



# Low Q-value decays for absolute mass scale determination of the neutrino

T. Eronen, Z. Ge, J. Kostensalo, A. de Roubin, J. Suhonen



# The determination of the absolute mass scale of the neutrino

The determination of the **absolute mass scale of the neutrino** is one of the **burning question in physics**

Neutrino mixing experiments have revealed that neutrinos have a non-zero mass

- ↳ BUT: not able to gauge the absolute mass values!  
(only the difference of squared neutrino masses)

**How to pinpoint the (anti)neutrino mass?**

- Precisely
- In a model independent way



**Kinematical studies**

- $\beta^-$  decay
- Electron capture

# Direct (anti)neutrino mass measurements

## Single Electron Capture

- Decay energy shared between:
  - Emitted neutrino
  - Atomic excitation of the daughter atom
  - (recoiling nucleus)
- Experimental approach:
  - Low temperature calorimetry measurements  
**(ECHO, HOLMES, NuMECS)**  
*L. Gastaldo et al., Eur. Phys. J. Special Topics **226**, 1623 (2017)*  
*M. Faverzani et al., J. Low Temp. Phys. **184**, 922 (2016)*  
*A. Faessler et al., Phys. Rev. C **91**, 045505 (2015)*

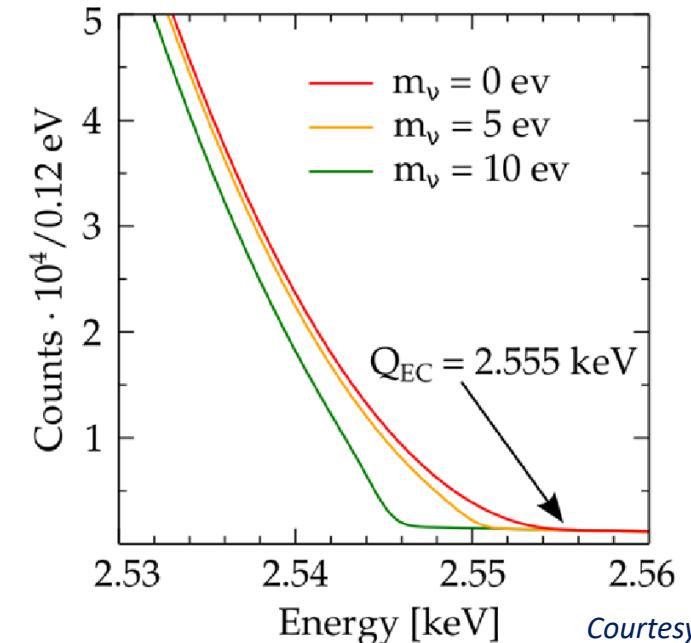
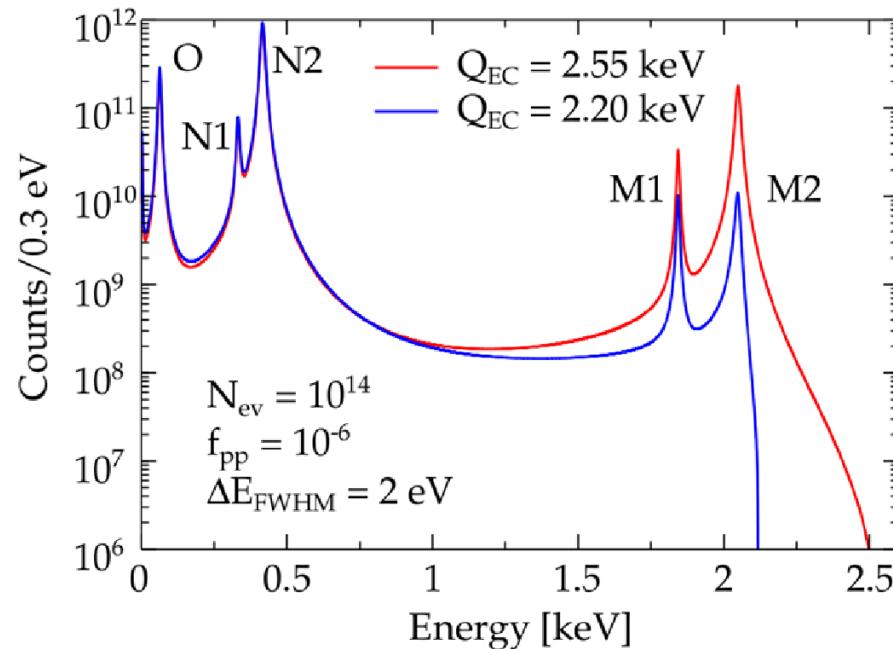
## Single $\beta^-$ decay

- Energy is distributed between the decay products
- Experimental approaches:
  - Electron spectroscopy (KATRIN)  
*C. Weinheimer, Prog. Part. Nucl. Phys., **48**, 141 (2002)*  
*KATRIN collaboration, Nat. Phys., **18**, 160 (2022)*
  - Cyclotron radiation emission spectroscopy (Super8)  
*B. Montreal et al. Mass. Phys. Rev., D **80**, 051301 (2009)*

Interested in the endpoint of the energy spectrum!

Need decay with a **small Q value** to maximize the sensitivity to the neutrino mass!

# Single electron capture



Courtesy of C. Marquet

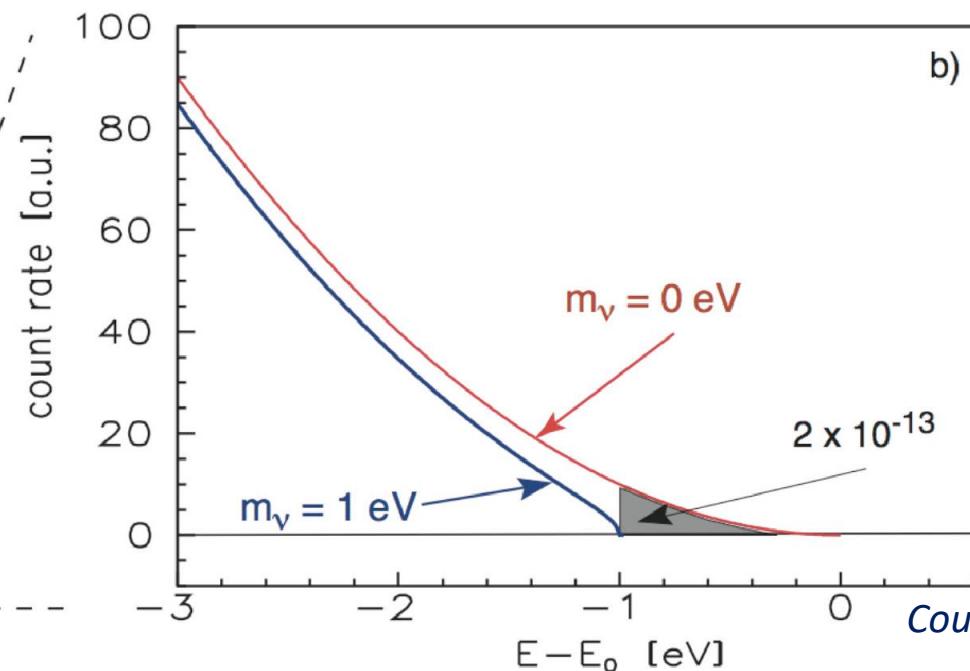
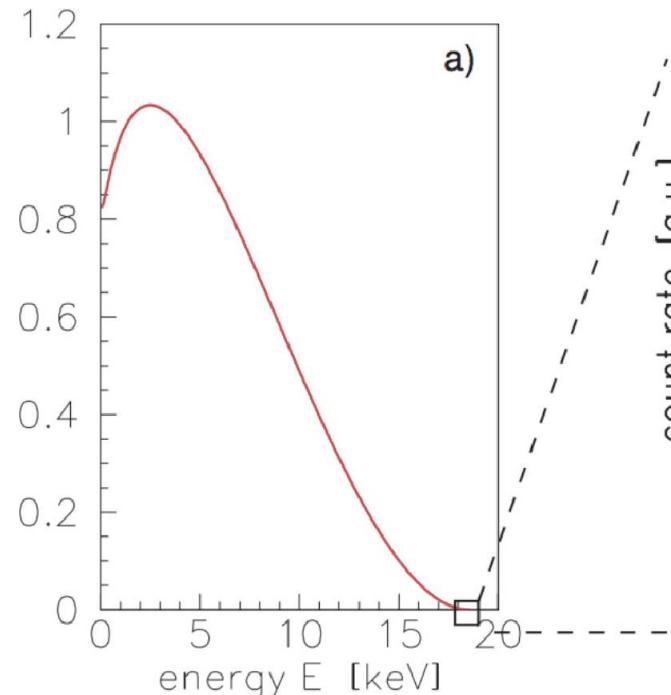
- Measurement of emitted particles and their energies following the EC
- The mismatch of energy available in decay and emitted energy reveals the neutrino mass
- Upper limit of the effective electron-neutrino mass  $m_{\nu_e} = 150 \text{ eV/c}^2$  (95% confidence level)

C. Velte et al., Eur. Phys. J. C **79**, 1026 (2019)

# Single $\beta^-$ decay



$$Q_{EC} = 18.6 \text{ keV}$$



Courtesy of C. Marquet

- Measurement of emitted electron energy
- The maximum energy is linked to the neutrino mass
- Upper limit of the effective electron-neutrino mass  $m_{\nu_e} = 0.8 \text{ eV}/c^2$  (90% confidence level)

KATRIN collaboration, Nat. Phys., 18, 160 (2022)

# Ultra low Q-value $\beta$ decay for neutrino physics

Interested in the endpoint of the energy spectrum!

Need decay with a **small Q value** to maximize the sensitivity to the neutrino mass!



Smallest GS-to-GS Q-values around 1 keV

# Ultra low Q-value $\beta$ decay for neutrino physics

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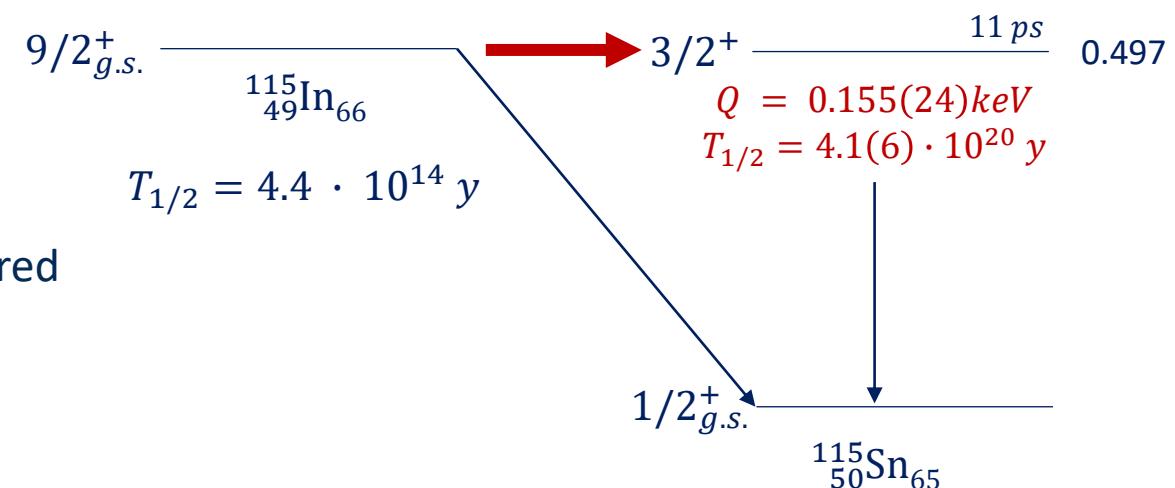
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Smallest GS-to-GS Q-values around 1 keV

- Possibility to use decays with even smaller Q-values

- $^{115}\text{In}(9/2^+) \xrightarrow{\beta^-} {}^{115}\text{Sn}(3/2^+)$
- $Q = 0.155(24)$  keV → smallest  $\beta$  Q-value ever measured
- A « detector » for the neutrino mass ?



- Other possible low Q-values

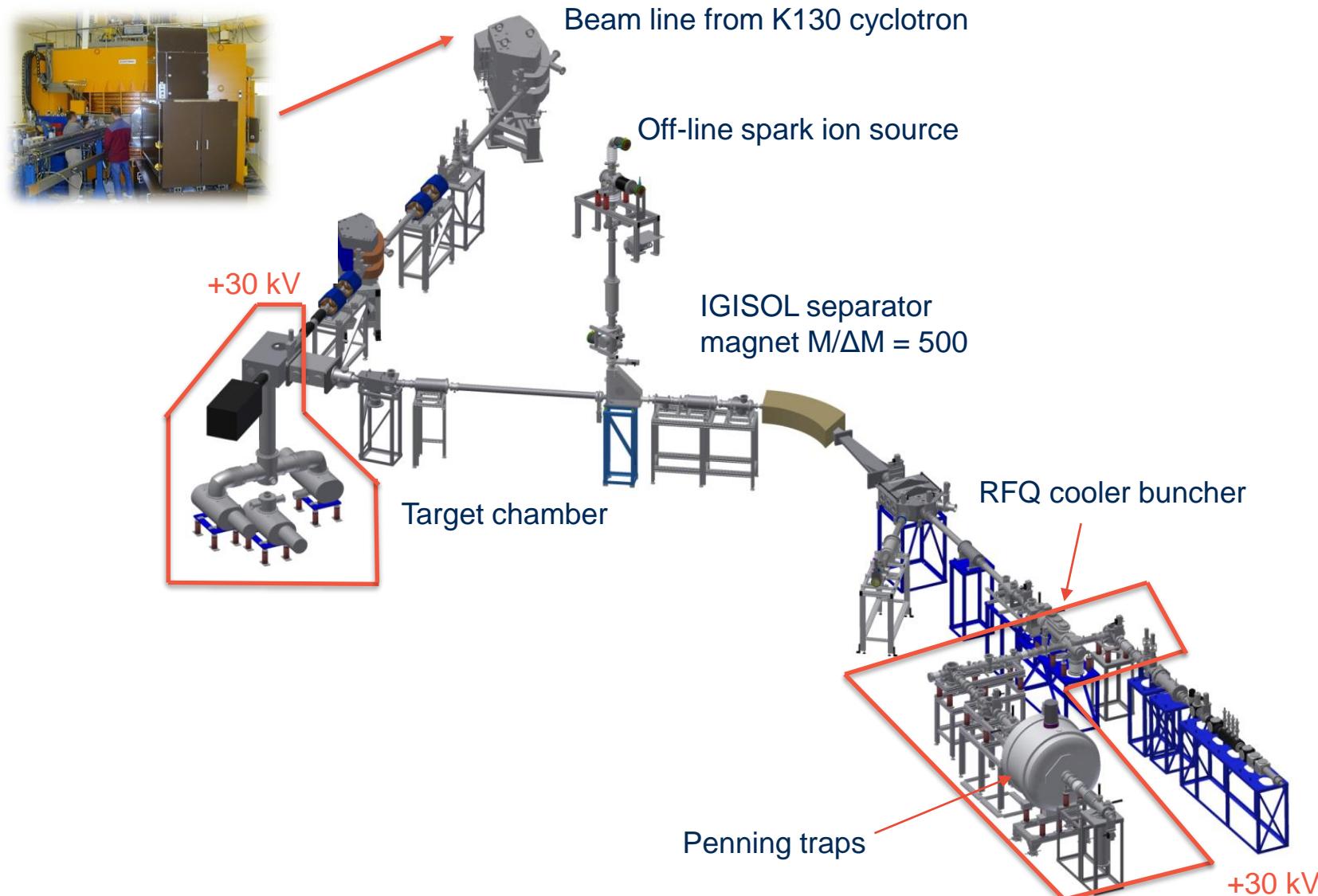
- Many potential candidates
- Need to identify them with Penning traps

B.J. Mount, M. Redshaw, E.G. Myers, Phys. Rev. Lett. 103 122502 (2009)  
J. S. E. Wieslander, Phys. Rev. Lett. 103, 122501 (2009)  
C.M. Cattadori, Nucl. Phys. A, 748, 333-347 (2005)

# Ultra low Q-value $\beta^-$ decay for neutrino physics

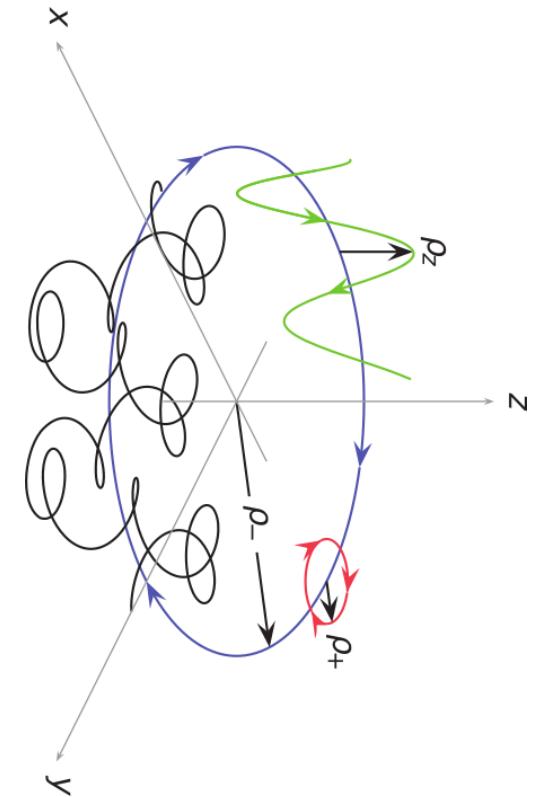
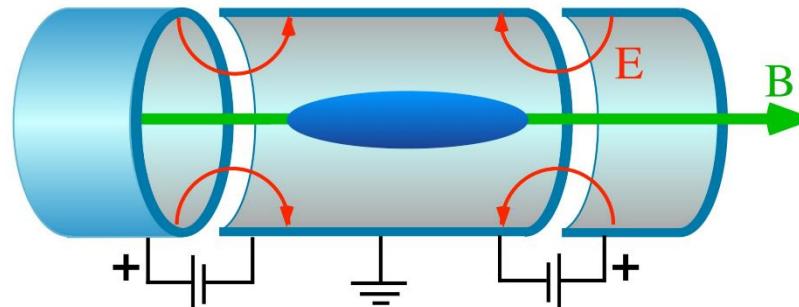
Mother( $J^\pi$ ) <i>Ground state</i>	Daughter ( $J^\pi$ ) <i>Excited state</i>	$E^*$ (keV)	$Q$ (keV)	Type of decay
$^{135}\text{Cs}(7/2^+)$	$^{135}\text{Ba}(11/2^-)$	268.218(20)	0.5(12)	$\beta^-$
$^{159}\text{Dy}(3/2^-)$	$^{159}\text{Tb}(5/2^-)$	363.5449(14)	1.7(12)	EC
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$^{131}\text{I}(7/2^+)$	$^{131}\text{Xe}(9/2^+)$	971.22(13)	-0.42(61)	$\beta^-$

# The IGISOL-4 facility



# Penning trap

- \ Radial confinement
  - strong homogeneous magnetic field
- \ Axial confinement
  - electric field



3 ion motions

- Axial
- Magnetron
- Reduced cyclotron



3 ion frequencies

- $v_z$
- $v_-$
- $v_+$

• Invariance theorem

$$v_c^2 = v_-^2 + v_+^2 + v_z^2$$

• Cyclotron frequency

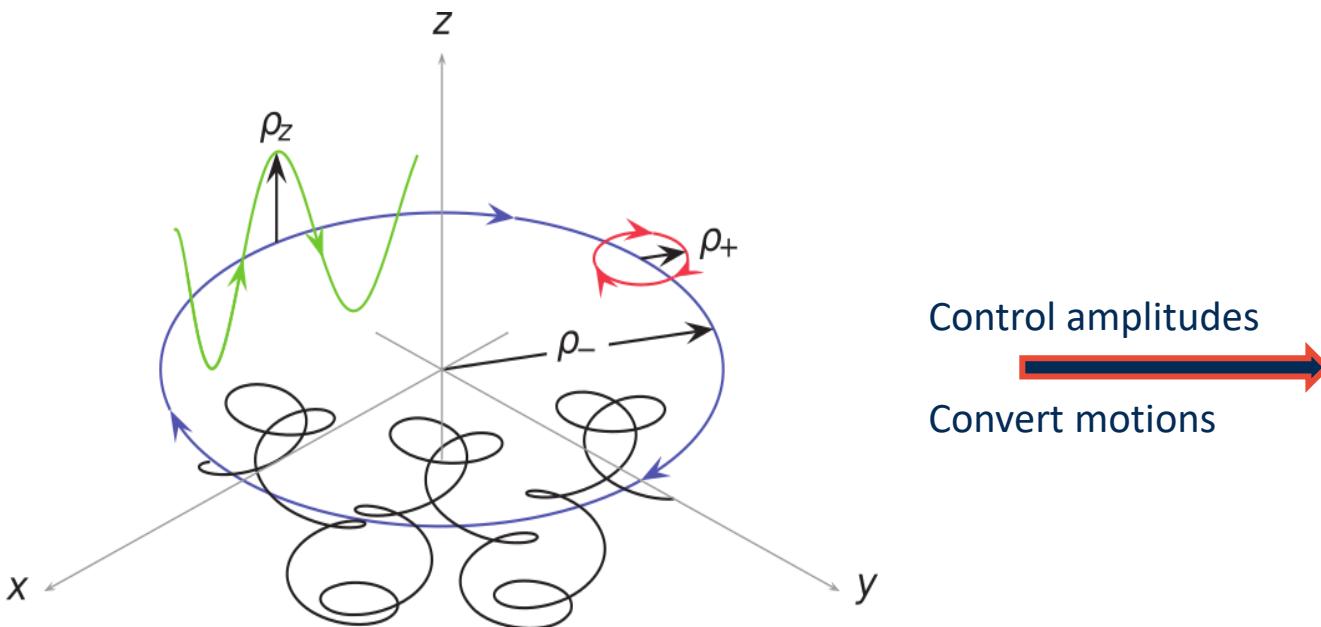
$$v_c = v_- + v_+$$

Cyclotron frequency

$$v_c = \frac{1}{2\pi} \frac{q}{m} B$$

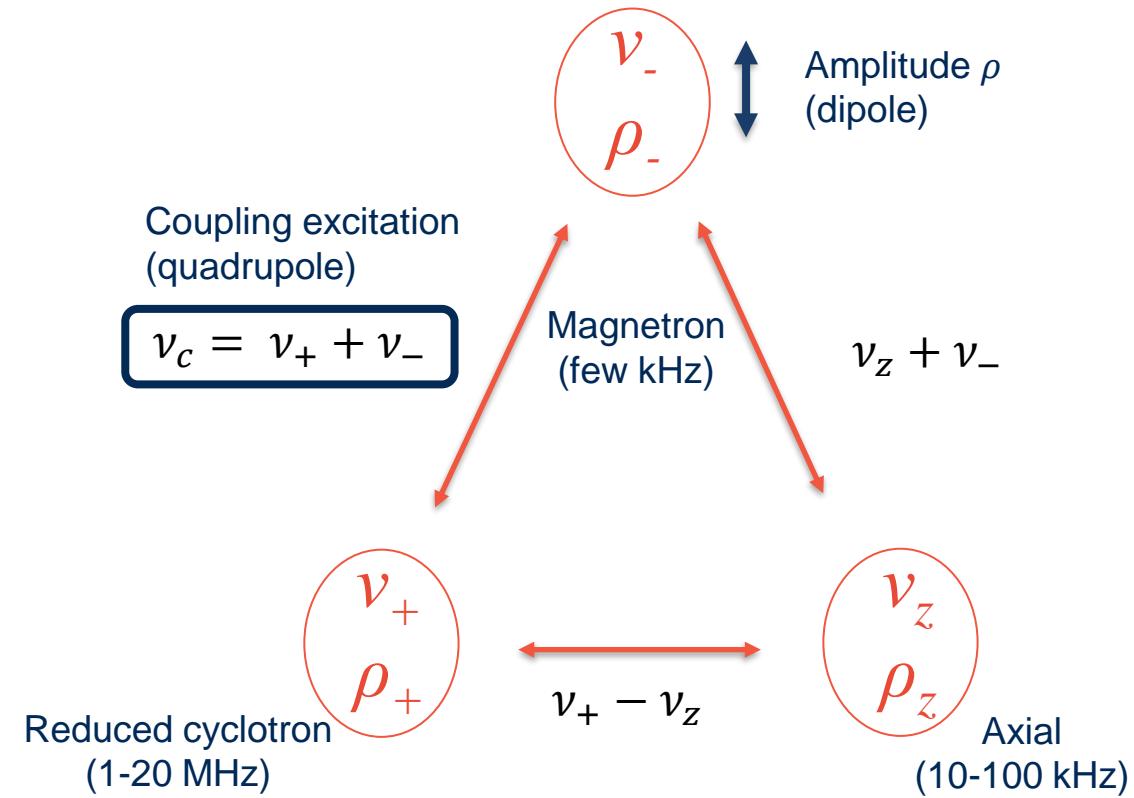
q : electric charge  
B : magnetic field  
m : mass

# Penning trap



Control amplitudes

Convert motions



3 ion motions

- Axial
- Magnetron
- Reduced cyclotron

3 ion frequencies

- $v_z$
- $v_-$
- $v_+$

Invariance theorem

$$v_c^2 = v_-^2 + v_+^2 + v_z^2$$

Cyclotron frequency

$$v_c = v_- + v_+$$

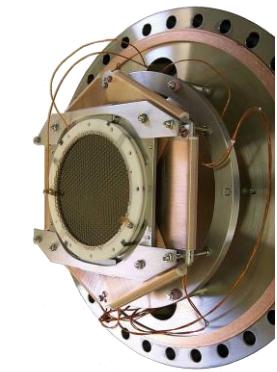
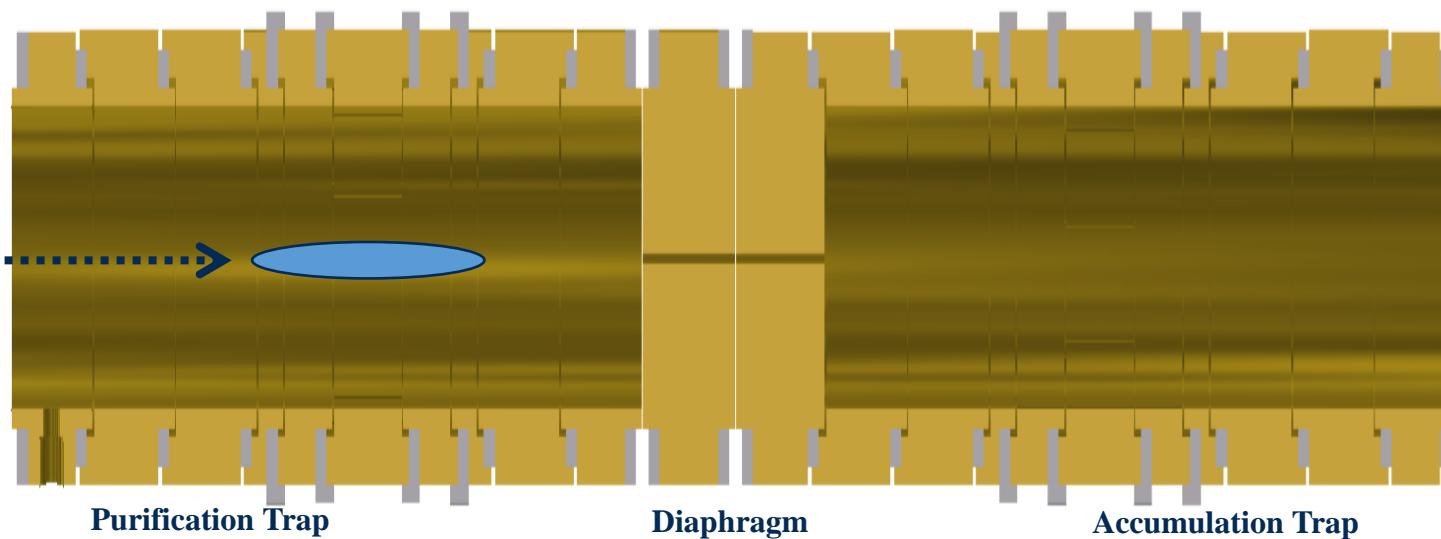
Cyclotron frequency

$$v_c = \frac{1}{2\pi} \frac{q}{m} B$$

q : electric charge  
B : magnetic field  
m : mass

# Buffer gas cooling technique

From RFQ CB



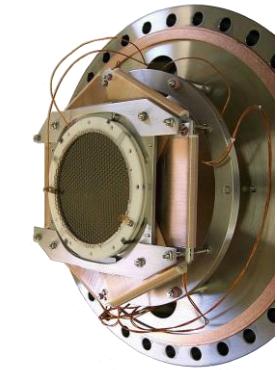
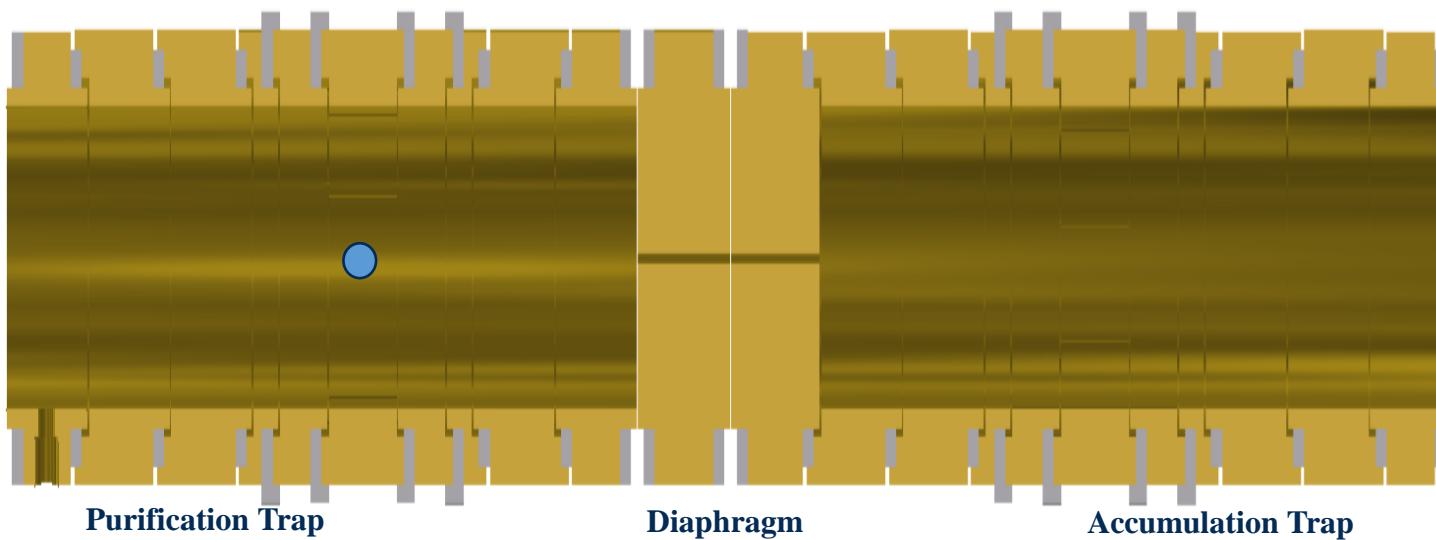
MicroChannel Plate detector  
(position sensitive)

Injection and capture of the ions

➤ 100  $\mu$ s

# Buffer gas cooling technique

From RFQ CB



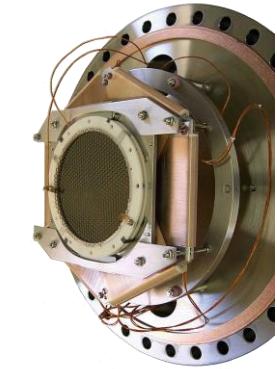
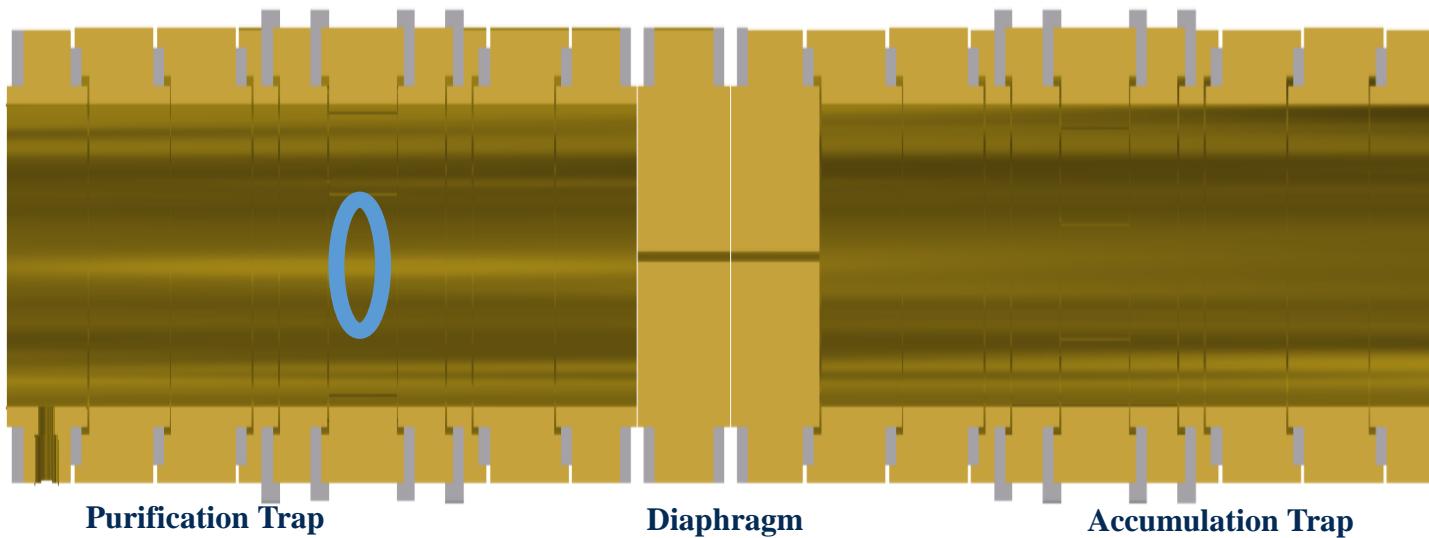
MicroChannel Plate detector  
(position sensitive)

Cooling of radial and axial motions

- 30 - 100 ms

# Buffer gas cooling technique

From RFQ CB



MicroChannel Plate detector  
(position sensitive)

## Buffer gas cooling technique

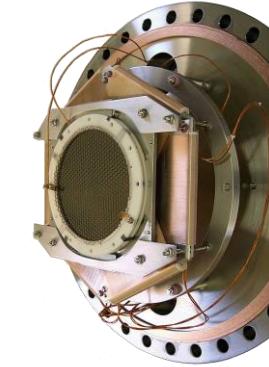
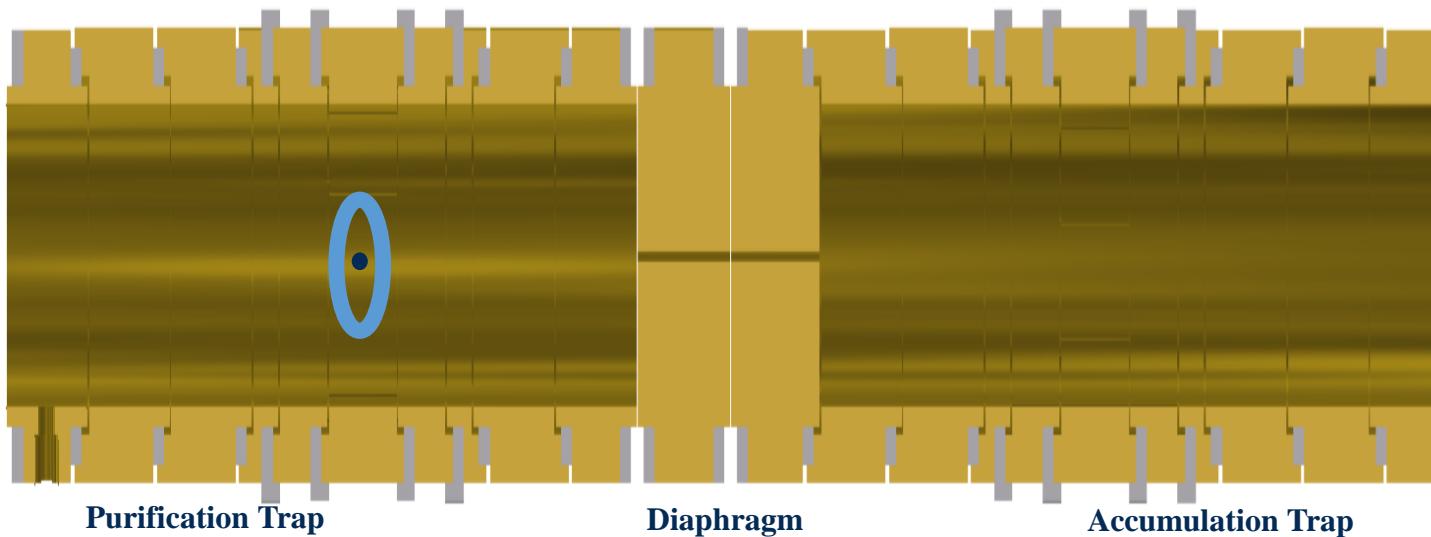
1. Magnetron excitation:  $v_{\perp}$   
➤ 10 ms



This excitation is mass independent

# Buffer gas cooling technique

From RFQ CB



MicroChannel Plate detector  
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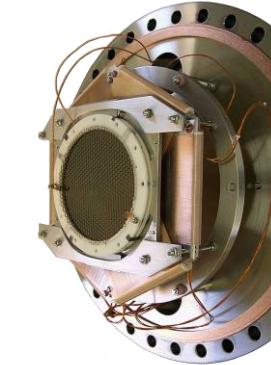
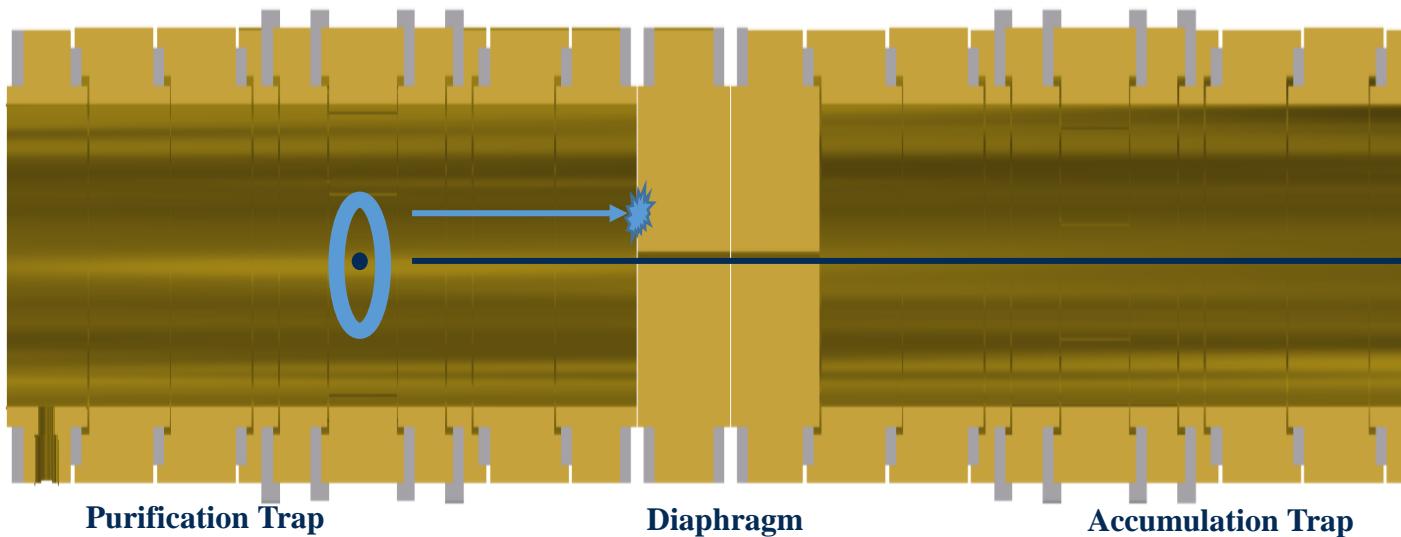
## Buffer gas cooling technique

1. Magnetron excitation:  $v_-$ 
  - 10 ms
2. Quadrupole excitation:  $v_c = v_+ + v_-$ 
  - Convert the radial magnetron motion ( $v_-$ ) into modified cyclotron motion ( $v_+$ )
  - 40 – 400 ms
  - Centering the « good guys »



This excitation is mass **dependent !!**  
Magnetron motion is amplified  
modified cyclotron motion is damped

# Buffer gas cooling technique



MicroChannel Plate detector  
(position sensitive)

## \ Mass resolving power of Penning trap

$$R = \frac{M}{\Delta M} = \frac{v_c}{\Delta v_c} \propto \frac{1}{\Delta v_d} \frac{q}{m} B \rightarrow \text{Scaling}$$

Constant for each method 0.1 ... 100 Hz

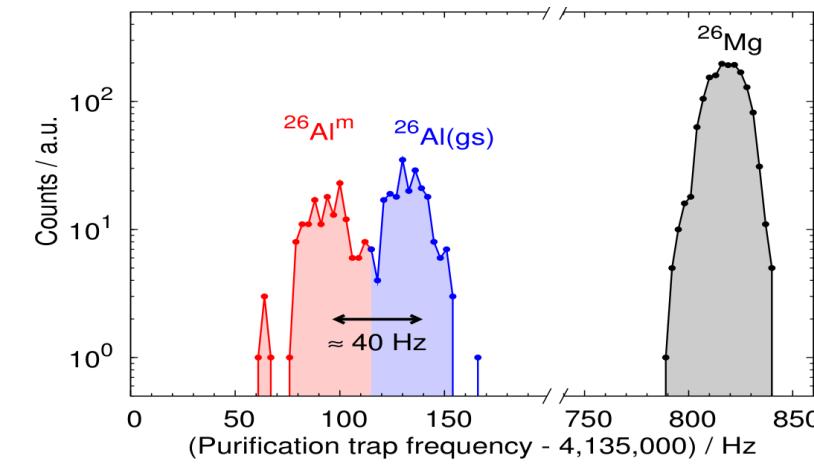
## \ Rule of thumb:

$$B = 7 \text{ T}, q = 1e, m = 100u \\ \rightarrow v_c \sim 1 \text{ MHz}, 100 \text{ keV/Hz}$$

## \ Buffer gas cooling technique

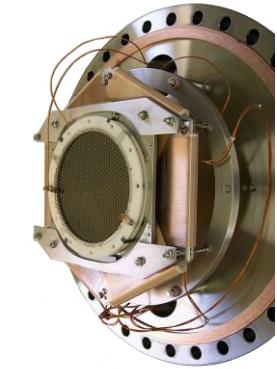
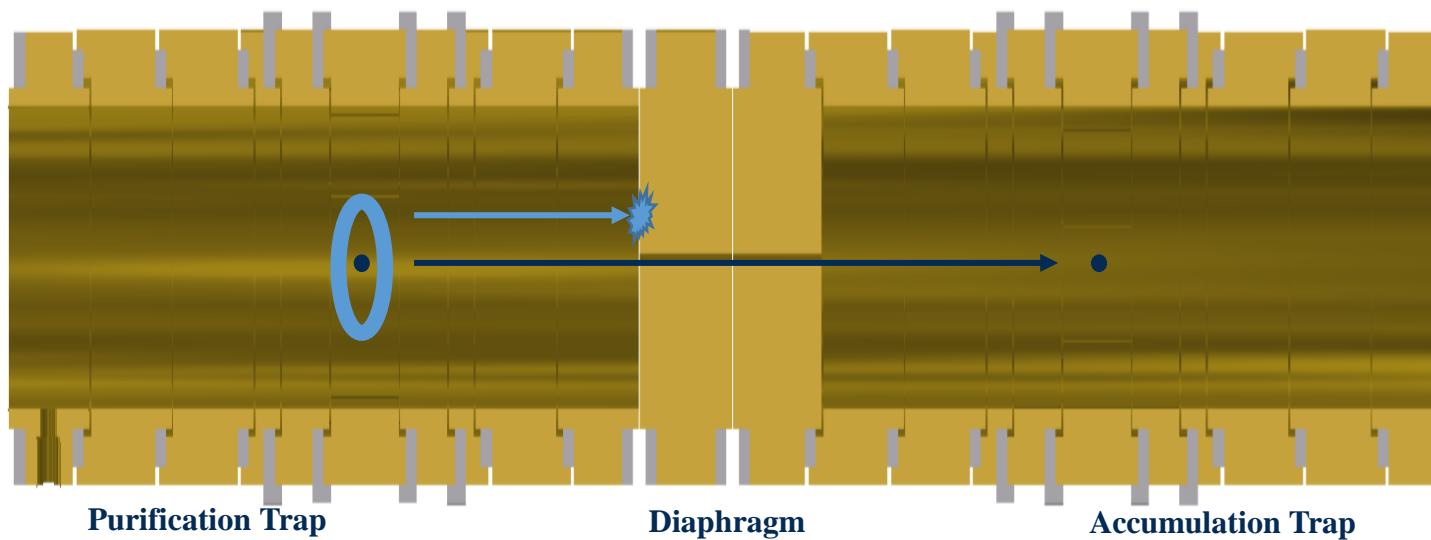
- Gas filled purification trap
- Separation
  - 10 ... 100 Hz
  - $R = 10^4 \dots 10^5$
- Also cooling

G. Savard et al., Phys. Lett. A 158 (1991) 247–252



# Time-of-flight ion cyclotron resonance technique (ToF-ICR)

From RFQ CB



MicroChannel Plate detector  
(position sensitive)

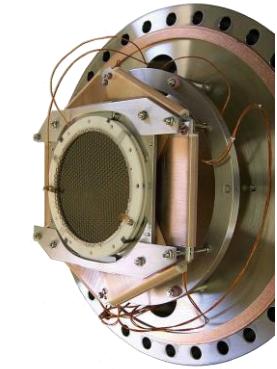
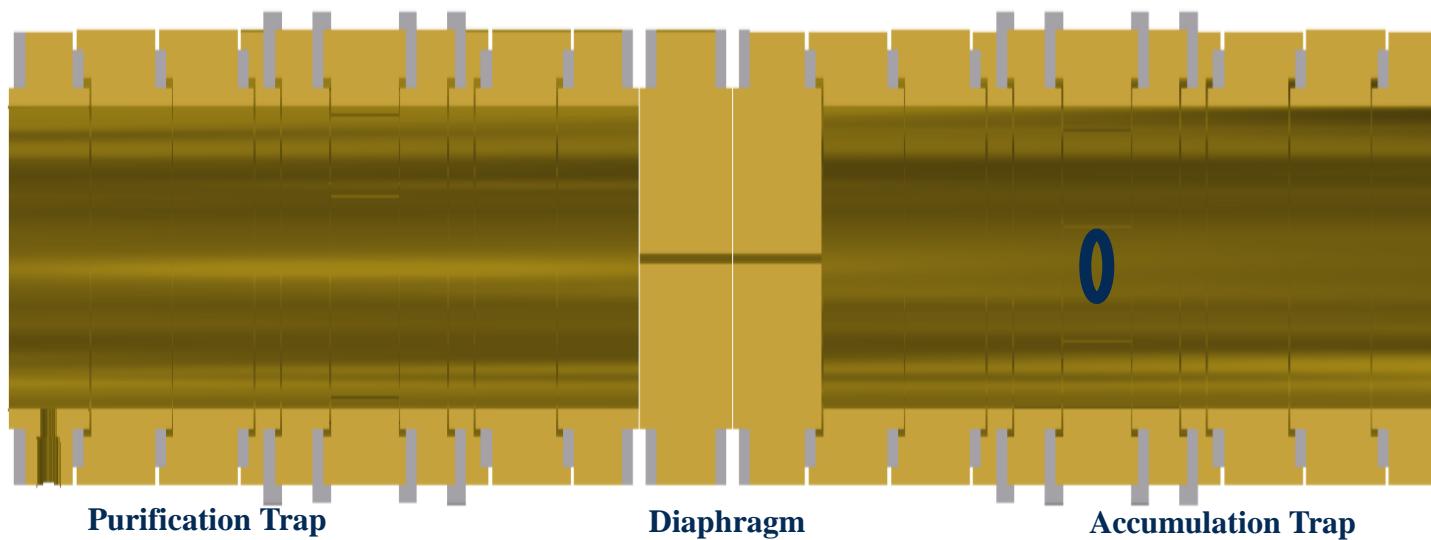
ToF-ICR technique (Time-of-Flight Ion Cyclotron Resonance)



Transfer of the clean ion sample to the measurement trap

# Time-of-flight ion cyclotron resonance technique (ToF-ICR)

From RFQ CB



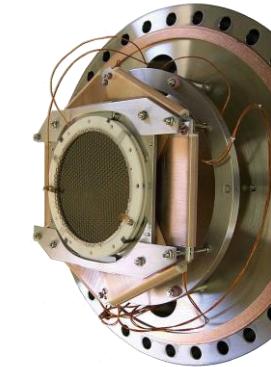
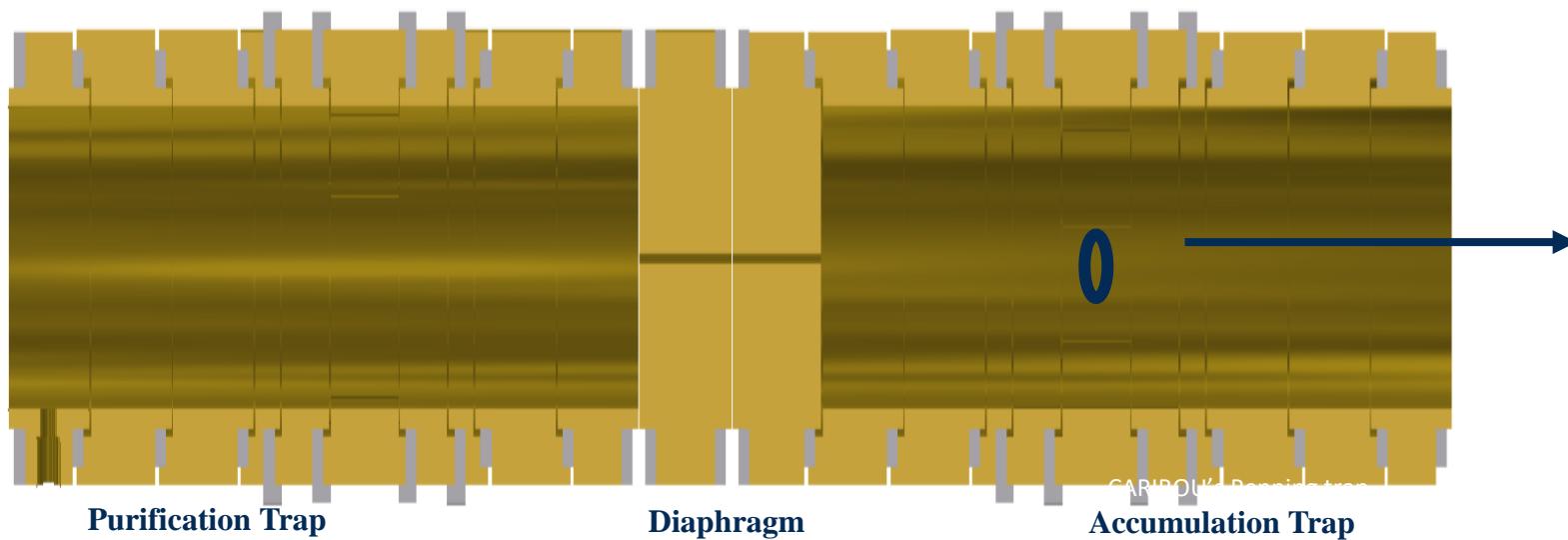
MicroChannel Plate detector  
(position sensitive)

## ToF-ICR technique

1. Magnetron excitation:  $v_\perp$ 
  - 10 ms
  - Give a slow radial motion to the ions

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MicroChannel Plate detector  
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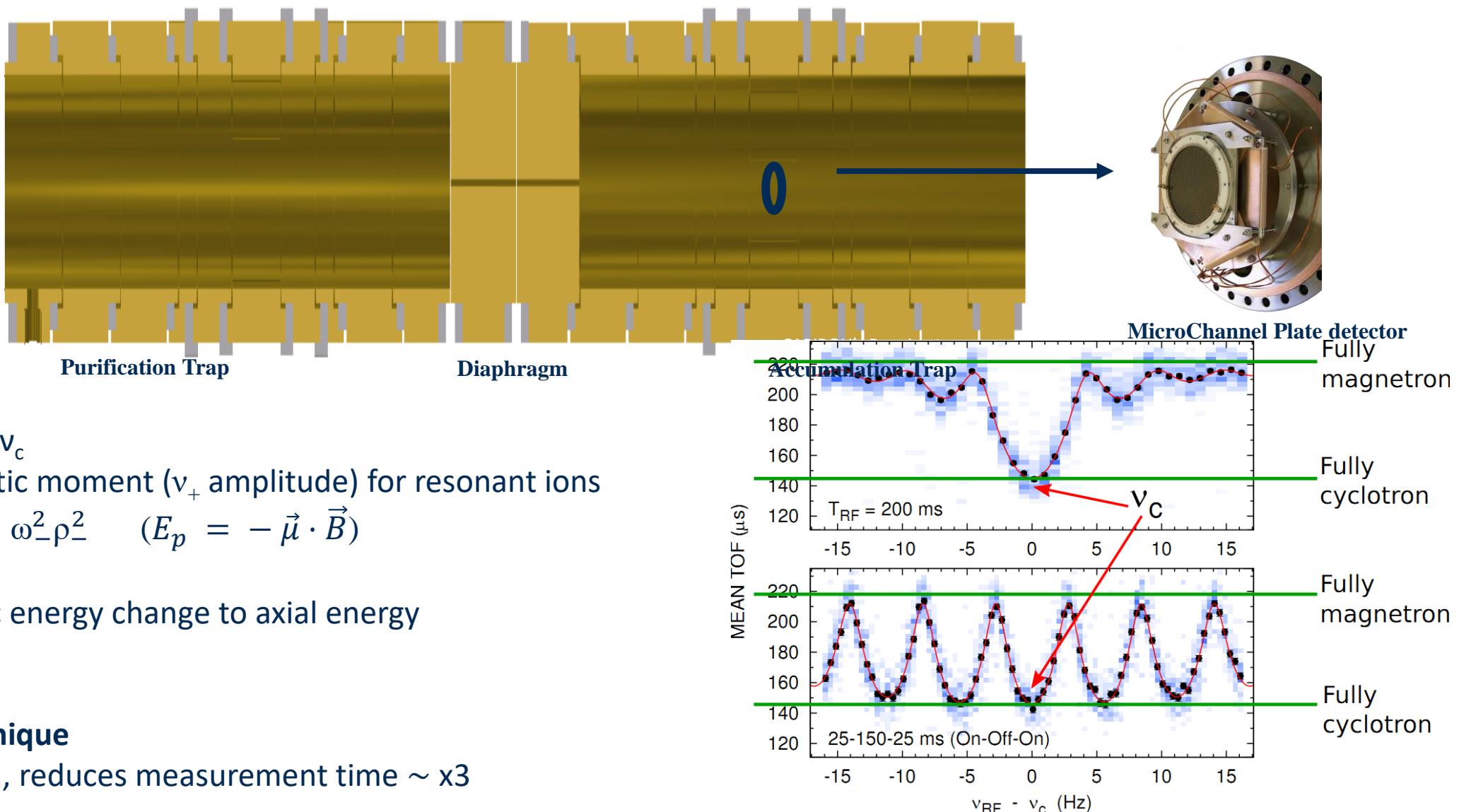
## ToF-ICR technique

1. Magnetron excitation:  $v_-$ 
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  - Give a slow radial motion to the ions
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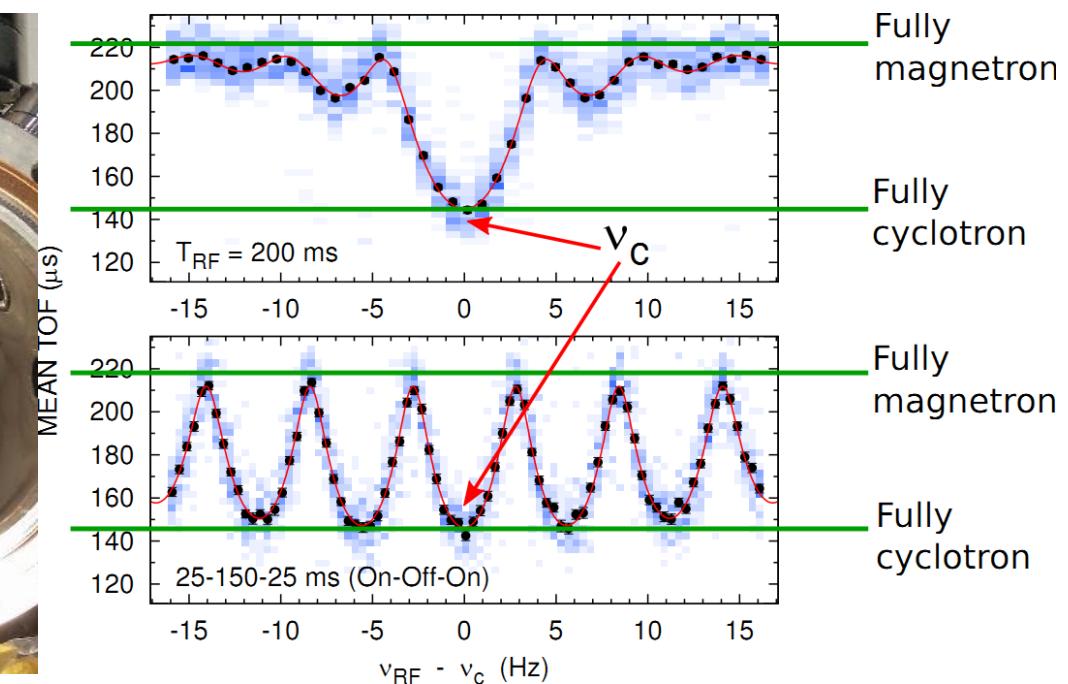
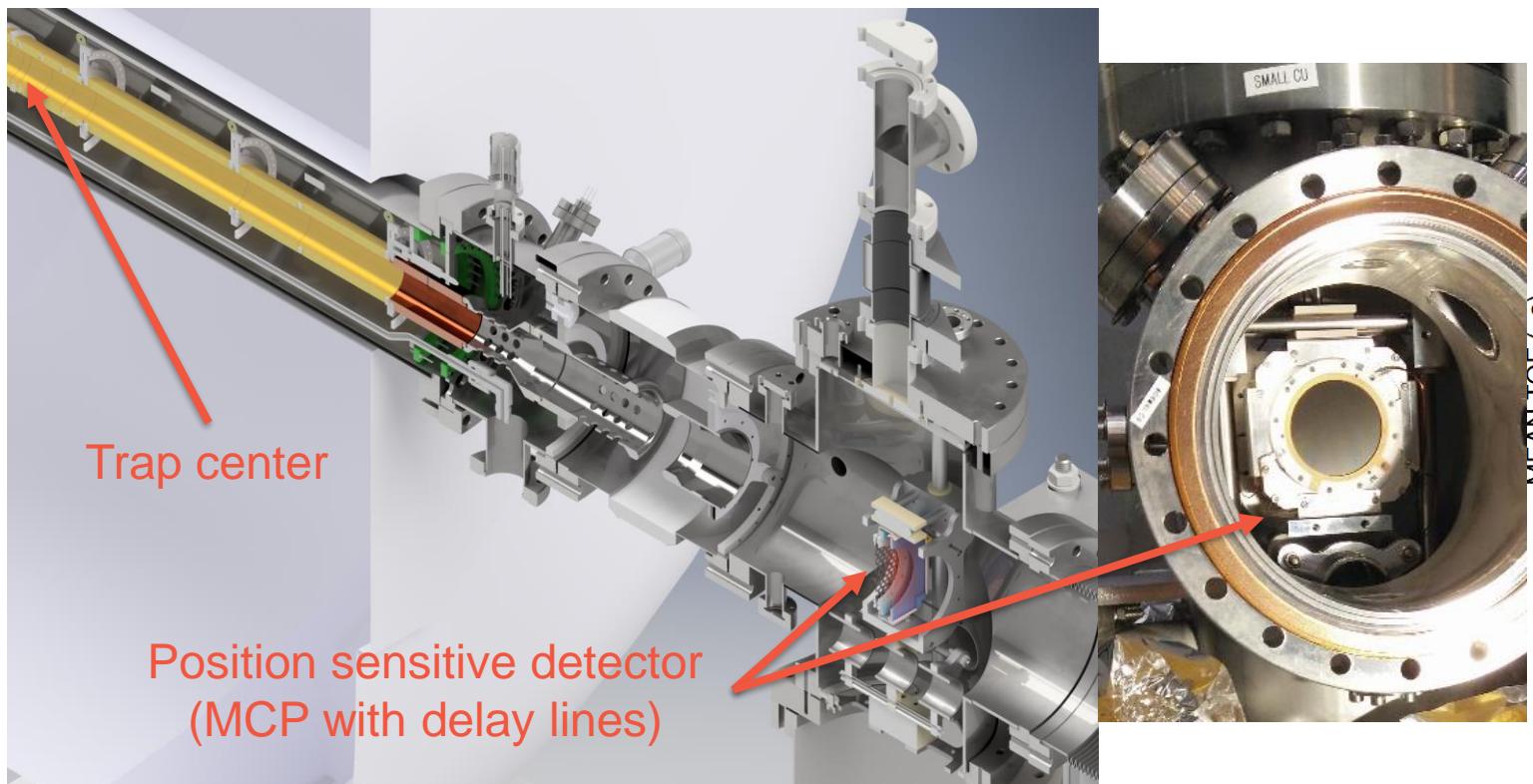


- \ The modified cyclotron motion is a fast motion
- \ The ions are not recentered (no gas)
- \ Extraction towards the MCP

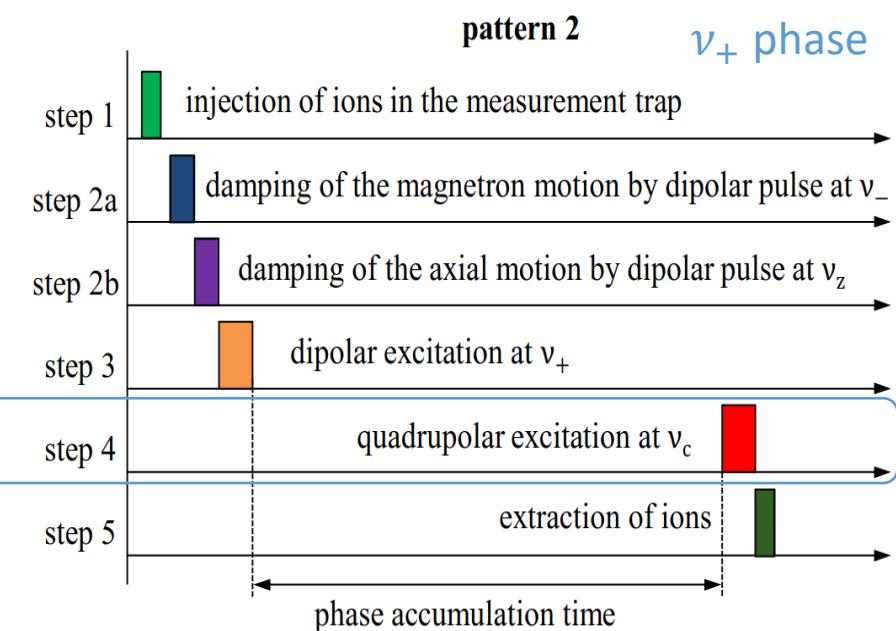
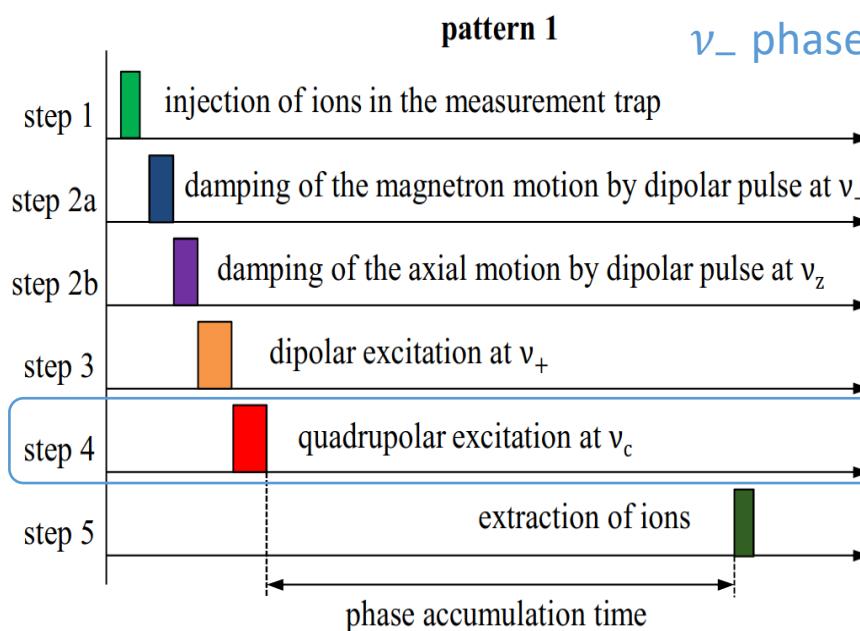
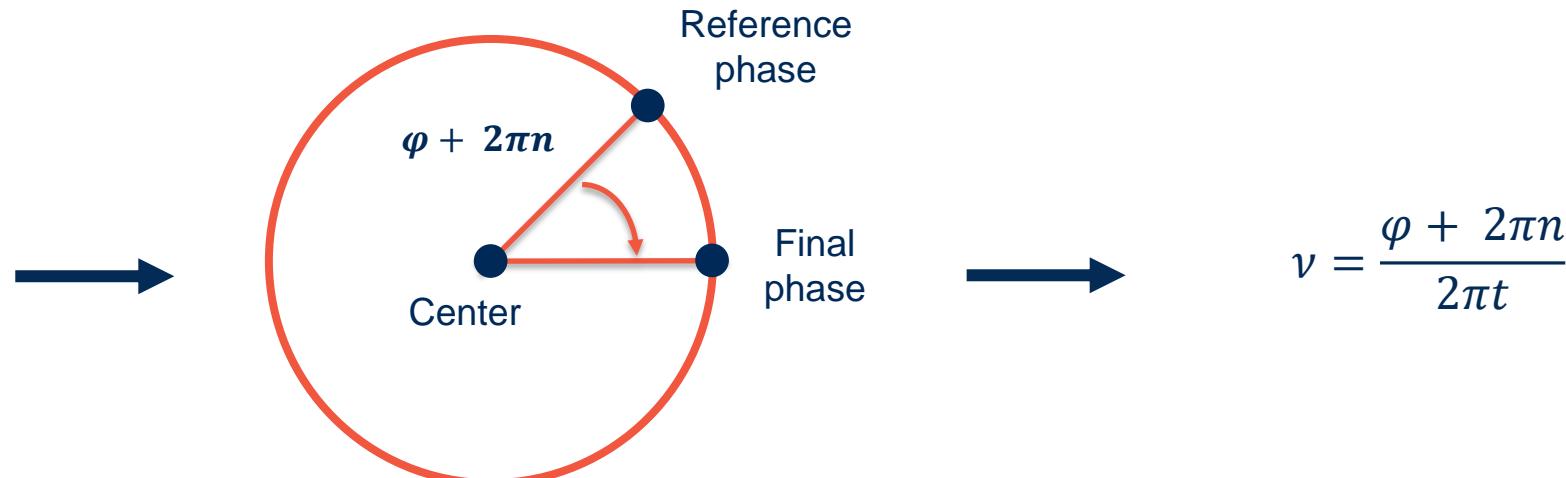
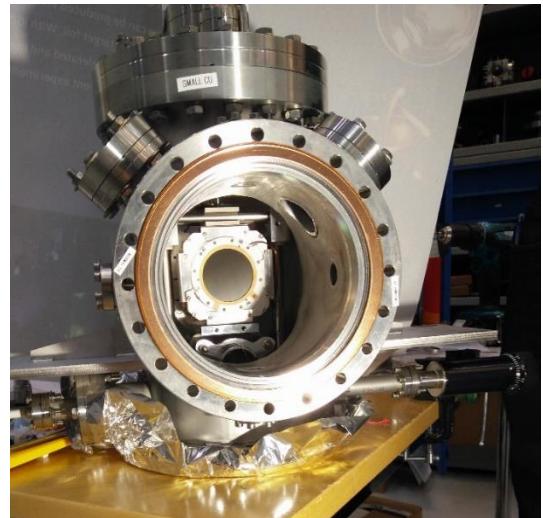
# Time-of-flight ion cyclotron resonance technique (ToF-ICR)



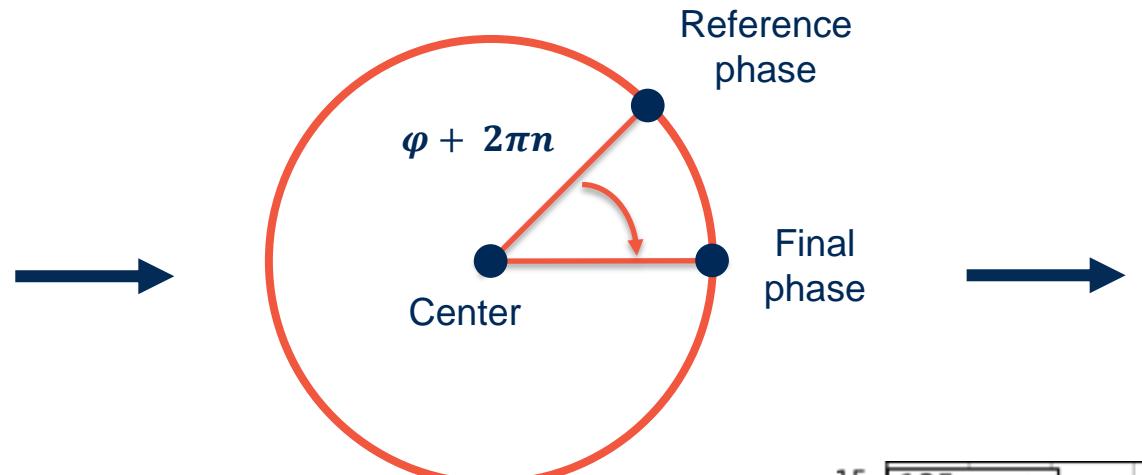
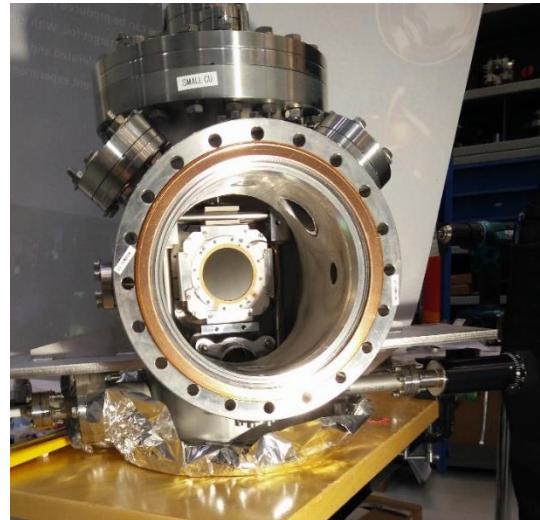
# Position sensitive detector



# Phase-imaging ion cyclotron resonance technique (PI-ICR)



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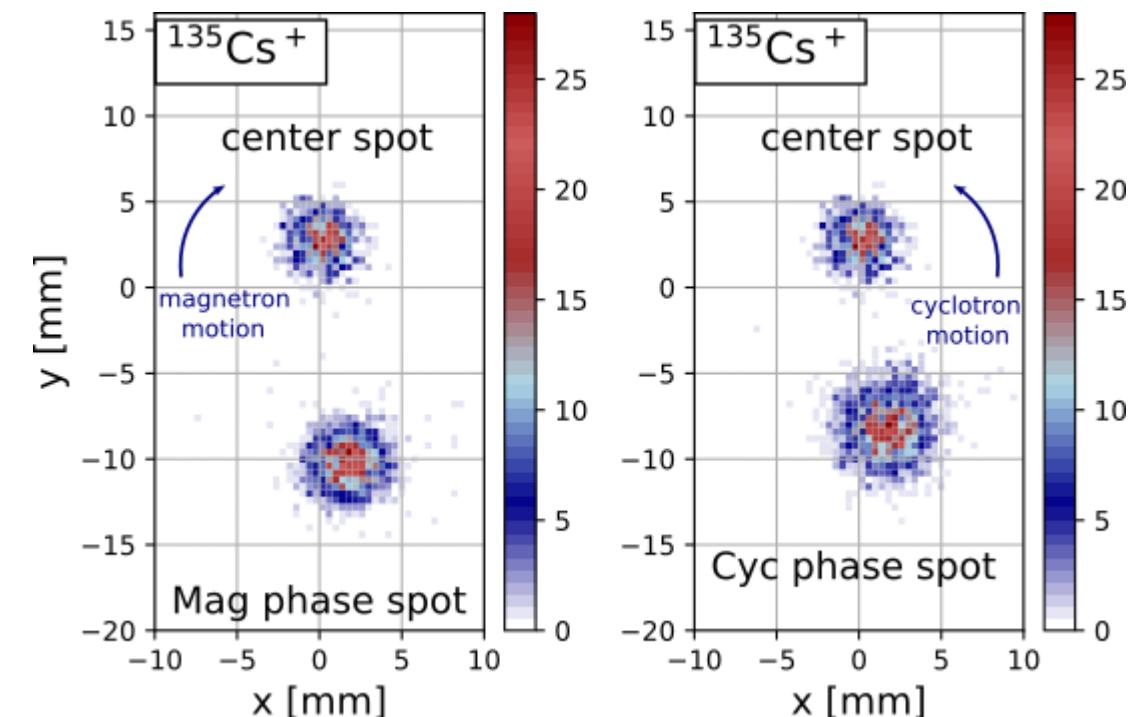
$$\nu = \frac{\varphi + 2\pi n}{2\pi t}$$

## Advantages of PI-ICR over TOF-ICR:

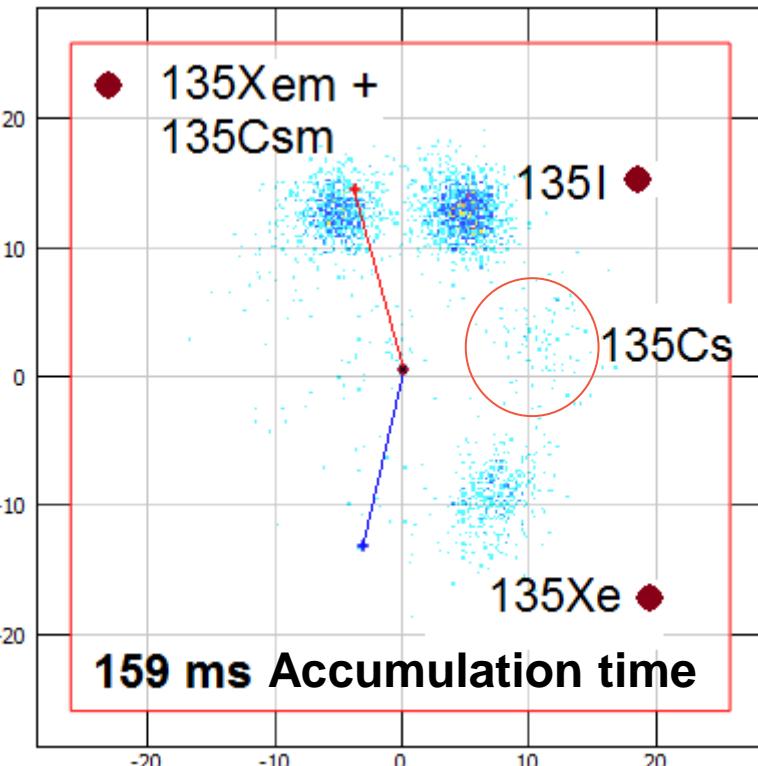
- No scanning of frequency, just data collection to one spot
- x40 faster x5 increase in precision

## Requirements:

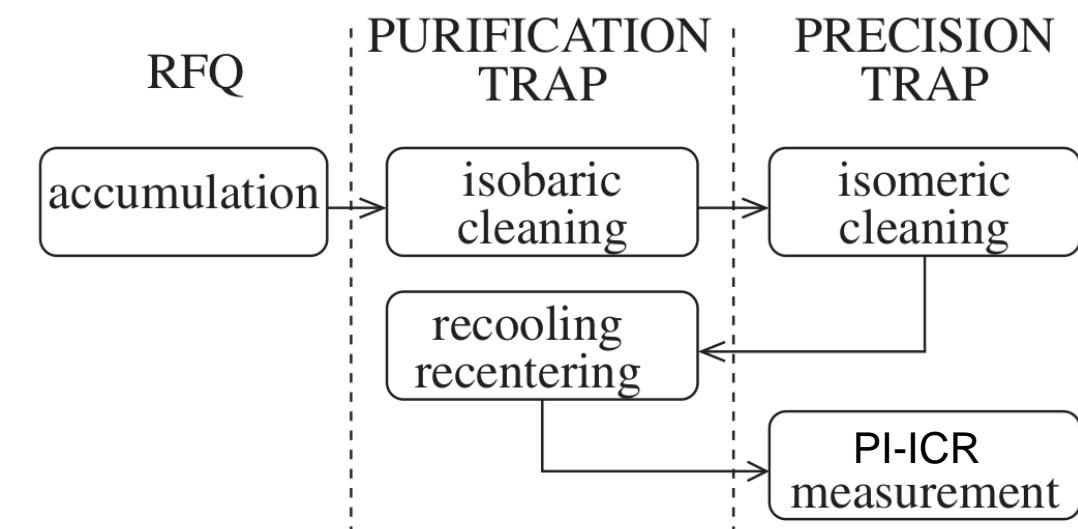
- Need to prepare the ion more carefully
- Damping of ion motions; longer setting up time
- Sensitive to voltage fluctuations



# Isomeric cleaning



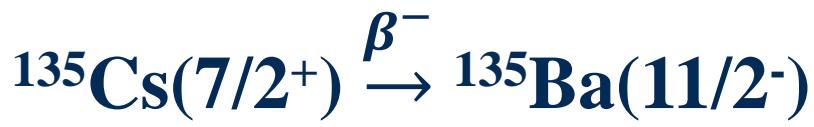
Ramsey cleaning



Same cleaning processed was needed for different measurements presented here

# Ultra low Q-value $\beta$ decay for neutrino physics

Mother( $J^\pi$ ) <i>Ground state</i>	Daughter ( $J^\pi$ ) <i>Excited state</i>	$E^*$ (keV)	$Q$ (keV)	Type of decay
$^{111}\text{In}(9/2^+)$	$^{111}\text{Cd}(7/2^+)$	853.94(7)	6.3(34)	EC
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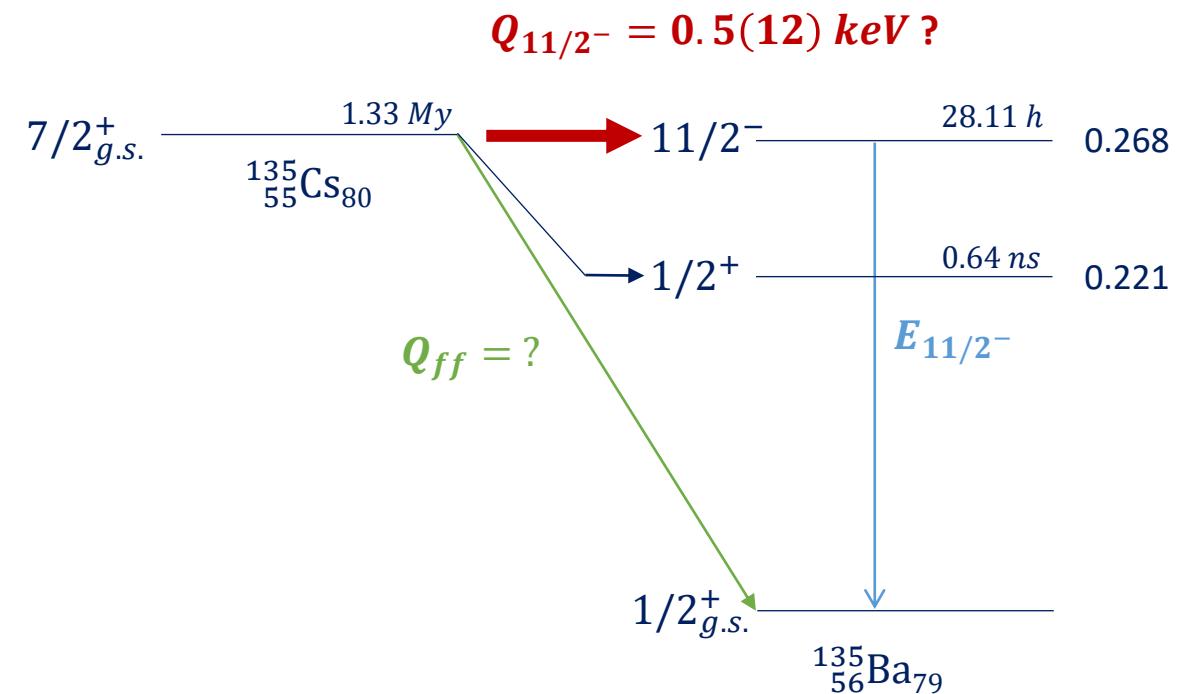


**But :** The transition is poorly known!

- Not yet proven that it is energetically possible :  $Q_{11/2^-} < 0$  ?
- Decay never observed directly

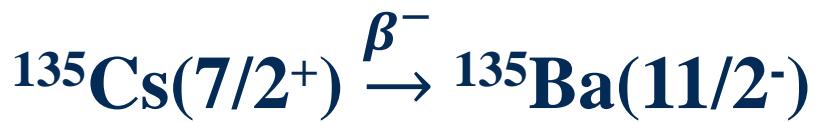
To determine  $Q_{11/2^-}$  we need:

- The excitation energy  $E_{11/2^-} = 268.218(20) \text{ keV}$
- The ground-state-to-ground-state Q-value  $Q_{ff}$
- $Q_{ff} = 268.9(1.1) \text{ keV}$  [1]



$$Q_{ff} = 268.9(1.1) \text{ keV} \rightarrow Q_{11/2^-} = 0.5(1.2) \text{ keV}$$

New measurement of  $Q_{ff}$  with Penning traps!!



$$Q_{gs-gs} = 268.66(30) \text{ keV}$$

$$\rightarrow Q_{11/2^-} = 0.44(31) \text{ keV}$$

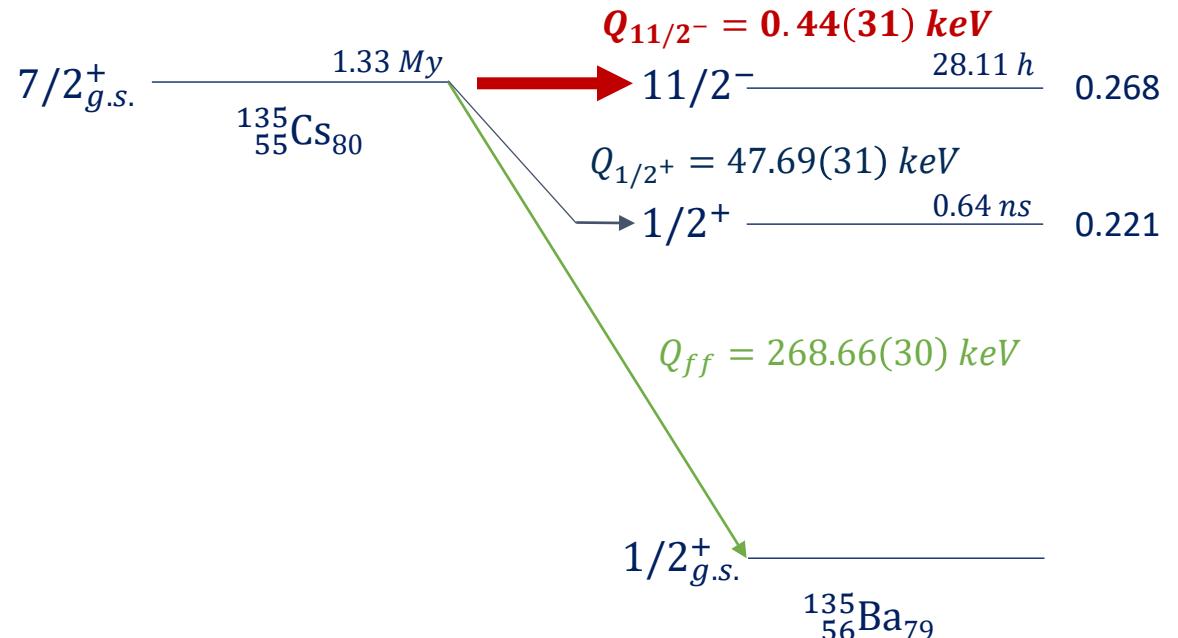
$$\rightarrow Q_{1/2^+} = 47.69(31) \text{ keV}$$

Half-lives calculations computed with NuShell@MSU

- $T_{1/2}({}^{135}\text{Ba}(11/2^-)) = 8.2(32) \cdot 10^{11} \text{ y}$
- $T_{1/2}({}^{135}\text{Ba}(1/2^+)) = 6.5(17) \cdot 10^{13} \text{ y}$



Branching ratio  $(0.04 - 16) \cdot 10^{-6}$



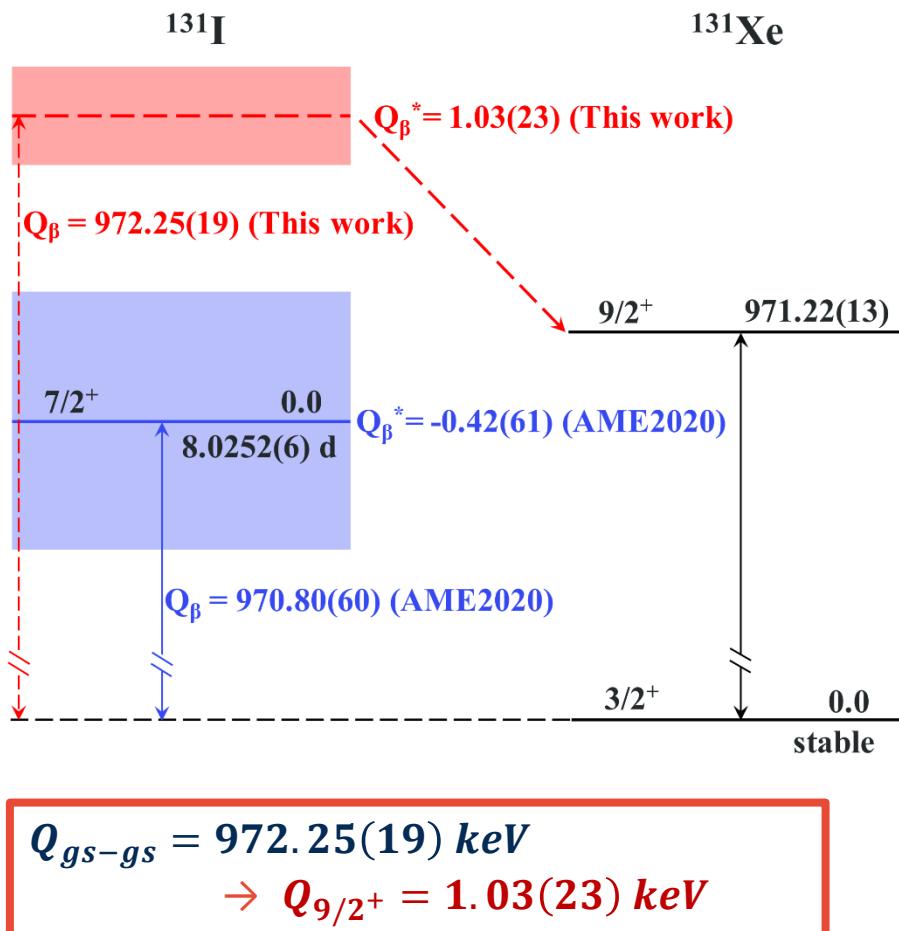
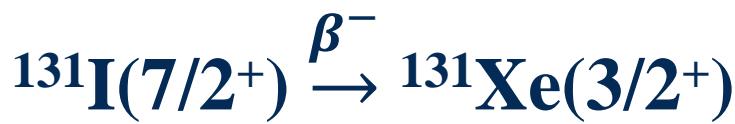
A. de Roubin et al., Phys. Rev. Lett. A **124**, 222503 (2020)

### Conclusion:

- ${}^{135}\text{Cs}(7/2^+) \rightarrow {}^{135}\text{Ba}(11/2^-) > 0$
- First direct Q value measurement
- Direct measurement of the antineutrino mass?

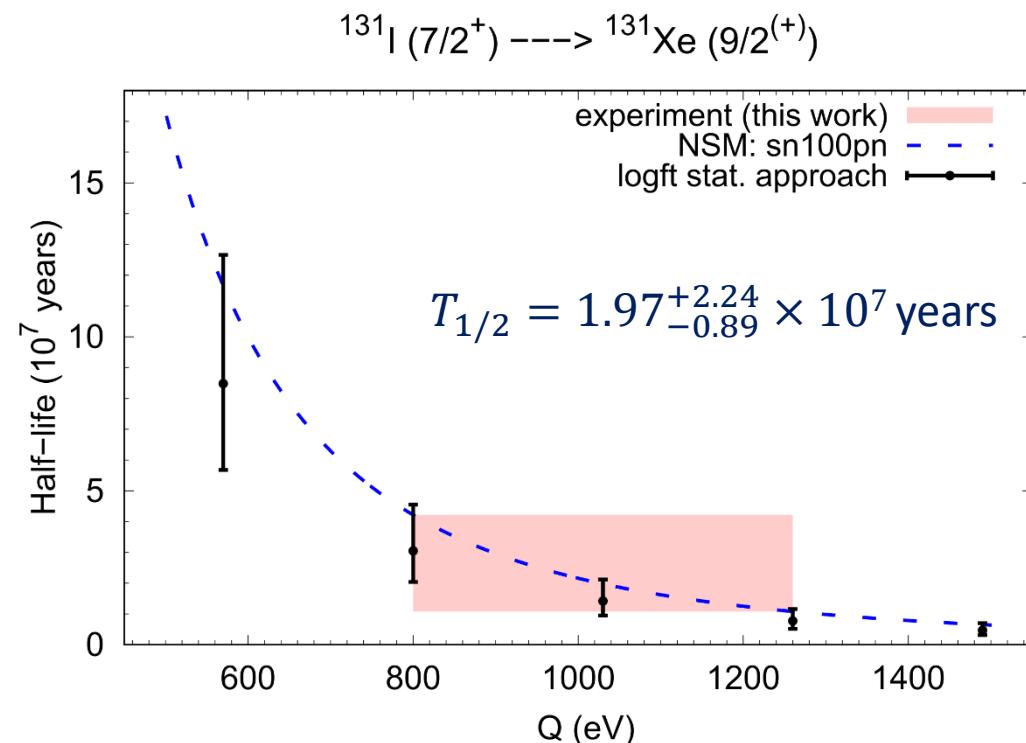
### Expected challenges:

- Half-life of the 11/2- state too long
- Cannot be used in coincidence



Half-lives calculations for this transition

- Nuclear shell model calculations with NuShellX  
*B. Brown, W. Rae, Nucl. Data Sheets 120, 115 (2014)*
- Partial half-life is extremely sensitive to the exact value of the decay energy



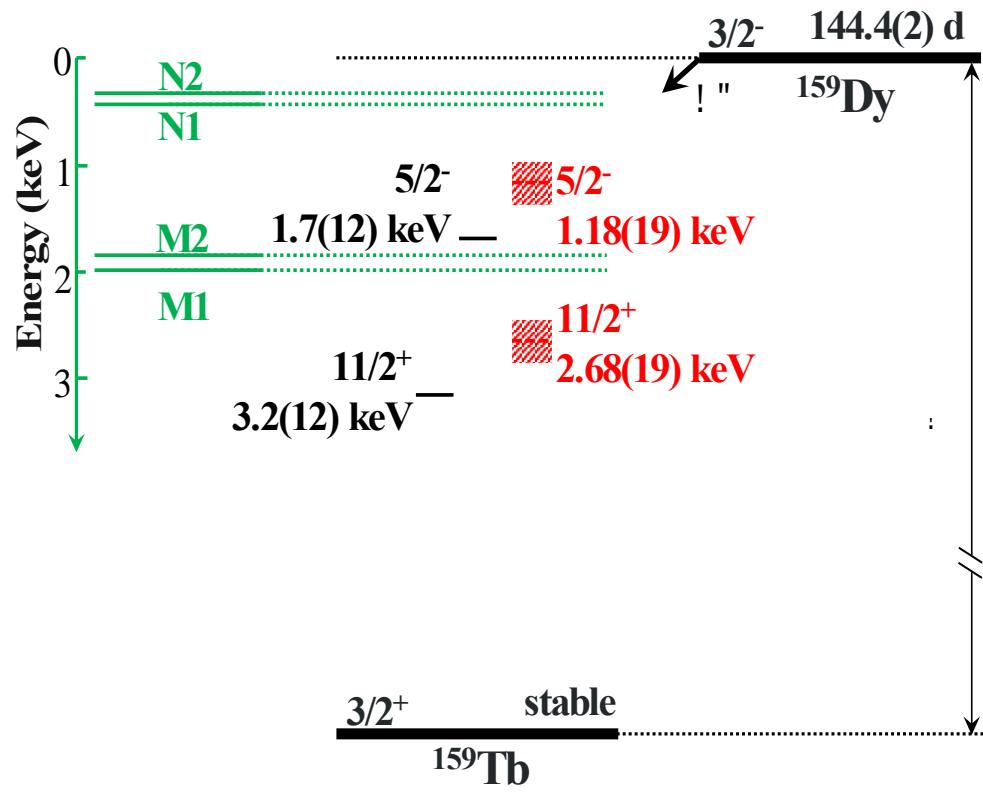
T. Eronen et al. accepted for publication in PLB

#### Conclusion:

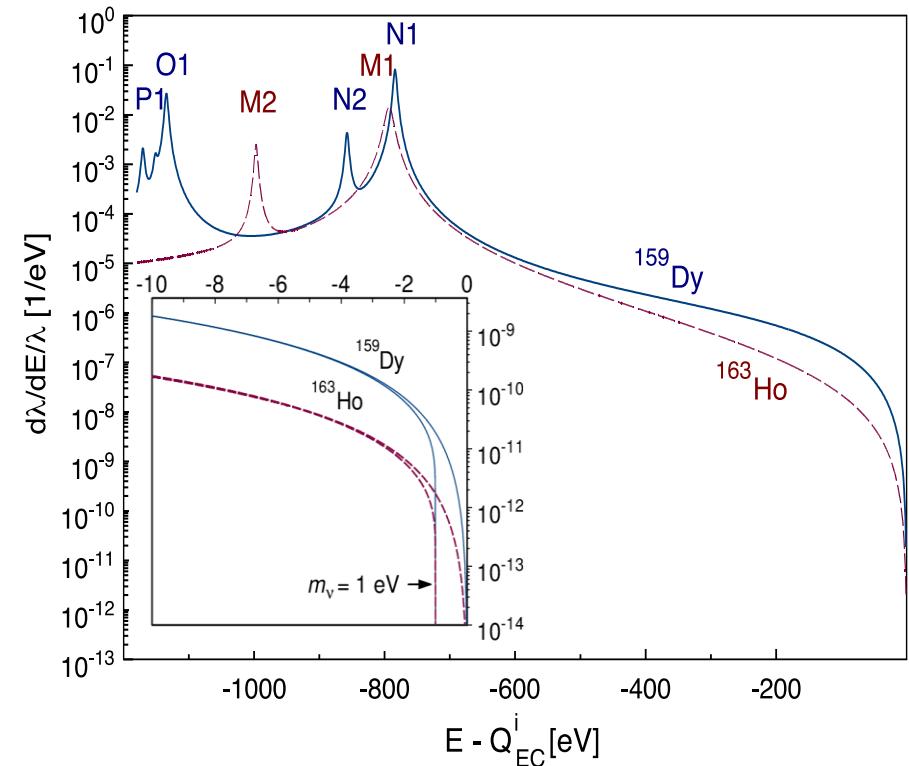
- The decay  $7/2^+ \rightarrow 9/2^+$  is of allowed type
- The transition has a simple universal shape

#### Expected challenge:

- The branching ratio  $\sim 10^{-10}$



EC spectrum of  $^{159}\text{Dy}$  ( $3/2^- \rightarrow 5/2^-$ ) compared to  $^{163}\text{Ho}$   
(Dirac-Hartree-Fock atomic many-body calculations)



Courtesy of Z. Ge

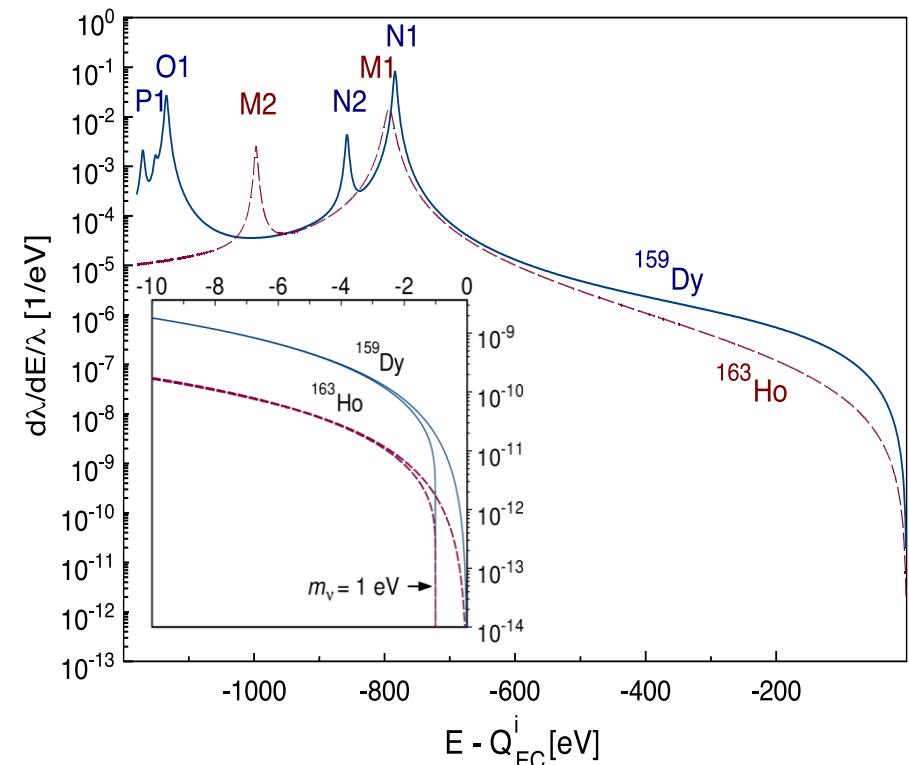
Z. Ge, T. Eronen, K. S. Tyrin et al., Phys. Rev. Lett. 127, 272301 (2021)



$$Q_{\text{EC}}^* = 1.18(19) \text{ keV}$$

- Lowest EC Q value
- Lower than the GS-to-GS  $Q_{\text{EC}}$  of  $^{163}\text{Ho}$ , utilized in presently running or planned direct neutrino mass experiments
- allowed transition
- known branching ratio  $1.9(5) \times 10^{-6}$
- Smallest EC Q value
  - ➡ The most promising gs-to-excited state transition for future calorimetric experiment

EC spectrum of  $^{159}\text{Dy}$  ( $3/2^- \rightarrow 5/2^-$ ) compared to  $^{163}\text{Ho}$   
(Dirac-Hartree-Fock atomic many-body calculations)



Courtesy of Z. Ge

Z. Ge, T. Eronen, K. S. Tyrin et al., Phys. Rev. Lett. 127, 272301 (2021)

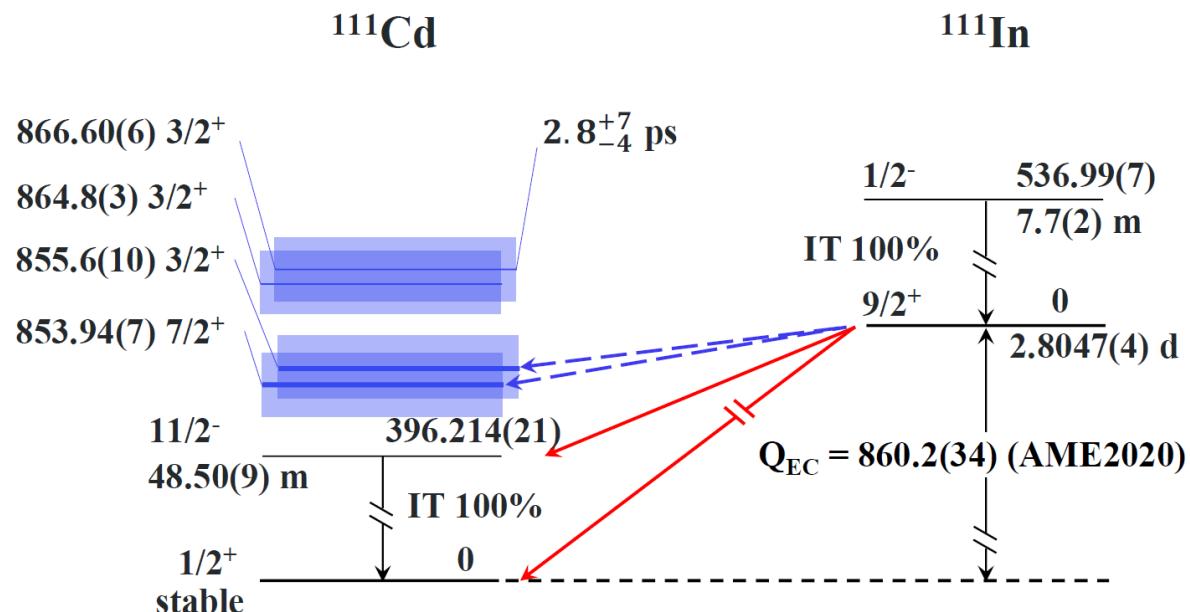
# $^{111}\text{In}(9/2^+) \xrightarrow{EC} {}^{111}\text{Cd}(7/2^+)$

$$Q_{gs-gs} = 857.63(17) \text{ keV}$$

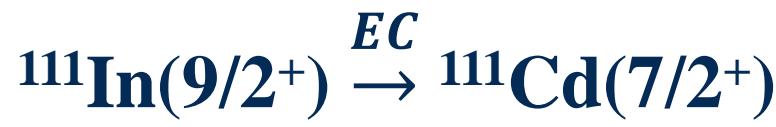
Mother( $J^\pi$ )	Daughter ( $J^\pi$ )	$E^*$ (keV)	$Q$ (keV)	Decay type
$^{111}\text{In}(9/2^+)$	$^{111}\text{Cd}(7/2^+)$	853.94(7)	3.69(19)	allowed
$^{111}\text{Cd}(3/2^+)$	$^{111}\text{Cd}(3/2^+)$	855.6(10)	2.0(10)	2 <sup>nd</sup> FU
$^{111}\text{Cd}(3/2^+)$	$^{111}\text{Cd}(3/2^+)$	864.8(3)	-7.17(35)	
$^{111}\text{Cd}(3/2^+)$	$^{111}\text{Cd}(3/2^+)$	866.60(6)	-8.97(18)	

Estimated half-life for  $9/2^+ \rightarrow 3/2^+$  transition  $t_{1/2} = 5.6 \times 10^{17}$

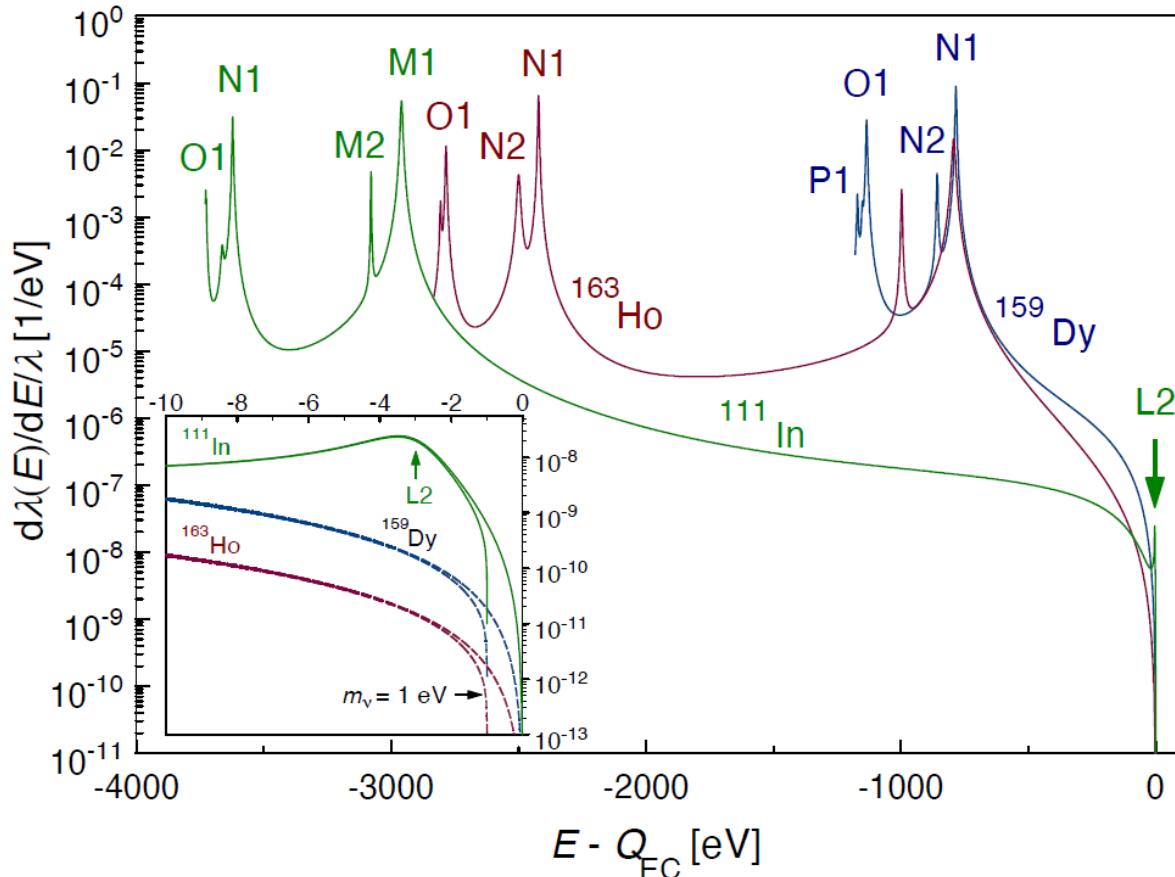
➤ Transition excluded!



Z. Ge et al., submitted to Elsevier



EC spectrum of  $^{111}\text{In}(9/2^+ \rightarrow 5/2^-)$  compared to  $^{163}\text{Ho}$  and  $^{159}\text{Dy}$



- EC spectrum shape investigated with atomic Dirac-HF many-body calculations
- Presence of a L2 resonance near the end point (3 eV)
- Increases significantly the counting rate in the ROI

$$Q = 2.0(10) \text{ keV}$$

Need more precise excitation energy measurement !

Z. Ge et al., arXiv:2201.12573v1

# Summary of the measured Q-values of potential candidates

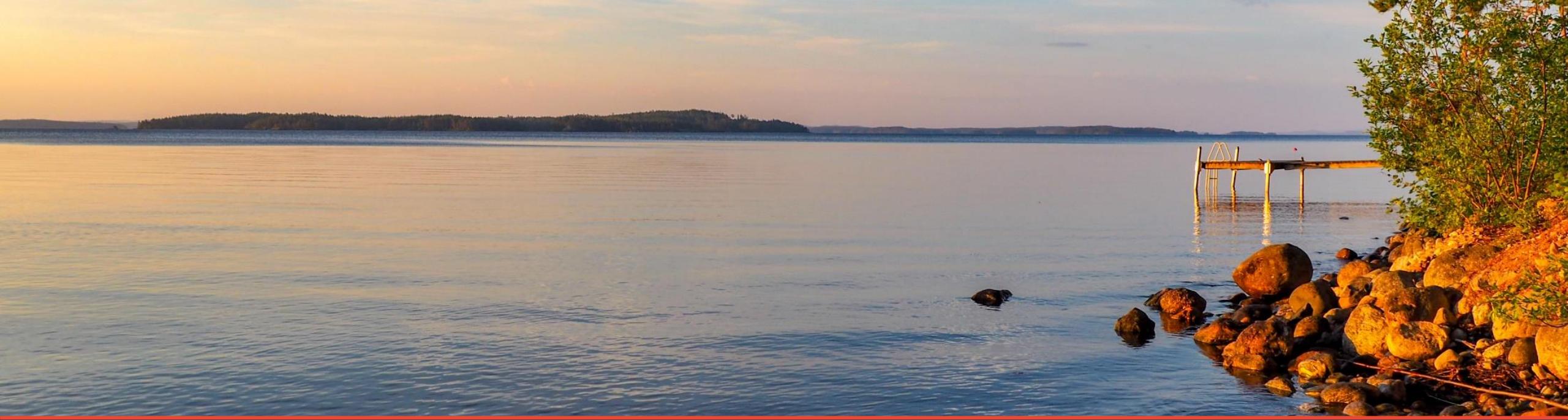
- List of measured promising low Q-value decay candidates for neutrino mass determination

Parent	T1/2	Daughter	E* (keV)	decay type	Q* (keV)	Decay	Q <sub>0</sub> (keV)	dQ <sub>0</sub> (keV)
146Pm(3-)	5.53(5) y	146Nd(2+)	1470.63(6)	1st FNU	1.3(4.2)	EC	1472.000	4.000
149Gd(7/2-)	9.28(10) dy	149Eu(5/2+)	1312(4)	1st FNU	2(6.4)	EC	1314.100	4.000
155Tb(3/2+)	5.32(6) dy	155Gd{3/2+}	815.731(3)	Allowed{?}	4.2(10.1)	EC	820.000	10.000
159Dy(3/2-)	144.4(2) dy	159Tb(5/2-)	363.5449(14)	Allowed	1.7(1.2)	EC	365.200	1.200
Z. Ge, T. Eronen et al., Phys. Rev. Lett. 127, 272301		159Tb(11/2+)	362.050(40)	3rd FU	3.2(1.2)	EC	365.200	1.200
161Ho(5/2-)	18.479(4) hr	161Dy{7/2+}	858.502(7)	1st FNU	1.0(2.2)	EC	858.500	2.200
		161Dy{3/2-}	858.7919(18)	Allowed	-0.3(2.2)	EC	858.500	2.200
72As(2-)	26.0(1)h	72Ge{1}	4358.7(3)	Allowed{?}	-2.8(4.0)	EC	4356.000	4.000
Z. Ge, T. Eronen et al., PHYSICAL REVIEW C 103, 065502 (2021)		72Ge(3-)	3325.01(3)	Allowed	8.9(4.0)	$\beta^+$	4356.000	4.000
		72Ge(2+)	3327(3)	1st FNU	6.9(5.0)	$\beta^+$	4356.000	4.000
		72Ge{1+}	3338.0(3)	1st FNU{?}	-4.1(4.0)	$\beta^+$	4356.000	4.000
		72Ge{2-}	3341.76(4)	Allowed{?}	-7.9(4.0)	$\beta^+$	4356.000	4.000
159Gd(3/2-)	26.24(9) h	159Tb{1/2+}	971	1st FNU{?}	0.0(1.8)	$\beta^-$	970.900	0.800
77As(3/2-)	38.79(5) h	77Se(5/2+)	680.1035(17)	1st FNU	3.1(1.7)	$\beta^-$	683.200	1.700
76As(2-)	26.24(9) h	76Se{2-}	2968.4(7)	Allowed{?}	-7.8(1.1)	$\beta^-$	2960.600	0.900
153Tb(5/2+)	2.34(1)dy	153Gd(5/2-)	548.7645(18)	1st FNU	-1.2(4.0)	$\beta^+$	1569.000	4.000
		153Gd{5/2}	551.092(19)	Allowed{?}	-3.5(4.0)	$\beta^+$	1569.000	4.000
Submitted		111In(9/2+)	3dy	111Cd(3/2+)	864.8(3)	2nd FU	-6.6(3.0)	EC
				111Cd(3/2+)	864.8(3)	2nd FU	-4.6(3.0)	EC
				111Cd(3/2+)	855.6(1.0)	2nd FU	4.6(3.2)	EC
				111Cd(7/2+)	853.94(7)	Allowed	6.3(3.0)	EC
131I(7/2+)	8dy	131Xe{9/2+}	971.22(13)	Allowed{?}	-0.42(0.61)	$\beta^-$	970.80	0.60
		131Xe(7/2+)	973.11(14)	Allowed	-2.31(0.62)	$\beta^-$	970.80	0.60
155Eu(5/2+)	5yr	155Gd(9/2-)	251.7056(10)	1st FU	0.1(1.8)	$\beta^-$	252.00	2.40

Q<sub>0</sub> from: M. Wang et al. , Chinese Physics C 45, 030003 (2021)

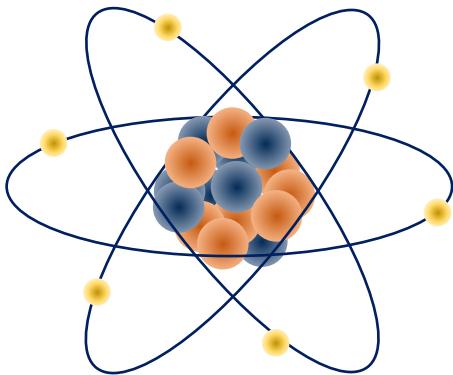
E\* from: National nuclear data center, Available at <https://www.nndc.bnl.gov>

Courtesy of Z. Ge



Thanks a lot for your attention

# Binding energy



$$M_{Nuclei} = N \times M_{Neutron} + Z \times M_{Proton} - B(N, Z)/c^2$$

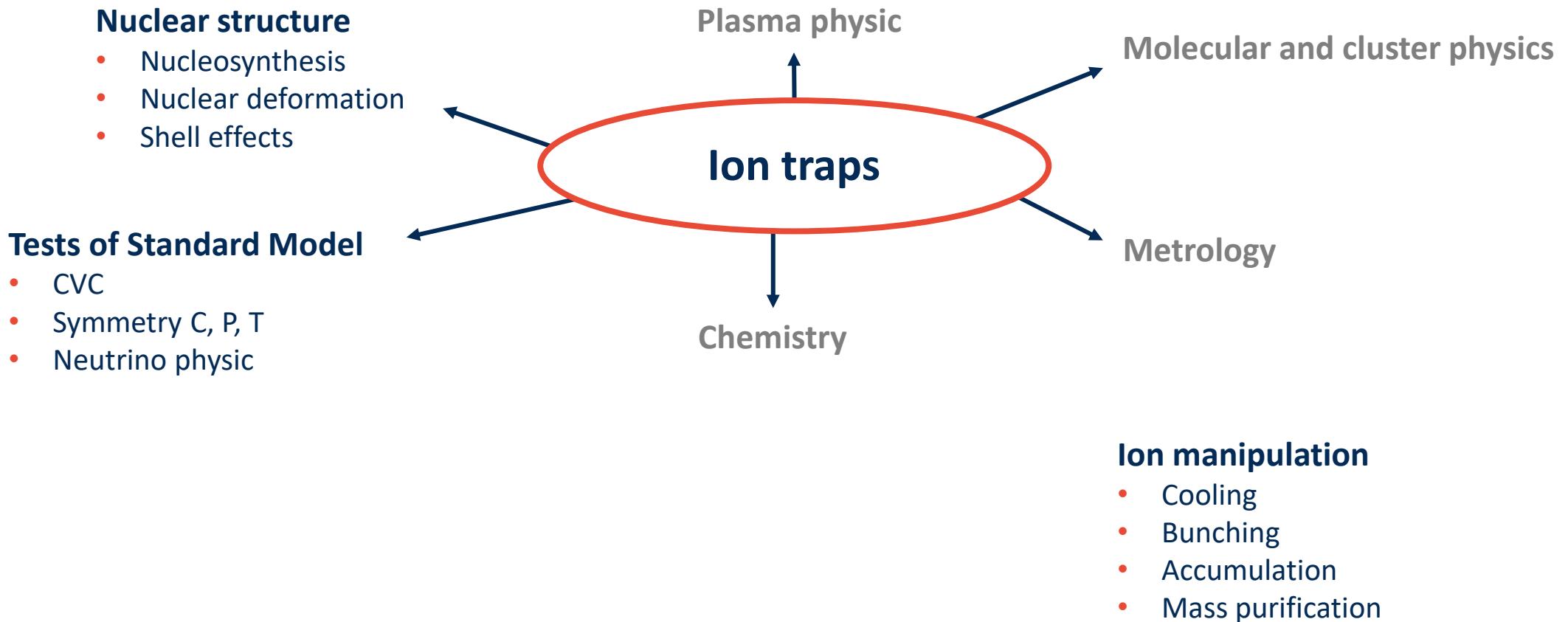
↳  $E = mc^2 \rightarrow$  The binding energy corresponds to the missing mass

## Measuring $B(N, Z)$

- $\delta M/M = 10^{-7} - 10^{-9}$  (For  $A = 100 u \rightarrow 100 GeV$ )
- Nuclear deformation  $\rightarrow \delta M/M = 10^{-7} \rightarrow 10 \text{ keV}$
- Neutrino physic  $\rightarrow \delta M/M = 10^{-9} \rightarrow 100 \text{ eV}$



# Ion traps



# The ECHO experiment

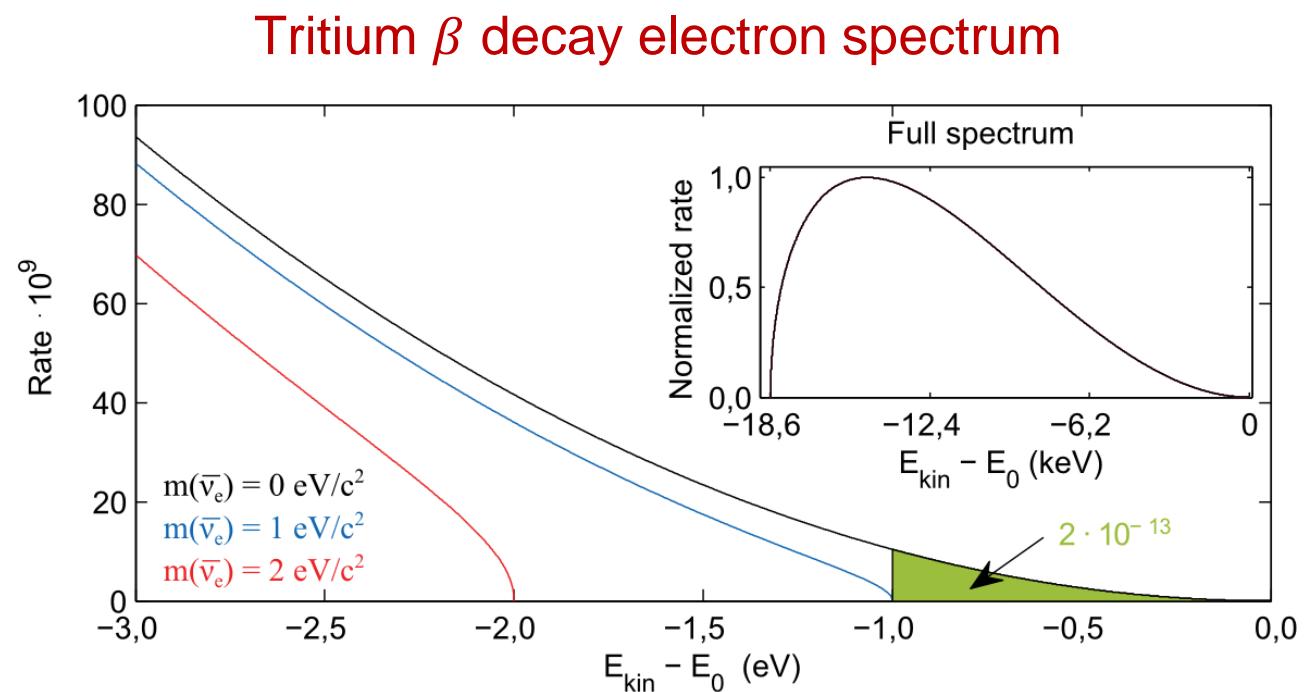
Electron capture of  $^{163}\text{Ho}$  with  $Q_{EC} = 2.8 \text{ keV}$

$^{163}\text{Ho}$  source is enclosed in large array of magnetic calorimeters

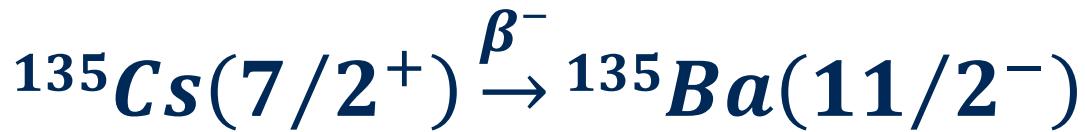
- Deposition of energy
- Temperature increased
- Change the magnetization of a paramagnetic temperature sensor
- Change the magnetic flux of a voltage convertor
- The output voltage signal is proportional to the deposited energy

# The KATRIN experiment

- $\beta$  decay via the mass of the electron antineutrino
  - A slight distortion of the  $\beta$  decay spectrum relates directly to the electron-neutrino mass
- KATRIN [1] experiment
  - ${}^3H(1/2^+) \xrightarrow{\beta^-} {}^3He(1/2^+)$
  - Allowed decay
  - $Q = 18.5920(3) \text{ keV}$
- Low  $Q \rightarrow$  higher sensitivity



[1] C. Weinheimer, Prog. Part. Nucl. Phys. **48**, 141 (2002)



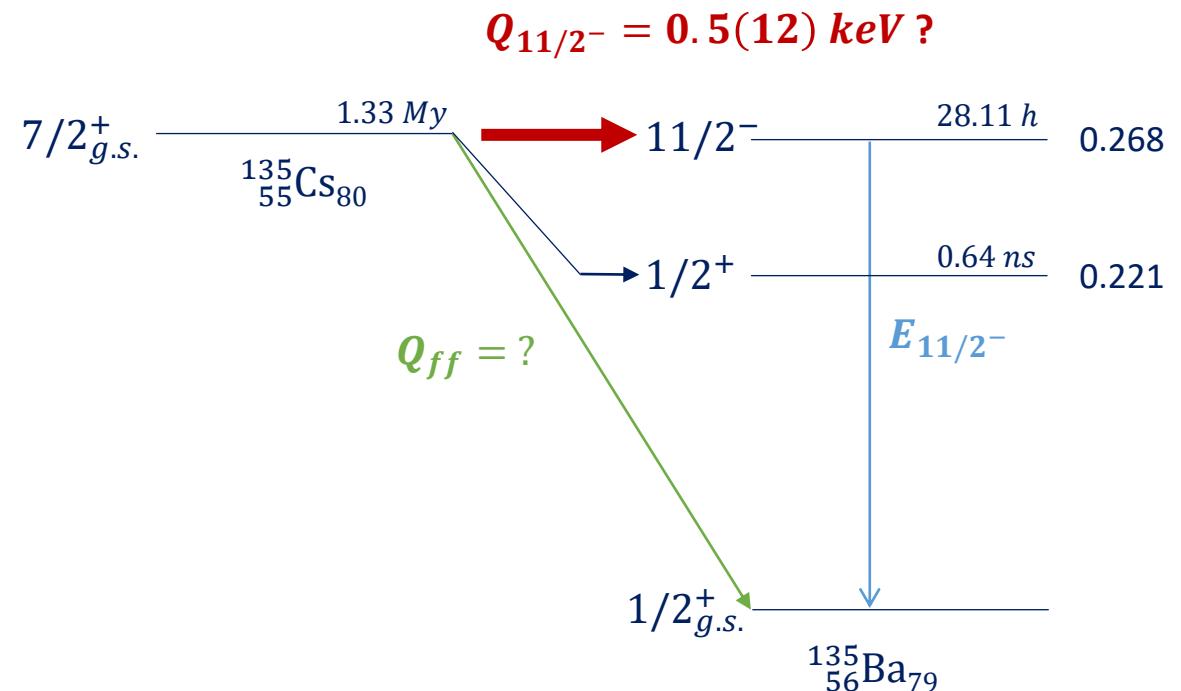
**But :** The transition is poorly known!

- Not yet proven that it is energetically possible :  $Q_{11/2^-} < 0$  ?
- Decay never observed directly

To determine  $Q_{11/2^-}$  we need:

- The excitation energy  $E_{11/2^-} = 268.218(20) \text{ keV}$
- The ground-state-to-ground-state Q-value  $Q_{ff}$
- $Q_{ff} = 268.9(1.1) \text{ keV}$  [1]

$$Q_{ff} = 268.9(1.1) \text{ keV} \rightarrow Q_{11/2^-} = 0.5(1.2) \text{ keV}$$



New measurement of  $Q_{ff}$  with Penning traps!!

# PI-ICR measurements

- \ Pure sample of  $^{135}\text{Cs}$  sent in the measurement trap
- \ Every few rounds, switched between  $^{135}\text{Cs}$  from IGISOL and  $^{135}\text{Ba}$  from the off-line spark source
- \ Measurement of the GS-to-GS Q-value performed with
  - TOF-ICR Ramsey technique
  - PI-ICR technique

