



# MADNESS

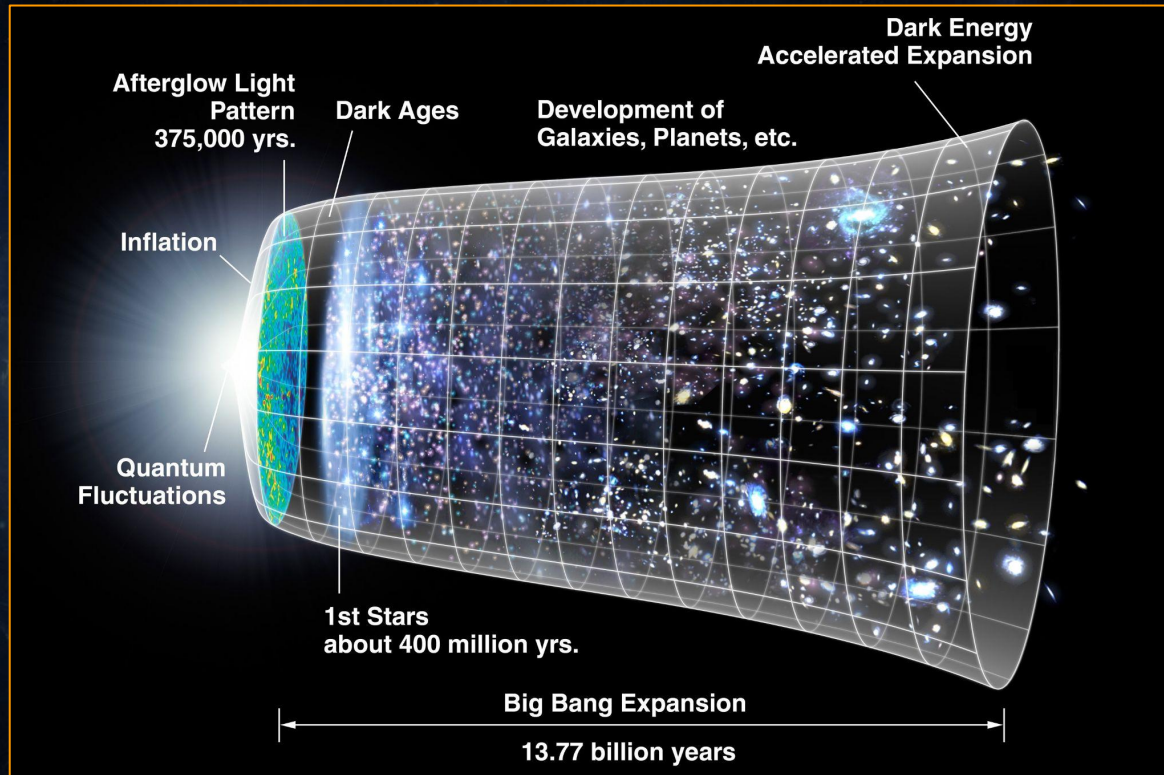
Maximum-**A**-posteriori solution with **D**eep generative **NE**tworks  
for **S**ource **S**eparation

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LSST France Meeting  
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# Dark Energy



Credits: NASA/WMAP Science Team



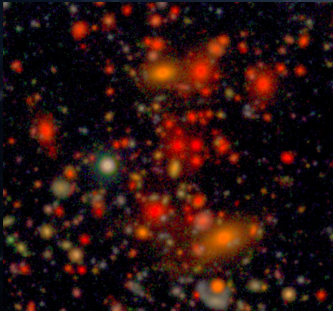
# Surveys and Challenges



Large survey of Space and Time (LSST) at Vera Rubin Observatory:

- Ground-based
- constrain Dark Energy
- 3.2 billion pixel camera
- 6 observation bands in visible range

more depth + area of coverage  $\Rightarrow$  More statistics!



HSC ultra-deep image

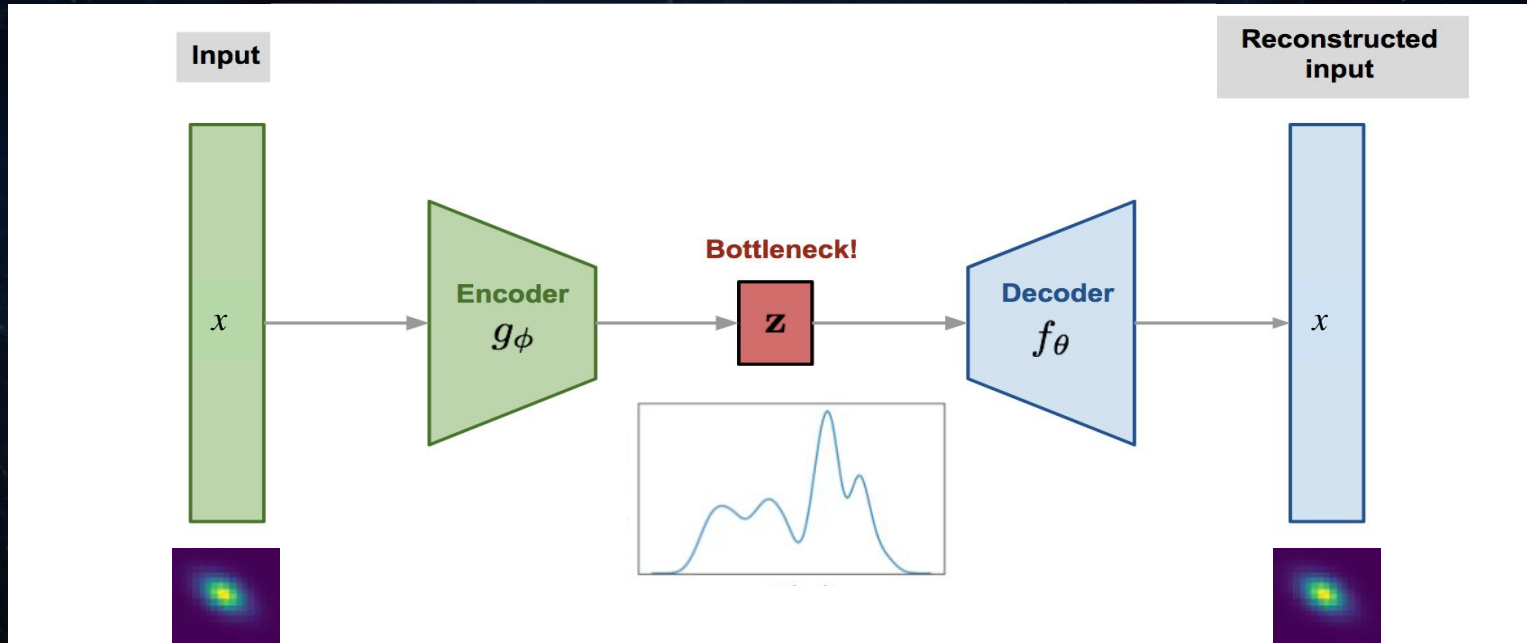
greater depth means more complex data!

~ Galaxies (60% in LSST ) are expected to overlap (**blending**) in images due to increased depth

# Why AI for deblending?

- Large data [billions of galaxies]
- Exploit advances in the field of image processing
- predict complex galaxy shapes
- Multi-band, multi-instrumental approach

# Train VAE as generative model

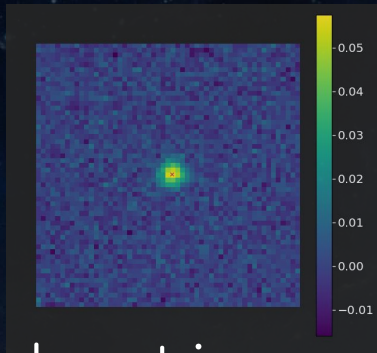


For example: Lanusse et al ([arXiv:2008.03833](https://arxiv.org/abs/2008.03833))  
Arcelin et al ([arXiv:2005.12039](https://arxiv.org/abs/2005.12039))

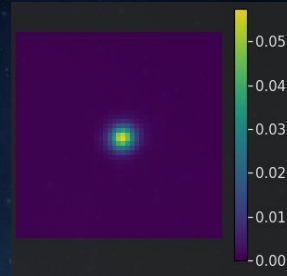
The VAE creates an underlying distribution from which galaxies are drawn!



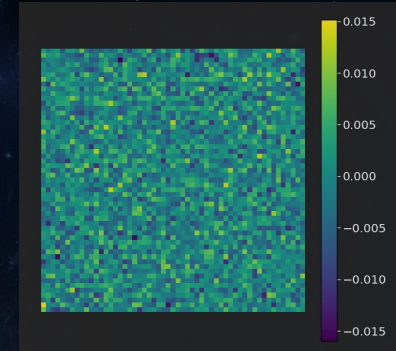
# Denoising (Single source)



Input image  
( $y$ )



Predicted image ( $x$ )



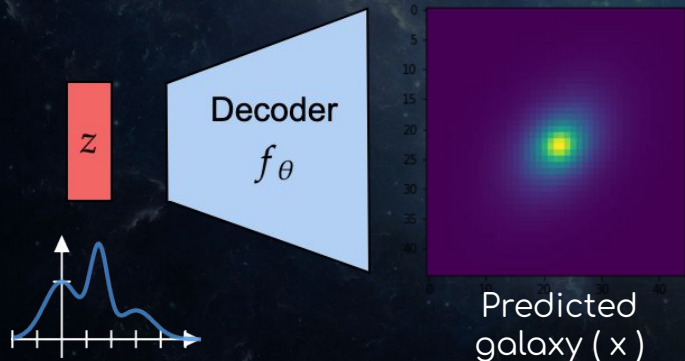
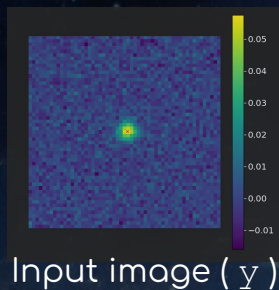
Residual ( $y-x$ )

$$x^* = \arg \min_x -\log p(y|x) - \log p(x)$$

$$x^* = \arg \min_x \frac{\|y - x\|^2}{2\sigma_{noise}^2} - \log p(x)$$

Where,  $x^*$  is the maximum a posteriori probability (MAP) estimate

# MAP estimate in latent space



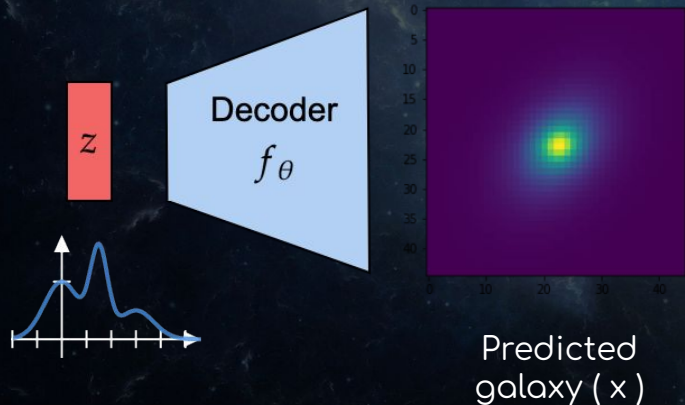
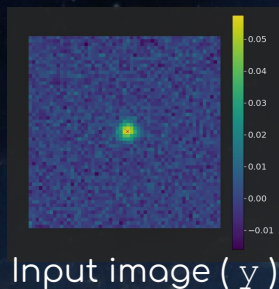
$$x^* = \arg \min_x - \frac{\|y - x\|^2}{2\sigma_{noise}^2} - \log p(x)$$

Going to the latent space

$$z^* = \arg \min_z \frac{\|y - f_\theta(z)\|^2}{2\sigma_{noise}^2} - \log p(z)$$

Where,  $z^*$  is the maximum a posteriori probability estimate in the latent space

# Minimization



- Start with random  $z$
- Do gradient descent in the latent space to minimize the objective function

$$z^* = \arg \min_z \frac{\|y - f_{\theta}(z)\|^2}{2\sigma_{noise}^2} - \log p(z)$$

Where,  $z^*$  is the maximum a posteriori probability estimate in the latent space



# Deblending (Multiple sources)

$$Z = \{z_i \mid z_i \text{ being the latent space representation of } i^{\text{th}} \text{ galaxy}\}$$

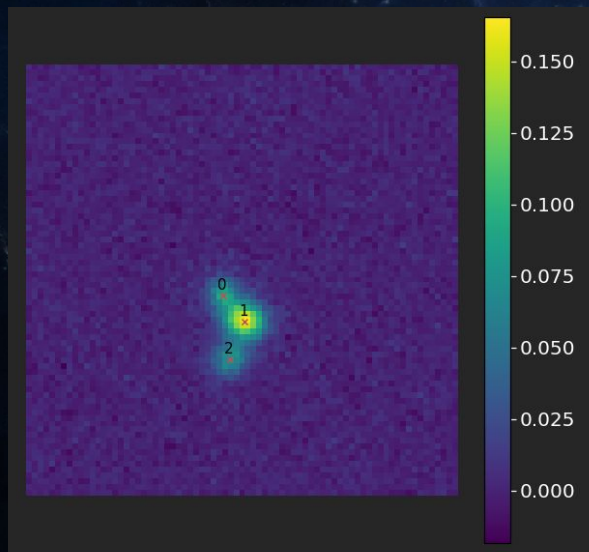
$$Z^* = \arg \min_Z -\log p(y|Z) - \log p(Z)$$

Reconstructed field

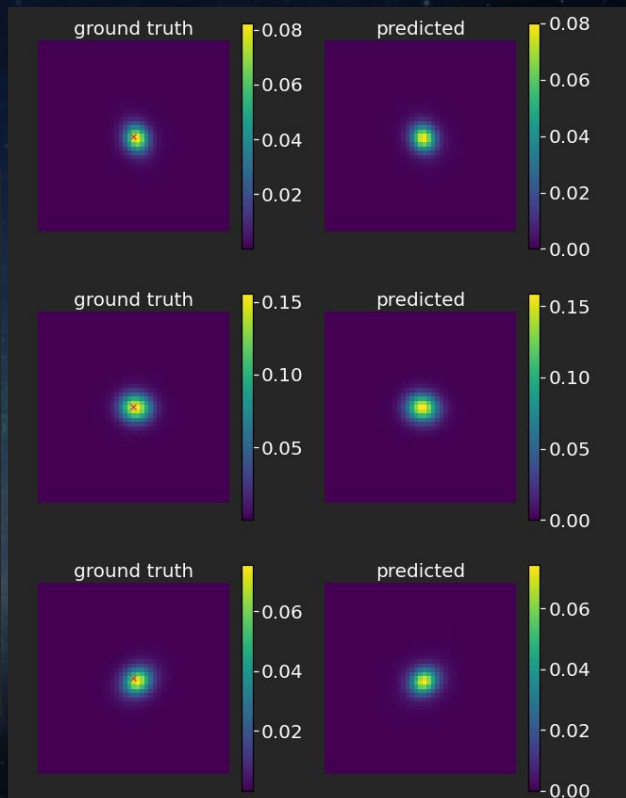
Probability that predictions are galaxies!

$$Z^* = \arg \min_Z \frac{\|y - \sum_i f_\theta(z_i)\|^2}{2\sigma_{\text{noise}}^2} - \sum_i \log p(z_i)$$

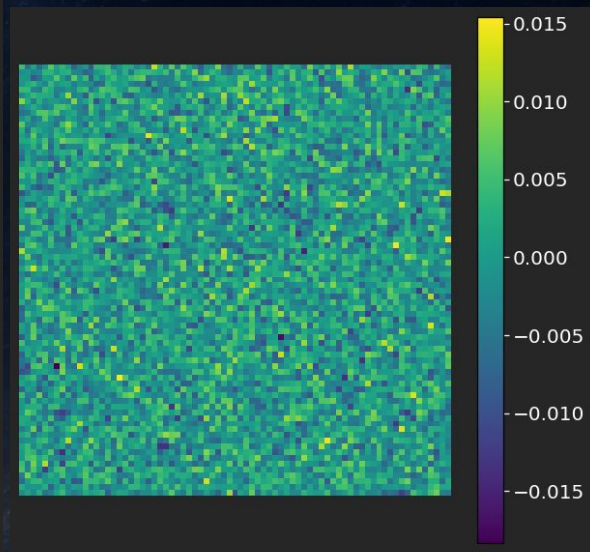
# Deblending Example



Input image



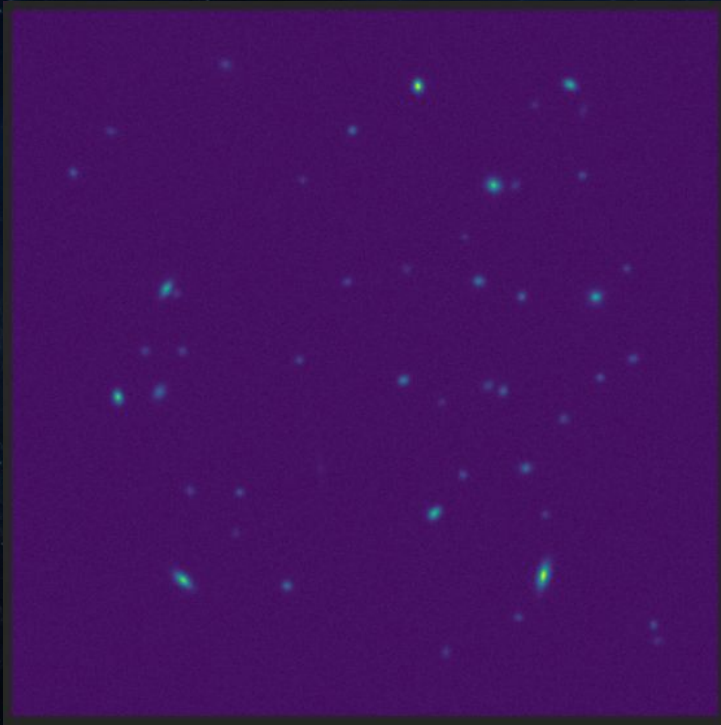
Predictions



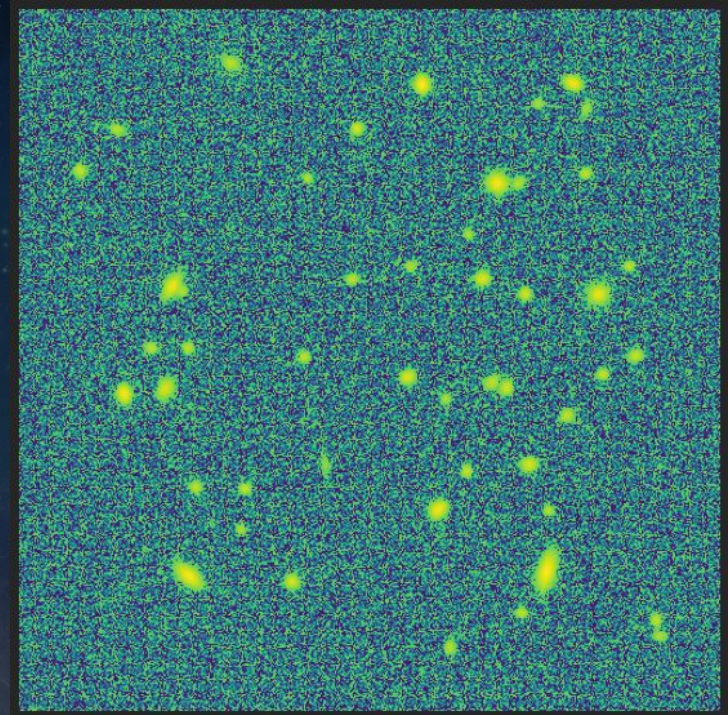
Residual image  
(input - predictions)



# Moving to a larger field...



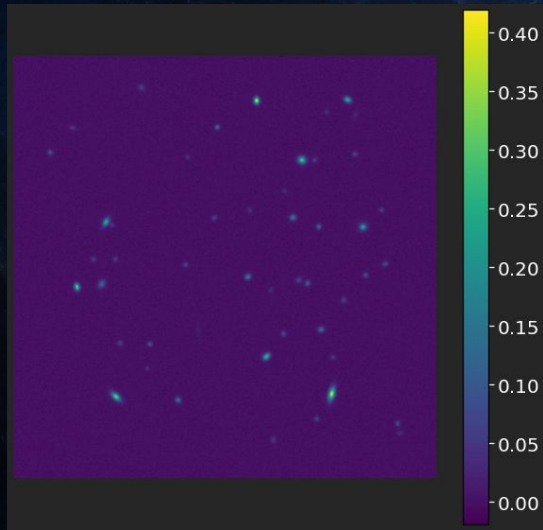
Input field



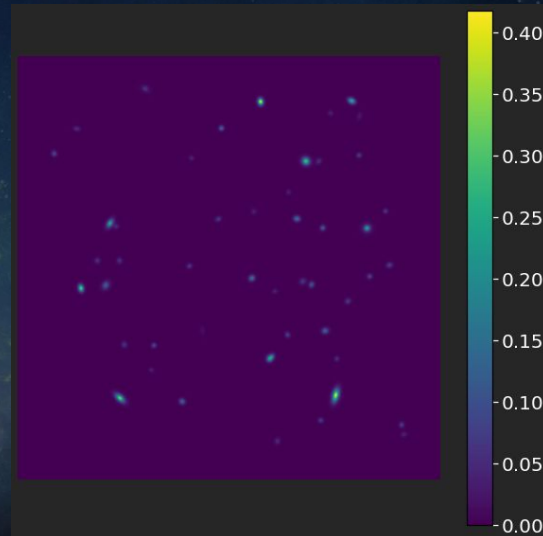
$\text{Sinh}^{-1}$ ( Input field )



# Moving to a larger field...

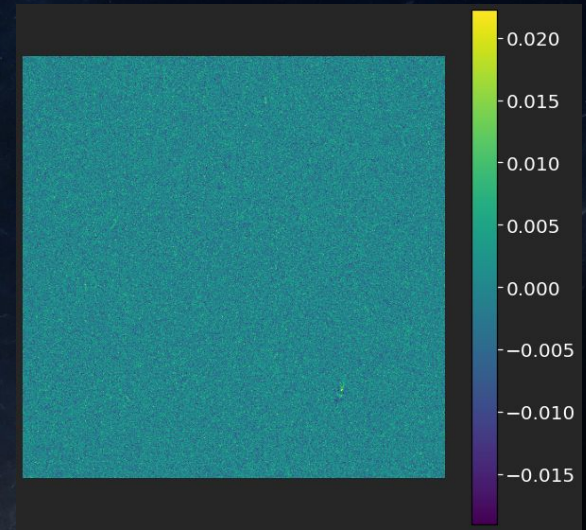


Input field



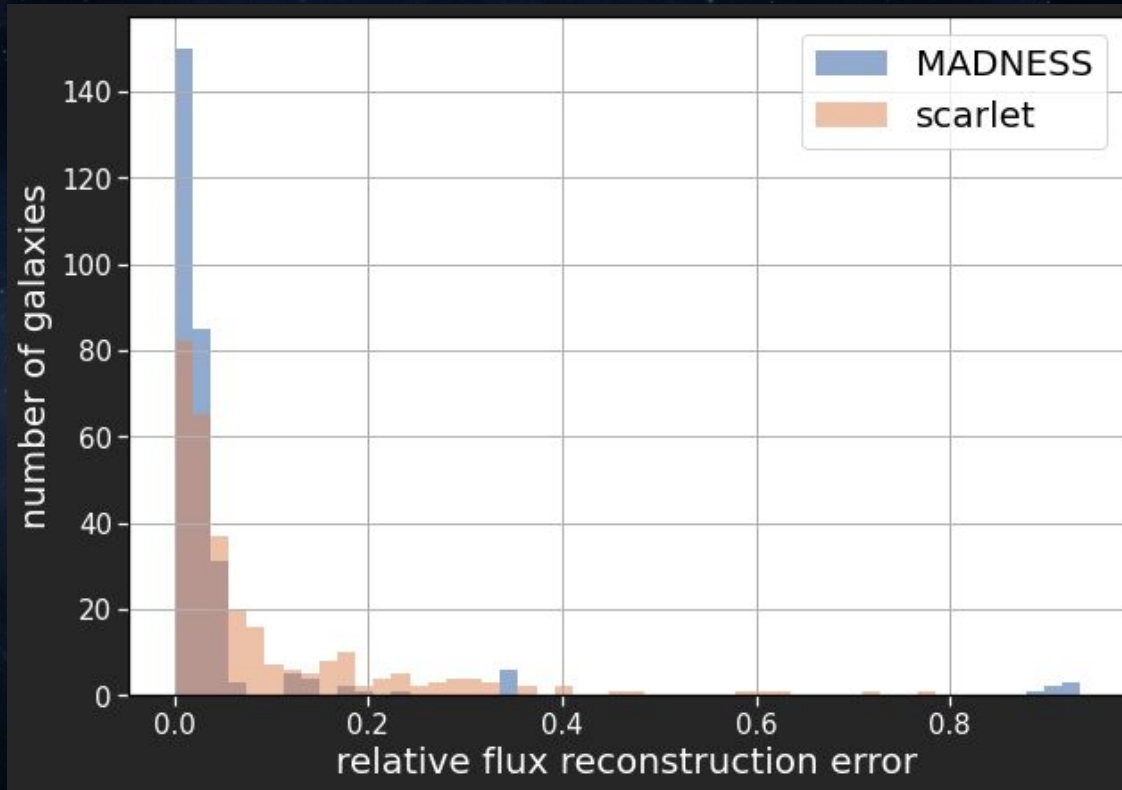
predicted field

Preliminary results\*



residual field  
(Input - predicted)

# Compare with scarlet



Preliminary results\*

# Conclusion and Future work

- Encouraging initial results!
- Time to get back to the basics (network architecture, loss function...)
- Choose metrics to evaluate the deblending results. (Flux reconstruction, SSIM...)
- Real data?





Thank you!