



# Gravitational waves: Opening a new window on the universe

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GraSPA summer school 2022

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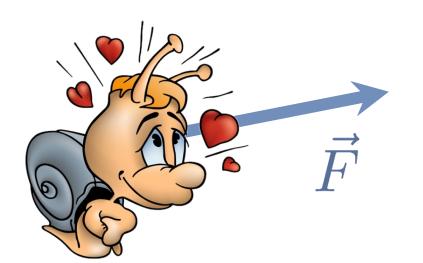
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# **Gravitation: the classical theory**

SIR ISAAC HEWTON (443-1127)

- Flat space, absolute time
- Instantaneous interaction between distant masses

$$\vec{F} = G \cdot m_1 m_2 \cdot \frac{1}{r^2} \cdot \vec{u}$$

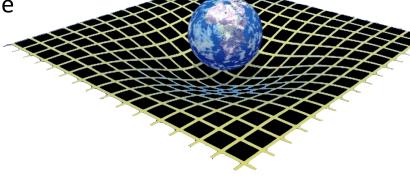




# **Gravitation: the modern theory**

- Theory of General Relativity (GR)
- Einstein 1915-1918: geometric theory of gravitation
- A mass "bends" and "deforms " space-time

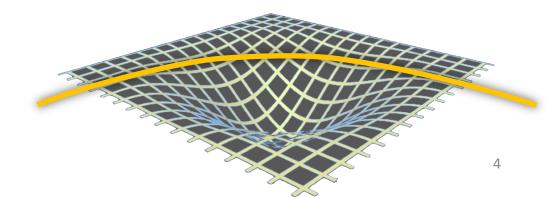




The trajectory of a mass is influenced by the curvature of space-time

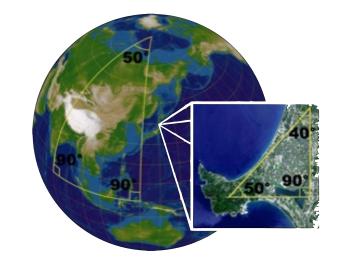


J. A. Wheeler: "Space tells matter how to move and matter tells space how to curve"



# Theoretical piece: curved space

- What is a curved space ? ( = "manifold" )
  - examples : sphere, saddle
- Can we measure curvature ?
  - we cannot see our space from "outside"
  - but we can measure angles
  - ▶ the sum of the angles of a triangle is not always equal to  $\pi$ !

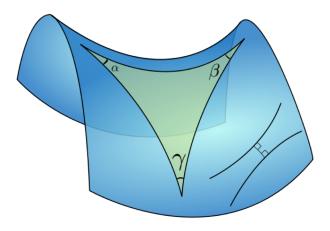


positive curvature

$$\sum \text{angles} = \alpha + \beta + \gamma > \pi$$

negative curvature

$$\sum \text{angles} = \alpha + \beta + \gamma < \pi$$



# Theoretical piece: curved space-time

- In General Relativity
  - space is curved and time is defined locally
  - one cannot go "out" to see the curvature
    - "intrinsically" curved space
      => intrinsic curvature

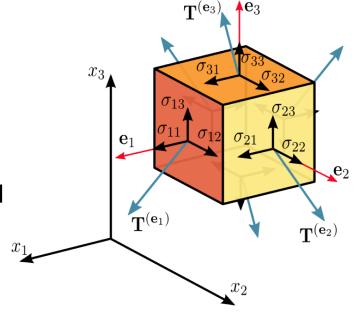


- go straight (free fall) = follow a "geodesic"
- note that the time is also curved!
- as a first approximation, finds the results (trajectories) of newtonian mechanics

# Theoretical piece: tensors

- ► Tensor = mathematical object
- Does not depend on the coordinate system
- Extends the notion of vector
- In a specific coordinate system, multidimensional array
- Example: electrical conductivity of an anisotropic cristal

$$j^i = \sigma^i_j E^j$$



Note: summation is implicit over repeated indices (Einstein convention)

$$\sigma_j^i E^j \equiv \sum_j \sigma_j^i E^j$$

# Theoretical piece: the metric tensor

- In space-time, need to measure
  - the distance between two points
  - the angle between two vectors
- Measure of the distance between two infinitesimally close events in spacetime
- Need a "metric", start from the "line element" seen in special relativity:

$$ds^2 = -dt^2 + dx^2 + dy^2 + dz^2$$
 with c = 1!

$$lacksquare Mhich can be written$$
  $ds^2 = \eta_{lphaeta} dx^lpha dx^eta$ 

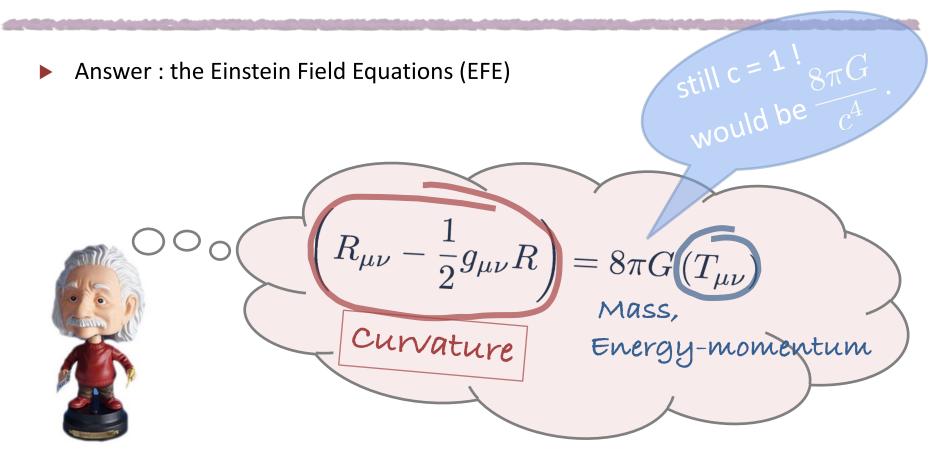
$$\eta_{\mu\nu} = \left( egin{array}{cccc} -1 & 0 & 0 & 0 \ 0 & 1 & 0 & 0 \ 0 & 0 & 1 & 0 \ 0 & 0 & 0 & 1 \end{array} 
ight) \qquad ext{and} \qquad dx^0 = dt, \quad dx^1 = dx, \ dx^2 = dy, \quad dx^3 = dz$$

lacksquare  $\eta_{\mu
u}$  is the metric of a flat spacetime, the Minkowski spacetime, used in special relativity

# Theoretical piece: the metric tensor

- What if space is not flat ?
- lacktriangle The metric can be general :  $g_{\mu
  u}$
- It contains all information about spacetime curvature
- It is a rank 2 tensor
- $\blacktriangleright$  The curvature is also defined by another tensor, which depends on  $g_{\mu\nu}$  and its derivatives: the Ricci tensor  $R_{\mu\nu}$
- But what relates deformation of space-time and energy-momentum ?

# The Einstein Field Equations



- Energy-momentum bends spacetime
  - Deformation ? => change of distance btw objects
- Spacetime tells mass (energy momentum) how to move
- These equations are non-linear

# From Einstein Field Equations to Gravitational Waves

- Start from a flat space-time = Minkowski metric
  - lacktriangledown Add a perturbation  $h_{\mu
    u}$  to the metric :  $\,g_{\mu
    u}=\eta_{\mu
    u}+h_{\mu
    u}$
  - Linearize Einstein Field Equations  $(h_{\mu\nu}\ll 1)$
  - Choose a suitable coordinate system (« Transverse Traceless » or TT gauge)
- Obtain a wave equation

$$(
abla^2-rac{1}{c^2}rac{\partial^2}{\partial t^2})h_{\mu
u}=0$$
 (in vacuum, no  $T_{\mu
u}$  )

Which solution is

$$h_{\mu\nu} = A_{\mu\nu} \cdot e^{-i(\vec{k}\cdot\vec{x} - \omega \cdot t)}$$

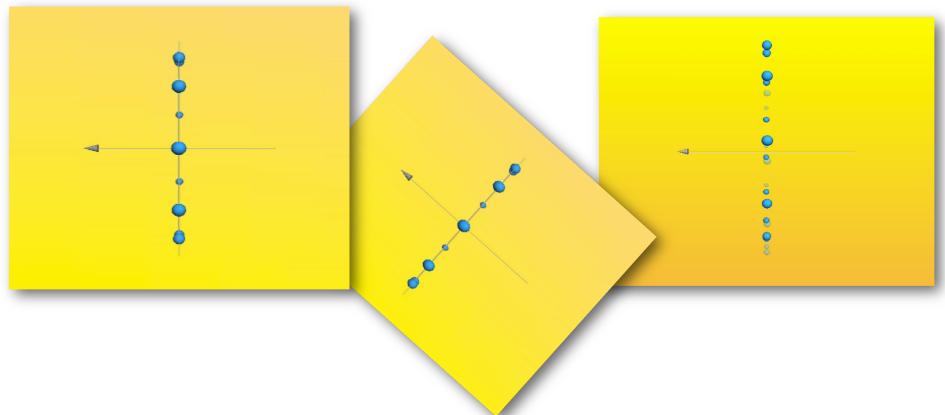
## **Gravitational waves: effect on matter**

$$h_{\mu\nu} = A_{\mu\nu} \cdot e^{-i(\vec{k}\cdot\vec{x} - \omega \cdot t)}$$

- Transverse plane wave
- Propagating at the speed of light
- Two states of polarization: + and x

# **Gravitational waves: effect on matter**

► Effect on free falling masses (test masses) in circle:



Masses always in free fall => only distances are changing

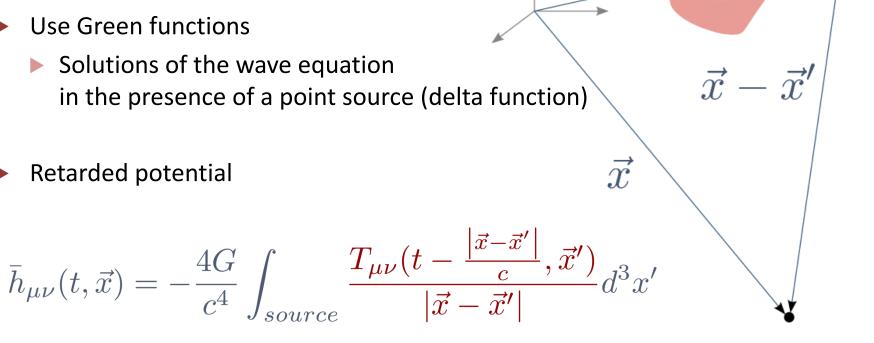
# **Gravitational waves: generation**

Linearized Einstein equations with a stress-energy tensor (source term)

$$\Box \bar{h}_{\mu\nu} = -\frac{16\pi G}{c^4} T_{\mu\nu}$$

- Use Green functions
  - Solutions of the wave equation in the presence of a point source (delta function)
- Retarded potential

$$\bar{h}_{\mu\nu}(t,\vec{x}) = -\frac{4G}{c^4} \int_{source} \vec{x} dt$$



extended source of GW

# **Gravitational waves: generation**

- Approximations :
  - isolated source
  - compact source
  - observer far from the source (  $R=|\vec{x}-\vec{x}'|$  >> typical size of the source)
- Amplitude of the wave written as a function of

$$\bar{h}_{ij}(t) = \frac{2G}{Rc^4} \frac{d^2I_{ij}}{dt^2} \left(t - \frac{R}{c}\right) \qquad \begin{array}{l} I_{ij} = \text{reduced quadrupolar} \\ \text{moment of the source} \\ = \int_{source} d\vec{x} \; x_i x_j \; T_{00}(t, \vec{x}) \\ \frac{G}{c^4} \approx 8.24 \times 10^{-45} \; \text{s}^2 \cdot \text{m}^{-1} \cdot \text{kg}^{-1} \end{array}$$

Remark:

Need a quadrupolar moment to generate a GW, the dipolar case is impossible (because of momentum conservation).

# Orders of magnitude

► Amplitude:

$$h \approx \frac{G}{c^4} \cdot \frac{\ddot{I}}{R}$$

- Example with two orbiting objects : a binary system
  - ightharpoonup M = total system mass, r = distance between the components
  - ▶ R = observer system distance
  - $lacksquare I pprox M.r^2$  hence  $\ddot{I} pprox M \cdot v_{NS}^2 pprox E_c^{NS}$ 
    - where NS is the part of the source motion without spherical symmetry
- Hence

$$h \approx \frac{G}{c^4} \cdot \frac{E_c^{NS}}{R}$$

# Orders of magnitude

- ightharpoonup Luminosity:  $L_{GW} pprox rac{G}{c^5} \cdot \ddot{I}^2$
- lacktriangledown Reminder:  $\ddot{I} pprox E_c^{NS}$  hence  $\dddot{I} pprox E_c^{NS}/T$ 
  - ► T = characteristic time of energy-momentum (or mass) motion from one side of the system to the other
- ► In case of a transient, violent event

$$L_{GW} pprox rac{G}{c^5} \cdot \ddot{I}^2 pprox rac{G}{c^5} \cdot \left(rac{E_c^{NS}}{T}
ight)^2$$

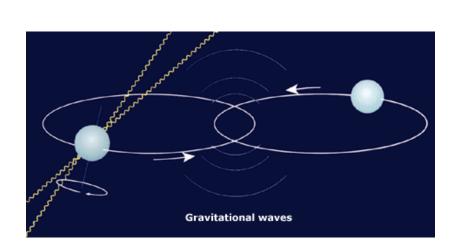
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For a quasi-stationary dynamics

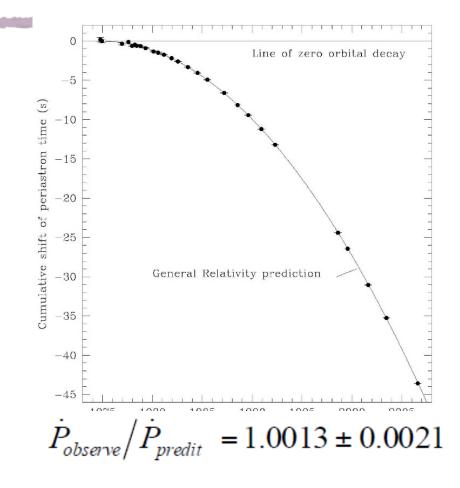
$$L_{GW} pprox rac{G}{c^5} \cdot \ddot{I}^2 pprox rac{c^5}{G} \cdot \left(rac{GM}{c^2R}
ight)^2 \cdot \left(rac{v_{NS}}{c}
ight)^6$$

where one may introduce the Schwarzschild radius  $R_S = rac{2GM}{c^2}$ 

## Indirect evidence: PSR 1913+16



- Binary system of neutron stars
- One neutron star is a radio pulsar
- ▶ Discovered in 1975 by Hulse and Taylor
- Studied by Taylor, Weisberg and co.
- Decay of the orbital period compatible with GW emission
- ▶ Frequency of GW emitted by PSR 1913+16: ~ 0.07 mHz
  - Undetectable by ground-based detectors (bandwidth 10 Hz- 10 kHz)

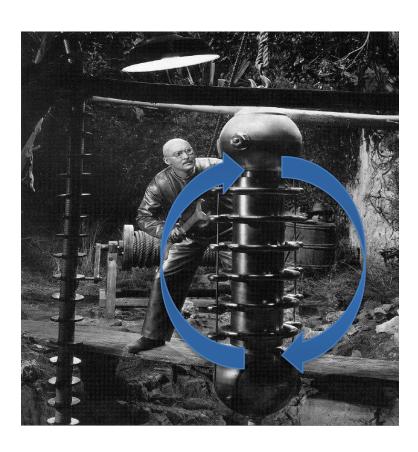


# Orders of magnitude

Mass distribution : needs a quadrupolar moment







Examples for a binary system

$$h \approx 32\pi^2 \cdot \frac{G}{c^4} \cdot \frac{1}{R} \cdot M \cdot r^2 \cdot f_{orb}^2$$

M = 1000 kg, r = 1 m, f = 1 kHz,R = 300 m

$$h \sim 10^{-35}$$

M = 1.4  $M_{\odot}$ , r = 20 km, f = 400 Hz, R = 10<sup>23</sup> m (15 Mpc = 48,9 Mlyr)  $h \sim 10^{-21}$ 

# **Astrophysical sources**

Need high masses and velocities : astrophysical sources

#### Binary system

- Need to be compact to be observed by ground based detectors
   → Neutron stars, black holes
- Signal well modeled but rates not well known... yet

#### Spinning neutron stars

- Nearly monotonic signals
- Long duration
- Strength not well known

#### Asymmetric explosion

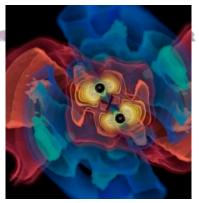
- Ex: core collapse supernovae
- « burst » transient
- Not well modeled

#### Gravitational wave background

- First type : superposition of many faint sources
- Second type : Residue of the Big Bang or Inflation
- Stochastic in nature



Casey Reed, Penn State

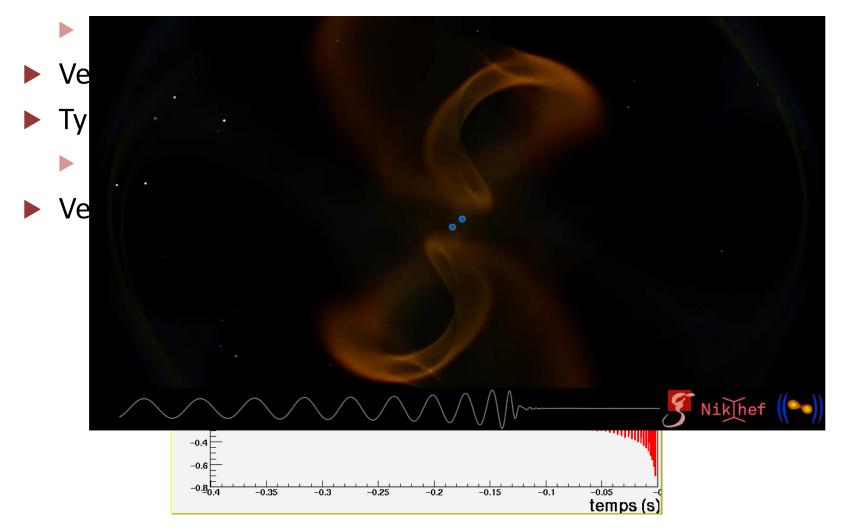


Credit: AEI, CCT, LSU



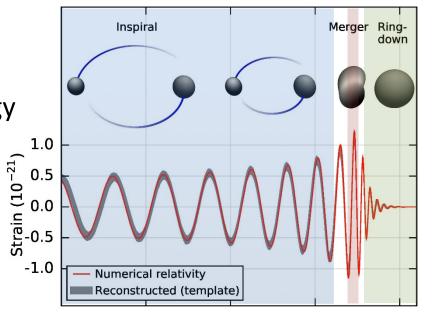


Binary systems of compact stars at the end of their evolution



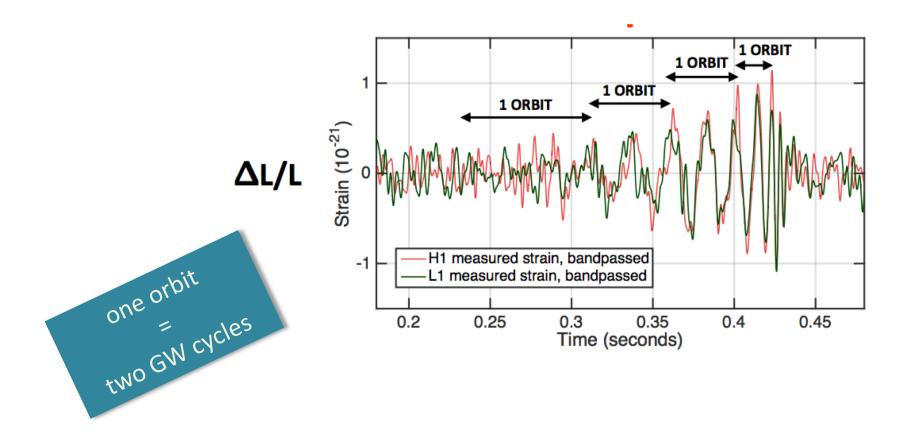
- System may be binary neutron stars (BNS), binary black holes (BBH) or NS-BH
- Phases of the coalescence
- Inspiral
  - Masses m1 and m2 orbit each other
  - GW emission -> system looses energy
  - ► => Frequency ¬, amplitude ¬
  - Waveform characterised by a « chirp mass »

$$\mathcal{M} = \frac{(m_1 m_2)^{3/5}}{(m_1 + m_2)^{1/5}} = \frac{c^3}{G} \left[ \frac{5}{96} \pi^{-8/3} f^{-11/3} \dot{f} \right]^{3/5}$$

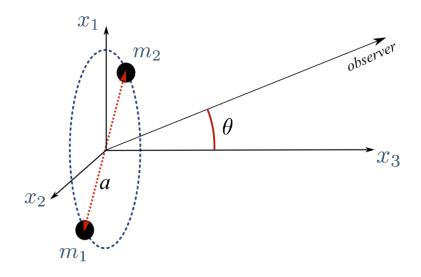


- Merger: computed numerically (numerical GR)
- ► Ringdown: quasi-normal modes decomposition

#### First detection : GW150914



► For the sake of simplicity, let's take a simple system :

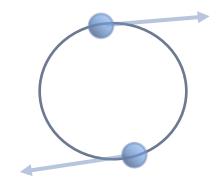


- lacksquare Masses  $m_{1}$  and  $m_{2}$ , total mass  $M=m_{1}+m_{2}$ , reduced mass  $\mu=rac{m_{1}m_{2}}{M}$
- ▶ Distance between stars: *a*, take circular orbits
- lacktriangle Compute  $h_+$  and  $h_ imes$  , the amplitude of the two modes of the emitted wave seen by an observer situated at a distance  $R\gg a$

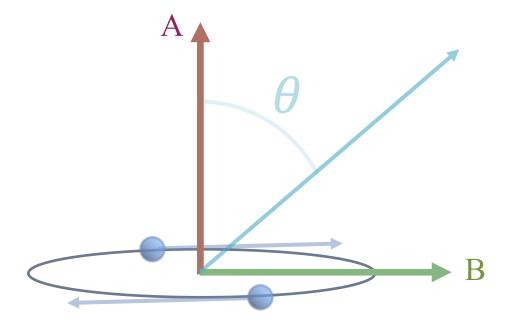
Understanding the two polarization amplitudes

$$h_{+}(t) = \frac{4G\mu a^2 \omega^2}{Rc^4} \frac{1 + \cos^2 \theta}{2} \cos 2\omega t$$

$$h_{\times}(t) = \frac{4G\mu a^2 \omega^2}{Rc^4} \cos\theta \sin 2\omega t$$



Observer A :  $\cos \theta = 1$  sees the two polarizations





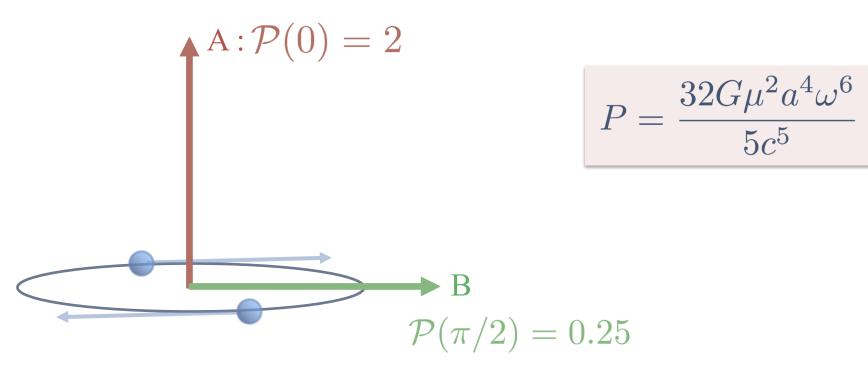
sees a linear polarization

Radiated power per unit solid angle

$$\frac{dP}{d\Omega} = \frac{2G\mu^2 a^4 \omega^6}{\pi c^5} \mathcal{P}(\theta)$$

$$\mathcal{P}(\theta) = \frac{1}{4} (1 + 6\cos^2\theta + \cos^4\theta)$$

Radiated power non zero whatever the direction of emission



- Some examples
- Sun-Jupiter system

$$m_J = 1.9 \times 10^{27} \text{kg}, \quad a = 7.8 \times 10^{11} \text{m}, \quad \omega = 1.68 \times 10^{-7} \text{s}^{-1}$$
  
 $\Rightarrow P = 5 \times 10^3 \text{ J/s}$ 

Very small, compared to the light power emitted by the sun:

$$L_{\odot} \approx 3.8 \times 10^{26} \,\mathrm{J/s}$$

Binary pulsar PSR1913+16 (Hulse and Taylor)

$$P = 7.35 \times 10^{24} \text{ J/s}$$

### **Continuous waves**

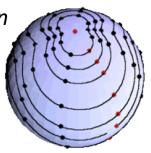
Rotating neutron stars  $\nu \sim 1 - 10^3 \; \mathrm{Hz}$   $h \sim 10^{-25} \; \mathrm{at} \; 3 \; \mathrm{kpc}$ 

$$h \sim 10^{-25} \text{ at } 3 \text{ kpc}$$

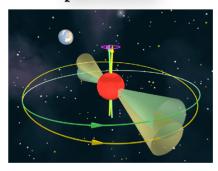
Not perfectly spherical



Oscillation modes



precession



« mountains » or assymetry

$$h_0 = \frac{4\pi^2 G}{c^4} \frac{I_{zz} \, \varepsilon \, f_{gw}^2}{d}$$

 $I_{ZZ}$  Moment of inertia along the rotation axis

$$\mathbf{\epsilon} = rac{I_{xx} - I_{yy}}{I_{zz}}$$
 Ellipticity in the equatorial plane

- $ightharpoonup I_{ZZ}$  and  $\mathcal E$  very poorly known
- Motion and orientation of the detector around the sun
  - Doppler modulation of the signal

# The End of episode I



# **Gravitational waves**

Sitzung der physikalisch-mathematischen Klasse vom 22. Juni 1916 688

#### Näherungsweise Integration der Feldgleichungen der Gravitation.

Von A. Einstein.

Bei der Behandlung der meisten speziellen (nicht prinzipiellen) Probleme auf dem Gebiete der Gravitationstheorie kann man sich damit begnügen, die  $g_{\mbox{\tiny gr}}$ in erster Näherung zu berechnen. Dabei bedient man sich mit Vorteil der imaginären Zeitvariable  $x_{\scriptscriptstyle 4}=it$  aus denselben Gründen wie in der speziellen Relativitätstheorie. Unter »erster Näherung« ist dabei verstanden, daß die durch die Gleichung (1)

$$g_{\mu\nu} = -\delta_{\mu\nu} + \gamma_{\mu\nu} \tag{1}$$

definierten Größen  $\gamma_u$ , welche linearen orthogonalen Transformationen gegenüber Tensorcharakter besitzen, gegen 1 als kleine Größen behandelt werden können, deren Quadrate und Produkte gegen die erster Potenzen vernachlässigt werden dürfen. Dabei ist  $\delta_{\mu\nu}=1$  bzw.  $\delta_{\mu\nu}=0$ je nachdem  $\mu = \nu$  oder  $\mu \neq \nu$ .

Wir werden zeigen, daß diese  $\gamma_{\omega}$  in analoger Weise berechn werden können wie die retardierten Potentiale der Elektrodynam Daraus folgt dann zunächst, daß sich die Gravitationsfelder mit Lie geschwindigkeit ausbreiten. Wir werden im Anschluß an diese gemeine Lösung die Gravitationswellen und deren Entstehungsw untersuchen. Es hat sich gezeigt, daß die von mir vorgeschlag Wahl doe Remosevetame comit der Radinoung a- | a | --

PRL 116, 061102 (2016)

Selected for a Viewpoint in *Physics* PHYSICAL REVIEW LETTERS

week ending 12 FEBRUARY 2016

# Observation of Gravitational Waves from a Binary Black Hole Merger

B. P. Abbott et al.\*

(LIGO Scientific Collaboration and Virgo Collaboration) (Received 21 January 2016; published 11 February 2016)

On September 14, 2015 at 09:50:45 UTC the two detectors of the Laser Interferometer Gravitational-Wave Observatory simultaneously observed a transient gravitational-wave signal. The signal sweeps upwards in frequency from 35 to 250 Hz with a peak gravitational-wave strain of  $1.0 \times 10^{-21}$ . It matches the waveform predicted by general relativity for the inspiral and merger of a pair of black holes and the ringdown of the resulting single black hole. The signal was observed with a matched-filter signal-to-noise ratio of 24 and a false alarm rate estimated to be less than 1 event per 203 000 years, equivalent to a significance greater than 5.1 $\sigma$ . The source lies at a luminosity distance of  $410^{+160}_{-180}$  Mpc corresponding to a redshift  $z = 0.09^{+0.03}_{-0.04}$ . In the source frame, the initial black hole masses are  $36^{+5}_{-4}M_{\odot}$  and  $29^{+4}_{-4}M_{\odot}$ , and the final black hole mass is  $62^{+4}_{-4}M_{\odot}$ , with  $3.0^{+0.5}_{-0.5}M_{\odot}c^2$  radiated in gravitational waves. All uncertainties define 90% credible intervals. These observations demonstrate the existence of binary stellar-mass black hole systems. This is the first direct detection of gravitational waves and the first observation of a binary black hole merger.

DOI: 10.1103/PhysRevLett.116.061102

#### I. INTRODUCTION

In 1916, the year after the final formulation of the field equations of general relativity, Albert Einstein predicted the existence of gravitational waves. He found that

The discovery of the binary pulsar system PSR B1913+16 by Hulse and Taylor [20] and subsequent observations of its energy loss by Taylor and Weisberg [21] demonstrated the existence of gravitational waves. This discovery,

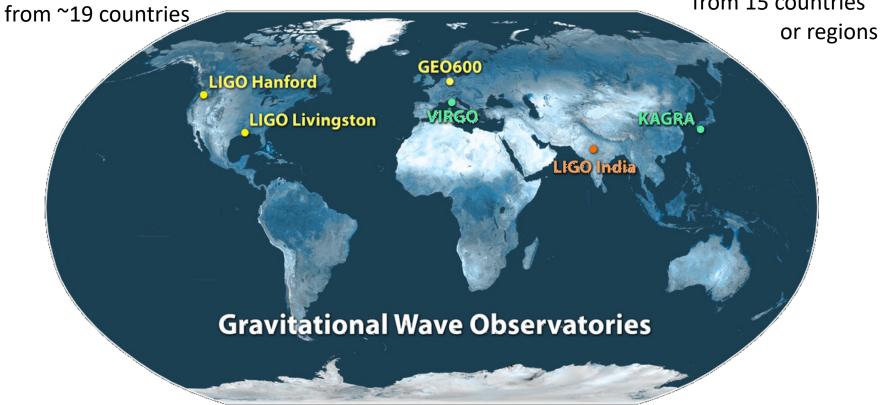
# The LIGO-Virgo-KAGRA collaboration

Virgo: ~700+ members 129 institutions

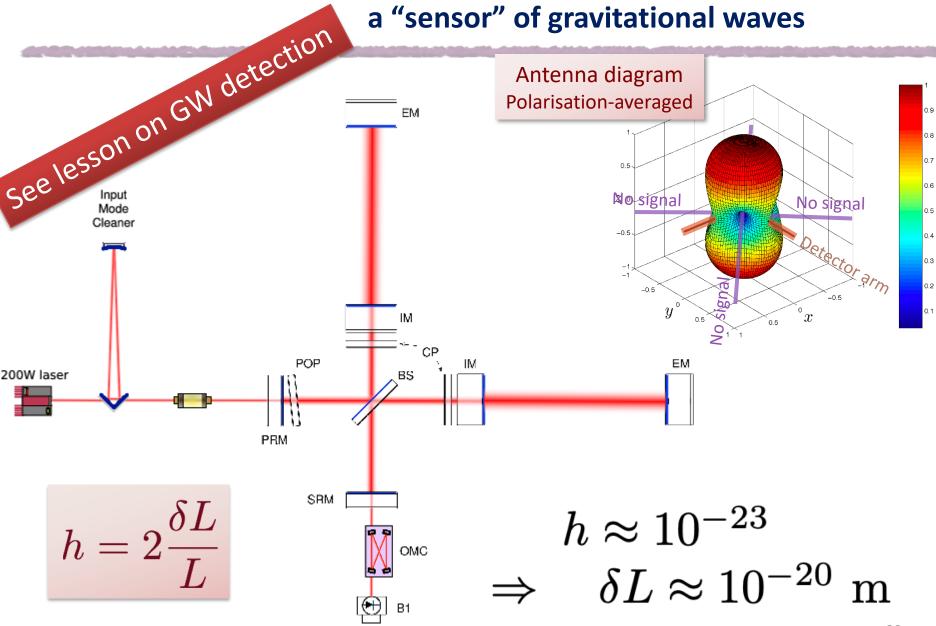
LSC: ~1400+ members

~127 institutions

KAGRA: ~400+ members from 16 countries 110 institutions from 15 countries



## Michelson interferometer: a "sensor" of gravitational waves



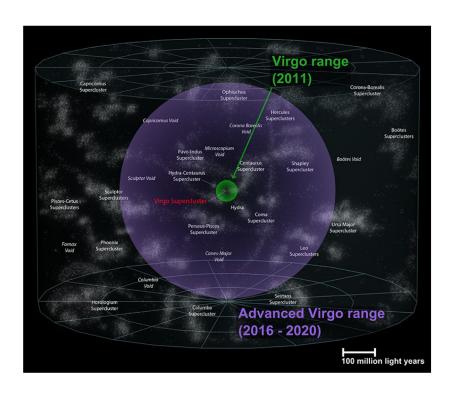
# LIGO-Virgo past runs



Reminder: 1 pc (parsec) = 3.26 ly (light-years)

### **Horizon distance**

- « Horizon » distance :
  - Distance at which a particular reference event
     emitted a signal which can be detected with Signal over Noise Ratio (SNR) = 8
- ► Reference event = binary neutron star coalescence with 1.4 M<sub>☉</sub> for each component

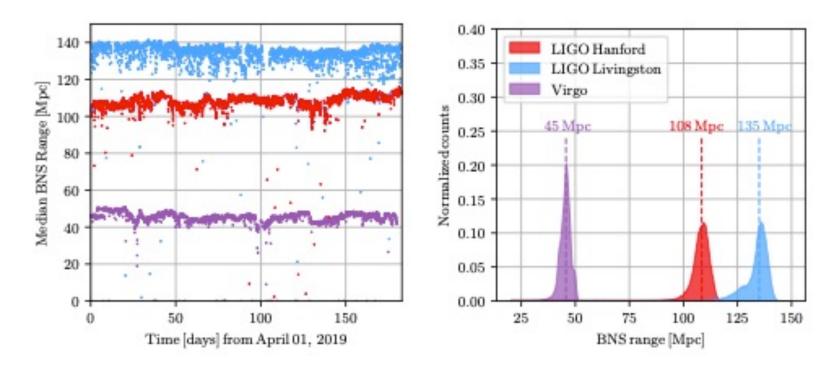


Improving the sensitivity (or horizon) by a factor 10

Increase the volume (or event rate) by 10<sup>3</sup>

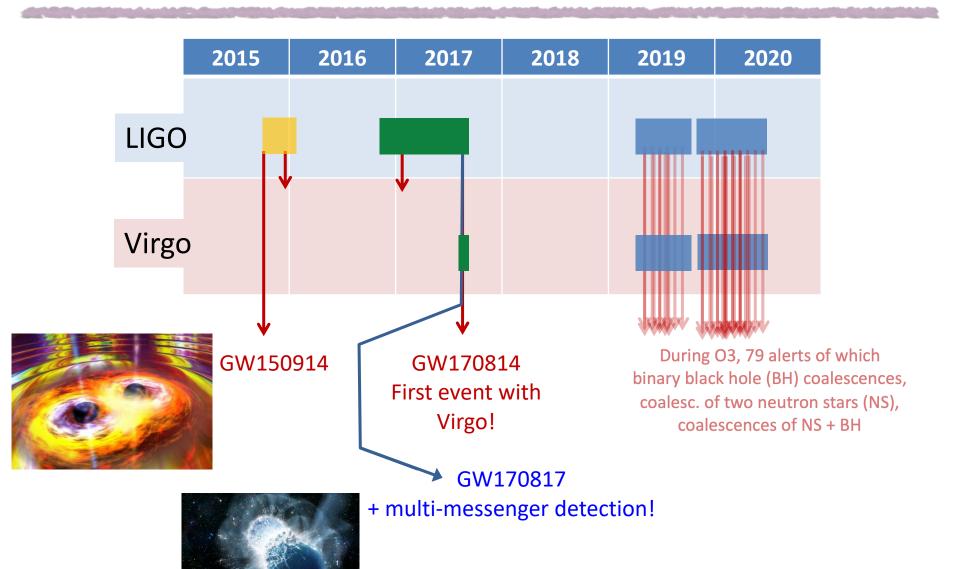
### **Horizon distance**

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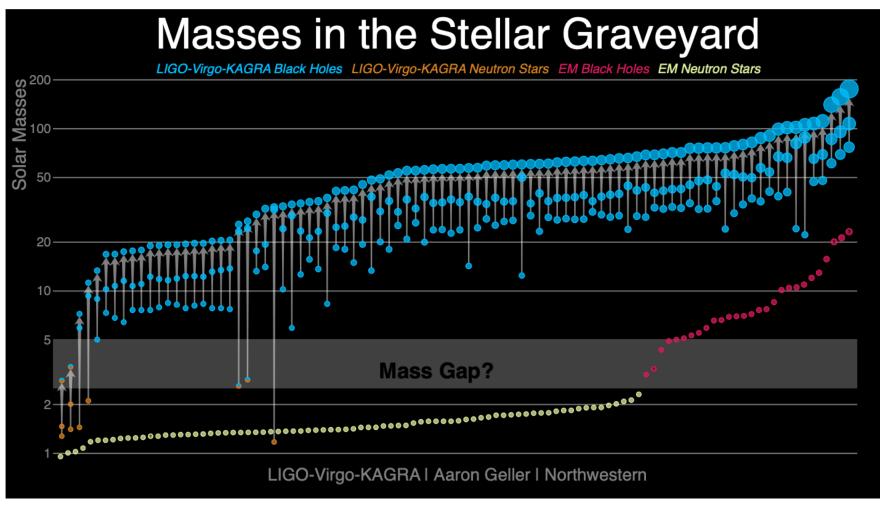


Can define a horizon distance for BBH or any event type

#### **Events and alerts**



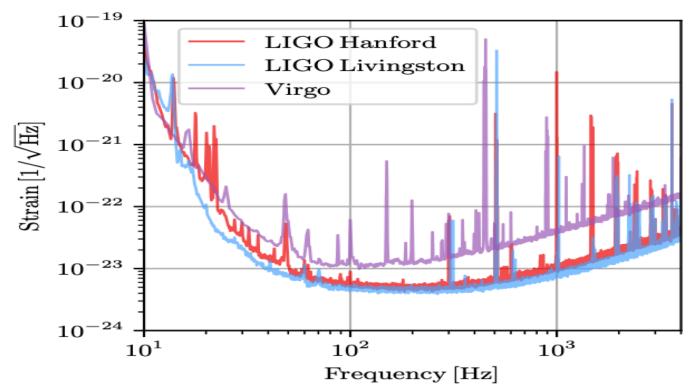
### **Diversity of binary compact objects**



https://ligo.northwestern.edu/media/mass-plot/index.html

### O3a run

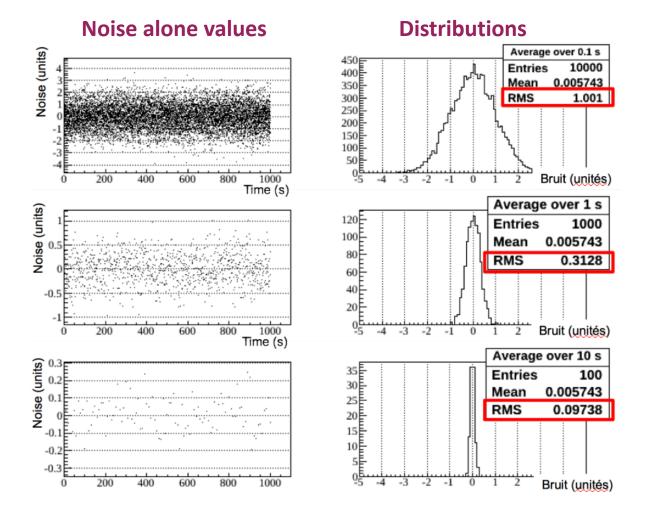
- ► April 1, 2019 October 1, 2019 (O3 = April 1, 2019 March 27, 2020)
  - ▶ 3 detectors simultaneously observing : 44.5 % (81.4 days)
    - ► H1 = LIGO Hanford, L1 = LIGO Livingston



- Strain sensitivities for H1 and L1 : similar
  - $\sim 5.10^{-24}/\sqrt{\text{Hz}}$  @ 100 Hz

## **Characterizing noise level**

▶ Hypothesis : constant signal  $S_0$  in gaussian noise  $N e^{-\frac{1}{2}\frac{(x-\langle x \rangle)^2}{\sigma_x^2}}$ 



If *T* is the averaging time, the noise variance goes as

$$\sigma_{noise} \propto rac{1}{\sqrt{T}}$$

## Characterizing noise level

Variance can be expressed as

$$\sigma_{noise} = \frac{D}{\sqrt{T}}$$

- Where D characterizes the level of noise
- D is written in terms of

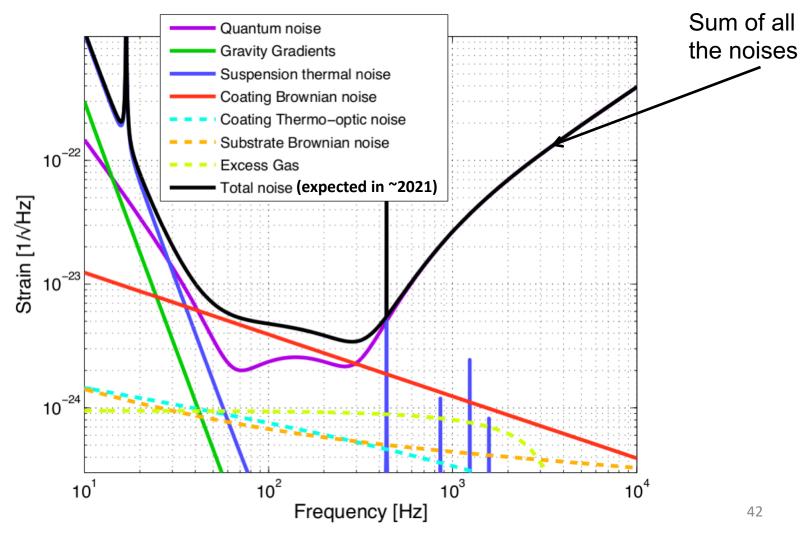
$$\frac{\text{data units}}{\sqrt{\text{Hz}}}$$

- ▶ Its value is the value of the noise variance when averaging over 1 s of signal
- lacktriangle Doing a Fourier transform, D(f) is also expressed in terms of

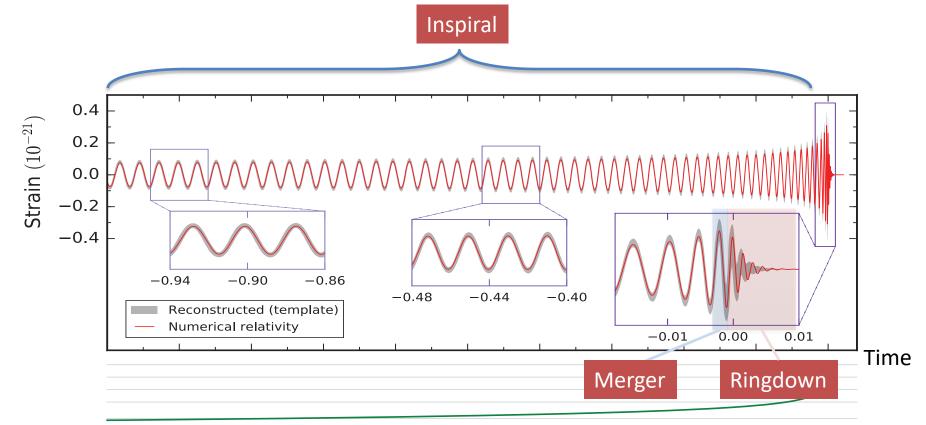
$$\frac{\text{data units}}{\sqrt{\text{Hz}}}$$

## **Nominal sensitivity of Advanced Virgo**

Fundamental noise only
Possible technical noises not shown



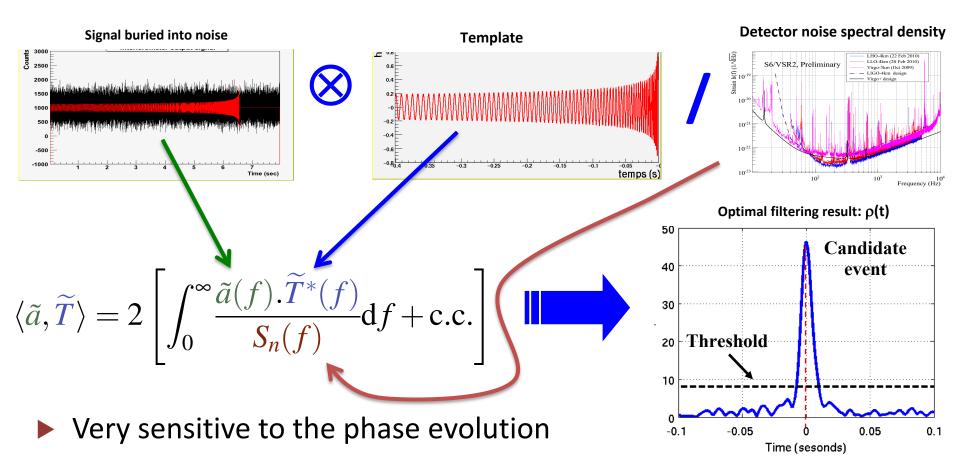
- ► Target: Signals from the coalescence of a binary system of compact objects
- Phases of the coalescence:



Waveform characterized by « chirp mass »

$$\mathcal{M} = \frac{(m_1 m_2)^{3/5}}{(m_1 + m_2)^{1/5}} = \frac{c^3}{G} \left[ \frac{5}{96} \pi^{-8/3} f^{-11/3} \dot{f} \right]^{3/5}$$

- Template based search
  - Production of a bank of templates (theoretical waveforms)
  - Optimal filtering = weighted inter-correlation btw signal and template



- Intrinsic parameters
  - masses, spins (aligned) drive
    - ► the system dynamics
    - the waveform evolution

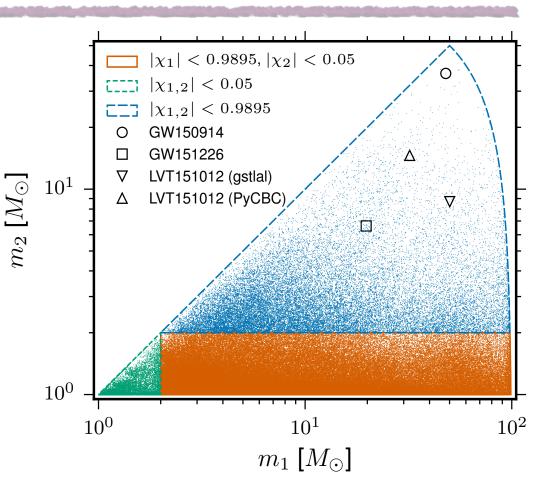
- Extrinsic parameters
  - Orientation of the binary, initial phase,...

#### impact:

- Arrival time of the signal
- Global amplitude and phase
- Maximized over (no need of templates)

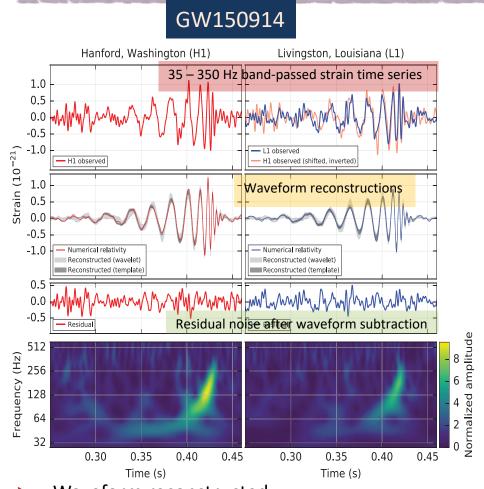
- ► For each template
  - Extract the maximum in the signal-to-noise time series
- ► Refinements :  $\chi^2$ ,  $\rho(t)$  coincidence, data quality, ...

- This is only for the detection...
  - Going further needs parameter estimation

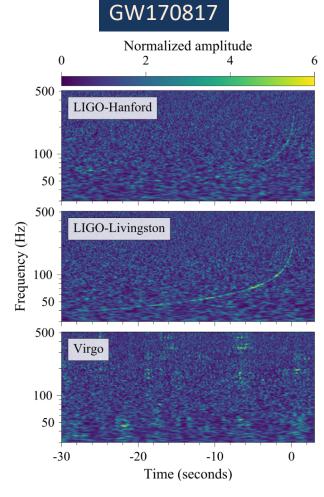


- Each point represents a template (test waveform)
- 4-D parameter space scanned with ~250,000 templates

#### Naked eye view of GW150914 and GW170817



- Waveform reconstructed
  - Coherent signal in both detectors
  - Agreement with best-fit theoretical waveforms
     (waveforms from perturbative theory + NR = Numerical Relativity)



Residual noise consistent with instrumental noise

#### **Parameter Estimation**

- Intrinsic parameters (8)
- Masses (2) + Spins (6)

- Extrinsic parameters (9)
- ► Location : luminosity distance, right ascension, declination (3)
- ▶ Orientation: inclination, polarization (2)
- ► Time and phase of coalescence (2)
- Eccentricity (2)

17 dimensions parameter space

+ 10 to acount for various systematic uncertainties.

- Estimation of the parameters of the source
- Reconstruct the Probability Density Function = "PDF" =  $p(\vec{\theta}|\vec{d})$  that a waveform of parameters  $\vec{\theta}$  is present in the data  $\vec{d}$

#### **Parameter Estimation**

Estimation of the source parameters

PDF = Probability Density Function

PDF to have a waveform of parameters  $\vec{\theta}$  given the data  $\vec{d}$ 

Prior PDF to have a waveform of parameters  $\overrightarrow{\theta}$ . (before considering the data)

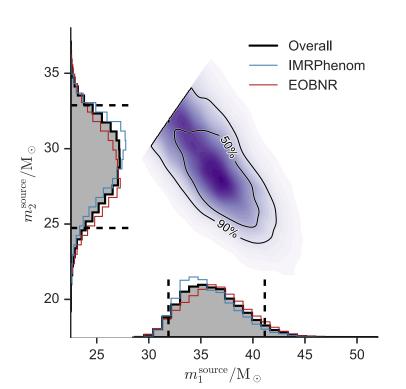
Likelihood that the data  $\vec{d}$  contains a signal, or waveform, of given parameters  $\vec{\theta}$ .

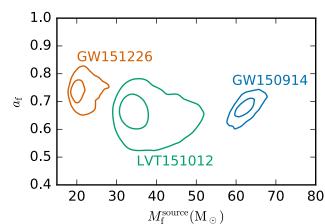
Based on the optimal filtering described in lesson II

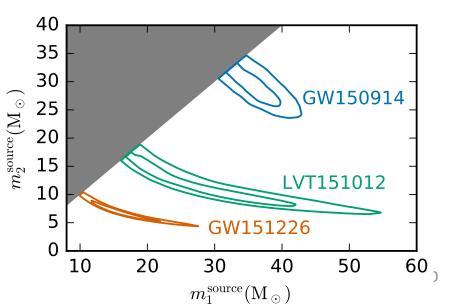
⇔ use the Bayes Theorem

#### **Parameter Estimation**

- ► Bayesian framework
- Various methods to sample the parameter space :
  - MCMC = Markov Chain Monte-Carlo
  - Nested sampling
- Example for some intrinsic parameters





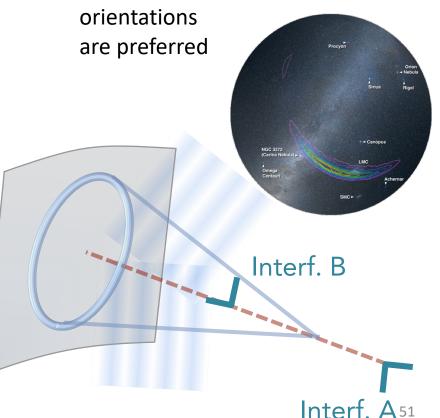


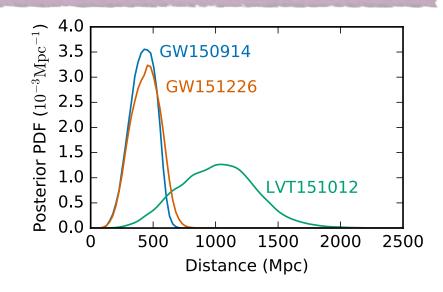
## **Extrinsic Parameters : examples**

 Amplitude depends on masses, distance, and geometrical factors

Distance – inclination degeneracy

Distant sources with favorable





#### Source location

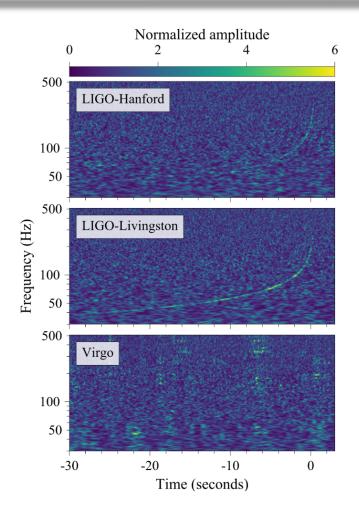
- inferred primarily from
  - ightharpoonup time of flight  $6.9^{+0.5}_{-0.4} \, \mathrm{ms}$  or GW150914
  - amplitude and phase consistency
- Limited accuracy with two detector network
- Sky locations with good detector response are preferred

### **Important events**

- First detection : GW150914
- First binary neutron star coalescence : GW170817
- Coalescences of a neutron star and a black hole : GW200105 and GW 200115
- Most massive final black hole: GW190521

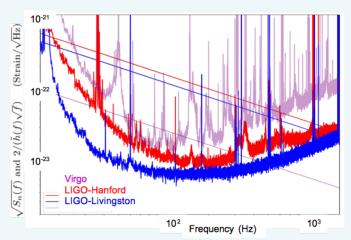
# **GW170817**: the merger of two neutron stars

- Detected on August 17, 2017 at 12:41:04.4 UTC
- Combined SNR = 32.4
- False alarm rate f < 1 over 80000 years</p>

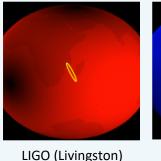


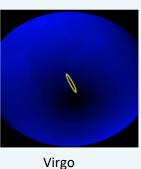
Abbott et al., PRL, 119, 161101 (2017)

- Weak signal in Virgo
  - Lower sensitivity + unfavorable orientation
  - Does not participate to the detection
  - Significant effect on parameter estimation
  - Particularly sky localization

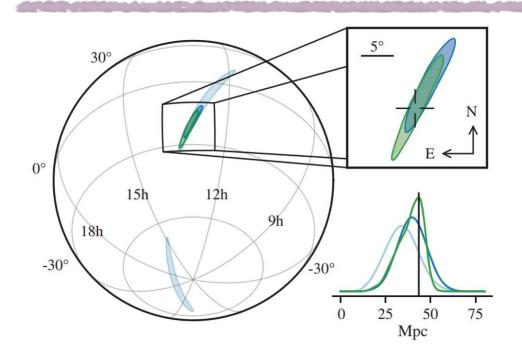


Antenna pattern projected on Earth (darker = less sensitive)





### **GW170817**: source localization



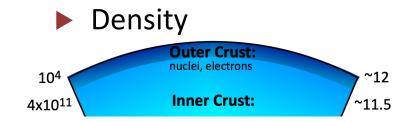
- · Sky location:
  - rapid loc. with HL: 190 deg<sup>2</sup>
     rapid loc. with HLV: 31 deg<sup>2</sup>
- final loc. with HLV: 28 deg<sup>2</sup>
- Luminosity distance: 40 Mpc (~120 millions of light-years)
- → 3D position: 380 Mpc<sup>3</sup>
- Source closest and best localized even today
- ► Triggered electromagnetic and neutrino followup observations
- Identified NGC4993 as the host galaxy

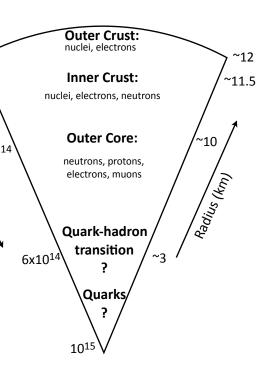


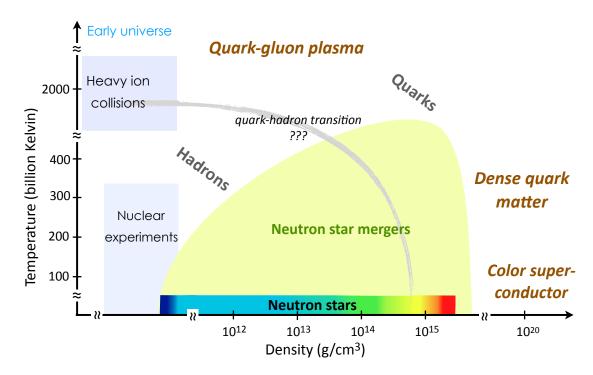




#### **Neutron star: internal structure**







#### **Neutron star: internal structure**

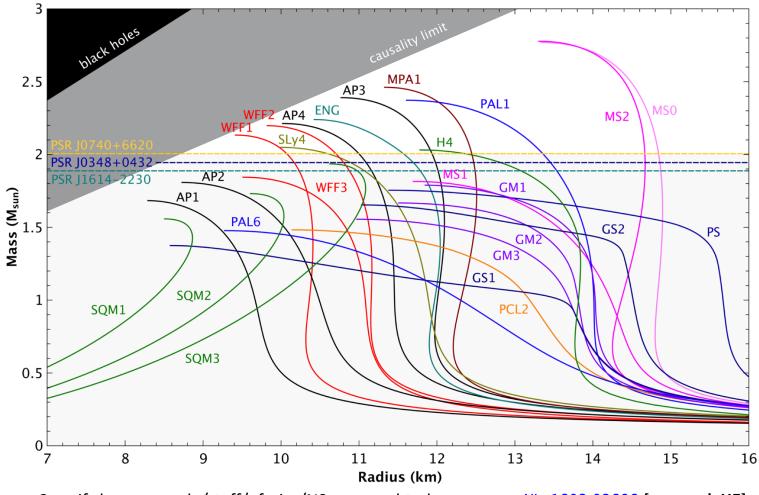
- Spherical symmetry body in GR
  - Isotropical material
  - Gravitational equilibrium, stationary
- => Tolman-Oppenheimer-Volkoff (TOV) equation:

$$rac{dP}{dr} = -rac{Gm}{r^2}
ho\left(1+rac{P}{
ho c^2}
ight)\left(1+rac{4\pi r^3P}{mc^2}
ight)\left(1-rac{2Gm}{rc^2}
ight)^{-1}$$

- ightharpoonup r radial coordinate, ho(r) energy density, P(r) pressure
- ightharpoonup m(r) total mass in a sphere of radius r
- ▶ If includes the equation of state (EOS)  $F(P, \rho) = 0$ 
  - => completely determines the internal structure
- But F is poorly known!

#### **Neutron star: internal structure**

#### Equations of state



## **GW170817**: intrinsic parameters

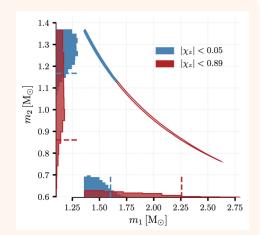
Abbott et al., PRL, 119, 161101 (2017)

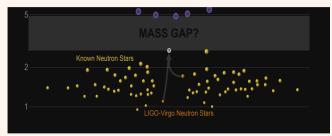
	low-spin ( $ \chi  < 0.05$ )	high-spin ( $ \chi  < 0.89$ )
$M_{chirp}(M_{\odot})$	$1.188^{+0.004}_{-0.002}$	
$m_1 (M_{\odot})$	1.36 - 1.60	1.36 - 2.26
$m_2 (M_{\odot})$	1.17 – 1.36	0.86 - 1.36
$m_{tot} \ (M_{\odot})$	$2.74^{+0.04}_{-0.01}$	$2.82^{+0.47}_{-0.09}$

#### **Object masses**

Degeneracy btw mass ratio and spin aligned components.

→ Masses < 2.3 M





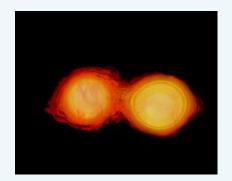
Masses consistent with neutron stars

#### **Equation of state of neutron stars**

Tidal field of the companion

Deformation of the neutron star

Deformation of the shape of the GW for f>600 Hz

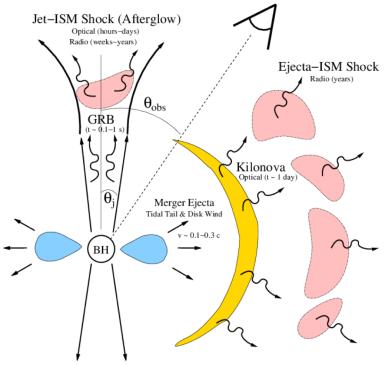


Merger happens earlier than w/o tidal effect, final spin modified

Result favors equations of state of neutron stars that predict more compact stars: radius < 15 km

## **Expected electro-magnetic counterparts?**

Metzger & Berger, ApJ, 746, 48 (2012)



### Short gamma-ray burst (sGRB): Jet

→ prompt γ-ray emission

- few seconds after merger
- last for <2 s
- beamed

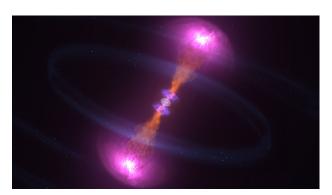
#### Interaction of jet with interstellar medium

- → afterglow emission
  - few days after merger
  - evolves from X-ray to radio

#### Kilonova (or macronova)

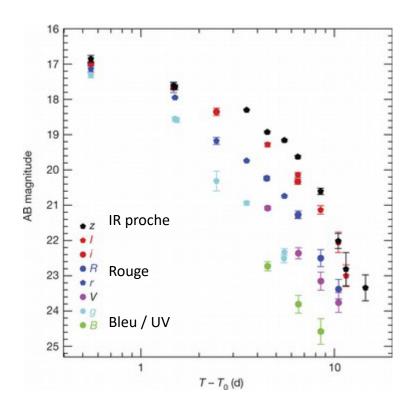
Conversion of hot ejected matter into r-processed elements, disintegration and thermal emission

- → black body continuum + broad structures
  - few hours-days after merger
  - visible in UV, optical, IR
  - rapid spectral evolution





## **Optical transient evolution**



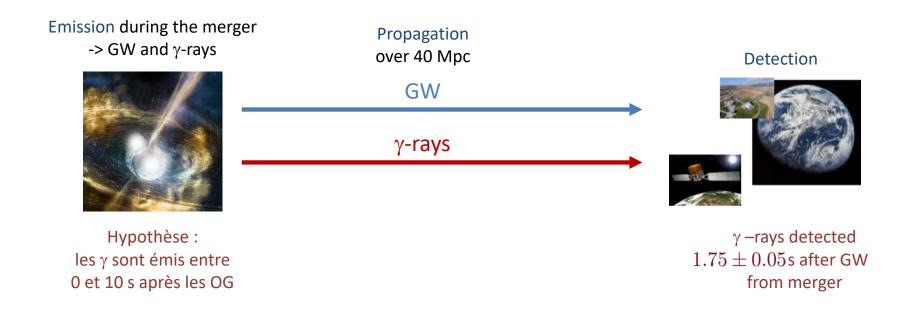
2.0 0818 Flux 10,000 25,000 Wavelength (Å) Bleu IR moyen IR proche

Light curves

Spectrum evolution

- ► Consistent with kilonova (=macronova) models
- First spectroscopic identification of a kilonova
- Probably the main source of heavy elements in the universe

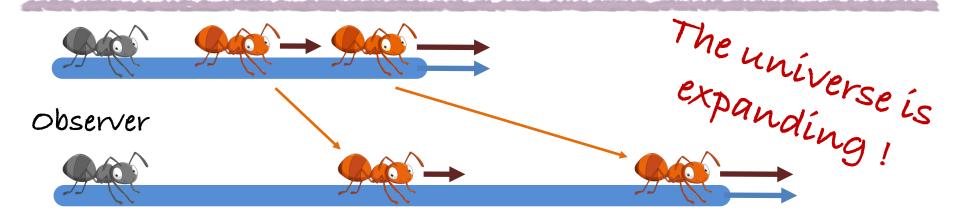
# GW170817: association btw GW/GRB, speed of gravitational waves



Difference btw speed of light and speed of GW

$$[-3 \times 10^{-15}; +7 \times 10^{-16}] \times c$$

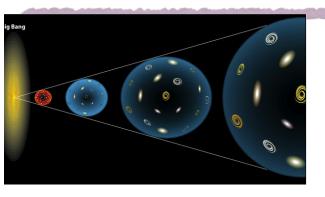
## **Cosmology: ants in the universe**



- Motionless ants on an expanding rubber band
- Ant at twice the distance=> seems to move away at twice the speed

$$V_{apparent} = H \times D_{object}$$

## **Cosmology: the universe with ants**



Determined from the redshift of host galaxy

$$(3017 \pm 166 \, \text{km/s})$$



Today's expansion rate of the universe

Luminosity distance estimated from GW signal

$$(43.8^{+2.9}_{-6.9} \,\mathrm{Mpc})$$

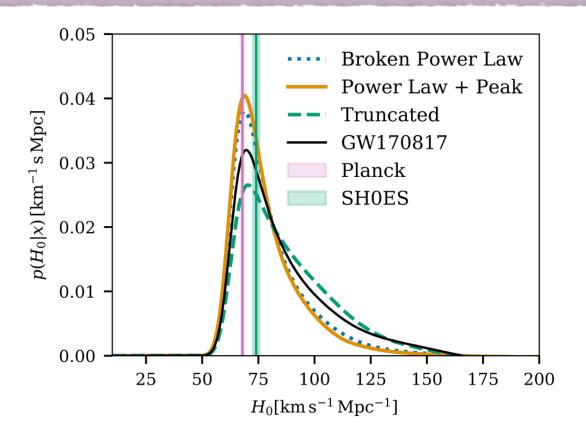
→ infer

$$H_0 = 70^{+12}_{-8} \text{ km/s.Mpc}^{-1}$$

GW170817 may be used as a "standard siren"

Reminder: 1 Mpc = 3.26 Mly

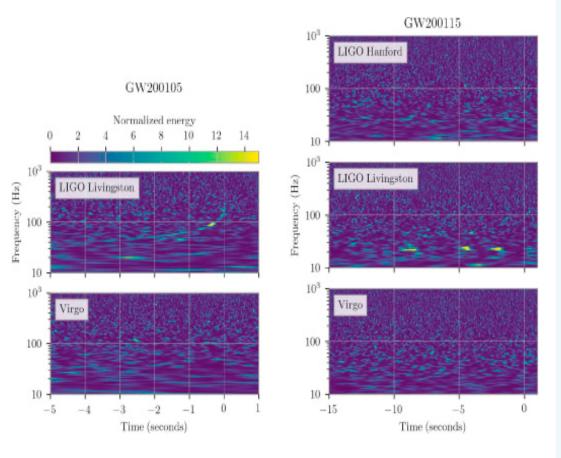
### **Cosmology: Hubble constant measurement**



Independent measurement of H₀
 → may help to understand the current « tension »
 btw different measurements

# **GW200105** and **GW200115 Neutron star and black hole**

- Detected on January 5 and January 15 2020
- Combined SNR = 13.9 and 11.6



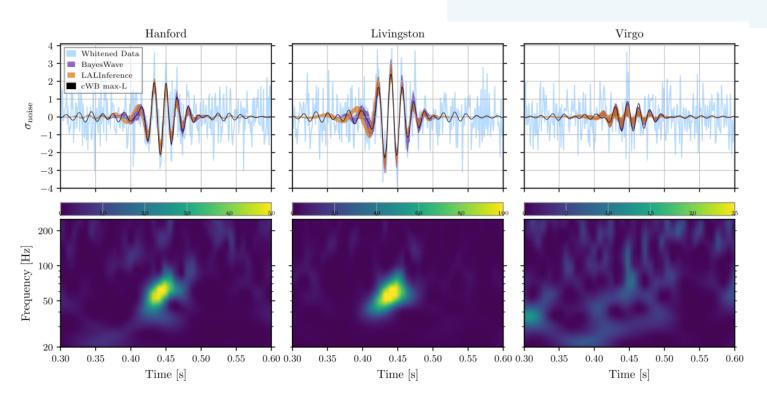
- **Distance**:  $(280^{+110}_{-110} \text{ and } 300^{+150}_{-100}) \text{ Mpc}$
- Masses:  $(8.9^{+1.2}_{-1.5} \text{ and } 1.9^{+0.3}_{-0.2}) M_{\odot}$ and  $(5.7^{+1.8}_{-2.1} \text{ and } 1.5^{+0.7}_{-0.3}) M_{\odot}$
- Modeling the formation of such binaries is difficult
- No EM or neutrino counterparts

R. Abbott *et al* 2021 *ApJL* **915** L5

## GW190521: Big is big!

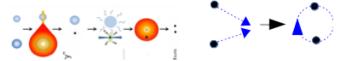
- Detected0 on May 21 2019 at 03:02:29 UTC
- Combined SNR = 14.7
- False alam rate f < 1 over 4900 years

- Distance:  $5.3^{+2.4}_{-2.6}$  Gpc (redshift of 0.82)
- Masses:  $85^{+21}_{-14}~M_{\odot}$  and  $66^{+17}_{-18}~M_{\odot}$
- Final black hole mass:  $142^{+28}_{-16}~M_{\odot}$
- First intermediate mass black hole



# Non exhaustive list of current and future studies

- Astrophysical implications
  - ► Formation mechanism of NS or BH binaries

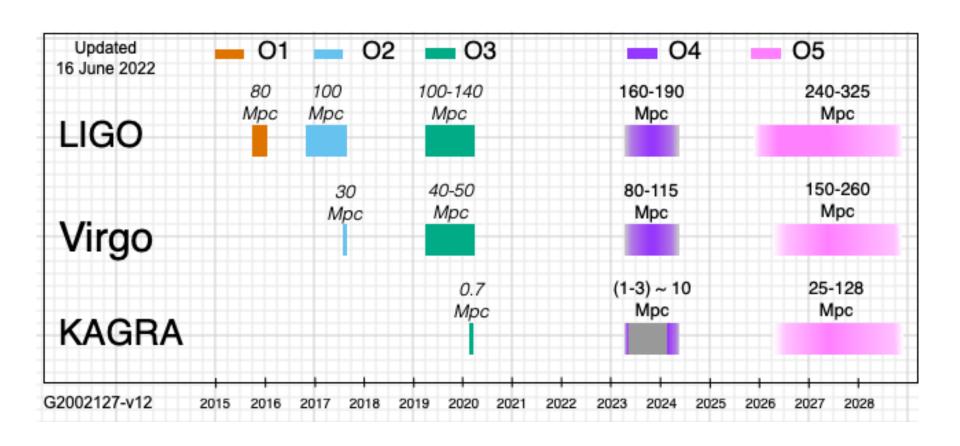


- GRB origin, jet focusing / structure
- Kilonovae modeling
- Equation of state of neutron stars
- Neutron star result of a merger: long or short-lived ?
- Inference of binary neutron star population distribution and coalescence rate

$$R = 1540^{+3200}_{-1220} \text{ Gpc}^{-3}.\text{yr}^{-1}$$
  
 $(R < 12600 \text{ Gpc}^{-3}.\text{yr}^{-1} \text{ from } 01)$ 

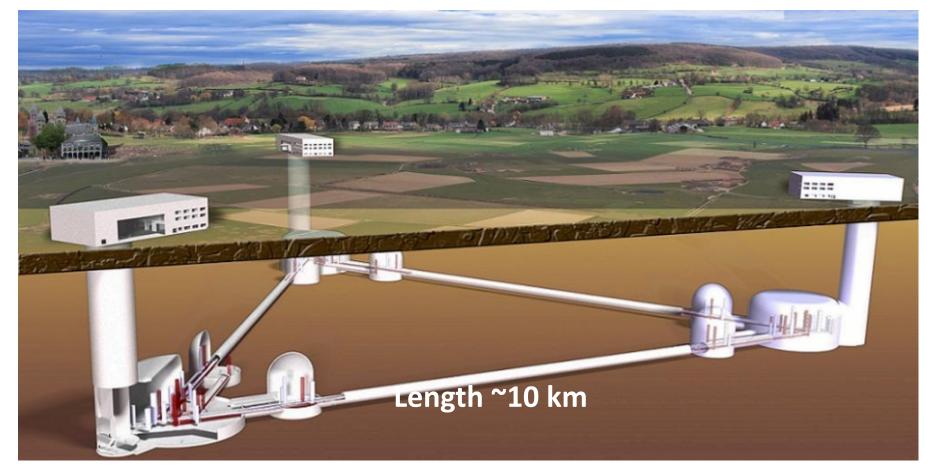
- ▶ GW stochastic background coming from BNS coalescences (astrophysical stochastic background)
  - ► To be detected in the coming years
- Tests of GR
  - Difference in speed between GW and light
  - Search for deviations from GR in GW waveforms
  - Study of the GW polarization
  - New limits on Lorentz invariance violation
  - New test of the equivalence principle
- Cosmologie
  - Independent measurement of the Hubble constant

### An eye on the future

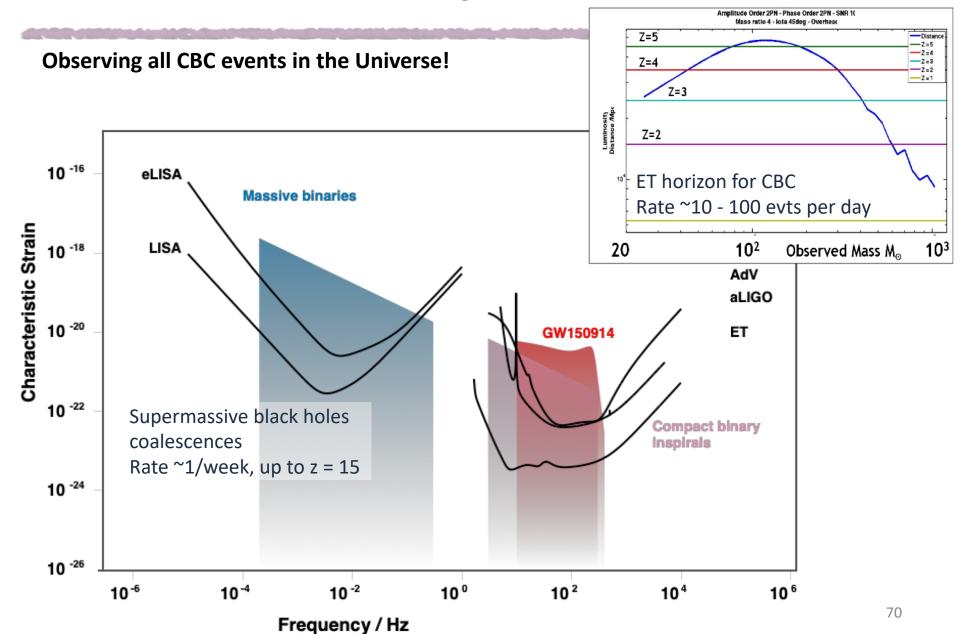


## **Einstein Telescope**

- Third generation interferometer
- Located underground, ~10 km arms
- Technical design to be written in ~2024 -2025, detector operational after 2035?



## ET and LISA performances



## The End of episode II