

# The NewHorizon Project: Resolving disks in cosmic environment



Katarina Kraljic

&

NewHorizon collaboration

Laboratoire d'Astrophysique de Marseille

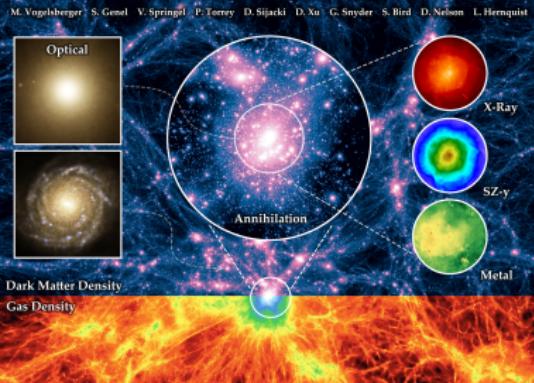
June 15th, 2022, Montpellier

# Simulations

Large-scale hydrodynamical

1/28

## The Illustris Simulation

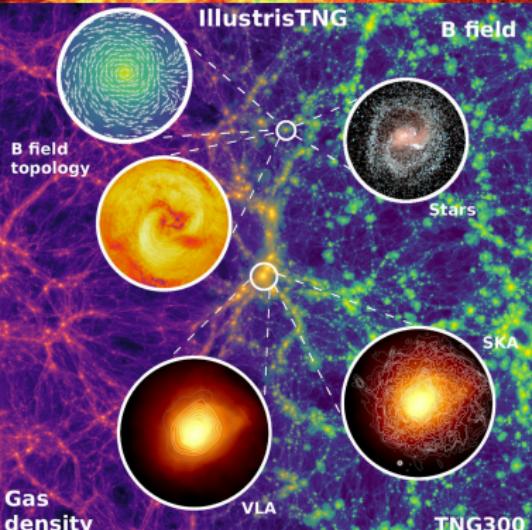
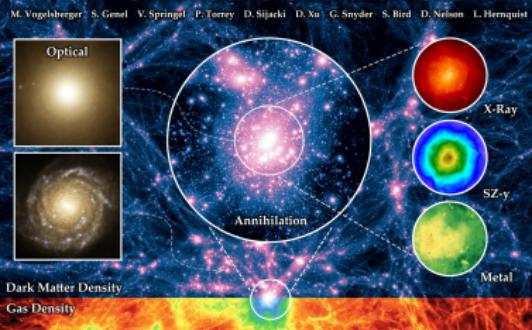


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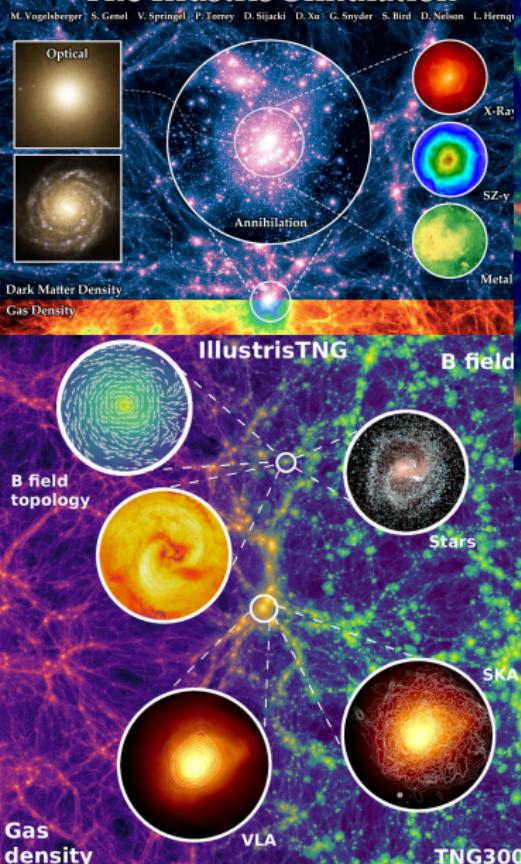


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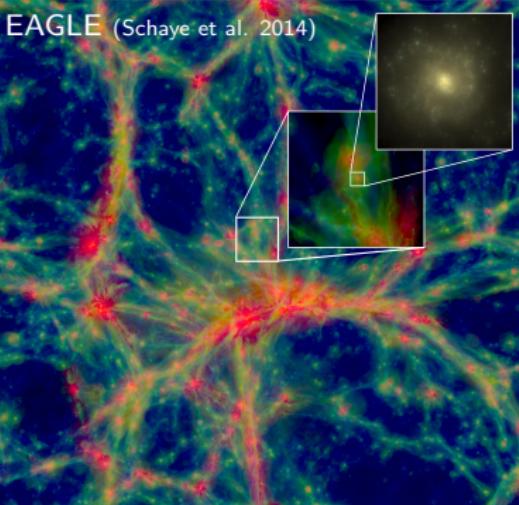
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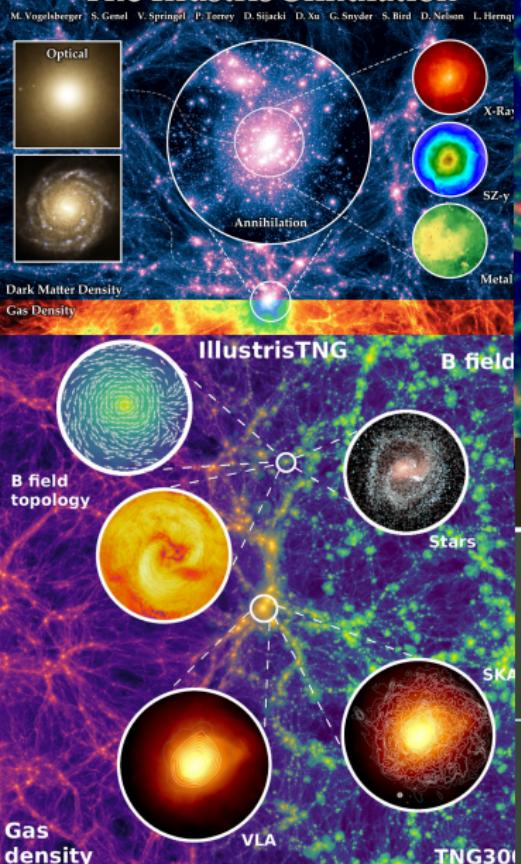


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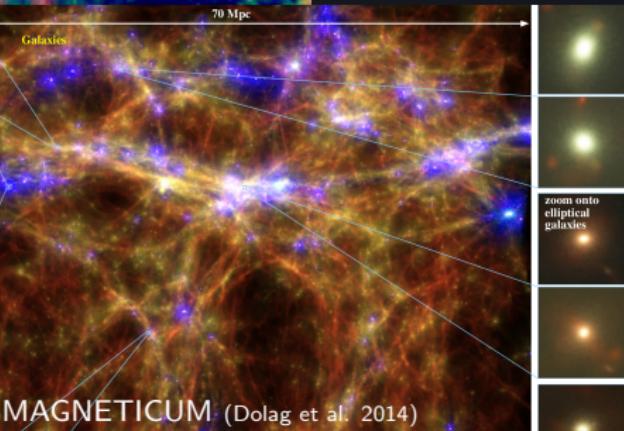
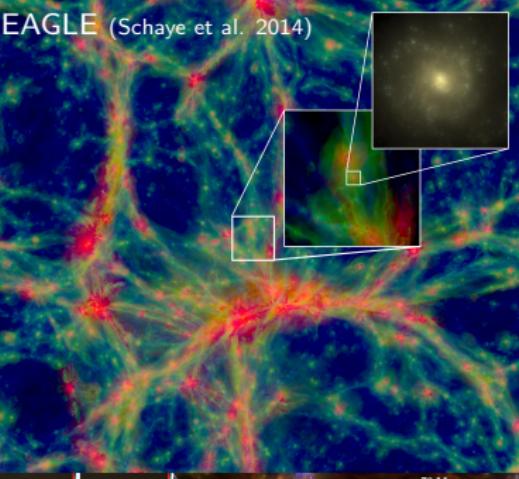
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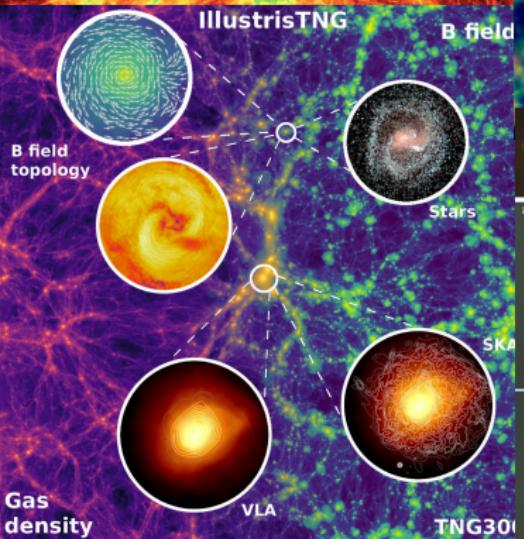
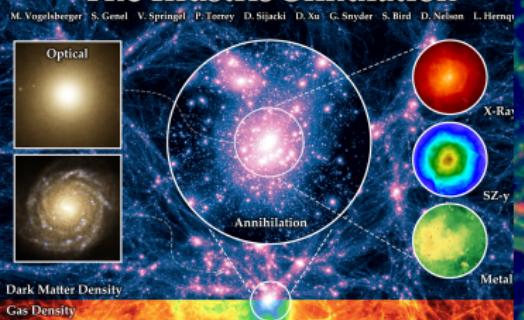


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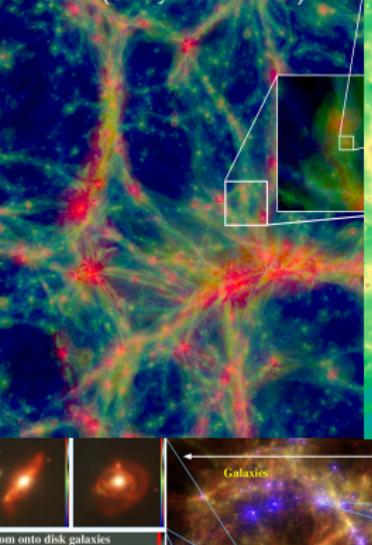
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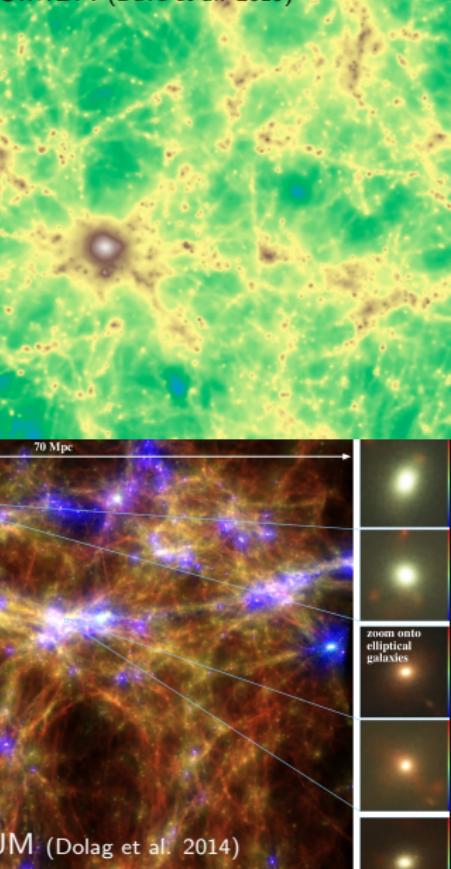
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## EAGLE (Schaye et al. 2014)



## SIMBA (Davé et al. 2019)



## MAGNETICUM (Dolag et al. 2014)

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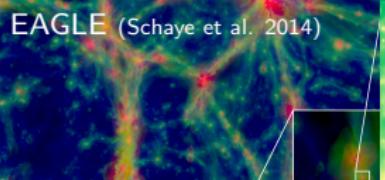
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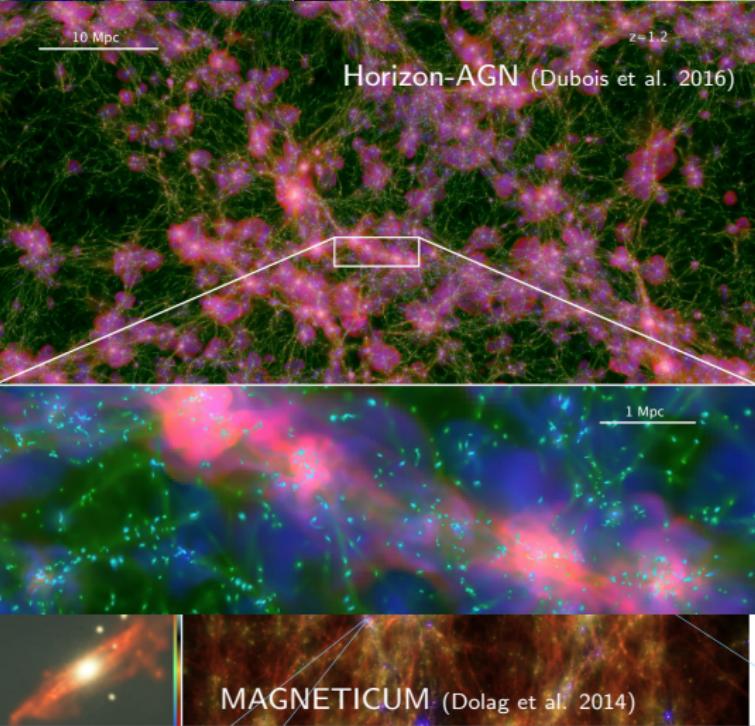
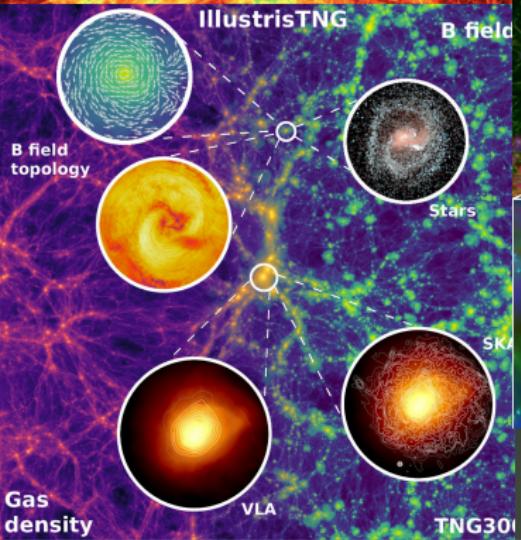
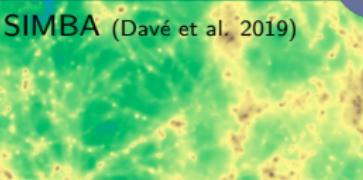
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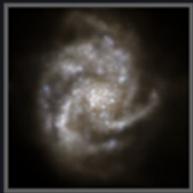
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ellipticals



irregular

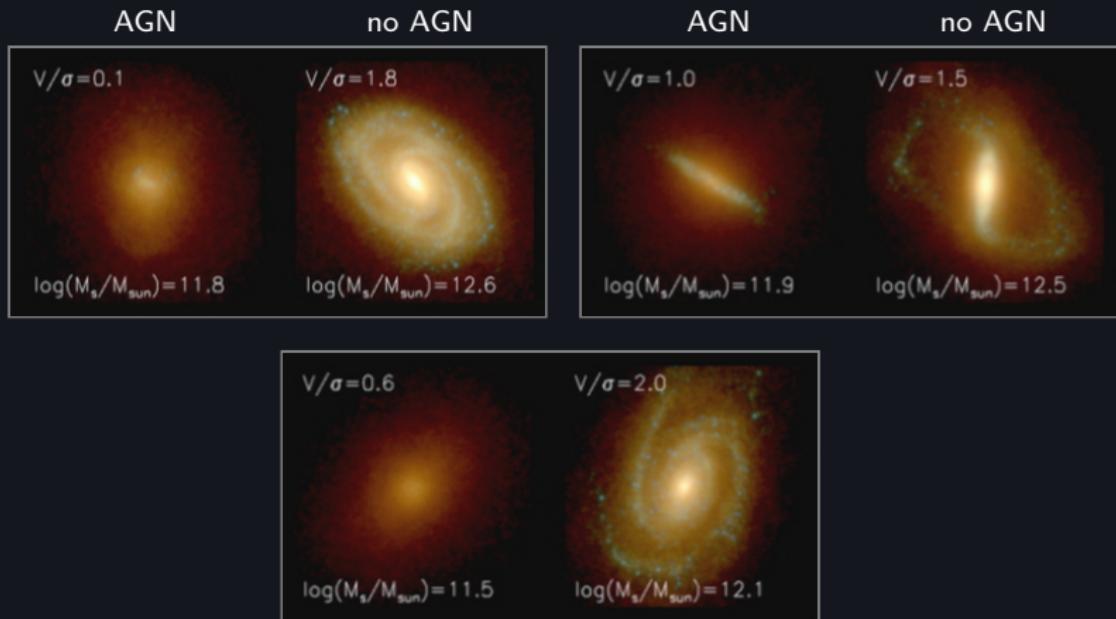


disk galaxies

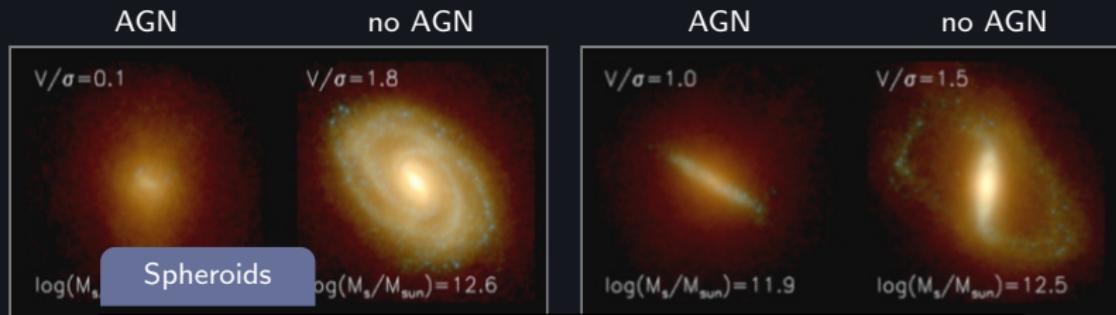


ILLUSTRIS (Vogelsberger et al. 2014)

see also HORIZON-AGN (Dubois et al. 2014)  
EAGLE (Schaye et al. 2015)

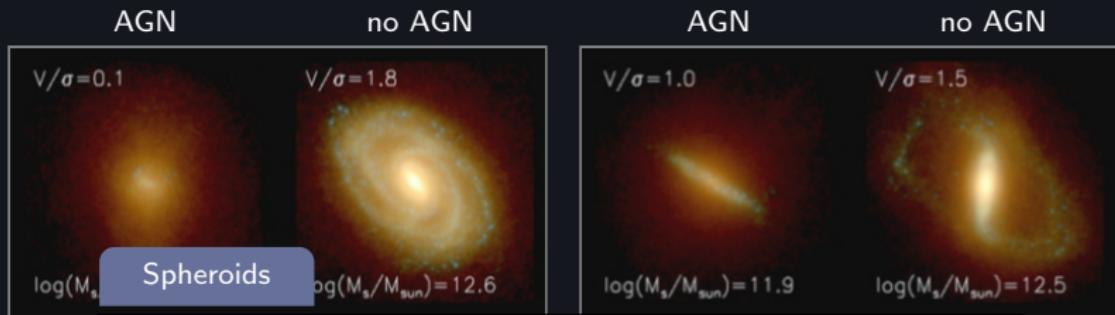


HORIZON-AGN/HORIZON-NOAGN (Dubois et al. 2014, 2016)



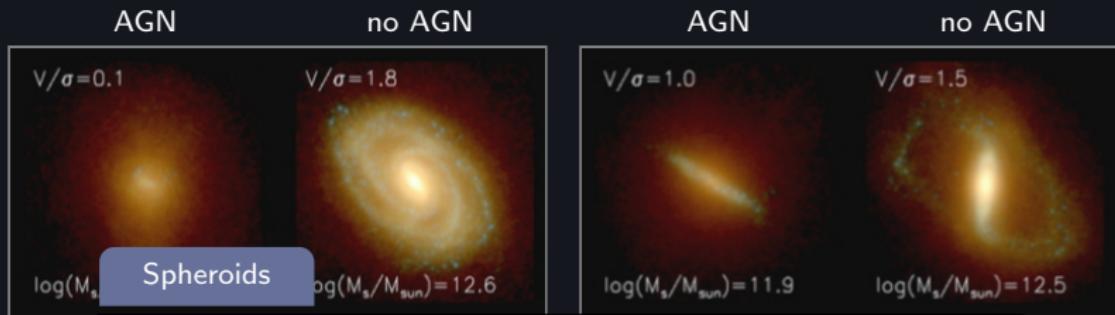
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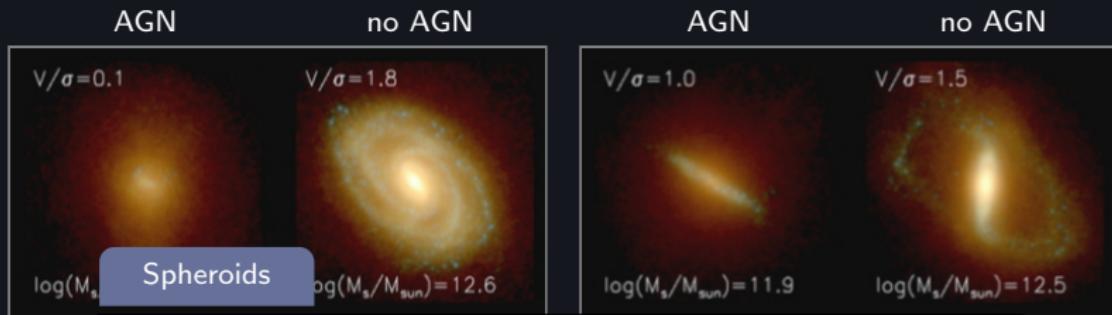
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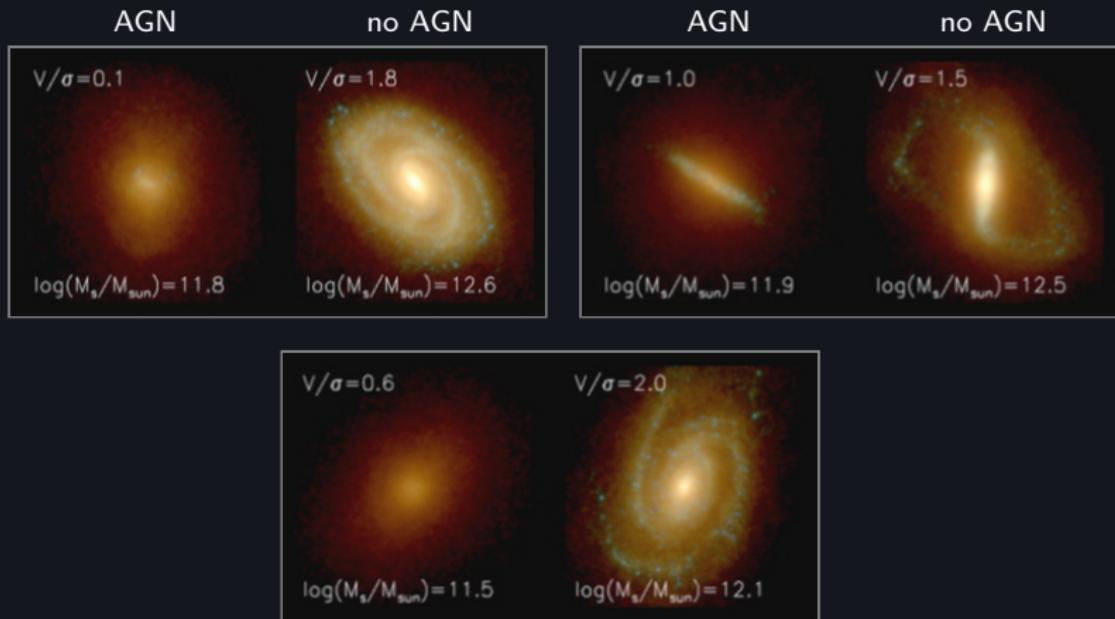
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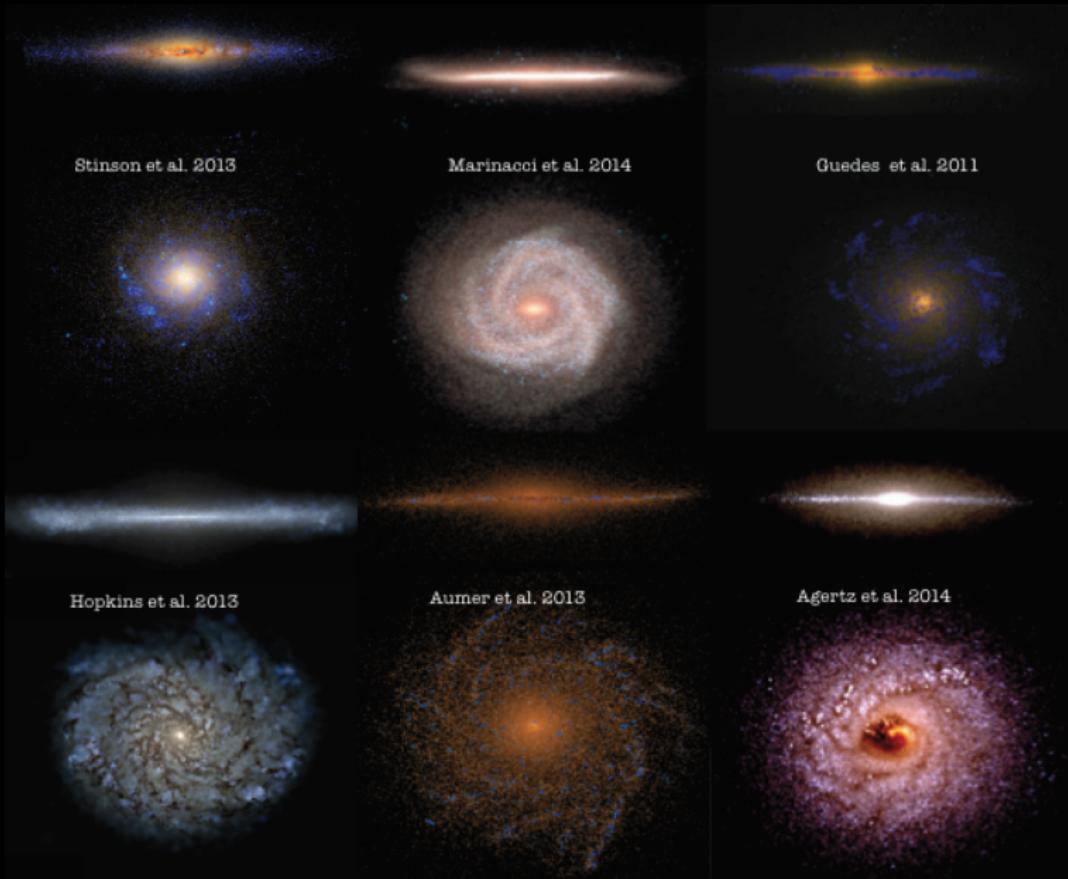


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- *problems*: too massive, central SFR too high,  
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- *origin*: too-efficient cooling & SF
- *solution*: consume or remove gas early →
  - ejective AGN feedback ('jet mode')
  - preventive AGN feedback ('radiative mode')

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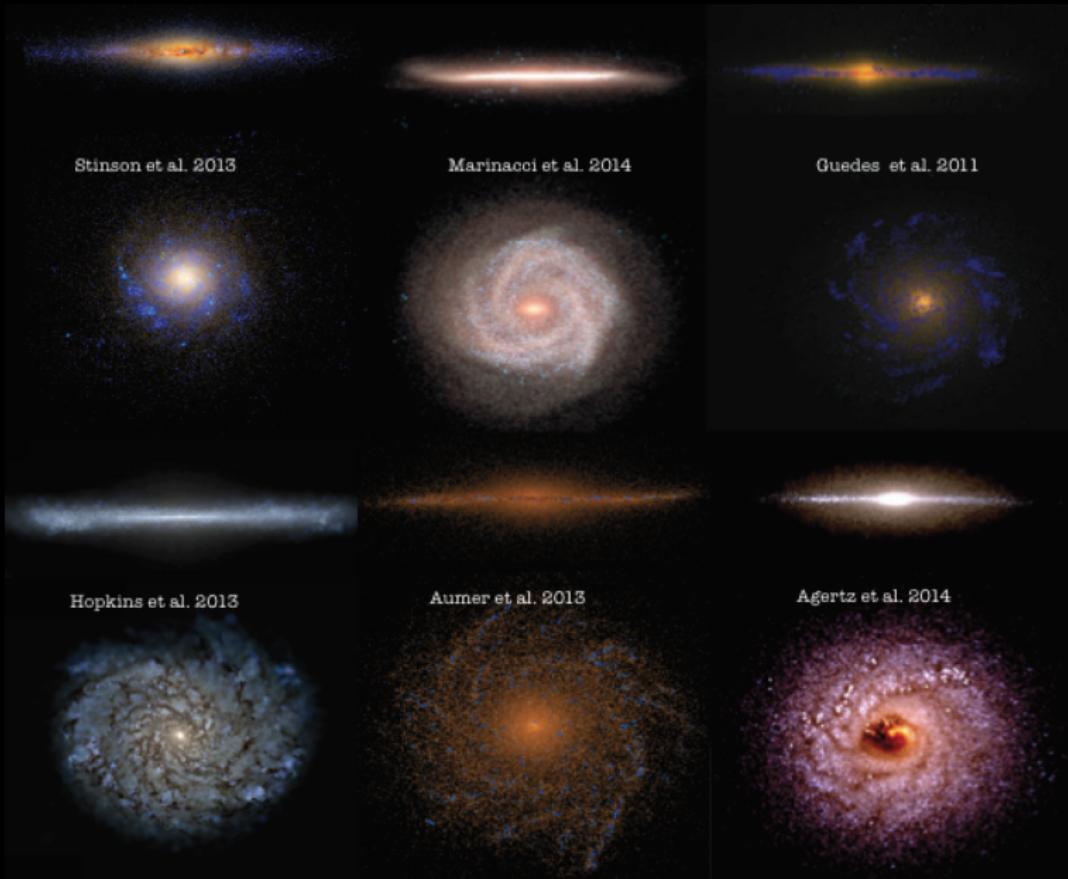
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Naab & Ostriker 2016



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- *solution:*
  - stellar feedback  $\longrightarrow$  keep SF efficiency low & stellar winds  $\longrightarrow$  remove preferentially low-AM material
  - SF  $\longrightarrow$  in dense & highly clustered environment

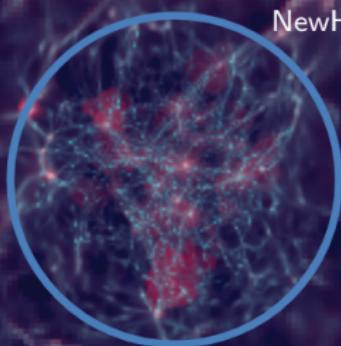


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# NewHorizon Simulation

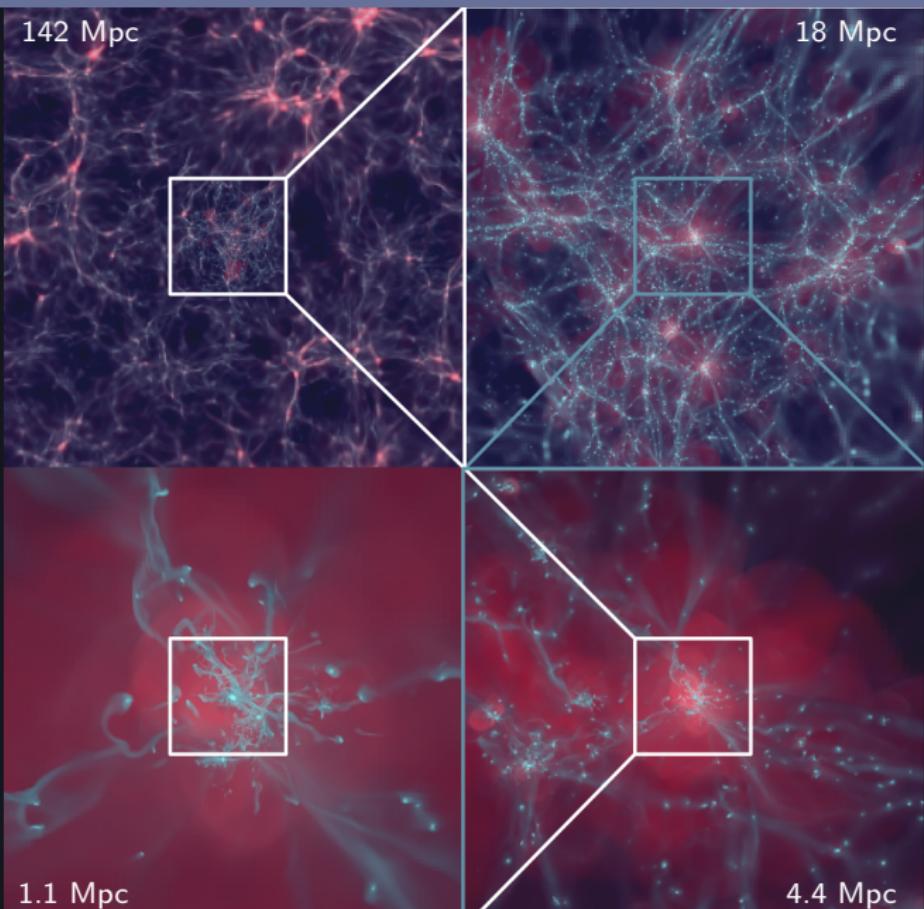
Resolving galactic disks in their cosmic environment

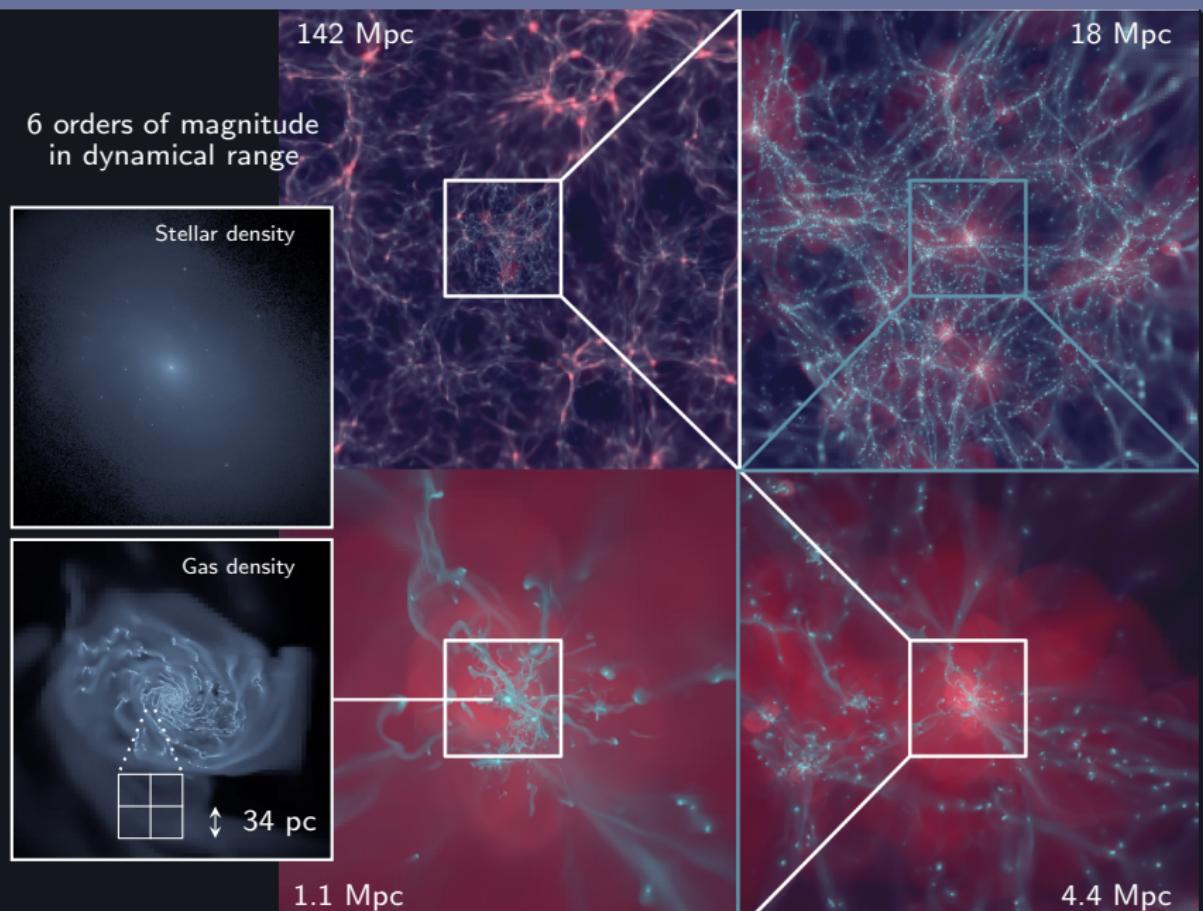
<https://new.horizon-simulation.org/>



NewHorizon

Horizon-AGN





- hydrodynamical cosmological simulation
- RAMSES (Teyssier 2002)



Dubois et al. 2021

- hydrodynamical cosmological simulation
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- $R_{\text{sphere}} = 10 h^{-1} \text{ Mpc}$   
 $\Delta x = 34 \text{ pc}$  (vs 1 kpc in Horizon-AGN)
- $M_{\text{DM}} = 10^6 M_{\odot}$  (vs  $10^8 M_{\odot}$  in Horizon-AGN)  
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Dubois et al. 2021

## Turbulent star formation

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$$\epsilon_* \propto \epsilon \exp \sigma_s^2 \left[ 1 + \operatorname{erf} \left( \frac{\sigma_s^2 - s_{\text{crit}}}{\sqrt{2\sigma_s^2}} \right) \right]$$

$$\sigma_s^2 = \ln(1 + b^2 \mathcal{M}^2)$$

- variance of the density PDF

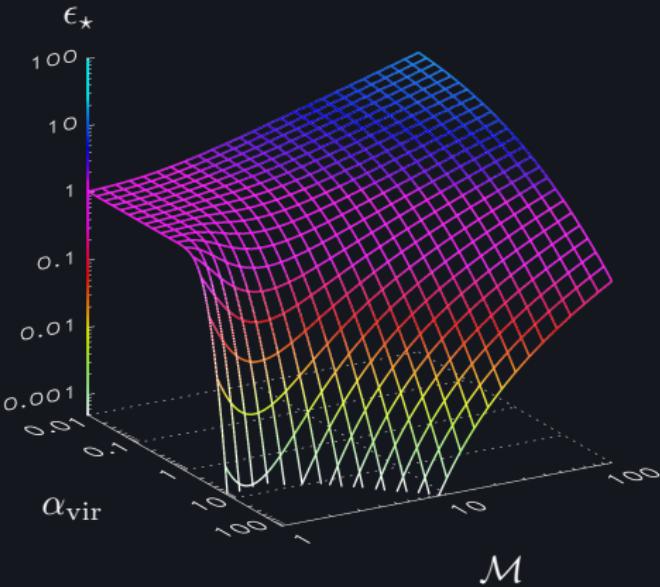
$$s_{\text{crit}} \propto \ln(\alpha_{\text{vir}} \mathcal{M}^2)$$

- critical density contrast

$$\epsilon = 0.5$$

- proto-stellar feedback parameter

multi-freefall PN model



Federrath & Klessen 2012

see also Padoan & Nordlund 2011, Hennebelle & Chabrier 2011

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Dubois et al. 2021

## Mechanical Supernovae feedback

(Kimm & Cen 2014)

Three phases of SN explosions:

### 1) Free expansion phase

- mass of the remnant dominates the swept-up mass (never resolved in practice)

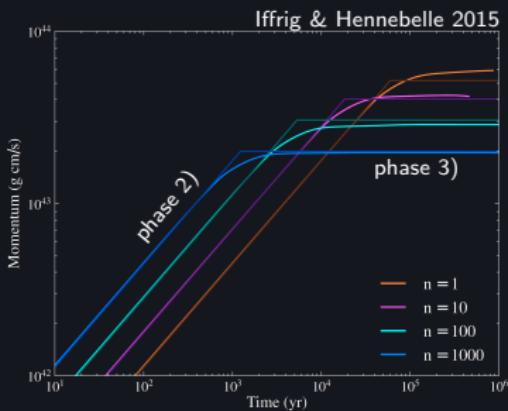
### 2) Energy-conserving (Sedov-Taylor) phase

- swept-up mass comparable to the mass of ejecta
- the initial energy of SN is conserved

### 3) Momentum-conserving (snowplough) phase

- the internal energy of the shocked shell has been radiated away & momentum is set up according to gas properties and energy of the explosion:

$$p_{\text{SN,snow}} \approx 3 \times 10^5 \text{ km s}^{-1} M_{\odot} E_{51}^{16/17} n_{\text{H}}^{-2/17} Z'^{-0.14}$$



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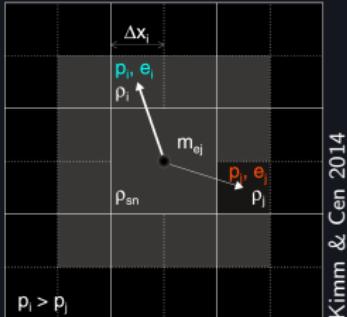
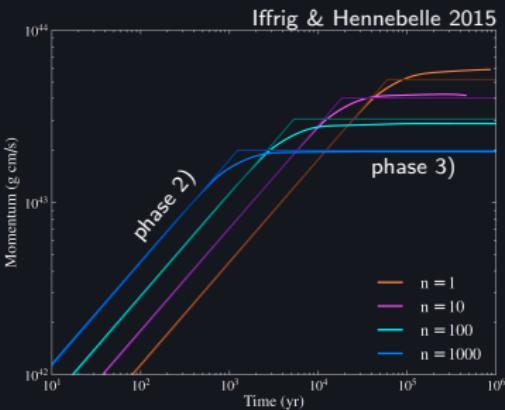
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Implementation:

- if in 2) deposit internal energy
- if in 3) deposit right amount of momentum ( $p_{SN, \text{snow}}$ )  
 $2 \times$  momentum (UV from OB stars)  
 (Geen et al. 2014)



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- AGN feedback & BH spin-dependent model  
(Dubois et al. 2014)



Dubois et al. 2021

## Black holes & AGN feedback

### BH formation:

- density  $>$  SF threshold
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$\epsilon_r$  - spin-dependent radiative efficiency

$$\dot{M}_{\text{Bondi}} = \frac{4\pi\bar{\rho}(GM_{\text{MBH}})^2}{(\bar{u}^2 + \bar{c}_s^2)^{3/2}}$$

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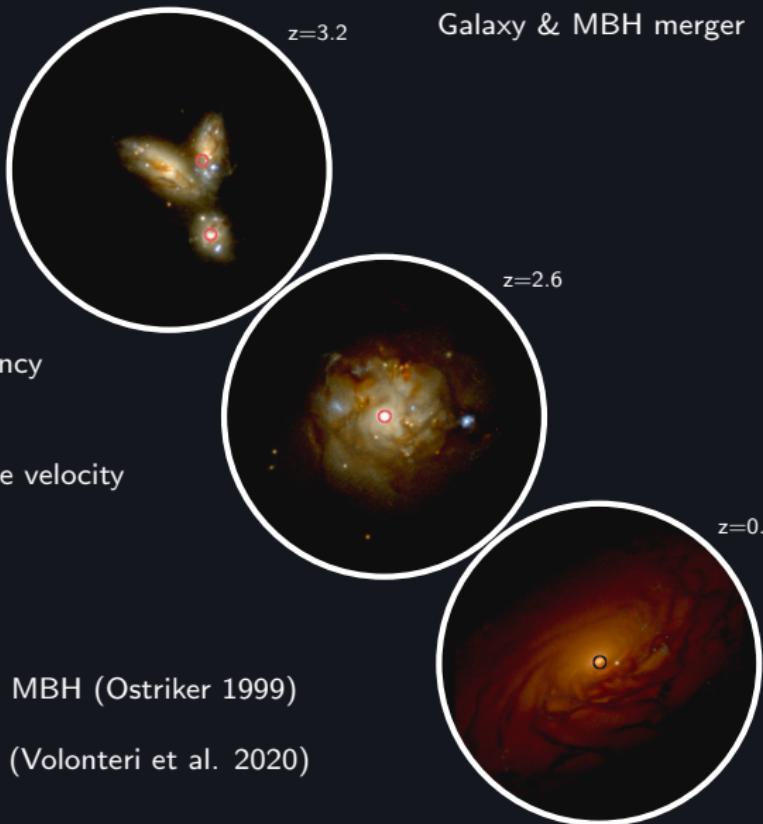
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### BH dynamics:

- explicit drag force of the gas onto the MBH (Ostriker 1999)
- allowed to merge when:  $d_{\text{rel}} < 4\Delta x$

$$v_{\text{rel}} < v_{\text{esc}} \quad (\text{Volonteri et al. 2020})$$



### Black holes & AGN feedback

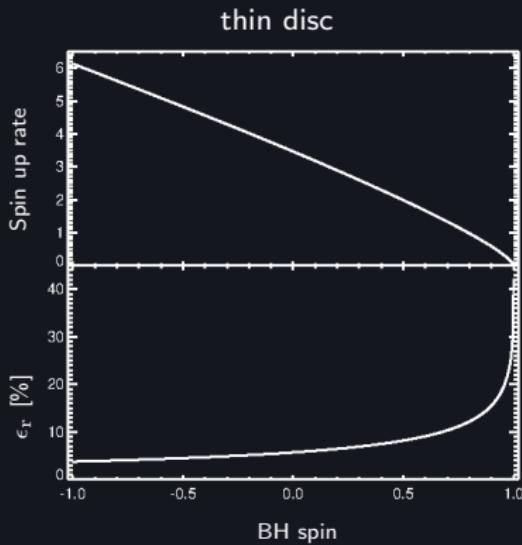
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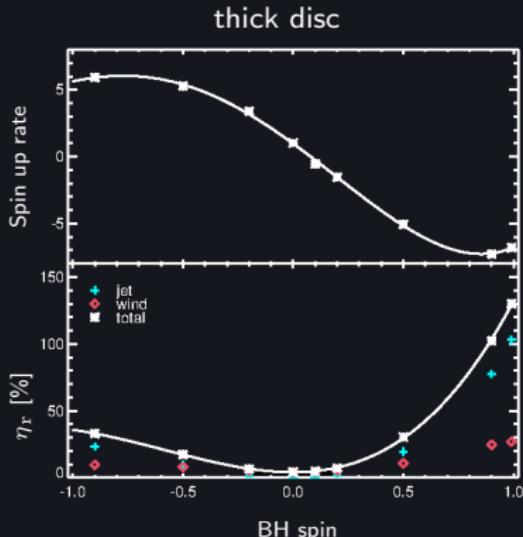
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- released power

$$\dot{E}_{\text{AGN,R,Q}} = \eta_{\text{R,Q}} \dot{M}_{\text{MBH}} c^2$$

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- thermal energy released only  
 $\eta_Q = 0.15\epsilon_r$

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$$\eta_Q = 0.15 \epsilon_r$$
- radio jet mode
- bipolar jets:  $10^4$  km/s;  $0^\circ$  angle
- deposit mass momentum energy

- hydrodynamical cosmological simulation
- RAMSES (Teyssier 2002)
- $R_{\text{sphere}} = 10 h^{-1} \text{ Mpc}$   
 $\Delta x = 34 \text{ pc}$  (vs 1 kpc in Horizon-AGN)
- $M_{\text{DM}} = 10^6 M_{\odot}$  (vs  $10^8 M_{\odot}$  in Horizon-AGN)  
 $M_{\star} = 10^4 M_{\odot}$  (vs  $10^6 M_{\odot}$  in Horizon-AGN)
- SF: turbulent criterion (Padoan & Nordlund 2011)  
 $\epsilon_{\star} = f(\mathcal{M}, \alpha_{\text{vir}})$  (vs const  $\sim 1\%$  in Horizon-AGN)
- mechanical SNII feedback (Kimm & Cen 2014)
- AGN feedback & BH spin-dependent model  
(Dubois et al. 2014)



Dubois et al. 2021

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- AGN feedback & BH spin-dependent model  
(Dubois et al. 2014)
- outputs every 15 Myr ( $\sim 150 \text{ GB}$  each)
- to  $z \sim 0.8$ , French & Korean effort: 25 Mhr  
to  $z \sim 0.17$ , **Grand Challenge project**  
*Extreme-Horizon*: 65 Mhr at TGCC



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## Horizon-AGN

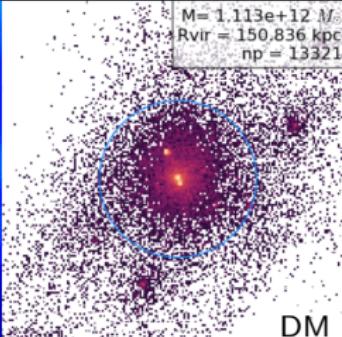
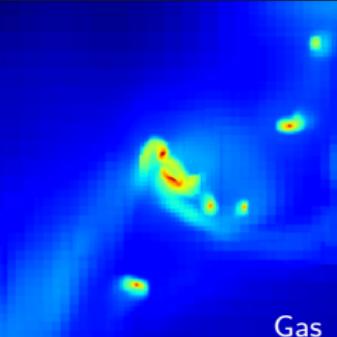
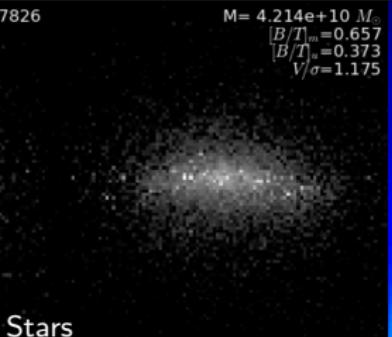
ID= 27826

 $M = 4.214 \times 10^{10} M_{\odot}$   
 $[B/T]_m = 0.657$   
 $[B/T]_n = 0.373$   
 $V/\sigma = 1.175$ 

Stars

Gas

DM



## NewHorizon

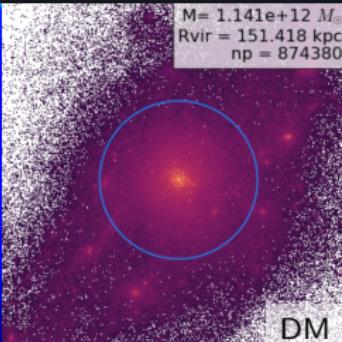
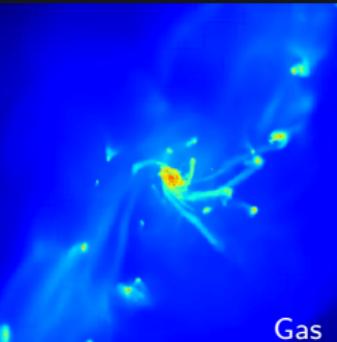
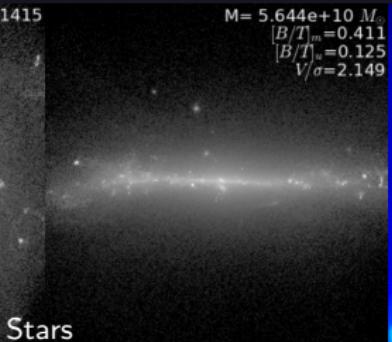
ID= 1415

 $M = 5.644 \times 10^{10} M_{\odot}$   
 $[B/T]_m = 0.411$   
 $[B/T]_n = 0.125$   
 $V/\sigma = 2.149$ 

Stars

Gas

DM

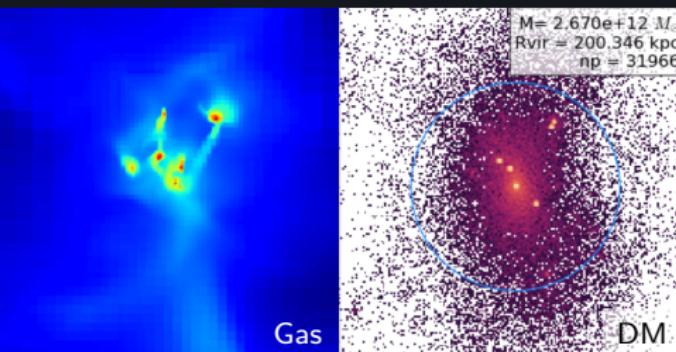


## Horizon-AGN

ID= 28172

 $M = 7.596\text{e}+10 M_{\odot}$   
 $[B/T]_m = 0.900$   
 $[B/T]_n = 0.900$   
 $V/\sigma = 0.224$ 

Stars



Gas

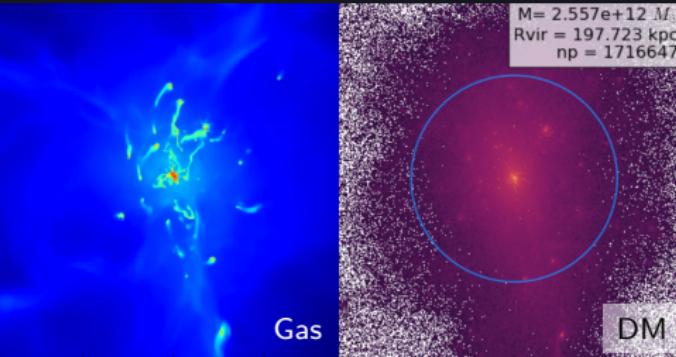
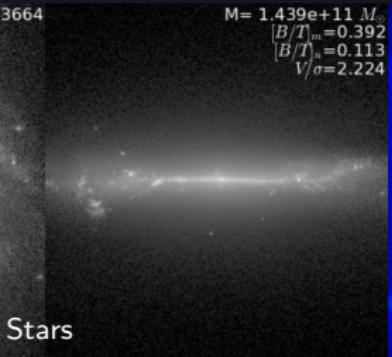
DM

## NewHorizon

ID= 3664

 $M = 1.439\text{e}+11 M_{\odot}$   
 $[B/T]_m = 0.392$   
 $[B/T]_n = 0.113$   
 $V/\sigma = 2.224$ 

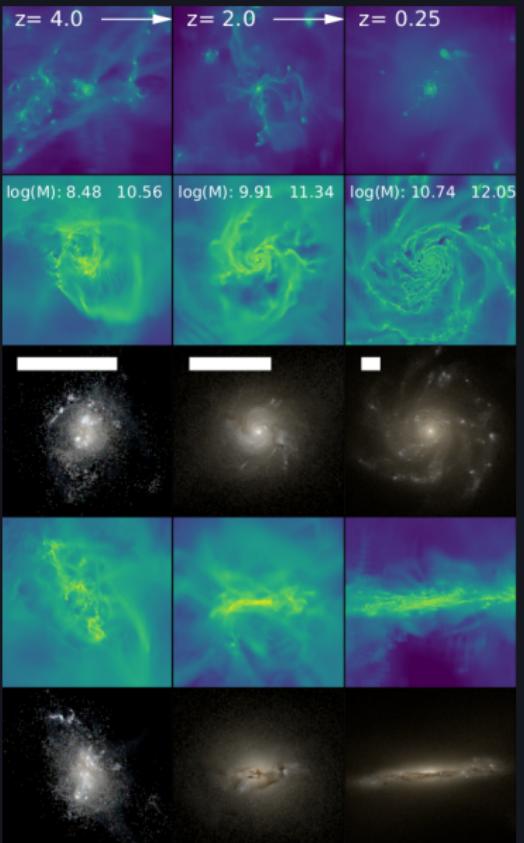
Stars



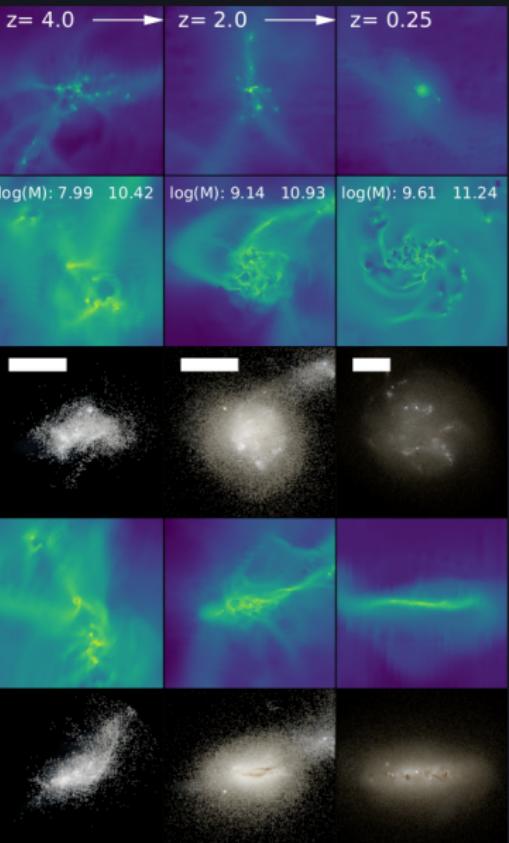
Gas

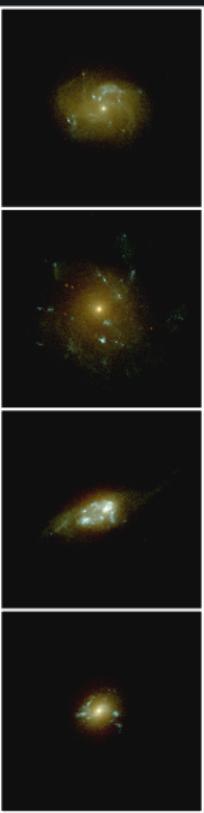
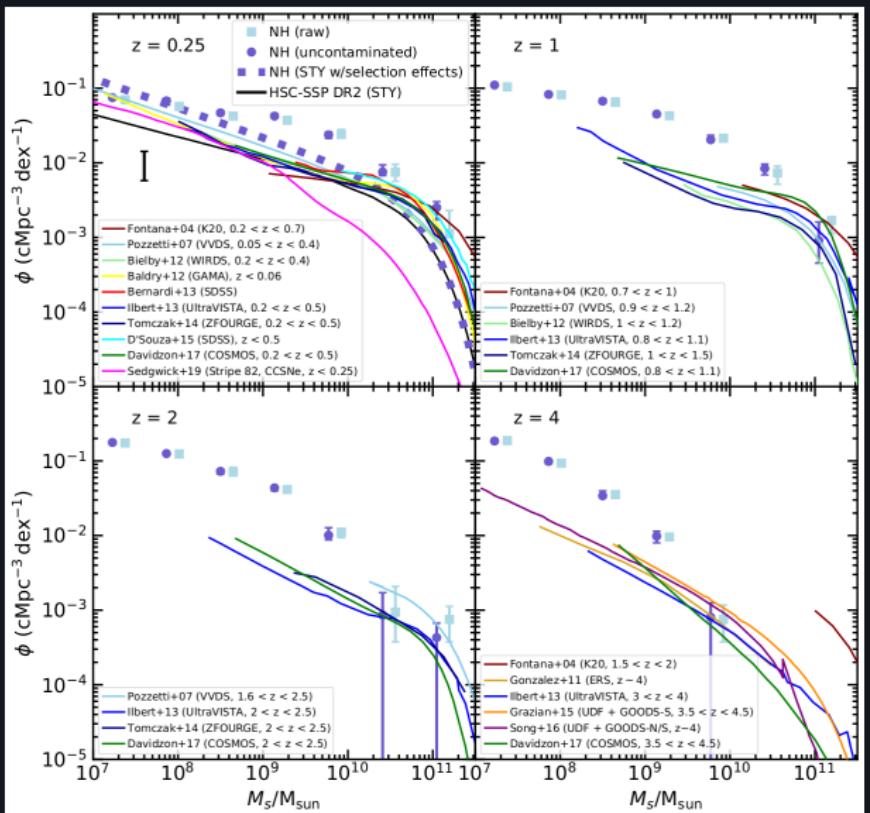
DM

## High-mass

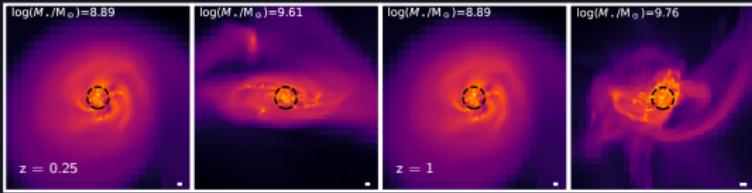
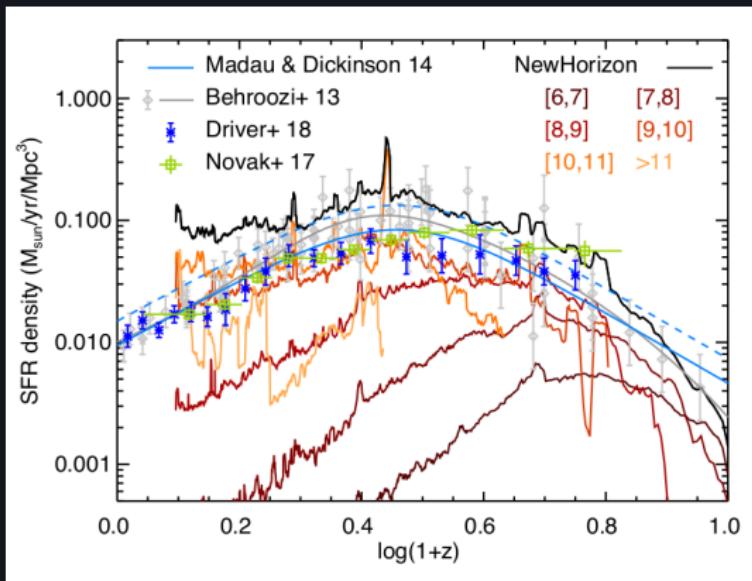


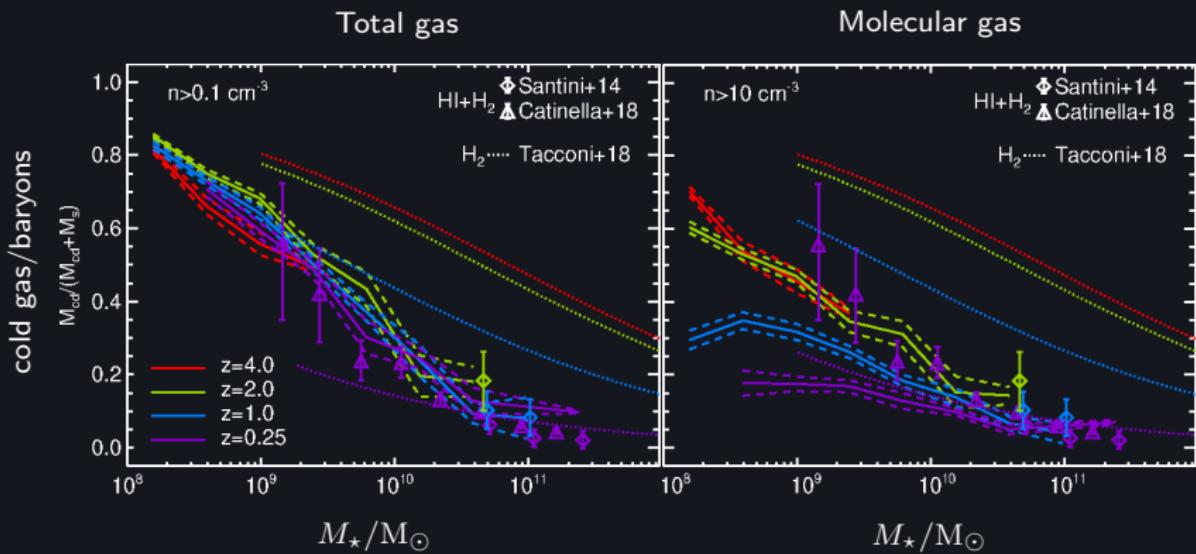
## Lower-mass





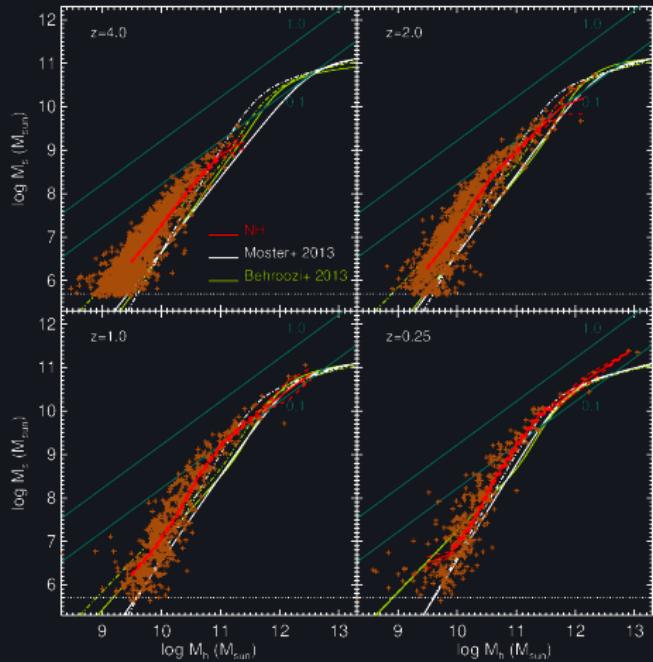
Dubois et al. 2021





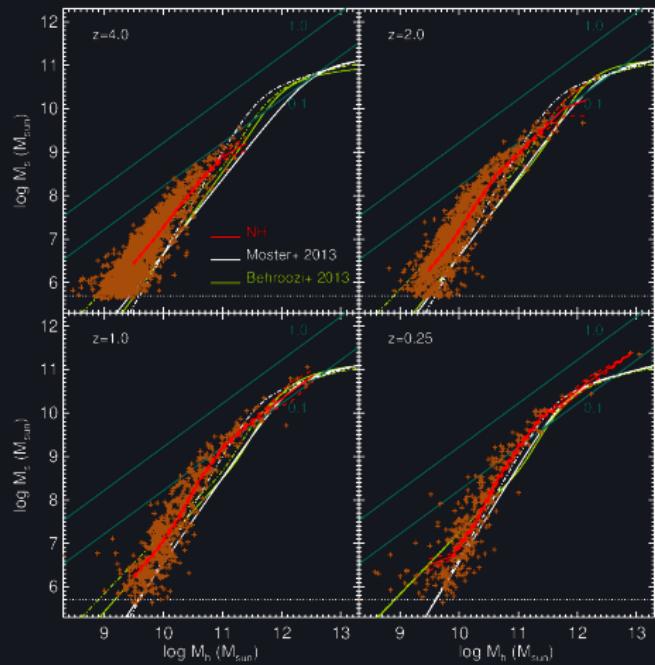
- less gas rich at high  $M_\star$  and low  $z$ : qualitative agreement
- significantly less molecular gas at low  $M_\star$  and high  $z$

## Stellar-to-halo mass

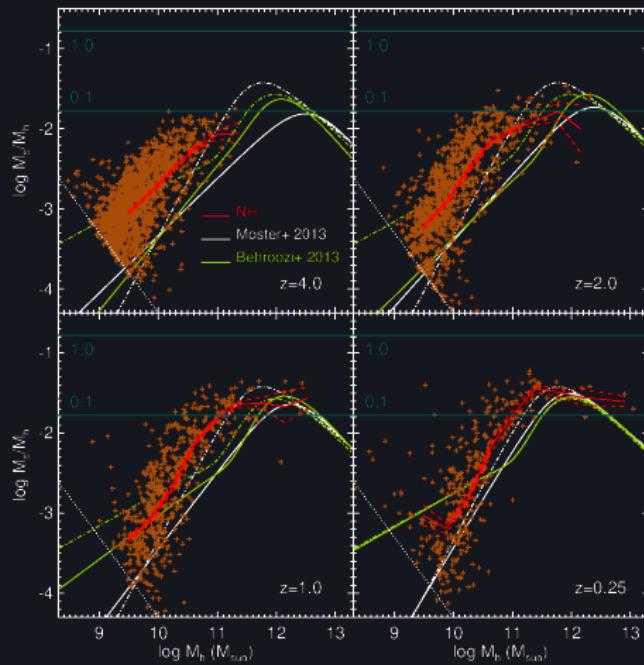


- fairly good qualitative agreement

Stellar-to-halo mass

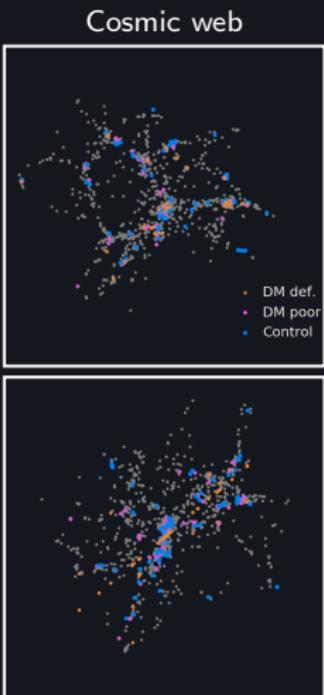
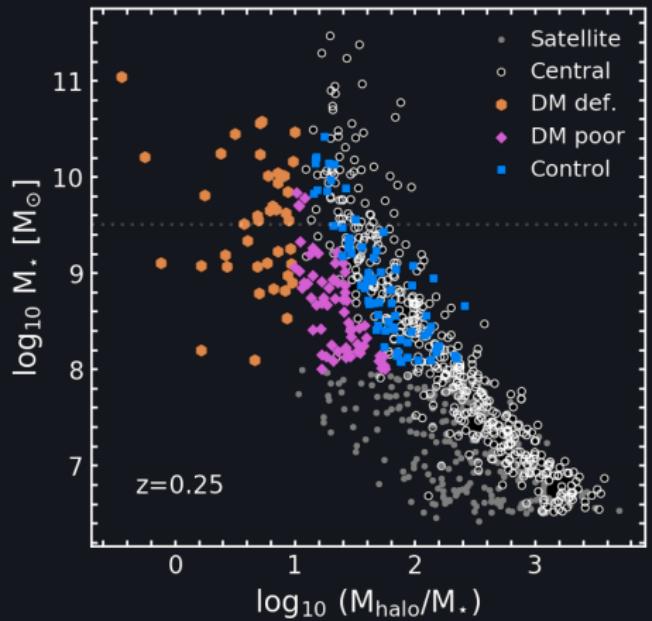


Baryon conversion efficiency



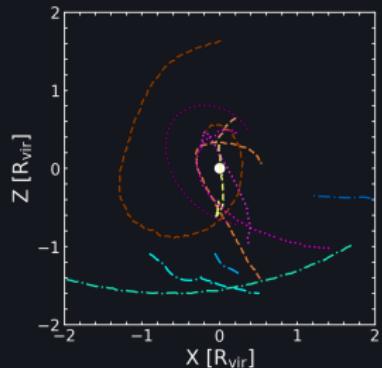
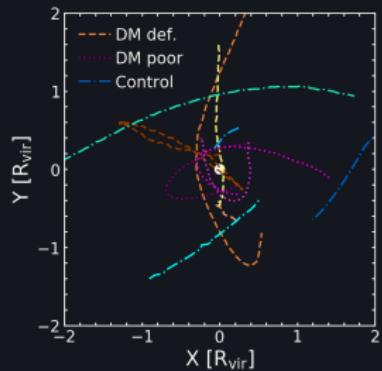
- fairly good qualitative agreement

- overestimated below the peak



Jackson et al. 2021

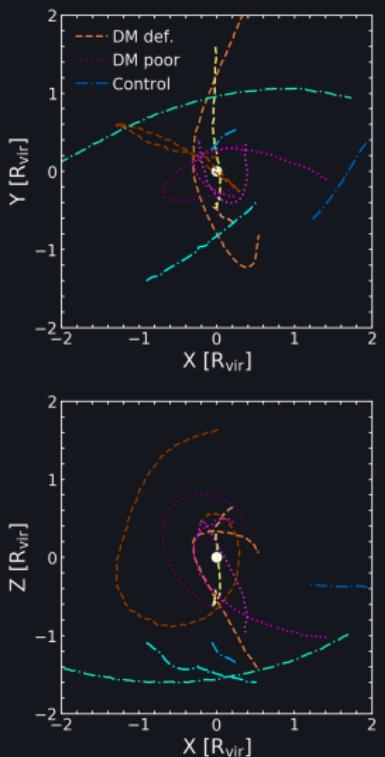
## Orbits



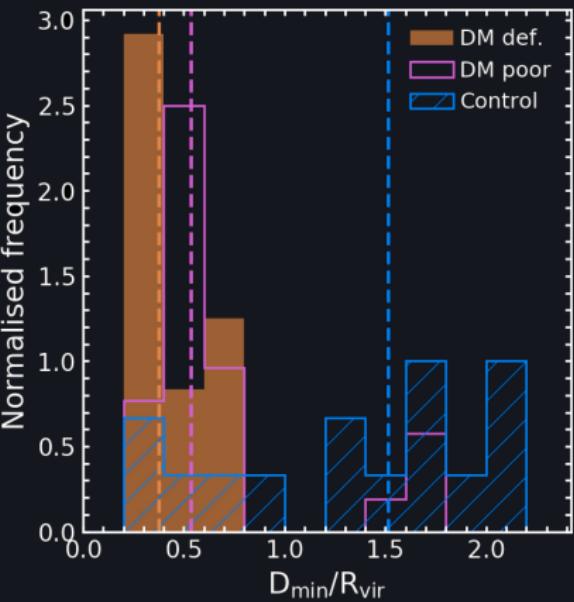
- DM deficient/poor exhibit closer orbits than control

Jackson et al. 2021

Orbits

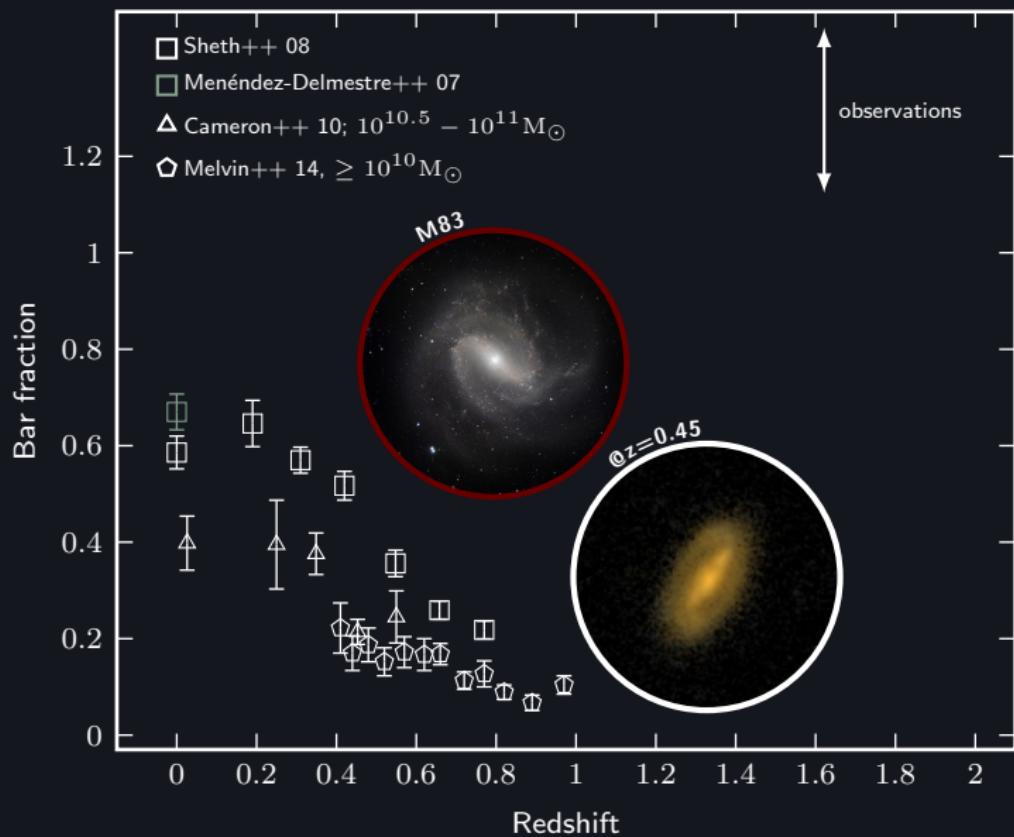


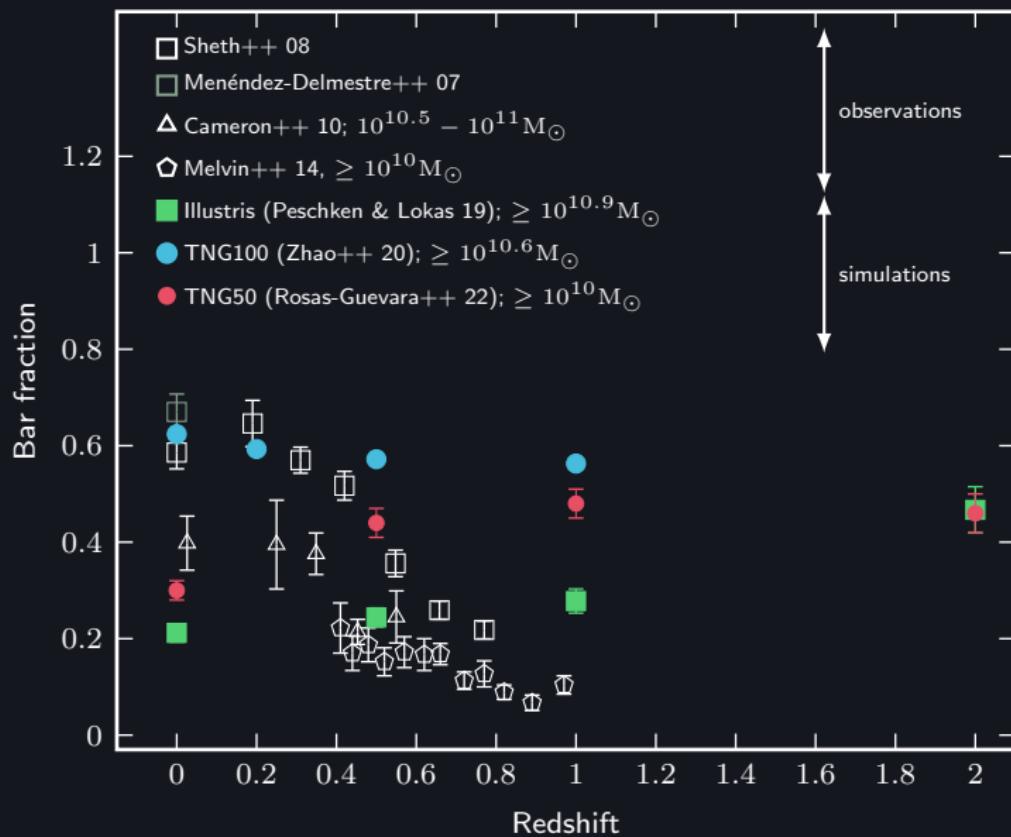
Minimum distance satellite-central

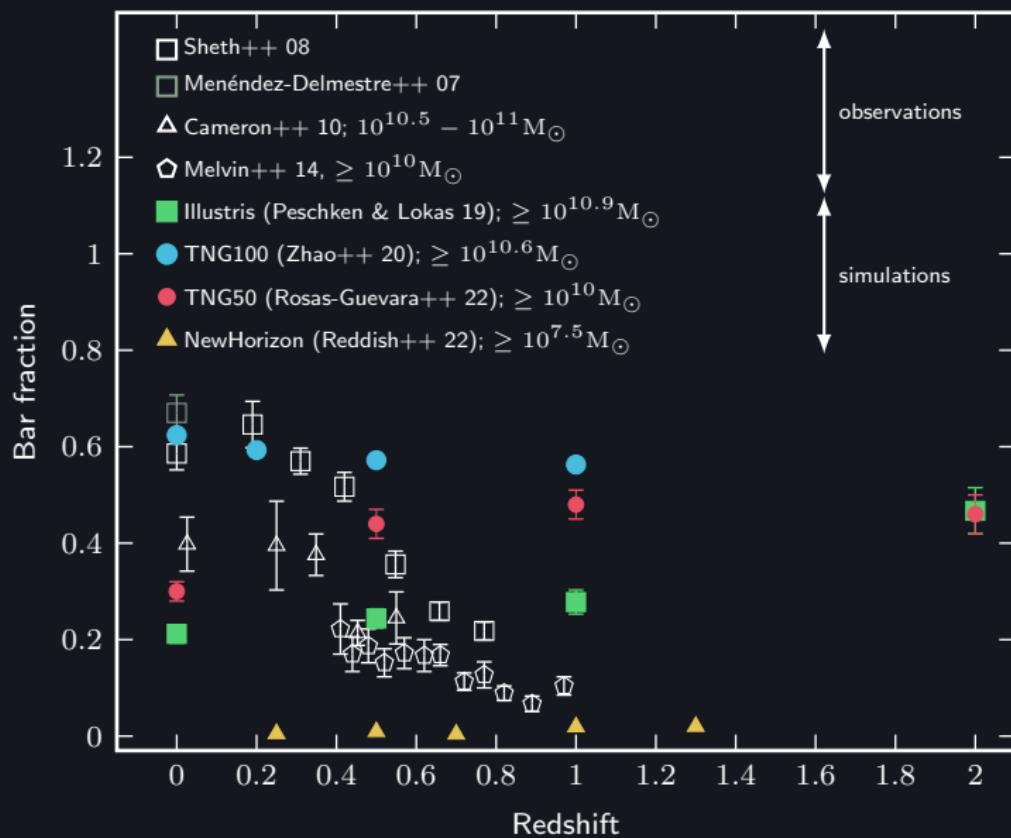


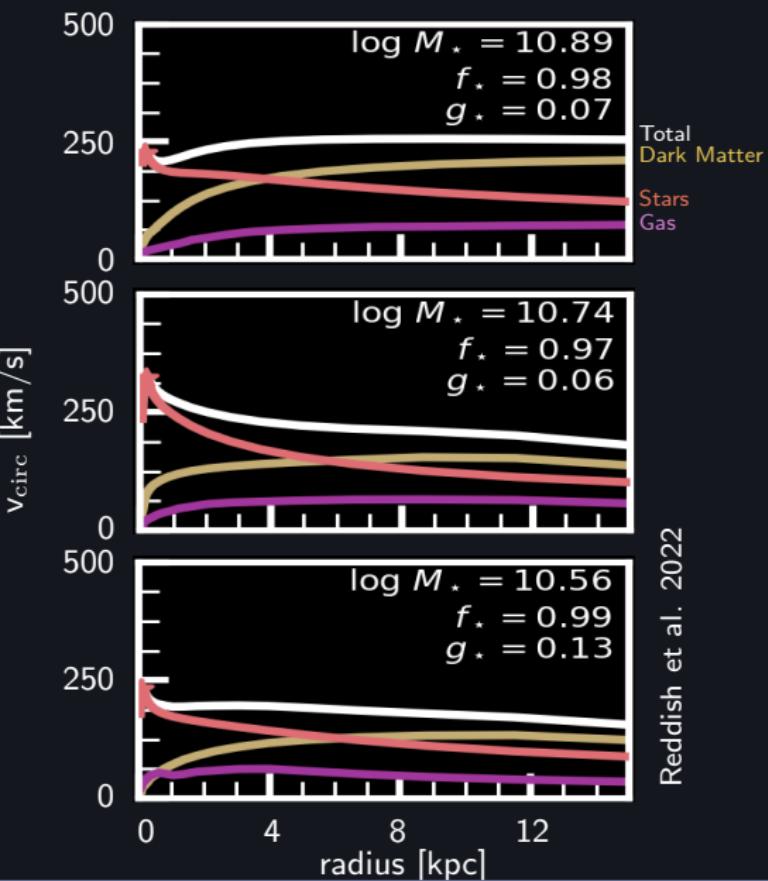
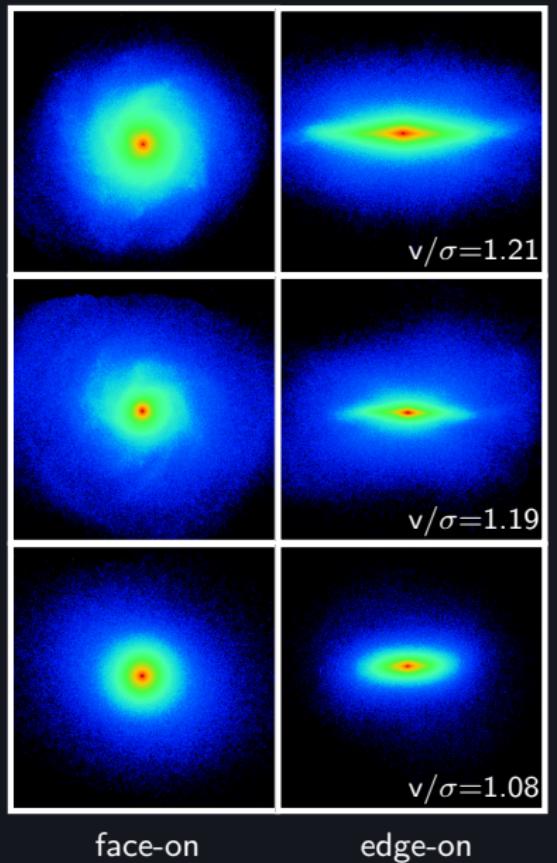
- DM deficient/poor exhibit closer orbits than control

Jackson et al. 2021

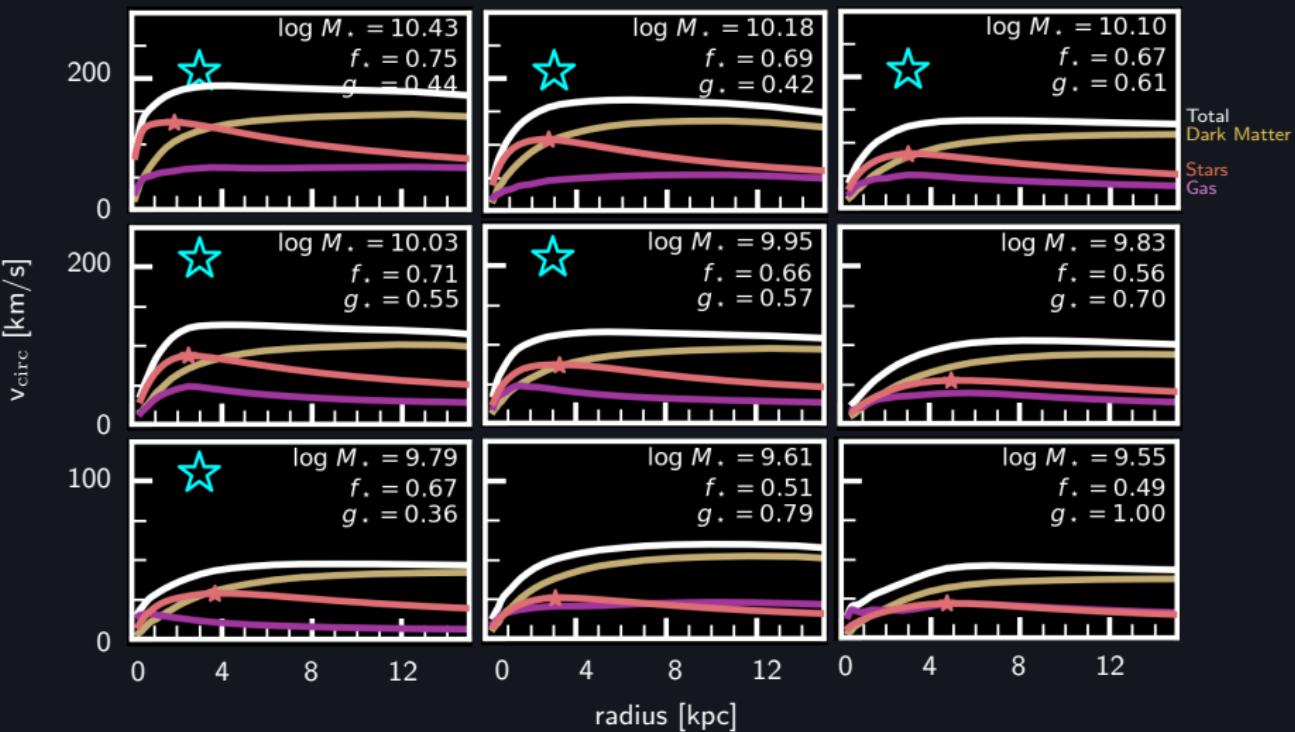


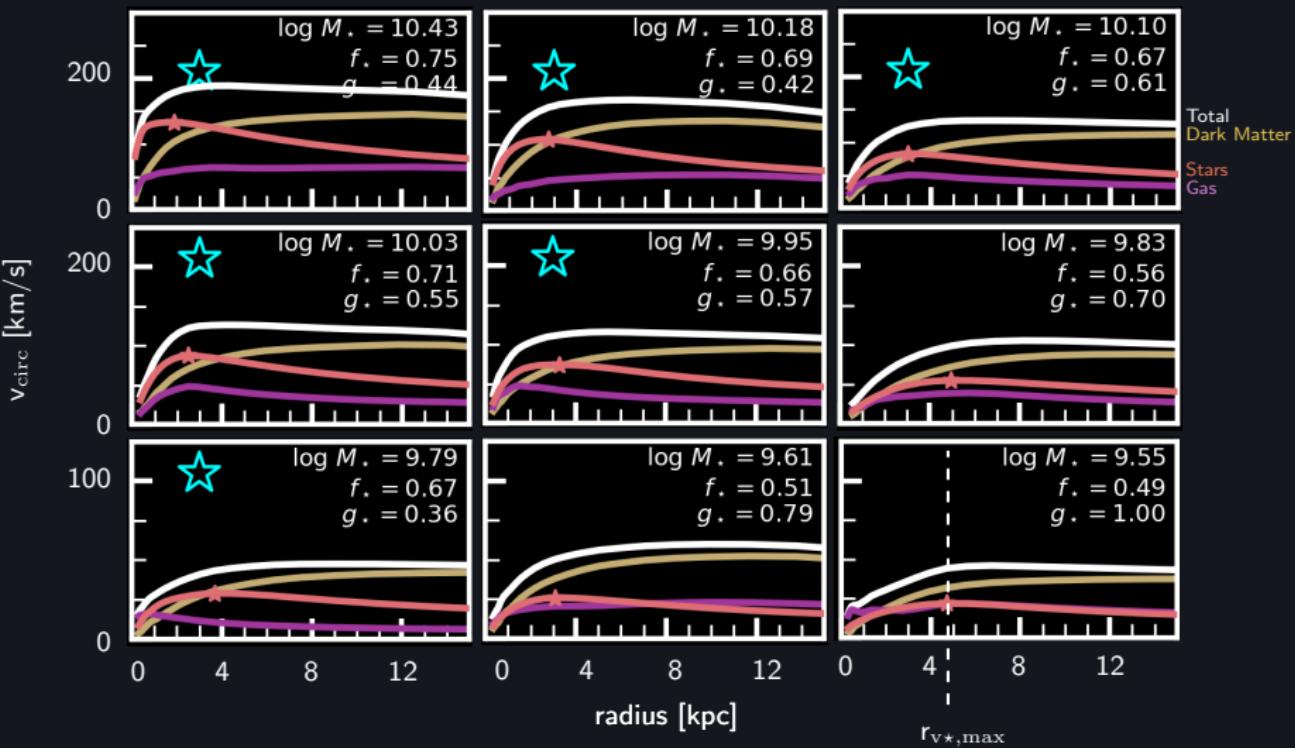






Reddish et al. 2022





$$f_{\star} \equiv \frac{v_{\star}(r_{\star}, \text{max})}{v_{\text{tot}}(r_{\star}, \text{max})}$$

- how '**maximal**'  
the galaxy is

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- how '**maximal**'  
the galaxy is

$$g_{\star} \equiv \frac{v_{\text{gas}}(r_{\star}, \text{max})}{v_{\star}(r_{\star}, \text{max})}$$

- **gas fraction** in  
galaxy

$$f_{\star} \equiv \frac{v_{\star}(r_{\star}, \text{max})}{v_{\text{tot}}(r_{\star}, \text{max})}$$

- how '**maximal**'  
the galaxy is

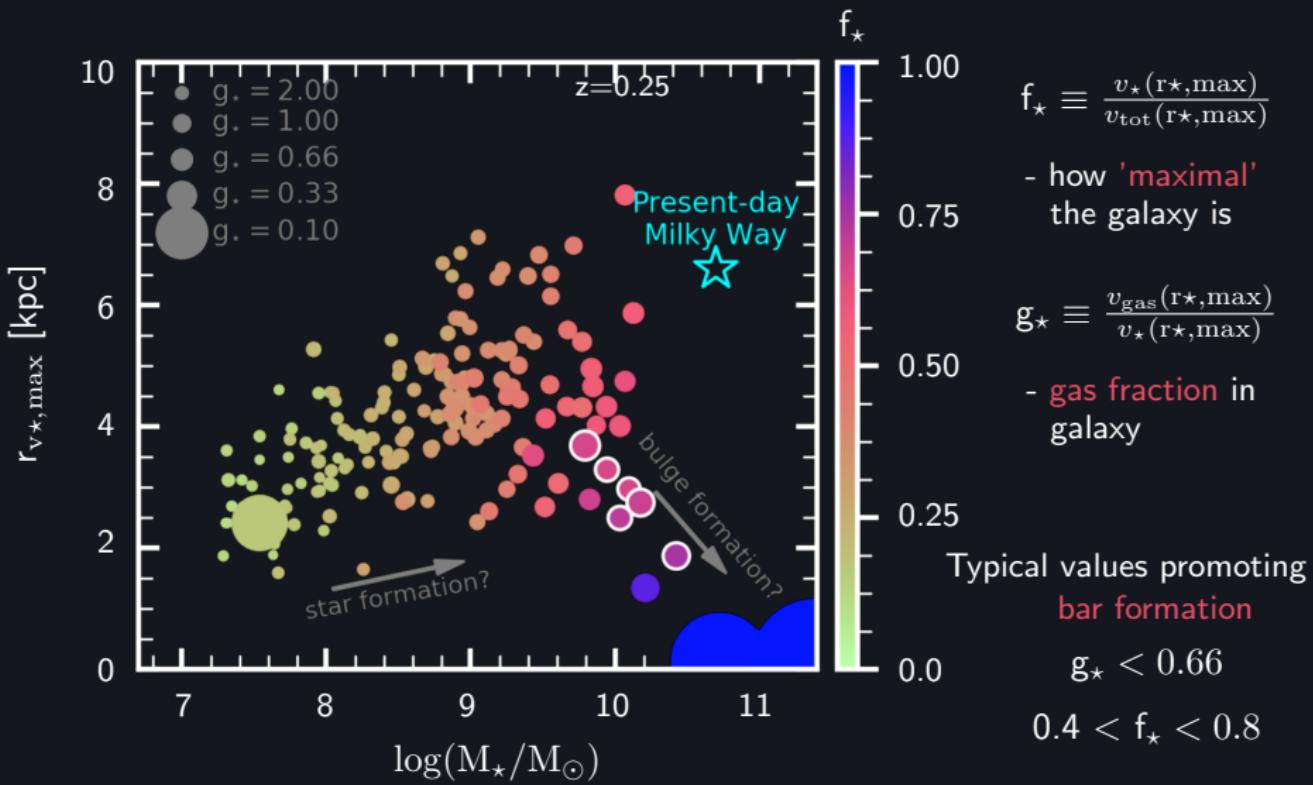
$$g_{\star} \equiv \frac{v_{\text{gas}}(r_{\star}, \text{max})}{v_{\star}(r_{\star}, \text{max})}$$

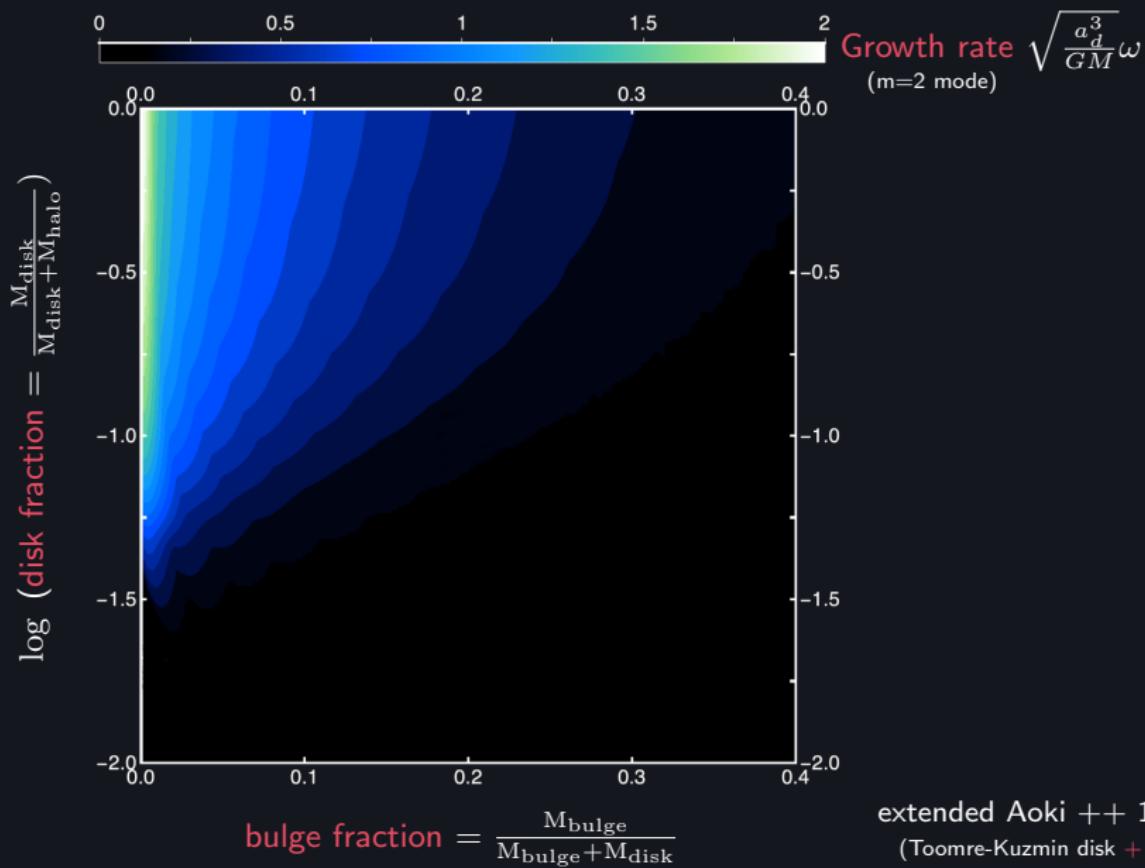
- **gas fraction** in  
galaxy

Typical values promoting  
**bar formation**

$$g_{\star} < 0.66$$

$$0.4 < f_{\star} < 0.8$$





extended Aoki ++ 1979 model  
(Toomre-Kuzmin disk + halo + bulge)

