Introduction to Deep Learning

Veronica Sanz Universitat de Valencia - IFIC (Spain) & Sussex University (UK)

@SoS '22



Today, we will talk about

Machine Learning techniques: Supervised Unsupervised Reinforcement Transfer Time-evolution Generative

My aim today is to introduce a range of uses of ML in Physics & beyond and some concepts and keywords to help you start looking Tomorrow: hands-on!

Human vs Machine Learning



repeat and improve on a task



repeat and improve on a task

predict the evolution of a situation



repeat and improve on a task

predict the evolution of a situation

discover unknown relations



repeat and improve on a task

predict the evolution of a situation

Previous experience discover unknown relations

choose the option that maximises return



repeat and improve on a task

predict the evolution of a situation

Previous experience discover unknown relations

choose the option that maximises return

imagine new possibilities

VERY IMPRESSIVE, YET human learning is limited by our personal viewpoint, our collective intelligence (*newspeak?*) & our inherent capacity to process information (amount , speed, level of detail)

ON THE OTHER HAND

the ultimate limitations of machine learning are unknown (if they do exist) CPU-> GPU, TPU, FPGA, IPU -> ... Quantum Computing, Neurophotonics...





Machine learning

repeat and improve on a task **SUPERVISED MACHINE LEARNING** predict the evolution of a situation **TIME-SERIES LEARNING**

discover unknown relations CLUSTERING/UNSUPERVISED

choose the option that maximises return **REINFORCEMENT LEARNING**

> imagine new possibilities GENERATIVE AI



Machine learning

TOMORROW's HANDS-ON

repeat and improve on a taskSUPERVISED MACHINE LEARNING

predict the evolution of a situation TIME-SERIES LEARNING

Previous experience discover unknown relations
CLUSTERING/UNSUPERVISED

choose the option that maximises return **REINFORCEMENT LEARNING**

> imagine new possibilities GENERATIVE AI

This technology is truly disruptive

we are unable to predict how fast is going to evolve and the extent of its applications

new algorithms and applications appear every day, and this tendency does not seem to slow down **ARTIFICIAL INTELLIGENCE** A programme that can feel, reason, act and adapt to the environment

MACHINE LEARNING Algorithms which improve as they are exposed to more data

> DEEP LEARNING Neural Networks which learn from huge amounts of data



Learning by example: Supervised ML repeat and improve on a task

A basic task: good or bad?



Is it a crocodile? Yes/No answer



A basic task: good or bad?



Is it a crocodile? Yes/No answer



To learn, dataset $\mathcal{D}(x_i, y_i) \ y \in \{0, 1\}$ with labels



Cat or dog?

Is this New Physics?

The simplest classification problem

Interpret the output of this transformation as a binomial probability

$$P(y_i = 1) = f(\mathbf{x}_i^T \mathbf{w}) = 1 - P(y_i = 0).$$

e.g. event b-tagged or not, event new physics or not

logistic regression: probability datapoint x_i as true or false

We define a cost function for this problem using Maximum Likelihood Estimation (MLE)

$$P(\mathcal{D}|\mathbf{w}) = \prod_{i=1}^{n} \left[f(\mathbf{x}_{i}^{T}\mathbf{w}) \right]^{y_{i}} \left[1 - f(\mathbf{x}_{i}^{T}\mathbf{w}) \right]^{1-y_{i}}$$

prob dataset *D* explained by our *model* w

Binary cost function: Cross-entropy

n

then log-likelihood is

$$l(\mathbf{w}) = \sum_{i=1}^{n} y_i \log f(\mathbf{x}_i^T \mathbf{w}) + (1 - y_i) \log \left[1 - f(\mathbf{x}_i^T \mathbf{w})\right]$$

best description: parameters w maximize the log-likelihood

$$\hat{\mathbf{w}} = \arg\max_{\boldsymbol{\theta}} \sum_{i=1}^{n} y_i \log f(\mathbf{x}_i^T \mathbf{w}) + (1 - y_i) \log \left[1 - f(\mathbf{x}_i^T \mathbf{w})\right]$$

Cost function is then chosen to be CROSS-ENTROPY

$$\mathcal{C}(\mathbf{w}) = -l(\mathbf{w})$$
 +regularization

Logistic regression

Take a dataset (**X**,y) where y is binary build a *cost function* = *cross-entropy m*inimise it and find the parameters **w**

We can use L1 or L2 regularisation

Binary is an example of *categorical* outputs When we have more than 2 categories, we use a cost function called SOFTMAX REGRESSION (a generalization of cross-entropy)



often convenient to describe the categories with ONE-HOT vectors

Logistic regression: measures of performance



How do we measure performance in a classification task?

 $Accuracy = \frac{Number of correct predictions}{Total number of predictions}$

'We now can distinguish cats and dogs with 95% accuracy' but maybe identifying cats is easier than dogs you nearly always get cats right (98%), but sometimes confuse a little dog for a cat (3%)

Moreover, in your learning you may want to specialise in id'ing dogs because want to make sure you don't miss any. You raise your threshold for them, paying a price cat performance

Logistic regression: measures of performance

So, let's say your focus is on dogs (you were bitten or had a bad experience) You would care about True positives (**TP**) : how many dogs you id False negatives (**FN**): how many you miss False positives (**FP**): how many cats you confuse with dogs True negatives (**TN**): cats you id



Neural Networks

Learning inspired by biology

Neural Networks (NNs)

A framework to develop AI, based on an architecture of *neurons* ONE NEURON = BUILDING BLOCKS OF NNs



First, a linear transformation z = w.x + bSecond, a non-linear function y = f(z)y: output, scalar (passes information, or not) f: activation function

Examples of activation functions



NN Architecture

Taking many neurons together, we can build an *architecture*



each circle is a neuron,

where the inputs (in-arrows) are transformed into output (out-arrows) the outputs of each layer serve as input for the next

Why are we doing this?



This NN transforms inputs (at the input layer) into an output (output layer) by passing via the hidden layers non-linear transformations of many non-linear transformations= highly non-linear transformation of input into output

Why are we doing this?



This NN transforms inputs (at the input layer) into an output (output layer) y(x)

which couldn't be captured by simple functional forms

Why are we doing this?



Neural Networks can model **complexity** They have a high degree of expressivity /exhibit high representational power More hidden layers=> more complex features Deep learning, deep NN Nowadays, Machine Learning is in the middle of a revolution: processing speed and storing capacity have increased enormously but **more importantly** the *way* machines learn has changed

TRADITIONALLY

learning was limited to lines of code we (humans) were writing

we can write *extremely complex* codes and the machine can improve in performing tasks but the structure of *thought* behind decision making is human if something_is_in_the_way is True:
 stop_moving()
else:

continue_moving()



The Machine can't describe relations we haven't coded in *like a born-blind person who is asked to think of blue*

A new way of thinking: Neural Networks

Structures made of units called *neurons* and organised by *layers*



The network learns from data with no structured instructions

Neural networks are able to explore relations between inputs and outputs which cannot be contained in lines of codes their degree of expressivity is immense *and* it is extremely fast built from simple units and in a layered architecture

Complex features

images, speech : are complex For example: cats/dogs



you can distinguish these cats and dogs, right? but how? would you be able to write a code which classifies them with ~ 100% accuracy? well, a NN can learn to do this!

Convolutional Neural Networks CNNs

Complex features are often *local*



Apart from shape and color,

we know a cat is a cat because there are relations among their features, e.g. the position of the eyes/ ears respect to the head centre, independently of where in the image the cat is **Locality** and **translational invariance** must end up playing a role in the identification task

Convolutional Neural Network (CNN) a type of NN architecture designed to exploit these two characteristics





Two types of basic layers

Convolution layer: Height, Width and Depth (e.g. RGB channels) *Convolution*= operation to reduce information while maintaining spatial relations (locality and translation properties)

Pooling: Take areas of the image and reduce them. Example, max-pooling would take 2X2 neurons and replace by a single neuron with input the max of the 4





Why do we do this? **Too much superfluous information in an image** Need to transform the image and capture the essentials while maintaining spatial relations

As we advance in the layers, the CNN is transforming the original image into something more and more abstract In physics, translationally invariant systems can be parametrised by wave number and functional form (sin, cos) whereas an arbitrary system would be *much more complex*

Why are NNs so good at learning?

Good at learning: ability to learn with little *domain knowledge* That's something physicists (as humans) are good at (Physics -> other things) DNNs are good at this too, they are able to take large streams of data

and learn features with little guidance, work like *black boxes*



Good at handling large amounts of data: needle in a haystack The NN structure (layers, 0/1 gates) allows a high representation power with moderate computational demands, e.g. allows parallelisation, use of GPUs... It scales better than other learning methods (like SVMs)

A lot of ML in Particle Physics is answering YES/NO questions Is it a W? Is it a Higgs? Is it DM?



mostly using Neural Networks to deal with images (CNNs)



A lot of ML in Particle Physics is answering YES/NO questions Is it a W? Is it a Higgs? Is it DM?



mostly using Neural Networks to deal with images (CNNs)




Diving into the unknown

what if we did not know what we were looking for?

So far getting better at predicting outputs

Multivariate linear regression



Classification task with images DNNs, CNNs



Binary classification in particle physics



in all these cases we knew the labels, the output of each input we knew what we were looking for our learning was guided, supervised

What if we didn't know what we were looking for?

what if the labels were not there? because they are unknown or too costly to be obtained or you wanted to learn something beyond these labels?

4.02210010110002L-01	-4.00 1020202000002-00	-1.014100010022002700	T.JJJJTULUULIJTLIL-UI	2.111011001004000-01	1.01000001000010100	0.0000000000000000000000000000000000000	-2.040000000121-01	1.20410012020002400	-2.021004001040002-01	0.001100004001102-01	1.00000020000012-01	1.02001 1010122042400	1.00100041004202400
8.65126013755798E-01	-1.10967397689819E+00	1.37884104251862E+00	1.2258266210556E+00	-1.59931445121765E+00	-3.35545927286148E-01	4.52621191740036E-01	1.396528840065E+00	1.43482126295567E-02	7.61019229888916E-01	8.73991847038269E-01	6.46077632904053E-01	6.55984878540039E-01	2.75867860764265E-02
6.79041624069214E-01	-1.16113260388374E-01	-1.44924676418304E+00	7.25930333137512E-01	8.32636177539825E-01	-1.06863963603973E+00	7.34275758266449E-01	6.16540551185608E-01	1.10223841667175E+00	-3.8318920135498E-01	6.74581229686737E-01	9.89126741886139E-01	1.30116701126099E+00	2.11356925964355E+00
6.96710646152496E-01	1.53248345851898E+00	4.51736569404602E-01	9.53612387180328E-01	1.08532404899597E+00	-1.26148509979248E+00	2.19569746404886E-02	7.69306182861328E-01	1.76076497882605E-02	3.32875728607178E-01	6.81880474090576E-01	1.27228811383247E-01	1.65573984384537E-01	4.10077683627605E-02
1.00609767436981E+00	-2.18872010707855E-01	1.27333605289459E+00	1.62148654460907E+00	7.60176777839661E-02	5.86132228374481E-01	5.61284124851227E-01	1.70752331614494E-01	5.829758644104E-01	4.111288189888E-01	1.04620361328125E+00	7.77394592761993E-01	6.59388244152069E-01	1.17781555652618E+00
8.37866902351379E-01	1.13452970981598E+00	-9.11251723766327E-01	6.16625964641571E-01	1.00015830993652E+00	1.2927371263504E+00	1.27245831489563E+00	-6.76616489887238E-01	7.64919698238373E-01	1.16551697254181E+00	6.31192624568939E-01	7.86714017391205E-01	1.10604000091553E+00	8.15494537353516E-01
1.64174771308899E+00	-1.82980680465698E+00	1.50152146816254E-01	2.70264196395874E+00	-1.2972204387188E-01	-1.38081395626068E+00	1.94475173950195E-01	-1.47864866256714E+00	5.51068745553493E-02	3.0361208319664E-01	2.63883185386658E+00	6.36116921901703E-01	2.13914230465889E-01	2.300715893507E-01
1.46664869785309E+00	1.15517094731331E-01	-1.03616142272949E+00	8.77246916294098E-01	6.90861403942108E-01	1.13006901741028E+00	8.9072197675705E-01	4.26515430212021E-01	1.28321182727814E+00	-5.63879549503326E-01	1.0900456905365E+00	1.32757031917572E+00	1.08076226711273E+00	1.58807563781738E+00
1.64159500598907E+00	-1.04459571838379E+00	5.43058097362518E-01	7.44841694831848E-01	-3.0812594294548E-01	-9.56824660301208E-01	1.24903869628906E+00	-1.47708666324615E+00	7.31511473655701E-01	-8.47167015075684E-01	1.16093373298645E+00	1.60183656215668E+00	1.2244086265564E+00	1.25674676895142E+00
1.36144161224365E+00	-5.06246566772461E-01	-6.46163880825043E-01	1.04786920547485E+00	1.13672995567322E+00	6.98664963245392E-01	1.65792429447174E+00	-6.15012310445309E-02	2.15440988540649E+00	1.67285251617432E+00	1.52531015872955E+00	1.11749887466431E+00	6.50135576725006E-01	0E+00
1.29748213291168E+00	-2.54911869764328E-01	1.11683440208435E+00	9.79169011116028E-01	-1.35346204042435E-01	-6.9715404510498E-01	1.02749526500702E+00	-1.66322216391563E-01	1.2542005777359E+00	-4.79648977518082E-01	9.85065758228302E-01	1.2597473859787E+00	1.13483691215515E+00	7.60779619216919E-01
1.29748213291168E+00 3.7850496172905E-01	-2.54911869764328E-01 -1.08213400840759E+00	1.11683440208435E+00 1.00809907913208E+00	9.79169011116028E-01 6.11425042152405E-01	-1.35346204042435E-01 -1.28556573390961E+00	-6.9715404510498E-01 -6.55805096030235E-02	1.02749526500702E+00 9.16272640228271E-01	-1.66322216391563E-01 -8.86185646057129E-01	1.2542005777359E+00 1.371866106987E+00	-4.79648977518082E-01 -4.21904683113098E-01	9.85065758228302E-01 3.91696661710739E-01	1.2597473859787E+00 7.90428757667542E-01	1.13483691215515E+00 1.79072606563568E+00	7.60779619216919E-01 1.38843953609467E+00
1.29748213291168E+00 3.7850496172905E-01 6.75932705402374E-01	-2.54911869764328E-01 -1.08213400840759E+00 1.26536428928375E-01	1.11683440208435E+00 1.00809907913208E+00 9.56136286258698E-01	9.79169011116028E-01 6.11425042152405E-01 6.86048328876495E-01	-1.35346204042435E-01 -1.28556573390961E+00 -1.99499741196632E-01	-6.9715404510498E-01 -6.55805096030235E-02 -1.70811021327972E+00	1.02749526500702E+00 9.16272640228271E-01 9.24258589744568E-01	-1.66322216391563E-01 -8.86185646057129E-01 -6.93052709102631E-01	1.2542005777359E+00 1.371866106987E+00 1.38742446899414E+00	-4.79648977518082E-01 -4.21904683113098E-01 -5.49809157848358E-01	9.85065758228302E-01 3.91696661710739E-01 5.77164828777313E-01	1.2597473859787E+00 7.90428757667542E-01 1.04205667972565E+00	1.13483691215515E+00 1.79072606563568E+00 1.60216736793518E+00	7.60779619216919E-01 1.38843953609467E+00 1.92126834392548E+00
1.29748213291168E+00 3.7850496172905E-01 6.75932705402374E-01 4.63986992835999E-01	-2.54911869764328E-01 -1.08213400840759E+00 1.26536428928375E-01 1.13328350707889E-02	1.11683440208435E+00 1.00809907913208E+00 9.56136286258698E-01 3.69053810834885E-01	9.79169011116028E-01 6.11425042152405E-01 6.86048328876495E-01 5.53186655044556E-01	-1.35346204042435E-01 -1.28556573390961E+00 -1.99499741196632E-01 3.89279514551163E-01	-6.9715404510498E-01 -6.55805096030235E-02 -1.70811021327972E+00 3.0157333612442E-01	1.02749526500702E+00 9.16272640228271E-01 9.24258589744568E-01 1.65791296958923E+00	-1.66322216391563E-01 -8.86185646057129E-01 -6.93052709102631E-01 1.52030777931213E+00	1.2542005777359E+00 1.371866106987E+00 1.38742446899414E+00 2.4887318611145E+00	-4.79648977518082E-01 -4.21904683113098E-01 -5.49809157848358E-01 -5.59999048709869E-01	9.85065758228302E-01 3.91696661710739E-01 5.77164828777313E-01 4.2525789141655E-01	1.2597473859787E+00 7.90428757667542E-01 1.04205667972565E+00 1.12646055221558E+00	1.13483691215515E+00 1.79072606563568E+00 1.60216736793518E+00 2.35060715675354E+00	7.60779619216919E-01 1.38843953609467E+00 1.92126834392548E+00 2.46035838127136E+00
1.29748213291168E+00 3.7850496172905E-01 6.75932705402374E-01 4.63986992835999E-01 1.16491532325745E+00	-2.54911869764328E-01 -1.08213400840759E+00 1.26536428928375E-01 1.13328350707889E-02 -1.21687364578247E+00	1.11683440208435E+00 1.00809907913208E+00 9.56136286258698E-01 3.69053810834885E-01 1.38738358020782E+00	9.79169011116028E-01 6.11425042152405E-01 6.86048328876495E-01 5.53186655044556E-01 1.28936243057251E+00	-1.35346204042435E-01 -1.28556573390961E+00 -1.99499741196632E-01 3.89279514551163E-01 8.53503286838531E-01	-6.9715404510498E-01 -6.55805096030235E-02 -1.70811021327972E+00 3.0157333612442E-01 -8.64189207553864E-01	1.02749526500702E+00 9.16272640228271E-01 9.24258589744568E-01 1.65791296958923E+00 5.52336990833282E-01	-1.66322216391563E-01 -8.86185646057129E-01 -6.93052709102631E-01 1.52030777931213E+00 3.71582925319672E-01	1.2542005777359E+00 1.371866106987E+00 1.38742446899414E+00 2.4887318611145E+00 8.29125940799713E-01	-4.79648977518082E-01 -4.21904683113098E-01 -5.49809157848358E-01 -5.59999048709869E-01 -1.4921934902668E-01	9.85065758228302E-01 3.91696661710739E-01 5.77164828777313E-01 4.2525789141655E-01 1.86399924755096E+00	1.2597473859787E+00 7.90428757667542E-01 1.04205667972565E+00 1.12646055221558E+00 9.7541731595993E-01	1.13483691215515E+00 1.79072606563568E+00 1.60216736793518E+00 2.35060715675354E+00 4.64367836713791E-01	7.60779619216919E-01 1.38843953609467E+00 1.92126834392548E+00 2.46035838127136E+00 1.68607497215271E+00
1.29748213291168E+00 3.7850496172905E-01 6.75932705402374E-01 4.63986992835999E-01 1.16491532325745E+00 8.00468981266022E-01	-2.54911869764328E-01 -1.08213400840759E+00 1.26536428928375E-01 1.13328350707889E-02 -1.21687364578247E+00 -9.84456762671471E-02	1.11683440208435E+00 1.00809907913208E+00 9.56136286258698E-01 3.69053810834885E-01 1.38738358020782E+00 -7.95078039169312E-01	9.79169011116028E-01 6.11425042152405E-01 6.86048328876495E-01 5.53186655044556E-01 1.28936243057251E+00 4.77954834699631E-01	-1.35346204042435E-01 -1.28556573390961E+00 -1.99499741196632E-01 3.89279514551163E-01 8.53503286838531E-01 -4.29955363273621E-01	-6.9715404510498E-01 -6.55805096030235E-02 -1.70811021327972E+00 3.0157333612442E-01 -8.64189207553864E-01 1.08130276203156E+00	1.02749526500702E+00 9.16272640228271E-01 9.24258589744568E-01 1.65791296958923E+00 5.52336990833282E-01 8.88447284698486E-01	-1.66322216391563E-01 -8.86185646057129E-01 -6.93052709102631E-01 1.52030777931213E+00 3.71582925319672E-01 -3.40310782194138E-01	1.2542005777359E+00 1.371866106987E+00 1.38742446899414E+00 2.4887318611145E+00 8.29125940799713E-01 9.66846108436584E-01	-4.79648977518082E-01 -4.21904683113098E-01 -5.49809157848358E-01 -5.59999048709869E-01 -1.4921934902668E-01 8.3782559633255E-01	9.85065758228302E-01 3.91696661710739E-01 5.77164828777313E-01 4.2525789141655E-01 1.86399924755096E+00 5.76379001140594E-01	1.2597473859787E+00 7.90428757667542E-01 1.04205667972565E+00 1.12646055221558E+00 9.7541731595993E-01 6.60021543502808E-01	1.13483691215515E+00 1.79072606563568E+00 1.60216736793518E+00 2.35060715675354E+00 4.64367836713791E-01 1.01617026329041E+00	7.60779619216919E-01 1.38843953609467E+00 1.92126834392548E+00 2.46035838127136E+00 1.68607497215271E+00 6.41459822654724E-01
1.29748213291168E+00 3.7850496172905E-01 6.75932705402374E-01 4.63986992835999E-01 1.16491532325745E+00 8.00468981266022E-01 3.41047215461731E+00	-2.54911869764328E-01 -1.08213400840759E+00 1.26536428928375E-01 1.13328350707889E-02 -1.21687364578247E+00 -9.84456762671471E-02 5.90151190757751E-01	1.11683440208435E+00 1.00809907913208E+00 9.56136286258698E-01 3.69053810834885E-01 1.38738358020782E+00 -7.95078039169312E-01 1.50781488418579E+00	9.79169011116028E-01 6.11425042152405E-01 6.86048328876495E-01 5.53186655044556E-01 1.28936243057251E+00 4.77954834699631E-01 2.19785332679749E+00	-1.35346204042435E-01 -1.28556573390961E+00 -1.99499741196632E-01 3.89279514551163E-01 8.53503286838531E-01 -4.29955363273621E-01 9.15379881858826E-01	-6.9715404510498E-01 -6.55805096030235E-02 -1.70811021327972E+00 3.0157333612442E-01 -8.64189207553864E-01 1.08130276203156E+00 -2.43708327412605E-01	1.02749526500702E+00 9.16272640228271E-01 9.24258589744568E-01 1.65791296958923E+00 5.52336990833282E-01 8.88447284698486E-01 1.00378489494324E+00	-1.66322216391563E-01 -8.86185646057129E-01 -6.93052709102631E-01 1.52030777931213E+00 3.71582925319672E-01 -3.40310782194138E-01 9.47994440793991E-02	1.2542005777359E+00 1.371866106987E+00 1.38742446899414E+00 2.4887318611145E+00 8.29125940799713E-01 9.66846108436584E-01 8.52464973926544E-01	-4.79648977518082E-01 -4.21904683113098E-01 -5.49809157848358E-01 -5.59999048709869E-01 -1.4921934902668E-01 8.3782559633255E-01 -5.42668044567108E-01	9.85065758228302E-01 3.91696661710739E-01 5.77164828777313E-01 4.2525789141655E-01 1.86399924755096E+00 5.76379001140594E-01 2.5086042881012E+00	1.2597473859787E+00 7.90428757667542E-01 1.04205667972565E+00 1.12646055221558E+00 9.7541731595993E-01 6.60021543502808E-01 2.03399634361267E+00	1.13483691215515E+00 1.79072606563568E+00 1.60216736793518E+00 2.35060715675354E+00 4.64367836713791E-01 1.01617026329041E+00 7.19505548477173E-01	7.60779619216919E-01 1.38843953609467E+00 1.92126834392548E+00 2.46035838127136E+00 1.68607497215271E+00 6.41459822654724E-01 4.56694543361664E-01



what would you do? as a physicist, you would start thinking on possible physical relations, plotting things, trying to obtain the **best data representation** the representation which **manifests** a behaviour

So everything starts with data visualization

But we can't visualise things in more than 3D when most data we want to mine is high-dimensional...

So you need to do DIMENSIONAL REDUCTION from original space to **latent space**



Reduction n-D to few-D isn't simply projecting in a lower dimensional space one dimension at a time Choice: *direction* to project to keep as much info as possible

Bad choice



end up with a *crowding problem* the best choice to represent this data is 2D, going to 1D does limit your ability to learn There's hope, stat dynamics shows micro->macro can work

Being smart at dimensional reduction

The direction to project out dimensions is important We need a criteria

Principal Component Analysis (PCA)



-	0.	8	

In our representation of the data -0.6 there are clearly some redundancies there could be one or more -0.4 LINEAR COMBINATIONS 0.2 of some of these variables which 0.0 capture most of the information -0.2

PCA

The procedure is simple enough, take the correlation matrix

$$\boldsymbol{\Sigma}(\boldsymbol{X}) = \frac{1}{N-1} \boldsymbol{X}^T \boldsymbol{X}.$$

and diagonalize it

$$X = USV^{T} \text{ with } S \text{ diagonal}$$

$$\Sigma(X) = \frac{1}{N-1} VSU^{T} USV^{T}$$

$$= V \left(\frac{S^{2}}{N-1}\right) V^{T}$$

$$\equiv V\Lambda V^{T}.$$
(is)

Λ

is a diagonal matrix with ordered eigenvalues

V

contains the eigenvectors the directions of decreasing eigenvalue

We can then dimensionally reduce, but removing the directions in V with the smallest eigenvalues, the ones which carry less information in correlations

eqs. from this excellent <u>review</u>

t-SNE

PCA is good as a first try at visualisation but is limited by its linearity Often we would like to preserve **local** structures in higher-dimensions, and PCA won't do that A good example of non-linear techniques is **t-SNE** (t-stochastic neighbour embedding)

In a nutshell,

t-SNE compares local distributions in the original and latent space

$$\begin{array}{l} \mathbf{ORIGINAL} & \exp(-||x_i - x_j||^2 / 2\sigma_i^2) \\ p_{i|j} = \frac{1}{\sum_{k \neq i} \exp(-||x_i - x_k||^2 / 2\sigma_i^2)} \end{array}$$

$$\begin{array}{l} \mathbf{LATENT} & (1+||y_i - y_j||^2)^{-1} \\ q_{ij} = \frac{1}{\sum_{k \neq i} (1+||y_i - y_k||^2)^{-1}} \end{array}$$

with sigma_i some parameter and Y the projected latent space

chosen as latent space

and provides a criteria for

minimisation

$$ilde{m{Y}} = m{X} ilde{m{V}}_{p'}$$



Now that we have reduced dimensionality by PCA or t-SNE or another method we can start thinking on finding patterns in it



Clustering is the most intuitive way to find patterns Finding clusters of common behaviour using some distance criteria in the latent space

Clustering is an iterative procedure start with some parameters like N clusters, cluster size etc and try clustering the data using these criteria The mathematical expressions are cumbersome (many definitions of running parameters) but the intuitive meaning is clear

Different clustering methods



From SCIKIT webpage on clustering methods



Can I have a cookie?

Learning by reward

Additional

Types of learning



Supervised to Reinforced Learning

Cool ways to accelerate learning, capture important aspects of the data, incorporate different types of data

Learn **from** humans to do what humans **already do**, but better and faster, and in more difficult situations

But, what if we wanted a machine to become **better** than a human at completing a high-level task?

* See <u>these lectures</u>

Let's find a DIFFICULT task

A truly human-difficult task

not just a task that a machine can do faster or with lower resolution

Supervised / unsupervised learning identifies *patterns* in data But this isn't the same as learning to develop a *strategy* and to do it better than a human



Chess is a high-level activity different players develop different strategies the goal is *long-term* important pieces can be sacrificed to achieve checkmate some moves along the way and you have an adversary which will oblige you to *reassess* your strategy at each step *combinatorics* is ginormous

Human vs Machine



February 1996 Deep Blue (IBM) beat Garry Kasparov (World Champion) and did it again many times after brute-force computing power analysing many hundreds of millions positions / second

Human vs Machine





February 1996 Deep Blue (IBM) beat Garry Kasparov (World Champion) and did it again many times after brute-force computing power analysing many hundreds of millions positions / second October 2015 AlphaGo Zero beats a professional Go player learned from playing against *itself* November 2017 AlphaZero builds on DNNs to beat world champions in Go, chess and shogi

Human vs Machine

February 1996 Deep Blue (IBM) beat Garry Kasparov (World Champion) and did it again many times after brute-force computing power analysing many hundreds of millions positions / second October 2015 AlphaGo Zero beats a professional Go player learned from playing against itself November 2017 AlphaZero builds on DNNs to beat world champions in Go, chess and shogi

A new paradigm of learning: **REINFORCEMENT**

Go game

Simple game: moves are simple no hierarchy like chess king/queen/bishop/pawn... goal: surround and capture opponents' pieces

Simple rules, extreme levels of complexity when building strategies no machine could beat a Go-master until 2015 Why is it so difficult? how would you teach a machine to learn this game?

X,y

Go game

Simple game: moves are simple no hierarchy like chess king/queen/bishop/pawn... goal: surround and capture opponents' pieces

develop a strategy for long-term winning: 3^(19*19)~10^172 configurations at one step decision in this one step guided by possible future gains but opponent's actions change every subsequent move

Reinforcement learning

The task of getting better at Go was too difficult too many possibilities, no human could teach from example To beat humans we had to allow machines to learn in a different way

Machine needs to learn to make good sequences of decisions dealing with delayed labels and developing a long-term strategy Some form of iterative way of improving strategy which can examine many steps ahead

agent interacts with the environment in state *st* takes actions based on reward *rt* which tells about good current state is GOAL: maximise total about of rewards (return) RL help the agent to achieve goal

Reinforcement learning: concepts

State/Observation: some kind of tensor (e.g. *an image*) **Action:** possible transformation of the state (e.g. *move pawn*) **Policy:** rule used by the agent to decide what action to take $a_t = \pi(s_t)$

can be deterministic or stochastic and often parametrised $a_t = \pi_{\theta}(s_t)$

by some form of modelling of possible new situations this sampling of possible trajectories $\tau(s_0, a_0, s_1, a_1...)$

often done with DNNs (Deep Reinforcement)

Reinforcement learning: concepts

Reward: some function of current state and action taken, and next state

Return: total reward in a full sequence, a trajectory

$$R(\tau) = \sum_{t=0}^{T} r_t$$

Real problems have limitations, so not all trajectories can be taken at no cost (e.g. *time limit, loss at each step...*) and we introduce a **discount**

$$R(\tau) = \sum_{t=0} \gamma^t r_t$$

cash now/cash in few years

Reinforcement learning: fun video

And a super fun <u>blog</u> and <u>video</u>

ramps

Fully Connected

x, v of ramps Masked Average Pooling

Grabbing

Action

Movement

Action

LSTM

Locking

Action

Reinforcement learning: overview

Clearly, this is a complex set-up states could contain lots of information an agent could choose among many actions the number of possible steps could be very large rewards are set to help the algorithm to increase final return (policy optimisation) but their efficiency depends on ability to explore

how the state changes by itself (opponent) or by the action RL helps learning an *environment*

There are many, many possibilities most successful are based on Deep Learning & good adaptation to environment changes e.g. ability to dynamically drop and add terms in policy

Going further?

You could follow a *Tensorflow* <u>tutorial</u> on training agents using different policies Environment: <u>Cartpole</u> (start reading this <u>post</u>)

In Physics, mostly unexplored complex numerical simulations: many body, fluid dynamics...

situations with many agents and interactions see e.g. this nice <u>example</u> fish coordinated swimming for energy saving

Transfer Learning

Additional

Transfer Learning

So far, our Machine was like a newborn baby looking at a dataset/environment and learning from it with or without guidance, using rewards Complex datasets require Deep Learning long time to run and optimise and *specific* to the dataset

BUT babies do not learn every task from scratch

example: **language** learn generic concepts actions->verbs objects/people->names characteristics->adjectives

Babies are able to TRANSFER LEARNING ENGLISH -> SPANISH, CHINESE etc and our Machine should do too

Supervised learning

Image classification problem

Input Image

Hidden layers are transforming the initial image into something more abstract (simple/complex shapes->shapes specific to a flower) and at the end this is transformed into a set of vectors which are then fed to a set of FC NNs **initial layers** are more problem-independent **later layers** are more specific to the problem at hand

Changing the target

What if now I want to classify types of dogs or leaves or cars? I would start by changing...

But probably build a very similar NN architecture **Transfer learning:** allows me to keep some of the architecture and initial computations (some weights in the hidden layers) and just re-run part of the network to specialise on this new problem

Increase AI's speed, reusability and generalisation

Repurposing pre-trained networks

as we run the network, we update the weights to improve the accuracy this weight updating is costly we can **freeze** some of the weights that are generic for problem = image and just adjust the later layers

All ML frameworks contained pre-trained models

Images==> VGG/ResNet/DenseNet/Inception/Xception... Language (NLP) ==> Word2Vec, GloVe, FastText...

An example of pre-trained model: VGG16

Freeze initial layers and tune the rest

This strategy reduces a lot the computing time and helps generalising tasks Data augmentation is typically used to make the procedure more robust

Going further?

In this <u>notebook</u> you can find some brief examples of transfer learning for MNIST and for a PP example Use PYTORCH and FASTAI, syntax is compact PP example: LHC Olympics 2020 images of boosted jets produced by SM and by a new heavy particle small dataset, use augmentation

If you got time, check-out some of the newest applications, like *Feynman AI* or <u>Transfer Learning for music</u>

Knowing the past, predicting the future predict the evolution of a situation

"Experience is a lantern that you carry on your back and that only lights up the path you have traveled." *Confucius*

Additional

Never mind, Confucius! ML *can* predict the future

By learning from examples of time series (snapshots of past->future sequences) and using RNNs (recurrent NNs) in particular LSTMs (long short term memory)

Time evolution of the solar activity blue-> reality orange-> prediction

Going further

imagine new possibilities

Here be dragons!

Additional

What if we didn't ask for an outcome?

Supervised learning input-> predict output what if we just asked 'look at this!' with no determined output? **GANs (Generative Adversarial Networks)** and **VAEs (Variational AutoEncoders)** In CNNs, benchmarks were cats/dogs and hand-written digits (MNIST) Here, human faces

What if we didn't ask for an outcome?

Supervised learning input-> predict output what if we just asked 'look at this!' with no determined output? **GANs (Generative Adversarial Networks)** and **VAEs (Variational AutoEncoders)** In CNNs, benchmarks were cats/dogs and hand-written digits (MNIST) Here, human faces

STEP 1 - 'LEARN' what is a human face

Doing this many times, while the DISCRIMINATOR says: 'You are going in the right direction', 'You are completely lost!'
What if we didn't ask for an outcome?

Supervised learning input-> predict output what if we just asked 'look at this!' with no determined output? **GANs (Generative Adversarial Networks)** and **VAEs (Variational AutoEncoders)** In CNNs, benchmarks were cats/dogs and hand-written digits (MNIST) Here, human faces

STEP 2- AFTER MANY ITERATIONS...



When the avatars are indistinguishable to the DISCRIMINATOR, game is over

What if we didn't ask for an outcome?

Supervised learning input-> predict output what if we just asked 'look at this!' with no determined output? **GANs (Generative Adversarial Networks)** and **VAEs (Variational AutoEncoders)** In CNNs, benchmarks were cats/dogs and hand-written digits (MNIST) Here, human faces

STEP 3- CREATE NEW POSSIBILITIES



This woman does not exist. It has been generated from noise. The NN has learnt the concept of 'human face' and now can create human faces from noise

What if we didn't ask for an outcome?

Supervised learning input-> predict output what if we just asked 'look at this!' with no determined output? **GANs (Generative Adversarial Networks)** and **VAEs (Variational AutoEncoders)** In CNNs, benchmarks were cats/dogs and hand-written digits (MNIST) Here, human faces

Anomaly Detection



Ask to look only to Standard Model ('normal') events

Learns to ID outliers ('New Physics')



In this document: lots of links to learn more Tomorrow: a <u>hands-on</u> starting from the dataset David gave you yesterday

We are just starting to understand the applications of ML in Physics

So far, dominated by the low-hanging fruit: supervised classification ML brings added value, shortening data-taking times

They go beyond a mere iteration of our traditional statistical methods: unsupervised methods, generative AI, reinforcement learning...

Remember that through AI methods we could get interesting cross-pollination between our area (PP) and others Opportunity to learn from other areas in Science

Keep exploring!