

Neutrino masses and structure formation

"Review" + the example of Lyman-alpha forest

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Action Dark Energy - Marseille 06/05/2022



Standard Model neutrinos

	I	II	III	
mass	$\approx 2.2 \text{ MeV}/c^2$	$\approx 1.28 \text{ GeV}/c^2$	$\approx 173.1 \text{ GeV}/c^2$	0
charge	$2/3$	$2/3$	$2/3$	0
spin	$1/2$	$1/2$	$1/2$	0
QUARKS	u up	c charm	t top	g gluon
	d down	s strange	b bottom	γ photon
LEPTONS	e electron	μ muon	τ tau	Z Z boson
	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	W W boson

ν : Lightest + "least" interacting fermions in SM

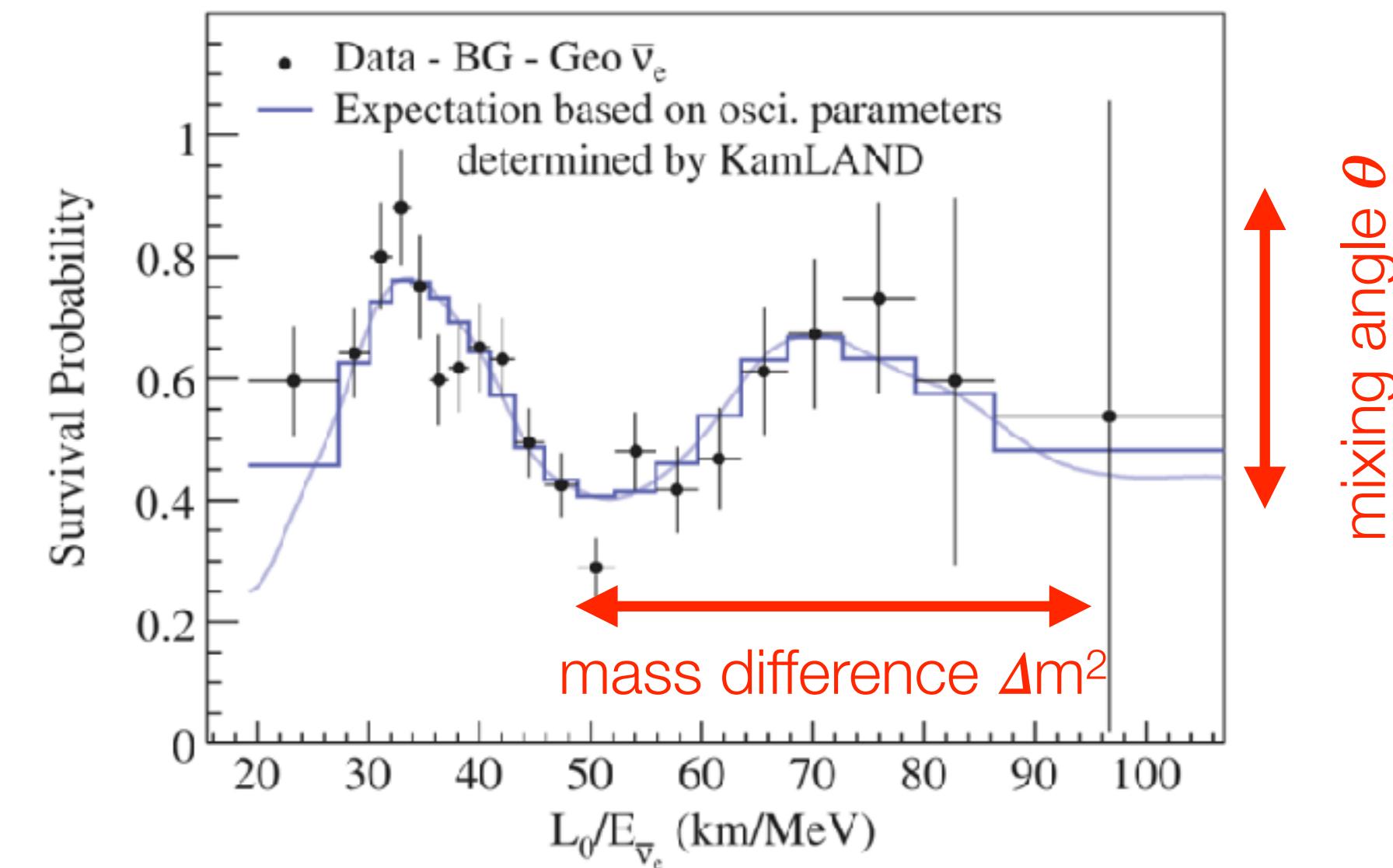
Interact by flavors

Mass terms:

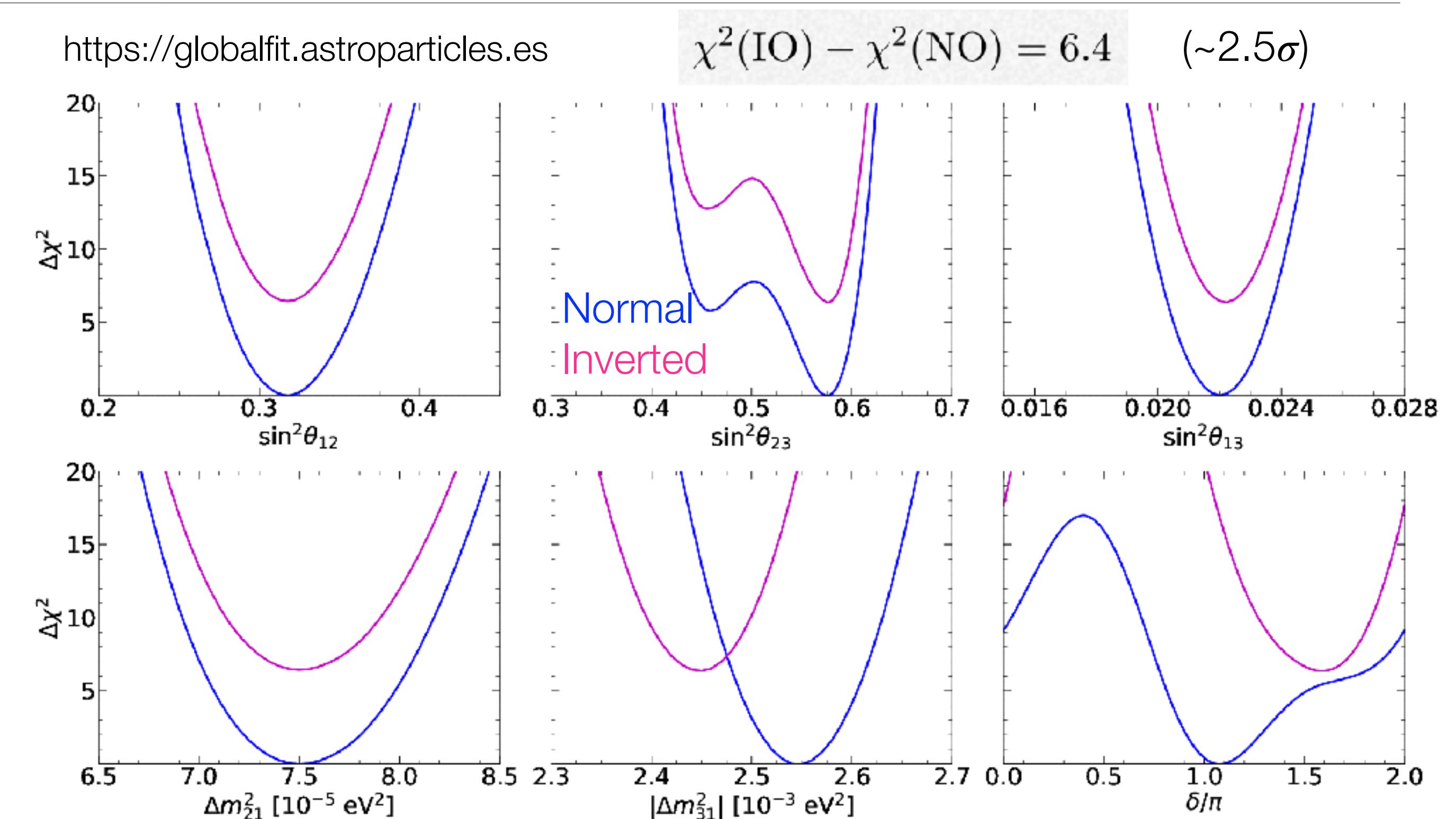
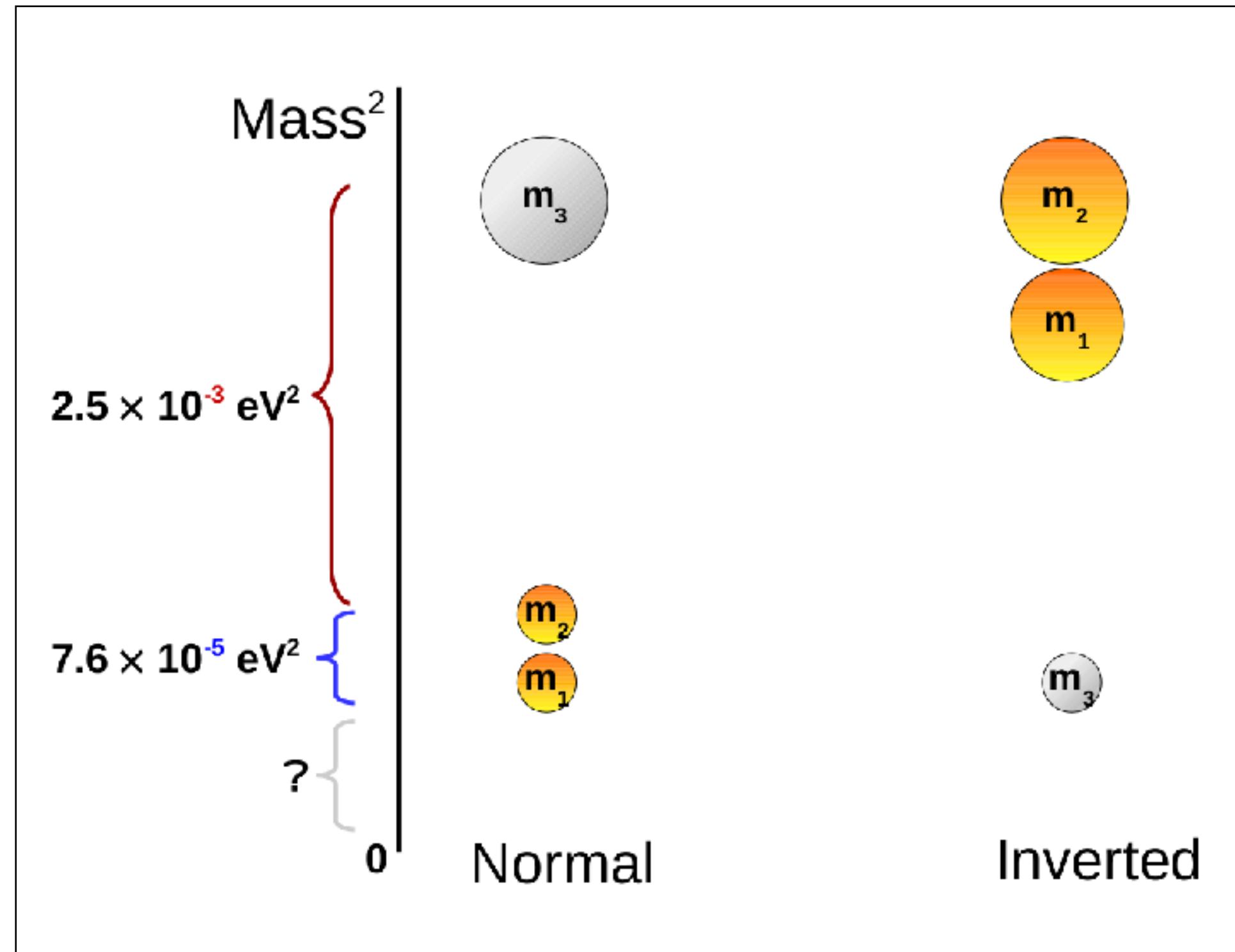
- Dirac (SM-like = Higgs coupling)
- Majorana (permitted, see-saw)

Mass measured: oscillations

$$P_{\text{osc}} = \sin^2(2\theta) \sin^2\left(\frac{\Delta m^2 L}{4E}\right)$$

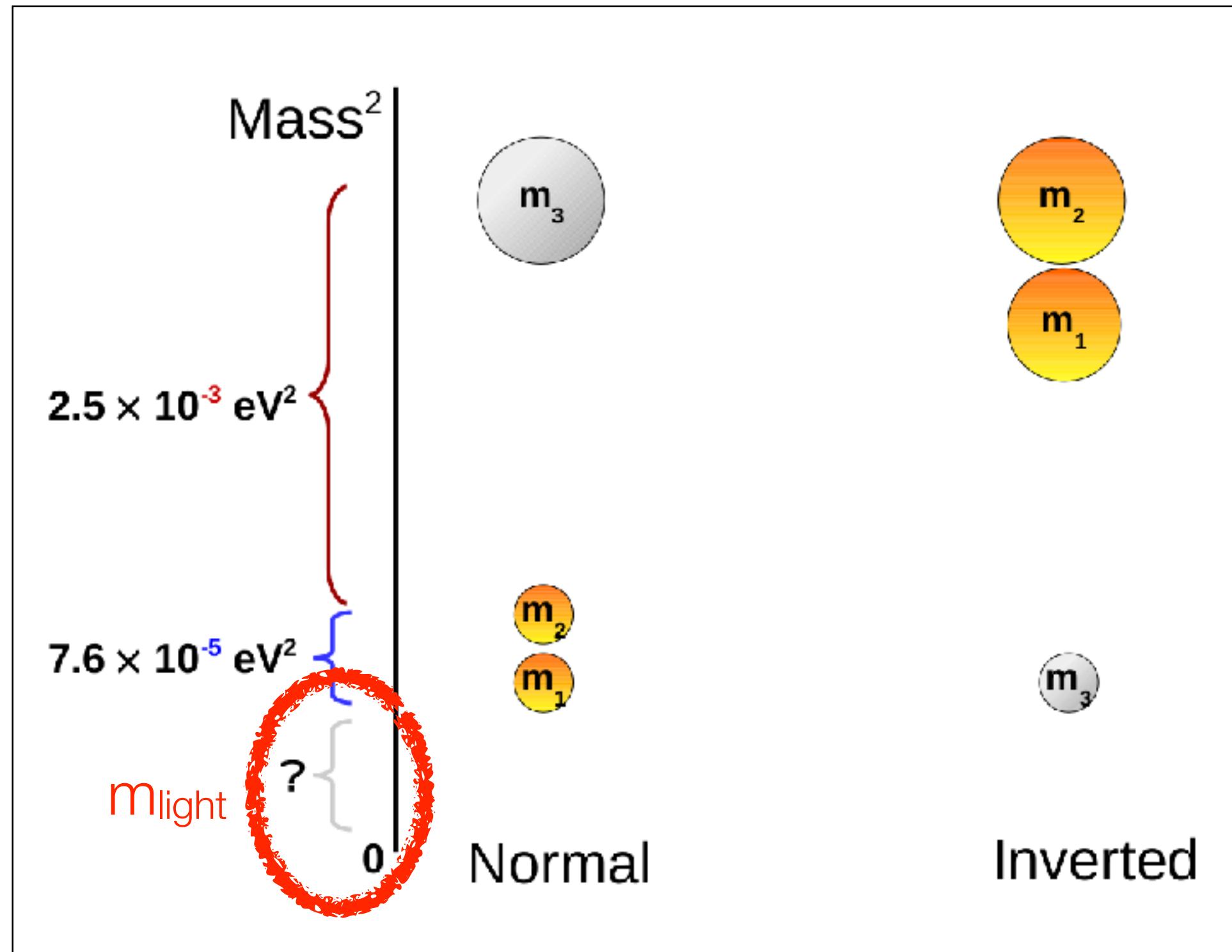


Neutrino masses and mass ordering



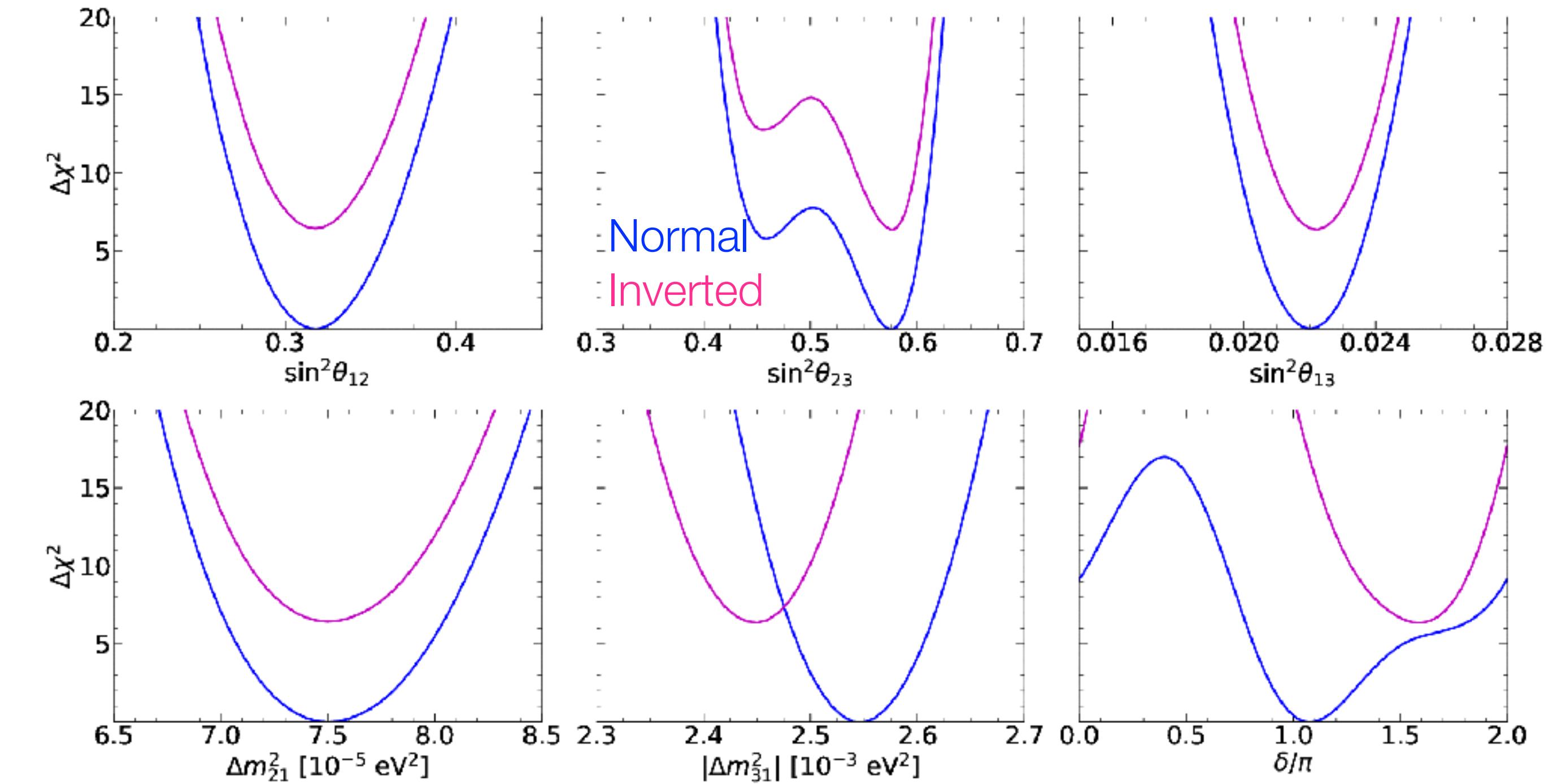
Upcoming experiments to settle mass ordering - ORCA, JUNO, IceCube, HyperK, DUNE...

Neutrino masses and mass ordering



<https://globalfit.astroparticles.es>

$$\chi^2(\text{IO}) - \chi^2(\text{NO}) = 6.4 \quad (\sim 2.5\sigma)$$



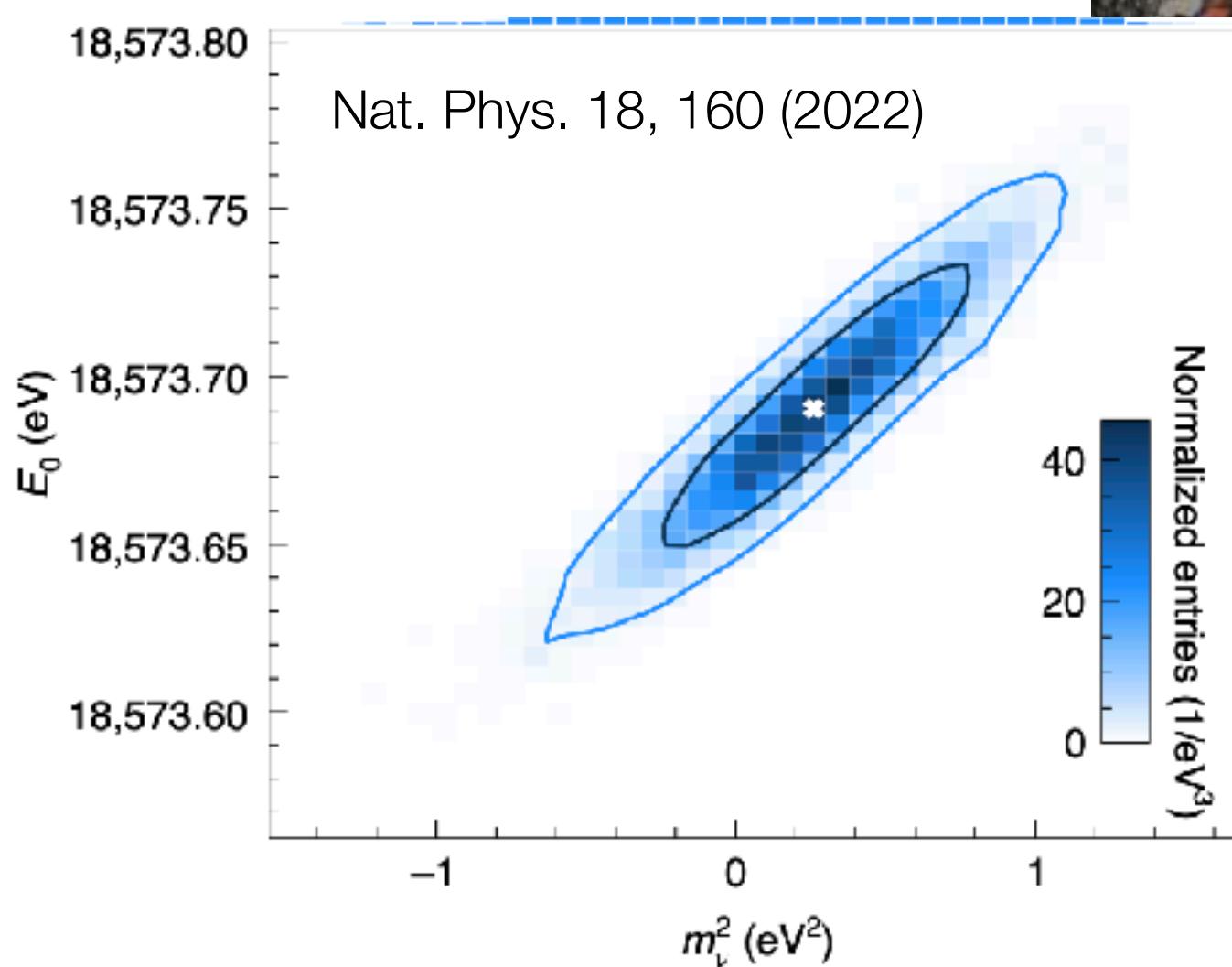
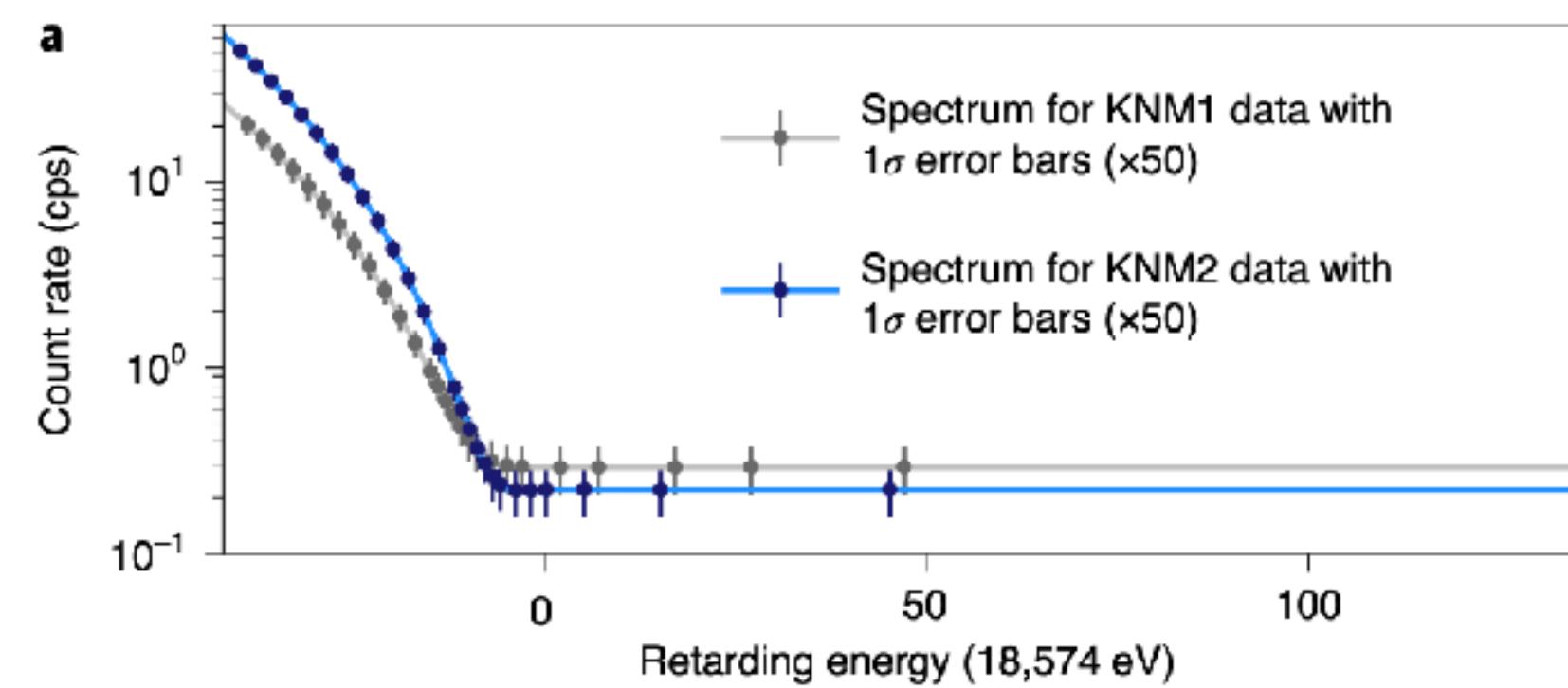
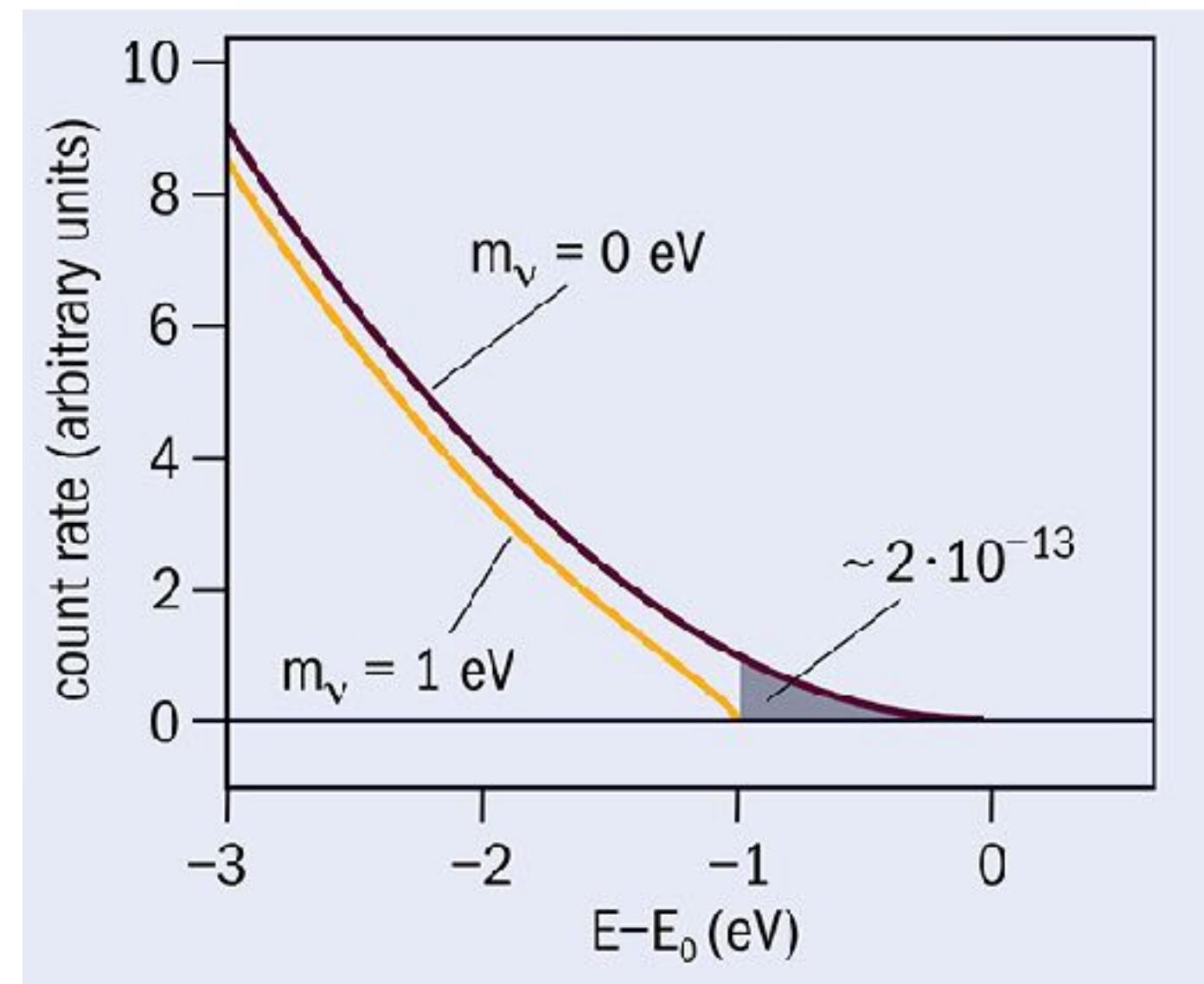
Upcoming experiments to settle mass ordering - ORCA, JUNO, IceCube, HyperK, DUNE...

Cosmology: measure $\Sigma m_\nu = m_1 + m_2 + m_3$

Normal: $\Sigma m_\nu > 58 \text{ meV}$

Inverted: $\Sigma m_\nu > 100 \text{ meV}$

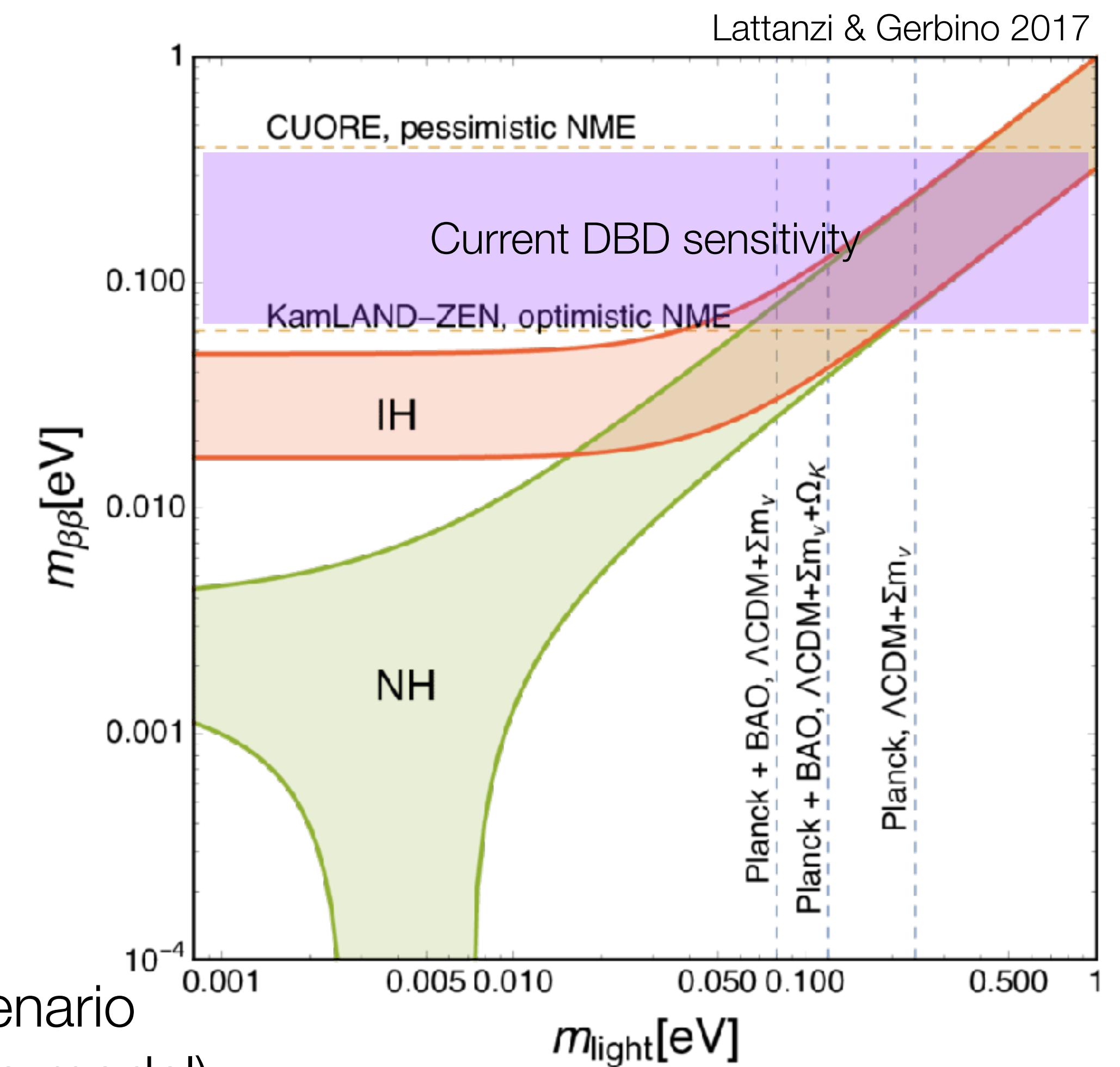
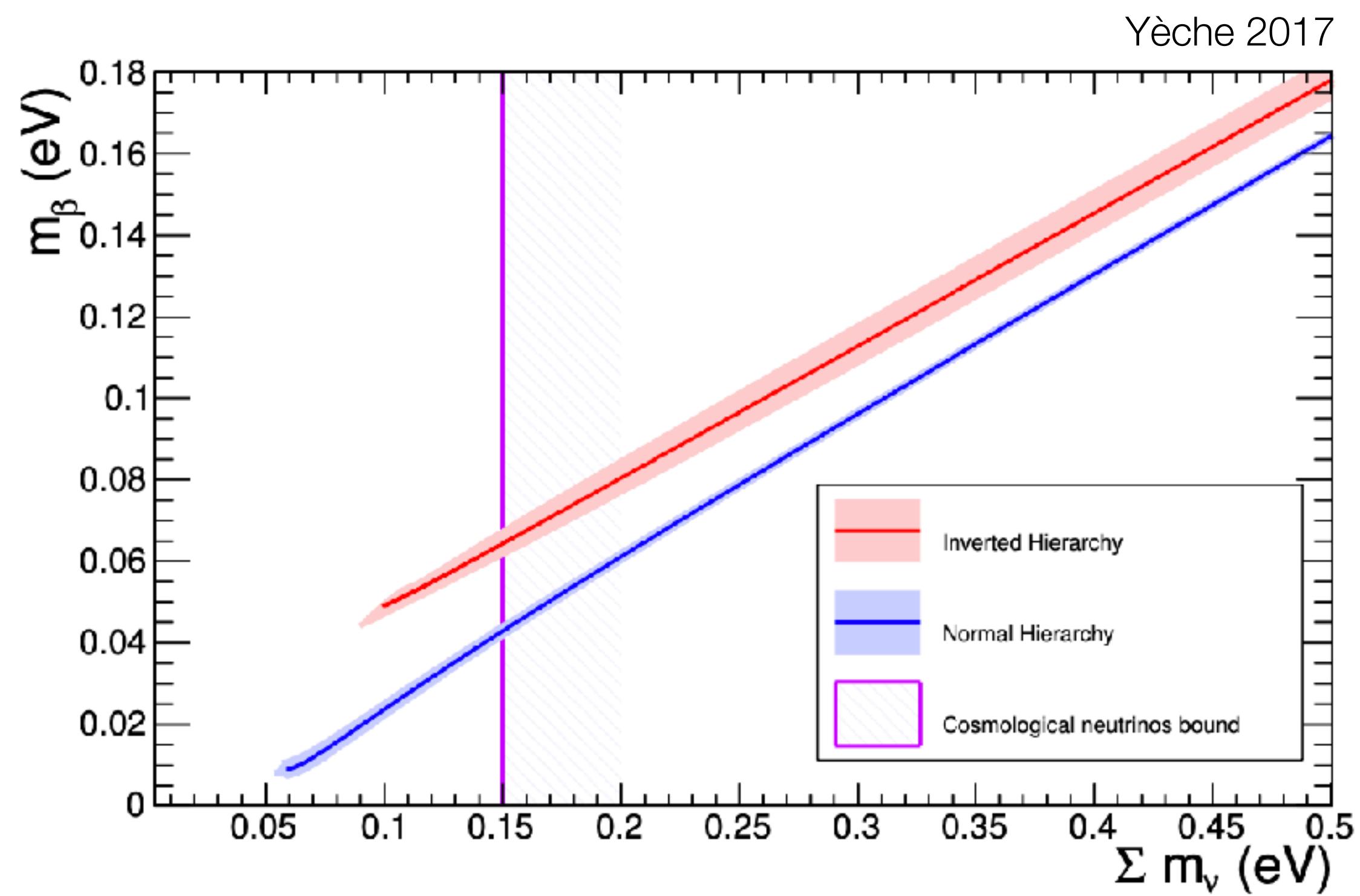
Absolute mass scale: KATRIN



$m_\beta < 0.8$ eV @ 90% CL

$$m_\beta = \left(\sum_i |U_{ei}|^2 m_i^2 \right)^{1/2}$$

Tritium, neutrinoless double beta decay (DBD), and cosmology



- Different "absolute" neutrino mass scales
- DBD more sensitive than tritium, but only for Majorana scenario
- Cosmology most competitive (with assumptions on cosmo model)

Cosmological neutrinos (CνB)

Very abundant cosmic fluid, well-known (in principle)

Thermal relic (decoupling @ T~MeV)

Transition to non-relativistic regime (at least 2/3): $1 + z_{\text{nr}} = 189 \left(\frac{m_\nu}{0.1 \text{eV}} \right)$

Hot dark matter (HDM)

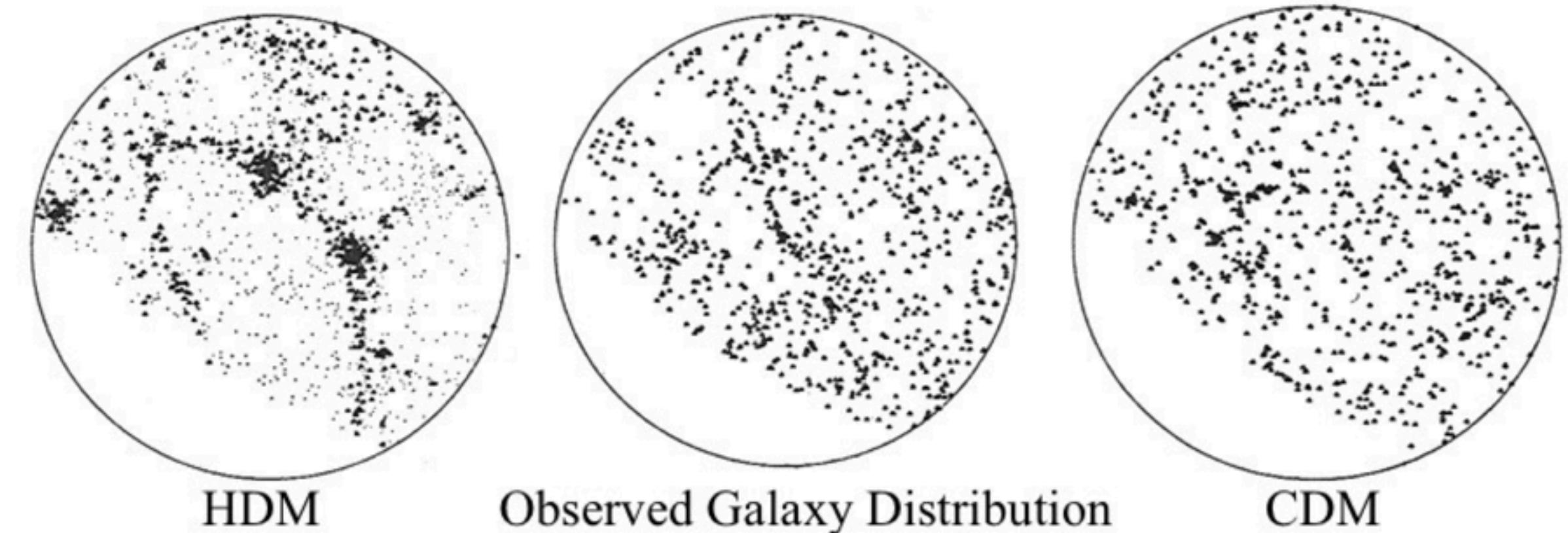
Relic energy density: $f_\nu = \frac{\Omega_\nu}{\Omega_m} \simeq 0.023 \left(\frac{\sum m_\nu}{0.3 \text{ eV}} \right) \left(\frac{0.14}{\omega_m} \right)$

S. White 1986

Back to the 80s... :

DM = neutrinos ?

Needed HDM, $m_\nu \sim 15 \text{ eV}$



Neutrino free-streaming

Relativistic fluid (not coupled to baryons):

$$\lambda_{\text{fs}} \sim \frac{c}{H}$$

⇒ In comoving coordinates : **maximum free-streaming scale @ NR**

transition:

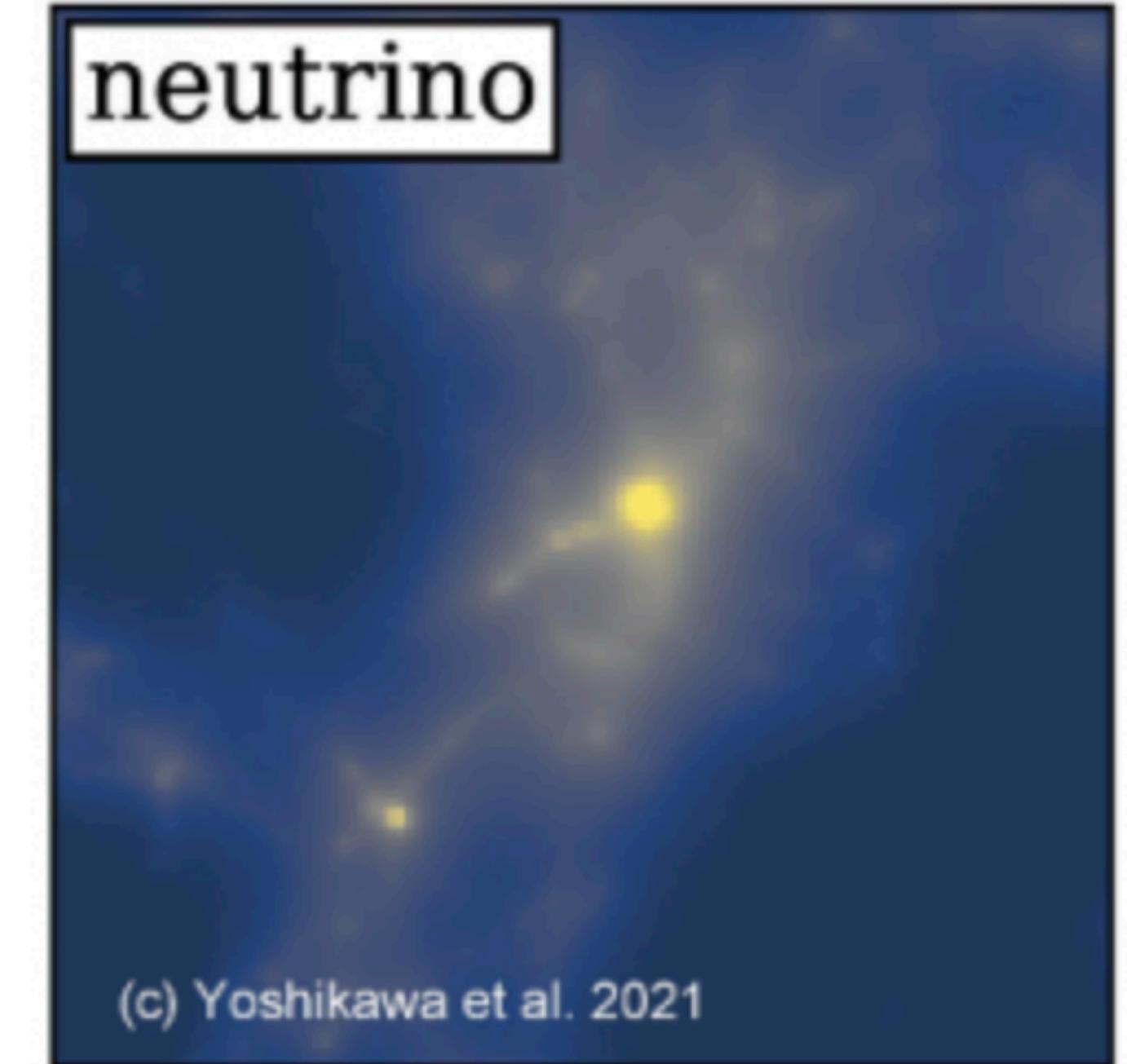
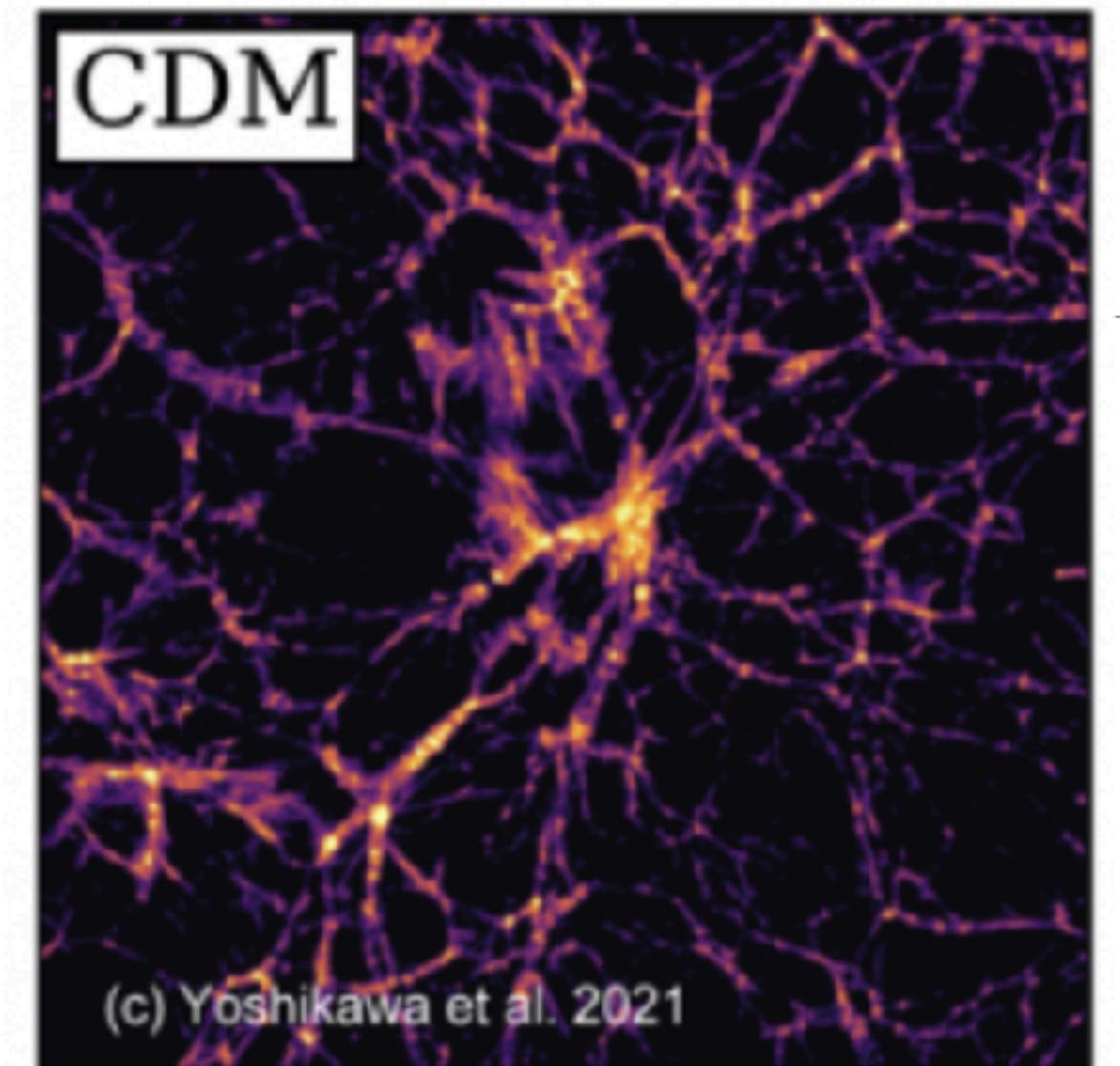
$$k_{\text{nr}} \simeq 0.002 \left(\frac{\omega_m}{0.14} \right)^{1/2} \left(\frac{m_\nu}{0.1 \text{ eV}} \right)^{1/2} \text{ Mpc}^{-1}$$

$k < k_{\text{nr}}$: $\delta_\nu \sim \text{CDM}$

$k \gg k_{\text{nr}}$: δ_ν highly damped

Non-relativistic regime:

$$\lambda_{\text{fs}} \sim \frac{3 T_\nu^0}{m_\nu} \frac{a_0}{aH}$$



Massive neutrinos: impact on matter P(k)

1) Do not contribute to **total** P(k):

$$P_m = P(c + b + \nu) = \langle \delta_c^2 \rangle \quad k < k_{\text{nr}} \\ = (1 - f_\nu)^2 \langle \delta_c^2 \rangle \quad k \gg k_{\text{nr}}$$

2) Backreaction on the gravitational potential:

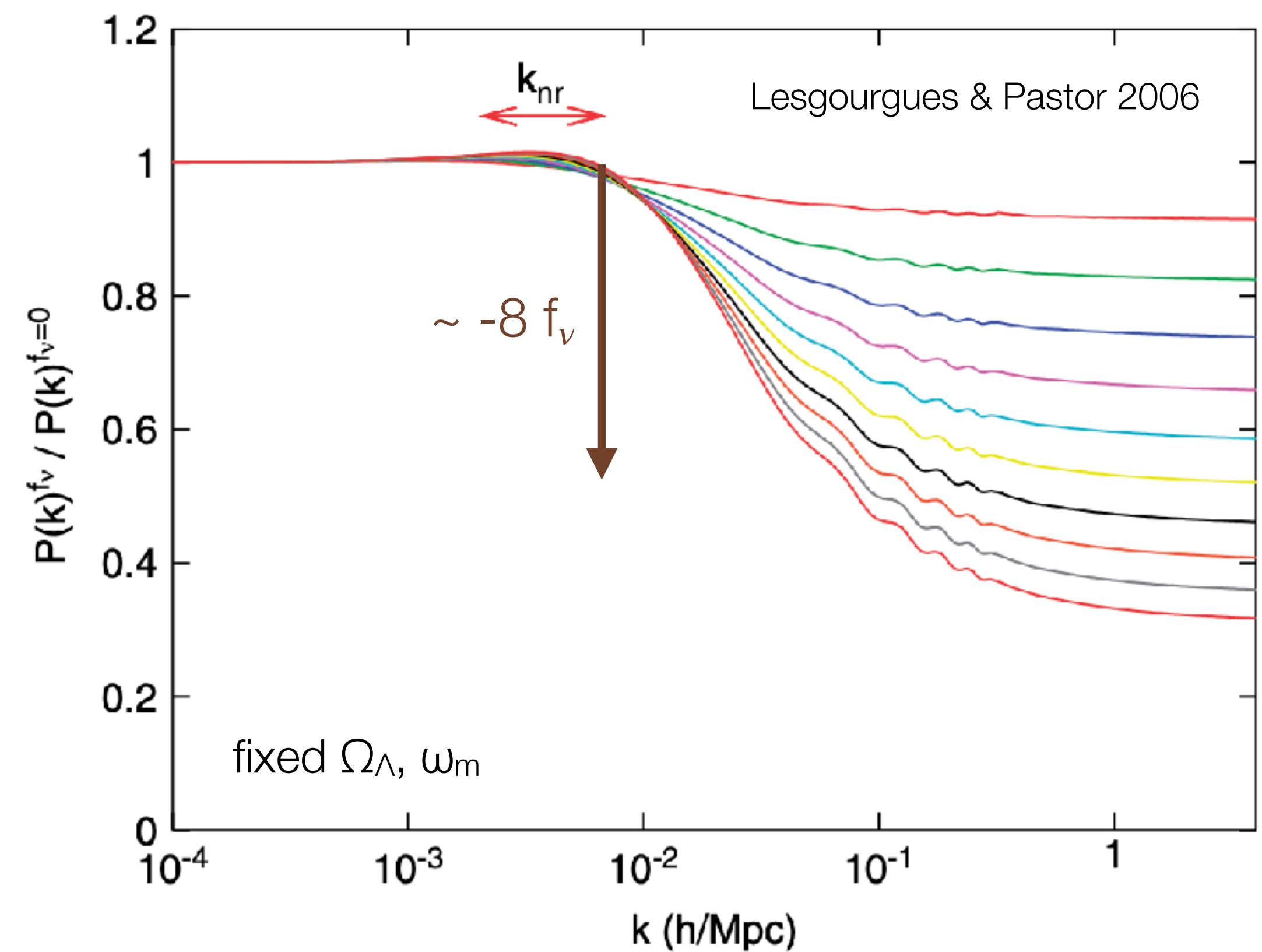
$$\ddot{\delta}_{\text{cdm}} + \frac{\dot{a}}{a} \dot{\delta}_{\text{cdm}} = 4\pi G a^2 \delta \rho, \quad \nu \text{ does not contribute}$$

ν contributes

$$\Rightarrow \ddot{\delta}_{\text{cdm}} + \frac{2}{\tau} \dot{\delta}_{\text{cdm}} - \frac{6}{\tau^2} (1 - f_\nu) \delta_{\text{cdm}} = 0.$$

$$\delta_{\text{cdm}} \sim a^{1-3f_\nu/5}$$

$$P_m(k \gg k_{\text{nr}}) \sim P_m(f_\nu = 0) \times (1 - 8f_\nu)$$



Non-linear evolution / simulations

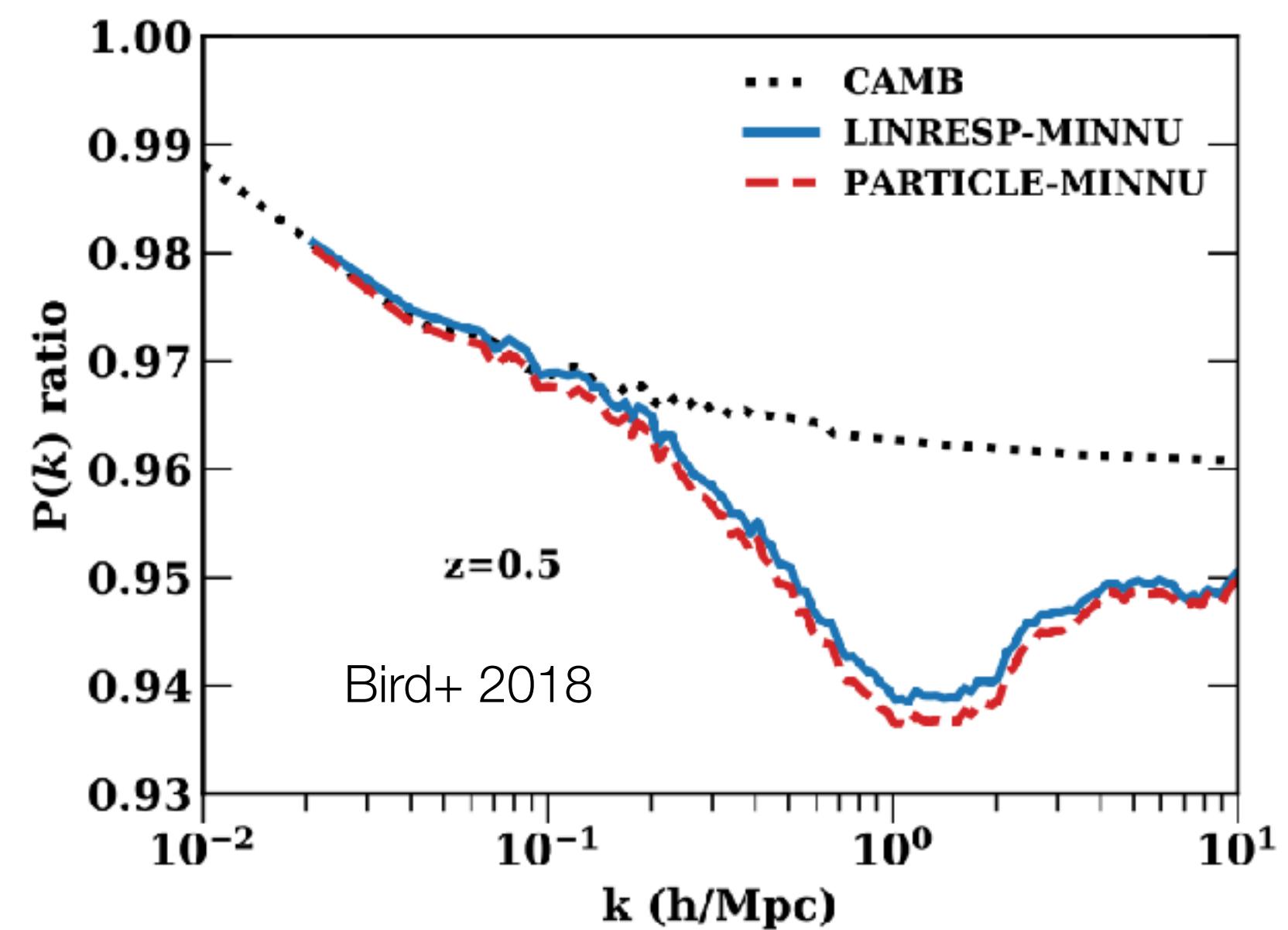
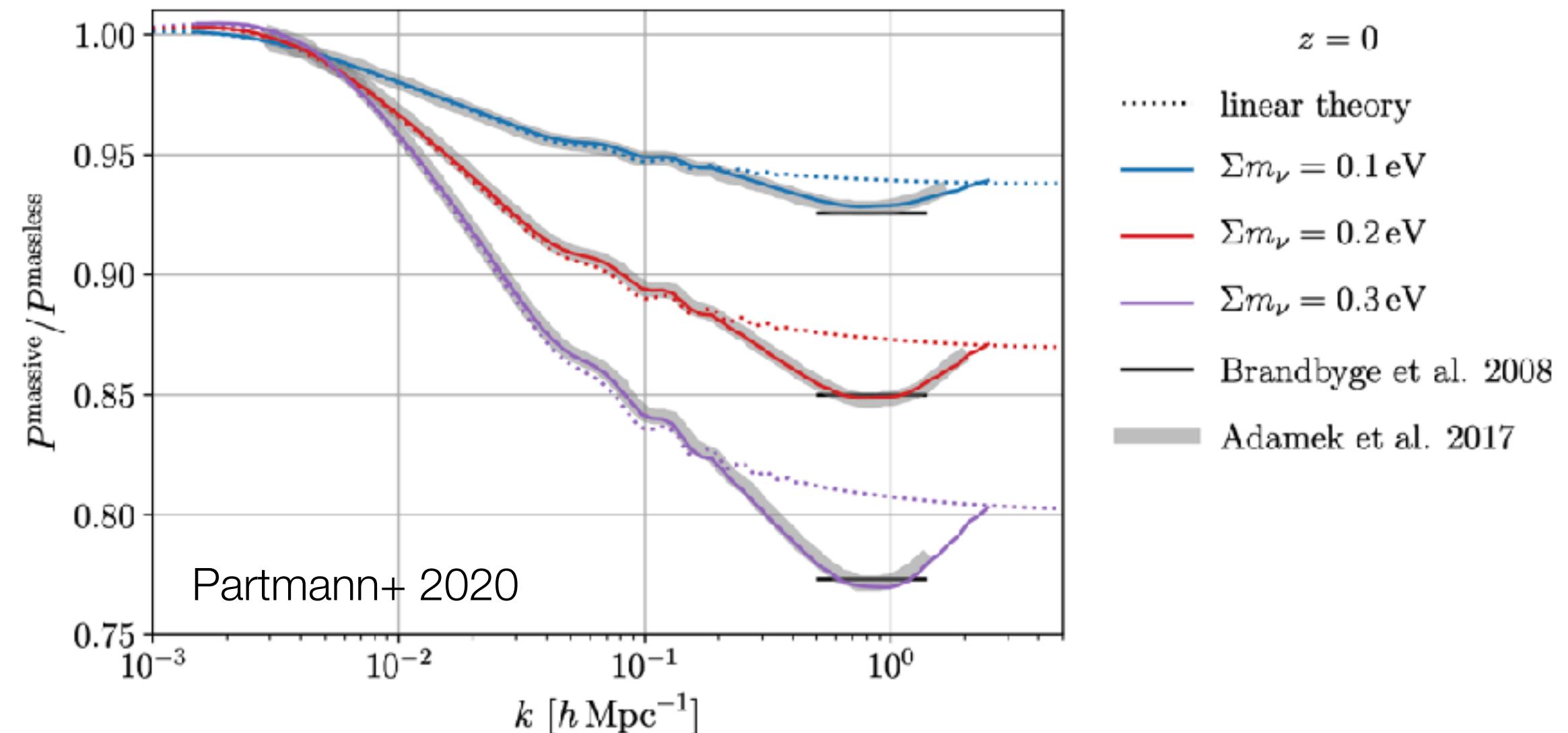
See Julian Adamek's talk

Velocity dispersion

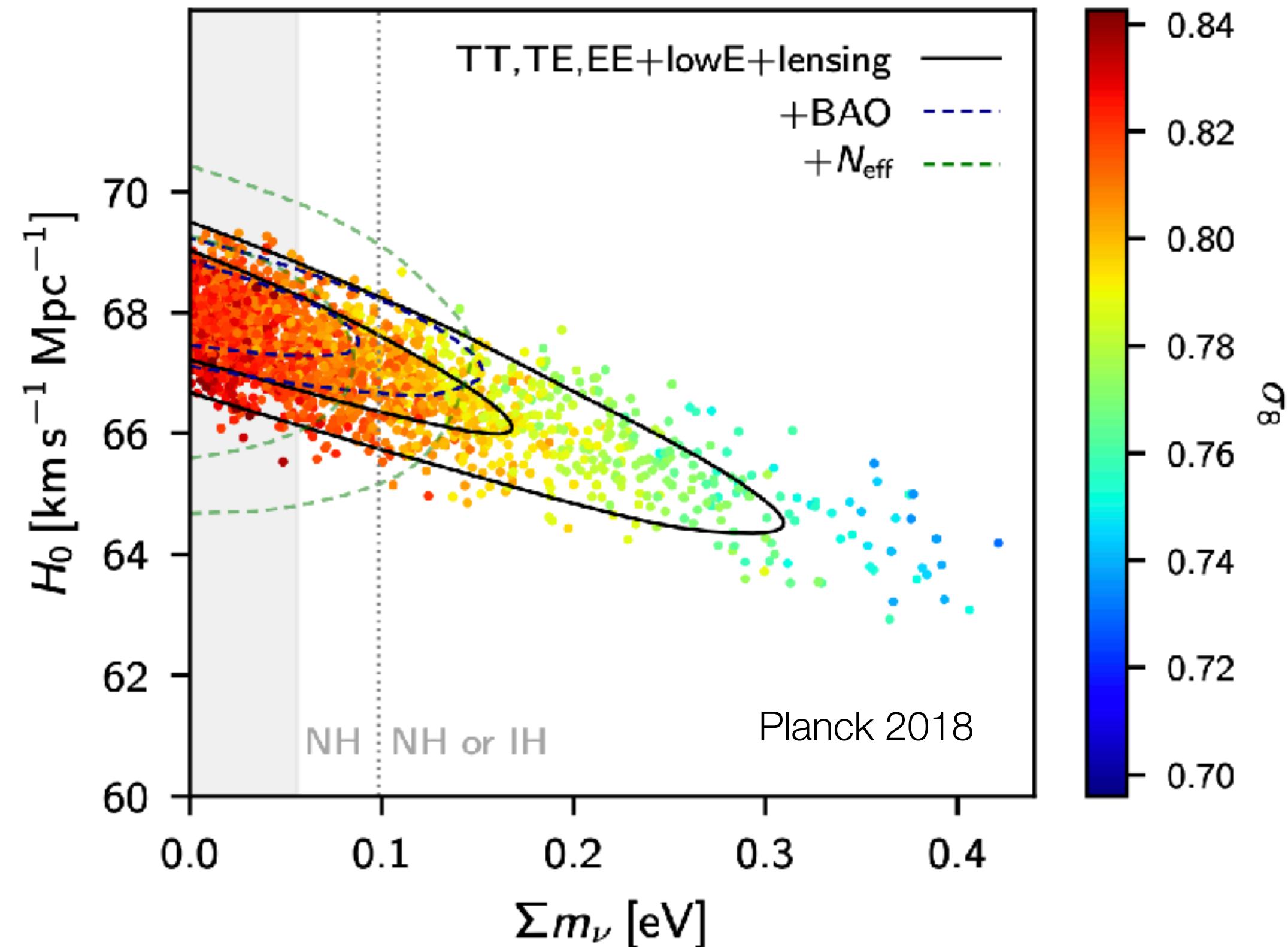
⇒ Need more particles than for CDM

Many strategies proposed

- eg. map with- ν simulations with no- ν simulations, varying cosmo parameters to mimick P_{lin} in RoI ("spoon effect" is not specific to ν)
- eg. linear response approximation

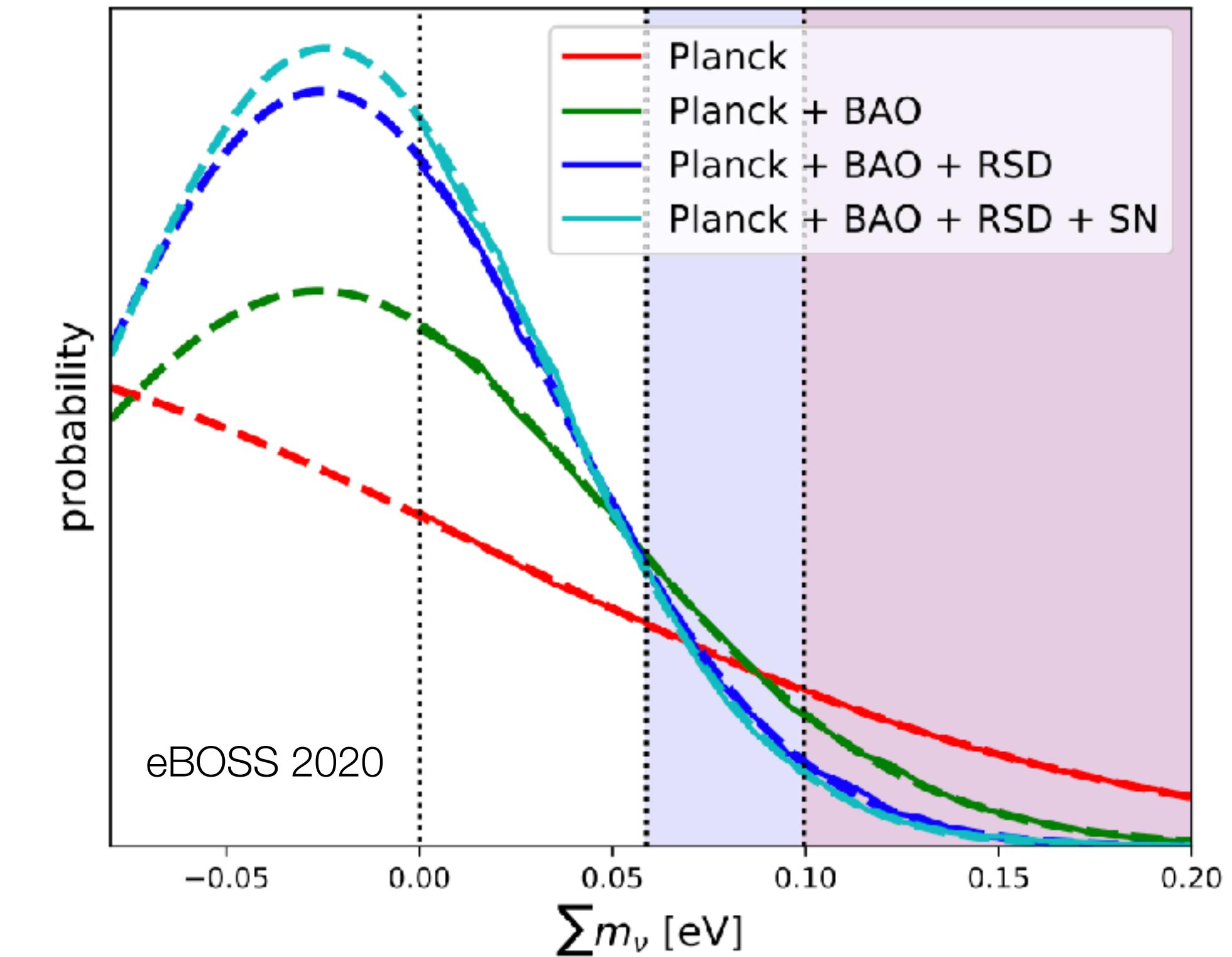


Current CMB + BAO mass bounds



$\sum m_\nu < 0.26$ eV (95 %, Planck TT,TE,EE+lowE)

Planck data somewhat favors "unphysical" neutrino mass



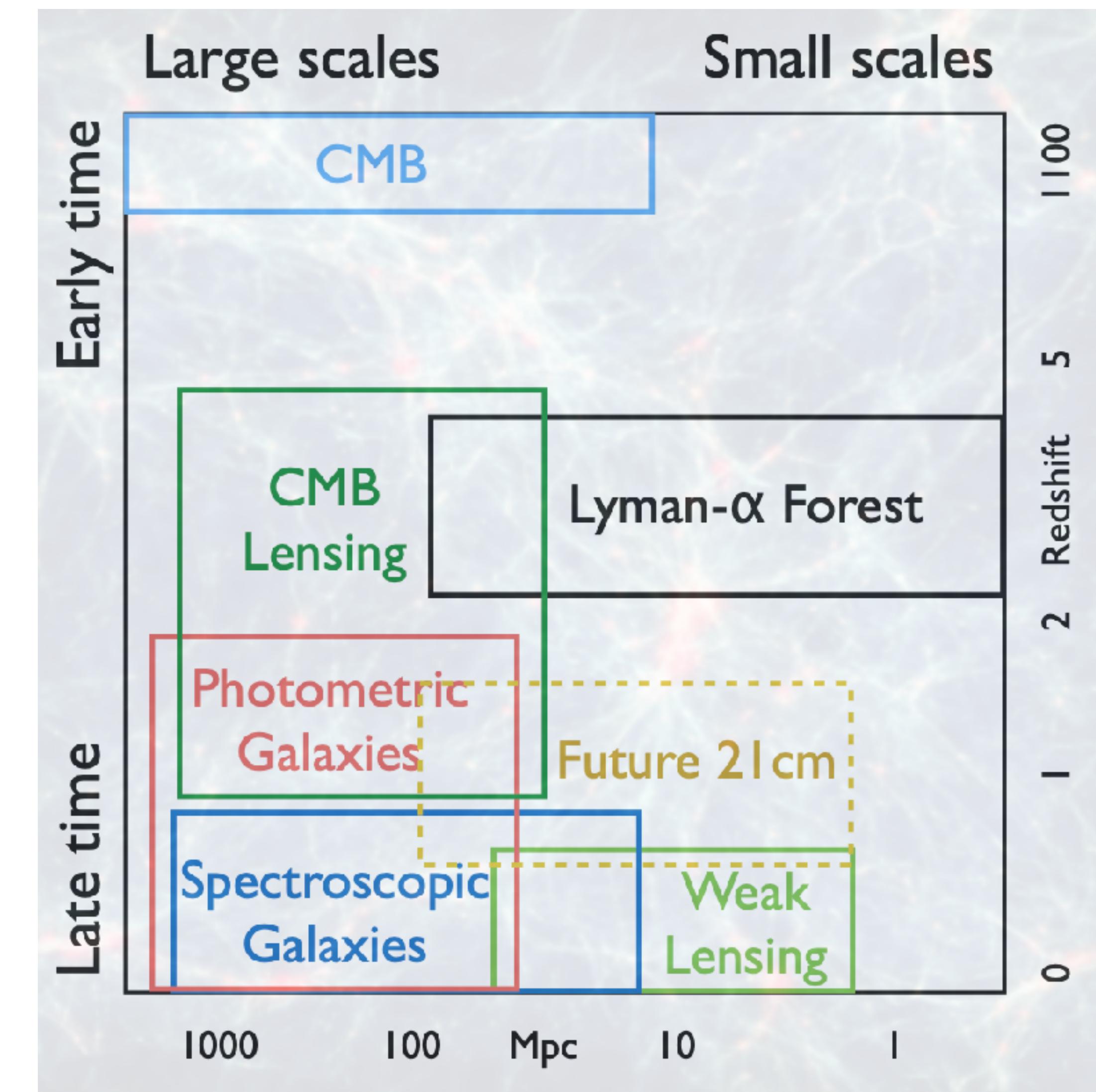
Planck+BAO: $\sum m_\nu < 126$ meV

Probes of Σm_ν with matter distribution

Many probes in the market
All with sensitivity to Σm_ν
Degeneracies with other cosmo pars
Mitigate impacts of systematics

- NL effects (optimal k / ell range)
- baryons, bias, IA, others ...

CMB lensing
Full-shape $P(k)$ from clustering (incl. RSD)
Galaxy WL statistics
Void properties
Lyman-alpha forest
Cross-correlations
...



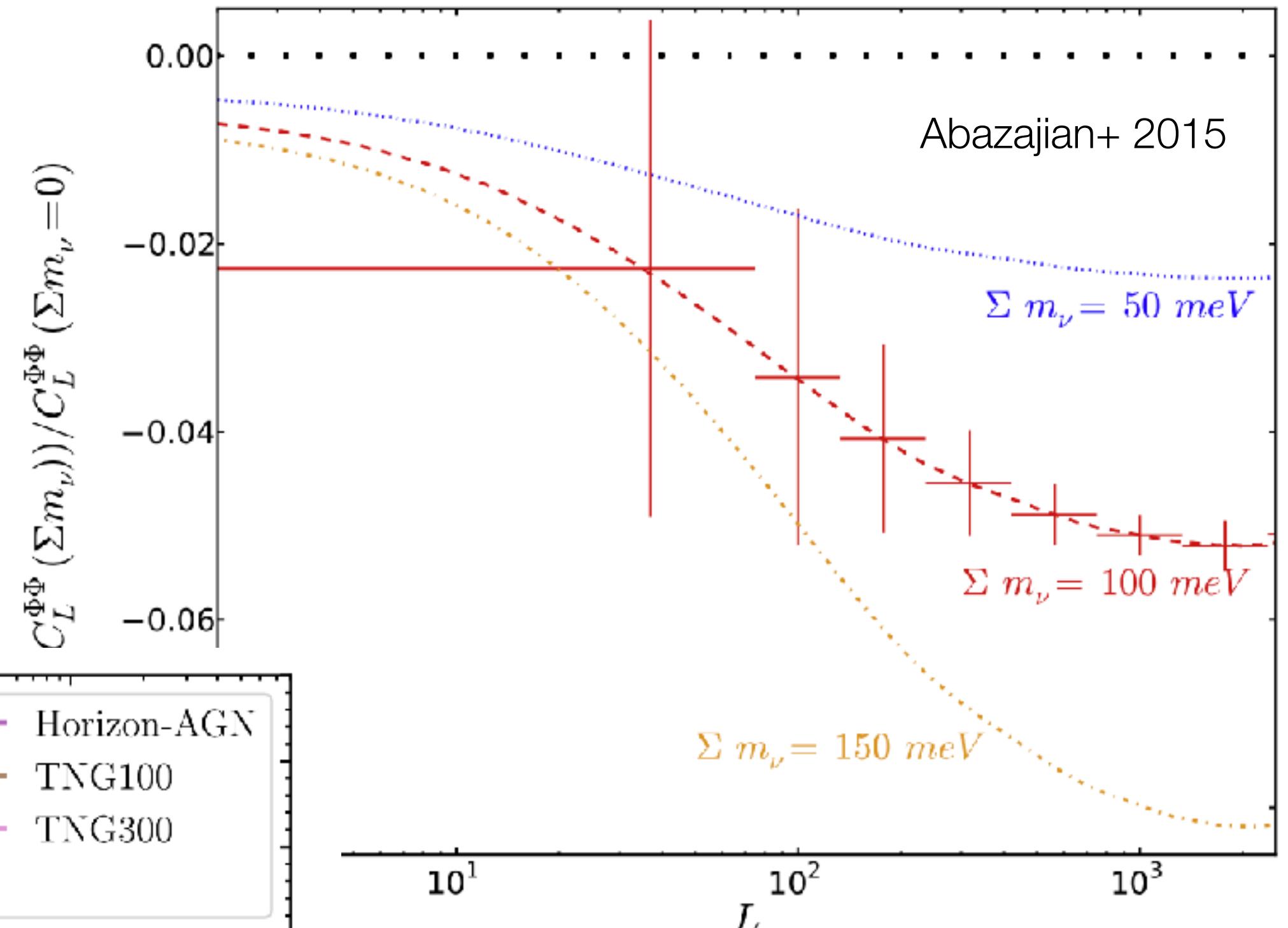
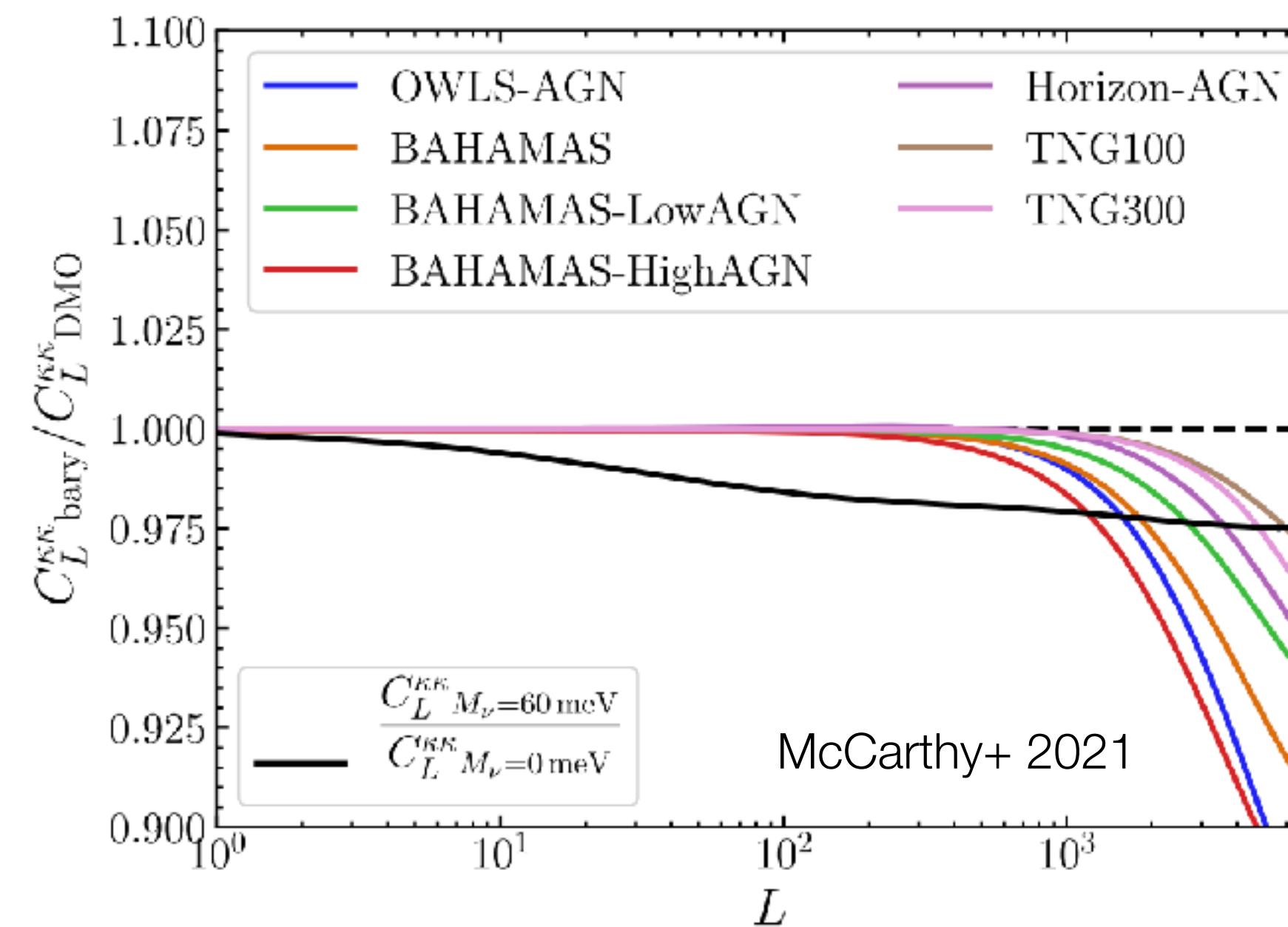
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high-ell data contaminated by feedback

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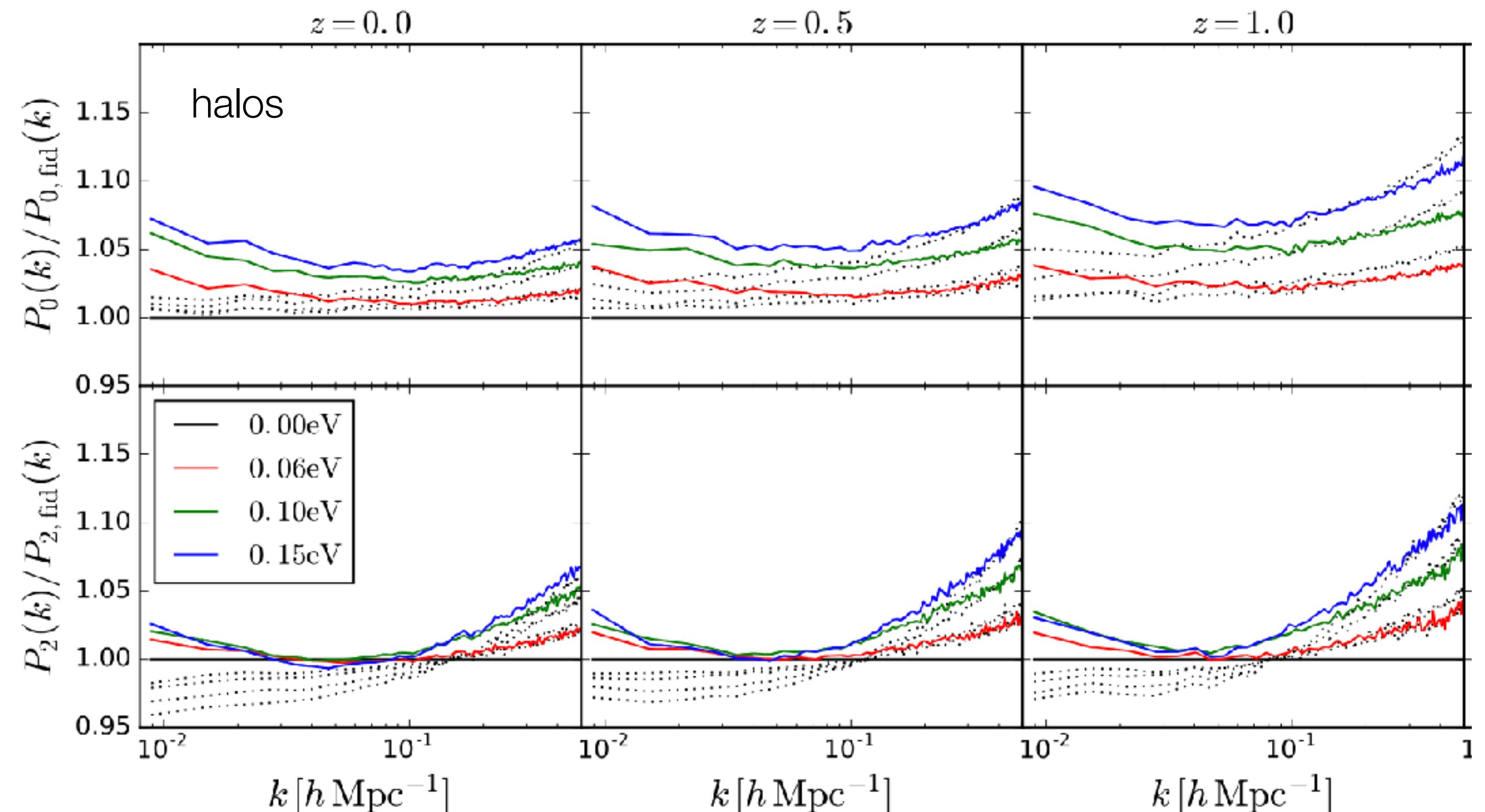
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...



subtleties about bias...

Villaescusa-Navarro+ 2017

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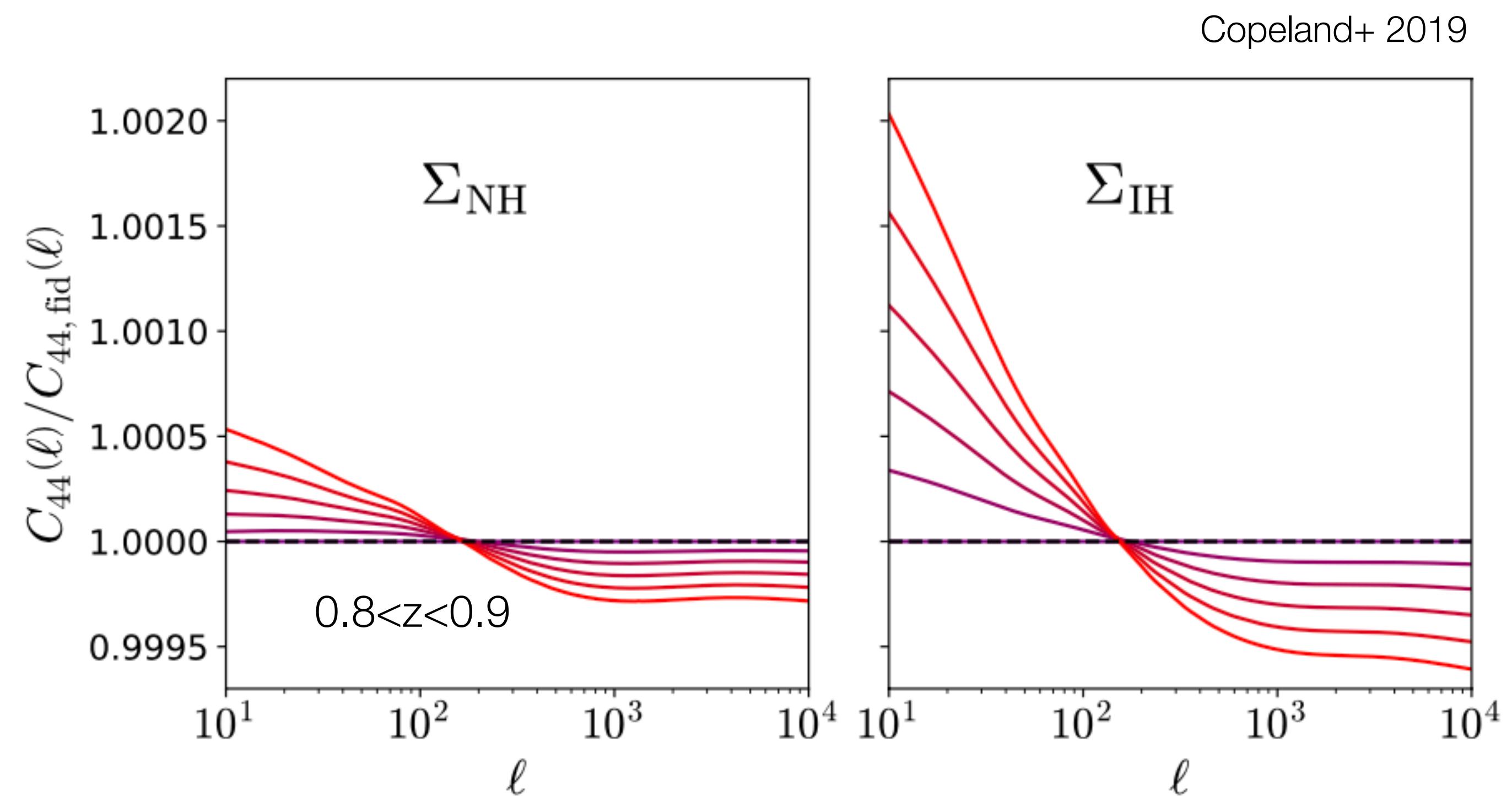
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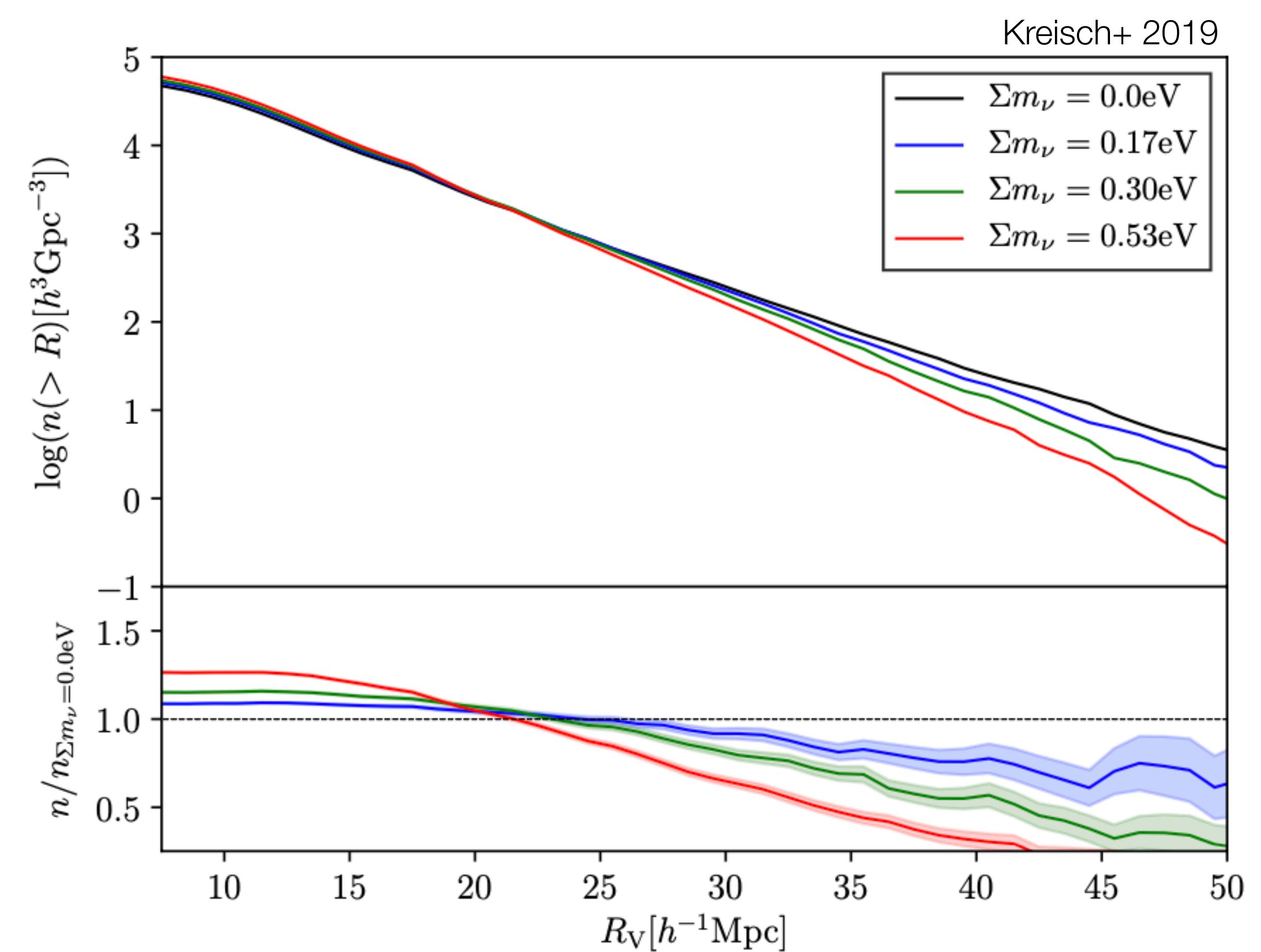
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...



Forecast ...



Data	$\sigma_{\Sigma m_\nu}$ [eV]	$\sigma_{N_{\nu, \text{eff}}}$
Planck	0.56	0.19
Planck + BAO	0.087	0.18
Gal ($k_{\text{max}} = 0.1 h \text{ Mpc}^{-1}$)	0.030	0.13
Gal ($k_{\text{max}} = 0.2 h \text{ Mpc}^{-1}$)	0.021	0.083
Ly- α forest	0.041	0.11
Ly- α forest + Gal ($k_{\text{max}} = 0.2$)	0.020	0.062



Parameter	Modified Gravity	Dark Matter	f_{NL}	Dark Energy		
	γ	m_ν/eV		w_p	w_a	FoM
Euclid Primary	0.010	0.027	5.5	0.015	0.150	430
Euclid All	0.009	0.020	2.0	0.013	0.048	1540
Euclid+Planck	0.007	0.019	2.0	0.007	0.035	4020
Current	0.200	0.580	100	0.100	1.500	~10
Improvement Factor	30	30	50	>10	>50	>300

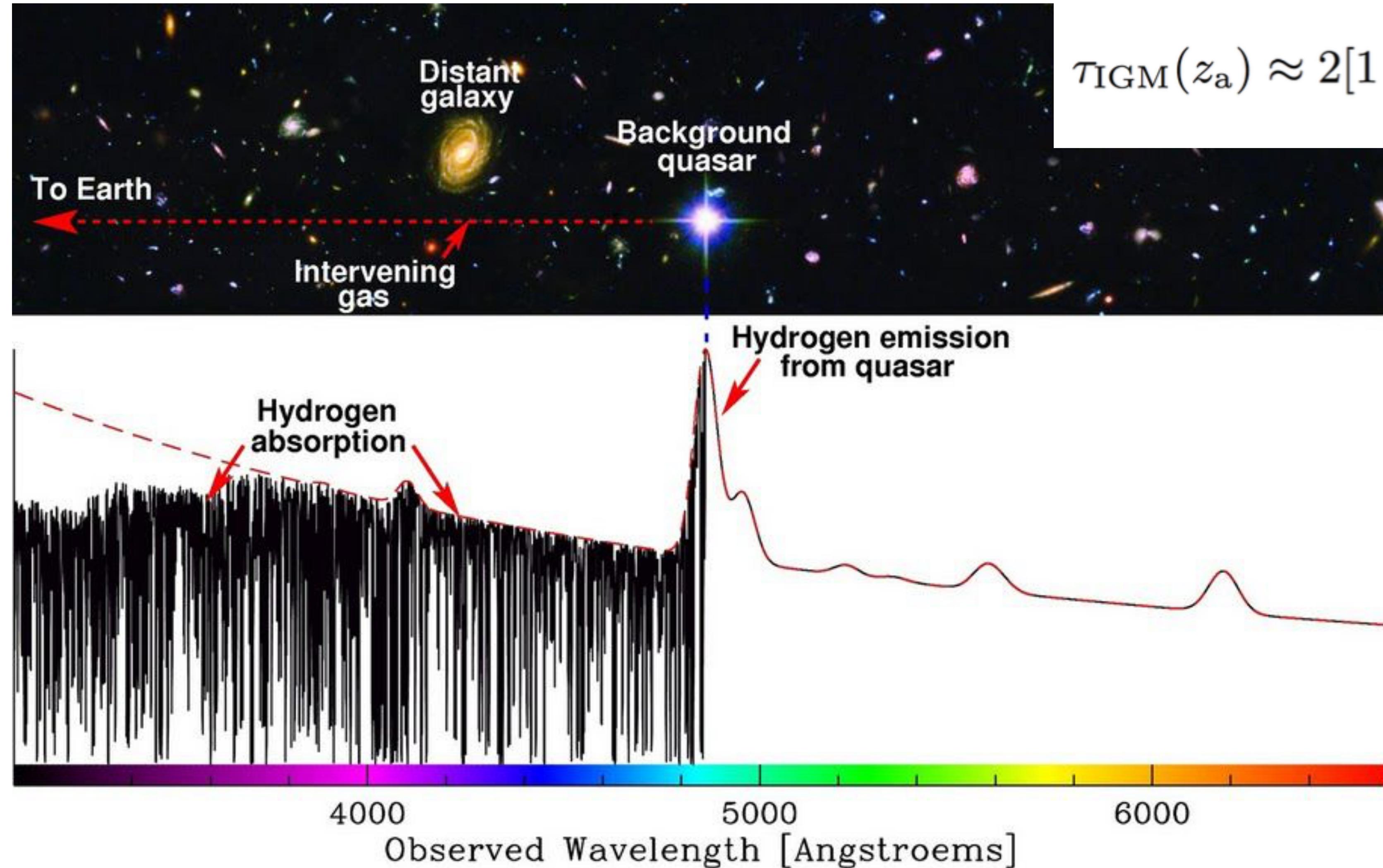


Setup	$\sigma(\Sigma m_\nu)$ [meV]	$\sigma(\Sigma m_\nu)$ [meV]	$\sigma(\Omega_k)$ $[\times 10^{-3}]$	$\sigma(w_0)$	$\sigma(w_a)$
S4	73	111	0.79	1.14	2.46
(+ DESI BAO)	29	76	0.48	0.13	0.41
LSST-clustering	69	91	3.33	0.42	1.22
LSST-shear	41	120	2.99	0.19	0.57
LSST-shear+clust	32	72	2.06	0.11	0.33
S4+LSST	23	28	0.49	0.10	0.26
	-	24	0.49	-	-

Setup (+CV- τ)	$\sigma(\Sigma m_\nu)$ [meV]	$\sigma(\Sigma m_\nu)$ [meV]	$\sigma(\Omega_k)$ $[\times 10^{-3}]$	$\sigma(w_0)$	$\sigma(w_a)$
LSST-clustering	69	91	3.3	0.42	1.20
LSST-shear	31	117	2.82	0.18	0.55
LSST-shear+clust	24	72	1.99	0.11	0.31
S4+LSST	14	21	0.49	0.10	0.26
	-	15	0.49	-	-

From C. Yèche, ADE 2019

The example of Lyman- α forest



$$\tau_{\text{IGM}}(z_a) \approx 2[1 + \delta(z_a)]^2 \frac{\alpha_{\text{rec}}(T)}{\Gamma} \left(\frac{1 + z_a}{4}\right)^{4.5}$$

n_{HI}

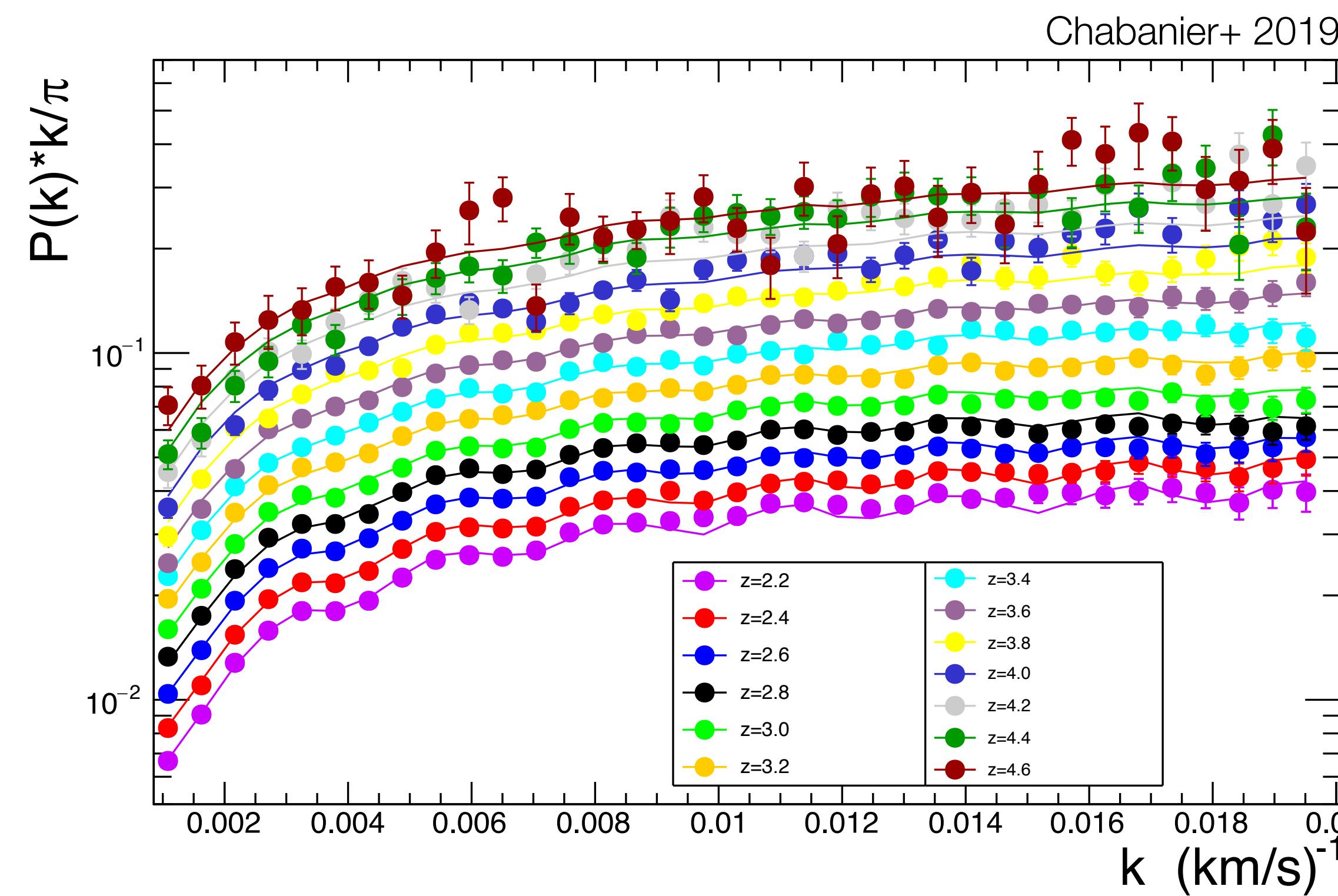
Measure $\exp(-\tau)$

$\tau \sim 1$ for **mild density fluctuations in the IGM**

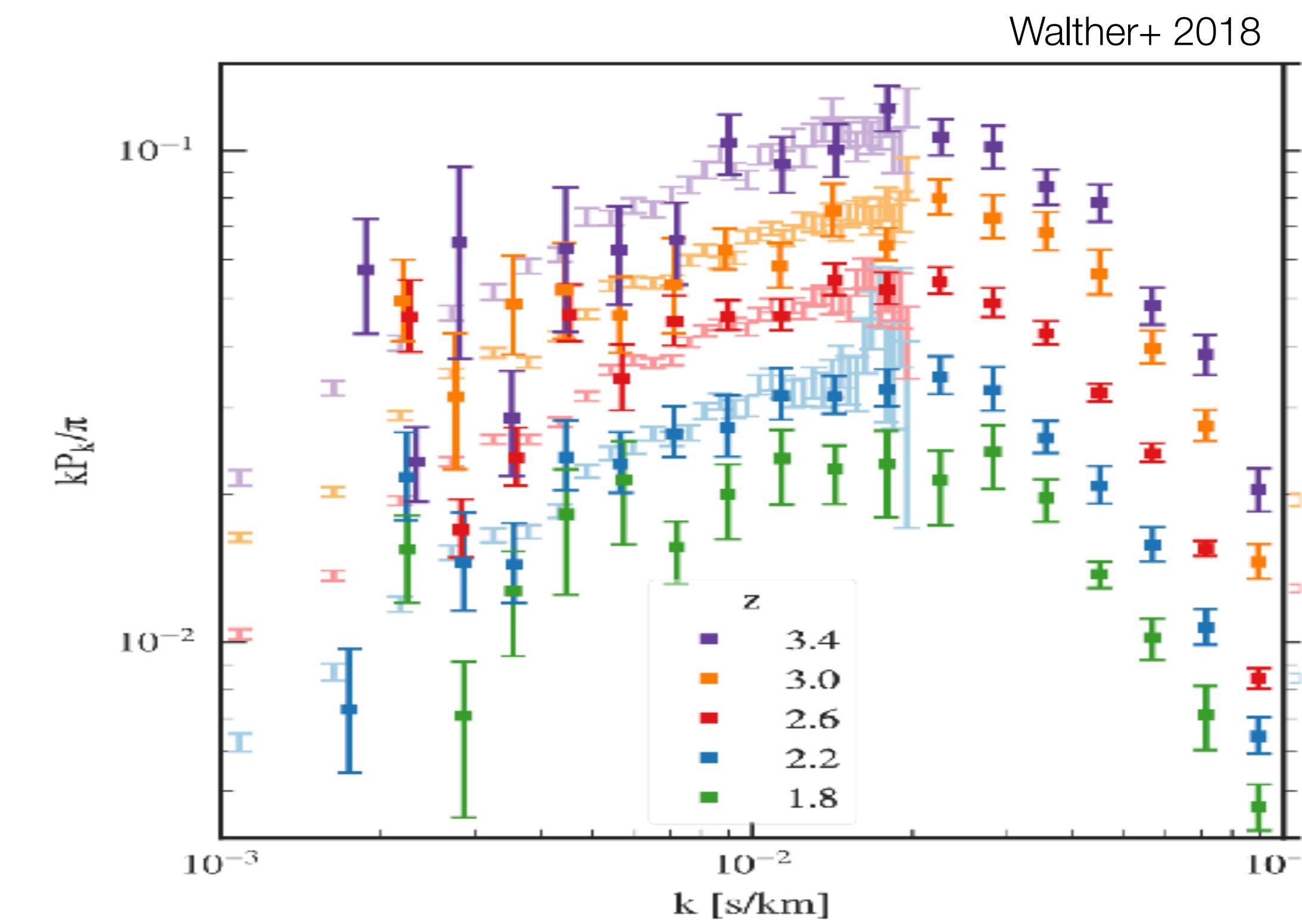
Measured small-scale correlations in Ly- α forest: P1D

Currently, separation between lines-of-sight $>>$ Mpc

\Rightarrow measure **1D power spectrum of absorption fluctuations** \sim correlations within individual lines-of-sight



eBOSS



high-resolution

"Full-shape" modelling P1D

Hydro simulations

Gadget (SPH for baryons) with "QUICKLYA" ~ do not model galaxies

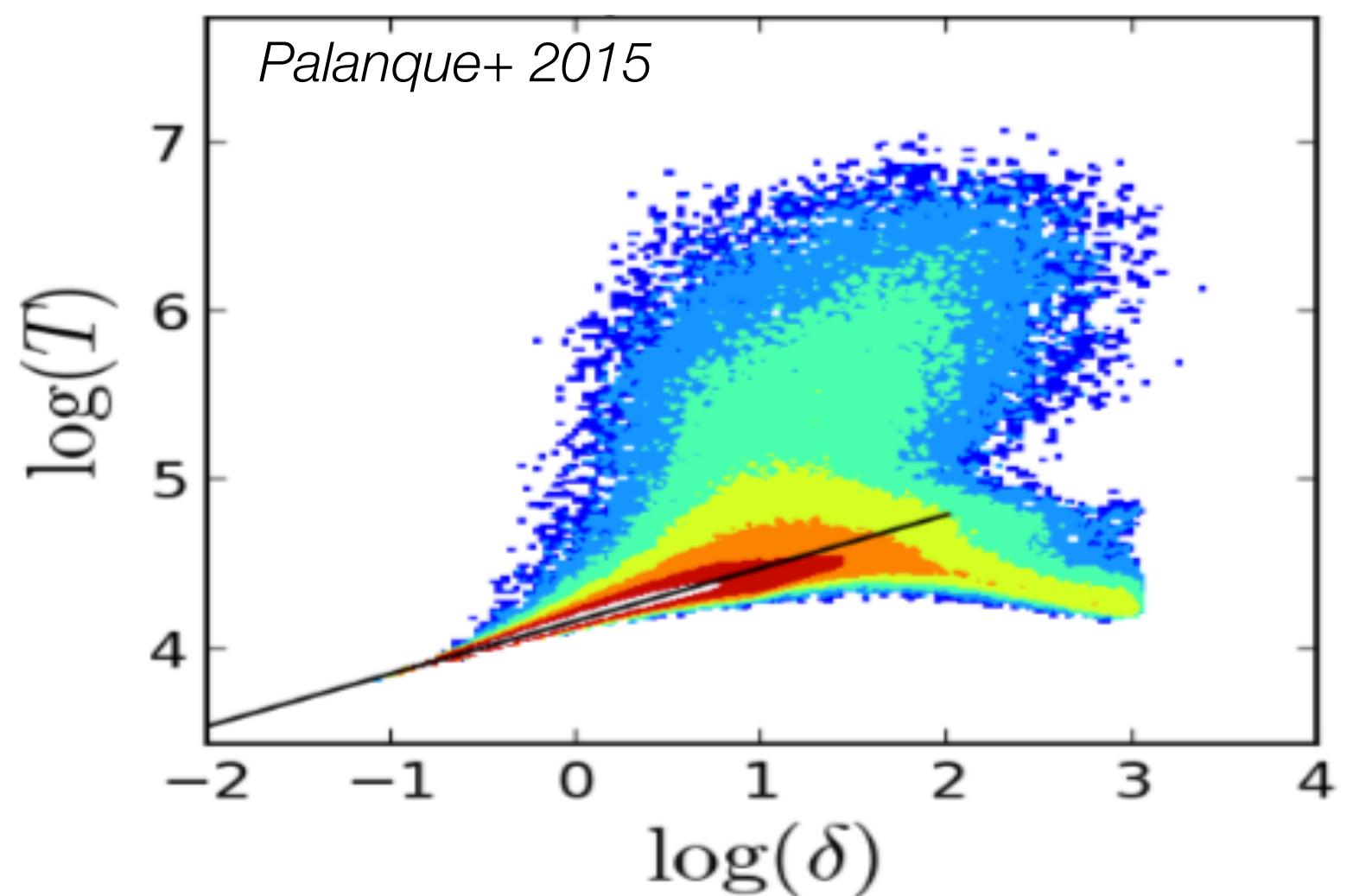
Draw skewers through snapshots, compute $(P1D)_{\text{model}}$

Box size ~ 100 Mpc

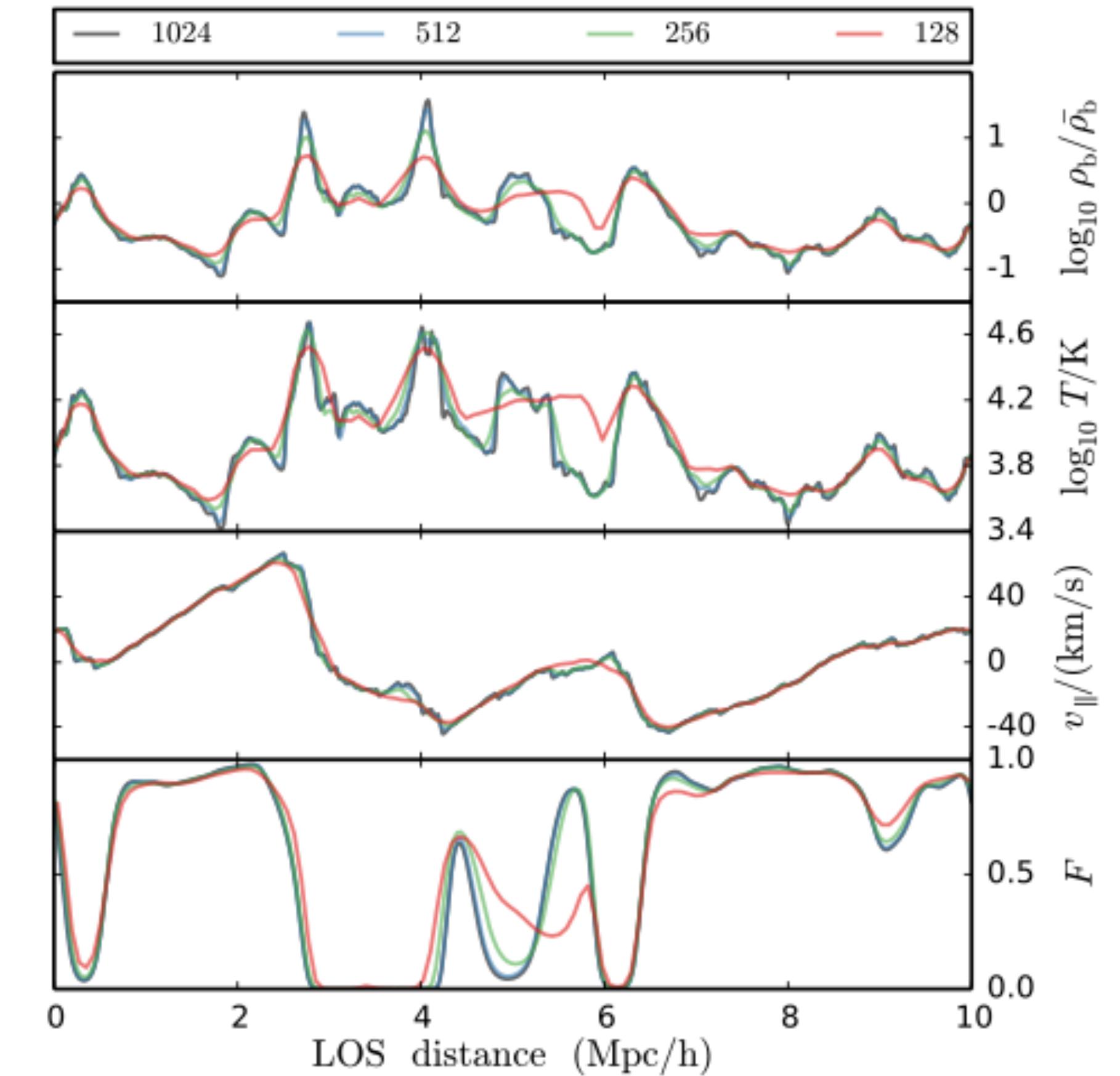
Start simulation @ $z=30$ (massive neutrinos) !

Grid of cosmology + IGM parameters

"Taylor" interpolation between simulation points



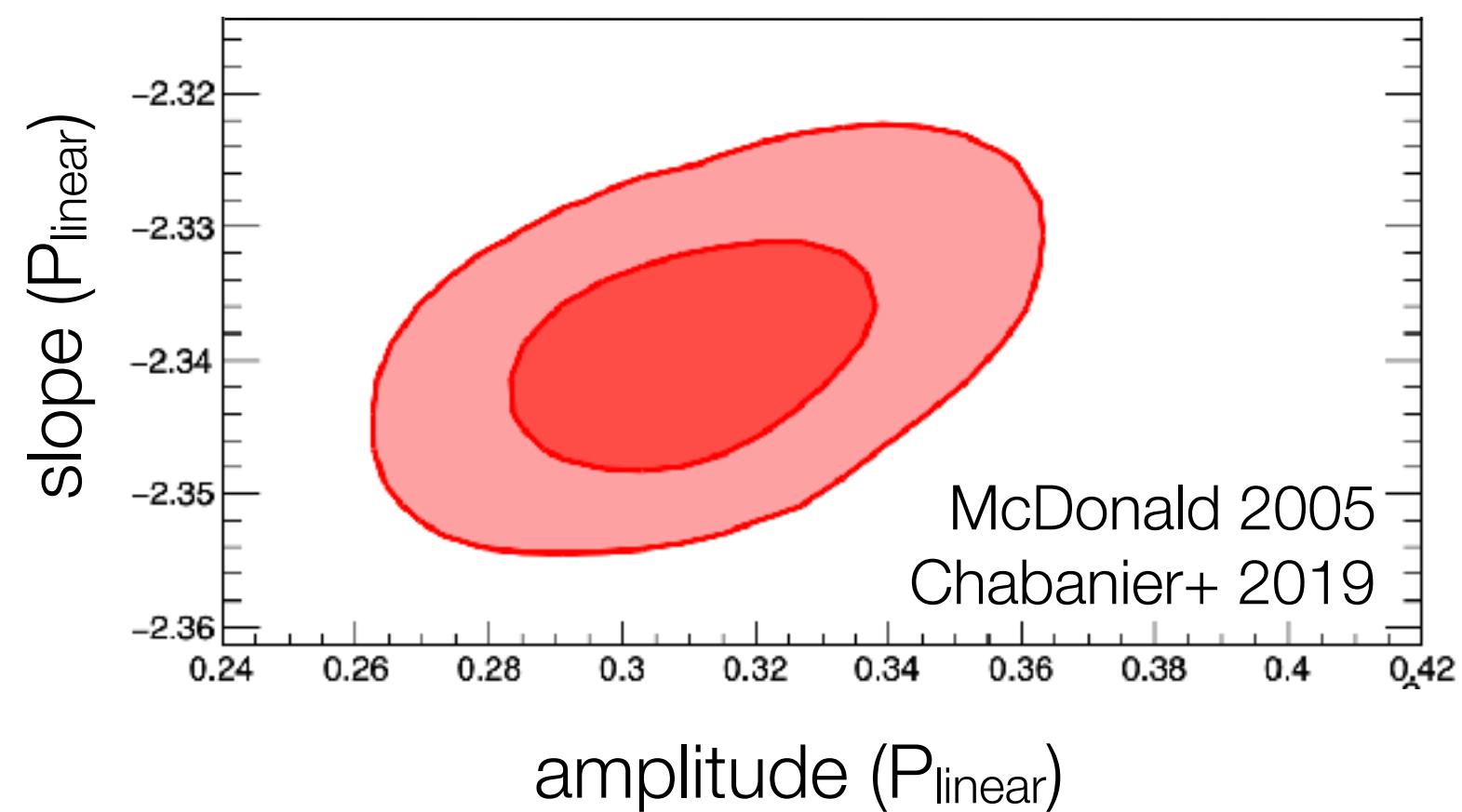
Parameter	Central value	Range
$n_s \dots\dots$	0.96	± 0.05
$\sigma_8 \dots\dots$	0.83	± 0.05
$\Omega_m \dots\dots$	0.31	± 0.05
$H_0 \dots\dots$	67.5	± 5
$T_0(z=3)$	14000	± 7000
$\gamma(z=3) \dots$	1.3	± 0.3
$A^{\tau} \dots\dots$	0.0025	± 0.0020
$\eta^{\tau} \dots\dots$	3.7	± 0.4
$\sum m_{\nu}$ (eV)	0.0	0.4, 0.8



$\sum m_\nu$ from P1D

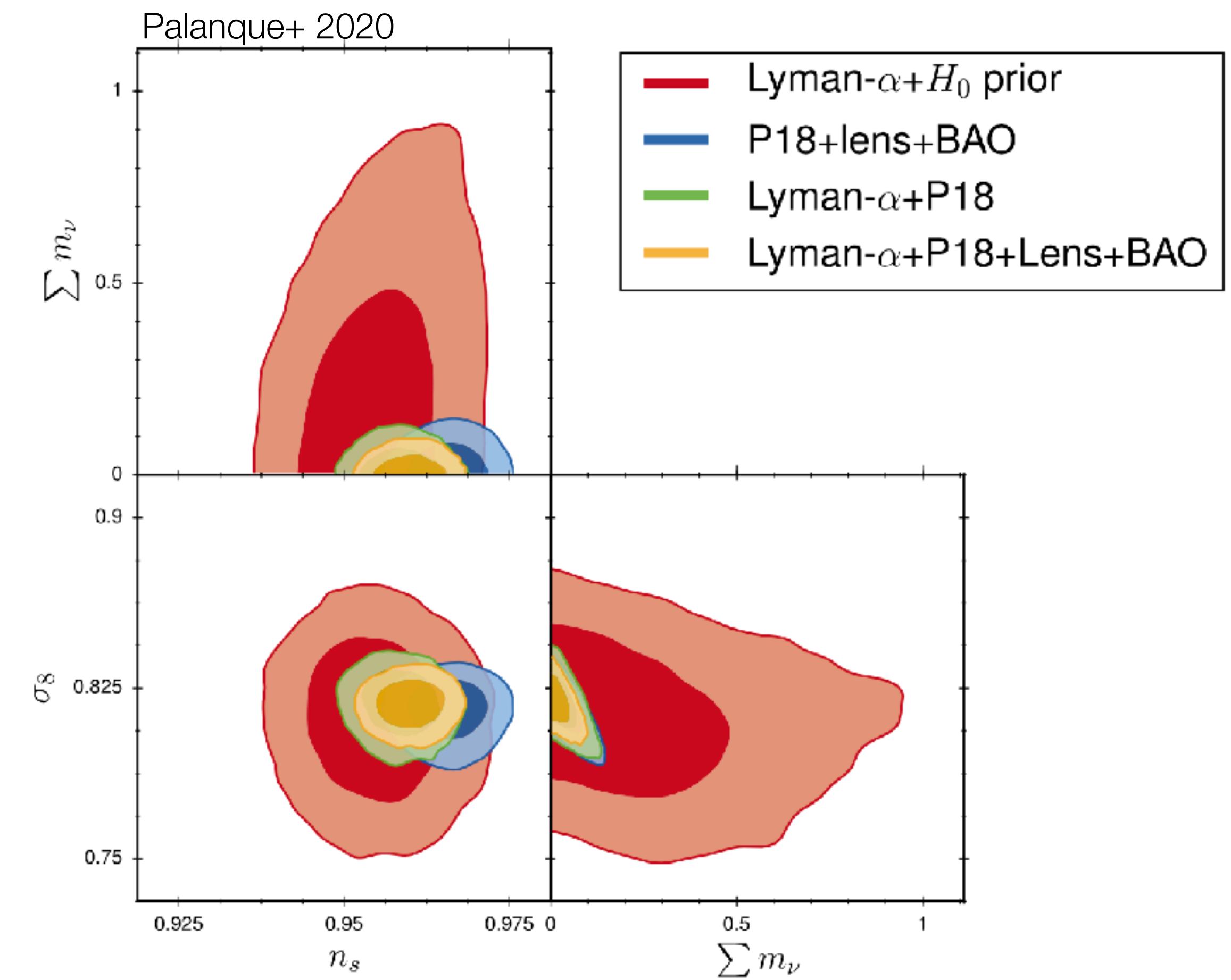
Main "cosmo" information in P1D:

$$\mathbf{P}_{\text{linear}} @ (\mathbf{zp}, \mathbf{kp}) = (3, 0.009 \text{ s/km})$$



nuisance parameters:

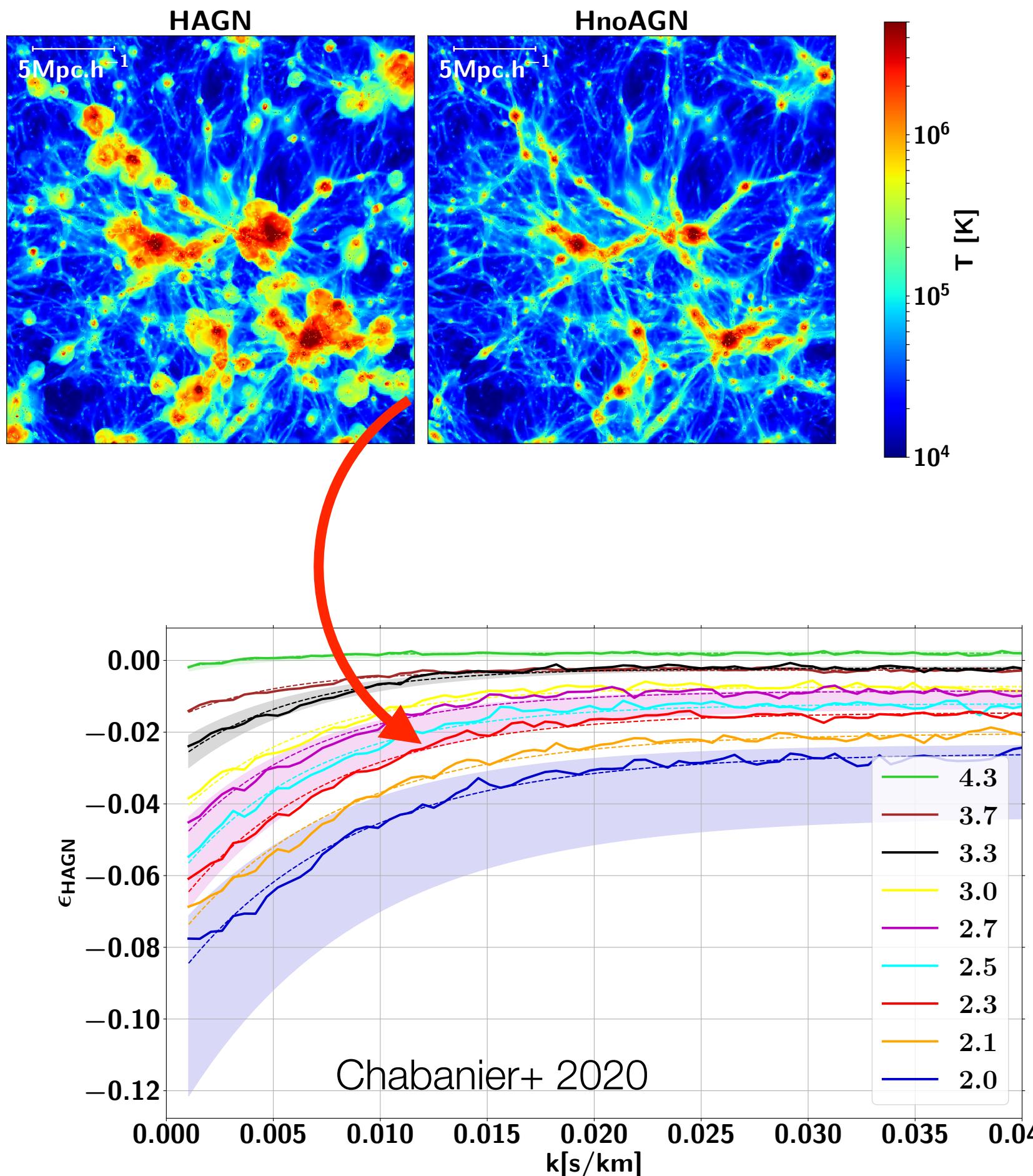
$T_0(z=3)$	Normalization temperature of IGM at $z=3$
$\gamma(z=3)$	Logarithmic slope of δ -dependence of IGM temperature at $z=3$
$\eta^T(z < 3)$	Logarithmic slope of z -dependence of T_0 for $z < 3$
$\eta^T(z > 3)$	Logarithmic slope of z -dependence of T_0 for $z > 3$
η^γ	Logarithmic slope of z -dependence of γ
A^τ	Amplitude of the effective optical depth of Ly α absorption τ_{eff}
η^τ	Logarithmic slope of redshift dependence of τ_{eff}
$f_{\text{Si III}}$	Fraction of Si III absorption relative to Ly α absorption
$f_{\text{Si II}}$	Fraction of Si II absorption relative to Ly α absorption
z_{reio}	Redshift of reionization
A^{splice}	Amplitude of splicing correction
η^{splice}	Small-scale slope of splicing correction
A^{SN}	Amplitude of supernova feedback correction
A^{AGN}	Amplitude of AGN feedback correction
A^{UVfluct}	Amplitude of UV fluctuation correction
$A^{n,i}$	Amplitude of noise power correction for redshift bin i



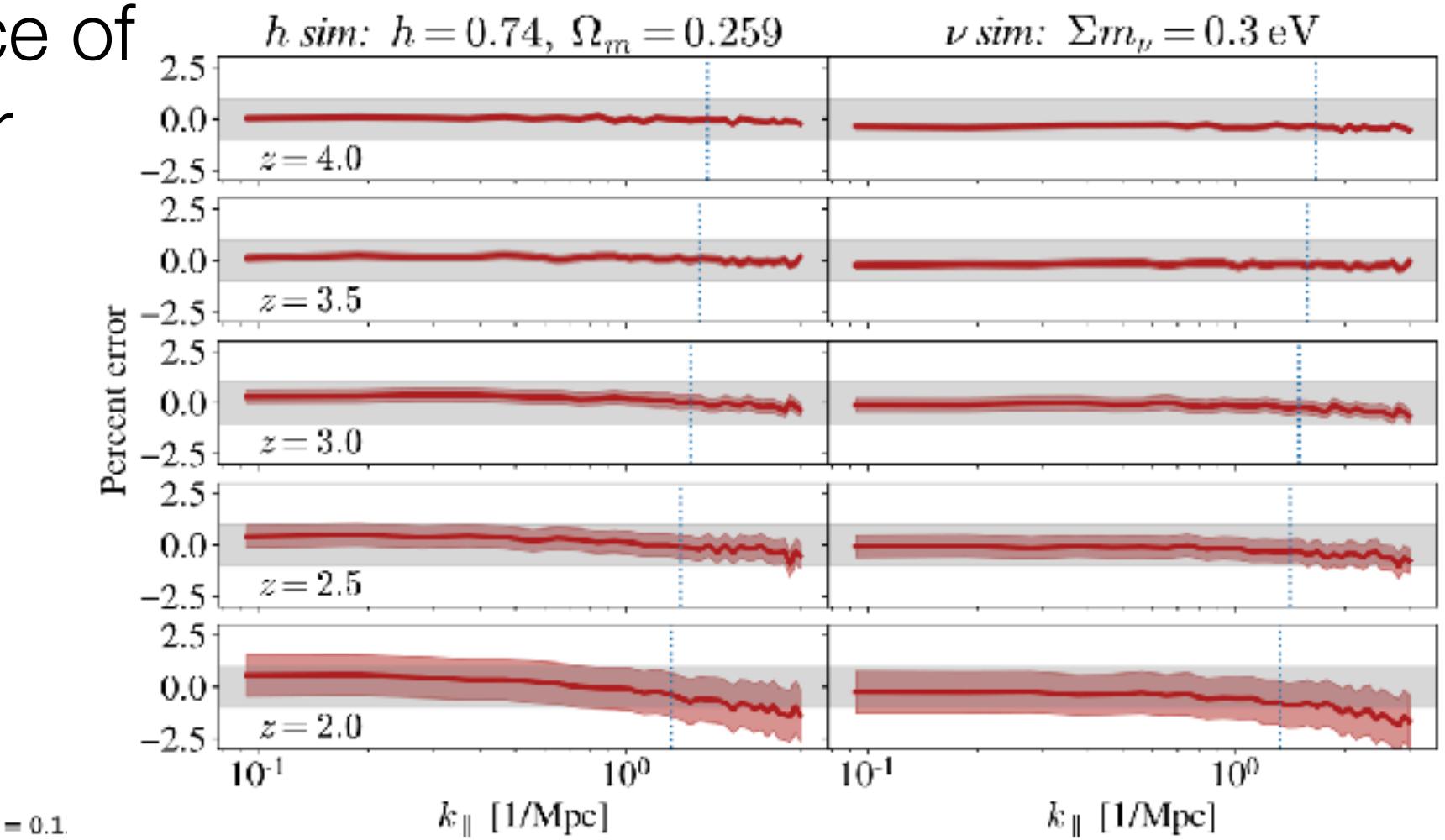
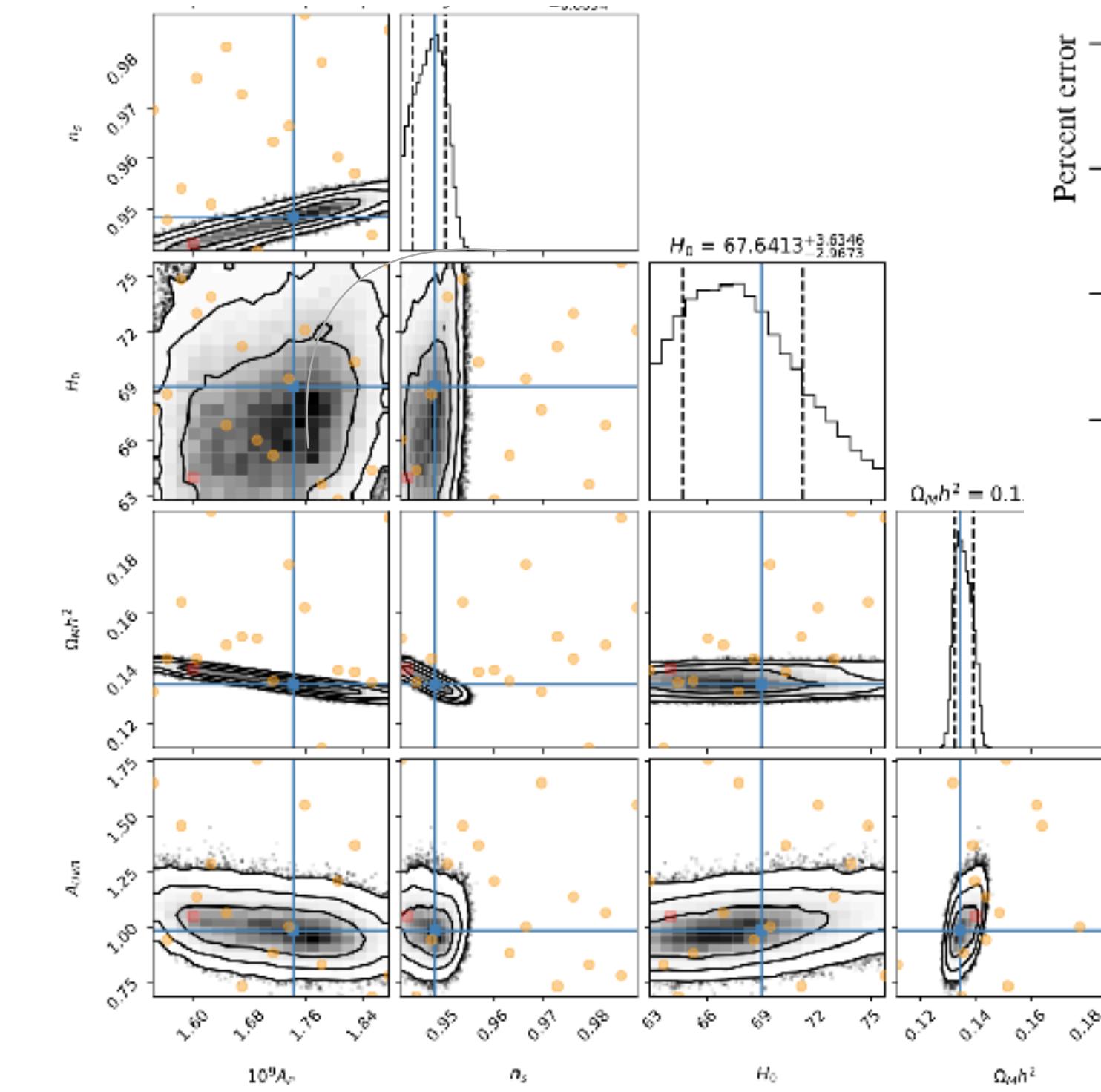
Planck + P1D: $\sum m_\nu < 110 \text{ meV}$

Lyman- α ongoing improvements: modelling

- Quantify feedback, inhomogeneous UV background ...



- Optimize hydro grid : choice of parameter space, emulator

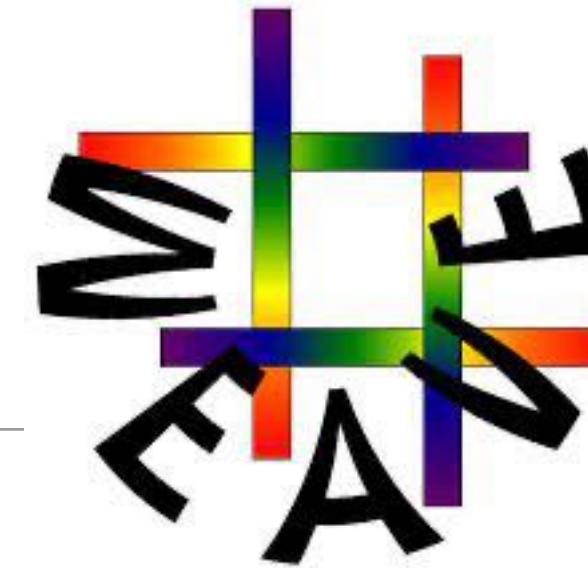


- See also LyAI-Net (Chotipan yesterday), LyMAS (Peirani 2022), ...

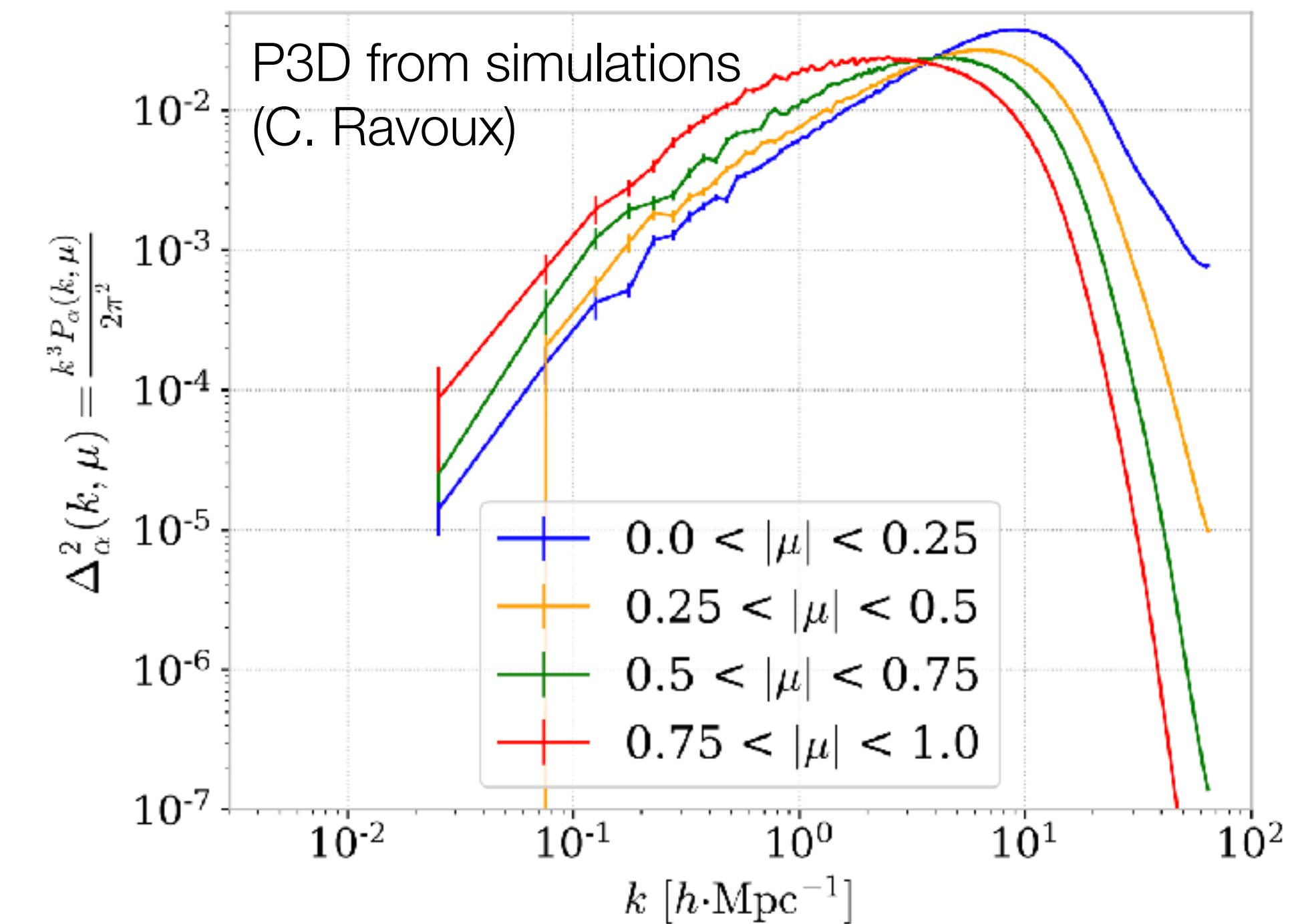
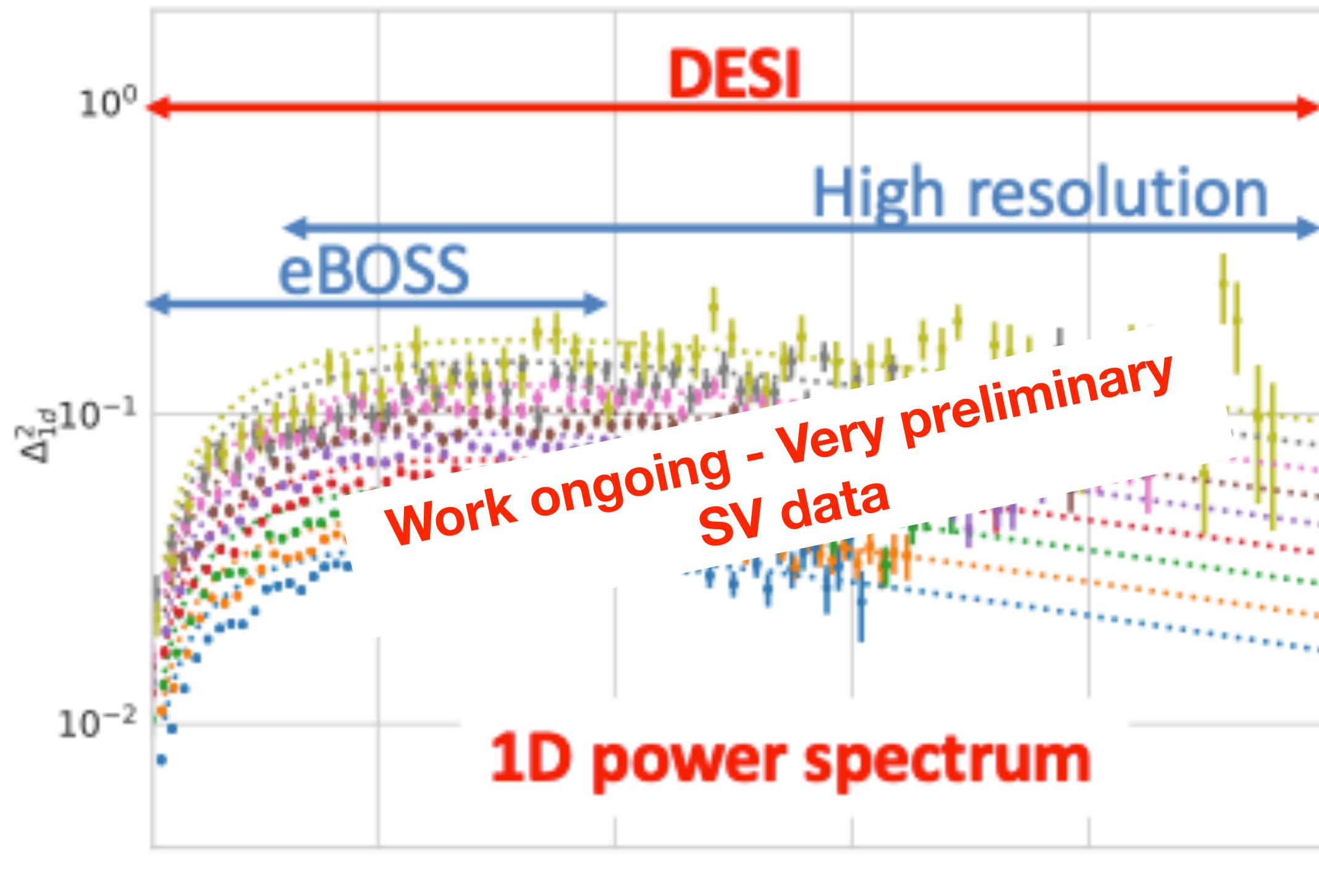
Lyman- α ongoing improvements: data

DESI & WEAVE-QSO : more statistics, higher resolution

Large lines-of-sight density \Rightarrow measure P3D (improve IGM thermal params) ?



First analysis of DESI-SV ongoing !



Conclusions

- Measuring Σm_ν would be an achievement for "precision cosmology"
 - Short-term ~2025 ? $\sigma(\Sigma m_\nu) \sim 20\text{-}30 \text{ meV}$, $\sim 3\sigma$ detection ?
 - Later ? improved τ measurement $\Rightarrow \sim 4\text{-}5\sigma$?
- Several probes in the market for small-scale $P(k)$
 - Have to demonstrate control of their own systematics
- **Other "beyond standard model" neutrino physics with cosmology:**
 - Sterile neutrinos: N_{eff} , $P(k)$ cut-off @ high k
 - New interactions (connection to dark sector): $P(k)$, reionization...

