

Recoil proton polarization in DVCS

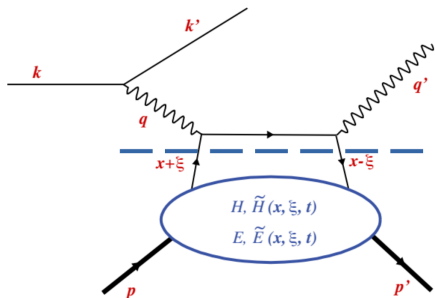
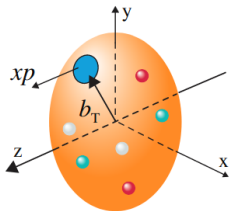
Assemblée General GDR QCD

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Proton structure and GPDs

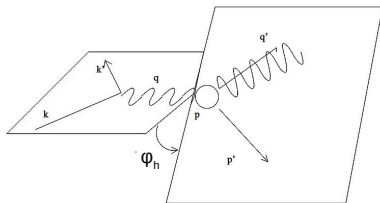
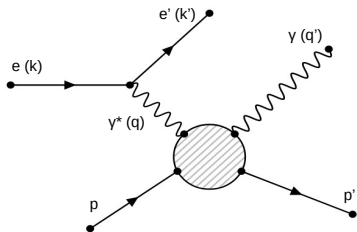


Generalized Parton Distributions (GPDs): nucleon structure in terms of longitudinal momentum & transverse position.

- Measured in exclusive processes like Deeply Virtual Compton Scattering (DVCS).

Factorization: splitting into perturbative hard part + non-perturbative soft part (GPDs).

GPDs are accessible through **Compton Form Factors (CFFs):** integrals over x - longitudinal momentum fraction of struck quark.



DVCS parameters

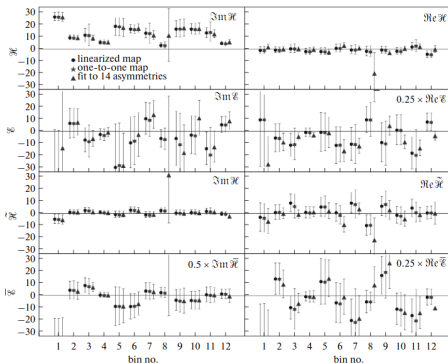
- E_k : beam energy.
- Q^2 : virtuality of the photon, $Q^2 = -q^2 = -(k - k')^2$.
- $x_B = \frac{Q^2}{2p \cdot q}$.
- t : 4-momentum transfer to the proton, $t = (p' - p)^2$
- ϕ_h : angle between the leptonic and hadronic planes.

These parameters determine the kinematics of the scattered particles.

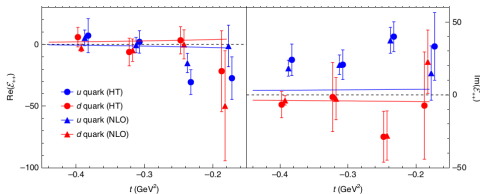
Measuring CFFs

Measurements outline

- \mathcal{H} : unpolarized target
- $\tilde{\mathcal{H}}$: longitudinally polarized target
- \mathcal{E} : transversely polarized target - challenge!
 - Gaseous transversely polarized target by HERMES (low luminosity).



Alternative: DVCS measurement on the neutron at Hall A, JLab



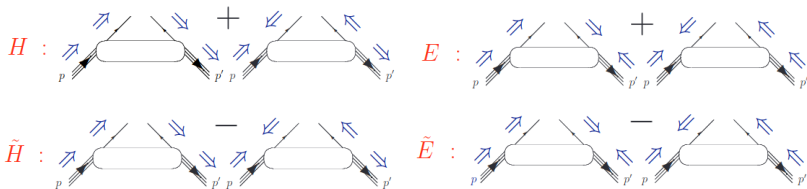
Uses a deuterium target.

Complications: FSI, bound state.

Back to basics

Connection to the total orbital angular momentum of the quarks through Ji's sum rule: $J^q = \frac{1}{2} \int dx x [H^q(x, \xi, t = 0) + E^q(x, \xi, t = 0)]$

Can we introduce a new observable to measure \mathcal{E} to higher precision?



E describes the process when the proton changes helicity.

Can we extract more information on CFF \mathcal{E} by measuring the **polarization** of the **recoil proton**?

Polarization

- Code by Pierre Guichon at leading order, leading twist, using the exact mathematical expressions.
- The polarization $\vec{P} = (P_x, P_y, P_z)$ is computed for the DVCS+Bethe-Heitler process, including their interference.
- P_y (normal to the hadronic plane) is particularly sensitive to CFF \mathcal{E} .

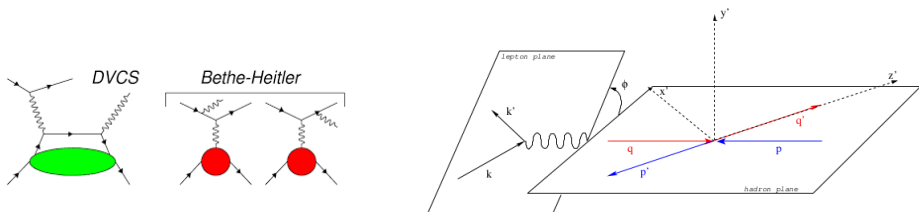
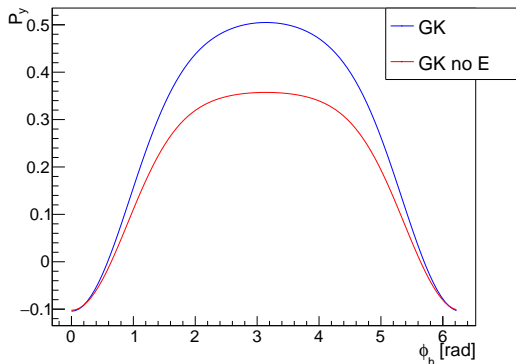


Figure 1: Rotated CM frame $(x'y'z')$

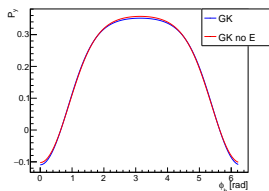
Polarization ϕ_h -dependence



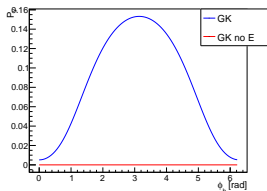
- P_y is sensitive to \mathcal{E} for the Goloshokov-Kroll (GK) model.
- P_x and P_z are not sensitive to \mathcal{E} .
- For $\phi_h = \pi$ there is a large difference in P_y when switching off \mathcal{E} .

Polarization contributions

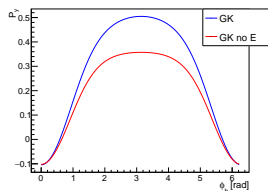
BH-DVCS interference



DVCS

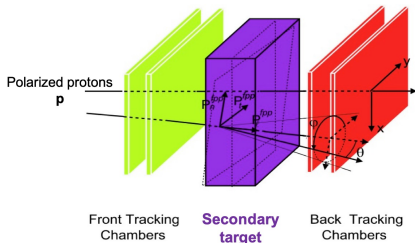


Total



- The total magnitude of P_y comes largely from the interference with Bethe-Heitler.
- The sensitivity of P_y to \mathcal{E} comes from DVCS.

Proton polarimeter



- Rescatter the proton with θ_{pol} , ϕ_{pol} inside a carbon analyzer.
- A set of trackers before and after the analyzer detect the incoming and outgoing protons.

A polarization perpendicular to the proton momentum will result in an asymmetry in ϕ_{pol} :

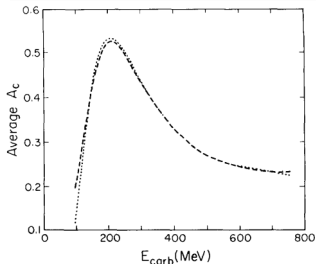
$$N(\theta_{pol}, \phi_{pol}) = N_0[1 + A_p(\theta_{pol})(P_y \sin \phi_{pol} - P_x \cos \phi_{pol})]$$

- The P_x dependence cancels out at $\phi_h = \pi$ for an unpolarized beam.
- P_y can be extracted by fitting the distribution.

Polarimeter performance

Analyzing power

- $A_p(\theta_{pol}, p')$: sensitivity of the scattering to the polarization.
- McNaughton's low-energy parametrization.



Efficiency

- $\epsilon(\theta_{pol}, p', e_c)$: probability to have a useful scattering in the analyzer.
Bonin et al.

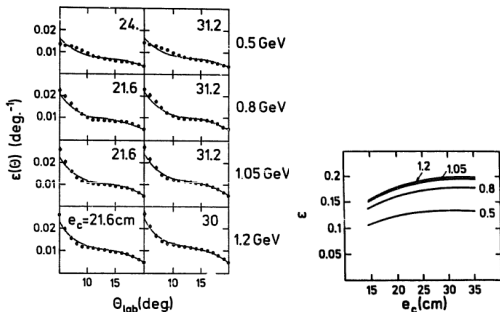


Figure of merit to characterise a polarimeter: $F^2 = \int_{\theta_{min}}^{\theta_{max}} A_p(\theta)^2 \epsilon(\theta) d\theta$

Challenges

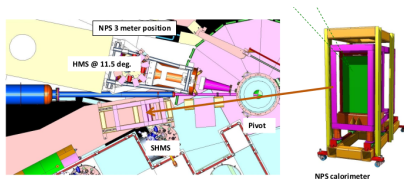
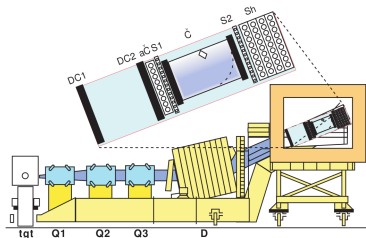
- DVCS has a low cross section compared to (semi-)inclusive processes.
- We need to rescatter the recoil proton, expecting a polarimeter efficiency of order 0.1.
- To achieve high statistics we need a high luminosity.

Candidate facility: **Hall C** at **Jefferson Lab**, using an **unpolarized electron beam** and an **unpolarized liquid hydrogen target**.

Example settings

- Target length: 15 cm.
- Beam current: 20 μA during 3 weeks of data taking.
- This gives an integrated luminosity $L = 7.2 \cdot 10^7 \text{ pb}^{-1}$.

Electron and photon detection



Electron detection: HMS

- Focusing spectrometer.
- Scattering angle range $10.5\text{-}80^\circ$.
- Angular acceptance: $\pm 1.8^\circ$ in-plane, $\pm 4.9^\circ$ out-of-plane.
- Momentum acceptance $\pm 10\%$.

Photon detection: calorimeter

- Angular acceptance: $\pm 5.3^\circ$ horizontally, $\pm 6.7^\circ$ vertically.
- 30×36 PbWO_4 crystals.
Position resolution: 2-3 mm.
- Sweeping magnet reduces low energy electron background.

- The protons will be created from DVCS events.
- The event kinematics (momenta, angles) are determined by the DVCS parameters (E_k, Q^2, x_B, ϕ_h).
- The polarization depends on the CFFs - model dependence.

Model	P_y
GK	0.50
GK no E	0.36
VGG	0.24
KM15	0.15

- GK model: considerable sensitivity of P_y to \mathcal{E} . Used for optimization.
- We aim to discriminate between: GK, GK no E, VGG and KM15.

Procedure

- Generate a grid in Q^2 , x_B and t , setting $\phi_h = \pi$, $E_k = 10.6$ GeV.
- Compute the particle kinematics, the CFFs, the differential cross section and polarization.
- Construct a figure of merit \mathcal{F}' proportional to $\Delta P_y = P_y(\mathcal{E}) - P_y(0)$.
- \mathcal{F}' is inspired by accuracy of polarimeter $\delta_P \propto \frac{1}{F\sqrt{N_{inc}}}$, with $\delta P \rightarrow \Delta P_y$, $N_{inc} \rightarrow$ differential cross section:

$$\mathcal{F}' = F \cdot \sqrt{d\sigma} \cdot \Delta P_y.$$

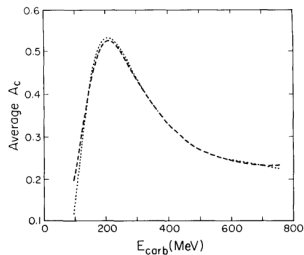
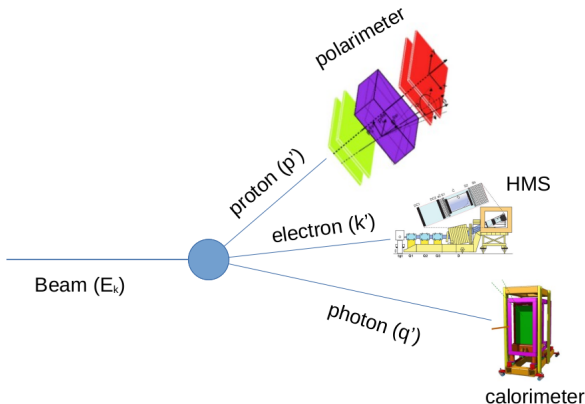
- Refine after Geant4 simulation, taking into account detector acceptance - larger lepton momenta preferred.
- Require: $|\theta_{k'}| > 10.5^\circ$, $\theta_{q'}, \theta_{p'} > 10^\circ$, $\Delta\theta_{i,j} > 10^\circ$ (isolation).

Optimization result

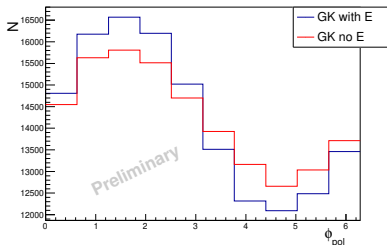
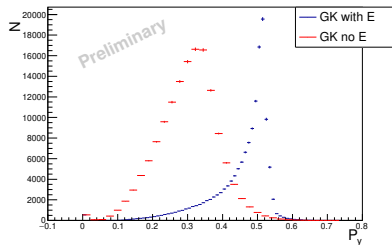
Maximizing \mathcal{F}' gives:

$$E_k = 10.6 \text{ GeV}, Q^2 = 1.8 \text{ GeV}^2, x_B = 0.17, t = -0.45 \text{ GeV}^2, \phi_h = \pi$$

electron	$ k' $	$\theta_{k'}$	photon	$ q' $	$\theta_{q'}$	proton	$ p' $	E_{carb}	$\theta_{p'}$
	4.96 GeV/c	10.6°		5.40 GeV/c	-15.1°		0.71 GeV/c	0.19 GeV/c	44°



Fitting the polarization



Toy simulation of the polarimeter

- We assume a 1 str polarimeter to detect the recoil proton.
- This gives 3.6M events. Assign θ_{pol} , ϕ_{pol} .
- Knowing A_p , P_y can then be extracted (back) from ϕ_{pol} .

Fit results

$$P_y(GK) = 0.475 \pm 0.011 \text{ (cf weighted average: 0.463)}$$

$$P_y(\mathcal{E} = 0) = 0.316 \pm 0.011 \text{ (cf weighted average: 0.304)}.$$

Summary

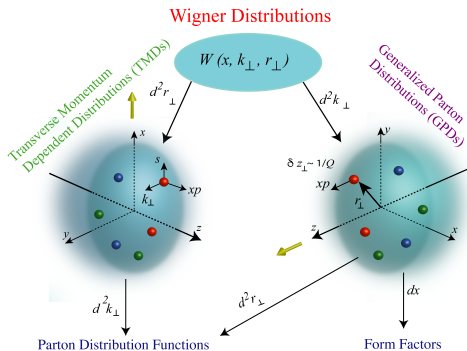
- We have explored a new way of measuring \mathcal{E} - by looking at the **polarization** of the **recoil proton** in DVCS.
- P_y is highly sensitive to \mathcal{E} and to different models.
- **Very high statistics** for 1 str polarimeter, 3 weeks data-taking, $20\mu A$.
- **Good discrimination** between the baseline and null hypothesis and between GK, VGG and KM15 in the statistical analysis.
- A starting point for a proposal has been identified.

Plan to upload on arXiv shortly

Perspectives

- Develop a polarimeter design.
- Determine polarimeter dimensions.
- Consider the **background** and how to reduce it.

GPDs and proton structure



GPDs

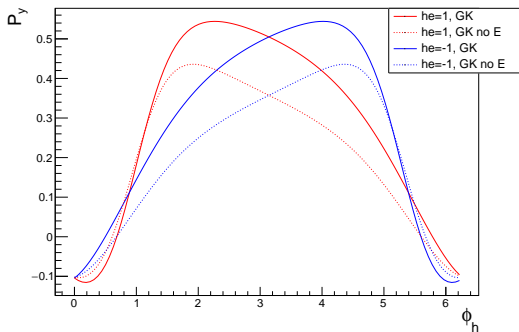
- GPDs and TMDs can both be obtained from Wigner distributions.

From helicity-dependent cross-section difference:

$$[\mathcal{C}_n^I]^{exp} \simeq [\mathcal{C}_n^I] = F_1 \mathcal{H} + \xi(F_1 + F_2) \tilde{\mathcal{H}} - \frac{t}{4M^2} F_2 \mathcal{E}$$

- Dominated by \mathcal{H} , $\tilde{\mathcal{H}}$ for a proton.
- In neutron:
 - F_1 is small.
 - Cancellation between u , d polarized distributions in $\tilde{\mathcal{H}}$.

Polarization ϕ_h -dependence with a polarized beam



- P_y is sensitive to switching \mathcal{E} on or off for the GK model.
- P_x and P_z are not sensitive to \mathcal{E} .
- For $\phi_h = \pi$ there is a large difference in P_y when switching off \mathcal{E} .

Luminosity

$$\mathcal{L} = \Phi \cdot \rho \cdot L$$

Beam

- 20 μA electron beam
- $1A = 6.24 \cdot 10^{18}$ electrons/s
- $\rightarrow \Phi = 12 \cdot 10^{13}/s$

Target

- 0.15 m LH2 target.
- Density:
 - Density: $71 \text{ kg}/m^3$
 - Molar mass: $2.016 \text{ g} / \text{mol} = 3.35 \cdot 10^{27} \text{ kg/particle}$
 - $\rightarrow \rho = 2.1 \cdot 10^{28}/m^3$

$$\mathcal{L} = 4.0 \cdot 10^{41} /s/m^2.$$

$$t = 9.1 \cdot 10^5 s = 3 \text{ weeks of data-taking}$$

$$L = \mathcal{L} \cdot t = 7.2 \cdot 10^{47} /m^2 = 7.2 \cdot 10^7 \text{ pb}^{-1} \text{ (conversion factor } 10^{-(28+12)})$$

CFF inputs

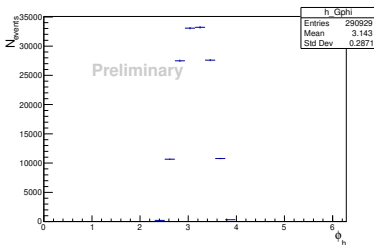
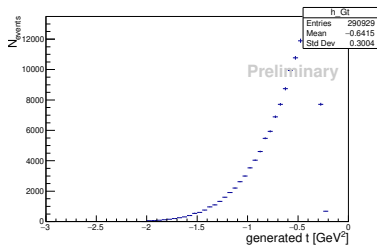
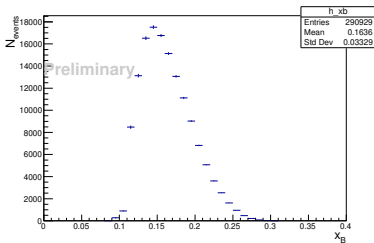
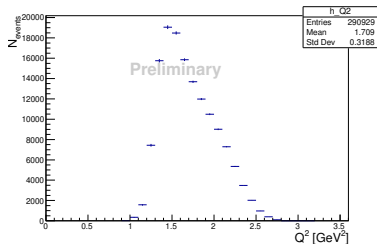
Model	\mathcal{H}	\mathcal{E}	$\tilde{\mathcal{H}}$	P_y
GK	$-1.1 + 5.41i$	$-2.4 - 0.4i$	$0.7 + 1.8i$	0.50
GK no \mathcal{E}	$-1.1 + 5.41i$	0	$0.7 + 1.8i$	0.36
VGG	$-2.5 + 5.0i$	$-1.1 + 1.6i$	$0.5 + 1.5i$	0.24
KM15	$-2.9 + 3.2i$	1.6	$0.5 + 1.5i$	0.15

Model	\mathcal{H}	\mathcal{E}	$\tilde{\mathcal{H}}$	$\tilde{\mathcal{E}}$	P_y
ANN	$-1.8^{\pm 1.3} + 3.4^{\pm 1.7}i$	$-4^{\pm 7} + 0^{\pm 9}i$	$0.4^{\pm 1.4} + 1.2i^{\pm 1.8}$	$-25^{\pm 65} + 3^{\pm 59}i$	0.45

- Larger $|t| \rightarrow$ larger ΔP_y , smaller $d\sigma$.
- Larger $Q^2 \rightarrow$ smaller ΔP_y , smaller $d\sigma$.
- Larger $x_B \rightarrow$ smaller $d\sigma$.
- Large $|k'|$ (small Q^2/x_B) \rightarrow larger acceptance.

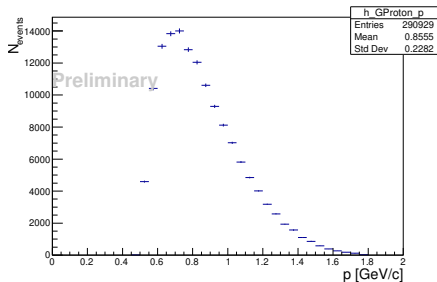
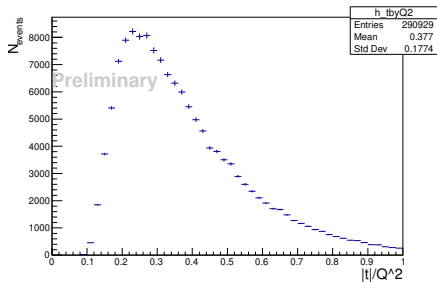
Also require $|t|/Q^2 \leq 0.25$.

Distributions



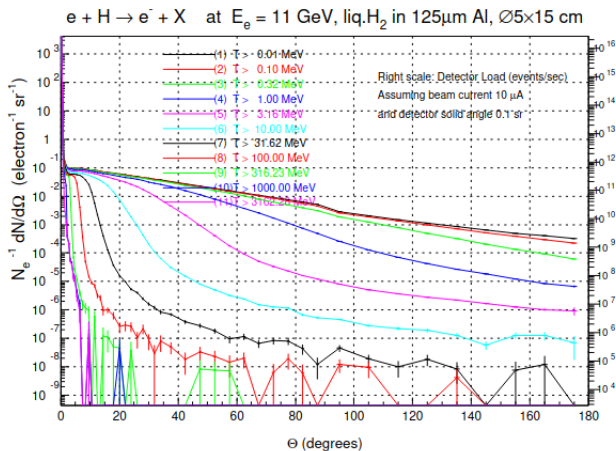
Imposing $\theta_{p'} = \theta_{p'}^{\text{target}} \pm 20^\circ$, $\phi_{p'} = \phi_{p'}^{\text{target}} \pm 30^\circ$ gives these distributions, with Q^2 , x_B , ϕ_h centered near the target values (1.8, 0.17, π).

Distributions (2)



$|t|/Q^2$ and scattered proton momentum

Accidental background



- The background of accidental electrons is largest at small angles from the beam.

Refining the optimization

Q^2, x_B, t	\mathcal{F}'	N_{evts}^{obs}	ΔP_y^{obs}	Fitted δ_P
1.6,0.12,-0.40	0.057	0.5M	0.13	0.031
1.7,0.14,-0.42	0.049	1.6M	0.15	0.017
1.7,0.15,-0.42	0.046	2.6M	0.16	0.013
1.8,0.17,-0.45	0.039	3.6M	0.16	0.011
1.9,0.19,-0.47	0.032	4.1M	0.14	0.010

Selection: $\theta_{p'} \pm 20^\circ$, $\phi_{p'} \pm 30^\circ$ + requirement of non-zero reconstructed scattered lepton p_x .

Increasing x_B , decreasing Q^2/x_B or increasing θ_{calo}^{min} and recomputing \mathcal{F}' post-simulation until it reaches the peak gives the same optimal configuration.