

# Accessing GPDs through the exclusive photoproduction of a $\gamma$ -meson pair with large invariant mass

Assemblée Générale du GdR QCD

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With S. Wallon, L. Szymanowski, B. Pire, R. Boussarie, G. Duplančić,  
K. Passek-Kumerički

# Introduction

## GPDs: DVCS

**DVCS**: exclusive process (non forward amplitude)

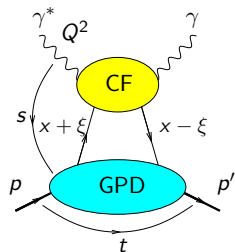
(DVCS: Deep Virtual Compton Scattering)

**Fourier** transf.:  $t \leftrightarrow$  impact parameter

$(x, t) \Rightarrow$  3-dimensional structure

**Coefficient Function** (hard)  $\otimes$  **Generalized Parton Distribution** (soft)

Müller et al. '91 - '94; Radyushkin '96; Ji '97

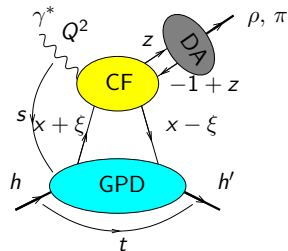


# Introduction

## GPDs: Meson Production

Meson production:  $\gamma$  replaced by  $\rho, \pi, \dots$

GPD (soft)  $\otimes$  CF (hard)  $\otimes$  Distribution Amplitude (soft)



Collins, Frankfurt, Strikman '97; Radyushkin '97

proofs valid only for some restricted cases

Quark GPDs at twist 2

without helicity flip (chiral-even  $\Gamma$  matrices): 4 chiral-even GPDs:  
(Note:  $\Delta = p' - p$ )

$$\begin{aligned} F^q &= \frac{1}{2} \int \frac{dz^-}{2\pi} e^{ixP^+z^-} \langle p' | \bar{q}(-\frac{1}{2}z) \gamma^+ q(\frac{1}{2}z) | p \rangle \Big|_{z^+=0, z_\perp=0} \\ &= \frac{1}{2P^+} \left[ H^q(x, \xi, t) \bar{u}(p') \gamma^+ u(p) + E^q(x, \xi, t) \bar{u}(p') \frac{i \sigma^{+\alpha} \Delta_\alpha}{2m} u(p) \right], \end{aligned}$$

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$$H^q \xrightarrow{\xi=0, t=0} \text{PDF } q \qquad \tilde{H}^q \xrightarrow{\xi=0, t=0} \text{polarized PDF } \Delta q$$

# Introduction

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with helicity flip (chiral-odd  $\Gamma$  matrices): 4 chiral-odd GPDs:

$$\begin{aligned} & \frac{1}{2} \int \frac{dz^-}{2\pi} e^{ixP^+z^-} \langle p' | \bar{q}(-\frac{1}{2}z) i\sigma^{+i} q(\frac{1}{2}z) | p \rangle \Big|_{z^+=0, z_\perp=0} \\ &= \frac{1}{2P^+} \bar{u}(p') \left[ H_T^q i\sigma^{+i} + \tilde{H}_T^q \frac{P^+ \Delta^i - \Delta^+ P^i}{m^2} \right. \\ & \quad \left. + E_T^q \frac{\gamma^+ \Delta^i - \Delta^+ \gamma^i}{2m} + \tilde{E}_T^q \frac{\gamma^+ P^i - P^+ \gamma^i}{m} \right] u(p), \end{aligned}$$

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$$H_T^q \xrightarrow{\xi=0, t=0} \text{quark transversity PDFs } \delta q$$

**Note:**  $\tilde{E}_T^q(x, -\xi, t) = -\tilde{E}_T^q(x, \xi, t)$



# Why consider a gamma-meson pair?

## Understanding transversity

- ▶ Transverse spin content of the proton:

$$\begin{array}{lcl} |\uparrow\rangle_{(x)} & \sim & |\rightarrow\rangle + |\leftarrow\rangle \\ |\downarrow\rangle_{(x)} & \sim & |\rightarrow\rangle - |\leftarrow\rangle \\ \text{spin along } x & & \text{helicity states} \end{array}$$

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- ▶ Transversity GPDs can thus be accessed through **chiral-odd  $\Gamma$**  matrices.

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- ▶ Transversity GPDs can thus be accessed through **chiral-odd**  $\Gamma$  matrices.
- ▶ Since (in the massless limit) QCD and QED are chiral-even ( $\gamma^\mu, \gamma^\mu\gamma^5$ ), **the chiral-odd quantities** ( $1, \gamma^5, [\gamma^\mu, \gamma^\nu]$ ) **which one wants to measure should appear in pairs.**

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Can we probe transversity GPDs in meson production?

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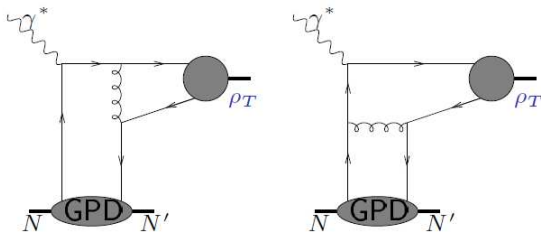
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- ▶ lowest order diagrammatic argument:



$$\gamma^\alpha [\gamma^\mu, \gamma^\nu] \gamma_\alpha = 0$$

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Go to higher twist?

- ▶ This vanishing only occurs at twist 2
- ▶ At twist 3 this process does not vanish [Ahmad, Goldstein, Liuti], [Goloskokov, Kroll]

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- ▶ This vanishing only occurs at **twist 2**
- ▶ At twist 3 this process does not vanish [Ahmad, Goldstein, Liuti], [Goloskokov, Kroll]
- ▶ However processes involving **twist 3 DAs** may face problems with factorization (end-point singularities)  
can be made safe in the high-energy  $k_T$ -factorization approach  
[Anikin, Ivanov, Pire, Szymanowski, Wallon]



# Why consider a gamma-meson pair?

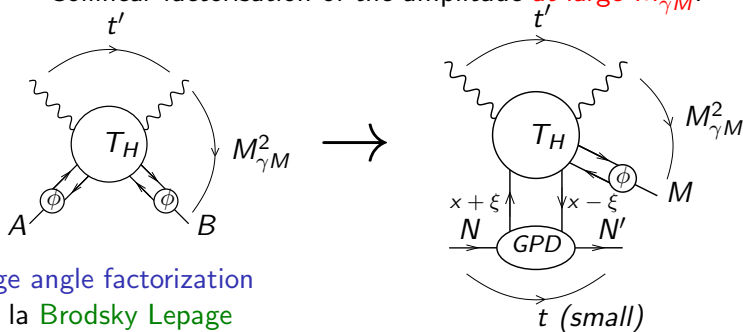
A convenient alternative solution

- ▶ Circumvent this using 3-body final states [Ivanov, Pire, Szymanowski, Teryaev], [Enberg, Pire, Szymanowski], [El Beiyad, Pire, Segond, Szymanowski, Wallon]
- ▶ Consider the process  $\gamma N \rightarrow \gamma MN'$ ,  $M = \text{meson}$ .

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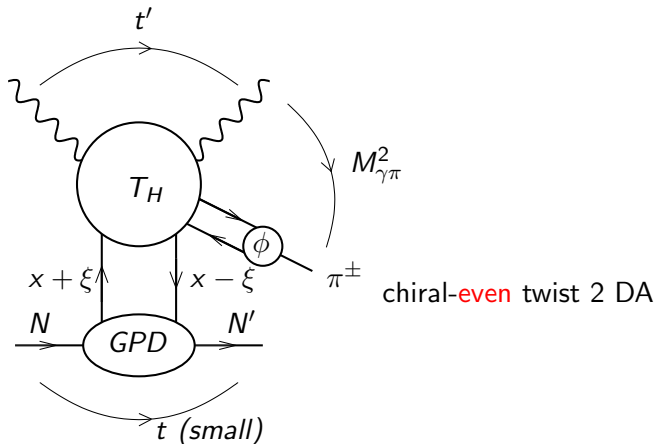
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- ▶ Consider the process  $\gamma N \rightarrow \gamma M N'$ ,  $M = \text{meson}$ .
- ▶ Collinear factorisation of the amplitude at large  $M_{\gamma M}^2$ .



large angle factorization  
à la Brodsky Lepage

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Chiral-even GPDs using  $\pi^\pm \gamma$  production

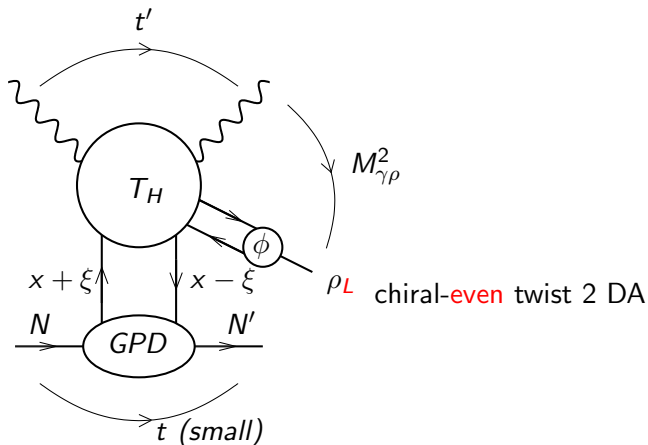


chiral-even twist 2 GPD

[G. Duplančić, K. Passek-Kumerički, B. Pire, L. Szymanowski, S. Wallon]

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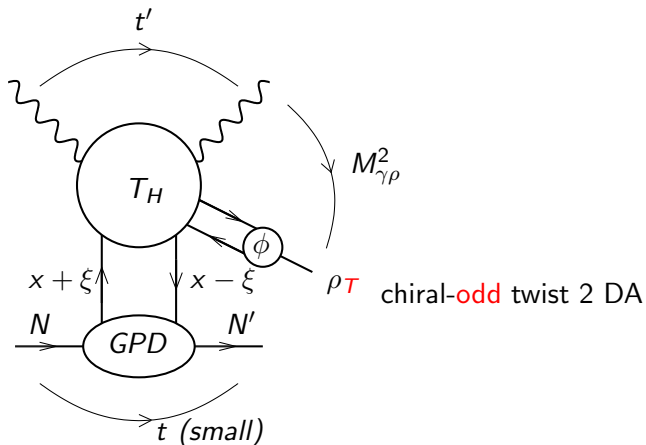


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Chiral-odd GPDs using  $\rho_T \gamma$  production



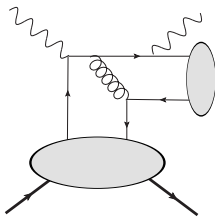
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# Why consider a gamma-meson pair?

Chiral-odd GPDs using  $\rho_T\gamma$  production

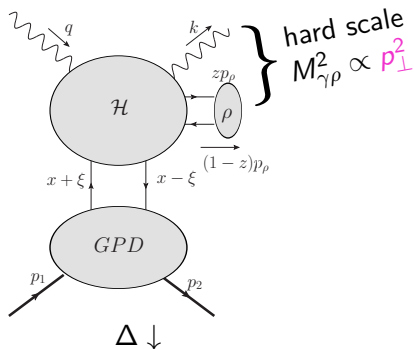
How does it work?



Typical non-zero diagram for a **transverse**  $\rho$  meson

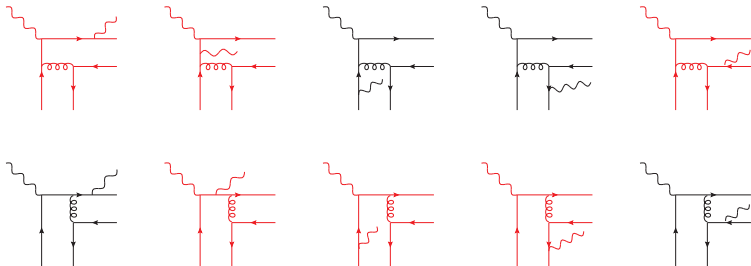
the  $\sigma$  matrices (from either the DA or the GPD) do not kill it anymore!

$$\gamma^{(*)}(q) + N(p_1) \rightarrow \gamma(k) + \rho^0(p_\rho, \varepsilon_\rho) + N'(p_2)$$



Useful Mandelstam variables:  $t = (p_2 - p_1)^2$ ,  $u' = (p_\rho - q)^2$

A total of 20 diagrams to compute



- ▶ The other half can be deduced by  $q \leftrightarrow \bar{q}$  (anti)symmetry depending on  $C$ -parity in  $t$ -channel
- ▶ Red diagrams cancel in the chiral-odd case



# Computation

Parametrising the GPDs: 2 scenarios for polarized PDFs

We parameterise the GPDs in terms of *double distributions*  
(*Radyushkin-type parametrisation*)

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For **polarized** PDFs (and hence **transversity** PDFs), two scenarios are proposed for the parameterization:

- ▶ “**standard**” scenario, with flavor-symmetric light sea quark and antiquark distributions.
- ▶ “**valence**” scenario with a completely flavor-asymmetric light sea quark densities.

- ▶ We take the simplistic **asymptotic** form of the DAs

$$\phi_{\pi}(z) = \phi_{\rho\parallel}(z) = \phi_{\rho\perp}(z) = 6z(1-z).$$

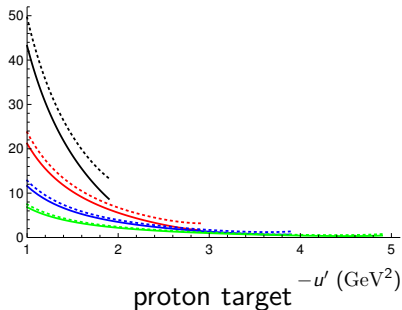
- ▶ A **non asymptotical** wave function can be also investigated (preliminary):

$$\phi_{sing}(z) = \frac{8}{\pi} \sqrt{z(1-z)}.$$

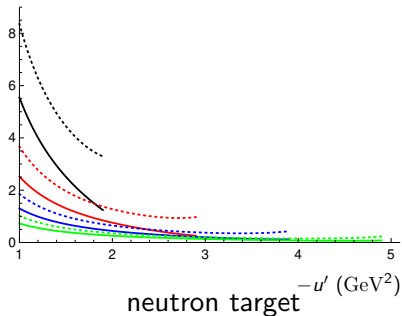
# Results

Fully-differential cross-sections:  $\rho_L$  (Chiral even)

$$\frac{d\sigma_{\text{even}}}{dM_{\gamma\rho}^2 d(-u') d(-t)} \quad (\text{pb} \cdot \text{GeV}^{-6})$$



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$$S_{\gamma N} = 20 \text{ GeV}^2, \text{ at } -t = (-t)_{\text{min}}$$

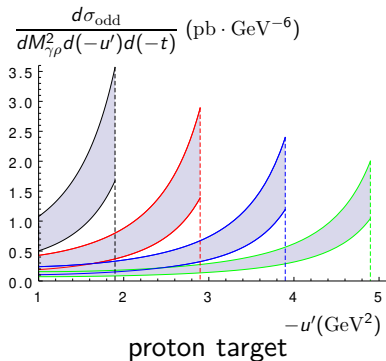
$$M_{\gamma\rho}^2 = 3, 4, 5, 6 \text{ GeV}^2$$

dotted: "standard" model

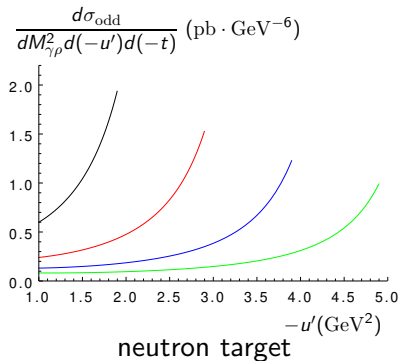
solid: "valence" model

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Fully-differential cross-sections:  $\rho_T$  (Chiral odd)



“valence” and “standard” models,  
each of them with  $\pm 2\sigma$  [S. Melis]



“valence” model only

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$$M_{\gamma\rho}^2 = 3, 4, 5, 6 \text{ GeV}^2$$

# Results

## Phase space integration

large angle scattering:  $M_{\gamma\rho}^2 \sim -u' \sim -t'$

$\Rightarrow -u' > 1 \text{ GeV}^2$  and  $-t' > 1 \text{ GeV}^2$  and  $(-t)_{\min} \leq -t \leq .5 \text{ GeV}^2$

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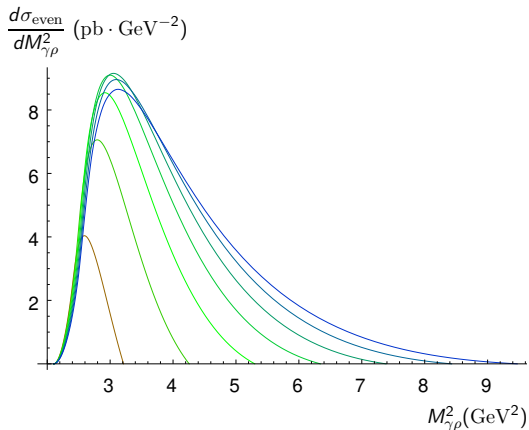
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*See backup slides for more details, including information on the phase space evolution in the  $(-t, -u')$  plane.*

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Single differential cross-section:  $\rho_L$  (Chiral even)



proton target, "valence" scenario

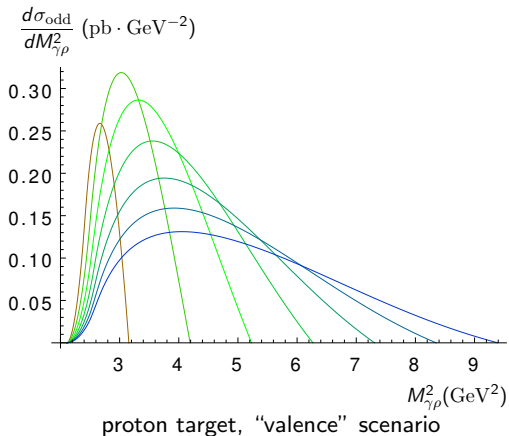
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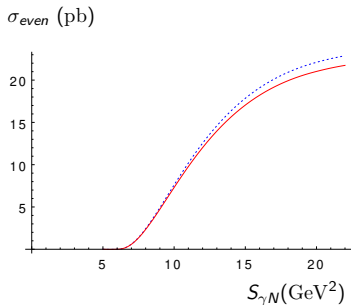


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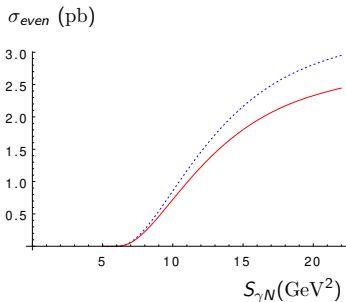
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Integrated cross-section: Valence vs Standard:  $\rho_L$  (Chiral even)



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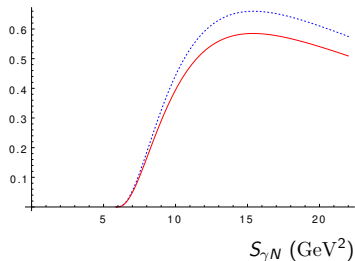
**solid red:** "valence" scenario

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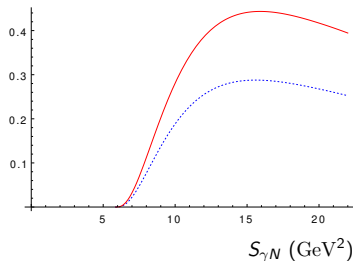
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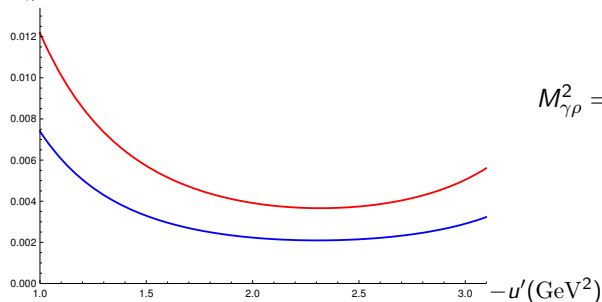
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comparing singular DA ( $\propto \sqrt{z(1-z)}$ )  
vs asymptotical DA ( $\propto z(1-z)$ ).

“valence” model for the polarized PDFs

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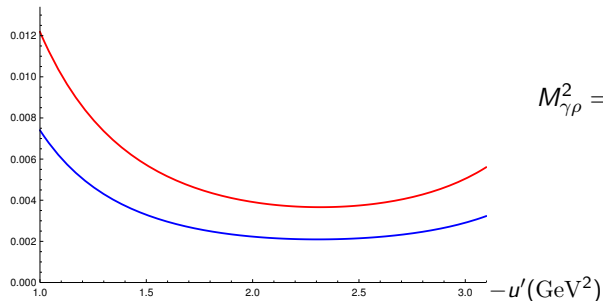
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⇒ sizable effect, larger than the one due to uncertainties on polarized PDFs

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Counting rates: JLab

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- ▶ with an expected luminosity of  $\mathcal{L} = 100 \text{ nb}^{-1}\text{s}^{-1}$ , for 100 days of run:
  - $\rho_L^0 : \approx 7.6 \times 10^4$  (Chiral-even)
  - $\rho_T^0 : \approx 7.5 \times 10^3$  (Chiral-odd)
  - $\pi^+ : \approx 5.8 \times 10^4$  (Chiral-even)
  - $\pi^- : \approx 4.1 \times 10^4$  (Chiral-even)

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EIC, LHC at UPC,...

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- ▶ For data already taken, about 1 order of magnitude less...  
 $\implies$  *Low luminosity not being compensated by larger photon flux.*

- ▶ Use **non-asymptotical DA**,  $\phi_M(z) = \frac{8}{\pi} \sqrt{z(1-z)}$ , (instead of  $\phi_M(z) = 6z(1-z)$ ) to model the outgoing meson  $M$ : suggested by AdS/QCD correspondence, dynamical chiral symmetry breaking. [Ongoing]

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- ▶ Investigate **polarisation asymmetries** of the initial  $\gamma$ . [Ongoing]
- ▶ **Adjust kinematics** for searches at EIC, LHC at UPC, LHeC and COMPASS. [Ongoing]

- ▶ Use **non-asymptotical DA**,  $\phi_M(z) = \frac{8}{\pi} \sqrt{z(1-z)}$ , (instead of  $\phi_M(z) = 6z(1-z)$ ) to model the outgoing meson  $M$ : suggested by AdS/QCD correspondence, dynamical chiral symmetry breaking. [Ongoing]
- ▶ Investigate **polarisation asymmetries** of the initial  $\gamma$ . [Ongoing]
- ▶ **Adjust kinematics** for searches at EIC, LHC at UPC, LHeC and COMPASS. [Ongoing]
- ▶ Add **Bethe-Heitler** component (photon emitted from incoming lepton)
  - zero in chiral-odd case.
  - suppressed in chiral-even case, but could estimate their contributions.

- ▶ Compute **NLO** corrections.
  - ▶ Cancellation of IR divergences: Indication that QCD factorisation works.

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- ▶ Consider **twist-3** contributions.
- ▶ Generalise to **electroproduction** ( $Q^2 \neq 0$ ) (and include Bethe-Heitler contributions).

The END

## BACKUP SLIDES

# What are GPDs?

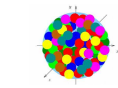
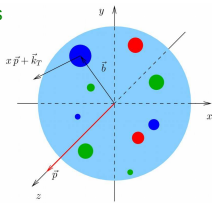
From Wigner distributions to GPDs and PDFs

6D/5D

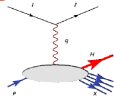
Wigner distributions  
for hadrons

$$W(x, \vec{b}, k_T)$$

Experimentally  
*inaccessible* directly



3D  
perturbative Regge  
limit



Semi-inclusive  
processes

uPDFs (gluons)

Unintegrated parton  
distributions

$$\int d^3 \vec{b}$$

TMDs

$$f(x, k_T)$$

Transverse momentum  
dependent distributions

$$\int d^2 k_T \int d b_z$$

Impact parameter  
distributions

$$f(x, b_T)$$

Impact parameter  
distributions

$$b_T \leftrightarrow \Delta$$

$$f(x, b_T) \leftrightarrow H(x, 0, t)$$

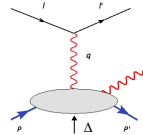
$$t = -\Delta^2$$

$$\int d^2 k_T \int \text{Fourier}(\vec{b})$$

$\xi=0$  GPDs

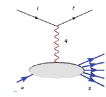
$$H(x, \xi, t)$$

generalised parton  
distributions



exclusive  
processes

1D



inclusive and semi-  
inclusive processes

$$\int d^2 k_T$$

PDFs

$$f(x)$$

parton distributions

$$\int d^2 b_T$$



$$t=0$$



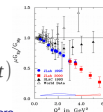
elastic processes

$$\int dx$$

FFs

$$G_{E,M}(t)$$

form factors



$$\int dx x^{n-1}$$

GFFs

generalized form factors

lattices

# Computation

Parametrising the GPDs:  $\rho_L$  and  $\pi$  case, Chiral-even

$$\int \frac{dz^-}{4\pi} e^{ixP^+z^-} \langle p_2, \lambda_2 | \bar{\psi}_q \left( -\frac{1}{2}z^- \right) \gamma^+ \psi \left( \frac{1}{2}z^- \right) | p_1, \lambda_1 \rangle$$
$$= \frac{1}{2P^+} \bar{u}(p_2, \lambda_2) \left[ H^q(x, \xi, t) \gamma^+ + E^q(x, \xi, t) \frac{i\sigma^{\alpha+} \Delta_\alpha}{2m} \right] u(p_1, \lambda_1)$$

$$\int \frac{dz^-}{4\pi} e^{ixP^+z^-} \langle p_2, \lambda_2 | \bar{\psi}_q \left( -\frac{1}{2}z^- \right) \gamma^+ \gamma^5 \psi \left( \frac{1}{2}z^- \right) | p_1, \lambda_1 \rangle$$
$$= \frac{1}{2P^+} \bar{u}(p_2, \lambda_2) \left[ \tilde{H}^q(x, \xi, t) \gamma^+ \gamma^5 + \tilde{E}^q(x, \xi, t) \frac{\gamma^5 \Delta^+}{2m} \right] u(p_1, \lambda_1)$$

- ▶ Take the limit  $\Delta_\perp = 0$ .
- ▶ In that case and for small  $\xi$ , the dominant contributions come from  $H^q$  and  $\tilde{H}^q$ .

# Computation

Parametrising the GPDs:  $\rho_T$  case, Chiral-odd

$$\begin{aligned} & \int \frac{dz^-}{4\pi} e^{ixP^+z^-} \langle p_2, \lambda_2 | \bar{\psi}_q \left( -\frac{1}{2}z^- \right) i\sigma^{+i} \psi \left( \frac{1}{2}z^- \right) | p_1, \lambda_1 \rangle \\ &= \frac{1}{2P^+} \bar{u}(p_2, \lambda_2) \left[ H_T^q(x, \xi, t) i\sigma^{+i} + \tilde{H}_T^q(x, \xi, t) \frac{P^+ \Delta^i - \Delta^+ P^i}{M_N^2} \right. \\ &+ \left. E_T^q(x, \xi, t) \frac{\gamma^+ \Delta^i - \Delta^+ \gamma^i}{2M_N} + \tilde{E}_T^q(x, \xi, t) \frac{\gamma^+ P^i - P^+ \gamma^i}{M_N} \right] u(p_1, \lambda_1) \end{aligned}$$

- ▶ Take the limit  $\Delta_\perp = 0$ .
- ▶ In that case and for small  $\xi$ , the dominant contributions come from  $H_T^q$ .

- ▶ GPDs can be represented in terms of **Double Distributions**  
[Radyushkin]

$$H^q(x, \xi, t = 0) = \int_{-1}^1 d\beta \int_{-1+|\beta|}^{1-|\beta|} d\alpha \delta(\beta + \xi\alpha - x) f^q(\beta, \alpha)$$

- ▶ GPDs can be represented in terms of **Double Distributions** [Radyushkin]

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- ▶ ansatz for these Double Distributions [Radyushkin]:

- ▶ chiral-even sector:

$$\begin{aligned} f^q(\beta, \alpha, t = 0) &= \Pi(\beta, \alpha) q(\beta) \Theta(\beta) - \Pi(-\beta, \alpha) \bar{q}(-\beta) \Theta(-\beta), \\ \tilde{f}^q(\beta, \alpha, t = 0) &= \Pi(\beta, \alpha) \Delta q(\beta) \Theta(\beta) + \Pi(-\beta, \alpha) \Delta \bar{q}(-\beta) \Theta(-\beta). \end{aligned}$$

- ▶ chiral-odd sector:

$$f_T^q(\beta, \alpha, t = 0) = \Pi(\beta, \alpha) \delta q(\beta) \Theta(\beta) - \Pi(-\beta, \alpha) \delta \bar{q}(-\beta) \Theta(-\beta).$$



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$$f_T^q(\beta, \alpha, t = 0) = \Pi(\beta, \alpha) \delta q(\beta) \Theta(\beta) - \Pi(-\beta, \alpha) \delta \bar{q}(-\beta) \Theta(-\beta).$$

- ▶  $\Pi(\beta, \alpha) = \frac{3}{4} \frac{(1-\beta)^2 - \alpha^2}{(1-\beta)^3}$  : profile function

- ▶ simplistic factorized ansatz for the  $t$ -dependence:

$$H^q(x, \xi, t) = H^q(x, \xi, t = 0) \times F_H(t)$$

with  $F_H(t) = \frac{C^2}{(t-C)^2}$  a standard **dipole form factor**  
( $C = 0.71\text{GeV}^2$ )

- ▶  $q(x)$  : unpolarized PDF [GRV-98]  
and [MSTW2008lo, MSTW2008nnlo, ABM11nnlo, CT10nnlo]
- ▶  $\Delta q(x)$  polarized PDF [GRSV-2000]
- ▶  $\delta q(x)$  : transversity PDF [Anselmino *et al.*]

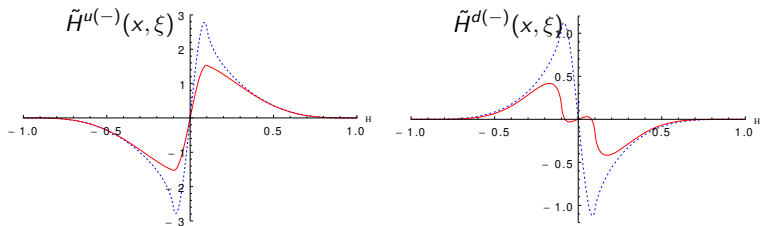
Effects are not significant! But relevant for NLO corrections!

# Computation

Valence vs Standard scenarios in  $\tilde{H}$  (Chiral-even, Axial)

Typical kinematic point:  $\xi = .1 \leftrightarrow S_{\gamma N} = 20 \text{ GeV}^2$  and  $M_{\gamma\rho}^2 = 3.5 \text{ GeV}^2$

$$\tilde{H}^{q(-)}(x, \xi, t) = \tilde{H}^q(x, \xi, t) - \tilde{H}^q(-x, \xi, t) \quad [C = -1]$$



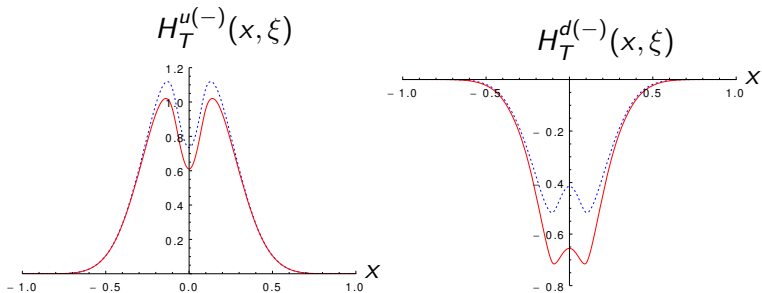
“valence” and “standard”: two GRSV Ansätze for  $\Delta q(x)$

# Computation

Valence vs Standard scenarios in  $H_T$  (Chiral-odd)

Typical Kinematic Point:  $\xi = .1 \leftrightarrow S_{\gamma N} = 20 \text{ GeV}^2$  and  $M_{\gamma\rho}^2 = 3.5 \text{ GeV}^2$

$$H_T^{q(-)}(x, \xi, t) = H_T^q(x, \xi, t) + H_T^q(-x, \xi, t) \quad [C = -1]$$



“valence” and “standard”: two GRSV Ansätze for  $\Delta q(x)$

$\Rightarrow$  two Ansätze for  $\delta q(x)$

- Helicity conserving (vector) DA at twist 2:  $\rho_L$

$$\langle 0 | \bar{u}(0) \gamma^\mu u(x) | \rho^0(p, s) \rangle = \frac{p^\mu}{\sqrt{2}} f_\rho \int_0^1 du e^{-iup \cdot x} \phi_{\parallel}(u)$$

- $\rho_T$  DA at twist 2:

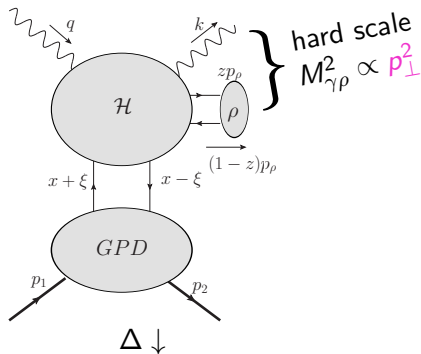
$$\langle 0 | \bar{u}(0) \sigma^{\mu\nu} u(x) | \rho^0(p, s) \rangle = \frac{i}{\sqrt{2}} (\epsilon_\rho^\mu p^\nu - \epsilon_\rho^\nu p^\mu) f_\rho^\perp \int_0^1 du e^{-iup \cdot x} \phi_\perp(u)$$

# Computation

## Kinematics

► Work in the limit of:

- $\Delta_{\perp} \ll p_{\perp}$
- $M^2, m_{\rho}^2 \ll M_{\gamma\rho}^2$



# Computation

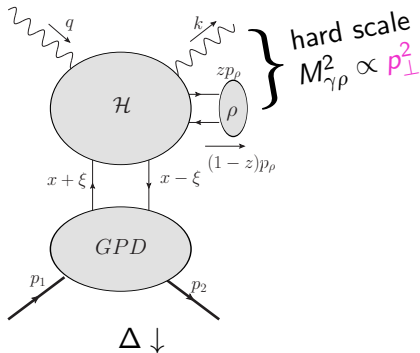
## Kinematics

► Work in the limit of:

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- $M^2, m_{\rho}^2 \ll M_{\gamma\rho}^2$

► initial state particle momenta:

$$q^{\mu} = n^{\mu},$$
$$p_1^{\mu} = (1 + \xi) p^{\mu} + \frac{M^2}{s(1+\xi)} n^{\mu}$$





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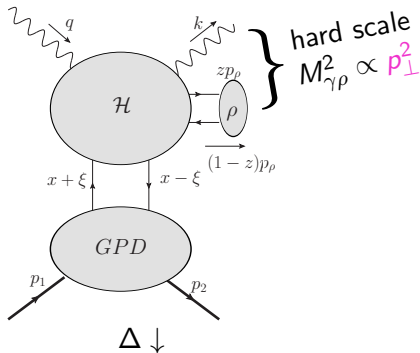
$$p_1^{\mu} = (1 + \xi) p^{\mu} + \frac{M^2}{s(1+\xi)} n^{\mu}$$

- ▶ final state particle momenta:

$$p_2^{\mu} = (1 - \xi) p^{\mu} + \frac{M^2 + \vec{p}_t^2}{s(1 - \xi)} n^{\mu} + \Delta_{\perp}^{\mu}$$

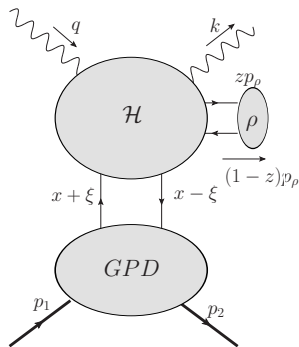
$$k^{\mu} = \alpha n^{\mu} + \frac{(\vec{p}_t - \vec{\Delta}_t/2)^2}{\alpha s} p^{\mu} + p_{\perp}^{\mu} - \frac{\Delta_{\perp}^{\mu}}{2},$$

$$p_{\rho}^{\mu} = \alpha_{\rho} n^{\mu} + \frac{(\vec{p}_t + \vec{\Delta}_t/2)^2 + m_{\rho}^2}{\alpha_{\rho} s} p^{\mu} - p_{\perp}^{\mu} - \frac{\Delta_{\perp}^{\mu}}{2},$$



$$\mathcal{A} \propto \int_{-1}^1 dx \int_0^1 dz T(x, \xi, z) H(x, \xi, t) \Phi_\rho(z)$$

- ▶  $z$  integration performed **analytically** using an asymptotic DA  $\propto z(1-z)$
- ▶ GPD models plugged into expression for amplitude and the integral performed w.r.t.  $x$  **numerically**.

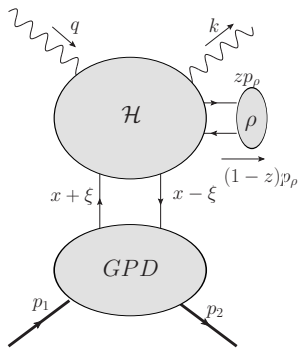


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- ▶  $z$  integration performed **analytically** using an asymptotic DA  $\propto z(1-z)$
- ▶ GPD models plugged into expression for amplitude and the integral performed w.r.t.  $x$  **numerically**.
- ▶ Differential cross section:

$$\left. \frac{d\sigma}{dt du' dM_{\gamma\rho}^2} \right|_{-t=(-t)_{min}} = \frac{|\overline{\mathcal{A}}|^2}{32 S_{\gamma N}^2 M_{\gamma\rho}^2 (2\pi)^3} \cdot$$

- ▶ Kinematic parameters:  $S_{\gamma N}$ ,  $M_{\gamma\rho}^2$  and  $-u'$   
**Recall:**  $u' = (p_\rho - q)^2$ ,  $t = (p_2 - p_1)^2$



# Results

Phase space integration: Evolution in  $(-t, -u')$  plane

large angle scattering:  $M_{\gamma\rho}^2 \sim -u' \sim -t'$

$\Rightarrow -u' > 1 \text{ GeV}^2$  and  $-t' > 1 \text{ GeV}^2$  and  $(-t)_{\min} \leq -t \leq .5 \text{ GeV}^2$

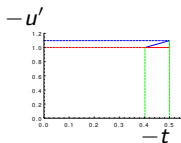
# Results

Phase space integration: Evolution in  $(-t, -u')$  plane

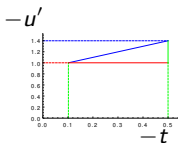
large angle scattering:  $M_{\gamma\rho}^2 \sim -u' \sim -t'$

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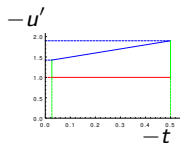
example:  $S_{\gamma N} = 20 \text{ GeV}^2$



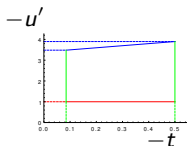
$$M_{\gamma\rho} = 2.2 \text{ GeV}^2$$



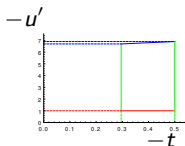
$$M_{\gamma\rho}^2 = 2.5 \text{ GeV}^2$$



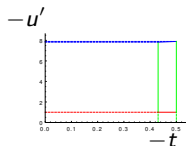
$$M_{\gamma\rho} = 3 \text{ GeV}^2$$



$$M_{\gamma\rho} = 5 \text{ GeV}^2$$



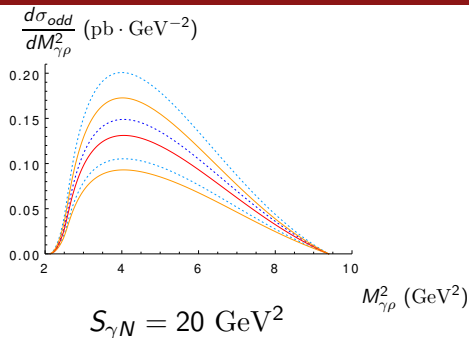
$$M_{\gamma\rho} = 8 \text{ GeV}^2$$



$$M_{\gamma\rho} = 9 \text{ GeV}^2$$

# Results

Single differential cross-section: Valence vs Standard:  $\rho_T$  (Chiral odd)



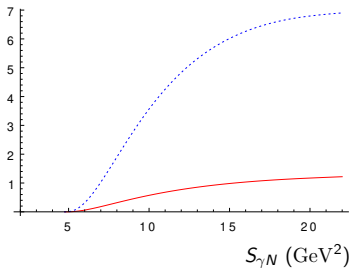
Various ansätze for the PDFs  $\Delta q$  used to build the GPD  $H_T$ :

- ▶ *dotted curves*: “standard” scenario
- ▶ *solid curves*: “valence” scenario
- ▶ *deep-blue* and *red* curves: central values
- ▶ *light-blue* and *orange*: results with  $\pm 2\sigma$ .

# Results

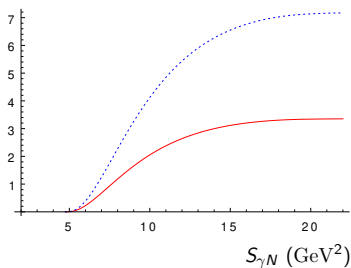
Integrated cross-section: Valence vs Standard:  $\pi^\pm$  (Chiral even)

$\sigma_{\gamma\pi^+}$  (pb)



proton target

$\sigma_{\gamma\pi^-}$  (pb)



neutron target

**solid red:** "valence" scenario

**dashed blue:** "standard" one