



Theory overview of B -physics anomalies

Olcyr Sumensari

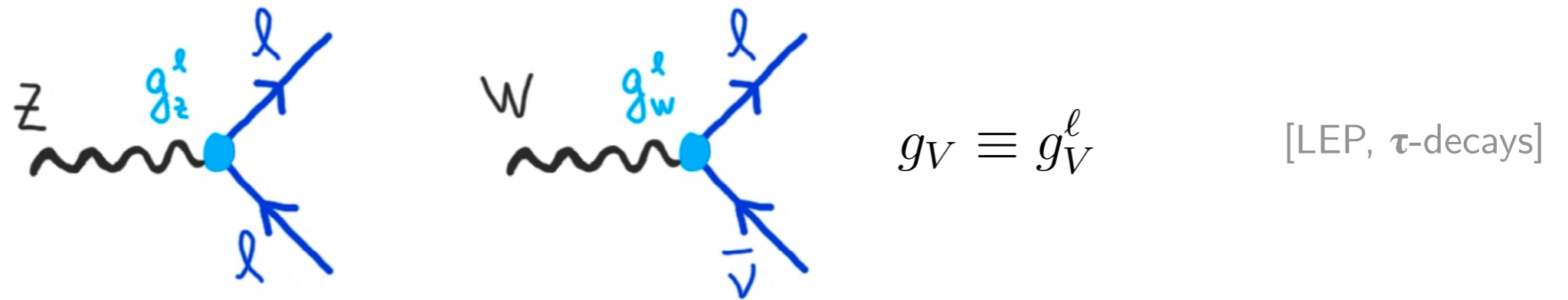
IJCLab (Orsay)

"IRN Terascale @ Bonn", 29 March, 2022



Lepton Flavor Universality (LFU)

- **Well-tested** property of the SM **gauge sector**, which is *broken by Yukawas*:



- Several discrepancies have been observed in **b-hadron** decays:

See also:

$$R_{K^{(*)}} = \frac{\mathcal{B}(B \rightarrow K^{(*)} \mu\mu)}{\mathcal{B}(B \rightarrow K^{(*)} ee)} \Bigg|_{q^2 \in [q_{\min}^2, q_{\max}^2]} \quad \& \quad R_{K^{(*)}}^{\text{exp}} < R_{K^{(*)}}^{\text{SM}}$$

R_{pK}

$$R_{D^{(*)}} = \frac{\mathcal{B}(B \rightarrow D^{(*)} \tau \bar{\nu})}{\mathcal{B}(B \rightarrow D^{(*)} \ell \bar{\nu})} \Bigg|_{\ell \in (e, \mu)} \quad \& \quad R_{D^{(*)}}^{\text{exp}} > R_{D^{(*)}}^{\text{SM}}$$

$R_{J/\psi}$

[LHCb, *B-factories*]

- **If confirmed** with more data, they will be a clear evidence of **New Physics!**

Outline

I. Introduction

II. Lepton Flavor Universality

- Current status
- EFT interpretations
- From EFTs to complete models

III. From LFUV to high- p_T physics

IV. Predictions at low-energies

V. Summary

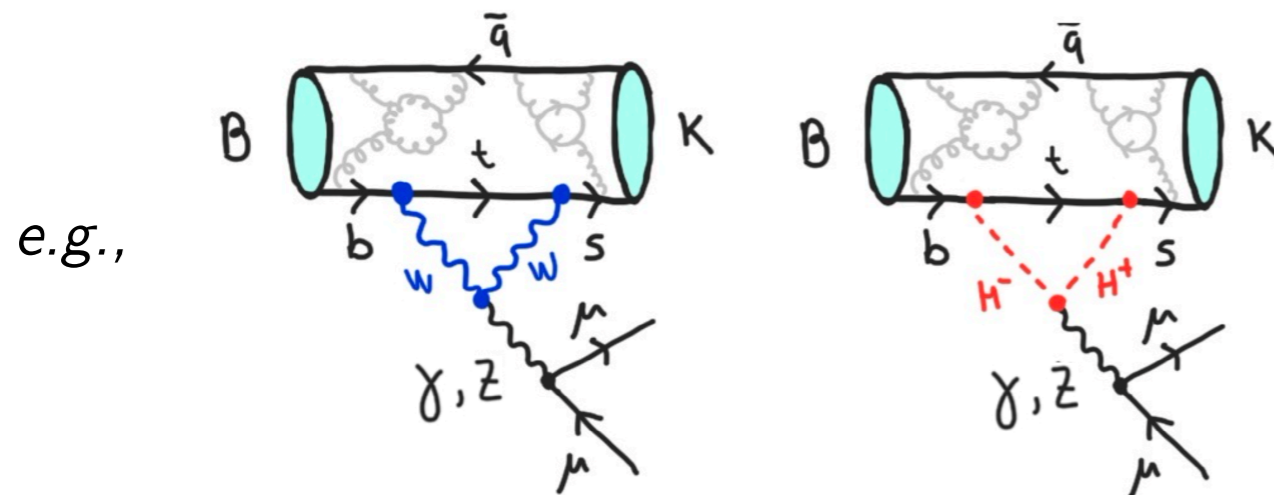
*See talk by F. Bernlochner on the experimental part!

Introduction

Seeking New Physics with flavor

Indirect searches of New Physics

i. Search deviations w.r.t. SM predictions:



$$\mathcal{O}_{\text{exp}} = \mathcal{O}_{\text{SM}} (1 + \delta_{\text{NP}})$$

Both **exp.** and **theory** must be **precise!**

Look for observables:

- (Highly) sensitive to contributions from New Physics
- Mildly sensitive to hadronic uncertainties
- Accessible in current and/or (near) future experiments.

LFU ratios are an excellent example!

Indirect searches of New Physics

ii. Search processes forbidden (by accidental symmetries) in the SM

Global symmetry of the SM gauge sector:

$$U(3)^5 \equiv U(3)_Q \times U(3)_L \times U(3)_U \times U(3)_D \times U(3)_E$$

Broken by Yukawas to

$$U(1)_B \times U(1)_e \times U(1)_\mu \times U(1)_\tau$$

Examples:

- Proton decay (**BNV**): $p \rightarrow \pi^0 e^+$
- $0\nu\beta\beta$ (**LNV**): $(A, Z) \rightarrow (A, Z + 2) + 2e^-$
- Lepton **F**lavor **V**iolation (**LFV**): $\mu \rightarrow e\gamma$

Clean probes of New Physics!

Lepton Flavor Universality

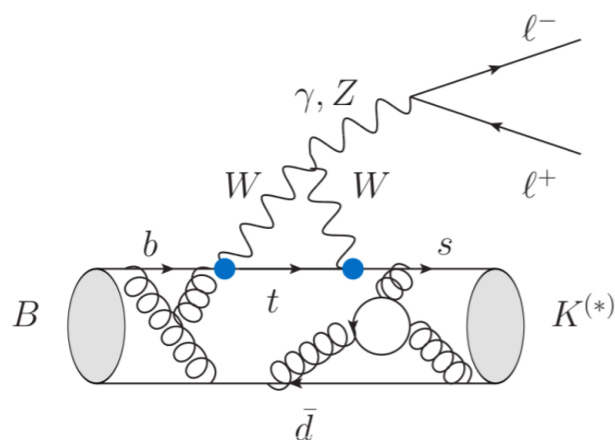
Current status

LFU in $b \rightarrow s \ell \ell$

Experiment

See talk by F. Bernlochner

$$R_{K^{(*)}} = \frac{\mathcal{B}(B \rightarrow K^{(*)} \mu \mu)}{\mathcal{B}(B \rightarrow K^{(*)} e e)}$$



Theory (loop induced)

- Hadronic uncertainties almost fully cancel.

⇒ **Clean observables!**

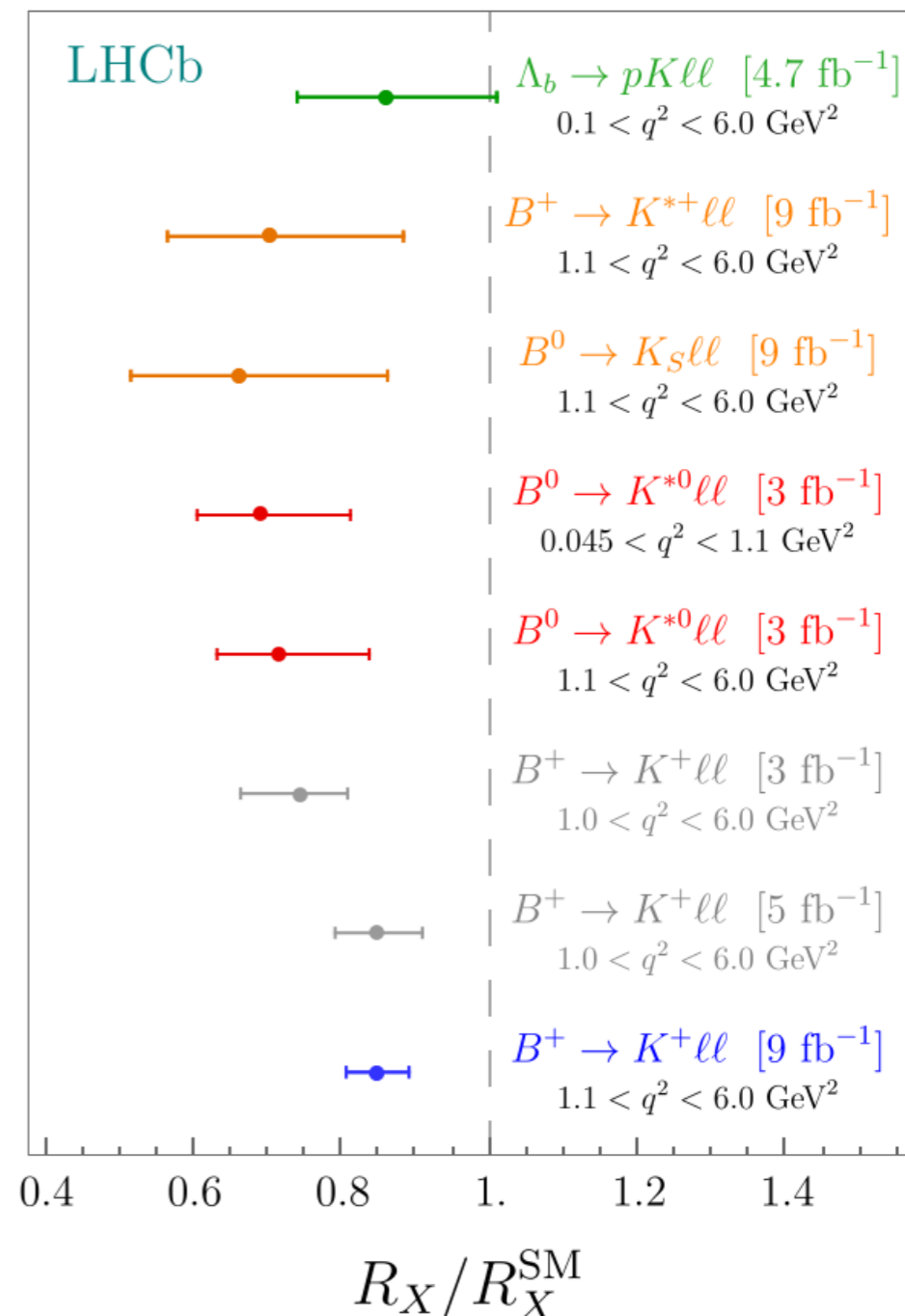
[working below the narrow $c\bar{c}$ resonances]

[Hiller, Kruger. '04]

- However, QED corrections important,

$$R_{K^{(*)}}^{\text{SM}} = 1.00(1)$$

[Isidori et al. '20]



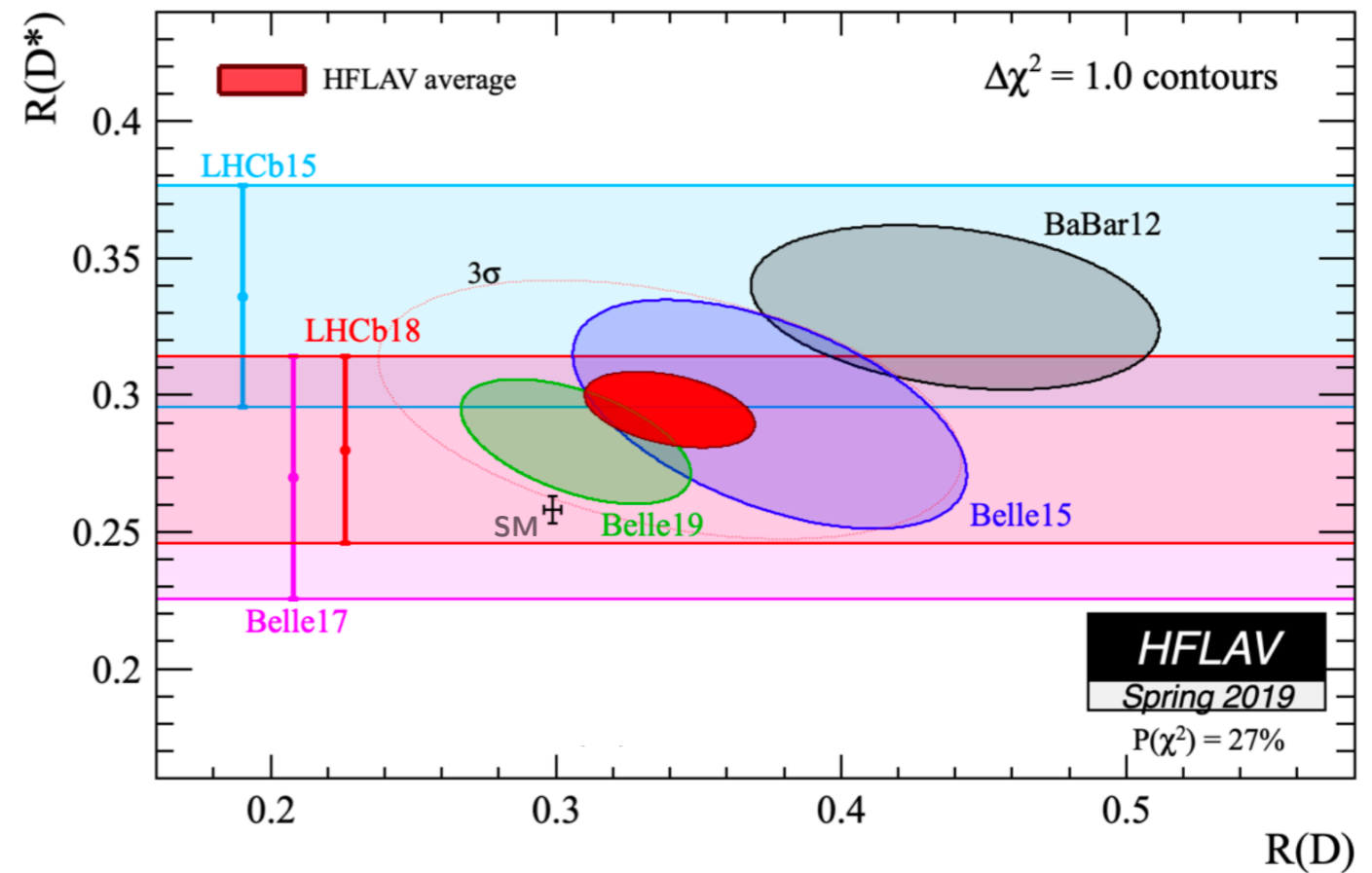
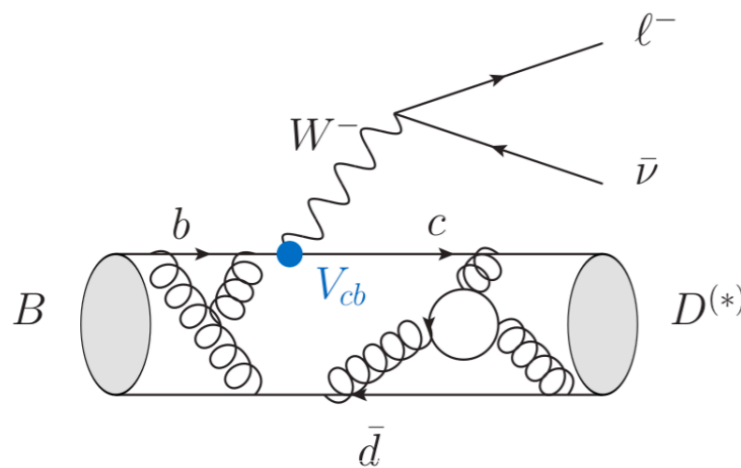
Needs independent cross-check from Belle-II

LFU in $b \rightarrow c\tau\bar{\nu}$

See talk by F. Bernlochner

Experiment

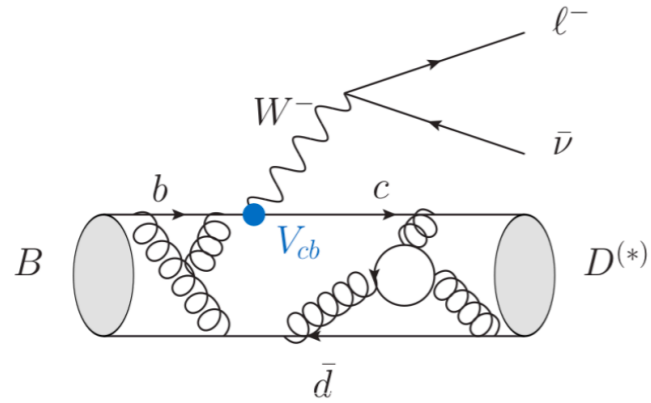
$$R_{D^{(*)}} = \frac{\mathcal{B}(B \rightarrow D^{(*)}\tau\nu)}{\mathcal{B}(B \rightarrow D^{(*)}\mu\nu)}$$



- R_D^{exp} and $R_{D^*}^{\text{exp}}$: dominated by BaBar!
- LHCb confirmed tendency $R_{J/\psi}^{\text{exp}} > R_{J/\psi}^{\text{SM}}$, i.e. $B_c \rightarrow J/\psi\ell\bar{\nu}$ — with large uncertainties.

Needs clarification from **Belle-II** and **LHCb (run-2)** data!

Form-factors: $B \rightarrow D^{(*)} \ell \bar{\nu}$

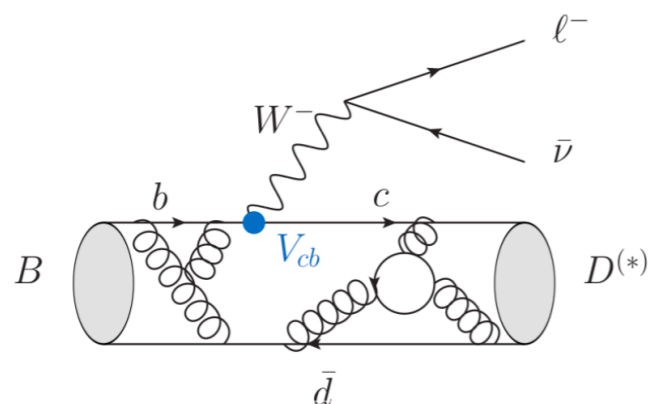


$$\langle D^{(*)} | \bar{c}_L \gamma^\mu b_L | B \rangle = \sum_a K_a^\mu \mathcal{F}_a(q^2)$$

Known Lorentz factors

Form-factors (from lattice, exp...)

Form-factors: $B \rightarrow D^{(*)} \ell \bar{\nu}$



$$\langle D^{(*)} | \bar{c}_L \gamma^\mu b_L | B \rangle = \sum_a K_a^\mu \mathcal{F}_a(q^2)$$

Known Lorentz factors
↓
Form-factors (from lattice, exp...)
↑

For light (heavy) leptons:

- $B \rightarrow D$: one (two) form-factors with $f_0(0) = f_+(0)$ at $q^2 = 0$;
 \Rightarrow Lattice QCD at $q^2 \neq q_{\max}^2$ ($w \neq 1$) for both form-factors. [MILC/Fermilab '15, HPQCD '15]

$$R_D^{\text{latt.}} = 0.293(5)$$

$$R_D^{\text{latt.+exp}} = 0.295(3) \quad [\text{FLAG '21}]$$

- $B \rightarrow D^*$: three (four) form-factors;
 \Rightarrow [NEW] First lattice computation at $q^2 \neq q_{\max}^2$ ($w \neq 1$) $B \rightarrow D^{(*)} l \bar{\nu}$ ($l = e, \mu$)

\Rightarrow [NEW] First lattice computation at $q^2 \neq q_{\max}^2$ ($w \neq 1$) [MILC/Fermilab '21]

$$R_{D^*}^{\text{latt.}} = 0.265(13)$$

$$R_{D^*}^{\text{latt.+exp}} = 0.2483(13) \quad [\text{See back-up!}]$$

1.3 σ apart

Way out: independent LQCD results + Belle-II!

New Physics interpretations

- EFT description
- From EFTs to concrete models

EFT for $b \rightarrow s\ell\ell$

$$\mathcal{L}_{\text{eff}} = \frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \left[\sum_{i=1}^6 C_i(\mu) \mathcal{O}_i + \sum_{7,8,9,10,P,S} \left(C_i(\mu) \mathcal{O}_i + C'_i(\mu) \mathcal{O}'_i \right) \right] + \text{h.c.}$$

- Semileptonic operators:**

$$\mathcal{O}_9^{(\prime)} = (\bar{s} \gamma_\mu P_{L(R)} b) (\bar{\ell} \gamma^\mu \ell)$$

$$\mathcal{O}_{10}^{(\prime)} = (\bar{s} \gamma_\mu P_{L(R)} b) (\bar{\ell} \gamma^\mu \gamma_5 \ell)$$

$$\mathcal{O}_S^{(\prime)} = (\bar{s} P_{R(L)} b) (\bar{\ell} \ell)$$

$$\mathcal{O}_P^{(\prime)} = (\bar{s} P_{R(L)} b) (\bar{\ell} \gamma_5 \ell)$$

- Dimension-6 *tensor operator* is *not allowed* by $SU(2)_L \times U(1)_Y$

[Buchmuller, Wyler. '85]

- (Pseudo)scalar operators* are *tightly constrained* by

$$\bar{\mathcal{B}}(B_s \rightarrow \mu\mu)^{\text{exp}} = (2.85 \pm 0.22) \times 10^{-9}$$

[Our exp. average: CMS, ATLAS, LHCb]

$$\bar{\mathcal{B}}(B_s \rightarrow \mu\mu)^{\text{SM}} = (3.66 \pm 0.14) \times 10^{-9}$$

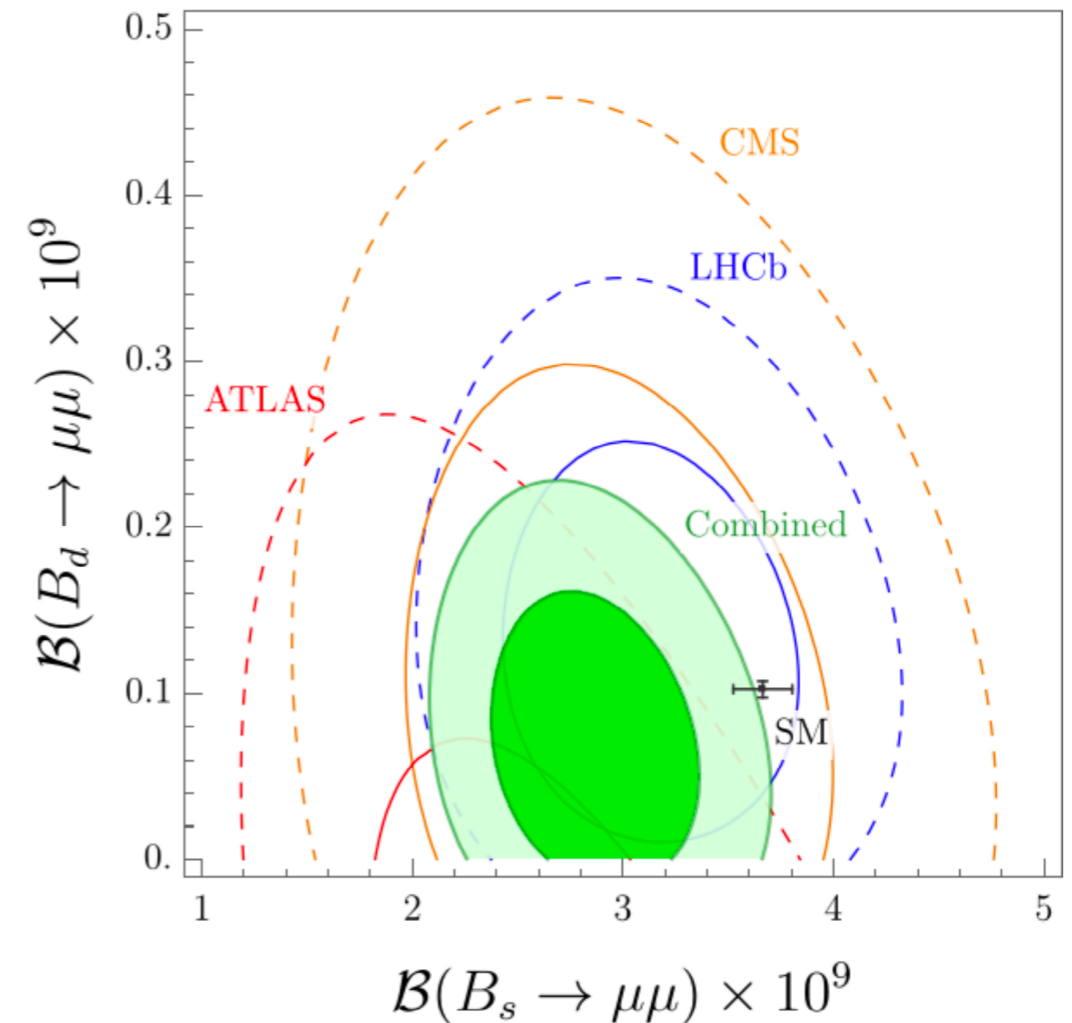
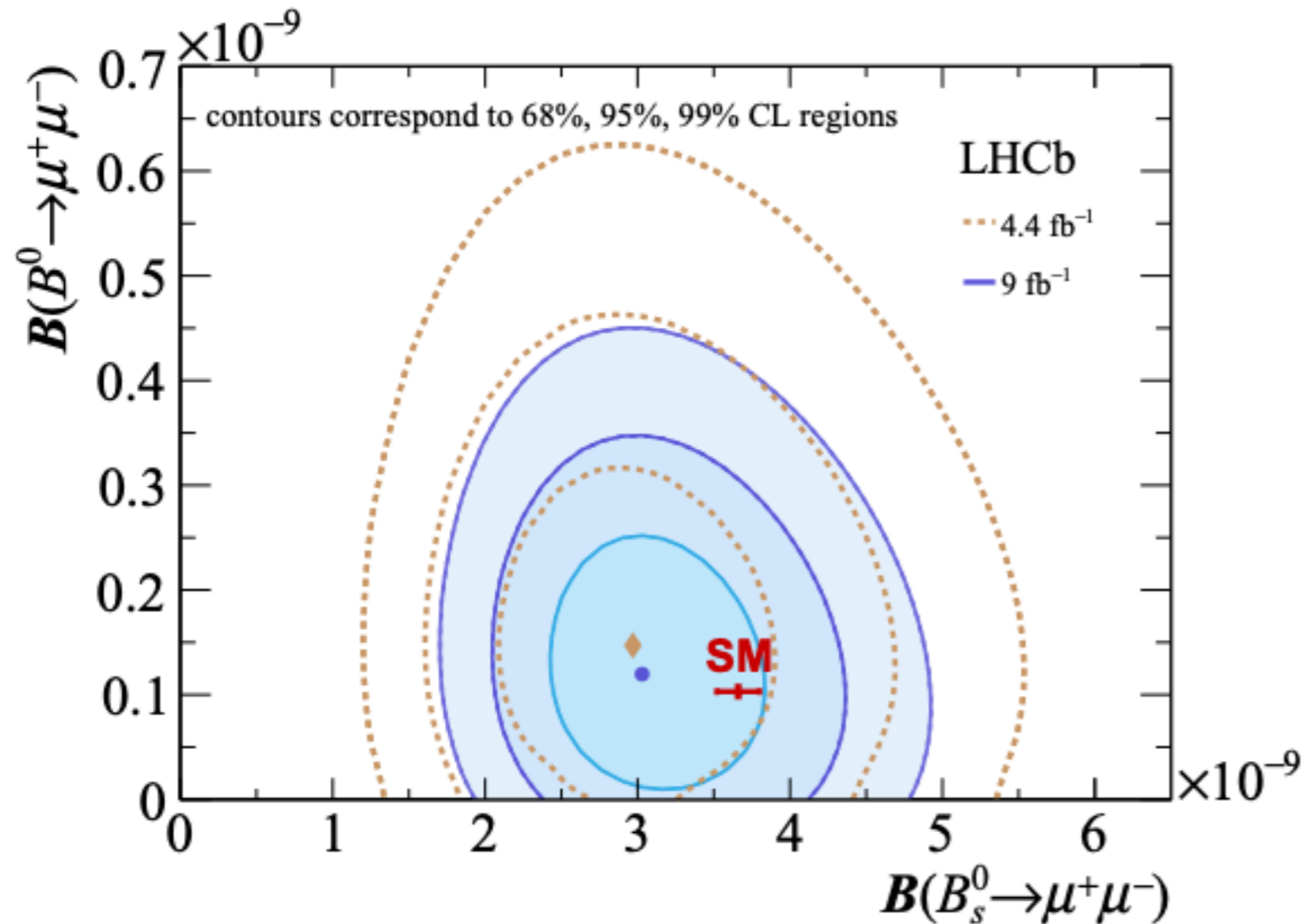
[Beneke et al. '19]

[Intermezzo] $B_s \rightarrow \mu\mu$

[Angelescu, Becirevic, Faroughy, Jaffredo, OS. '21]

[LHCb '21]

[Our exp. average: CMS, ATLAS, LHCb]



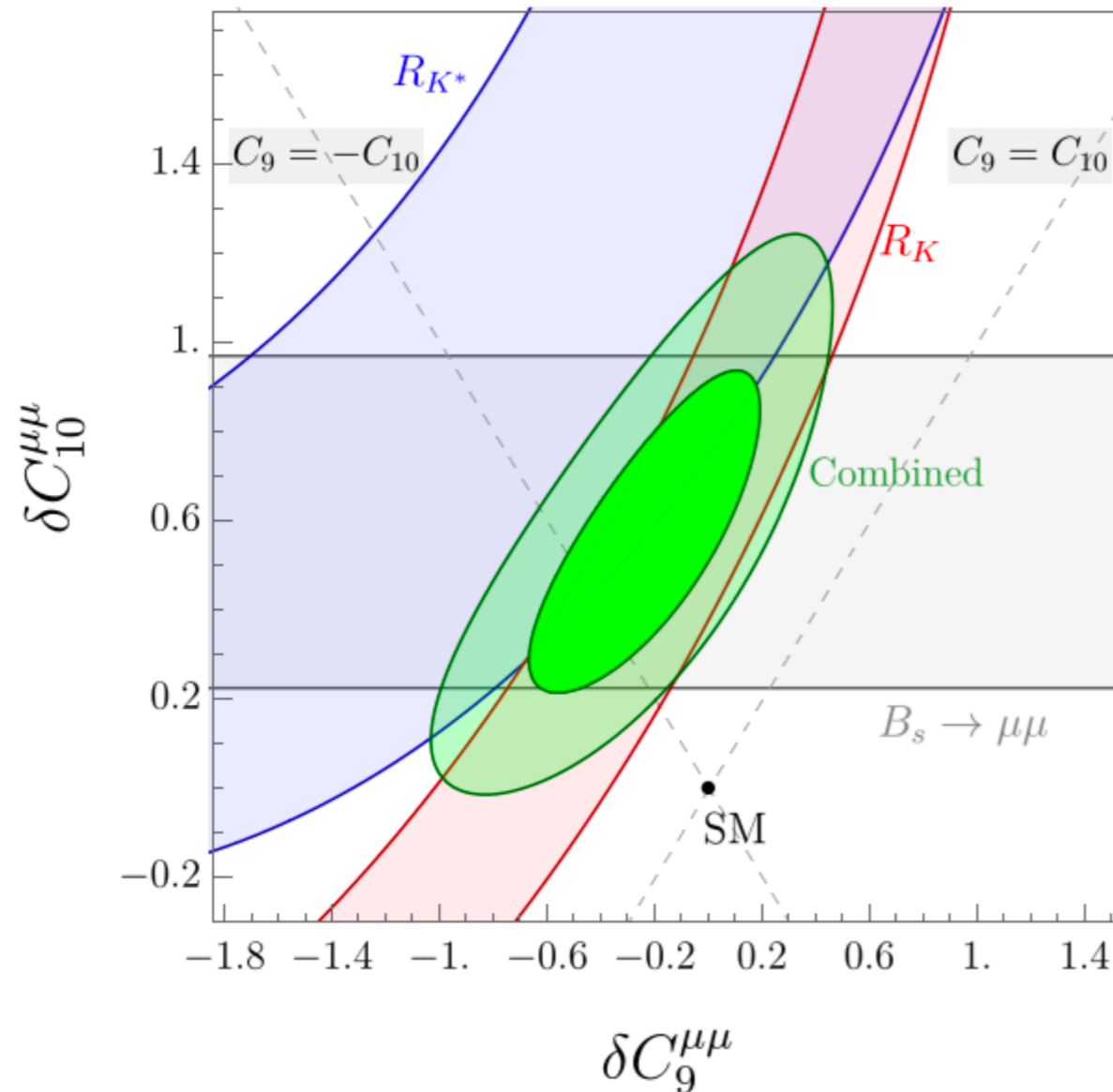
- **Good agreement** between **LHCb** results and the SM predictions;
- Small deficit in the exp. average — *due to ATLAS measurement*.

EFT for $b \rightarrow s\ell\ell$

[Angelescu, Becirevic, Faroughy, Jaffredo, OS. '21]

Clean quantities: R_K , R_{K^*} and $\mathcal{B}(B_s \rightarrow \mu\mu)$

- Only vector(axial) coefficients can accommodate data.
- $C'_{9,10}$ disfavored by $R_{K^*}^{\text{exp}} < R_{K^*}^{\text{SM}}$.
- Purely left-handed operator preferred **[4.6 σ]**:



$$\begin{aligned} \delta C_9^{\mu\mu} &= -\delta C_{10}^{\mu\mu} \\ &= -0.41 \pm 0.09 \end{aligned}$$

Interesting: Conclusion corroborated by global $b \rightarrow s\ell\ell$ fit!

[Algueró et al. '21, Altmannshofer et al. '21, Hurth et al. '21]

EFT for $b \rightarrow c\tau\bar{\nu}$

$$\mathcal{L}_{\text{eff}} = -2\sqrt{2}G_F V_{cb} \left[(1 + g_{V_L}) (\bar{c}_L \gamma_\mu b_L) (\bar{\ell}_L \gamma_\mu \nu_L) + g_{V_R} (\bar{c}_R \gamma_\mu b_R) (\bar{\ell}_L \gamma_\mu \nu_L) \right. \\ \left. + g_{S_R} (\bar{c}_L b_R) (\bar{\ell}_R \nu_L) + g_{S_L} (\bar{c}_R b_L) (\bar{\ell}_R \nu_L) + g_T (\bar{c}_R \sigma_{\mu\nu} b_L) (\bar{\ell}_R \sigma_{\mu\nu} \nu_L) \right] + \text{h.c.}$$

- $SU(3)_c \times SU(2)_L \times U(1)_Y$ gauge invariance:

⇒ g_{V_R} is LFU at dimension 6

⇒ Four coefficients left: g_{V_L} , g_{S_L} , g_{S_R} and g_T

- Several viable explanations of $R_{D^{(*)}}$:

⇒ e.g., $g_{V_L} = 0.07 \pm 0.02$, **but not only!**

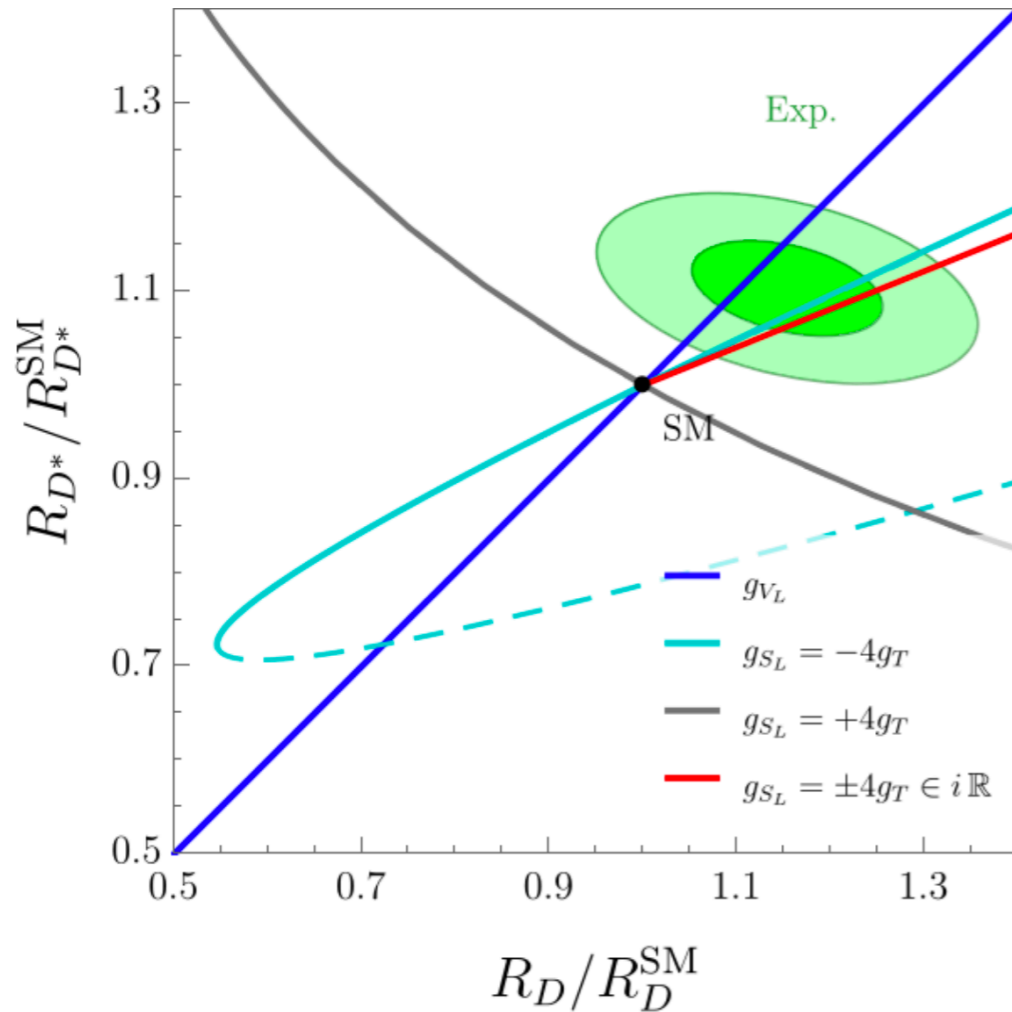
[Angelescu, Becirevic, Faroughy, Jaffredo, **OS**. '21]

see also [Murgui et al. '19, Shi et al. '19, Blanke et al. '19]

EFT for $b \rightarrow c\tau\bar{\nu}$

Which operators to pick?

[Angelescu, Becirevic, Faroughy, Jaffredo, OS. '21]



- Viable solutions (at $\mu \approx 1$ TeV):

$$\Rightarrow g_{V_L} \text{ and } g_{S_L} = \pm 4g_T$$

- More **exp. information** is **needed**:

\Rightarrow e.g., *angular observables*:

$$B \rightarrow D\tau\bar{\nu}$$

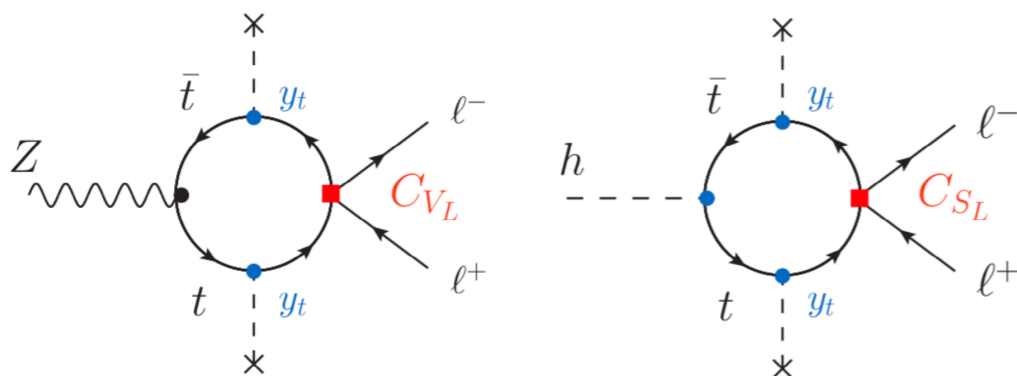
$$B \rightarrow D^*(D\pi)\tau\bar{\nu}$$

[Becirevic, Jaffredo, Peñuelas, OS. '20]

[Becirevic et al. '19], [Murgui et al. '19]

...

Electroweak/Higgs observables can also be an useful handle



[Feruglio et al. '17]

[Feruglio, Paradisi, OS. '18]

From EFTs to concrete models

From EFTs to concrete models

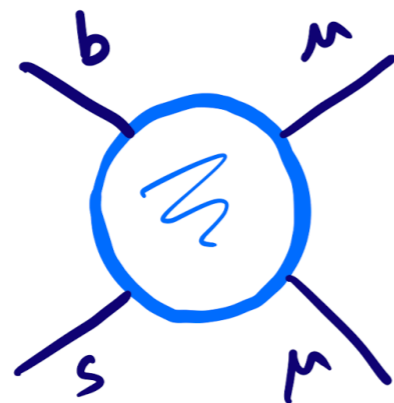
What do we know so far?

- What is the **scale of New Physics**?

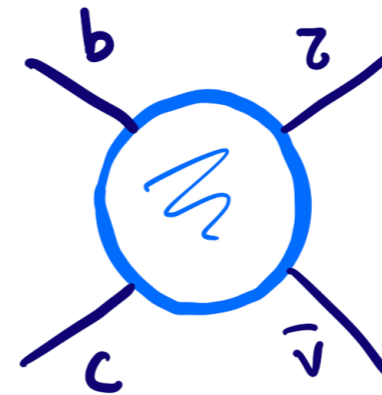
[Di Luzio et al. '17]

- For perturbative couplings:

$$\Lambda_{R_{K^{(*)}}} \lesssim 30 \text{ TeV}$$



$$\Lambda_{R_{D^{(*)}}} \lesssim 3 \text{ TeV}$$



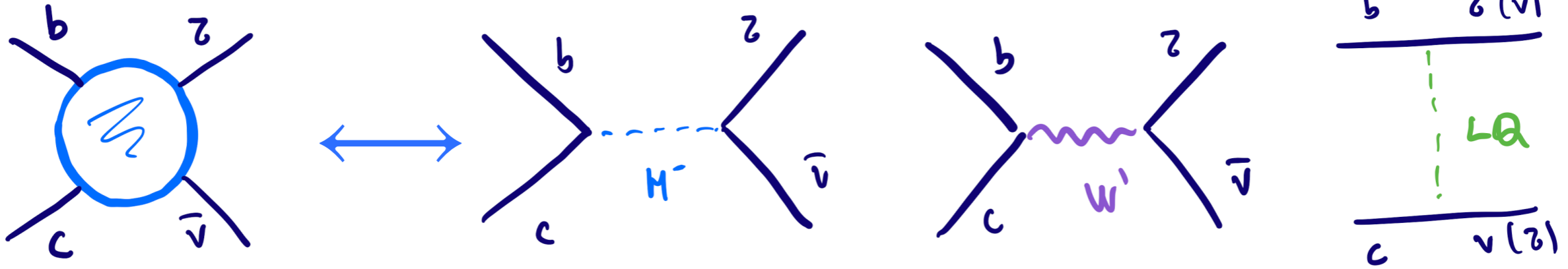
- Moreover, *good agreement* between theory and experiment in LFU tests with K -, D -meson and τ -lepton decays.

⇒ ***New Physics*** couplings to SM fermions must be hierarchical.

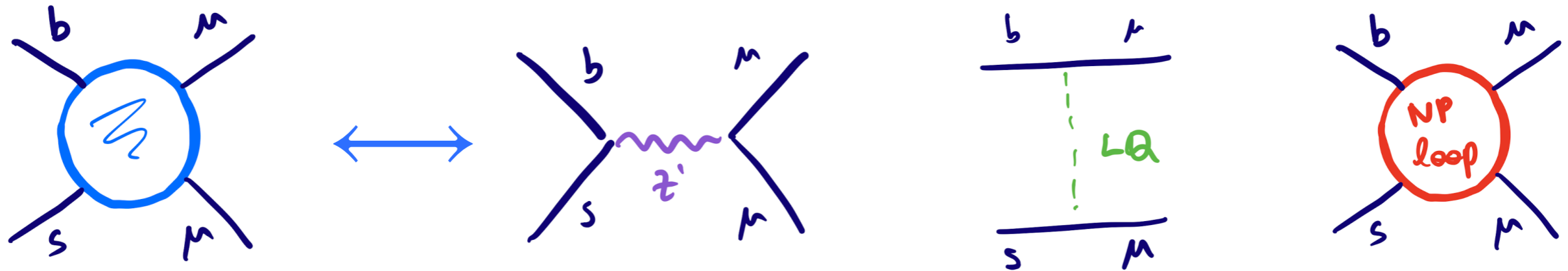
From EFTs to concrete models

Many papers in the literature...

- $b \rightarrow c\tau\bar{\nu}$:



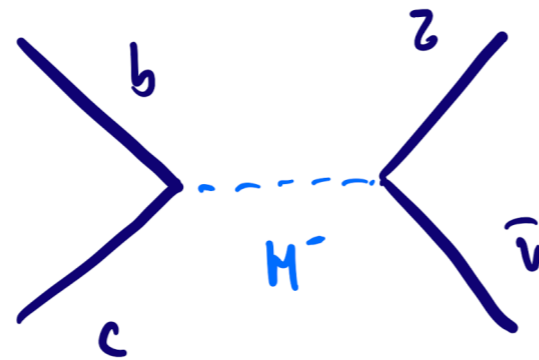
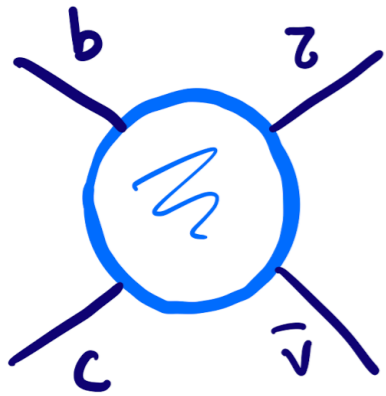
- $b \rightarrow s\ell\bar{\ell}$:



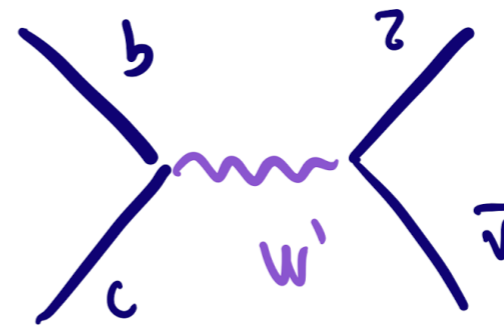
From EFTs to concrete models

Many papers in the literature...

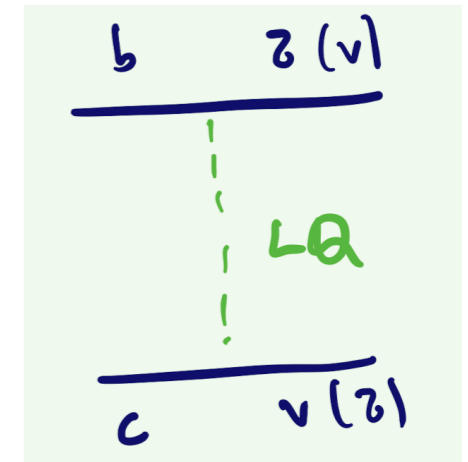
- $b \rightarrow c\tau\bar{\nu}$:



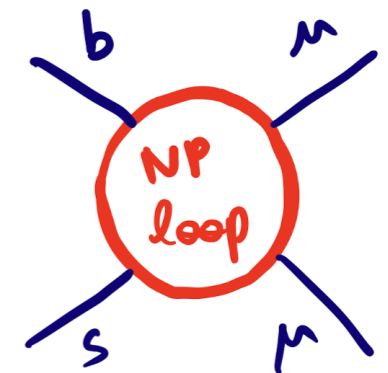
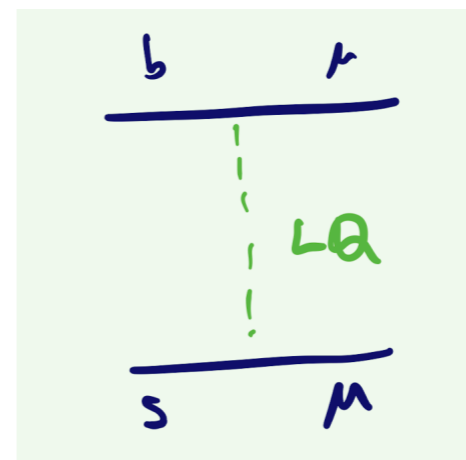
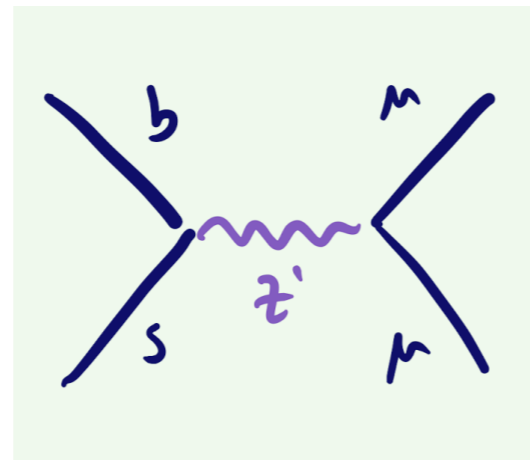
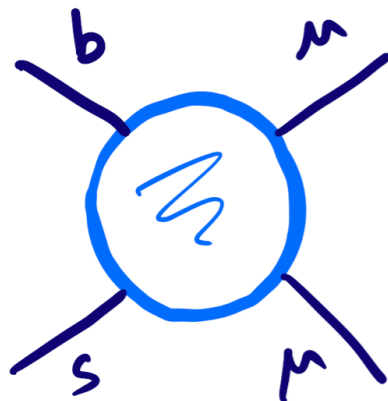
$(B_c\text{-meson lifetime})$



$(\Delta F = 2, pp \rightarrow \tau\tau\dots)$



- $b \rightarrow s\ell\bar{\ell}$:



Challenging task because of the numerous exp. constraints: *flavor, LHC, EWPT...*

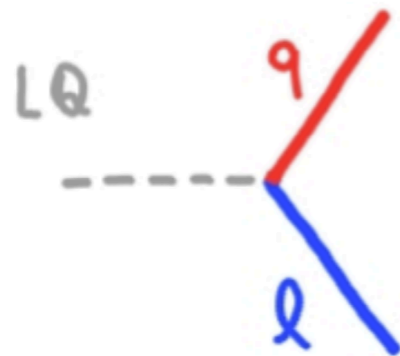
Which leptoquark?

[Angelescu, Becirevic, Faroughy, Jaffredo, OS. '21]

[Buchmuller, Wyler. '88]

Few scenarios are viable!

$(SU(3)_c, SU(2)_L, U(1)_Y)$



Model		$R_{K^{(*)}}$	$R_{D^{(*)}}$	$R_{K^{(*)}} \& R_{D^{(*)}}$
Spin 0	$S_3 \ (\bar{\mathbf{3}}, \mathbf{3}, 1/3)$	✓	✗	✗
	$S_1 \ (\bar{\mathbf{3}}, \mathbf{1}, 1/3)$	✗	✓	✗
	$R_2 \ (\mathbf{3}, \mathbf{2}, 7/6)$	✗	✓	✗
Spin 1	$U_1 \ (\mathbf{3}, \mathbf{1}, 2/3)$	✓	✓	✓
	$U_3 \ (\mathbf{3}, \mathbf{3}, 2/3)$	✓	✗	✗

- Only the U_1 LQ can do the job alone, but UV completion needed.

- $\mathcal{G}_{PS} = SU(4) \times SU(2)_L \times SU(2)_R$ contains $U_1 \sim (\mathbf{3}, \mathbf{1}, 2/3)$

See back-up!

- Viable TeV models proposed: $U_1 + Z' + g'$ (more than one mediator!)

[Di Luzio et al. '17, Bordone et al. '18, Blanke et al. '18...]

- Two scalar LQs are also viable:

- $S_1 \& S_3$, or $R_2 \& S_3$.

[Becirevic et al. '18]

[Crivellin et al. '17, Marzocca '18]

From LFUV to high- p_T physics

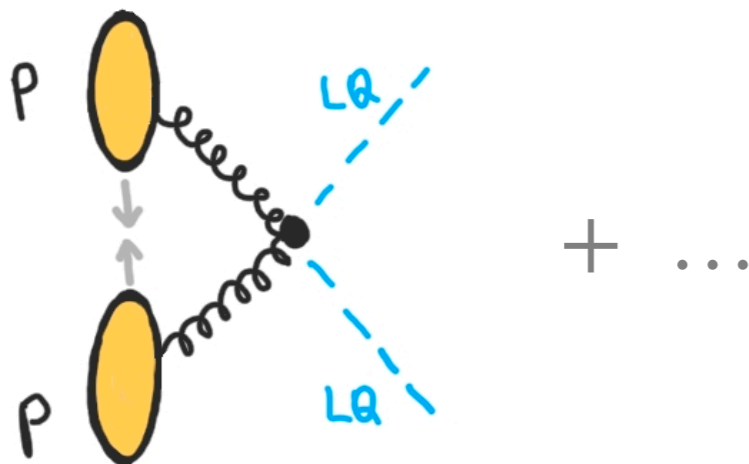
LHC constraints

See talk by K. Yong Sheng!

i. LQ pair-production

Production dominated by QCD:

$$\sigma(pp \rightarrow \text{LQ LQ}^\dagger) \times \underbrace{\mathcal{B}(\text{LQ} \rightarrow \ell q)^2}_{\equiv \beta^2}$$



see [Dorsner et al. '18] for a recent review

ATLAS and CMS results for $\beta = 1$ (or 0.5)

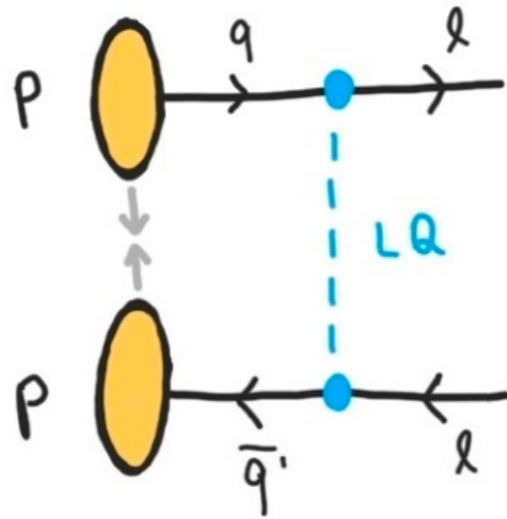
Decays	Scalar LQ limits	Vector LQ limits	\mathcal{L}_{int} / Ref.
$jj \tau\bar{\tau}$	–	–	–
$b\bar{b} \tau\bar{\tau}$	1.0 (0.8) TeV	1.5 (1.3) TeV	36 fb ⁻¹ [39]
$t\bar{t} \tau\bar{\tau}$	1.4 (1.2) TeV	2.0 (1.8) TeV	140 fb ⁻¹ [40]
$jj \mu\bar{\mu}$	1.7 (1.4) TeV	2.3 (2.1) TeV	140 fb ⁻¹ [41]
$b\bar{b} \mu\bar{\mu}$	1.7 (1.5) TeV	2.3 (2.1) TeV	140 fb ⁻¹ [41]
$t\bar{t} \mu\bar{\mu}$	1.5 (1.3) TeV	2.0 (1.8) TeV	140 fb ⁻¹ [42]
$jj \nu\bar{\nu}$	1.0 (0.6) TeV	1.8 (1.5) TeV	36 fb ⁻¹ [43]
$b\bar{b} \nu\bar{\nu}$	1.1 (0.8) TeV	1.8 (1.5) TeV	36 fb ⁻¹ [43]
$t\bar{t} \nu\bar{\nu}$	1.2 (0.9) TeV	1.8 (1.6) TeV	140 fb ⁻¹ [44]

[Angelescu, Becirevic, Faroughy, Jaffredo, OS. '21]

LHC constraints

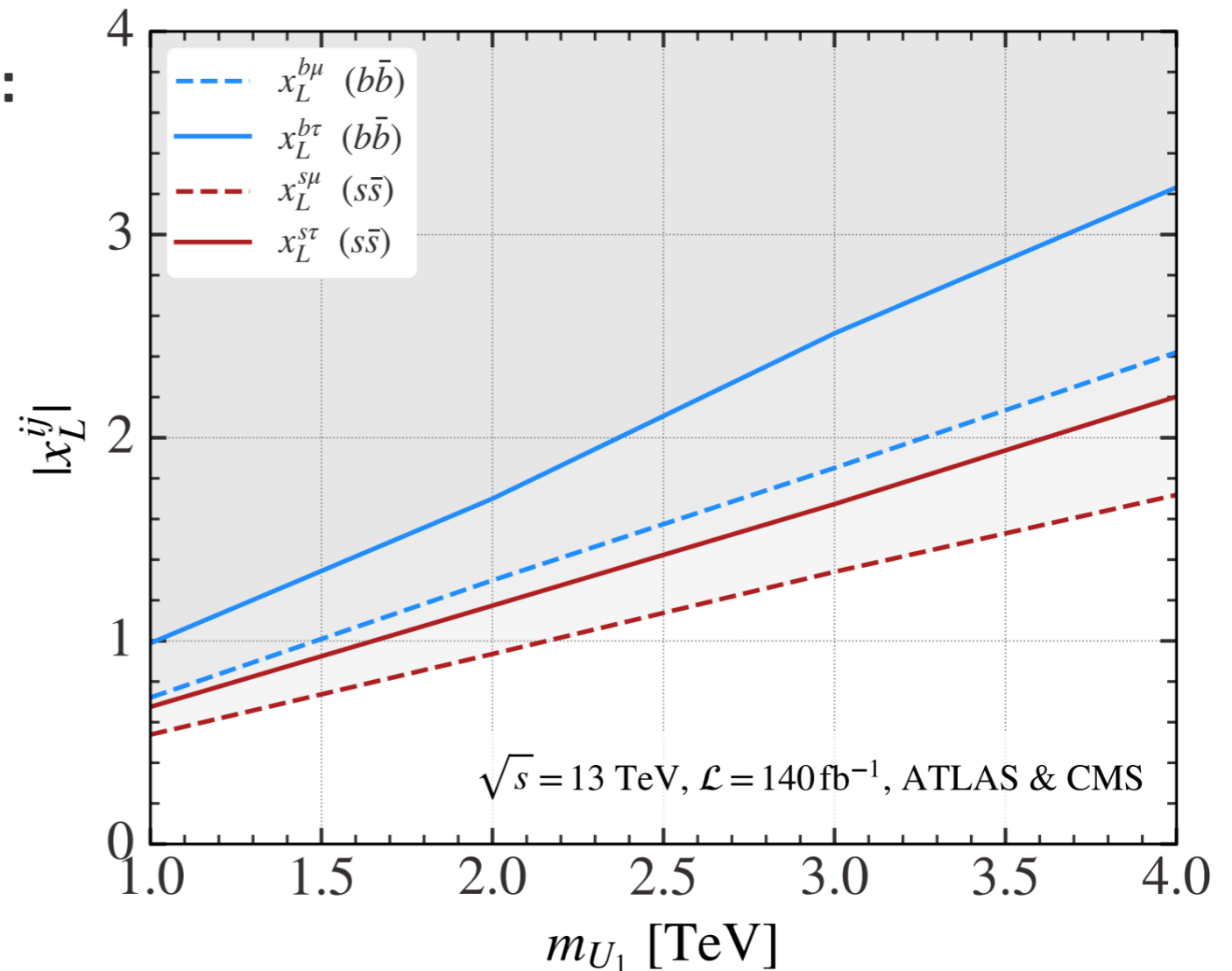
ii. Di-lepton production at high- p_T

Useful upper limits on LQ couplings:



Example: $U_1 \sim (3, 1, 2/3)$

$$\mathcal{L}_{U_1} = x_L^{ij} \bar{Q}_i \gamma^\mu L_j U_1^\mu + \text{h.c.}$$



[Angelescu, Becirevic, Faroughy, Jaffredo, **OS**. '21]

First considered by [Eboli, '88]

High- p_T package

[Allwicher, Faroughy, Jaffredo, OS, Wilsch. 2204.XXXXXX]

<<HighPT`



HighPT : **High- p_T Tails**

Authors : **Lukas Allwicher, Darius A. Faroughy, Florentin Jaffredo, Olcyr Sumensari, and Felix Wilsch**

Reference : **arXiv:22xx.xxxxx**

Website : **<https://github.com/HighPT/HighPT>**

HighPT is free software under the terms of the MIT License.

Please submit bugs and feature requests using GitHub's issue system at:

<https://github.com/HighPT/HighPT/issues>

Recast of LHC searches for the SMEFT and simplified scenarios



$$pp \rightarrow \tau\tau$$

$$pp \rightarrow ee, \mu\mu$$

$$pp \rightarrow \tau\nu$$

$$pp \rightarrow e\nu, \mu\nu$$

$$pp \rightarrow e\mu, e\tau, \mu\tau$$

[arXiv:2002.12223]

CMS-PAS-EXO-19-019

ATLAS-CONF-2021-025

[arXiv:1906.05609]

CMS-PAS-EXO-19-014

High- p_T package

[Allwicher, Faroughy, Jaffredo, OS, Wilsch. 2204.XXXXXX]

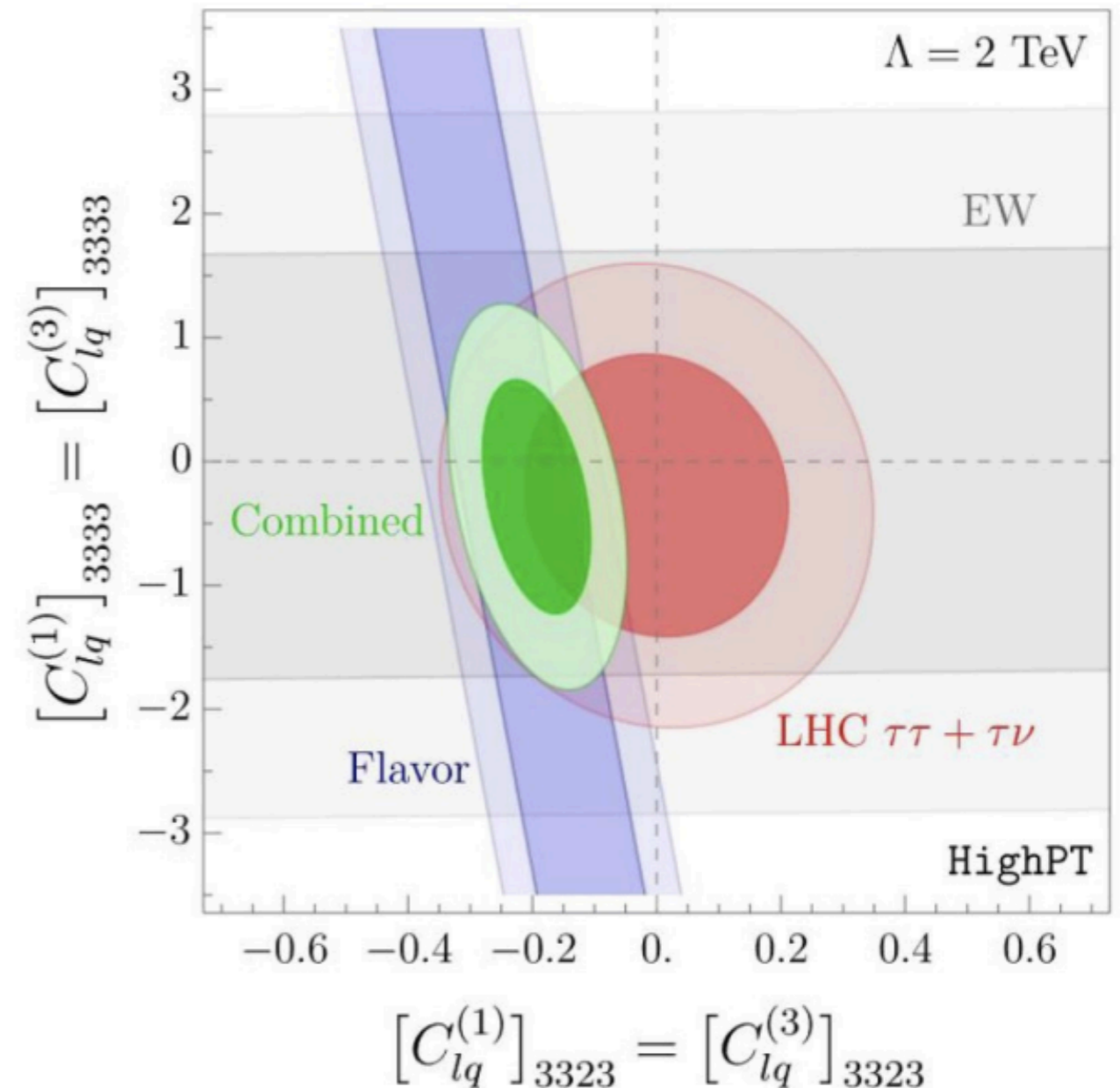
Example: SMEFT

Effective operators predicted by the $U_1 \sim (\mathbf{3}, \mathbf{1}, 2/3)$ leptoquark:

$$[C_{lq}^{(1)}]_{ijkl} = (\bar{L}_i \gamma^\mu L_j) (\bar{Q}_k \gamma_\mu Q_l)$$

$$[C_{lq}^{(3)}]_{ijkl} = (\bar{L}_i \gamma^\mu \tau^I L_j) (\bar{Q}_k \gamma_\mu \tau^I Q_l)$$

High- p_T constraints are needed to remove the flat direction!



Predictions at low-energies

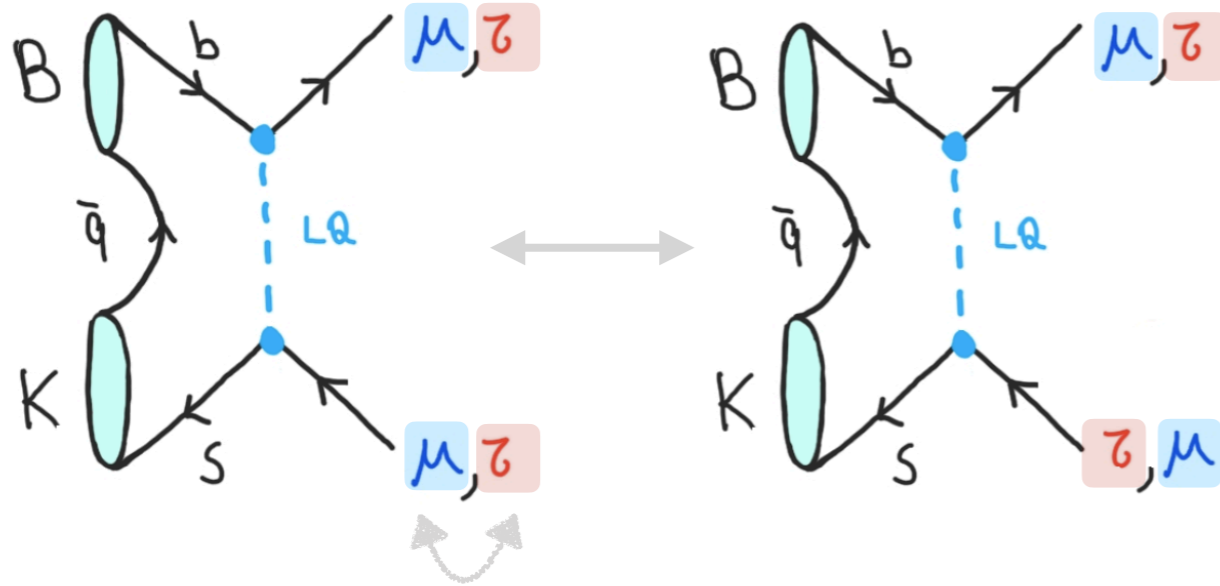
- LFV in *B*-decays
- *B*-decays with missing energy

Lepton Flavor Violation

[Angelescu, Becirevic, Faroughy, Jaffredo, OS. '21]

see also [Glashow et al. '14]

- LFUV \leftrightarrow LFV:



Predictions for

$$B_s \rightarrow \mu\tau \quad B \rightarrow K^{(*)}\mu\tau$$

New searches (95% CL): [LHCb]

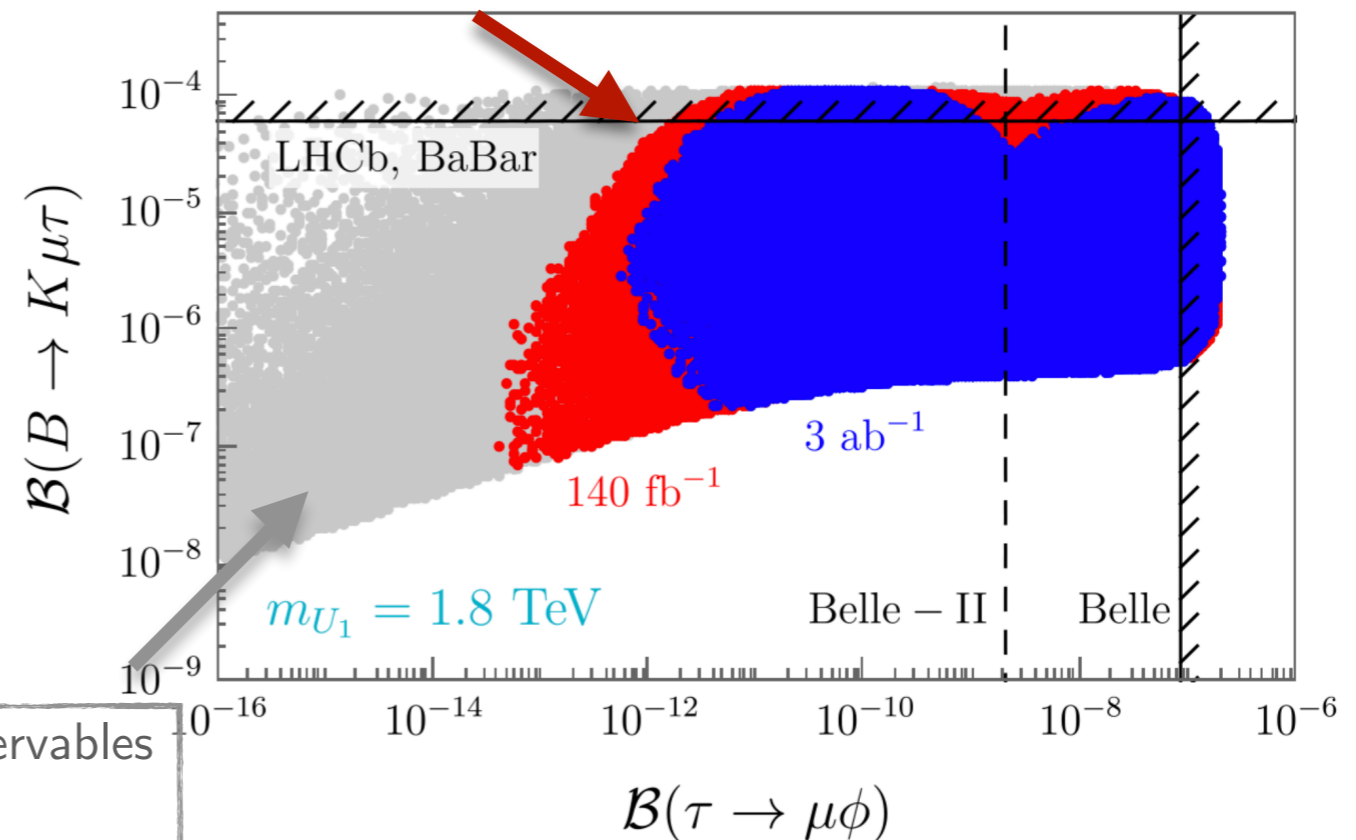
$$\mathcal{B}(B_s \rightarrow \mu\tau)^{\text{exp}} < 4.2 \times 10^{-5}$$

$$\mathcal{B}(B \rightarrow K^{(*)}\mu\tau)^{\text{exp}} < 4.5 \times 10^{-5}$$

High- p_T constraints set lower bounds on $\mathcal{B}(B \rightarrow K\mu\tau)$!

LHC constraints

Example: $U_1 \sim (3, 1, 2/3)$



Several flavor observables
(at tree-level)

B-decays with missing energy

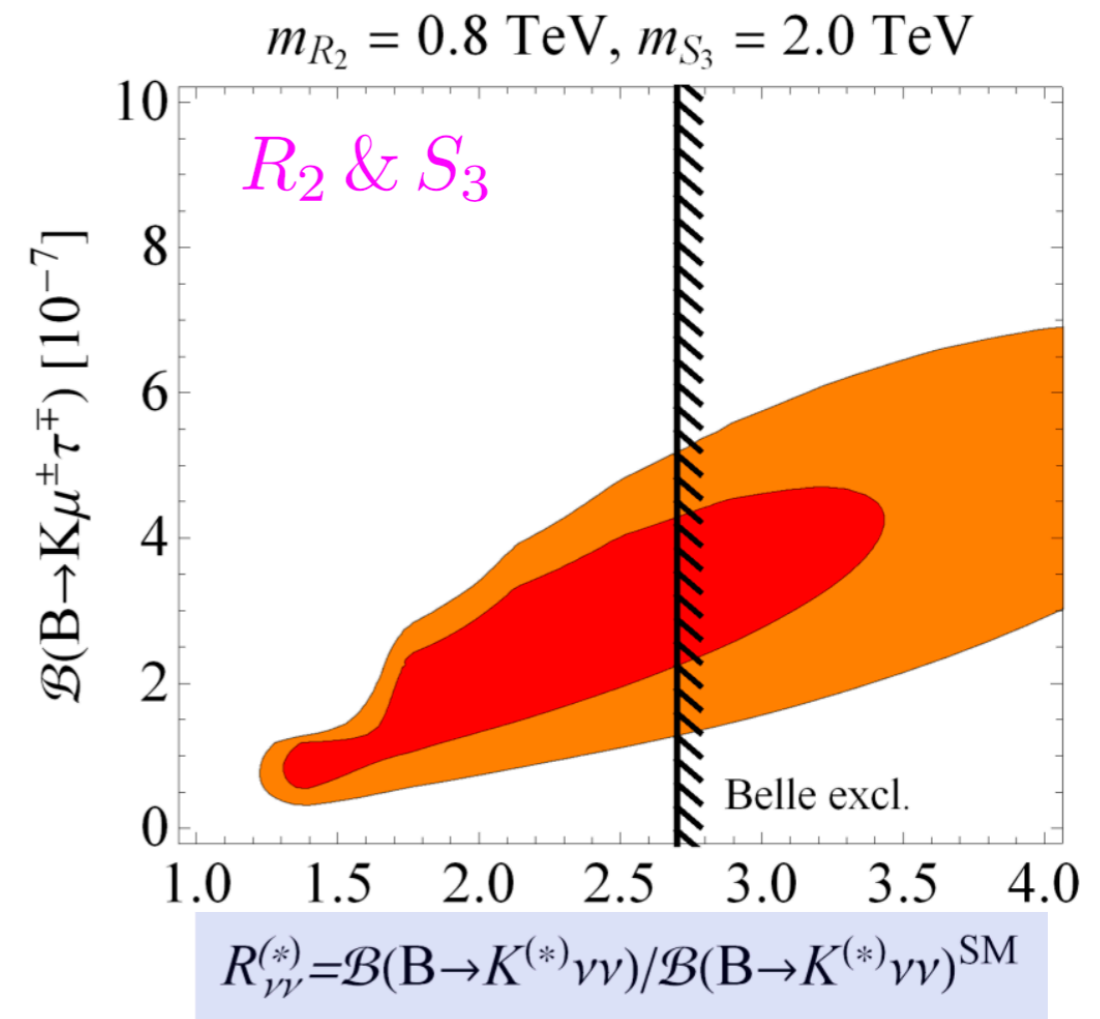
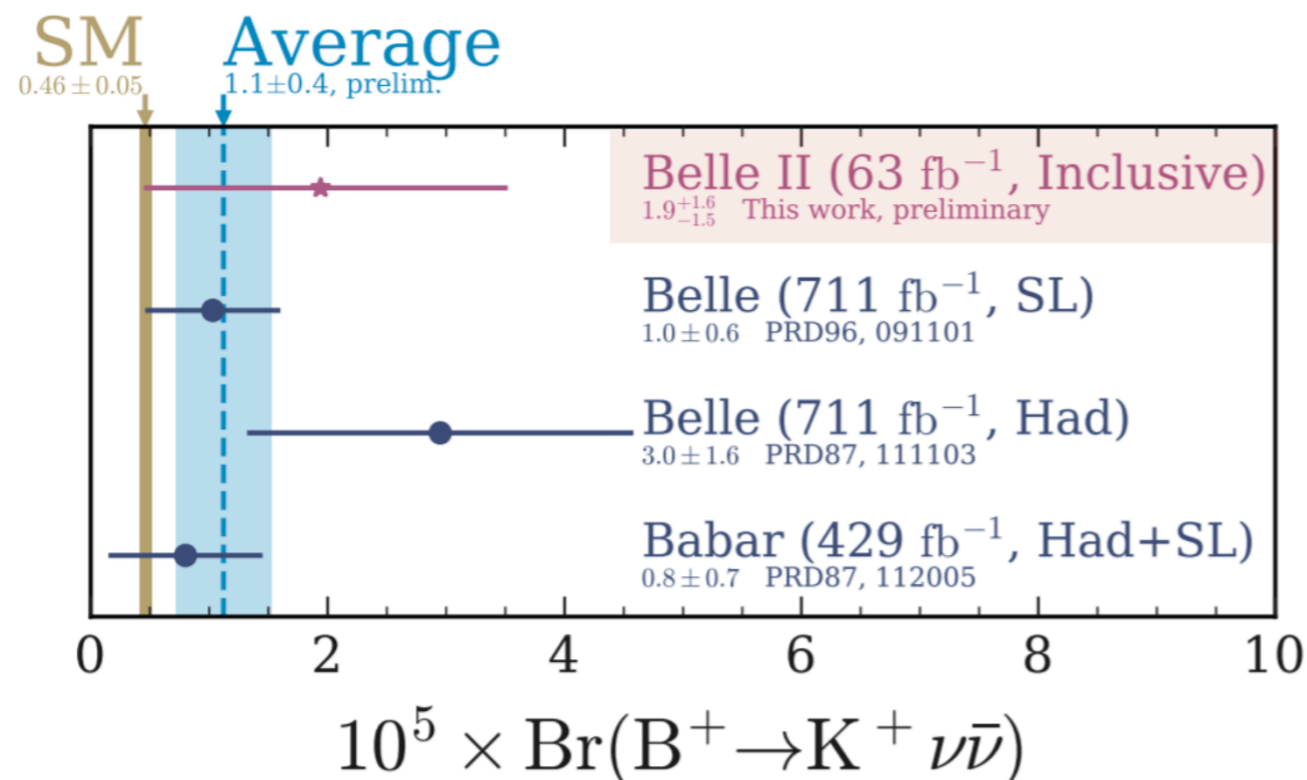
e.g. [Becirevic et al. '18]

- Clean observable in the SM:

$$\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu})^{\text{SM}} = 4.6(5) \times 10^{-6}$$

[Buras et al. '14, Blake et al. '16]

- Models for the **B-anomalies** predict **sizable deviations** from SM predictions.
- Unique access to operators with (left-handed) **τ -leptons**; i.e. $L_3 = (\nu_{\tau L}, \tau_L)^T$.



Promising results from early **Belle-II data!**

Summary and perspectives

- Renewed interest in B -physics anomalies since the latest LHCb results.

Wait for Belle-II for an independent cross-check!

- We identified the mediators that can explain $R_{K^{(*)}}$ and/or $R_{D^{(*)}}$.

Only the vector U_1 is viable. Two scalar LQs can do the job too.

- There is a pronounced complementarity of flavory-physics constraints with those obtained from high- p_T searches at the LHC.

LHC di-tau constraints \Rightarrow lower bound $\mathcal{B}(B \rightarrow K^{(*)} \mu \tau) \gtrsim \text{few} \times 10^{-7}$

- Many upcoming low-energy measurements will be fundamental to refute or confirm the remaining viable models.

$$R_{D^{(*)}, D_s^{(*)}, \Lambda_c^{(*)}, \dots} \quad R_{K^{(*)}, \phi, \dots} \quad B \rightarrow K^{(*)} \mu \tau \quad B \rightarrow K^{(*)} \nu \bar{\nu} \quad \dots$$

- Building a minimal model to simultaneously explain the various anomalies in flavor observables remain a challenging task.

Data-driven model building!

Thank you!

Back-up

SM predictions

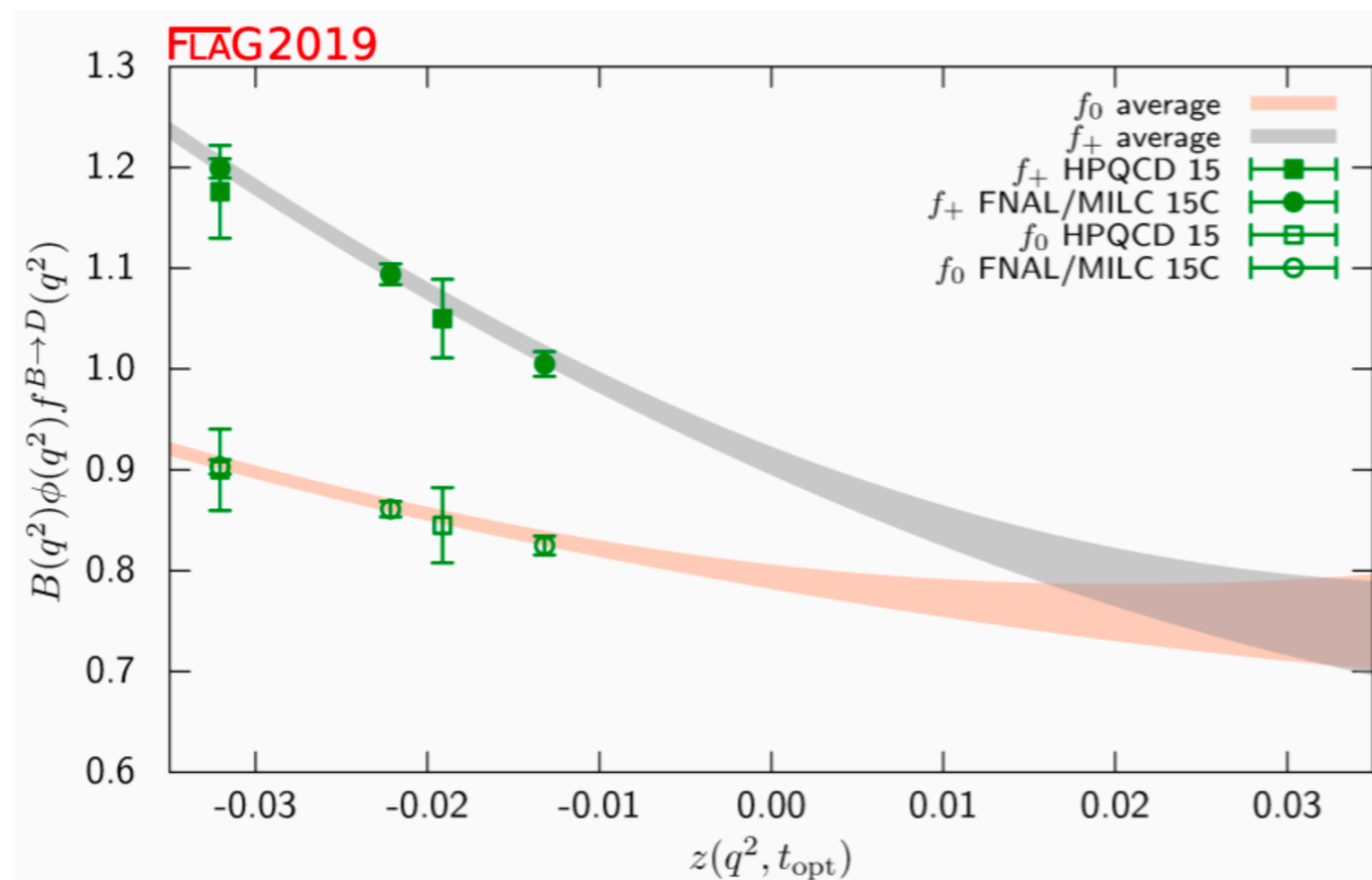
Form-factors: R_D

- **Lattice QCD** at $q^2 \neq q_{\max}^2$ ($w \neq 1$) available for both leading (vector) and subleading (scalar) form-factors:

$$\langle D(k) | \bar{c} \gamma^\mu b | B(p) \rangle = \left[(p+k)^\mu - \frac{m_B^2 - m_D^2}{q^2} q^\mu \right] f_+(q^2) + q^\mu \frac{m_B^2 - m_D^2}{q^2} f_0(q^2)$$

with $f_+(0) = f_0(0)$

[MILC/Fermilab '15, HPQCD '15]



[FLAG' 21] average:

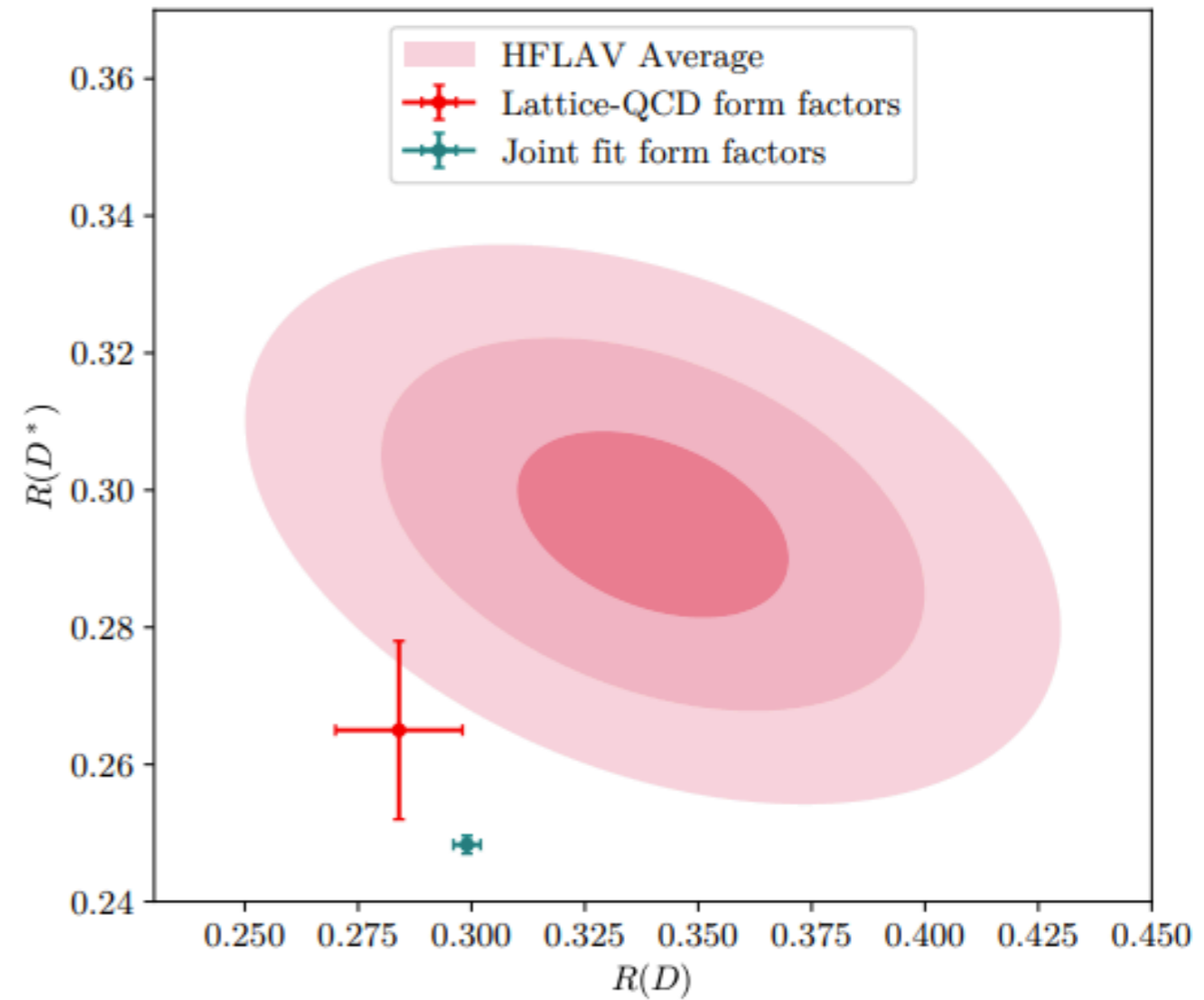
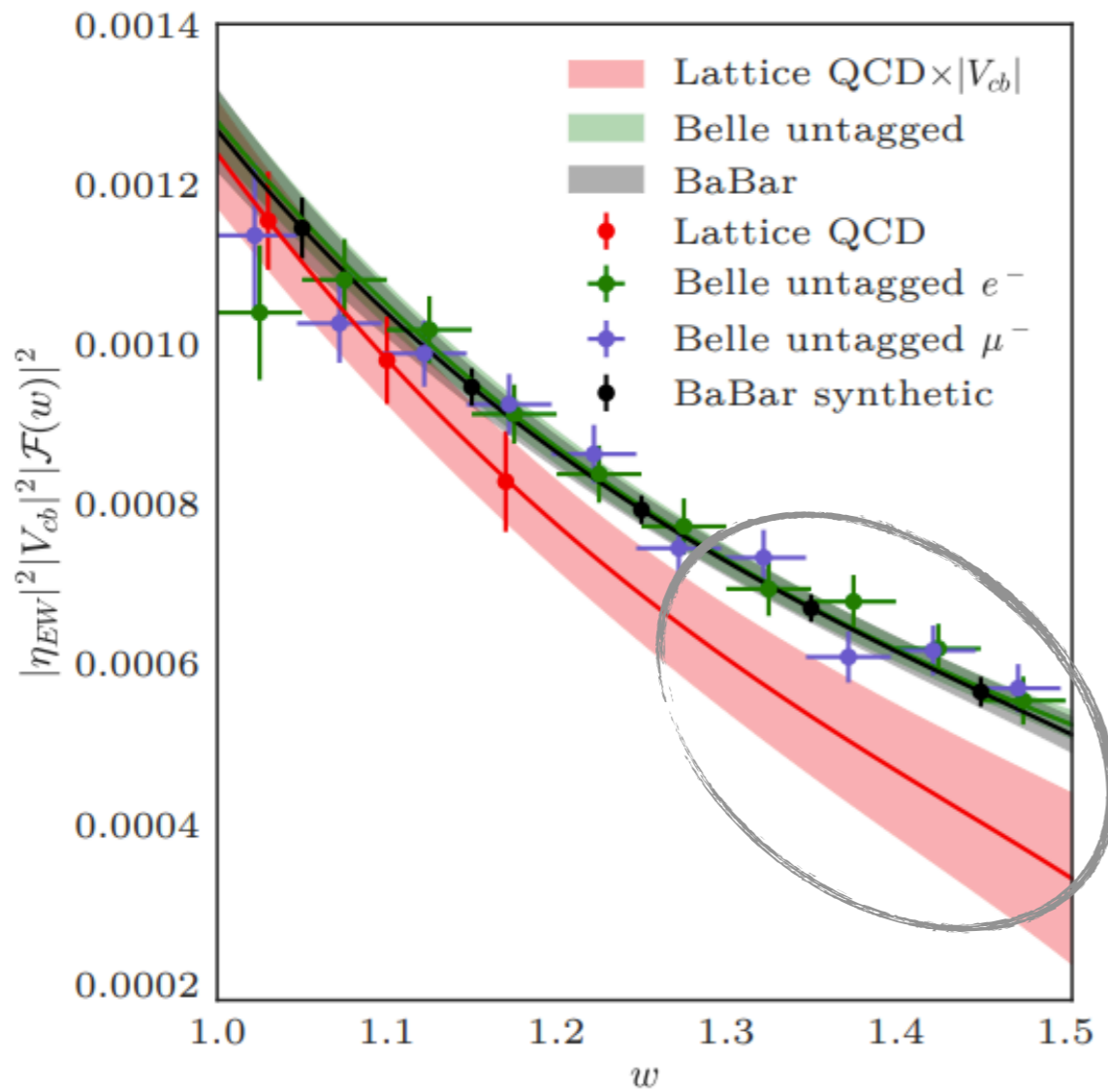
$$R_D^{\text{SM}} = 0.300(10)$$

Warning!

[MILC/Fermilab, 2105.14019]

$$\frac{d\mathcal{B}}{dq^2}(B \rightarrow D^* \ell \nu) \propto |V_{cb}|^2 |\mathcal{F}(w)|^2$$

$$\left[w = \frac{m_B^2 + m_{D^*}^2 - q^2}{2m_B m_{D^*}} \right]$$



[Intermezzo] How to improve the SM prediction for R_{D^*} ?

- **Theory uncertainties** are related to m_τ , i.e the only source of **LFU breaking** in the SM:

$$\frac{d\mathcal{B}}{dq^2}(B \rightarrow D^* \ell \bar{\nu}) = \Phi(q^2) \omega_\ell(q^2) \left[H_V(q^2)^2 + \frac{m_\ell^2}{m_\ell^2 + 2q^2} H_S(q^2)^2 \right] \quad (\text{see back-up})$$

$$\propto A_1(q^2), A_2(q^2), V(q^2) \quad \propto A_0(q^2)$$

- A **simple redefinition** can reduce these uncertainties:

$$R_{D^*}^{(\tau/\mu)} = \frac{\int_{m_\tau^2}^{q_{\max}^2} dq^2 \frac{d\mathcal{B}}{dq^2}(B \rightarrow D^* \tau \bar{\nu})}{\int_{m_\mu^2}^{q_{\max}^2} dq^2 \frac{d\mathcal{B}}{dq^2}(B \rightarrow D^* \mu \bar{\nu})} \quad \longrightarrow \quad R_{D^*}^{(\tau/\mu)}[q_{\min}^2] = \frac{\int_{q_{\min}^2}^{q_{\max}^2} dq^2 \frac{d\mathcal{B}}{dq^2}(B \rightarrow D^* \tau \bar{\nu})}{\int_{q_{\min}^2}^{q_{\max}^2} dq^2 \frac{d\mathcal{B}}{dq^2}(B \rightarrow D^* \mu \bar{\nu})}$$

	Observable	Latt.	Latt. +Exp
Usual definition	R_{D^*}	0.27(1) [5%]	0.248(1) [0.5 %]
Definition with same bins	$R_{D^*}[m_\tau^2]$	0.343(6) [2%]	0.337(1) [0.4%]
	$R_{D^*}[5 \text{ GeV}^2]$	0.422(3) [0.5 %]	0.422(1) [0.2%]

[Isidori, OS. '20]

NB. Re-weighting of the muon rate by $\omega_\tau(q^2)/\omega_\mu(q^2)$ can further reduce the theory uncertainties.

Example: $U_1 = (3, 1, 2/3)$

[Angelescu, Becirevic, Faroughy, OS. '18]

$$\mathcal{L} = x_L^{ij} \bar{Q}_i \gamma_\mu U_1^\mu L_j + x_R^{ij} \bar{d}_{Ri} \gamma_\mu U_1^\mu \ell_{Rj} + \text{h.c.},$$

- $b \rightarrow c\tau\bar{\nu}$:

$$\mathcal{L}_{\text{eff}} \supset -\frac{(x_L^{b\tau})^* (Vx_L)^{c\tau}}{m_{U_1}^2} (\bar{c}_L \gamma^\mu b_L) (\bar{\tau}_L \gamma_\mu \nu_L)$$

- $b \rightarrow s\mu\mu$:

$$\mathcal{L}_{\text{eff}} \supset -\frac{(x_L)^{s\mu} (x_L^{b\mu})^*}{m_{U_1}^2} (\bar{s}_L \gamma^\mu b_L) (\bar{\mu}_L \gamma_\mu \mu_L)$$

$$x_L = \begin{pmatrix} 0 & 0 & 0 \\ 0 & x_L^{s\mu} & x_L^{s\tau} \\ 0 & x_L^{b\mu} & x_L^{b\tau} \end{pmatrix}$$

- Other observables: $\tau \rightarrow \mu\phi$, $B \rightarrow \tau\bar{\nu}$, $D_{(s)} \rightarrow \mu\bar{\nu}$, $D_s \rightarrow \tau\bar{\nu}$,
 $K \rightarrow \mu\bar{\nu}/K \rightarrow e\bar{\nu}$, $\tau \rightarrow K\bar{\nu}$ and $B \rightarrow D^{(*)}\mu\bar{\nu}/B \rightarrow D^{(*)}e\bar{\nu}$.

UV completion: $U_1 = (\mathbf{3}, \mathbf{1}, 2/3)$

Pati-salam unification:

[Pati, Salam. '74]

- $\mathcal{G}_{\text{PS}} = SU(4) \times SU(2)_L \times SU(2)_R$ contains U_1 as gauge boson.
- Main difficulty: flavor universal $\Rightarrow m_{U_1} \gtrsim 100 \text{ TeV}$ from FCNC.

Viable scenario for B-anomalies:

[Di Luzio et al. '17]

- $SU(4) \times SU(3)' \times SU(2)_L \times U(1)'$ $\rightarrow \mathcal{G}_{\text{SM}} = SU(3)_c \times SU(2)_L \times U(1)_Y$
- Flavor violation from (ad-hoc) mixing with vector-like fermions.
- Main feature: $U_1 + Z' + g'$ at the **TeV scale**.

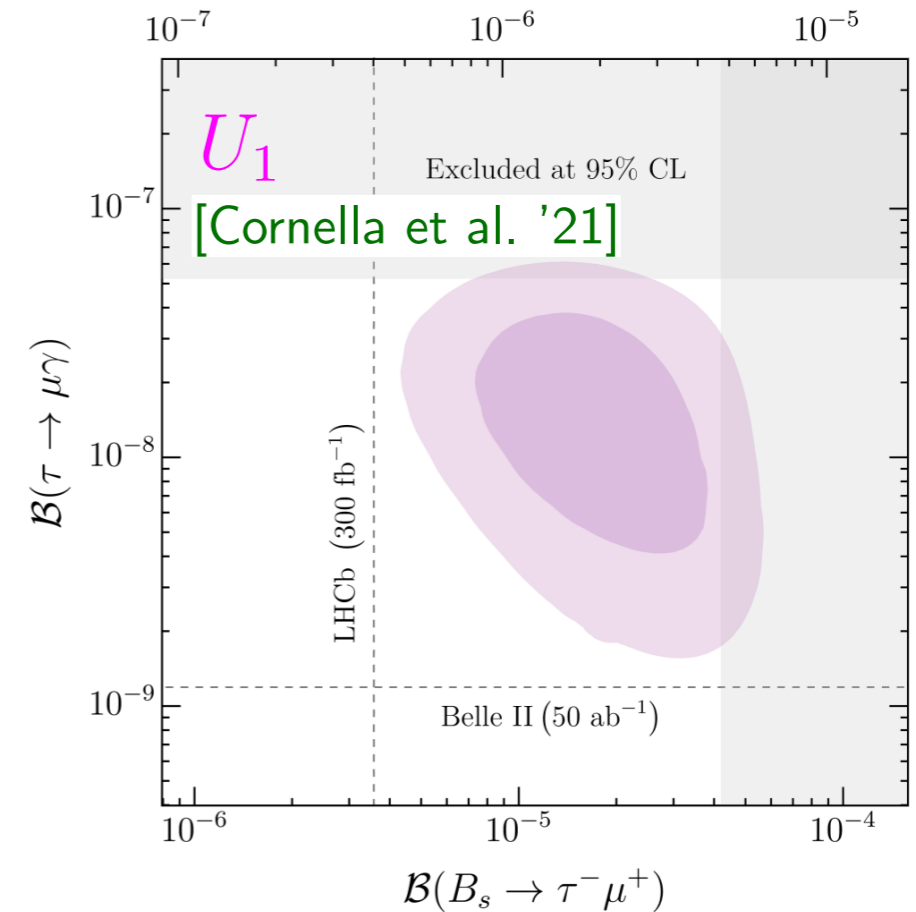
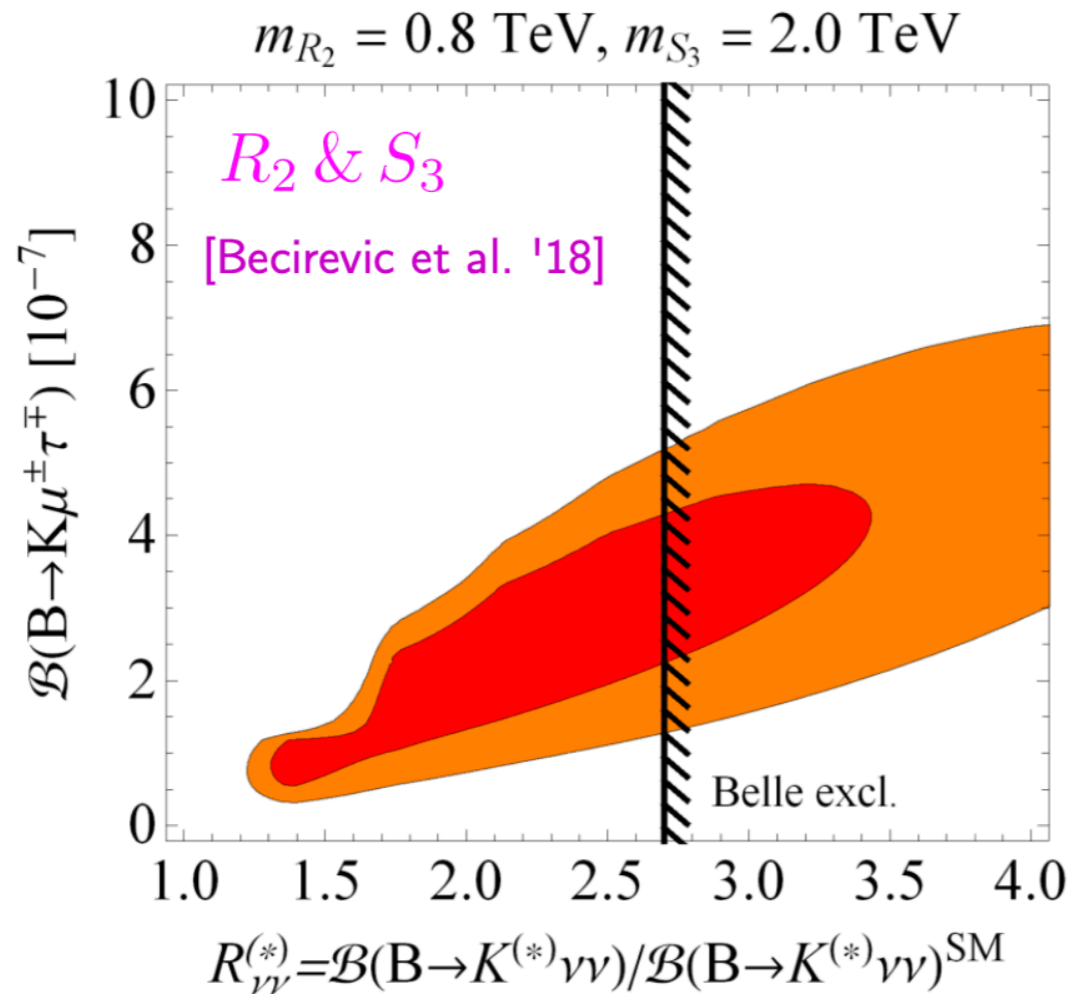
Rich LHC pheno, cf. [Baker et al. '19], [Di Luzio et al. '18]

Step beyond: $[\text{PS}]^3 = [SU(4) \times SU(2)_L \times SU(2)_R]^3$

[Bordone et al. '17]

- Hierarchical LQ couplings fixed by symmetry breaking pattern.
- **Explanation** of fermion masses and mixing (**flavor puzzle**)!

Large contributions to $b \rightarrow s\mu\tau$ is a **prediction** of the minimalistic solutions to the **B -physics anomalies**.



EFT predictions:

[Becirevic, OS, Zukanovich. '16]

i. LH operators:

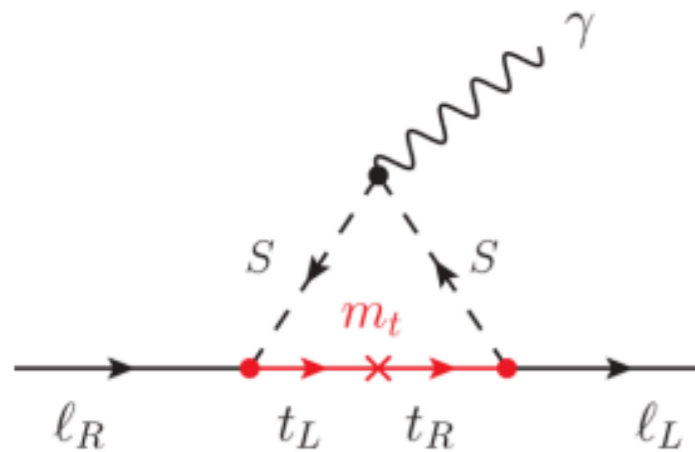
$$\frac{\mathcal{B}(B_s \rightarrow \mu\tau)}{\mathcal{B}(B \rightarrow K\mu\tau)} \simeq 0.8, \quad \frac{\mathcal{B}(B \rightarrow K^*\mu\tau)}{\mathcal{B}(B \rightarrow K\mu\tau)} \simeq 1.8$$

ii. Scalar operators:

$$\frac{\mathcal{B}(B_s \rightarrow \mu\tau)}{\mathcal{B}(B \rightarrow K^{(*)}\mu\tau)} \gg 1$$

Scalar LQs for $(g - 2)_\mu$

- LQs should couple to $\bar{\mu}_L q_R S$ and $\bar{\mu}_R q_L S$:



Symbol	$(SU(3)_c, SU(2)_L, U(1)_Y)$	Interactions	$F = 3B + L$
S_3	$(\bar{\mathbf{3}}, \mathbf{3}, 1/3)$	$\bar{Q}^C L$	-2
R_2	$(\mathbf{3}, \mathbf{2}, 7/6)$	$\bar{u}_R L, \bar{Q} e_R$	0
\tilde{R}_2	$(\mathbf{3}, \mathbf{2}, 1/6)$	$\bar{d}_R L$	0
\tilde{S}_1	$(\bar{\mathbf{3}}, \mathbf{1}, 4/3)$	$\bar{d}_R^C e_R$	-2
S_1	$(\bar{\mathbf{3}}, \mathbf{1}, 1/3)$	$\bar{Q}^C L, \bar{u}_R^C e_R$	-2

[Cheung. '01], [Crivellin et al. '20], [Dorsner, Fajfer, OS. '19]

\Rightarrow Two viable candidates (R_2 and S_1), but *not the ones needed for $R_{K^{(*)}}$* .

\Rightarrow Connection to $R_{D^{(*)}}$ is difficult due to *LFV bounds*: $\tau \rightarrow \mu\gamma$.

See [Gherardi et al., '20] for the best attempt so far; tuning needed to avoid LFV bounds, tension with Δm_{B_s} (?) .

Minimal solutions to B -physics anomalies and muon $g-2$ do not point to the **same interactions.** Possible in next-to-minimal scenarios (many papers...)