

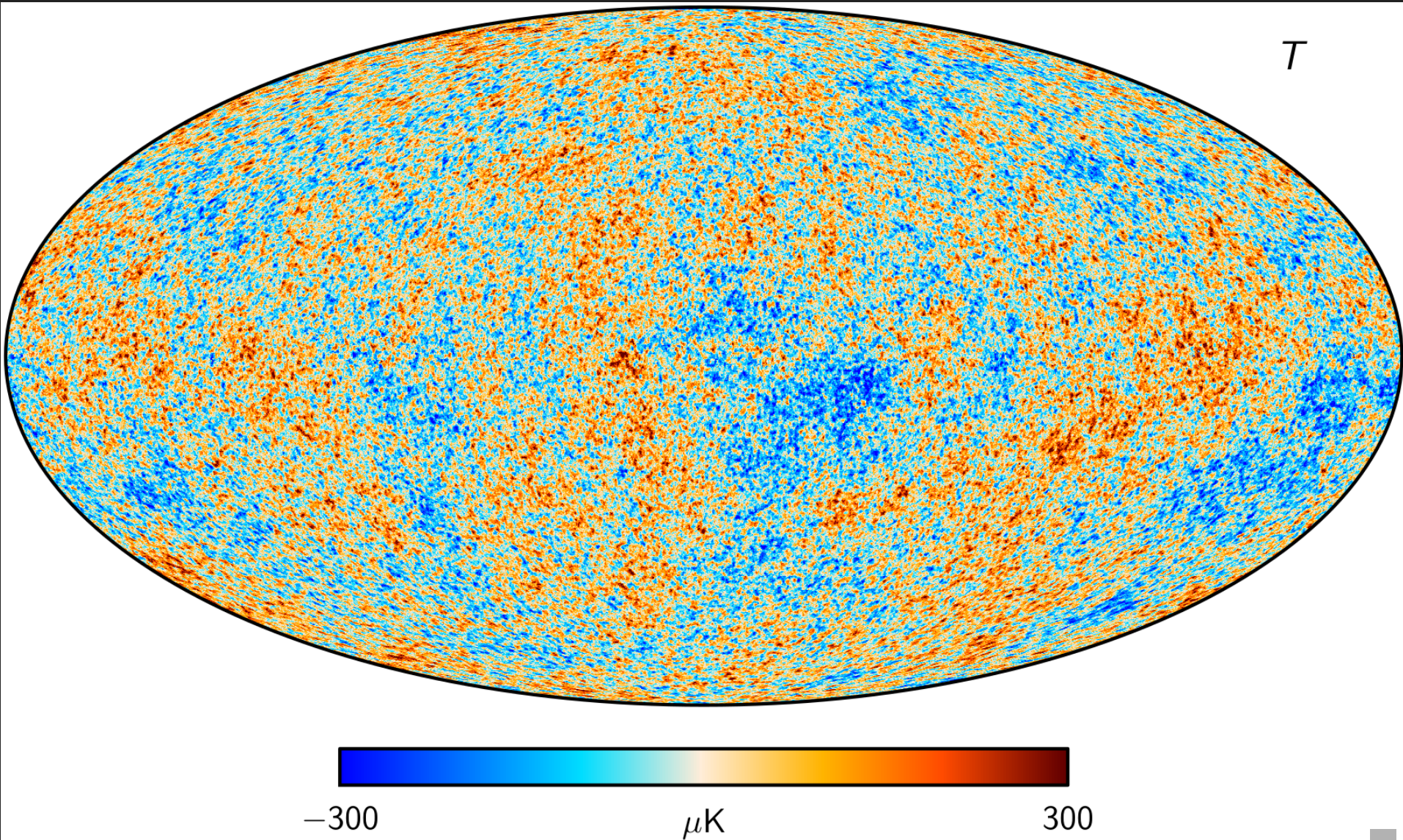
# Next-generation forecasts for screened and unscreened models of modified gravity

Santiago Casas, TTK, RWTH Aachen University

With collaboration from Euclid TWG WPs 1-6-7 and more...



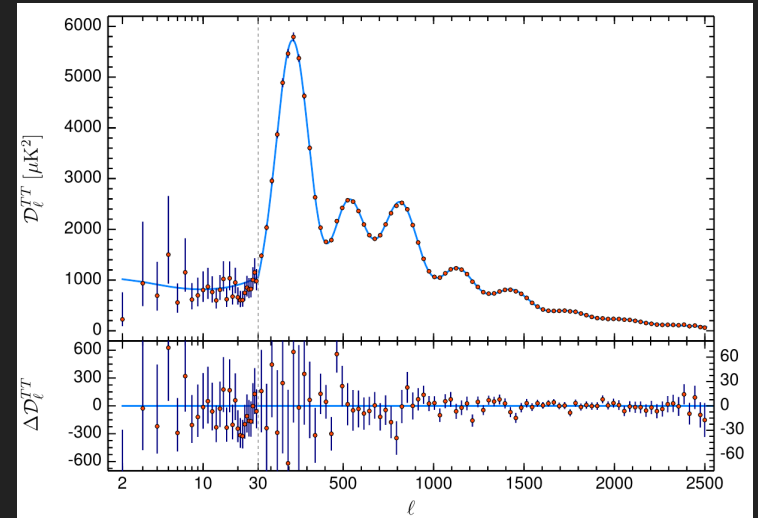
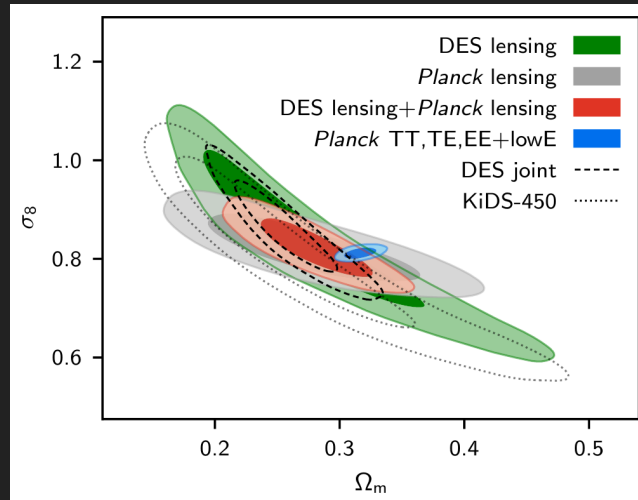
# Cosmic Microwave Background



# Large Scale Structure

# The Standard $\Lambda$ CDM model

- $\Lambda$ CDM is still best fit to observations.
- Concordance Cosmology:
- Combination of different observables.



- Lensing
- CMB
- Clustering
- Supernovae
- Clusters

$$G_{\mu\nu} + \Lambda g_{\mu\nu} = 8\pi G T_{\mu\nu}$$

# The Standard $\Lambda$ CDM model

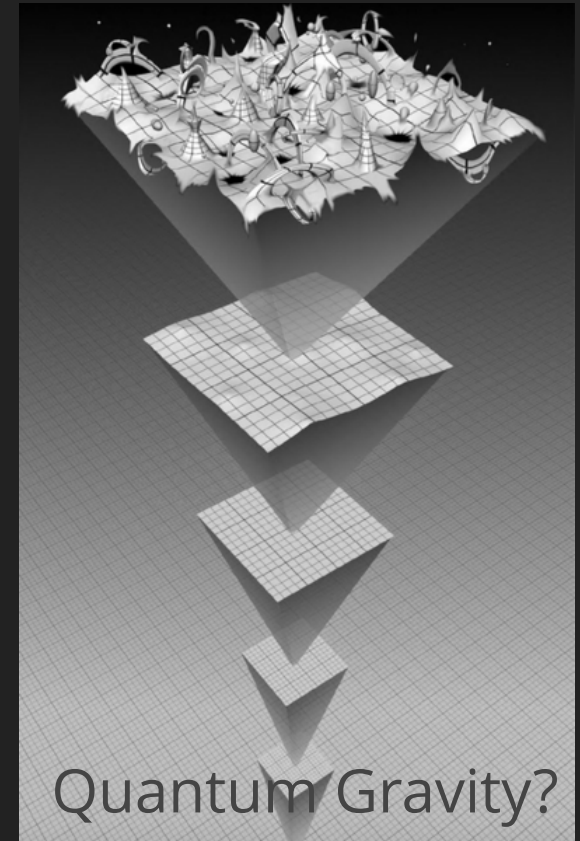
$$G_{\mu\nu} + \Lambda g_{\mu\nu} = 8\pi G T_{\mu\nu}$$

- $\Lambda$ CDM is still best fit to observations.
- Some questions remain:
- $\Lambda$  and CDM.
- Cosmological Constant Problem:

O(100) orders of magnitude wrong

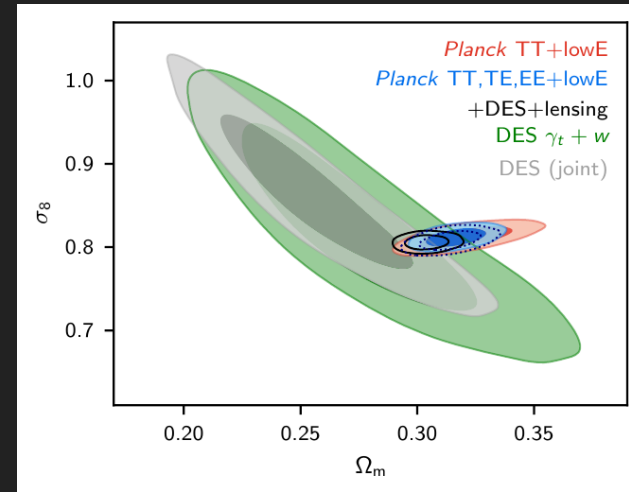
(Zeldovich 1967, Weinberg 1989, Martin 2012).

Composed of naturalness and coincidence sub-problems, among others.

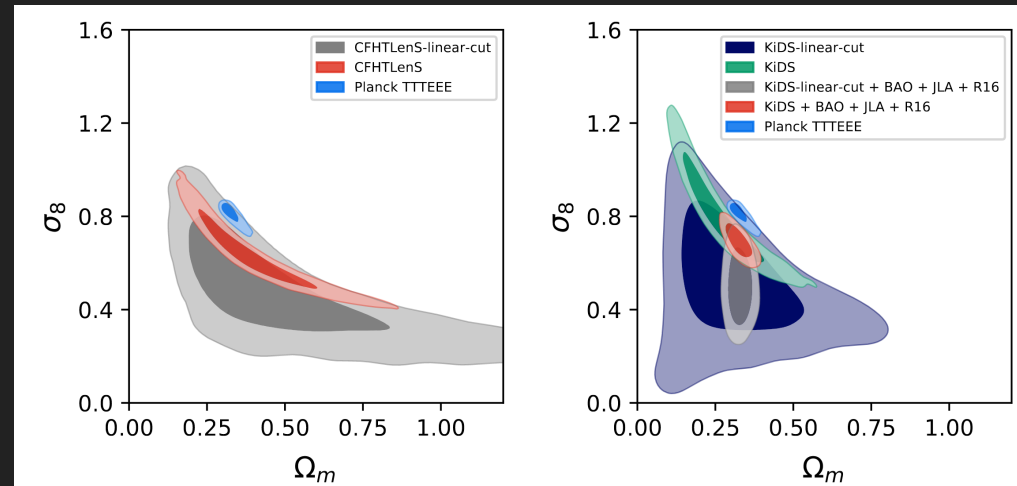
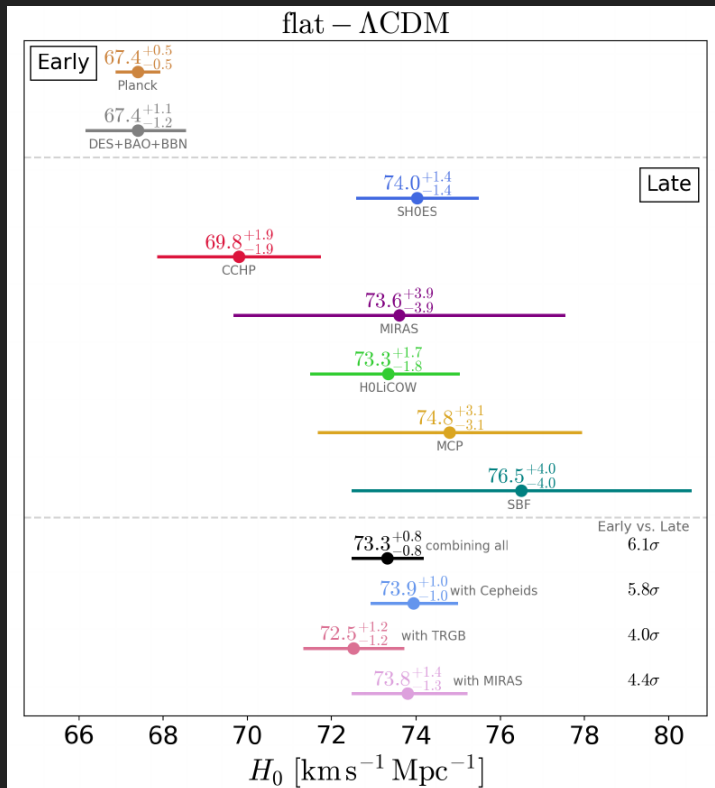


# The Standard $\Lambda$ CDM model

- $\Lambda$ CDM is still best fit to observations.
- Some questions remain:
- $H_0$  tension, now  $\sim 5\sigma$

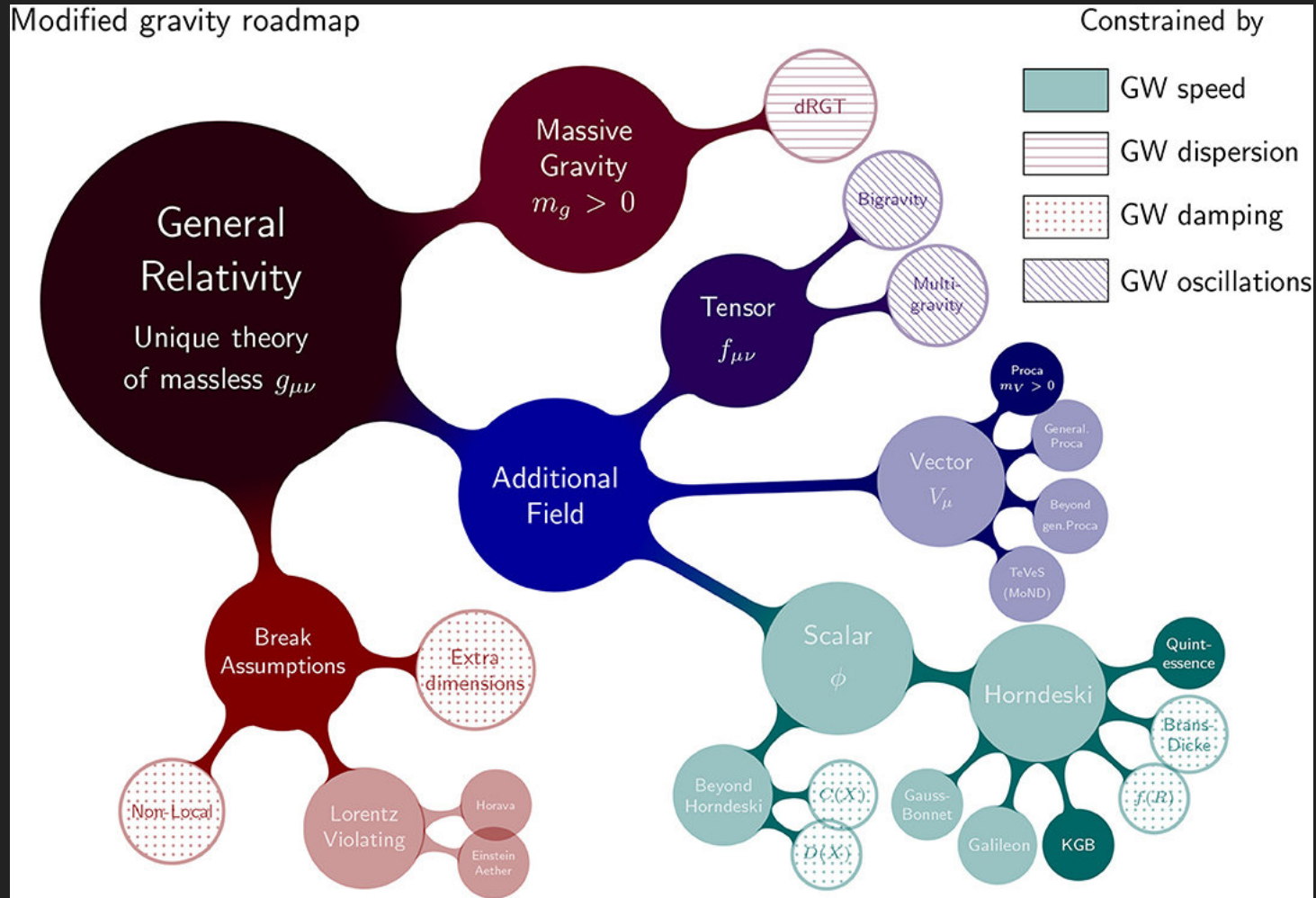


- $\sigma_8 - \Omega_m$  discrepancy at  $\sim 2\sigma$



# Alternatives to $\Lambda$ CDM

Modified gravity roadmap



# Constraints on Theories

- Background is well constrained to be around  $w = -1$
- Gravitational Wave speed =  $c$
- Galaxy morphology and solar system
- Black holes
- Coupling to baryons
- Non-linear regime still pretty much unconstrained
- Fifth forces
- Neutrinos?



# Scalar field models

At lowest order in the perturbation of the scalar field  $\varphi \equiv \phi - \phi_0$

$$\mathcal{L}_2 = \frac{Z(\phi_0)}{2} (\partial_\mu \varphi)^2 + \frac{m_\phi^2(\phi_0)}{2} \varphi^2 - \delta g_{\mu\nu} \delta T^{\mu\nu}$$

- Matter is coupled to the perturbed Jordan metric
- In the case of a cosmological-stress energy tensor and a non-negligible scalar field mass :

$$G_{\text{eff}} = \left( 1 + \frac{2\beta^2(\phi_0)}{Z(\phi_0)} e^{-m(\phi_0)r} \right) G_N$$

Yukawa term: Short range forces

# Screened Scalar fields

$$G_{\text{eff}} = \left( 1 + \frac{2\beta^2(\phi_0)}{Z(\phi_0)} e^{-m(\phi_0)r} \right) G_N$$

Different types of screening:

- **Chameleon**: The mass  $m(\phi_0)$  increases sharply inside matter
- **Damour-Polyakov**: The coupling  $\beta(\phi_0)$  vanishes inside matter
- **K-mouflage** and **Vainshtein**:  $Z(\phi_0) \gg 1$

# Screened models

As an effective field theory, the normalization factor can be expanded in a power series:

$$Z(\phi_0) = 1 + a(\phi_0)r_c^2 \frac{\square\varphi}{m_{\text{Pl}}} + b(\phi_0) \frac{(\partial\varphi)^2}{\Lambda^4} + c(\phi) \frac{\square^2\varphi}{\Lambda^5} + \dots$$

**K-mouflage:** first derivative term  $\partial\varphi/\Lambda^2$  dominates, which implies:

$$|\vec{\nabla}\Phi_N| \geq \frac{\Lambda^2}{2\beta(\phi_0)m_{\text{Pl}}} \longrightarrow \text{Screening where Newtonian acceleration } a = -\vec{\nabla}\Phi_N \text{ large enough}$$

**Vainshtein:** second derivative term  $\square\varphi$  dominates, which implies:

$$\nabla^2\Phi_N \geq \frac{1}{2\beta(\phi_0)r_c^2} \longrightarrow \text{Screening where spatial curvature is large}$$

When the  $\square^2\varphi$  dominates  $\rightarrow$  massive gravity

# Screened models

To summarize, screening mechanisms can be characterized by the inequality:

$$\nabla^k \Phi_N \gtrsim C$$

- **Chameleon**:  $k = 0$  (surface N. potential is large)
- **K-mouflage**:  $k = 1$  (N. acceleration is large)
- **Vainshtein**:  $k = 2$  (curvature is large)

For DE applications and under some assumptions:

- Chameleon screens everything above a certain potential threshold
- K-mouflage does not screen galaxy clusters
- Vainshtein screens all structures that turn non-linear

# Examples of screened models

- **Chameleon**:  $f(R)$  Hu-Sawicki
- **K-mouflage**:  $k$ -essence + universal coupling
- **Vainshtein**: nDGP (3+1)d brane embedded in 5d
  - Solar system and other local constraints and instabilities forbid self-acceleration in these models
  - $\Lambda$ CDM-like background
  - Just one free parameter each
  - Universal couplings

# f(R) Hu-Sawicki model

Modification of the Einstein-Hilbert action

$$S = \frac{c^4}{16\pi G} \int d^4x \sqrt{-g} [R + f(R)]$$

Induces changes in the gravitational potentials \*

$$-k^2 \Psi = \frac{4\pi G}{c^4} a^2 \mu \bar{\rho} \Delta$$

Scale-dependent growth of matter perturbations

$$\mu(a, k) = \frac{1}{1+f_R(a)} \frac{1+4k^2 a^{-2} m_{f_R}^{-2}(a)}{1+3k^2 a^{-2} m_{f_R}^{-2}(a)}$$

Free parameter:  $f_{R0}$

$$f(R) = -6\Omega_{\text{DE}} H_0^2 + |f_{R0}| \frac{\bar{R}_0^2}{R}$$

Hu, Sawicki (2007)

$$-k^2 (\Phi + \Psi) = \frac{8\pi G}{c^4} a^2 \Sigma \bar{\rho} \Delta$$

Small changes in lensing potential

$$\Sigma(a) = \frac{1}{1+f_R(a)}$$

"Fifth-force" scale for cosmological densities

$$\lambda_C = 32 \text{Mpc} \sqrt{|f_{R0}|/10^{-4}}$$

\*for negligible matter anisotropic stress

# f(R) as a scalar field theory

Universal coupling through a conformal transformation between Einstein and Jordan metrics

$$\tilde{g}_{\mu\nu} = A^2(\phi, X)g_{\mu\nu} + B^2(\phi, X)\partial_\mu\phi\partial_\mu\phi$$

General **Chameleon** scalar models are given by specifying  $V$  and  $A$

$$V_{\text{eff}}(\phi) = V(\phi) + (A(\phi) - 1)\rho$$

- With a coupling function:
- Map to a scalar field by:
- Carefully chosen potential can realize chameleon mechanism:

$$A(\phi) = e^{\beta\phi/m_{\text{Pl}}}$$

$$\frac{df}{dR} = e^{-2\beta\phi/m_{\text{Pl}}}$$

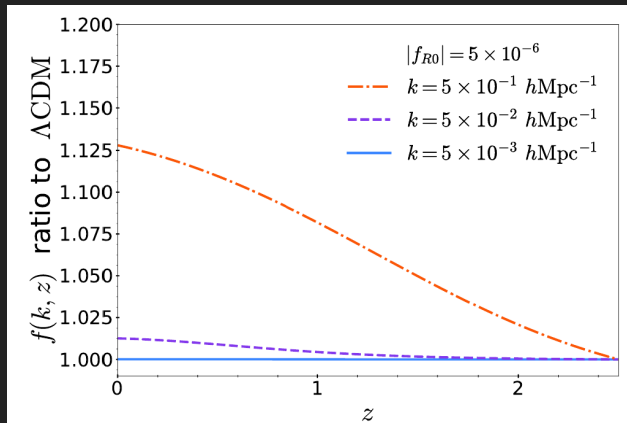
$$V(\phi) = \frac{m_{\text{Pl}}^2}{2} \frac{R \frac{df}{dR} - R}{\left(\frac{df}{dR}\right)^2}$$

- Objects **screened** when:

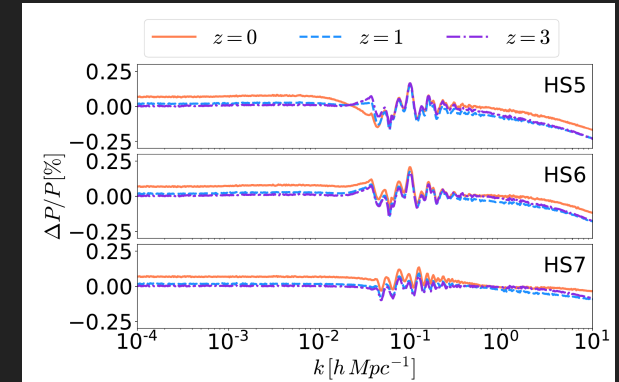
$$\Phi_N \gtrsim \frac{3}{2} |f_{R_0}|$$

# f(R) Hu-Sawicki predictions

Scale-dependent growth



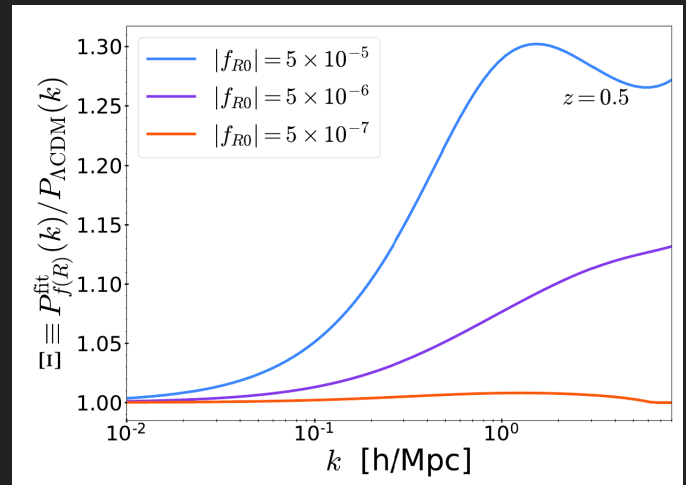
Codes used: for linear perturbations:  
MGCAMB and EFTCAMB



Fitting formula for non-linear power spectrum:

Winther, Casas, Baldi, Koyama, Li (2019)

\*Forge Emulator not available at time of first review





# Scale-independent models

nDGP, K-mouflage and Jordan-Brans-Dicke have scale-independent growth

"Extreme cases" far away from  $\Lambda$ CDM and close to current upper bounds

**nDGP**: free parameter  $\Omega_{rc}$  (related to the transition scale)

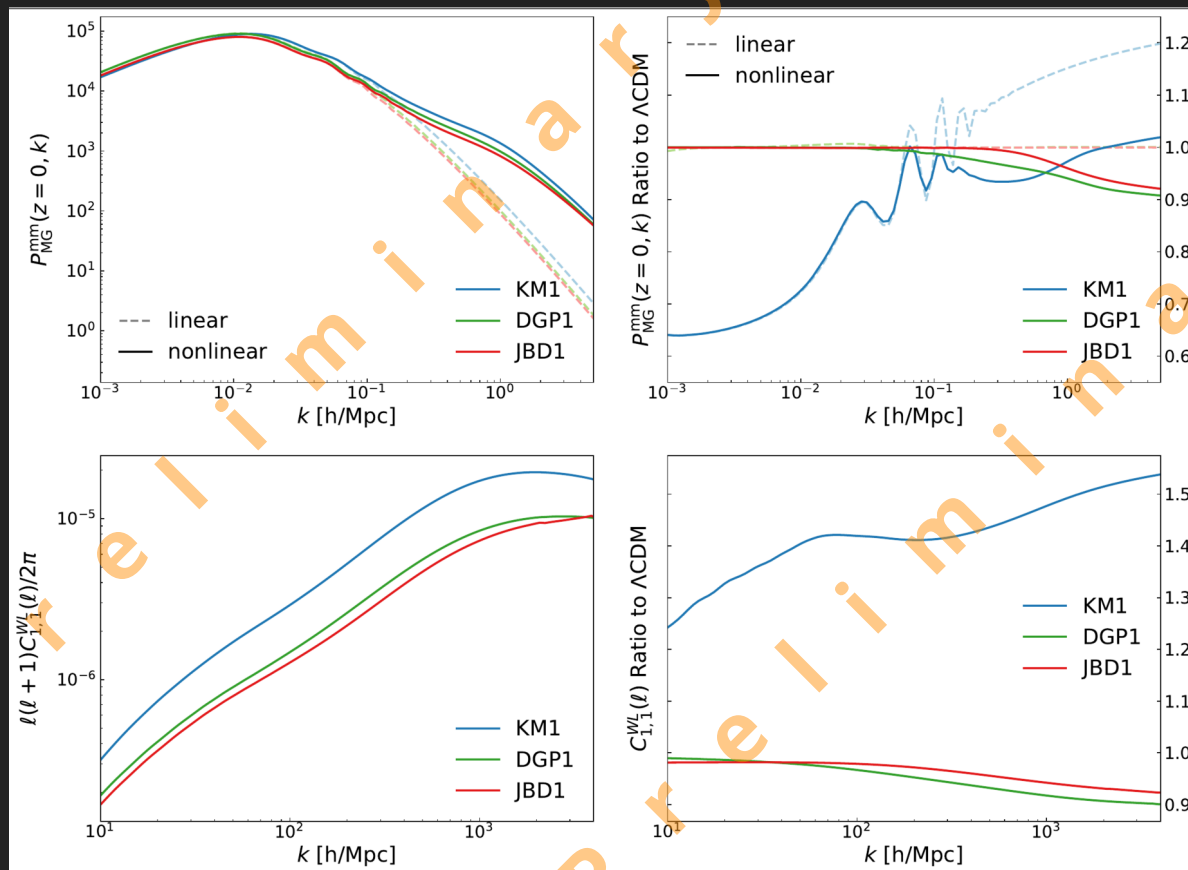
**ReACT**

**KM**: free parameter  $\epsilon_2$  (related to the conformal coupling amplitude)

**Halo+PT**

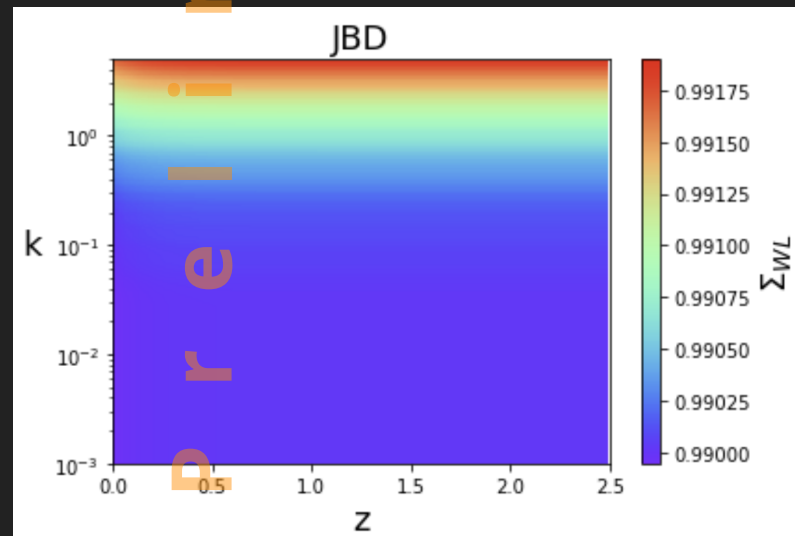
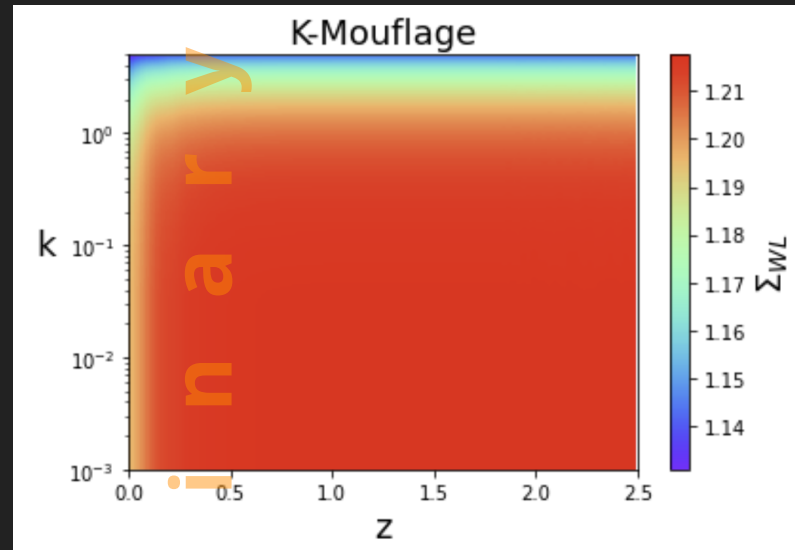
**JBD**: free parameter  $\omega_{BD}$  (related to the scalar coupling)

**HMCode**



# Scale-independent models

- K-Mouflage presents a large enhancement of the lensing potential
- Definitely detectable with next-generation WL observations



# Next-generation Galaxy Surveys

# DESI telescope



- 14 000 square degrees in the sky
- 30 million accurate galaxy spectra
- Redshifts:  $0 < z < 2$
- Quasars up to  $z \sim 3.5$
- 5 years of observation

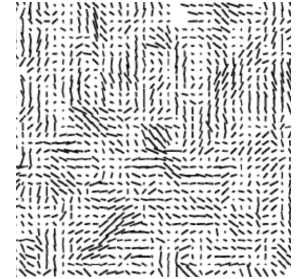
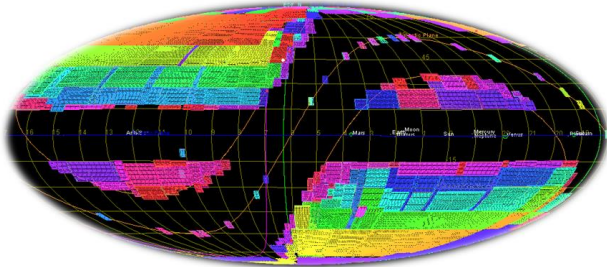
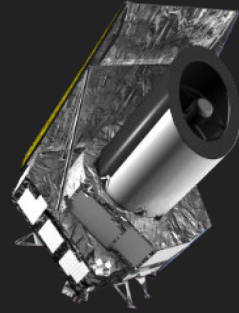
# Vera Rubin Observatory



- Located in Chile, 8.4m telescope
- 20 billion galaxies
- Redshifts:  $0 < z \sim < 3$
- 18,000 square degrees
- 11 years of observation

# Euclid Space Satellite

- Two instruments:
- VIS (visible photometer): shape and orientation of 1.5 billion galaxies!
- NISP (near infrared spectrograph): 30 million galaxy spectra!



- 15 000 square degrees in the sky
- 16 countries, ~1500 members
- ~170 Petabyte of data!

# Photometric cross-correlations

Also known as 3x2pt analysis

Shear-Shear, Galaxy-Galaxy, Galaxy-Lensing **correlations**

Shear-Shear      Intrinsic Alignments

$$\mathcal{W}_i^L = \mathcal{W}_i^g(z) - \frac{\mathcal{A}_{IA} C_{IA} \Omega_m \mathcal{F}_{IA}(z)}{D(z)} \mathcal{W}_i^{IA}(z)$$

XC

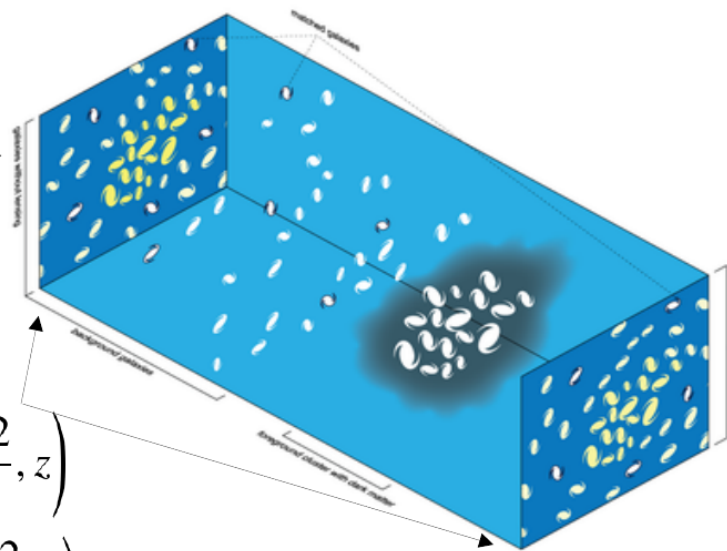
$$C_{ij}^{GL}(\ell) = \int \frac{dz}{H(z)r^2(z)} \mathcal{W}_i^G(z) \mathcal{W}_j^L(z) P_{\delta\delta} \left( \frac{\ell + 1/2}{r(z)}, z \right)$$

GCph

$$C_{ij}^{GG}(\ell) = \int \frac{dz}{H(z)r^2(z)} \mathcal{W}_i^G(z) \mathcal{W}_j^G(z) P_{\delta\delta} \left( \frac{\ell + 1/2}{r(z)}, z \right)$$

WL

$$C_{ij}^{LL}(\ell) = \int_{z_{\min}}^{z_{\max}} \frac{dz}{H(z)r^2(z)} \mathcal{W}_i^L(z) \mathcal{W}_j^L(z) P_{\delta\delta} \left( \frac{\ell + 1/2}{r(z)}, z \right)$$



# Weak Lensing

The cosmic shear angular power spectrum depends on the Weyl spectrum (of gravitational potentials  $\Phi + \Psi$ )

$$C_{ij}^{\gamma\gamma}(\ell) = \frac{c}{H_0} \int \frac{\hat{W}_i^\gamma(z) \hat{W}_j^\gamma(z)}{E(z) r^2(z)} P_{\Phi+\Psi}(k_\ell, z) dz$$

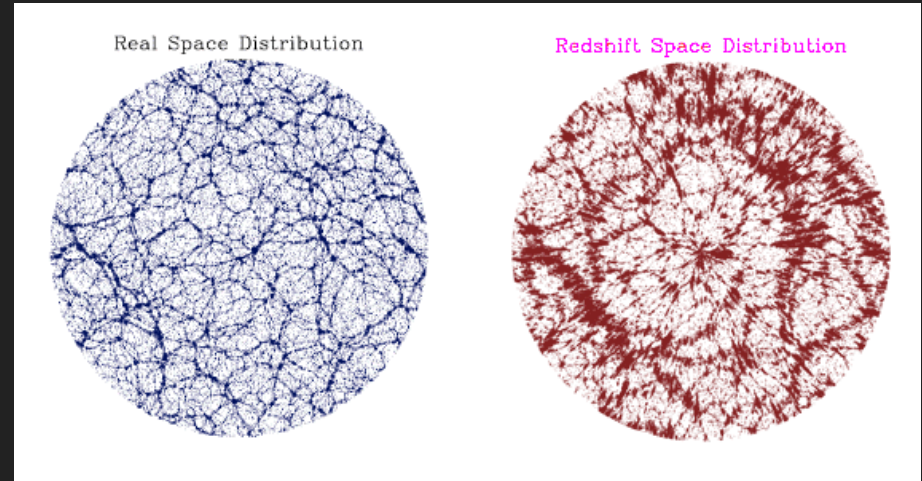
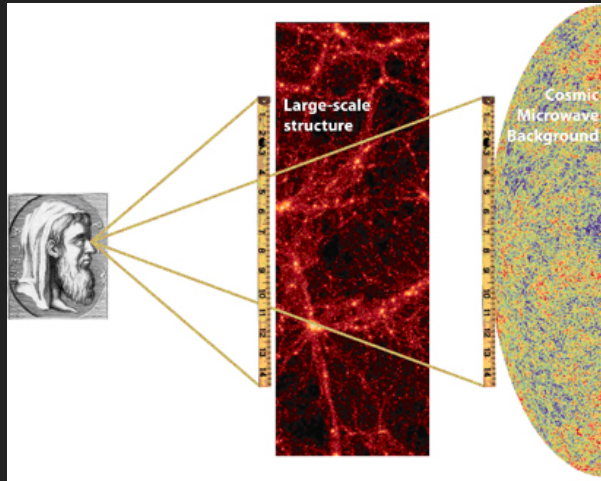
Which is related to the matter power spectrum (of density contrast  $\delta$ ) through

$$P_{\Phi+\Psi} = \left[ 3 \left( \frac{H_0}{c} \right)^2 \Omega_M^0 (1+z) \Sigma(k, z) \right]^2 P_{\delta\delta}$$

Information about background geometry, matter content and clustering



# Spectroscopic Galaxy Clustering



BAO

Clustering

RSD

Spec-z

$$P_{\text{obs}}(k_{\text{ref}}, \mu_{\text{ref}}; z) = \frac{1}{q_{\perp}^2 q_{\parallel}} \left\{ \frac{[b\sigma_8(z) + f\sigma_8(z)\mu^2]^2}{1 + [f(z)k\mu\sigma_p(z)]^2} \right\} \frac{P_{\text{dw}}(k, \mu; z)}{\sigma_8^2(z)} F_z(k, \mu; z) + P_s(z)$$

# Spectroscopic Galaxy Clustering

$$\langle \delta(\mathbf{k})\delta(\mathbf{k}') \rangle \equiv P(\mathbf{k})\delta_D(\mathbf{k} + \mathbf{k}')$$

One loop Power Spectrum

$$\langle \delta(\mathbf{k})\delta(\mathbf{k}') \rangle \approx \langle \delta^{(1)}(\mathbf{k})\delta^{(1)}(\mathbf{k}') \rangle + 2 \langle \delta^{(1)}(\mathbf{k})\delta^{(3)}(\mathbf{k}') \rangle + \langle \delta^{(2)}(\mathbf{k})\delta^{(2)}(\mathbf{k}') \rangle$$
$$P_{1-loop}(k) \equiv P_{lin}(\mathbf{k}) + 2P_{13}(\mathbf{k}) + P_{22}(\mathbf{k})$$

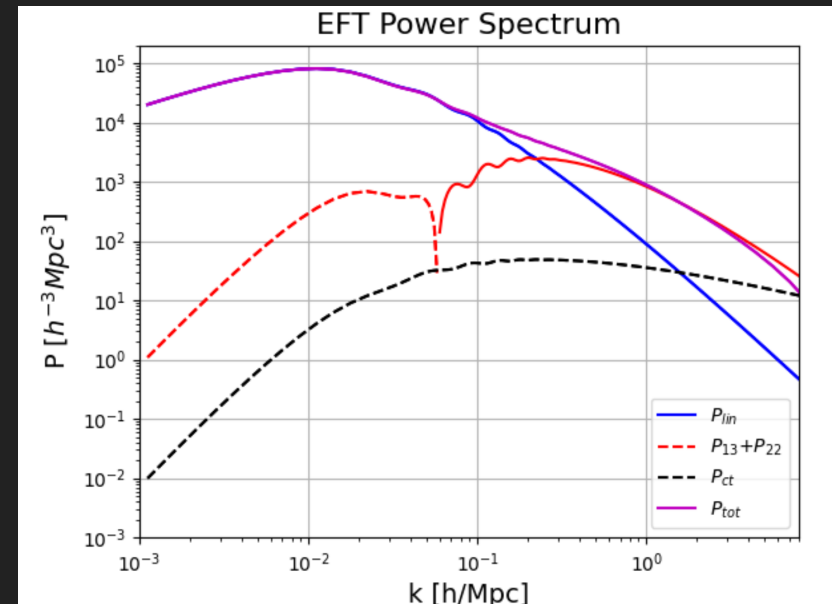
$$P_{22}(k, \eta) = 2 \int F_2^s(\mathbf{k} - \mathbf{q}, \mathbf{q})^2 P_{lin}(\mathbf{k} - \mathbf{q}, \eta) P_{lin}(\mathbf{q}, \eta) d^3 \mathbf{q}$$

$$P_{13}(k, \eta) = 3 \int F_3^s(\mathbf{k}, \mathbf{q}, -\mathbf{q}) P_{lin}(\mathbf{k}, \eta) P_{lin}(\mathbf{q}, \eta) d^3 \mathbf{q}$$

- EFT smoothing over terms -  
> UV counterterms  
(see previous talk by Filippo)
- Already being implemented into MCMC and Fisher pipelines like CosmicFish and CLOE

For mildly non-linear scales we need to use perturbation theory

- SPT is not enough



# The Matter Power Spectrum

Current data:

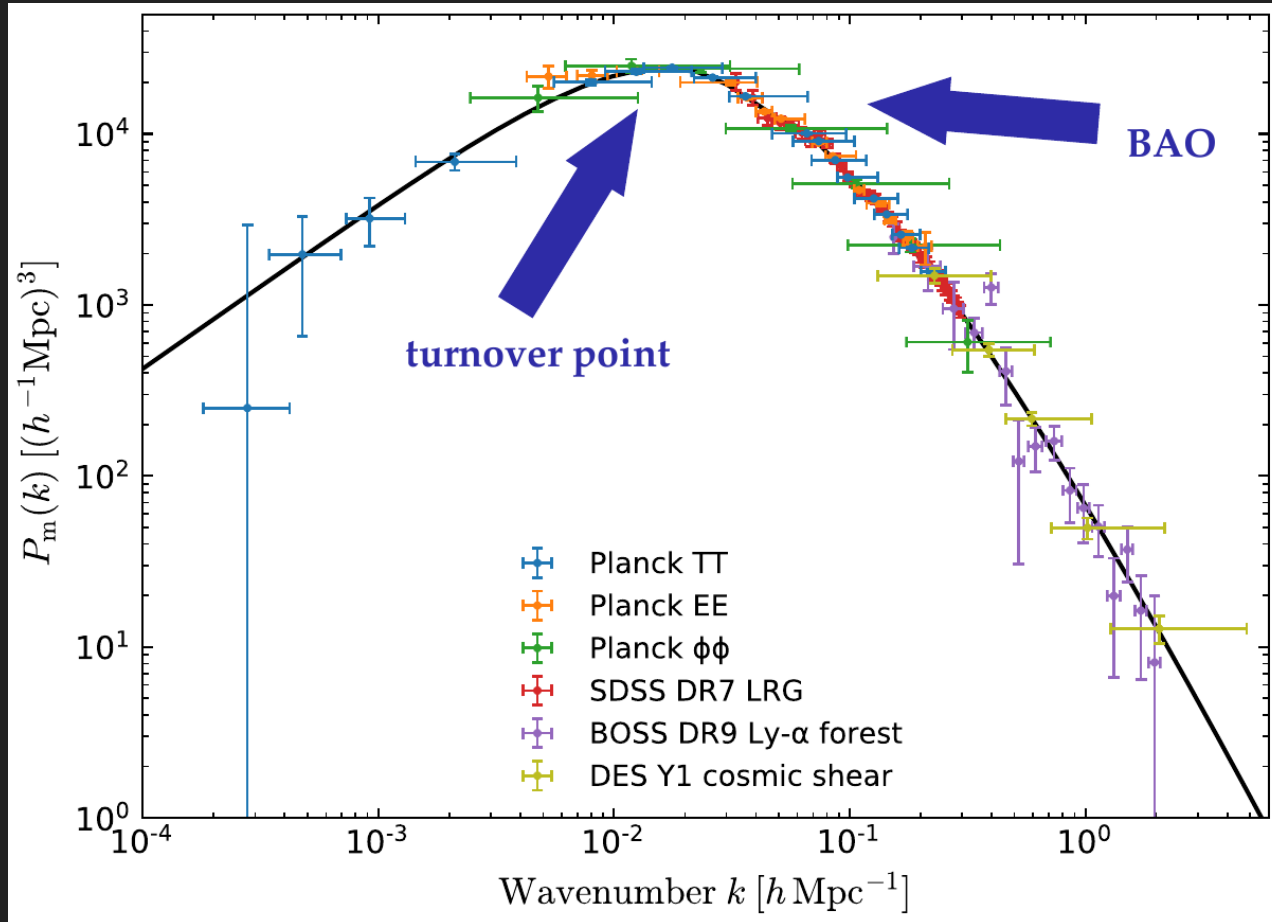
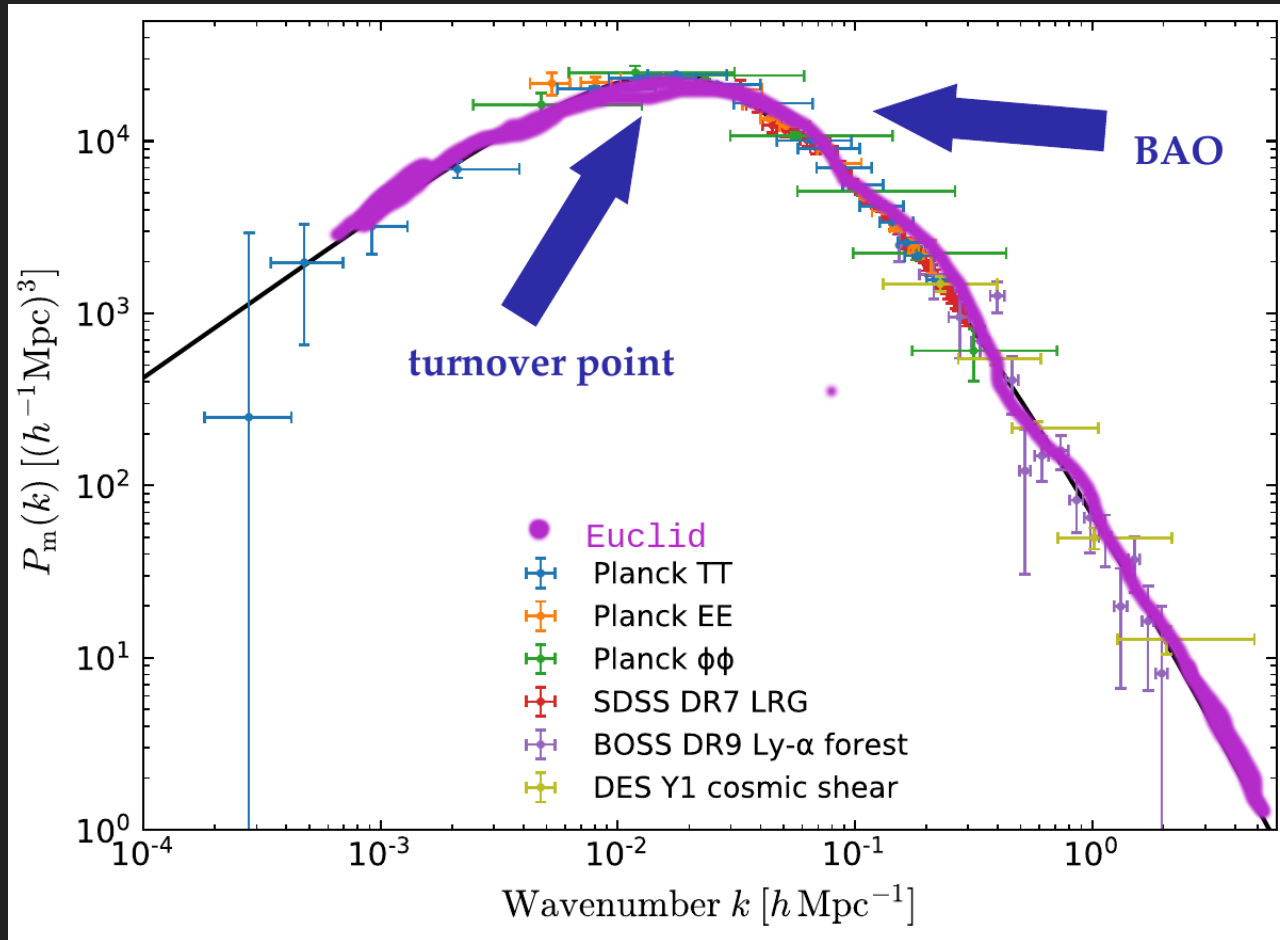


Image: <https://www.cosmos.esa.int/web/planck/picture-gallery>

# The Matter Power Spectrum

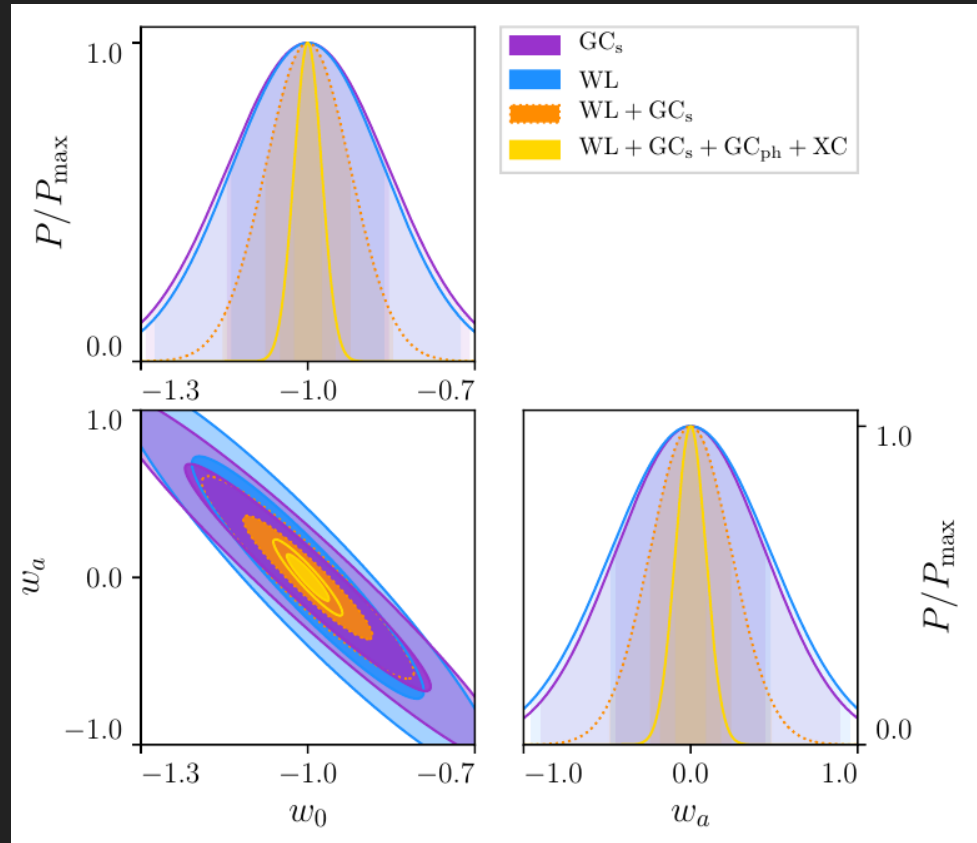
Euclid:



Scales from:  $\sim 10^{-3}$  to  $10 \text{ hMpc}^{-1}$

# Euclid: IST:Forecasts

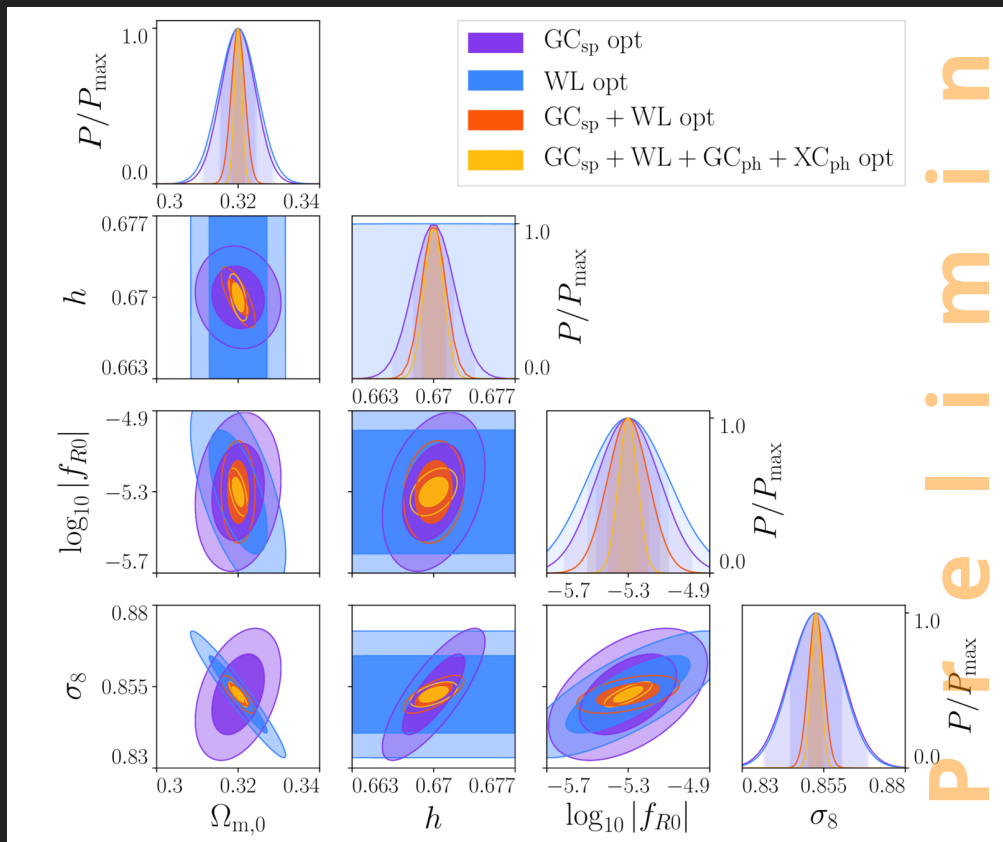
- Here: Flat  $w_0 w_a$  CDM
- GCsp+WL+GCph+XC
- Figure of Merit: 1257
- Non-flat FoM: 500
- Optimistic:  
 $\sigma_{w_0} = 0.025$   
 $\sigma_{w_a} = 0.092$



# Forecasts for $f(R)$ from Euclid probes

$\Theta = \{\Omega_{m,0}, \Omega_{b,0}, h, n_s, \sigma_8, \log_{10} |f_{R0}|\},$   
 HS5 :  $\Theta_{\text{fid,HS5}} = \{0.32, 0.05, 0.67, 0.96, 0.911, -4.301\},$   
 HS6 :  $\Theta_{\text{fid,HS6}} = \{0.32, 0.05, 0.67, 0.96, 0.853, -5.301\},$   
 HS7 :  $\Theta_{\text{fid,HS7}} = \{0.32, 0.05, 0.67, 0.96, 0.823, -6.301\}.$

- Combined constraints from GCsp and Photo probes



- $\sigma_{\log_{10} |f_{R0}|} = 0.16$  with spectroscopic GC<sub>sp</sub> alone (corresponding to a relative 3.0% error);
- $\sigma_{\log_{10} |f_{R0}|} = 0.20$  with WL alone (corresponding to a relative 3.8% error);
- $\sigma_{\log_{10} |f_{R0}|} = 0.07$  combining WL, GC<sub>ph</sub>, and XC<sub>ph</sub> (corresponding to a relative 1.3% error);
- $\sigma_{\log_{10} |f_{R0}|} = 0.05$  using the full combination GC<sub>sp</sub>+WL+GC<sub>ph</sub>+XC<sub>ph</sub> (corresponding to a relative 0.9% error).

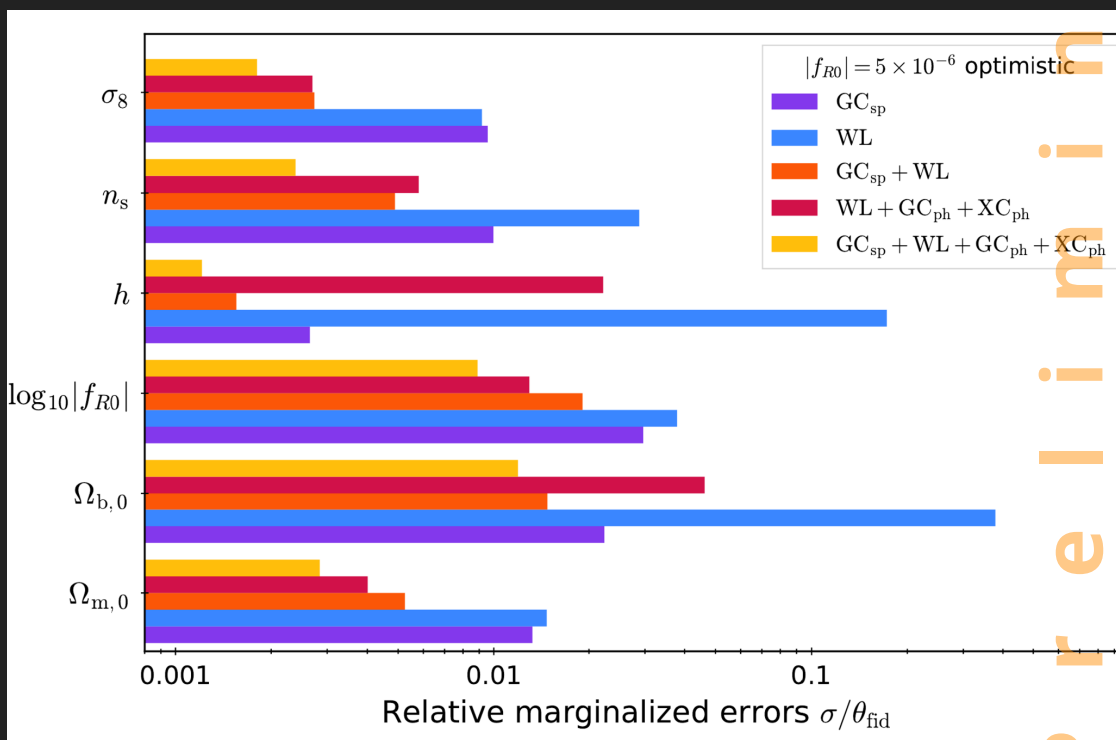
P r e l i m i n a r y

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Primary

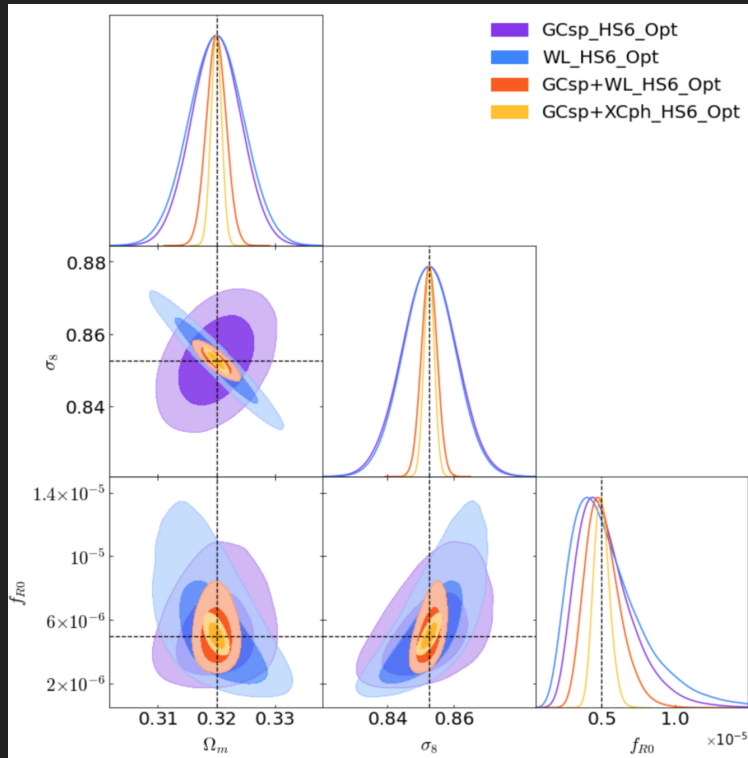
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 HS7 :  $\Theta_{\text{fid,HS7}} = \{0.32, 0.05, 0.67, 0.96, 0.823, -6.301\}.$



- Transform into original space

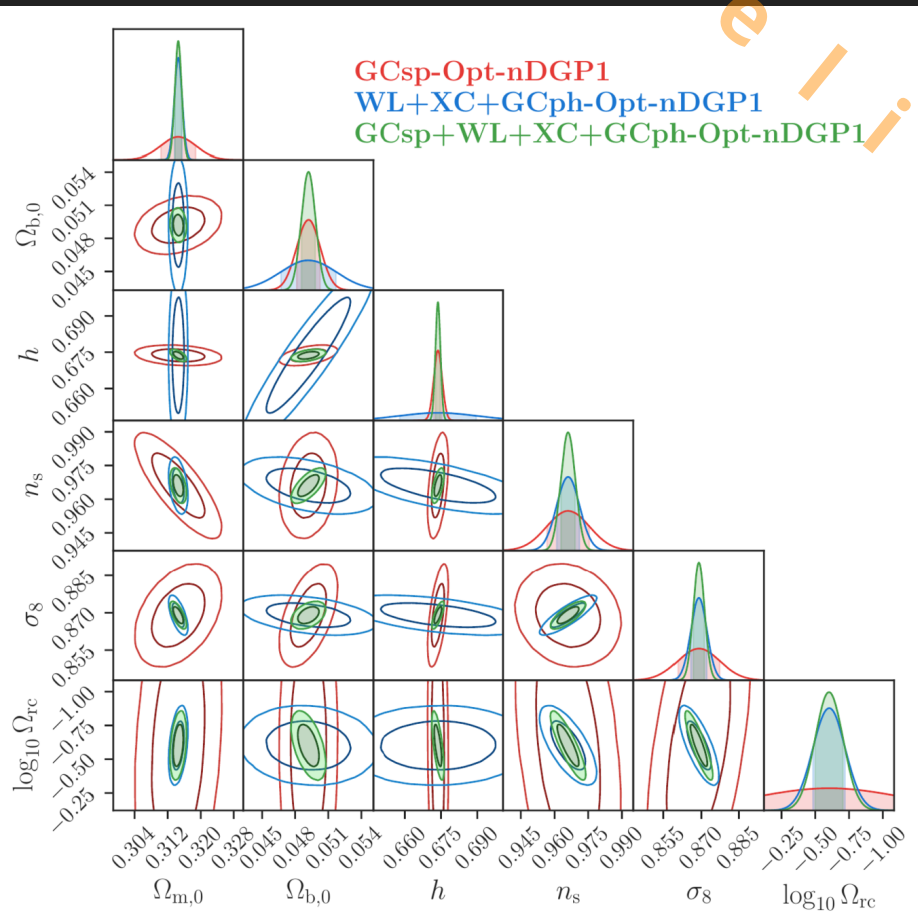
$- |f_{R0}| = (5.0^{+0.58}_{-0.52} \times 10^{-6})$   
 with the combination  $GC_{\text{sp}} + WL + GC_{\text{ph}} + XC_{\text{ph}}$ .

- Current LSS data: "just" upper bounds of the order of  $< 10^{-4}$



# Forecasts for nDGP

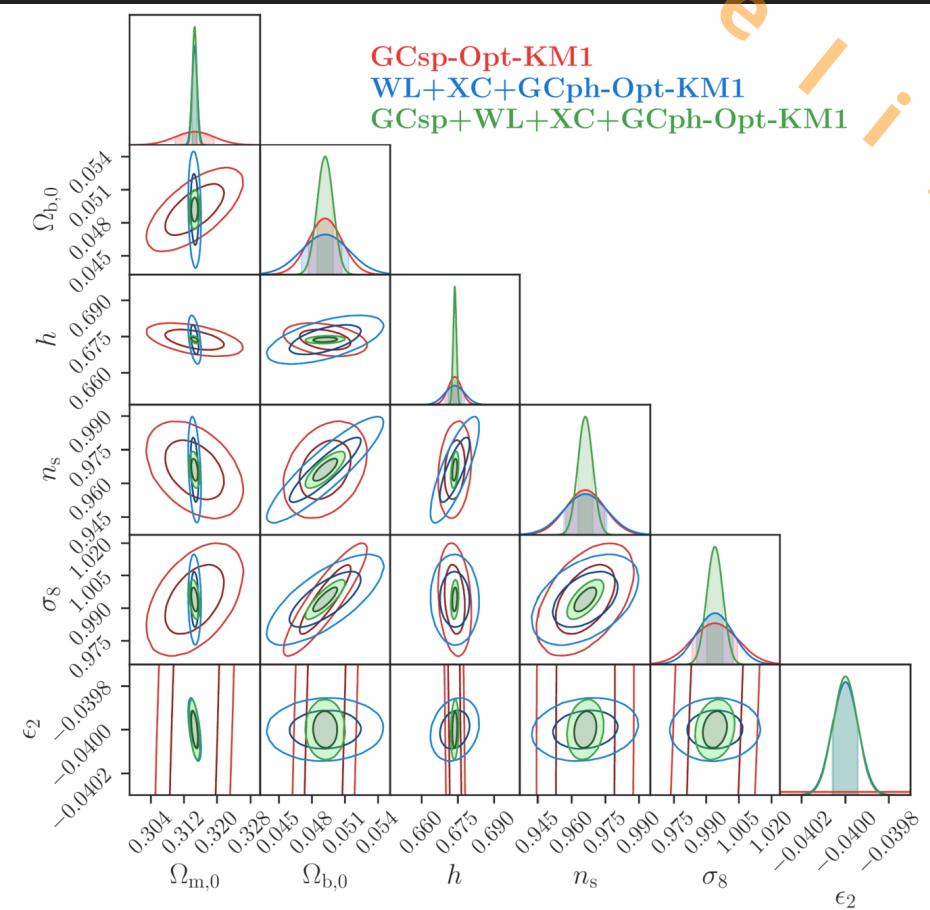
- GCsp does not constrain the free parameter very well
- Most gain is at NL-scales for Photo probes



nDGP1 $\Omega_{rc} = 0.25$			
	$\Omega_{m,0}$	$\Omega_{b,0}$	$\log_{10}(\Omega_{rc})$
Pessimistic setting			
GC <sub>sp</sub> ( $k_{max} = 0.15 h \text{ Mpc}^{-1}$ )	2.23 %	4.30 %	142.20 %
GC <sub>sp</sub> ( $k_{max} = 0.25 h \text{ Mpc}^{-1}$ )	1.41 %	2.43 %	97.63 %
WL+XC+GC <sub>ph</sub>	1.13 %	5.64 %	49.59 %
GC <sub>sp</sub> +WL+XC+GC <sub>ph</sub>	0.55 %	1.95 %	40.27 %
Optimistic setting			
GC <sub>sp</sub> ( $k_{max} = 0.3 h \text{ Mpc}^{-1}$ )	1.33 %	2.15 %	90.06 %
WL+XC+GC <sub>ph</sub>	0.30 %	5.08 %	19.59 %
GC <sub>sp</sub> +WL+XC+GC <sub>ph</sub>	0.25 %	1.28 %	16.99 %
nDGP2 $\Omega_{rc} = 10^{-6}$			
Pessimistic setting			
GC <sub>sp</sub> ( $k_{max} = 0.15 h \text{ Mpc}^{-1}$ )	2.36 %	4.51 %	3020.58 %
GC <sub>sp</sub> ( $k_{max} = 0.25 h \text{ Mpc}^{-1}$ )	1.46 %	2.51 %	1923.03 %
WL+XC+GC <sub>ph</sub>	0.86 %	5.61 %	398.64 %
GC <sub>sp</sub> +WL+XC+GC <sub>ph</sub>	0.89 %	1.84 %	378.82 %
Optimistic setting			
GC <sub>sp</sub> ( $k_{max} = 0.3 h \text{ Mpc}^{-1}$ )	1.38 %	2.21 %	1801.03 %
WL+XC+GC <sub>ph</sub>	0.29 %	5.08 %	81.02 %
GC <sub>sp</sub> +WL+XC+GC <sub>ph</sub>	0.25 %	1.12 %	80.83 %

# Forecasts for K-Mouflage

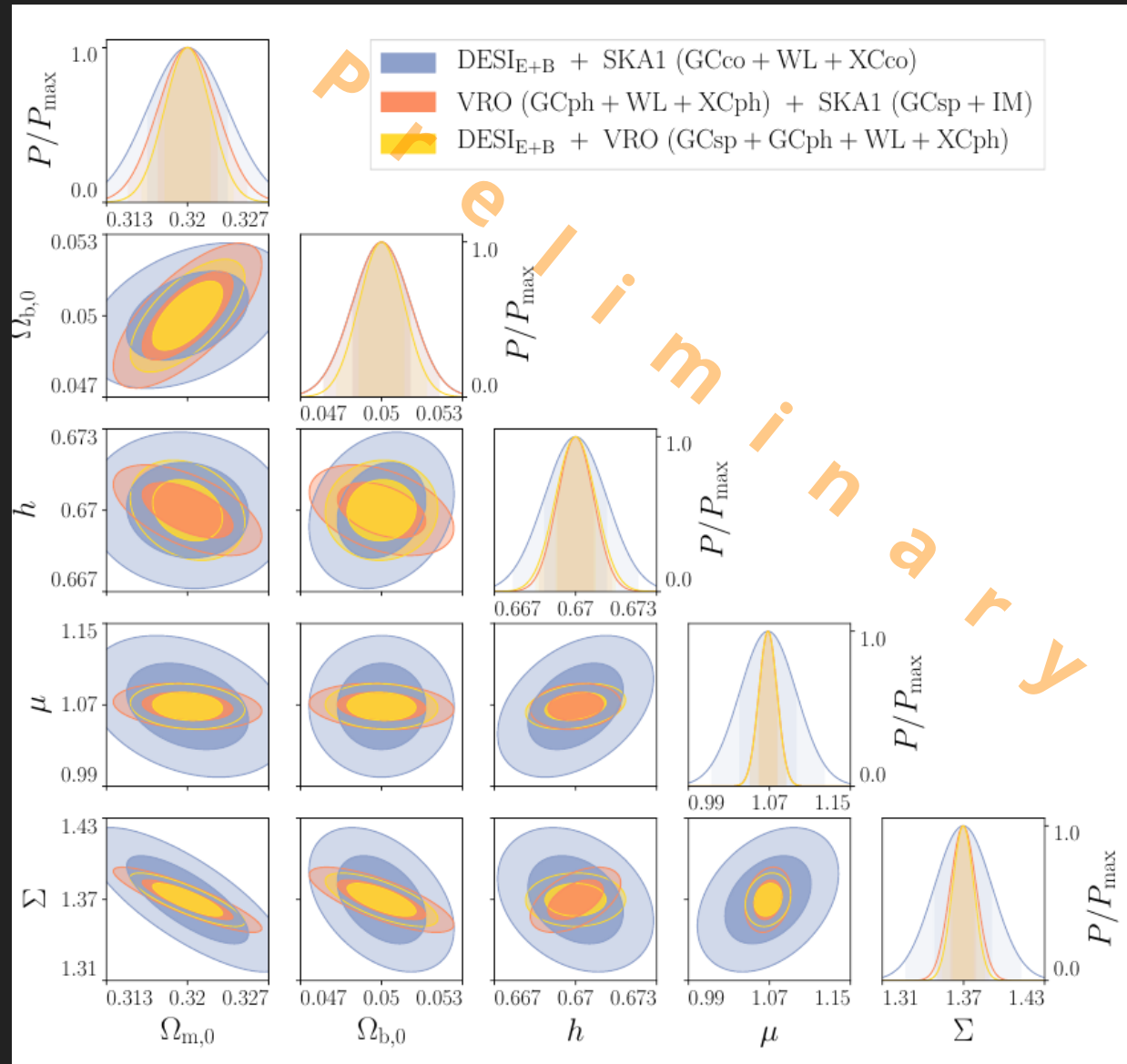
- For KM1:
  - GCsp can constrain the free parameter at  $\sim 10\%$
  - Photo at  $\sim 1\%$  (remember  $\Sigma_{WL}$ )
  - KM2 is basically  $\Lambda$ CDM, non detectable



KM1 $\epsilon_{2,0} = -0.04$			
	$\Omega_{m,0}$	$\Omega_{b,0}$	$\epsilon_{2,0}$
Pessimistic setting			
GC <sub>sp</sub> ( $k_{\max} = 0.15 h \text{ Mpc}^{-1}$ )	2.68 %	5.34 %	11.14 %
GC <sub>sp</sub> ( $k_{\max} = 0.25 h \text{ Mpc}^{-1}$ )	1.57 %	3.22 %	5.77 %
WL+XC+GC <sub>ph</sub>	0.36 %	7.36 %	0.22 %
GC <sub>sp</sub> +WL+XC+GC <sub>ph</sub>	0.34 %	1.73 %	0.22 %
Optimistic setting			
GC <sub>sp</sub> ( $k_{\max} = 0.3 h \text{ Mpc}^{-1}$ )	1.48 %	3.08 %	4.99 %
WL+XC+GC <sub>ph</sub>	0.20 %	4.30 %	0.15 %
GC <sub>sp</sub> +WL+XC+GC <sub>ph</sub>	0.17 %	1.47 %	0.14 %
KM2 $\epsilon_{2,0} = -0.0001$			
Pessimistic setting			
GC <sub>sp</sub> ( $k_{\max} = 0.15 h \text{ Mpc}^{-1}$ )	2.99 %	5.61 %	1264.58 %
GC <sub>sp</sub> ( $k_{\max} = 0.25 h \text{ Mpc}^{-1}$ )	1.60 %	3.08 %	824.38 %
WL+XC+GC <sub>ph</sub>	1.18 %	5.22 %	939.23 %
GC <sub>sp</sub> +WL+XC+GC <sub>ph</sub>	0.68 %	1.90 %	645.16 %
Optimistic setting			
GC <sub>sp</sub> ( $k_{\max} = 0.3 h \text{ Mpc}^{-1}$ )	1.45 %	2.69 %	759.45 %
WL+XC+GC <sub>ph</sub>	0.40 %	3.43 %	658.67 %
GC <sub>sp</sub> +WL+XC+GC <sub>ph</sub>	0.32 %	1.52 %	464.38 %

# Bonus: Forecasts on parameterized MG

- DESI+Rubin have similar power than Euclid alone (under many assumptions)
- Optical + Radio is also competitive and can remove systematics / degeneracies
- Constraints on  $\mu$ ,  $\Sigma$  of the order of  $\sim 5\text{-}10\%$  under optimistic assumptions
- PPN-approach screening assumed



# Conclusions

- Screening mechanisms can save scalar field models
- Current constraints don't allow for self-acceleration
- Screening mechanisms can be classified by the derivative order
- Euclid and next-generation surveys will be powerful probes for Cosmology.
- Primary LSS probes: Galaxy Clustering and Weak Lensing
- Many challenges ahead in non-linear modelling
- Next-generation surveys can constrain free parameters with percent precision accuracy

**Thanks!**

**Merci!**