

# Precision measurement in the Top quark sector using Effective Field Theory and entanglement and violation of Bell inequalities at LHC

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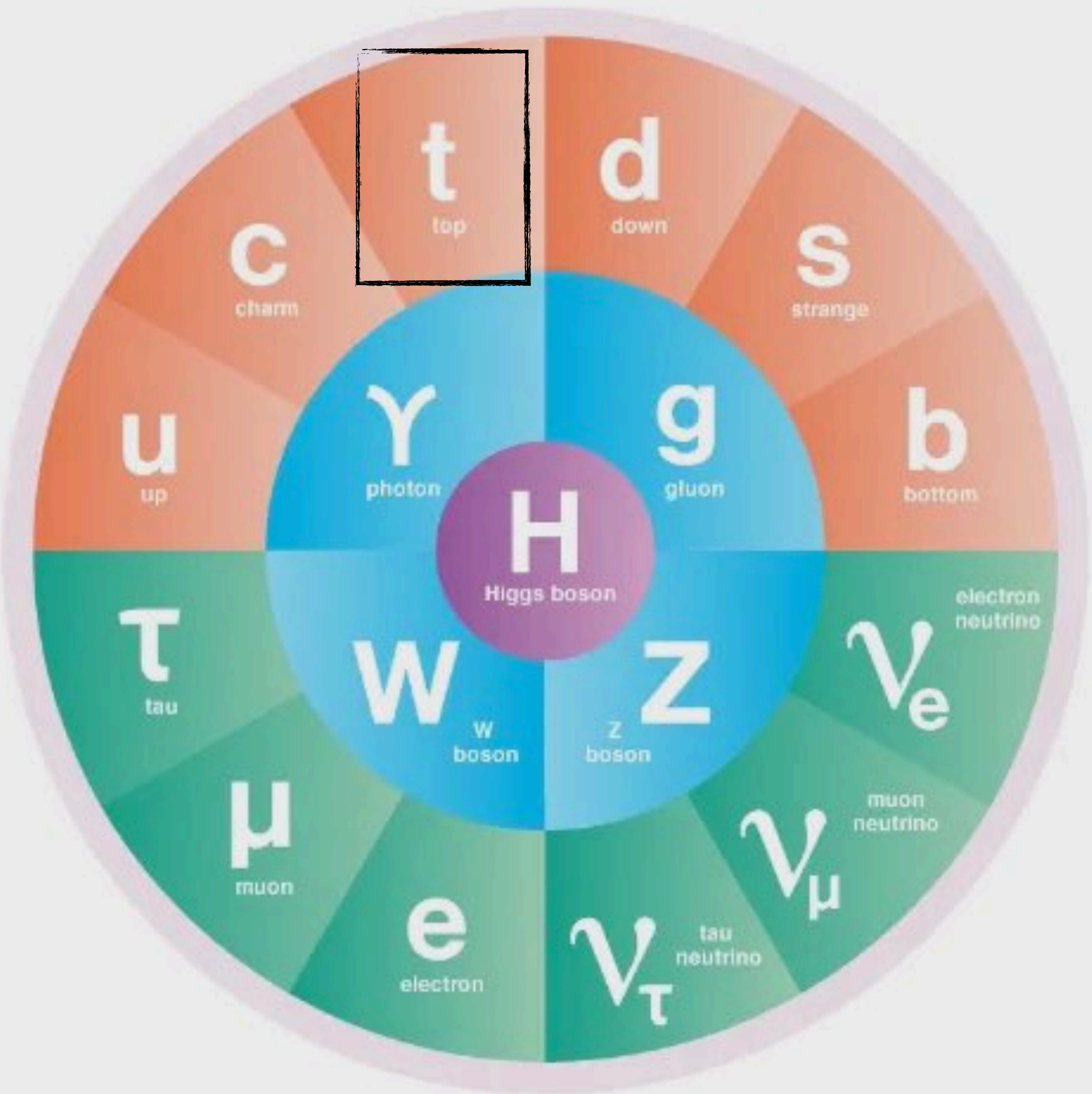
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- Evidence of quantum entanglement at LHC
- Evidence of violation of Bell inequalities at LHC

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# The Standard Model of Particle Physics



● QUARKS   
 ● LEPTONS   
 ● BOSONS   
 ● HIGGS BOSON

$$\text{lifetime} < \text{QCD timescale} \ll \text{spin-flip timescale}$$

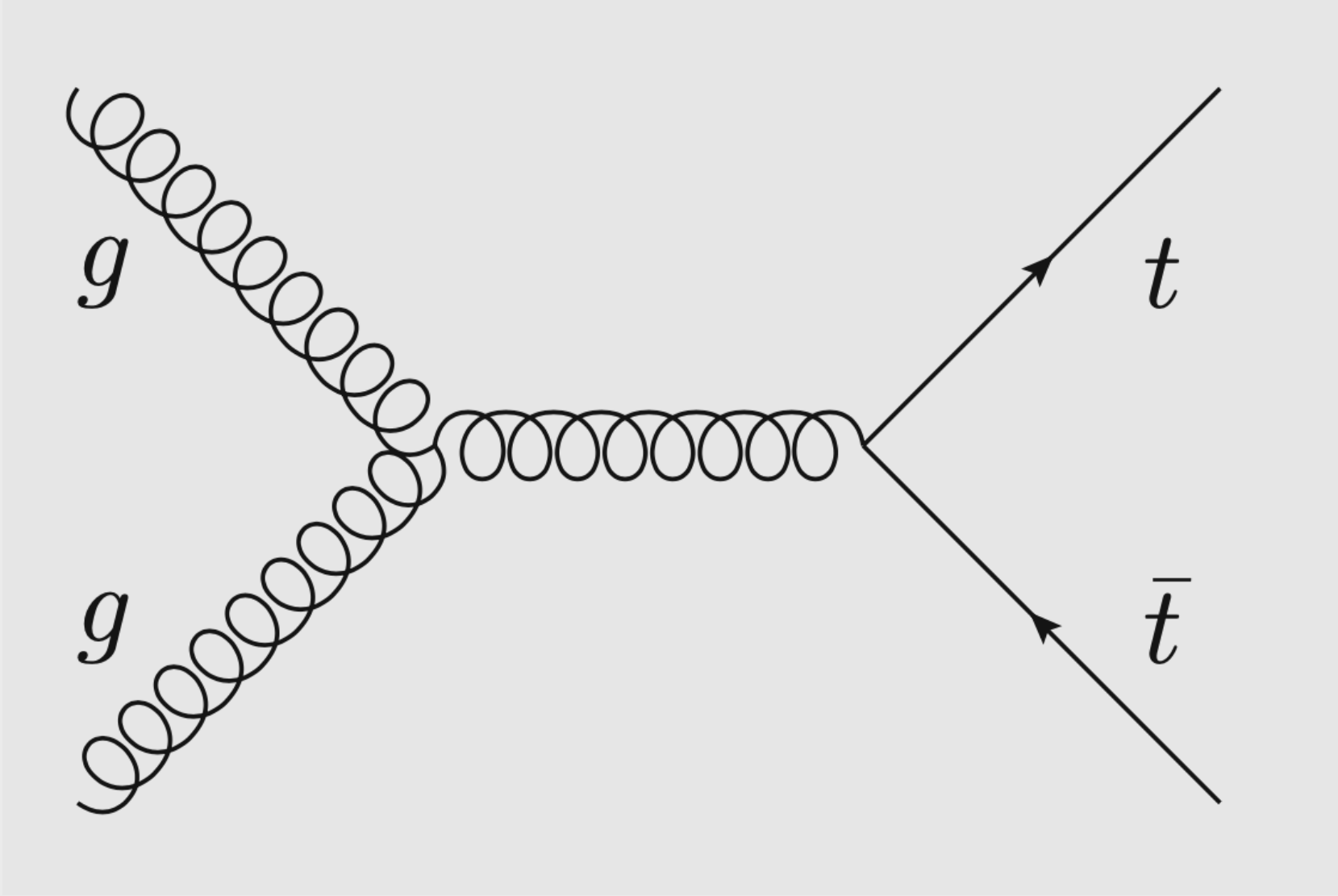
$$10^{-25} \text{ s} < 10^{-24} \text{ s} \ll 10^{-21} \text{ s}$$

● Top Decays before it can form bound states:

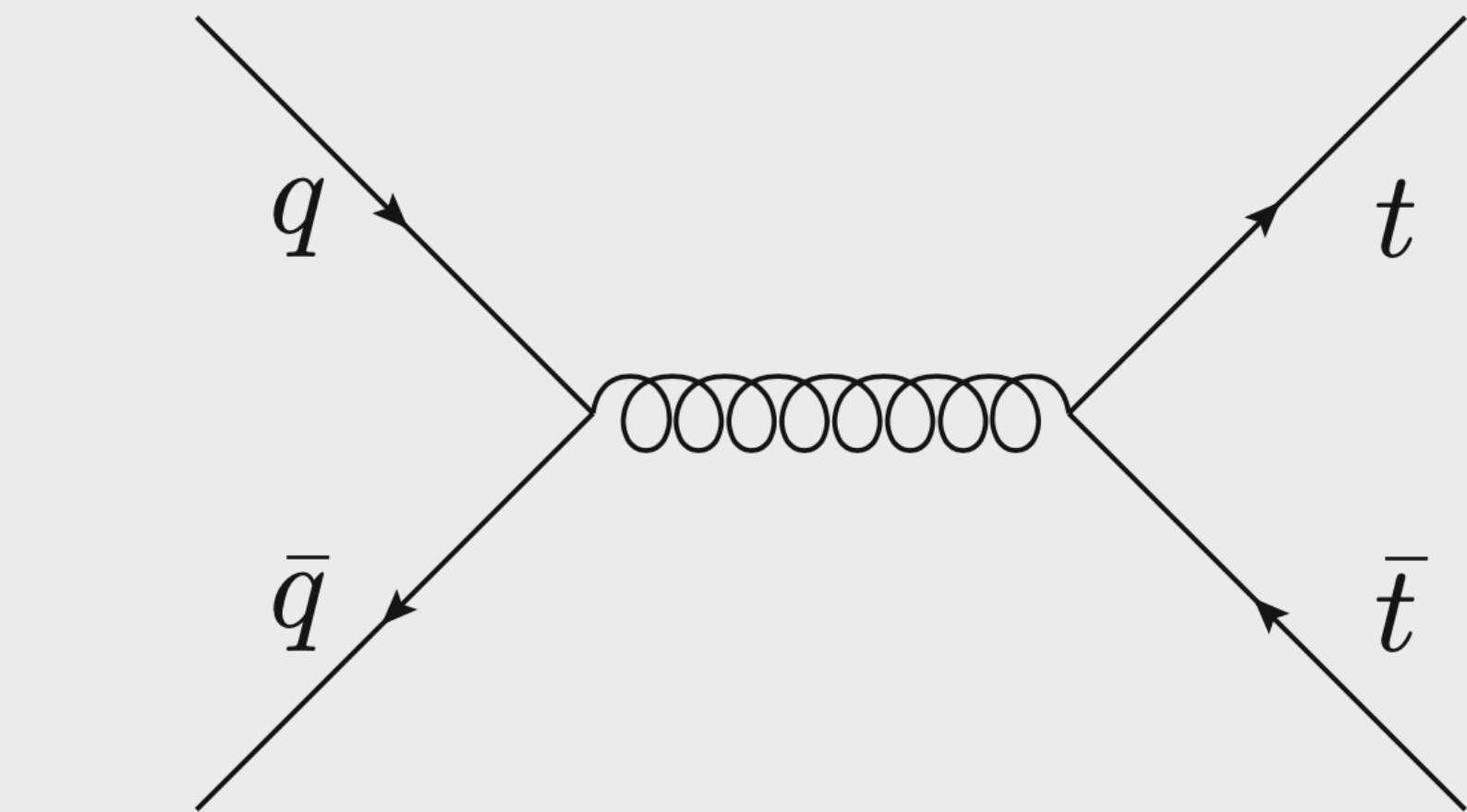
- ♣ Unique opportunity to study the spin information of top quark.

# Top Quark pair production at LHC

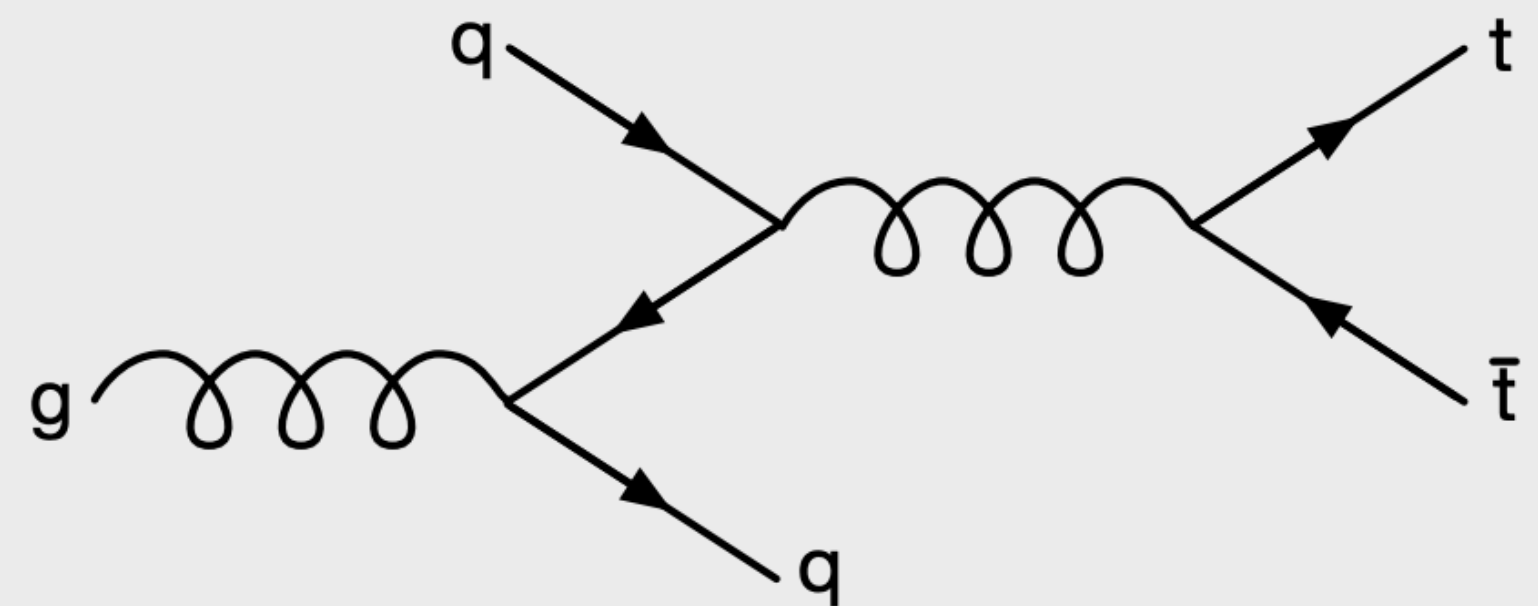
Top quark-antiquark pairs ( $t\bar{t}$ ) produced via strong interaction



gluon fusion  $\approx 90\%$

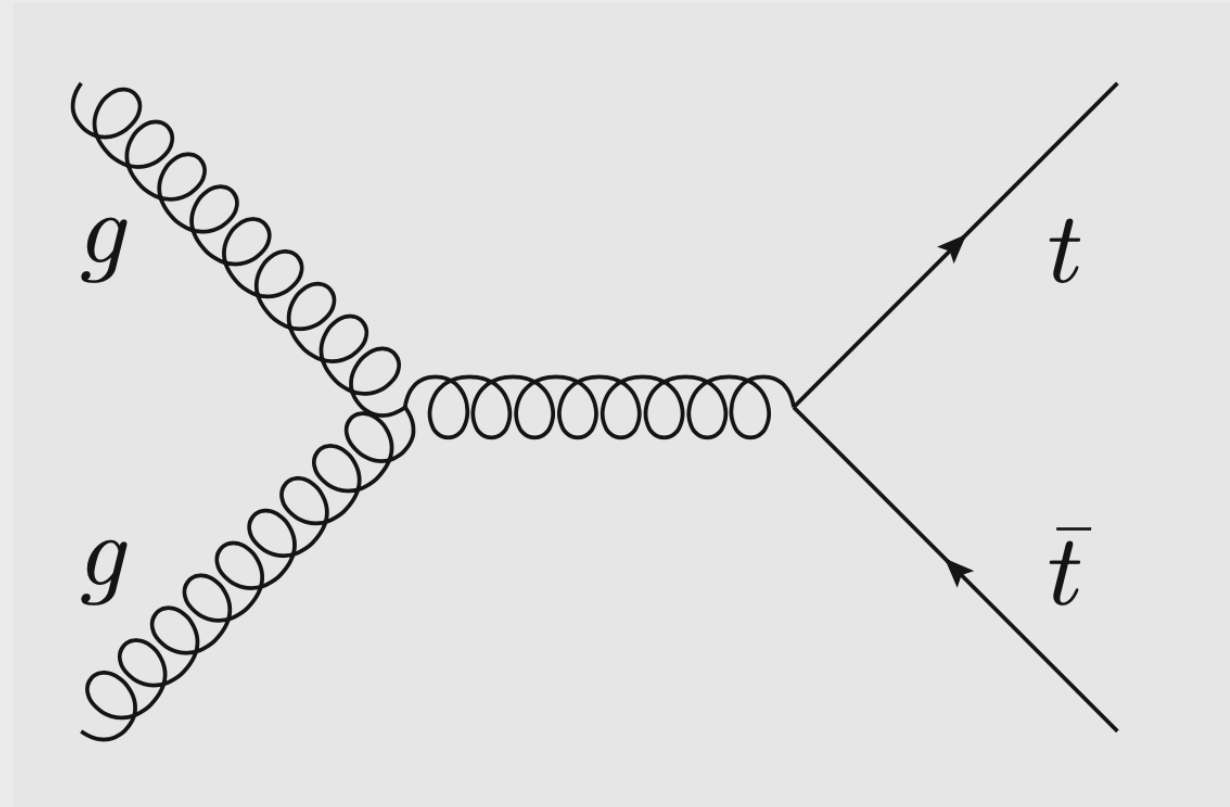


$q\bar{q}$  annihilation  $\approx 8\%$

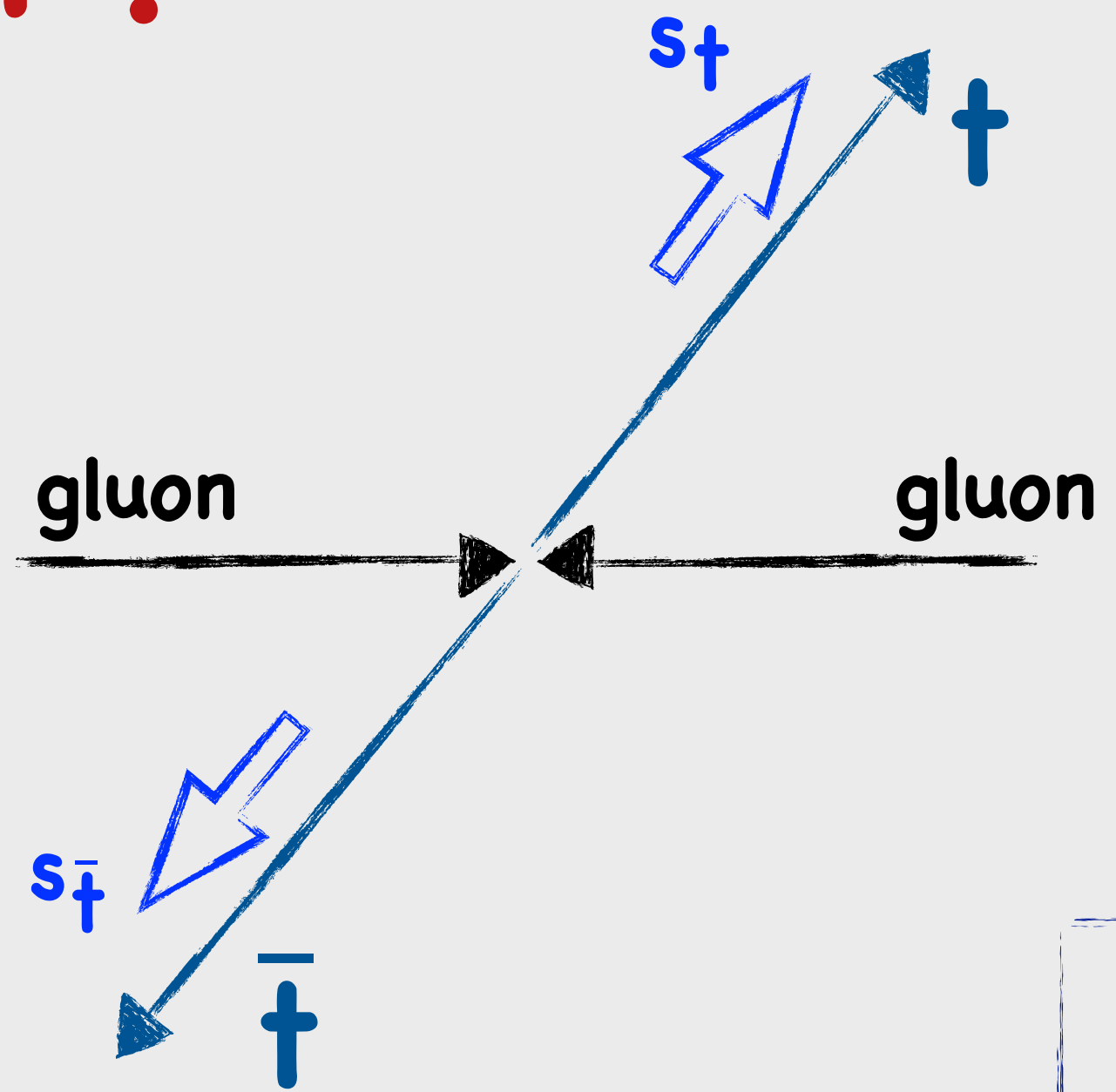


$qg \approx 2\%$

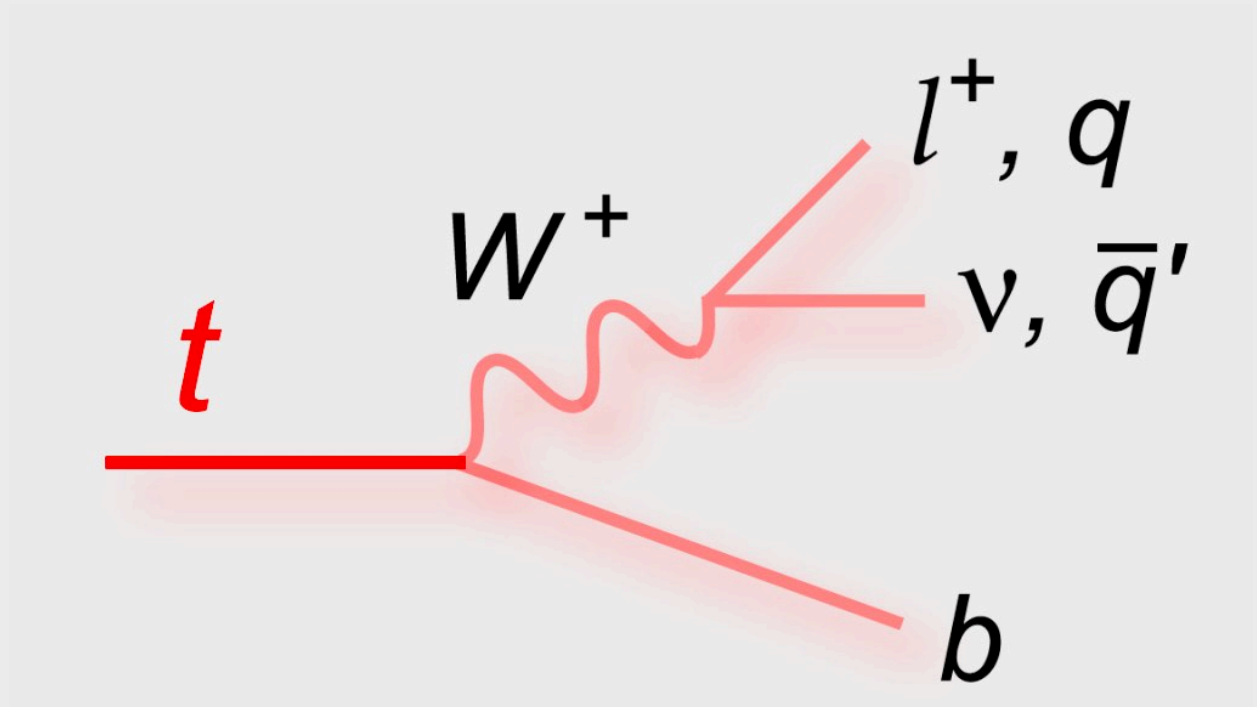
# What is spin correlation ?



Centre Mass Frame



Can we measure spin correlations between top and anti-top ?

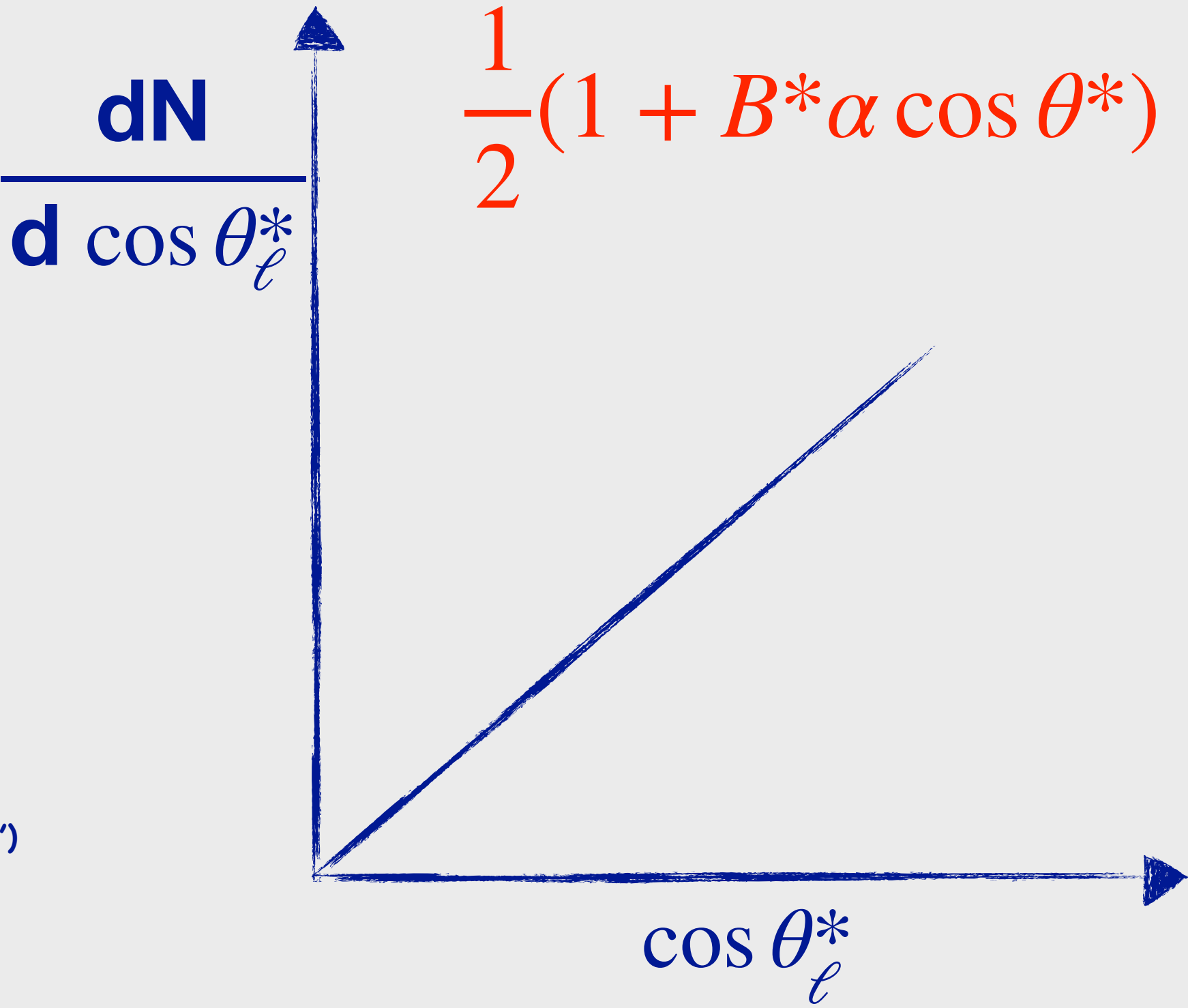
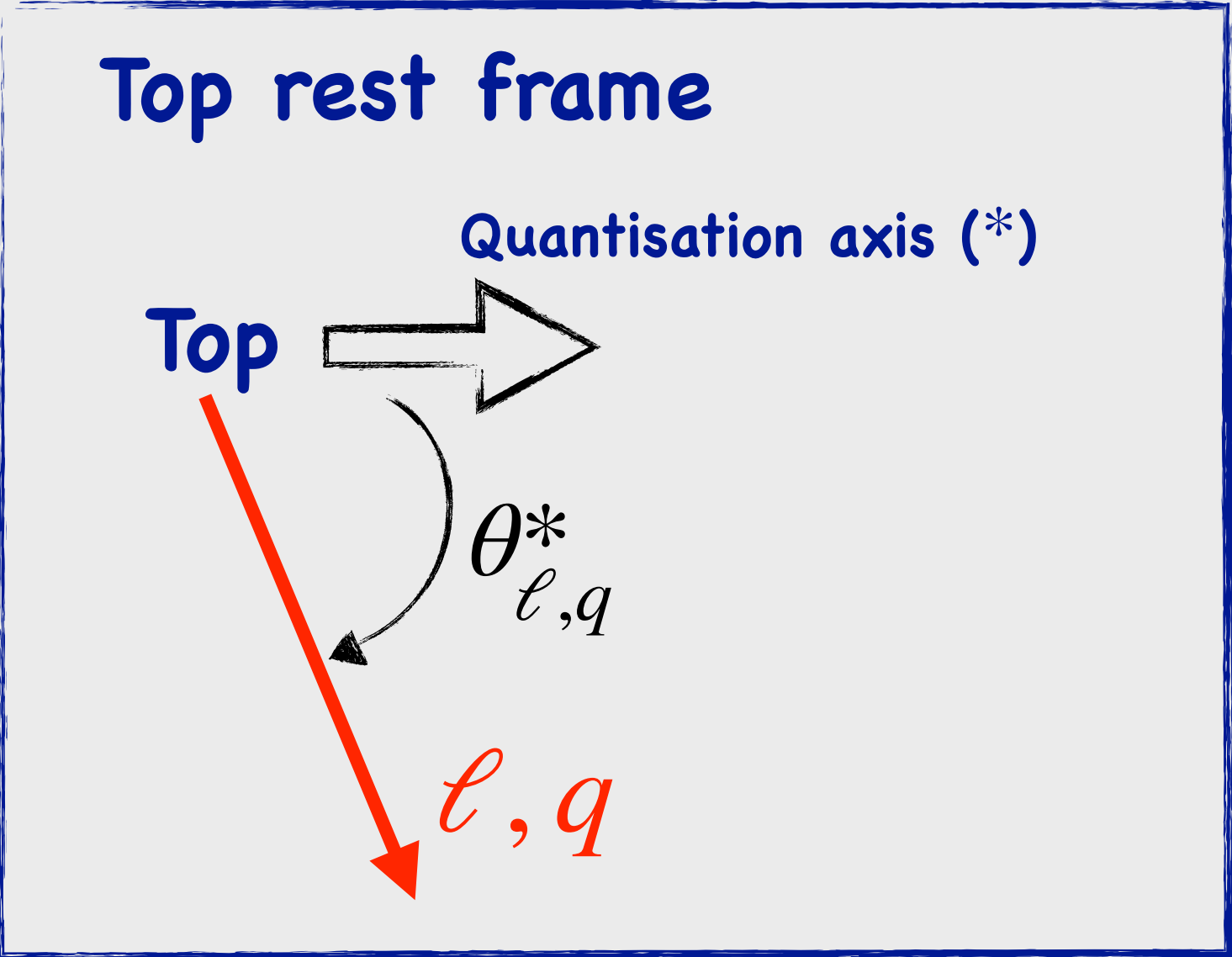


lifetime < QCD timescale << spin-flip timescale  
 $10^{-25} \text{ s} < 10^{-24} \text{ s} \ll 10^{-21} \text{ s}$

Spin information transferred to daughter particles

# Spin analysis power $\alpha$

●  $\alpha$  measures how well a given daughter probes the spin of its parent

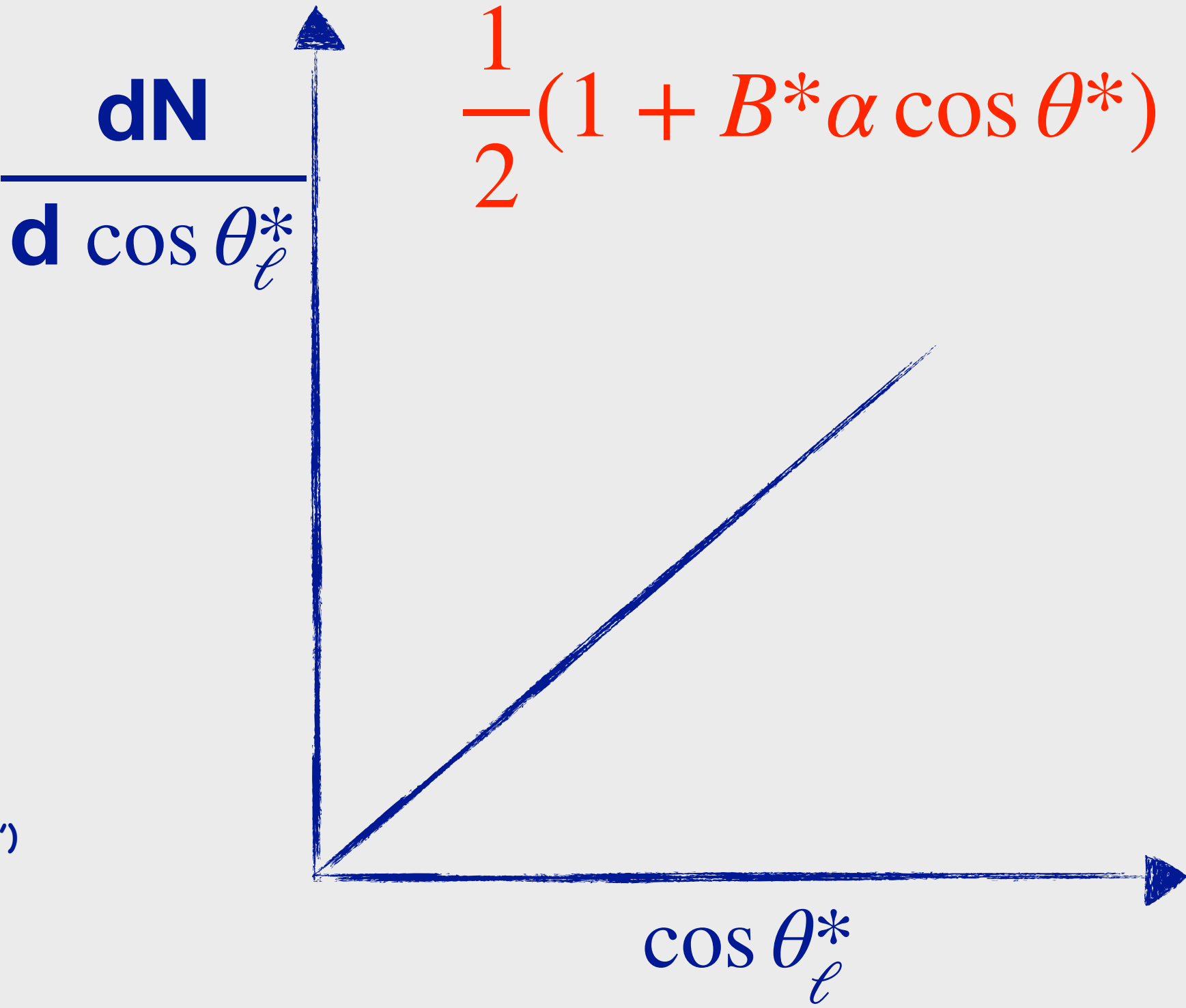
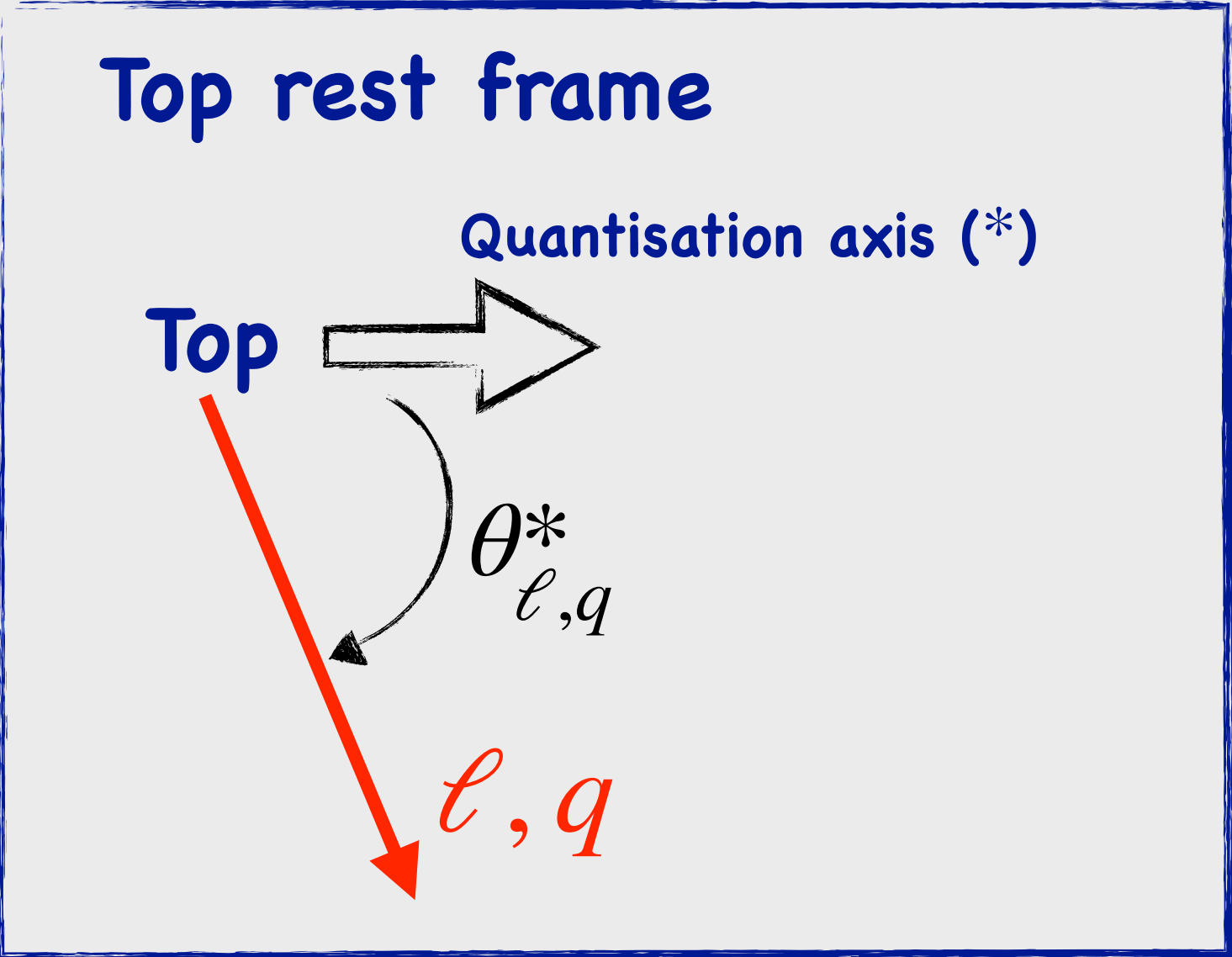


Particle	$\alpha$
$e^+, \mu^+, \tau^+$	1.00
$\bar{d}, \bar{s}$	0.94
$u, c$	-0.30
$b$	-0.39

$\theta_{\ell, q}^*$  measured in top rest frame relative to boost direction ("helicity basis")

# Spin analysis power $\alpha$

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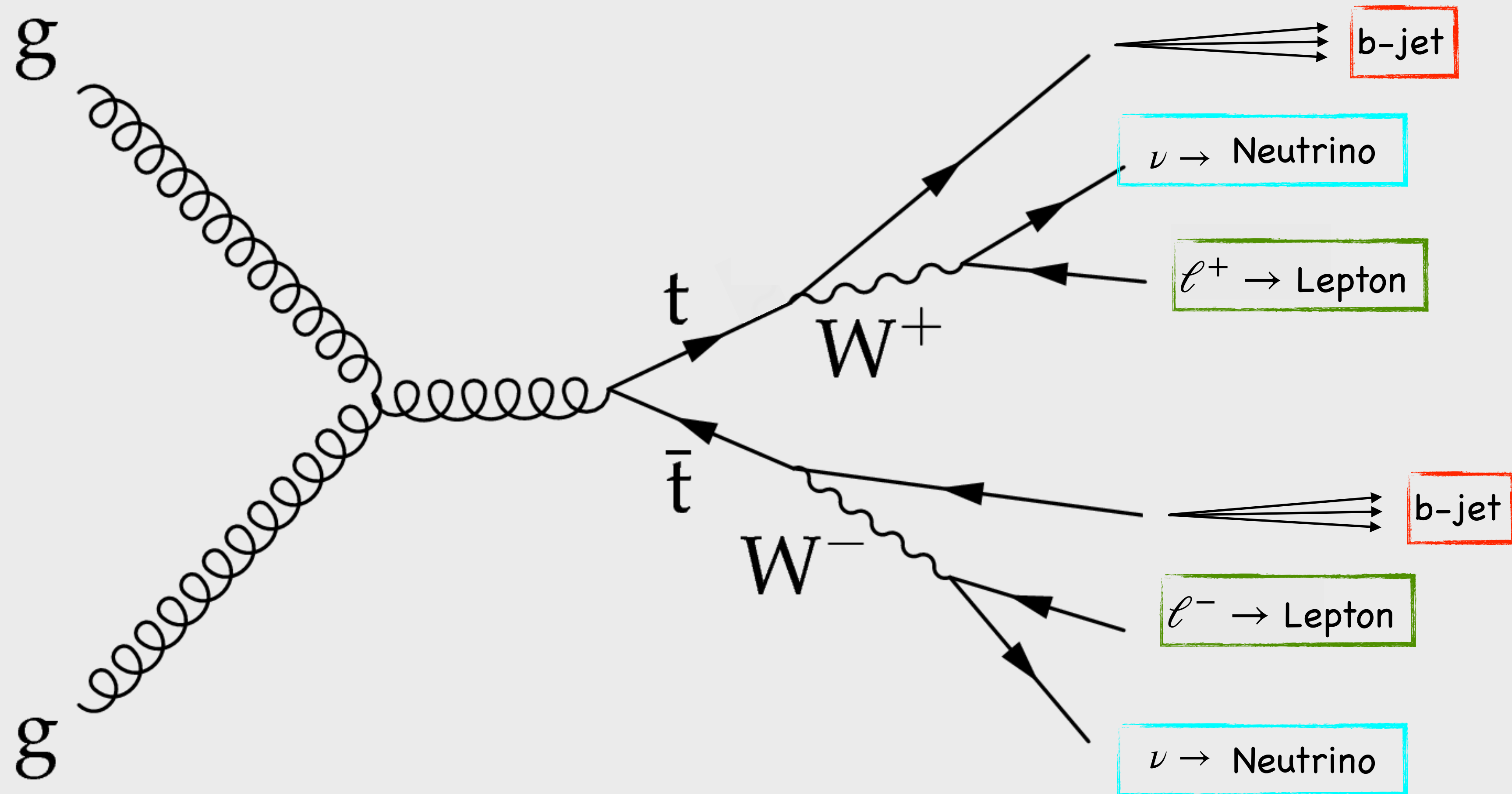


- For lepton  $\alpha=1$ 
  - ❖ Leptons ( $\ell$ ) are preferentially produced in the top spin direction
  - ❖ Measurements of  $\cos \theta^*$  lepton can provide information about top spin

$\theta_{\ell, q}^*$  measured in top rest frame relative to boost direction ("helicity basis")

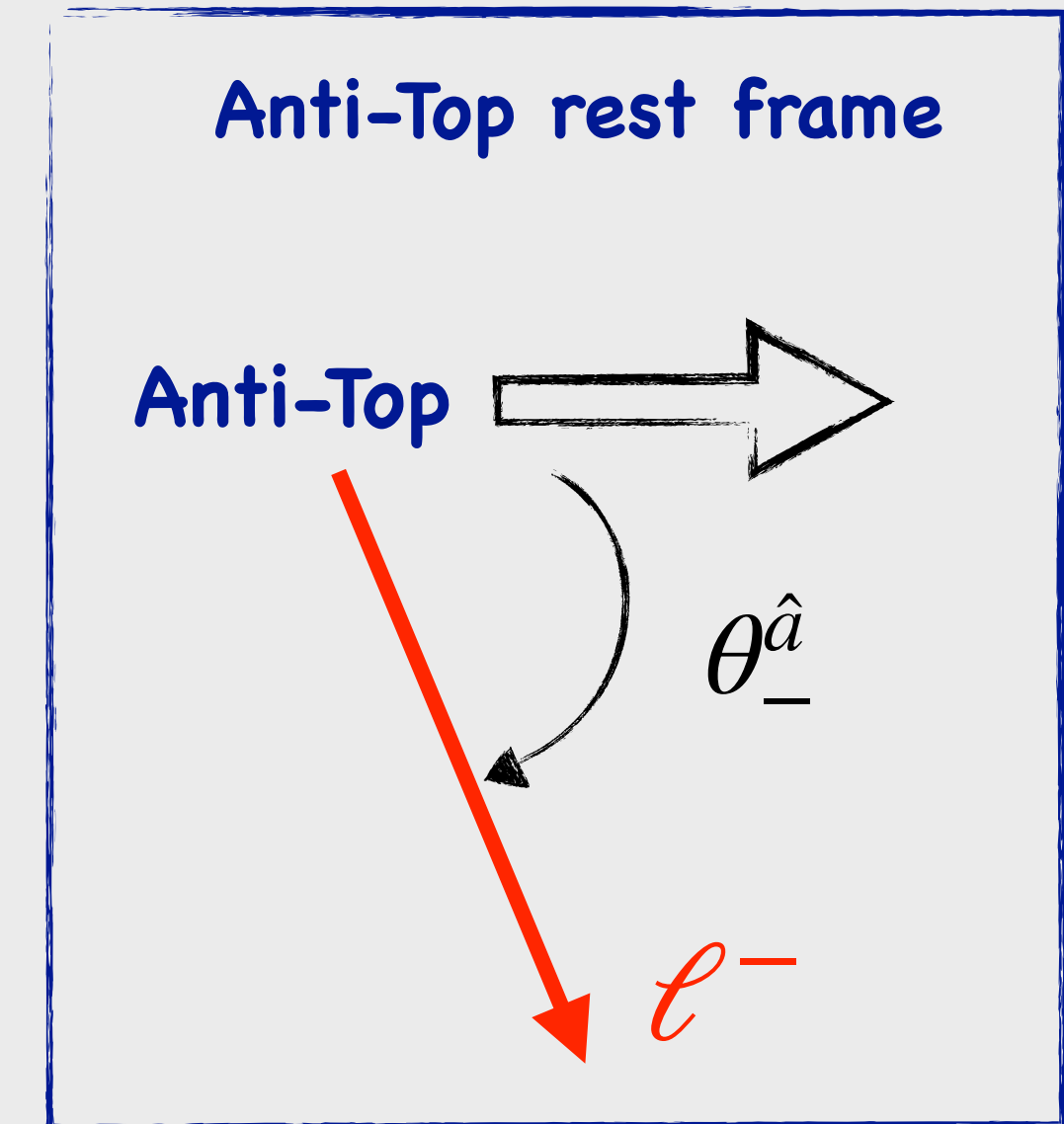
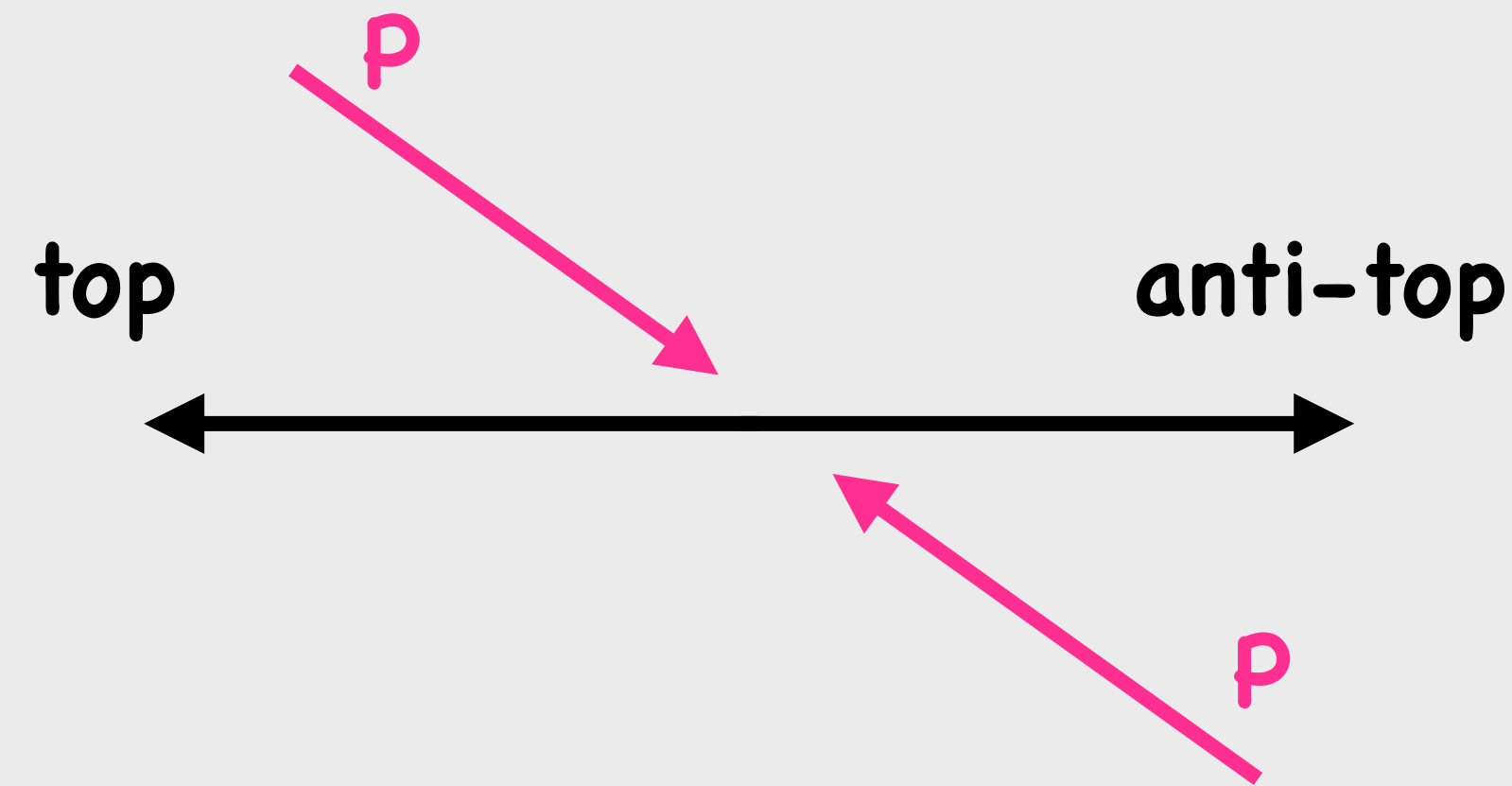
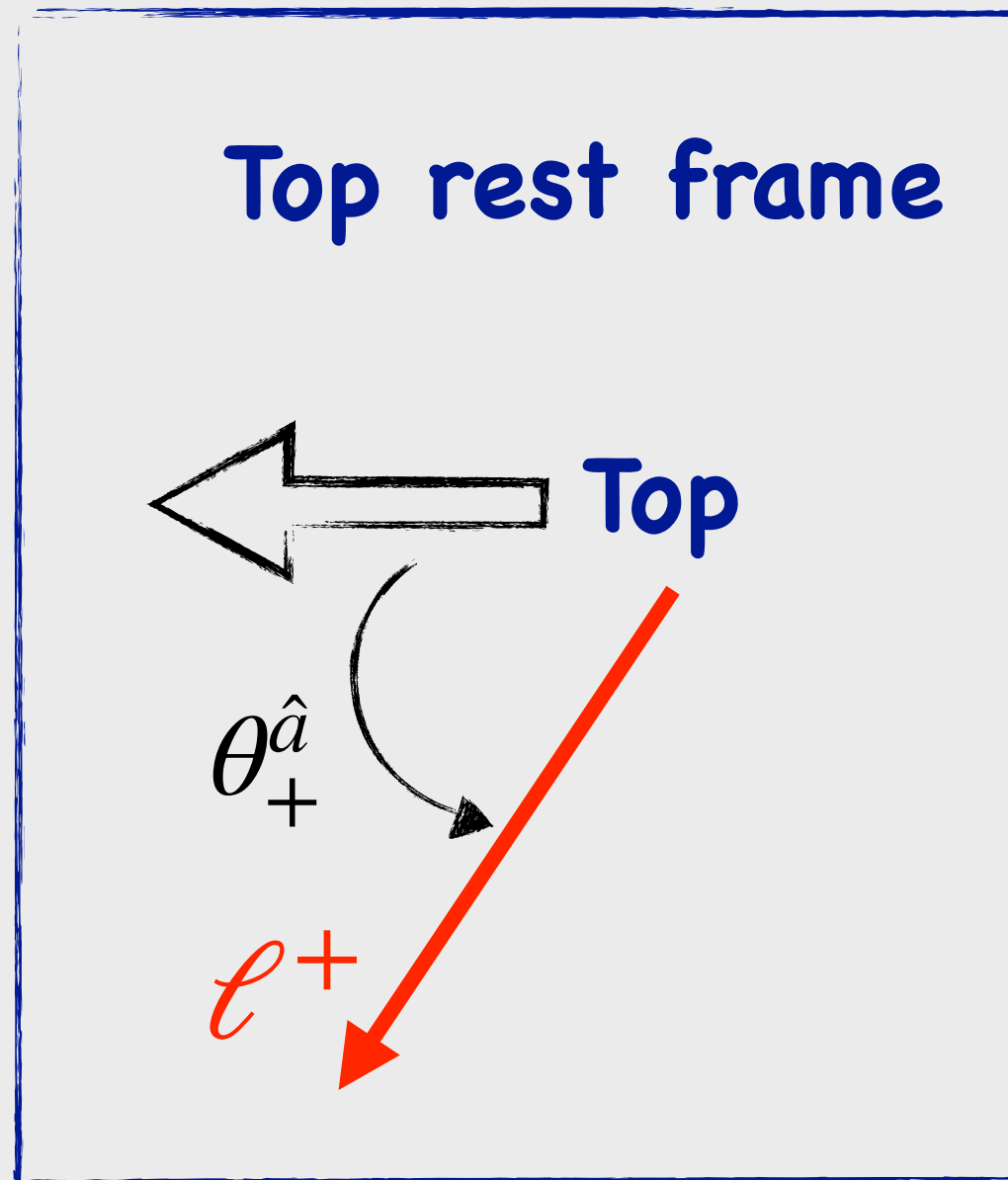
# $t\bar{t}$ di-lepton channel

● The best spin analyser is Lepton, which is why di-lepton channel should be chosen





# $t\bar{t}$ Spin Correlations in the di-lepton channel



$$\frac{1}{\sigma} \frac{d^2\sigma}{d \cos \theta_+^{\hat{a}} d \cos \theta_-^{\hat{b}}} = \frac{1}{4} \left( 1 + B_+^{\hat{a}} \cos \theta_+^{\hat{a}} + B_-^{\hat{b}} \cos \theta_-^{\hat{b}} - C(\hat{a}, \hat{b}) \cos \theta_+^{\hat{a}} \cos \theta_-^{\hat{b}} \right)$$



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Top (+)

Anti-Top (-)

$\cos(\theta_+^{\hat{k}})$

$\cos(\theta_-^{\hat{k}})$

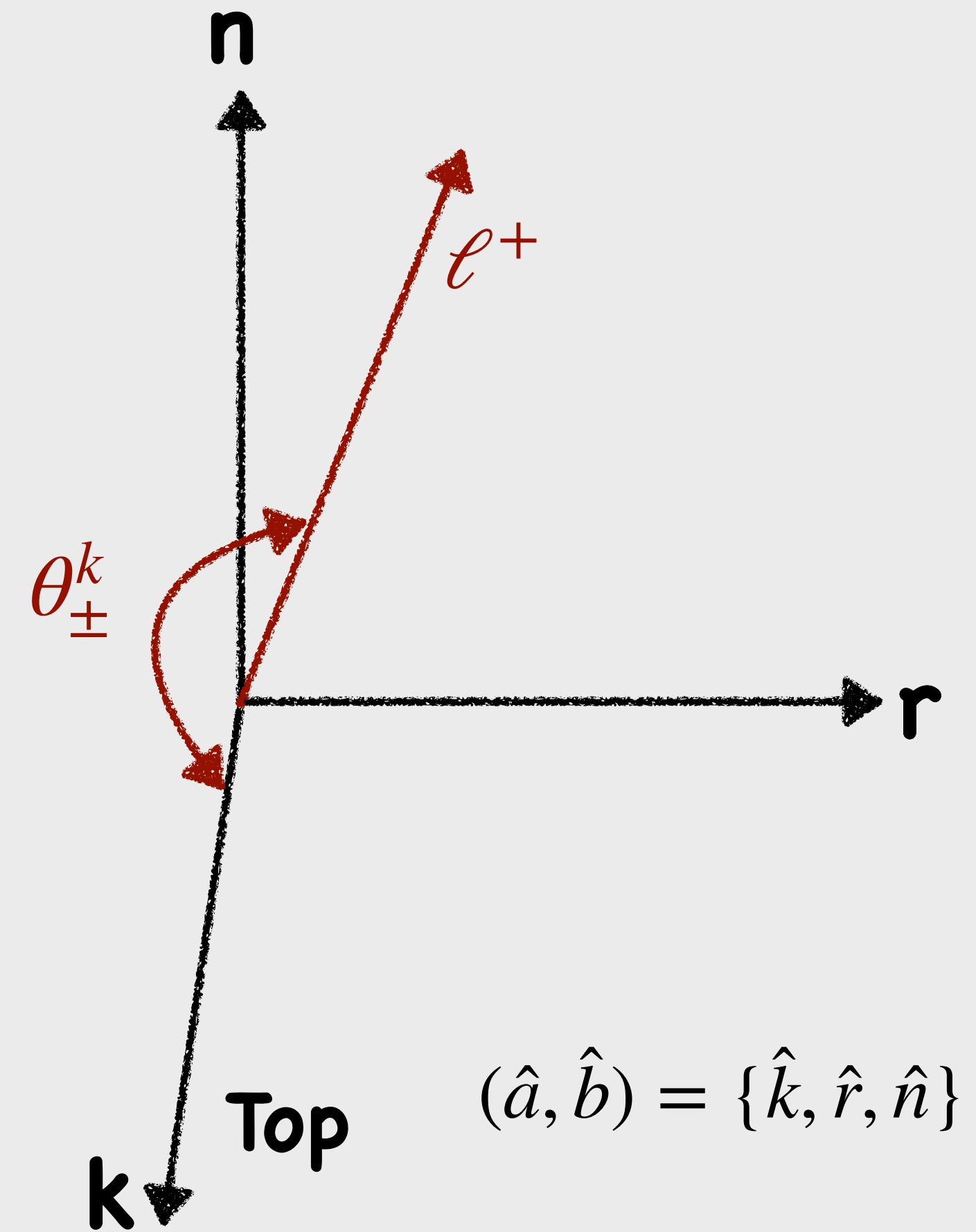
$\cos(\theta_+^{\hat{r}})$

$\cos(\theta_-^{\hat{r}})$

$\cos(\theta_+^{\hat{n}})$

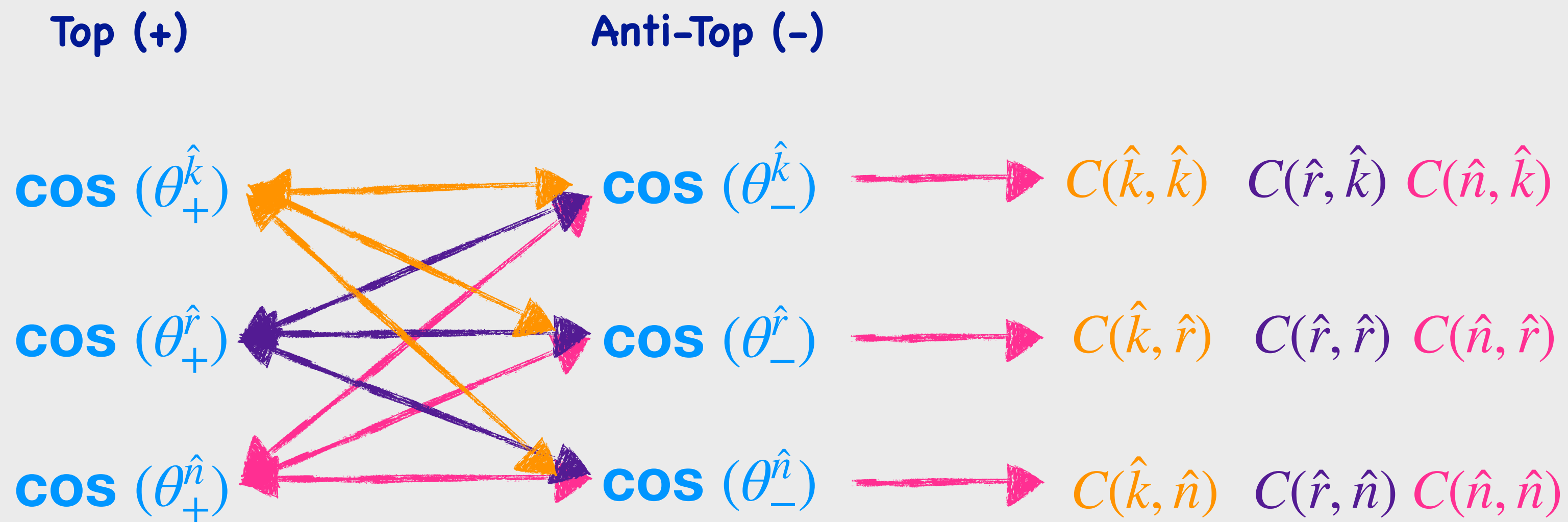
$\cos(\theta_-^{\hat{n}})$

$B_{\pm}^{\hat{a}, \hat{b}} = 6$  polarisations observables

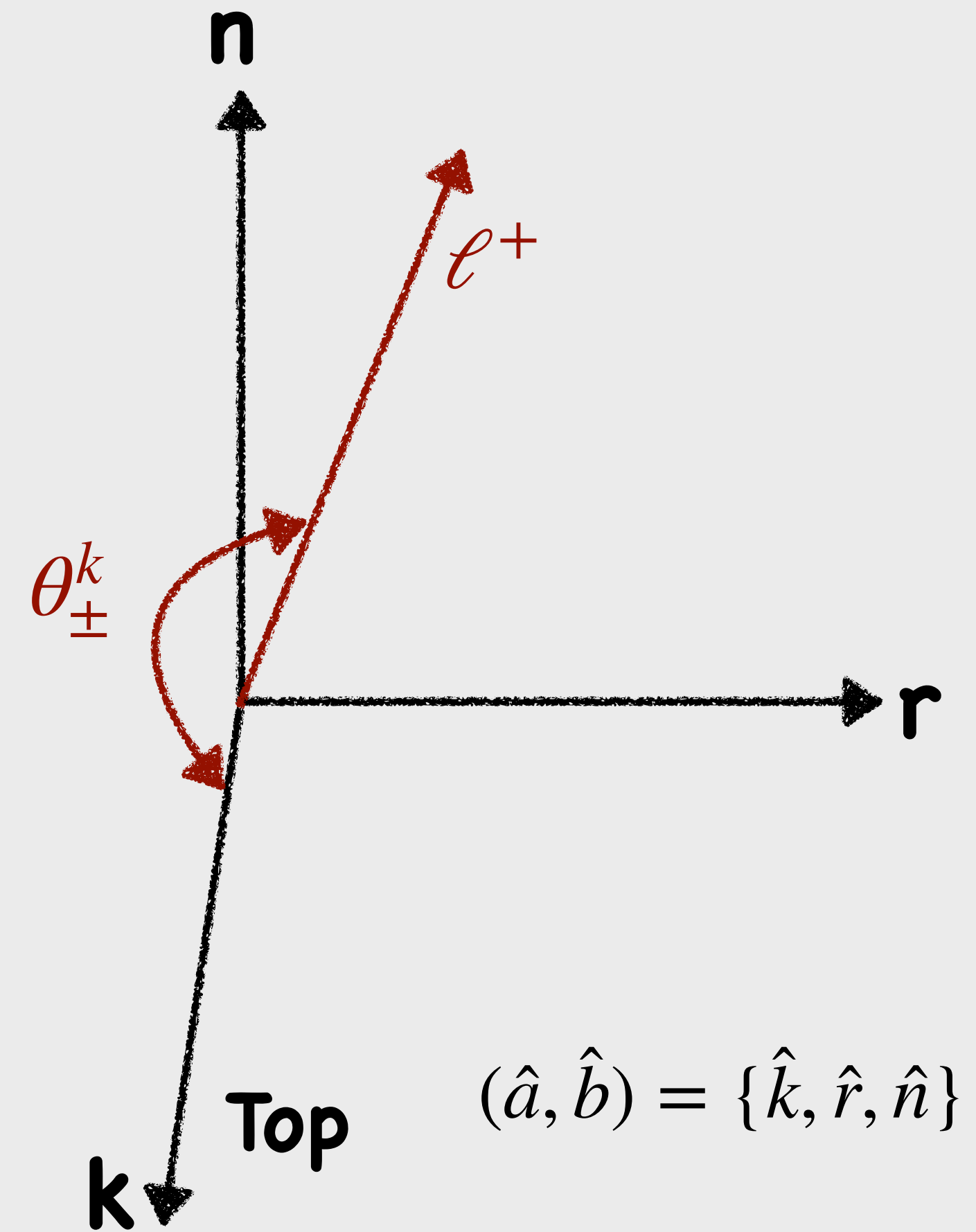


# $t\bar{t}$ Spin Correlations in the di-lepton channel

$$\frac{1}{\sigma} \frac{d^2\sigma}{d\cos\theta_+^{\hat{a}} d\cos\theta_-^{\hat{b}}} = \frac{1}{4} \left( 1 + B_+^{\hat{a}} \cos\theta_+^{\hat{a}} + B_-^{\hat{b}} \cos\theta_-^{\hat{b}} - C(\hat{a}, \hat{b}) \cos\theta_+^{\hat{a}} \cos\theta_-^{\hat{b}} \right)$$



3x3 matrix  $C(\hat{a}, \hat{b})$  of spin correlation coefficients.



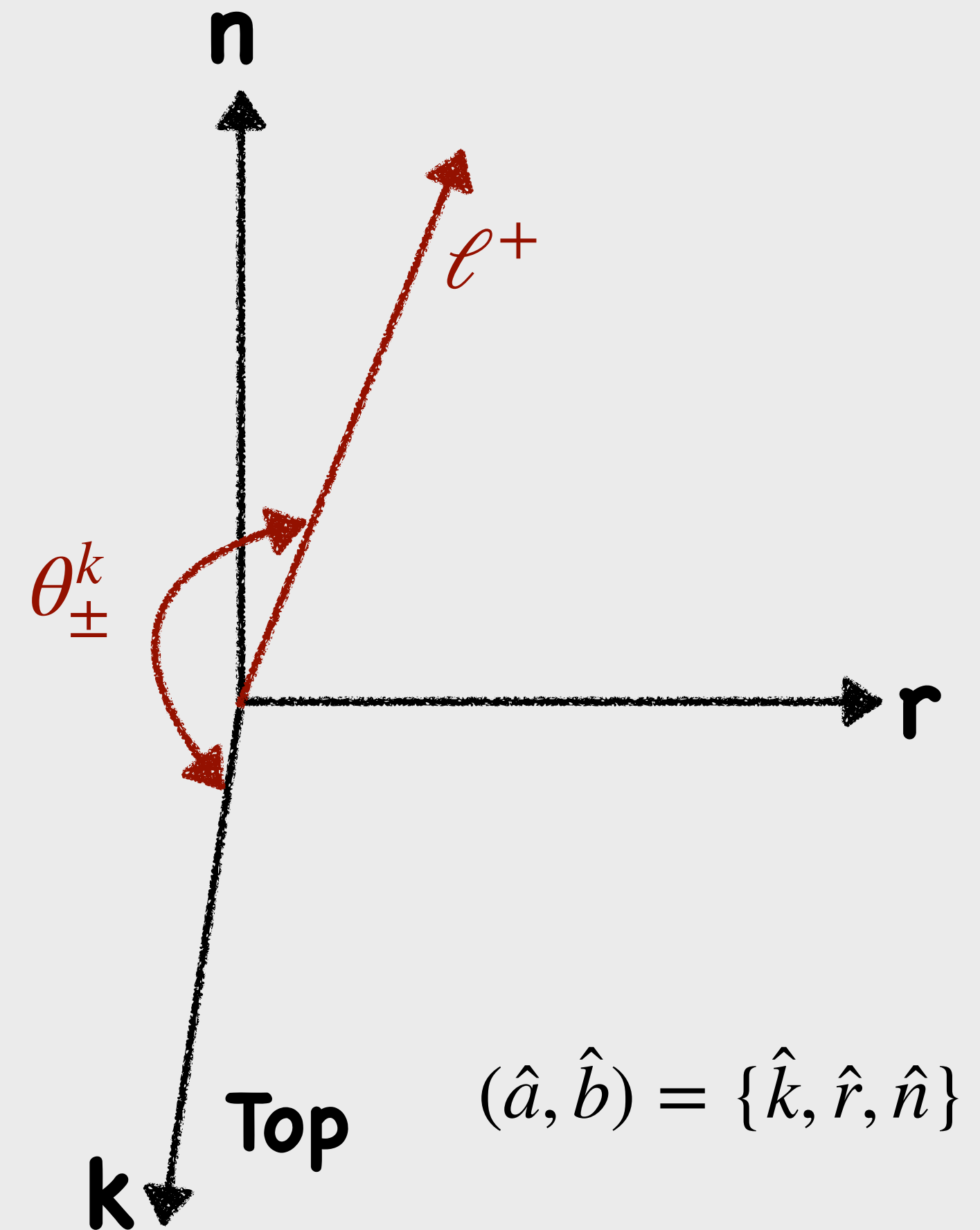
# $t\bar{t}$ Spin Correlations in the di-lepton channel

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$B_+^{\hat{k}}$	$B_-^{\hat{k}}$	$C(\hat{k}, \hat{k})$	$C(\hat{r}, \hat{k})$	$C(\hat{n}, \hat{k})$
$B_+^{\hat{r}}$	$B_-^{\hat{r}}$	$C(\hat{k}, \hat{r})$	$C(\hat{r}, \hat{r})$	$C(\hat{n}, \hat{r})$
$B_+^{\hat{n}}$	$B_-^{\hat{n}}$	$C(\hat{k}, \hat{n})$	$C(\hat{r}, \hat{n})$	$C(\hat{n}, \hat{n})$



15 polarisation and spin correlation observables



# How to probe Spin Correlation observables ?

$$\frac{1}{\sigma} \frac{d^2\sigma}{d \cos \theta_+^{\hat{a}} d \cos \theta_-^{\hat{b}}} = \frac{1}{4} \left( 1 + B_+^{\hat{a}} \cos \theta_+^{\hat{a}} + B_-^{\hat{b}} \cos \theta_-^{\hat{b}} - C(\hat{a}, \hat{b}) \cos \theta_+^{\hat{a}} \cos \theta_-^{\hat{b}} \right)$$

$$\frac{1}{\sigma} \frac{d\sigma}{dx} = \frac{1}{2} (1 + [\mathbf{Coef.}] x) f(x) \quad x = \begin{matrix} \cos \theta_+^{\hat{a}}, \cos \theta_-^{\hat{b}} \\ \cos \theta_+^{\hat{a}} \cos \theta_-^{\hat{b}} \end{matrix} \text{ or}$$

$$B_+^{\hat{a}} = 3 \langle \cos \theta_+^{\hat{a}} \rangle, \quad B_-^{\hat{b}} = 3 \langle \cos \theta_-^{\hat{b}} \rangle$$

$$C(\hat{a}, \hat{b}) = -9 \langle \cos \theta_+^{\hat{a}} \cos \theta_-^{\hat{b}} \rangle$$

**Mean Method**

$$B_{\pm}^{\hat{a}, \hat{b}} \quad C(\hat{a}, \hat{b})$$

**Slope Method**

# Spin Correlation Measurements

# Spin correlation, Data/MC

## ◎ Full Run2 data

## ◎ MC Samples

- Signal:  $t\bar{t}$  (PowHeg + Pythia8)

- Backgrounds:

• Z and W+jets

• Single top (Wt channel)

• Di-boson

• Fakes from  $t\bar{t}$  and single-top

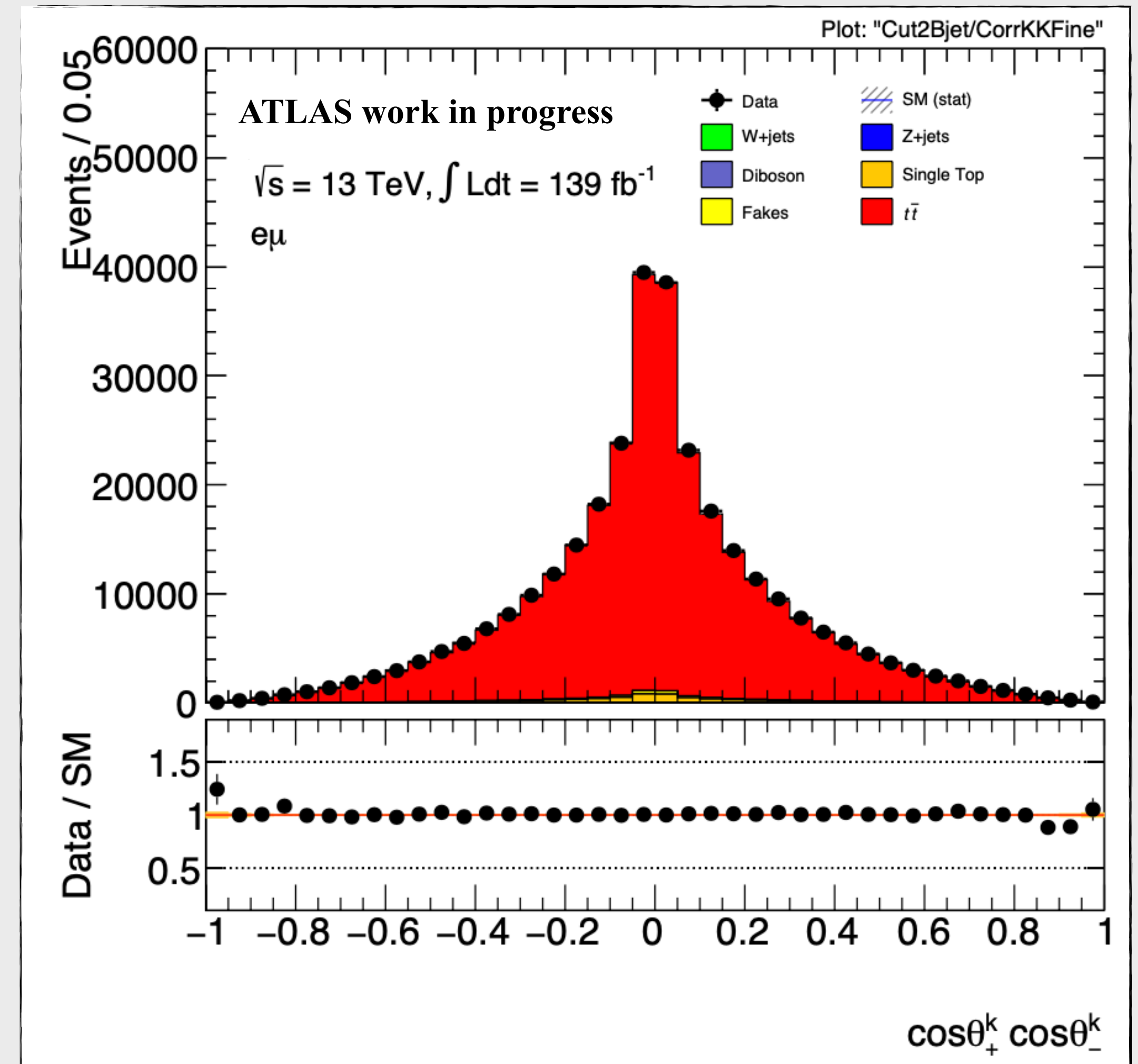
## ◎ Event Selection

- Exactly two leptons (e or  $\mu$ ),  $p_T^{lep} \geq 25 \text{ GeV}$

- Opposite charge leptons

-  $N_{b\text{-jets}} \geq 2$

S/B is extremely high and Data/MC is very good





# Spin correlation, Unfolding

Using Mc16a only as a starting point but the analysis is aimed at using the full Run2 dataset.

● Using TReXFitter to perform a profile likelihood unfolding

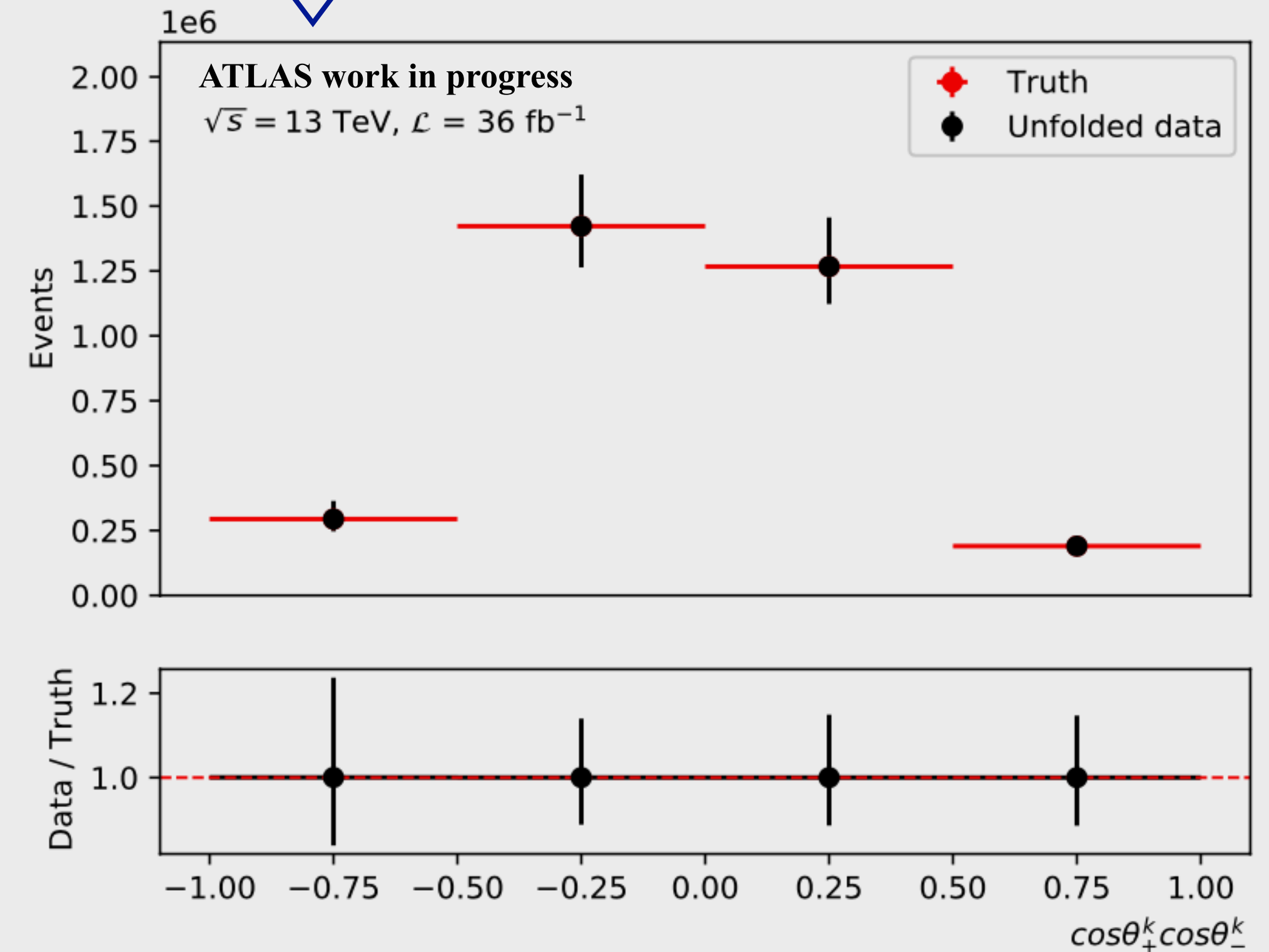
● Included systematics:

●  $t\bar{t}$  modelling systematics

● Weight systematics

➔ Larger impact from  $t\bar{t}$  modelling systematics

● Unfolded  $C(k,k) = 0.332^{+0.054}_{-0.067}$  (mean method, in agreement with the SM prediction)



Uncertainty source	$\Delta C(k, k)$
$t\bar{t}$ modelling	+0.043 / -0.058
Weight systematics	+0.002 / -0.003
Background MC stat. (gammas)	+0.007 / -0.006
Total systematic uncert.	+0.044 / -0.059
Statistical uncert.	$\pm 0.032$
Total	+0.054 / -0.067

# EFT Interpretation

# Bottom-up approach, SM-EFT

$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}}^{(4)} + \sum_i \frac{c_i^{(5)} \mathcal{O}_i^{(5)}}{\Lambda} + \sum_i \frac{c_i^{(6)} \mathcal{O}_i^{(6)}}{\Lambda^2} + \mathcal{O}\left(\frac{1}{\Lambda^3}\right) = \mathcal{L}_{\text{NP}}$$

Dim 5
Dim 6

Lagrangian with new particles at  $\Lambda$

● 1 operator with  $D=5$ :  $\mathcal{O}^{(5)} = \bar{L}_L \tilde{\Phi} \tilde{\Phi}^T L_L^c$   
 → Weinberg operator

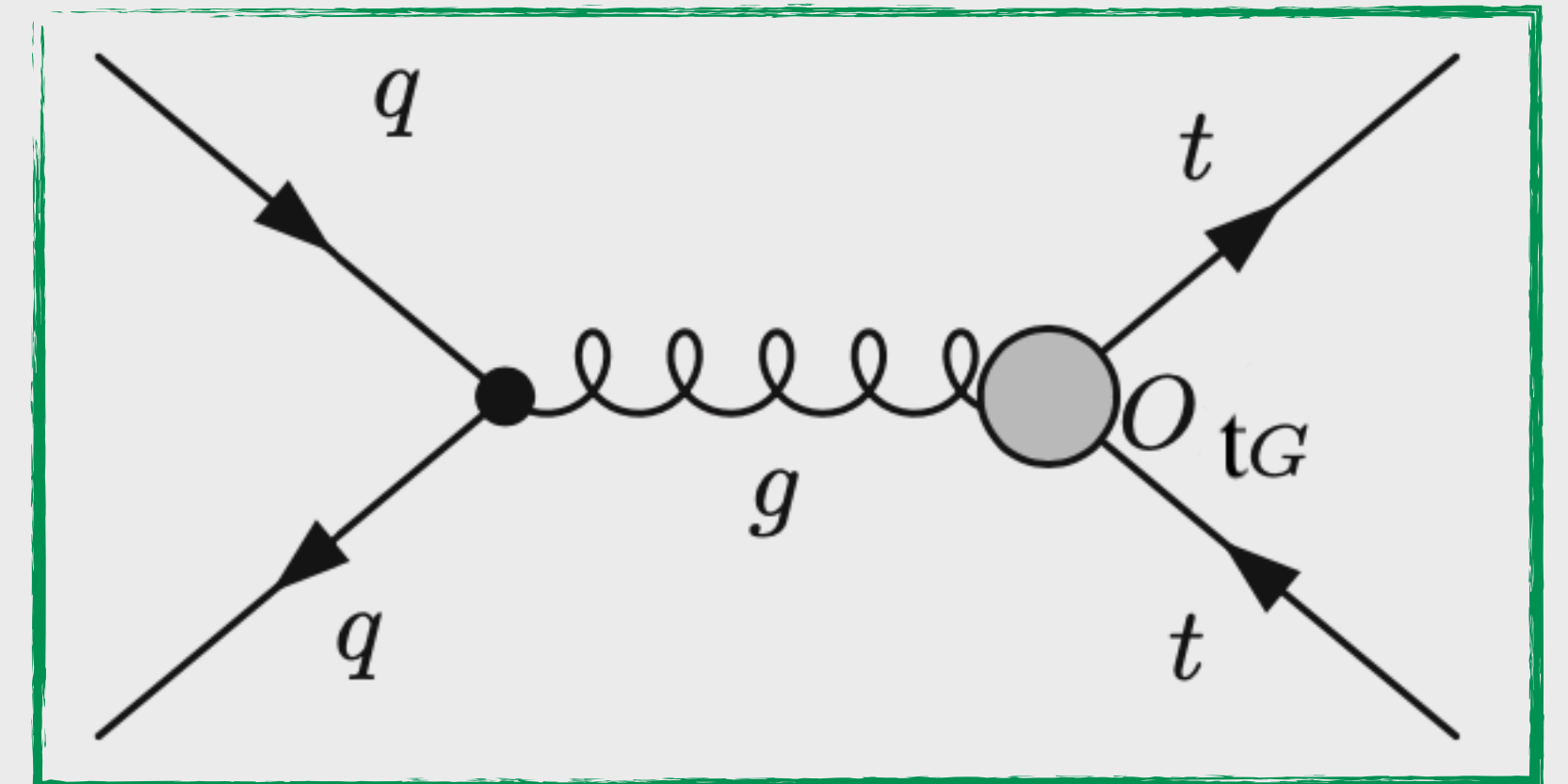
- 59 independent  $\mathcal{O}^{(6)}$  preserving B and L
- 5 independent  $\mathcal{O}^{(6)}$  violating B and L
- 3 generations: 2499 operators!

# SM-EFT, D=6 Basis, Top pair Sector

$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}}^{(4)} + \sum_i \frac{c_i^{(5)} \mathcal{O}_i^{(5)}}{\Lambda} + \boxed{\sum_i \frac{c_i^{(6)} \mathcal{O}_i^{(6)}}{\Lambda^2}} + \mathcal{O}\left(\frac{1}{\Lambda^3}\right)$$

● In Top quark sector, pair production, two examples:

♣ Top and an anti-top and one gluon operator



$$\mathcal{O}_{tG} = (\bar{Q} \sigma^{\mu\nu} T^A t) \tilde{\phi} G_{\mu\nu}^A$$

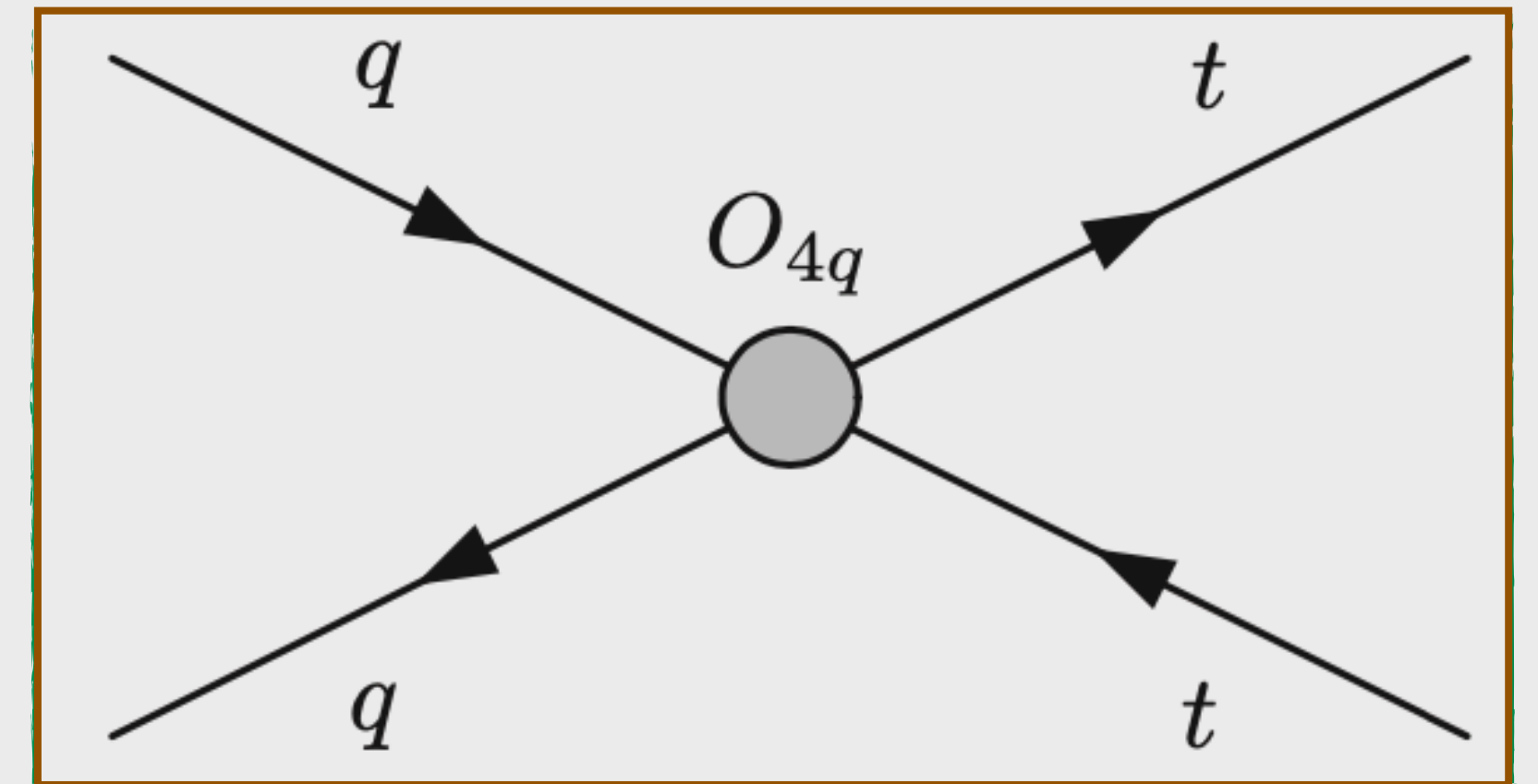
# SM-EFT, D=6 Basis, Top pair Sector

$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}}^{(4)} + \sum_i \frac{c_i^{(5)} \mathcal{O}_i^{(5)}}{\Lambda} + \boxed{\sum_i \frac{c_i^{(6)} \mathcal{O}_i^{(6)}}{\Lambda^2}} + \mathcal{O}\left(\frac{1}{\Lambda^3}\right)$$

◎ In Top quark sector, pair production, two examples:

♣ Top and an anti-top and one gluon operator

♣ 4-quark fermion operator



$$\mathcal{O}_{tq}^8 = \left( \bar{t} \gamma_\mu T^A t \right) \left( \bar{q}_i \gamma^\mu T^A q_i \right)$$

# Introduction

## Motivation

- Perform Global Fit using spin correlation observables at LO or NLO to constrain Wilson Coefficient ?

### Generate simulation samples:

- Define EFT model : SMEFT@NLO model (LO / NLO)
  - SM
  - SMEFT@NLO model ==> LO and NLO

### What Wilson coefficients should be considered ?

- Ctg
- 4-quark operators: ctq8

### Decay tops (using MadSpin)

- Possible at LO and impossible at NLO

ATLAS Top Workshop, slide 5

- What effect does this have on the EFT contribution to spin correlation at NLO?

# Global Fit at LO or NLO ?

## Motivation

- What effect does this have on the EFT contribution to spin correlation at NLO?

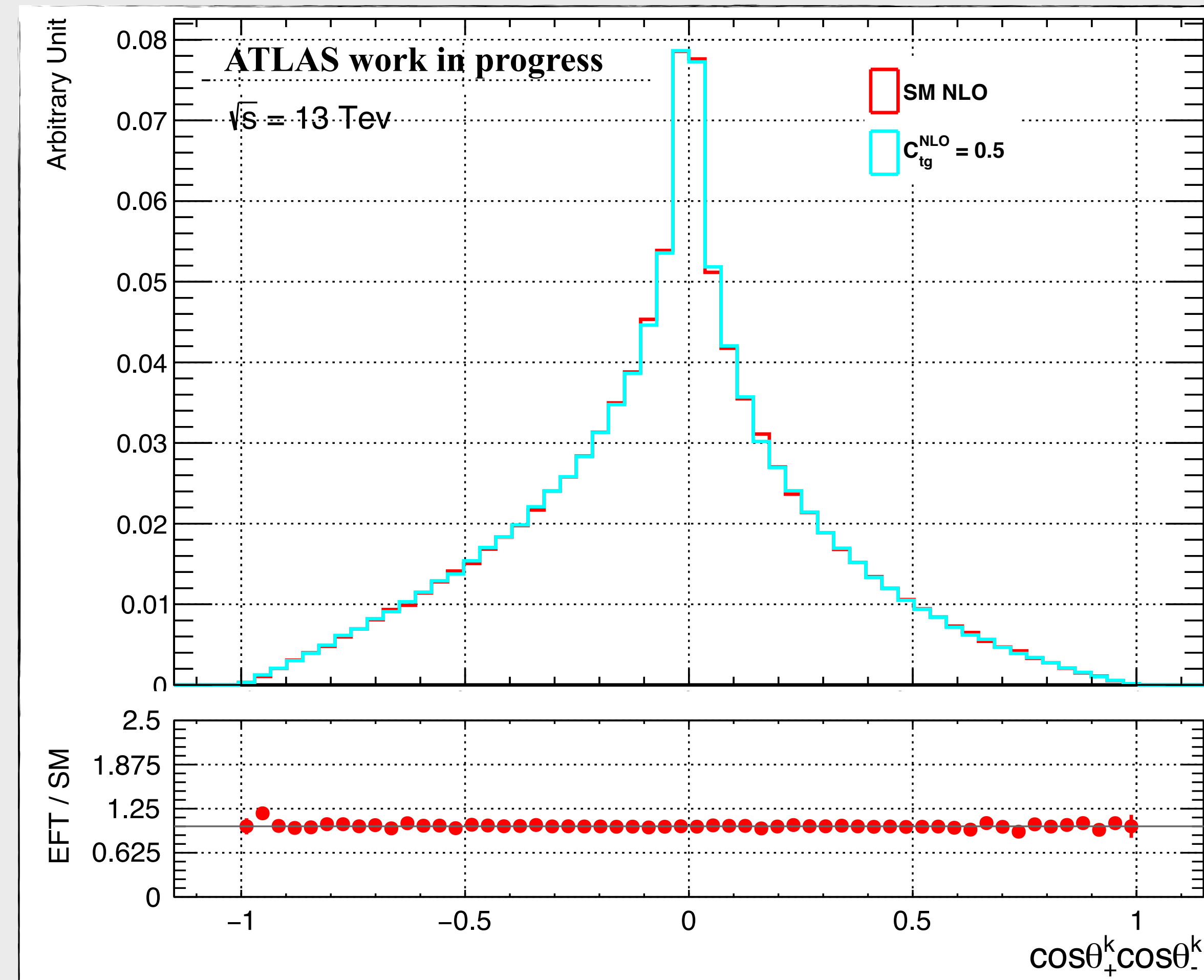
## Results

© Mean Method:  $C(\hat{k}, \hat{k}) = -9 \langle \cos \theta_+^{\hat{k}} \cos \theta_-^{\hat{k}} \rangle$

SM NLO :  $C(k, k) = 0.366313 \pm 0.0042$  (stat)

C<sub>tg</sub> NLO :  $C(k, k) = 0.375982 \pm 0.0042$  (stat)

©  $C_{tg}=0.5$  affect the SM value by 10%



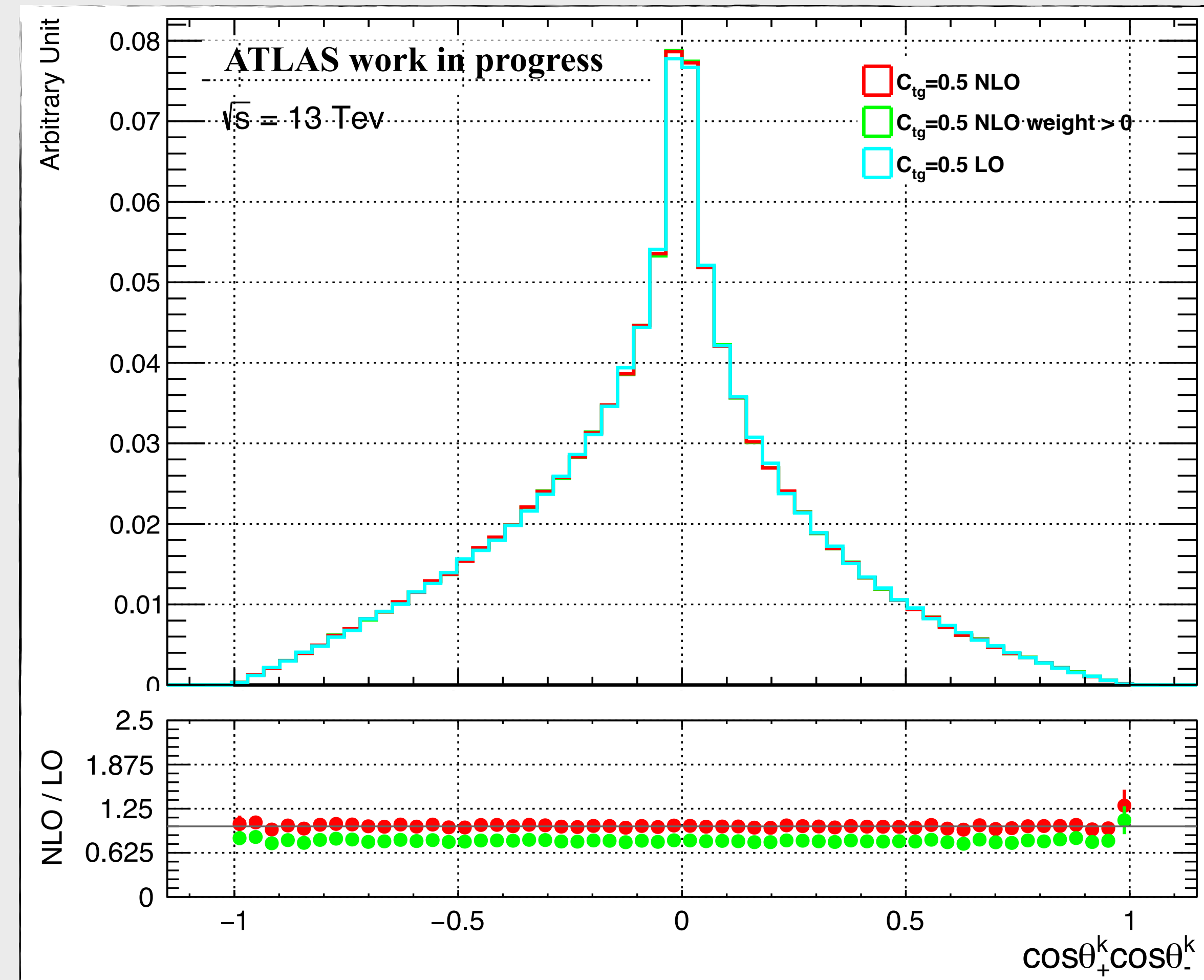
# Global Fit at LO or NLO ?

## Motivation

- What effect does this have on the EFT contribution to spin correlation at NLO?

## Results

- The impact of  $c_{tg}$  at NLO/LO is low
- Preform Global Fit at NLO using spin correlation observables.





# SMEFT dependence on Spin Correlation observables

## Motivation

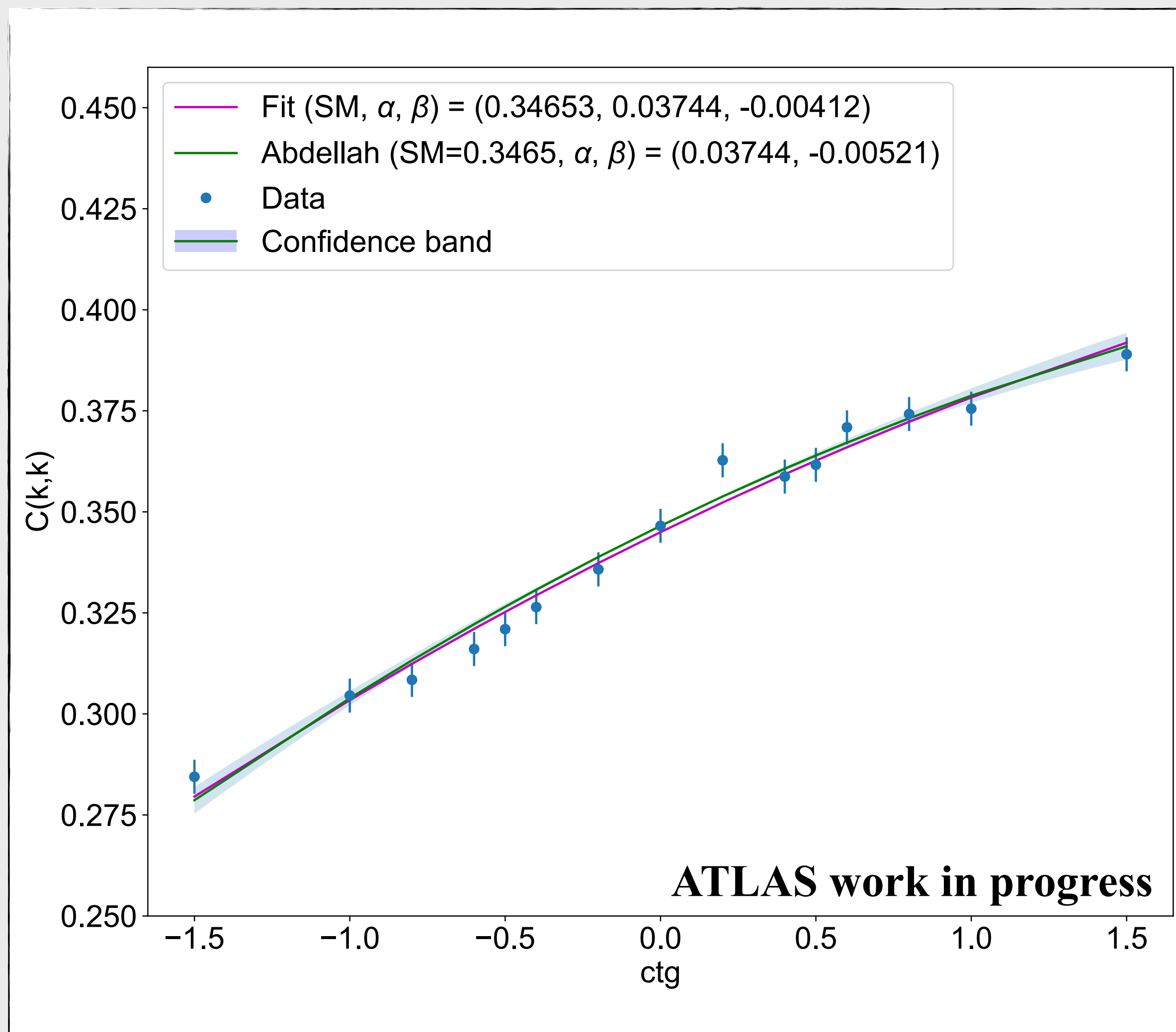
- SMEFT dependence parameterised as polynomials in

Wilson coefficients:

$$C(k, k) = C(k, k)_{SM} + \frac{C_{tg}}{\Lambda^2} \alpha + \frac{C_{tg}^2}{\Lambda^4} \beta$$

## Results

- Compute  $\alpha_{c_{tg}}$  and  $\beta_{c_{tg}}$ .
- We can use the measured  $C(k, k)$ , the estimated  $C(k, k)_{SM}$  with their statistical and systematic uncertainties, and the  $\alpha_{c_{tg}}$  and  $\beta_{c_{tg}}$ , to derive global constraints on the  $c_{tg}$  operator coefficient.
- $C_{tg}$  strongly affect the  $C(k, k)$  observable



# BONUS: SMEFT@NLO Vs Dim6Top

## Motivation

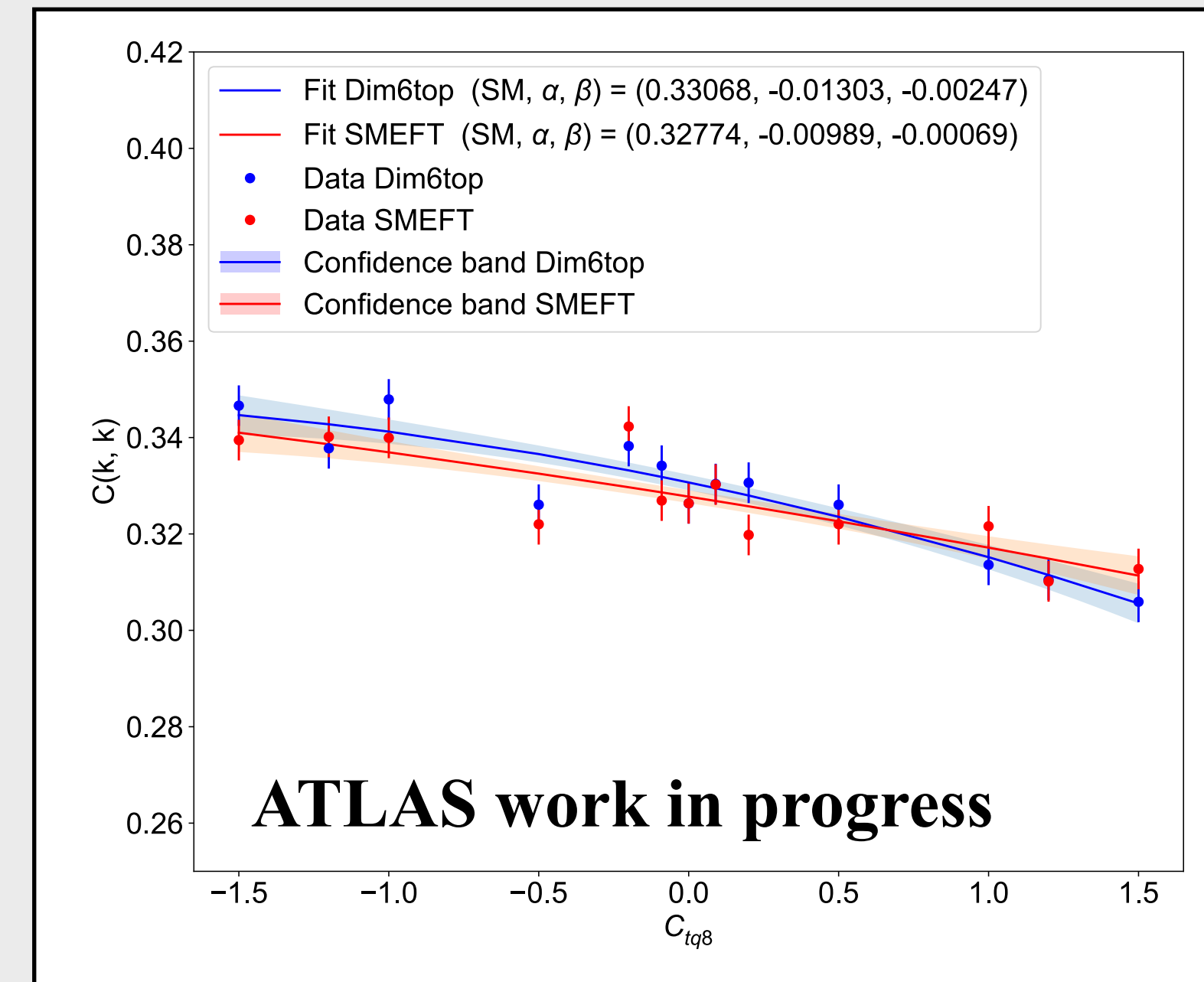
- **Standalone:** Individually generate EFT sample for given Wilson coefficient value (with same seeds ...)
- **Re-weighting:** User Re-weighting to generate EFT samples

## Results

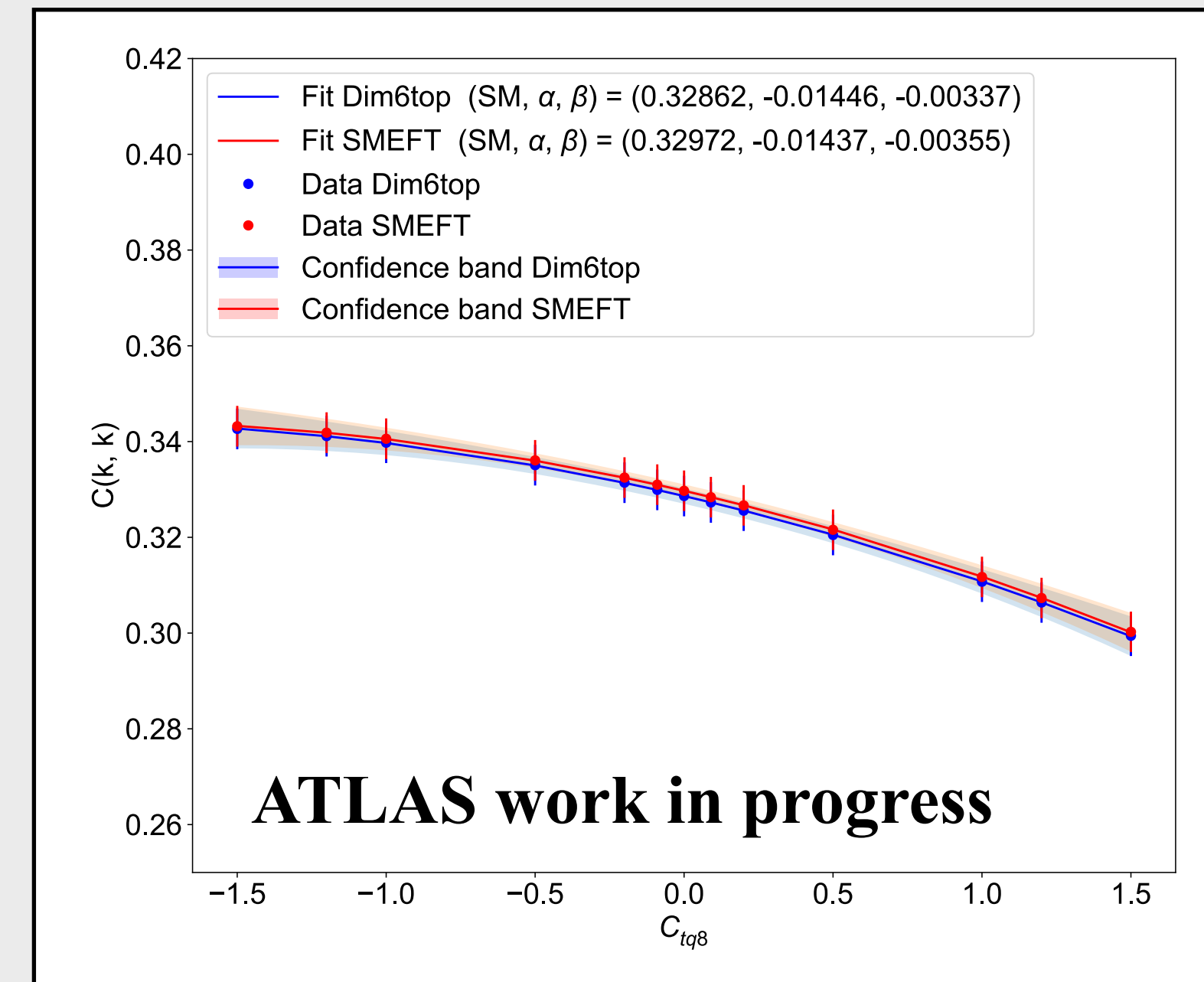
- Perfect agreement between two model using Re-weighting
  - ➔ **Cost:** weighted events have larger statistical uncertainty than an unweighted sample (Standalone) with the same number of events.

- SMEFT@NLO model and Dim6top model show appx. same value of  $\alpha_{ctq8}$  and  $\beta_{ctq8}$  [within the statistical uncertainties.]

## Standalone



## Re-weighting



# Summary

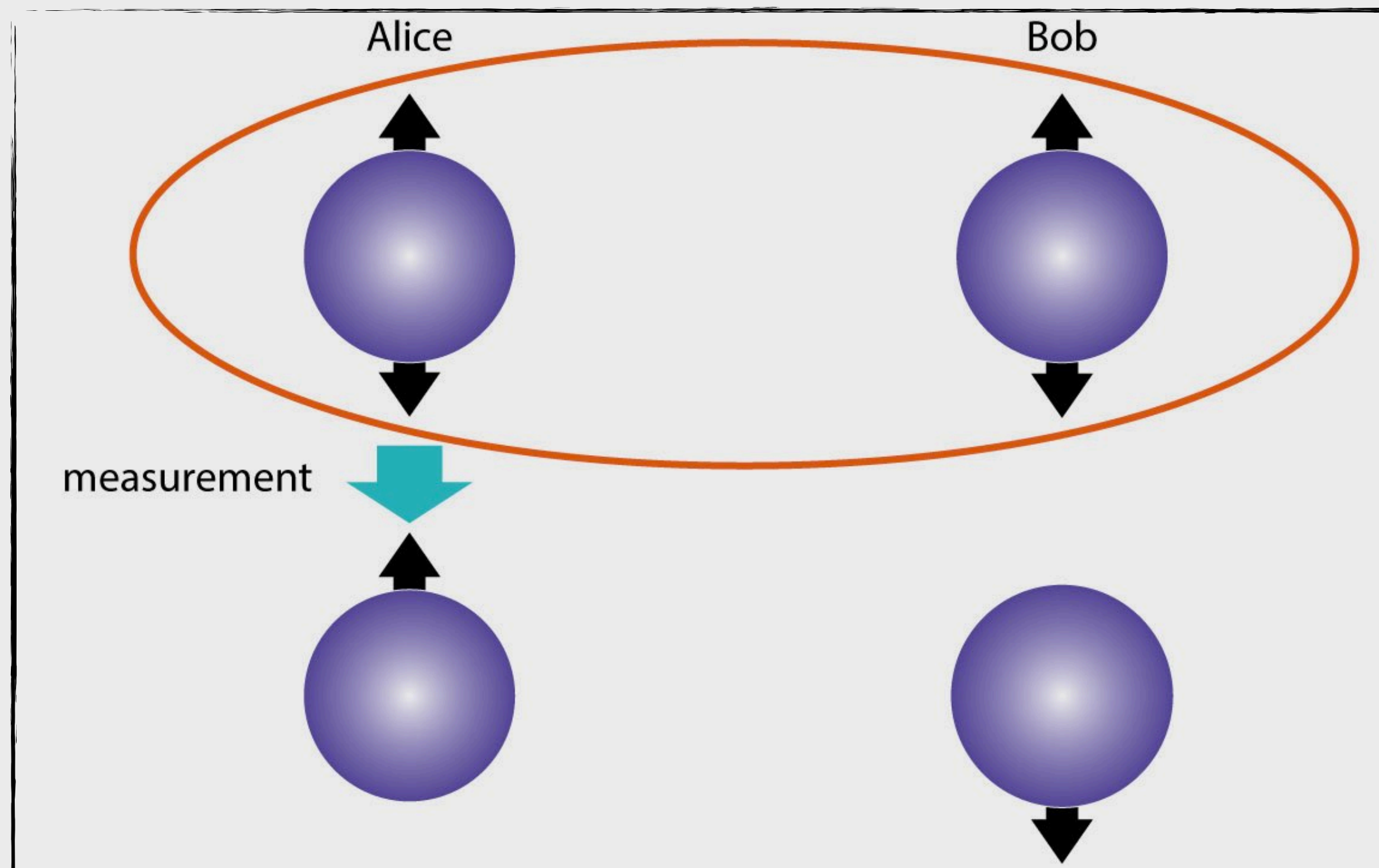
- ◎ Direct measurements of spin correlations in close agreement with SM predictions
- ◎ Precision top quark spin measurements are a powerful probe of new physics and complementary to other approaches.
- ◎ Study the impact of EFT at LO and NLO on spin correlation observables
  - ♣ Preform Global Fit at NLO
  - ♣ SMEFT@NLO and Dim6Top comparison

- **Quantum Entanglement at LHC**
- **Violation of Bell inequalities (BIs) at LHC**

# Quantum Entanglement in $t\bar{t}$

Motivation

What is Quantum Entanglement?

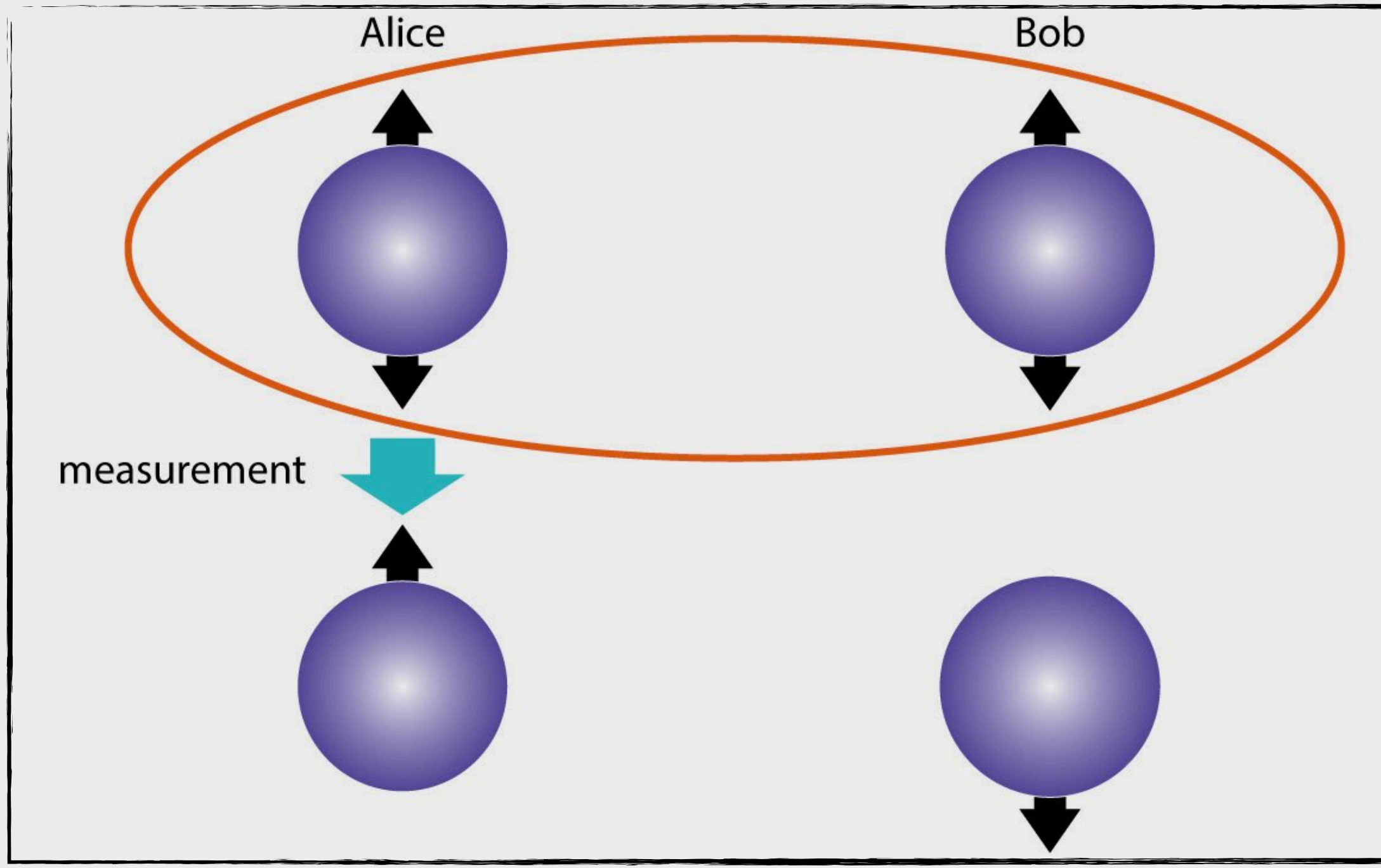


© Observed in photons, atoms, superconductors ... **Humm LHC ?**

# Quantum Entanglement in $t\bar{t}$

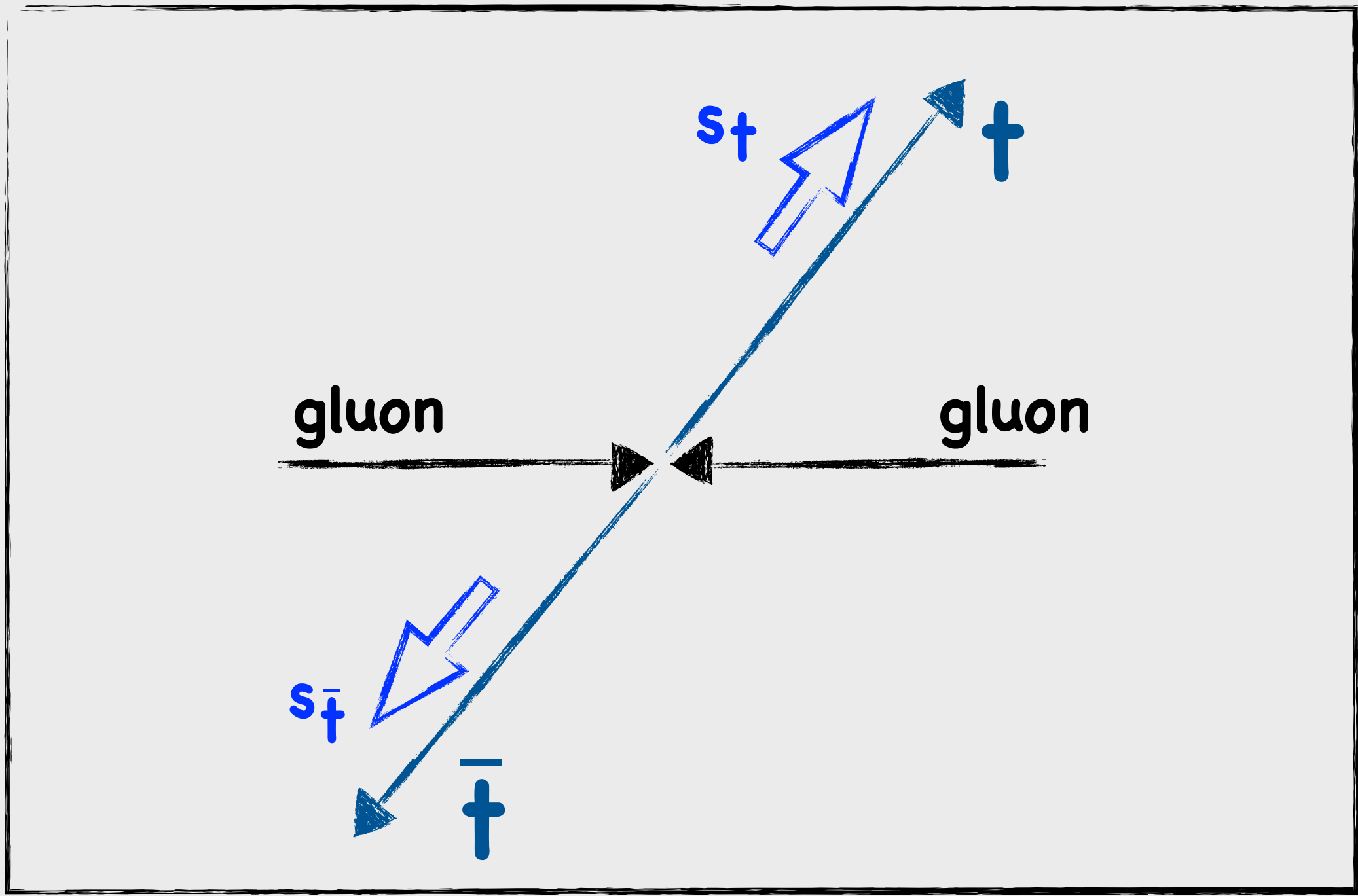
Motivation

What is Quantum Entanglement?



© Observed in photons, atoms, superconductors ... **Humm LHC ?**

How is it reflected in a  $t\bar{t}$  production?



© Spin state of  $t$  and  $\bar{t}$  quarks produced at the LHC can be entangled, and this can be probed experimentally

# Where to look for Quantum Entanglement in $t\bar{t}$ ?

## Entanglement Criterion - Concurrence

● The  $t\bar{t}$  production is described by the production spin density matrix:

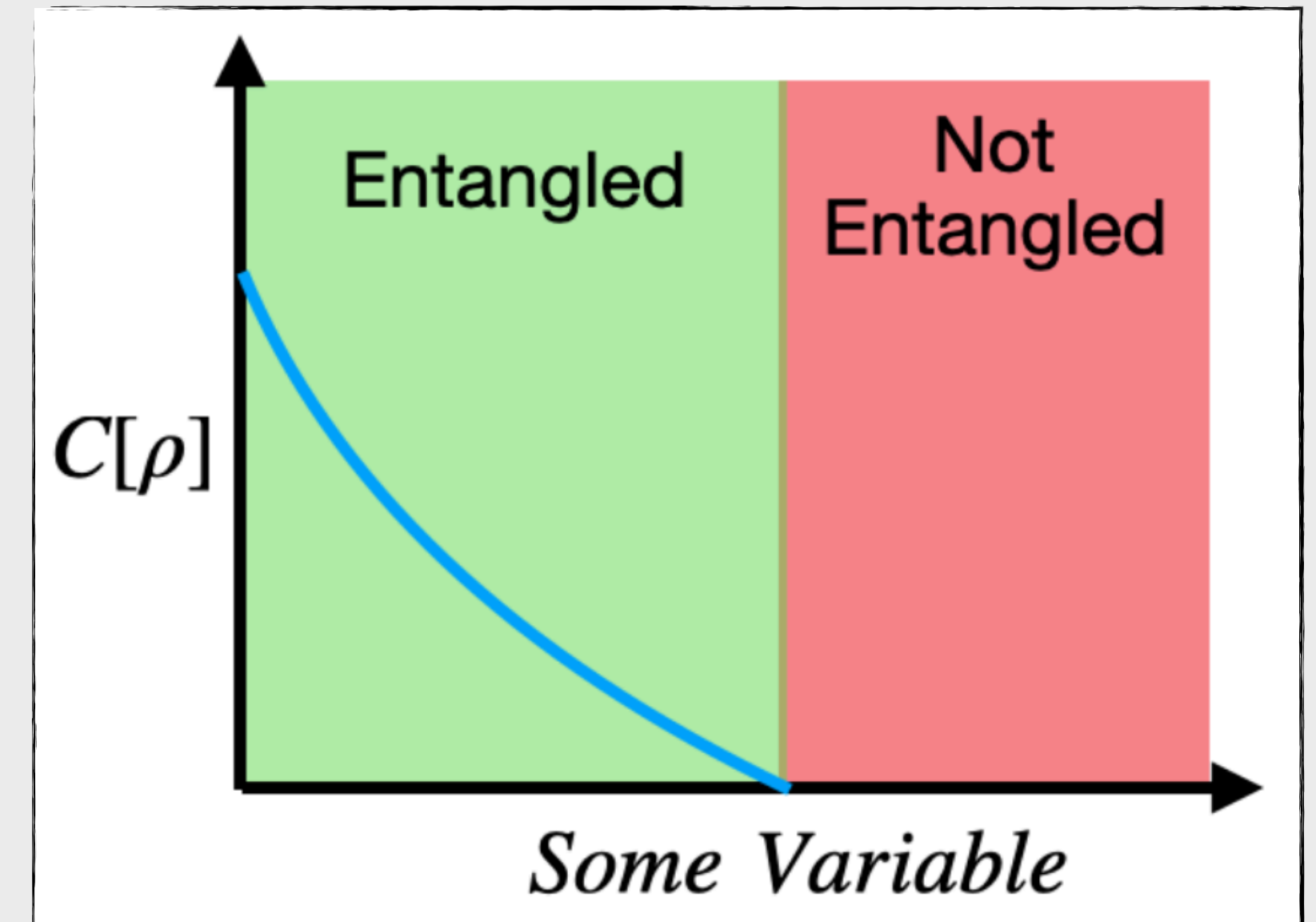
$$\rho = \frac{1}{4} \left( 1 \otimes 1 + B_i \sigma_i \otimes 1 + \bar{B}_j 1 \otimes \sigma_j + C_{ij} \sigma_i \otimes \sigma_j \right)$$

● By invoking the Peres-Horodecki criterion:

$$\Delta \equiv -C_{nn} + |C_{kk} + C_{rr}| - 1 > 0$$

is a sufficient condition for the presence of entanglement

● Concurrence  $C[\rho] = \frac{\max(\Delta, 0)}{2}$



# Where to look for Quantum Entanglement in $t\bar{t}$ ?

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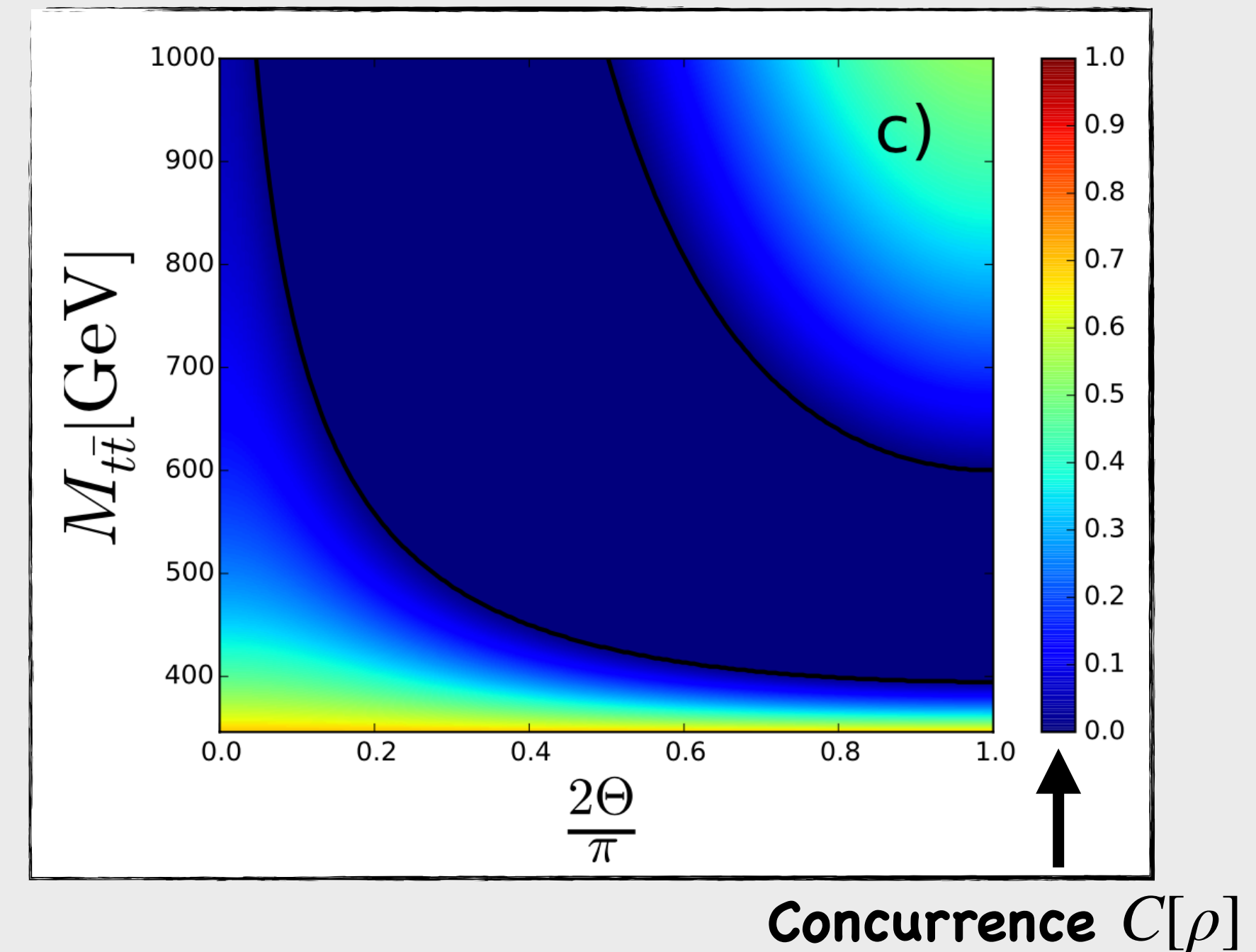
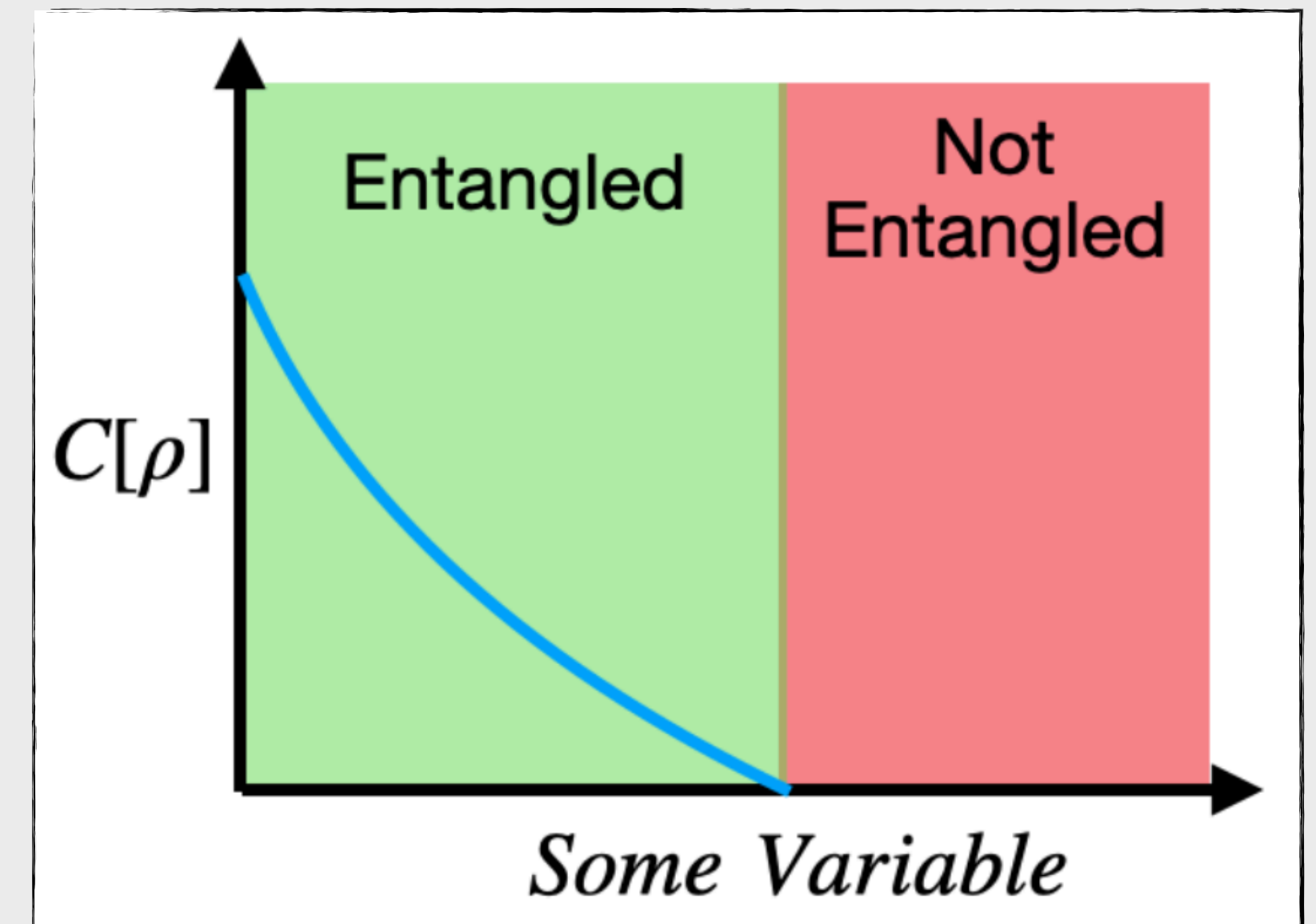
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# Where to look for Quantum Entanglement in $t\bar{t}$ ?

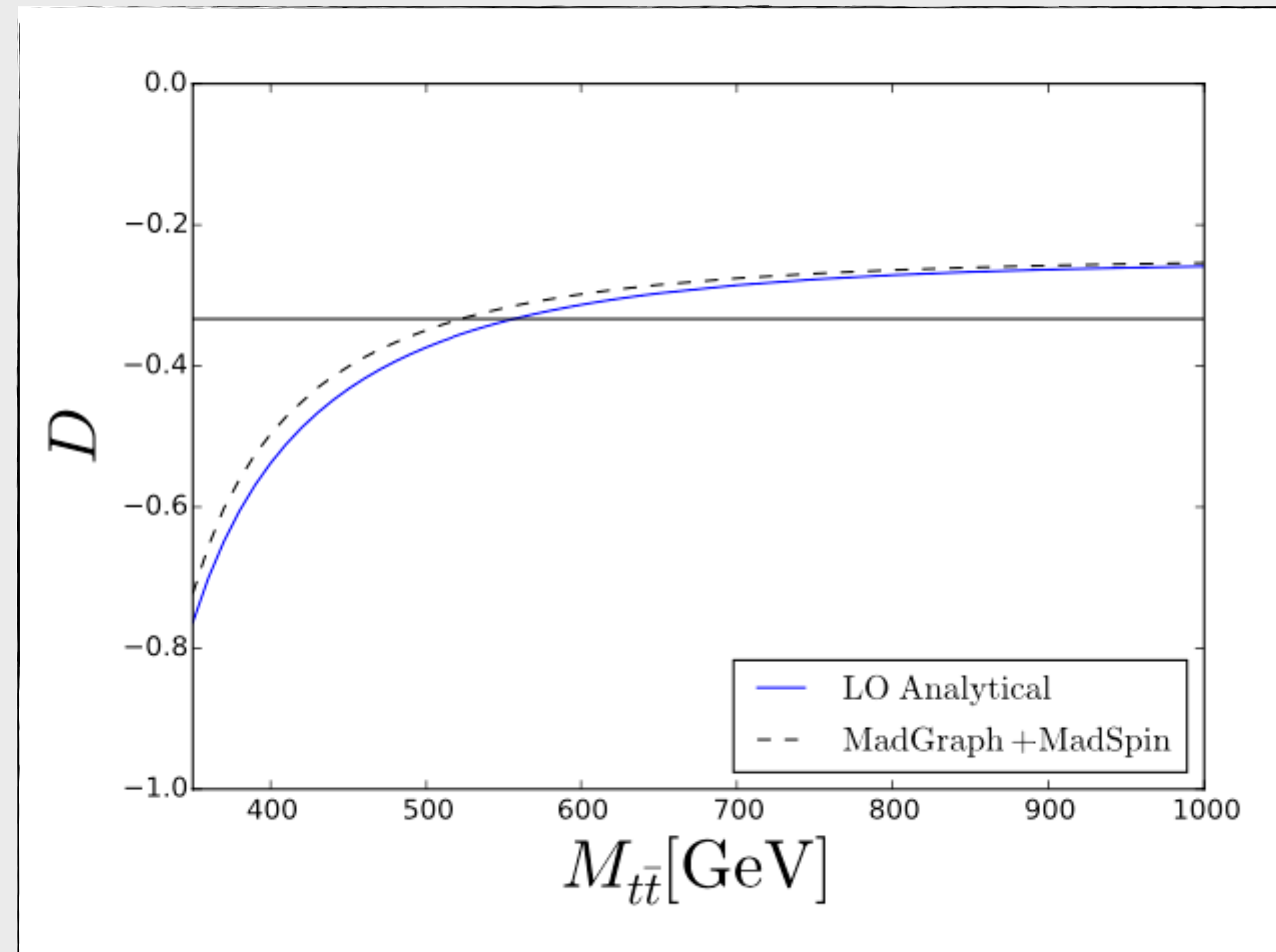
## Equivalent Measurable Observable

● The condition  $\Delta > 0$  translates into  $D < -1/3$ ,

$$\clubsuit D = - (C_{kk} + C_{rr} + C_{nn})/3$$

● Experimentally :  $\frac{1}{\sigma} \frac{d\sigma}{d \cos \varphi_{\ell\ell}} = \frac{1}{2} (1 - D \cos \varphi_{\ell\ell})$

● Needs to be measured differentially as a function of  $M_{t\bar{t}}$



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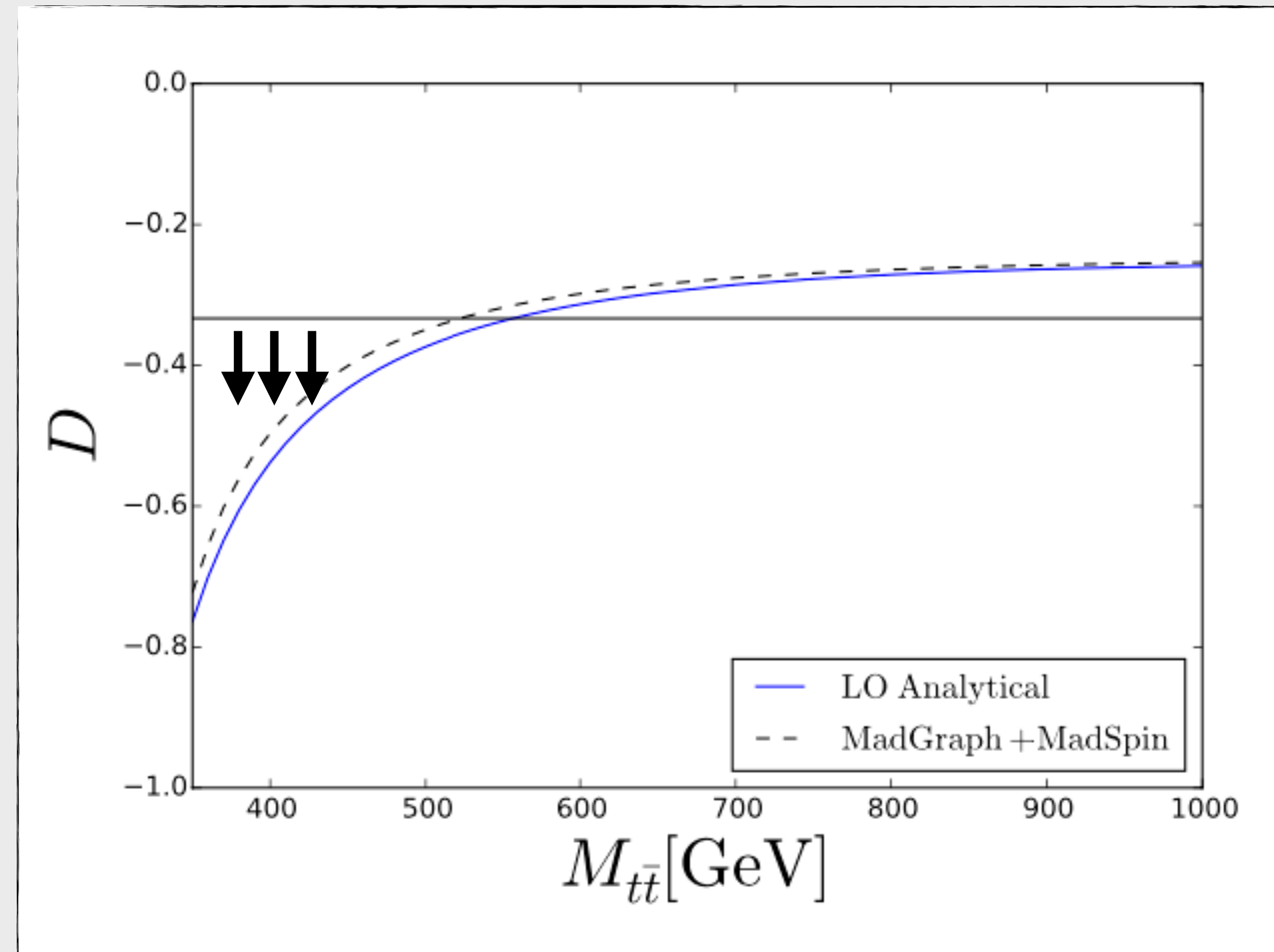
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● Needs to be measured differentially as a function of  $M_{t\bar{t}}$

$\clubsuit M_{t\bar{t}} \leq 400 \text{ GeV}$ :

➔ if  $D < -1/3$ , the stat is entangled!

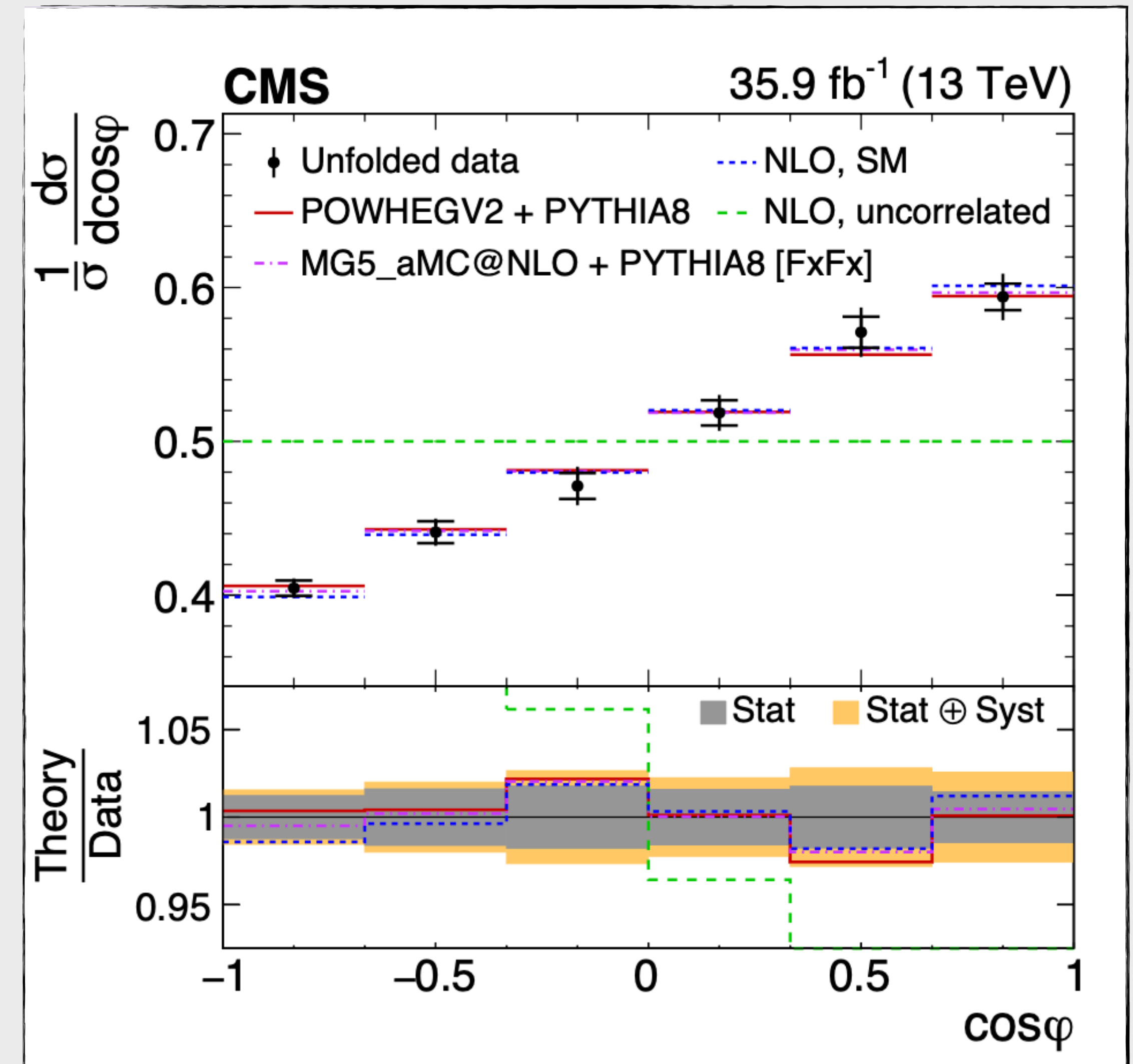


# Recent Related Measurement

◎ Recently,  $D$  was measured with no selection on  $M_{t\bar{t}}$  by the CMS collaboration.

♣  $D = -0.237 \pm 0.011 > -1/3$

♣ No search for entanglement



[CMS paper](#)

# What is the best method for measuring D observable ?

## Method

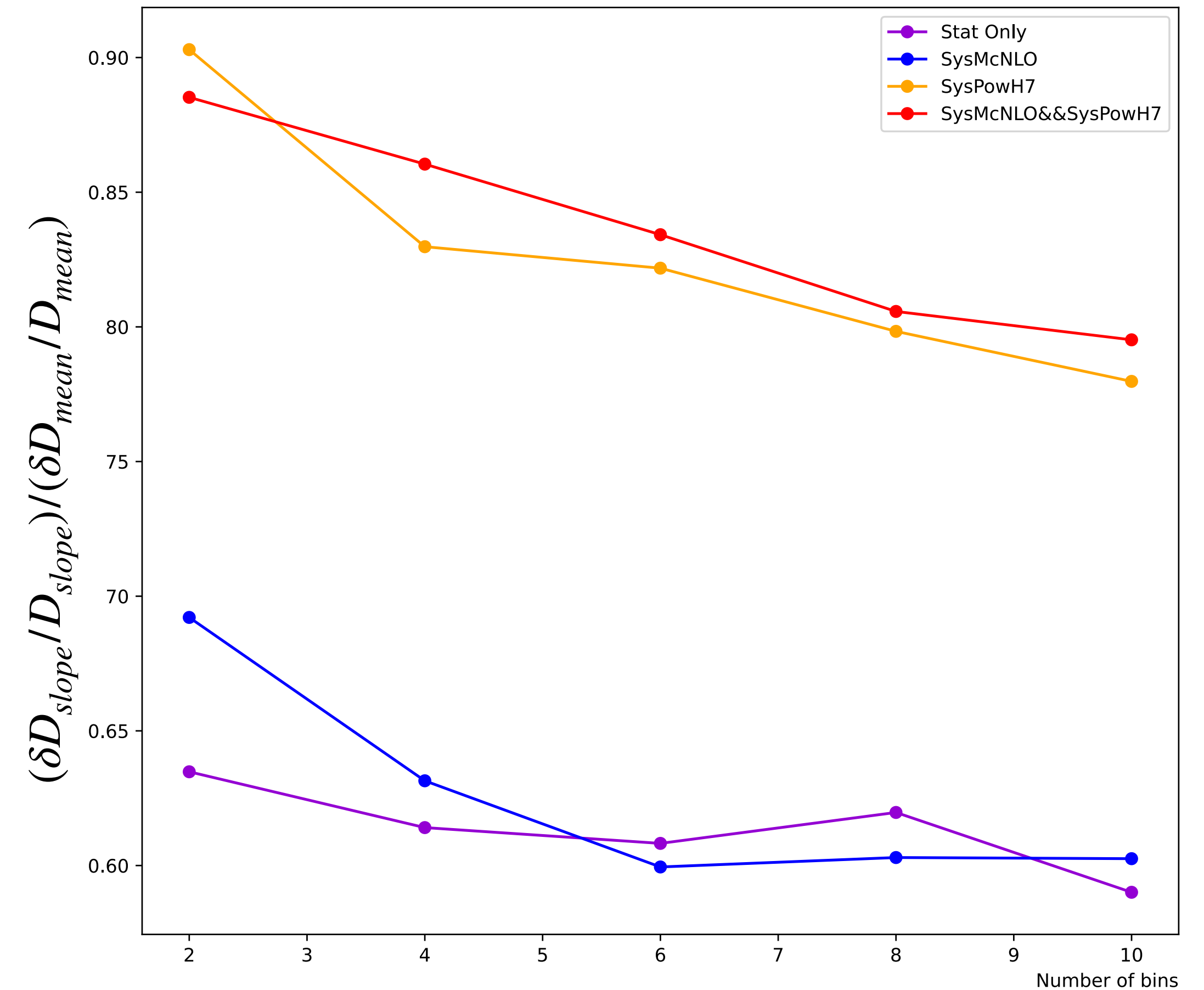
$$\frac{1}{\sigma} \frac{d\sigma}{d \cos \varphi_{\ell\ell}} = \frac{1}{2} (1 - D \cos \varphi_{\ell\ell})$$

- Slope method: Measuring the slope of the differential normalised cross-section
- Mean method: After integration, one can just measure the mean of the distribution:  $D = -3 \langle \cos \varphi_{\ell\ell} \rangle$
- Compare both methods:
  - Measure the unfolded D using different bin of the distribution  $\cos \varphi_{\ell\ell}$ : 2/4/6/8/10 Bins
- With Slope method
  - ➔ Stat Only: Gain 40%
  - ➔ Stat+syst: Gain 17%

## Results

ATLAS work in progress  $\sqrt{s} = 13$  TeV,  $\mathcal{L} = 36$  fb<sup>-1</sup>

SignalModellingSys em/ee/mm



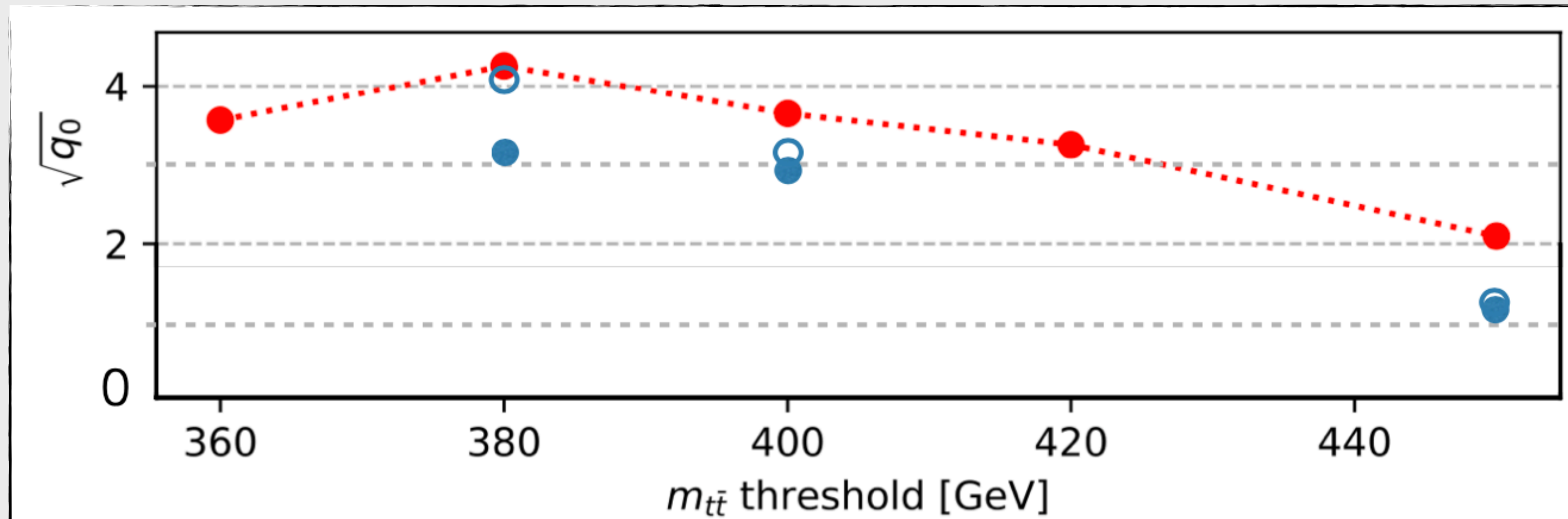
- Use Slope method for the measurement of D observable

# Entanglement at LHC ?

- Calculate the likelihood ratio by comparing the observed and the non-entangled values:

$$q_0 = -2 \ln \frac{\mathcal{L}(D = -1/3)}{\mathcal{L}(\hat{D})}$$

ATLAS work in progress



- **PLU**
- **IBU\*** (ME Pythia)
- **IBU\*** (ME herwig)

\*all modelling systematics in PLU, only ME & PS in IBU

- Unfold to parton-level:

- ➔ Profile Likelihood Unfolding (PLU)
- ➔ Iterative Bayesian Unfolding (IBU)

- Tests of both methods are ongoing, but a decision has not been made yet on which method to use.
- Possible first-time measurement of quantum entanglement.

# Bell inequalities (BIs) Historically?

◎ EPR Paradox: There are some hidden variables that are missing in order to have a full theory.

◎ If local hidden variables holds, they should satisfy some inequality.

✿  $\mathcal{C}_{A,B} \leq \text{constant}$ , where  $\mathcal{C}$  measures correlation between the supposedly non-interacting subsystems A and B.

Violation of BIs  $\implies$  Entanglement

~~Violation of BIs  $\longleftarrow$  Entanglement~~



# Evidence of Bell inequality violation

© The Bell/CHSH inequality

$$|\langle ab \rangle - \langle ab' \rangle + \langle a'b \rangle + \langle a'b' \rangle| \leq 2$$

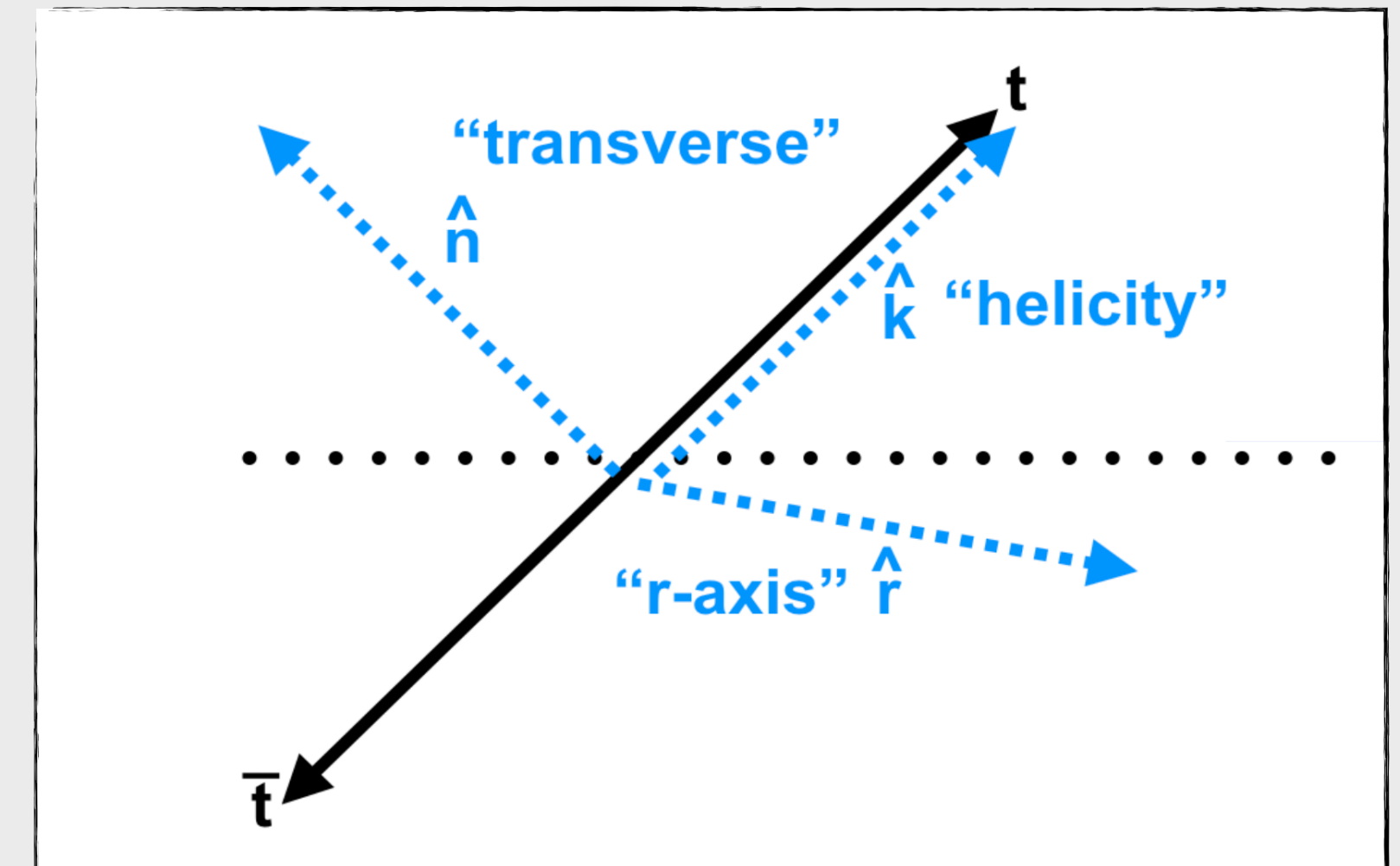
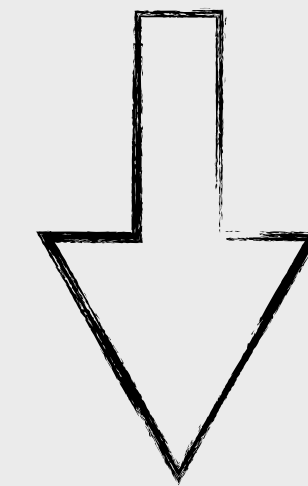
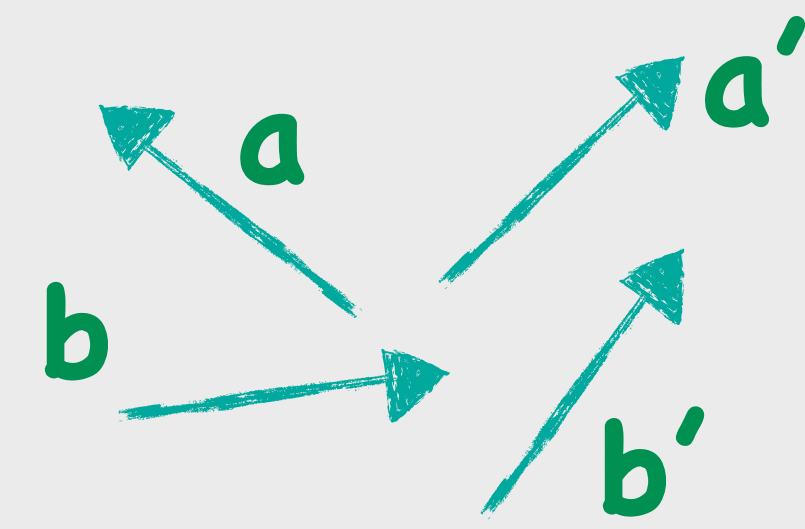
© The Bell/CHSH inequality evaluated for a system described by the  $t\bar{t}$  spin density matrix:

➔ Method 1:  $\max_{aa'bb'} |\langle ab \rangle - \langle ab' \rangle + \langle a'b \rangle + \langle a'b' \rangle| = 2\sqrt{\lambda + \lambda'}$

➔ Method 2:  $|-C_{rr} + C_{nn}| < \sqrt{2}$  (At high  $m_{t\bar{t}}$  and  $\theta_{CM}$ )

where  $\lambda$  and  $\lambda'$  are the two largest eigenvalues of  $C^T C$

$$C = \begin{pmatrix} C(\hat{k}, \hat{k}) & C(\hat{r}, \hat{k}) & C(\hat{n}, \hat{k}) \\ C(\hat{k}, \hat{r}) & C(\hat{r}, \hat{r}) & C(\hat{n}, \hat{r}) \\ C(\hat{k}, \hat{n}) & C(\hat{r}, \hat{n}) & C(\hat{n}, \hat{n}) \end{pmatrix}$$



# Evidence of Bell inequality violation

## ◎ The Bell/CHSH inequality

$$\left| \langle ab \rangle - \langle ab' \rangle + \langle a'b \rangle + \langle a'b' \rangle \right| \leq 2$$

## ◎ The Bell/CHSH inequality evaluated for a system described by the $t\bar{t}$ spin density matrix:

→ Method 1:  $\max_{aa'bb'} \left| \langle ab \rangle - \langle ab' \rangle + \langle a'b \rangle + \langle a'b' \rangle \right| = 2\sqrt{\lambda + \lambda'}$

→ Method 2:  $\left| -C_{rr} + C_{nn} \right| < \sqrt{2}$  (At high  $m_{t\bar{t}}$  and  $\theta_{CM}$ )

where  $\lambda$  and  $\lambda'$  are the two largest eigenvalues of  $C^T C$

$$C = \begin{pmatrix} C(\hat{k}, \hat{k}) & C(\hat{r}, \hat{k}) & C(\hat{n}, \hat{k}) \\ C(\hat{k}, \hat{r}) & C(\hat{r}, \hat{r}) & C(\hat{n}, \hat{r}) \\ C(\hat{k}, \hat{n}) & C(\hat{r}, \hat{n}) & C(\hat{n}, \hat{n}) \end{pmatrix}$$



# Evidence of Bell inequality violation

© The Bell/CHSH inequality

$$|\langle ab \rangle - \langle ab' \rangle + \langle a'b \rangle + \langle a'b' \rangle| \leq 2$$

© The Bell/CHSH inequality evaluated for a system described by the  $t\bar{t}$  spin density matrix:

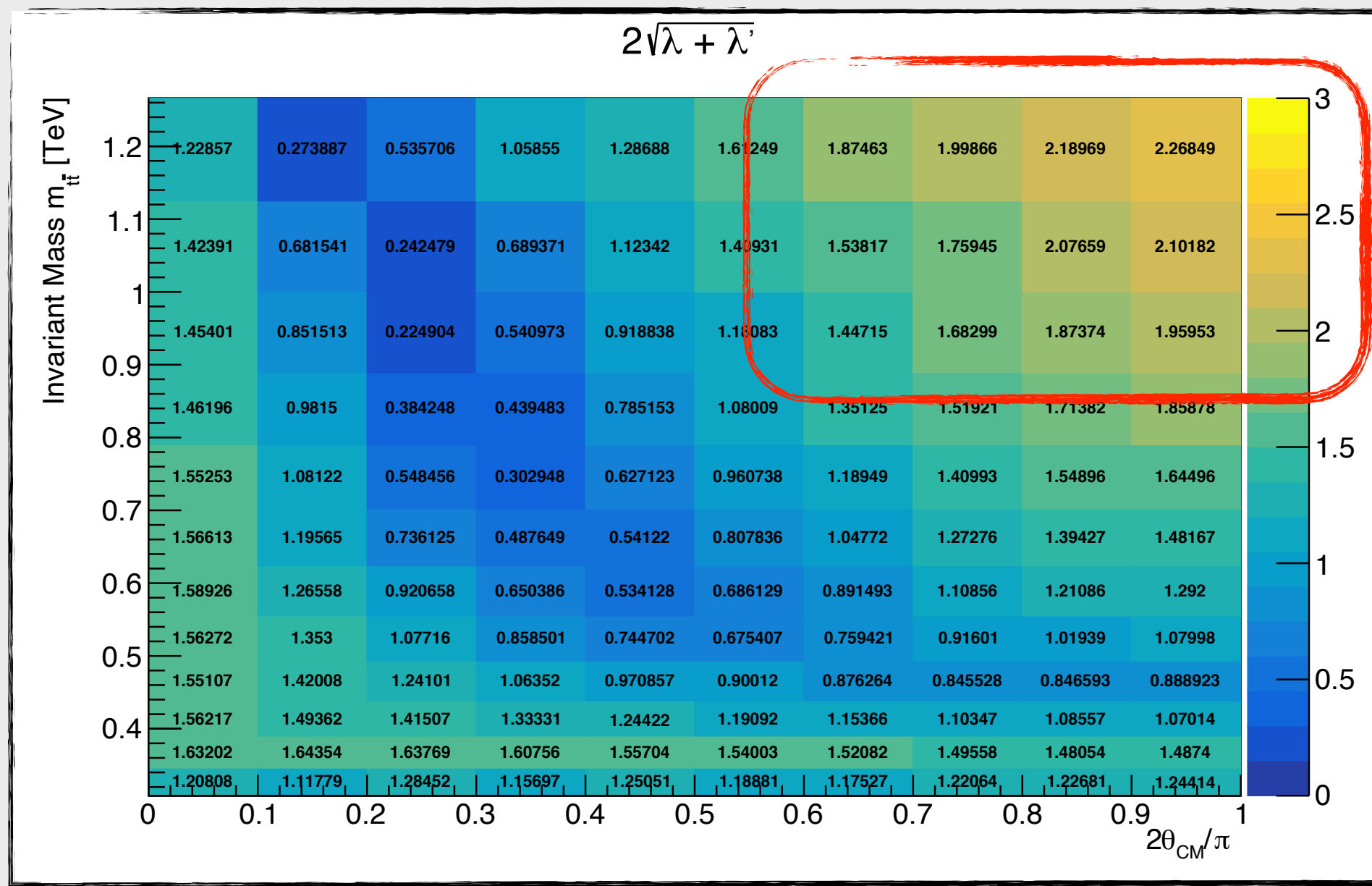
- ➔ Method 1:  $\max_{aa'bb'} |\langle ab \rangle - \langle ab' \rangle + \langle a'b \rangle + \langle a'b' \rangle| = 2\sqrt{\lambda + \lambda'}$
- ➔ Method 2:  $|-C_{rr} + C_{nn}| < \sqrt{2}$  (At high  $m_{t\bar{t}}$  and  $\theta_{CM}$ )

where  $\lambda$  and  $\lambda'$  are the two largest eigenvalues of  $C^T C$

$$C = \begin{pmatrix} C(\hat{k}, \hat{k}) & C(\hat{r}, \hat{k}) & C(\hat{n}, \hat{k}) \\ C(\hat{k}, \hat{r}) & C(\hat{r}, \hat{r}) & C(\hat{n}, \hat{r}) \\ C(\hat{k}, \hat{n}) & C(\hat{r}, \hat{n}) & C(\hat{n}, \hat{n}) \end{pmatrix}$$

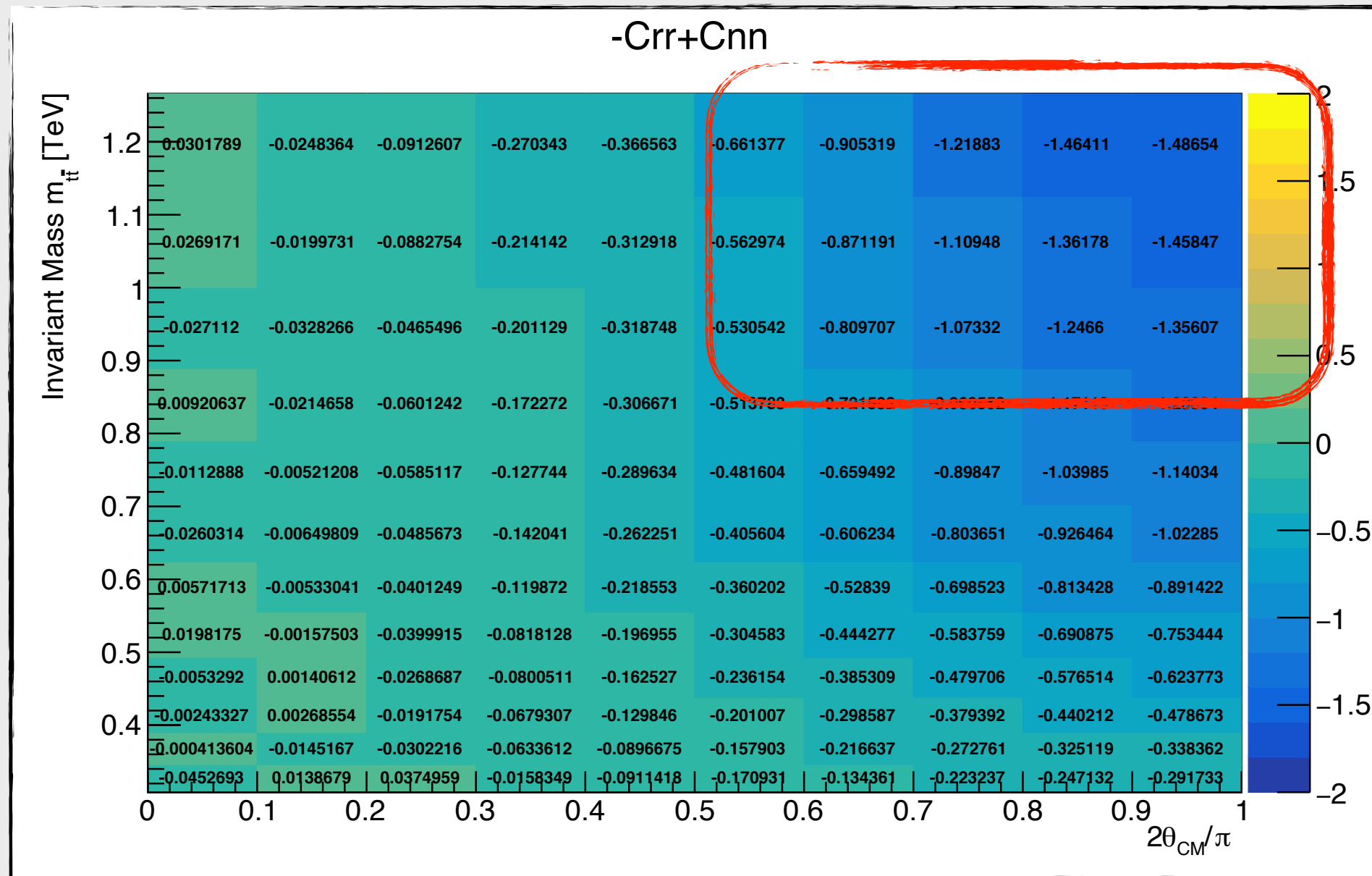
ATLAS work in progress

$\geq 2$  is a violation



ATLAS work in progress

$< -\sqrt{2}$  or  $> \sqrt{2}$  is a violation



# Summary

## ◎ Spin correlation and EFT interpretation

- ➔ Direct measurements of spin correlations with Full Run2 Data
- ➔ Precision top quark spin measurements are a powerful probe of new physics and complementary to other approaches.

## ◎ Entanglement and BIs

- ➔ ATLAS preliminary results show the sensitivity of Entanglement between top quarks at the LHC for the first time.
- ➔ Bell inequalities violations can be tested with LHC data, which is an important test that has not been conducted before.

**Thank You**

**Back-up**

Spacelike probability, %

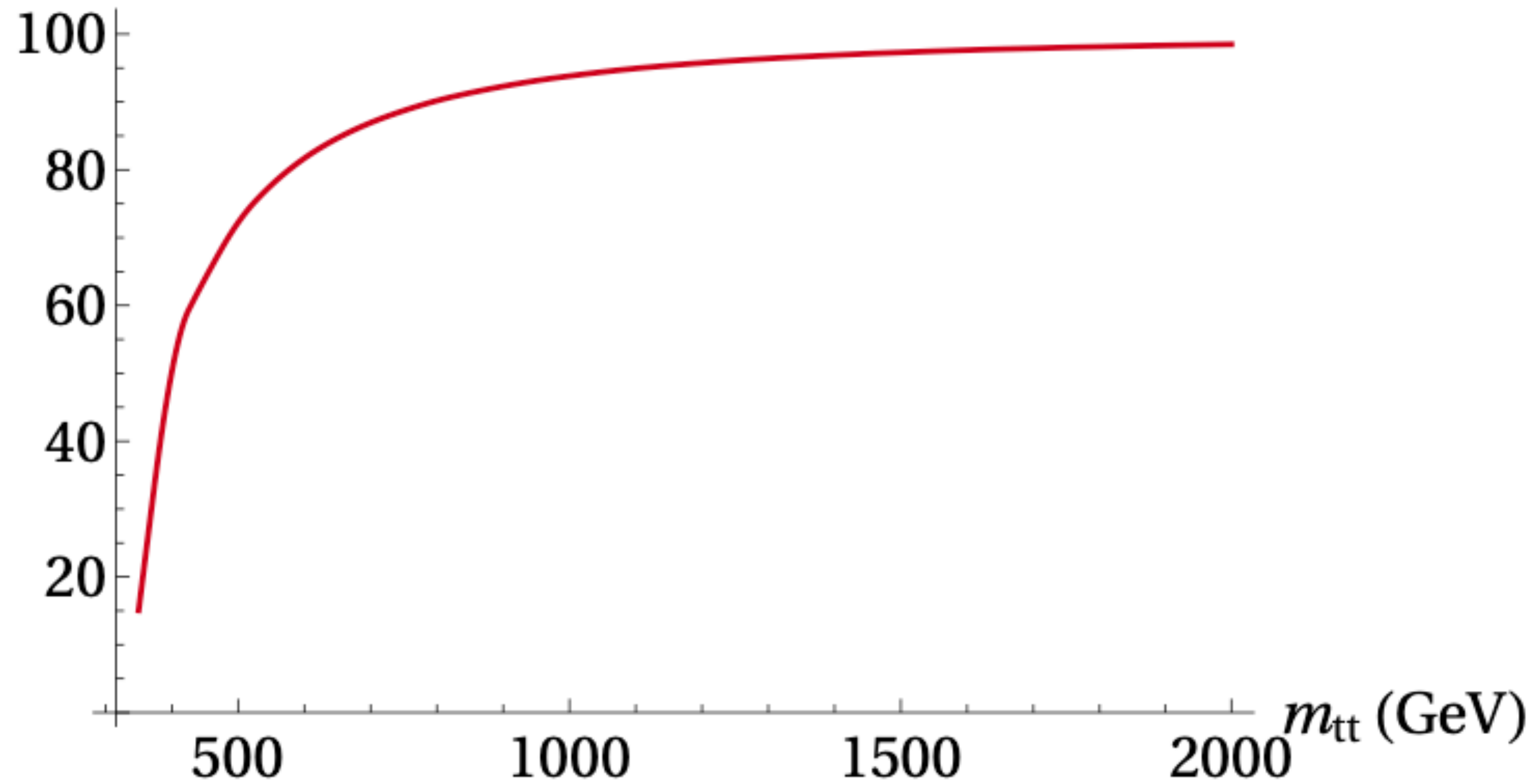


Figure 3.4: Fraction of  $t$  and  $\bar{t}$  decays that are spacelike separated, for  $t\bar{t}$  pairs with a given  $m_{t\bar{t}}$ .

# Comparison of methods

- Disclaimer: there are other unfolding method on the market

## IBU:

- ✓ well established method
- ? nominal result indep. on syst.
- ? cannot constrain systematics
- ✗ non-trivial to combine channels
- ✓ can have  $N_{\text{truth}} \neq N_{\text{reco}}$
- ✗ not easy to add control regions, simultaneous background fit...

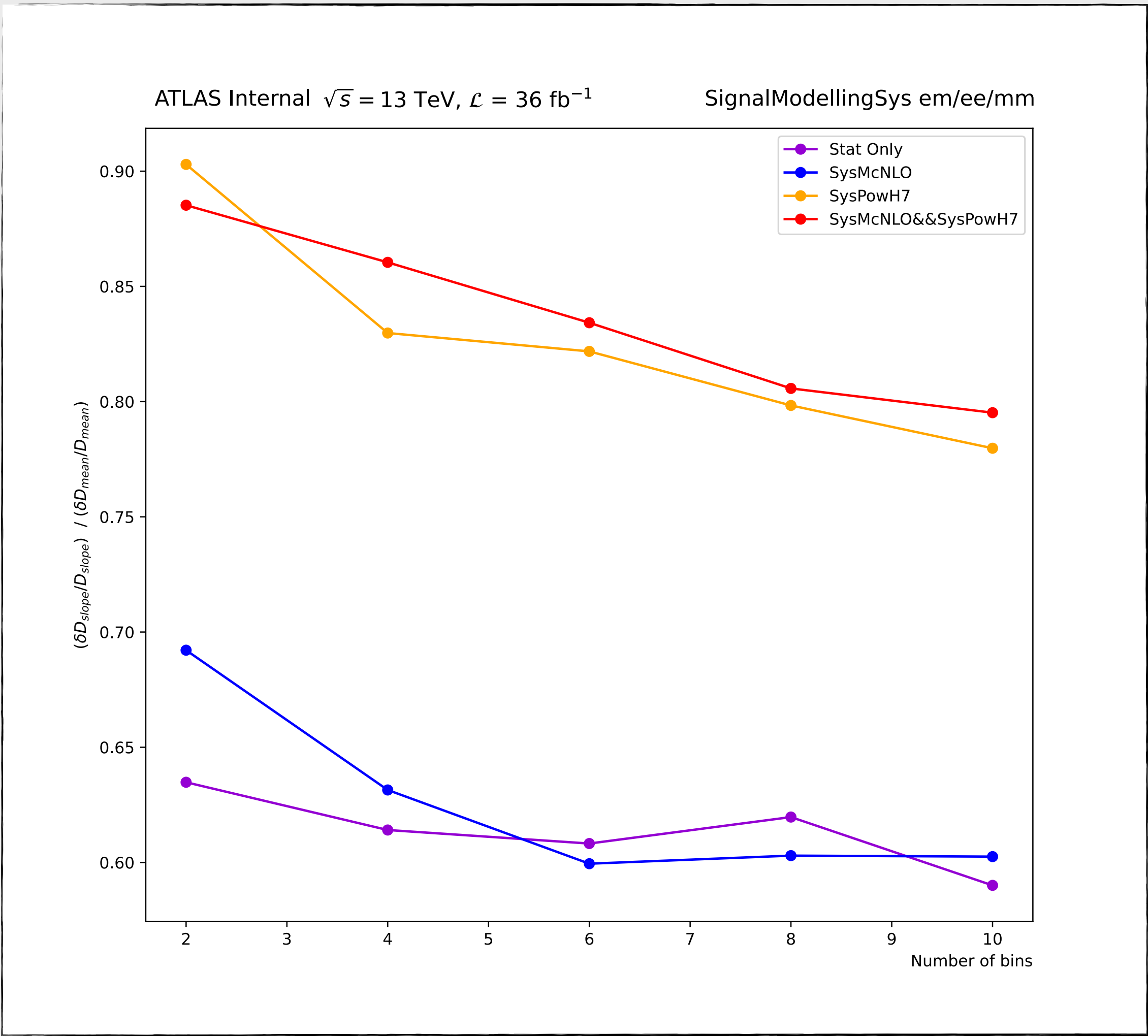
## FBU:

- ✓ successfully used in top analyses
- ✓ syst. included in the formalism
- ? regularization can be added as prior
- ✗ can become computationally intense
- ✓ can handle channel combination,  $N_{\text{truth}} \neq N_{\text{reco}}$ , secondary parameter extraction
- ? can constrain systematics (\*)

## PFU:

- ? relatively new → need testing!
- ✓ syst. included in the formalism
- ✓ regularization can be added as constraint term(s)
- ✓ easily handles channel combination,  $N_{\text{truth}} \neq N_{\text{reco}}$ , secondary parameter extraction
- ? can constrain systematics (\*)
- ✓ can easily add control regions
- ✓ coherent formalism with e.g. total cross-sections

# Measurement of D observables: Mean V.s Slope Uncertainty



**Uncertainty Gained**

NumOfBins	Stat Only	Sys McNLO	Sys PowH7	Sys McNLO,PowH7
2	36 %	31 %	10 %	12 %
4	39 %	37 %	18 %	14 %
6	40 %	41 %	18 %	17 %
8	39 %	40 %	21 %	20 %
10	42 %	40 %	22 %	20 %

# What is the best method for measuring D observable ?

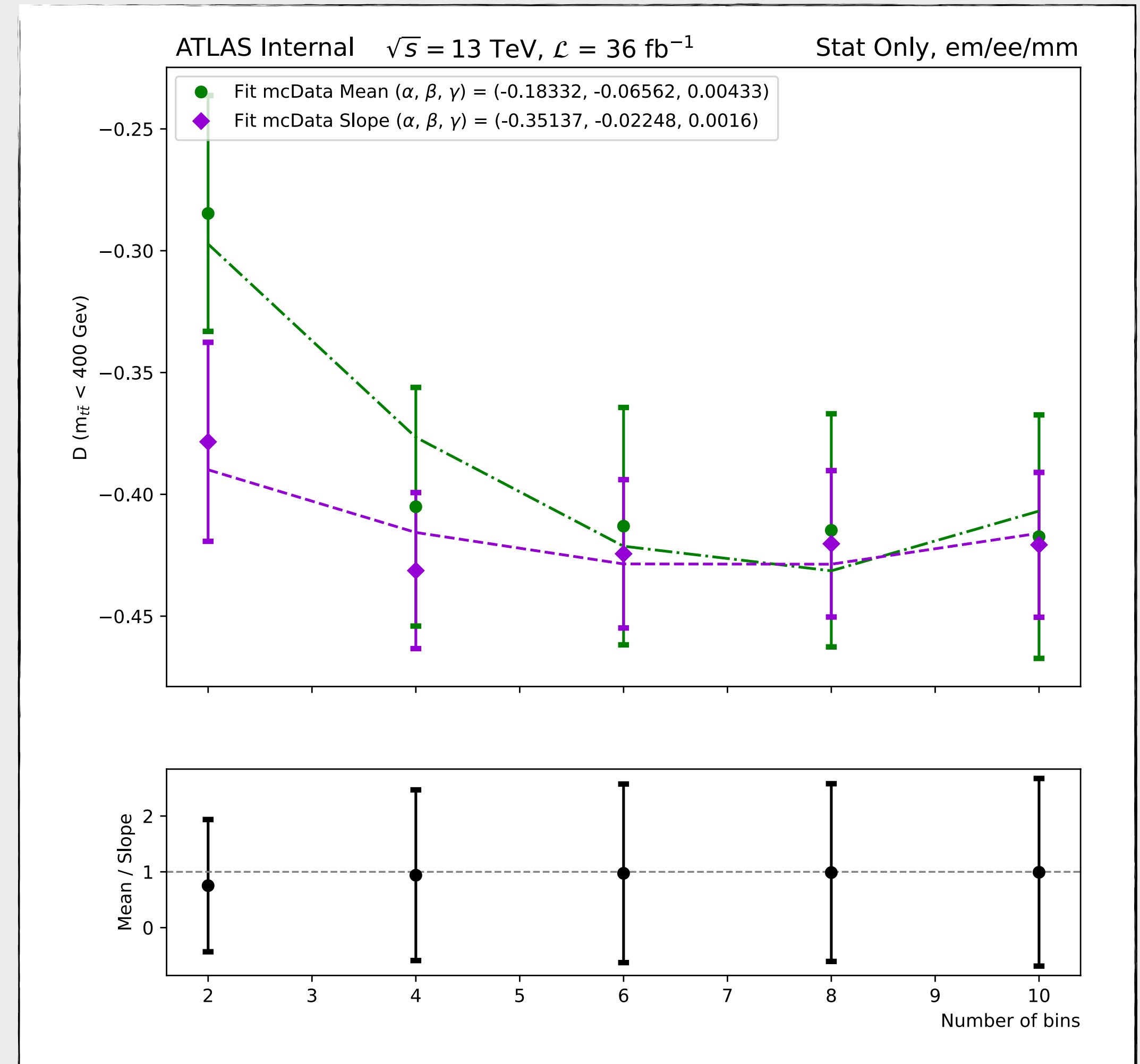
## Method

$$\frac{1}{\sigma} \frac{d\sigma}{d \cos \varphi_{\ell\ell}} = \frac{1}{2} (1 - D \cos \varphi_{\ell\ell})$$

- Slope: Measuring the slope of the differential normalised cross-section
- Mean: After integration, one can just measure the mean of the distribution:  $D = -3 \langle \cos \varphi_{\ell\ell} \rangle$
- Compare both methods:
  - Measure the unfolded D using different bin of the distribution  $\cos \varphi_{\ell\ell}$ : 2/4/6/8/10 Bins
    - ➔ Stat Only
    - ➔ Add Signal modelling systematics

## Results

work in progress



- The Mean method is biased by the number of bins
- The Slope method displays a small static error





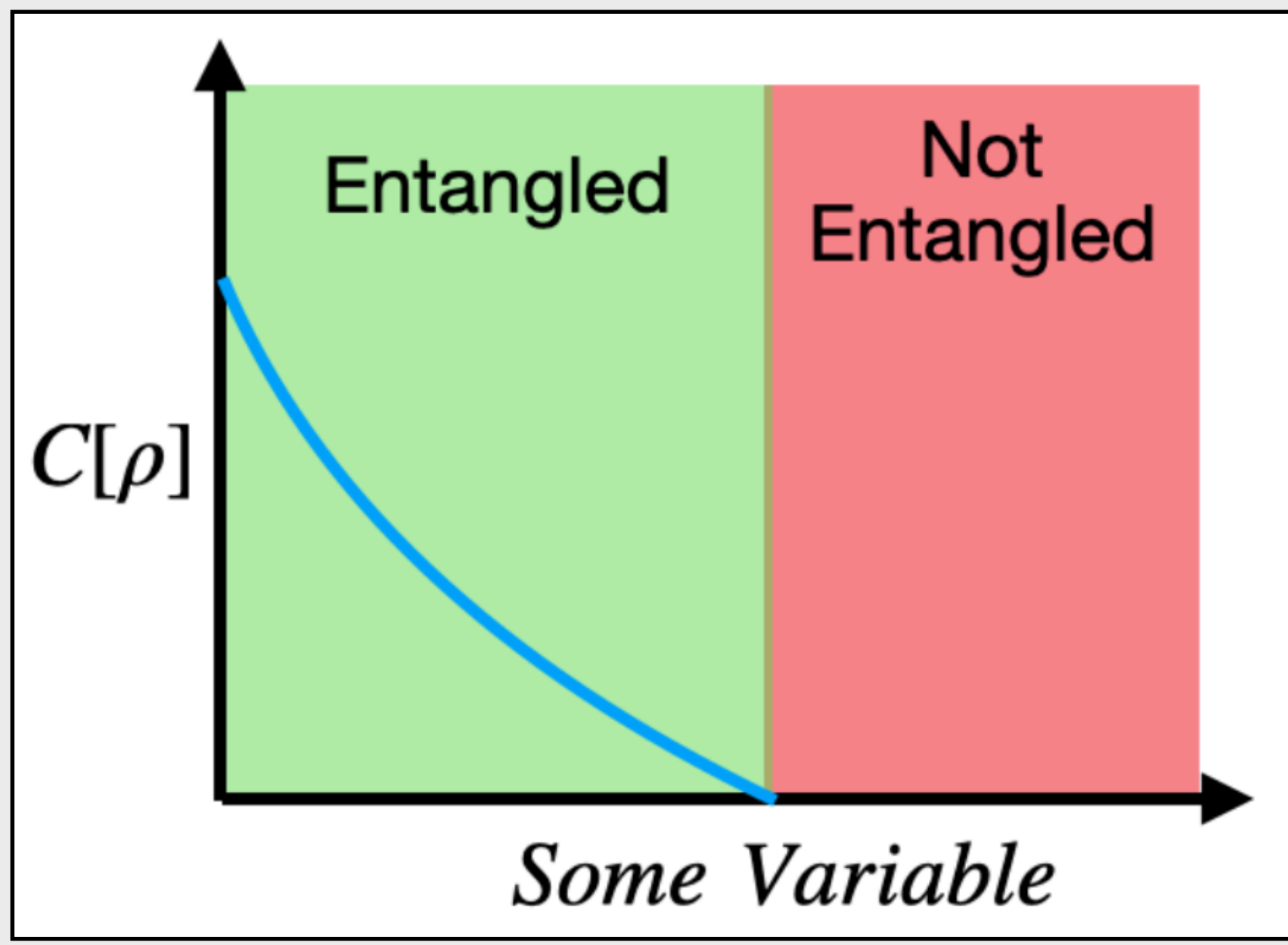
- Where to look for Quantum Entanglement ? → Entanglement Criterion - Concurrence

◎ The  $t\bar{t}$  production is described by the production spin density matrix:  

$$\rho = \frac{1}{4} \left( 1 \otimes 1 + B_i \sigma_i \otimes 1 + \bar{B}_j 1 \otimes \sigma_j + C_{ij} \sigma_i \otimes \sigma_j \right)$$
  
 ◎ By invoking the Peres-Horodecki criterion:  

$$\Delta \equiv -C_{nn} + |C_{kk} + C_{rr}| - 1 > 0$$
  
 is a sufficient condition for the presence of entanglement

Concurrence  $C[\rho] = \frac{\max(\Delta, 0)}{2}$



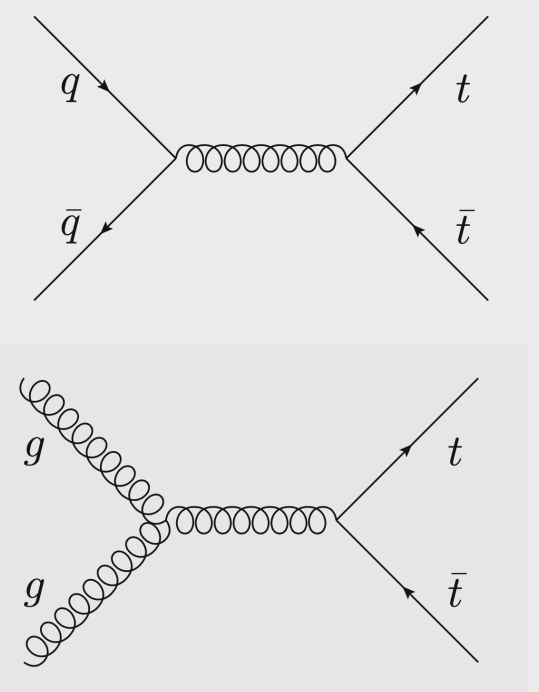
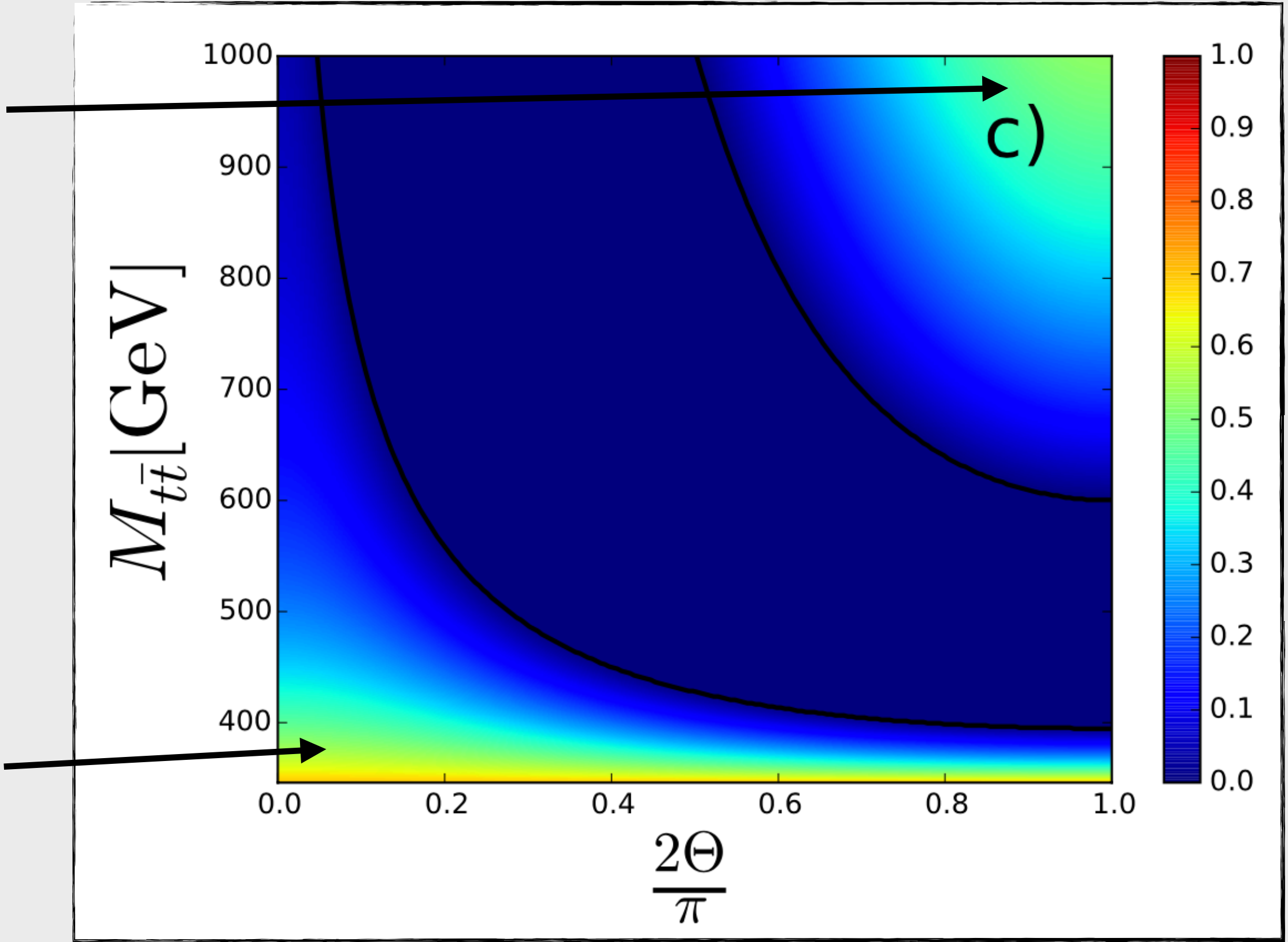
- Where to look for Quantum Entanglement ?    Entanglement Criterion - Concurrence

At high energies and production angles,  $t\bar{t}$  pair are produced in a spin-triplet pure state, not separable → **Max. Entangled**

$$|\Psi_\infty\rangle = \frac{|\uparrow\hat{n}\downarrow\hat{n}\rangle + |\downarrow\hat{n}\uparrow\hat{n}\rangle}{\sqrt{2}}$$

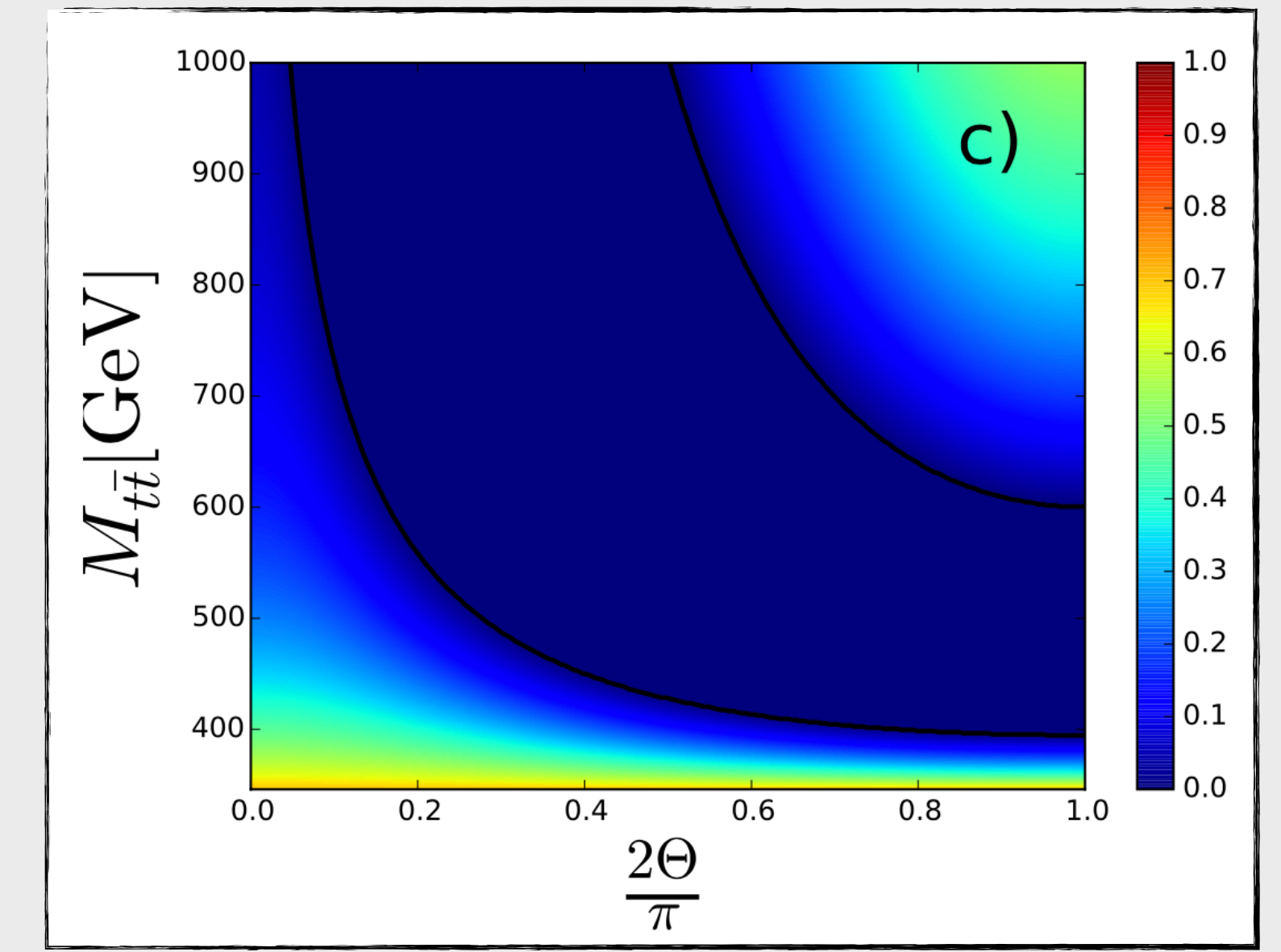
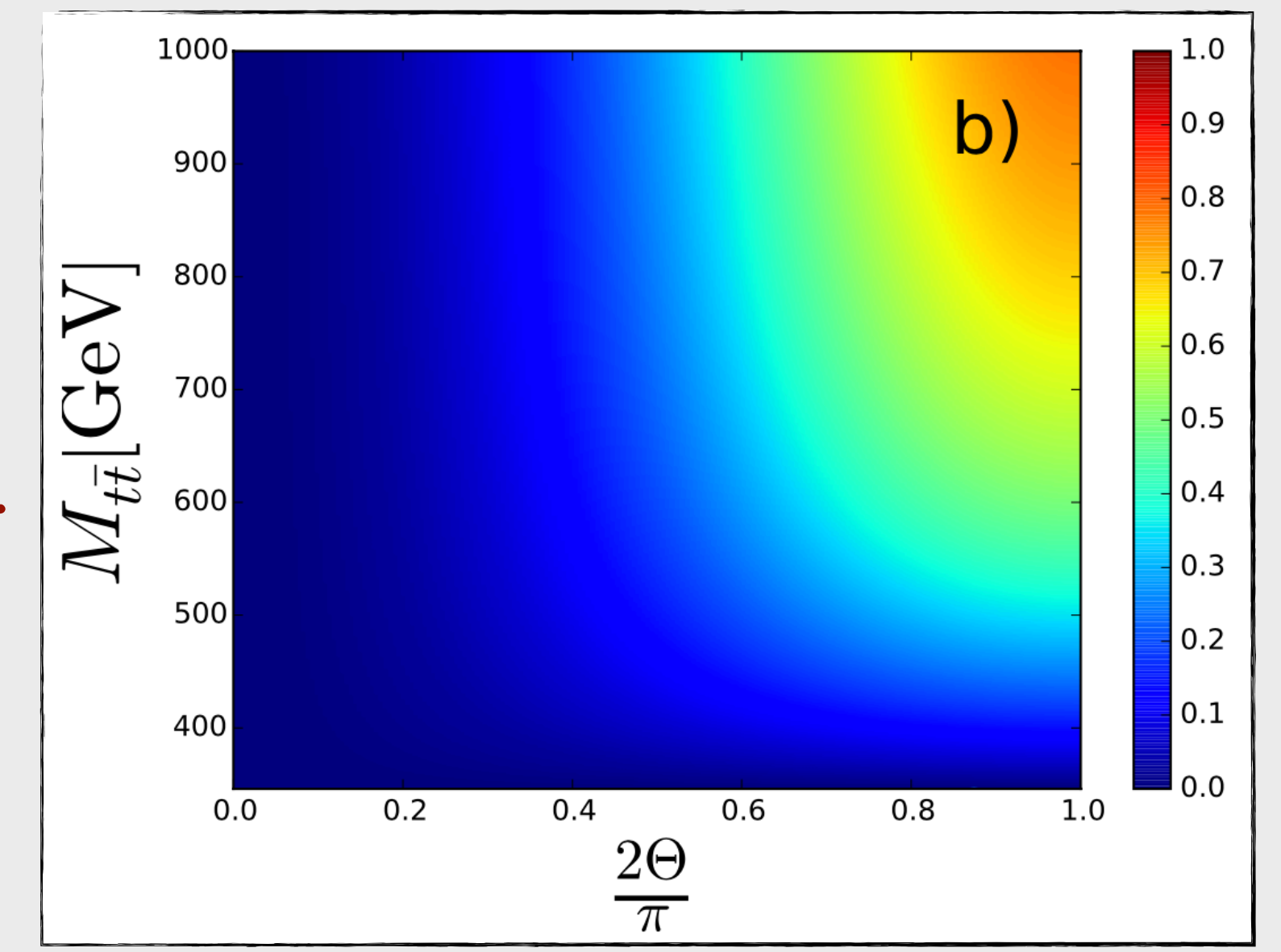
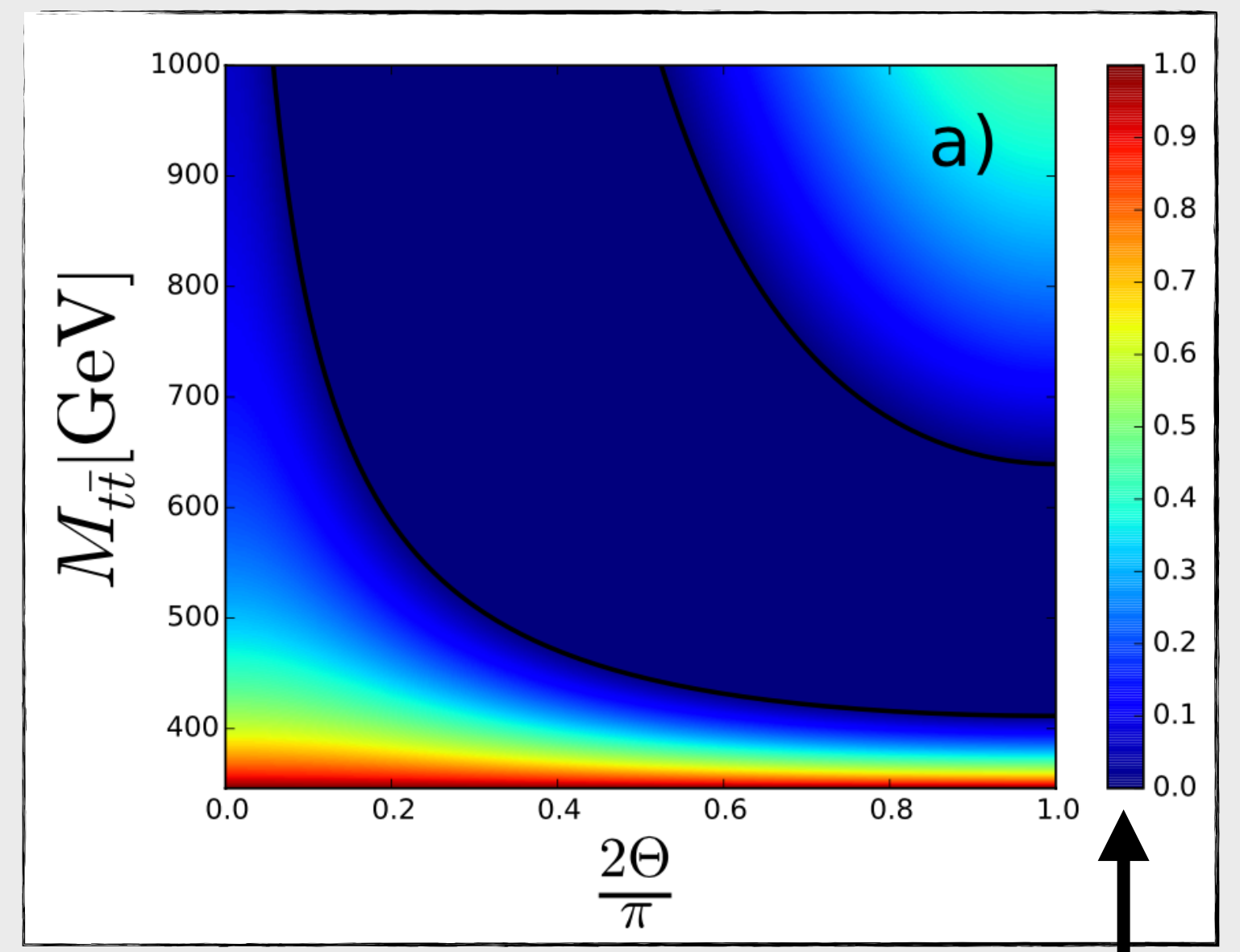
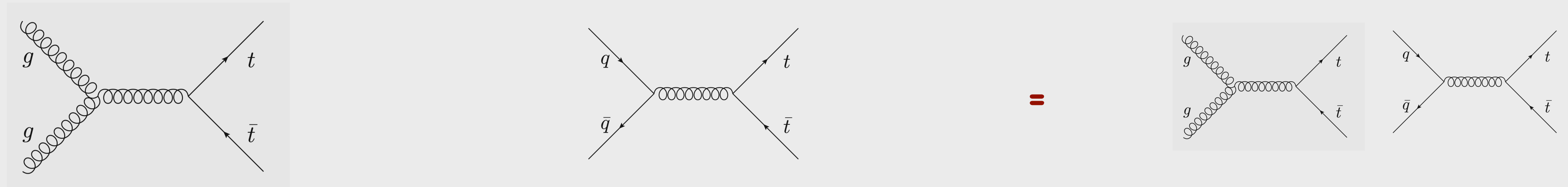
At threshold,  $t\bar{t}$  pair are produced in a spin-singlet state, not separable → **Max. Entangled**

$$|\Psi_0\rangle = \frac{|\uparrow\hat{n}\downarrow\hat{n}\rangle - |\downarrow\hat{n}\uparrow\hat{n}\rangle}{\sqrt{2}}$$





- Where to look for Quantum Entanglement ? → Entanglement Criterion - Concurrence



Concurrence  $C[\rho]$

Theoretical prediction (LO)

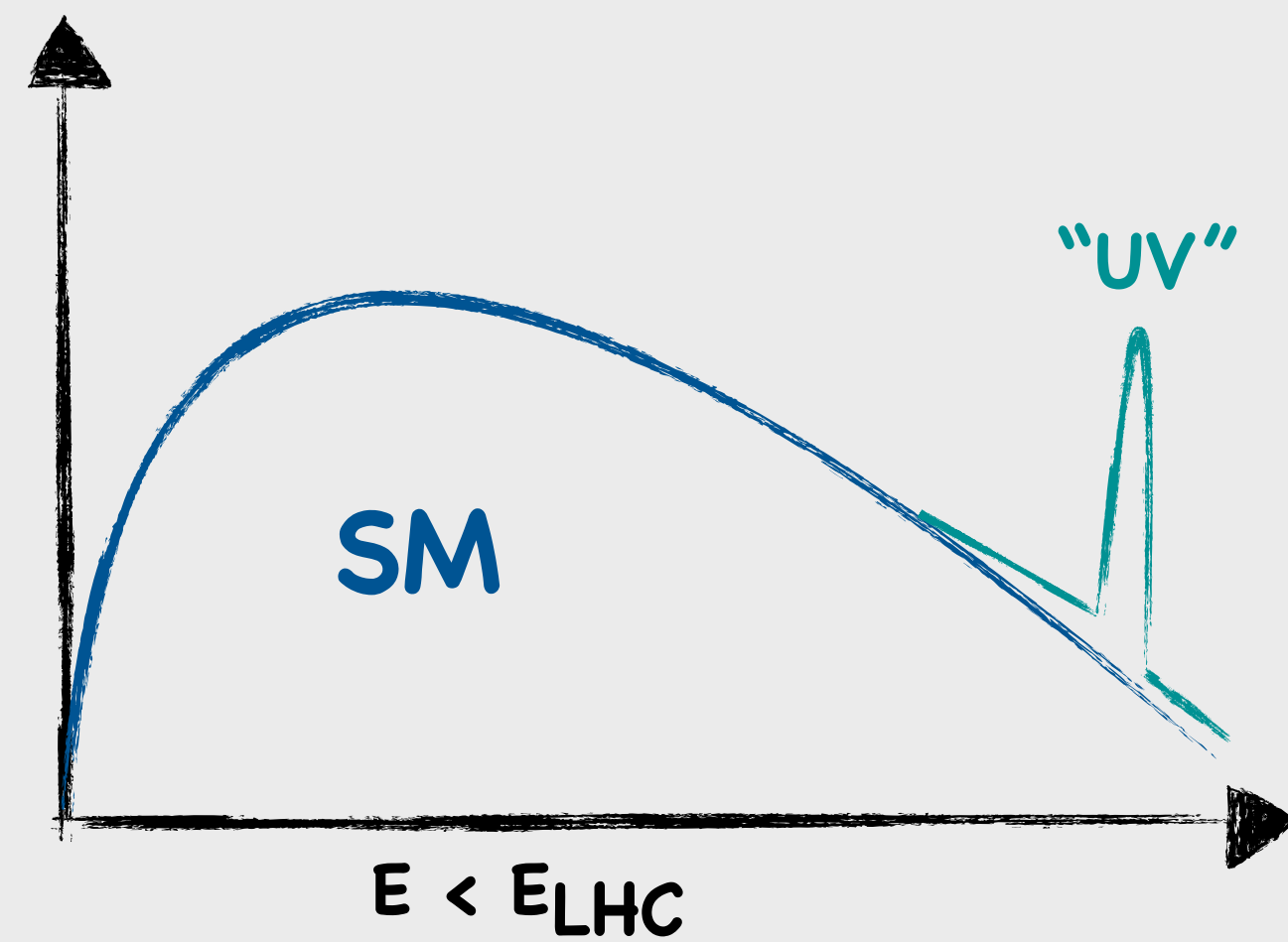
# How to look for new physics, physics beyond SM ?

Direct searches

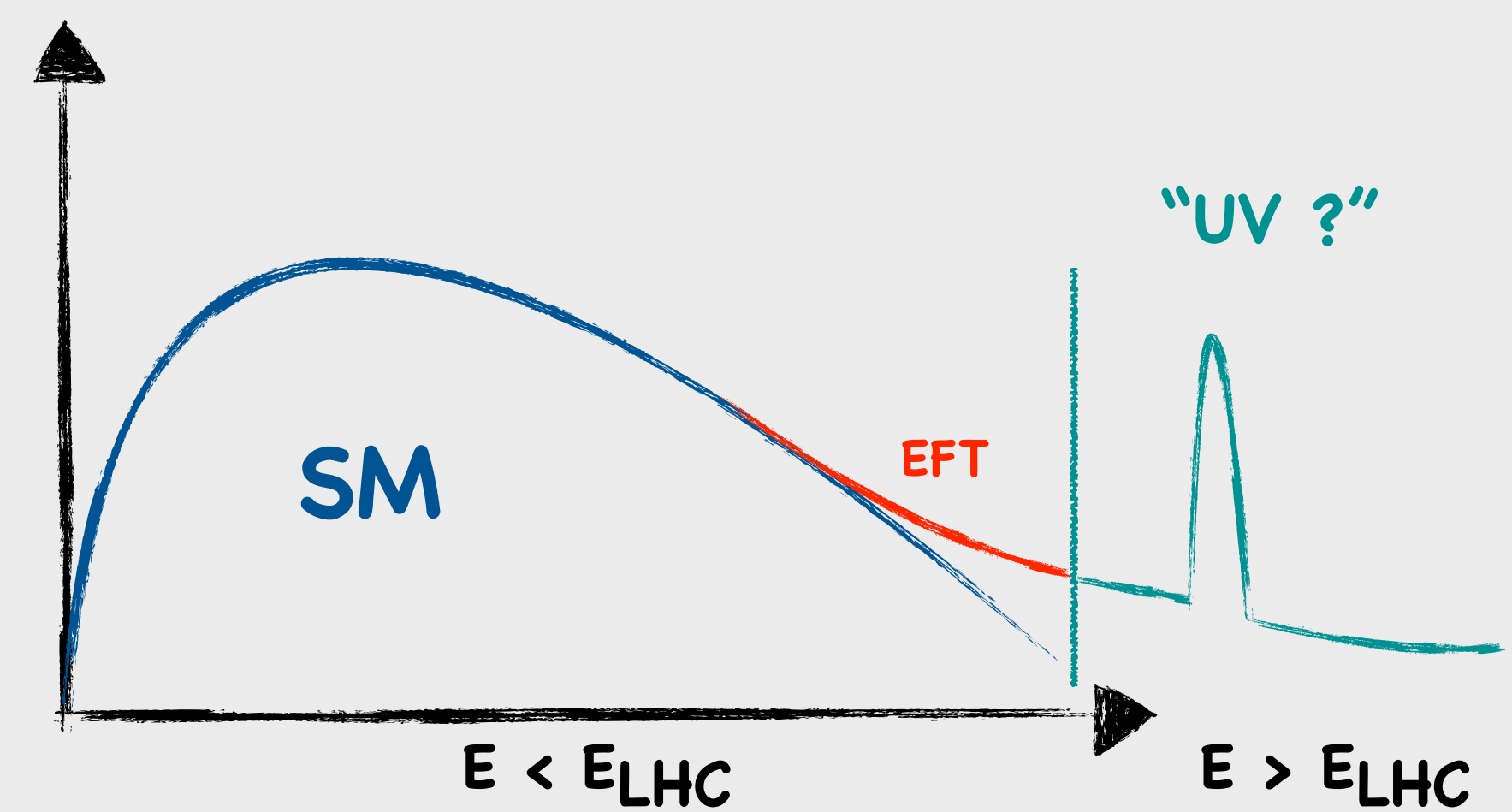
Model-Dependent, e.g. SUSY

Indirect searches

Model-Independent, e.g. Effective Field Theory (EFT)



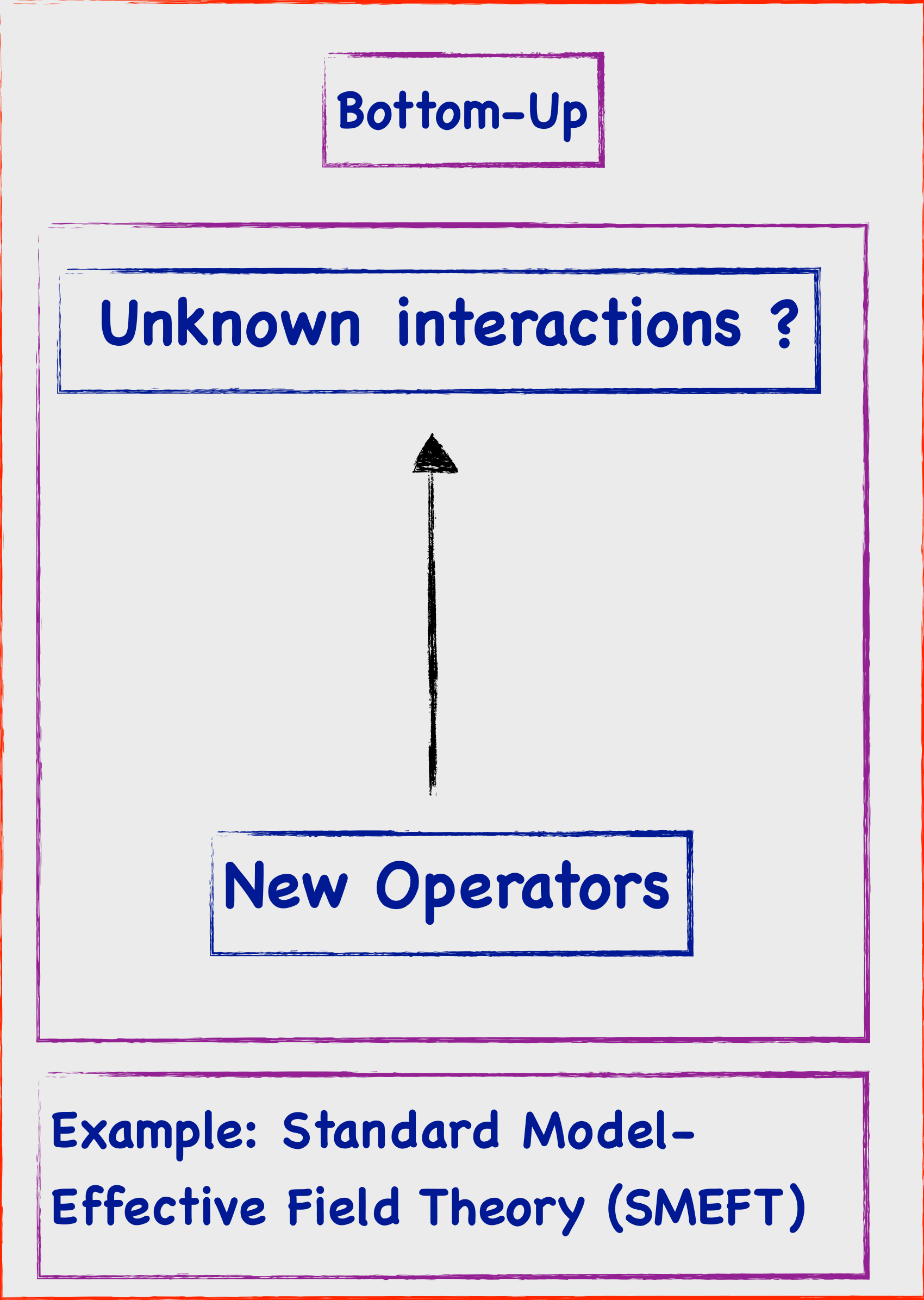
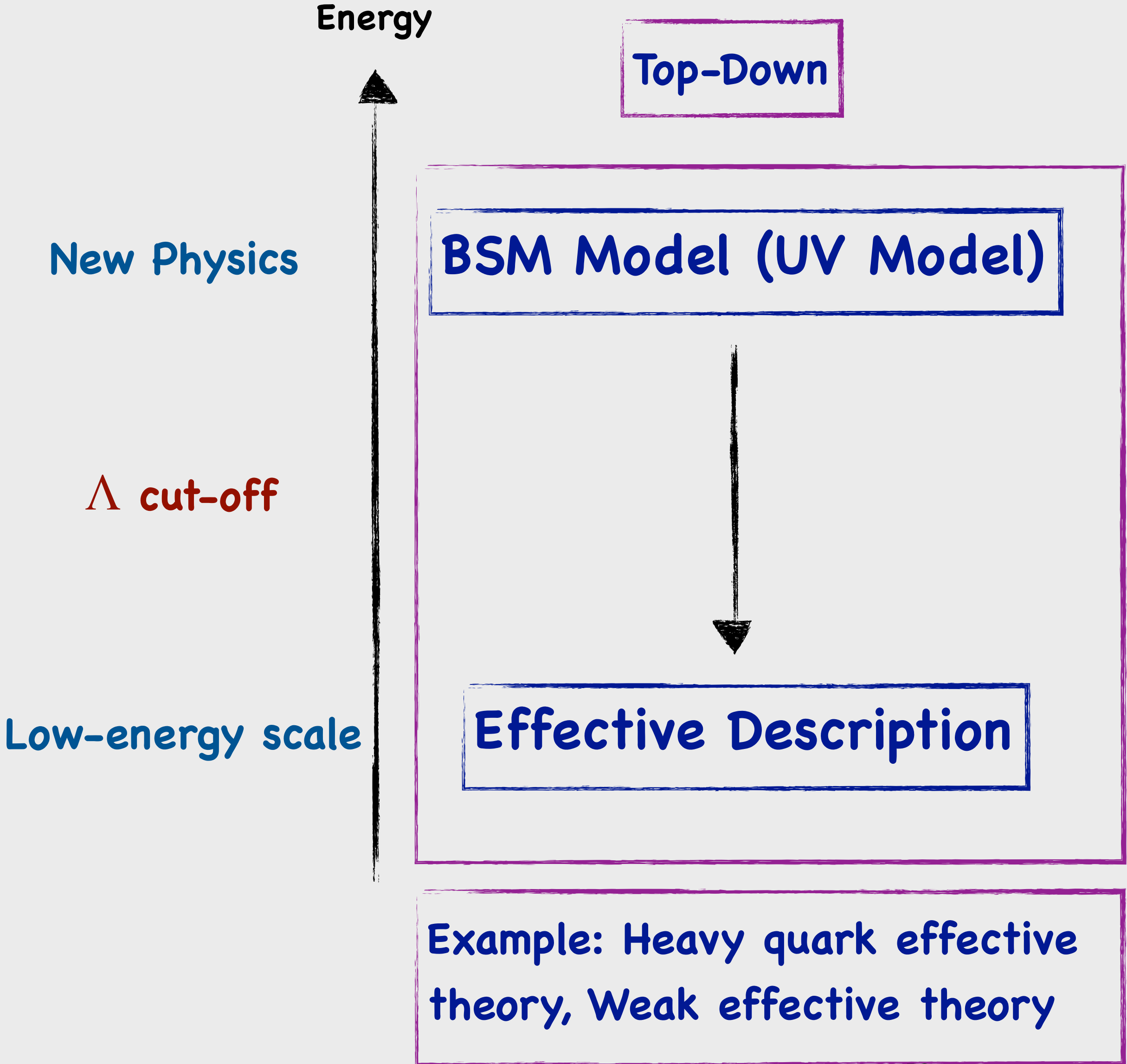
Bump hunts



Scouting tails

# EFT: What is it all about?

Focus of this talk



# SM-EFT: Dim6 operators

	$\psi$	$\Phi$	$X$	$D$
Dim	3/2	1	2	1

'Warsaw' basis

Grzadkowski–Iskrzynski–Misiak–Rosiek					
$(\bar{L}L)(\bar{L}L)$		$(\bar{R}R)(\bar{R}R)$		$(\bar{L}L)(\bar{R}R)$	
$\mathcal{O}_{ll}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{l}_s \gamma^\mu l_t)$	$\mathcal{O}_{ee}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{e}_s \gamma^\mu e_t)$	$\mathcal{O}_{le}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{e}_s \gamma^\mu e_t)$
$\mathcal{O}_{qq}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{q}_s \gamma^\mu q_t)$	$\mathcal{O}_{uu}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{u}_s \gamma^\mu u_t)$	$\mathcal{O}_{lu}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{u}_s \gamma^\mu u_t)$
$\mathcal{O}_{qq}^{(3)}$	$(\bar{q}_p \gamma_\mu \tau^I q_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	$\mathcal{O}_{dd}$	$(\bar{d}_p \gamma_\mu d_r)(\bar{d}_s \gamma^\mu d_t)$	$\mathcal{O}_{ld}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{d}_s \gamma^\mu d_t)$
$\mathcal{O}_{lq}^{(1)}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{q}_s \gamma^\mu q_t)$	$\mathcal{O}_{eu}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{u}_s \gamma^\mu u_t)$	$\mathcal{O}_{qe}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{e}_s \gamma^\mu e_t)$
$\mathcal{O}_{lq}^{(3)}$	$(\bar{l}_p \gamma_\mu \tau^I l_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	$\mathcal{O}_{ed}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{d}_s \gamma^\mu d_t)$	$\mathcal{O}_{qu}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{u}_s \gamma^\mu u_t)$
		$\mathcal{O}_{ud}^{(1)}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{d}_s \gamma^\mu d_t)$	$\mathcal{O}_{qu}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{u}_s \gamma^\mu T^A u_t)$
		$\mathcal{O}_{ud}^{(8)}$	$(\bar{u}_p \gamma_\mu T^A u_r)(\bar{d}_s \gamma^\mu T^A d_t)$	$\mathcal{O}_{qd}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{d}_s \gamma^\mu d_t)$
		$\mathcal{O}_{ud}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{d}_s \gamma^\mu T^A d_t)$	$\mathcal{O}_{qd}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{d}_s \gamma^\mu T^A d_t)$
$(\bar{L}R)(\bar{R}L)$ and $(\bar{L}R)(\bar{L}R)$		$B$ -violating			
$\mathcal{O}_{ledq}$	$(\bar{l}_p^j e_r)(\bar{d}_s^k q_t^j)$	$\mathcal{O}_{duq}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(d_p^\alpha)^T C u_r^\beta] [(q_s^{\gamma j})^T C l_t^k]$		
$\mathcal{O}_{quqd}^{(1)}$	$(\bar{q}_p^j u_r) \varepsilon_{jk} (\bar{q}_s^k d_t)$	$\mathcal{O}_{qqu}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(u_s^\gamma)^T C e_t]$		
$\mathcal{O}_{quqd}^{(8)}$	$(\bar{q}_p^j T^A u_r) \varepsilon_{jk} (\bar{q}_s^k T^A d_t)$	$\mathcal{O}_{qqq}^{(1)}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} \varepsilon_{mn} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(q_s^{\gamma m})^T C l_t^n]$		
$\mathcal{O}_{lequ}^{(1)}$	$(\bar{l}_p^j e_r) \varepsilon_{jk} (\bar{q}_s^k u_t)$	$\mathcal{O}_{qqq}^{(3)}$	$\varepsilon^{\alpha\beta\gamma} (\tau^I \varepsilon)_{jk} (\tau^I \varepsilon)_{mn} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(q_s^{\gamma m})^T C l_t^n]$		
$\mathcal{O}_{lequ}^{(3)}$	$(\bar{l}_p^j \sigma_{\mu\nu} e_r) \varepsilon_{jk} (\bar{q}_s^k \sigma^{\mu\nu} u_t)$	$\mathcal{O}_{duu}$	$\varepsilon^{\alpha\beta\gamma} [(d_p^\alpha)^T C u_r^\beta] [(u_s^\gamma)^T C e_t]$		

$q = q_L, l = l_L, u = u_R, d = d_R, e = e_R$ ,  $p, r, s, t =$  generation indices

Grzadkowski–Iskrzynski–Misiak–Rosiek					
$X^3$		$\Phi^6$ and $\Phi^4 D^2$		$\psi^2 \Phi^3$	
$\mathcal{O}_G$	$f^{ABC} G_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$\mathcal{O}_\Phi$	$(\Phi^\dagger \Phi)^3$	$\mathcal{O}_{e\Phi}$	$(\Phi^\dagger \Phi)(\bar{l}_p e_r \Phi)$
$\mathcal{O}_{\tilde{G}}$	$f^{ABC} \tilde{G}_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$\mathcal{O}_{\Phi\Box}$	$(\Phi^\dagger \Phi) \Box (\Phi^\dagger \Phi)$	$\mathcal{O}_{u\Phi}$	$(\Phi^\dagger \Phi)(\bar{q}_p u_r \tilde{\Phi})$
$\mathcal{O}_W$	$\varepsilon^{IJK} W_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$	$\mathcal{O}_{\Phi D}$	$(\Phi^\dagger D^\mu \Phi)^* (\Phi^\dagger D_\mu \Phi)$	$\mathcal{O}_{d\Phi}$	$(\Phi^\dagger \Phi)(\bar{q}_p d_r \Phi)$
$\mathcal{O}_{\tilde{W}}$	$\varepsilon^{IJK} \tilde{W}_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$				
$X^2 \Phi^2$		$\psi^2 X \Phi$		$\psi^2 \Phi^2 D$	
$\mathcal{O}_{\Phi G}$	$\Phi^\dagger \Phi G_{\mu\nu}^A G^{A\mu\nu}$	$\mathcal{O}_{eW}$	$(\bar{l}_p \sigma^{\mu\nu} e_r) \tau^I \Phi W_{\mu\nu}^I$	$\mathcal{O}_{\Phi l}^{(1)}$	$(\Phi^\dagger i \overleftrightarrow{D}_\mu \Phi)(\bar{l}_p \gamma^\mu l_r)$
$\mathcal{O}_{\Phi \tilde{G}}$	$\Phi^\dagger \Phi \tilde{G}_{\mu\nu}^A G^{A\mu\nu}$	$\mathcal{O}_{eB}$	$(\bar{l}_p \sigma^{\mu\nu} e_r) \Phi B_{\mu\nu}$	$\mathcal{O}_{\Phi l}^{(3)}$	$(\Phi^\dagger i \overleftrightarrow{D}_\mu^I \Phi)(\bar{l}_p \tau^I \gamma^\mu l_r)$
$\mathcal{O}_{\Phi W}$	$\Phi^\dagger \Phi W_{\mu\nu}^I W^{I\mu\nu}$	$\mathcal{O}_{uG}$	$(\bar{q}_p \sigma^{\mu\nu} T^A u_r) \tilde{\Phi} G_{\mu\nu}^A$	$\mathcal{O}_{\Phi e}$	$(\Phi^\dagger i \overleftrightarrow{D}_\mu \Phi)(\bar{e}_p \gamma^\mu e_r)$
$\mathcal{O}_{\Phi \tilde{W}}$	$\Phi^\dagger \Phi \tilde{W}_{\mu\nu}^I W^{I\mu\nu}$	$\mathcal{O}_{uW}$	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tau^I \tilde{\Phi} W_{\mu\nu}^I$	$\mathcal{O}_{\Phi q}^{(1)}$	$(\Phi^\dagger i \overleftrightarrow{D}_\mu \Phi)(\bar{q}_p \gamma^\mu q_r)$
$\mathcal{O}_{\Phi B}$	$\Phi^\dagger \Phi B_{\mu\nu} B^{\mu\nu}$	$\mathcal{O}_{uB}$	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tilde{\Phi} B_{\mu\nu}$	$\mathcal{O}_{\Phi q}^{(3)}$	$(\Phi^\dagger i \overleftrightarrow{D}_\mu^I \Phi)(\bar{q}_p \tau^I \gamma^\mu q_r)$
$\mathcal{O}_{\Phi \tilde{B}}$	$\Phi^\dagger \Phi \tilde{B}_{\mu\nu} B^{\mu\nu}$	$\mathcal{O}_{dG}$	$(\bar{q}_p \sigma^{\mu\nu} T^A d_r) \Phi G_{\mu\nu}^A$	$\mathcal{O}_{\Phi u}$	$(\Phi^\dagger i \overleftrightarrow{D}_\mu \Phi)(\bar{u}_p \gamma^\mu u_r)$
$\mathcal{O}_{\Phi WB}$	$\Phi^\dagger \tau^I \Phi W_{\mu\nu}^I B^{\mu\nu}$	$\mathcal{O}_{dW}$	$(\bar{q}_p \sigma^{\mu\nu} d_r) \tau^I \Phi W_{\mu\nu}^I$	$\mathcal{O}_{\Phi d}$	$(\Phi^\dagger i \overleftrightarrow{D}_\mu \Phi)(\bar{d}_p \gamma^\mu d_r)$
$\mathcal{O}_{\Phi \tilde{W}B}$	$\Phi^\dagger \tau^I \Phi \tilde{W}_{\mu\nu}^I B^{\mu\nu}$	$\mathcal{O}_{dB}$	$(\bar{q}_p \sigma^{\mu\nu} d_r) \Phi B_{\mu\nu}$	$\mathcal{O}_{\Phi ud}$	$i(\tilde{\Phi}^\dagger D_\mu \Phi)(\bar{u}_p \gamma^\mu d_r)$

$q = q_L, l = l_L, u = u_R, d = d_R, e = e_R$ ,  $\overleftrightarrow{D}_\mu^I \equiv \tau^I \overrightarrow{D}_\mu - \overleftarrow{D}_\mu \tau^I$ ,  $p, r =$  generation indices

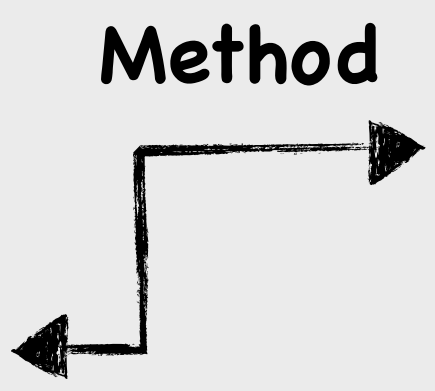
Field strength tensors,  $X_{\mu\nu} \in \{G_{\mu\nu}^A, W_{\mu\nu}^I, B_{\mu\nu}\}$



Goal

In what way does the EFT affect the spin correlation at LO and NLO?

- Cross validate the SMEFT@NLO implementation against Dim6Top model

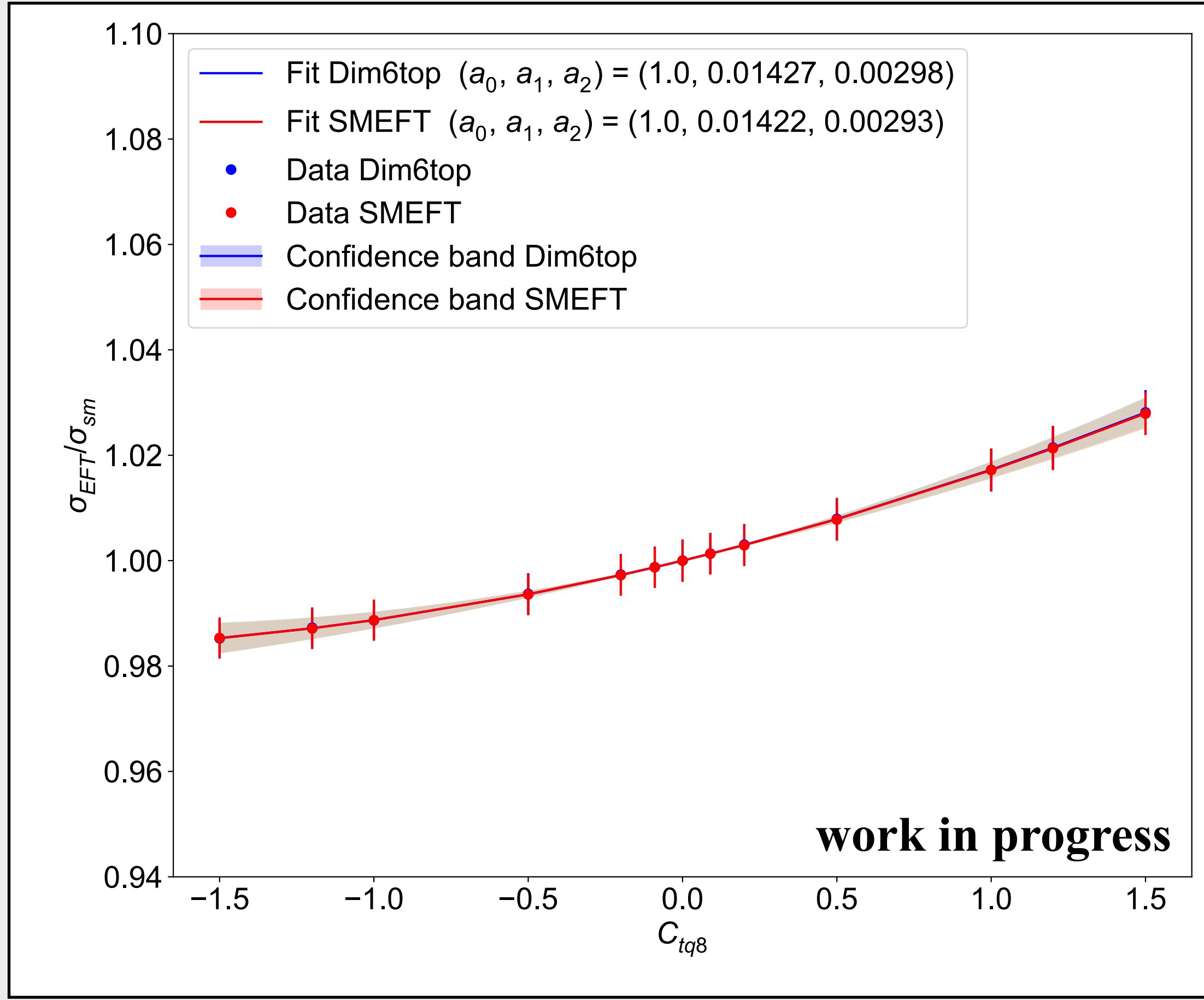


Comments

-  $\alpha_{ctq8}$  and  $\beta_{ctq8}$  are model dependent

- SMEFT@NLO model and Dim6top model show appx. same value of  $\alpha_{ctq8}$  and  $\beta_{ctq8}$  [within the statistical uncertainties.]

$$\sigma^k = \sigma_{SM}^k + \frac{C_{tq8}}{\Lambda^2} \alpha + \frac{C_{tq8}^2}{\Lambda^4} \beta$$



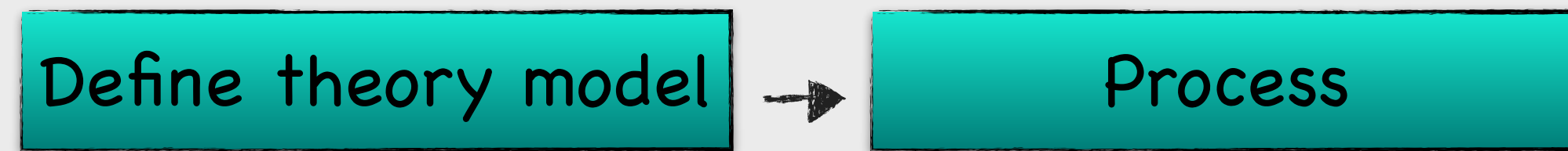
# Analysis strategy

Define theory model

- ☑ Standard Model (SM)
- ☑ EFT model to predict new physics (SMEFT@NLO, Dim6Top)

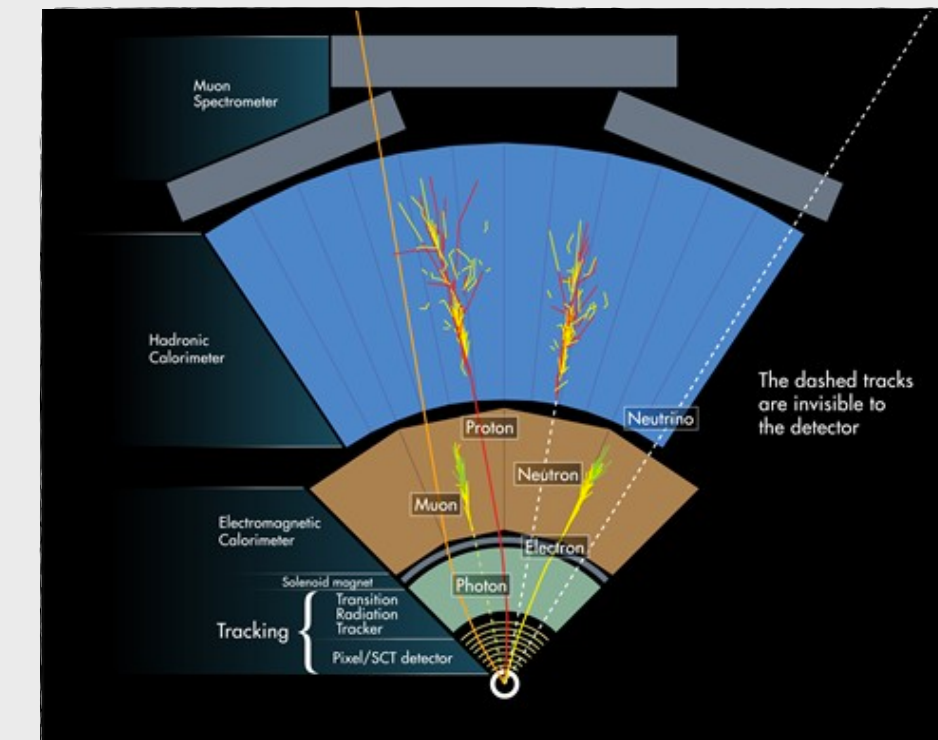
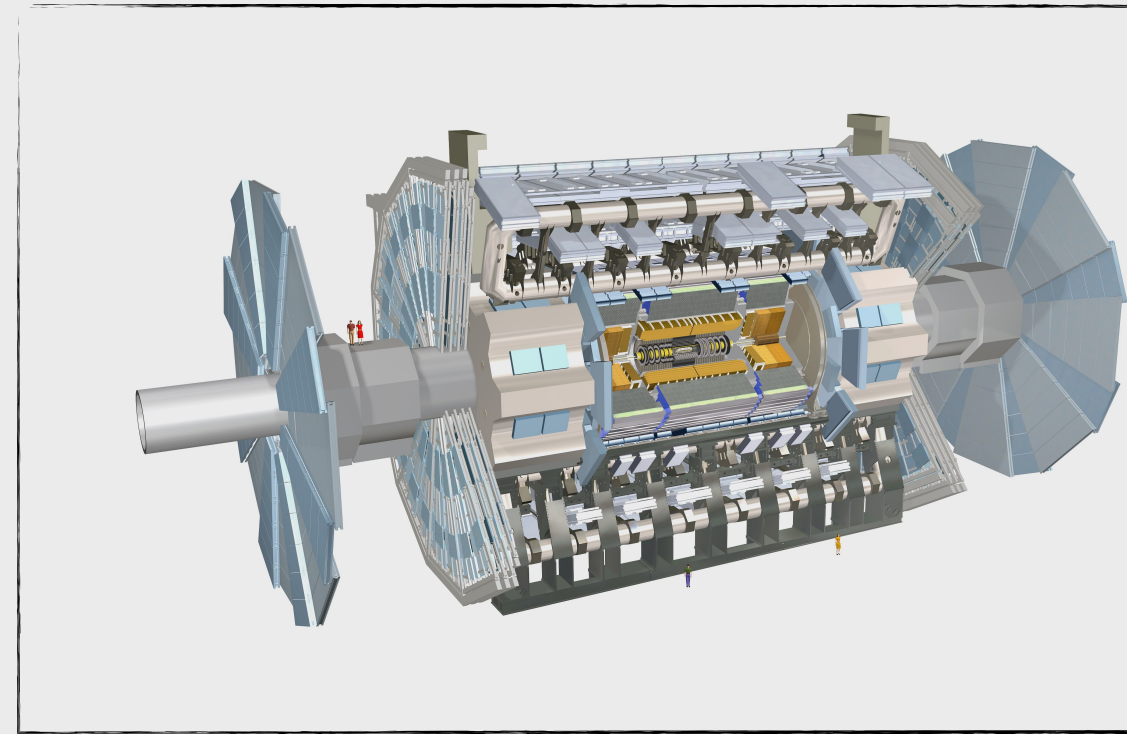


# Analysis strategy

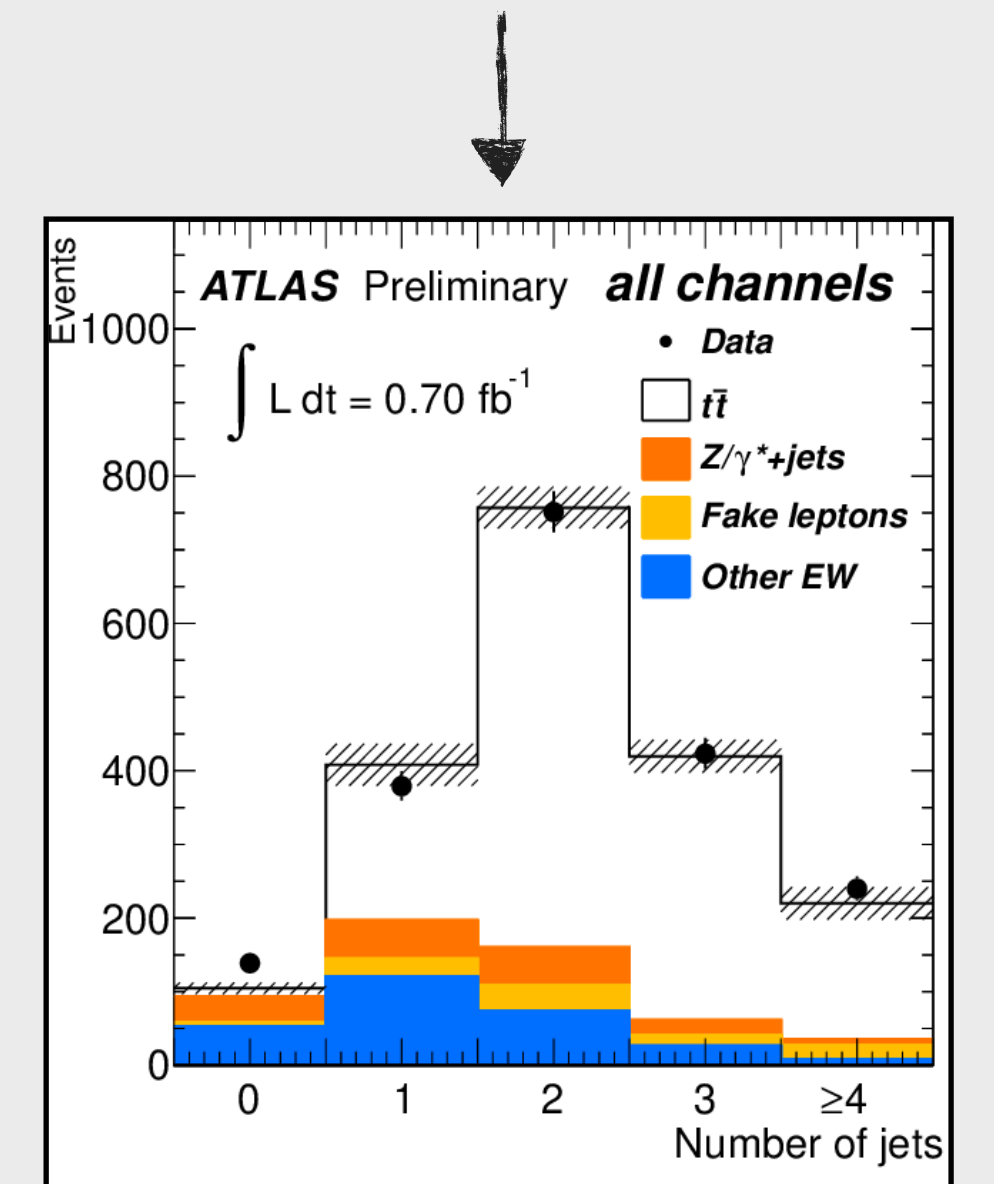
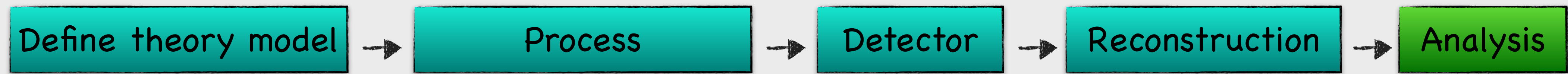


- Generate proton-proton collision
- Define the degree of precision of the simulation: **LO / NLO** ...

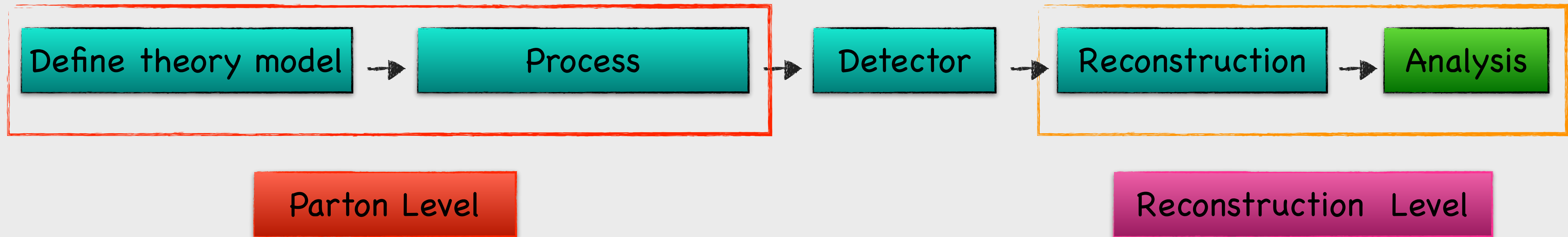
# Analysis strategy



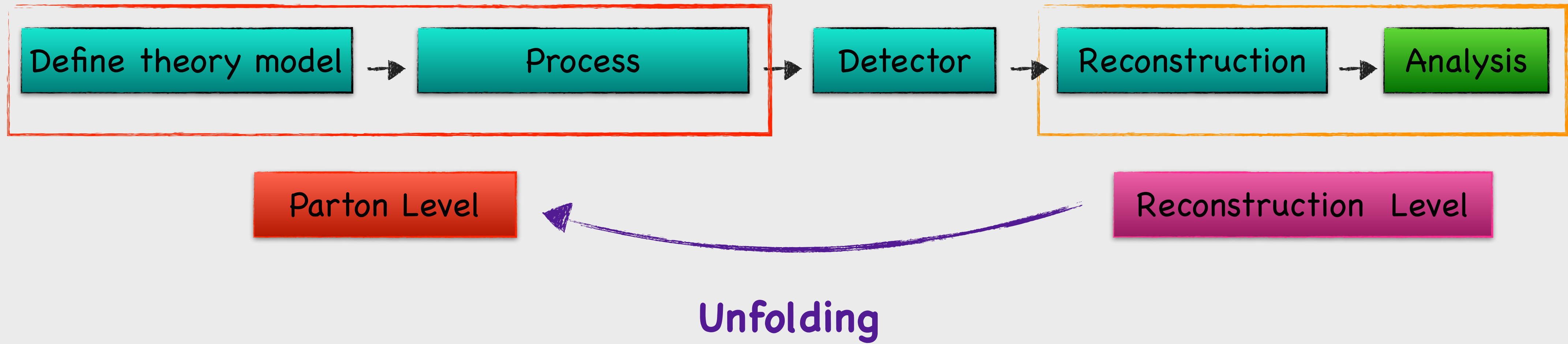
# Analysis strategy



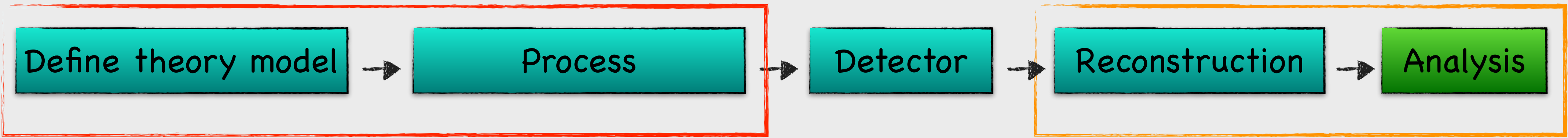
# Analysis strategy



# Analysis strategy



# Analysis strategy



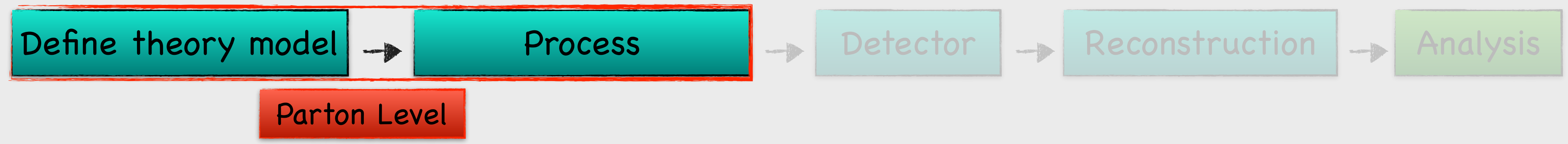
Parton Level

Reconstruction Level

Unfolding

- $t\bar{t}$  Spin Correlations in the di-leptons channel
- EFT Interpretation

- Quantum Entanglement at LHC
- Bell inequalities at LHC



### Motivation

- Perform Global Fit using Spin correlation observables at LO or NLO to constrain Wilson Coefficient ?

### Method

- ◎ Generate simulation samples:
  - ✦ Define EFT model : SMEFT@NLO model (LO / NLO)
    - ✦ SM
    - ✦ SMEFT@NLO model ==> LO and NLO



Motivation

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- ↓
- ✦ What Wilson coefficients should be considered ?
    - ✦  $C_{tg}$
    - ✦ 4-quark operators:  $ctq_8$





## Method

### Motivation

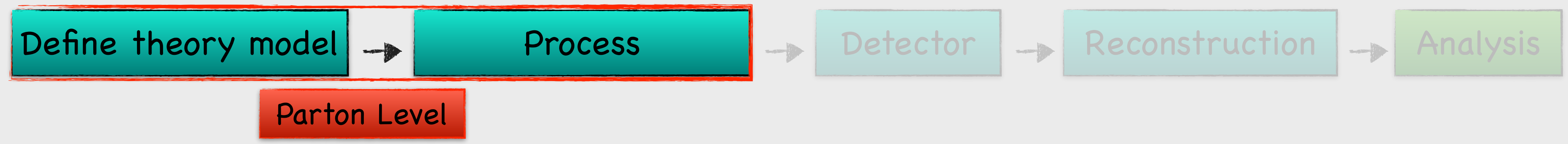
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  - ✦ SMEFT@NLO model ==> LO and NLO

- ✦ Decay tops (using MadSpin)
  - ✦ Possible at LO and impossible at NLO

- ✦ What Wilson coefficients should be considered ?
  - ✦  $C_{tg}$
  - ✦ 4-quark operators:  $ctq_8$



Motivation

- Perform Global Fit using Spin correlation observables at LO or NLO to constrain Wilson Coefficient ?

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Generate simulation samples:

- Define EFT model : SMEFT@NLO model (LO / NLO)
  - SM
  - SMEFT@NLO model ==> LO and NLO

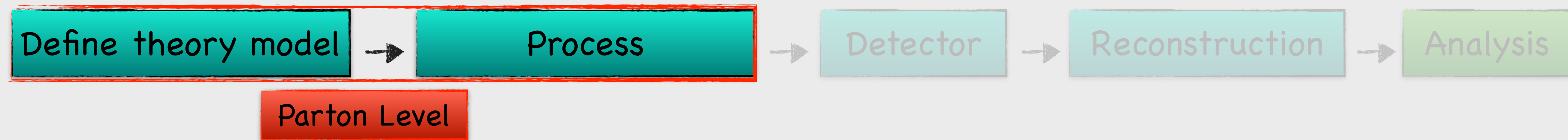
What Wilson coefficients should be considered ?

- Ctg
- 4-quark operators: ctq8

Decay tops (using MadSpin)

- Possible at LO and impossible at NLO

What effect does this have on the EFT contribution to spin correlation at LO and NLO?



**Goal**

- How does spin correlation change in SM at LO and NLO?
- In what way does the EFT affect the spin correlation at LO and NLO?

Mean Method:  $C(\hat{k}, \hat{k}) = -9 \langle \cos \theta_+^{\hat{k}} \cos \theta_-^{\hat{k}} \rangle$

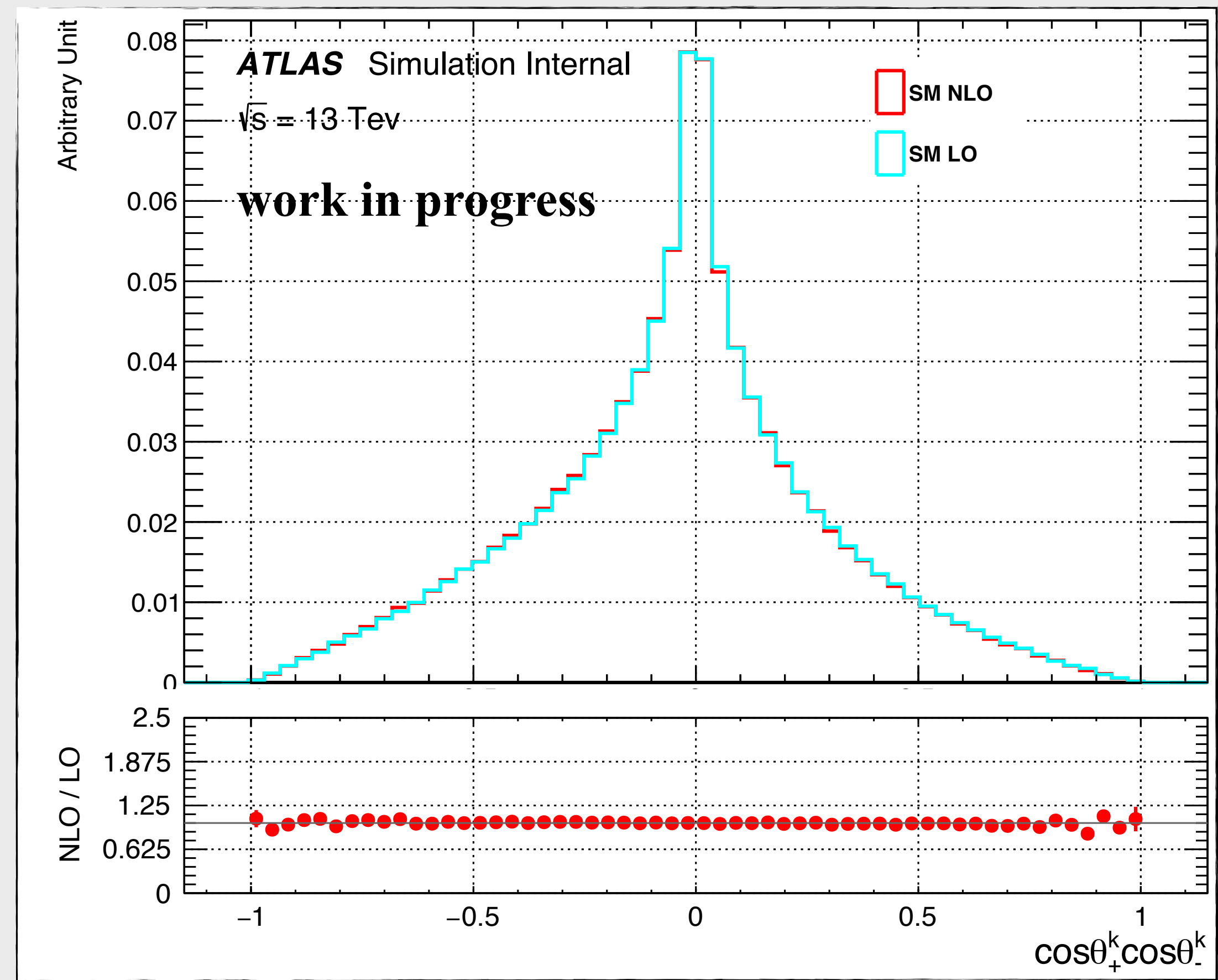
SM LO :  $C(k, k) = 0.341 \pm 0.004$  (stat)

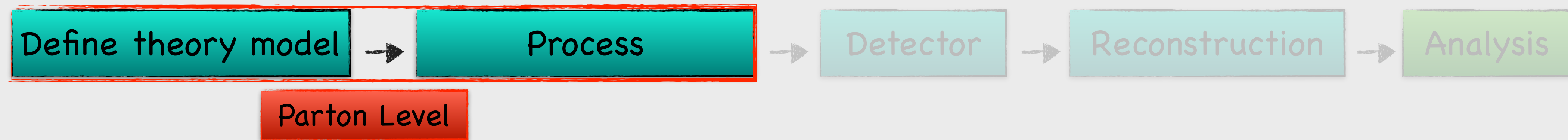
SM NLO :  $C(k, k) = 0.366 \pm 0.004$  (stat)

© Consistent with SM expectations (NLO from [1508.05271](#))

© Using SM at NLO: Gain 2%

**Results**





**Goal**

- How does spin correlation change in SM at LO and NLO?
- In what way does the EFT affect the spin correlation at LO and NLO?

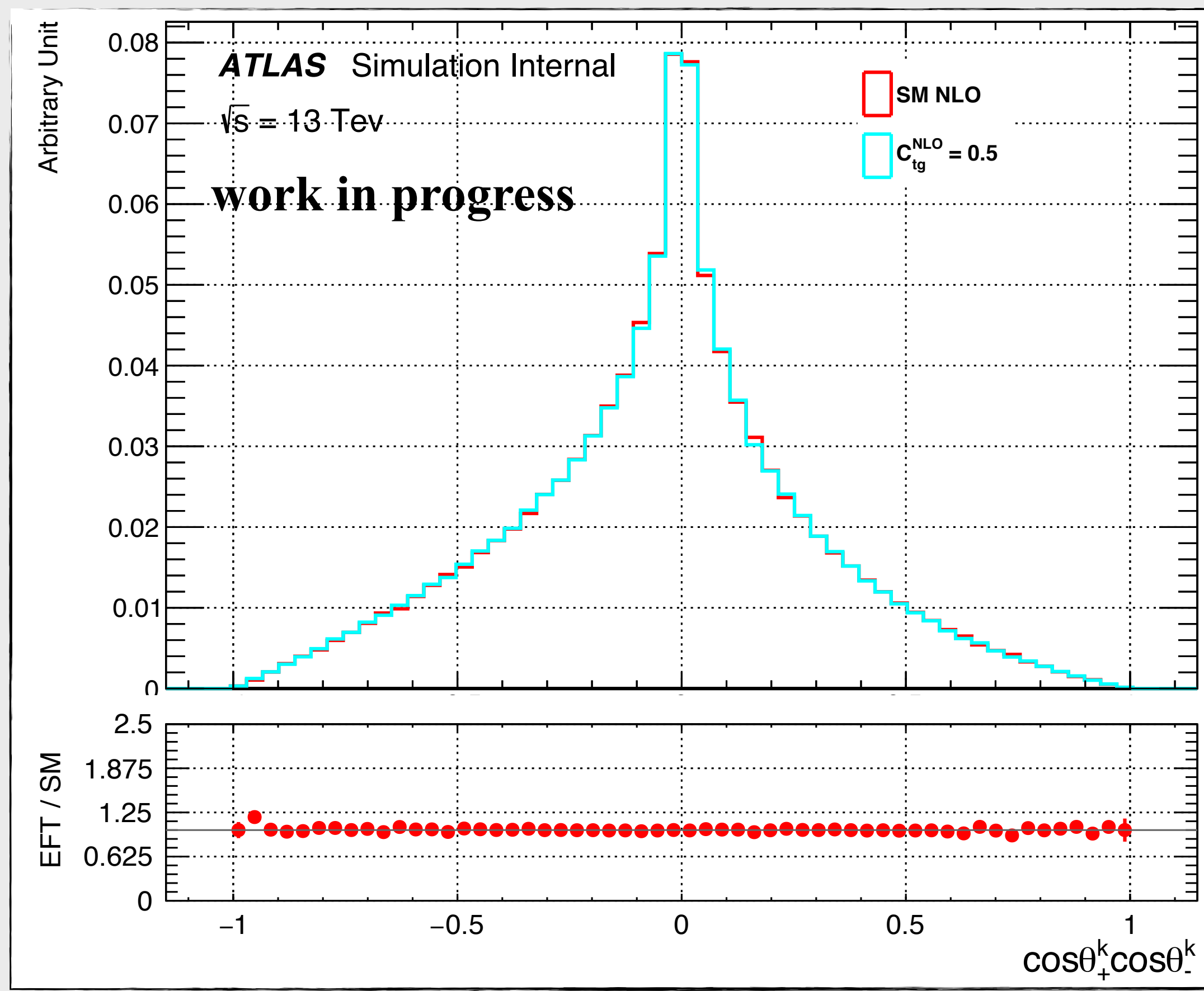
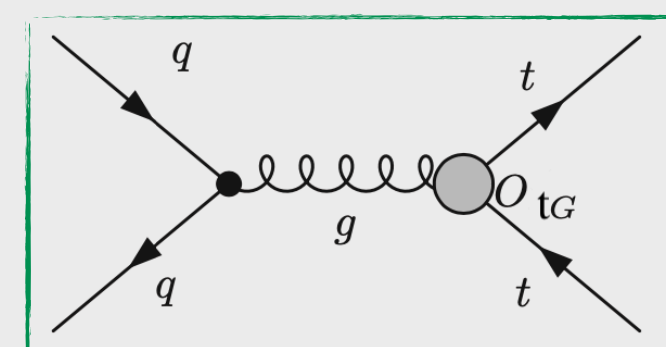
Mean Method:  $C(\hat{k}, \hat{k}) = -9 \langle \cos \theta_+^{\hat{k}} \cos \theta_-^{\hat{k}} \rangle$

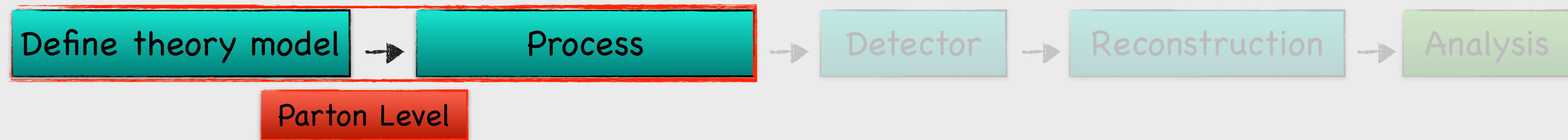
SM NLO :  $C(k, k) = 0.366313 \pm 0.0042 \text{ (stat)}$

Ctg NLO :  $C(k, k) = 0.375982 \pm 0.0042 \text{ (stat)}$

©  $c_{tg}=0.5$  affect the SM value by 10%.

**Results**



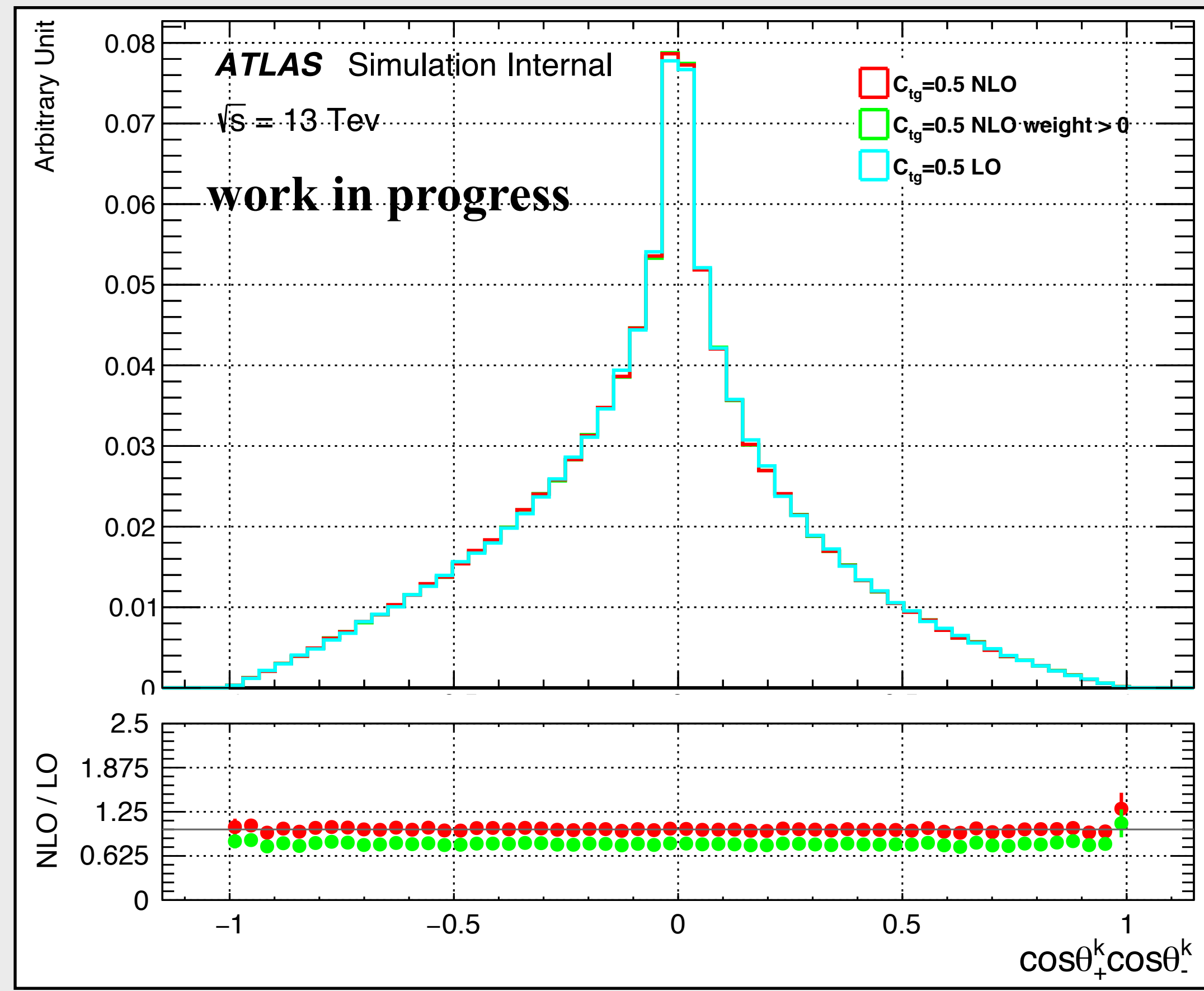
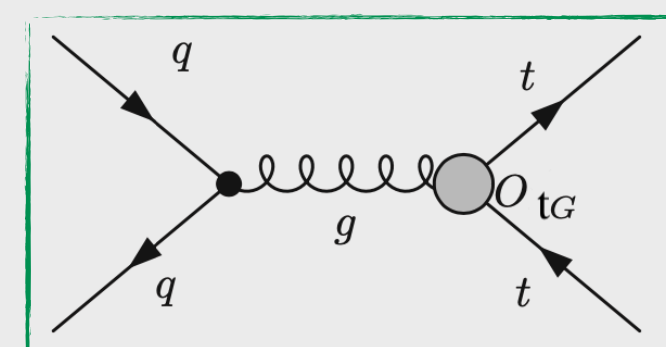


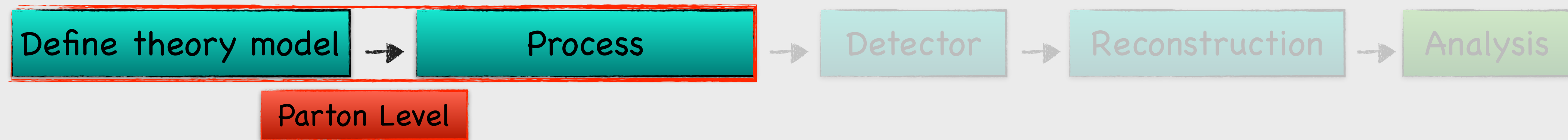
**Goal**

- How does spin correlation change in SM at LO and NLO?
- In what way does the EFT affect the spin correlation at LO and NLO?

- The impact of  $C_{tg}$  at NLO/LO is low
- Preform Global Fit at NLO using spin correlation observables.

**Results**





Parton Level

Goal

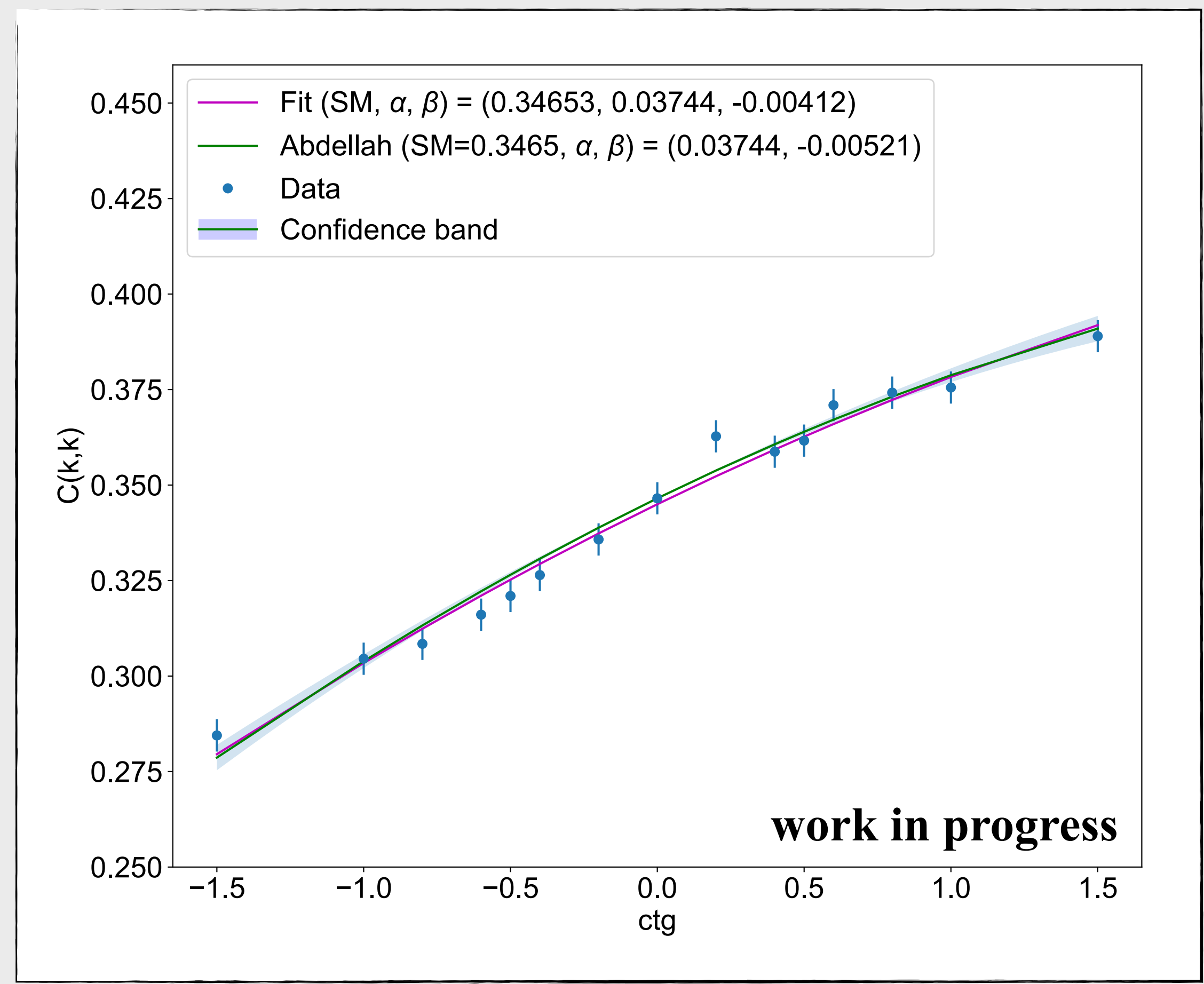
In what way does the EFT affect the spin correlation at LO and NLO?

- Compute  $\alpha$  and  $\beta$  ?

$$C(k, k) = C(k, k)_{SM} + \frac{C_{tg}}{\Lambda^2} \alpha + \frac{C_{tg}^2}{\Lambda^4} \beta$$

Comments

● We can use the measured  $c(k, k)$ , the estimated  $c(k, k)_{SM}$  with their statistical and systematic uncertainties, and the  $\alpha$  and  $\beta$ , to derive global constraints on the  $c_{tg8}$  operator coefficients.



work in progress

# Summary

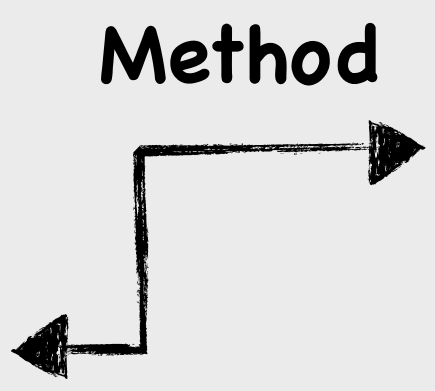
- ◎ Precision top quark spin measurements are a powerful probe of new physics and complementary to other approaches.
- ◎ Study the impact of EFT at LO and NLO on spin correlation observables
  - ♣ Preform Global Fit at NLO



Goal

In what way does the EFT affect the spin correlation at LO and NLO?

- Cross validate the SMEFT@NLO implementation against Dim6Top model

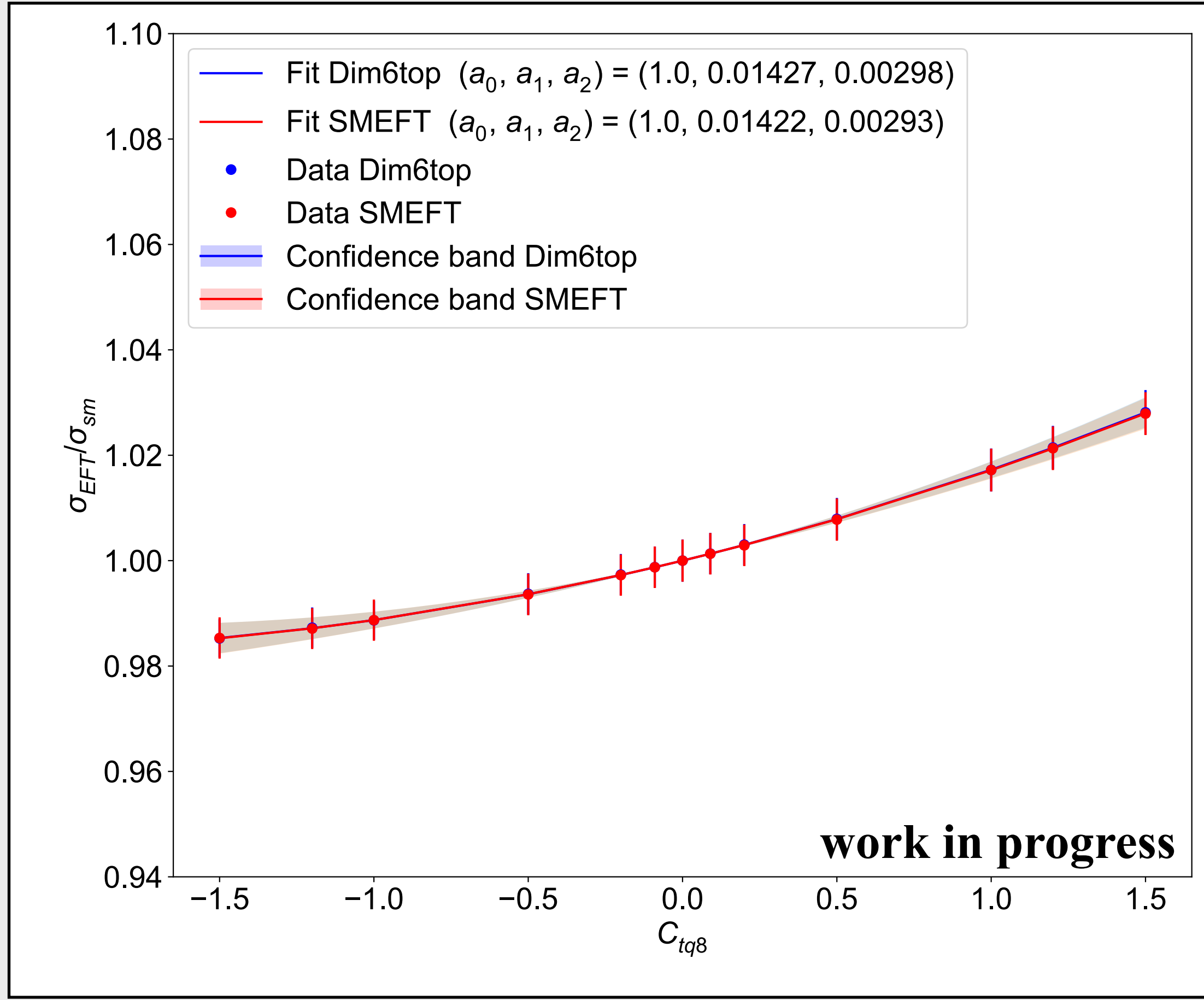


$$\sigma^k = \sigma_{SM}^k + \frac{C_{tq8}}{\Lambda^2} \alpha + \frac{C_{tq8}^2}{\Lambda^4} \beta$$

Comments

-  $\alpha_{ctq8}$  and  $\beta_{ctq8}$  are model dependent

- SMEFT@NLO model and Dim6top model show appx. same value of  $\alpha_{ctq8}$  and  $\beta_{ctq8}$  [within the statistical uncertainties.]





# Which Wilson coefficients affects $t\bar{t}$ production the most ?

☑ 18 operator expect to affect  $t\bar{t}$  process :

📌 4-quark (2-heavy, 2-light) operator

📌 Heavy quark boson

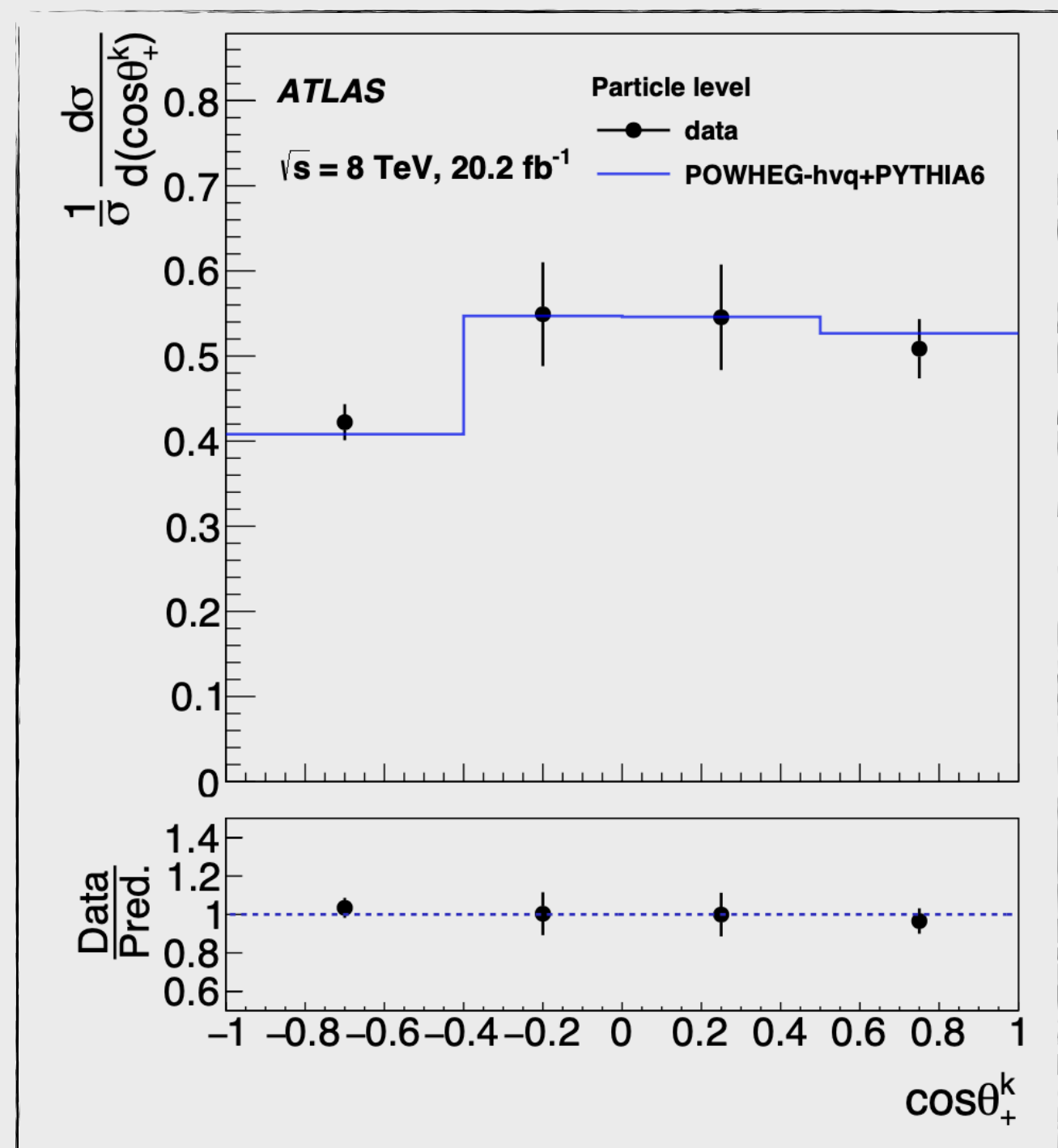
☑ We Can not prob gluon self-coupling  $c_G$  in dim6top or SMEFT@NLO

parameter	$t\bar{t}$	single $t$
$C_{Qq}^{1,8}$	$\Lambda^{-2}$	–
$C_{Qq}^{3,8}$	$\Lambda^{-2}$	$\Lambda^{-4} [\Lambda^{-2}]$
$C_{tu}^8, C_{td}^8$	$\Lambda^{-2}$	–
$C_{Qq}^{1,1}$	$\Lambda^{-4} [\Lambda^{-2}]$	–
$C_{Qq}^{3,1}$	$\Lambda^{-4} [\Lambda^{-2}]$	$\Lambda^{-2}$
$C_{tu}^1, C_{td}^1$	$\Lambda^{-4} [\Lambda^{-2}]$	–
$C_{Qu}^8, C_{Qd}^8$	$\Lambda^{-2}$	–
$C_{tq}^8$	$\Lambda^{-2}$	–
$C_{Qu}^1, C_{Qd}^1$	$\Lambda^{-4} [\Lambda^{-2}]$	–
$C_{tq}^1$	$\Lambda^{-4} [\Lambda^{-2}]$	–
$C_{\phi Q}^-$	–	–
$C_{\phi Q}^3$	–	$\Lambda^{-2}$
$C_{\phi t}$	–	–
$C_{\phi tb}$	–	$\Lambda^{-4}$
$C_{tZ}$	–	–
$C_{tW}$	–	$\Lambda^{-2}$
$C_{bW}$	–	$\Lambda^{-4}$
$C_{tG}$	$\Lambda^{-2}$	$[\Lambda^{-2}]$

# Top quark polarisation

In agreement with the predictions

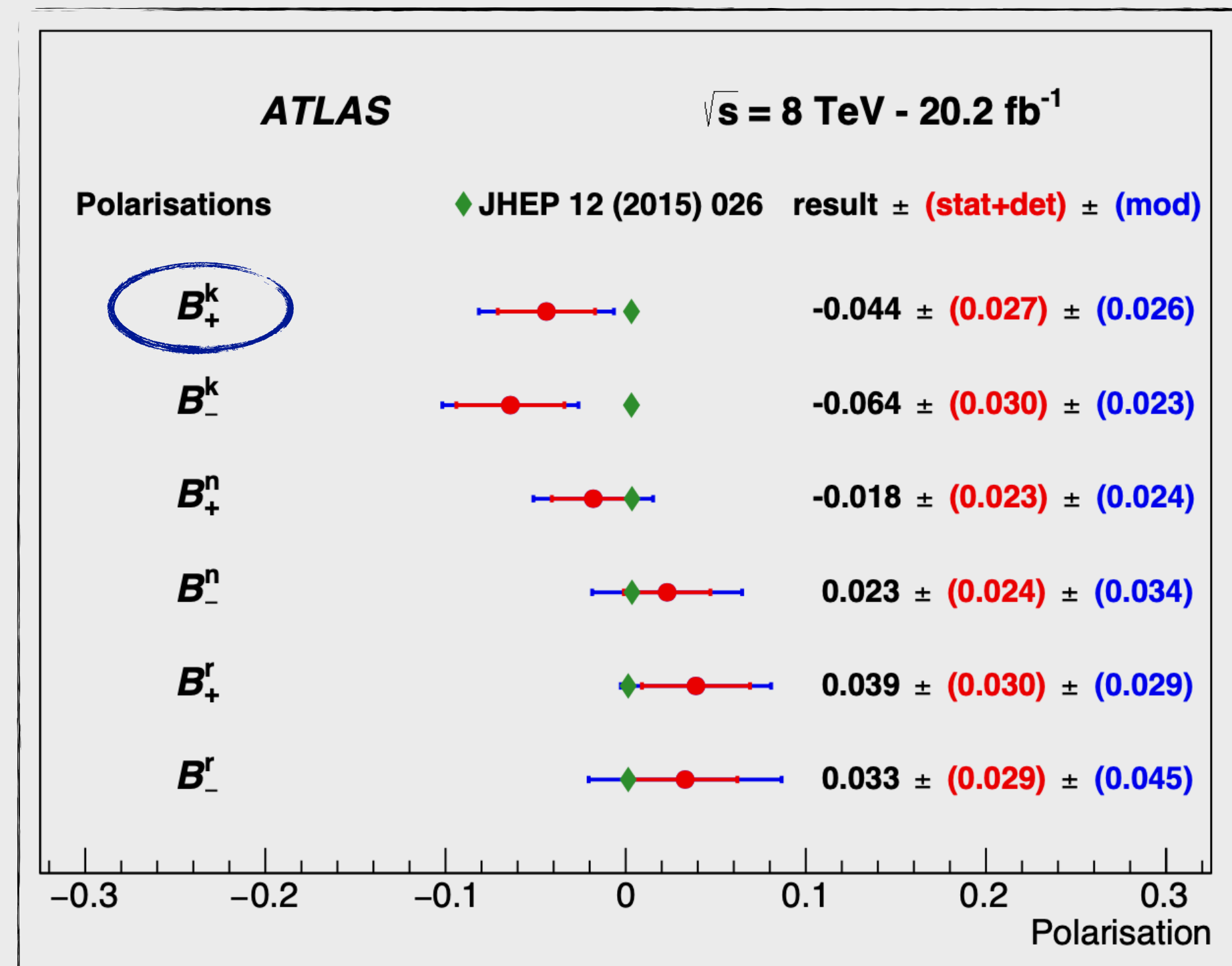
$$\begin{array}{cc}
 \hat{B}_+^k & \hat{B}_-^k \\
 \hat{B}_+^r & \hat{B}_-^r \\
 \hat{B}_+^n & \hat{B}_-^n
 \end{array}$$



ATLAS

$$\frac{1}{2}(1 + B_+^k \cos \theta_+^k)$$

→

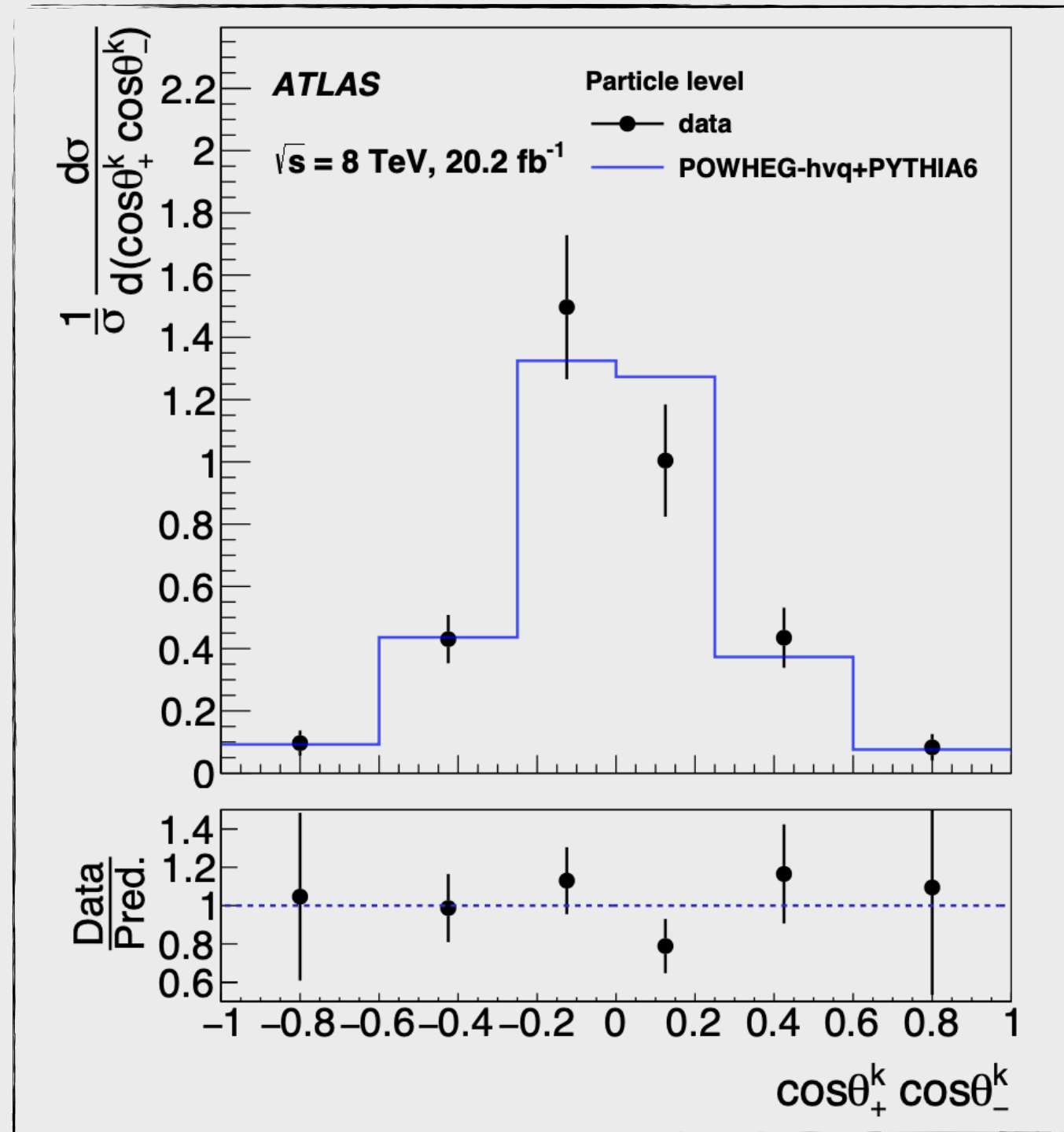


ATLAS

- ⊙ Measurements not yet sensitive to small level of polarisation in the SM
- ⊙ This distribution should be sloped if top quarks are produced with high polarisation:
  - ➡ Dominant uncertainty affects top rest frame reconstruction

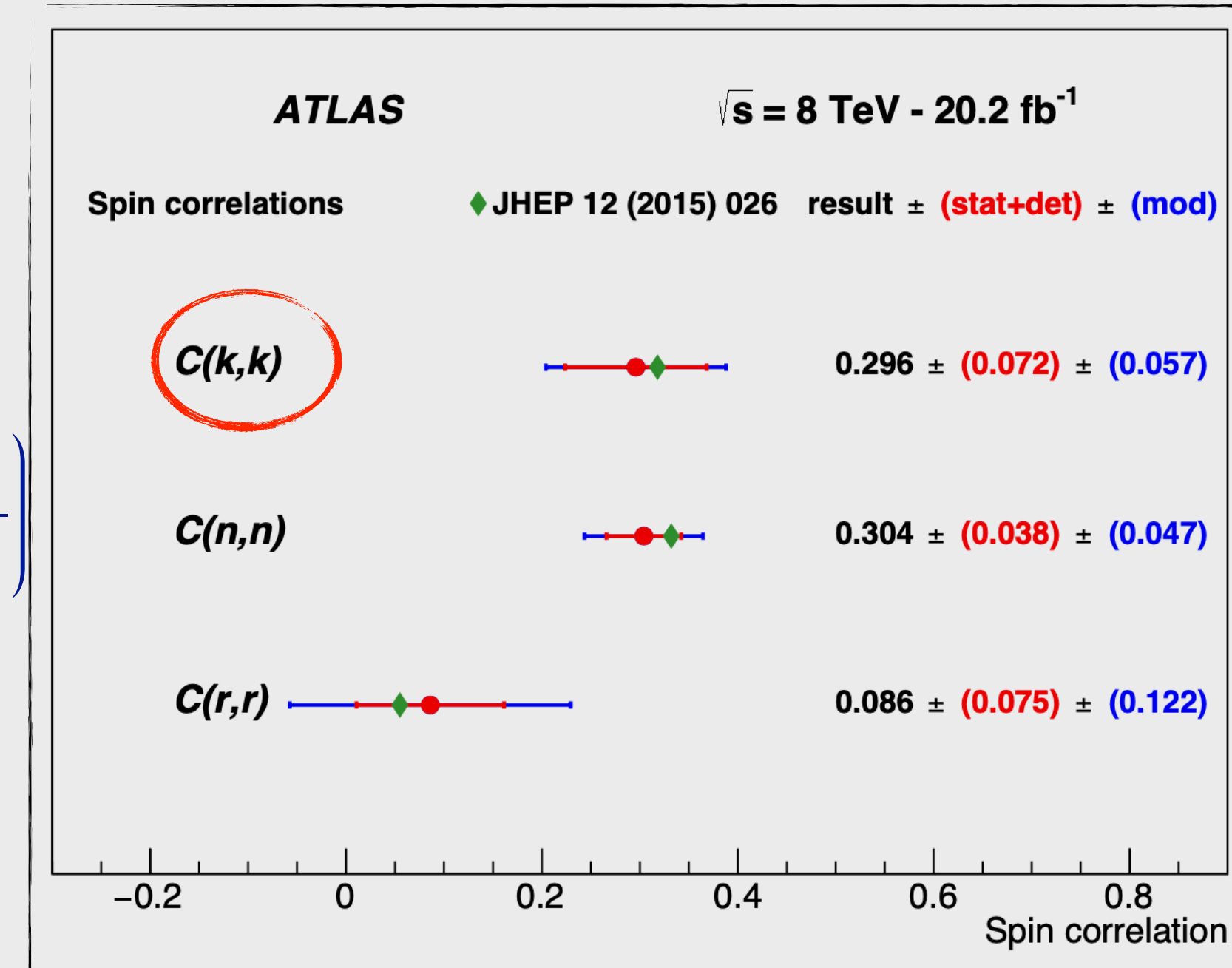
# Spin correlation

In agreement with the predictions



ATLAS

$$\frac{1}{2} \left( 1 - C(\hat{k}, \hat{k}) \cos \theta_+^{\hat{k}} \cos \theta_-^{\hat{k}} \right) \log \left( \frac{1}{|\cos \theta_+^{\hat{k}} \cos \theta_-^{\hat{k}}|} \right)$$



ATLAS

$$C(\hat{k}, \hat{k}) \quad C(\hat{r}, \hat{k}) \quad C(\hat{n}, \hat{k})$$

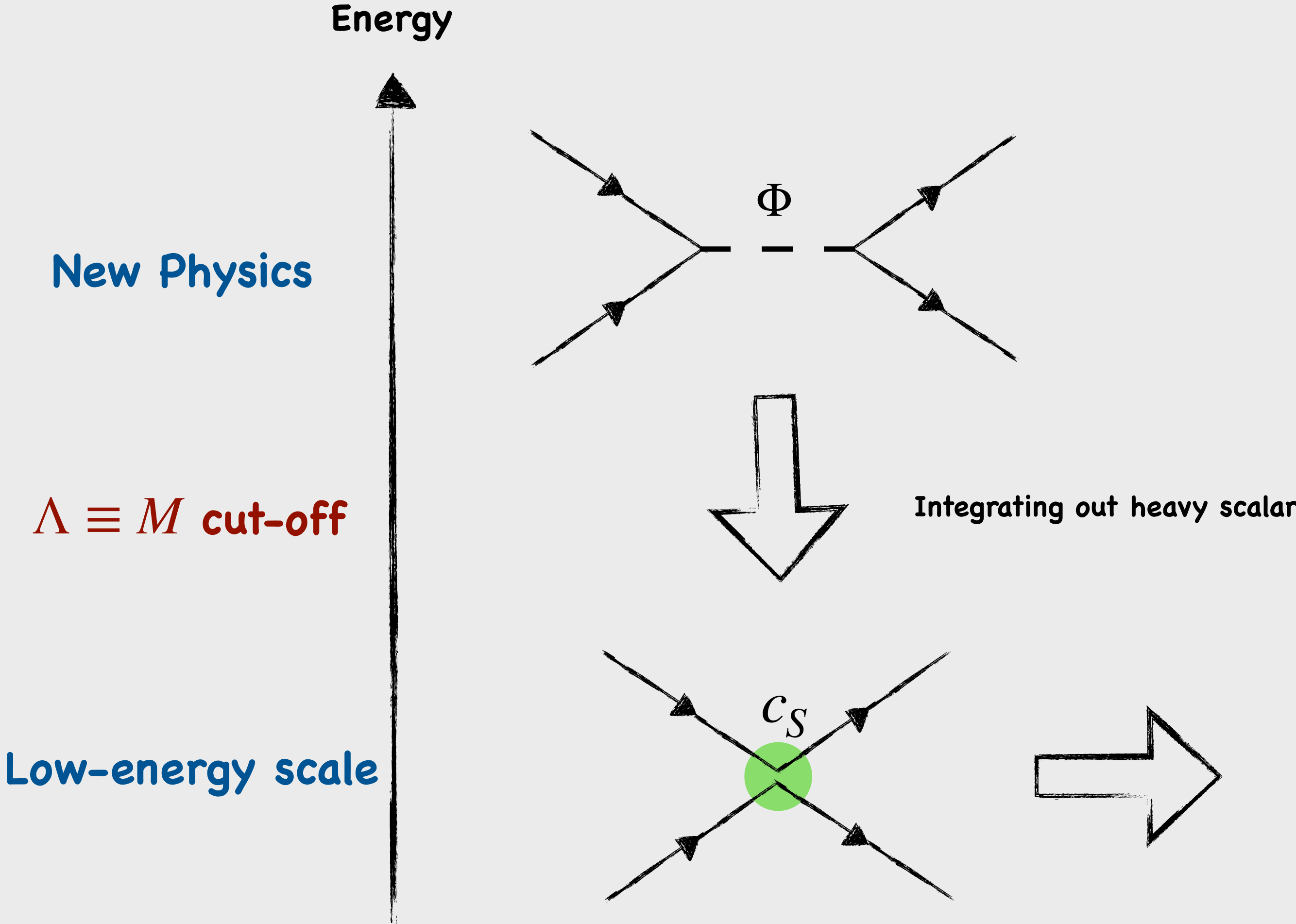
$$C(\hat{k}, \hat{r}) \quad C(\hat{r}, \hat{r}) \quad C(\hat{n}, \hat{r})$$

$$C(\hat{k}, \hat{n}) \quad C(\hat{r}, \hat{n}) \quad C(\hat{n}, \hat{n})$$

- This distribution should be symmetric if there was no spin correlations
- Spin correlations along each axis consistent with SM expectations

# SM-EFT: What is it all about?

Fermions:  $\psi$   
Heavy scalar:  $\Phi$

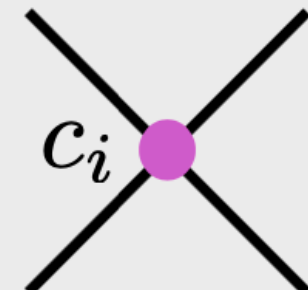


$$\mathcal{L}_{\text{Full}} = \mathcal{L}(\psi) + \mathcal{L}(\psi, \Phi)$$

$$\mathcal{L}_{\text{EFT}} = \mathcal{L}(\psi) + \frac{c_S}{M^2} \frac{1}{2} (\bar{\psi}\psi)(\bar{\psi}\psi)$$

# SM-EFT: What is it all about?

Couplings = Wilson coefficients



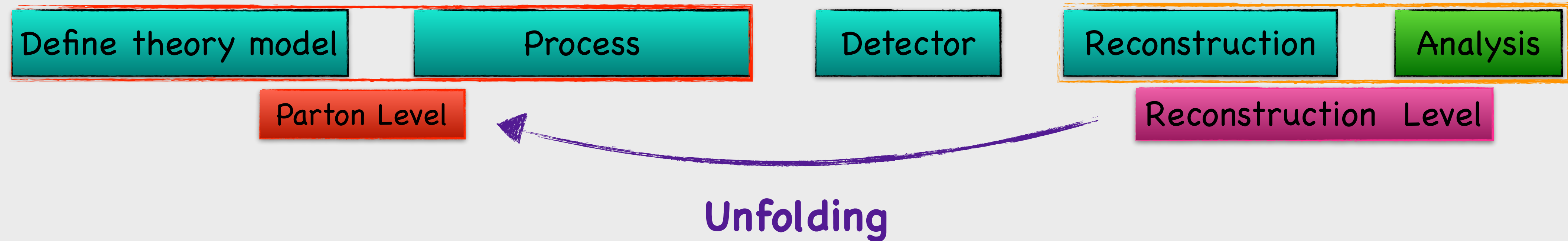
$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}}^{(4)} + \sum_i \frac{c_i^d \mathcal{O}_i^d}{\Lambda^{d-4}}$$

SM particles

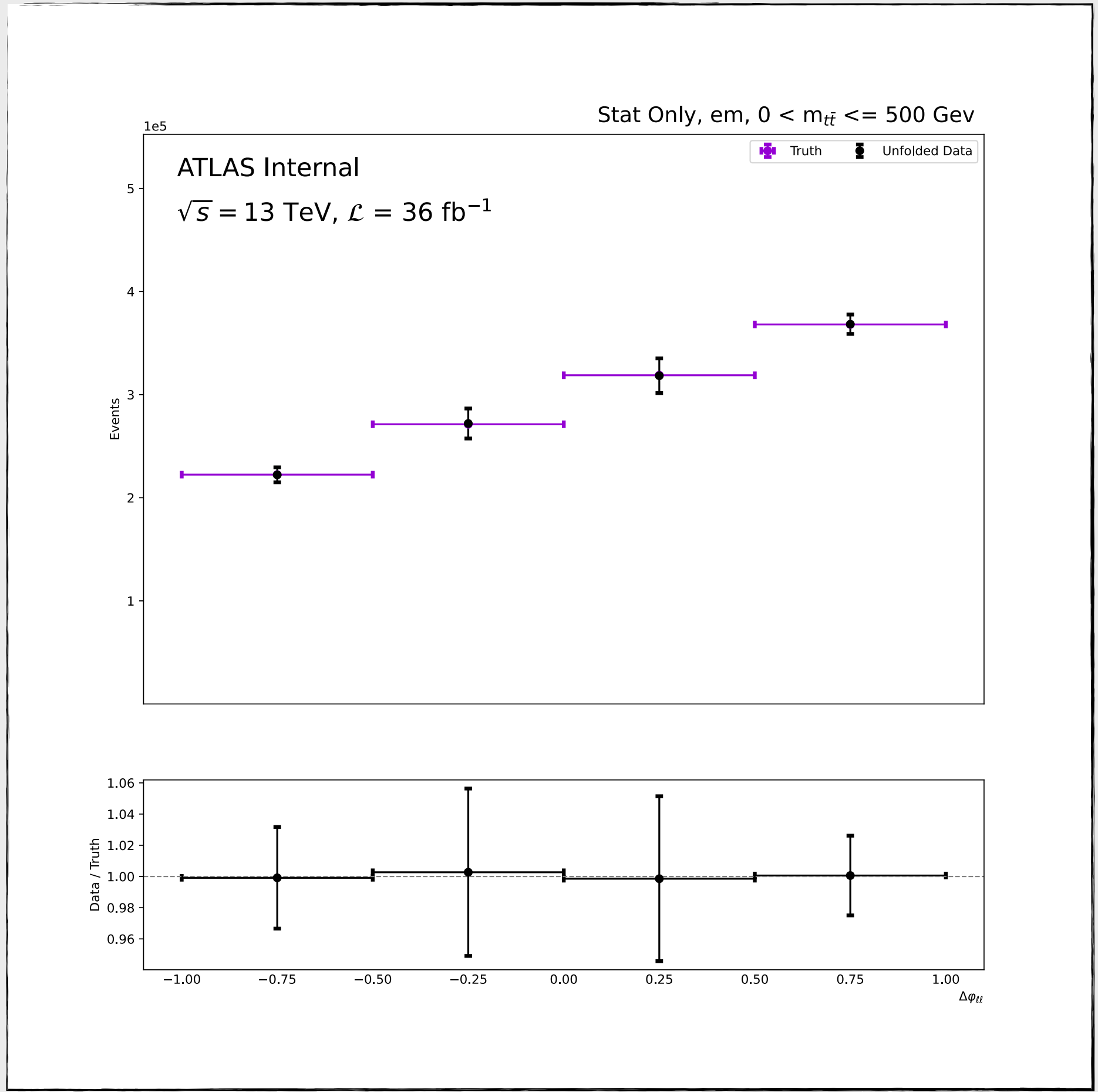
Higher (mass) dimension operators suppressed by NP scale

SM-EFT validly

$\odot \mathcal{L}_{\text{eft}} = \sum_{i,d \geq 5} \frac{c_i \mathcal{O}_i^d}{\Lambda^{d-4}}$ , should respect:  
 $\clubsuit SU(3)_C \otimes SU(2)_L \otimes U(1)_Y$



- Unfolding: remove detector effects, to get the truth-level distribution.
- Systematic uncertainties, for now only considering the main uncertainties, signal modelling systematics:
  - ♣ aMCNLO-Herwig Vs. aMCNLO-Pythia8



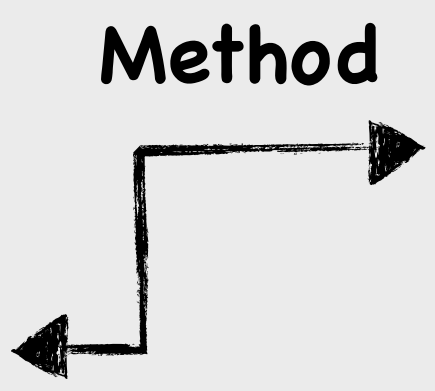
closure test



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In what way does the EFT affect the spin correlation at LO and NLO?

- Cross validate the SMEFT@NLO implementation against Dim6Top model

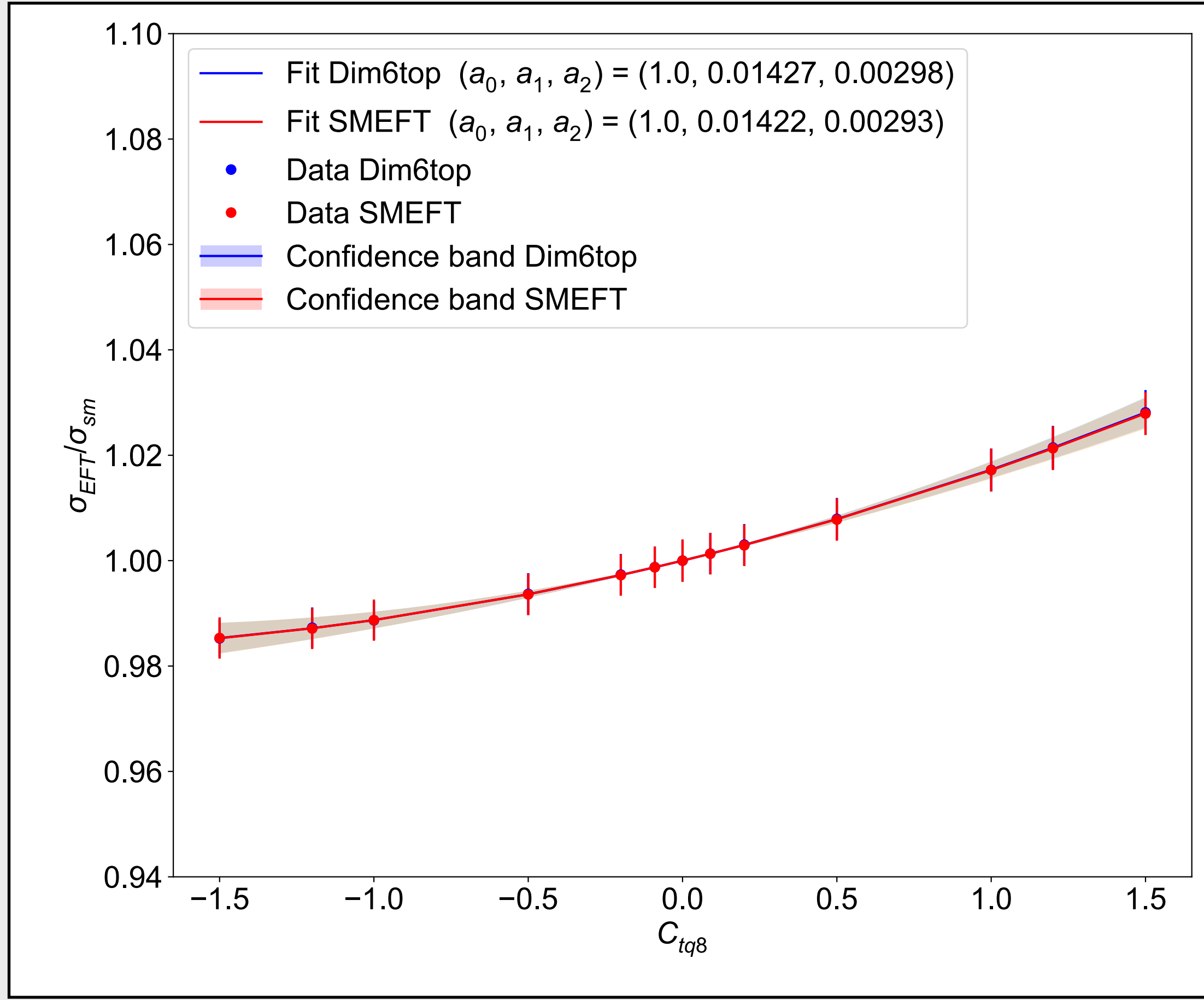


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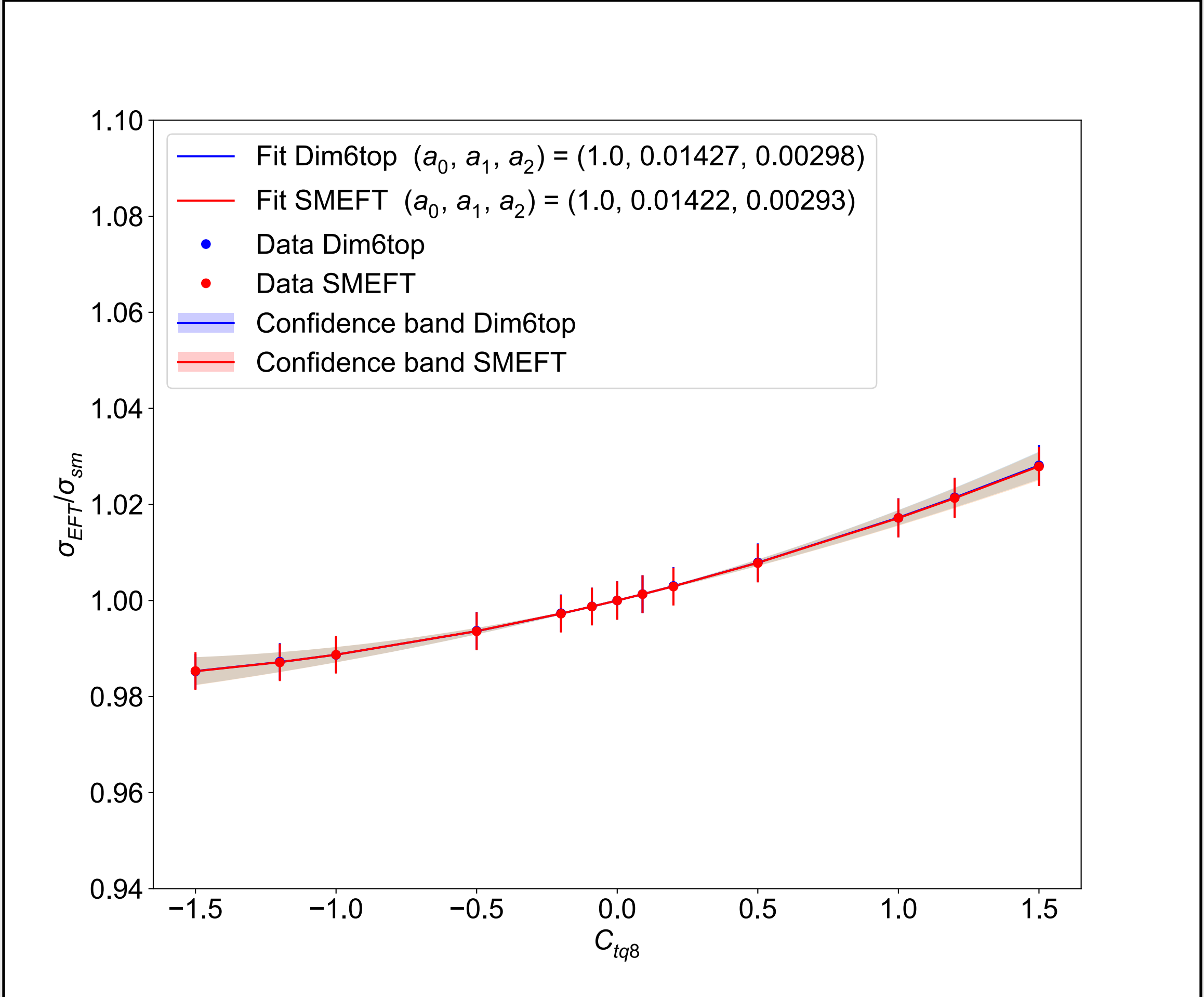
Comments

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# Cross Section, ctq8





# Evidence of Entanglement

- ⦿ Base selection:
  - ⦿ Two OS leptons ( $e\mu, \mu\mu, ee$ ).
  - ⦿ At least ~~two~~ one b-tagged jet

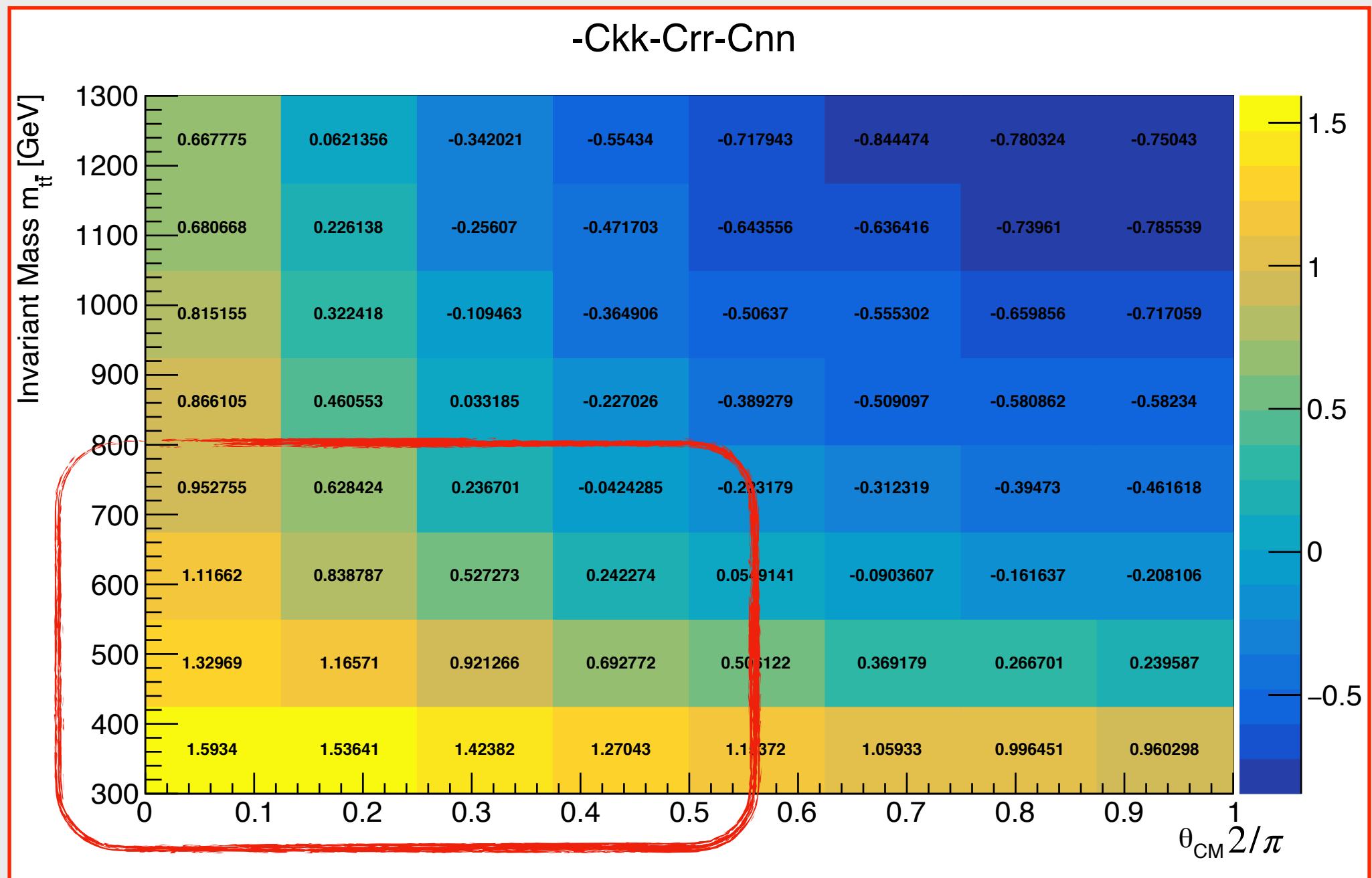
⦿ Other approach to look for Entanglement in  $t\bar{t}$  events:

- ✿  $-C_{kk} - C_{rr} - C_{nn} > 1$  at **threshold** (equivalent to measuring D)
- ✿  $C_{kk} + C_{rr} - C_{nn} > 1$  at high regime (high  $m_{t\bar{t}}$  and  $\theta_{CM}$ )

⦿ Work in progress, fresh results

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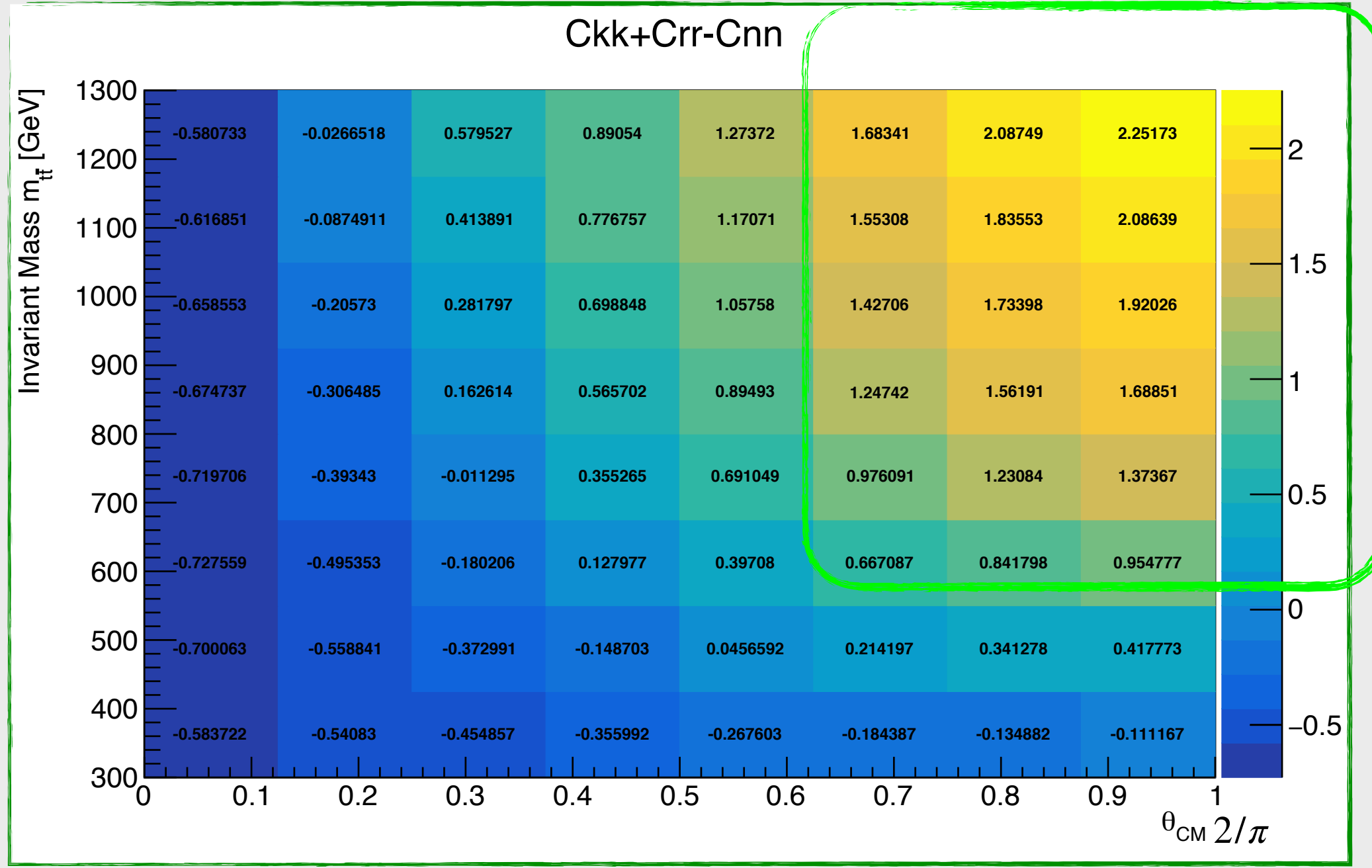
⦿  $> 1$  sufficient conditions for entanglement.

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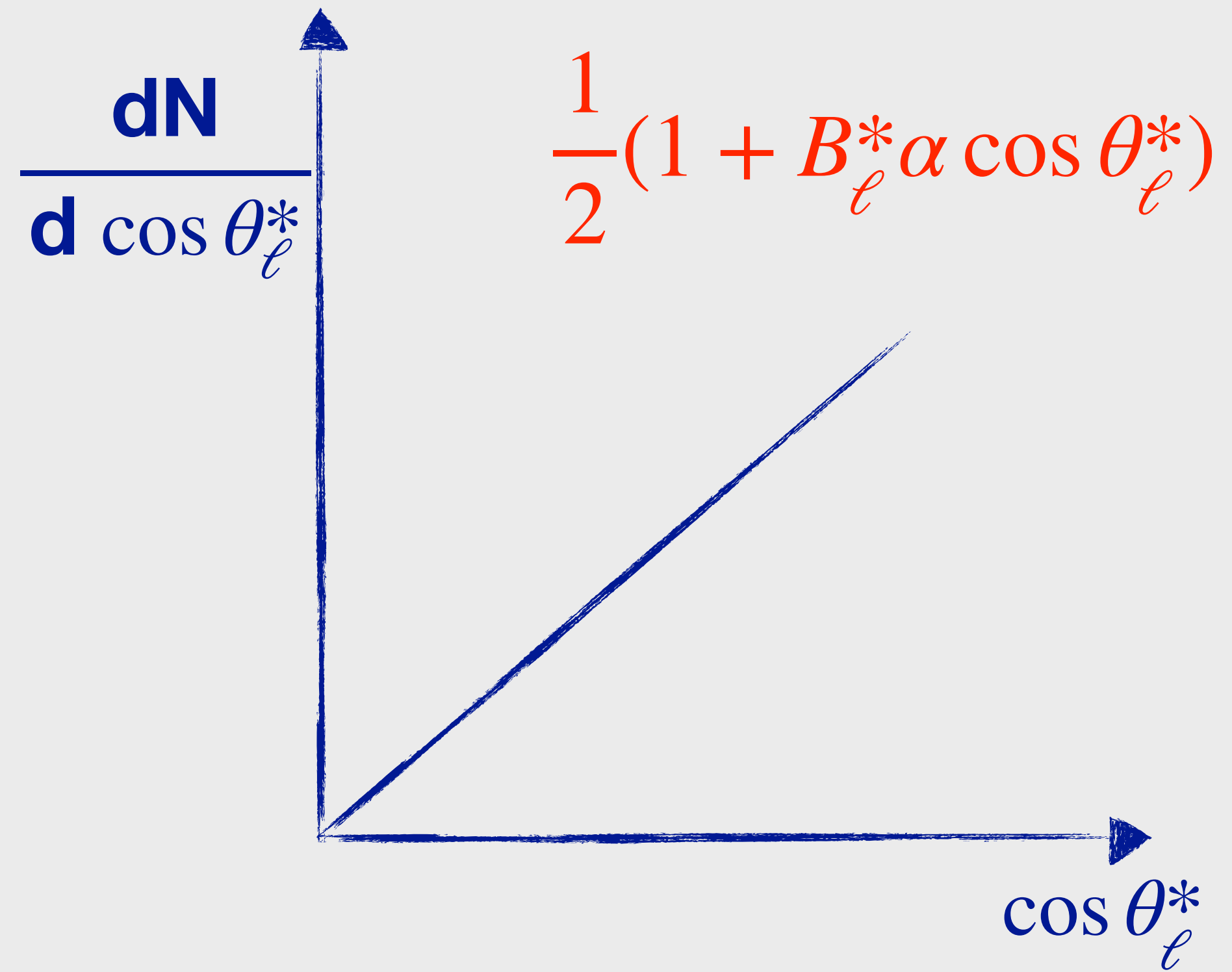
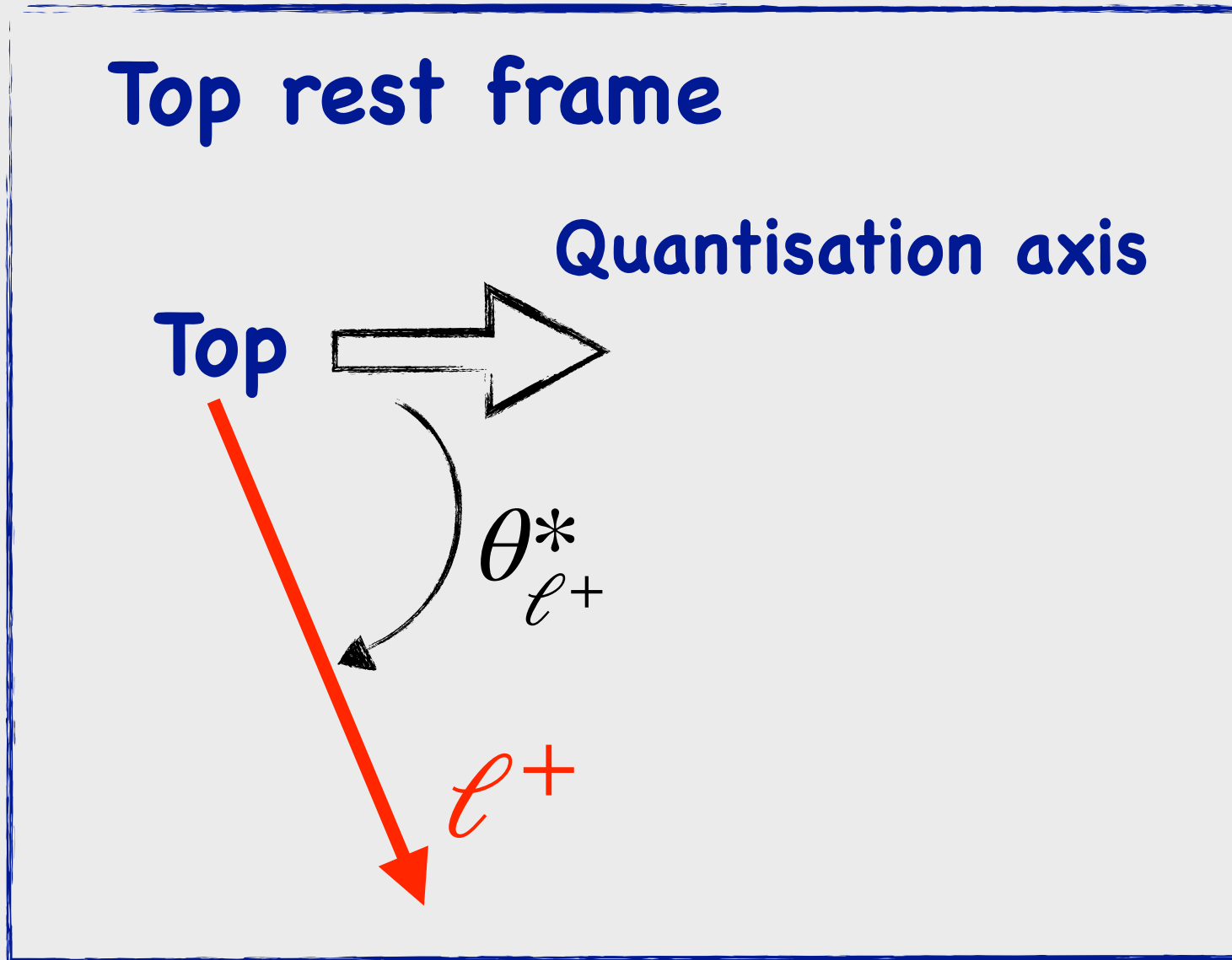


●  $> 1$  sufficient conditions for entanglement.

Selections	$C_{kk} + C_{rr} - C_{nn}$
Weak	
Intermediate	
Strong	

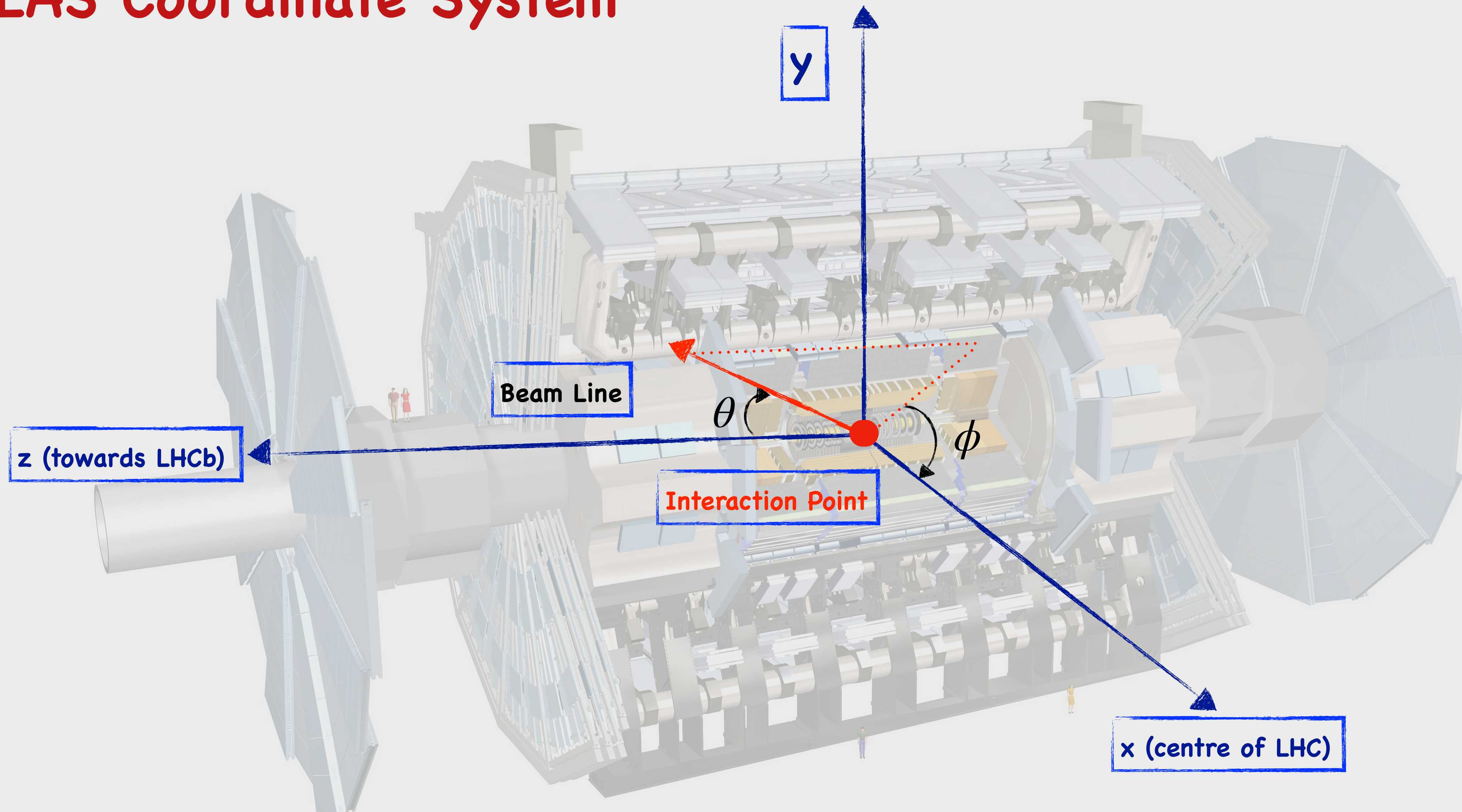
● At parton level

# Polarised Top quark decay



- $-1 \leq B_{\ell}^* \leq 1$  is polarisation, measured along chosen axis (\*)
- For a fully polarised ensemble of top quarks,  $B_{\ell}^* = 1$ .

# ATLAS Coordinate System



# The Standard Model of Particle Physics

	u
mass	$\approx 2.4 \text{ MeV}/c^2$
charge	$2/3$
spin	$1/2$
	up

	d
mass	$\approx 4.8 \text{ MeV}/c^2$
charge	$-1/3$
spin	$1/2$
	down

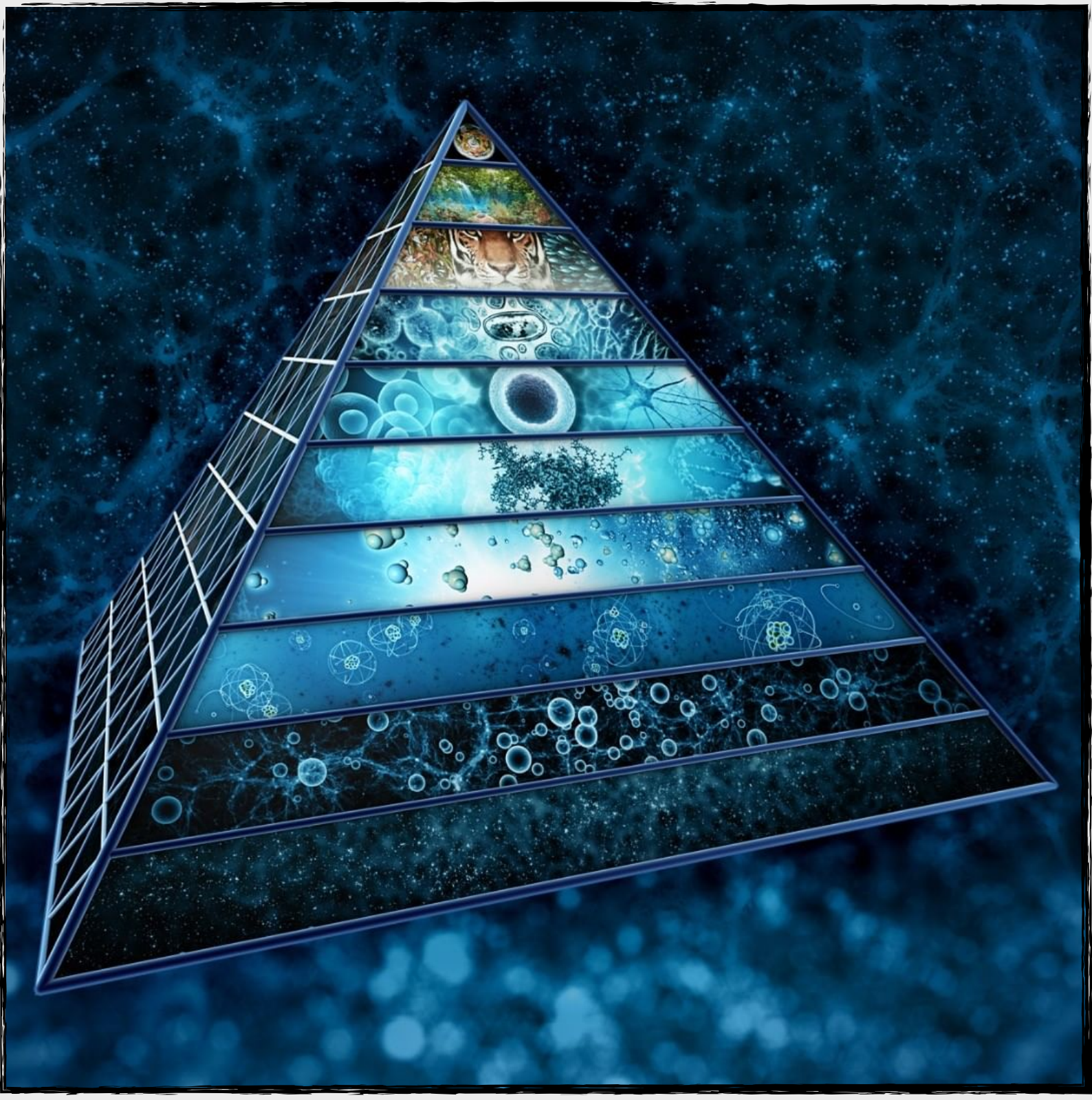
  

	e
mass	$\approx 0.511 \text{ MeV}/c^2$
charge	$-1$
spin	$1/2$
	electron

**QUARKS**

**LEPTONS**

© All ordinary matter is made from up quarks, down quarks, and electrons.



The Pyramid of Complexity

# The Standard Model of Particle Physics

## Standard Model of Elementary Particles

three generations of matter (fermions)

	I	II	III
mass	$\approx 2.4 \text{ MeV}/c^2$	$\approx 1.275 \text{ GeV}/c^2$	$\approx 172.44 \text{ GeV}/c^2$
charge	$2/3$	$2/3$	$2/3$
spin	$1/2$	$1/2$	$1/2$
	<b>u</b> up	<b>c</b> charm	<b>t</b> top
	$\approx 4.8 \text{ MeV}/c^2$	$\approx 95 \text{ MeV}/c^2$	$\approx 4.18 \text{ GeV}/c^2$
	$-1/3$	$-1/3$	$-1/3$
	$1/2$	$1/2$	$1/2$
	<b>d</b> down	<b>s</b> strange	<b>b</b> bottom
	$\approx 0.511 \text{ MeV}/c^2$	$\approx 105.67 \text{ MeV}/c^2$	$\approx 1.7768 \text{ GeV}/c^2$
	$-1$	$-1$	$-1$
	$1/2$	$1/2$	$1/2$
	<b>e</b> electron	<b><math>\mu</math></b> muon	<b><math>\tau</math></b> tau

**QUARKS**

**LEPTONS**

© There are three copies, or **generations**, of **quarks** and **leptons**  
 Same properties, only **heavier**

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	<b>e</b> electron	<b><math>\mu</math></b> muon	<b><math>\tau</math></b> tau
	<b><math>\nu_e</math></b> electron neutrino	<b><math>\nu_\mu</math></b> muon neutrino	<b><math>\nu_\tau</math></b> tau neutrino

There are three copies, or **generations**, of **quarks** and **leptons**. Same properties, only **heavier**.

Leptons also include **neutrinos**, one for each generation.

# The Standard Model of Particle Physics

## Standard Model of Elementary Particles

		three generations of matter (fermions)		
		I	II	III
QUARKS	mass	$\approx 2.4 \text{ MeV}/c^2$	$\approx 1.275 \text{ GeV}/c^2$	$\approx 172.44 \text{ GeV}/c^2$
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		$\approx 4.8 \text{ MeV}/c^2$	$\approx 95 \text{ MeV}/c^2$	$\approx 4.18 \text{ GeV}/c^2$
		$-1/3$	$-1/3$	$-1/3$
	$1/2$	$1/2$	$1/2$	
	<b>d</b> down	<b>s</b> strange	<b>b</b> bottom	
LEPTONS	mass	$\approx 0.511 \text{ MeV}/c^2$	$\approx 105.67 \text{ MeV}/c^2$	$\approx 1.7768 \text{ GeV}/c^2$
	charge	$-1$	$-1$	$-1$
	spin	$1/2$	$1/2$	$1/2$
		<b>e</b> electron	<b><math>\mu</math></b> muon	<b><math>\tau</math></b> tau
		$< 2.2 \text{ eV}/c^2$	$< 1.7 \text{ MeV}/c^2$	$< 15.5 \text{ MeV}/c^2$
		$0$	$0$	$0$
	$1/2$	$1/2$	$1/2$	
	<b><math>\nu_e</math></b> electron neutrino	<b><math>\nu_\mu</math></b> muon neutrino	<b><math>\nu_\tau</math></b> tau neutrino	

● There are three copies, or **generations**, of **quarks** and **leptons**. Same properties, only **heavier**.

● Leptons also include **neutrinos**, one for each generation.

● All of these are matter particles, or **fermions**.



# The Standard Model of Particle Physics

## Standard Model of Elementary Particles

		three generations of antimatter (elementary antifermions)		
		I	II	III
QUARKS	mass charge spin	$\approx 2.2 \text{ MeV}/c^2$ $-\frac{2}{3}$ $\frac{1}{2}$	$\approx 1.28 \text{ GeV}/c^2$ $-\frac{2}{3}$ $\frac{1}{2}$	$\approx 173.1 \text{ GeV}/c^2$ $-\frac{2}{3}$ $\frac{1}{2}$
		$\bar{u}$ antiup	$\bar{c}$ anticharm	$\bar{t}$ antitop
		$\bar{d}$ antidown	$\bar{s}$ antistrange	$\bar{b}$ antibottom
LEPTONS	mass charge spin	$\approx 0.511 \text{ MeV}/c^2$ 1 $\frac{1}{2}$	$\approx 105.66 \text{ MeV}/c^2$ 1 $\frac{1}{2}$	$\approx 1.7768 \text{ GeV}/c^2$ 1 $\frac{1}{2}$
		$e^+$ positron	$\bar{\mu}$ antimuon	$\bar{\tau}$ antitau
		$\bar{\nu}_e$ electron antineutrino	$\bar{\nu}_\mu$ muon antineutrino	$\bar{\nu}_\tau$ tau antineutrino

There are three copies, or **generations**, of **quarks** and **leptons**. Same properties, only **heavier**.

Leptons also include **neutrinos**, one for each generation.

All of these are matter particles, or **fermions**.

**Antimatter** is exactly the same as **matter** except one attribute is flipped: the **charge**.

# The Standard Model of Particle Physics

## Standard Model of Elementary Particles

		three generations of matter (fermions)				
		I	II	III		
QUARKS	mass	$\approx 2.4 \text{ MeV}/c^2$	$\approx 1.275 \text{ GeV}/c^2$	$\approx 172.44 \text{ GeV}/c^2$	0	GAUGE BOSONS
	charge	$2/3$	$2/3$	$2/3$	0	
	spin	$1/2$	$1/2$	$1/2$	1	
		<b>u</b> up	<b>c</b> charm	<b>t</b> top	<b>g</b> gluon	
		$\approx 4.8 \text{ MeV}/c^2$	$\approx 95 \text{ MeV}/c^2$	$\approx 4.18 \text{ GeV}/c^2$	0	
		$-1/3$	$-1/3$	$-1/3$	0	
	$1/2$	$1/2$	$1/2$	1		
	<b>d</b> down	<b>s</b> strange	<b>b</b> bottom	<b>γ</b> photon		
LEPTONS	mass	$\approx 0.511 \text{ MeV}/c^2$	$\approx 105.67 \text{ MeV}/c^2$	$\approx 1.7768 \text{ GeV}/c^2$	$\approx 91.19 \text{ GeV}/c^2$	GAUGE BOSONS
	charge	-1	-1	-1	0	
	spin	$1/2$	$1/2$	$1/2$	1	
		<b>e</b> electron	<b>μ</b> muon	<b>τ</b> tau	<b>Z</b> Z boson	
		$< 2.2 \text{ eV}/c^2$	$< 1.7 \text{ MeV}/c^2$	$< 15.5 \text{ MeV}/c^2$	$\approx 80.39 \text{ GeV}/c^2$	
		0	0	0	$\pm 1$	
	$1/2$	$1/2$	$1/2$	1		
	<b>ν<sub>e</sub></b> electron neutrino	<b>ν<sub>μ</sub></b> muon neutrino	<b>ν<sub>τ</sub></b> tau neutrino	<b>W</b> W boson		

There are three copies, or **generations**, of **quarks** and **leptons**. Same properties, only **heavier**.

Leptons also include **neutrinos**, one for each generation.

All of these are matter particles, or **fermions**.

The other group of particles in the Standard Model are **bosons**.  
 → These are the force carriers.

# The Standard Model of Particle Physics

## Standard Model of Elementary Particles

		three generations of matter (fermions)				
		I	II	III		
QUARKS	mass	$\approx 2.4 \text{ MeV}/c^2$	$\approx 1.275 \text{ GeV}/c^2$	$\approx 172.44 \text{ GeV}/c^2$	0	$\approx 125.09 \text{ GeV}/c^2$
	charge	$2/3$	$2/3$	$2/3$	0	0
	spin	$1/2$	$1/2$	$1/2$	1	0
		<b>u</b> up	<b>c</b> charm	<b>t</b> top	<b>g</b> gluon	<b>H</b> Higgs
		$\approx 4.8 \text{ MeV}/c^2$	$\approx 95 \text{ MeV}/c^2$	$\approx 4.18 \text{ GeV}/c^2$	0	
		$-1/3$	$-1/3$	$-1/3$	0	
	$1/2$	$1/2$	$1/2$	1		
	<b>d</b> down	<b>s</b> strange	<b>b</b> bottom	<b>γ</b> photon		
LEPTONS	mass	$\approx 0.511 \text{ MeV}/c^2$	$\approx 105.67 \text{ MeV}/c^2$	$\approx 1.7768 \text{ GeV}/c^2$	$\approx 91.19 \text{ GeV}/c^2$	
	charge	-1	-1	-1	0	
	spin	$1/2$	$1/2$	$1/2$	1	
		<b>e</b> electron	<b>μ</b> muon	<b>τ</b> tau	<b>Z</b> Z boson	
		$< 2.2 \text{ eV}/c^2$	$< 1.7 \text{ MeV}/c^2$	$< 15.5 \text{ MeV}/c^2$	$\approx 80.39 \text{ GeV}/c^2$	
		0	0	0	$\pm 1$	
	$1/2$	$1/2$	$1/2$	1		
	<b>ν<sub>e</sub></b> electron neutrino	<b>ν<sub>μ</sub></b> muon neutrino	<b>ν<sub>τ</sub></b> tau neutrino	<b>W</b> W boson		

There are three copies, or **generations**, of **quarks** and **leptons**. Same properties, only **heavier**.

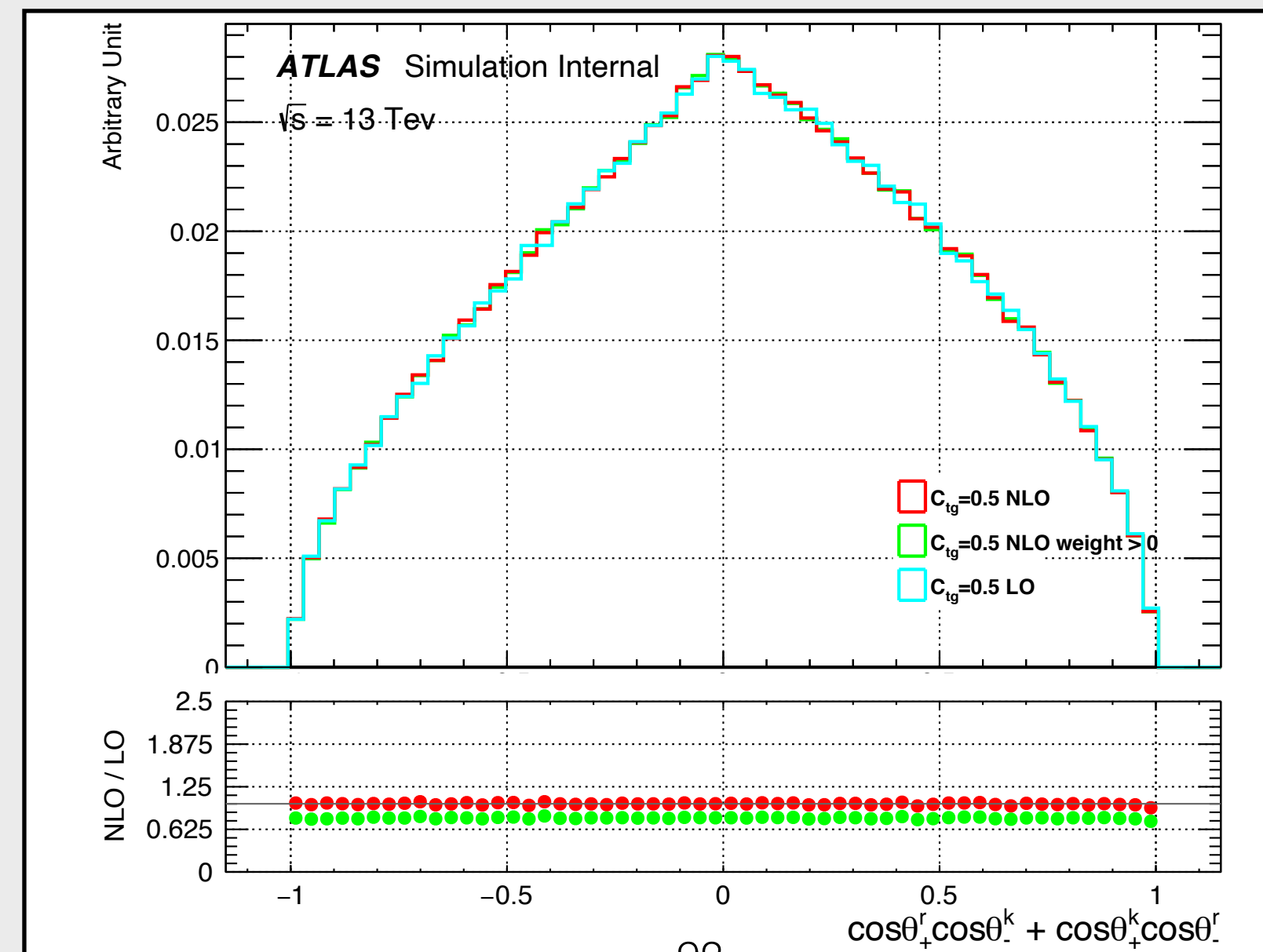
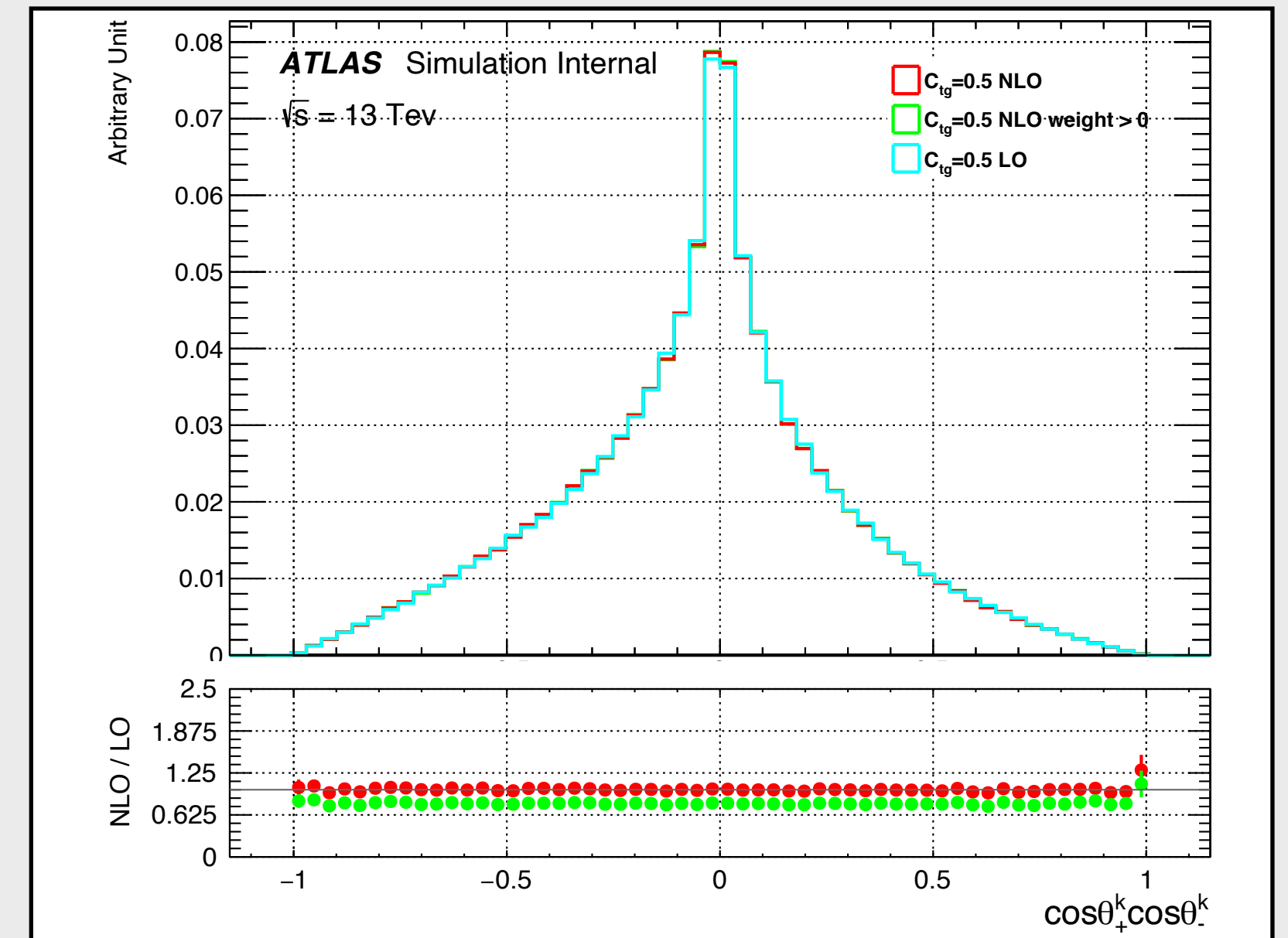
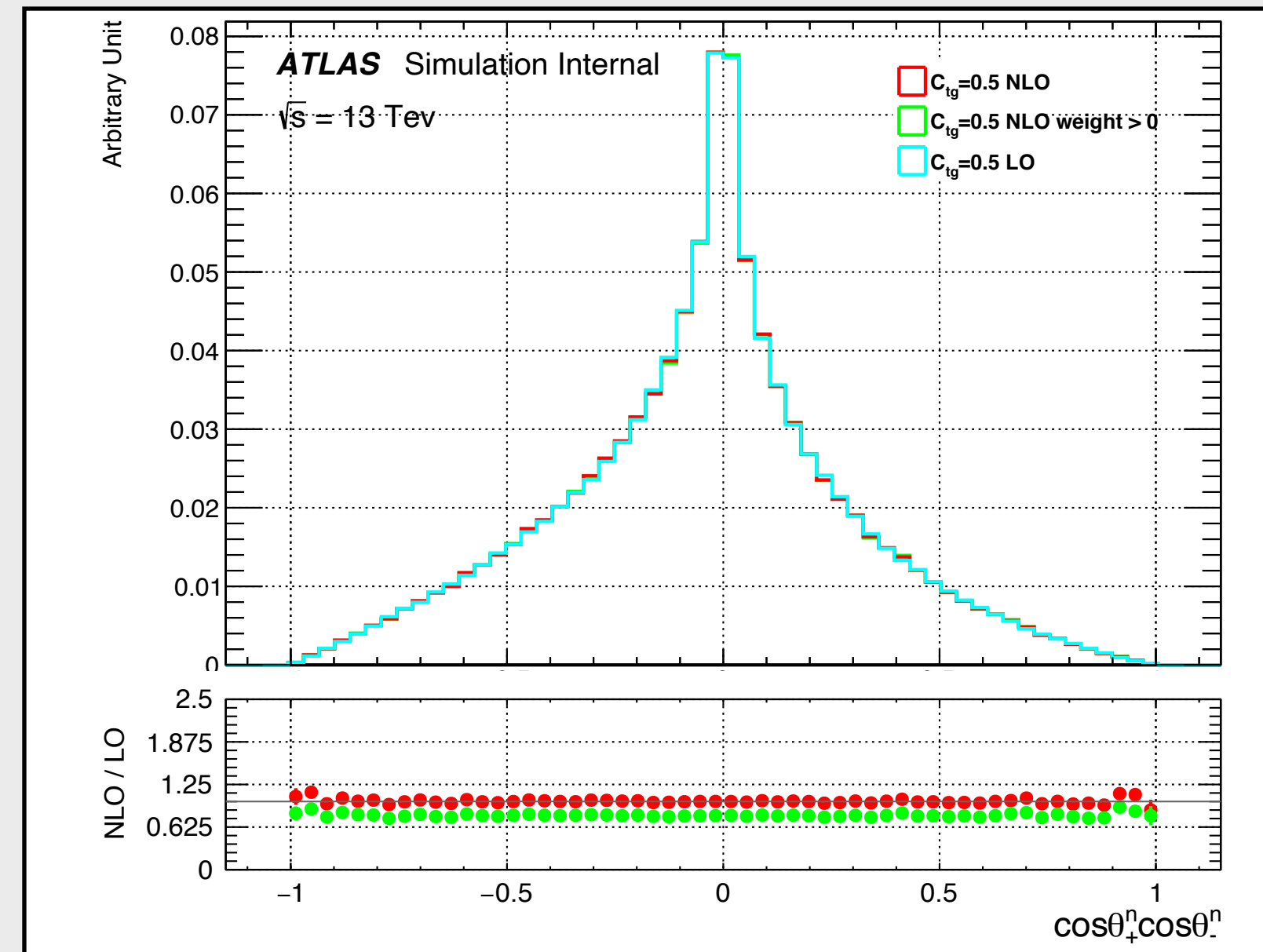
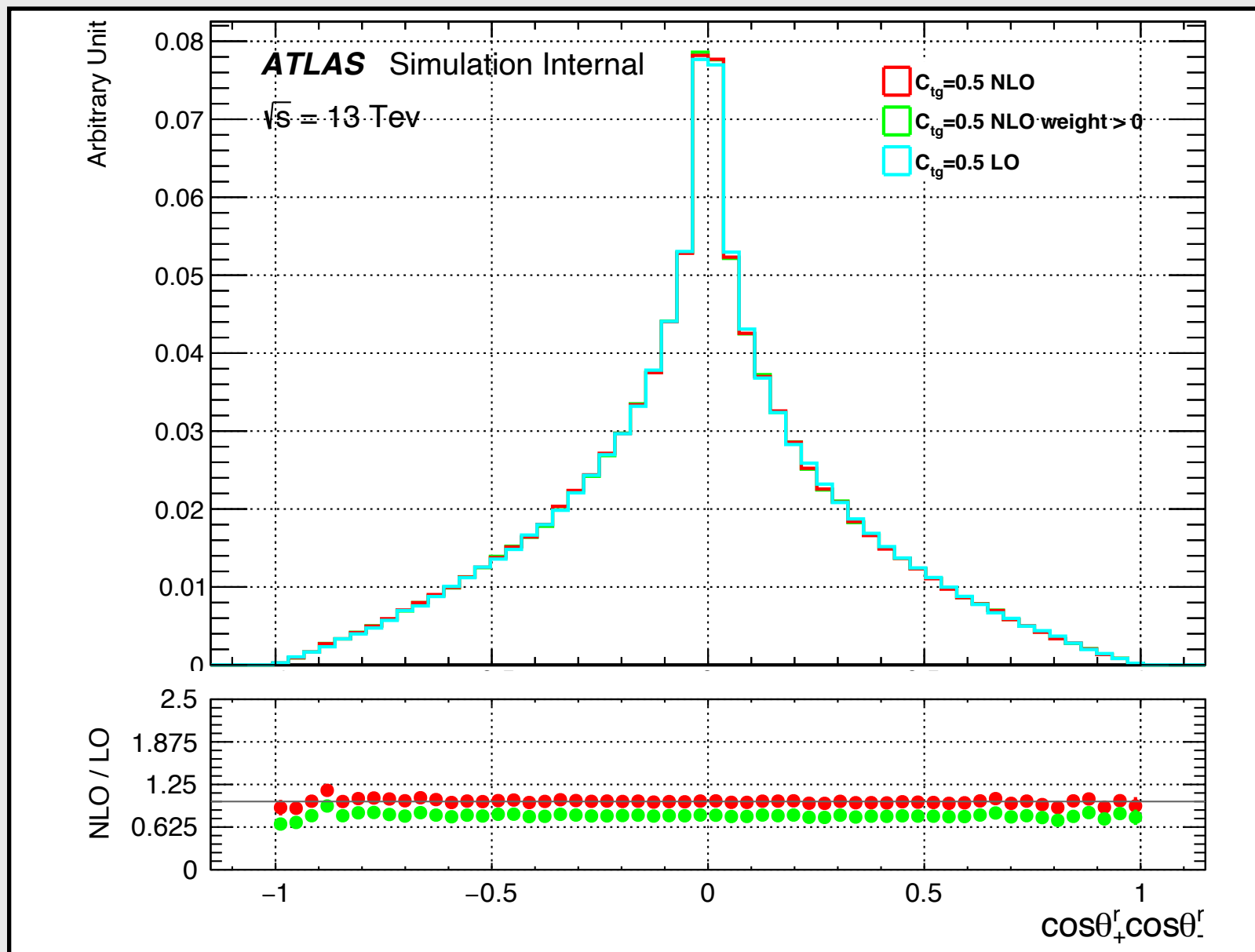
Leptons also include **neutrinos**, one for each generation.

All of these are matter particles, or **fermions**.

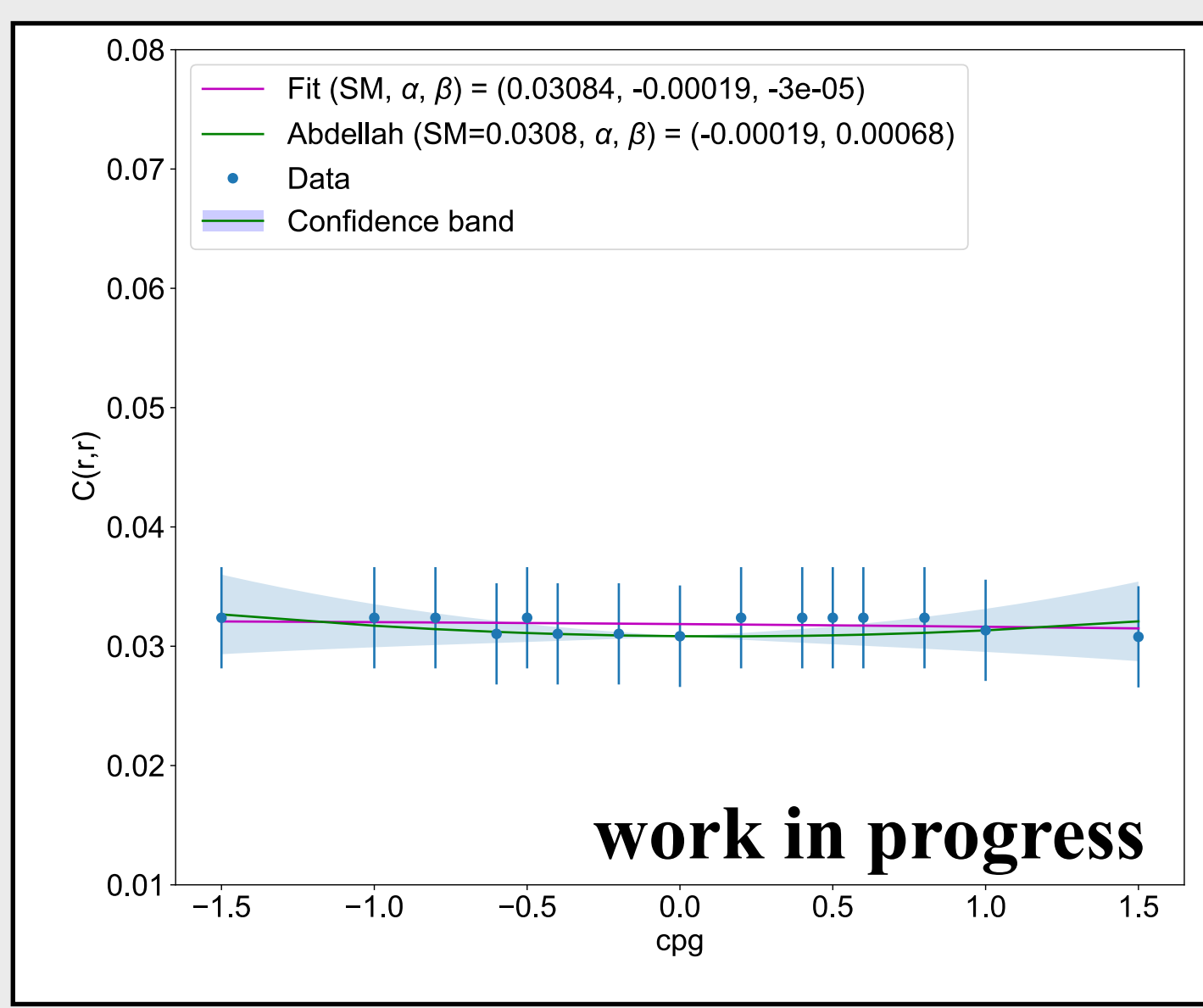
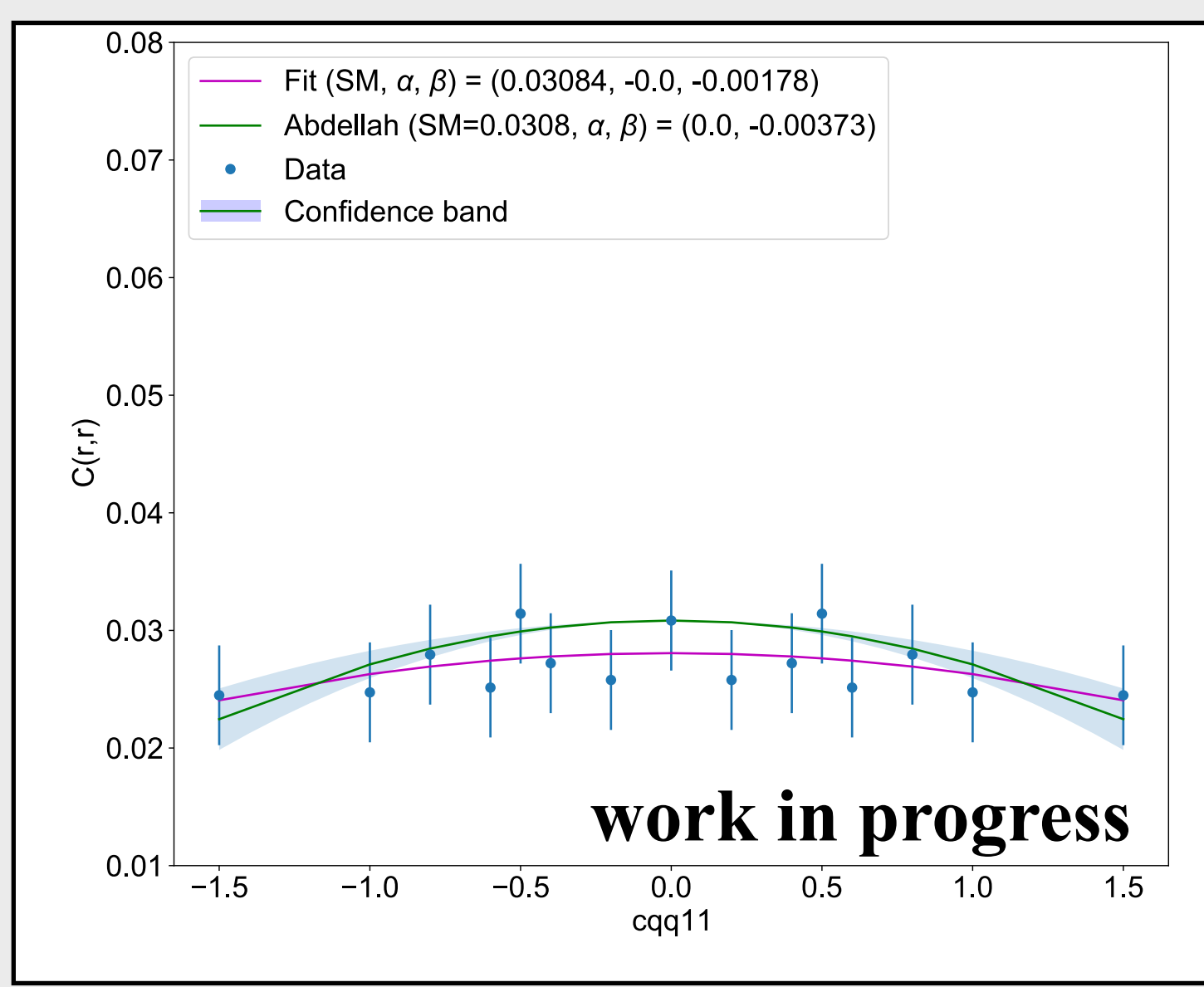
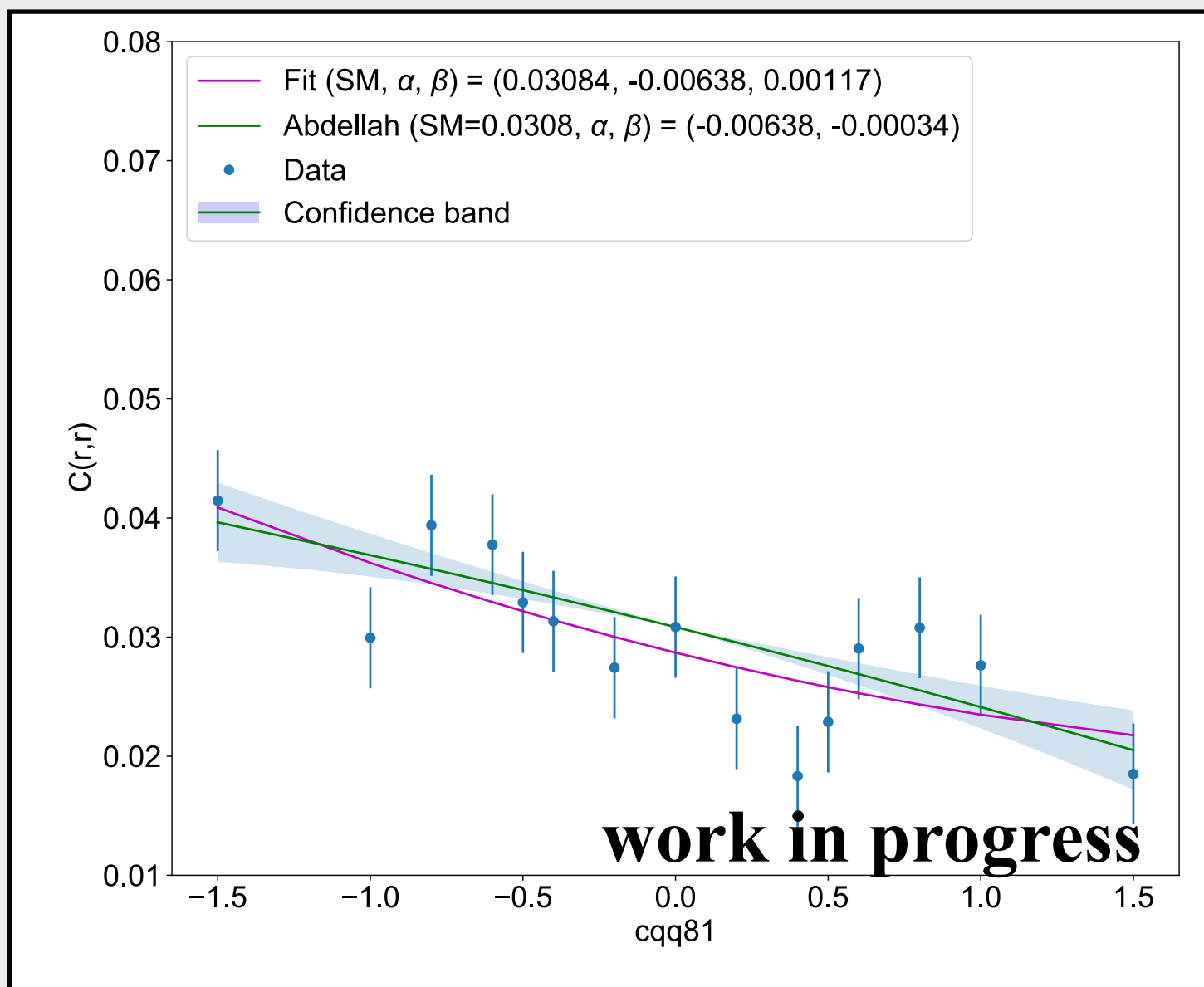
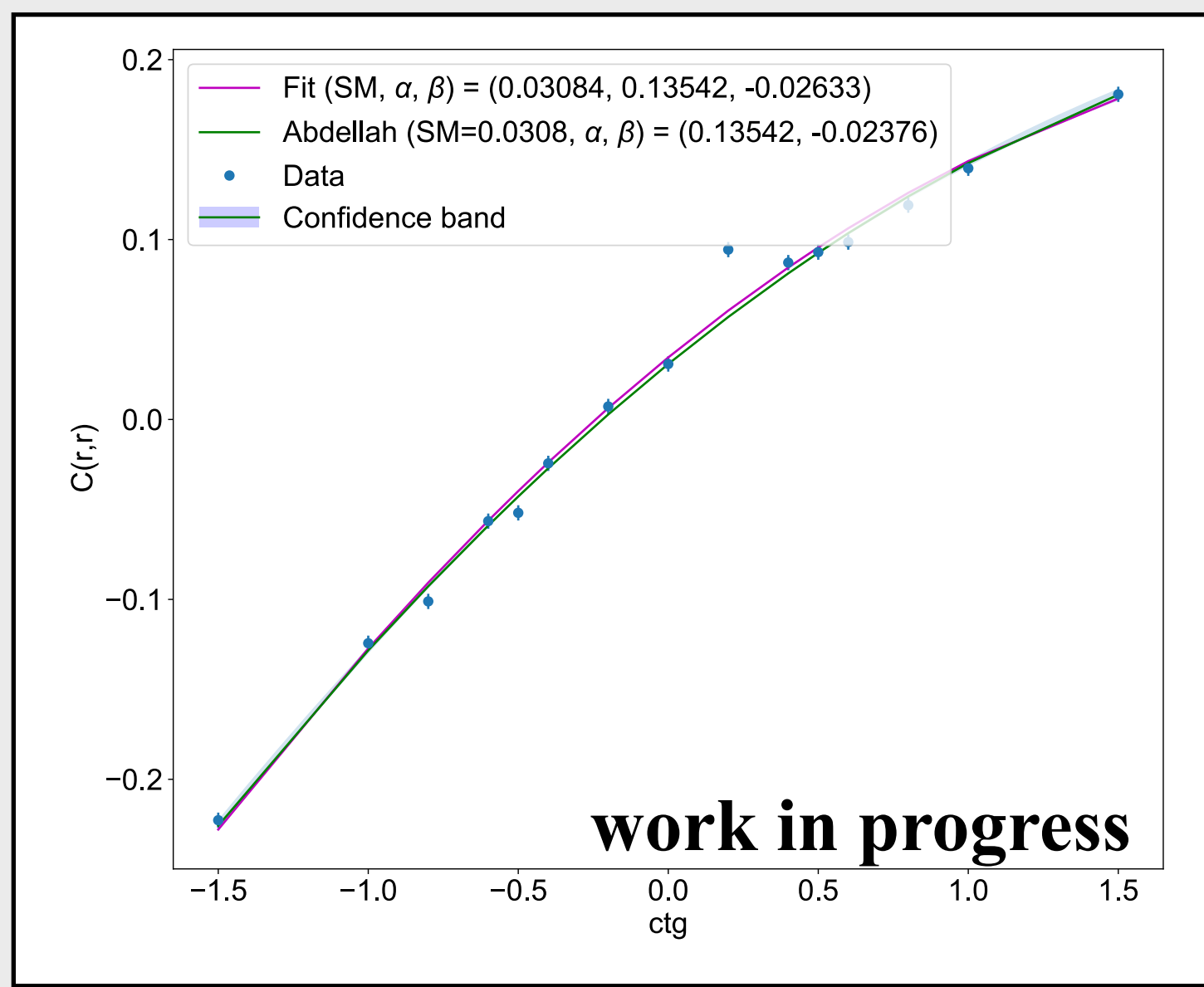
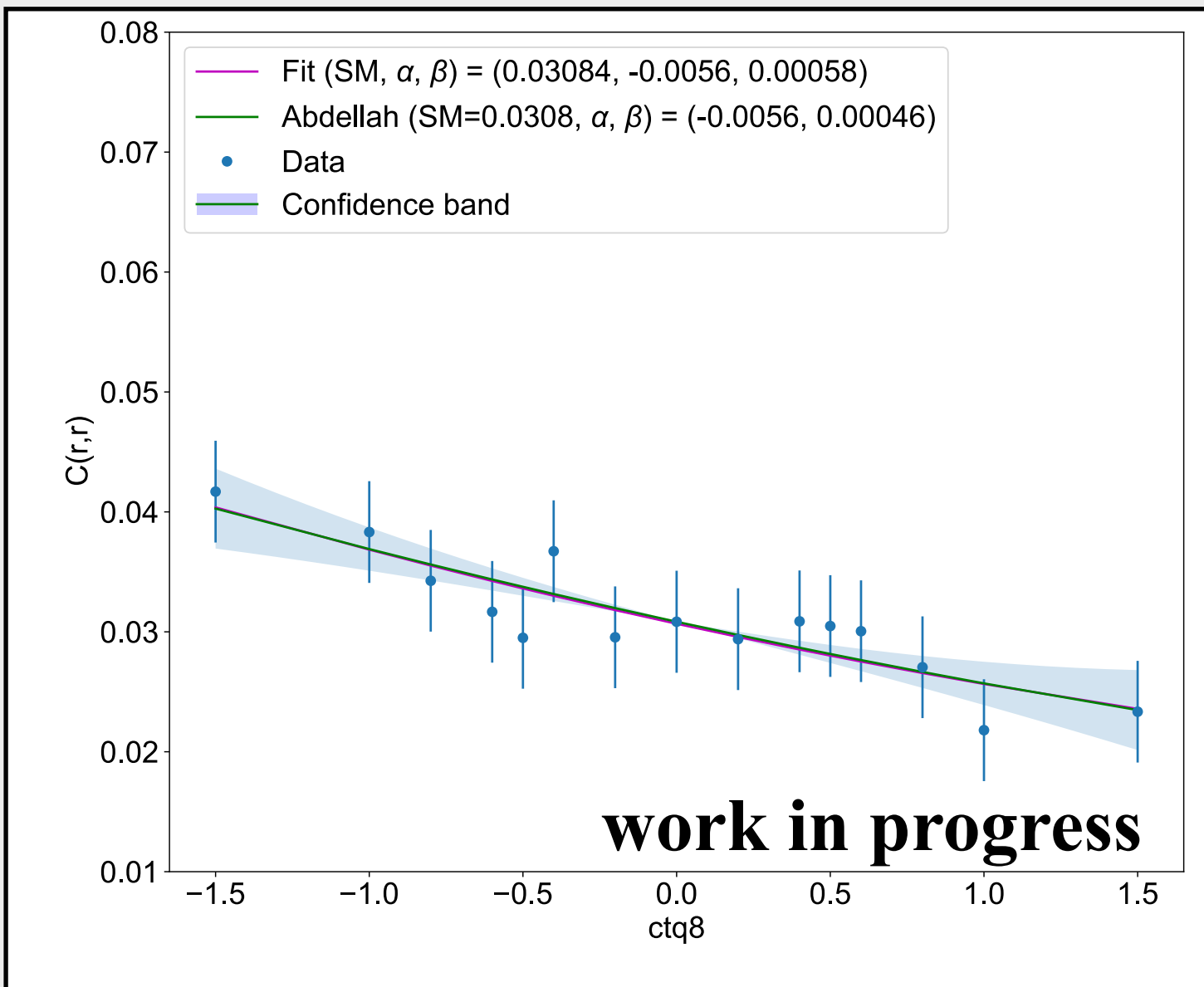
The other group of particles in the Standard Model are **bosons**.

**Higgs mechanism explains how particles get their mass**

# SM-EFT vs Dim6Top, Ctg

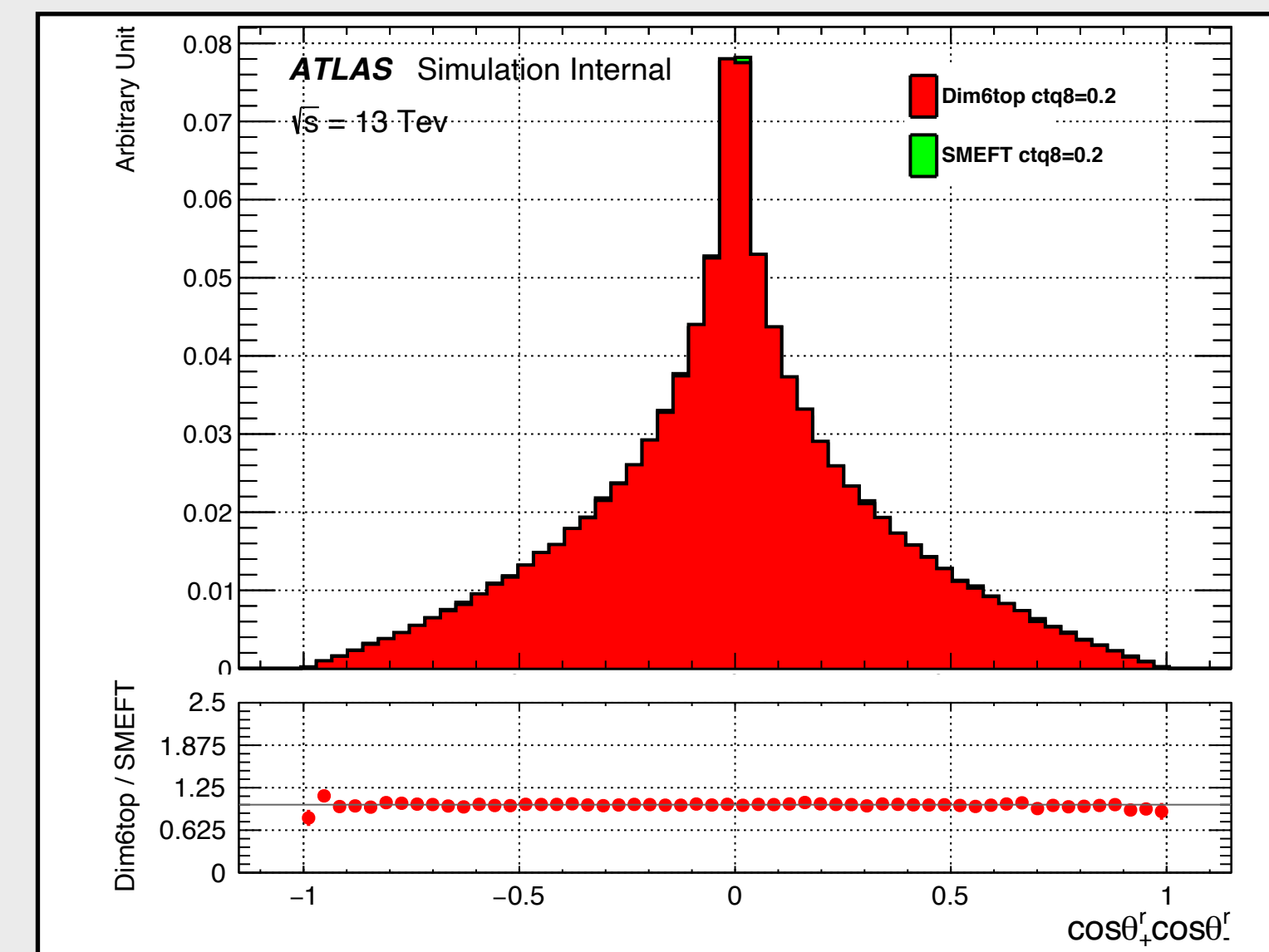
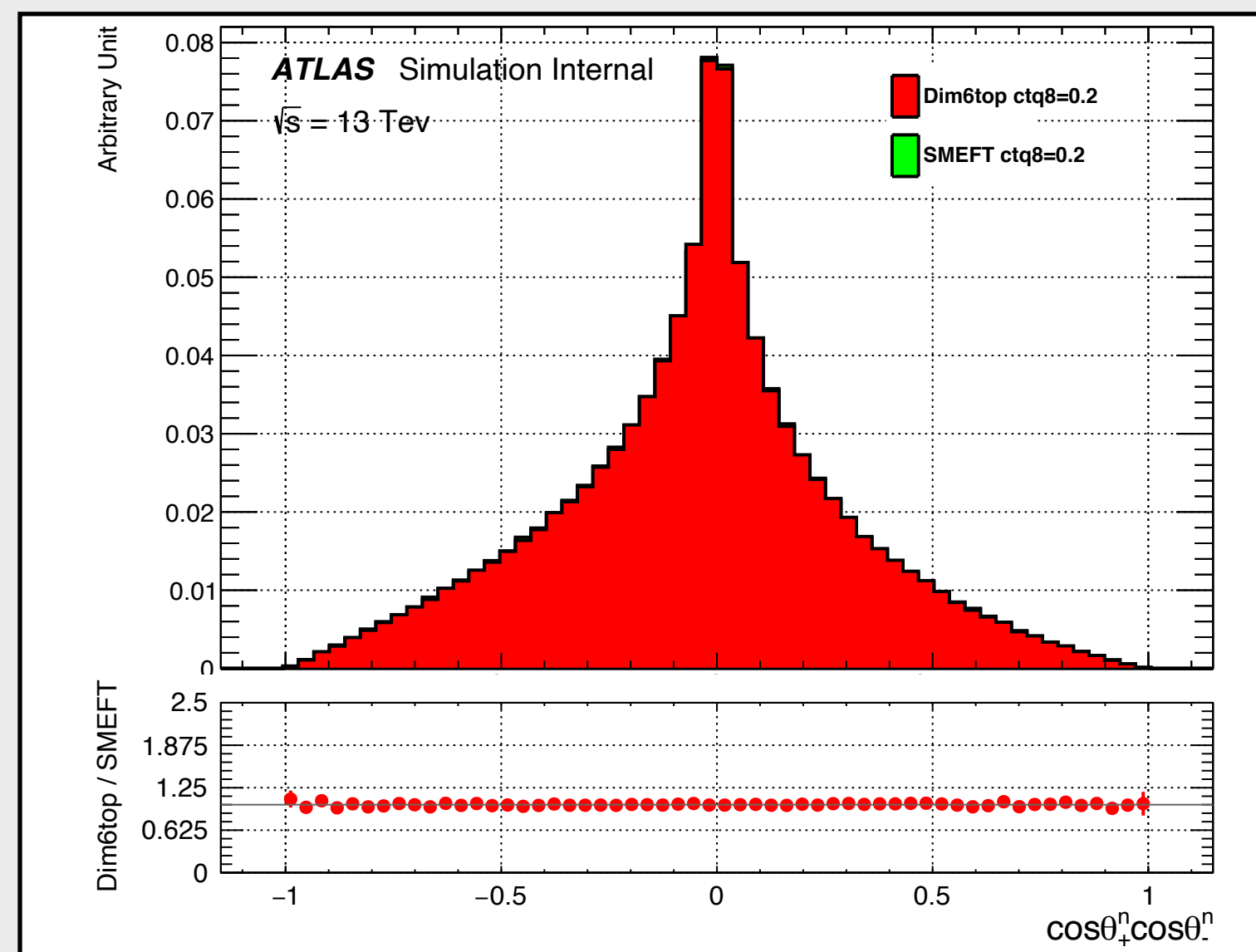
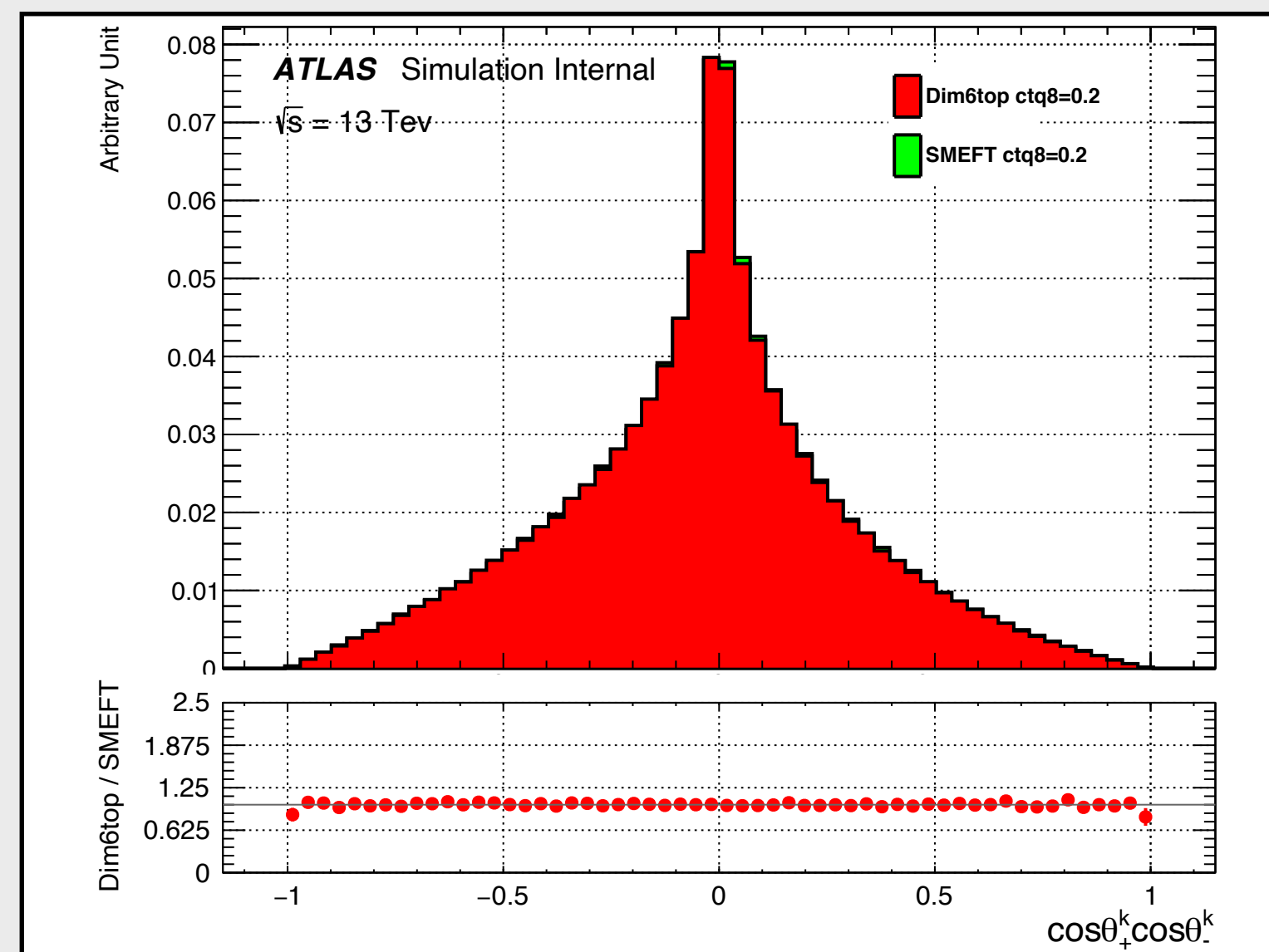
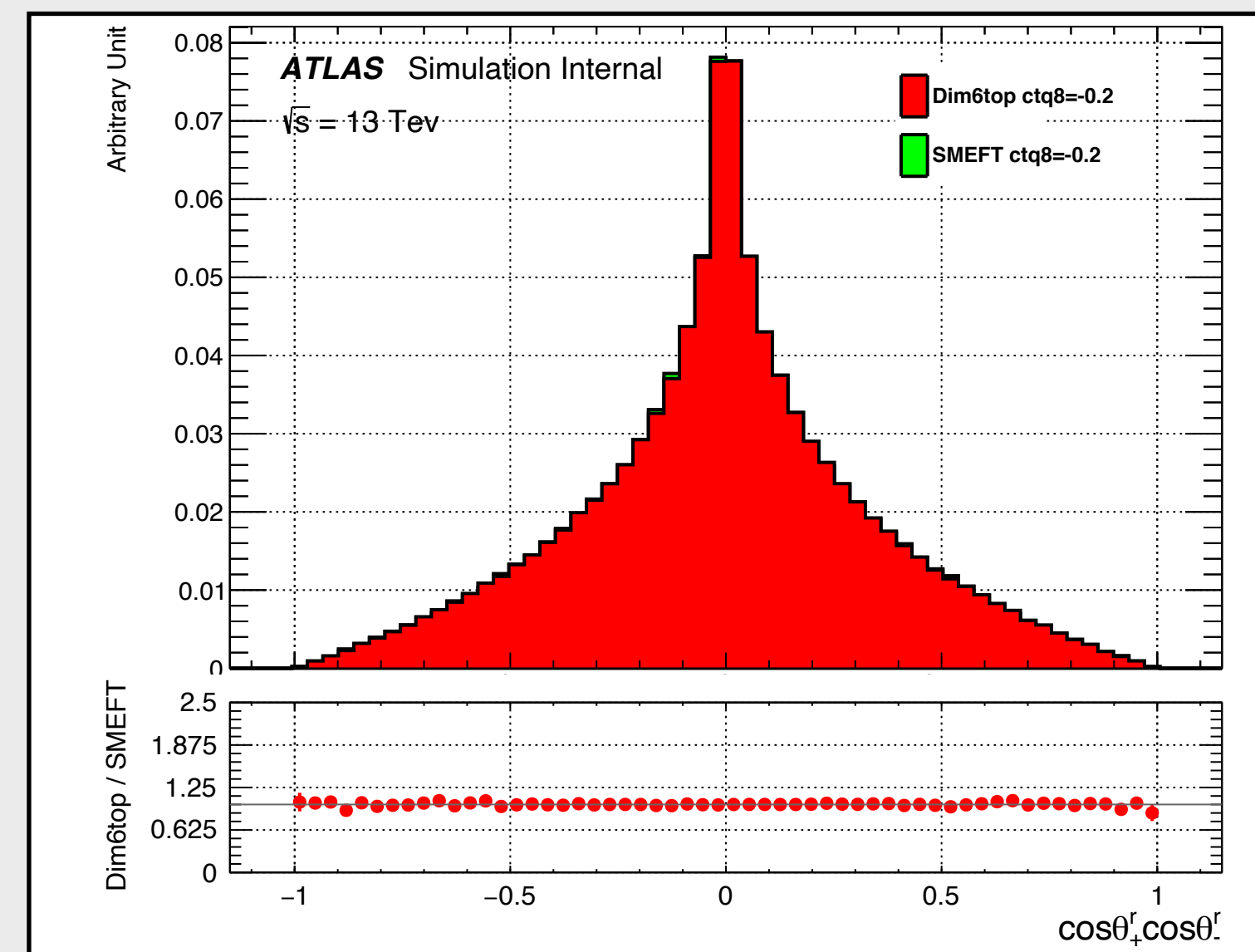
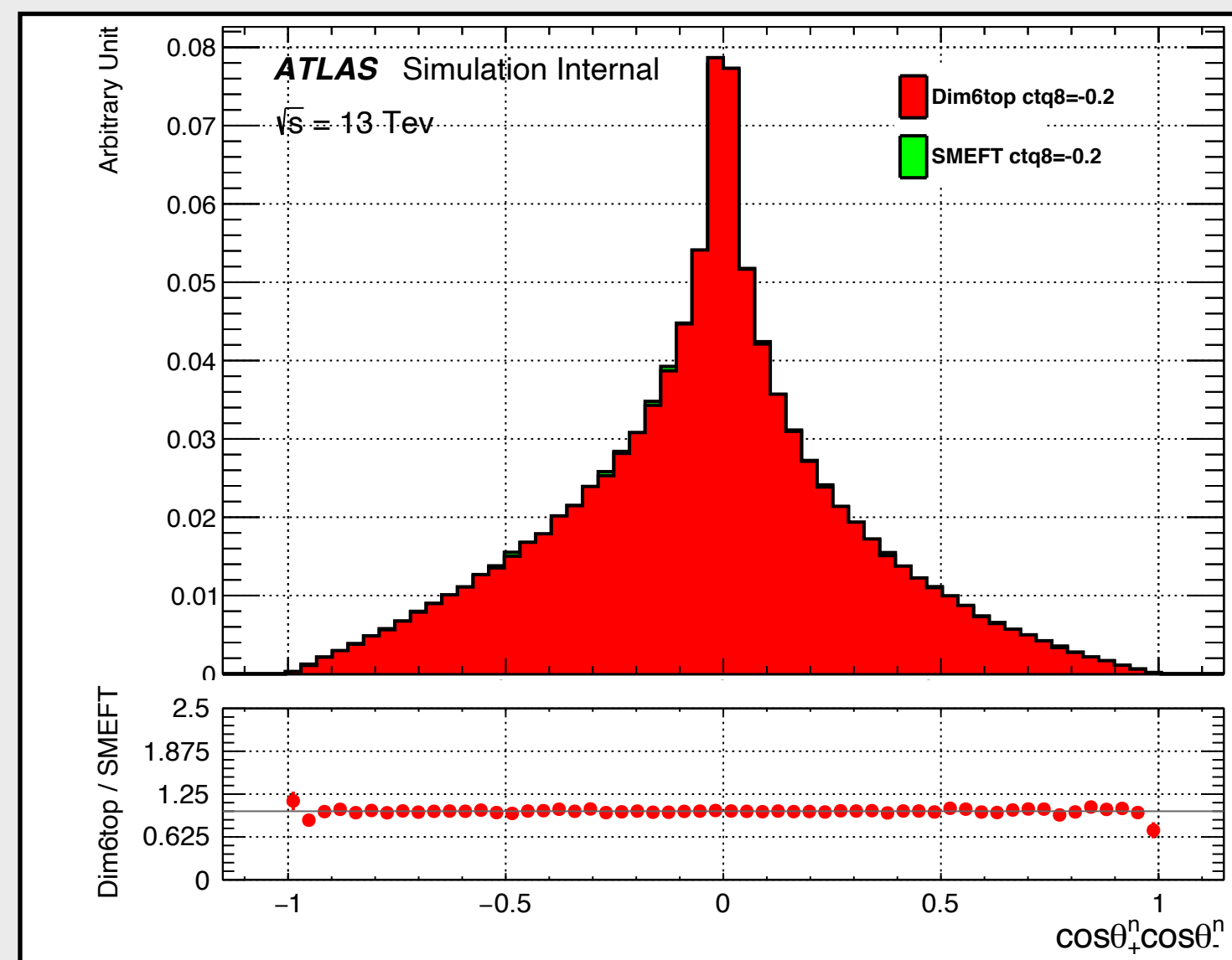
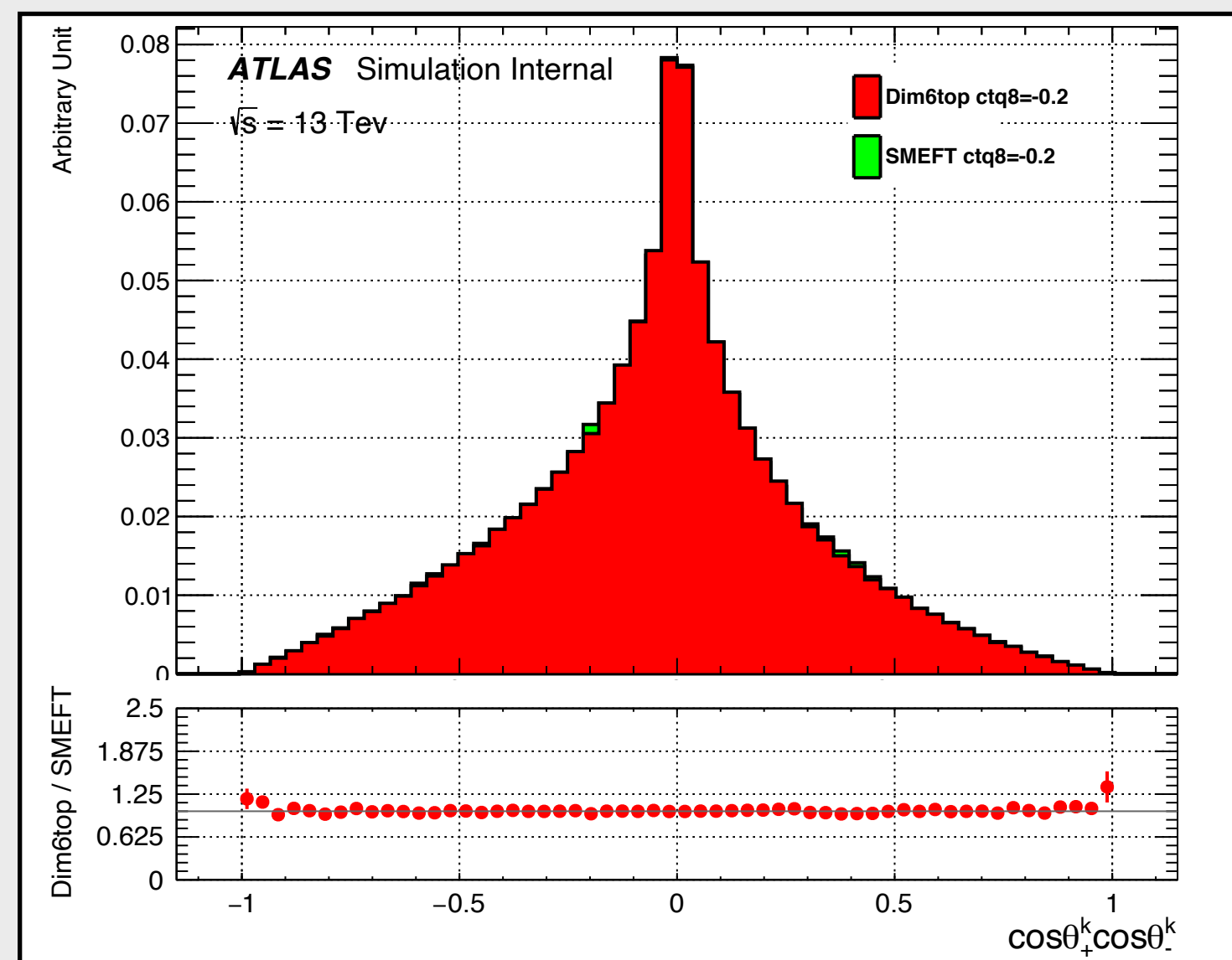


# $\alpha_i/\Lambda^2$ and $\beta_i/\Lambda^4$ at LO : $C(r,r)$



# SM-EFT vs Dim6Top, Ctq8 +/- 0.2

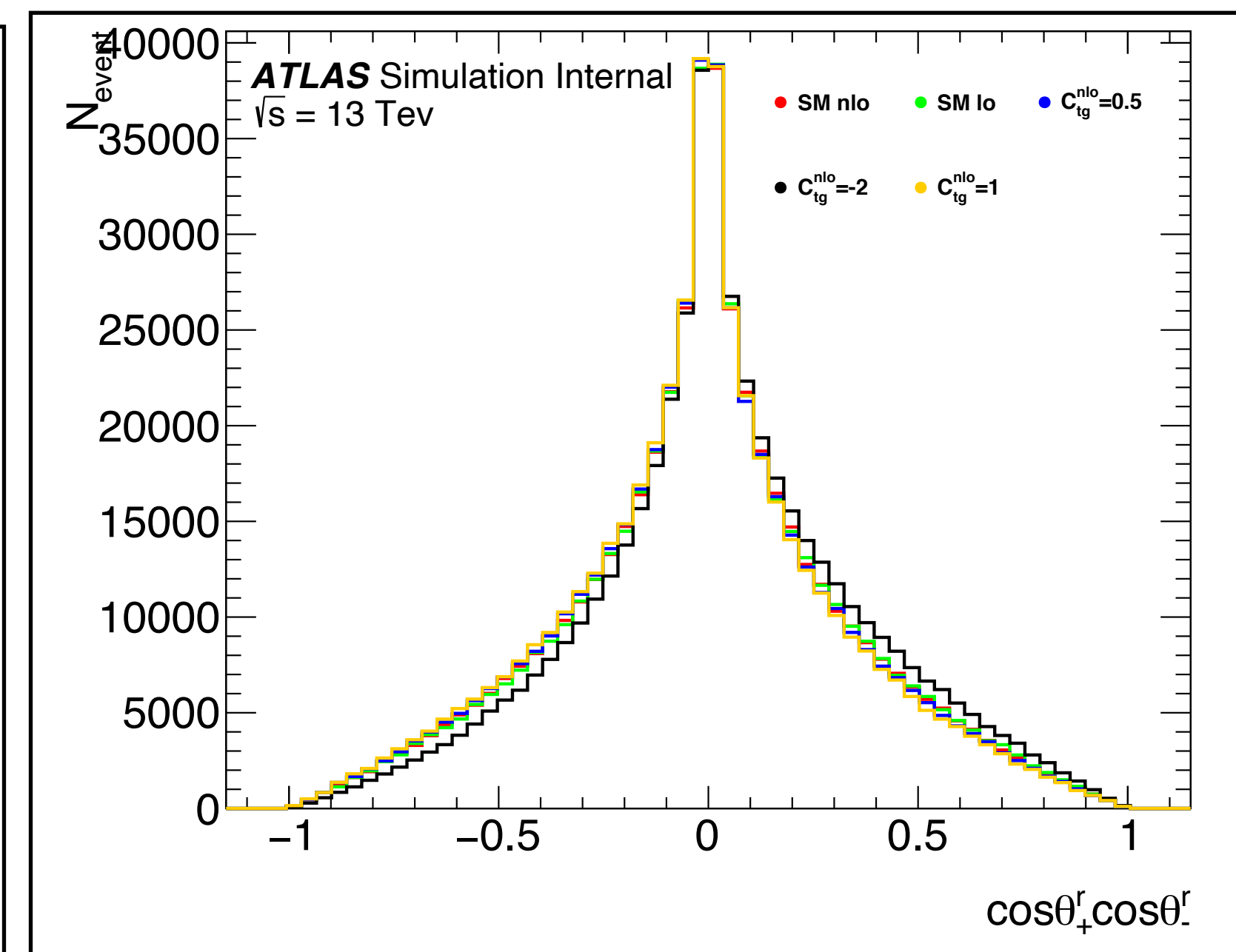
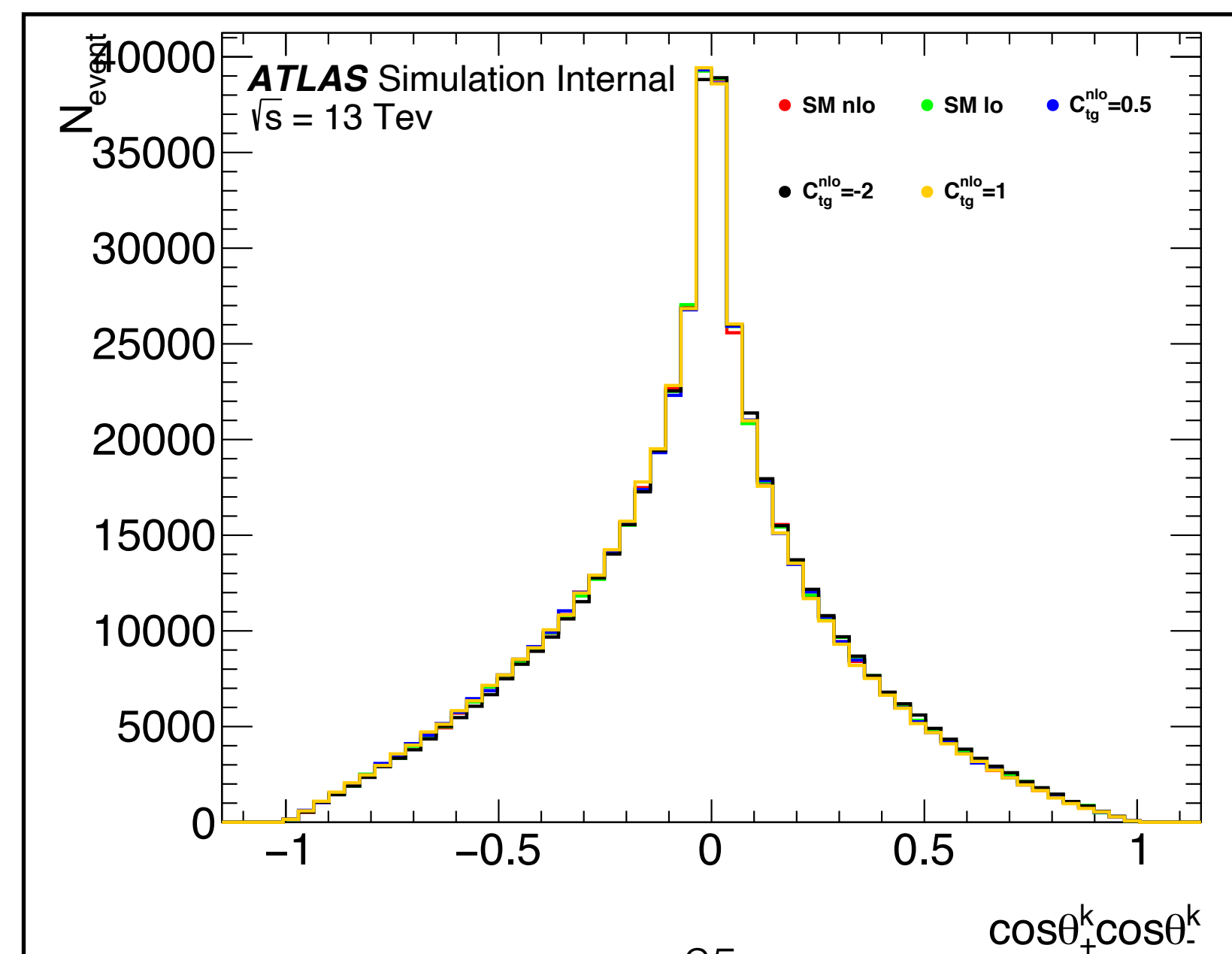
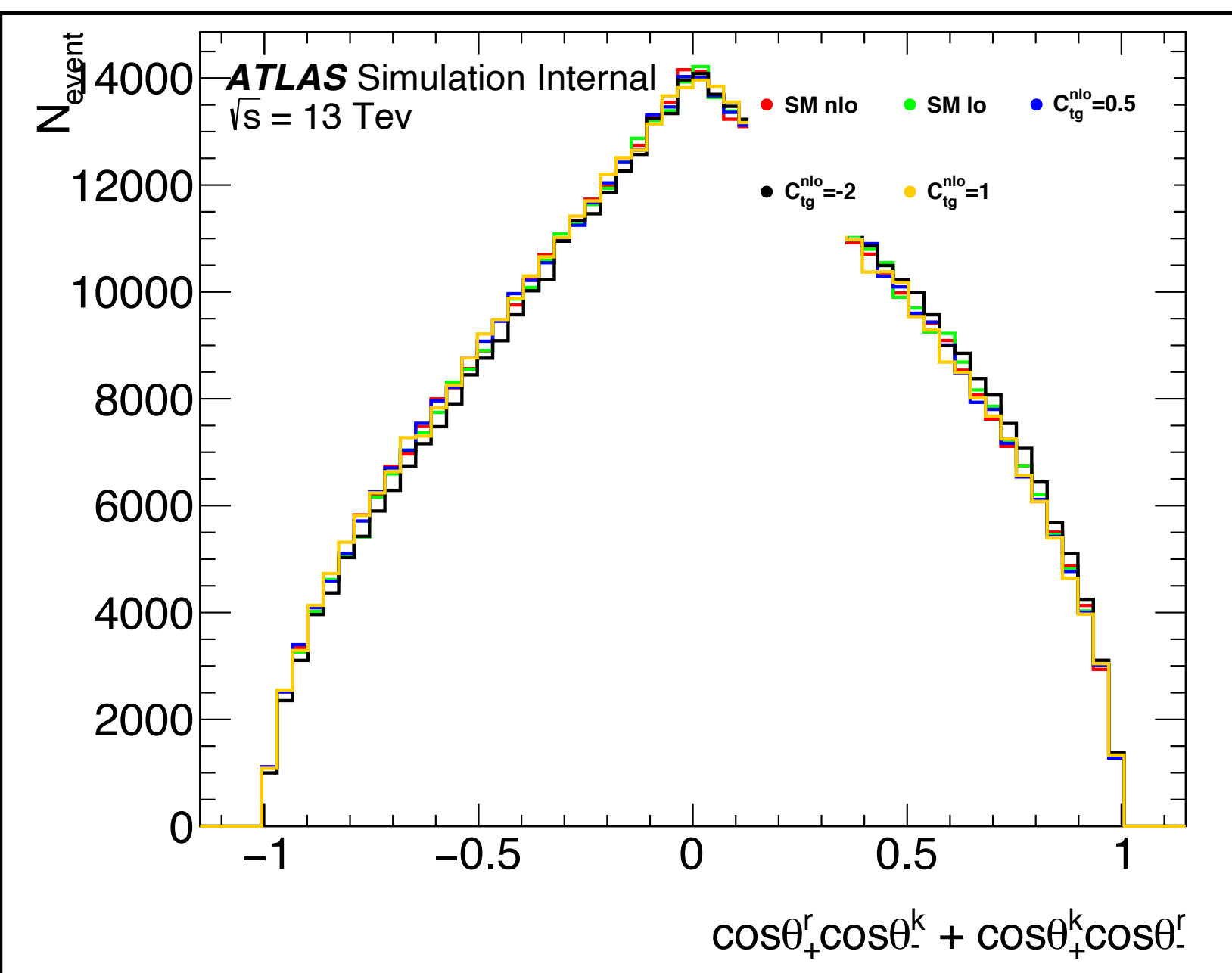
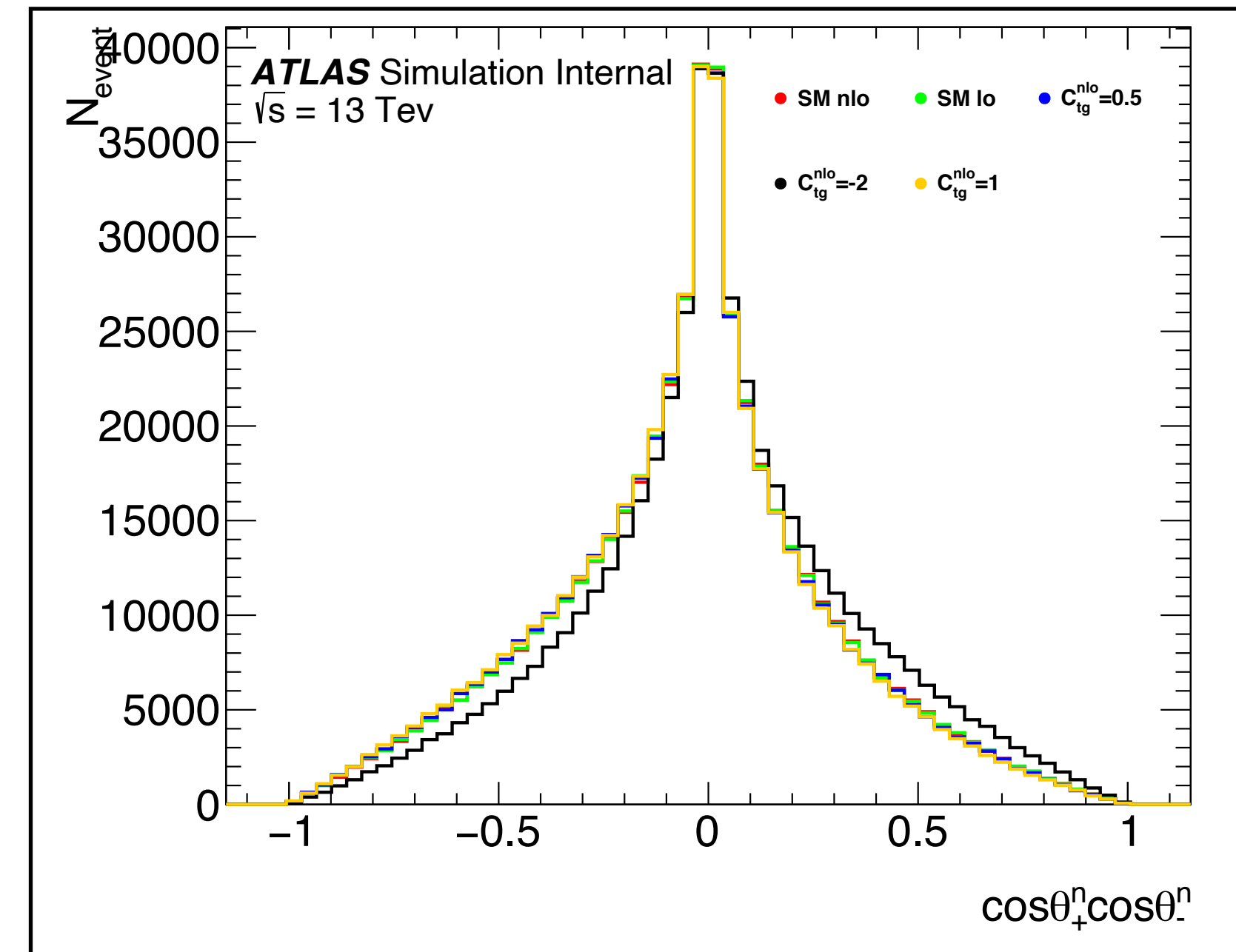
work in progress



# SM NLO/LO, Ctg

## \* Spin correlation :

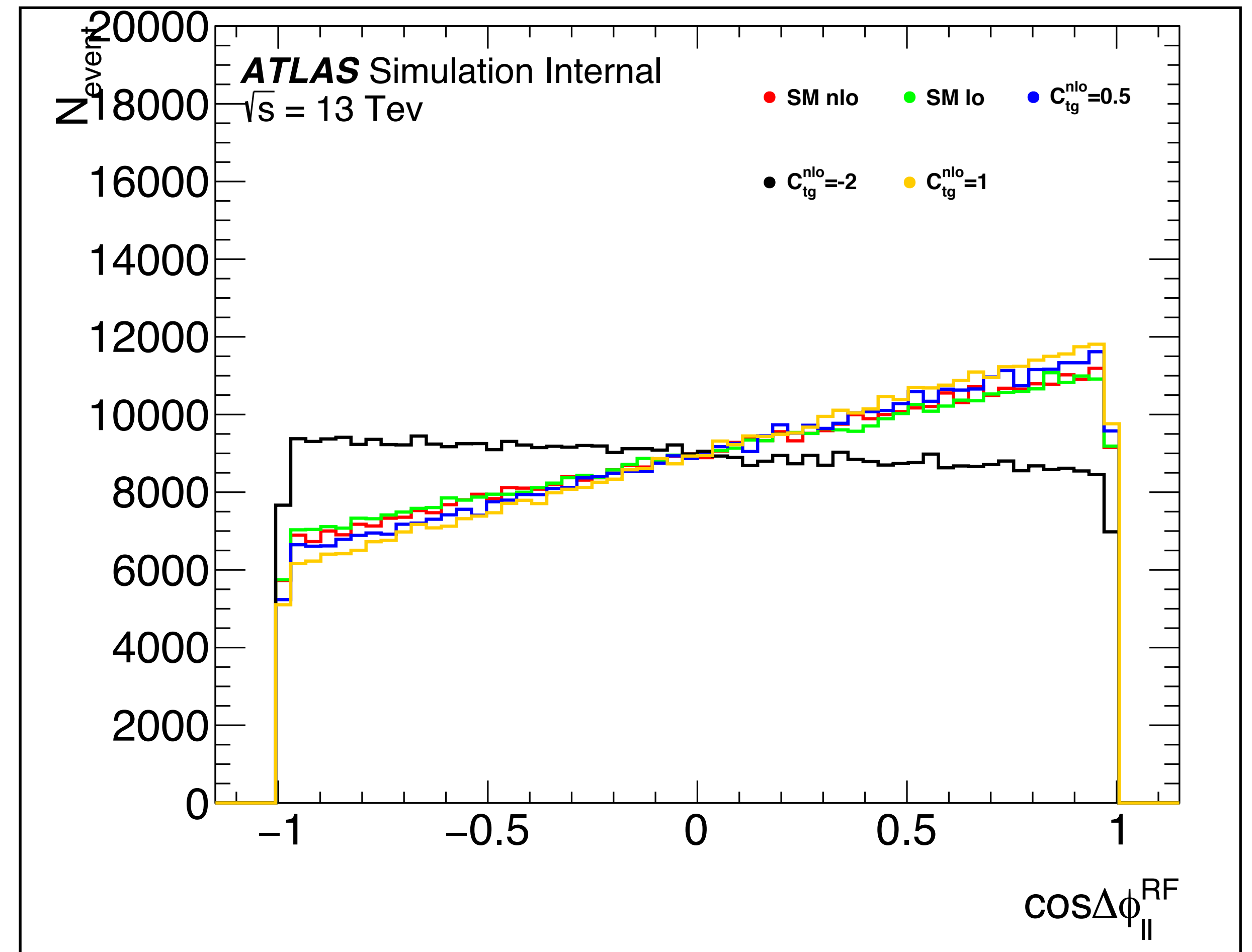
- Are directly affected by Ctg expect Ckk where the impact is small (we will discuss it in details in part 2 also).
- For other spin corrections observables, the effect is very low or not observed.



# SM NLO/LO Ctg

\*  $\cos\Delta\phi_{ll}^{RF}$  :

📌 For  $C_{tg}=-2$ , the distribution is  $\sim$  flat !!!





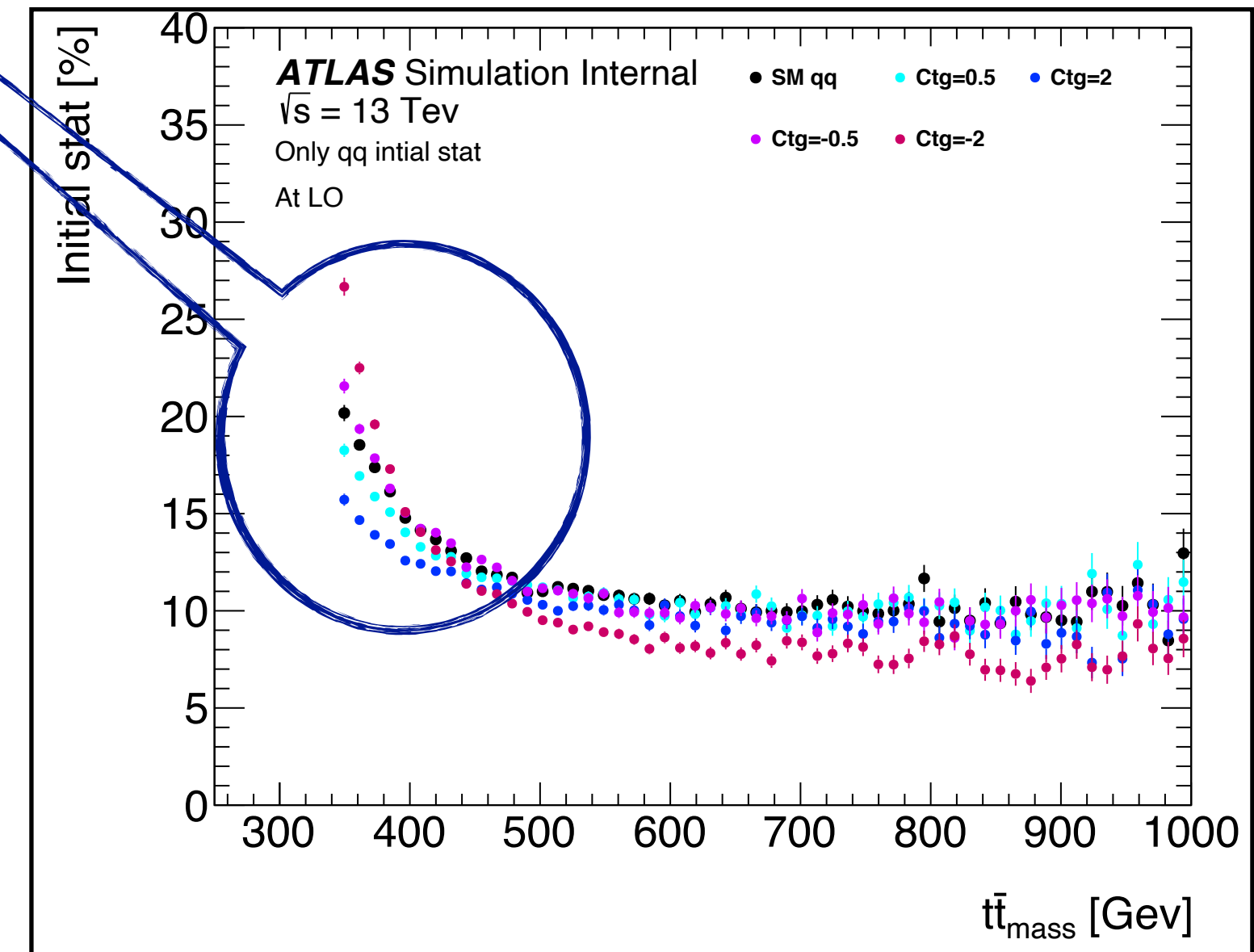
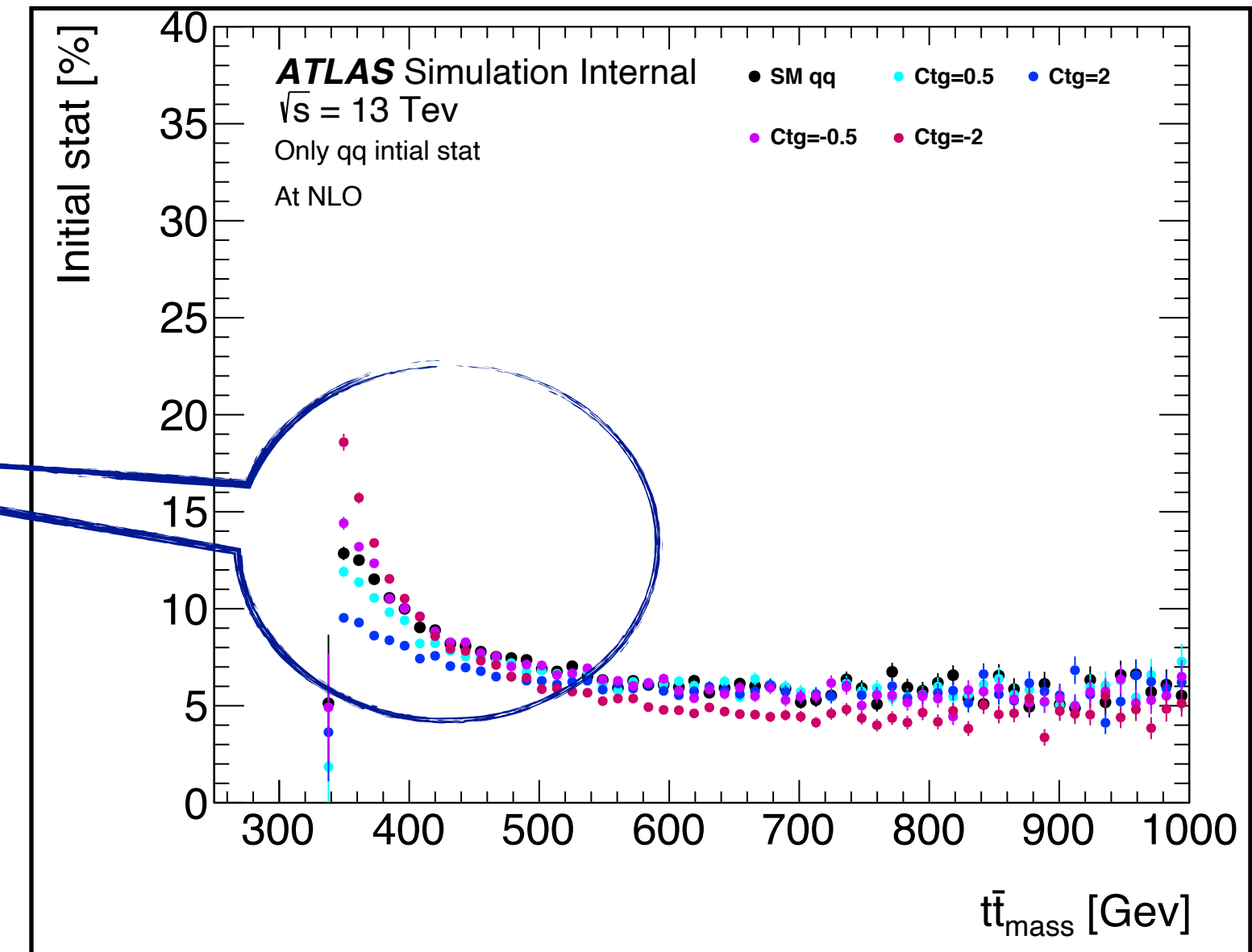
# Initial stat qq VS Ctg $M_{t\bar{t}}$

## ✱ Near Threshold

- ☑ Fraction of gg is effected by Ctg = +/- 2 (also +/- 1, 1,5)

## ✱ Above Threshold:

- ☑ Fraction of gg is stable w.r.t Ctg values !



# Initial stat qg VS Ctg $M_{t\bar{t}}$

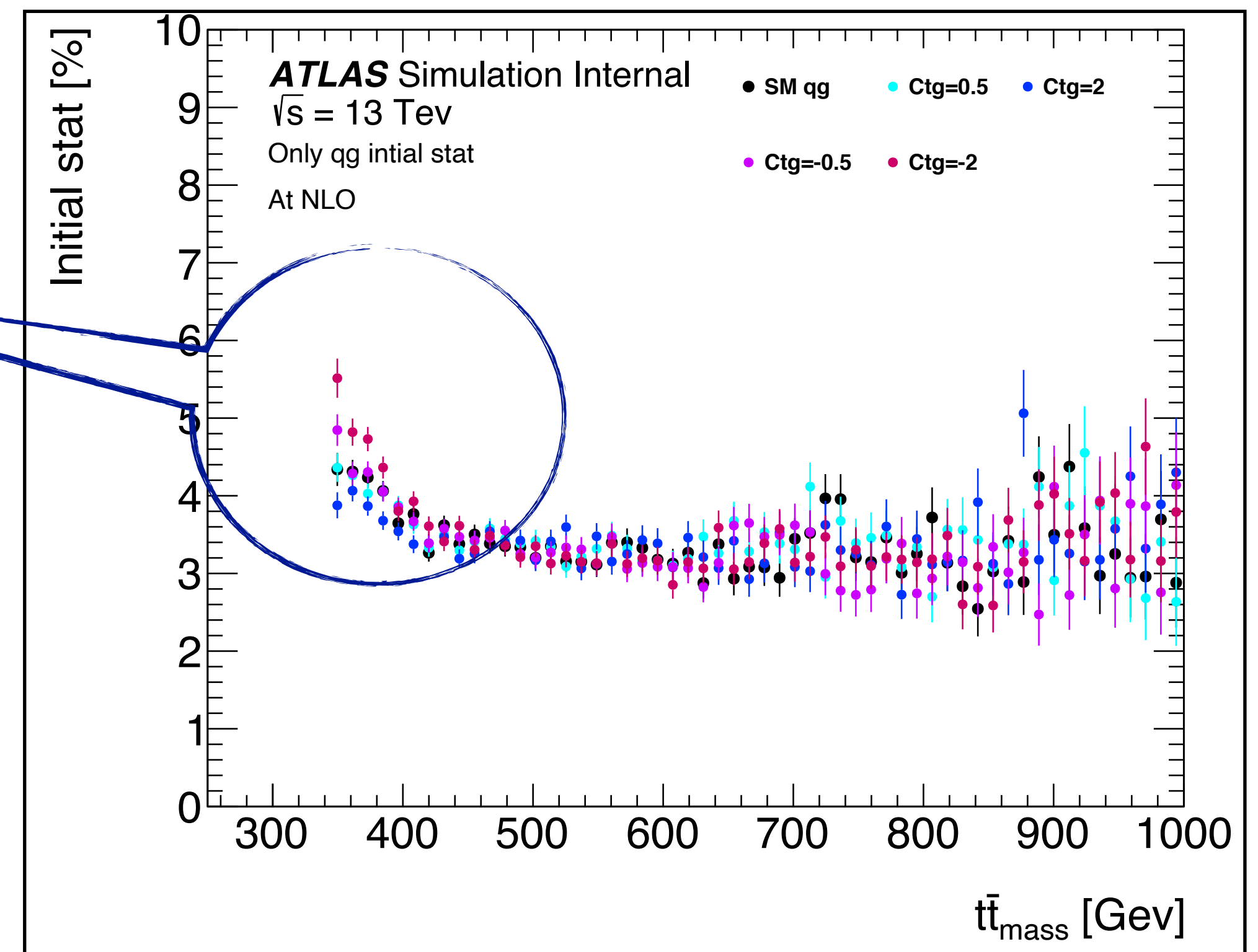
## ✱ Near Threshold

- ☑ Fraction of gg is effected by Ctg  
= +/- 2 (also +/- 1, 1,5)

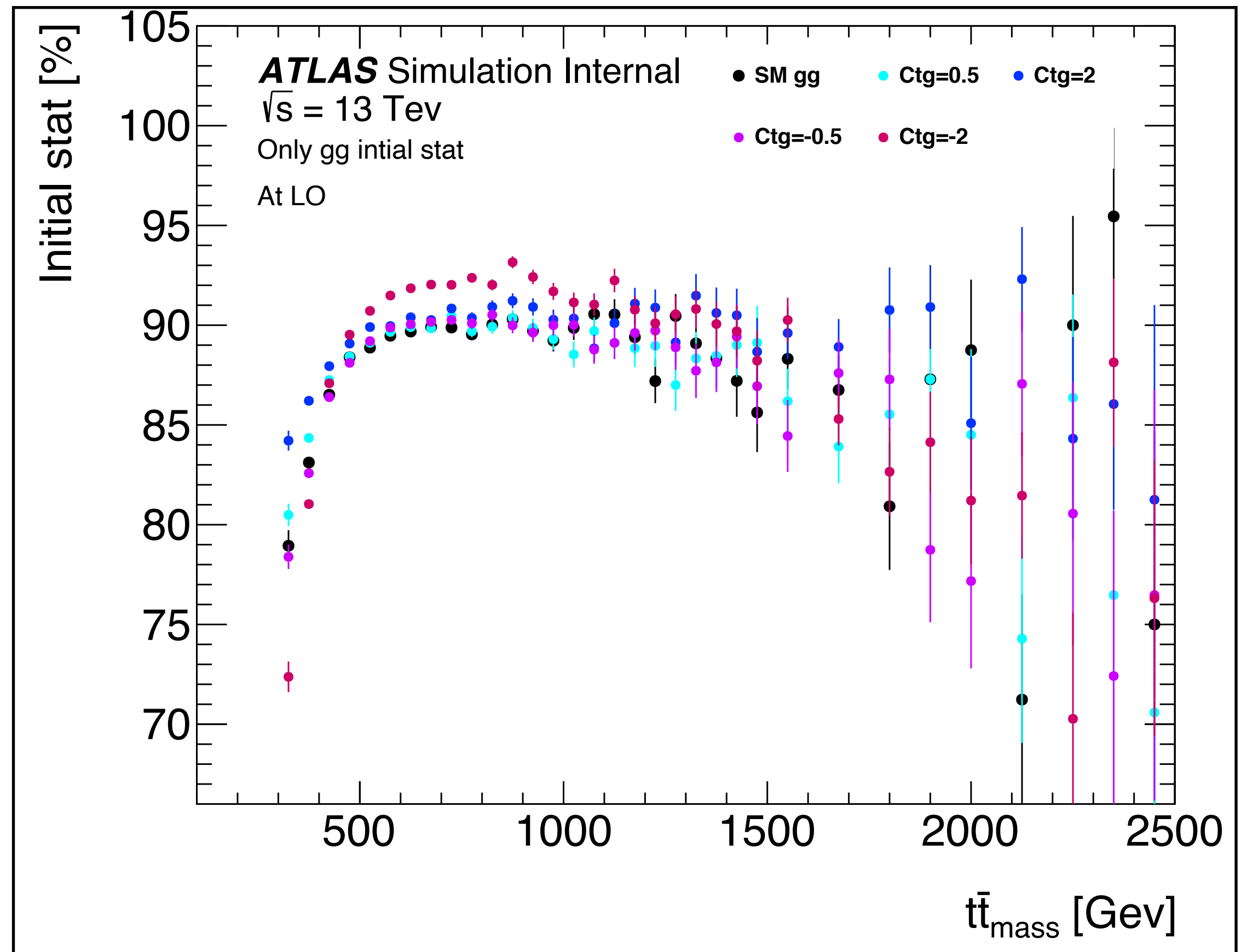
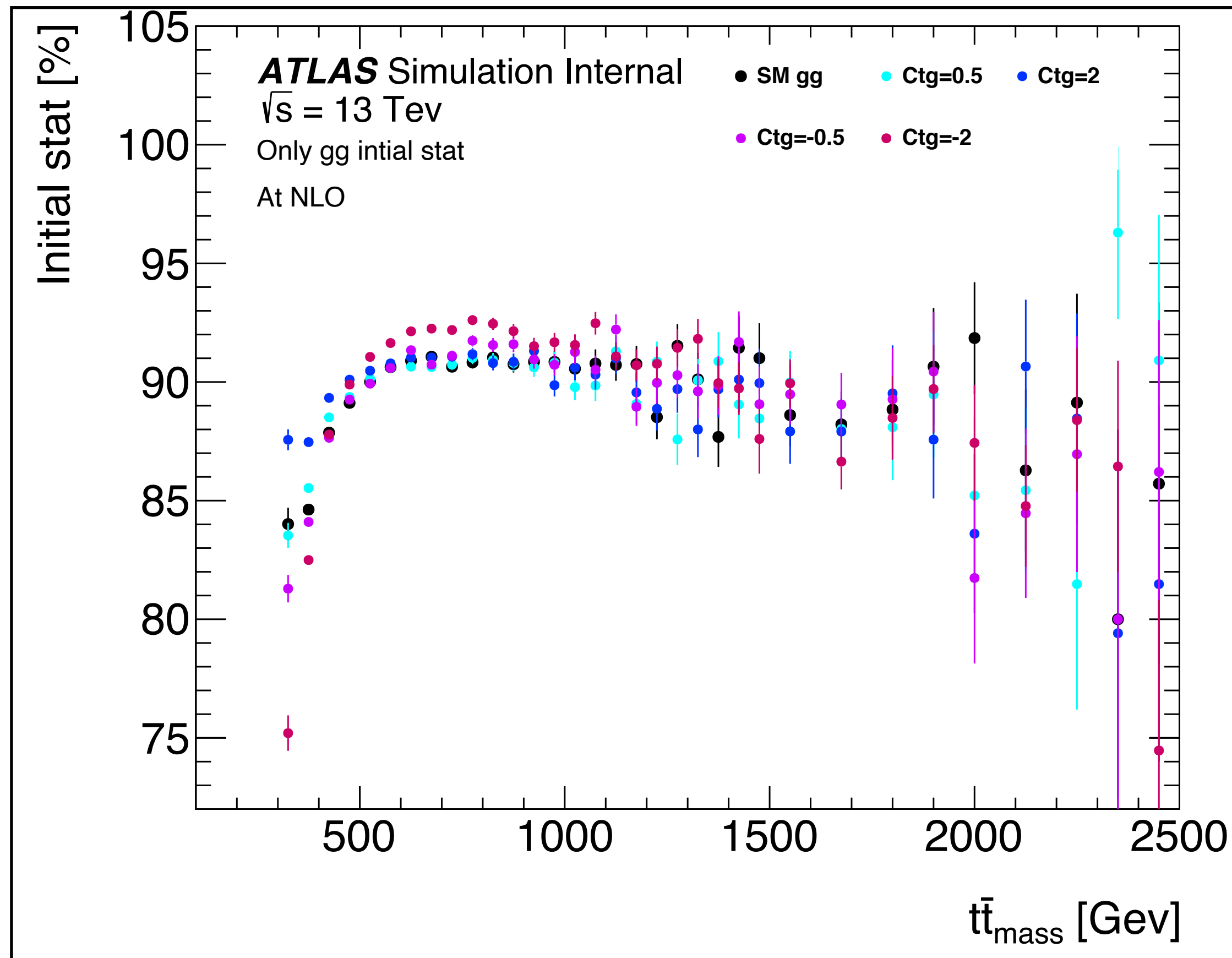
## ✱ Above Threshold:

- ☑ Fraction of gg is stable w.r.t Ctg values !

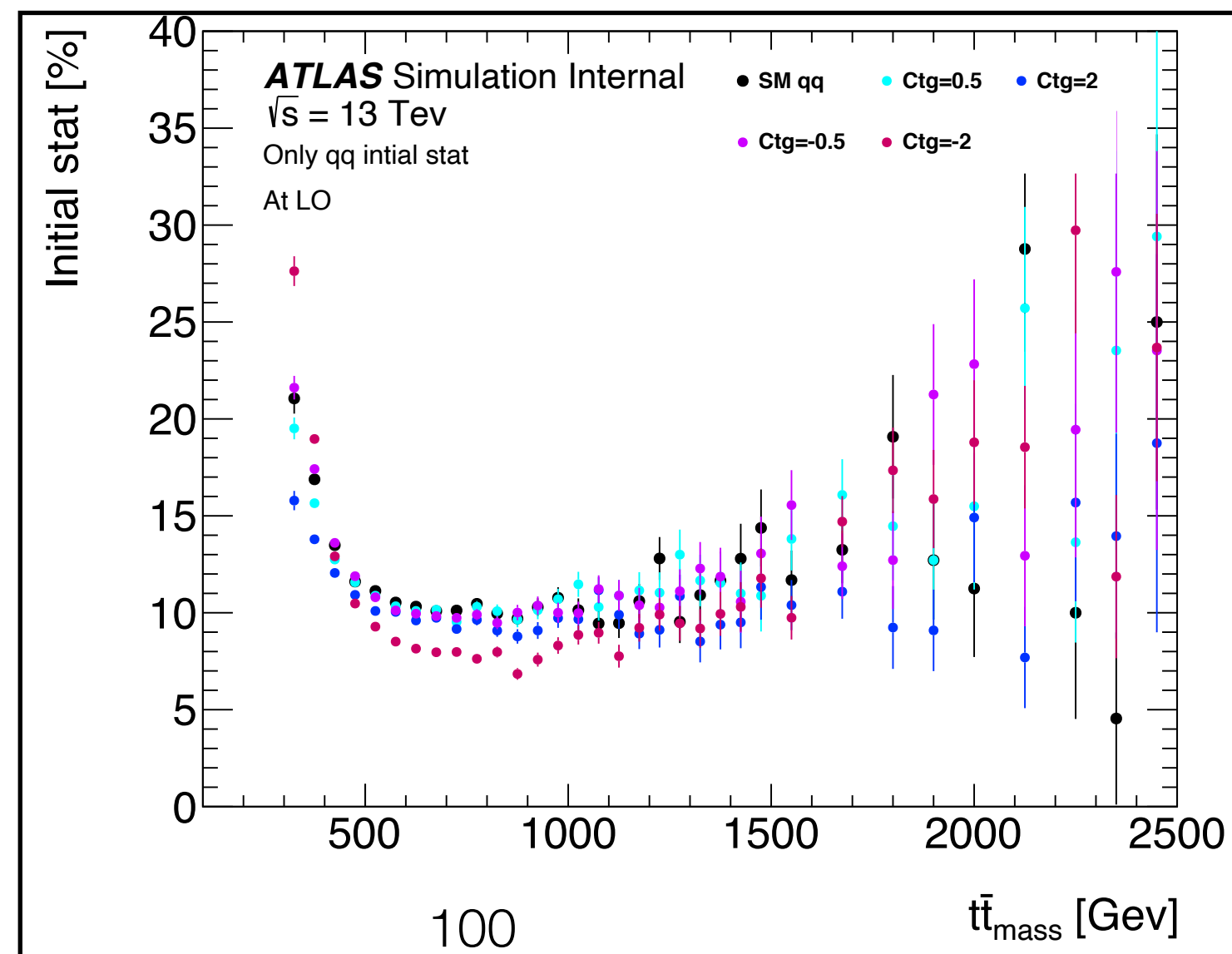
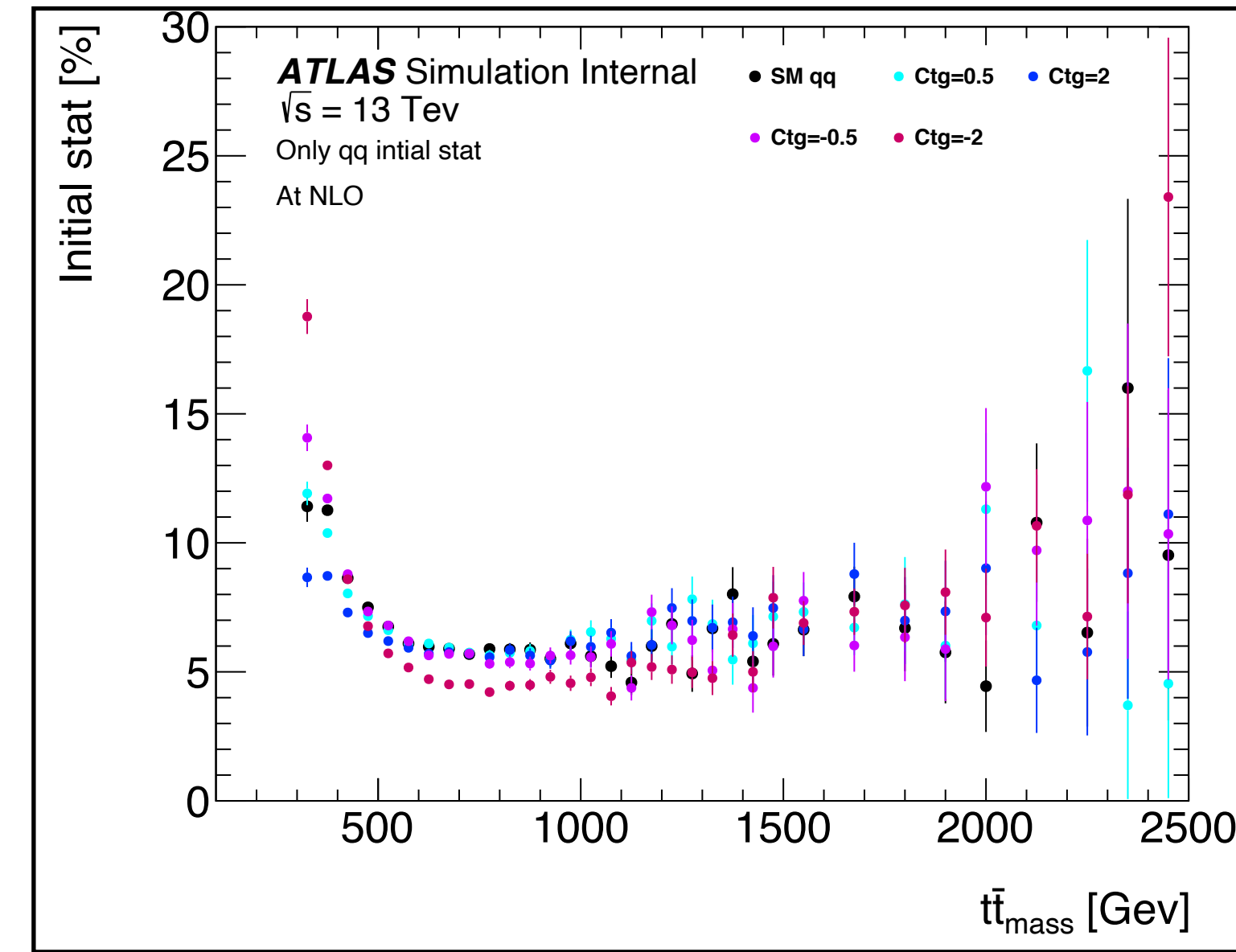
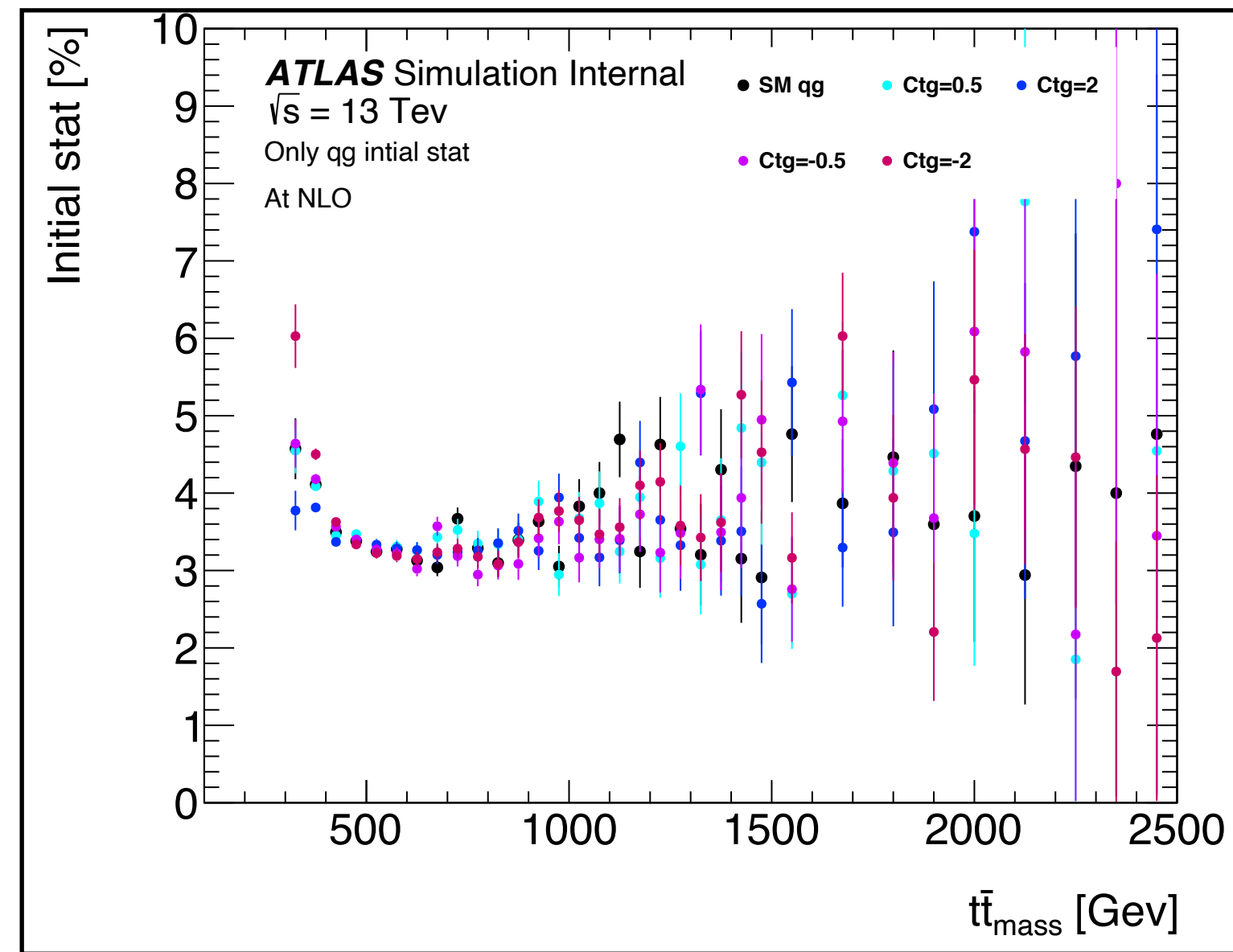
## ✱ Same comments for qq and qg (for NLO) ==> See BackUp.



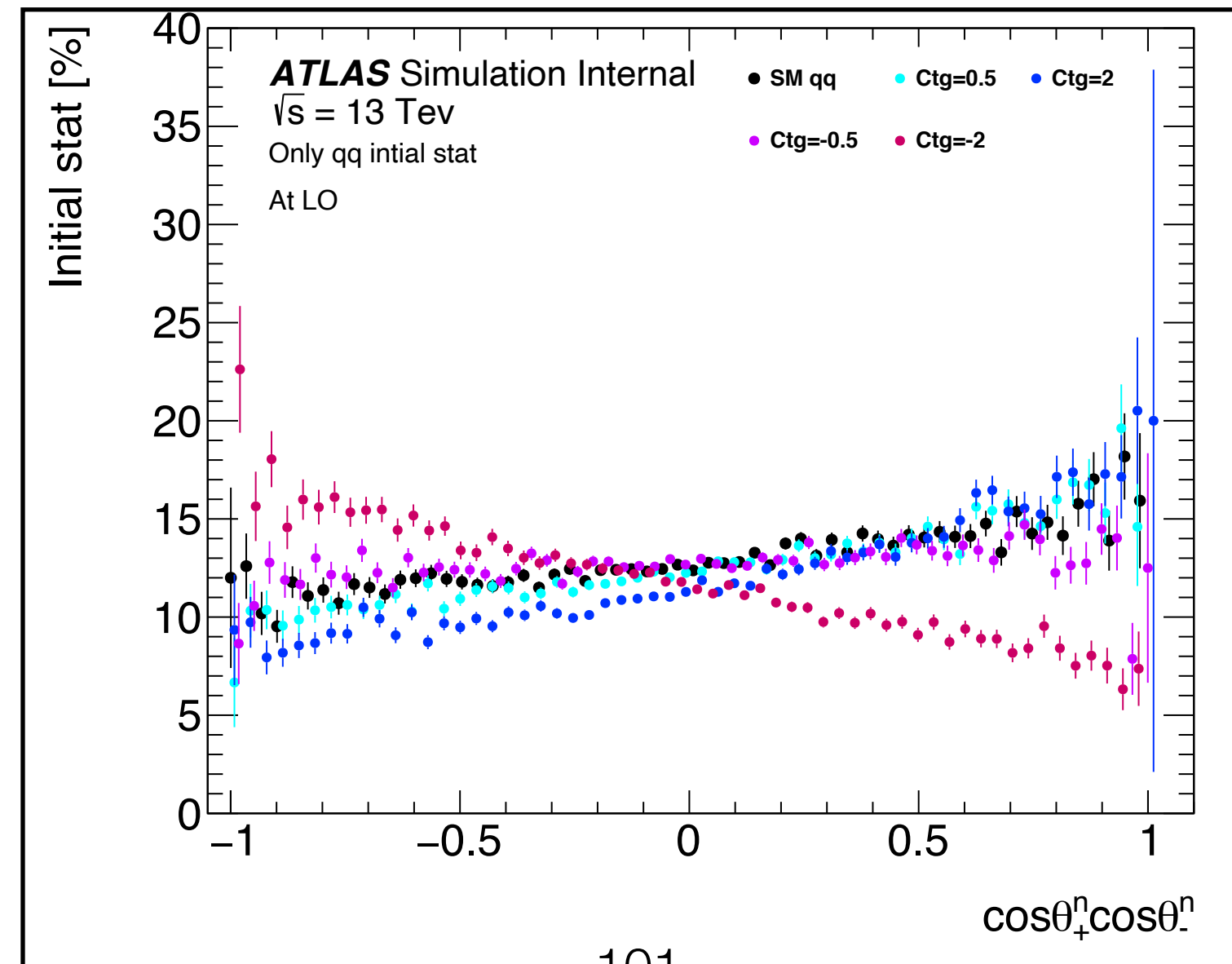
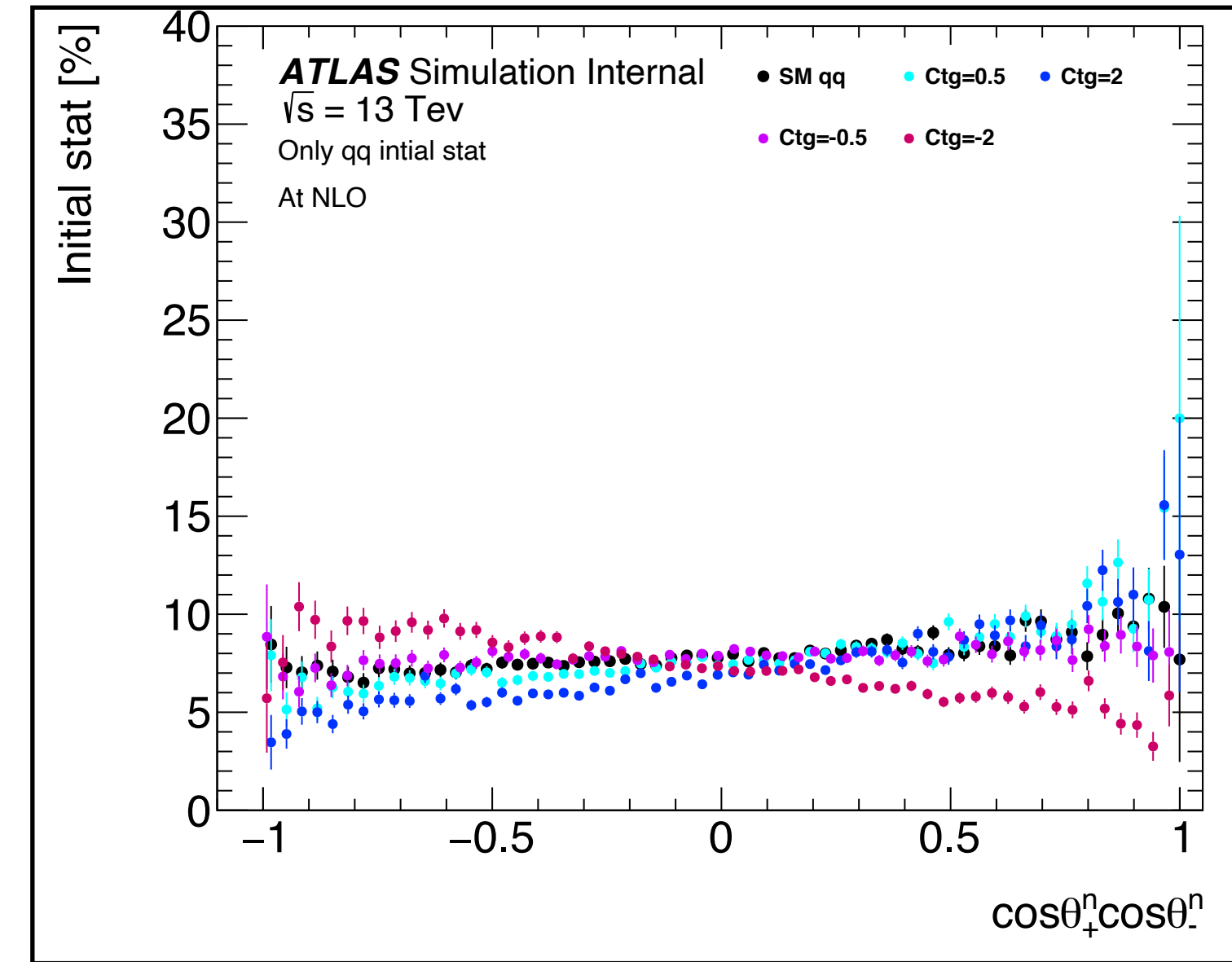
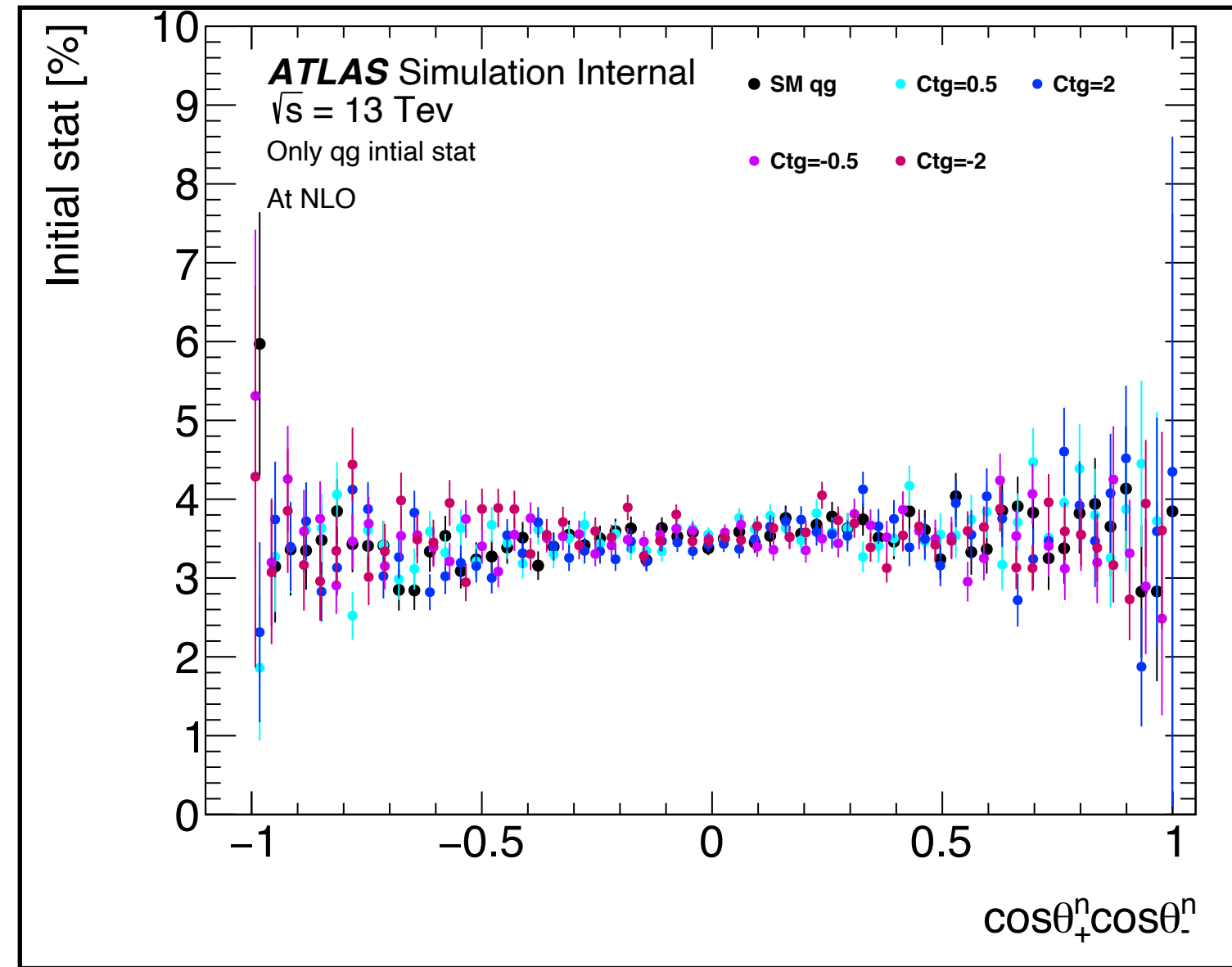
# gg initial stat VS $t\bar{t}$ mass



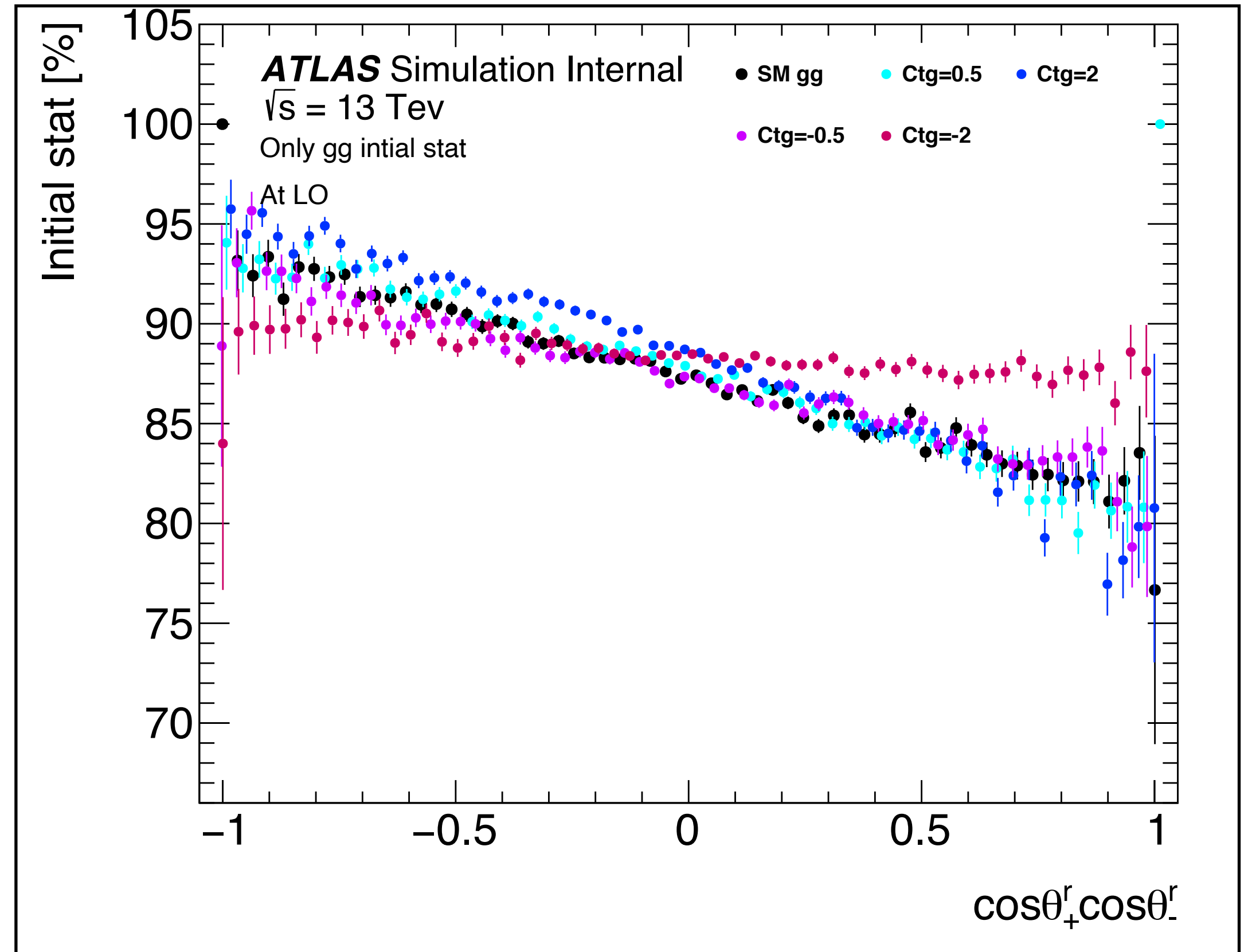
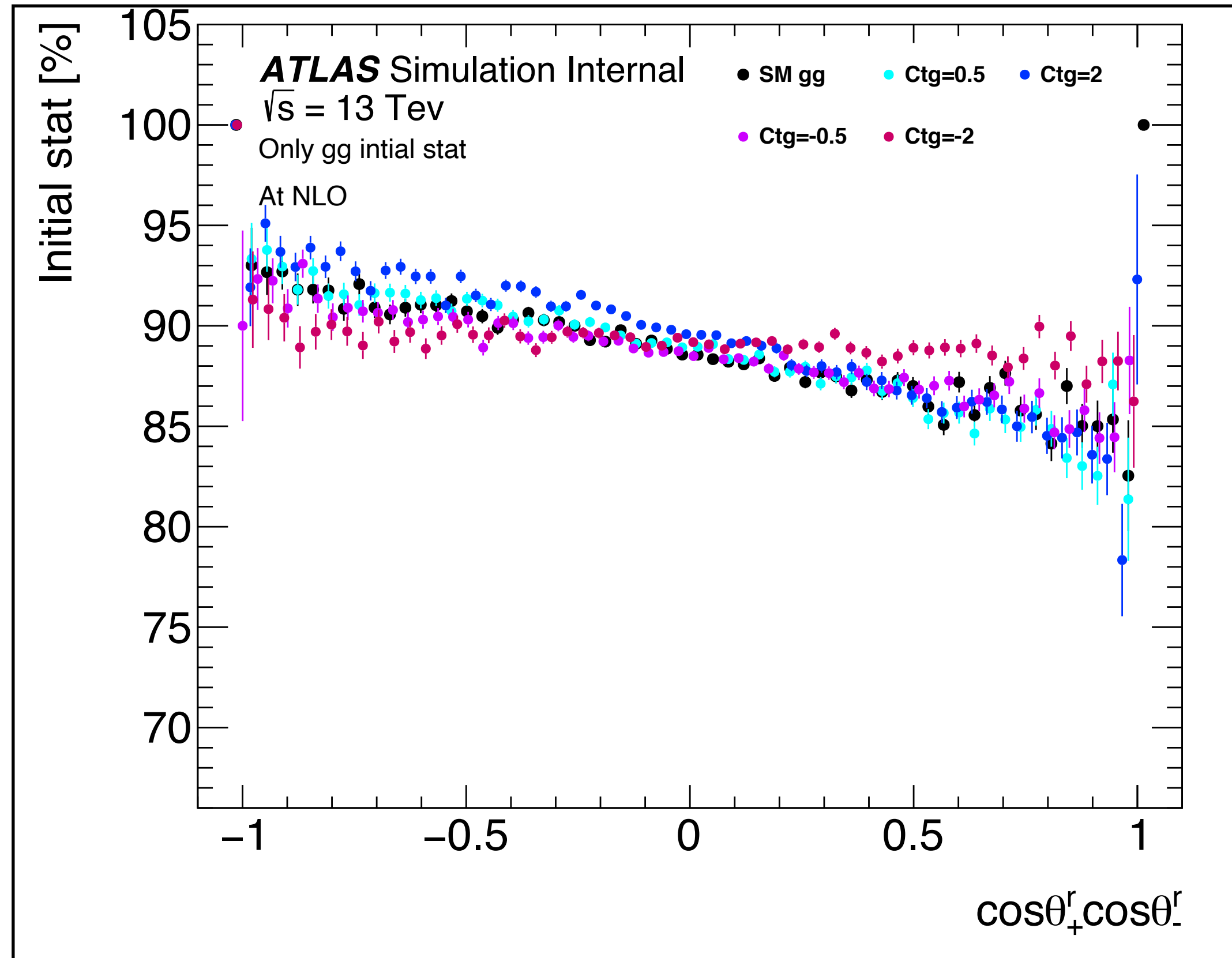
# qq/qg initial stat VS $t\bar{t}$ mass



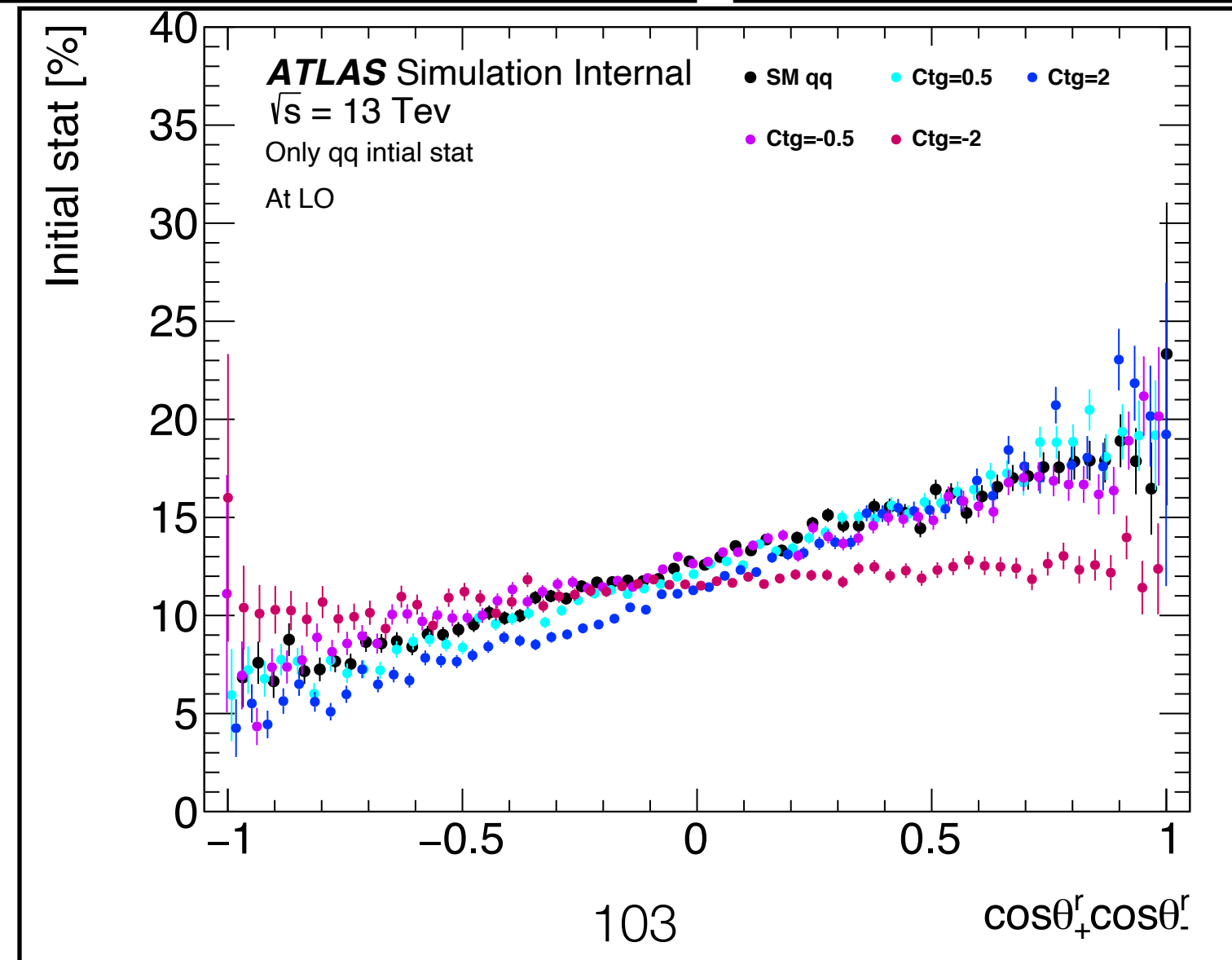
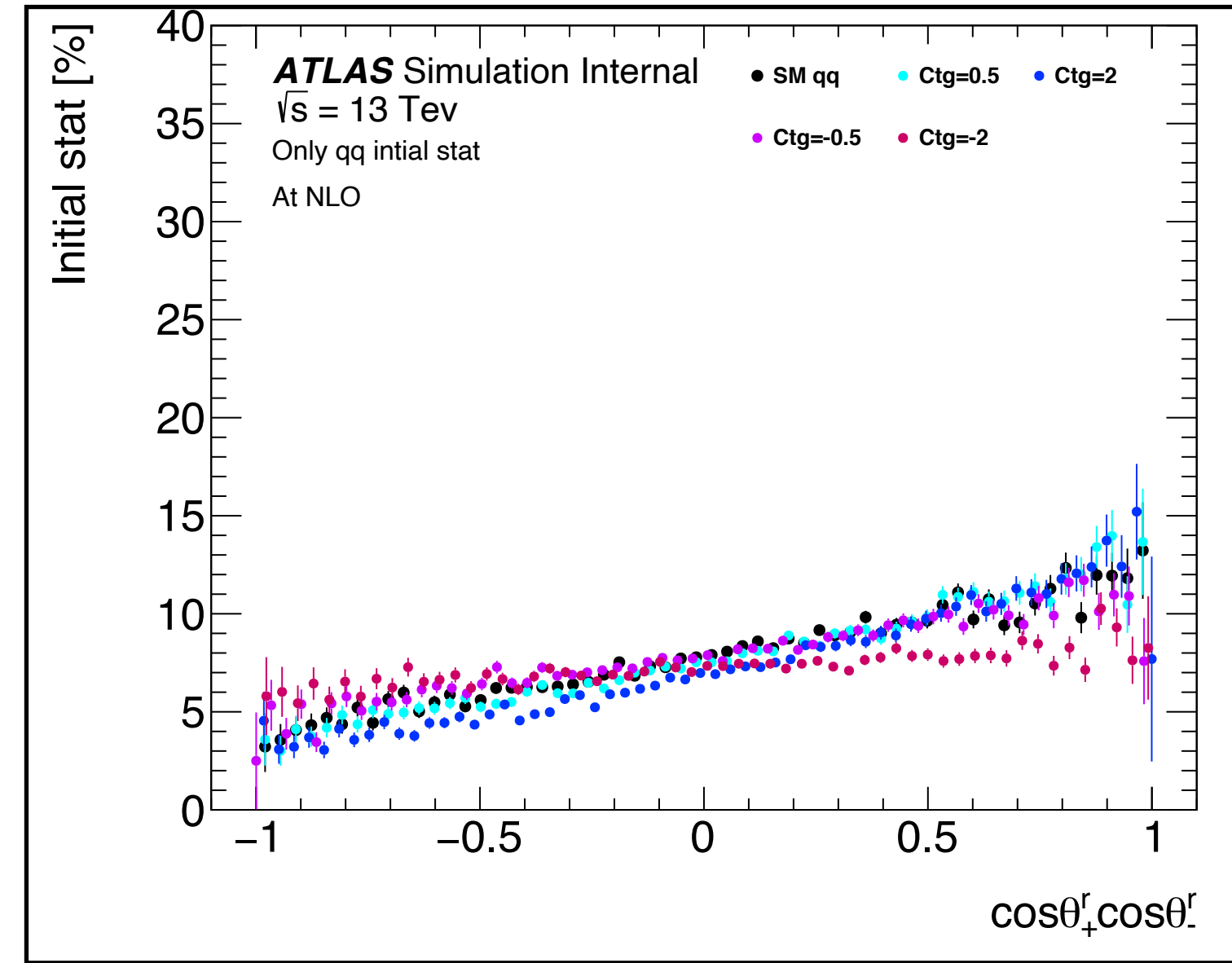
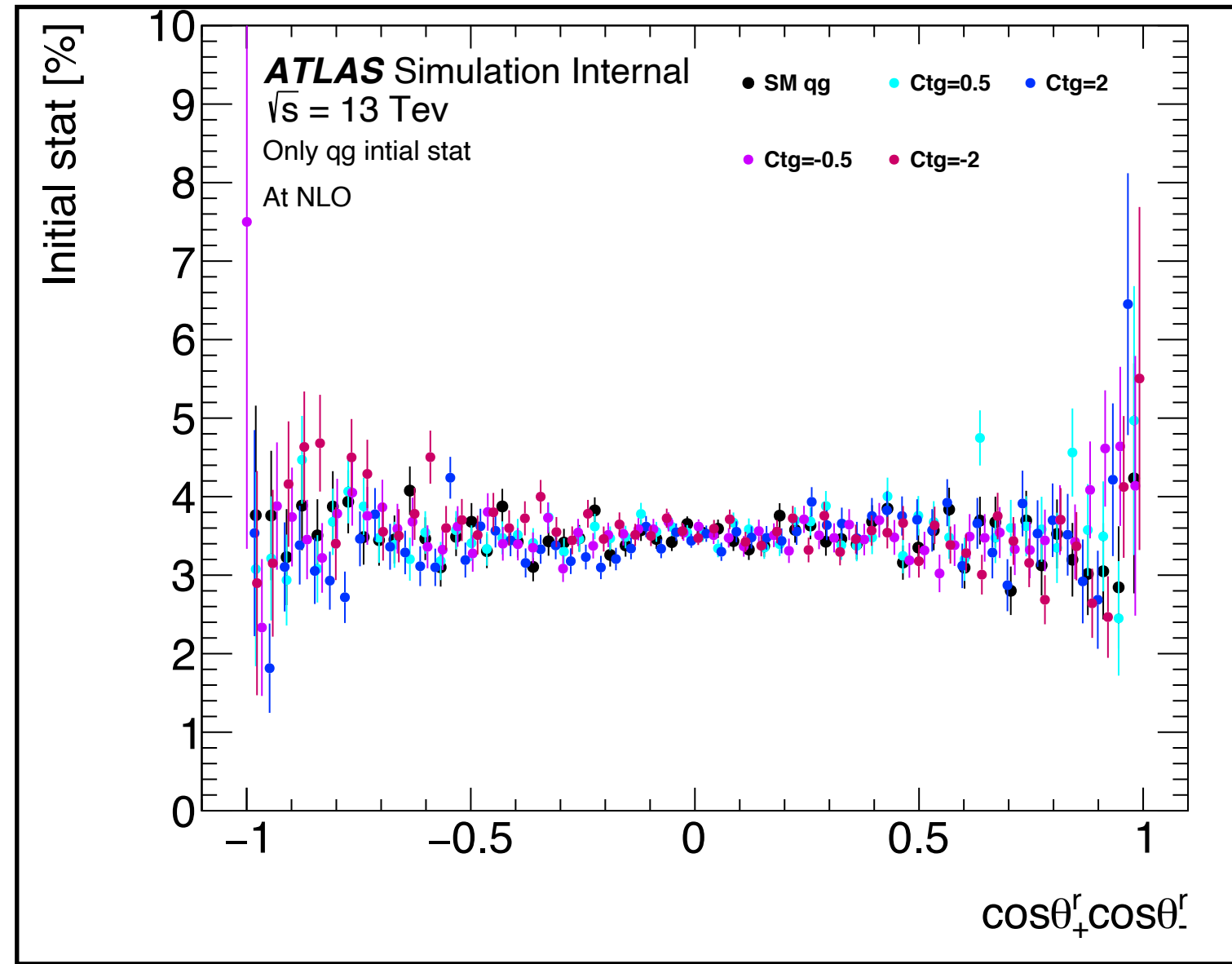
# qq/qg Initial stat VS C(n,n)



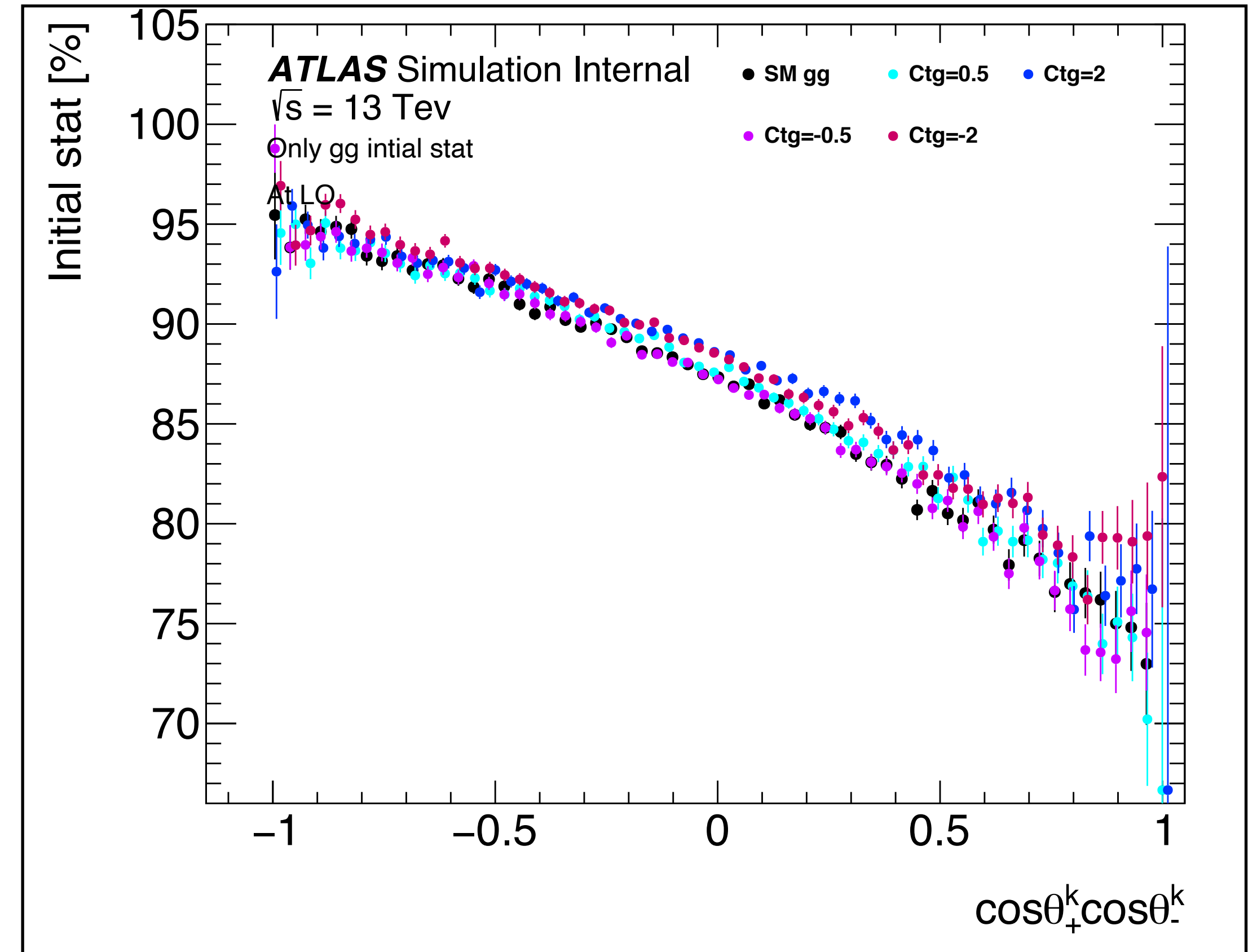
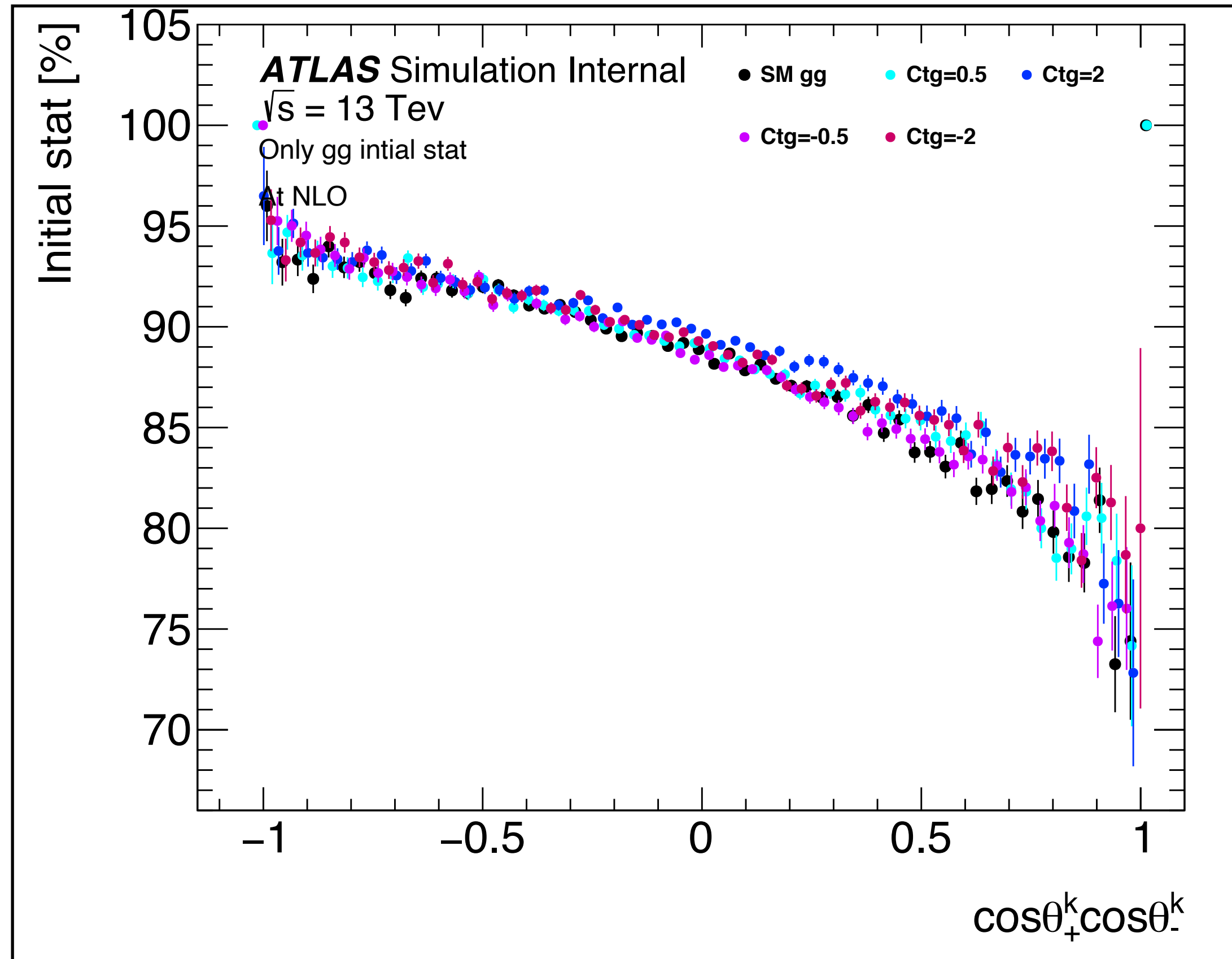
# gg Initial stat VS C(r,r)



# qq/qg Initial stat VS $C(r,r)$

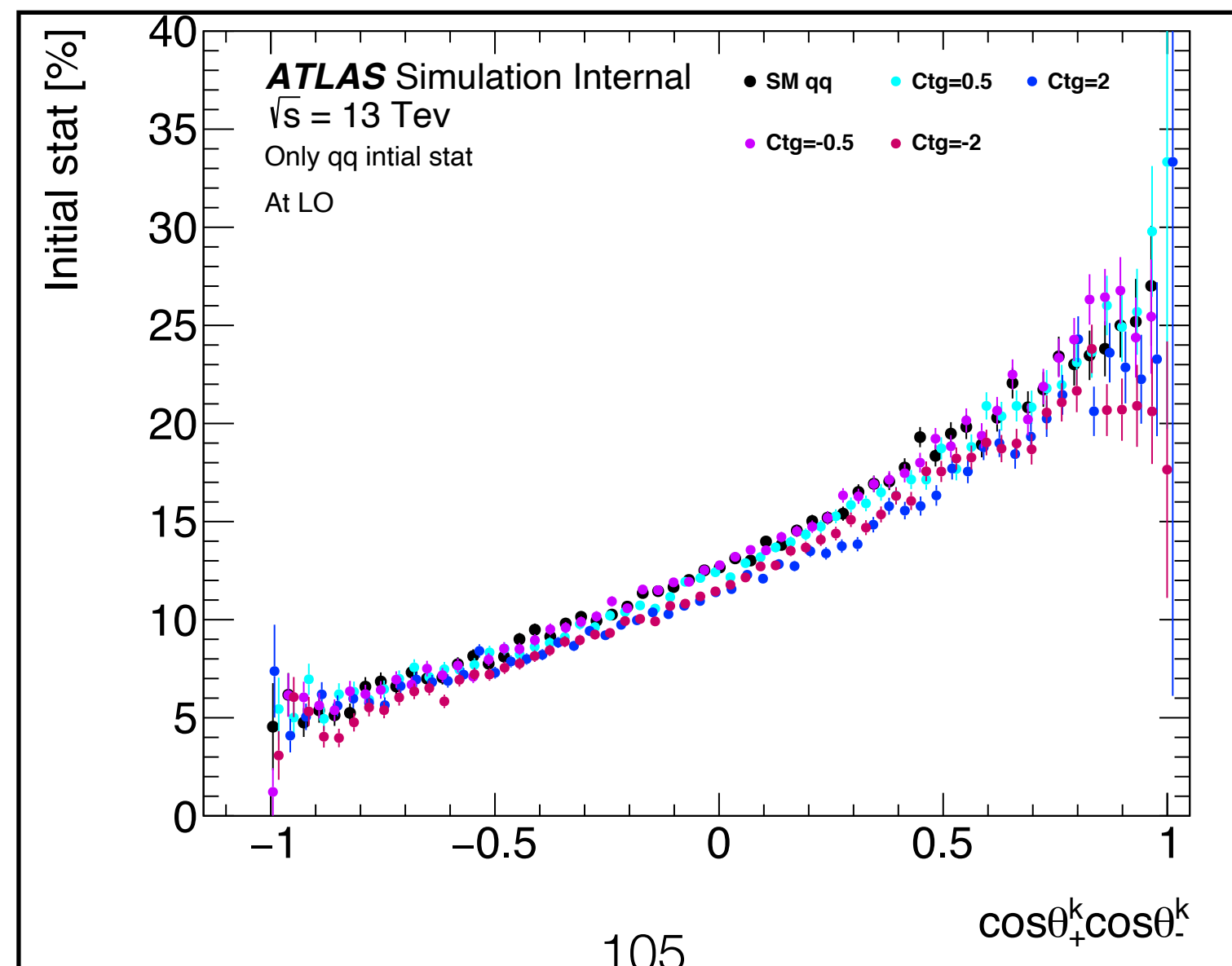
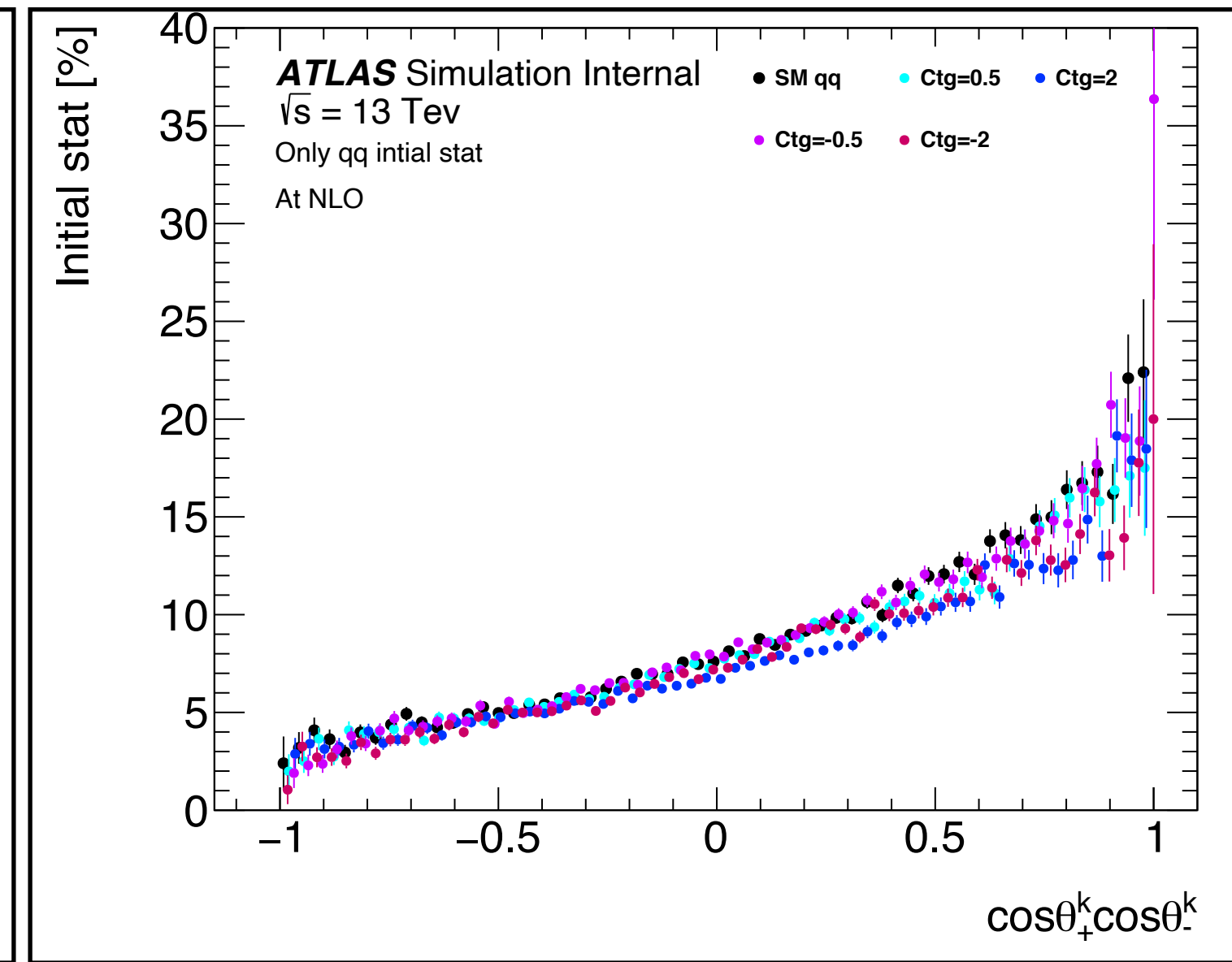
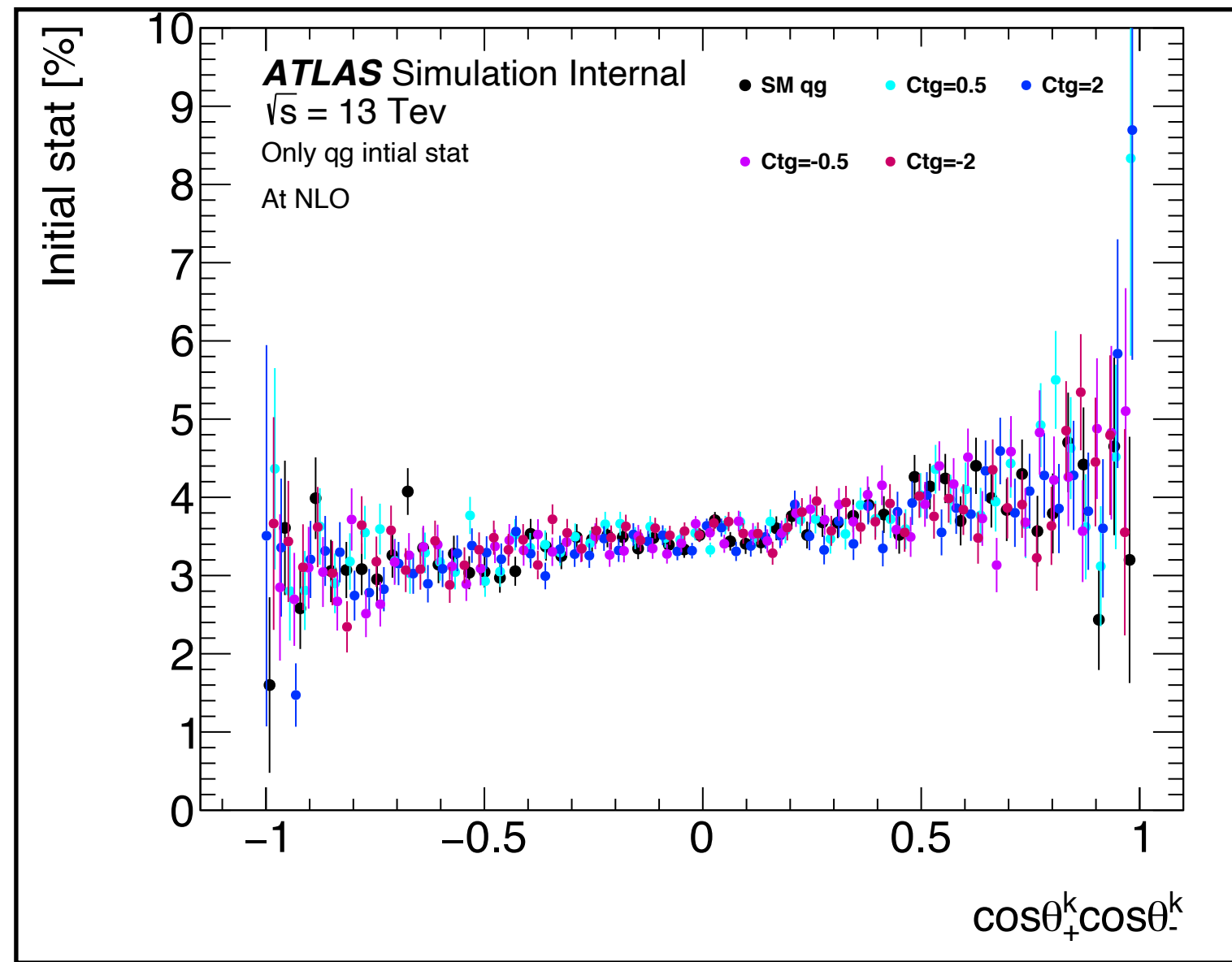


# gg Initial stat VS C(k,k)

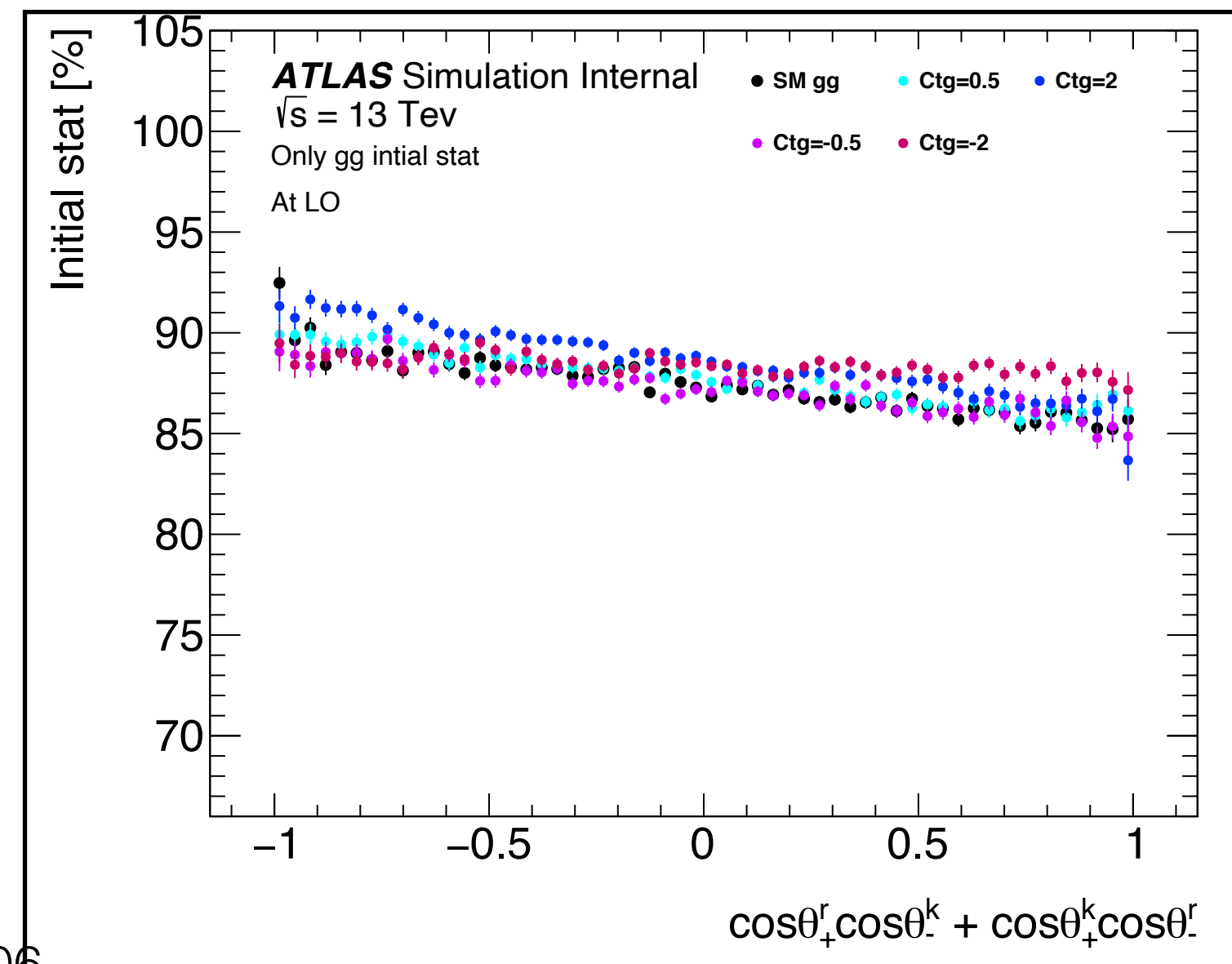
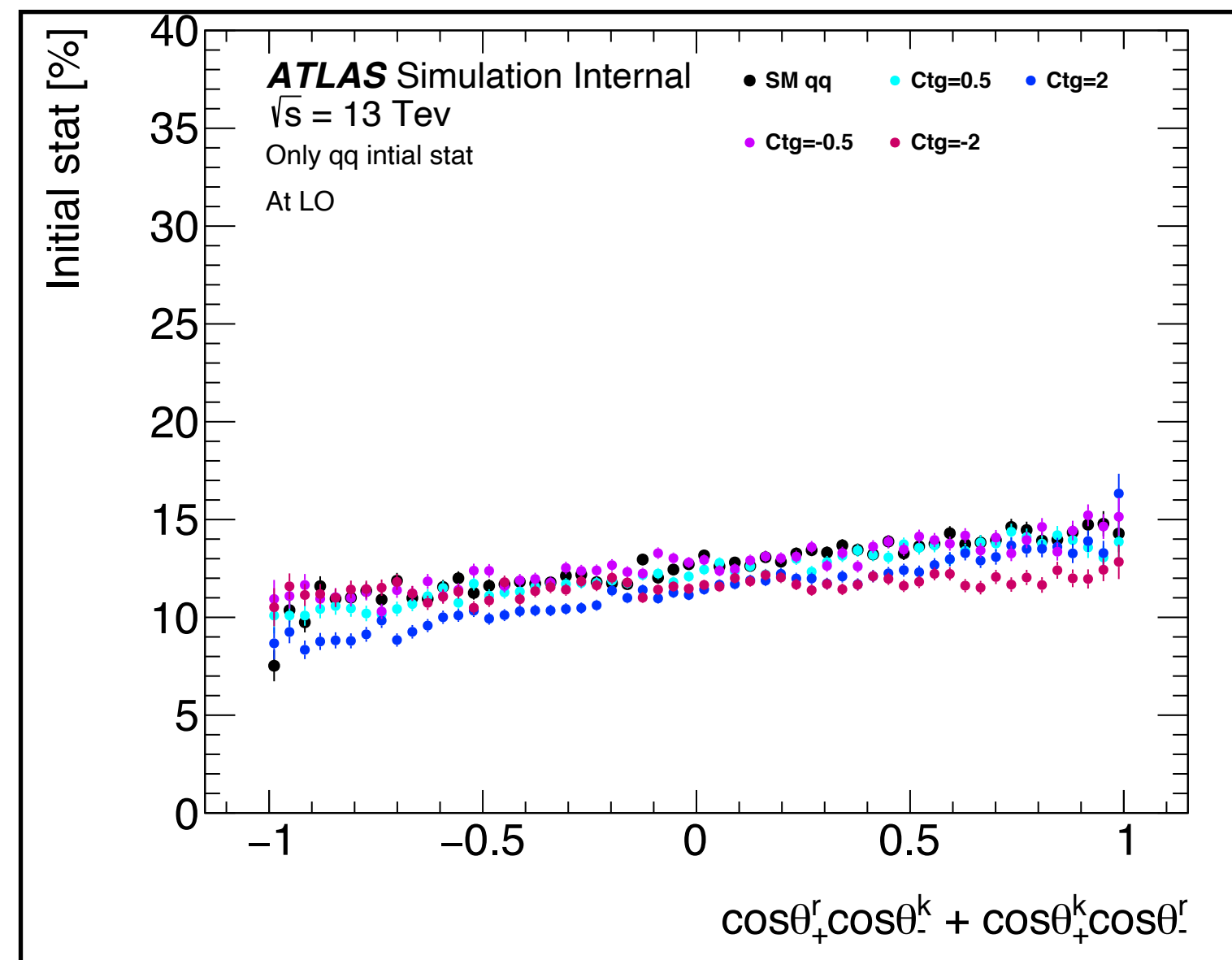
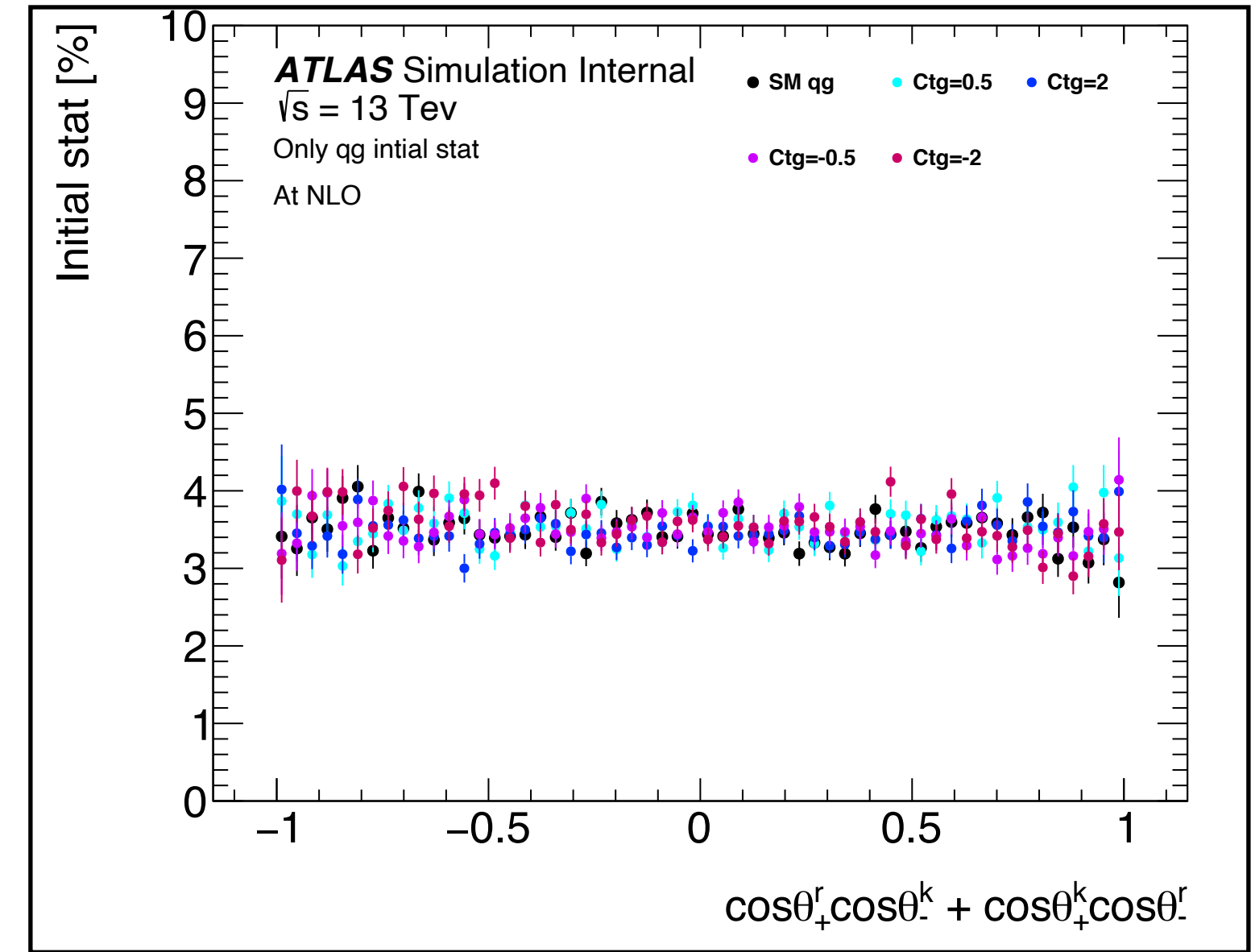
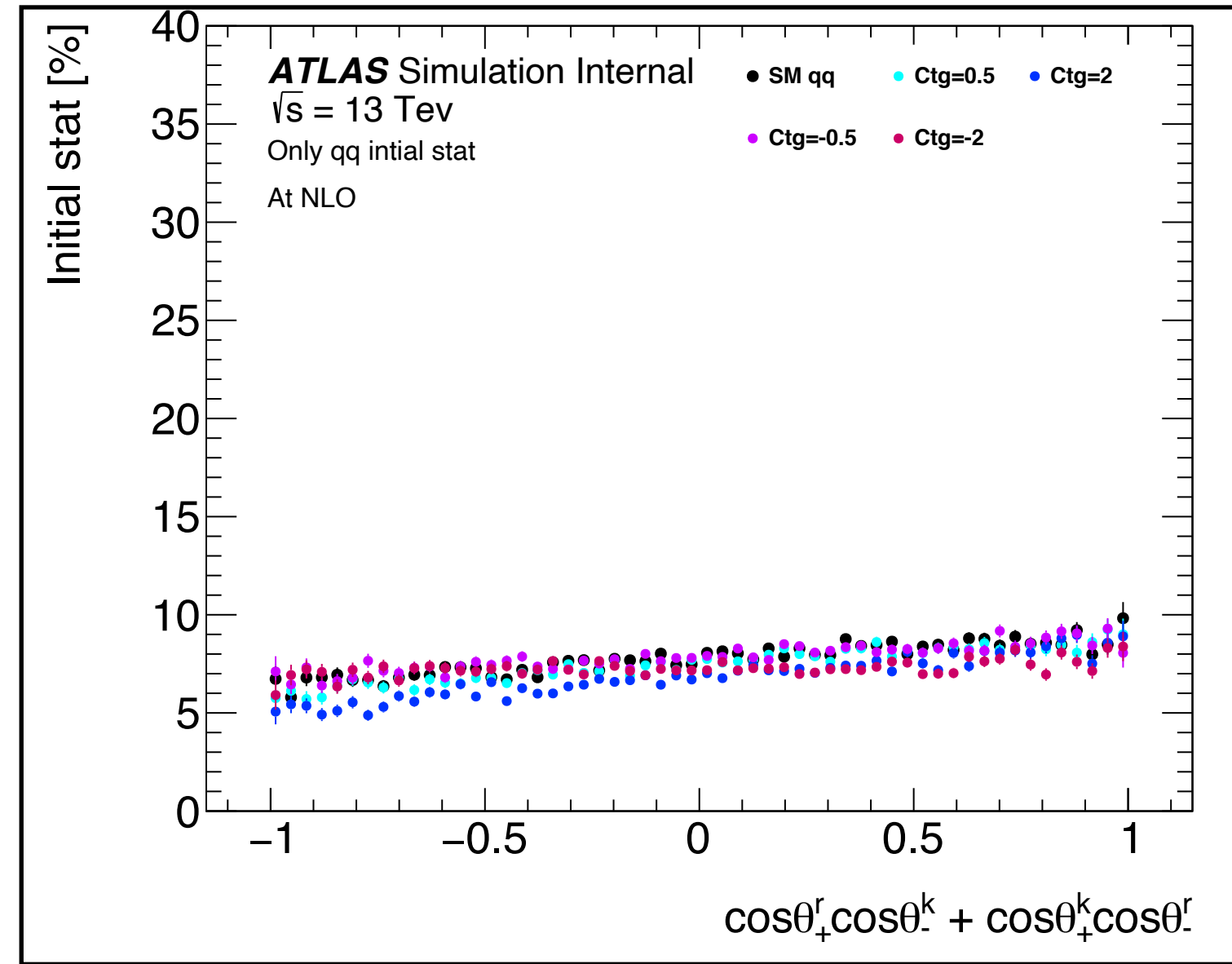
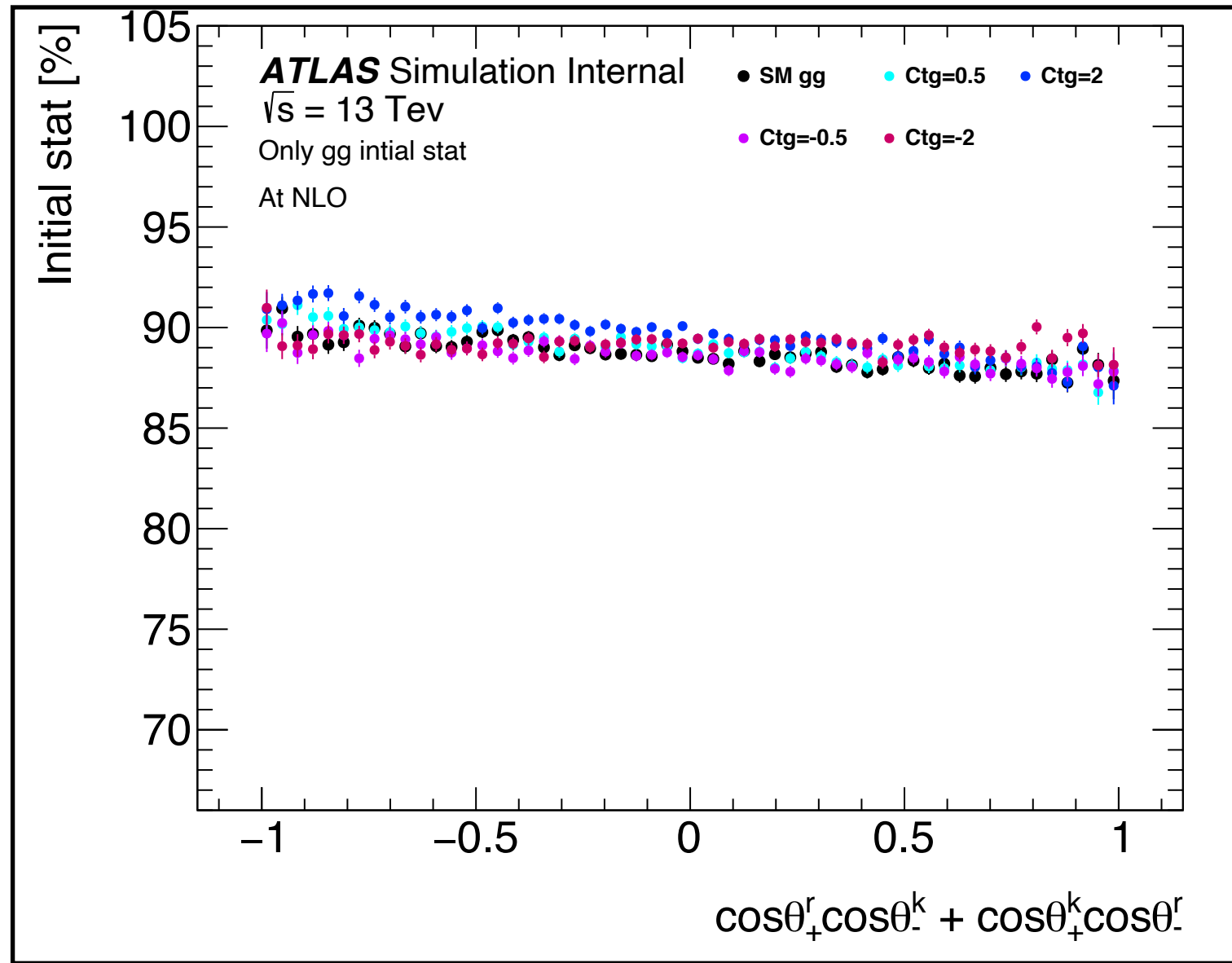




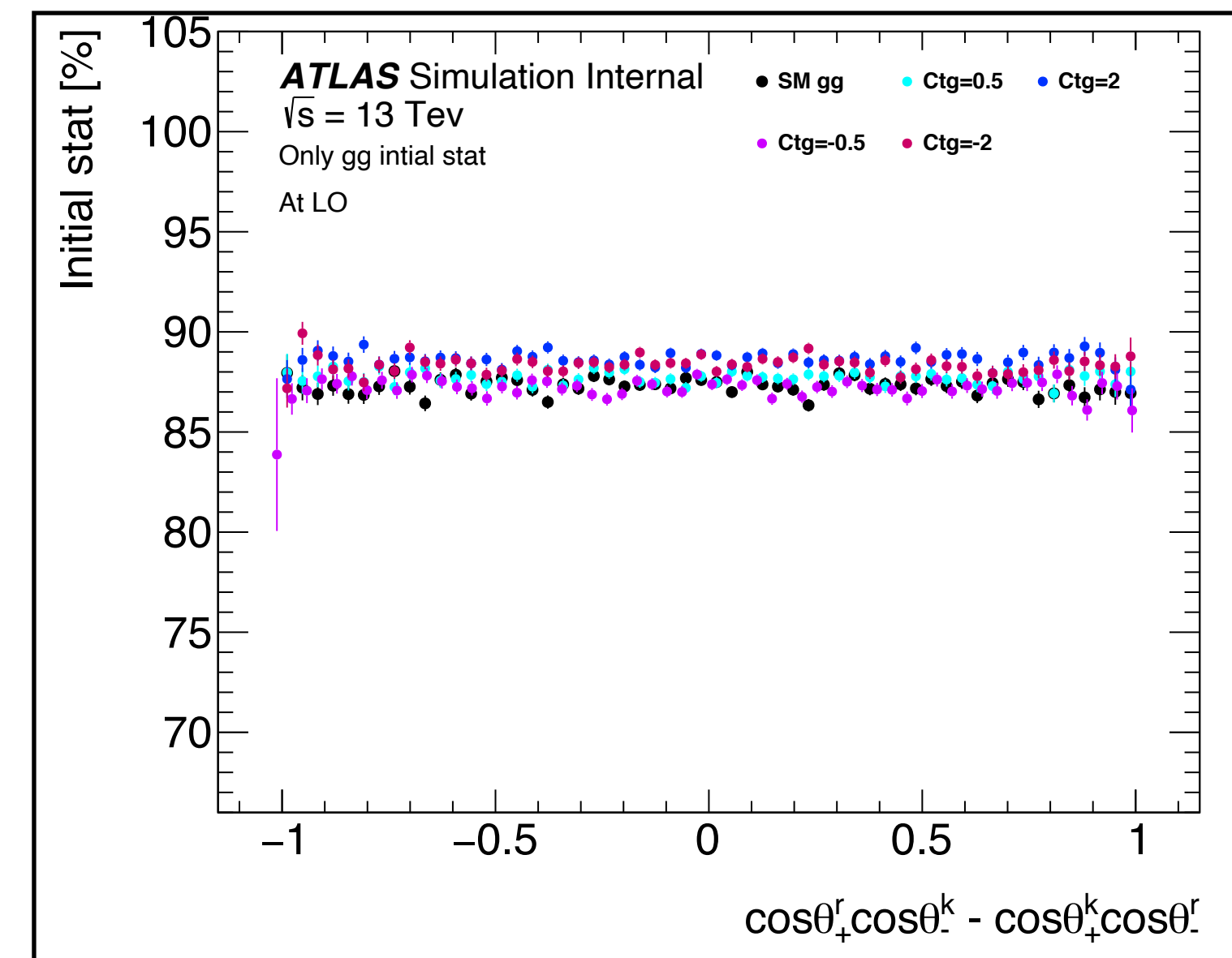
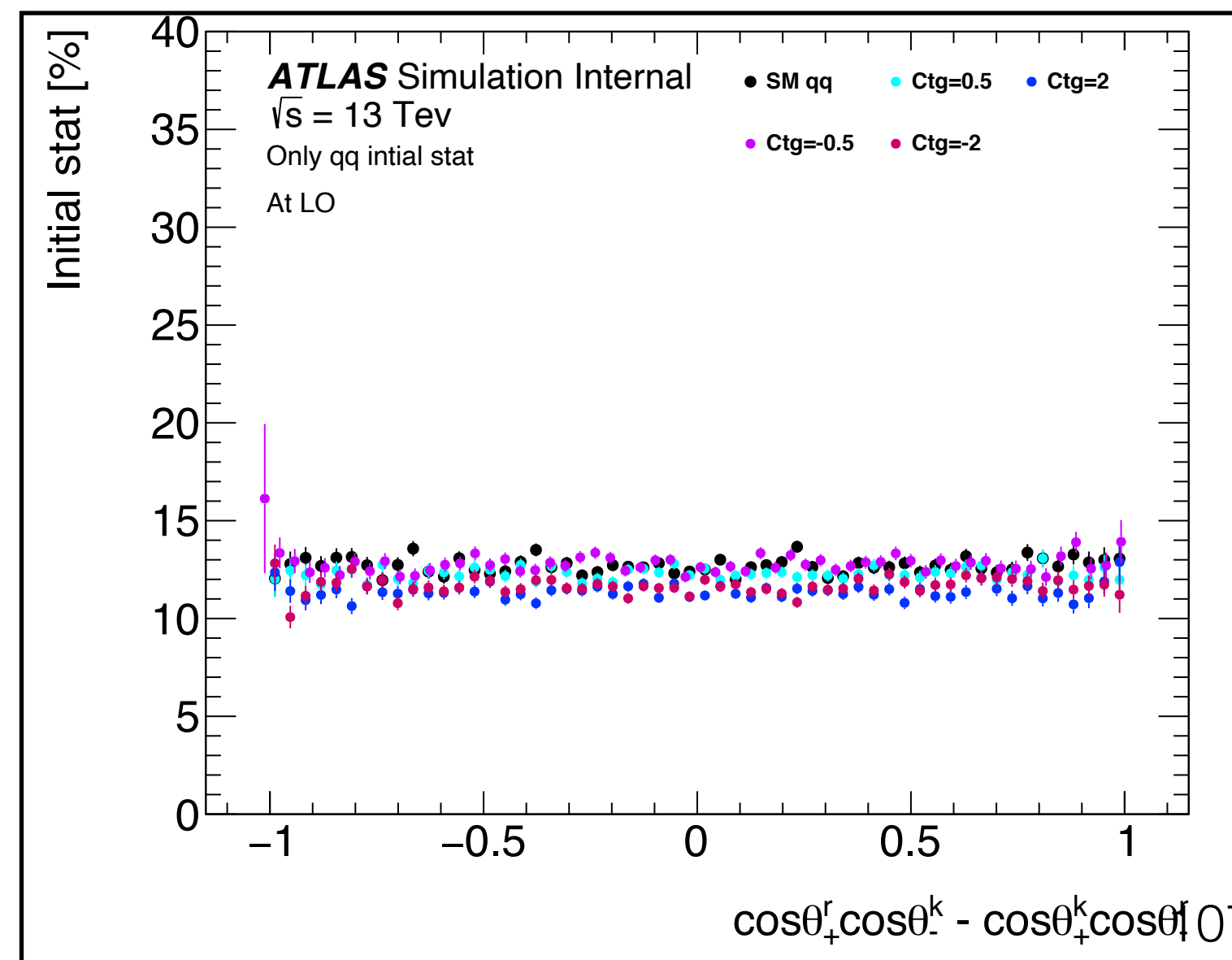
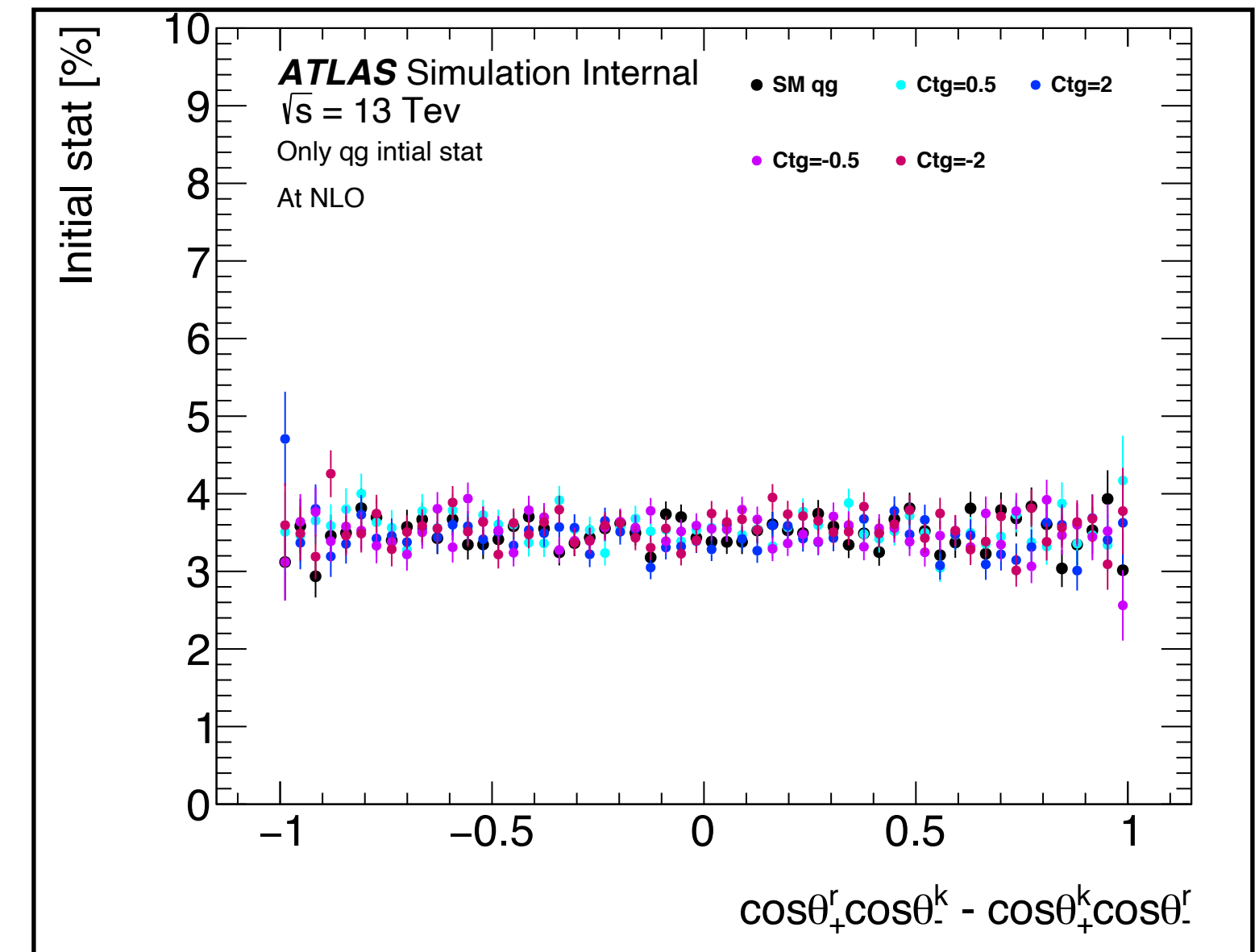
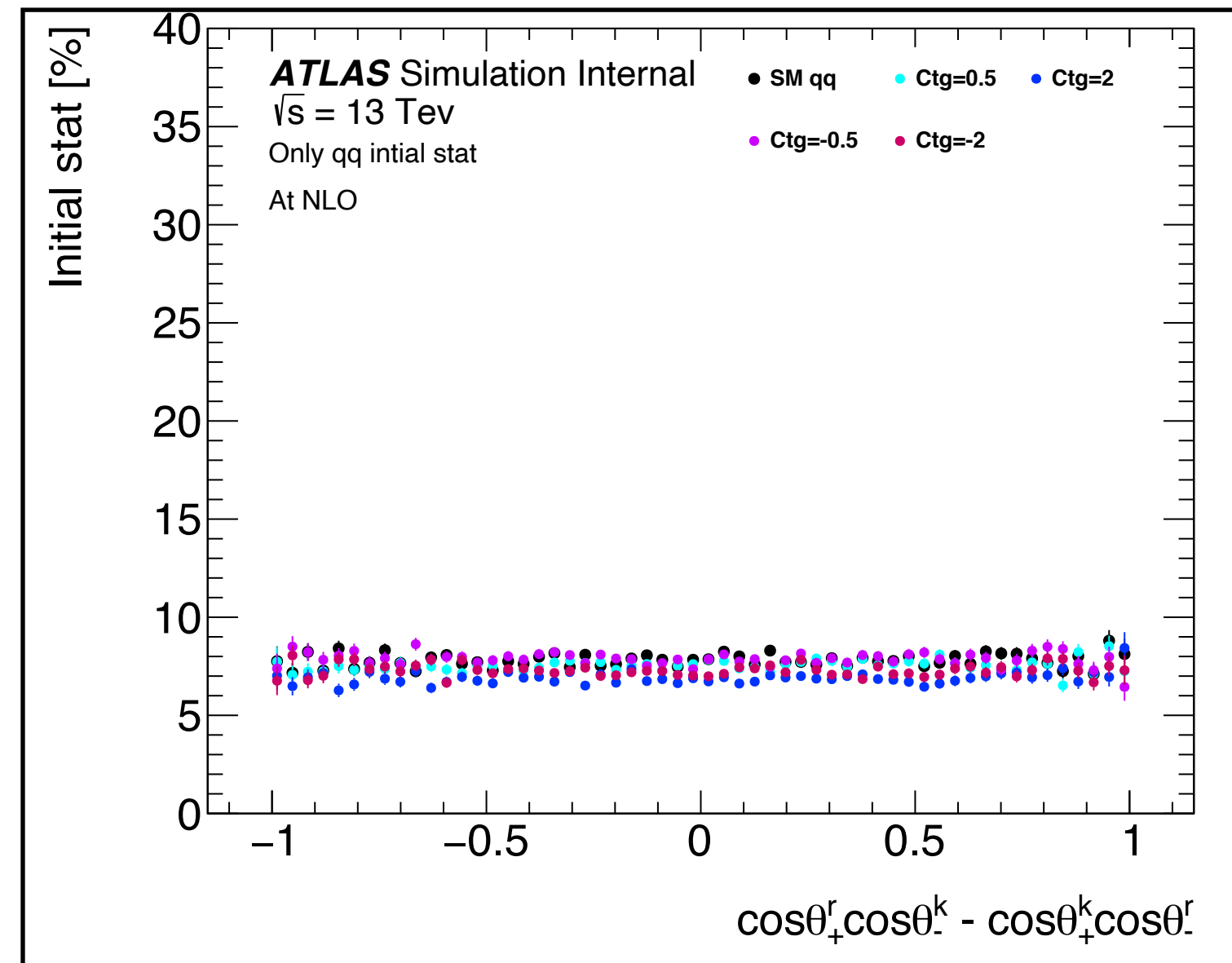
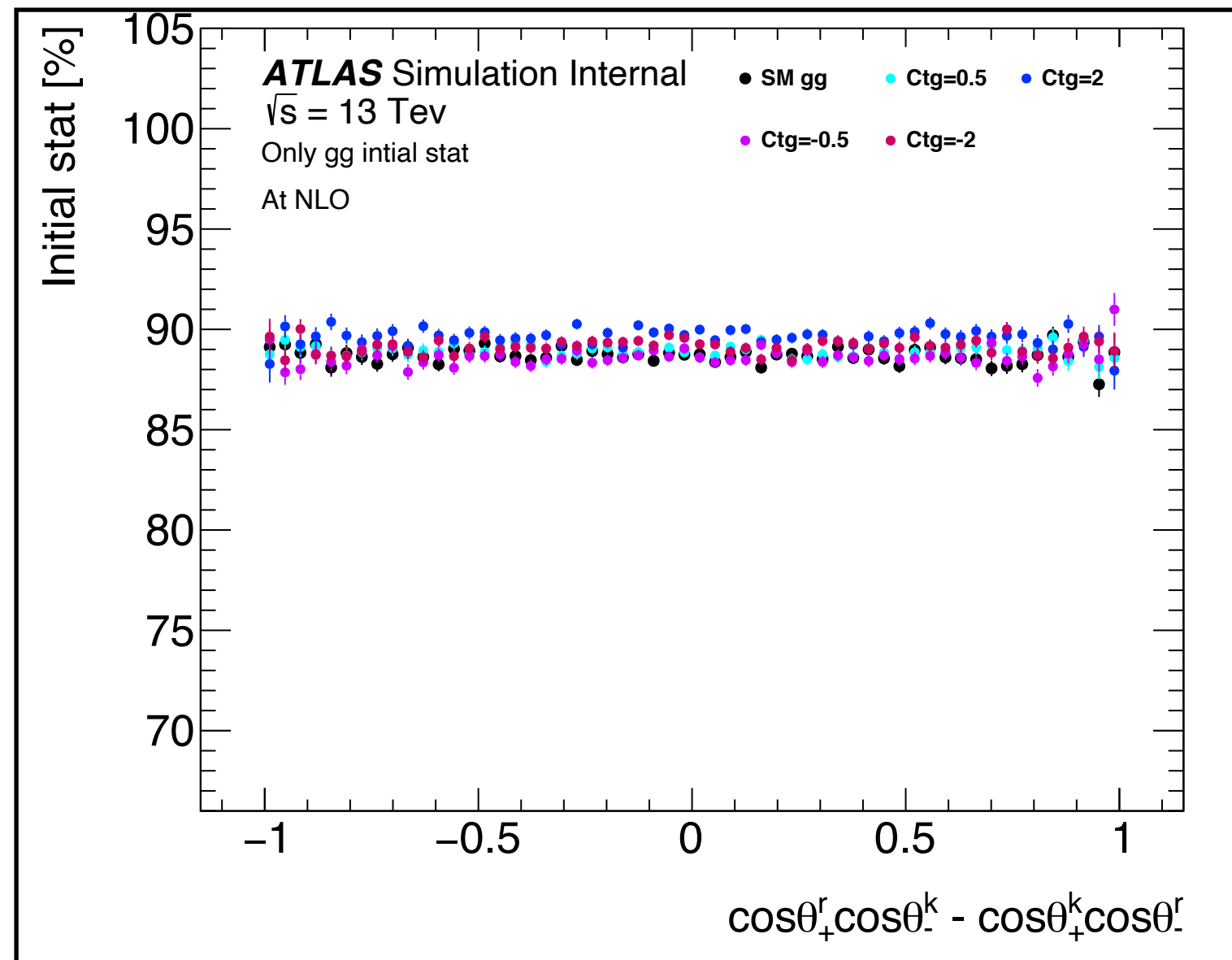
# qq/qg Initial stat VS $C(k,k)$



# Initial stat VS $C(r,k) + C(k,r)$



# Initial stat VS $C(r,k) - C(k,r)$



# Initial stat VS C<sub>tg</sub>

- ☑ C<sub>tg</sub> = 0 corresponds to the SM value.

