

$f\sigma_8$ with SN Ia

Carreres Bastien, Bautista Julian, Racine Benjamin,
Feinstein Fabrice, Fouchez Dominique

What is $f\sigma_8$?

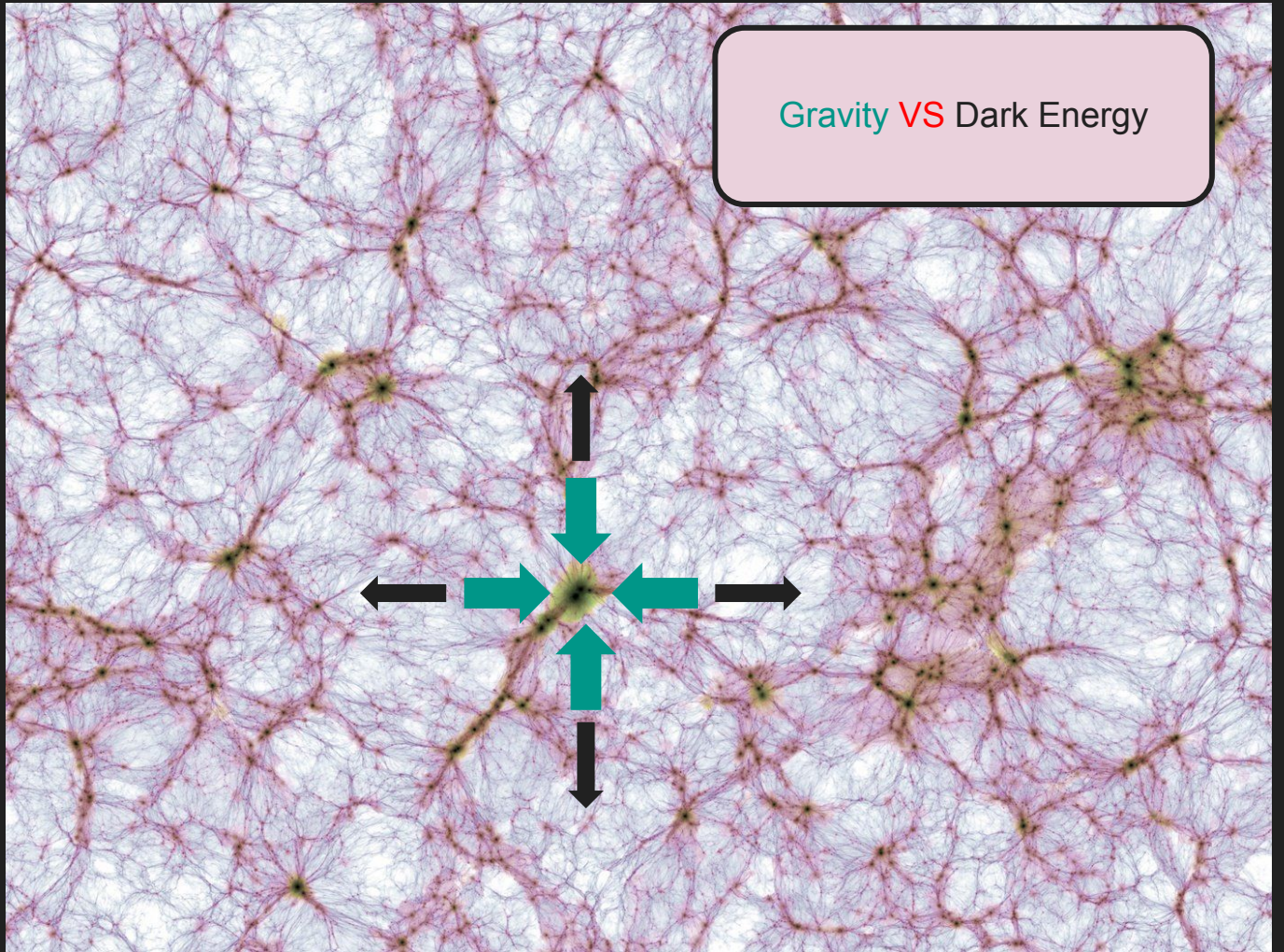
Growth factor

$$\delta_m = \hat{\delta}_m(\mathbf{x}) \boxed{D(t)}$$

Growth rate

$$f = \frac{d \ln D}{d \ln a}$$

Gravity VS Dark Energy



What is $f\sigma_8$?

Growth factor

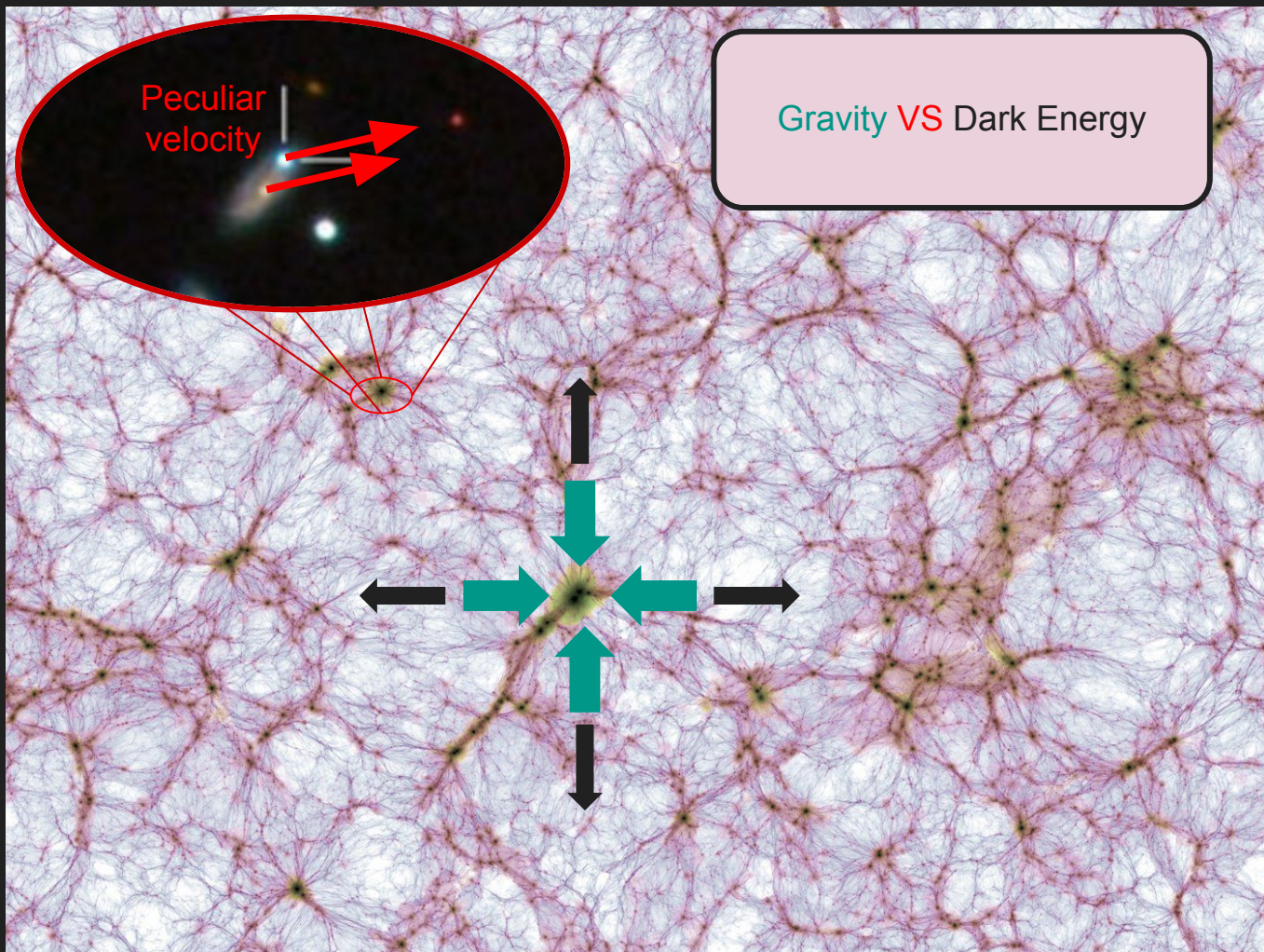
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Peculiar velocities

$$\nabla \cdot \mathbf{v} \propto fD$$



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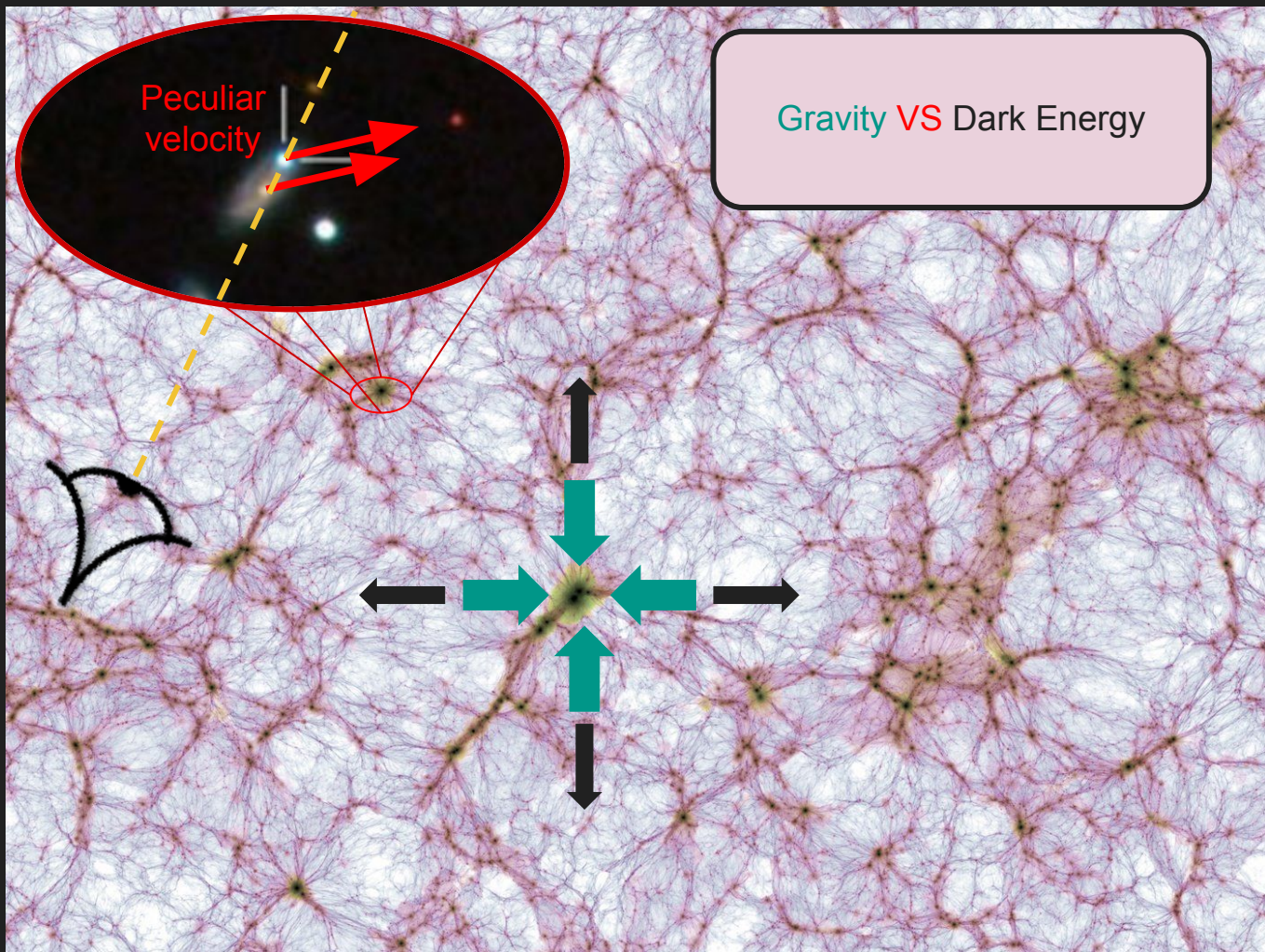
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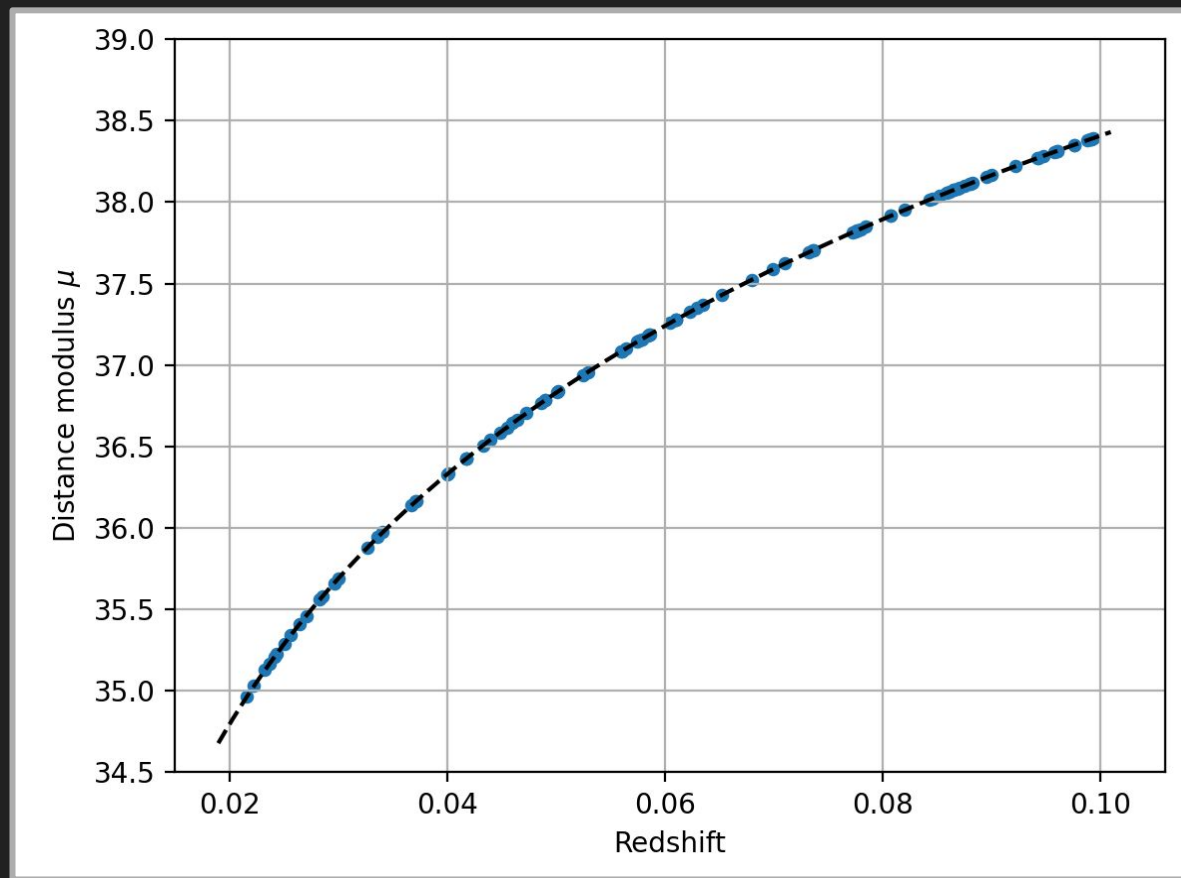
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Peculiar velocities

$$\nabla \cdot \mathbf{v} \propto fD$$



The Hubble diagram with peculiar velocities



The Hubble diagram with peculiar velocities

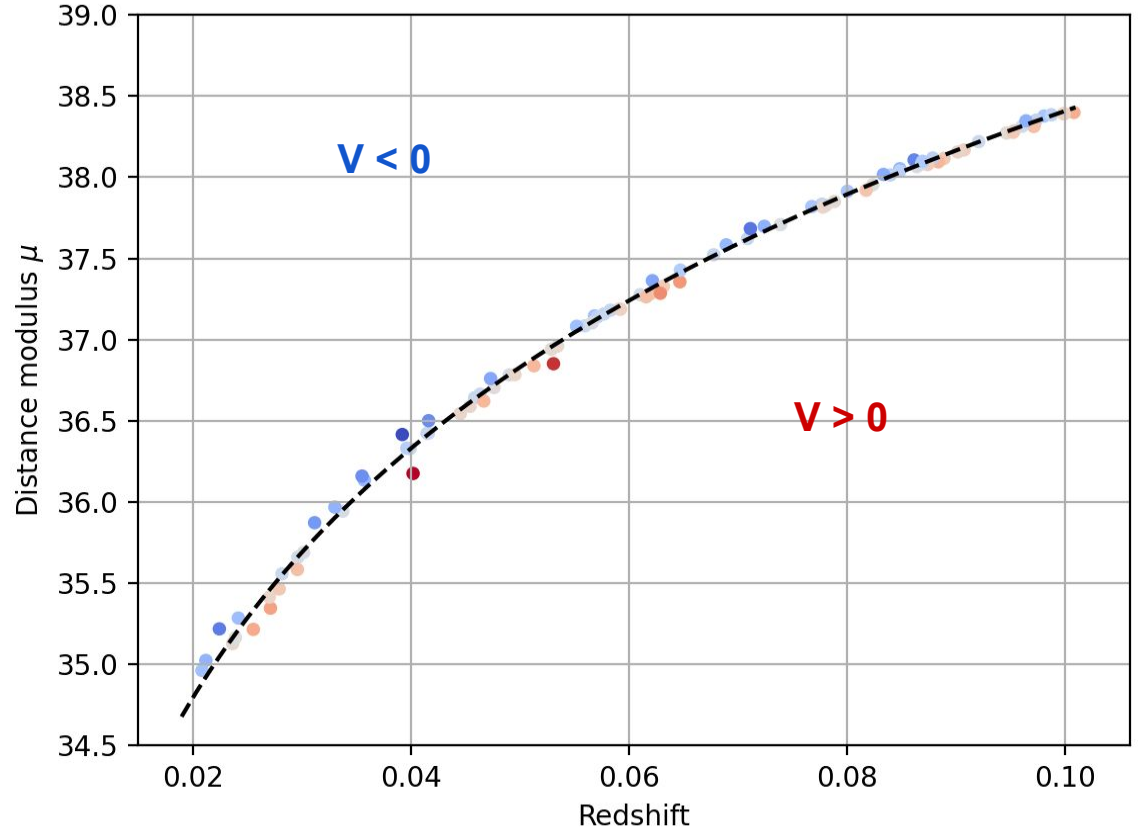
Adding peculiar velocity :

$v \sim 300 \text{ km / s}$

$\Delta z \sim 0.001$

$\Delta \mu \sim 0.004 \text{ mag}$

Variation has the same sign
as peculiar velocities



The Hubble diagram with peculiar velocities

Adding peculiar velocity :

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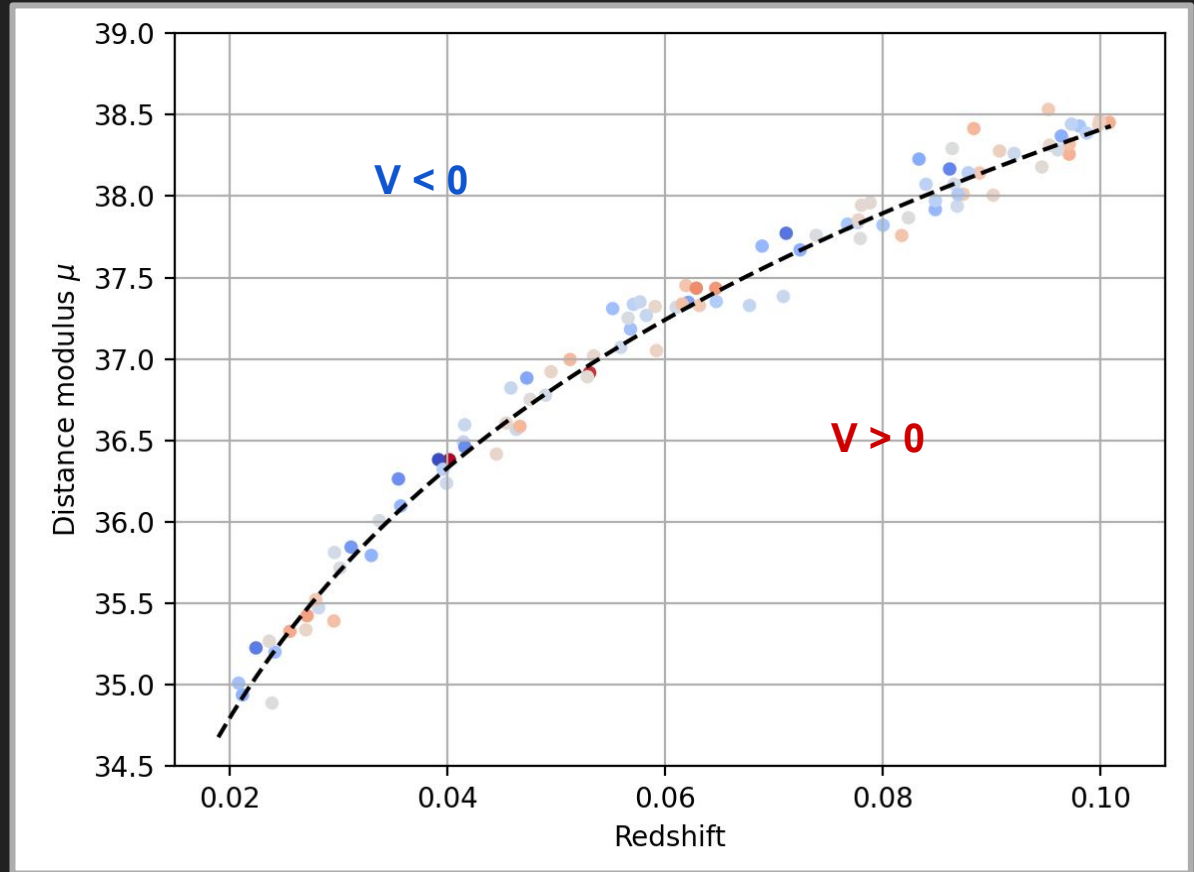
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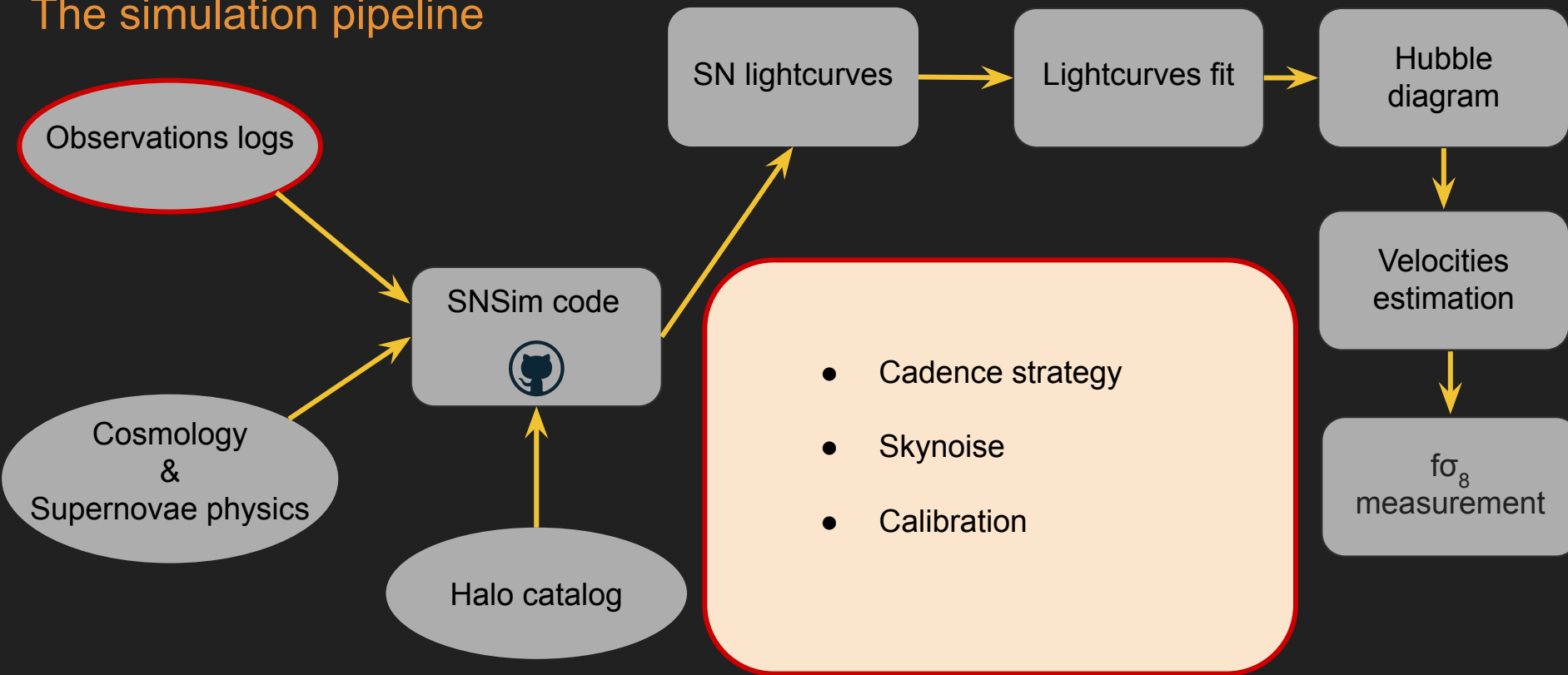
Variation has the same sign as peculiar velocities

Adding intrinsic scatter :

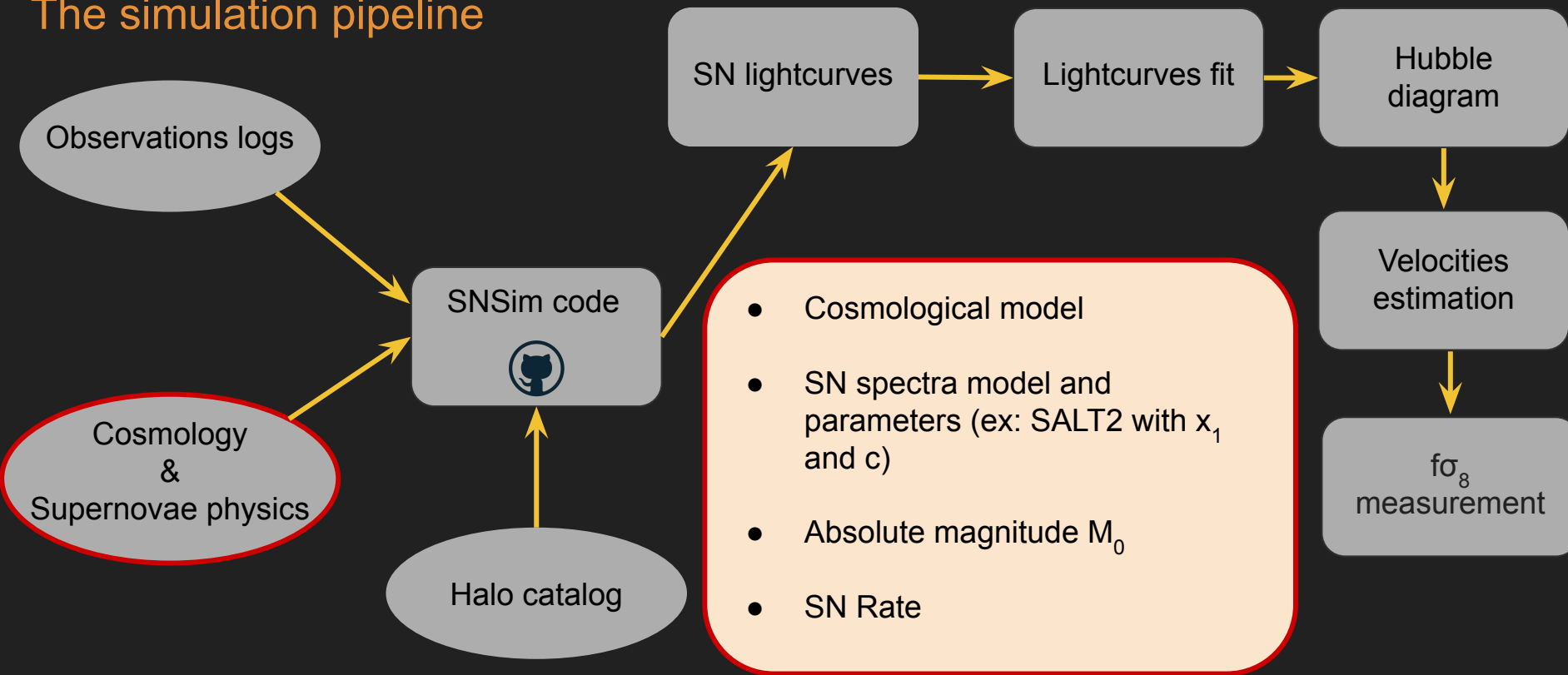
$$\sigma_{\text{int}} \sim 0.12 \text{ mag}$$



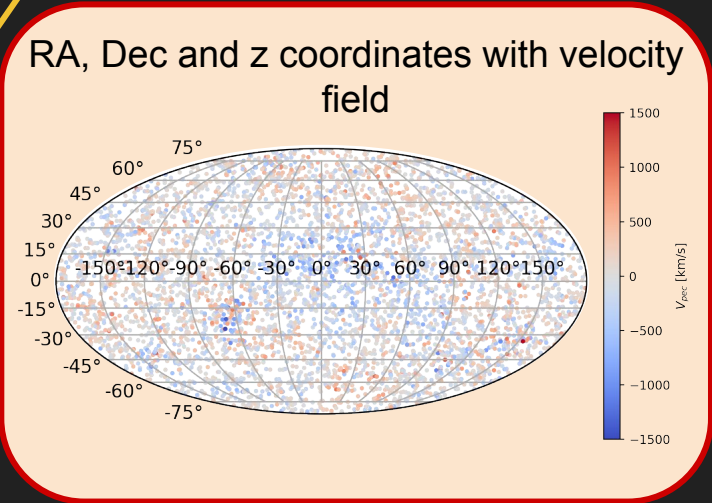
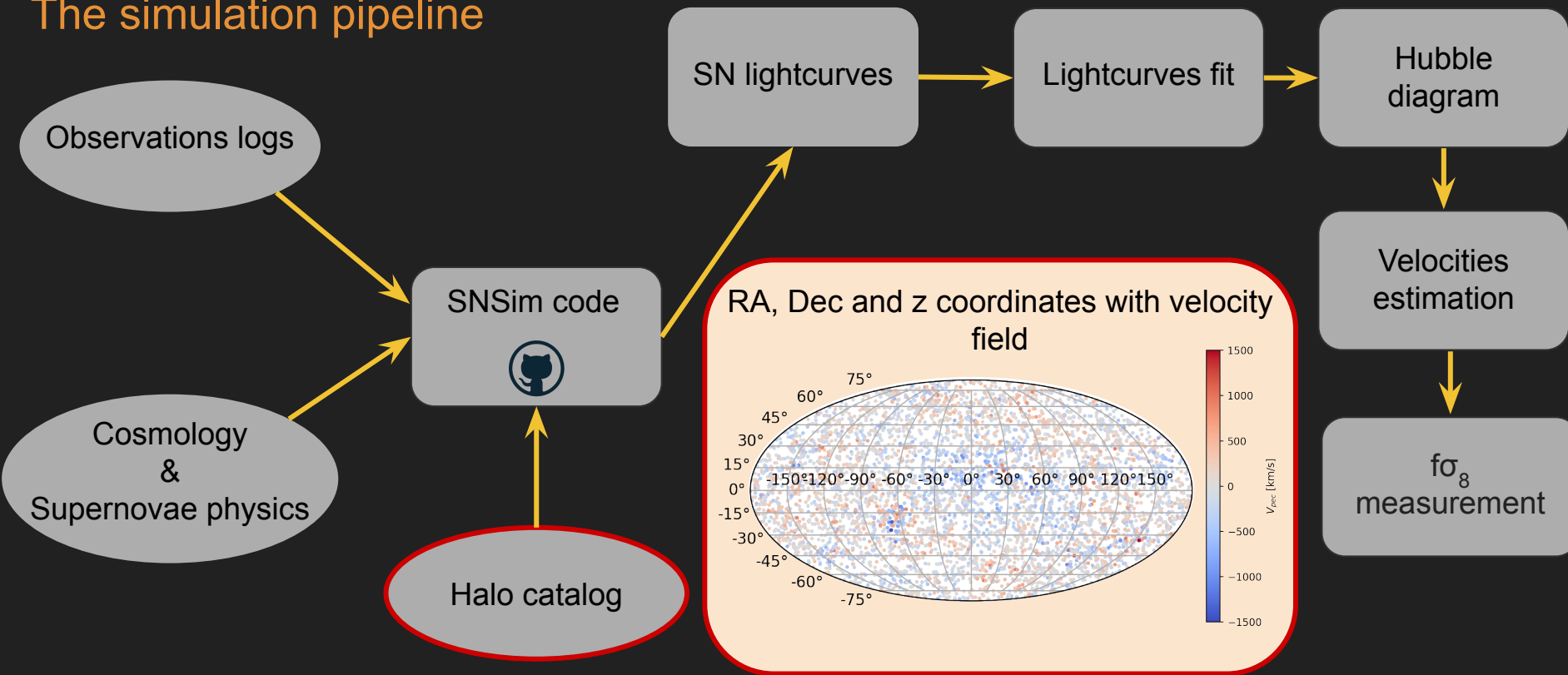
The simulation pipeline



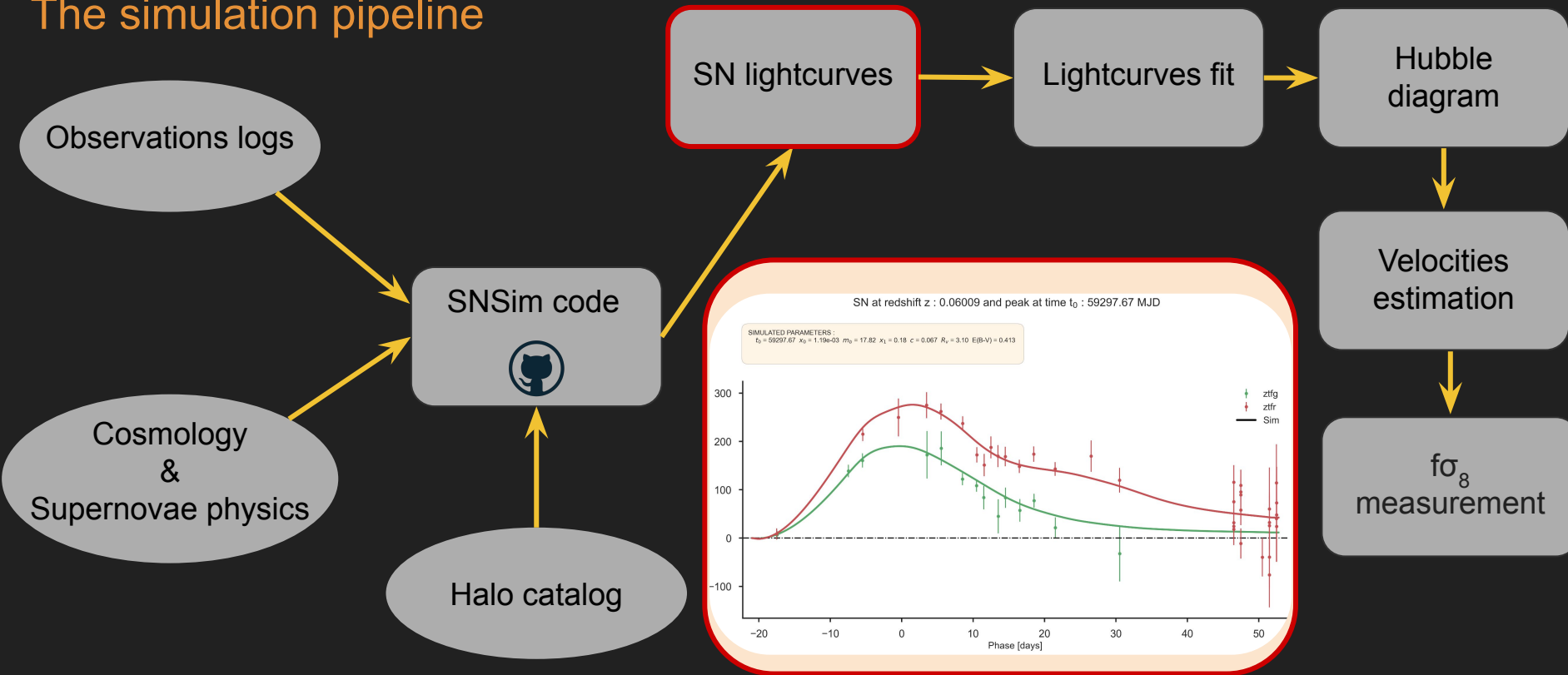
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SN lightcurves

Lightcurves fit

Hubble diagram

Velocities estimation

$f\sigma_8$ measurement

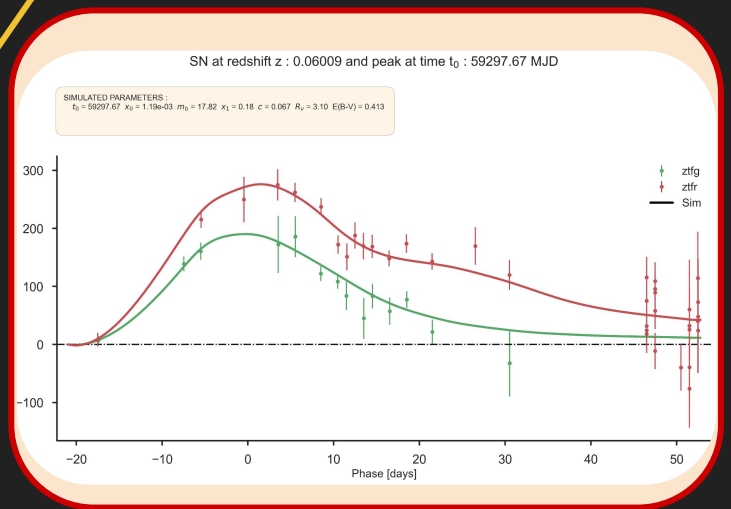
SNSim code



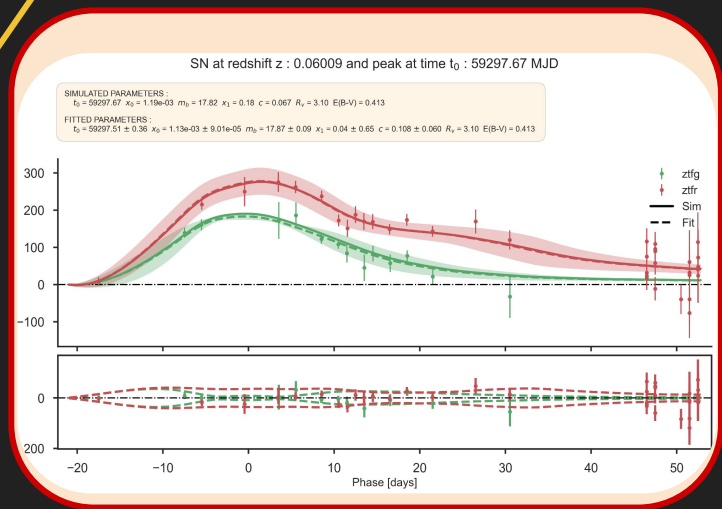
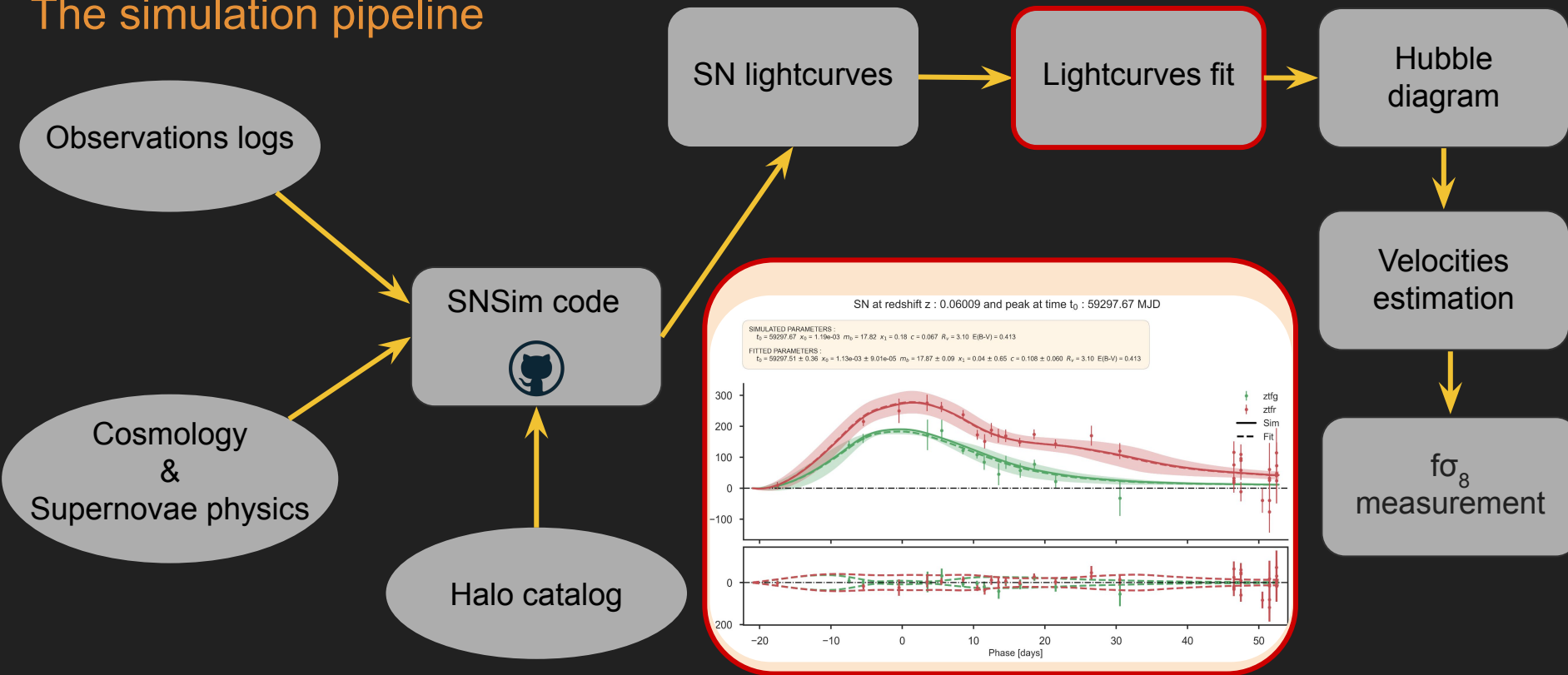
Cosmology & Supernovae physics

Observations logs

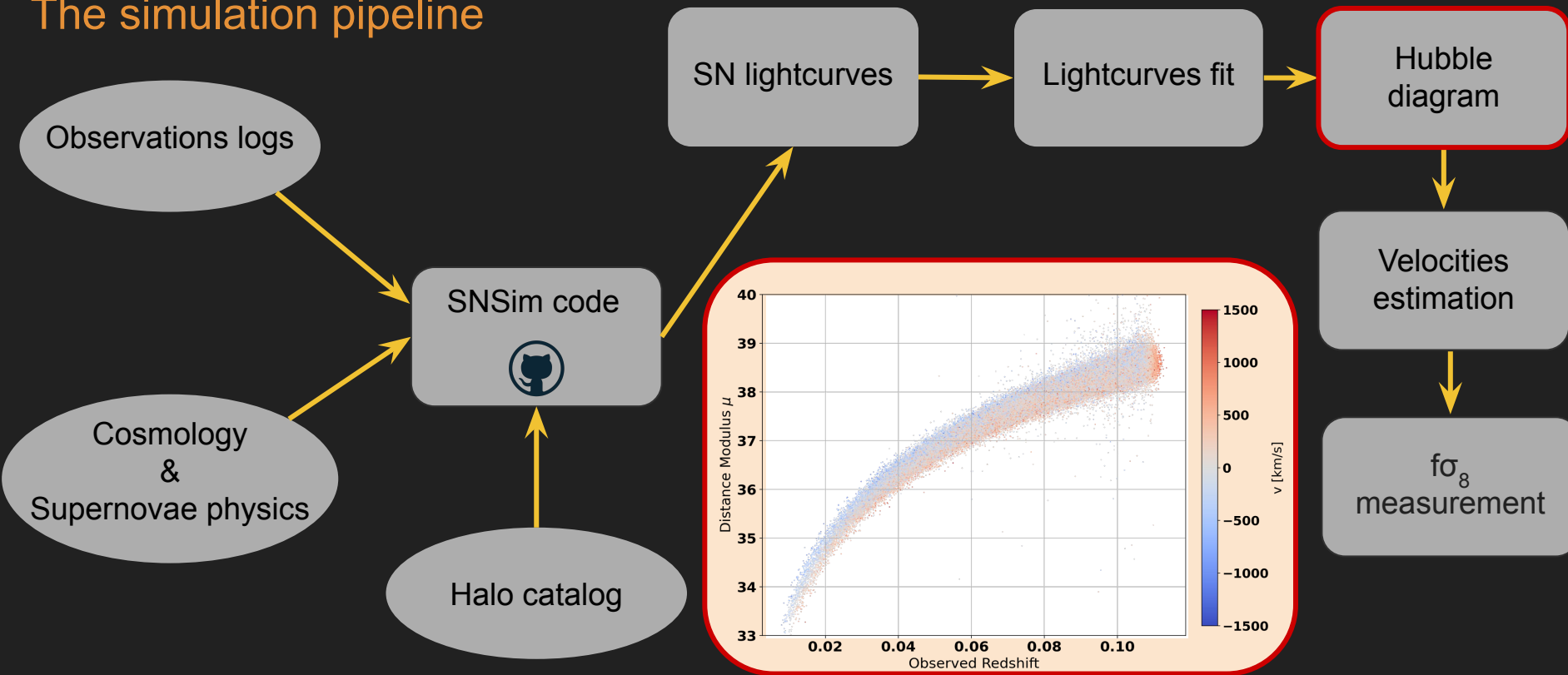
Halo catalog



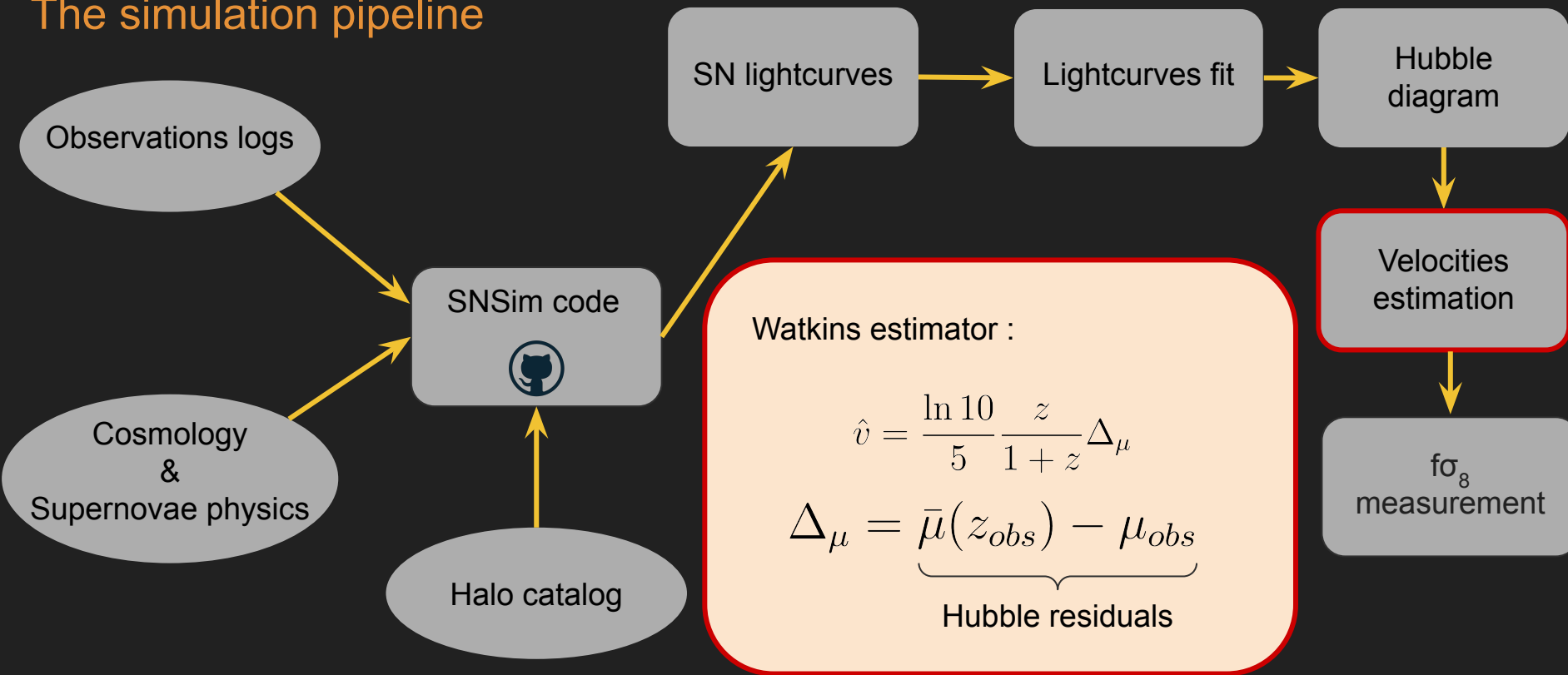
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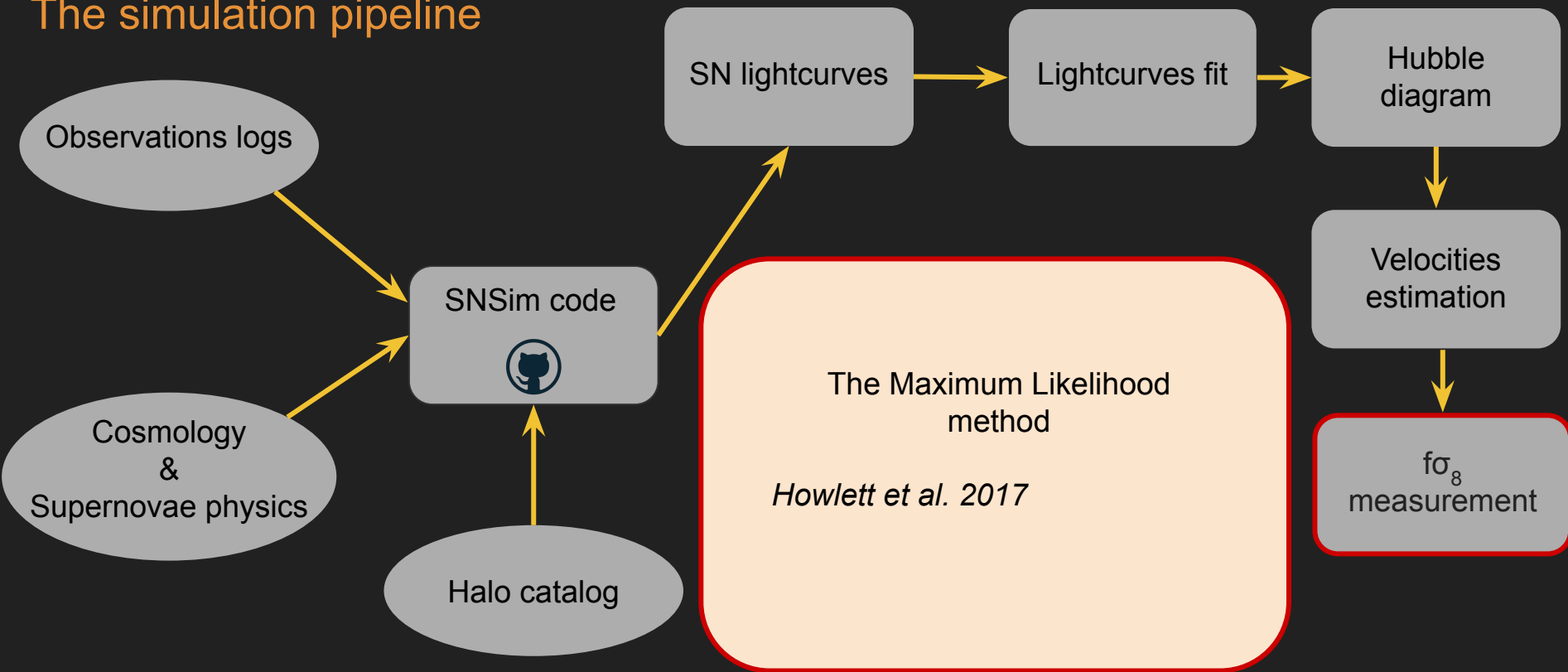
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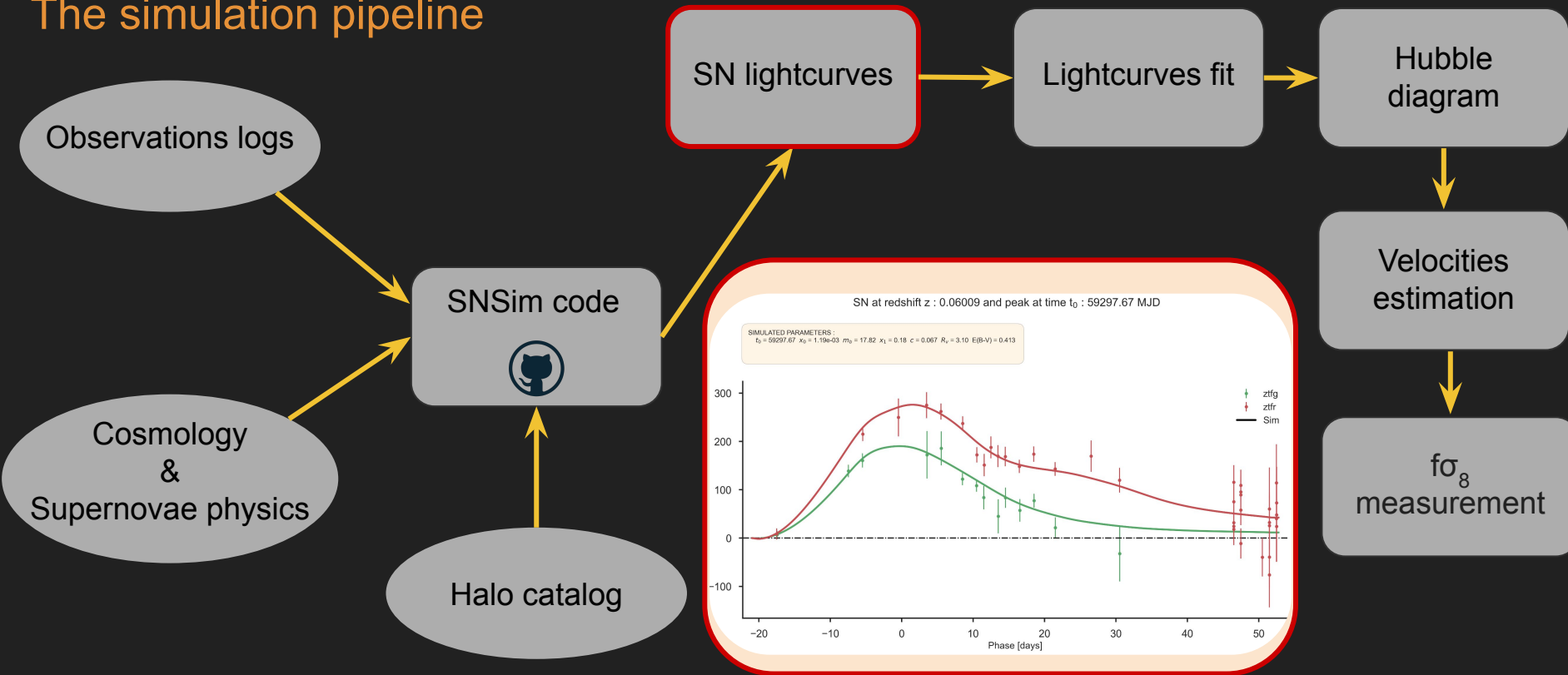
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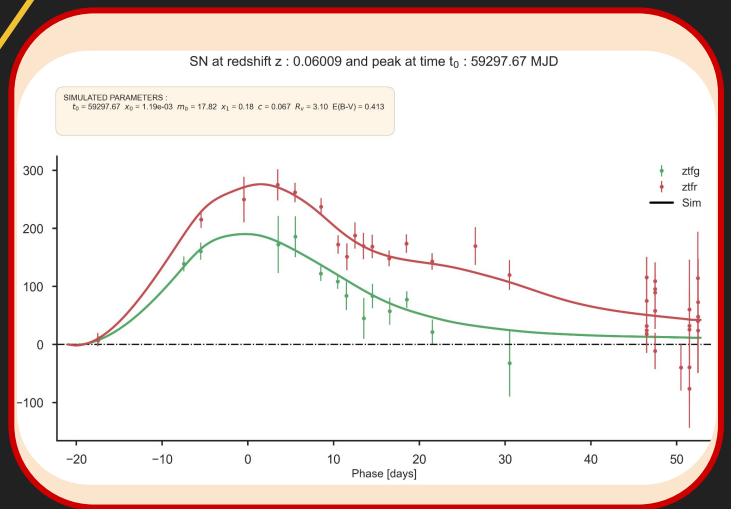
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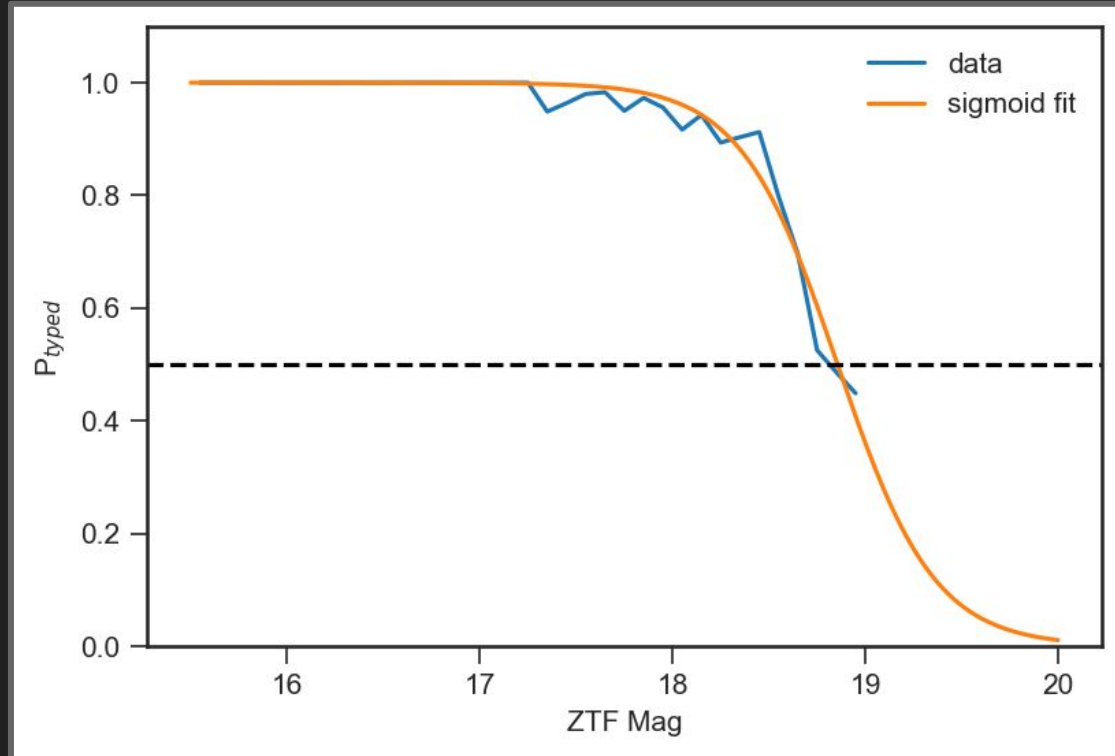


Build a selected SN sample

Quality cut on SN can bias σ_8 by changing peculiar velocities population.

Apply cuts :

- Detection : at least 4 epochs with SNR > 5
- Typing : use typing efficiency dependent on magnitude

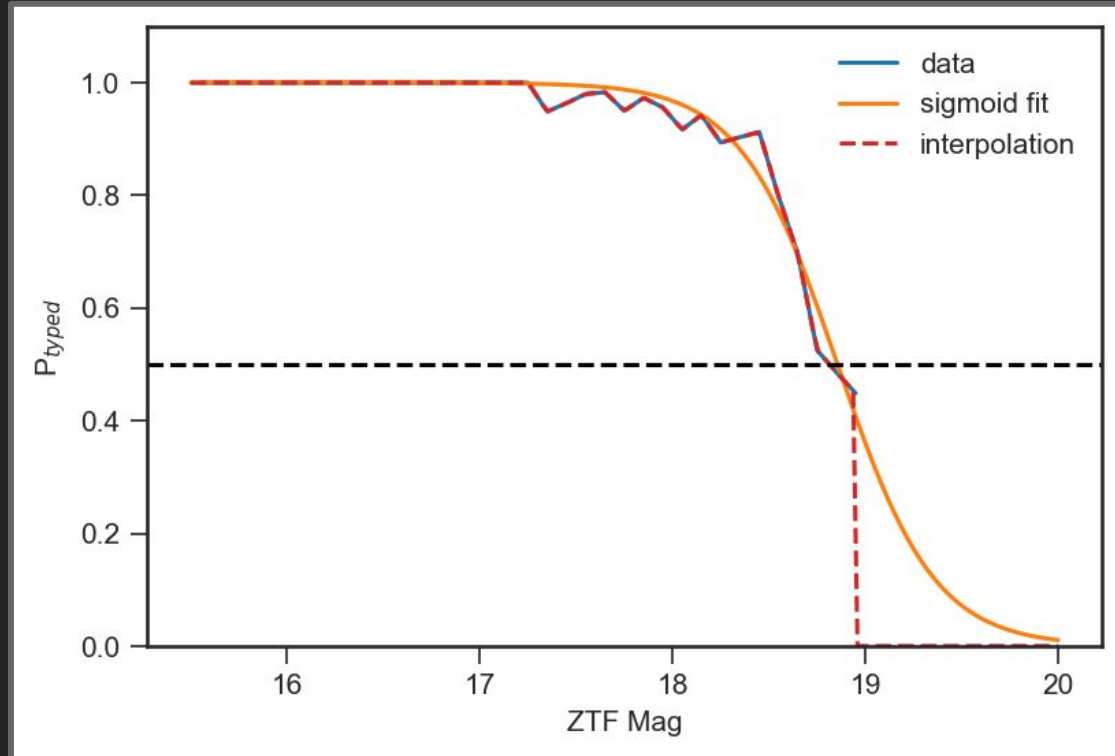


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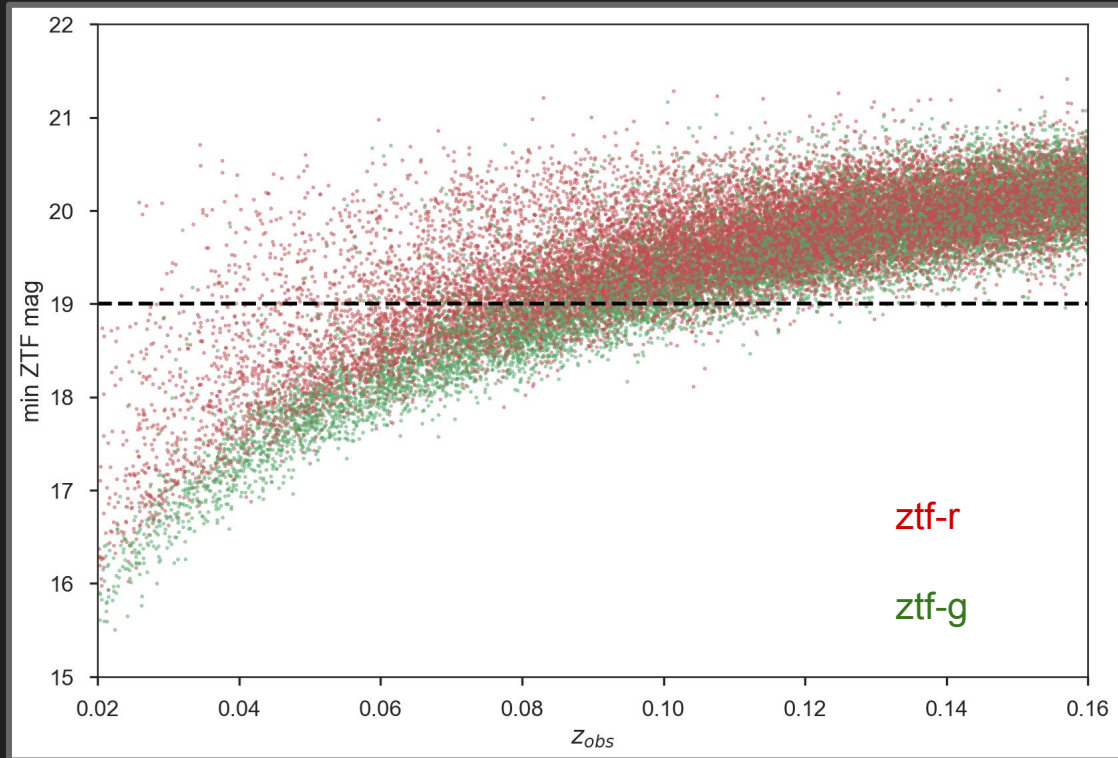


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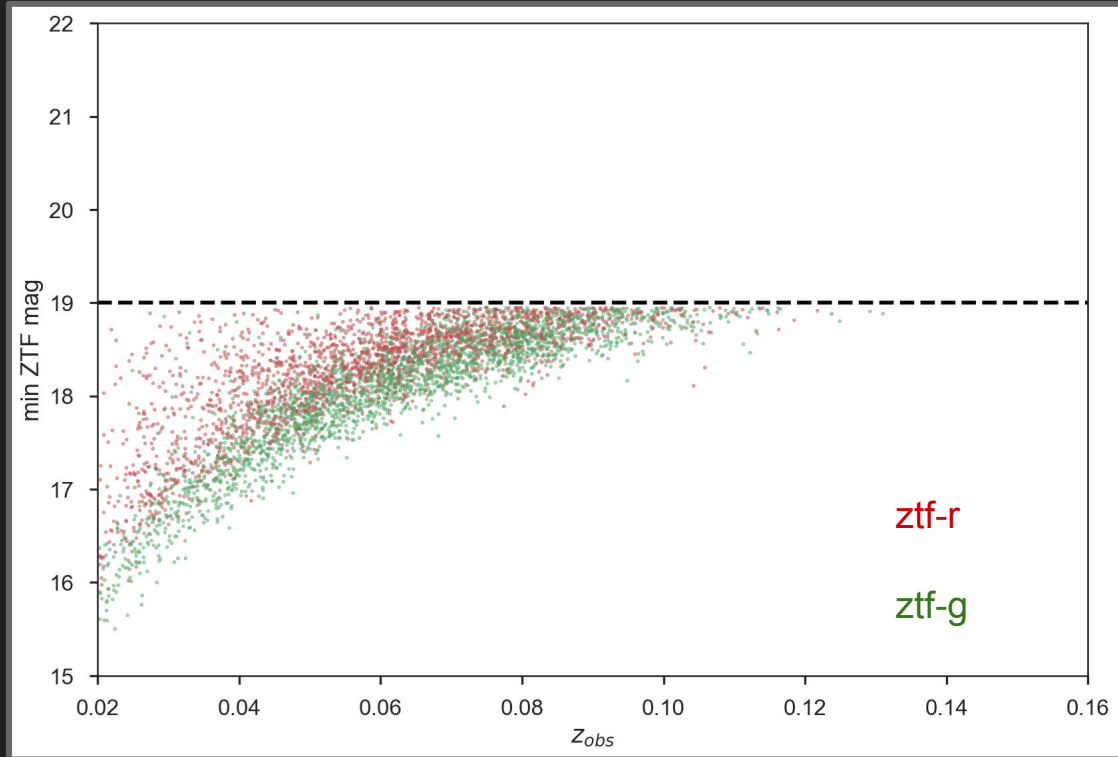


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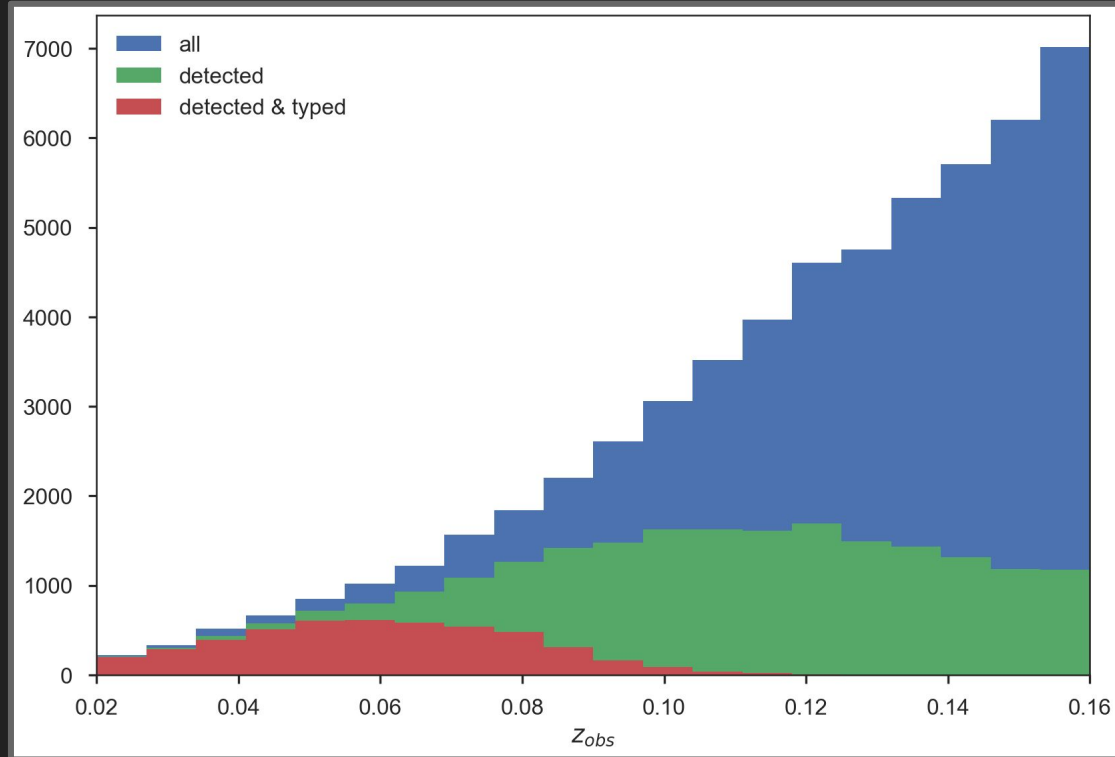


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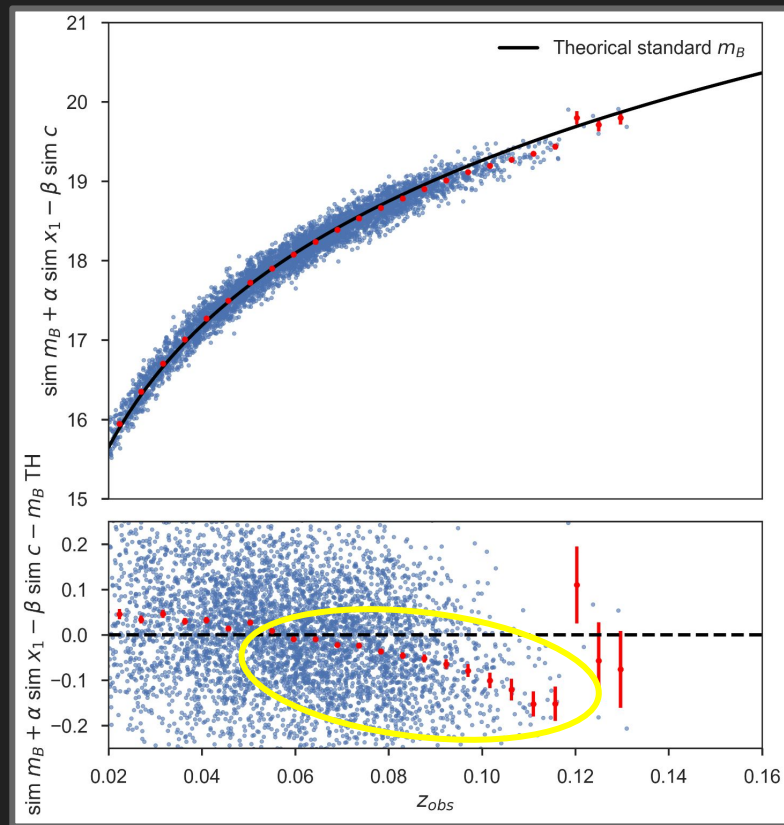
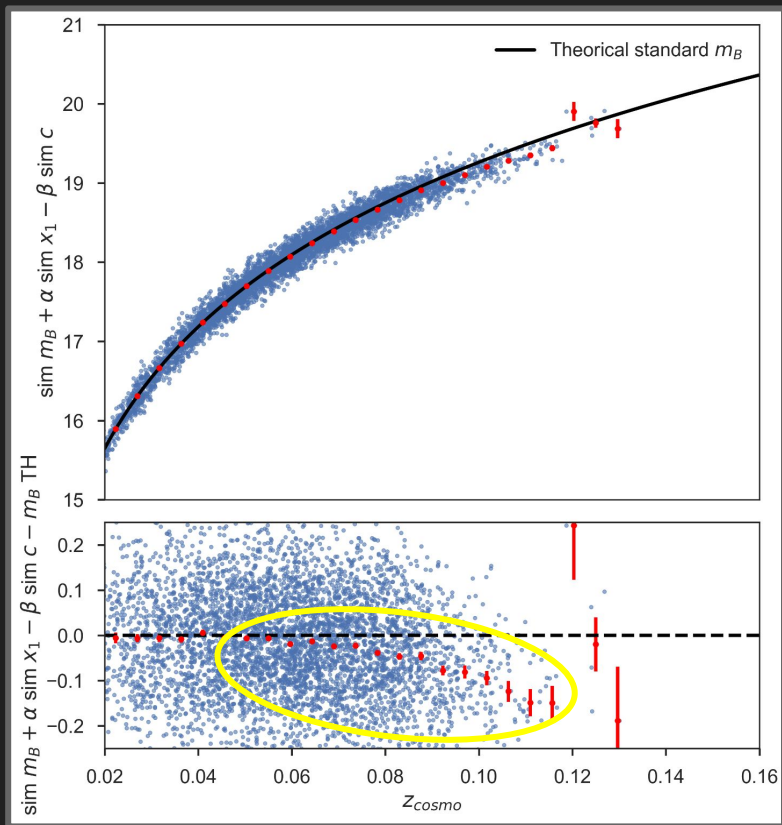
Selected SN :

- Median redshift = 0.06
- Max redshift = 0.13

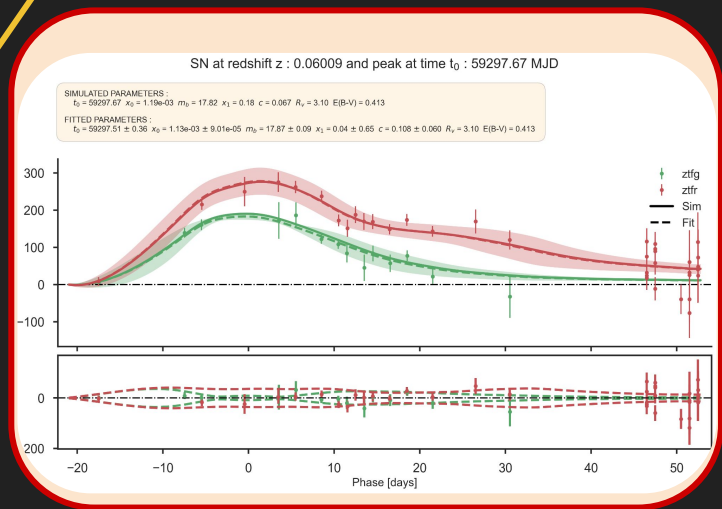
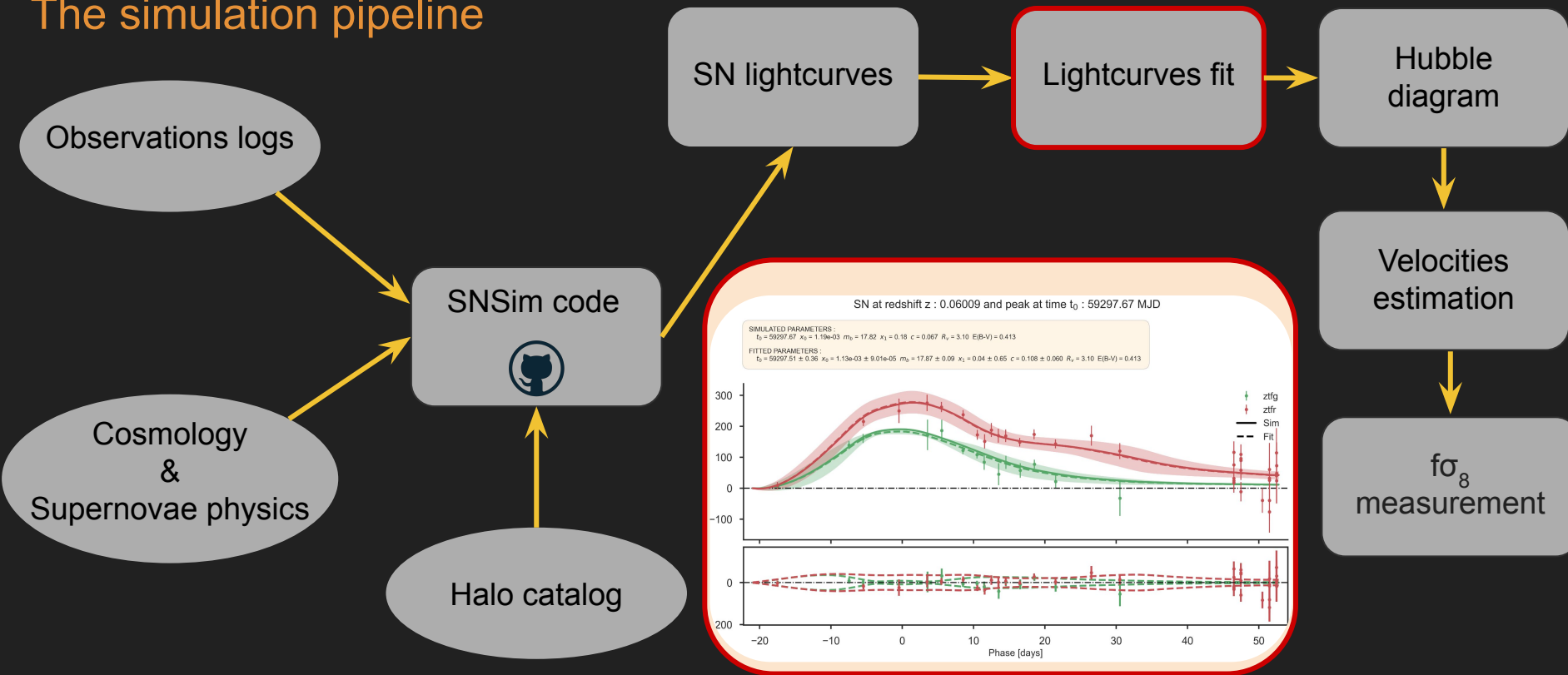


A first look to the simulated HD after selection

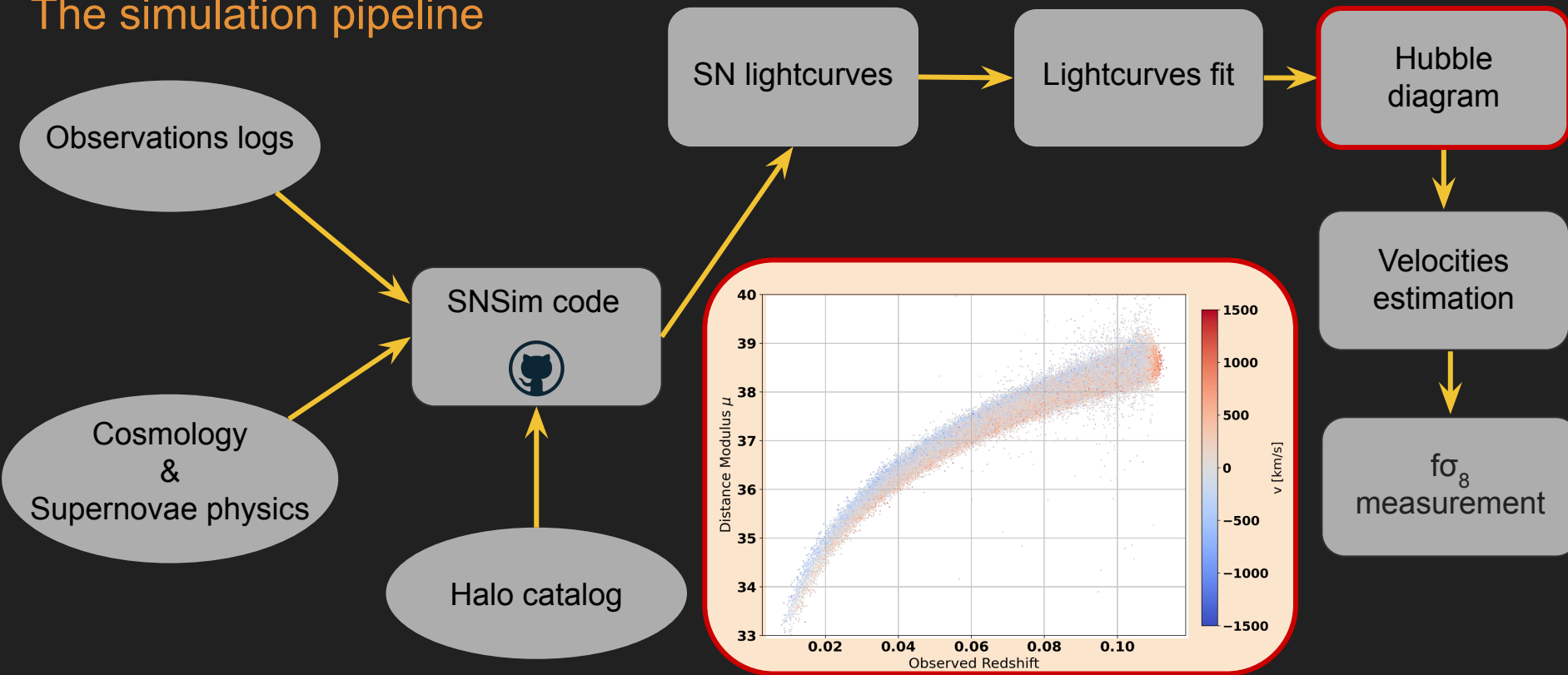
Selection bias appear at $z \sim 0.06$



The simulation pipeline



The simulation pipeline



Fit for α , β , M_0 and σ_M

$$\chi^2 = (\mu_i(\alpha, \beta, M_0) - \mu_{\Lambda\text{CDM}})^T C^{-1} (\mu_i(\alpha, \beta, M_0) - \mu_{\Lambda\text{CDM}})$$

$$-2 \ln \mathcal{L}_{\text{REML}} = \sum_i w_i (\mu_i - \mu_{\Lambda\text{CDM}})^2 - \sum_i \ln(w_i) + \ln \left(\sum_i w_i \right) \quad \text{from Betoule et al. 2014}$$

- 1 - Use χ^2 to fit α , β , M_0 a first time using a fixed $\sigma_M = 0.1$
- 2 - Use value of α , β , M_0 to compute σ_M with REML
- 3 - Re-do the χ^2 fit using the σ_M value obtained before

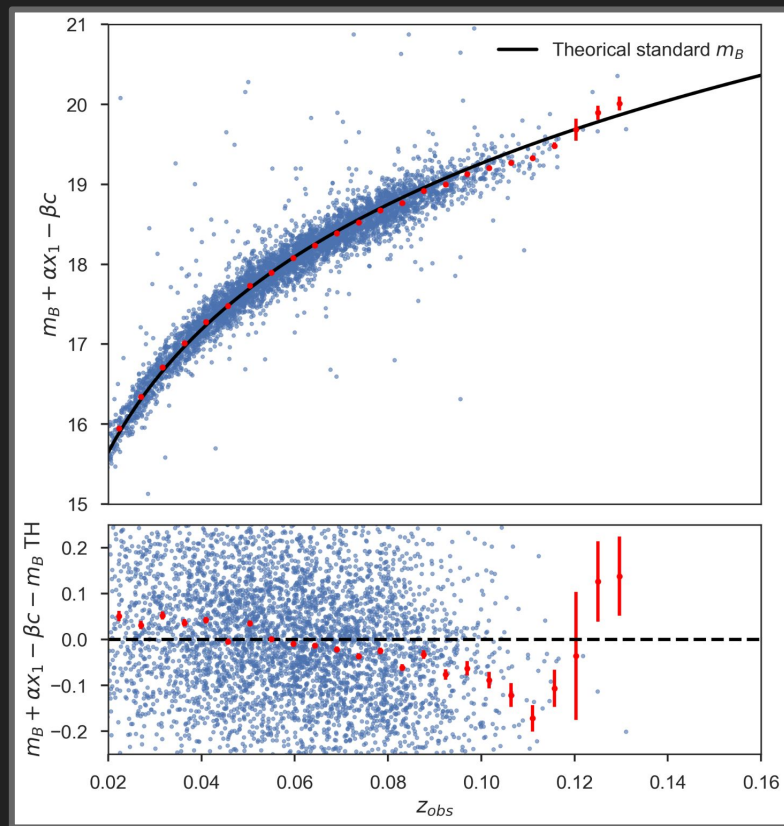
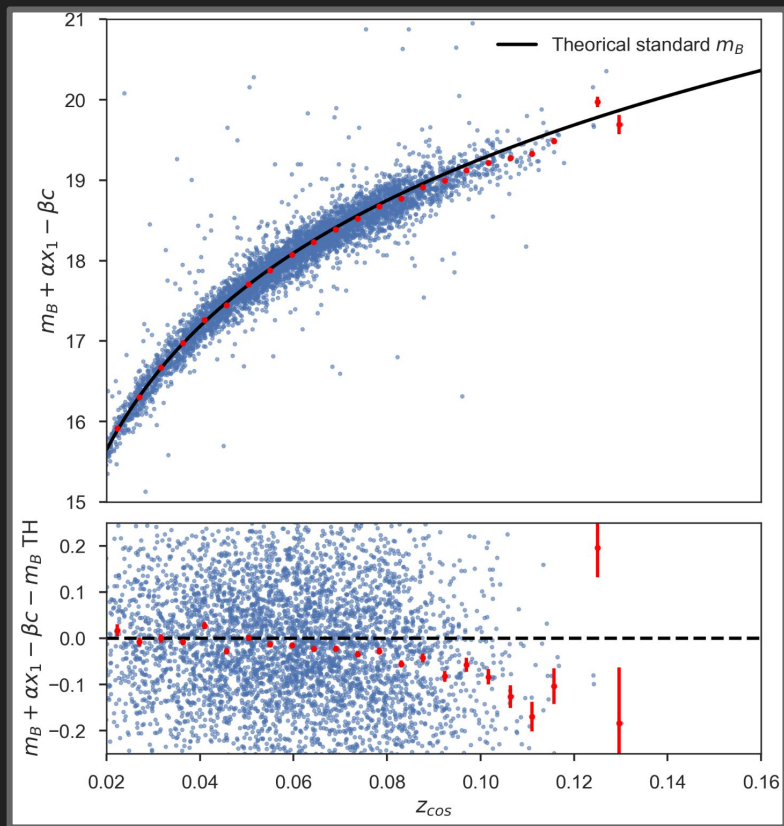
True values : $\alpha = 0.14$ $\beta = 2.9$ $M_0 = -19.1451$ $\sigma_M = 0.12$

Results on simulation : $\hat{\alpha} = 0.1453 \pm 0.0023$ $\hat{\beta} = 2.890 \pm 0.025$

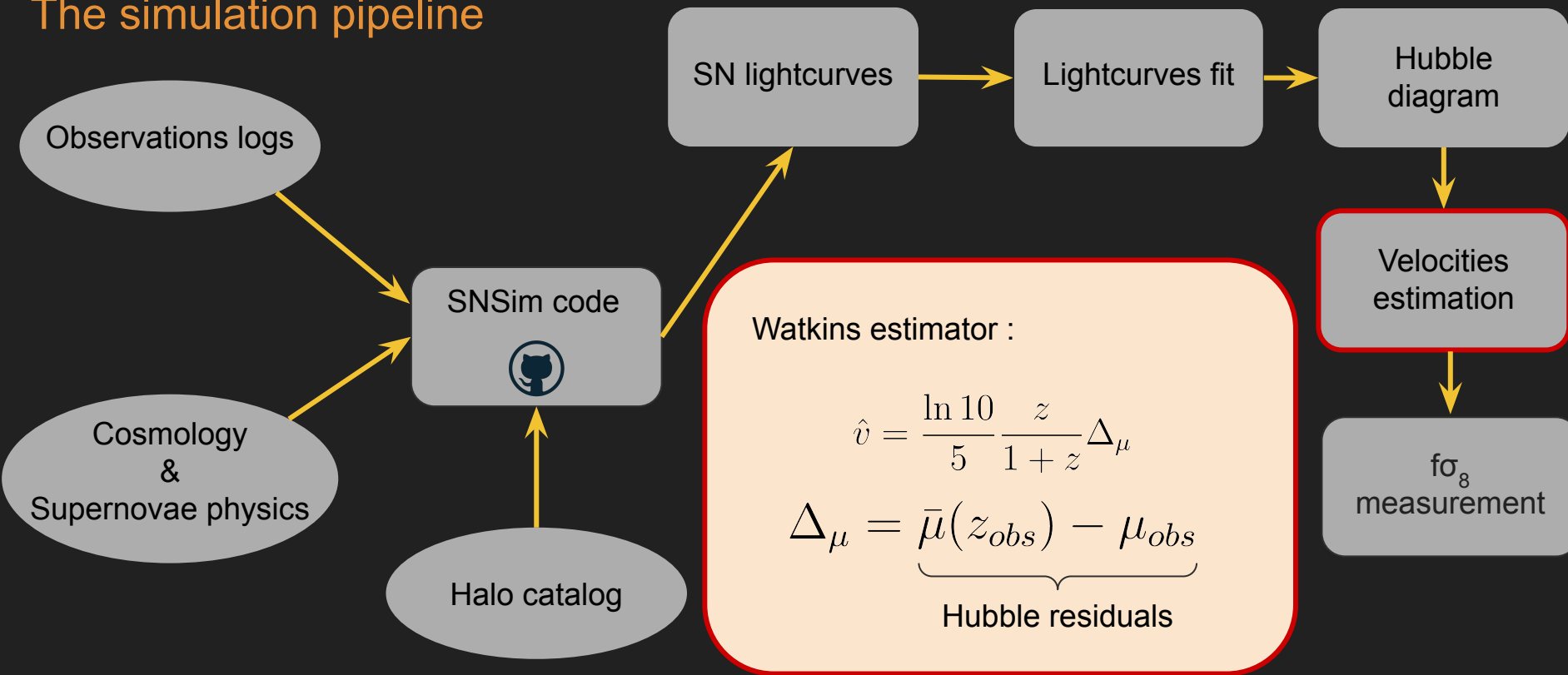
$\hat{M}_0 = -19.1654 \pm 0.022$ $\hat{\sigma}_M = 0.1211 \pm 0.0016$

The Hubble diagram after SALT fit

Selection bias appear at $z \sim 0.06$

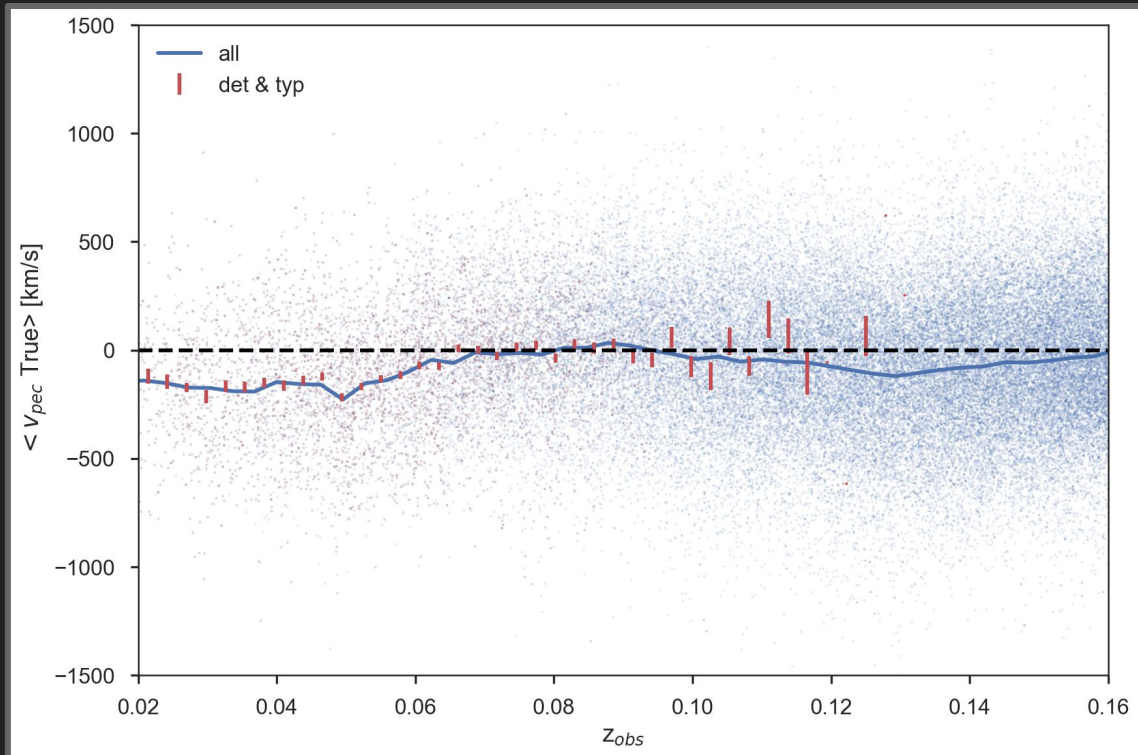


The simulation pipeline



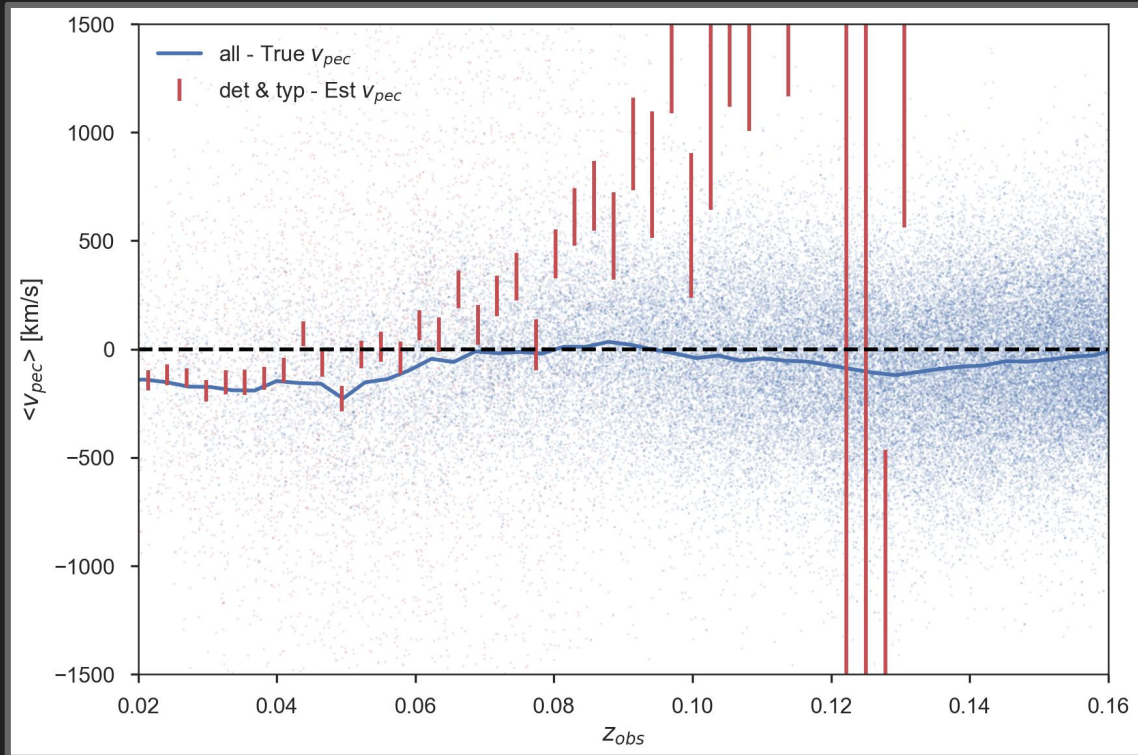
Velocities estimation from residuals

“No difference” between the true peculiar velocities of the full sample and of the selected sample...



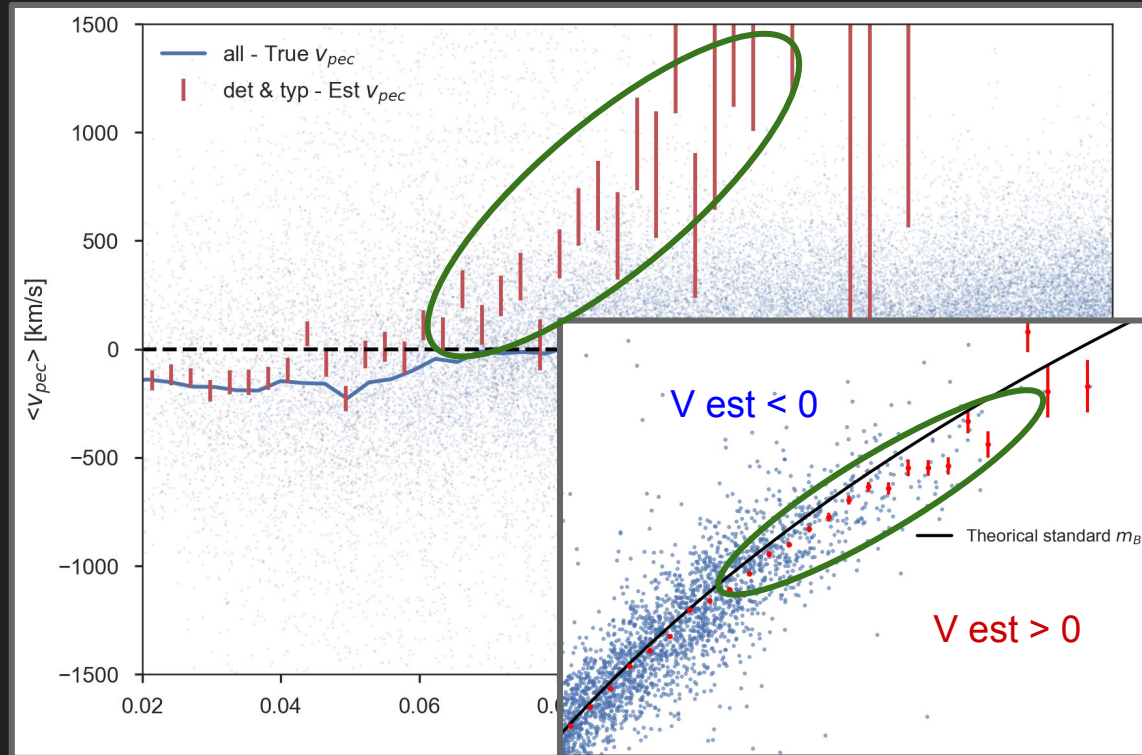
Velocities estimation from residuals

...But the mean of the estimate peculiar velocities are biased



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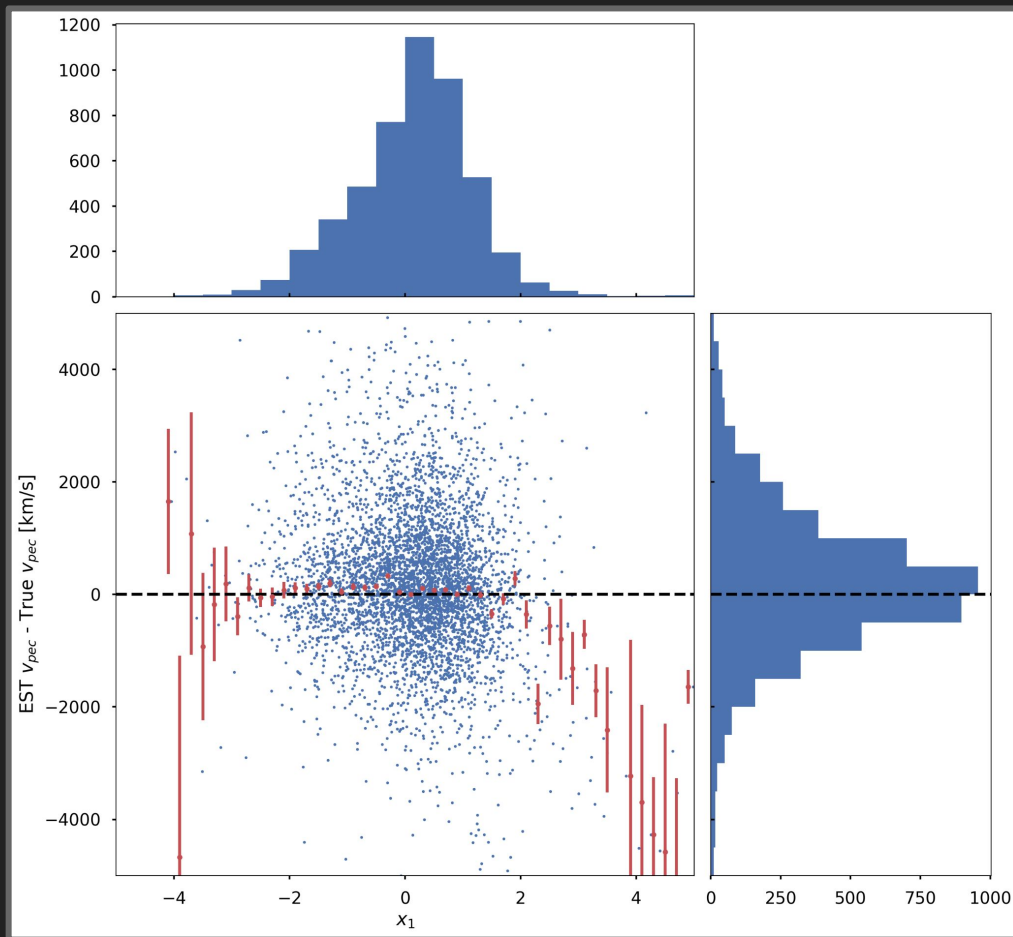
SALT x_1 effect on v_{pec} estimation

$+\alpha x_1 \rightarrow \mu \nearrow$



Over-estimate $x_1 \rightarrow$ Negative velocity

Under-estimate $x_1 \rightarrow$ Positive velocity



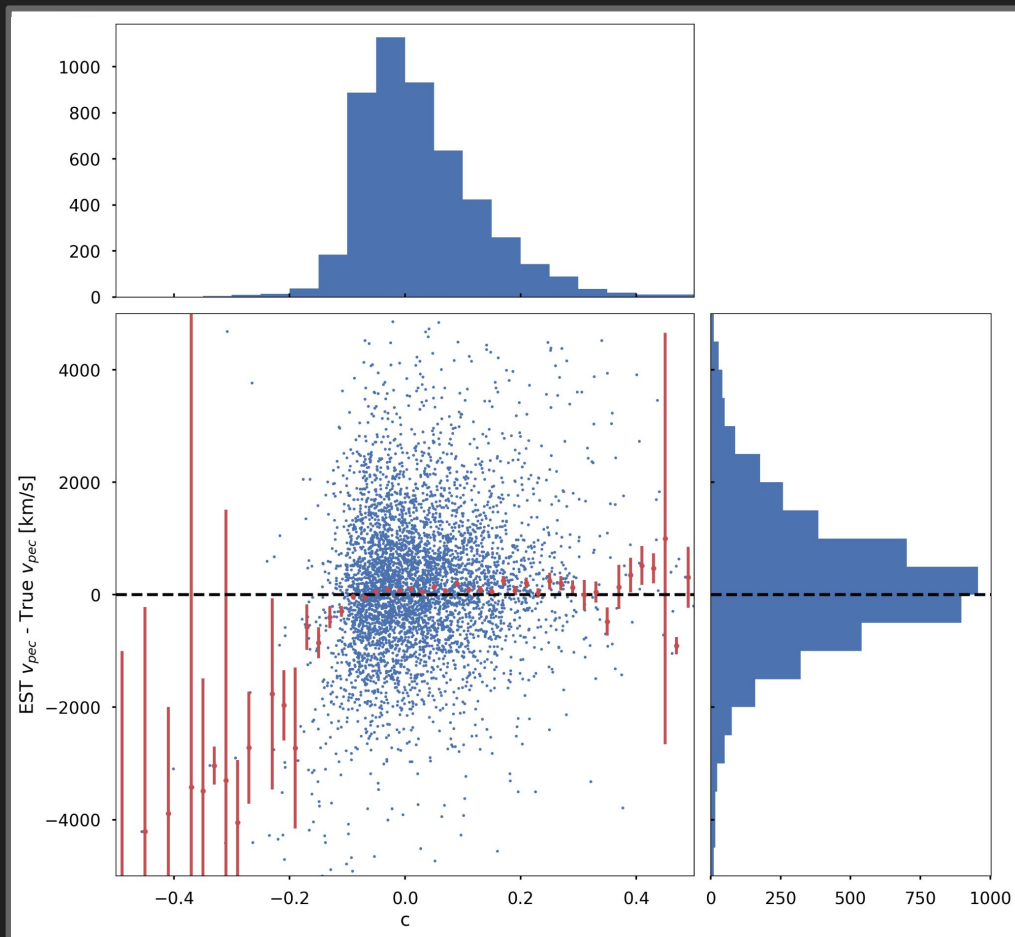
SALT c effect on v_{pec} estimation

$$-\beta c \rightarrow \mu \searrow$$



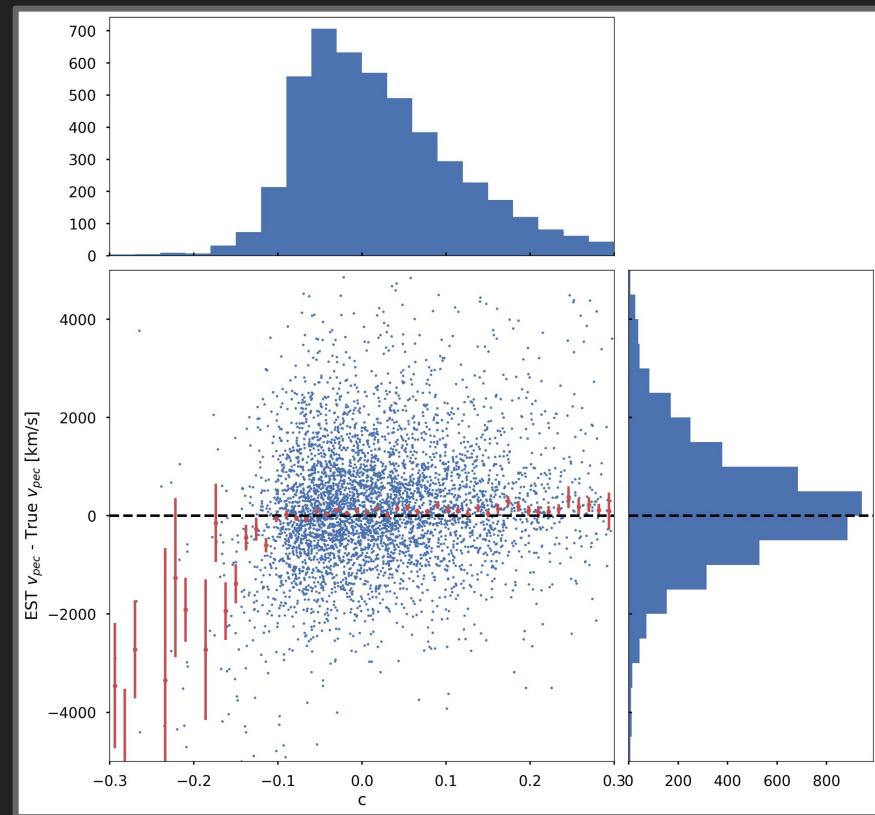
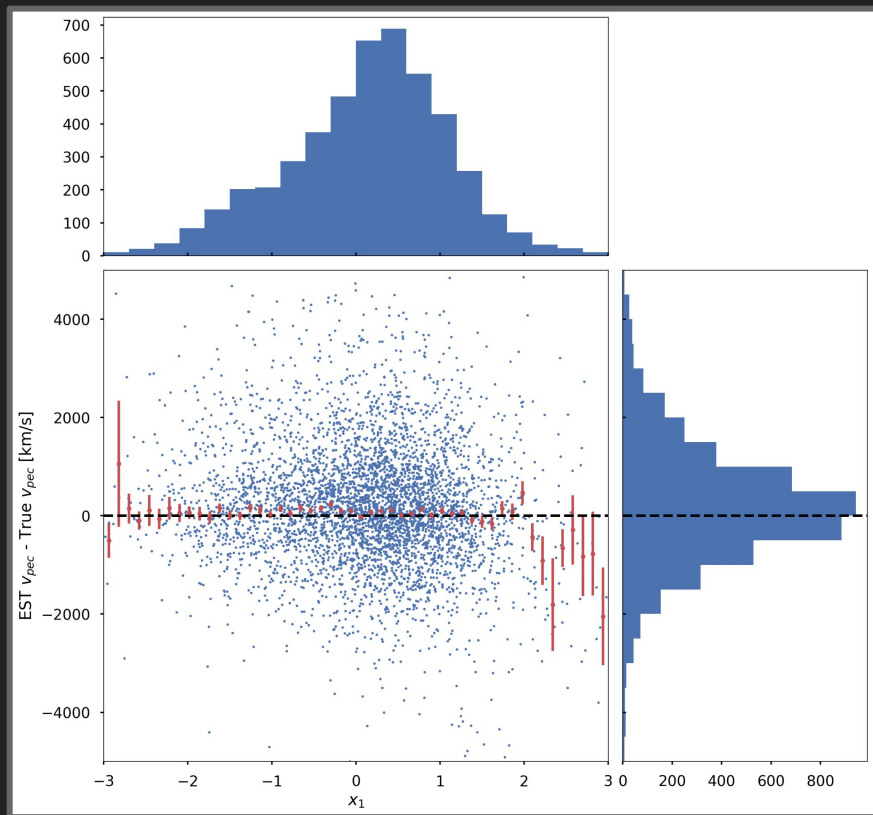
Over-estimate c \rightarrow Positive velocity

Under-estimate c \rightarrow Negative velocity

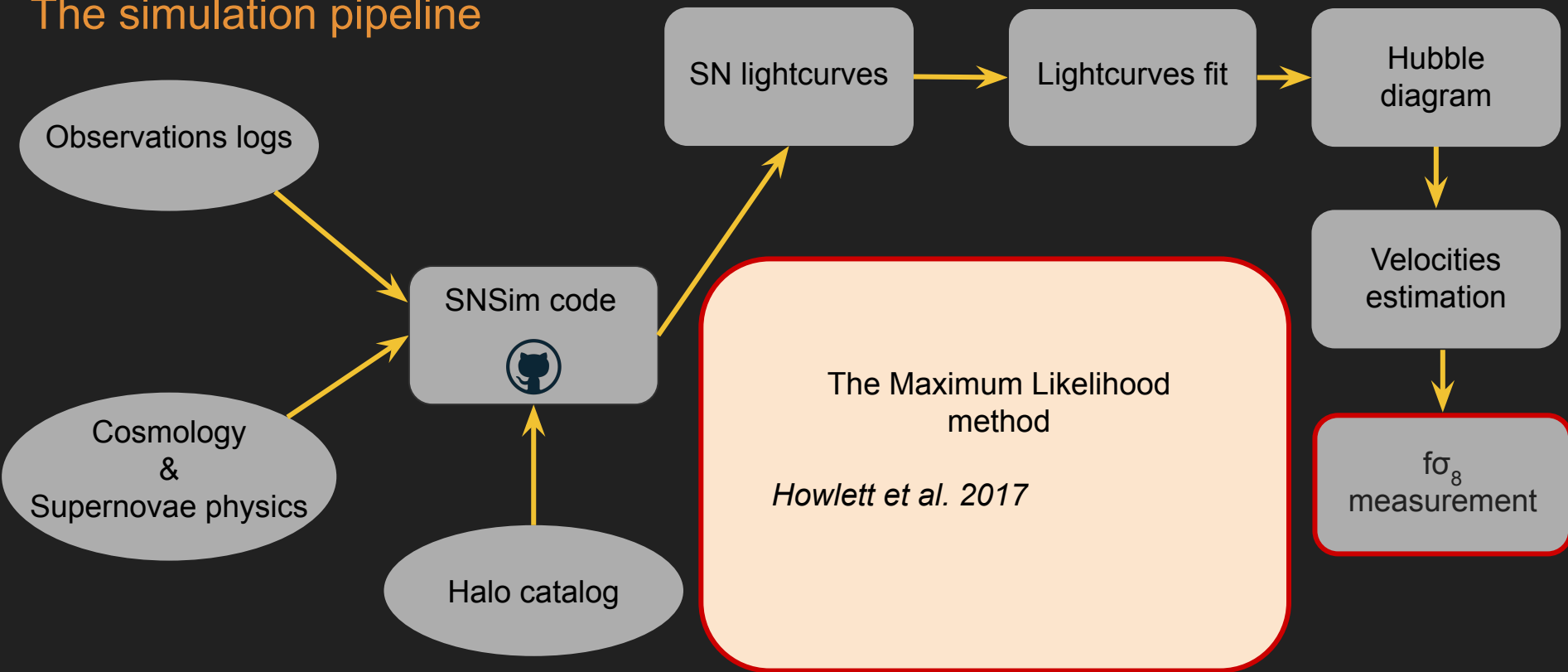


Velocities estimation from residuals

Apply ZTF - DR1 cuts $|x_1| < 3$ and $|c| < 0.3$



The simulation pipeline



Method we want to test : the maximum likelihood

From Howlett *et al.* 2017

$$\mathcal{L} = \frac{1}{(2\pi)^{\frac{n}{2}} \sqrt{|\mathbf{C}_{\text{tot}}|}} e^{-\frac{1}{2} \mathbf{v}^T \mathbf{C}_{\text{tot}}^{-1} \mathbf{v}}$$

Peculiar velocities

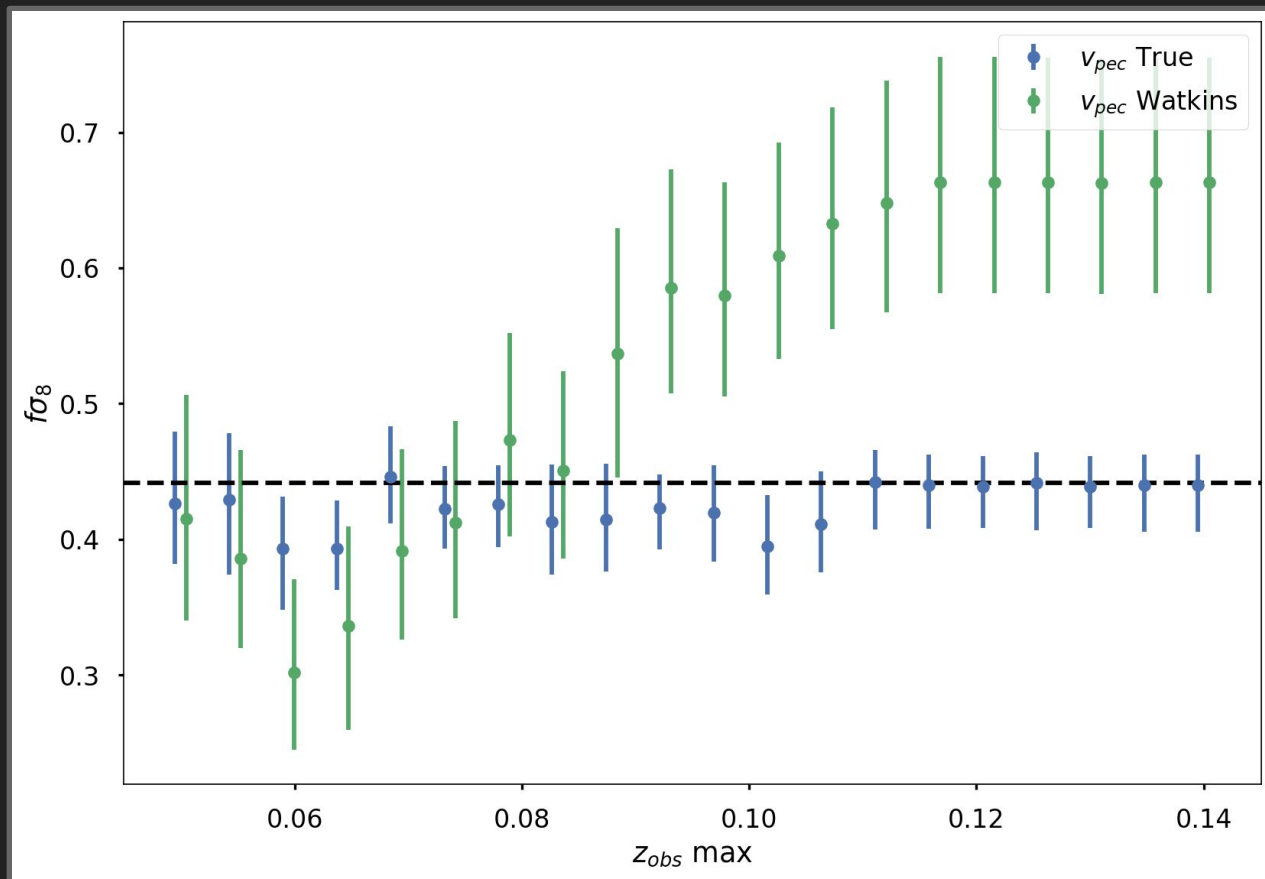
$$\mathbf{C}_{\text{tot}} = (f\sigma_8)^2 \mathbf{C}_{\text{cos}} + \mathbf{C}_{\text{obs}}$$

$f\sigma_8$ measurement

Fit with a binning grid of
 $80 \text{ Mpc}\cdot\text{h}^{-1}$

Effect of selection bias
appear after $z \sim 0.08$

Expected $f\sigma_8 = 0.441$



$f\sigma_8$ measurement

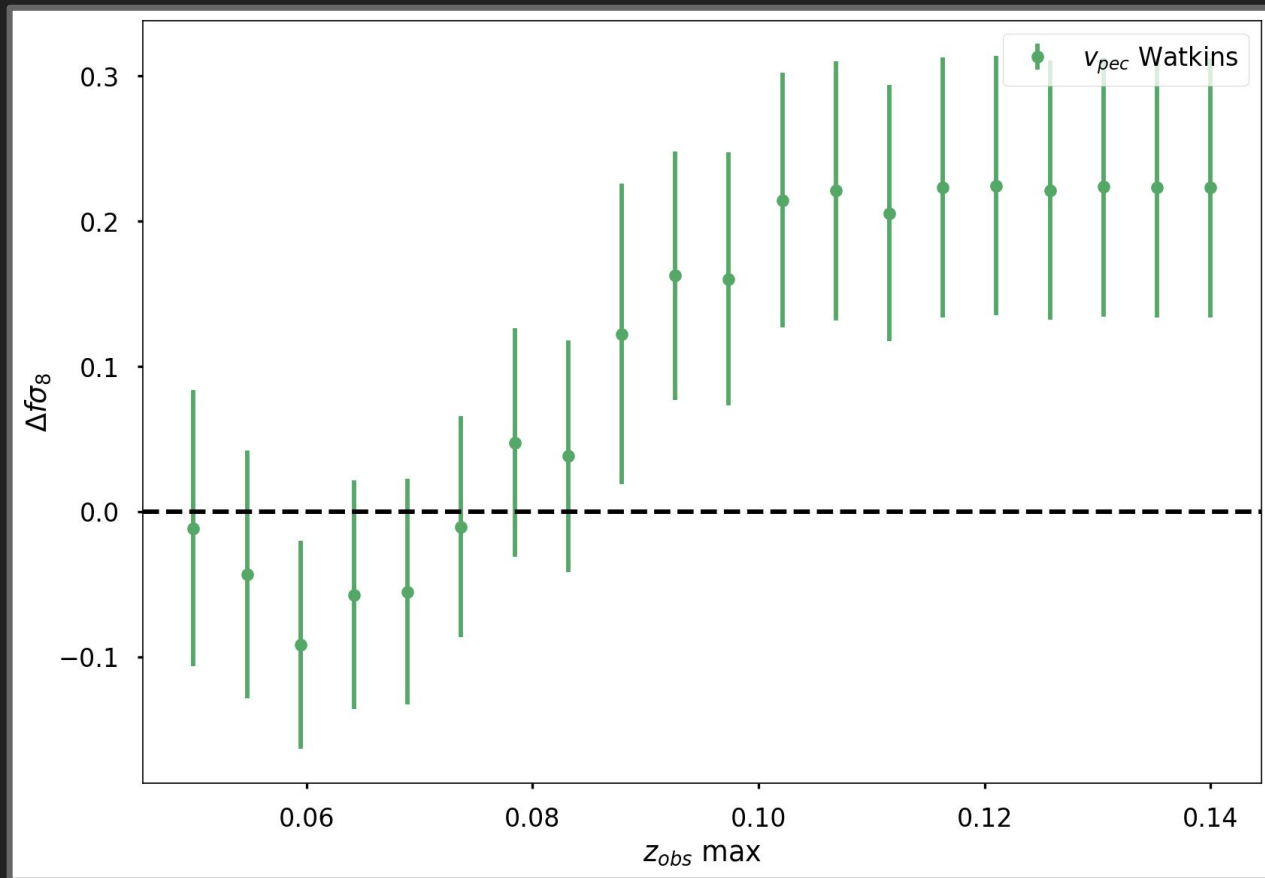
Fit with a binning grid of
80 Mpc.h⁻¹

Effect of selection bias
appear after $z \sim 0.08$

Expected $f\sigma_8 = 0.441$

Bias on $f\sigma_8 \sim 0.2$

$\Delta f\sigma_8 / f\sigma_8 \sim 45 \%$



Conclusion and future plan

- Using one mock we found that selection bias have a relative impact of $\sim 45\%$ on the measurement of $f\sigma_8$
- Preliminary result of $f\sigma_8 = 0.492 \pm 0.075$ using only SN with $z_{\text{obs}} < 0.08 \sim 4000$ SN
- We plan to make the same analysis for more mocks
- Validate the selection function
- Try to correct the bias

Thanks for your attention