

Shape evolution in neutron-rich nuclei around mass $A=100$

Giorgia Pasqualato

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V. Modamio², L.G.. Pedersen², and W. Korten³

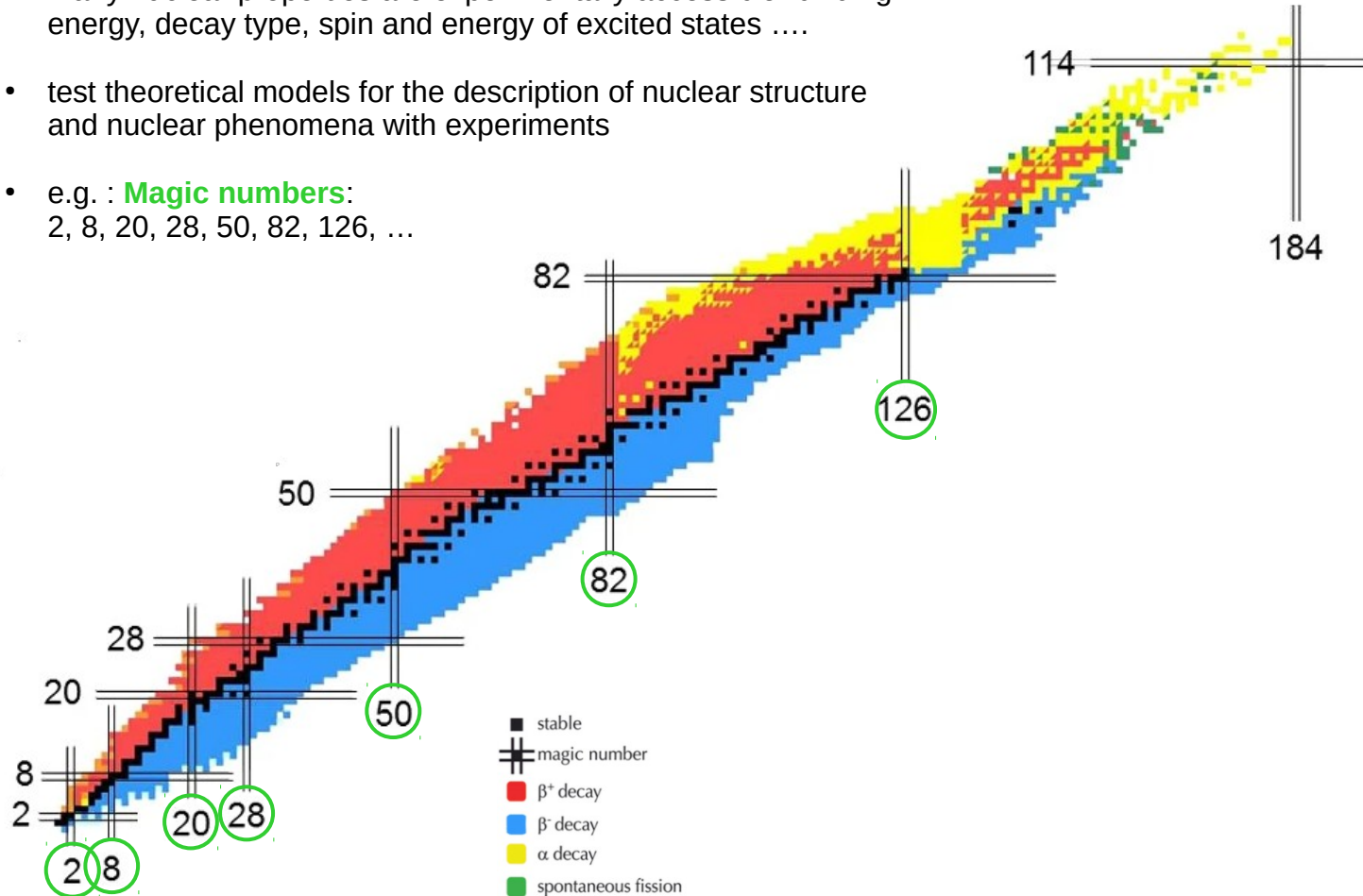
¹ IJCLab, IN2P3/CNRS, Université Paris-Saclay, Orsay, France.

² Department of Physics, University of Oslo, Norway.

³ CEA Paris-Saclay, DRF/IRFU/DPhN, Gif-sur-Yvette, France.

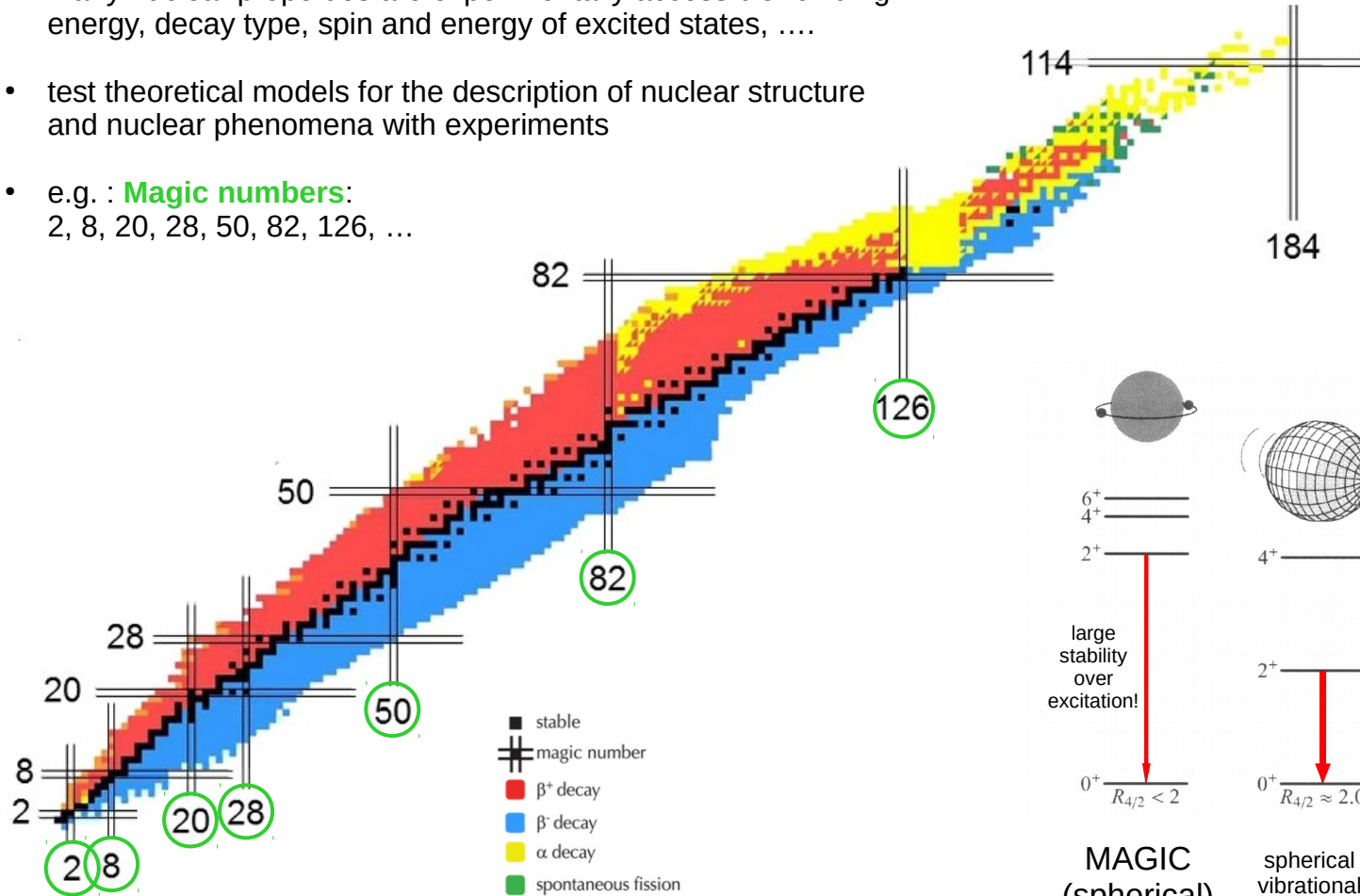
The nuclear landscape

- many nuclear properties are experimentally accessible: binding energy, decay type, spin and energy of excited states
- test theoretical models for the description of nuclear structure and nuclear phenomena with experiments
- e.g. : **Magic numbers**:
2, 8, 20, 28, 50, 82, 126, ...

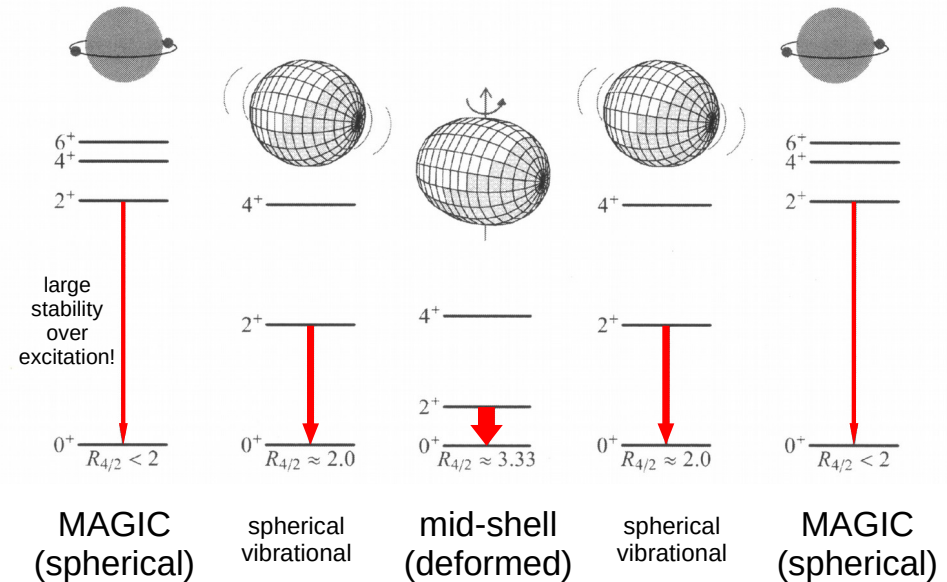


The nuclear landscape

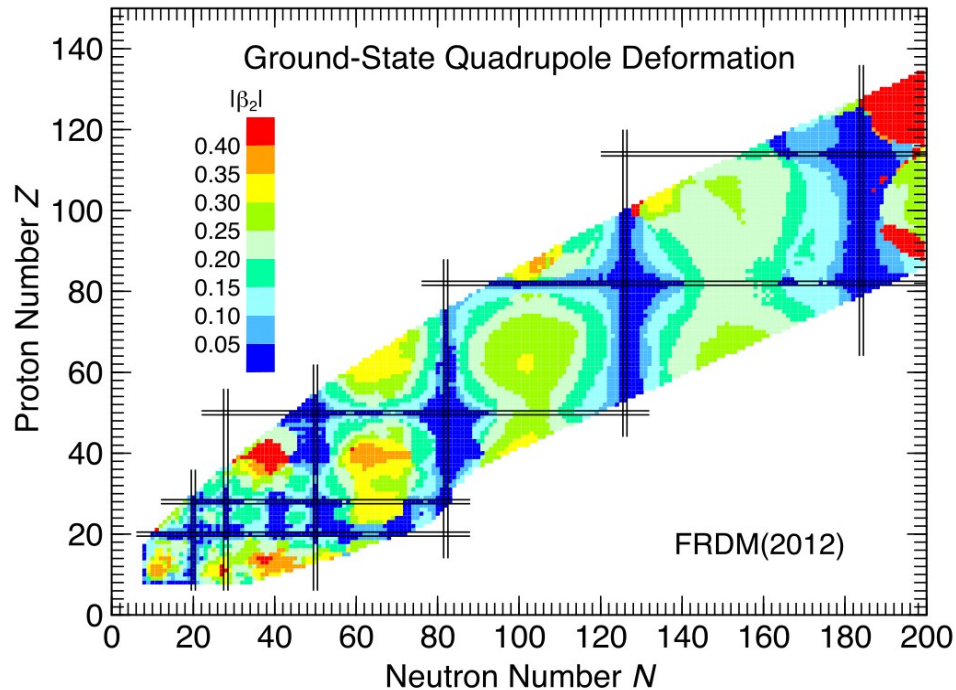
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Nuclei with a number of nucleons in between **magic configurations** are characterized by **deformation**.

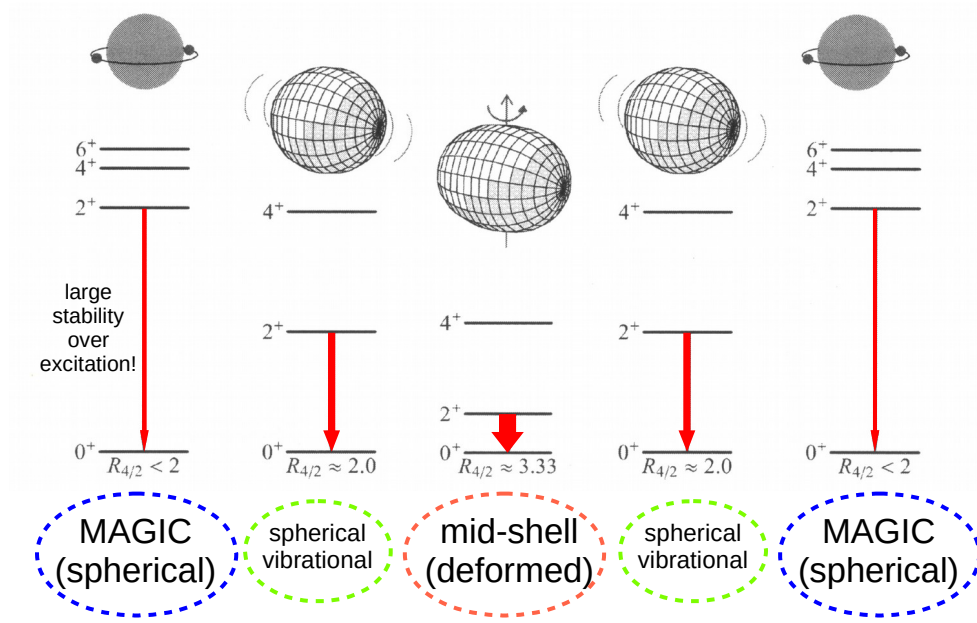


Shape evolution in nuclei

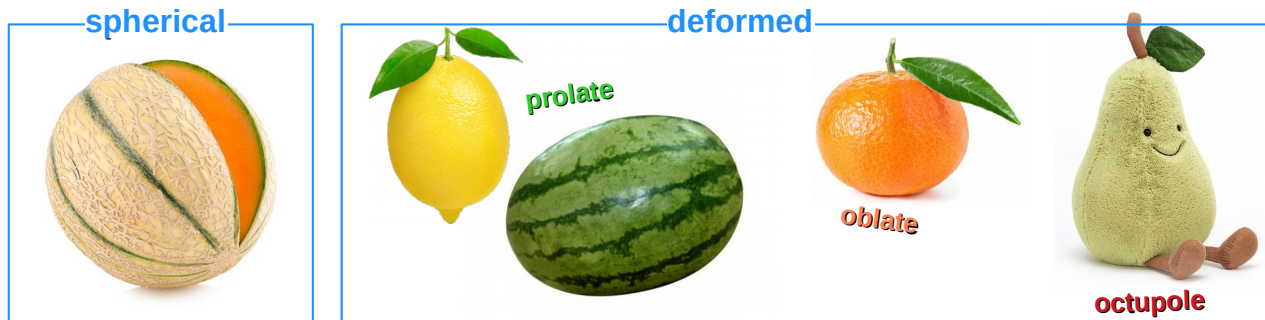


P. Möller, A.J. Sierk, T. Ichikawa, H. Sagawa,
Nuclear ground-state masses and deformations: FRDM(2012),
 Atomic Data and Nuclear Data Tables, 109–110, (2016),

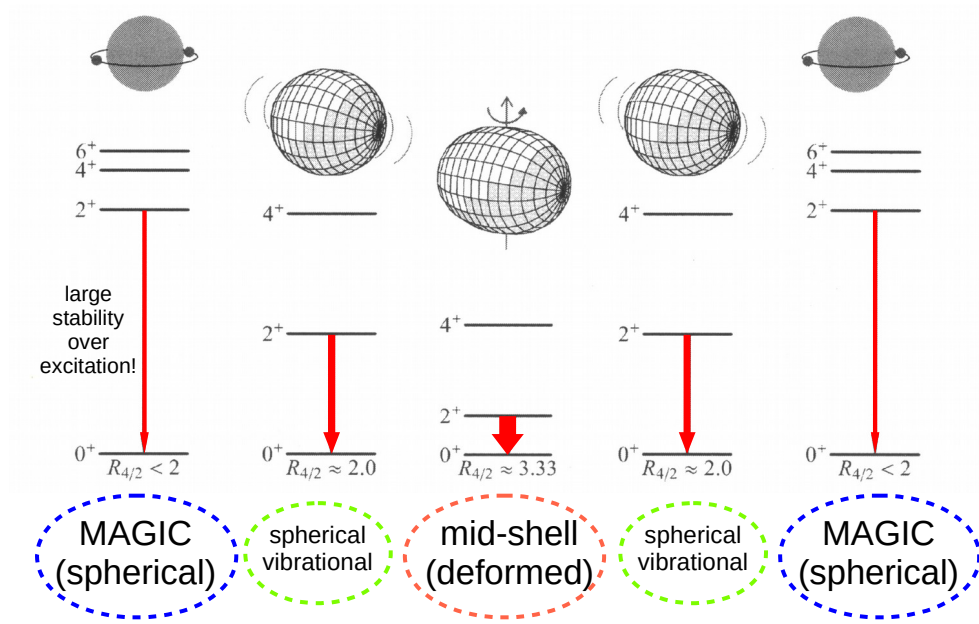
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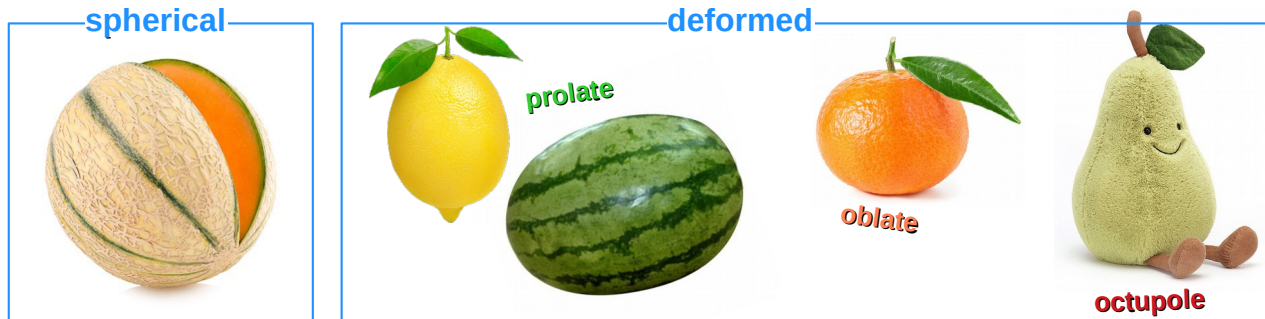
Shape evolution in nuclei



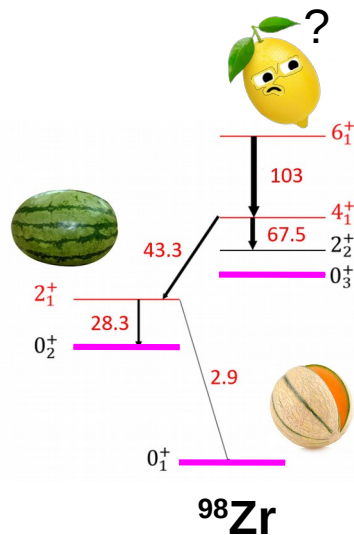
Deformed nuclei can manifest different shape.



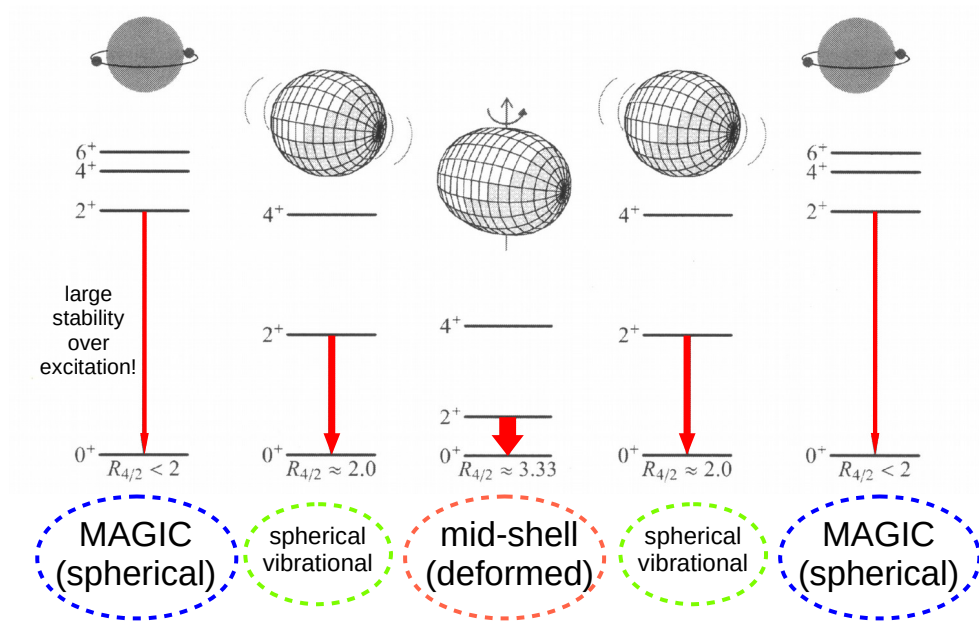
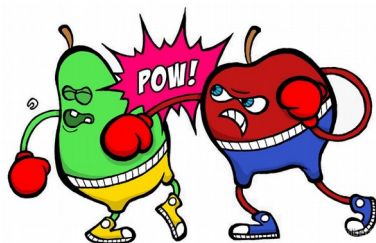
Shape evolution in nuclei



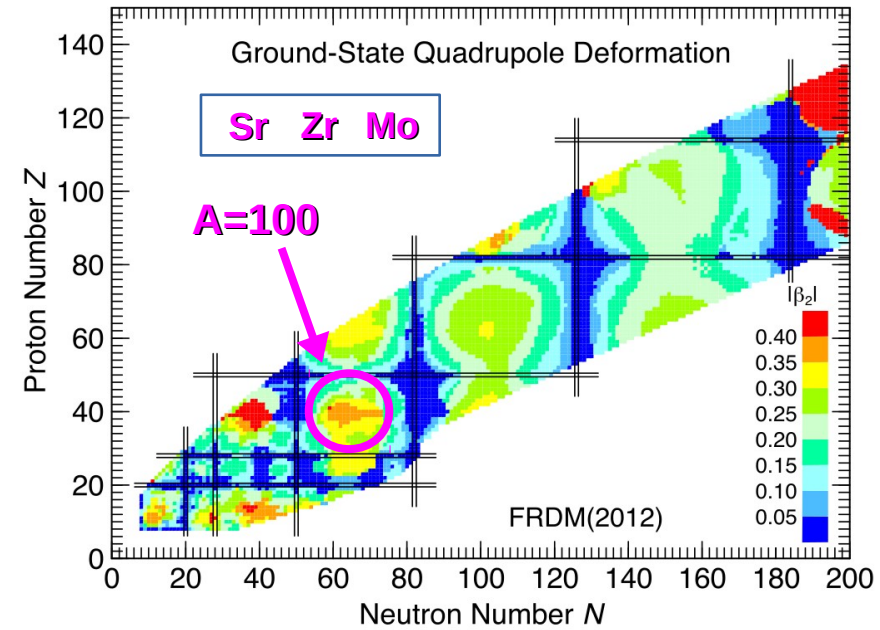
The systematic study of deformation and shape coexistence along the nuclear chart is a powerful way to test nuclear models !



• Shape coexistence



Shape evolution in nuclei around $A=100$

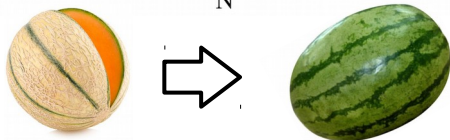
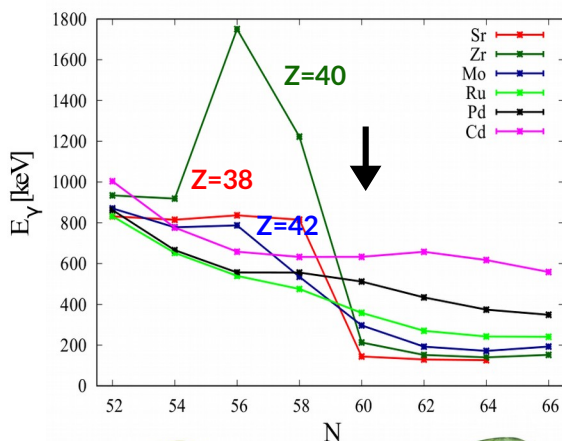


Rapid onset of deformation observed in the region around mass $A=100$.

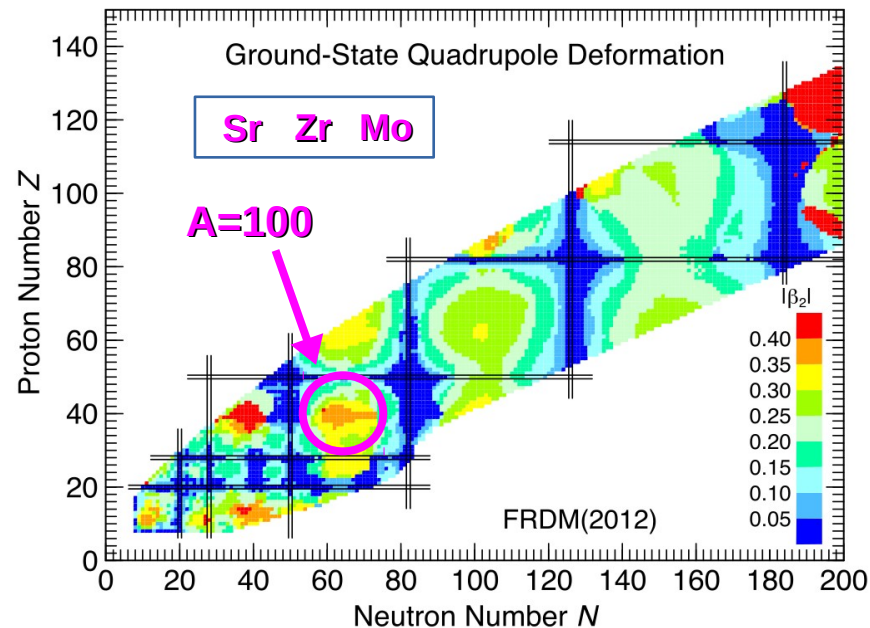
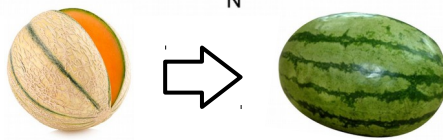
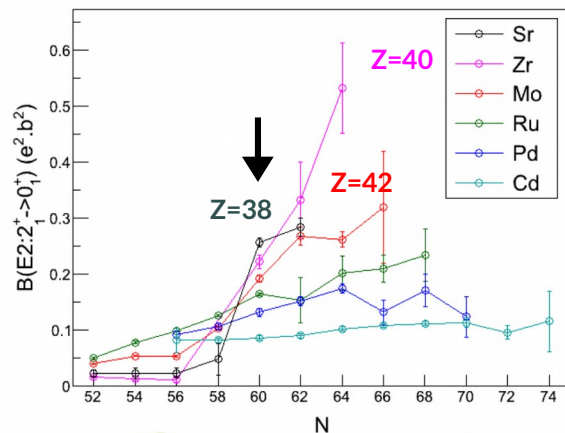
Shape evolution in nuclei around A=100

Drastic change in nuclear properties as a function of N (and Z) !

- Energies of the first 2_1^+



- Decay probability $B(E2; 2_1^+ \rightarrow 0_1^+)$



Rapid onset of deformation observed in the region around mass A=100.

Shape-phase transition in Zr isotopes

For the Zr chain, the onset of deformation at $N=60$ has been studied by many theoretical approaches.

generator coordinate method (GCM):

J. Skalski, P.-H. Heenen, and P. Bonche, Nucl. Phys. A 559, 221 (1993).

J.-P. Delaroche et al., Phys. Rev. C 81, 014303 (2010).

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Shell Model Monte Carlo

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Monte Carlo Shell Model:

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Hartree-Fock (HF) and Hartree-Fock-Bogoliubov (HFB) models:

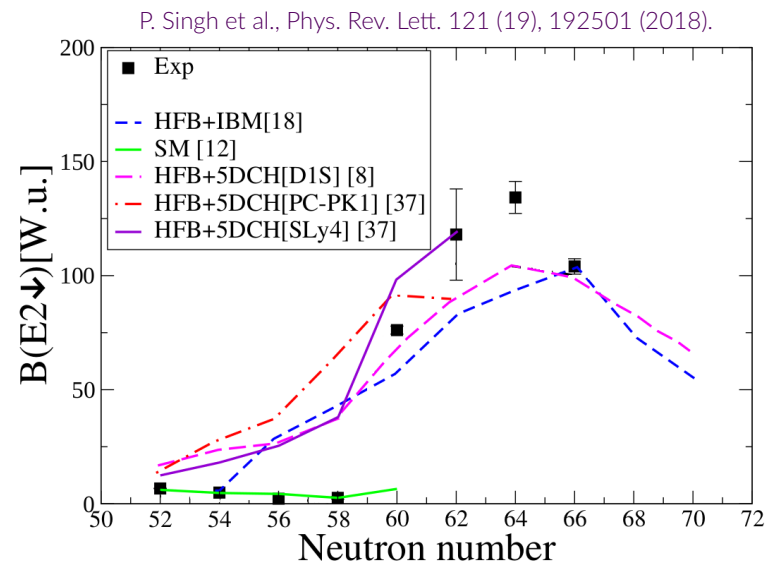
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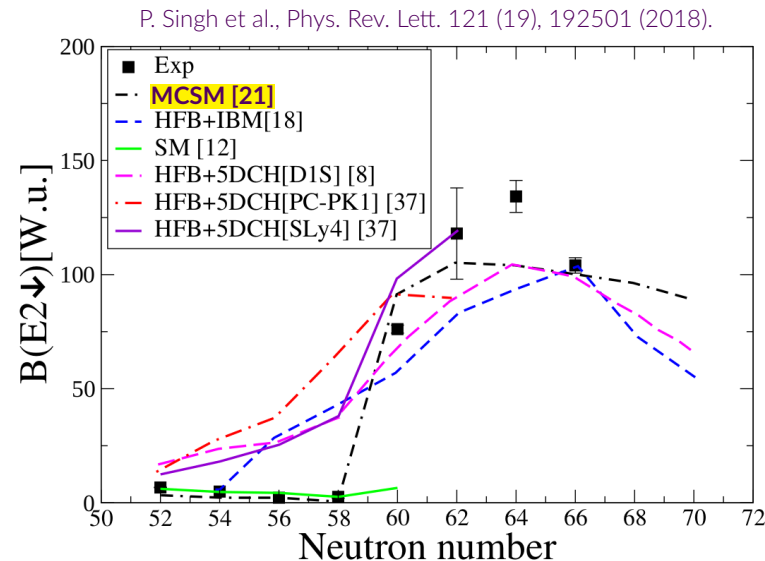
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- Description of the rapid shape change + shape coexistence

→ further experimental investigation in this region are needed !

Study nuclear shape through electromagnetic transition strengths

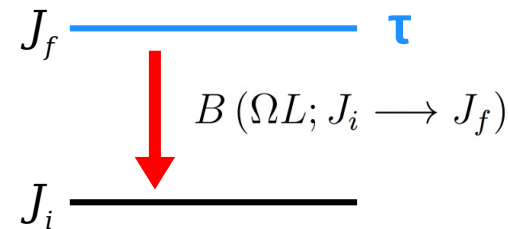
→ **GOAL** : obtain precise experimental information on nuclear deformation with **electromagnetic transition strengths T** through the measurement of the **lifetime τ** of nuclear excited states.

$$\tau = T^{-1} \rightarrow B(\Omega L; J_i \rightarrow J_f) = \frac{1}{2J_i + 1} |\langle J_f || M(\Omega L) || J_i \rangle|^2$$

EXPERIMENT : lifetimes

→ → →

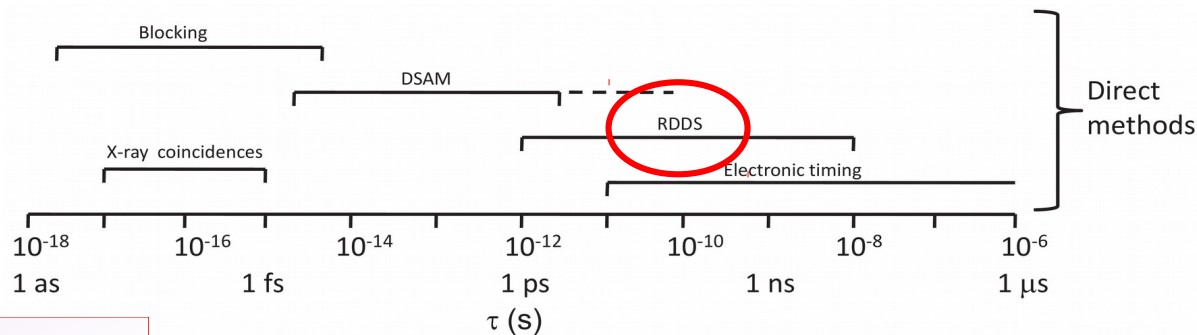
THEORY : matrix elements



LIFETIME MEASUREMENTS

The lifetime of a nuclear state can range from 10^{-20} seconds to billions of years

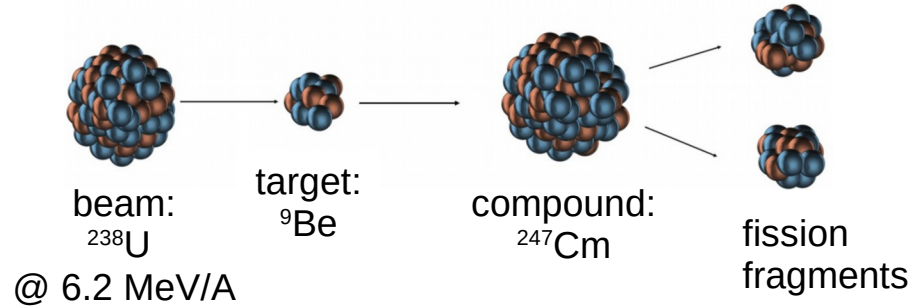
different techniques have been implemented



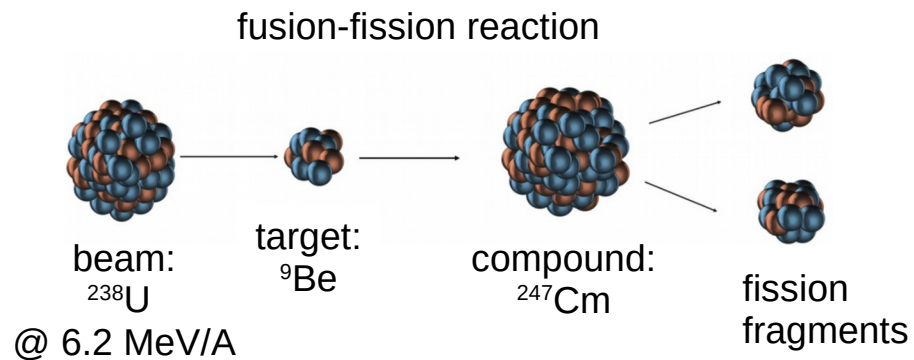
RDDS : Recoil Distance Doppler Shift technique for the ps range

Production and identification of fission fragments

fusion-fission reaction

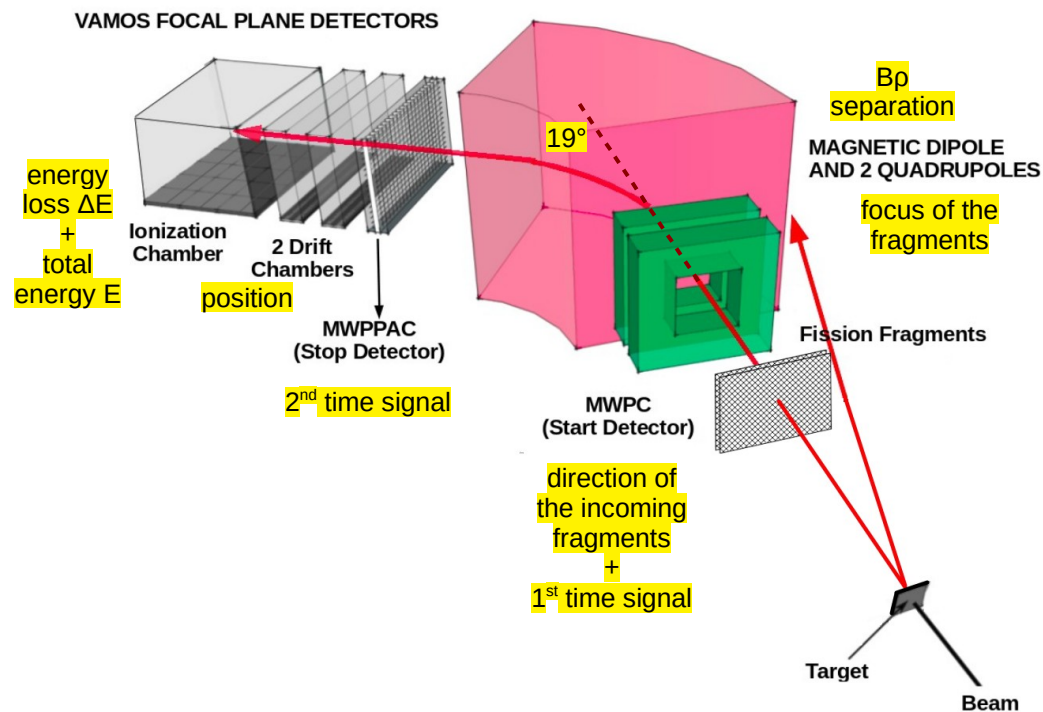


Production and identification of fission fragments

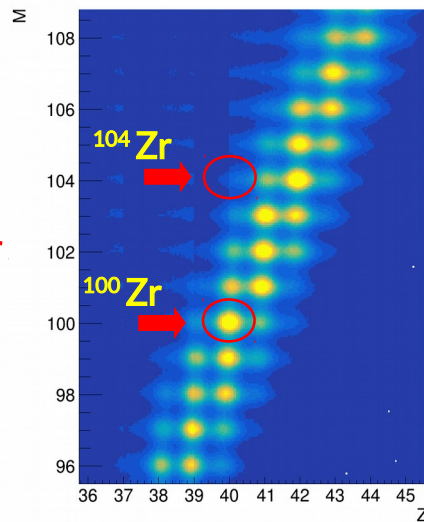
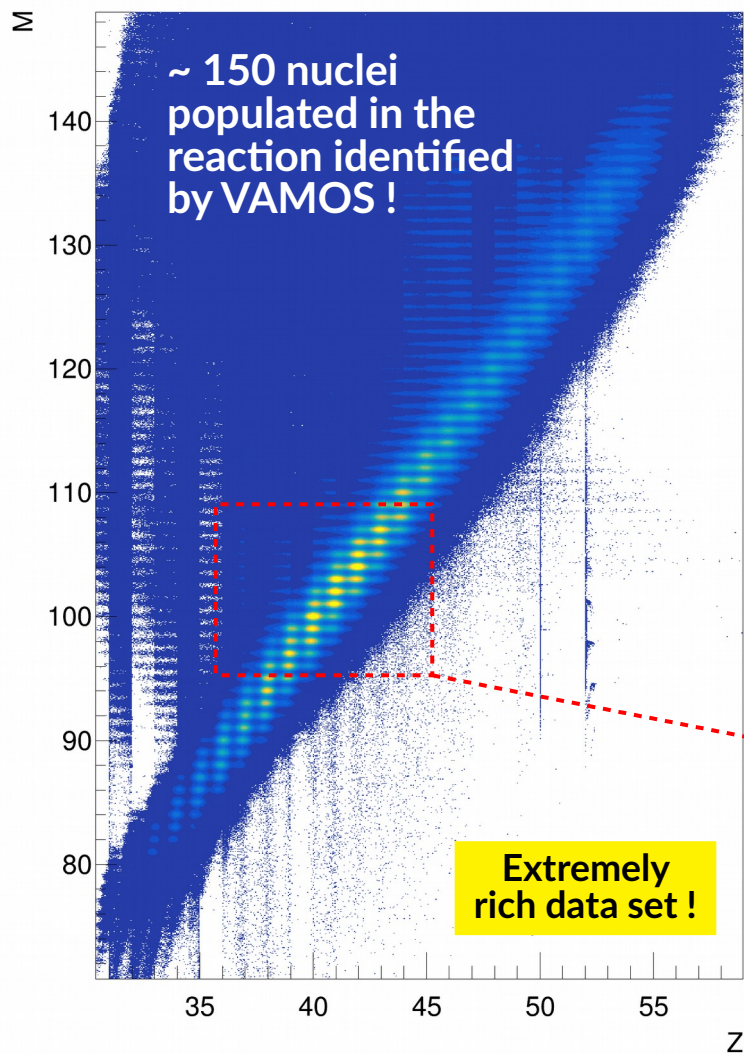


VAMOS large acceptance magnetic spectrometer

fragment identification based on atomic number Z , mass M and charge Q



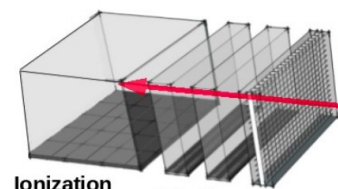
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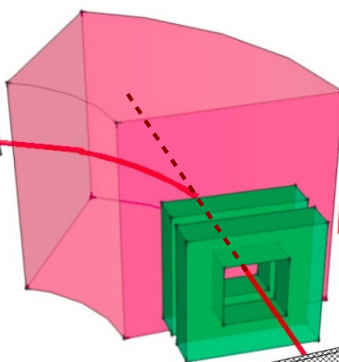
VAMOS FOCAL PLANE DETECTORS



Ionization Chamber

2 Drift Chambers

MWPPAC (Stop Detector)



MAGNETIC DIPOLE AND 2 QUADRUPOLES

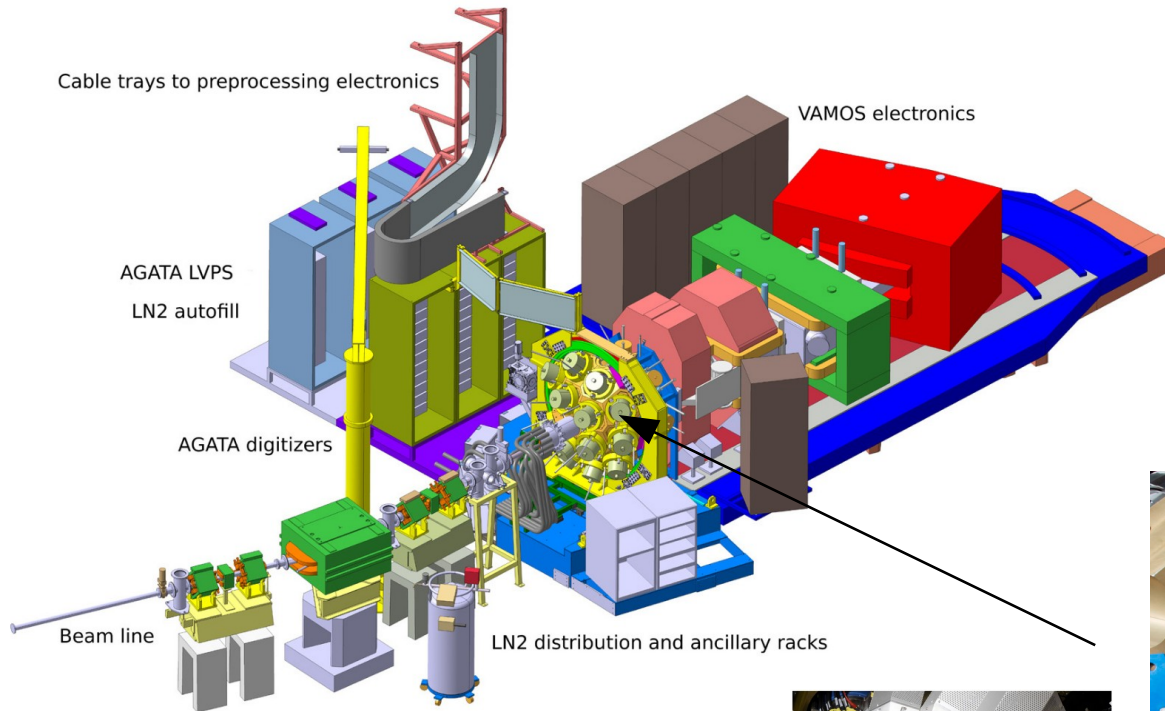
MWPC (Start Detector)

Fission Fragments

Target

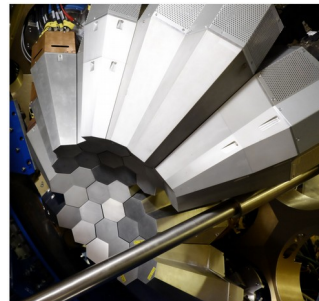
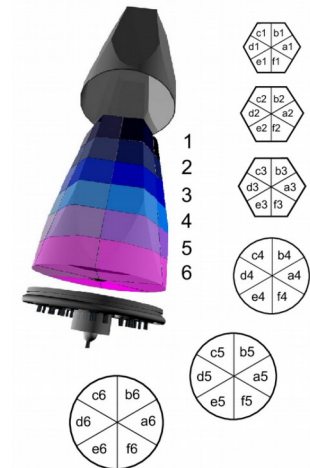
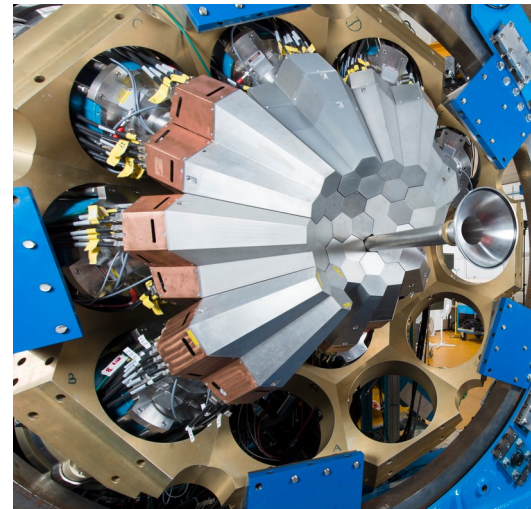
Beam

Detection of γ rays with AGATA

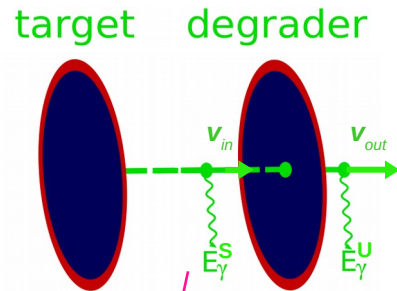
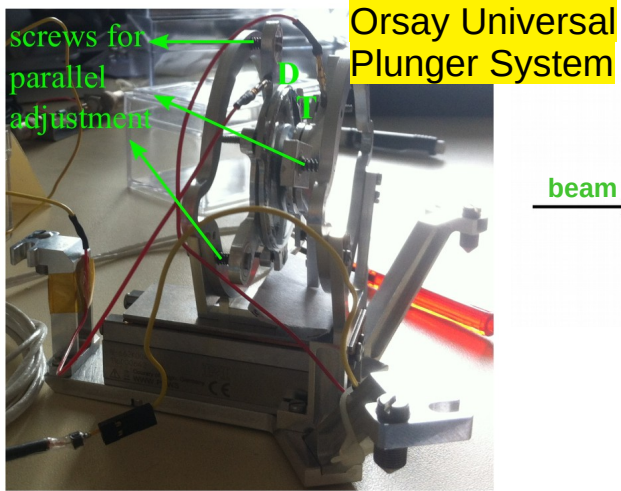


Advanced Gamma Tracking Array AGATA

Excellent energy resolution of HPGe detectors
+
unprecedented photo-peak efficiency
+
Pulse Shape Analysis (PSA) and γ -ray tracking



Recoil Distance Doppler Shift technique

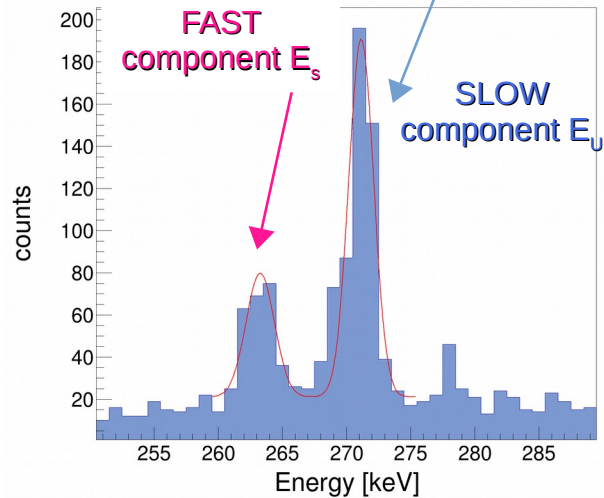


the energy detected is
Doppler-shifted:

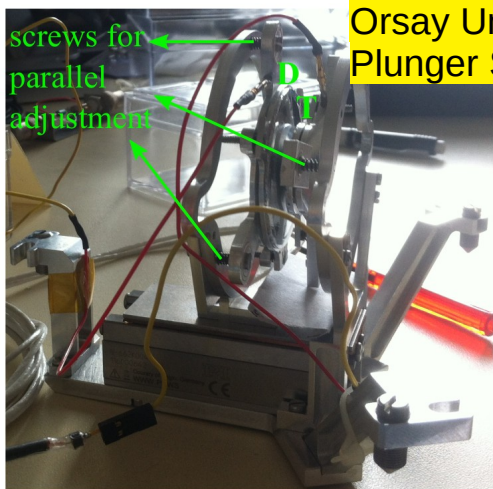
$$E = E_0 \frac{\sqrt{1 - \beta^2}}{1 - \beta \cos \Theta}$$

recoil
velocity

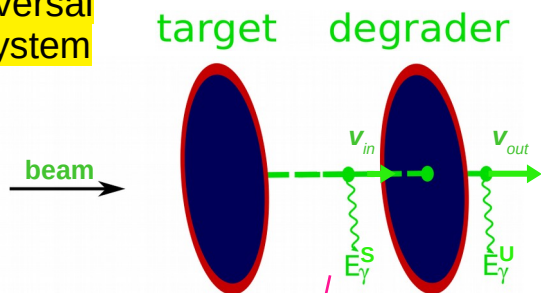
angle of
emission



Recoil Distance Doppler Shift technique



Orsay Universal Plunger System

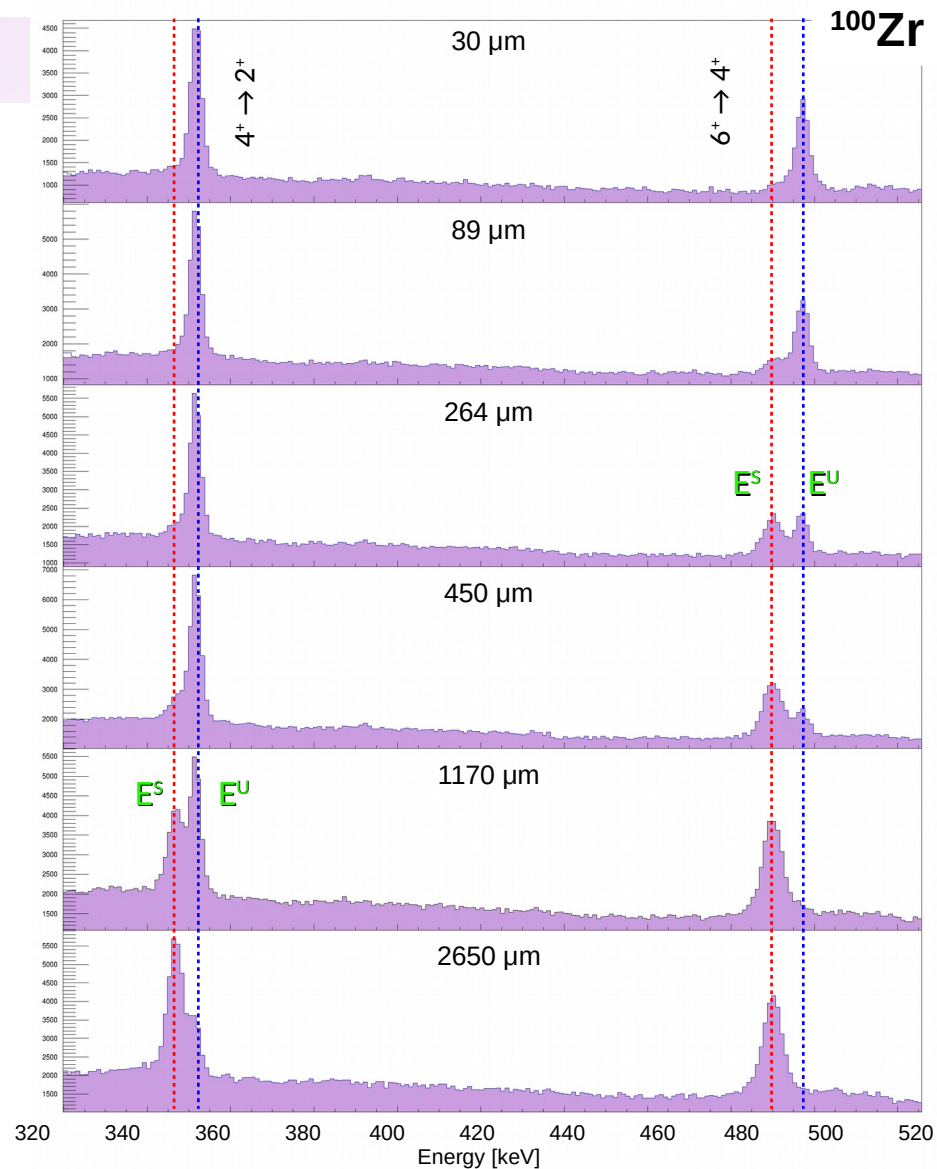
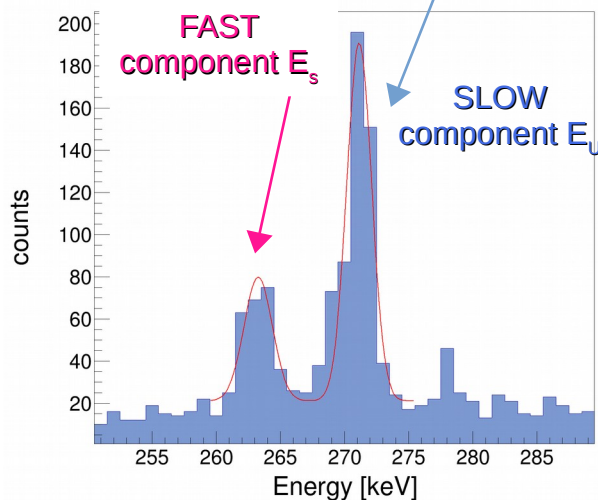


the energy detected is Doppler-shifted:

$$E = E_0 \frac{\sqrt{1 - \beta^2}}{1 - \beta \cos \Theta}$$

recoil velocity

angle of emission

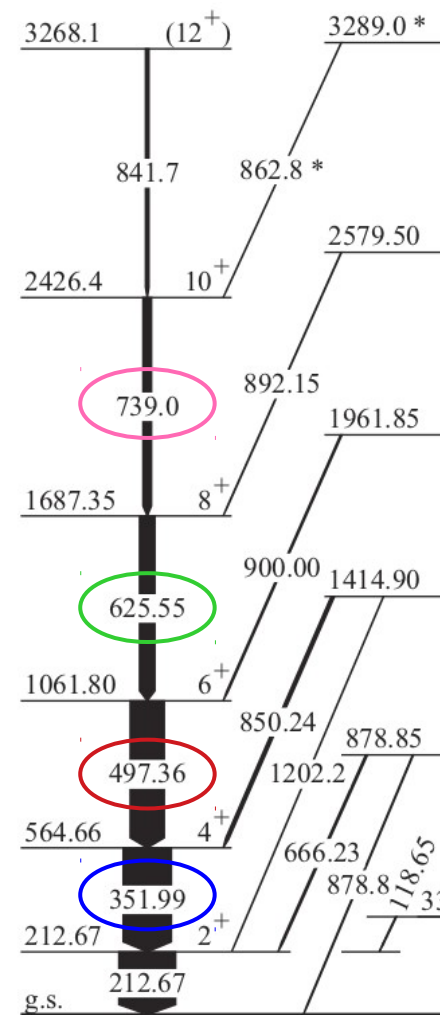


Preliminary results for ^{100}Zr in single γ and coincidence $\gamma\gamma$

- Lifetime measurements in gamma single and gamma-gamma coincidence.
- Comparison with previous results for the levels 4^+ , 6^+ , 8^+ , 10^+ of the yrast band :
 - The adopted value for the 4^+ may be overestimated.
 - The 6^+ and 8^+ adopted lifetimes also result larger.
 - Measurements in $\gamma\gamma$ gives shorter lifetimes (4^+ and 6^+) as expected.
 - The lifetime of the 8^+ is accurate in single γ due to the short-living feeding.

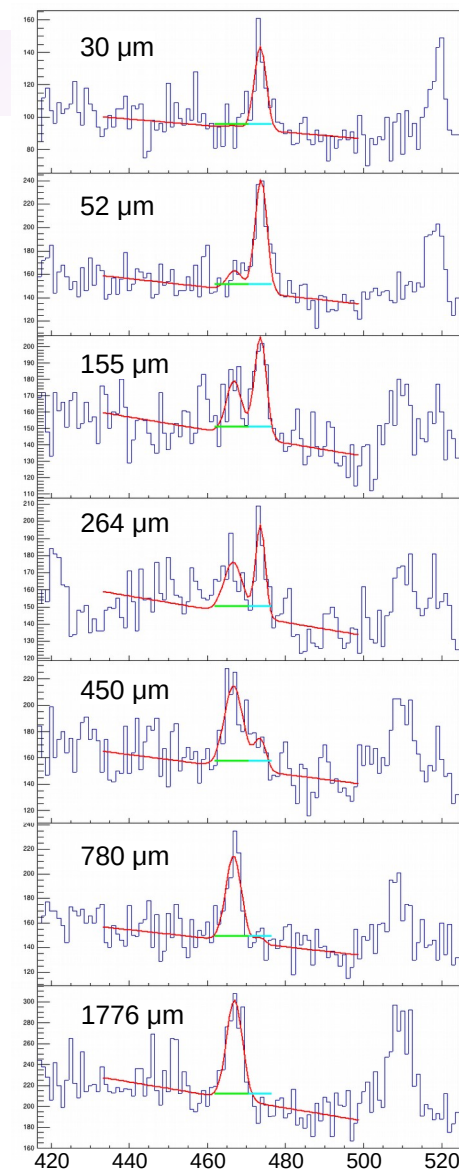
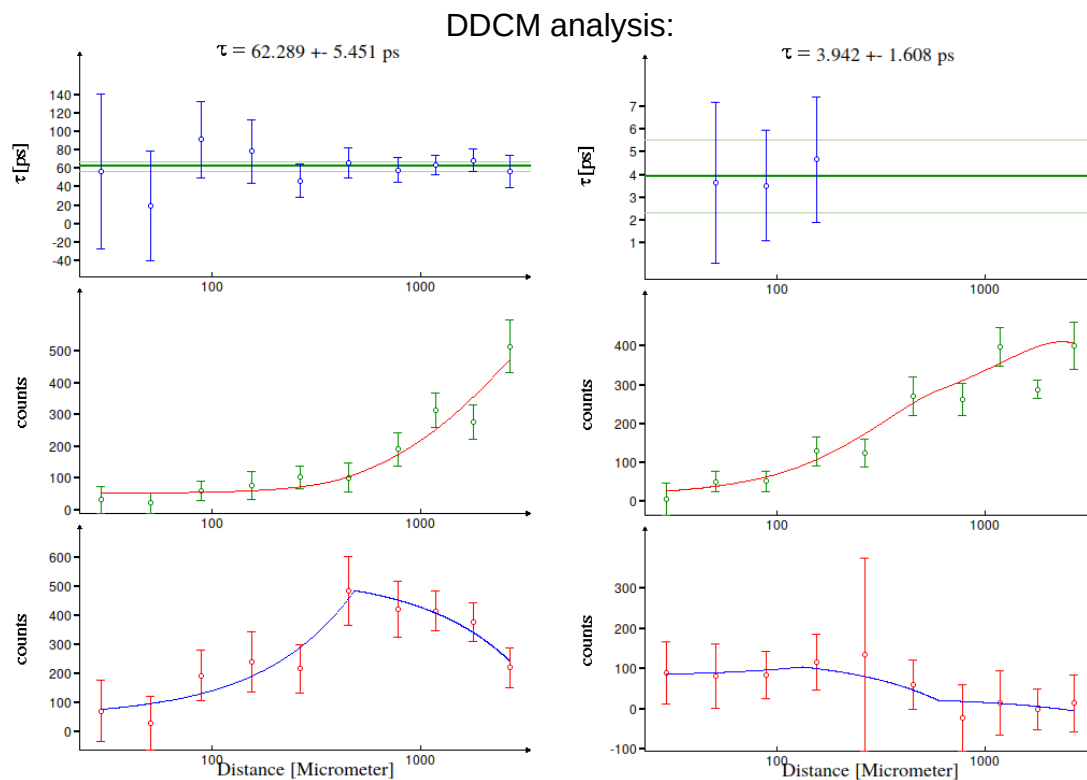
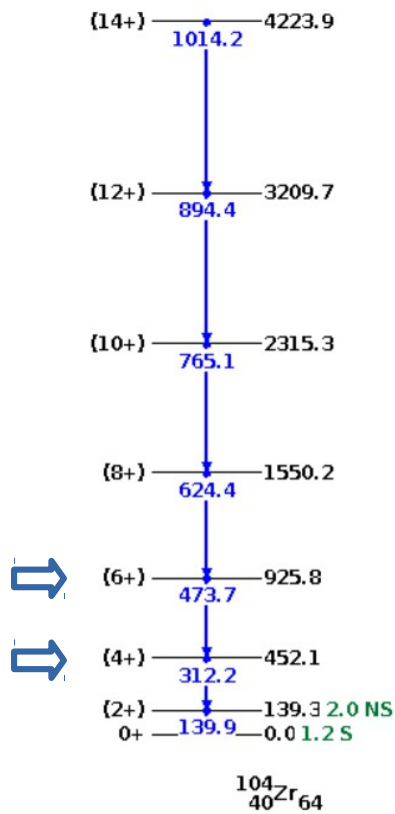
J^π	Energy [keV]	τ [ps] adopted	τ [ps] single γ	τ [ps] coincid $\gamma\gamma$
4+	352.0	53.4 (6)	36.9 (6)	30 (2) *
6+	497.4	7.5 (1.6)	5.7 (3)	5.0 (6)
8+	625.6	2.5 (2)	1.0 (1)	1.7 (4)
10+	739.0	0.53 (6)	0.6 (2)	/

*The feeding transition at 840.2 keV is not considered : difficult to resolve its shifted component from the 841.7 keV $12^+ \rightarrow 10^+$.



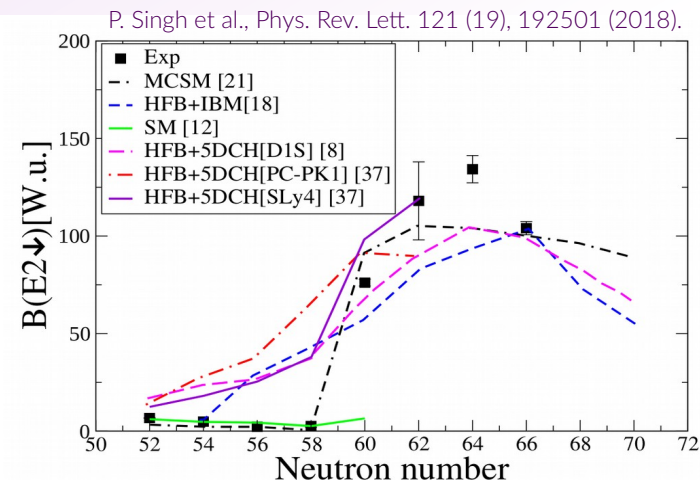
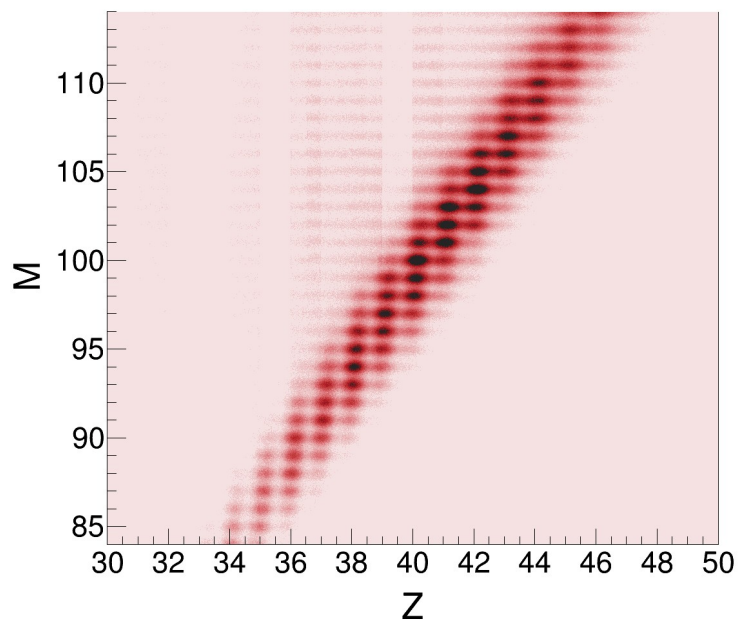
Preliminary results for ^{104}Zr in single γ

J^π	Energy [keV]	τ [ps] single γ
4+	312.3	62 (5)
6+	473.7	4 (2)



Conclusions

- The value of the lifetimes obtained for ^{100}Zr confirm the **strong deformed character** of this system, as predicted from different nuclear models and experimentally investigated.
- The **high efficiency of AGATA** and the **resolution of the VAMOS identification** allow us to measure the lifetime of exotic systems like ^{104}Zr
 - investigation of the trend and the limits of deformation in the $A \sim 100$ region.



- Many lifetimes have been already extracted for even-even isotopes in Zr, Mo and Ru, among which new values for ^{104}Zr , ^{108}Mo , $^{106,108,110,112}\text{Ru}$.
- Precise values of lifetimes and errors estimation in progress
 - many new results in this region.



Thanks for listening

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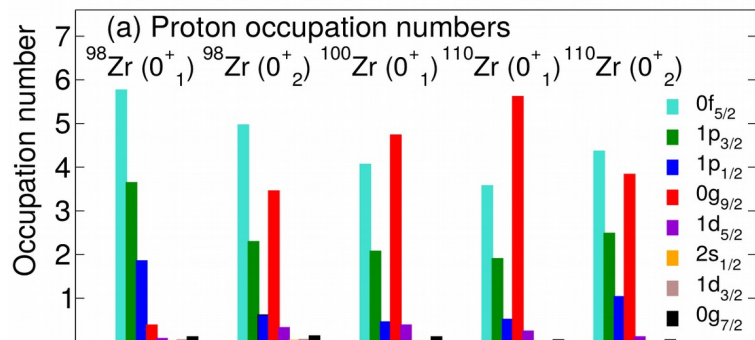
³ *CEA Paris-Saclay, DRF/IRFU/DPhN, Gif-sur-Yvette, France.*

Shape-phase transition in Zr isotopes

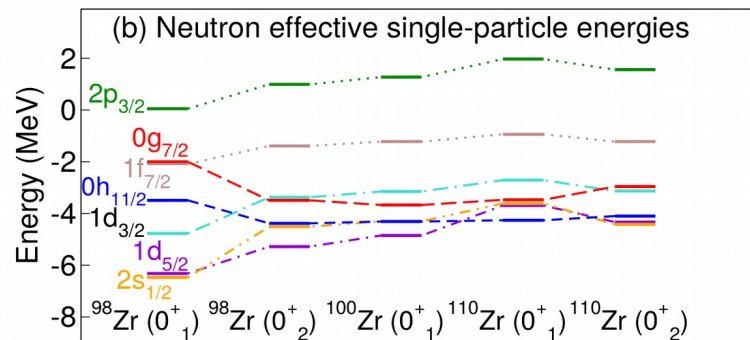
Results from recent MCSM calculations:

T. Togashi, Y. Tsunoda, T. Otsuka and N. Shimizu, Phys. Rev. Lett. 117, 172502 (2016).

The rapid shape change at N=60 appears as a results of shell evolution associated with proton excitation in the $g_{9/2}$.



The increasing number of neutrons increases the split of the spin-orbit partner $g_{7/2}$ - $g_{9/2}$ thus reducing the gap at N=40. Proton particle-hole excitations in the unique-parity orbital $g_{9/2}$ lower the ESPEs of neutron $g_{7/2}$ and $h_{11/2}$ orbitals, favoring quadrupole interactions and the coherent contribution of different configurations.



The ESPEs from $s_{1/2}$ to $g_{7/2}$ shrink abruptly starting from the second 0^+ in ^{98}Zr .

Both protons and neutron act coherently to induce the deformation.

Shape-phase transition in Zr isotopes

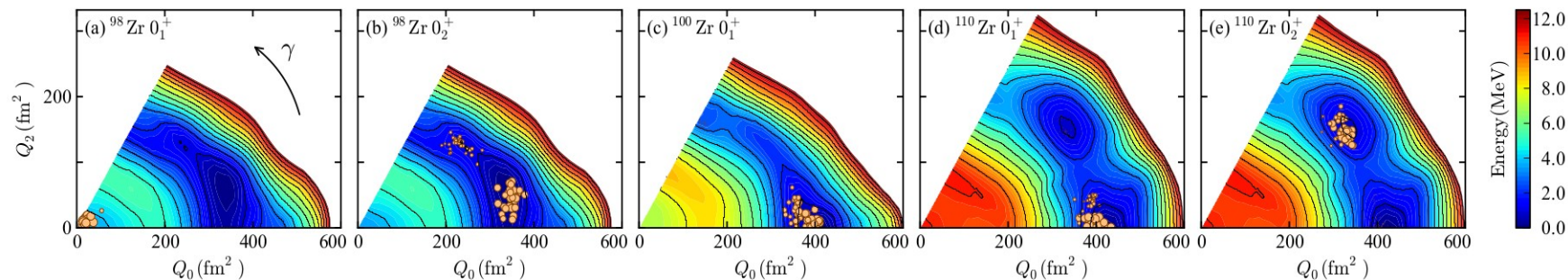
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The crossing of two distinct configurations at N=60 appears in the abrupt change in the ground state structure and is interpreted as a Quantum Phase Transition (QPT) at N=58-60 from “spherical phase” to “deformed phase”.

The lowering of the intruder 0_2^+ state from ^{96}Zr to ^{98}Zr continues in ^{100}Zr where it becomes the ground state.

T-plots for $0_{1,2}^+$ states of $^{98,100,110}\text{Zr}$ isotopes to analyze the intrinsic shape of SM eigenstates:



Shape coexistence have been established for $^{96,98}\text{Sr}$, $^{94,96}\text{Zr}$ and ^{98}Zr , key nucleus for the understanding of QPT.

E. Clément et al., Phys. Rev. Lett. 116, 022701 (2016).

E. Clément et al., Phys. Rev. C 94, 054326 (2016).

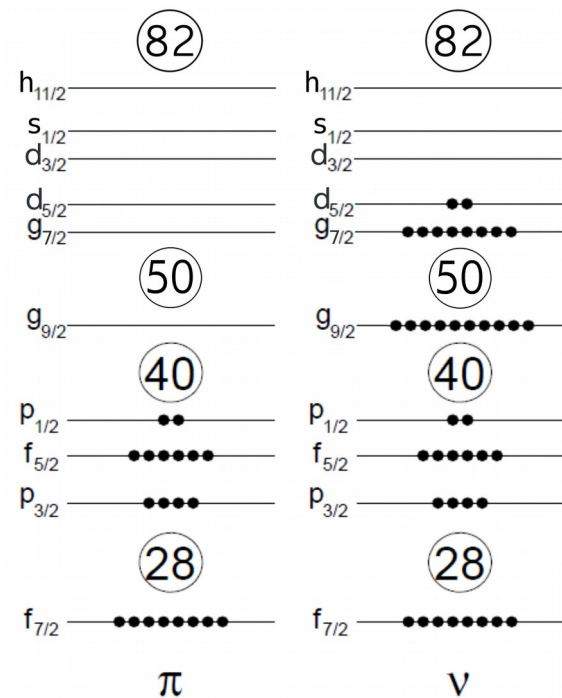
A. Chakraborty, E. E. Peters, B. P. Crider et al., Phys. Rev. Lett. 110, 022504 (2013).

C. Kremer et al., Phys. Rev. Lett. 117, 172503 (2016).

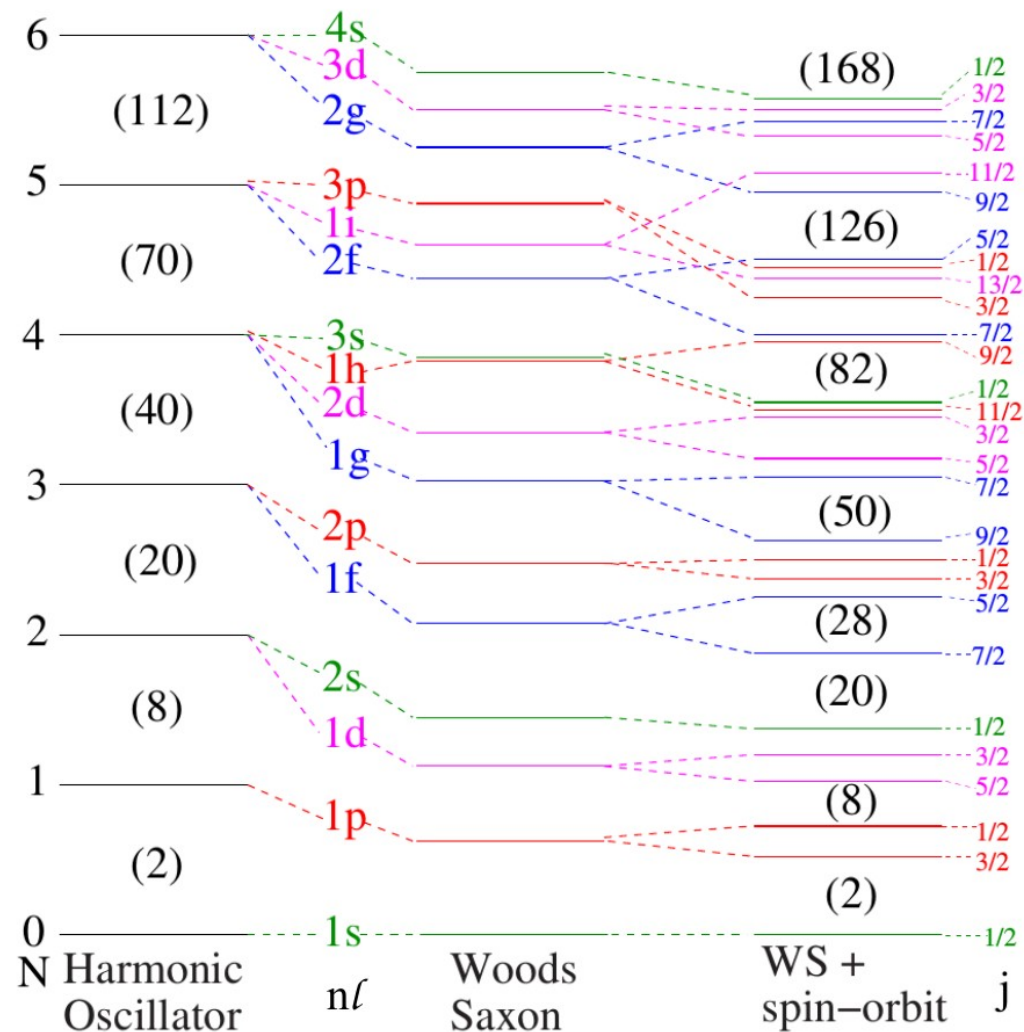
K. Heyde and J. L. Wood, Rev. Mod. Phys. 83, 1467 (2011).

P. Singh et al., Phys. Rev. Lett. 121(19) 192501 (2018).

Shell model orbitals



$^{100}_{40}\text{Zr}_{60}$



Lifetime measurements with the DDCM

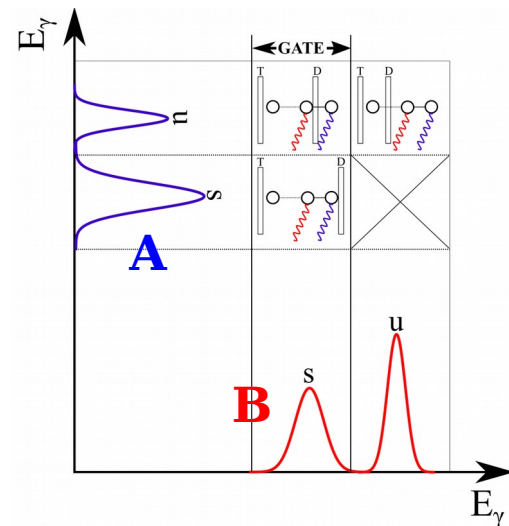
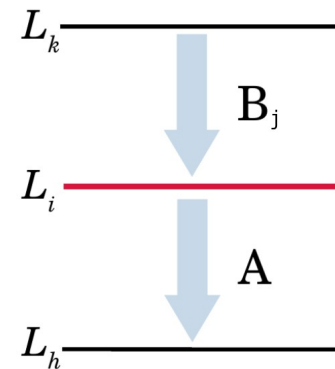
- Lifetime in single γ measurements are analyzed with the DDCM by using the following experimental information:

- the fast (S) and the slow (U) components of the transition A depopulating the state of interest L_i ,
- the fast and the slow components of all observed feeding transitions B_j in the γ -rays spectrum (the α coefficient take into account the feeding contribution from B_j in the lifetime calculation).
- the velocity of the recoiling fragment before the target v_{in} .

$$\tau(x_p) = \frac{-A^U(x_p) + \sum_j b_j \alpha_j B_j^U(x_p)}{v_{in} \frac{dA^U(x_p)}{dx}} \quad \alpha_j(x_p) = \frac{B_j^U(x_p) + B_j^S(x_p)}{A^U(x_p) + A^S(x_p)} \cdot \frac{\epsilon_A}{\epsilon_B}$$

- Lifetime in coincidence $\gamma\gamma$ are analyzed with the DDCM by gating in the shifted component of a direct feeding transition B of the state of interest. No other information about the feeding are needed

$$\tau(x_p) = \frac{\{A_S, B_U\}(x_p)}{\frac{d}{dx} \{A_S, B_S\}(x_p)} \cdot \frac{x_p}{\beta c}$$



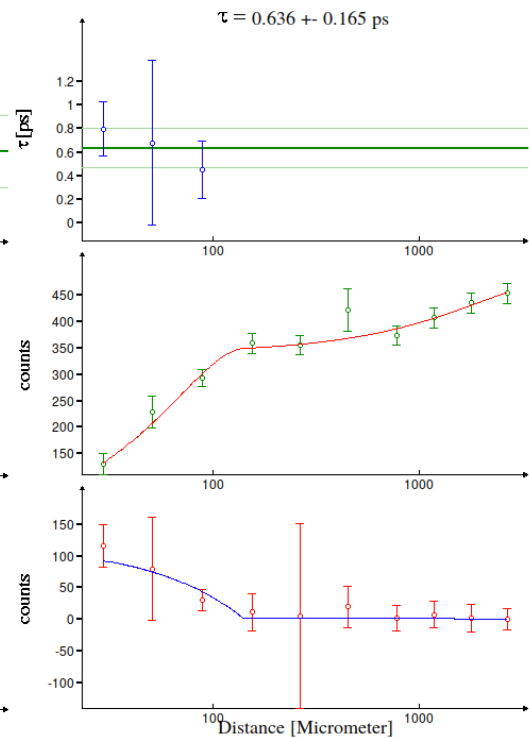
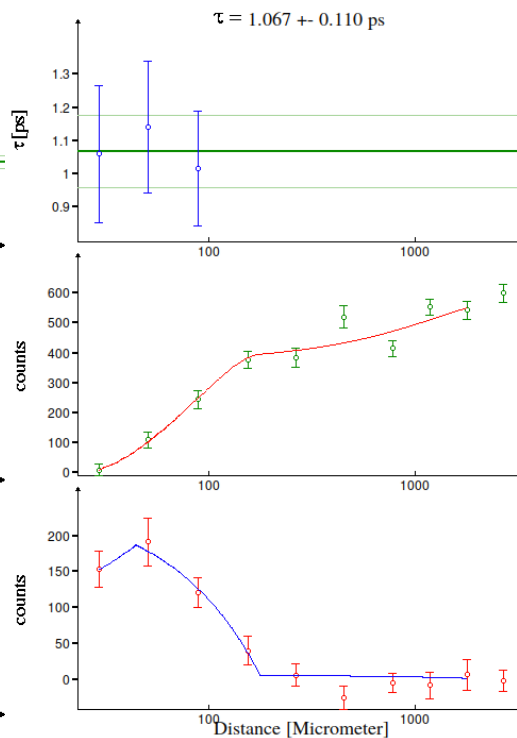
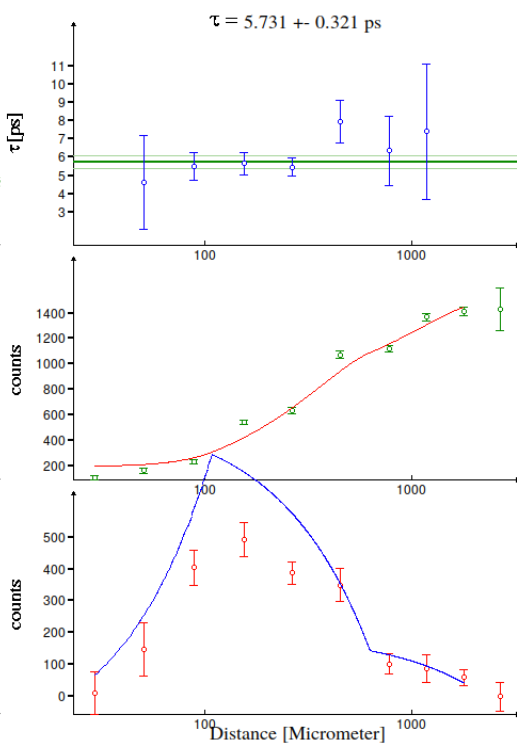
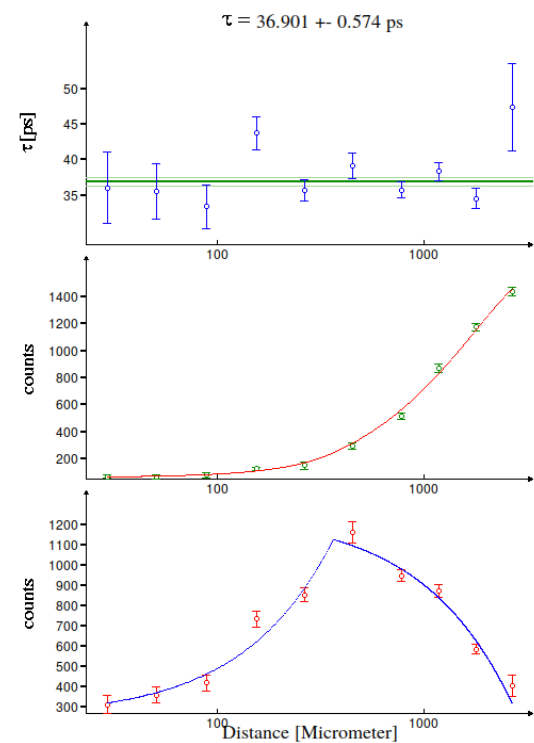
Decay curves for ^{100}Zr in single γ

$$4_1^+ \rightarrow 2_1^+$$

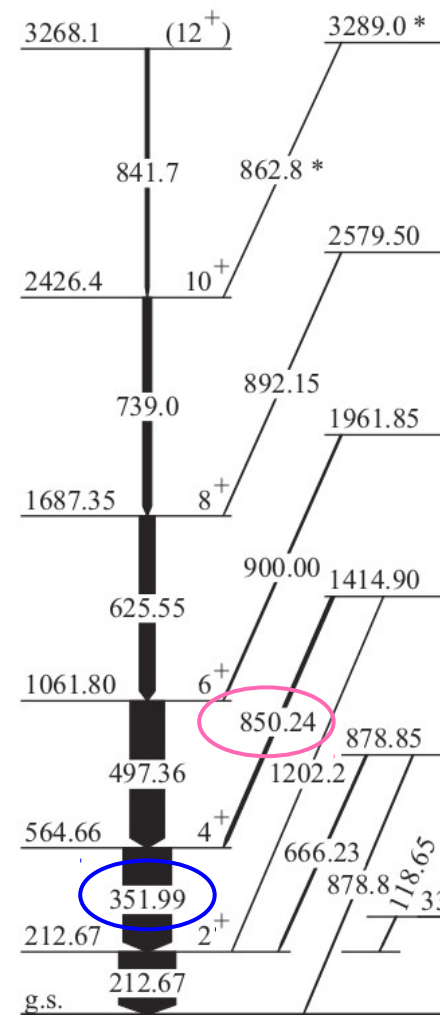
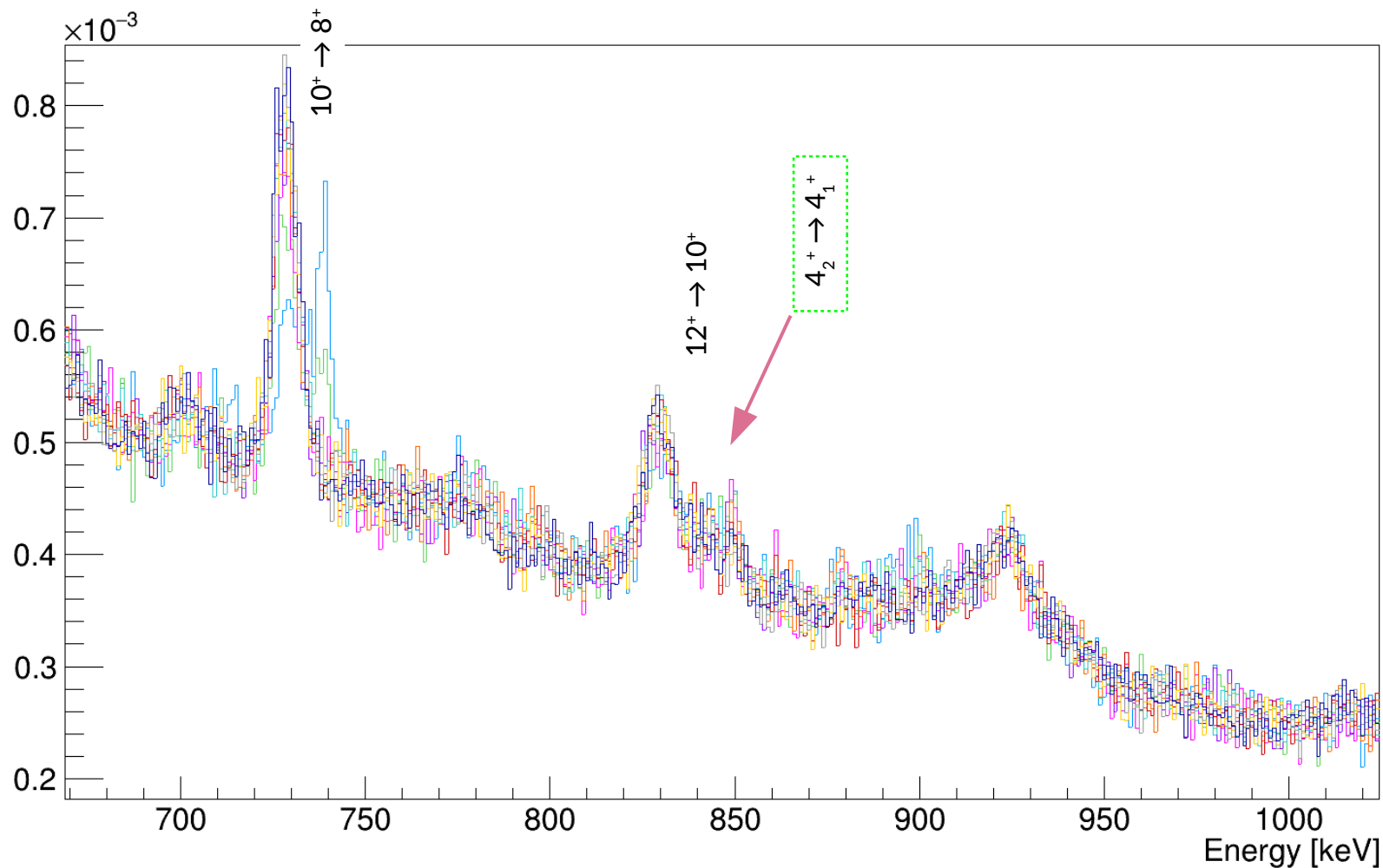
$$6_1^+ \rightarrow 4_1^+$$

$$8_1^+ \rightarrow 6_1^+$$

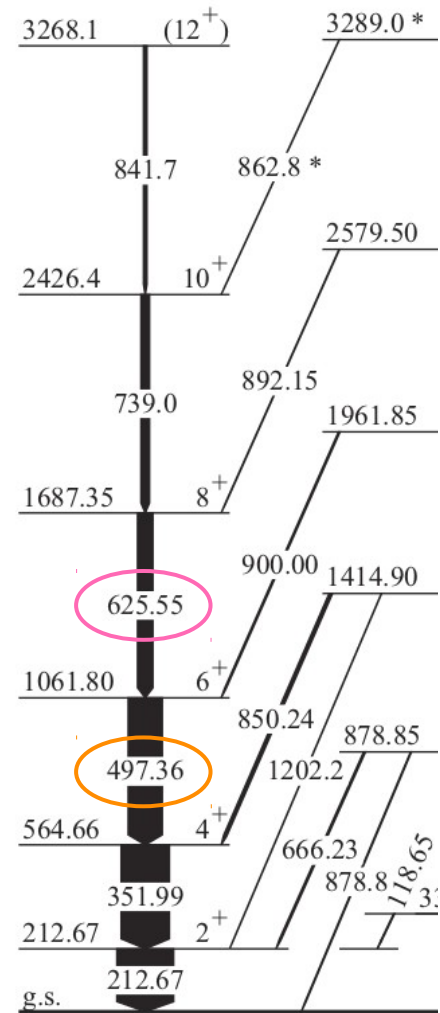
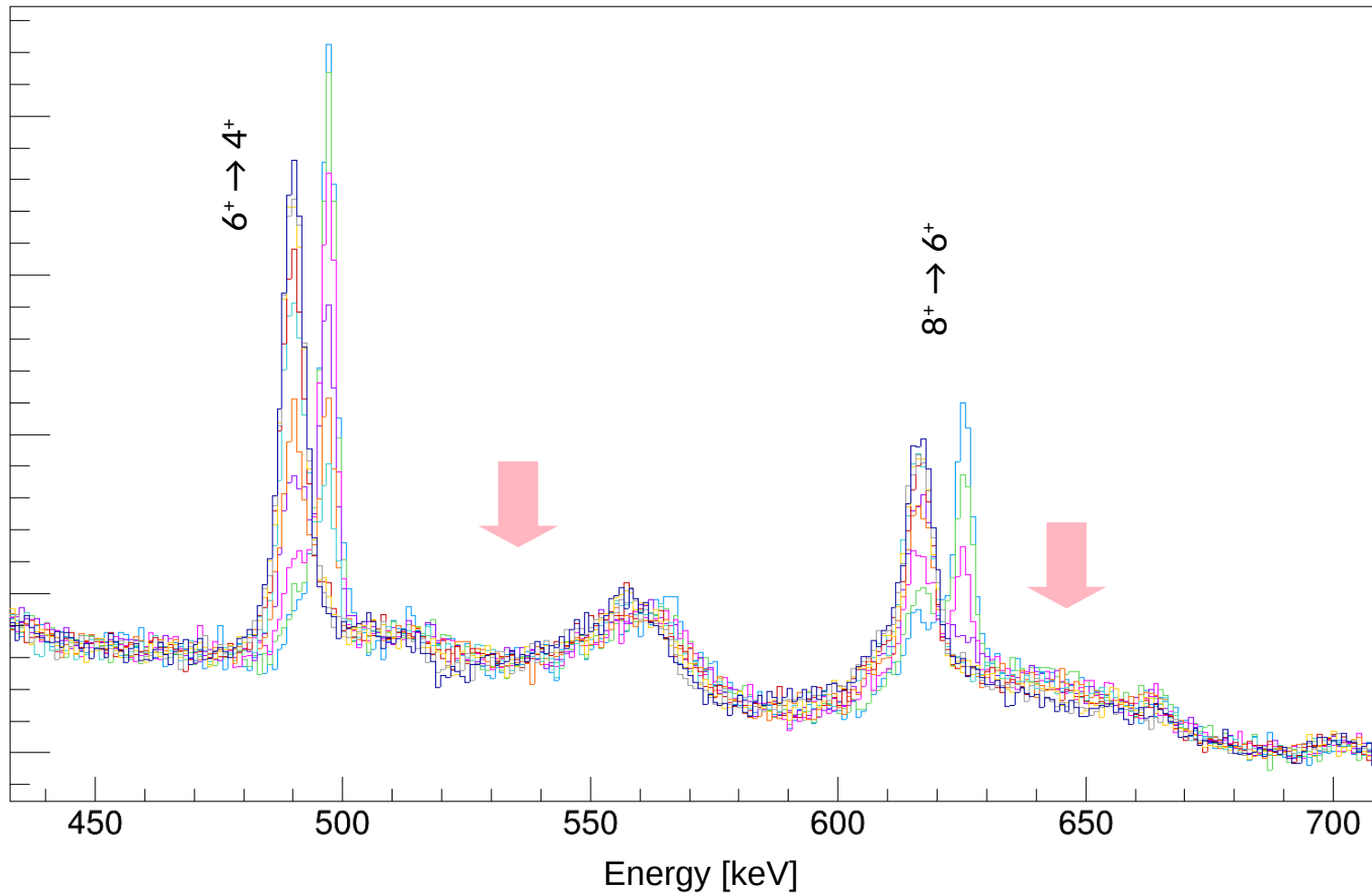
$$10_1^+ \rightarrow 8_1^+$$



Feeding for the 4^+ state in ^{100}Zr



Background around 550 keV and 650 keV state in ^{100}Zr



Preliminary results for ^{100}Zr in coincidence $\gamma\gamma$ – gate and BG subtraction

The analysis in $\gamma\gamma$ revealed problems in its applicability in this case.

→ The small energy difference between shifted and “stopped” peak of the feeding transition makes the set of the gate not easy:

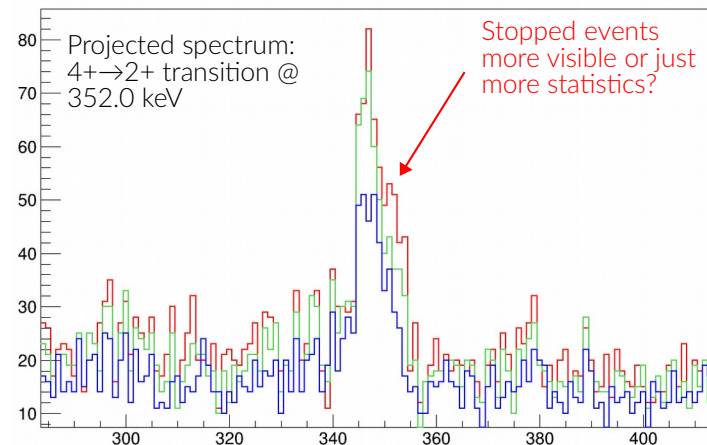
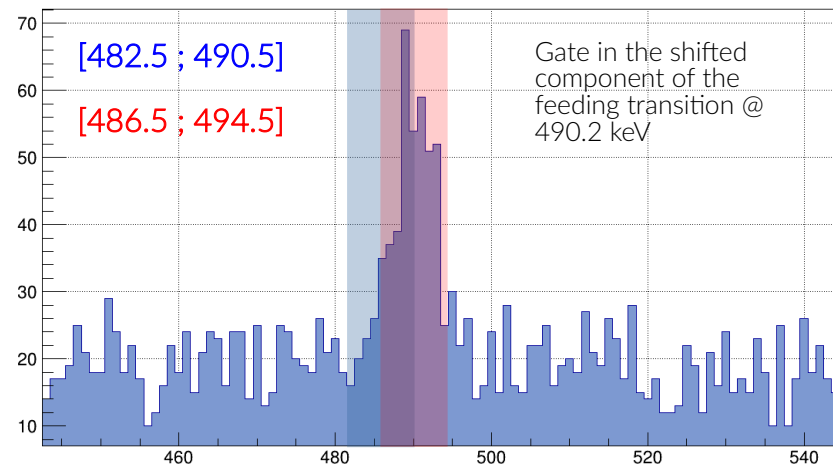
Different gates in the shifted feeding events (one left to avoid “stopped” contaminants, and one centered) lead to different results.

→ The subtraction of the BG also results in a different final value of tau.

When subtracting the BG and/or when using a left gate on the feeder, **the resulting lifetime is short:**

GATE [keV]	τ [ps] no BG sub	τ [ps] with BG sub
482.5, 490.5	32.8 (12)	30.0 (23)
486.5, 494.5	38.4 (25)	37.2 (38)

→ the left gate and the BG subtraction seems the best option for $\gamma\gamma$ analysis



Example of an odd-even system: ^{101}Nb in single γ

Good statistics: many gamma-rays transitions can be resolved in the stooped and shifted component

→ The complexity of the level scheme make the DDCM analysis in single γ impossible for this nucleus.

