



Precise measurement of neutrino solar oscillation parameters  $\theta_{12}$  and  $\Delta m_{21}^2$  with the JUNO experiment

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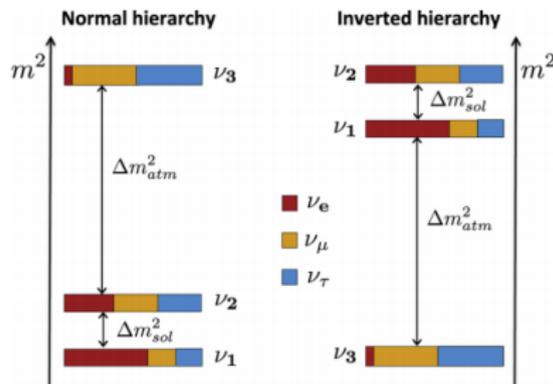
March 8th 2022

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# Mixing of neutrinos

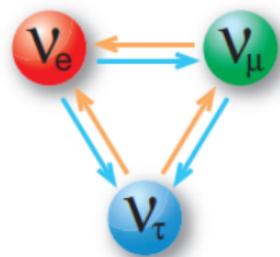
- The mass eigenstates  $|\nu_{1,2,3}\rangle$  are linear combinations of flavor eigenstates  $|\nu_{e,\mu,\tau}\rangle$
- Mixing of neutrinos with 3 masses  $m_1, m_2, m_3$ , 3 angles  $\theta_{12}, \theta_{13}$  and  $\theta_{23}$  and a phase  $\delta$  accounting for  $CP$  violation



$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{13}s_{23}e^{i\delta} & c_{12}c_{23} - s_{12}s_{13}s_{23}e^{i\delta} & c_{13}s_{23} \\ s_{12}s_{23} - c_{12}s_{13}c_{23}e^{i\delta} & -c_{12}s_{23} - s_{12}s_{13}c_{23}e^{i\delta} & c_{13}c_{23} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

With  $c_{ij} \equiv \cos \theta_{ij}$  and  $s_{ij} \equiv \sin \theta_{ij}$

# Oscillation of neutrinos



- Since the flavor eigenstates are linear combinations of mass eigenstates, there are oscillations :

- We study the example of reactor  $\bar{\nu}_e$  with their survival probability :

$$P^{2\nu}(\bar{\nu}_e \rightarrow \bar{\nu}_e) = 1 - \sin^2 2\theta_{12} \sin^2 \Delta_{21}$$

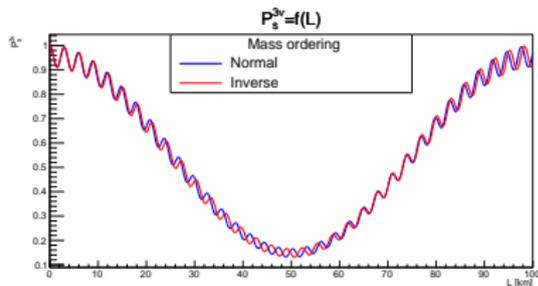
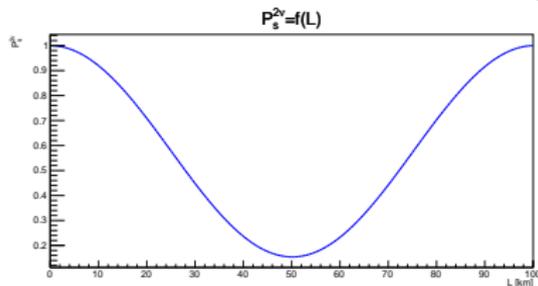
$$P^{3\nu}(\bar{\nu}_e \rightarrow \bar{\nu}_e) = 1 - \sin^2 2\theta_{13} (\cos^2 \theta_{12} \sin^2 \Delta_{31} + \sin^2 \theta_{12} \sin^2 \Delta_{32}) - \cos^4 \theta_{13} \sin^2 2\theta_{12} \sin^2 \Delta_{21}$$

Avec  $\Delta_{ij} = \frac{(m_i^2 - m_j^2) \times L}{4E}$ .

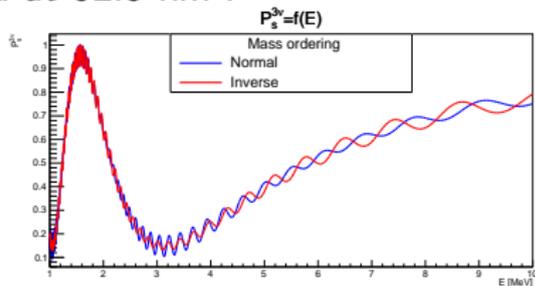
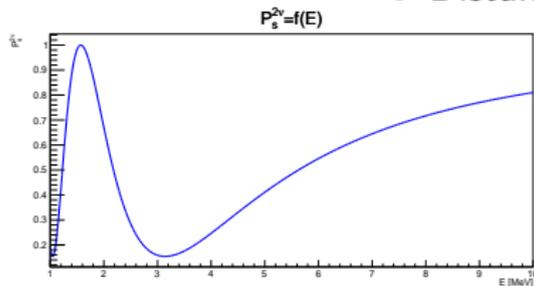
- The solar parameters (in red) were the ones of interest during my internship

# Probabilities of oscillations

- The 2 and 3 flavors survival probabilities are studied as a function of the distance travelled  $L$  and the energy  $E$  of the neutrino
  - Energy fixed at 3 MeV :



- Distance fixed at 52.5 km :

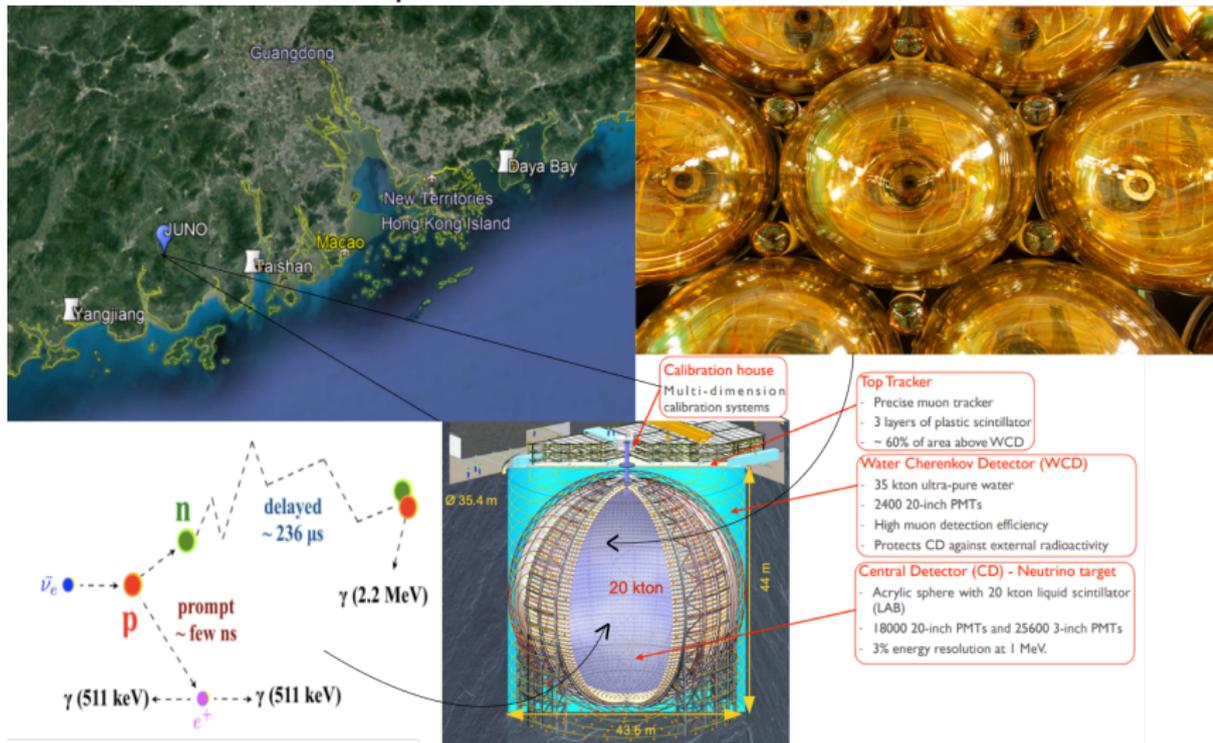


2 flavors

3 flavors

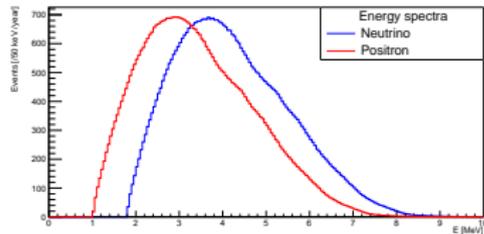
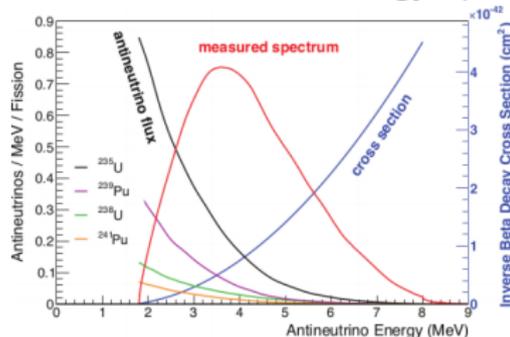
# JUNO experiment and IBD

- JUNO, at 700 m of depth in the South-Eastern China

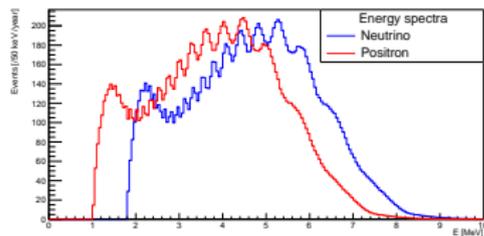
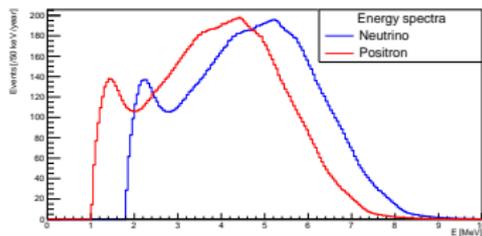


# Energy spectra of neutrino and positron

- Simulation of the energy spectrum near the nuclear plant :

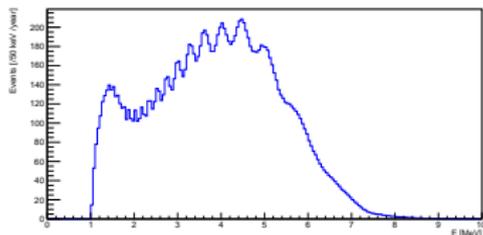


- Oscillation probability implementation :  $P_S^{2\nu}$  then  $P_S^{3\nu}$  :

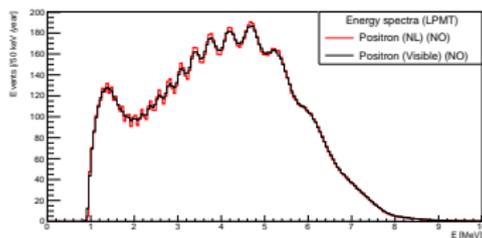


# Detector effects

- $e^+$  energy spectrum :



- Visible energy spectrum with the LPMTs  $Res \simeq 3\% @ 1 \text{ MeV}$

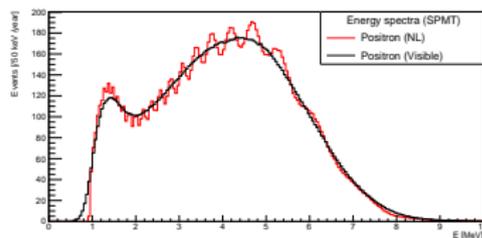


- $\theta_{13}$  et  $\Delta m_{31}^2$  have an effect on the spectrum

- Two main detector effects must be taken into account :

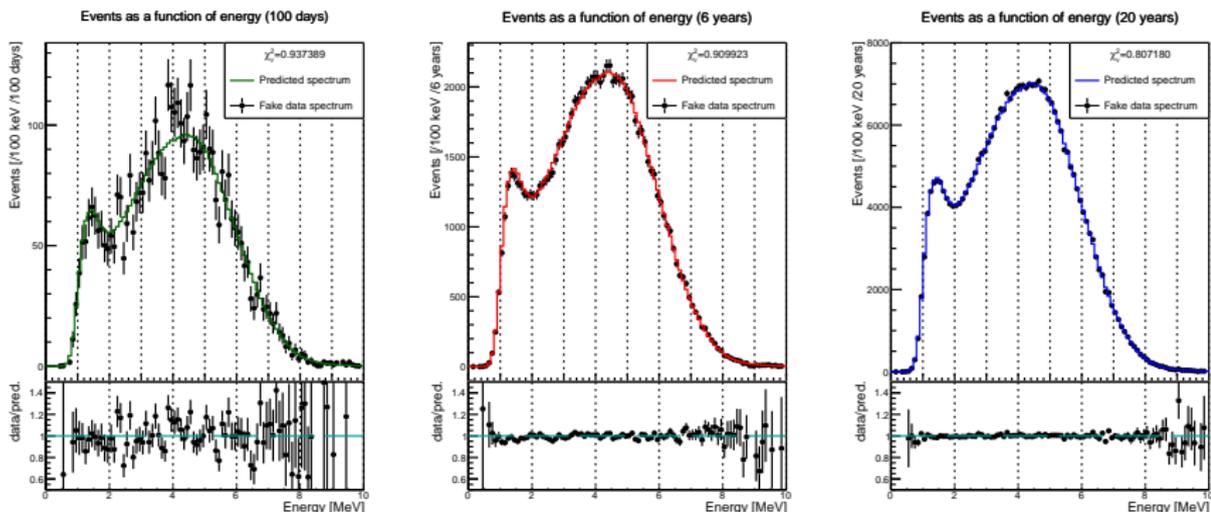
- ▶ The liquid scintillator non-linearity ▶ 19
- ▶ The energy resolution of PMTs ▶ 20

- Visible energy spectrum with the SPMTs  $Res \simeq 15\% @ 1 \text{ MeV}$



- Only  $\theta_{12}$  and  $\Delta m_{21}^2$  seem to have an impact

- Fake data<sup>1</sup> were generated on the vivble energy thanks to a gaussian random generator  $Gauss(N, \sqrt{N})$  to simulate the data JUNO is supposed to obtain from 2023

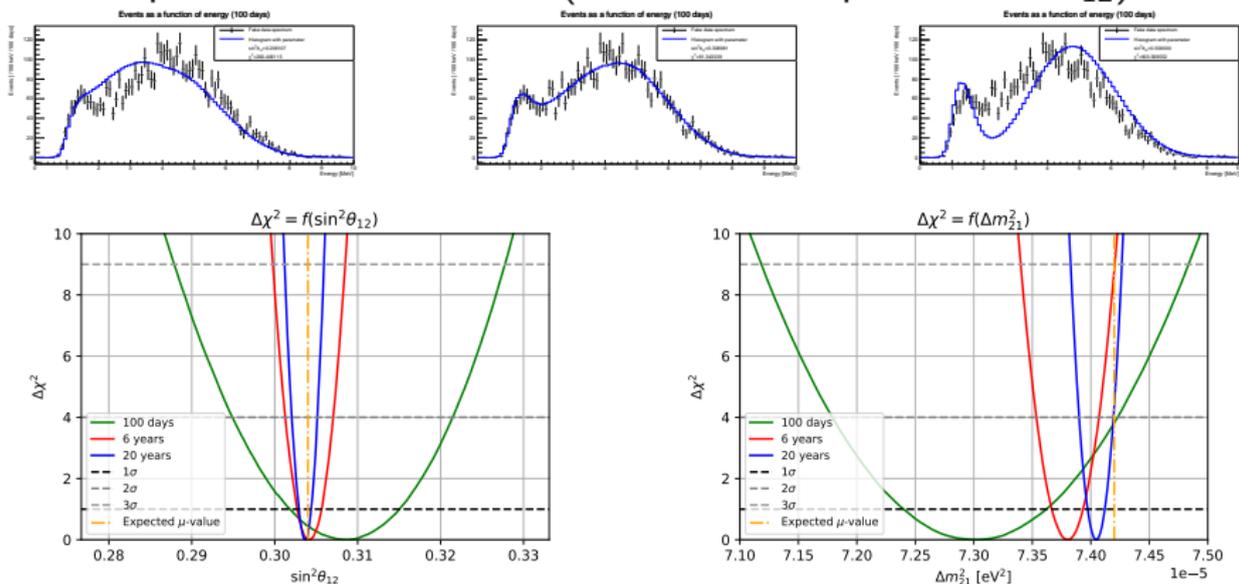


- $\chi^2_\nu$  is decreasing and the "fake data/pred." ratio approaches 1 thanks to the statistical uncertainty decreasing with time

1. Using NuFit5.0  $\sin^2 \theta_{12} = 0.304$ ,  $\sin^2 \theta_{13} = 0.02219$ ,  $\Delta m_{21}^2 = 7.42 \times 10^{-5} \text{eV}^2$  and  $\Delta m_{31}^2 = 2.517 \times 10^{-3} \text{eV}^2$

# $\Delta\chi^2$ as a function of 1 parameter

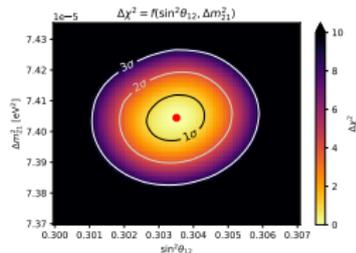
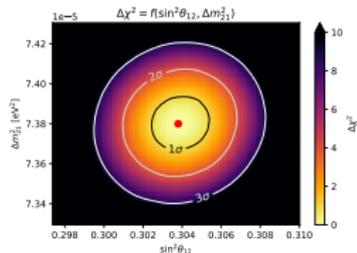
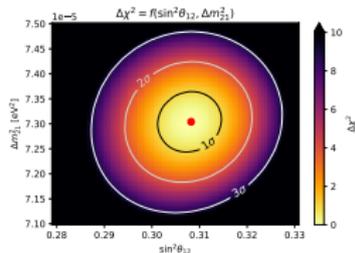
- A 1-parameter scan is made (here is an example with  $\sin^2 \theta_{12}$ ) ▶  $\Delta m_{21}^2$  :



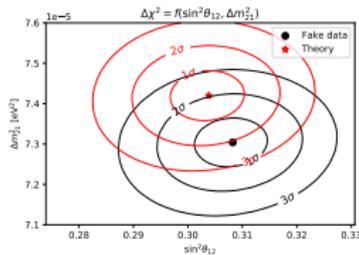
- The longer the experiment duration is, the better the accuracy will be
- A bias in the mean value is created by the choice of the seed

# $\Delta\chi^2$ test as a function of 2 parameters

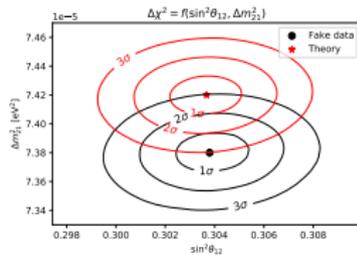
- A  $\Delta\chi^2$  test as a function of 2 parameters was done in order to see if the bias is decreasing and if the accuracy is improving



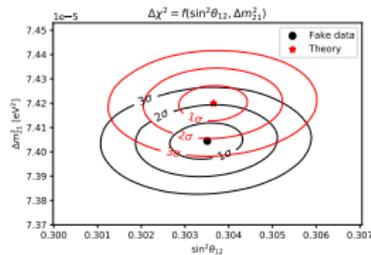
- Comparison with the theoretical values



100 days



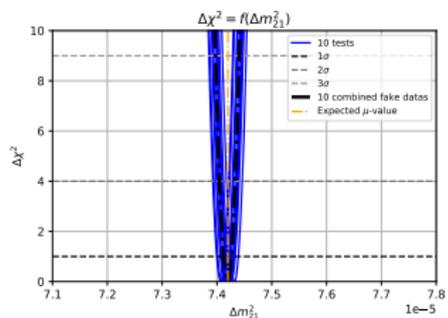
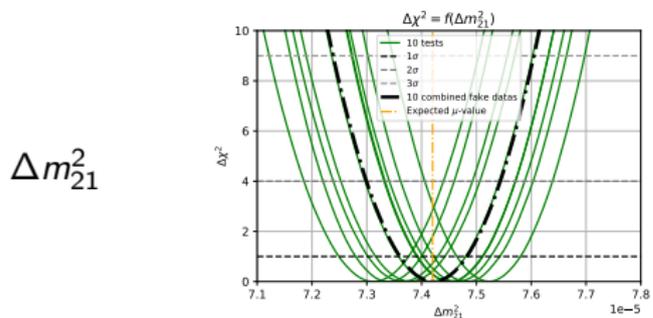
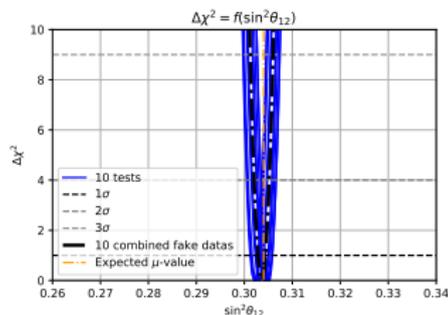
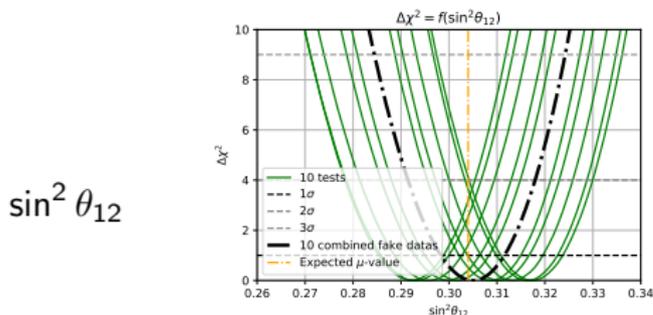
6 years



20 years

- The bias didn't decrease and the accuracy didn't improve

- 10 sets of fake data with 10 different seeds are generated and combined to avoid seed bias



100 days

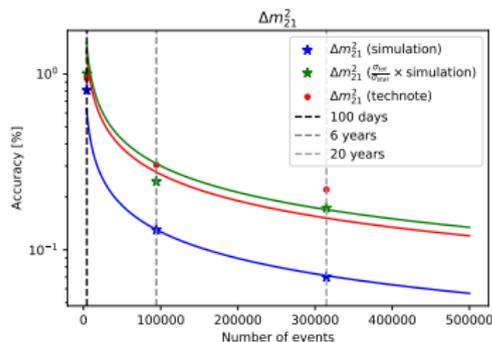
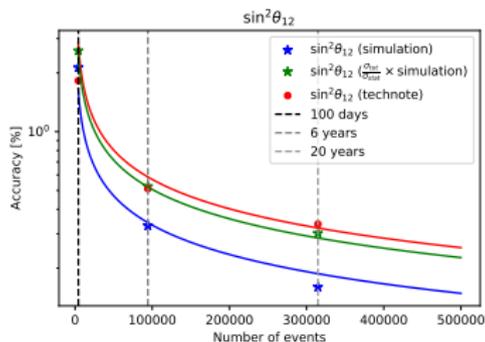
20 years

- The mean parabolas coincide with the theoretical mean values
- The bias is reduced with the duration of the experiment

# Accuracy obtained

- Accuracy obtained as a function of experiment duration

Parameter	Duration	Accuracies ( $1\sigma$ ) (stat)	Accuracies of the technote <sup>2</sup> (stat+sys)
$\sin^2 \theta_{12}$	100 days	2.13%	1.83%
	6 years	0.33%	0.51%
	20 years	0.16%	0.34%
$\Delta m_{21}^2$	100 days	0.81%	0.94%
	6 years	0.13%	0.30%
	20 years	0.07%	0.22%



- The data are comparable when multiplied by the  $\frac{\sigma_{tot}}{\sigma_{stat}}$  ratio

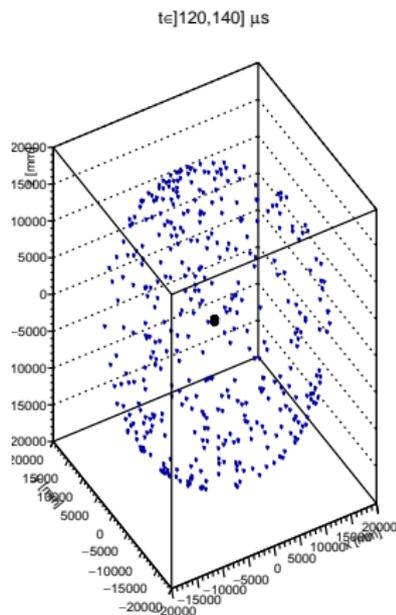
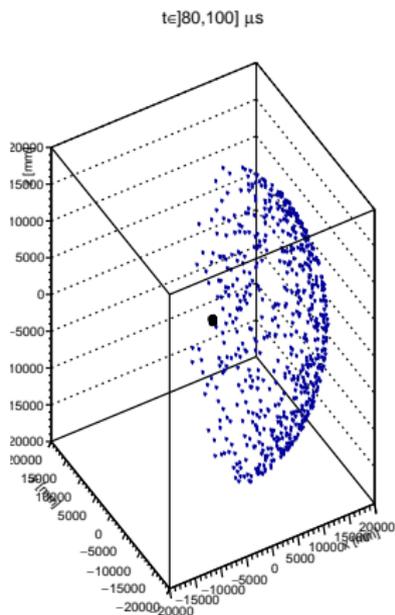
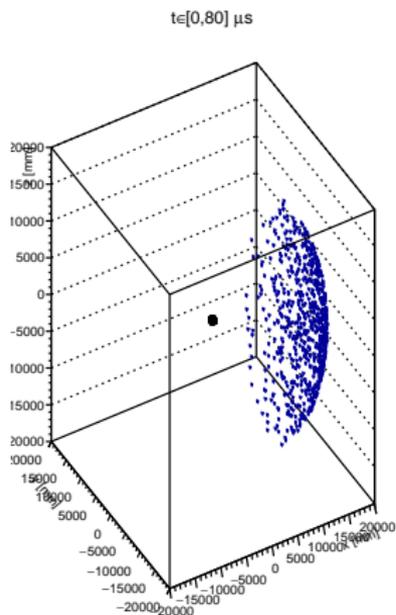
## 2. Work of 3 independant groups of the JUNO collaboration

# Conclusion

- A reconstruction of the  $\bar{\nu}_e$  theoretical energy spectrum was performed
- Simulations of observable data from 2023 onwards were then generated
- $\sin^2 \theta_{12}$  and  $\Delta m_{21}^2$  measurements thanks to  $\Delta\chi^2$  showed a seed bias
- This bias is almost entirely solved when combining 10 sets of fake data
- The accuracies that were obtained are comparable with the ones obtained by 3 independant groups of the JUNO collaboration when multiplied by the  $\frac{\sigma_{tot}}{\sigma_{stat}}$  ratio

# Perspectives

- Implementation of background and systematic uncertainties
- Combination of more sets of fake data
- Cross-referencing with LPMTs data



— Thank you —

— Backup —

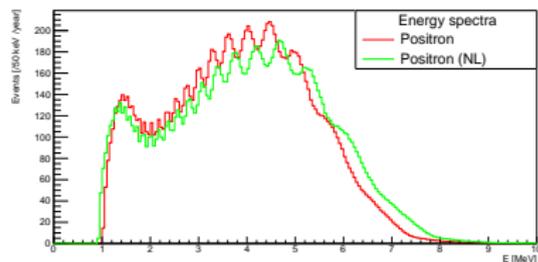
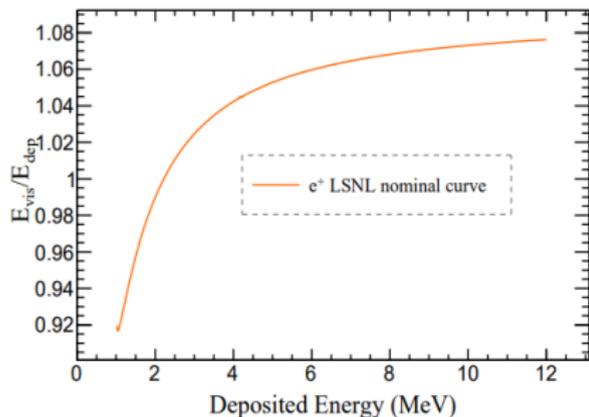
## Results obtained

Parameter	Duration	Value $\pm 1\sigma$	$2\sigma$ area	$3\sigma$ area
$\sin^2 \theta_{12}$ (1 fake data)	100 days	$0.309^{+0.006}_{-0.007}$	0.295 – 0.321	0.288 – 0.328
	6 years	$0.304^{+0.002}_{-0.001}$	0.301 – 0.307	0.300 – 0.309
	20 years	$0.304^{+0.001}_{-0.001}$	0.302 – 0.305	0.301 – 0.306
$\sin^2 \theta_{12}$ (10 combined fake datas)	100 days	$0.305^{+0.007}_{-0.007}$	0.291 – 0.318	0.284 – 0.324
	6 years	$0.304^{+0.001}_{-0.002}$	0.301 – 0.306	0.299 – 0.308
	20 years	$0.304^{+0.000}_{-0.001}$	0.302 – 0.305	0.301 – 0.306
$\sin^2 \theta_{12}$ (theoretical spectra)	100 days	$0.304^{+0.007}_{-0.007}$	0.290 – 0.317	0.283 – 0.323
	6 years	$0.304^{+0.001}_{-0.002}$	0.301 – 0.306	0.299 – 0.308
	20 years	$0.304^{+0.000}_{-0.001}$	0.302 – 0.305	0.301 – 0.306
$\Delta m_{21}^2 [\times 10^{-5} \text{eV}^2]$ (1 fake data)	100 days	$7.30^{+0.06}_{-0.06}$	7.18 – 7.42	7.12 – 7.48
	6 years	$7.38^{+0.01}_{-0.01}$	7.35 – 7.41	7.34 – 7.42
	20 years	$7.41^{+0.00}_{-0.01}$	7.39 – 7.42	7.38 – 7.43
$\Delta m_{21}^2 [\times 10^{-5} \text{eV}^2]$ (10 combined fake datas)	100 days	$7.42^{+0.06}_{-0.06}$	7.30 – 7.54	7.24 – 7.61
	6 years	$7.42^{+0.01}_{-0.01}$	7.39 – 7.44	7.38 – 7.46
	20 years	$7.42^{+0.01}_{-0.01}$	7.40 – 7.43	7.40 – 7.44
$\Delta m_{21}^2 [\times 10^{-5} \text{eV}^2]$ (theoretical spectra)	100 days	$7.42^{+0.06}_{-0.06}$	7.30 – 7.54	7.24 – 7.61
	6 years	$7.42^{+0.01}_{-0.01}$	7.39 – 7.44	7.38 – 7.46
	20 years	$7.42^{+0.01}_{-0.01}$	7.40 – 7.43	7.40 – 7.44

# The liquid scintillator non-linearity effects

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- The intensity of the light emitted is not perfectly proportional to the positron energy, so it has to be taken into account in the study :



- The normal mass ordering is considered here.

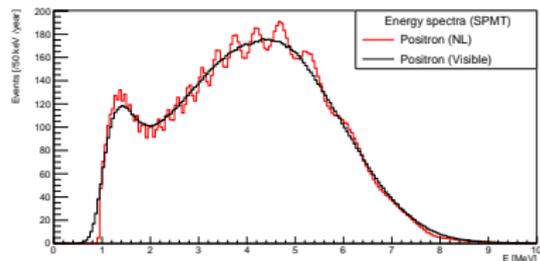
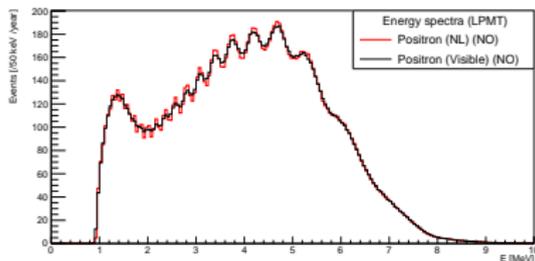
# Comparison of the LPMT and SPMT energy resolutions

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- In order to take into account the energy resolution, a random gaussian generator  $Gauss(E, \sigma_E)$  is applied on each of the bins of the data :

$$\frac{\sigma_E}{E} = \sqrt{\left(\frac{a}{\sqrt{E}}\right)^2 + b^2 + \left(\frac{c}{E}\right)^2}$$

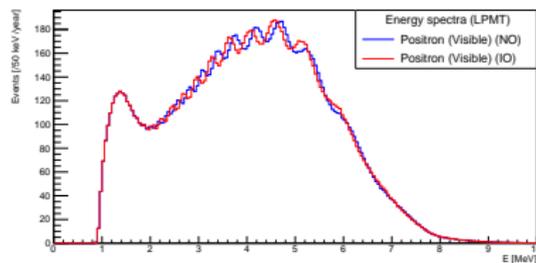
- With  $a_{LPMT} = 0.0261$ ,  $a_{SPMT} = 0.1536$ ,  $b = 0.0082$  and  $c = 0.0123$ .



- The visible energy spectrum of SPMTs is only influenced by the solar terms  $\theta_{12}$  and  $\Delta m_{21}^2$

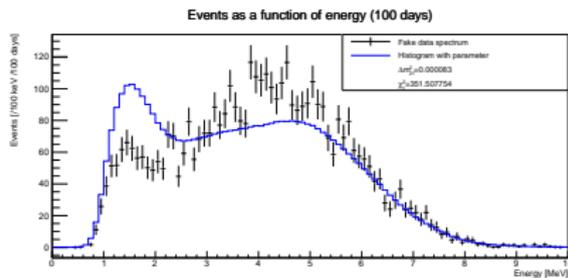
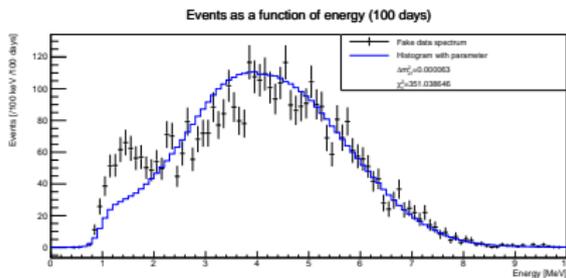
# Mass ordering

- One can study the mass ordering thanks to the energy resolution of the LPMTs :

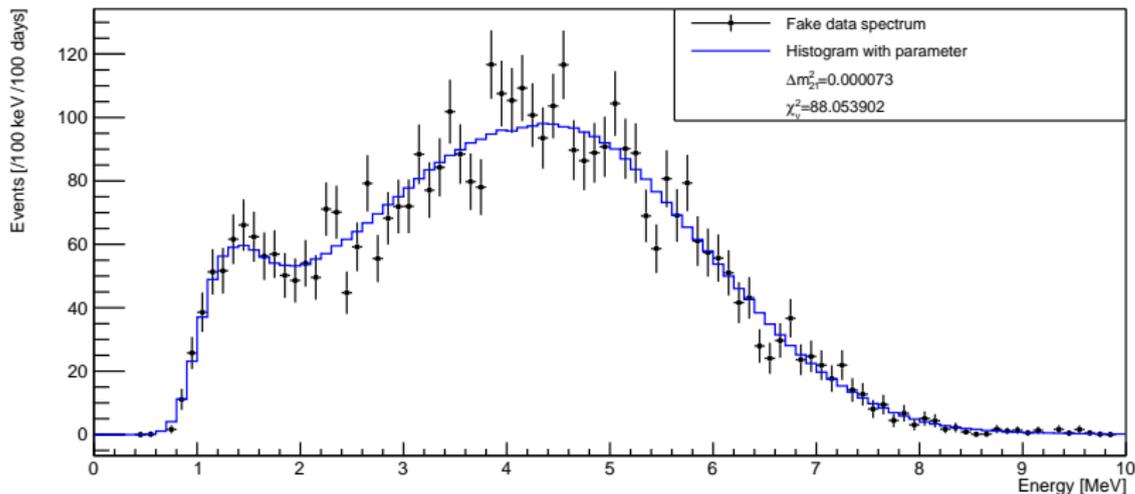


- A phase shift can be observed for  $E_{vis} \in [2.5; 5.5]$  MeV

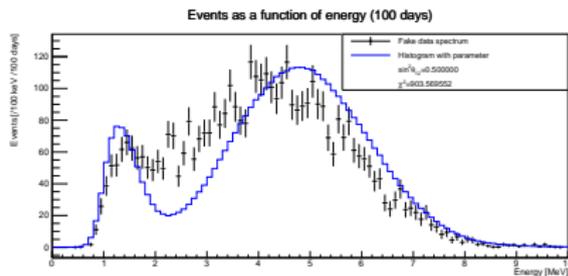
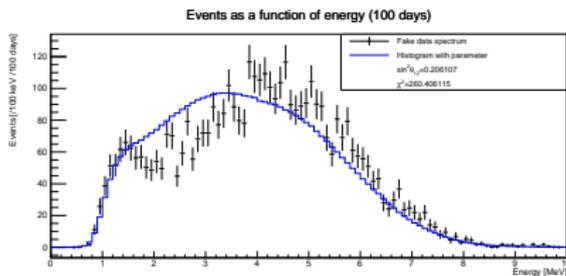
# Test for the $\Delta m_{21}^2$ parameter

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Events as a function of energy (100 days)



# Test for the $\sin^2 \theta_{12}$ parameter



Events as a function of energy (100 days)

