

Boosted decision trees

Yann Coadou

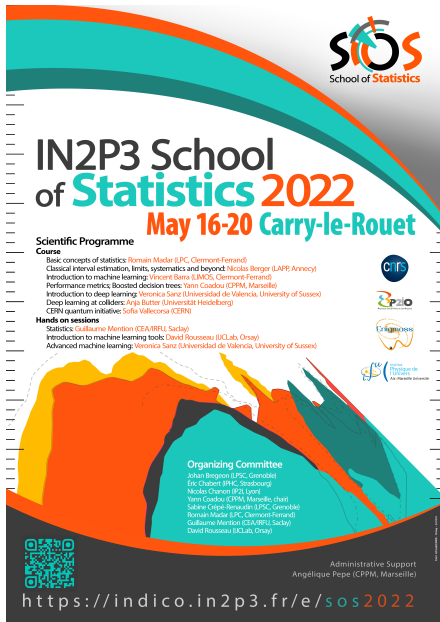
CPPM Marseille


SOS2022

Carry-le-Rouet, 17 May 2022



School of **Statistics**





IN2P3 School of Statistics 2022

May 16-20 Carry-le-Rouet





Scientific Programme

Course

- Basic concepts of statistics: Romain Mader (I.P.C., Clermont-Ferrand)
- Classical interval estimation, limits, systematics and beyond: Nicolas Berger (LAPP, Annecy)
- Introduction to machine learning: Vincent Bara (LMOS, Clermont-Ferrand)
- Performance metrics: Boosted decision trees: Yann Coadou (CPPM, Marseille)
- Introduction to deep learning: Veronica Sanz (Universidad de Valencia, University of Sussex)
- Deep learning at colliders: Anja Butter (Universität Heidelberg)
- CERN quantum initiative: Sofia Vallecora (CERN)

Hands on sessions


- Statistics: Guillaume Menton (CEA-IRFU, Saclay)
- Introduction to machine learning tools: David Rousseau (IJCLab, Orsay)
- Advanced machine learning: Veronica Sanz (Universidad de Valencia, University of Sussex)

Organizing Committee

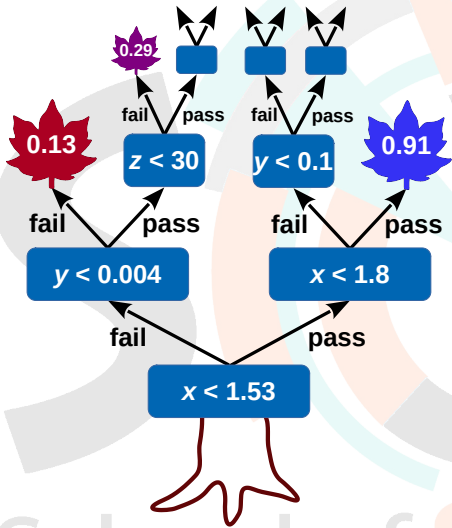
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- 1 Decision trees
- 2 Limitations
- 3 Boosted decision trees
- 4 Software
- 5 Conclusion
- 6 References



1 Decision trees

- Algorithm
- Tree hyperparameters
- Splitting a node
- Variable selection

Decision tree origin

- Machine-learning technique, widely used in social sciences. Originally data mining/pattern recognition, then medical diagnosis, insurance/loan screening, etc.



L. Breiman *et al.*, “Classification and Regression Trees” (1984)

Basic principle

- Extend cut-based selection
 - many (most?) events do not have *all* characteristics of signal or background
 - try not to rule out events failing a particular criterion
- Keep events rejected by one criterion and see whether other criteria could help classify them properly

Binary trees

- Trees can be built with branches splitting into many sub-branches
- In this lecture: mostly binary trees

Start with all events (signal and background) = first (root) node

- sort all events by each variable
- for each variable, find splitting value with best separation between two children
 - mostly signal in one child
 - mostly background in the other
- select variable and splitting value with best separation, produce two branches (nodes)
 - events failing criterion on one side
 - events passing it on the other

Keep splitting

- Now have two new nodes. Repeat algorithm recursively on each node
- Can reuse the same variable
- Iterate until stopping criterion is reached (min leaf size, max tree depth, insufficient improvement, perfect classification, etc.)
- Splitting stops: terminal node = leaf

- Consider signal (s_i) and background (b_j) events described by 3 variables: p_T of leading jet, top mass M_t and scalar sum of p_T 's of all objects in the event H_T



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 - $H_T^{b_5} \leq H_T^{b_3} \leq \dots \leq H_T^{s_{67}} \leq H_T^{s_{43}}$
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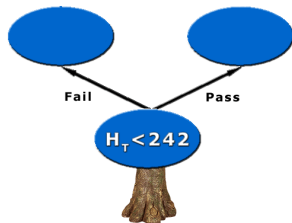
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 - best split (arbitrary unit):
 - $p_T < 56$ GeV, separation = 3
 - $H_T < 242$ GeV, separation = 5
 - $M_t < 105$ GeV, separation = 0.7



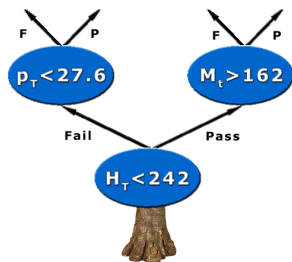
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- Repeat recursively on each node



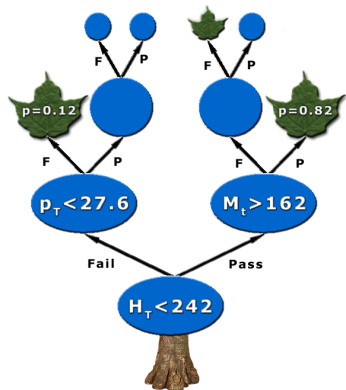
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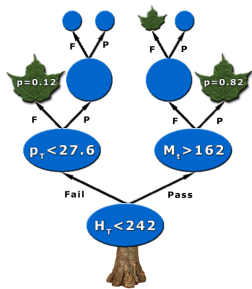
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- Splitting stops: e.g. events with $H_T < 242$ GeV and $M_t > 162$ GeV are signal like ($p = 0.82$)



Run event through tree

- Start from root node
- Apply first best cut
- Go to left or right child node
- Apply best cut for this node
- ...Keep going until...
- Event ends up in leaf



DT Output

- Purity ($\frac{s}{s+b}$, with weighted events) of leaf, close to 1 for signal and 0 for background
- or binary answer (discriminant function +1 for signal, -1 or 0 for background) based on purity above/below specified value (e.g. $\frac{1}{2}$) in leaf
- E.g. events with $H_T < 242$ GeV and $M_t > 162$ GeV have a DT output of 0.82 or +1

Normalization of signal and background before training

- Balanced classes: same total weight for signal and background events ($p = 0.5$, maximal mixing)

Selection of splits

- list of questions ($variable_i < cut_i?$, “Is jet b -tagged?”)
- goodness of split (separation measure)

Decision to stop splitting (declare a node terminal)

- minimum leaf size (for statistical significance, e.g. 100 events)
- insufficient improvement from further splitting
- perfect classification (all events in leaf belong to same class)
- maximal tree depth (like-size trees choice or computing concerns)

Assignment of terminal node to a class

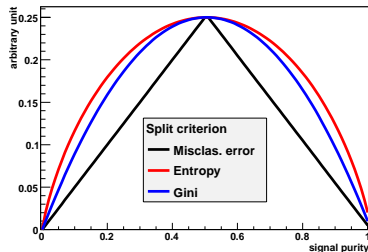
- signal leaf if purity > 0.5 , background otherwise

Optimal split: figure of merit

- Decrease of impurity for split s of node t into children t_P and t_F (goodness of split): $\Delta i(s, t) = i(t) - p_P \cdot i(t_P) - p_F \cdot i(t_F)$
- Aim: find split s^* such that $\Delta i(s^*, t) = \max_{s \in \{\text{splits}\}} \Delta i(s, t)$
- Maximising $\Delta i(s, t) \equiv$ minimising overall tree impurity

Common impurity functions

- misclassification error
 $= 1 - \max(p, 1 - p)$
- (cross) entropy
 $= -\sum_{i=s,b} p_i \log p_i$
- Gini index



- Also cross section $(-\frac{s^2}{s+b})$ and excess significance $(-\frac{s^2}{b})$

Reminder

- Need model giving good description of data

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Playing with variables

- Number of variables:
 - not affected too much by “curse of dimensionality”
 - CPU consumption scales as $nN \log N$ with n variables and N training events
- Variable order does not matter: all variables treated equal
- Order of training events is irrelevant (batch training)
- Irrelevant variables:
 - no discriminative power \Rightarrow not used
 - only costs a little CPU time, no added noise
- Can use continuous and discrete variables, simultaneously

Transforming input variables

- Completely insensitive to replacement of any subset of input variables by (possibly different) arbitrary strictly monotone functions of them (same order \Rightarrow same DT):
 - convert MeV \rightarrow GeV
 - no need to make all variables fit in the same range
 - no need to regularise variables (e.g. taking the log)

\Rightarrow Some immunity against outliers

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Note about actual implementation

- The above is strictly true only if testing all possible cut values
- If there is some computational optimisation (e.g., check only 20 possible cuts on each variable), it may not work anymore

Variable ranking (mean decrease impurity MDI)

- Ranking of x_i : add up decrease of impurity each time x_i is used
- Largest decrease of impurity = best variable

Shortcoming: masking of variables

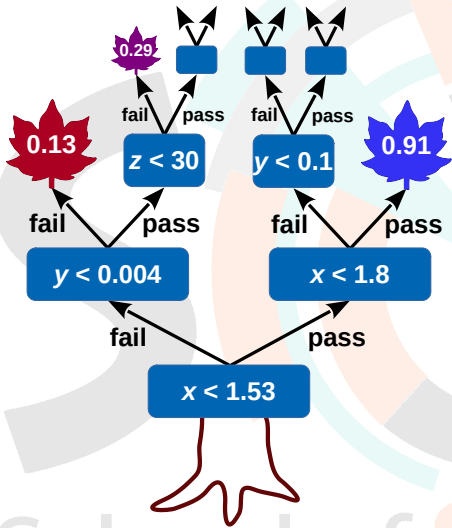
- x_j may be just a little worse than x_i but will never be picked
 - x_j is ranked as irrelevant
 - But remove x_i and x_j becomes very relevant
- ⇒ careful with interpreting ranking (specific to training)

Permutation importance (mean decrease accuracy MDA)

- Applicable to any already trained classifier
- Randomly shuffle each variable in turn and measure decrease of performance
- Important variable ⇒ big loss of performance
- Can also be performed on validation sample
- Beware of correlations

Choosing variables

- Usually try to have as few variables as possible
- But difficult: correlations, possibly large number to consider, large phase space with different properties in different regions
- *Brute force*: with n variables train all n , $n - 1$, etc. combinations, pick best
- *Backward elimination*: train with n variables, then train all $n - 1$ variables trees and pick best one; now train all $n - 2$ variables trees starting from the $n - 1$ variable list; etc. Pick optimal cost-complexity tree.
- *Forward greedy selection*: start with $k = 1$ variable, then train all $k + 1$ variables trees and pick the best; move to $k + 2$ variables; etc.



2 Limitations

- Training sample composition
- Pruning a tree
- Ensemble learning

- Small changes in sample can lead to very different tree structures (high variance)
- Performance on testing events may be as good, or not
- Not optimal to understand data from DT rules
- Does not give confidence in result:
 - DT output distribution discrete by nature
 - granularity related to tree complexity
 - tendency to have spikes at certain purity values (or just two delta functions at ± 1 if not using purity)

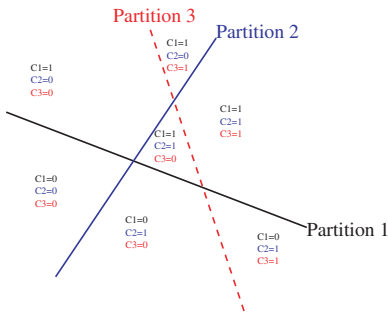
Why prune a tree?

- Possible to get a perfect classifier on training events
- Mathematically misclassification error can be made as little as wanted
- E.g. tree with one class only per leaf (down to 1 event per leaf if necessary)
- Training error is zero
- But run new independent events through tree (testing or validation sample): misclassification is probably > 0 , overtraining
- Pruning: eliminate subtrees (branches) that seem too specific to training sample:
 - a node and all its descendants turn into a leaf

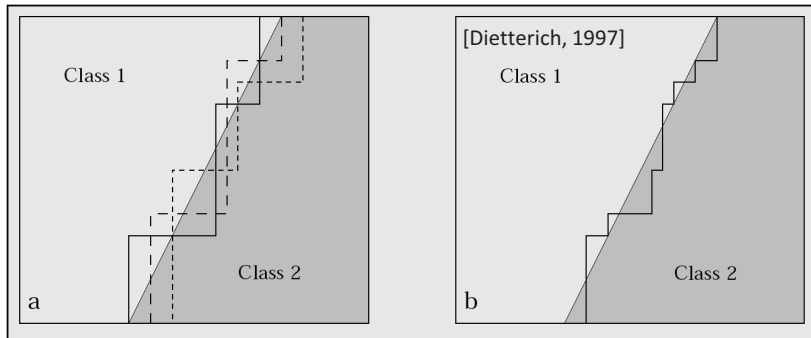
Pruning algorithms (details in [▶ backup](#))

- Pre-pruning (early stopping condition like min leaf size, max depth)
- Expected error pruning (based on statistical error estimate)
- Cost-complexity pruning (penalise “complex” trees with many nodes/leaves)

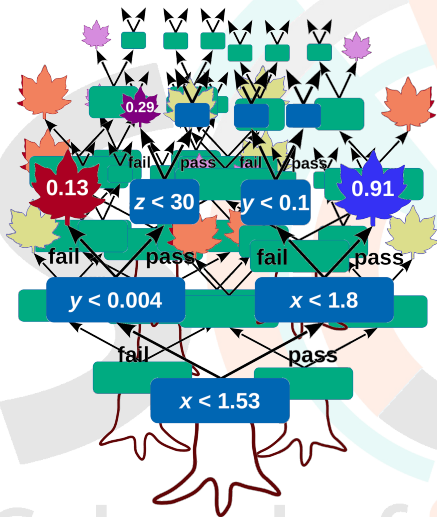
- One tree:
 - one information about event (one leaf)
 - cannot really generalise to variations not covered in training set (at most as many leaves as input size)
- Many trees:
 - **distributed representation**: number of intersections of leaves exponential in number of trees
 - many leaves contain the event \Rightarrow richer description of input pattern



- Build several trees and average the output



- K-fold cross-validation (good for small samples)
 - divide training sample \mathcal{L} in K subsets of equal size: $\mathcal{L} = \bigcup_{k=1..K} \mathcal{L}_k$
 - Train tree T_k on $\mathcal{L} - \mathcal{L}_k$, test on \mathcal{L}_k
 - DT output = $\frac{1}{K} \sum_{k=1..K} T_k$
- Bagging, boosting, random forests: **ensemble learning**



3 Boosted decision trees

- Introduction
- AdaBoost
- Figures of merit
- Clues to boosting performance
- Gradient boosting
- Other averaging techniques
- Performance examples
- BDT usage in HEP

First provable algorithm [Schapire 1990]

- Train classifier T_1 on N events
- Train T_2 on new N -sample, half of which misclassified by T_1
- Build T_3 on events where T_1 and T_2 disagree
- Boosted classifier: $\text{MajorityVote}(T_1, T_2, T_3)$

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Then

- Variation [Freund 1995]: boost by majority (combining many learners with fixed error rate)
- Freund&Schapire joined forces: 1st functional model **AdaBoost** (1996)

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When it really picked up in HEP

- MiniBooNe compared performance of different boosting algorithms and neural networks for particle ID [MiniBooNe 2005]
- D0 claimed first evidence for single top quark production [D0 2006]
- CDF copied 😊 (2008). Both used BDT for single top observation

What is boosting?

- General method, not limited to decision trees
- Hard to make a very good learner, but easy to make simple, error-prone ones (but still better than random guessing)
- Goal: combine such weak classifiers into a new more stable one, with smaller error

AdaBoost

- Introduced by Freund&Schapire in 1996
- Stands for *adaptive boosting*
- Learning procedure adjusts to training data to classify it better
- Many variations on the same theme for actual implementation
- Usually leads to better results than without boosting

- Check which events of training sample \mathbb{T}_k are misclassified by T_k :
 - $\mathbb{I}(X) = 1$ if X is true, 0 otherwise
 - for DT output in $\{\pm 1\}$: $\text{isMisclassified}_k(i) = \mathbb{I}(y_i \times T_k(x_i) \leq 0)$
 - or $\text{isMisclassified}_k(i) = \mathbb{I}(y_i \times (T_k(x_i) - 0.5) \leq 0)$ in purity convention
 - misclassification rate:

$$R(T_k) = \varepsilon_k = \frac{\sum_{i=1}^N w_i^k \times \text{isMisclassified}_k(i)}{\sum_{i=1}^N w_i^k}$$

- Derive tree weight $\alpha_k = \beta \times \ln((1 - \varepsilon_k)/\varepsilon_k)$
- Increase weight of misclassified events in \mathbb{T}_k to create \mathbb{T}_{k+1} :

$$w_i^k \rightarrow w_i^{k+1} = w_i^k \times e^{\alpha_k}$$

- Train T_{k+1} on \mathbb{T}_{k+1}
- Boosted result of event i :

$$T(i) = \frac{1}{\sum_{k=1}^{N_{\text{tree}}} \alpha_k} \sum_{k=1}^{N_{\text{tree}}} \alpha_k T_k(i)$$

Misclassification rate ε on training sample

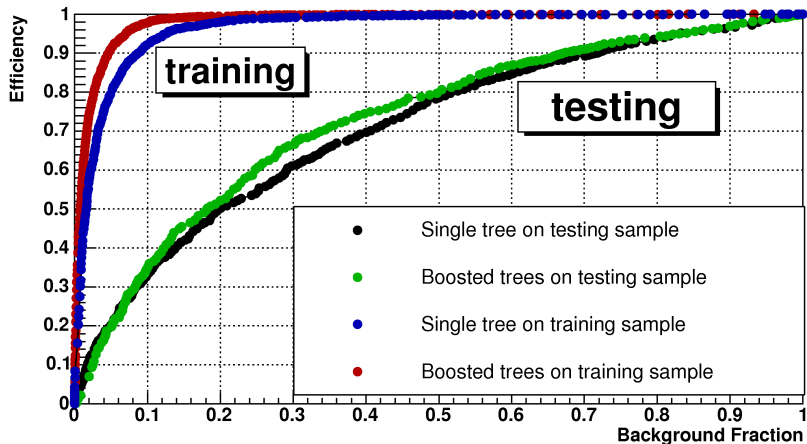
- Can be shown to be bound:

$$\varepsilon \leq \prod_{k=1}^{N_{tree}} 2\sqrt{\varepsilon_k(1 - \varepsilon_k)}$$
- If each tree has $\varepsilon_k \neq 0.5$ (i.e. better than random guessing):
the error rate falls to zero for sufficiently large N_{tree}
- Corollary: training data is overfitted

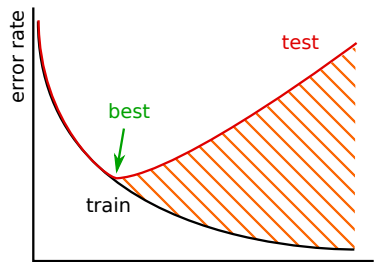
Overtraining?

- Error rate on test sample may reach a minimum and then potentially rise. Stop boosting at the minimum.
- In principle AdaBoost *must* overfit training sample
- In many cases in literature, no loss of performance due to overtraining
 - may have to do with fact that successive trees get in general smaller and smaller weights
 - trees that lead to overtraining contribute very little to final DT output on validation sample

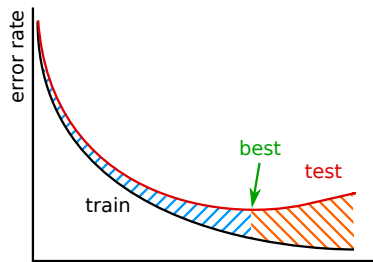
Efficiency vs. background fraction



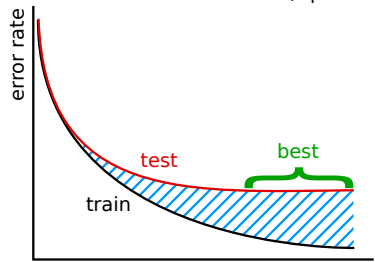
- Clear overtraining, but still better performance after boosting



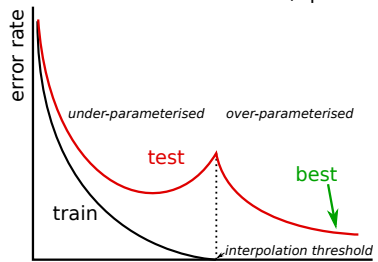
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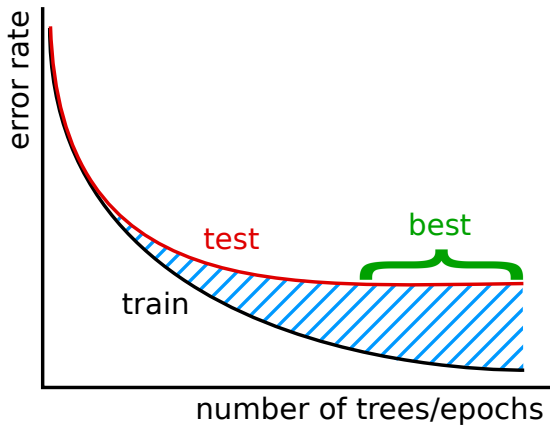
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“bad” overtraining (overfitting) / “good” overtraining (still underfitting)

- Typical situation for boosted decision trees

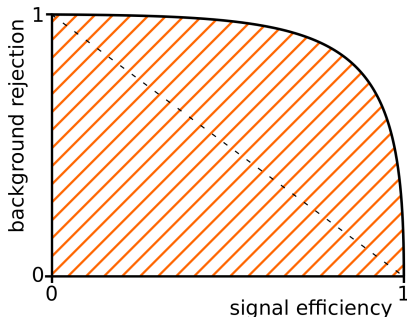


“bad” overtraining (overfitting) / “good” overtraining (still underfitting)

- Common in ML: **accuracy** = fraction of correctly classified samples
 - not appropriate with imbalanced classes

- Receiver operating characteristic (ROC)

- true positive rate vs. false positive rate
- ... or equivalently signal efficiency vs background efficiency
- can also replace bkg efficiency by bkg rejection (1 - bkg efficiency)
- Measure: **area under the curve (AUC)**



- **Excess significance** s/\sqrt{b} and **cross-section significance** $s/\sqrt{s+b}$

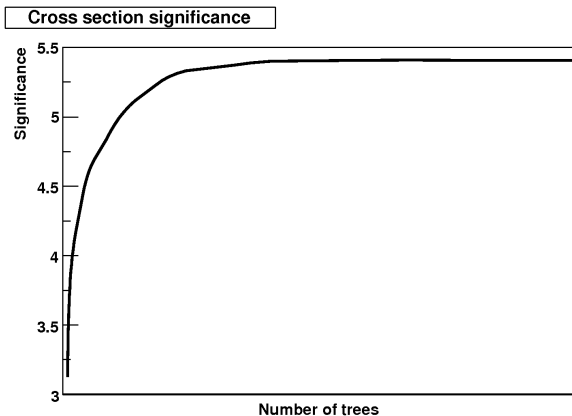
- Better: **approximate median significance** ($\approx s/\sqrt{b}$ for $s \ll b$):

$$\text{AMS} = \sqrt{2 \left((s + b) \ln \left(1 + \frac{s}{b} \right) - s \right)}$$

- Adding background uncertainty $b \rightarrow b \pm \sigma$ (observing n):

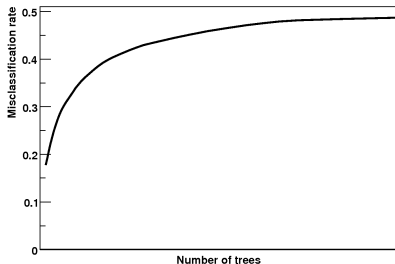
$$Z = \begin{cases} +\sqrt{2 \left(n \ln \left[\frac{n(b+\sigma^2)}{b^2+n\sigma^2} \right] - \frac{b^2}{\sigma^2} \ln \left[1 + \frac{\sigma^2(n-b)}{b(b+\sigma^2)} \right] \right)} & \text{if } n \geq b \\ -\sqrt{2 \left(n \ln \left[\frac{n(b+\sigma^2)}{b^2+n\sigma^2} \right] - \frac{b^2}{\sigma^2} \ln \left[1 + \frac{\sigma^2(n-b)}{b(b+\sigma^2)} \right] \right)} & \text{if } n < b \end{cases}$$

- simplifies to AMS for vanishing uncertainty ($\sigma = 0$)
 - recommended by ATLAS collaboration [▶ ATL-PHYS-PUB-2020-025](#)
- Simplifies to $s/\sqrt{b + \sigma^2}$ for $s \ll b$
- Many more metrics, see e.g. in [▶ scikit-learn documentation](#)

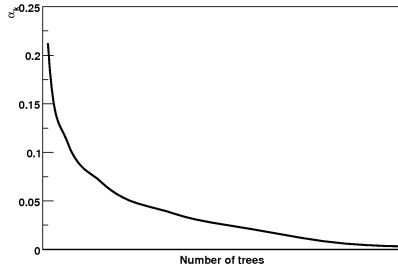


- More relevant than testing error
- Reaches plateau
- Afterwards, boosting does not hurt (just wasted CPU)
- Applicable to any other figure of merit of interest for your use case

Misclassification rate for each tree



Tree weight α_k



- First tree is best, others are minor corrections
- Specialised trees do not perform well on most events \Rightarrow decreasing tree weight and increasing misclassification rate
- Last tree is not better evolution of first tree, but rather a pretty bad DT that only does a good job on few cases that the other trees could not get right
- But adding trees may increase reliability of prediction: margins explanation [Shapire&Freund 2012]
- Double descent risk curve and interpolation regime [Belkin 2019]

- AdaBoost recast in a statistical framework: corresponds to minimising an exponential loss
- Generalisation: formulate boosting as numerical optimisation problem, minimise loss function by adding trees using gradient descent procedure
- Procedure:
 - Build imperfect model F_k at step k (sometimes $F_k(x) \neq y$)
 - Improve model: $F_{k+1}(x) = F_k(x) + h_k(x) = y$, or residual $h_k(x) = y - F_k(x)$
 - Train new classifier on residual
- Example: mean squared error loss function

$$L_{\text{MSE}}(x, y) = \frac{1}{2} (y - F_k(x))^2$$
 - minimising loss $J = \sum_i L_{\text{MSE}}(x_i, y_i)$ leads to $\frac{\partial J}{\partial F_k(x_i)} = F_k(x_i) - y_i$
 \Rightarrow residual as negative gradient: $h_k(x_i) = y_i - F_k(x_i) = -\frac{\partial J}{\partial F_k(x_i)}$
- Generalised to any differentiable loss function

Bagging (Bootstrap aggregating)

[Breiman 1996]

- Before building tree T_k take random sample of N events from training sample with replacement
- Train T_k on it
- Events not picked form “out of bag” validation sample
- Applicable to other techniques than DT
 - tends to produce more stable and better classifier

Bagging (Bootstrap aggregating)

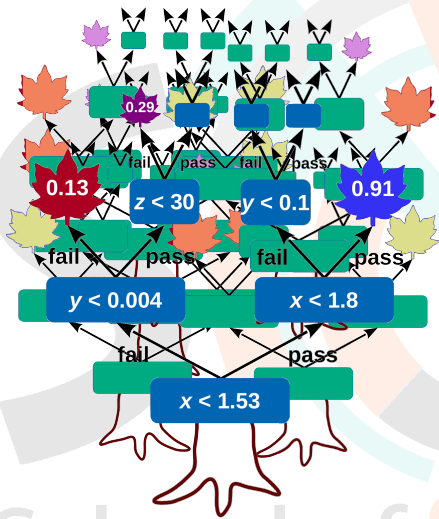
[Breiman 1996]

- Before building tree T_k take random sample of N events from training sample with replacement
- Train T_k on it
- Events not picked form “out of bag” validation sample
- Applicable to other techniques than DT
 - tends to produce more stable and better classifier

Random forests

[Breiman 2001]

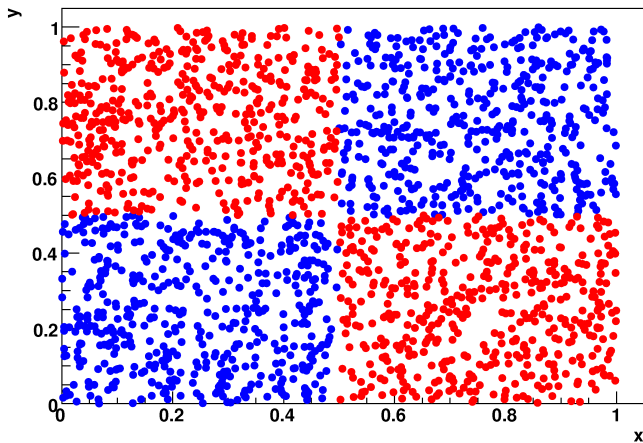
- Same as bagging
- In addition, pick random subset of variables to consider for each node split
- Two levels of randomisation, much more stable output
- Often as good as boosting

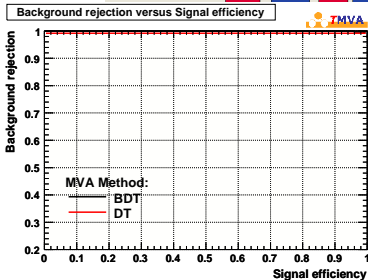
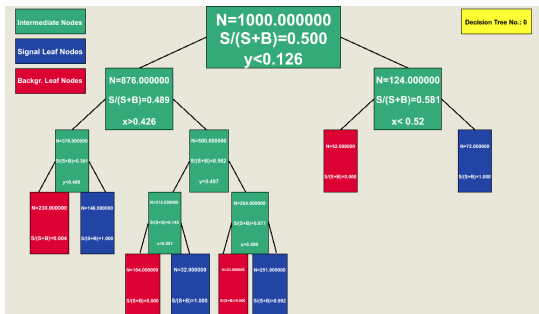
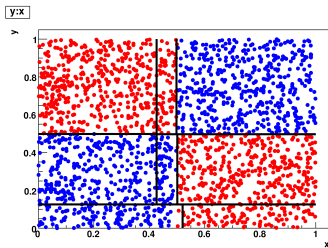


3 Boosted decision trees

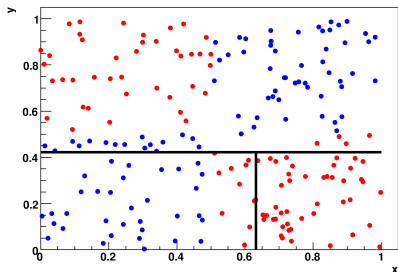
- Performance examples
 - XOR problem
 - Boosting longer
 - Many small trees or fewer large trees?

y:x





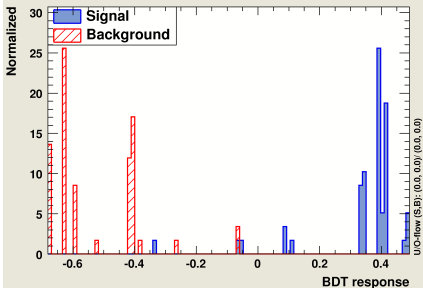
y:x



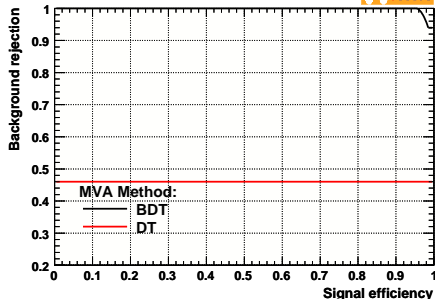
Small statistics

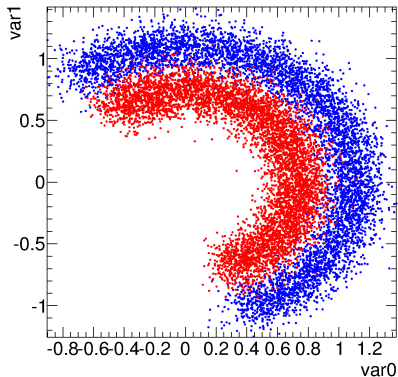
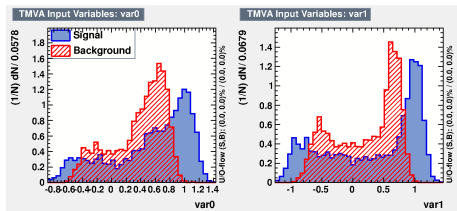
- Single tree not so good
- BDT very good: high performance discriminant from combination of weak classifiers

TMVA response for classifier: BDT

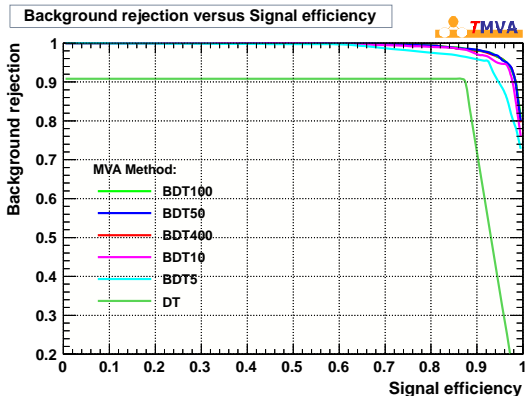


Background rejection versus Signal efficiency

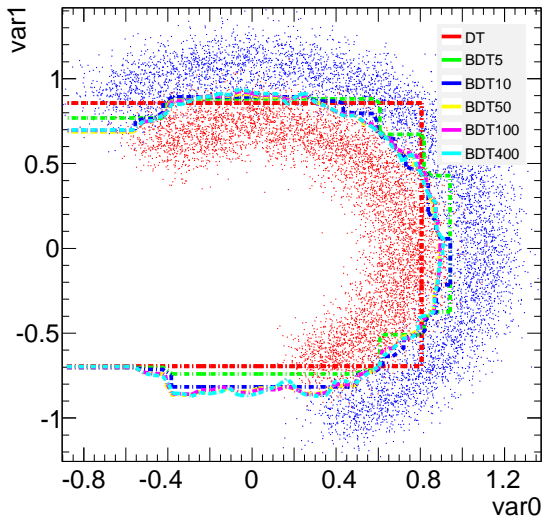




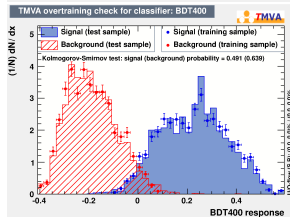
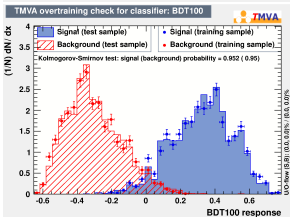
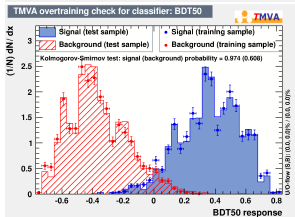
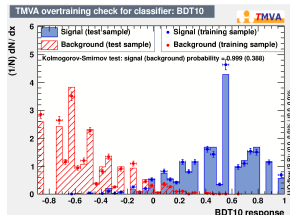
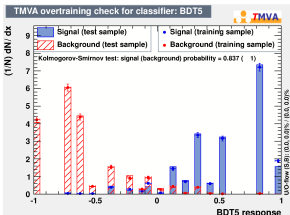
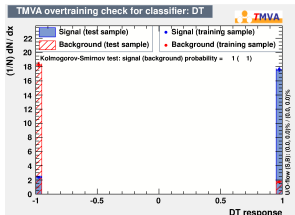
- Compare performance of single DT and BDT with more and more trees (5 to 400)
- All other parameters unchanged



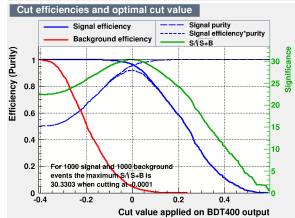
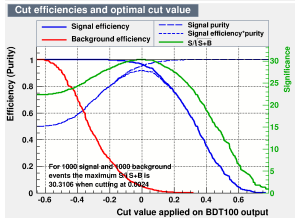
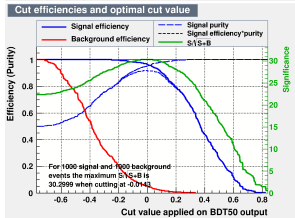
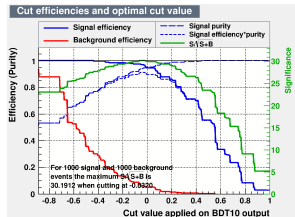
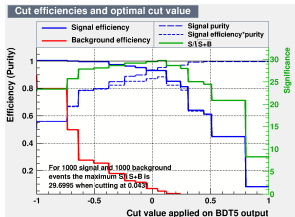
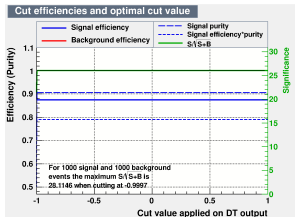
- Single (small) DT: not so good
- More trees \Rightarrow improve performance until saturation



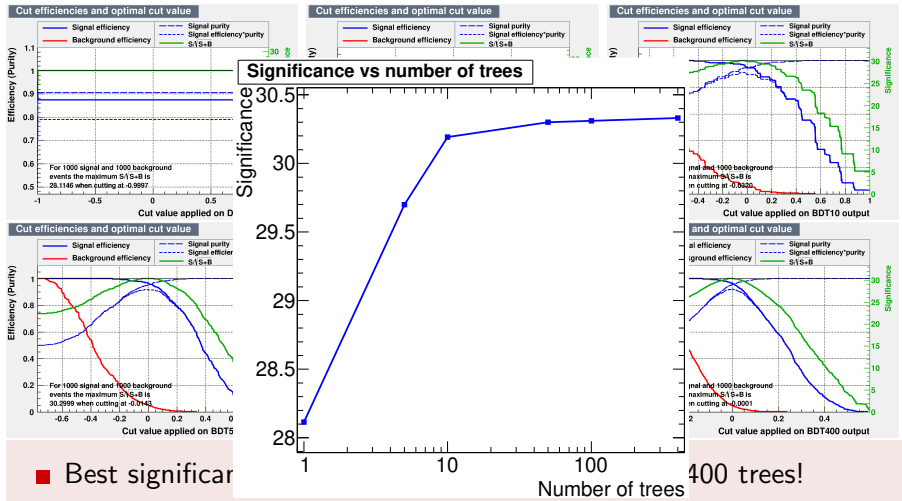
- Note: max tree depth = 3
- Single (small) DT: not so good. Note: a larger tree would solve this problem
- More trees \Rightarrow improve performance (less step-like, closer to optimal separation) until saturation
- Largest BDTs: wiggle a little around the contour \Rightarrow picked up features of training sample, that is, overtraining



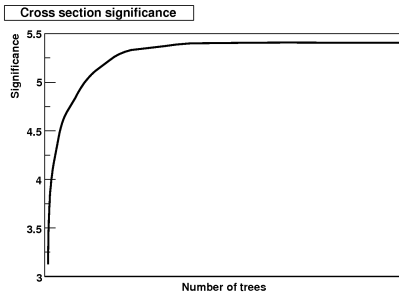
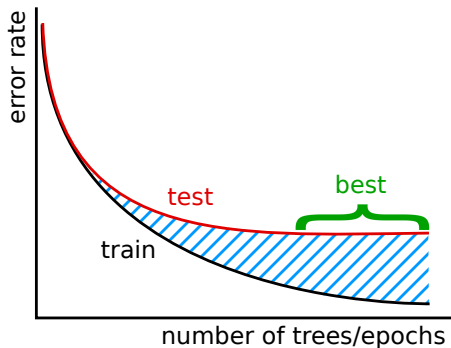
- Better shape with more trees: quasi-continuous
- Overtraining because of disagreement between training and testing?
Let's see. . .



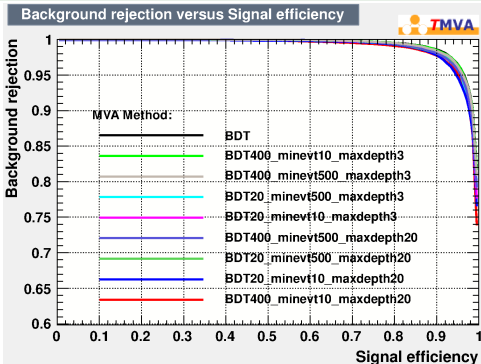
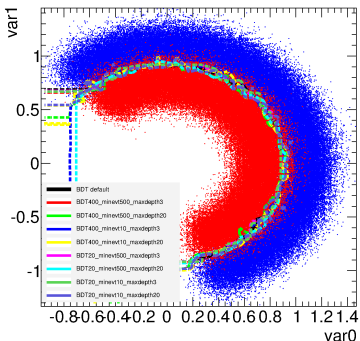
- Best significance actually obtained with last BDT, 400 trees!
- But to be fair, equivalent performance with 10 trees already
- Less “stepped” output desirable? \Rightarrow maybe 50 is reasonable



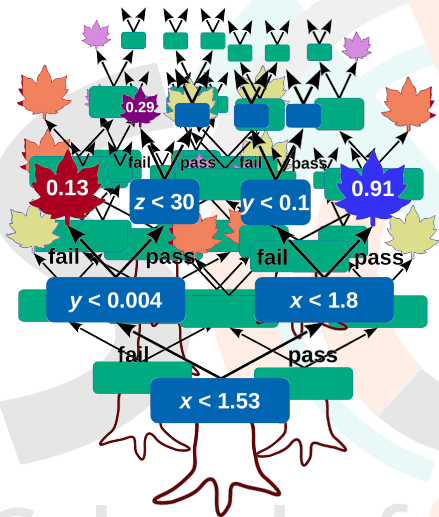
- Best significant
- But to be fair, equivalent performance with 10 trees already
- Less “stepped” output desirable? ⇒ maybe 50 is reasonable



- Generating larger dataset to avoid stats limitations
- 20 or 400 trees; minimum leaf size: 10 or 500 events
- Maximum depth (max # of cuts to reach leaf): 3 or 20



■ Overall: very comparable performance. Depends on use case.



3 Boosted decision trees

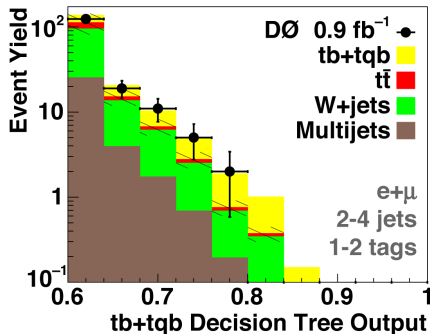
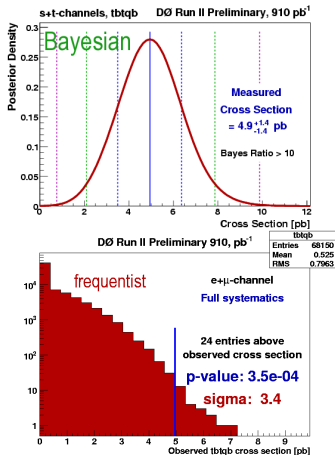
- BDT usage in HEP
 - Single top search at D0
 - LHC examples
 - BDT and systematics

- Three multivariate techniques: BDT, Matrix Elements, BNN
- Most sensitive: BDT

$$\sigma_{s+t} = 4.9 \pm 1.4 \text{ pb}$$

$$p\text{-value} = 0.035\% (3.4\sigma)$$

$$\text{SM compatibility: } 11\% (1.3\sigma)$$



$$\sigma_s = 1.0 \pm 0.9 \text{ pb}$$

$$\sigma_t = 4.2^{+1.8}_{-1.4} \text{ pb}$$

► Phys. Rev. D78, 012005 (2008)

Object Kinematics

$p_T(\text{jet1})$
 $p_T(\text{jet2})$
 $p_T(\text{jet3})$
 $p_T(\text{jet4})$
 $p_T(\text{best1})$
 $p_T(\text{notbest1})$
 $p_T(\text{notbest2})$
 $p_T(\text{tag1})$
 $p_T(\text{untag1})$
 $p_T(\text{untag2})$

Angular Correlations

$\Delta R(\text{jet1}, \text{jet2})$
 $\cos(\text{best1}, \text{lepton})_{\text{besttop}}$
 $\cos(\text{best1}, \text{notbest1})_{\text{besttop}}$
 $\cos(\text{tag1}, \text{alljets})_{\text{alljets}}$
 $\cos(\text{tag1}, \text{lepton})_{\text{btaggedtop}}$
 $\cos(\text{jet1}, \text{alljets})_{\text{alljets}}$
 $\cos(\text{jet1}, \text{lepton})_{\text{btaggedtop}}$
 $\cos(\text{jet2}, \text{alljets})_{\text{alljets}}$
 $\cos(\text{jet2}, \text{lepton})_{\text{btaggedtop}}$
 $\cos(\text{lepton}, Q(\text{lepton}) \times z)_{\text{besttop}}$
 $\cos(\text{lepton}_{\text{besttop}}, \text{besttop}_{\text{CMframe}})$
 $\cos(\text{lepton}_{\text{btaggedtop}}, \text{btaggedtop}_{\text{CMframe}})$
 $\cos(\text{notbest}, \text{alljets})_{\text{alljets}}$
 $\cos(\text{notbest}, \text{lepton})_{\text{besttop}}$
 $\cos(\text{untag1}, \text{alljets})_{\text{alljets}}$
 $\cos(\text{untag1}, \text{lepton})_{\text{btaggedtop}}$

Event Kinematics

$A_{\text{planarity}}(\text{alljets}, W)$
 $M(W, \text{best1})$ (“best” top mass)
 $M(W, \text{tag1})$ (“b-tagged” top mass)
 $H_T(\text{alljets})$
 $H_T(\text{alljets} - \text{best1})$
 $H_T(\text{alljets} - \text{tag1})$
 $H_T(\text{alljets}, W)$
 $H_T(\text{jet1}, \text{jet2})$
 $H_T(\text{jet1}, \text{jet2}, W)$
 $M(\text{alljets})$
 $M(\text{alljets} - \text{best1})$
 $M(\text{alljets} - \text{tag1})$
 $M(\text{jet1}, \text{jet2})$
 $M(\text{jet1}, \text{jet2}, W)$
 $M_T(\text{jet1}, \text{jet2})$
 $M_T(W)$
 $\text{Missing } E_T$
 $p_T(\text{alljets} - \text{best1})$
 $p_T(\text{alljets} - \text{tag1})$
 $p_T(\text{jet1}, \text{jet2})$
 $Q(\text{lepton}) \times \eta(\text{untag1})$
 \sqrt{s}
 $\text{Sphericity}(\text{alljets}, W)$

- Adding variables did not degrade performance
- Tested shorter lists, lost some sensitivity
- Same list used for all channels

Object Kinematics

$p_T(\text{jet1})$
 $p_T(\text{jet2})$
 $p_T(\text{jet3})$
 $p_T(\text{jet4})$
 $p_T(\text{best1})$
 $p_T(\text{notbest1})$
 $p_T(\text{notbest2})$
 $p_T(\text{tag1})$
 $p_T(\text{untag1})$
 $p_T(\text{untag2})$

Angular Correlations

$\Delta R(\text{jet1}, \text{jet2})$
 $\cos(\text{best1}, \text{lepton})_{\text{besttop}}$
 $\cos(\text{best1}, \text{notbest1})_{\text{besttop}}$
 $\cos(\text{tag1}, \text{alljets})_{\text{alljets}}$
 $\cos(\text{tag1}, \text{lepton})_{\text{btagedtop}}$
 $\cos(\text{jet1}, \text{alljets})_{\text{alljets}}$
 $\cos(\text{jet1}, \text{lepton})_{\text{btagedtop}}$
 $\cos(\text{jet2}, \text{alljets})_{\text{alljets}}$
 $\cos(\text{jet2}, \text{lepton})_{\text{btagedtop}}$
 $\cos(\text{lepton}, Q(\text{lepton}) \times z)_{\text{besttop}}$
 $\cos(\text{lepton}_{\text{besttop}}, \text{besttop})_{\text{CMframe}}$
 $\cos(\text{lepton}_{\text{btagedtop}}, \text{btagedtop})_{\text{CMframe}}$
 $\cos(\text{notbest}, \text{alljets})_{\text{alljets}}$
 $\cos(\text{notbest}, \text{lepton})_{\text{besttop}}$
 $\cos(\text{untag1}, \text{alljets})_{\text{alljets}}$
 $\cos(\text{untag1}, \text{lepton})_{\text{btagedtop}}$

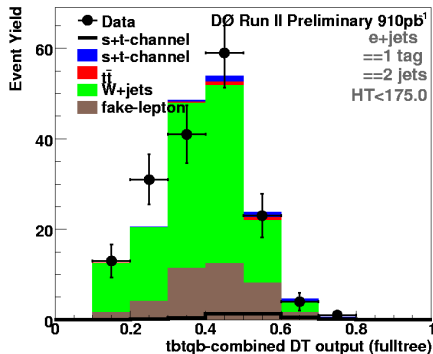
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 $H_T(\text{alljets})$
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 $H_T(\text{alljets} - \text{tag1})$
 $H_T(\text{alljets}, W)$
 $H_T(\text{jet1}, \text{jet2})$
 $H_T(\text{jet1}, \text{jet2}, W)$
 $M(\text{alljets})$
 $M(\text{alljets} - \text{best1})$
 $M(\text{alljets} - \text{tag1})$
 $M(\text{jet1}, \text{jet2})$
 $M(\text{jet1}, \text{jet2}, W)$
 $M_T(\text{jet1}, \text{jet2})$
 $M_T(W)$
 $\text{Missing } E_T$
 $p_T(\text{alljets} - \text{best1})$
 $p_T(\text{alljets} - \text{tag1})$
 $p_T(\text{jet1}, \text{jet2})$
 $Q(\text{lepton}) \times \eta(\text{untag1})$
 \sqrt{s}
 $\text{Sphericity}(\text{alljets}, W)$

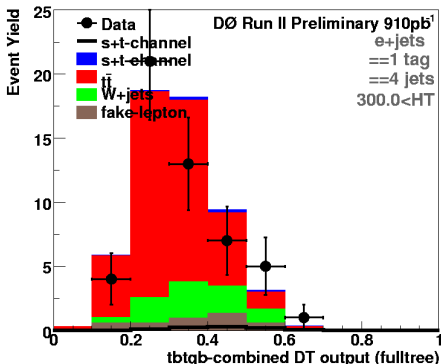
- Adding variables did not degrade performance
- Tested shorter lists, lost some sensitivity
- Same list used for all channels
- Best theoretical variable:
 $H_T(\text{alljets}, W)$.
 But detector not perfect \Rightarrow capture the essence from several variations usually helps “dumb” MVA

- Validate method on data in no-signal region

- **“W+jets”**: = 2 jets,
 $H_T(\text{lepton}, E_T^{\text{miss}}, \text{alljets}) < 175 \text{ GeV}$

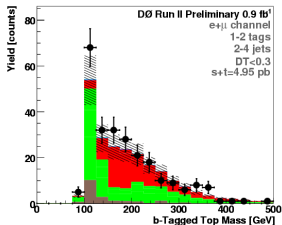


- **“ttbar”**: = 4 jets,
 $H_T(\text{lepton}, E_T^{\text{miss}}, \text{alljets}) > 300 \text{ GeV}$

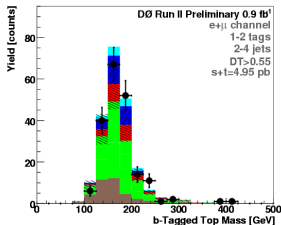


- Good agreement

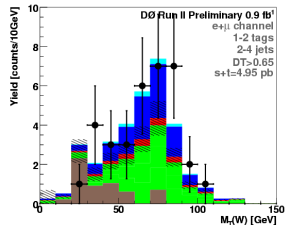
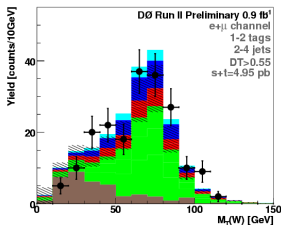
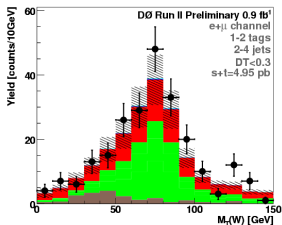
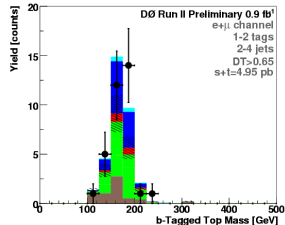
$DT < 0.3$



$DT > 0.55$

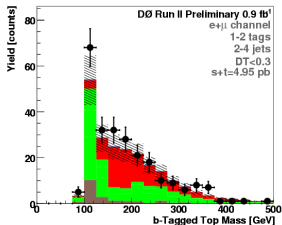


$DT > 0.65$

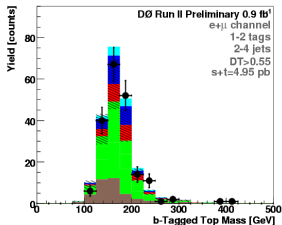


- High BDT region = shows masses of real t and $W \Rightarrow$ expected
- Low BDT region = background-like \Rightarrow expected

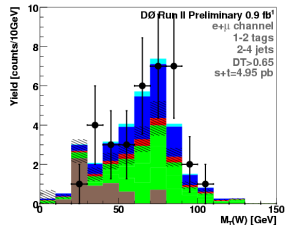
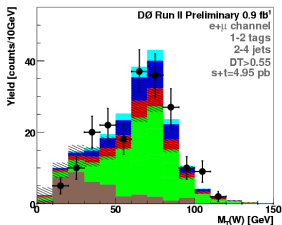
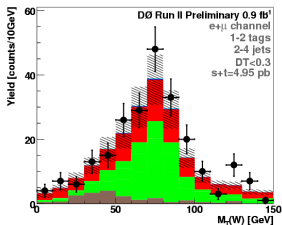
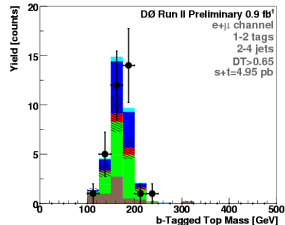
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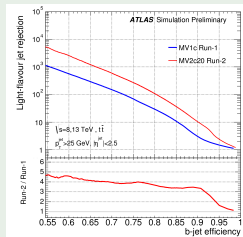


- High BDT region = shows masses of real t and W \Rightarrow expected
- Low BDT region = background-like \Rightarrow expected
- Above does NOT tell analysis is ok, but not seeing this could be a sign of a problem

ATLAS b -tagging in Run 2

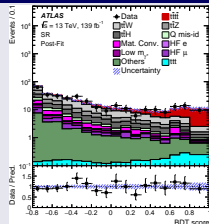
► Eur. Phys. J. C 79 (2019) 970

- Run 1 MV1c: NN trained from output of other taggers
- Run 2 MV2c20: BDT using feature variables of underlying algorithms and p_T , η of jets
- Run 2: introduced IBL (new innermost pixel layer)
 - ⇒ explains part of the performance gain, but not all



ATLAS $t\bar{t}t\bar{t}$ production evidence

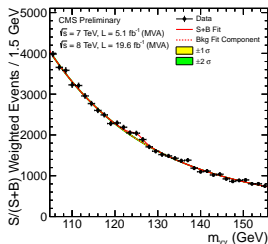
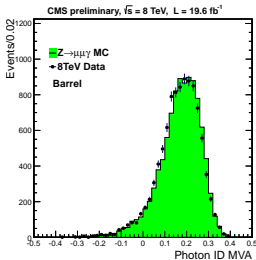
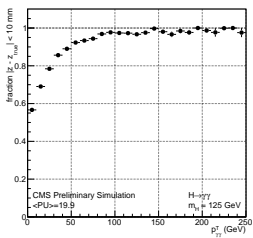
- ► Eur. Phys. J. C 80 (2020) 1085
- ► arXiv:2007.14858 [hep-ex]
- BDT output used in final fit to measure cross section
- Constraints on systematic uncertainties from profiling



► CMS-PAS-HIG-13-001

Hard to use more BDT in an analysis:

- vertex selected with BDT
- 2nd vertex BDT to estimate probability to be within 1cm of interaction point
- photon ID with BDT
- photon energy corrected with BDT regression
- event-by-event energy uncertainty from another BDT
- several BDT to extract signal in different categories

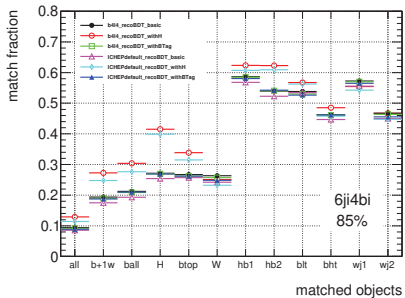
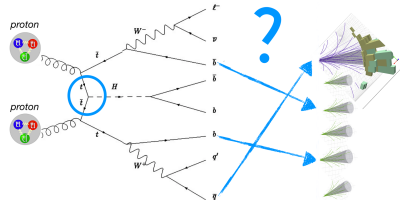


$t\bar{t}H(b\bar{b})$ reconstruction

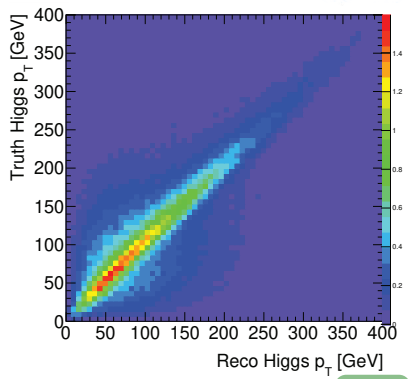
- Match jets and partons in high-multiplicity final state
- BDT trained on all combinations
- New inputs to classification BDT
- Access to Higgs p_T , origin of b -jets

► Phys. Rev. D 97, 072016 (2018)

► arXiv:2111.06712 [hep-ex]

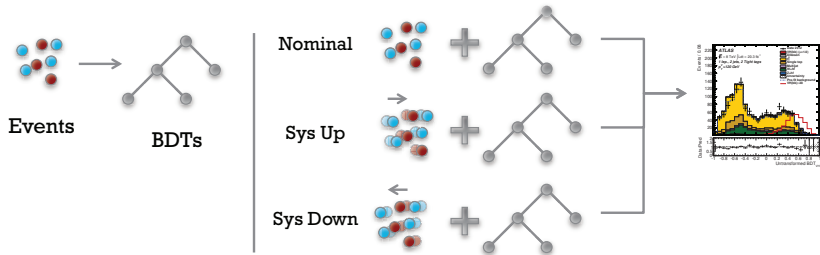


► thesis

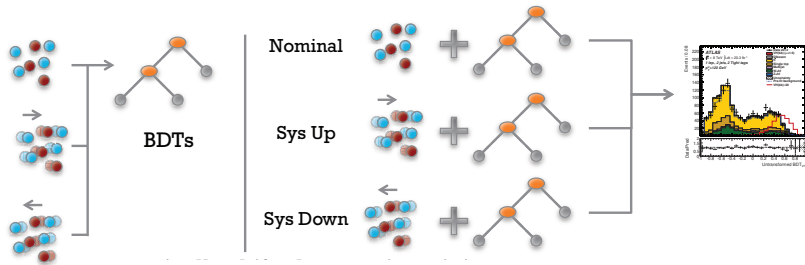


► thesis

- No particular rule
- BDT output can be considered as any other cut variable (just more powerful). Evaluate systematics by:
 - varying cut value
 - retraining
 - calibrating, etc.
- Most common (and appropriate): propagate other uncertainties (detector, theory, etc.) up to BDT output and check how much the analysis is affected
- More and more common: profiling.
Watch out:
 - BDT output powerful
 - signal region (high BDT output) probably low statistics
⇒ **potential recipe for disaster if modelling is not good**
- May require extra systematics, not so much on technique itself, but because it probes specific corners of phase space and/or wider parameter space (usually loosening pre-BDT selection cuts)

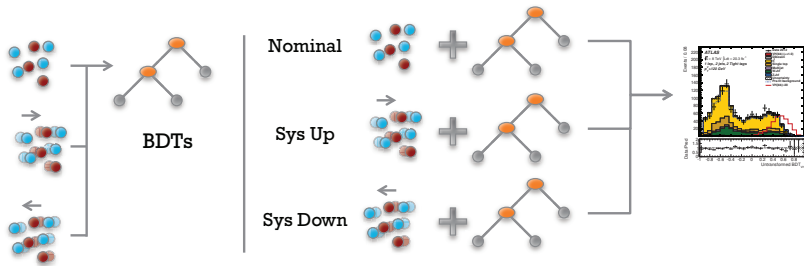


S. Hageböck

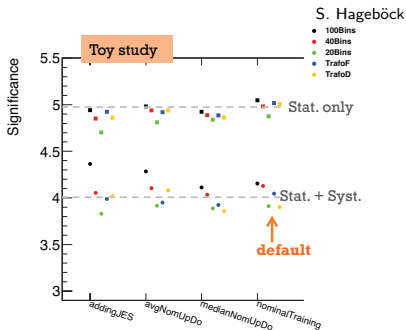


S. Hageböck

- Hope: seeing systematics-affected events during training may make the BDT less sensitive to systematic effects (data augmentation)



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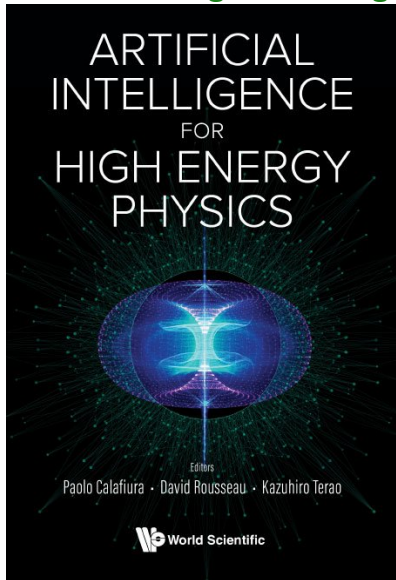
- PIDForest: Anomaly Detection via Partial Identification ▶ NeurIPS
- A Debiased MDI (Mean Decrease of Impurity) Feature Importance Measure for Random Forests ▶ NeurIPS
- MonoForest framework for tree ensemble analysis ▶ NeurIPS
- Faster Boosting with Smaller Memory (Yoav S Freund) ▶ NeurIPS
- Minimal Variance Sampling in Stochastic Gradient Boosting ▶ NeurIPS
- Regularized Gradient Boosting ▶ NeurIPS
- Partitioning Structure Learning for Segmented Linear Regression Trees ▶ NeurIPS
- Random Tessellation Forests ▶ NeurIPS
- Optimal Sparse Decision Trees ▶ NeurIPS
- Provably robust boosted decision stumps and trees against adversarial attacks ▶ NeurIPS
- Robustness Verification of Tree-based Models ▶ NeurIPS

- Go for a fully integrated solution
 - use different multivariate techniques easily
 - **spend your time on understanding your data and model**
- Examples:
 - **TMVA** (Toolkit for MultiVariate Analysis)
Integrated in ROOT, complete manual [▶ https://root.cern/tmva](https://root.cern/tmva)
 - scikit-learn (python) [▶ http://scikit-learn.org](http://scikit-learn.org)
- Dedicated to BDT (python):
 - XGBoost (popular in HEP) [▶ arXiv:1603.02754](https://arxiv.org/abs/1603.02754) [▶ https://github.com/dmlc/xgboost](https://github.com/dmlc/xgboost)
(note: cannot handle negative weights)
 - LightGBM (Microsoft) [▶ https://lightgbm.readthedocs.io](https://lightgbm.readthedocs.io)
 - CatBoost (Yandex) [▶ https://catboost.ai/](https://catboost.ai/)

- Decision trees: natural extension to cut-based analysis
- Greatly improved performance with boosting (and also with bagging, random forests)
- Very common in HEP results (soon has-been?)
 - often using TMVA in ROOT or python (see [▶ backup](#))
 - more and more with XGBoost, LightGBM, etc. (see hands-on)
- Possibly soon overpowered by deep learning algorithms, although trickier to optimise
- Whichever technique you use, expect a lot of scepticism: you will have to convince yourself and others that your advanced technique leads to meaningful and reliable results
 - ⇒ ensemble tests, use several techniques, compare to random grid search, etc. But DO NOT show them useless plots like BDT output on training and testing to measure overtraining, please!
- As with other advanced techniques,
no point in using them if data are not understood and well modelled

Artificial Intelligence for High Energy Physics

<https://doi.org/10.1142/12200>



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 - Boosted Decision Trees (Yann Coadou)
 - Deep Learning from Four Vectors (Pierre Baldi, Peter Sadowski and Daniel Whiteson)
 - Anomaly Detection for Physics Analysis and Less Than Supervised Learning (Benjamin Nachman)
- **Data Quality Monitoring:**
 - Data Quality Monitoring Anomaly Detection (Adrian Alan Pol, Gianluca Cerminara, Cecile Germain and Maurizio Pierini)
- **Generative Models:**
 - Generative Models for Fast Simulation (Michela Paganini, Luke de Oliveira, Benjamin Nachman, Denis Derkach, Fedor Ratnikov, Andrey Ustyuzhanin and Aishik Ghosh)
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 - Sequence-Based Learning (Rafael Teixeira de Lima)
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 - Bayesian Neural Networks (Tom Charnock, Laurence Perreault-Levasseur and François Lanusse)
 - Parton Distribution Functions (Stefano Forte and Stefano Carrazza)
- **Scientific Competitions and Open Datasets:**
 - Machine Learning Scientific Competitions and Datasets (David Rousseau and Andrey Ustyuzhanin)



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Y. Freund and R.E. Schapire, "Experiments with a New Boosting Algorithm" in *Machine Learning: Proceedings of the Thirteenth International Conference*, edited by L. Saitta (Morgan Kaufmann, San Fransisco, 1996) p. 148



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▶ *Journal of Japanese Society for Artificial Intelligence* 14 (1999) 771











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 B. P. Roe, H.-J. Yang, J. Zhu, Y. Liu, I. Stancu, and G. McGregor
 ▶ [Nucl. Instr. Meth. A 543 \(2005\) 577](#) ; H.-J. Yang, B.P. Roe, and J. Zhu
 ▶ [Nucl. Instr. Meth. A 555 \(2005\) 370](#)
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 V. M. Abazov *et al.* [D0 Collaboration], “Evidence for production of single top quarks” ▶ [Phys. Rev. D 78 \(2008\) 012005](#)

Backup

▶ Pruning a decision tree

▶ ML training with TMVA

Pre-pruning

- Stop tree growth during building phase
- Already seen: minimum leaf size, minimum separation improvement, maximum depth, etc.
- Careful: early stopping condition may prevent from discovering further useful splitting

Expected error pruning

- Grow full tree
- When result from children not significantly different from result of parent, prune children
- Can measure statistical error estimate with binomial error $\sqrt{p(1-p)/N}$ for node with purity p and N training events
- No need for testing sample
- Known to be “too aggressive”

- Idea: penalise “complex” trees (many nodes/leaves) and find compromise between good fit to training data (larger tree) and good generalisation properties (smaller tree)
- With misclassification rate $R(T)$ of subtree T (with N_T nodes) of fully grown tree T_{max} :
cost complexity $R_\alpha(T) = R(T) + \alpha N_T$
 $\alpha =$ complexity parameter
- Minimise $R_\alpha(T)$:
 - small α : pick T_{max}
 - large α : keep root node only, T_{max} fully pruned
- First-pass pruning, for terminal nodes t_L, t_R from split of t :
 - by construction $R(t) \geq R(t_L) + R(t_R)$
 - if $R(t) = R(t_L) + R(t_R)$ prune off t_L and t_R

- For node t and subtree T_t :
 - if t non-terminal, $R(t) > R(T_t)$ by construction
 - $R_\alpha(\{t\}) = R_\alpha(t) = R(t) + \alpha$ ($N_T = 1$)
 - if $R_\alpha(T_t) < R_\alpha(t)$ then branch has smaller cost-complexity than single node and should be kept
 - at critical $\alpha = \rho_t$, node is preferable
 - to find ρ_t , solve $R_{\rho_t}(T_t) = R_{\rho_t}(t)$, or:
$$\rho_t = \frac{R(t) - R(T_t)}{N_T - 1}$$
 - node with smallest ρ_t is *weakest link* and gets pruned
 - apply recursively till you get to the root node
 - This generates sequence of decreasing cost-complexity subtrees
 - Compute their true misclassification rate on validation sample:
 - will first decrease with cost-complexity
 - then goes through a minimum and increases again
 - pick this tree at the minimum as the best pruned tree
- Note: best pruned tree may not be optimal in a forest

- **TMVA**: Toolkit for MultiVariate Analysis

▶ <https://root.cern/tmva>

▶ <https://github.com/root-project/root/tree/master/tmva>

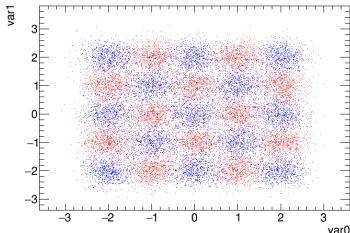
- Written by physicists
- In C++ (also python API), integrated in ROOT
- Quite complete manual
- Includes many different multivariate/machine learning techniques
- To compile, add appropriate header files in your code (e.g., `#include "TMVA/Factory.h"`) and this to your compiler command line:
`'root-config --cflags --libs' -lTMVA`
- More complete examples of code: `$ROOTSYS/tutorials/tmva`
 - `createData.C` macro to make example datasets
 - classification and regression macros
 - also includes Keras examples (deep learning)
- Sometimes useful performance measures (more in these headers):

```
#include "TMVA/ROCCalc.h"
TMVA::ROCCalc(TH1* S,TH1* B).GetROCIIntegral();
#include "TMVA/Tools.h"
TMVA::gTools().GetSeparation(TH1* S,TH1* B);
```

```
TFile* outputFile = TFile::Open("output.root", "RECREATE");  
TMVA::Factory *factory = new TMVA::Factory( "TMVAClassification", outputFile,  
      "!V:Color:DrawProgressBar:Transformations=I:AnalysisType=Classification");
```

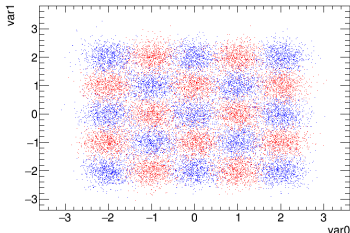
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double sigWeight = 1.0; double bkgWeight = 1.0;
TMVA::DataLoader *dataloader =
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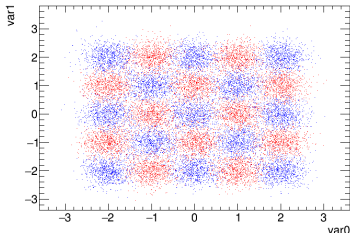
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dataloader->AddVariable("var1", 'F');
TCut mycut = "";
    
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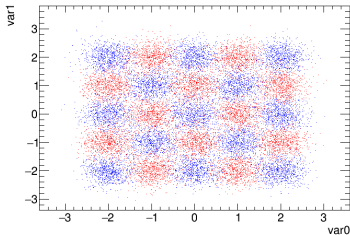
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TCut mycut = "";
dataloader->PrepareTrainingAndTestTree(mycut, "SplitMode=Random");
    
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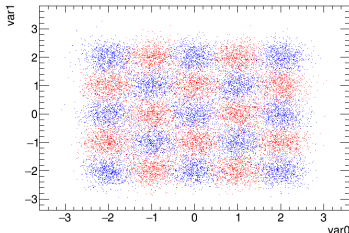

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dataloader->PrepareTrainingAndTestTree(mycut, "SplitMode=Random");
factory->BookMethod(dataloader, TMVA::Types::kBDT, "BDT", "!H:!V:NTrees=400:
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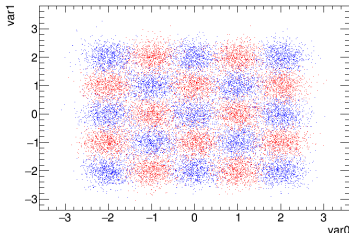
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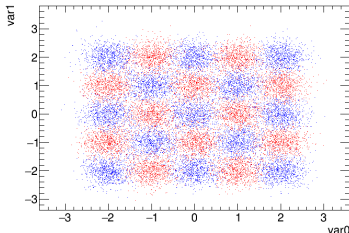
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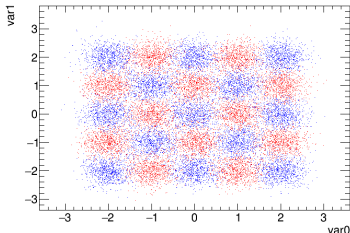
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factory->TrainAllMethods(); // Train MVAs using training events
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// ----- Evaluate and compare performance of all configured MVAs
factory->EvaluateAllMethods();
    
```



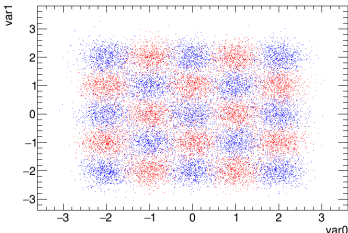
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factory->EvaluateAllMethods();
auto c1 = factory->GetROCCurve(dataloader); // Eager to compare performance
    
```



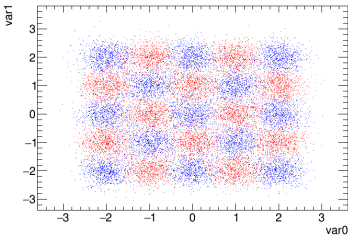
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factory->EvaluateAllMethods();
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outputFile->Close();
delete factory; delete dataloader;
    
```



```

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factory->BookMethod(dataloader, TMVA::Types::kFisher, "Fisher", "!H:!V:Fisher");
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factory->EvaluateAllMethods();
auto c1 = factory->GetROCCurve(dataloader); // Eager to compare performance
outputFile->Close();
delete factory; delete dataloader;
TMVA::TMVAGui("output.root");
    
```



```
TFile* inputFile = new TFile("dataSchachbrett.root");  
TTree* data = (TTree*)inputFile->Get("TreeS");  
Float_t var0=-99., var1=-99.;  
data->SetBranchAddress("var0", &var0);  
data->SetBranchAddress("var1", &var1);
```



```
TFile* inputFile = new TFile("dataSchachbrett.root");  
TTree* data = (TTree*)inputFile->Get("TreeS");  
Float_t var0=-99., var1=-99.;  
data->SetBranchAddress("var0", &var0);  
data->SetBranchAddress("var1", &var1);  
TMVA::Reader *reader = new TMVA::Reader();  
reader->AddVariable( "var0", &var0 );  
reader->AddVariable( "var1", &var1 );
```

```
TFile* inputFile = new TFile("dataSchachbrett.root");
TTree* data = (TTree*)inputFile->Get("TreeS");
Float_t var0=-99., var1=-99.;
data->SetBranchAddresses("var0", &var0);
data->SetBranchAddresses("var1", &var1);
TMVA::Reader *reader = new TMVA::Reader();
reader->AddVariable( "var0", &var0 );
reader->AddVariable( "var1", &var1 );
reader->BookMVA( "My BDT", "dataset/weights/TMVAClassification_BDT.weights.xml");
reader->BookMVA( "Fisher discriminant",
  "dataset/weights/TMVAClassification_Fisher.weights.xml");
```

```

TFile* inputFile = new TFile("dataSchachbrett.root");
TTree* data = (TTree*)inputFile->Get("TreeS");
Float_t var0=-99., var1=-99.;
data->SetBranchAddress("var0", &var0);
data->SetBranchAddress("var1", &var1);
TMVA::Reader *reader = new TMVA::Reader();
reader->AddVariable( "var0", &var0 );
reader->AddVariable( "var1", &var1 );
reader->BookMVA( "My BDT", "dataset/weights/TMVAClassification_BDT.weights.xml");
reader->BookMVA( "Fisher discriminant",
  "dataset/weights/TMVAClassification_Fisher.weights.xml");
// ----- start your event loop
for (Long64_t ievt=0; ievt<10; ++ievt) {
  data->GetEntry(ievt);
  double bdt = reader->EvaluateMVA("My BDT");
  double fisher = reader->EvaluateMVA("Fisher discriminant");
  cout<<"var0="<<var0<<" var1="<<var1<<" BDT="<<bdt<<" Fisher="<<fisher<<endl;
}
delete reader;
inputFile->Close();

```

```

TFile* inputFile = new TFile("dataSchachbrett.root");
TTree* data = (TTree*)inputFile->Get("TreeS");
Float_t var0=-99., var1=-99.;
data->SetBranchAddress("var0", &var0);
data->SetBranchAddress("var1", &var1);
TMVA::Reader *reader = new TMVA::Reader();
reader->AddVariable( "var0", &var0 );
reader->AddVariable( "var1", &var1 );
reader->BookMVA( "My BDT", "dataset/weights/TMVAClassification_BDT.weights.xml");
reader->BookMVA( "Fisher discriminant",
  "dataset/weights/TMVAClassification_Fisher.weights.xml");
// ----- start your event loop
for (Long64_t ievt=0; ievt<10; ++ievt) {
  data->GetEntry(ievt);
  double bdt = reader->EvaluateMVA("My BDT");
  double fisher = reader->EvaluateMVA("Fisher discriminant");
  cout<<"var0="<<var0<<" var1="<<var1<<" BDT="<<bdt<<" Fisher="<<fisher<<endl;
}
delete reader;
inputFile->Close();

```

- More complete tutorials:

▶ <https://github.com/lmoneta/tmva-tutorial>

- To make code compilable (and MUCH faster)
 - Need ROOT and TMVA corresponding header files
 - e.g., for Train.C:

```
#include "TFile.h"
#include "TTree.h"
#include "TMVA/Factory.h"
#include "TMVA/DataLoader.h"
#include "TMVA/TMVAGui.h"
```

- Need a “main” function

```
int main() {
    Train();
    return 0;
}
```

- Compilation:

```
g++ Train.C 'root-config --cflags --libs' -lTMVA -lTMVAGui -o TMVATrainer
```

- **Train.C**: file to compile
- **TMVATrainer**: name of executable
- **-lTMVAGui**: just because of `TMVA::TMVAGui("output.root");`

- Common technique: train on even event numbers, test on odd event numbers (and vice versa)
- Can also think of more than two-fold
- Achieve in TMVA by replacing:

```
dataloader->AddSignalTree(sig, sigWeight);  
dataloader->AddBackgroundTree(bkg, bkgWeight);
```

- with:

```
TString trainString = "(eventNumber % 2 == 0)";  
TString testString = "!" + trainString;  
dataloader->AddTree(sig, "Signal", sigWeight, trainString.Data(), "Training");  
dataloader->AddTree(sig, "Signal", sigWeight, testString.Data(), "Test");  
dataloader->AddTree(bkg, "Background", bkgWeight, trainString.Data(), "Training");  
dataloader->AddTree(bkg, "Background", bkgWeight, testString.Data(), "Test");
```

- Use individual event weights:

```
string eventWeight = "TMath::Abs(eventWeight)"; //Compute event weight  
dataloader->SetSignalWeightExpression(eventWeight);  
dataloader->SetBackgroundWeightExpression(eventWeight); //Can differ
```