

# Simulations and cascades: using INCL to boost nuclear models for neutrino interactions

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# Outlook

- 1 **Detection of neutrinos**
- 2  **$\nu$  - nucleus interaction simulation**
- 3 **Final state interactions (FSI) studies**
- 4 **Experimental observables sensitive to nuclear effects**
- 5 **Comparison to data**
- 6 **Production of nuclear clusters in neutrino interactions**

## $\nu$ energy reconstruction

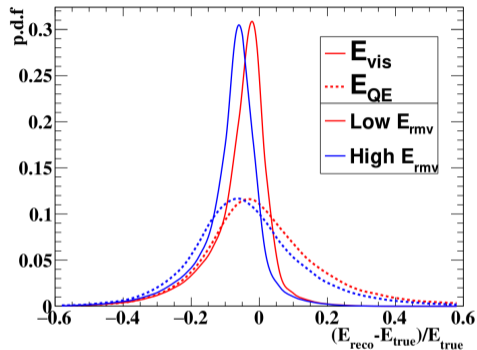
Energy reconstruction using only muon kinematics:

$$E_{\nu}^{QE} = \frac{m_p^2 - (m_n - E_B)^2 - m_{\mu}^2 + 2(m_n - E_B)E_{\mu}}{2((m_n - E_B) - E_{\mu} + p_{\mu} \cos \theta_{\mu})}$$

Energy reconstruction using **muon and kinetic energy of the nucleon**:

$$E_{\nu}^{vis} = E_{\mu} + T_N$$

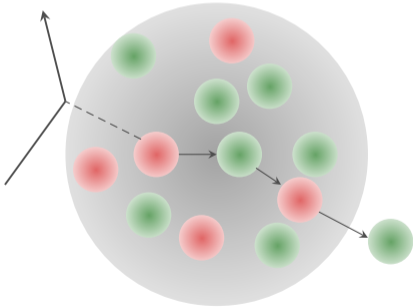
With ND280 upgrade, we can detect protons and neutrons at **low threshold** so we can measure the neutrino energy with the second formula which allows much **better resolution**, as shown in the figure.



$E_{\nu}^{vis}$ , dashed line — QE formula, solid line —  $\mu + N$  formula

# Importance of nuclear effects

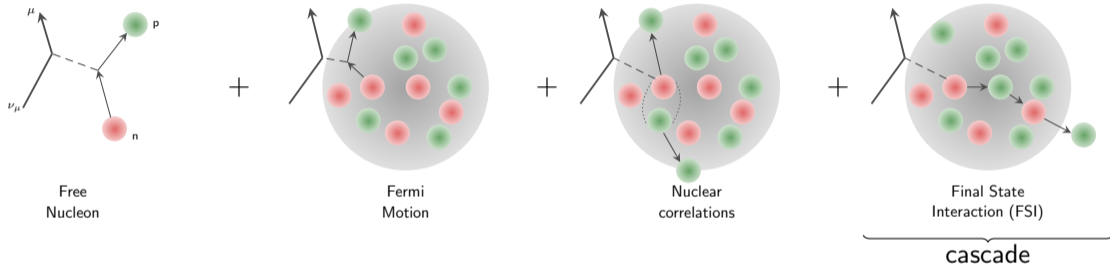
$\mu + N$  formula gives us more **opportunities**, but also it creates more **challenges** for modelling and we need to **understand better nuclear effects** also on neutrons and protons.



We need **not only** a better detector, but also better **modelling** of the neutrino-nucleus interactions, e.g. improved Monte-Carlo generators!



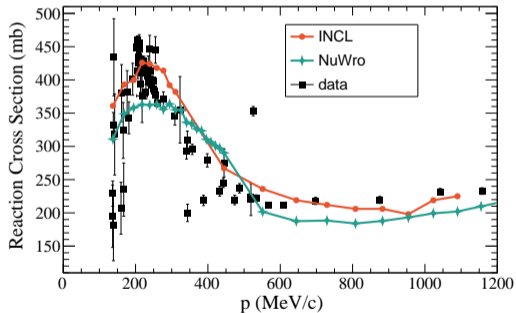
# Factorization scheme



We will focus on **cascades**.

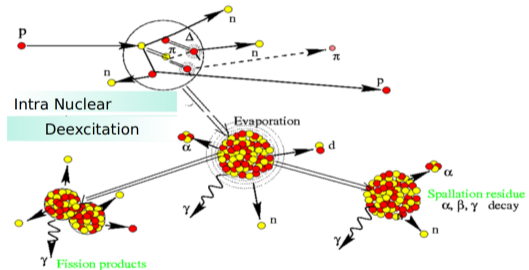
# Liège Intranuclear Cascade model

**Projectiles:** baryons (nucleons,  $\Lambda$ ,  $\Sigma$ ), mesons (pions and Kaons) or light nuclei ( $A \leq 18$ ). Shows a **remarkable agreement** with an exhaustive list of experimental data.



Example: proton-12 C interaction cross section as a function of the proton momentum

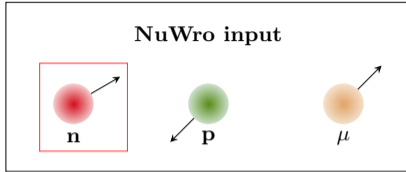
The INCL cascade is coupled to the **deexcitation codes**: ABLA, SMM or GEMINI++



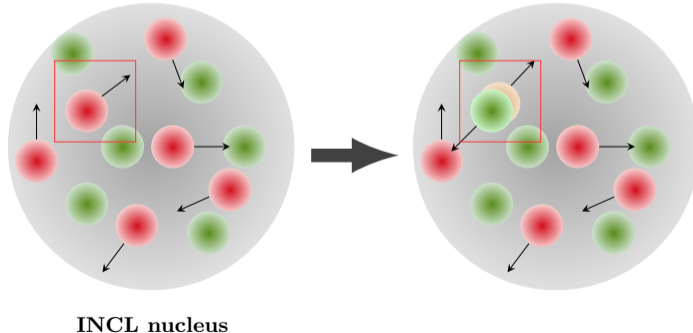
**Flexible tool** that has been implemented in GEANT4 and GENIE.

More information: [Phys.Rev.C 87, 014606 \(2013\)](#), [Phys.Rev.C 90, 054602 \(2014\)](#)

# Using INCL with NuWro input

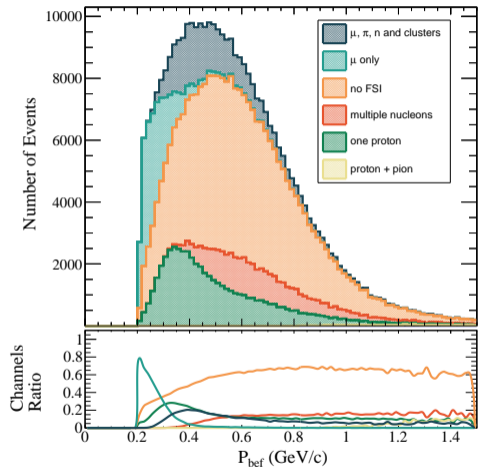


We substitute the chosen **INCL neutron** with **proton** and **muon** from NuWro. We use NuWro sample with **CCQE** events on **CH** target.

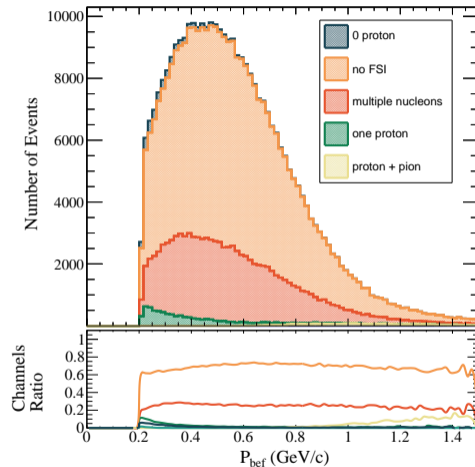


- 1 Detection of neutrinos
- 2  $\nu$  - nucleus interaction simulation
- 3 Final state interactions (FSI) studies**
- 4 Experimental observables sensitive to nuclear effects
- 5 Comparison to data
- 6 Production of nuclear clusters in neutrino interactions

# Proton momentum before FSI



INCL

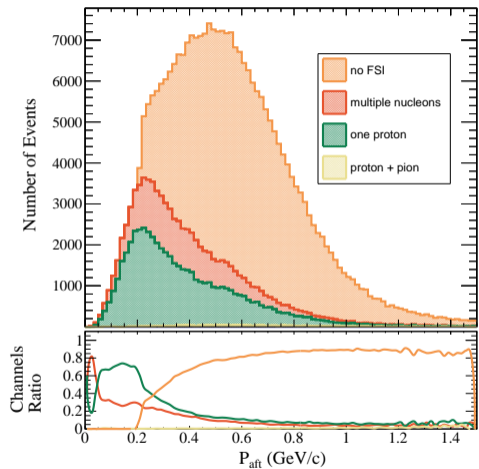


NuWro

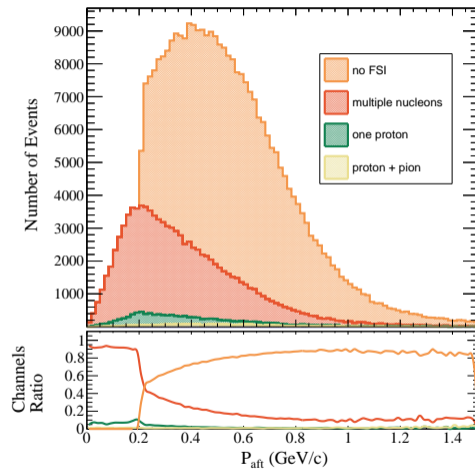
# Reaction channels

	Channel	NuWro SF	INCL+NuWro SF
	no protons	1.37%	19.47%
	protons	98.63%	80.53%
no proton	absorption	4.45%	39.49%
	neutron + $\pi$ production	3.40%	0.60%
	$\pi$ production	0.21%	0%
	neutron knock-out	91.4%	29.58%
	nuclear cluster knock-out	0%	30.33%
proton	1 proton, no FSI	70.38%	68.49%
	1 proton only with FSI	2.45%	19.21%
	1p + other nucleons or nuclear clusters	26.21%	11.68%
	1p + $\pi$ production	0.96%	0.62%

# Proton momentum after FSI



INCL



NuWro

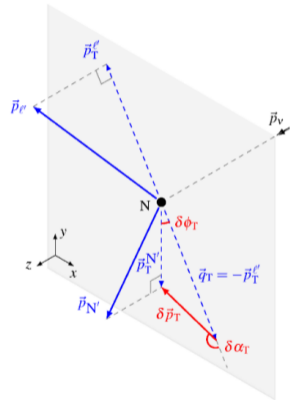
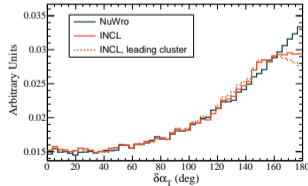
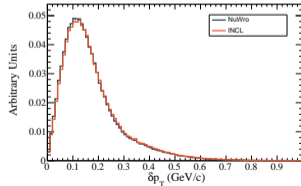
# Variables of interest

FSI affects proton's kinematics that gives systematics in  $\nu$  energy reconstruction.  
 We use **Single Transverse Variables (STV)** for better FSI estimation.

sensitive to FSI: 
$$\delta\alpha_T = \arccos \frac{-\vec{k}'_T \cdot \delta\vec{p}'_T}{k'_T \cdot \delta p'_T}$$

sensitive to FM: 
$$\delta\vec{p}'_T = \vec{p}'_T + \vec{p}'_{\mu} = \vec{p}'_{\tilde{\nu}}$$

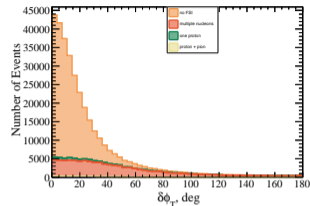
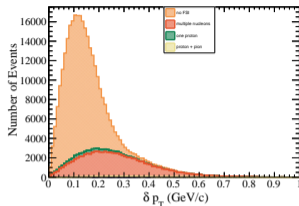
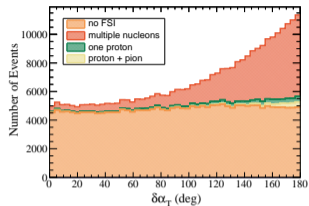
additional variable: 
$$\delta\phi_T = \arccos \frac{\vec{k}'_T \cdot (\vec{p}'_p)_T}{k'_T \cdot (p'_p)_T}$$



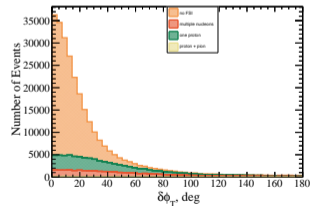
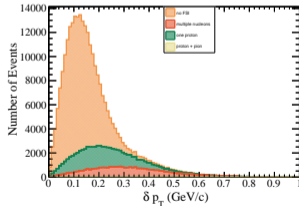
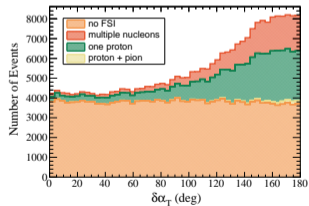
Phys. Rev. C, 94(1), 2016



# Single Transverse Variables (STV)



NuWro



INCL

# Comparison to T2K data

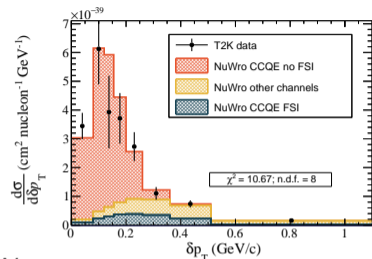
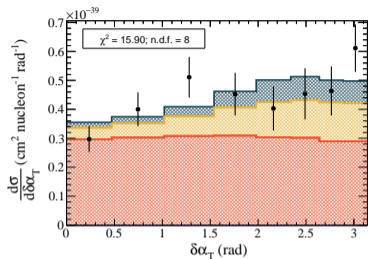
## Cuts:

$$p_\mu > 250$$

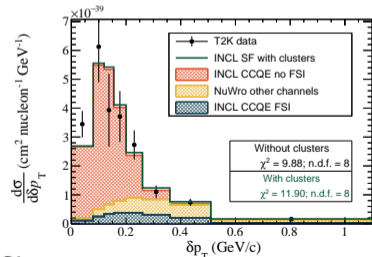
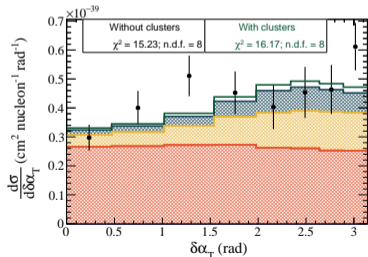
$$450 < p_p < 1000$$

$$\cos(\Theta_\mu) > -0.6$$

$$\cos(\Theta_p) > 0.4$$



NuWro



INCL

# Comparison to MINERvA data

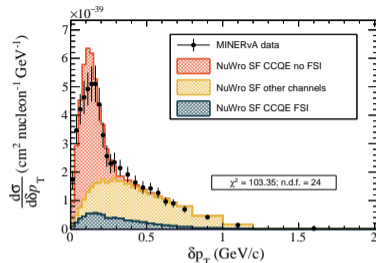
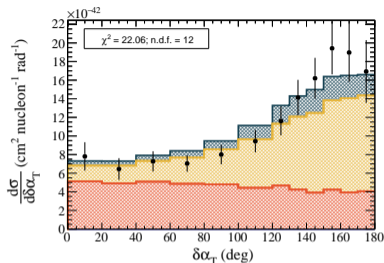
## Cuts:

$$1500 < p_\mu < 10000$$

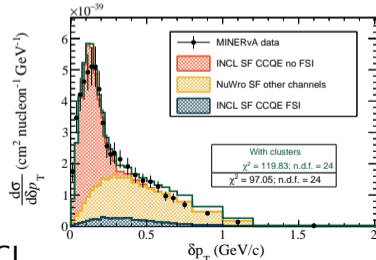
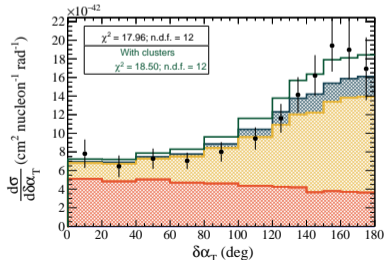
$$450 < p_p < 1200$$

$$\Theta_\mu < 20$$

$$\Theta_p < 70$$

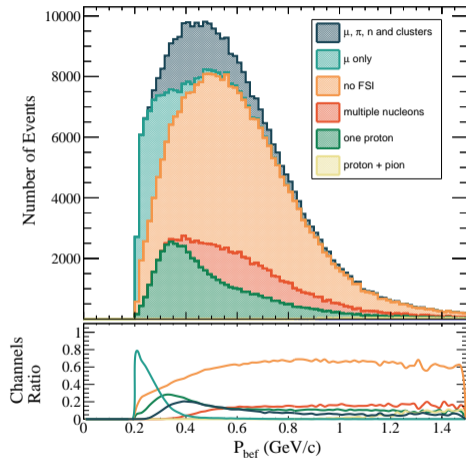


NuWro



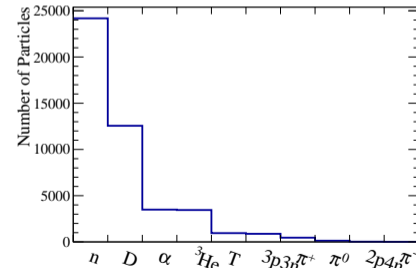
INCL

# What is produced in 0 proton events



proton momentum before FSI

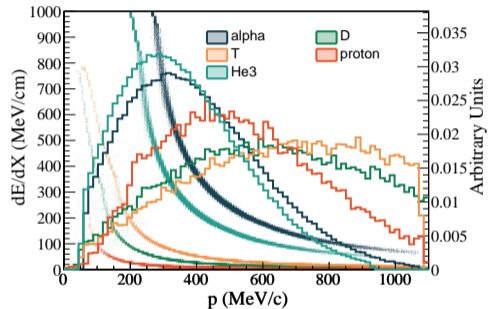
- can we **misidentify** nuclear clusters as protons?
- **how far** nuclear clusters can travel? Do we see them as a **track** or **vertex activity**?
- can we **see** their energy **deposited** in the detector?



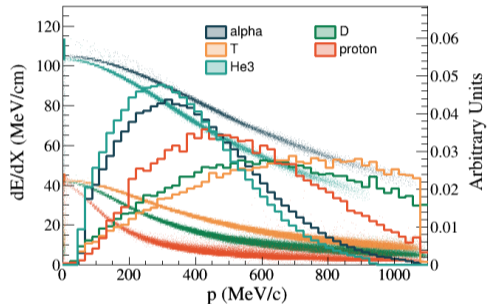
particles produced in 0 proton events

# Geant4 simulation

We have created a **Geant4 simulation** of the **uniform CH block**.

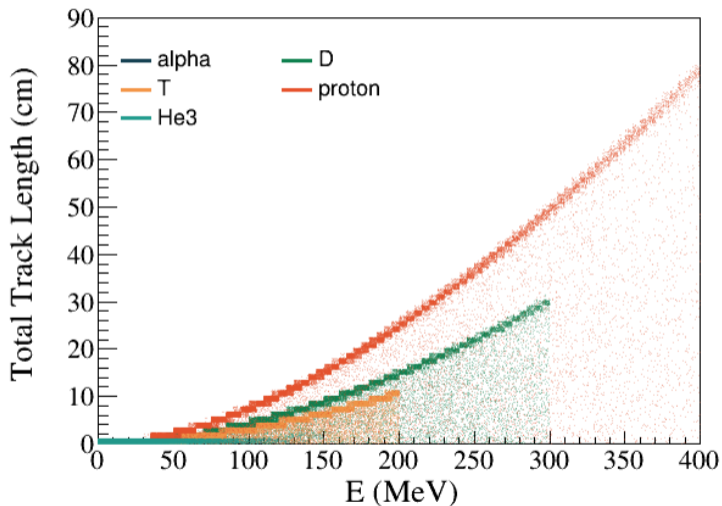


energy loss by ionization



visible energy loss by ionization (with Birks correction)

# Total path length dependence on kinetic energy



# Nuclear clusters reconstruction and identification

How often do nuclear clusters travel enough to be reconstructed as a track?

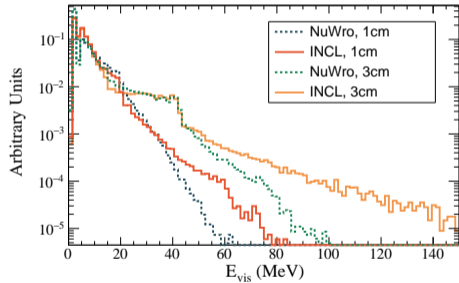
	$\alpha$	${}^3\text{He}$	T	D	proton
Travels more than 1 cm, %	0.3	1.3	60	72	87
Travels more than 3 cm, %	0	0	34	51	74

Can we **identify** nuclear clusters?

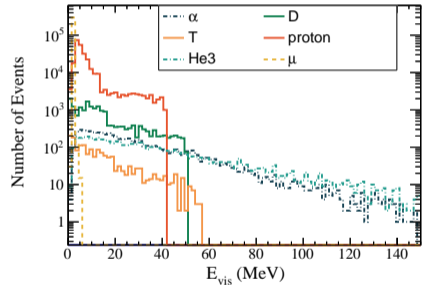
	$\alpha$	${}^3\text{He}$	D	T	proton	total misidentification
$\alpha$	-	0	0	0	0	0
${}^3\text{He}$	0	-	0	0	0	0
D	0	0	-	0	18%	18%
T	0	0	5%	-	6%	11%
proton	0	0	0	0	-	0

# Vertex activity

The distributions have two components depending if the particles leave the sphere or if they release all their energy inside the sphere.



total vertex activity



INCL 3 cm, vertex activity per particle



# Summary

- We have compared the simulation of the final-state interactions between the **NuWro** and **INCL** cascade models in CCQE events
- Differences in the FSI models:
  - INCL FSI simulation features a significant fraction of events **without a proton** in the final state, especially low momentum protons region
  - INCL tends to **re-absorb** other particles produced during the cascade
  - An essential novelty of this study is the **simulation of nuclear cluster production** by INCL in FSI of neutrino interactions

# Conclusion and prospects

Present detector acceptance **does not give access** to the most important for FSI characterization **low momentum protons**. **New detectors** with lower thresholds will **need reliable nuclear models** of FSI to confront the new data.

## Future prospects:

- We want to repeat the same study for the **antineutrinos**: the leading particle will be **neutron** and its modelling is crucial for the upgrade
- **Pion FSI**: INCL models  $\Delta$  resonance decay
- We want to continue the study of the detector response **of clusters**



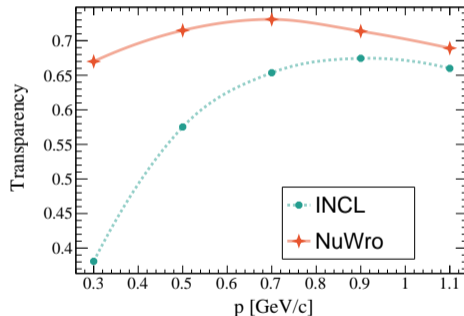
The paper [arXiv:2202.10402](https://arxiv.org/abs/2202.10402) has been submitted to the Phys. Rev. D

# BACKUP

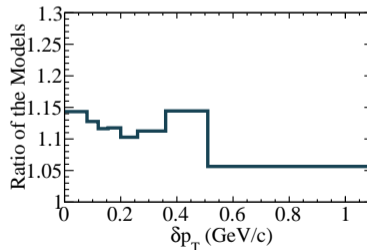
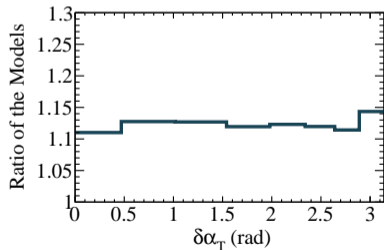
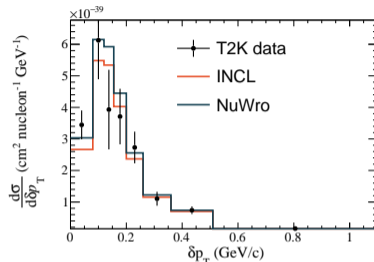
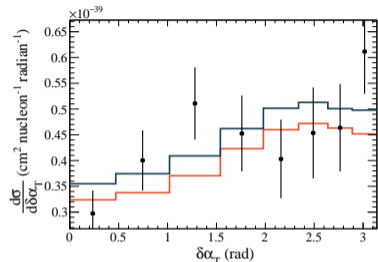
# Transparency

The **larger FSI strength** in INCL suggests a **larger dissipation of energy** across the nucleus through interactions.

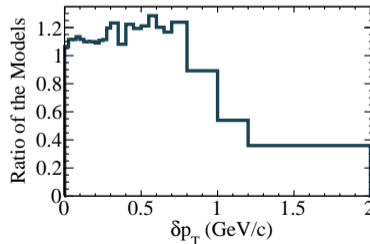
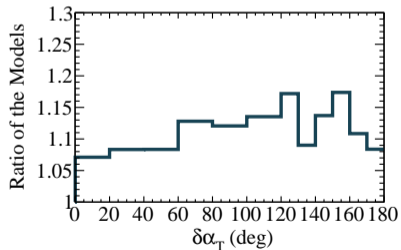
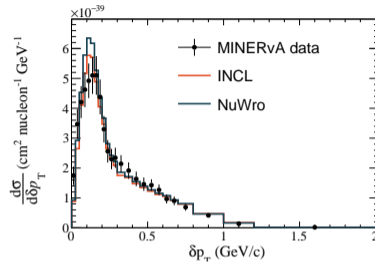
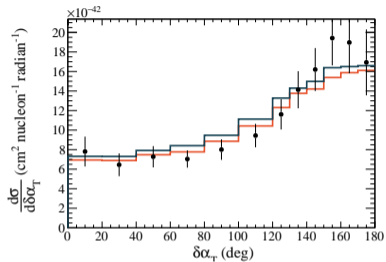
The nuclear model of INCL includes the probability to **form nuclear clusters** during the attempt of the nucleon to leave the nucleus. The events with no proton in the final state are in the large majority due to **charge exchange in NuWro** (91% of neutron production) while in INCL the probability of **nuclear cluster and neutron production** in events without protons in the final state is similar (around 30% each).



# Comparison to T2K data

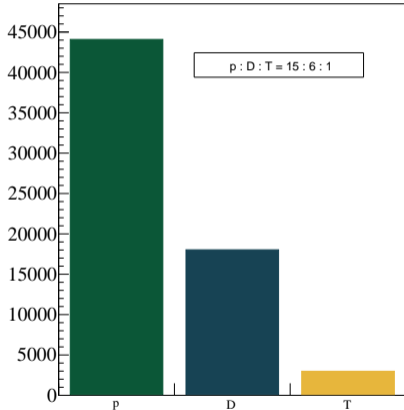


# Comparison to MINERvA data



# Nuclear clusters emission check

$^{12}\text{C}$  bombarded by 175 MeV neutrons



Progress in NUCLEAR SCIENCE and TECHNOLOGY, Vol. 1, p.69-72 (2011)

## ARTICLE

### Production of protons, deuterons, and tritons from carbon bombarded by 175 MeV quasi mono-energetic neutrons

Shusuke HIRAYAMA<sup>1\*</sup>, Yukinobu WATANABE<sup>1</sup>, Masateru HAYASHI<sup>1</sup>, Yuuki NAITO<sup>1</sup>, Takehito WATANABE<sup>1,5</sup>  
Riccardo BEVILACQUA<sup>2</sup>, Jan BLOMGREN<sup>2</sup>, Leif NILSSON<sup>2</sup>, Angelica ÖHRN<sup>2</sup>,  
Michael ÖSTERLUND<sup>2</sup>, Stephan POMP<sup>2</sup>, Alexander PROKOFIEV<sup>3</sup>, Vasily SIMUTKIN<sup>2</sup>,  
Pär-Anders SÖDERSTRÖM<sup>2</sup> and Udomrat TIPPAWAN<sup>4</sup>

<sup>1</sup>Department of Advanced Energy Engineering Science, Kyushu University, Kasuga, Fukuoka, 816-8580, Japan

<sup>2</sup>Department of Physics and Astronomy, Uppsala University, Box 516, SE-751 20 Uppsala, Sweden

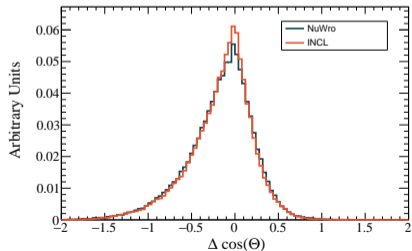
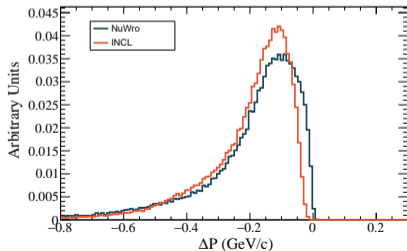
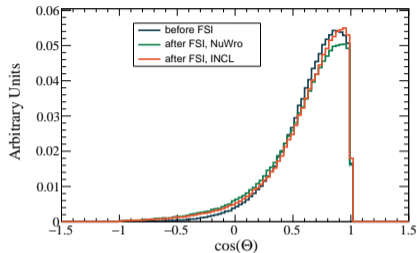
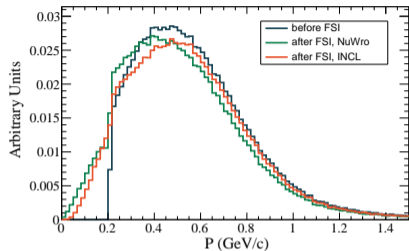
<sup>3</sup>The Svedberg Laboratory, Uppsala University, Box 533, SE-751 21 Uppsala, Sweden

<sup>4</sup>Fast Neutron Research Facility, Chiang Mai University, P.O.Box 217, Chiang Mai 50200, Thailand

<sup>5</sup>Los Alamos National Laboratory, Los Alamos, NM 87545, USA

Ratio  $\approx 10 : 3 : 1$

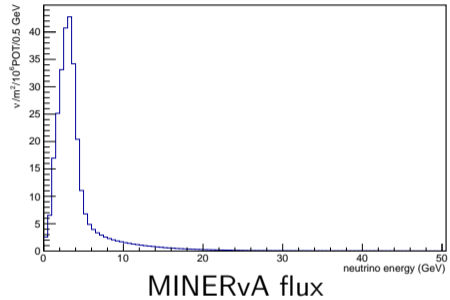
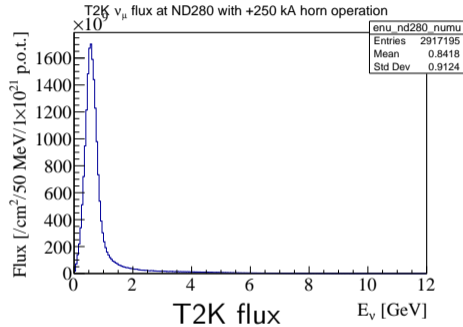
# Momentum and $\cos(\Theta)$ shape comparison





# Comparison to data

Normalization, as "other channels" part are always taken from NuWro.



- $p_\mu > 250$
- $450 < p_p < 1000$
- $\cos(\Theta_\mu) > -0.6$
- $\cos(\Theta_p) > 0.4$
- $1500 < p_\mu < 10000$
- $450 < p_p < 1200$
- $\Theta_\mu < 20$
- $\Theta_p < 70$

# Geant4 model

## Physics list

- G4EmStandardPhysics and G4EmExtraPhysics
- G4HadronPhysicsINCLXX
- G4DecayPhysics
- G4IonINCLXXPhysics

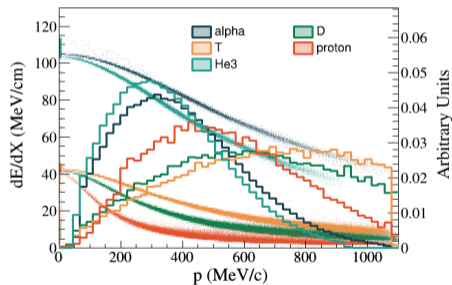
## Detector construction

- World volume 1000x1000x1550 cm **halfsize**
- beginning of coordinates is in the **center** of the world volume
- **uniform** CH block 50 cm **less** in all dimensions
- CH density =  $1.06 \text{ g/cm}^3$

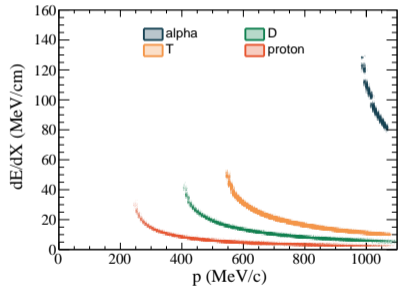
# Particle identification algorithm

We want to estimate the fraction of nuclear clusters that can be misidentified

**1st step:** The track is summed into 1 cm blocks corresponding to the detector granularity. The last part of the track that is shorter than 1 cm is not used in the analysis

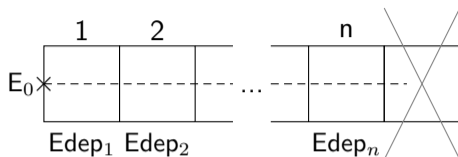


$dE/dX$  for step



$dE/dX$  for 1 cm cubes

# Particle identification algorithm

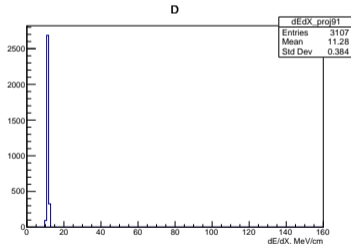


- **initial kinetic energy** is reconstructed as a sum of energy deposits along the whole track ( $E_0 = \sum_{i=1}^n Edep_i + Edep_{last}$ )
- **energy of the particle after passing 1 cm** in the material is  $E_1 = E_0 - Edep_1$ ;  
**momentum:**  $p_1^j = \sqrt{(E_1 + m^j)^2 - m^{j2}}$ , where  $j = \{\alpha, D, T, p\}$
- **for each momentum hypothesis**, the  $\frac{dE}{dX}_i$  is reconstructed using the  $\frac{dE}{dX}$  from the previous slide with uncertainty  $\sigma$
- $\chi^2 = \sum_{i=1}^n \frac{(Edep_i - \frac{dE}{dX}_i)^2}{\sigma_i^2}$  is calculated for each hypothesis
- we choose hypothesis with the **lowest**  $\chi^2$

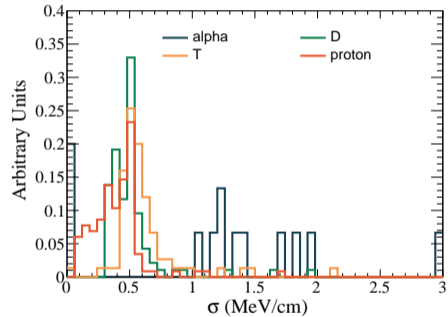
# $\sigma$ definition

To calculate  $\sigma$ , we need:

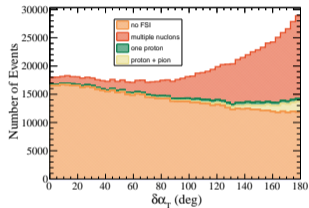
- take plot with  $dE/dX$  dependence on momentum
- find bin with the needed momentum
- to make a projection to  $dE/dX$  axis of this bin



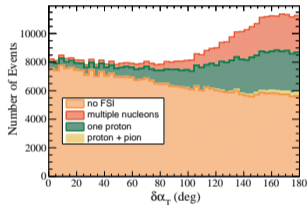
$\sigma$  is RMS of this plot



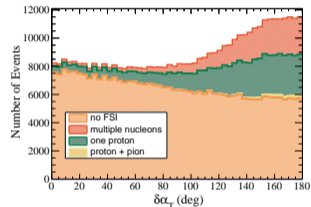
# Comparison to data: RW model



NuWro GFG



INCL RW



INCL + NuWro GFG