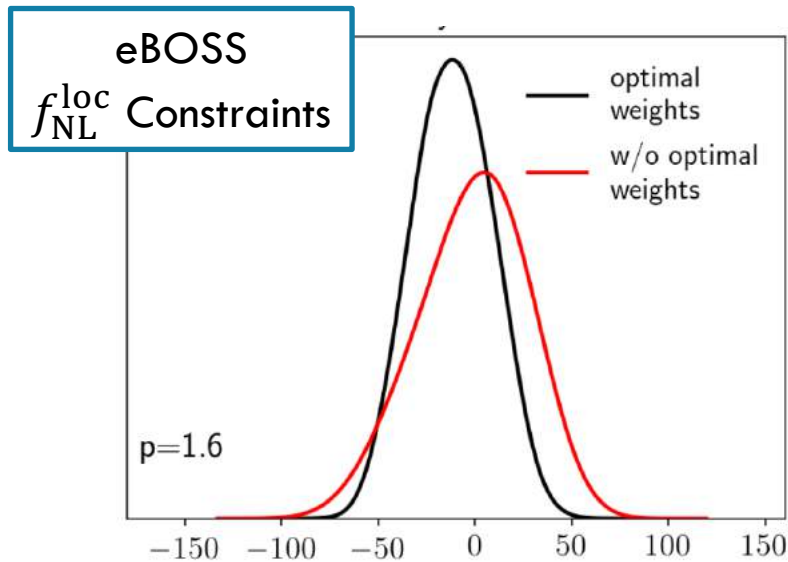
NON-GAUSSIAN INFLATION

$$B_{\zeta}(\mathbf{k}_1, \mathbf{k}_2) \approx \frac{6}{5} f_{\text{NL}} P_{\zeta}(k_1) P_{\zeta}(k_2) + 2 \text{ perms.}$$

How do we measure this?

1. CMB Bispectrum

2. Galaxy Power Spectrum



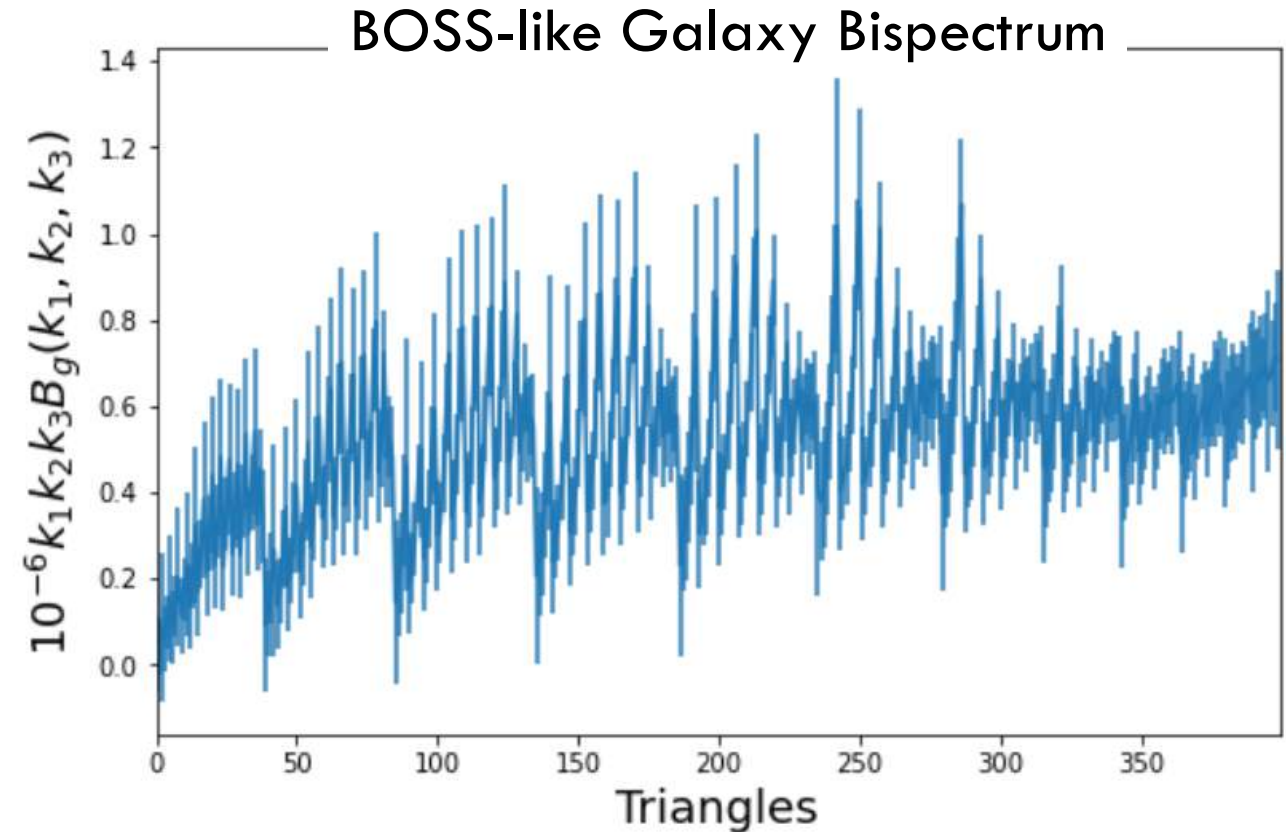
NON-GAUSSIAN INFLATION

$$B_{\zeta}(\mathbf{k}_1, \mathbf{k}_2) \approx \frac{6}{5} f_{\text{NL}} P_{\zeta}(k_1) P_{\zeta}(k_2) + 2 \text{ perms.}$$

How do we measure this?

1. CMB Bispectrum
2. Galaxy Power Spectrum
3. **Galaxy Bispectrum**

Need a good theory model and careful window function treatment!



MODELING PRIMORDIAL NON-GAUSSIANITIES

Theory model includes:

▷ Primordial bispectrum:

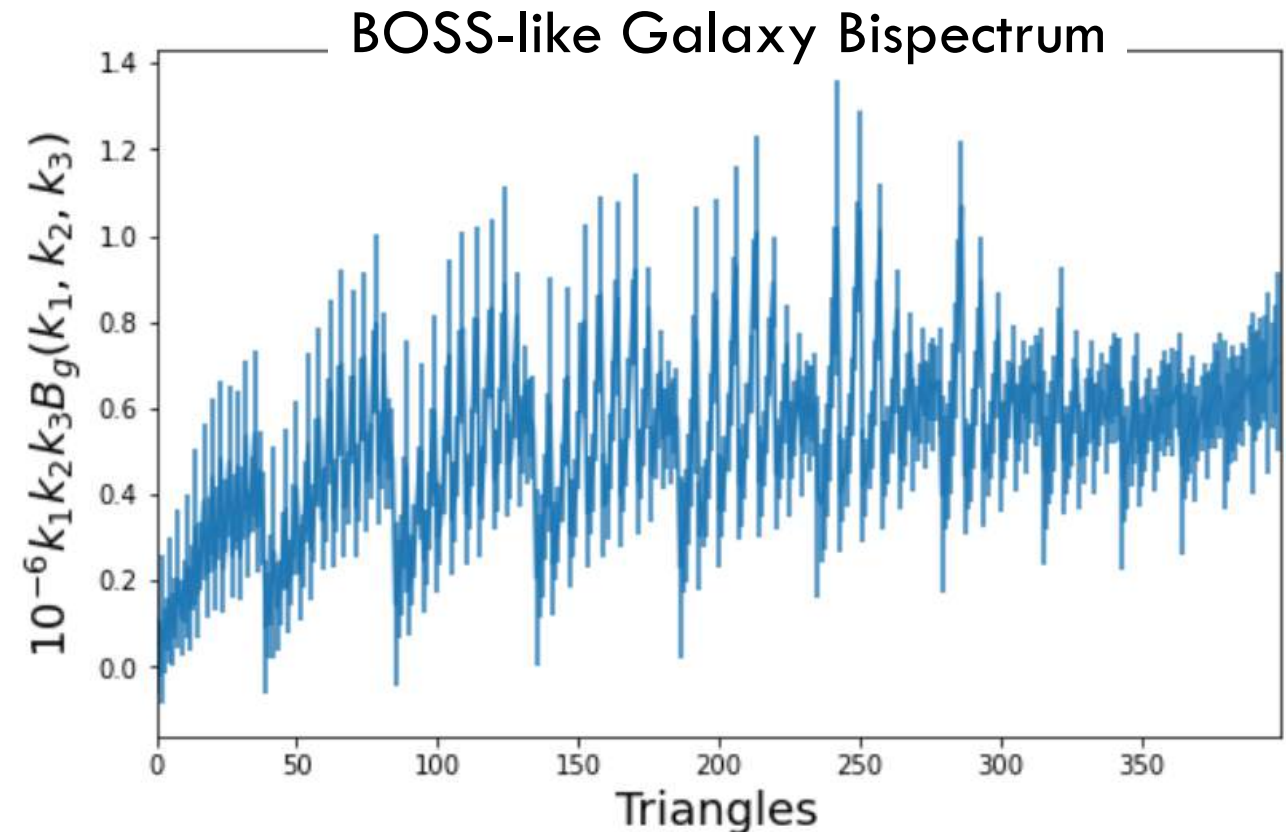
$$\langle \delta^{(1)} \delta^{(1)} \delta^{(1)} \rangle \sim f_{\text{NL}} P^2(k)$$

▷ Scale dependent bias:

$$b_1(f_{\text{NL}}) \rightarrow b_1 + (b_\phi f_{\text{NL}})/k^2$$

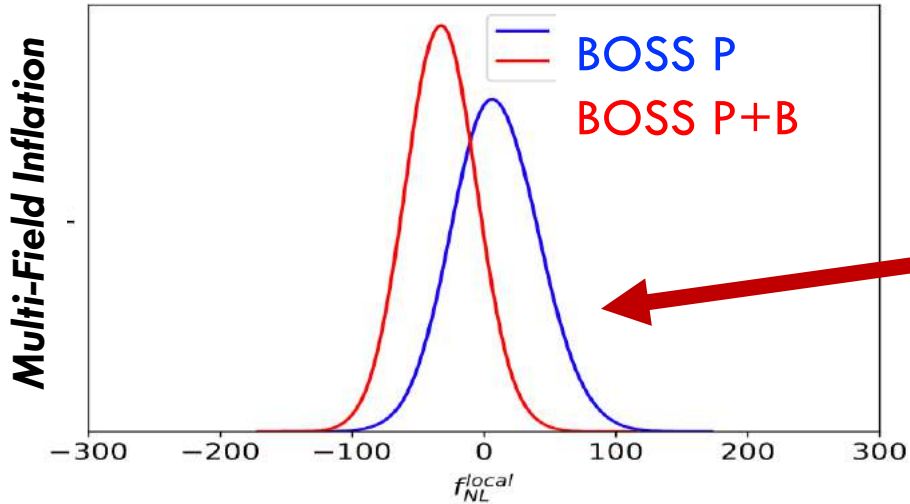
▷ Loop corrections:

$$P_{gg}(\mathbf{k}) \rightarrow P_{gg}(\mathbf{k}) + f_{\text{NL}} \int d\mathbf{q} \alpha P(\mathbf{q})P(\mathbf{k} - \mathbf{q})$$



$$B_g = B_g(f_{\text{NL}}^{\text{eq}}, f_{\text{NL}}^{\text{orth}}, f_{\text{NL}}^{\text{loc}})$$

CONSTRAINTS ON f_{NL}

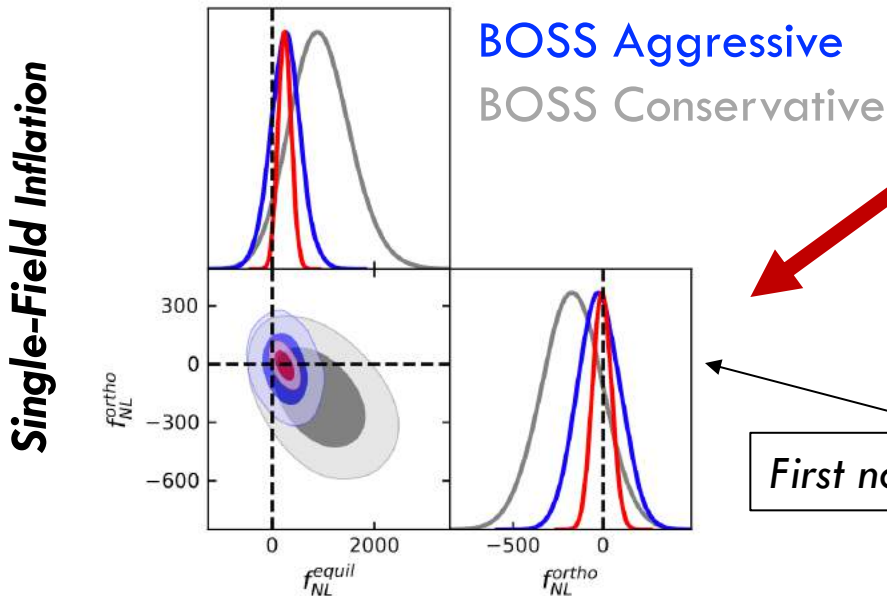


BOSS Power Spectrum + Bispectrum:

$$f_{\text{NL}}^{\text{local}} = -33 \pm 28 \quad [\text{fixing } b_\phi]$$

$$f_{\text{NL}}^{\text{equil}} = 940 \pm 600$$

$$f_{\text{NL}}^{\text{orth}} = 170 \pm 170$$

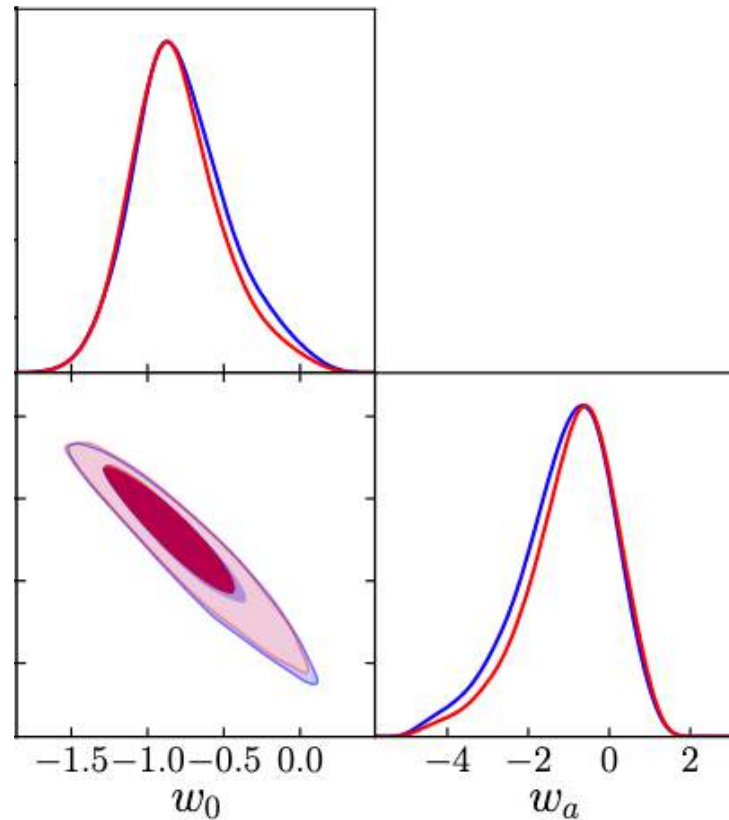


This constrains the effective field theory of inflation, e.g., the inflaton sound-speed:

$$c_s \geq 0.013 \text{ (95\% CI)}$$

First non-CMB measurements!

OTHER POST- Λ CDM CONSTRAINTS

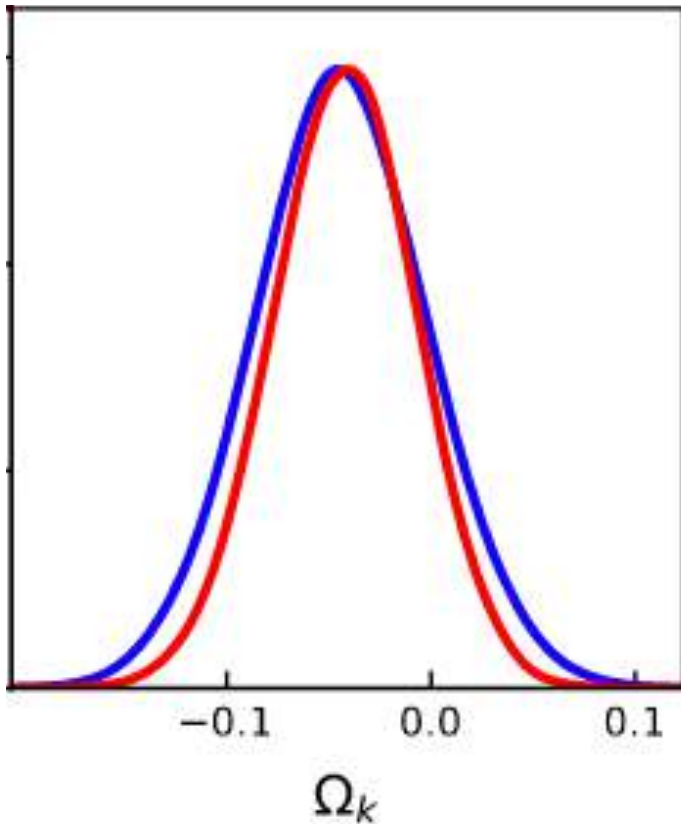


▷ w_0, w_a consistent with cosmological constant
[Chudaykin+20]

$$w_0 = -0.98 \pm 0.01$$

$$w_a = -0.3 \pm 0.6$$

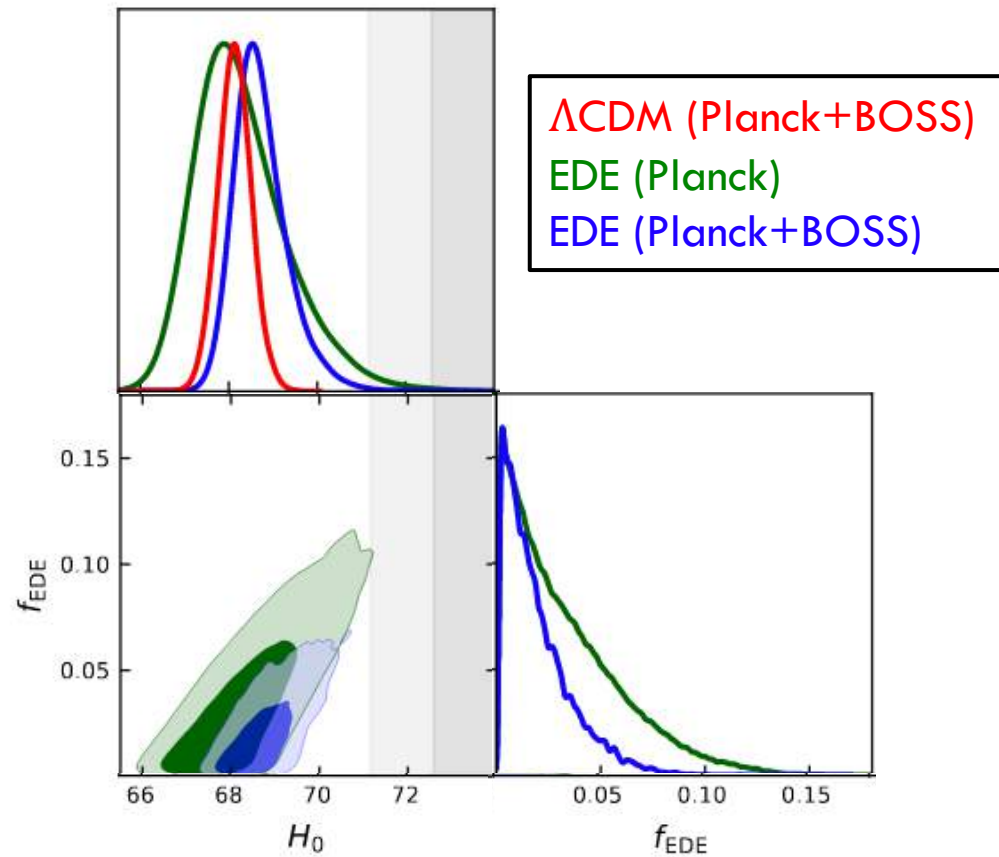
OTHER POST- Λ CDM CONSTRAINTS



$$\Omega_k = -0.04 \pm 0.04$$

- ▷ w_0, w_a consistent with cosmological constant [Chudaykin+20]
- ▷ Curvature consistent with zero [Chudaykin+20]

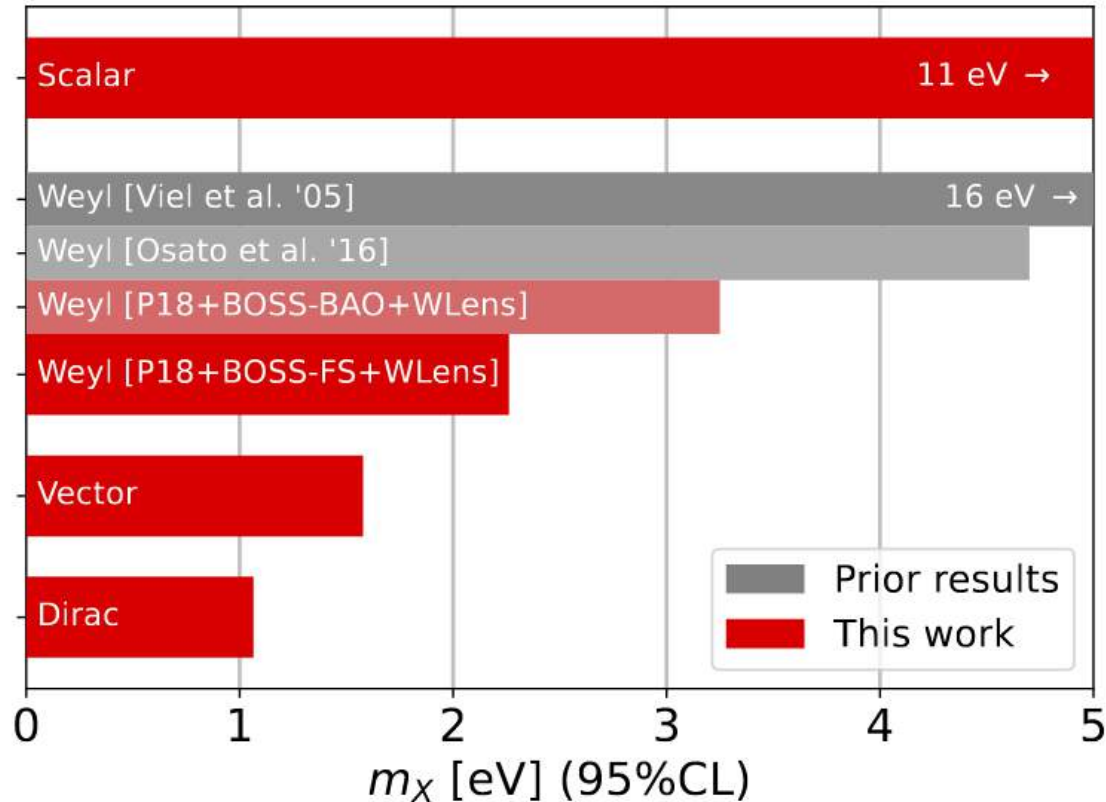
OTHER POST- Λ CDM CONSTRAINTS



$$f_{\text{EDE}} < 0.053 \text{ (95\% CL)}$$

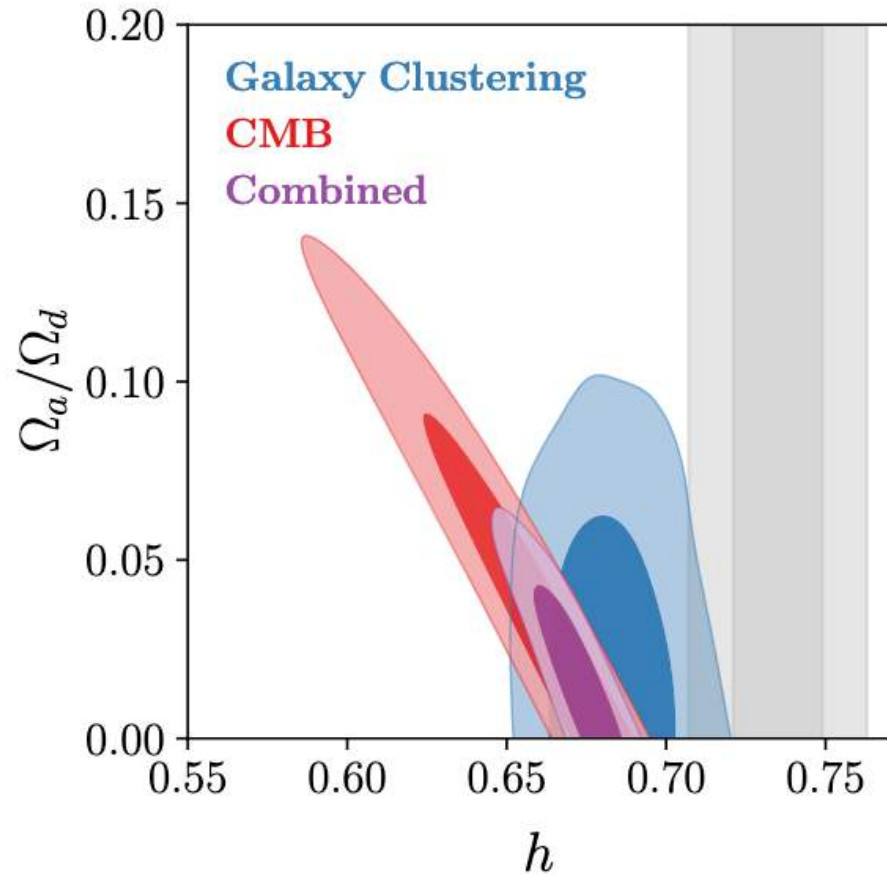
- ▷ w_0, w_a consistent with cosmological constant [Chudaykin+20]
- ▷ Curvature consistent with zero [Chudaykin+20]
- ▷ No evidence for early dark energy [Ivanov+20]

OTHER POST- Λ CDM CONSTRAINTS



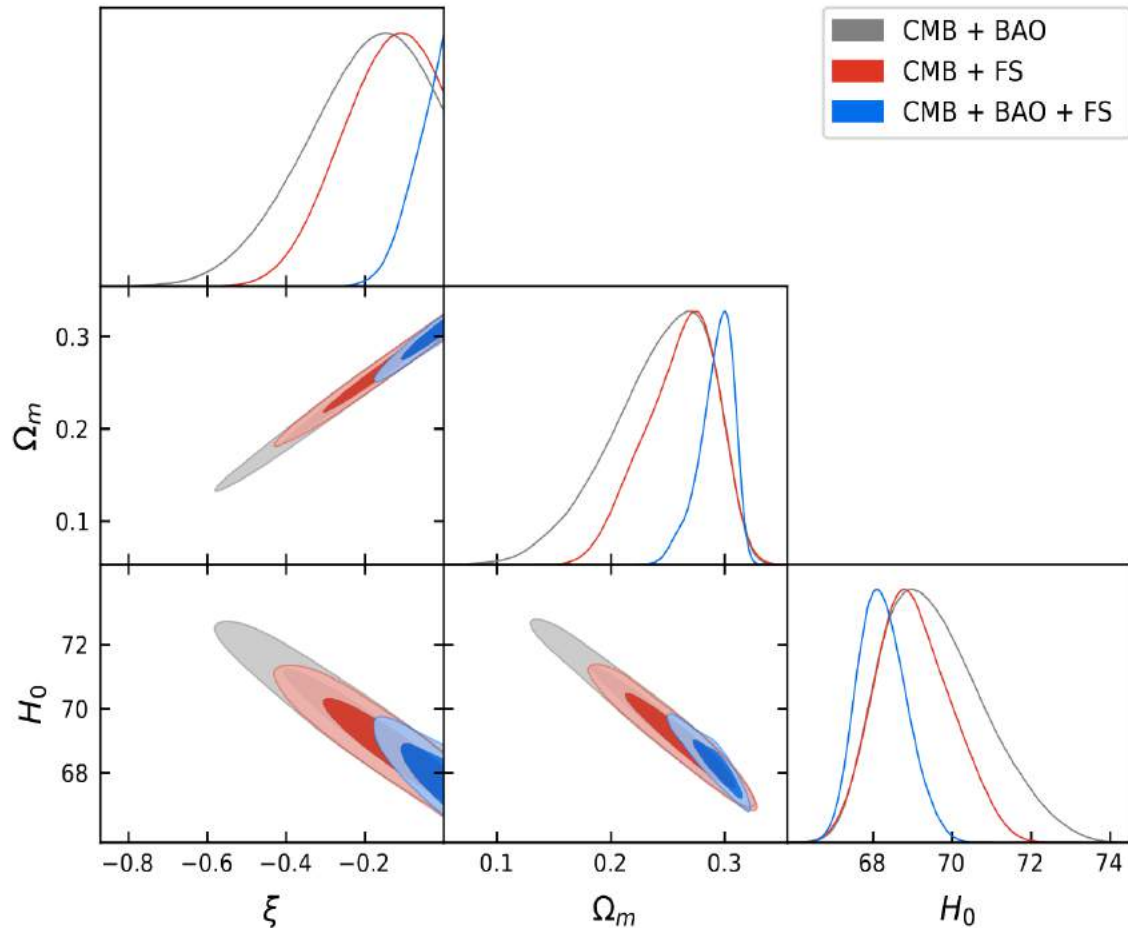
- ▷ w_0, w_a consistent with cosmological constant [Chudaykin+20]
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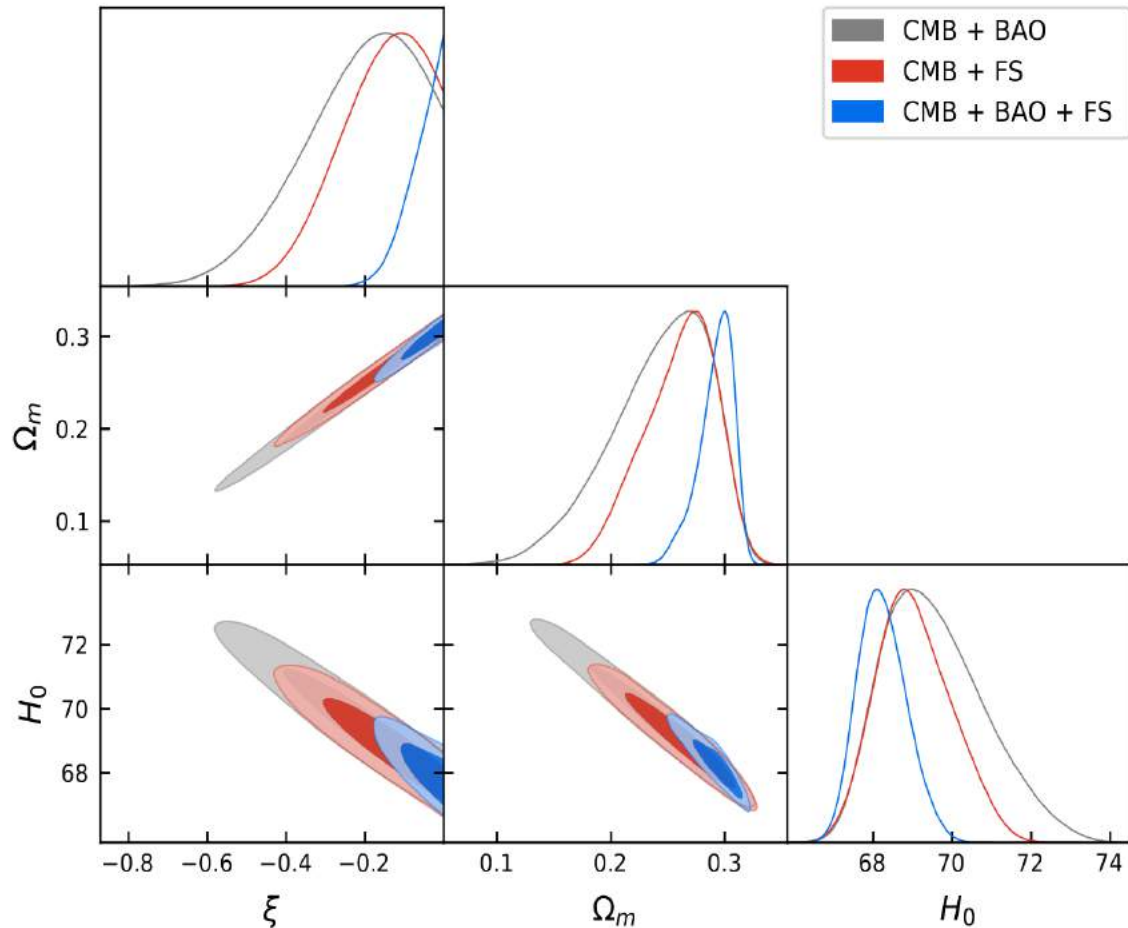
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And many more...

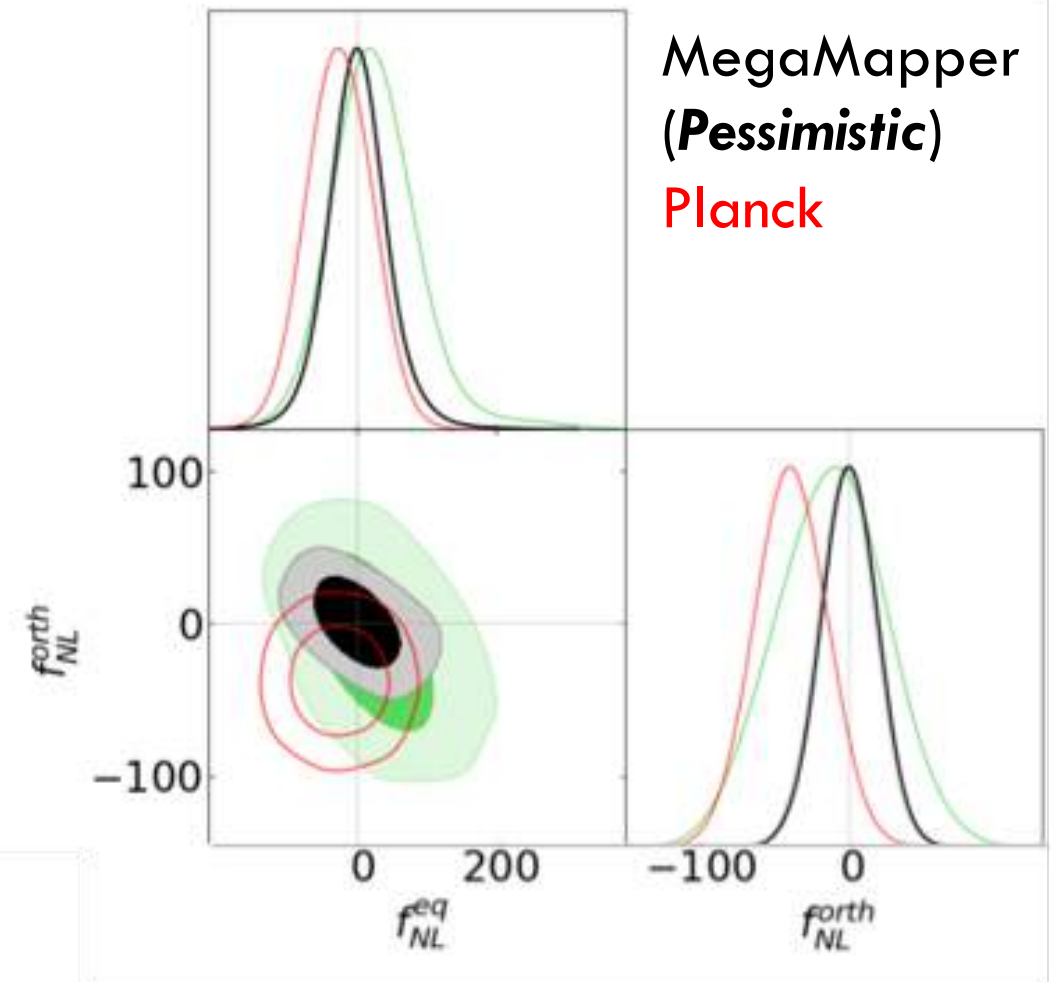
All analysis is public:

github.com/oliverphilcox/full_shape_likelihoods

WHAT'S NEXT?

- ▶ **Complete** bispectrum theory model at **one-loop**
- ▶ Bispectrum **Multipoles?**
- ▶ Trispectrum / correlation functions?
- ▶ Other new physics?
- ▶ **DESI / Euclid** + beyond?

LSS constraints will (eventually) beat the CMB!



CONCLUSIONS

- We can robustly **measure** and **model** the galaxy power spectrum and bispectrum of survey data
- This allows **direct** extraction of **cosmological parameters** including H_0 , Ω_m , σ_8 , f_{NL} , w_0 , Ω_k , f_{EDE}
- BOSS data is already useful: this will get much better with **Euclid** / **DESI**

arXiv

[2204.02984](#)

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