



Unraveling The Role of Cosmic Velocity Field in Dark Matter Halo Mass Function Using Deep Learning



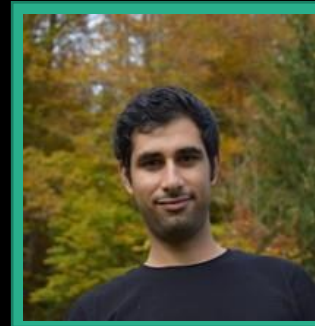
Saba Etezzad-Razavi
Sharif University of Technology



Erfan Abbasgholinezhad
Sharif University of Technology



Mohammad-Hadi Sotoudeh
Sharif University of Technology
Mila - Quebec Artificial Intelligence Institute
Université de Montréal



Farbod Hassani
Institute of Theoretical Astrophysics
University of Oslo



Sadegh Raeisi
Sharif University of Technology



Shant Baghrum
Sharif University of Technology

Introduction

Analytical models

Pros:

- Physical insight about the process of halo formation

Cons:

- Non accurate HMF for the smallest halos
- Simplified assumptions about the halos' shape

N-body Simulations

Pros:

- Accurate Halo Mass function
- Without any assumption about the halos' shape

Cons:

- Computationally expensive
- Lack of physical insight through the collapse process

Does the initial condition have enough information to capture all the properties of dark matter halos?

Analyt

Pros:

- Physical insight about the process of halo formation

Cons:

- Non accurate HMF for the smallest halos
- Simplified assumptions about the halos' shape

Pros:

- Accurate Halo Mass function
- Without any assumption about the halos' shape

Cons:

- Computationally expensive
- Lack of physical insight through the collapse process

Does the initial condition have enough information to capture all the properties of dark matter halos?

Analyt

Pros:

- Phy

Suppose the initial condition is enough to capture the dark matter mass distribution.

- No

Would initial density field information (isotropic or non-isotropic) be sufficient to predict the halo mass function accurately?

- Sim

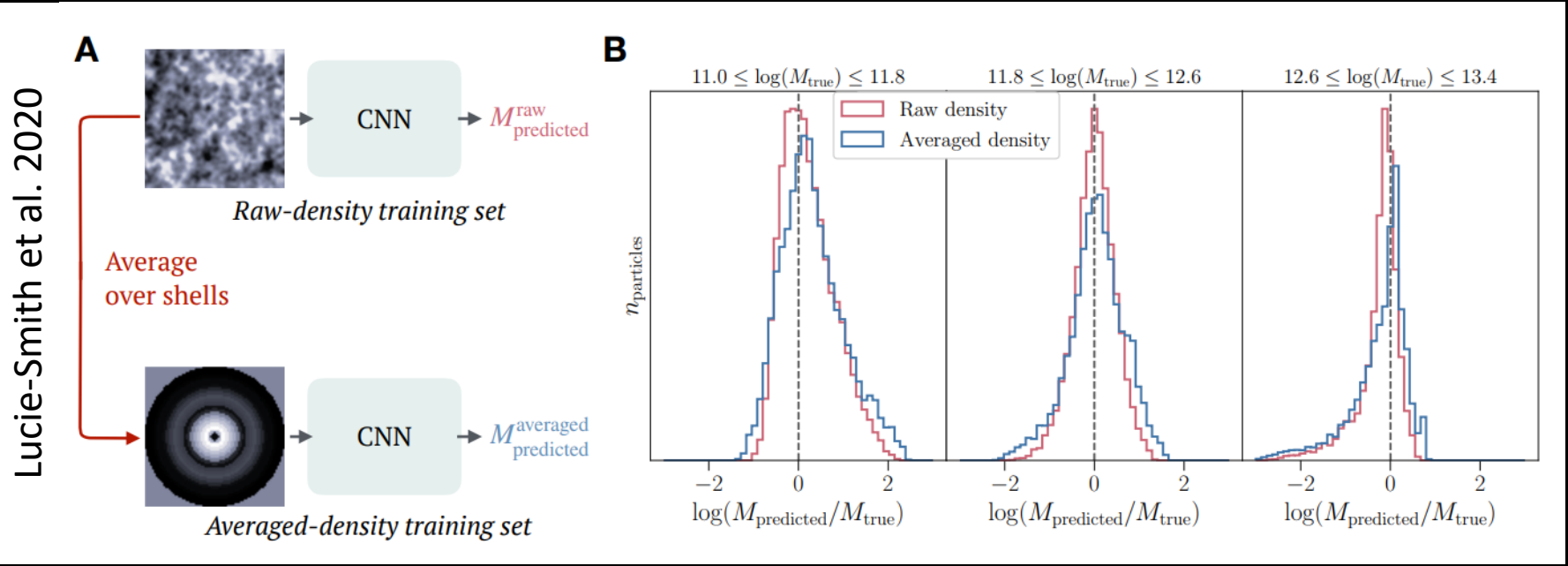
Pros:

ion

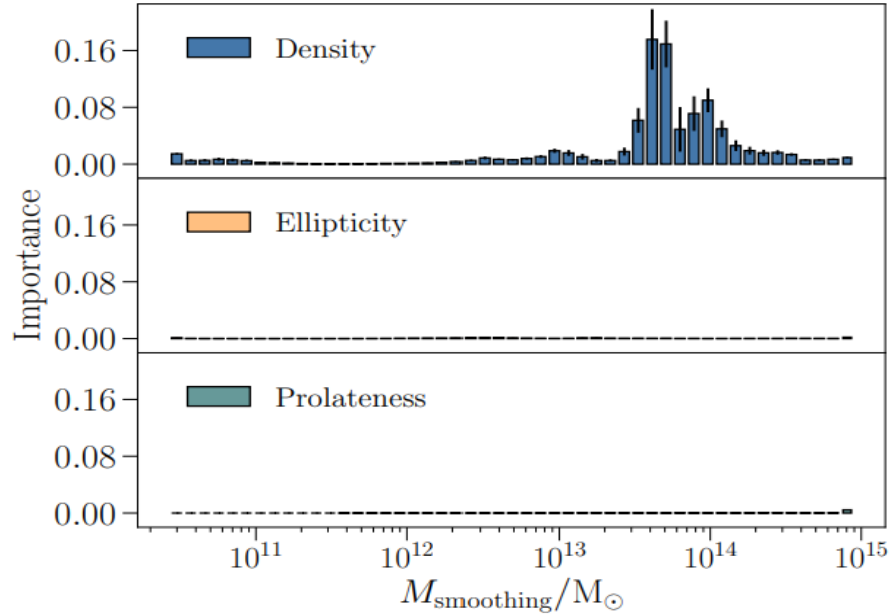
out the

h the

collapse process



Classifier: Random Forest



Lucie-Smith et al. 2019

Isotropic or anisotropic density field?

Method

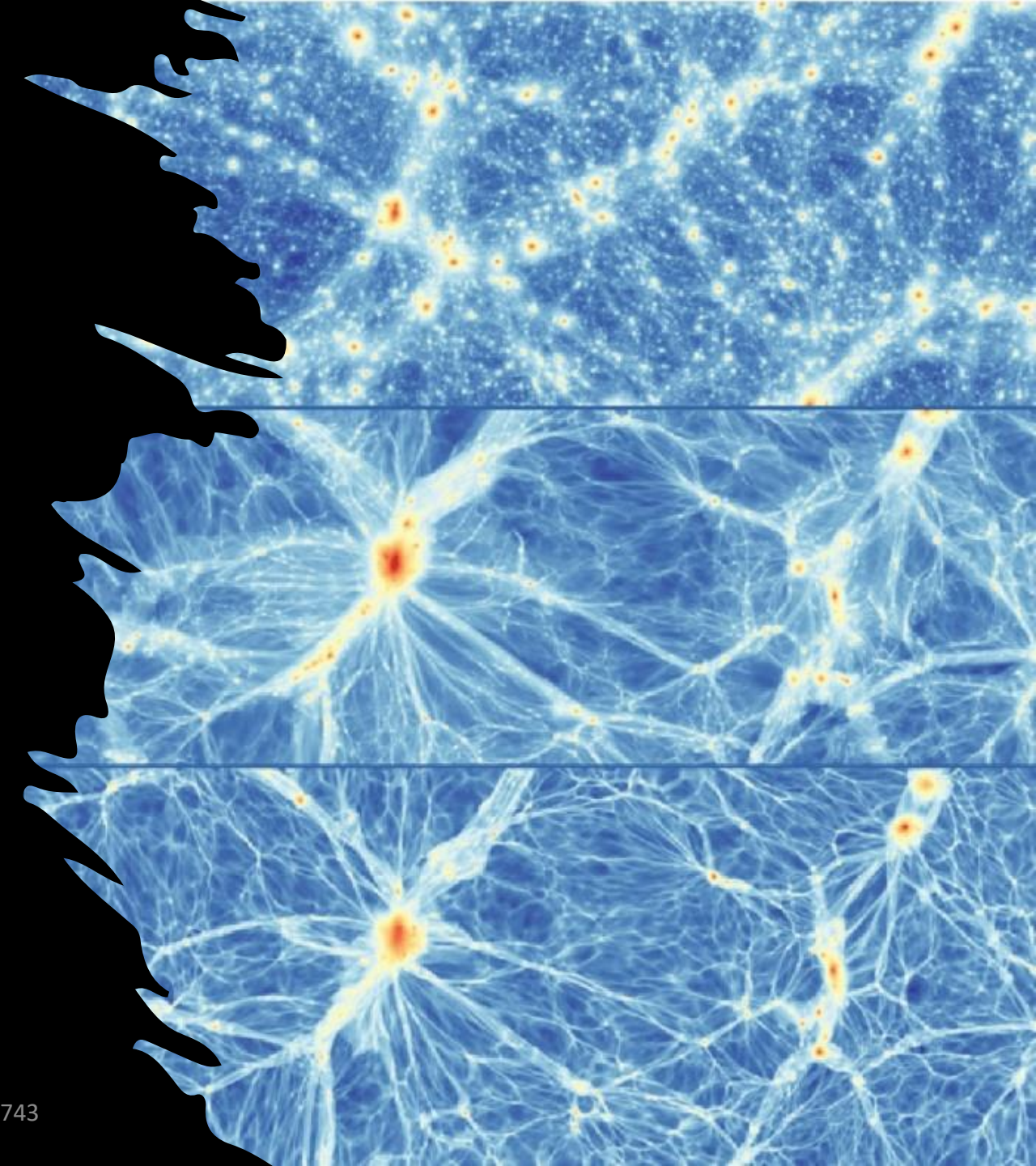


Simulation + Halo finder

- evolution relativistic simulation ([Adamek et al.](#)) – Dark Matter only N-body
- Box size = 50 Mpc/h
- #grids = 600^3
- #particles = 600^3

- Halo finder : Rockstar (Behroozi et al.) – grid independent and shape independent

- Fixed mesh grid: Reliable halo mass range is $10.5 \leq \log \left(\frac{M}{M_{sun}} \right) \leq 14$

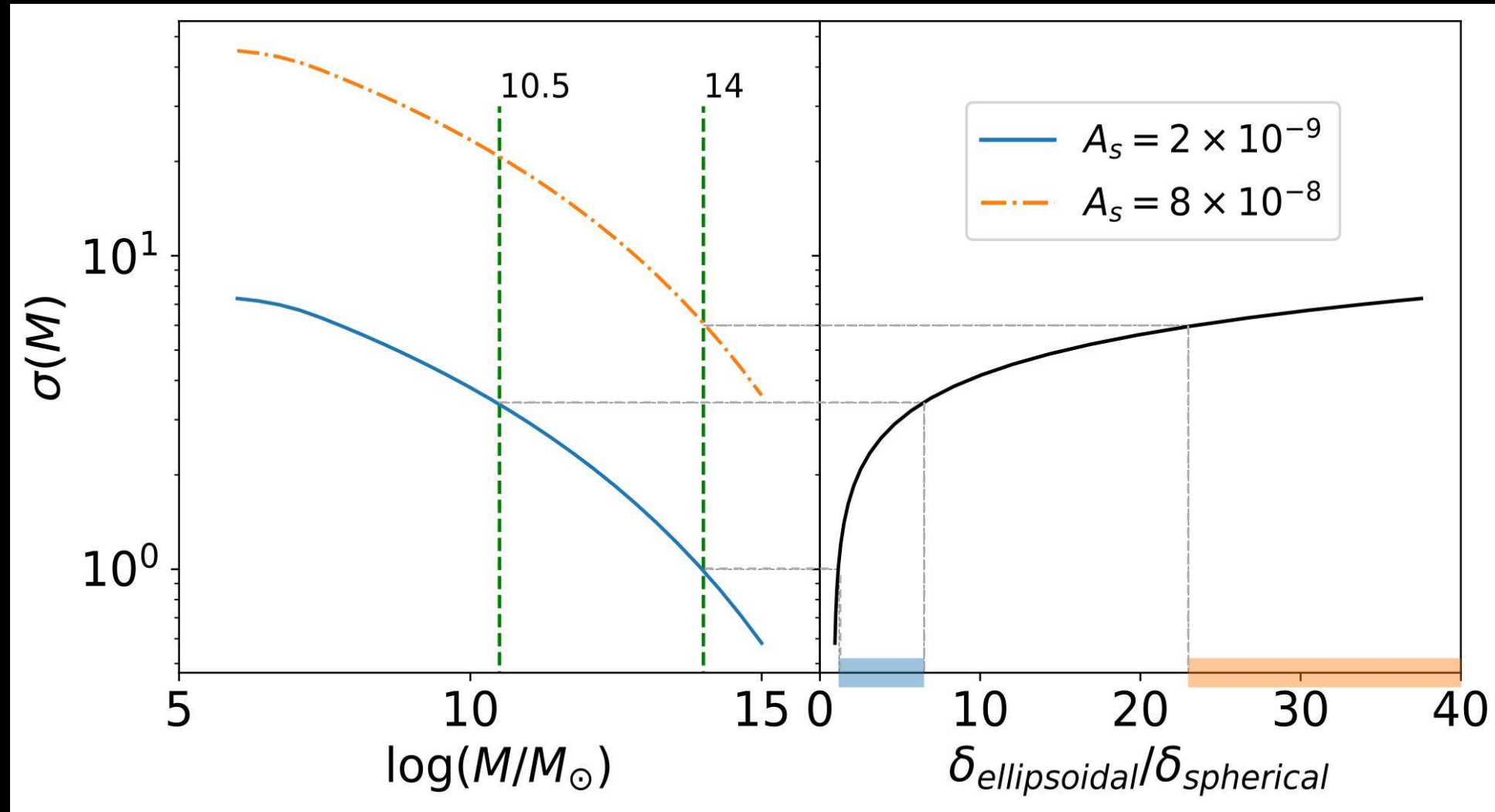


How to analyze the effects in the smaller mass scales?

- Effect of increasing the amplitude of initial curvature perturbations looks like moving to smaller mass scales in the standard cosmological model.

$$\sigma_M = \sigma_M(M_{halo}, A_S)$$

$$f \equiv \frac{\delta_{ellipsoidal}}{\delta_{spherical}} = f(\sigma_M)$$



Interpretable Deep Learning Frameworks \longrightarrow Learning the collapse process directly from N-Body sims

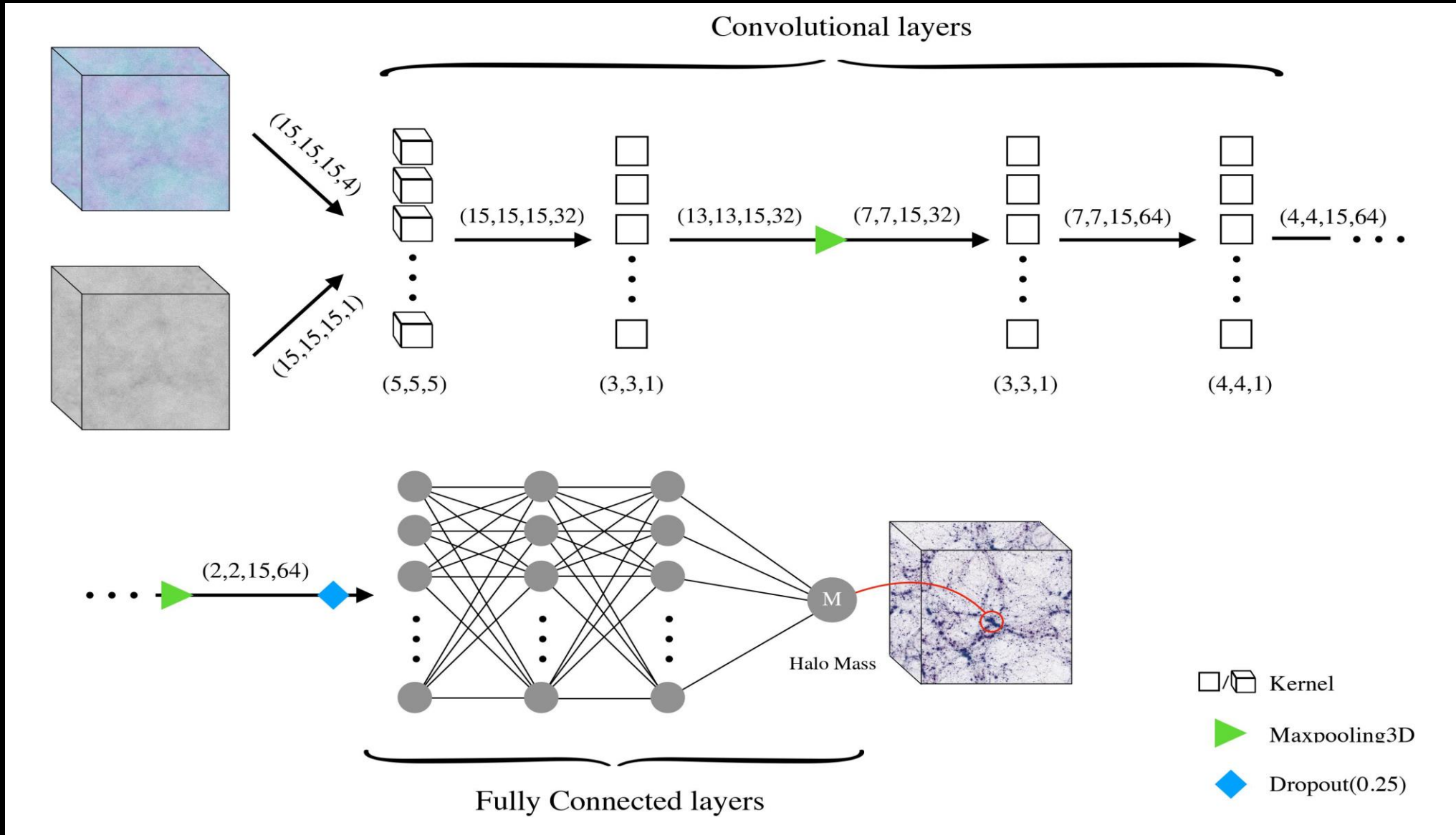
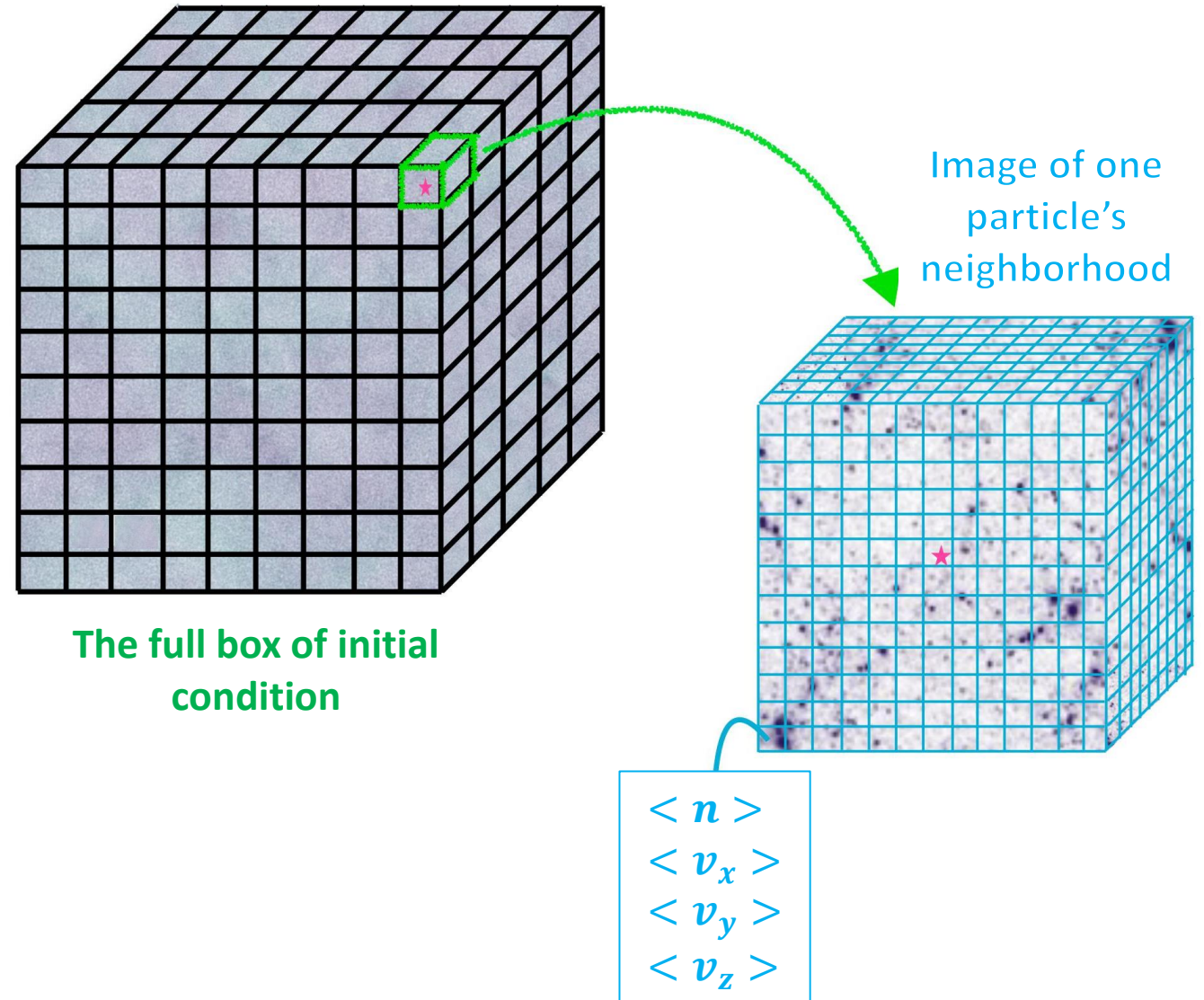
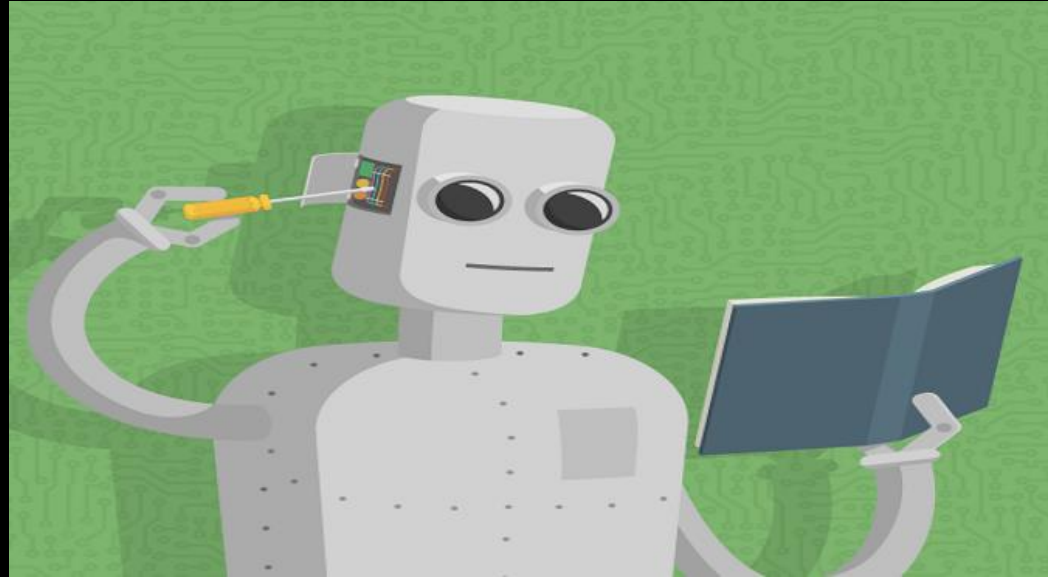


Image construction

- Physical size = 7.5 Mpc/h
- Physical resolution = 0.5 Mpc/h
- *Images shape* : $\begin{cases} (15,15,15,1) \\ \text{or} \\ (15,15,15,4) \end{cases}$





Things are not that simple!

Tunning hyper-parameters

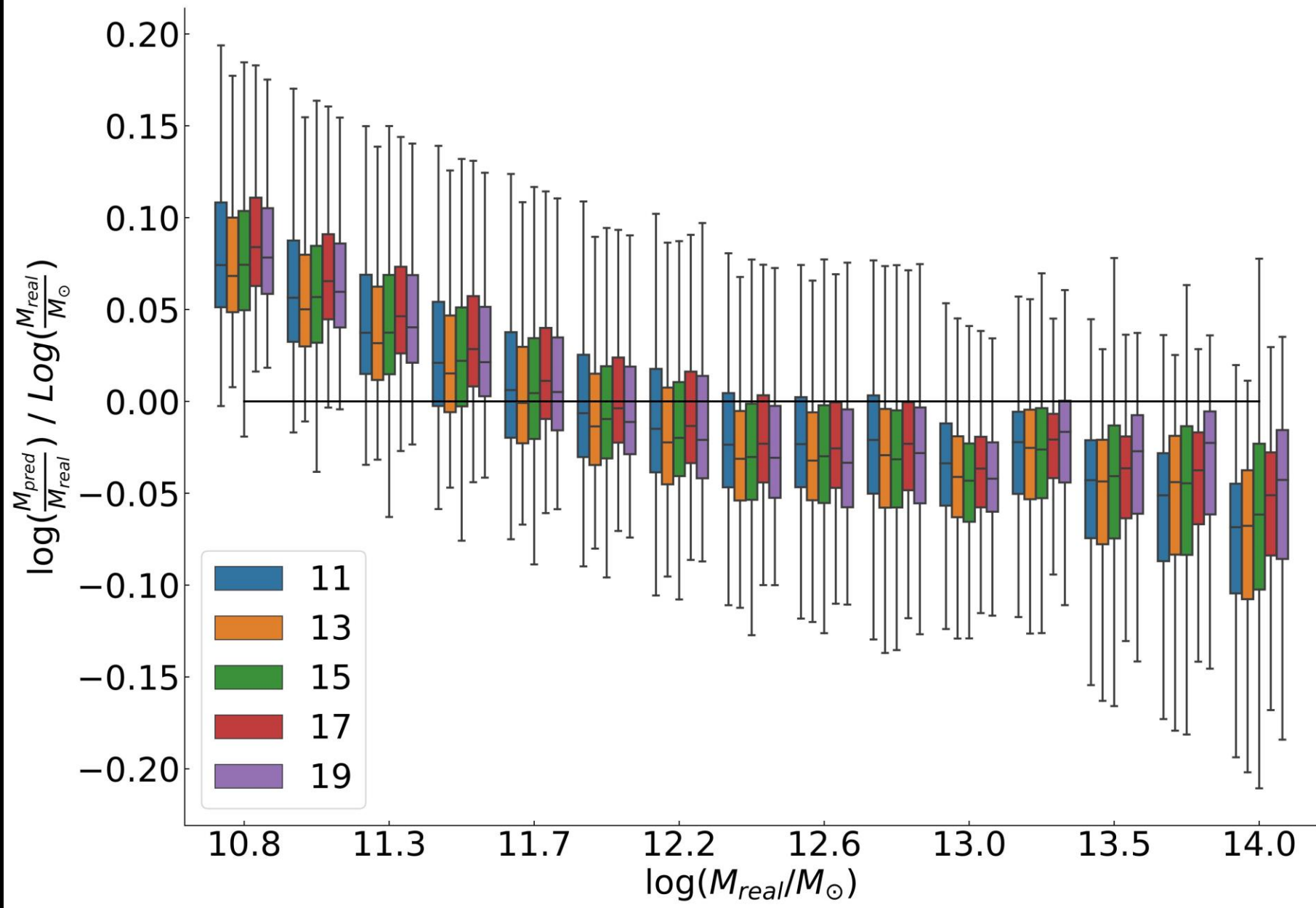


Image size

Image resolution

Minimum Halo Mass

Tunning hyper-parameters

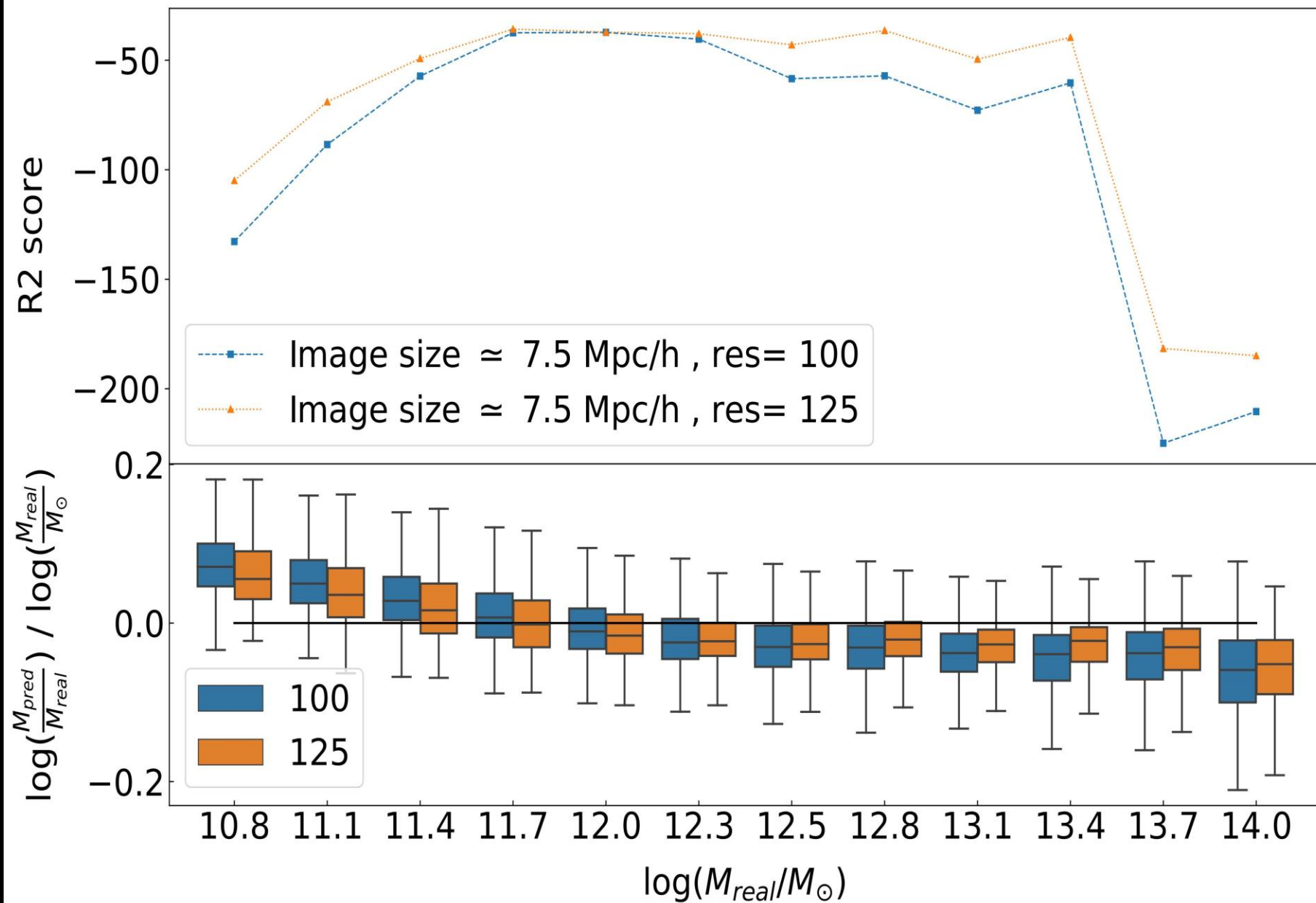


Image size

Image resolution

Minimum Halo Mass

Tunning hyper-parameters

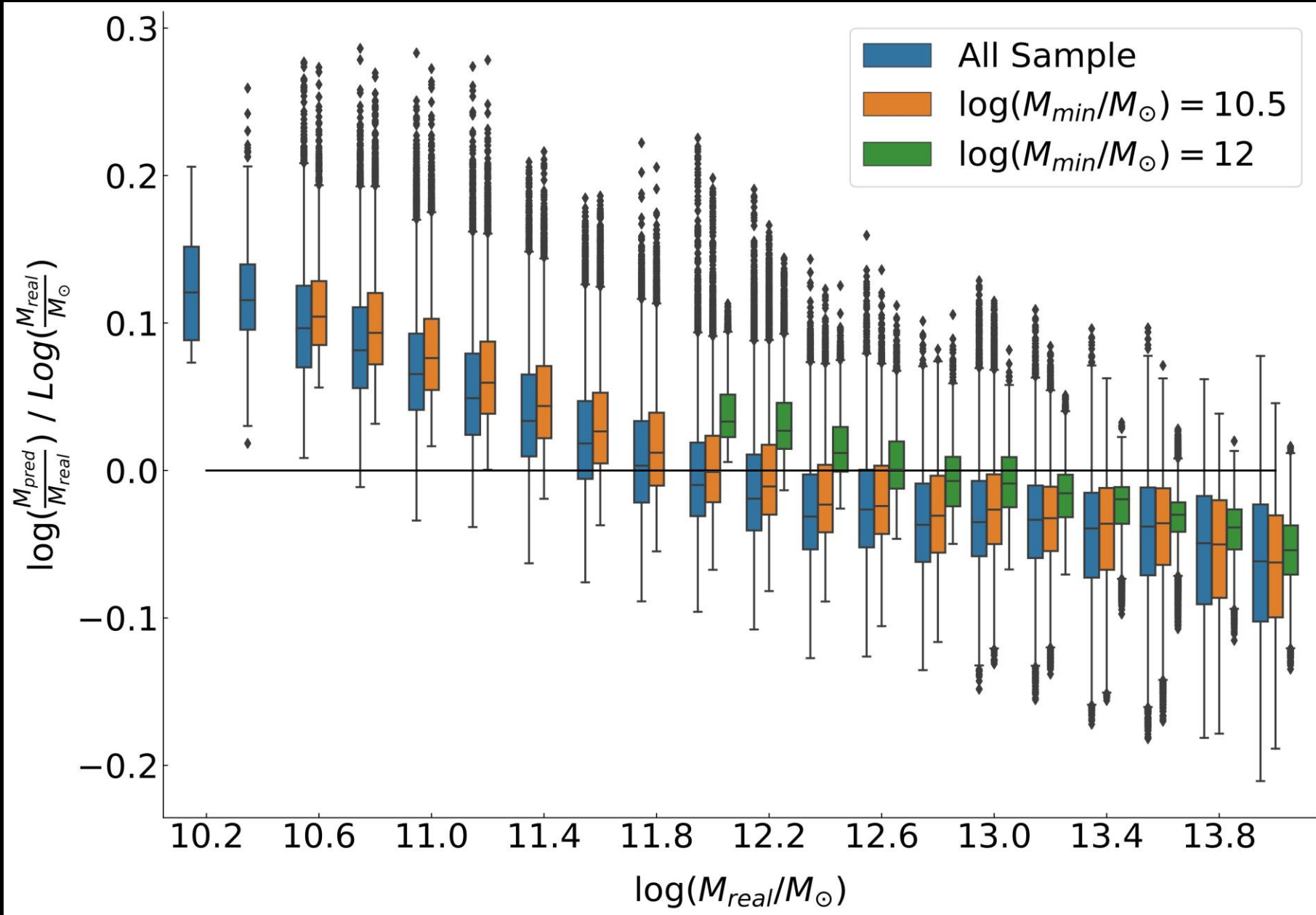
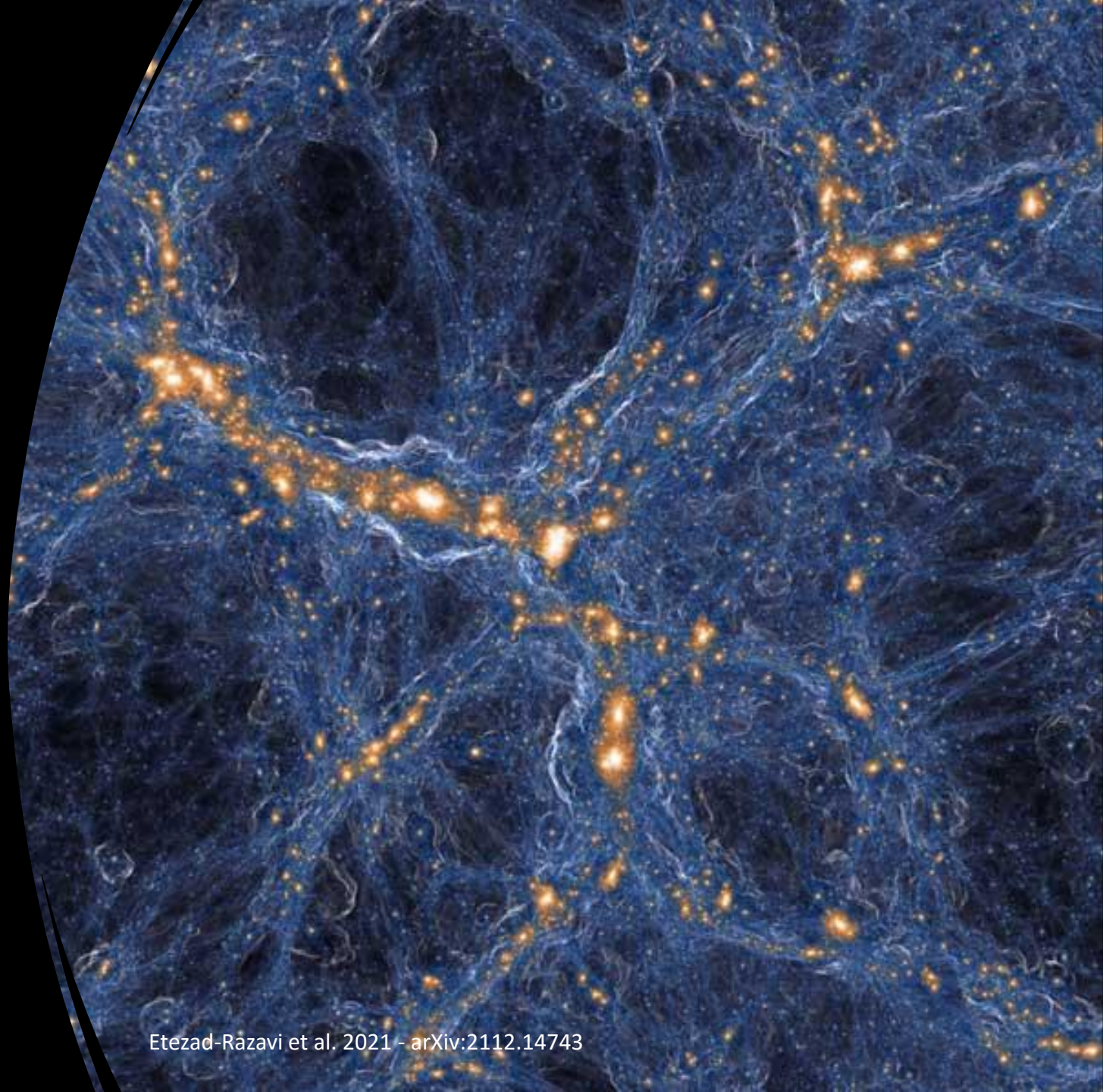


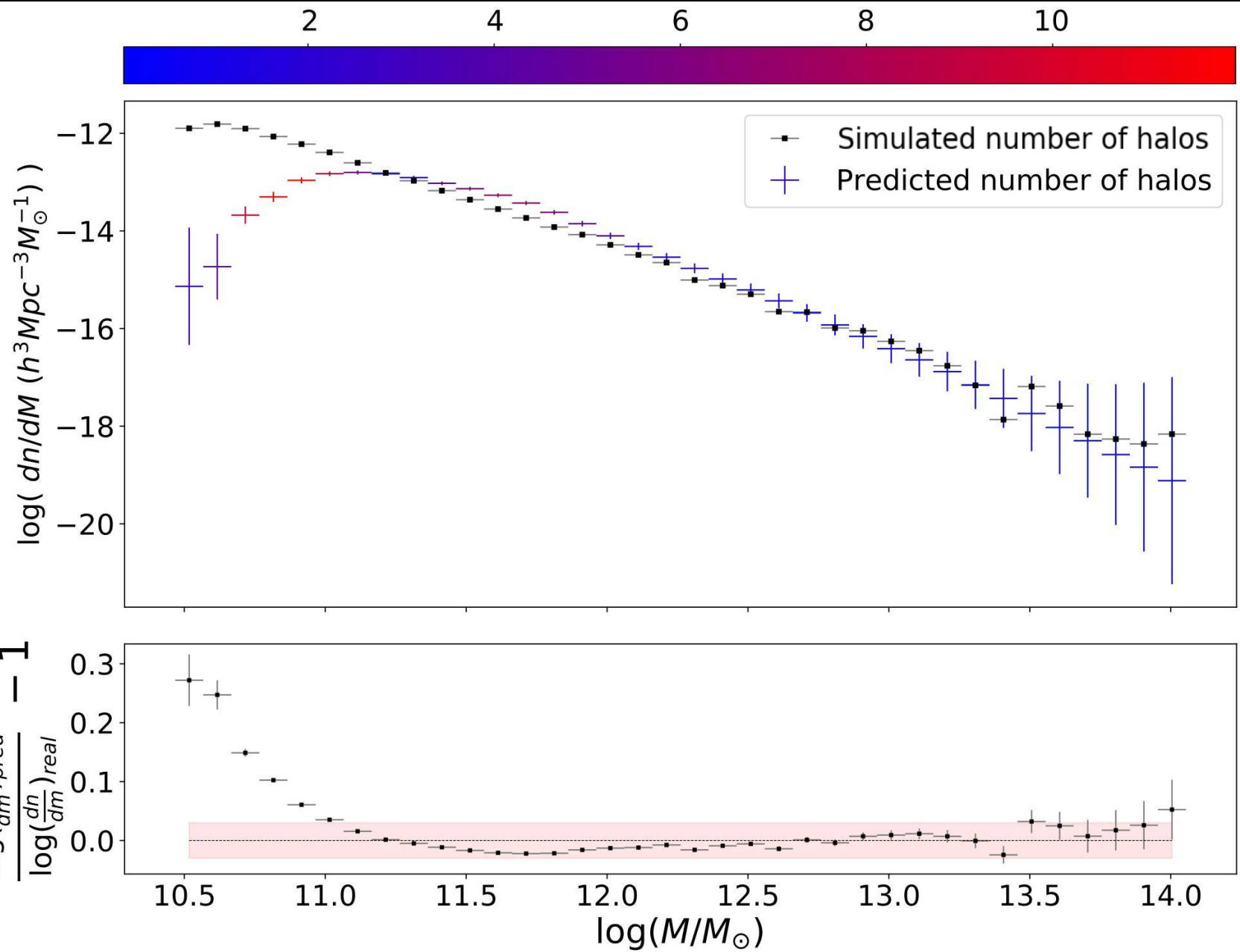
Image size

Image resolution

Minimum Halo Mass

Results



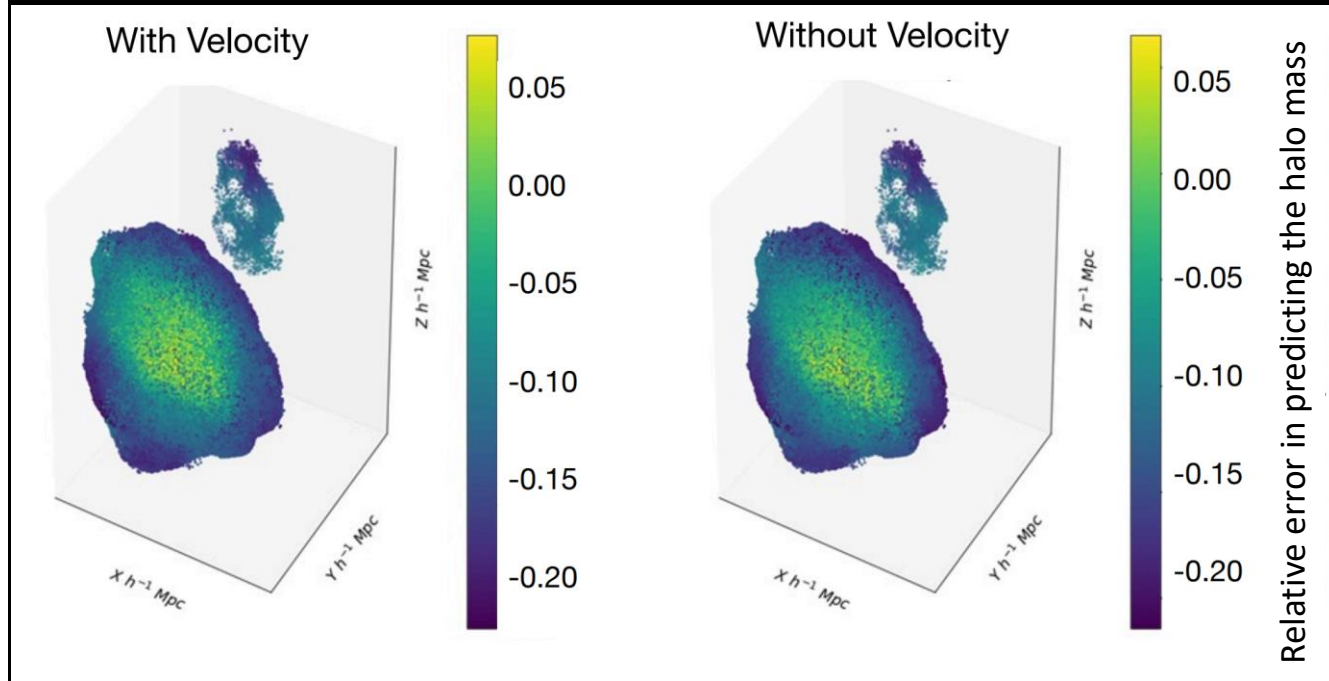
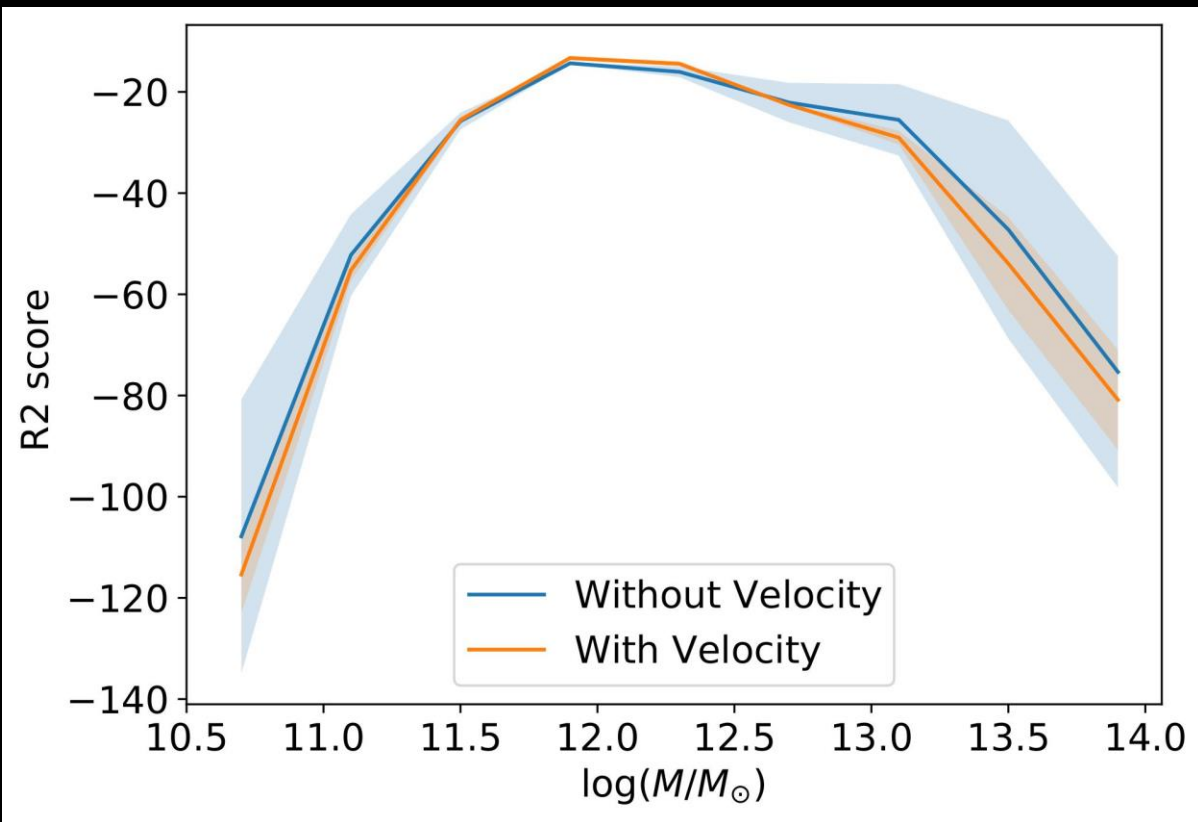


Halo Mass Function Prediction

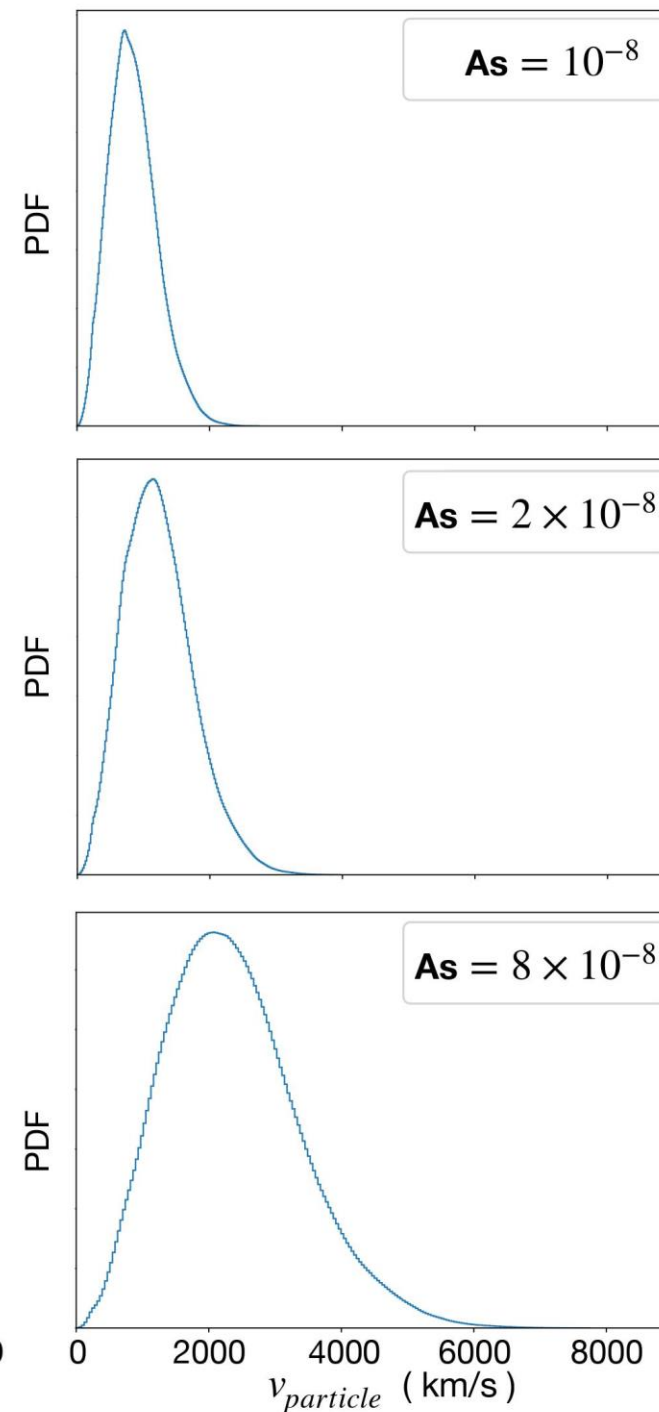
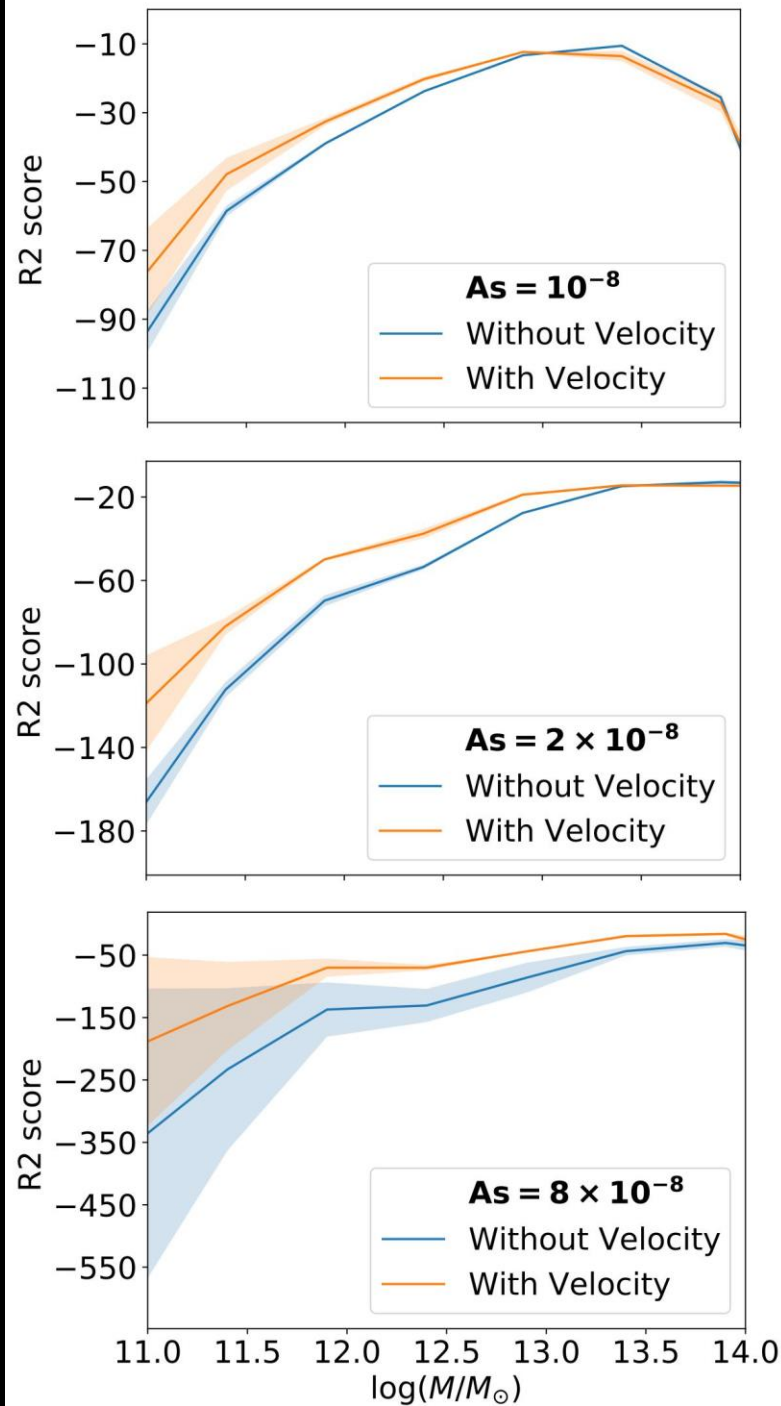
Standard Model of Cosmology

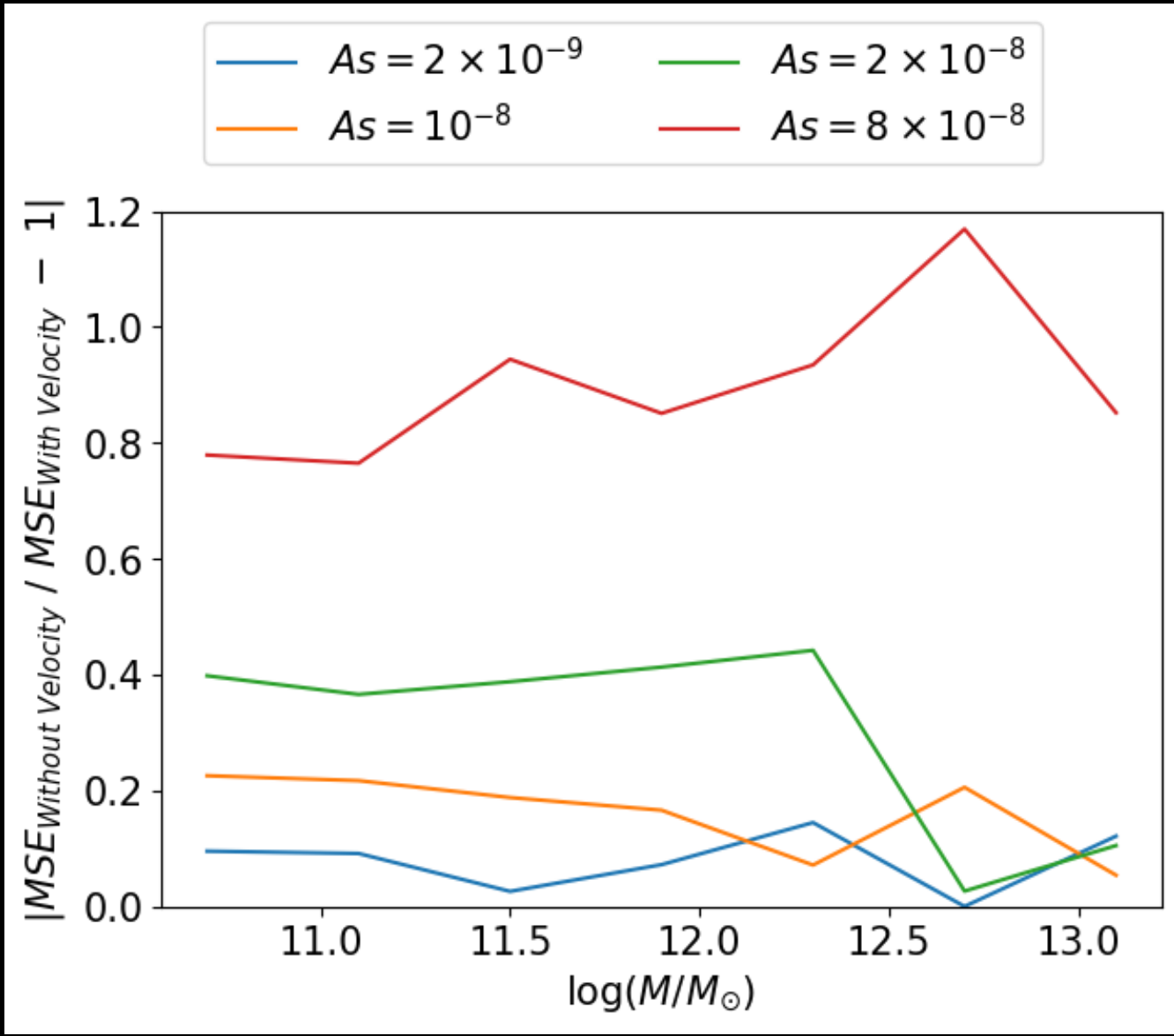
$$A_s = 2 \times 10^{-9}, \quad 10.5 \leq \log\left(\frac{M}{M_{sun}}\right) \leq 14$$

Adding velocity field information does not improve the performance of the model.

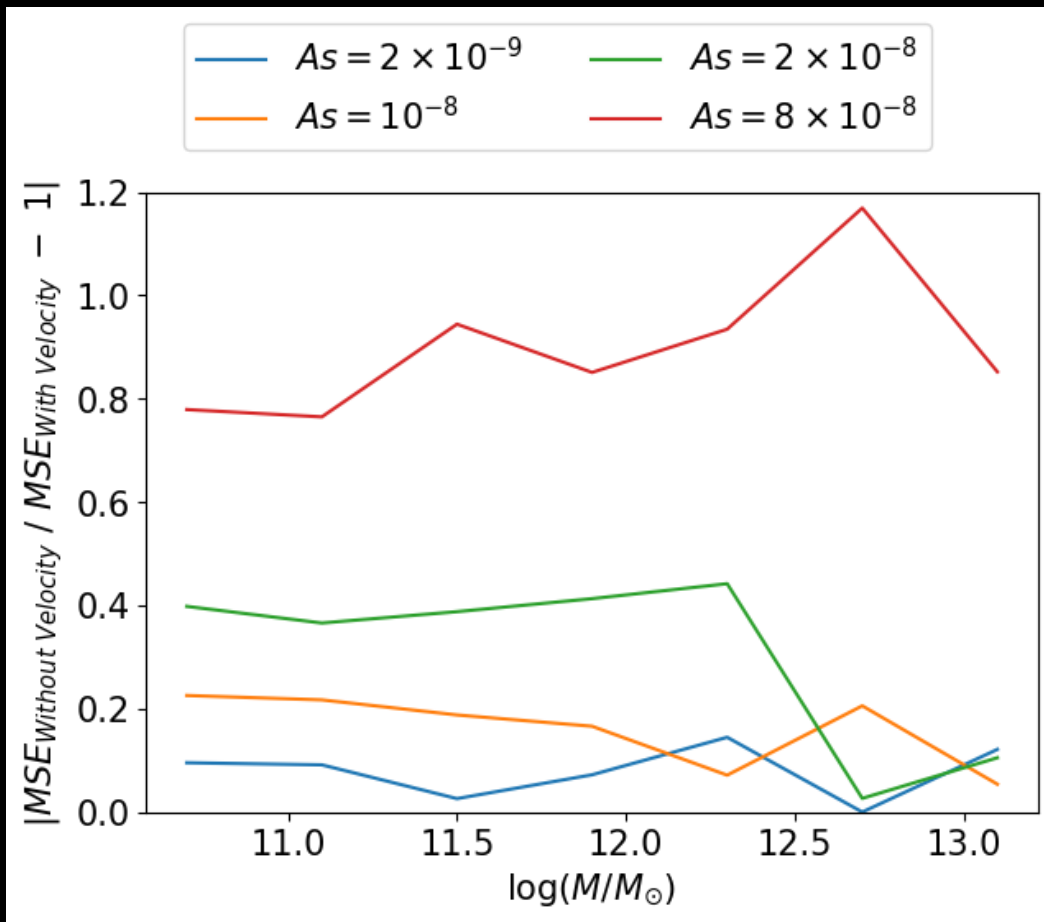


Effect of the velocity field information while increasing A_s

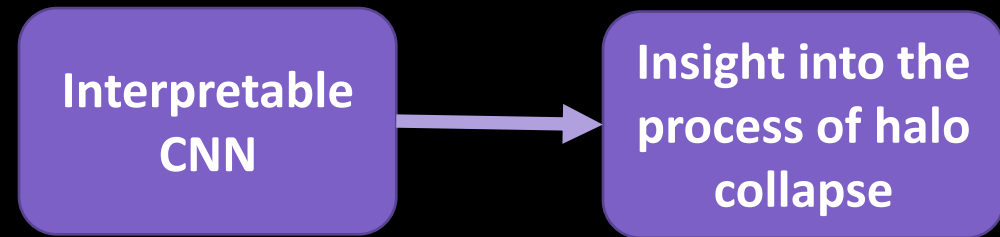




Model without velocity field information seems to fail to predict the Dark Matter halo mass for larger A_s values



Conclusion and future remarks



for Λ CDM with $A_s = 2 \times 10^{-9}$
 $10.5 \leq \log \frac{M}{M_\odot} \leq 14$

Adding initial velocity field info doesn't change the accuracy of HMF prediction.

for $A_s > 2 \times 10^{-9}$
 $10.5 \leq \log \frac{M}{M_\odot} \leq 14$

Neglecting initial velocity field info causes considerable inaccuracy compared to the model with velocity info.

Our result suggests that the effect of the velocity field on the halo formation is scale-dependent.

We can use this machinery to study structure formation in non-standard cosmologies.