Simulation-based inference for pulsar-population synthesis

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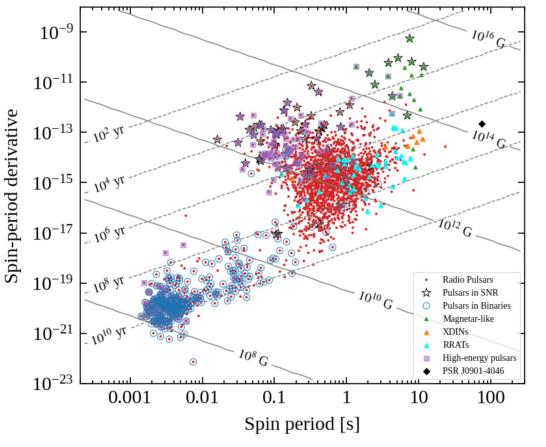
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The neutron-star zoo

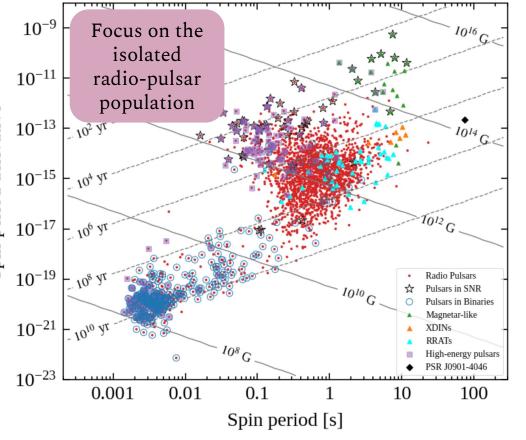


~ 3,000 pulsars are known to date

- Neutron stars are observed as pulsars across the electromagnetic spectrum from radio to X-rays and gamma-rays
- Different classes of neutron stars occupy different locations in the *PP*-plane probing different evolution paths and/or different origins

data from the ATNF pulsar catalogue (Manchester et al. 2005)

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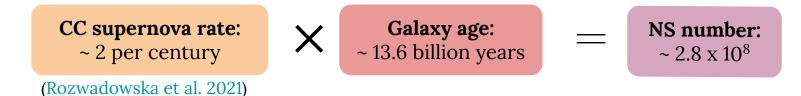


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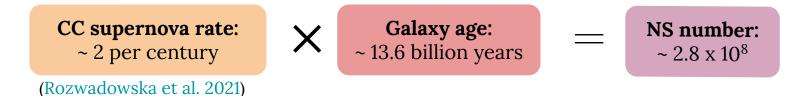
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Population synthesis

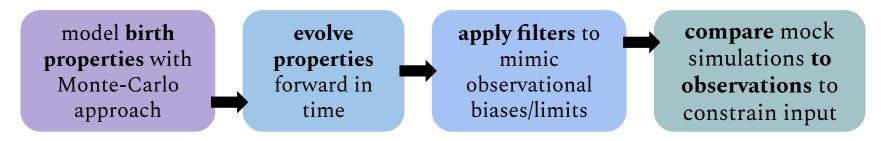


- We only **detect** a very **small fraction** of all neutron stars.
 - What are the **natal properties** and the **birth rate** of the NS population?
 - Is there any evolutionary link between different neutron-star classes?

Population synthesis

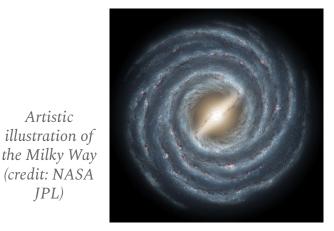


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 - What are the **natal properties** and the **birth rate** of the NS population?
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- Population synthesis bridges this gap by focusing on the full population of neutron stars (e.g. Faucher-Giguère & Kaspi 2006, Lorimer et al. 2006, Gullón et al. 2014, Cieślar et al. 2020):



Dynamical evolution

Neutron stars are born in star-forming regions, i.e., in • the Galactic disk along the Milky Way's spiral arms, and receive kicks during the supernova explosions.

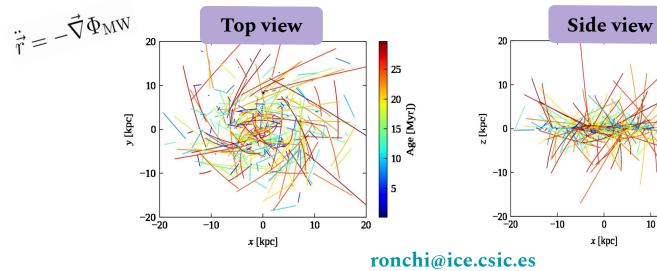


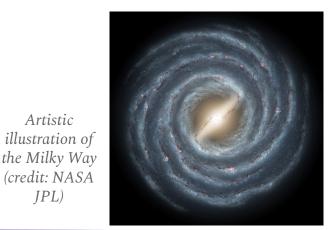
Artistic

JPL)

Dynamical evolution

- Neutron stars are born in star-forming regions, i.e., in the Galactic disk along the Milky Way's spiral arms, and receive kicks during the supernova explosions.
- We evolve the stars' position & velocity by **solving** Newtonian equations of motion in cylindrical galactocentric coordinates:





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5 12 3 Age [Myr])

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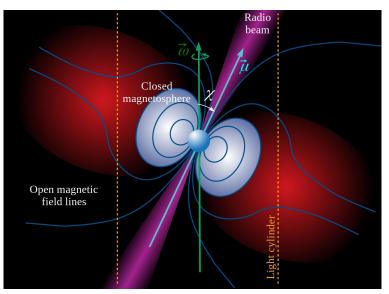
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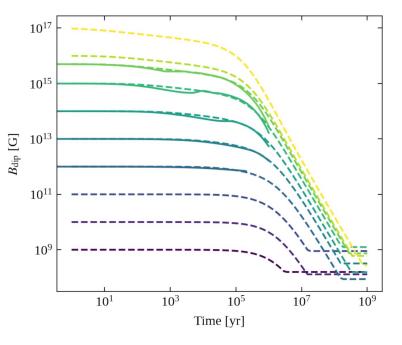
Artistic

IPL)

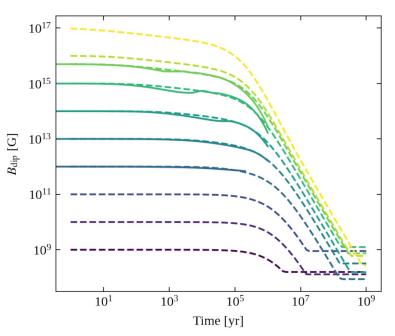
• The neutron-star magnetosphere exerts a **torque onto the star**. This causes **spin-down** and **alignment of the magnetic and rotation axes** (Spitkovsky 2006, Philippov et al. 2014).



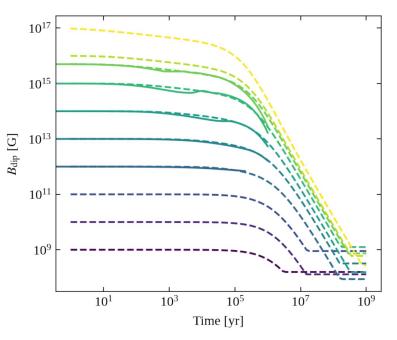
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- Neutron star **magnetic fields decay** due to the Hall effect and Ohmic dissipation in the outer stellar layer (crust) (e.g., Viganó et al. 2013 & 2021, De Grandis et al. 2020).

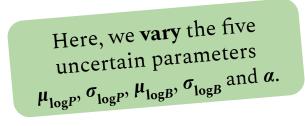


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- We make the following assumptions:
 - **Initial periods** follow a normal in log with $\mu_{\log P}$ Ο and $\sigma_{\log P}$ (Igoshev et al. 2022) Initial fields follow a normal in log with $\mu_{\log B}$
 - Ο and $\sigma_{\log B}$ (Gullón et al. 2014)
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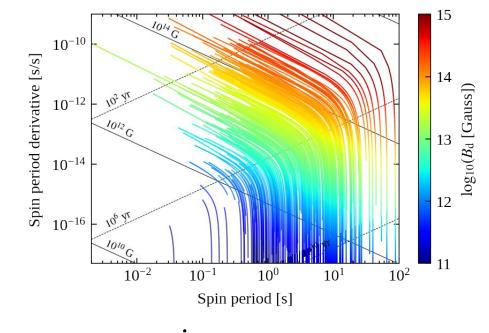




$$\dot{P} = \frac{\pi^2}{c^3} \frac{B^2 R^6}{IP} \left(\kappa_0 + \kappa_1 \sin^2 \chi\right)$$
$$\dot{\chi} = -\frac{\pi^2}{c^3} \frac{B^2 R^6}{IP^2} \left(\kappa_2 \sin \chi \cos \chi\right)$$

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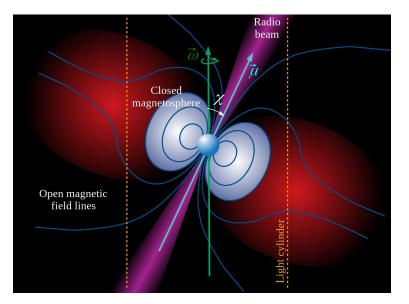
(Spitkovsky 2006, Philippov et al. 2014)



PP evolution tracks for $\mu_{\log P}$ = -0.6 , $\sigma_{\log P}$ = 0.3 , $\mu_{\log B}$ = 13.25, $\sigma_{\log B}$ = 0.75 and α = -2.0

• The stars' rotational energy E_{rot} is converted into coherent radio emission (Faucher-Giguère & Kaspi 2006; Gullón et al. 2014).

$$L_{
m radio} = L_0 igg(rac{\dot{P}}{P^3} igg)^{1/2} \propto \dot{E}_{
m rot}^{1/2}$$

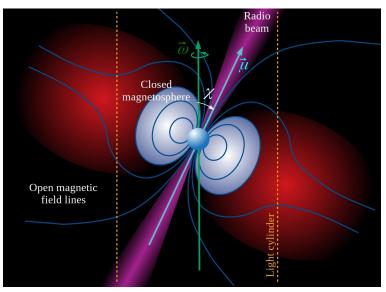


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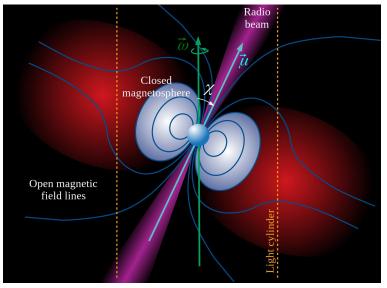
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• A signal-to-noise ratio can be estimated through the radiometer equation.

$$S/N = \frac{S_{\text{mean}} G \sqrt{N_{\text{pol}} \Delta \nu \Delta t_{\text{obs}}}}{\beta \left(T_{\text{rec}} + T_{\text{sky}}(l, b)\right)} \sqrt{\frac{P - w_{\text{eff}}}{w_{\text{eff}}}}$$



• The stars' **rotational energy** E_{rot} is converted into coherent radio emission (Faucher-Giguère & Kaspi 2006; Gullón et al. 2014).

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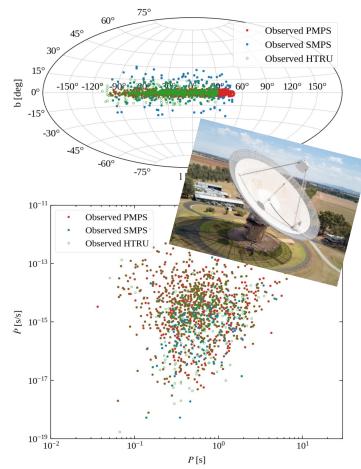
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A pulsar counts as detected, if it **exceeds the sensitivity threshold** for a survey recorded with a specific radio telescope.

Three radio surveys

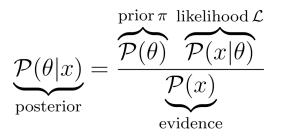
- We compare our simulated populations with three surveys from Murriyang (the Parkes Radio Telescope):
 - **Parkes Multibeam Pulsar Survey** (PMPS) (Manchester et al. 2001, Lorimer et al. 2006): 1,009 isolated pulsars
 - Swinburne Parkes Multibeam Pulsar Survey (SMPS) (Edwards et al. 2001, Jacoby et al. 2009): 218 isolated pulsars
 - High Time Resolution Universe Survey (HTRU) (Keith et al. 2018): 1,023 isolated pulsars

Can we constrain birth properties by looking at a current snapshot of the pulsar population?



Simulation-based (likelihood-free) inference (SBI)

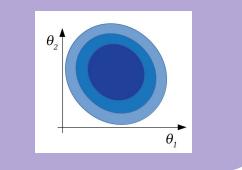
Based on some prior knowledge π(θ), a stochastic model and some observation x, we want to infer the most likely distribution P(θ|x) for our model parameters θ given the data x. This is encoded in Bayes' Theorem:



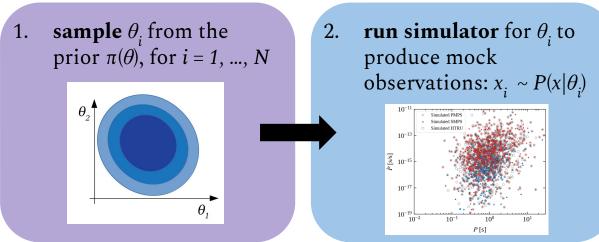
For complex simulators, the **likelihood is defined implicitly and often intractable**. This is overcome with **simulation-based** (likelihood-free) **inference** (see e.g. Cranmer et al. 2020).

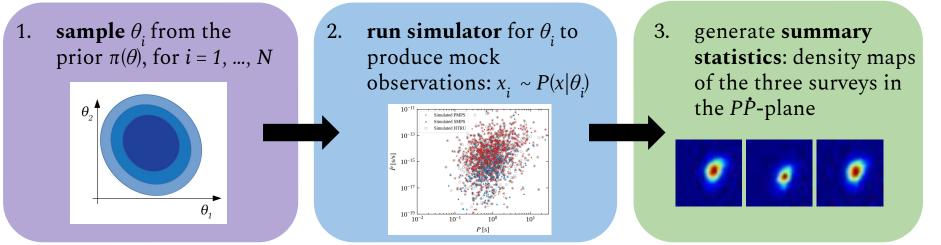
• Neural Posterior Estimation (NPE) (e.g., Papamakarios & Murray 2016) uses a neural network to learn a mapping between the simulated data and the posterior distribution of the underlying parameters.

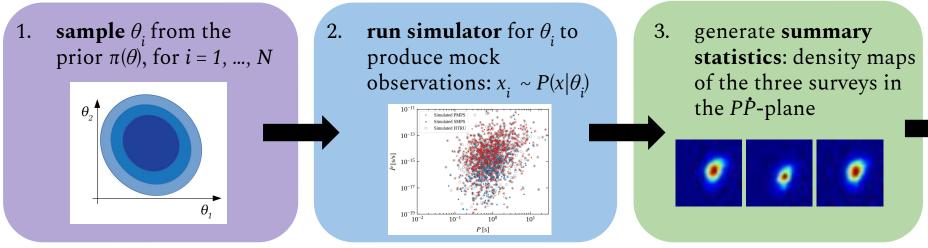
1. **sample** θ_i from the prior $\pi(\theta)$, for i = 1, ..., N



 $(\mu_{\log P}, \sigma_{\log P}, \mu_{\log B}, \sigma_{\log B}, \alpha)$

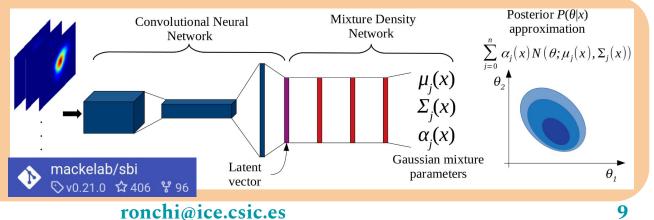






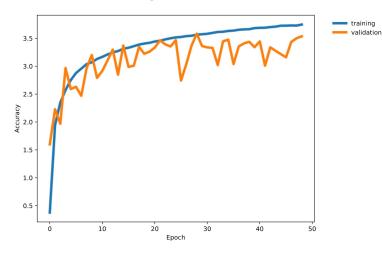
 4. train a neural network (conditional density estimator) on simulated data to approximate the posterior

Tejero-Cantero et al. 2020

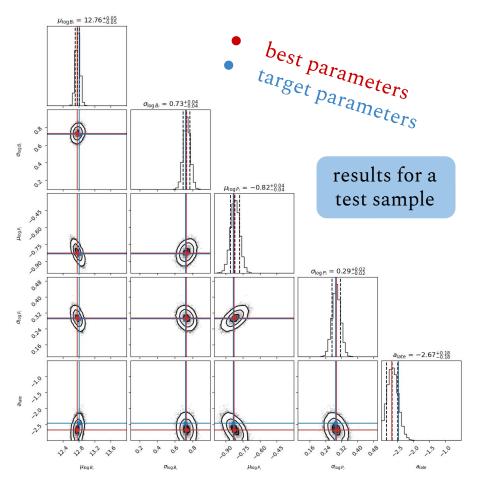


SBI - Results

120,000 simulations in total, we use
87 % for training, 10 % for validation,
3 % for testing.



The network is able to predict the posterior for any input simulation (amortized posterior).



SBI - Results for observed population

With our optimised neural network, we can also **infer the posteriors** for the **pulsar population detected in our three surveys** and recover the following constraints:

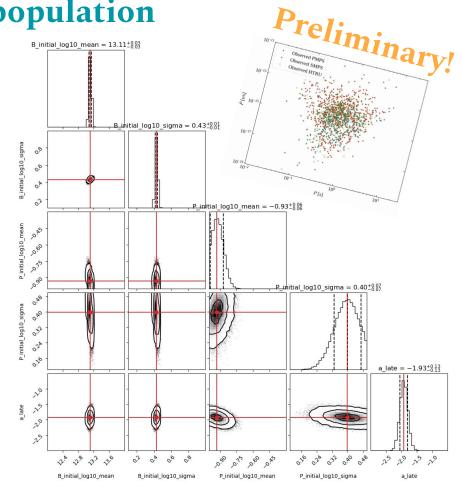
$$\mu_{\log B} = 13.10^{+0.06}_{-0.06}$$

$$\sigma_{\log B} = 0.43^{+0.03}_{-0.03}$$

$$\mu_{\log P} = -0.93^{+0.12}_{-0.12}$$

$$\sigma_{\log P} = 0.40^{+0.14}_{-0.14}$$

$$\alpha = -1.92^{+0.25}_{-0.25}$$



Future plans

IMPROVING THE SIMULATOR

- Explore different assumptions on initial period and magnetic-field distributions
- Extend framework to model also gamma-ray and X-ray emission and predict the multi-wavelength emission

IMPROVING SBI

• Expand the approach to active learning and derive posteriors sequentially using SNPE.

Thank you!

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