

# Precision electroweak physics at the LHC

Mieczyslaw Witold Krasny

University Pierre and Marie Curie, Paris and CERN

Annecy, 11th of December, 2009

# The energy and the precision frontier at the LHC

Present constraints on new (BSM) contact interactions

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM}} + \mathcal{O}/\Lambda^2$$

	operator $\mathcal{O}$	affects	present constraint on $\Lambda$
	$\frac{1}{2}(\bar{L}\gamma_\mu\tau^a L)^2$	$\mu$ -decay	10 TeV
	$\frac{1}{2}(\bar{L}\gamma_\mu L)^2$	LEP 2	5 TeV
T $\rightarrow$	$ H^\dagger D_\mu H ^2$	$\theta_W$ in $M_W/M_Z$	5 TeV
S $\rightarrow$	$(H^\dagger\tau^a H)W_{\mu\nu}^a B_{\mu\nu}$	$\theta_W$ in $Z$ couplings	8 TeV
	$i(H^\dagger D_\mu\tau^a H)(\bar{L}\gamma_\mu\tau^a L)$	$Z$ couplings	10 TeV
	$i(H^\dagger D_\mu H)(\bar{L}\gamma_\mu L)$	$Z$ couplings	8 TeV
$\Rightarrow$	$H^\dagger(\bar{D}\lambda_D\lambda_U\lambda_U^\dagger\gamma_{\mu\nu}Q)F^{\mu\nu}$	$b \rightarrow s\gamma$	5 TeV
$\Rightarrow$	$1/2(\bar{Q}\lambda_U\lambda_U^\dagger\gamma_\mu Q)^2$	$B$ mixing	6 TeV
$\Rightarrow$	$1/2(\bar{Q}\lambda_U\lambda_U^\dagger\gamma_\mu Q)^2$	$K$ mixing	6 TeV

The BSM discovery programme at the 10 (14?) TeV collider must be a precision measurements programme...

.... as much as the Standard Model “unitarity-cure” programme:

$$\mathcal{L}_{SM} = -\frac{1}{4}F_{\mu\nu}^a F^{a\mu\nu} + i\bar{\psi}D\psi \quad \text{The gauge sector}$$
$$+ \psi_i \lambda_{ij} \psi_j h + h.c. \quad \text{The flavor sector}$$
$$+ |D_\mu h|^2 - V(h) \quad \text{The EWSB sector}$$

### Challenges:

1. Understanding of the production, propagation, interactions, and decays of polarized electroweak bosons (not discussed in this talk) .
2. Precision measurements of the Standard Model parameters

# Electroweak Standard Model

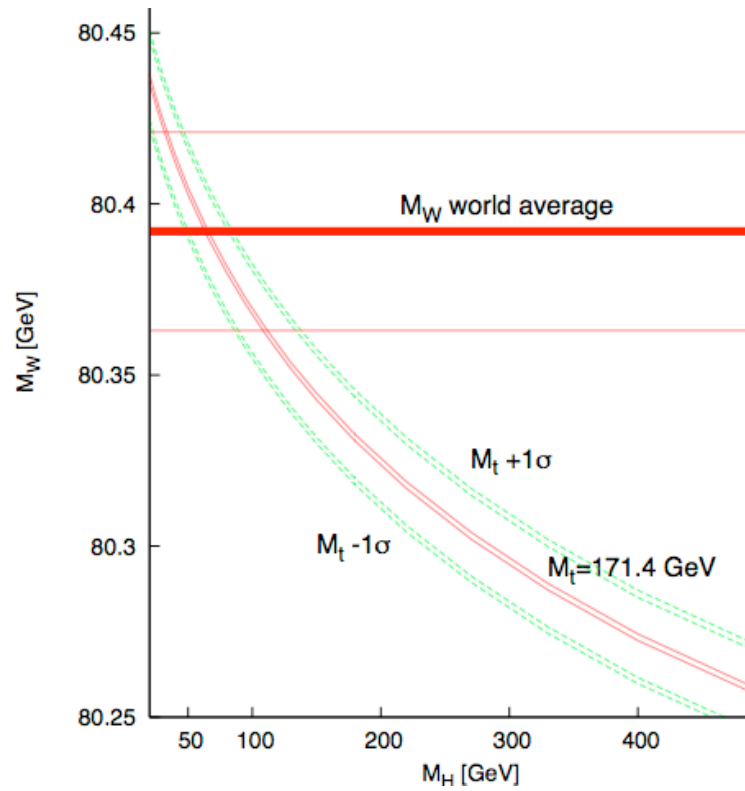
$\alpha, M_Z, G_F$



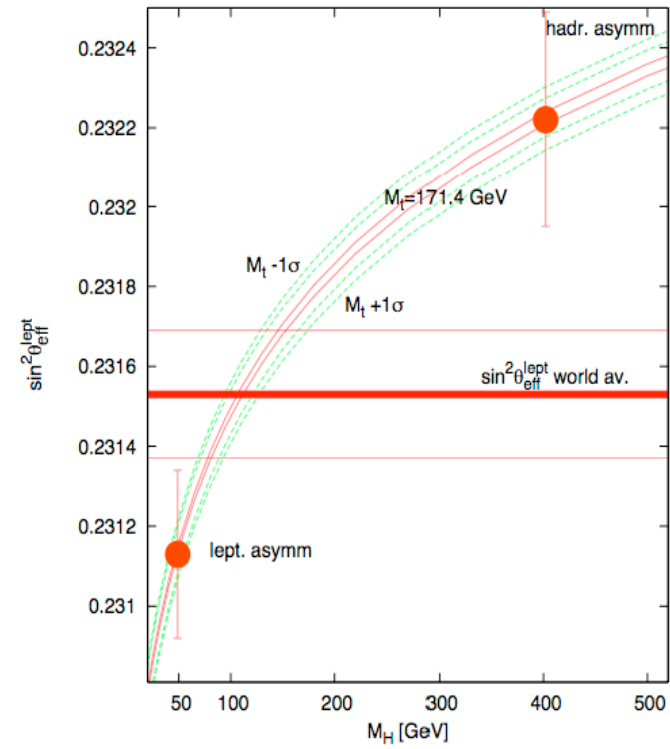
higgs?, supersymmetry?, ...any field theory

$M_W, \sin^2(\theta_W), \Gamma_W, \dots$

# Precision goals



precision target  $\sim 10$  MeV



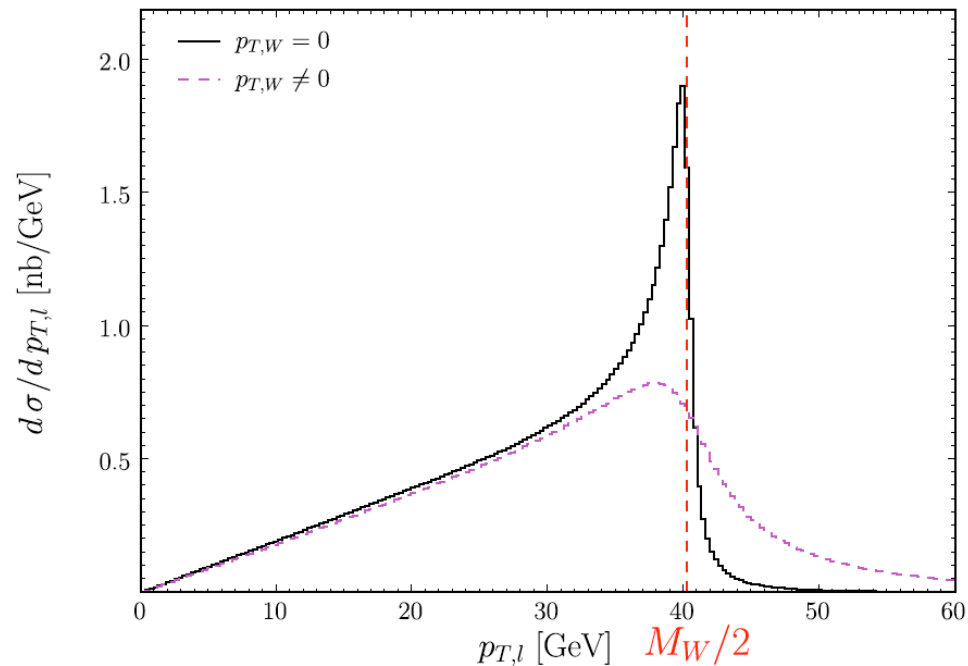
precision target  $\sim 0.0001$

...can we improve the  
measurement precision of  
the Standard Model  
parameters at the LHC?

Official reply of CMS and ATLAS:

**YES**

$M_W$  and  $\Gamma_W$  are determined from  $p_{t,l}$  distribution...



- factor **4000** between 40 GeV and  $\Delta(M_W) = 10$  MeV
- **utmost care** needed to anything that affects  $p_{t,l}$

(...those which affect  $W^+$ ,  $W^-$  and Z boson in a different way...)

# EXAMPLE:

## The $M_W$ measurement at the LHC - perspectives

Source	Effect	$\partial m_W / \partial_{rel} \alpha$ (MeV/%)	$\delta_{rel} \alpha$ (%)	$\delta m_W$ (MeV)
Prod. Model	W width	1.2	0.4	0.5
	$y^W$ distribution	—	—	1
	$p_T^W$ distribution	—	—	3
	QED radiation	—	—	<1 (*)
Lepton measurement	Scale & lin.	800	0.005	4
	Resolution	1	1.0	1
	Efficiency	—	—	4.5 (e); <1 ( $\mu$ )
Recoil measurement	Scale	—	—	—
	Resolution	—	—	—
Backgrounds	$W \rightarrow \tau \nu$	0.15	2.5	2.0
	$Z \rightarrow \ell(\ell)$	0.08	2.8	0.3
	$Z \rightarrow \tau \tau$	0.03	4.5	0.1
	Jet events	0.05	10	0.5
Pile-up and U.E			<1 (e); $\sim 0(\mu)$	
Beam crossing angle			<0.1	
Total ( $p_T^\ell$ )			$\sim 7$ (e); 6 ( $\mu$ )	

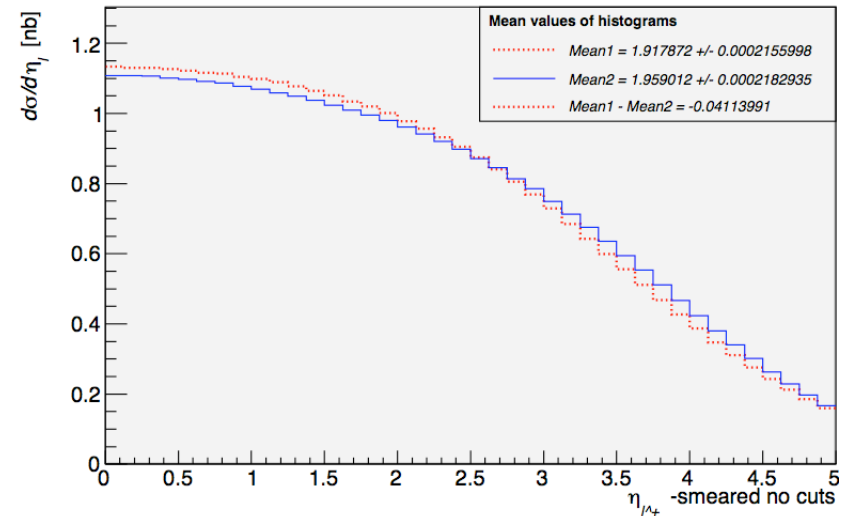
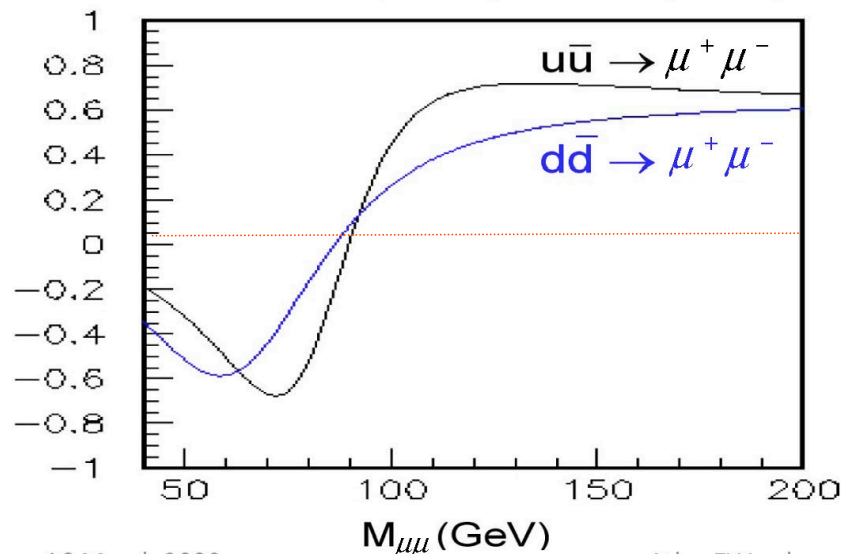
contribution to the Philadelphia ICHEP 2008 and EPS 2009 conference



$\sin^2(\theta_W)$  is determined from forward-backward asymmetry of positive and negative leptons...

$$A_{\text{FB}} = \frac{3}{4} \frac{-2q_q a_q a_\ell \text{Re}(\chi) + 2v_q a_q 2v_\ell a_\ell |\chi|^2}{q_q^2 - 2q_q v_q v_\ell \text{Re}(\chi) + (v_q^2 + a_q^2)(v_\ell^2 + a_\ell^2) |\chi|^2}; \quad \chi(\hat{s}) = \frac{\sqrt{2}G_F}{16\pi\alpha} \frac{\hat{s}M_Z^2}{\hat{s} - M_Z^2 + i\hat{s}\Gamma_Z/M_Z}$$

$$a_f = 2I_3^f; \quad v_f = 2I_3^f - 4q_f \sin^2 \theta_W; \quad f = q, \ell$$



# The $\sin^2(\theta_W)$ measurement at the LHC - perspectives

Source	$\delta A_{FB}$ (abs)	$\delta \sin^2 \theta_{eff}^{lept}$ (abs)
Energy scale	$2.7 \times 10^{-5}$	$1.5 \times 10^{-5}$
Reco. Eff.	$3.4 \times 10^{-5}$	$1.9 \times 10^{-5}$
Energy resol.	$1.9 \times 10^{-6}$	$1.1 \times 10^{-6}$
Charge ID	$2.6 \times 10^{-5}$	$1.4 \times 10^{-5}$
Background subtraction.	$< 10^{-5}$	$< 10^{-5}$
PDFs	-	$-2.4 \times 10^{-4}$ $+1.3 \times 10^{-4}$
$a$ and $b$ parameters	-	$3 \times 10^{-5}$
Statistical error	$2.7 \times 10^{-4}$	$1.5 \times 10^{-4}$

Table 4: Summary of the systematic and statistical uncertainties on  $A_{FB}$  and  $\sin^2 \theta_{eff}^{lept}$  for events with at least one electron in the central region (C-F). The uncertainty on  $\sin^2 \theta_{eff}^{lept}$  is determined using Eqs. 11 and  $a$  and  $b$  parameters from figure 21.

**BUT...**

...at the **LHC** we collide  $pp$

not  $p\bar{p}$  like at the Tevatron

# Symmetry relations not at work!

(need to understand the charge and polarization asymmetries in  $W$  and  $Z$  production)

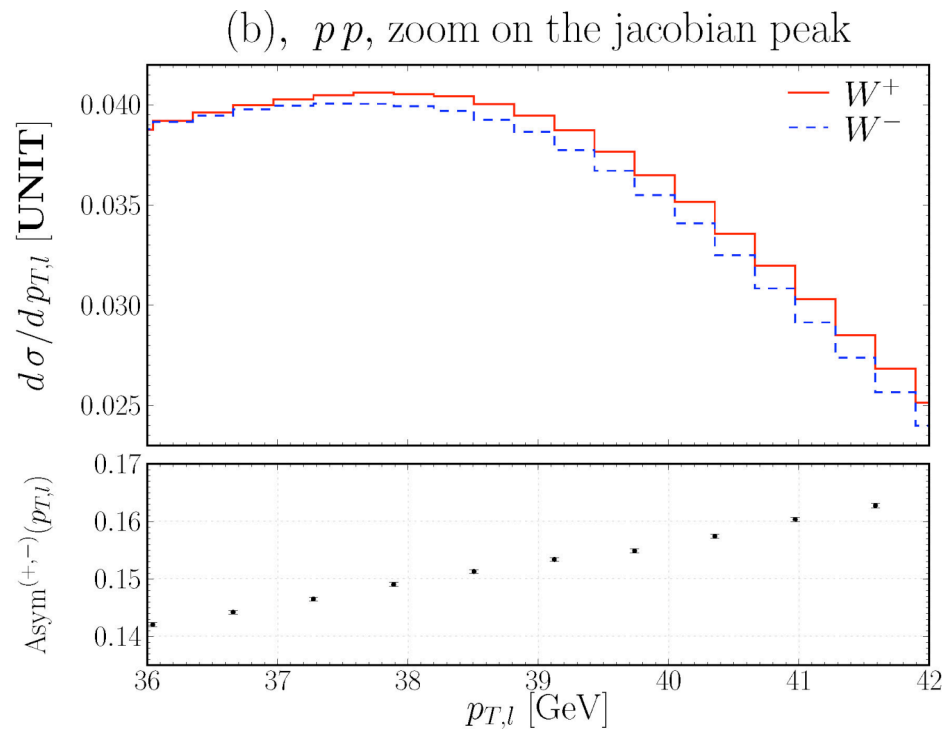
---

...also:

Collisions at much higher energy!

(need to understand heavy flavours with much better precision)

# Charge asymmetries

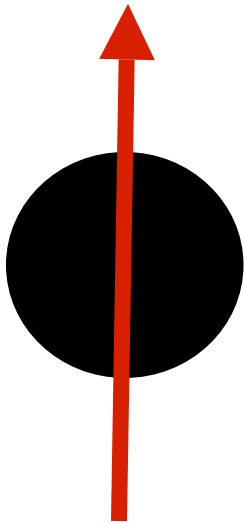


relative shifts of peak position estimated using a parabola fit in the range:

$$37 \text{ GeV} < p_{T,l} < 40 \text{ GeV}$$

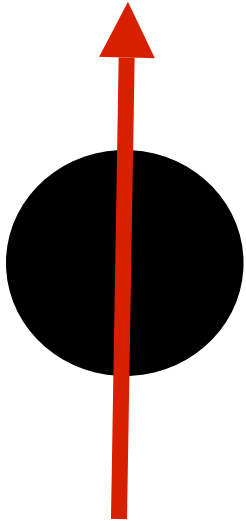
phase space domain	$\varpi_+ - \varpi_-$ [MeV]
Inclusive	170
$ y_W  < 0.3$	-100
$ \eta  < 0.3$	-240
$3.5 <  y_W  < 4.5$	300
$3.5 <  \eta  < 4.5$	2000

( $M_{W^+} - M_{W^-}$  biases at the level of  $\sim(200 - 4000)$  MeV ...at the Tevatron 0 MeV)



- $\theta =$  lepton emission angle w.r.t. spin vector
- $W(\theta) = 1 + \cos(\theta)$
- reflects V-A coupling

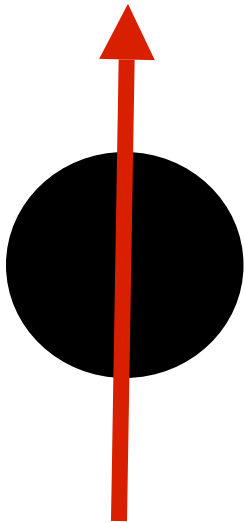
$$W^- \rightarrow l^- \nu$$



- $W(\theta) = 1 - \cos(\theta)$



$$Z \rightarrow l^+ l^-$$

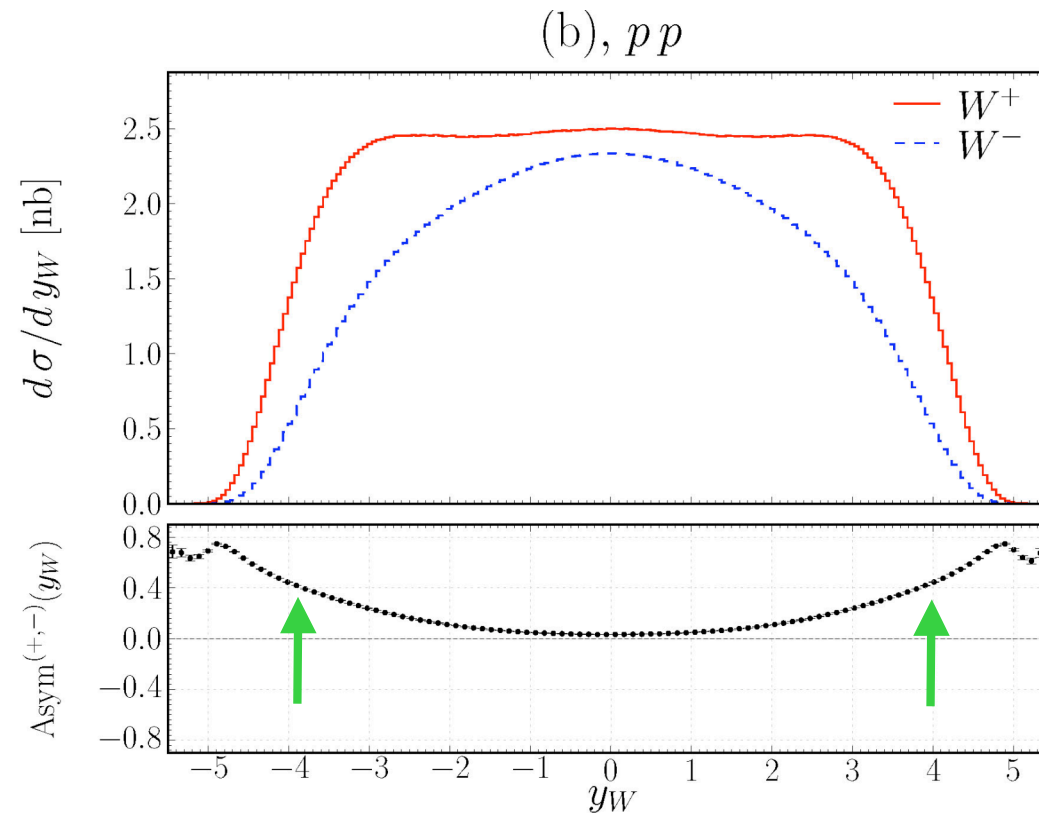


- $W(\theta) = \alpha + \beta \cos(\theta)$
- reflects mixture of V-A and V+A coupling

---

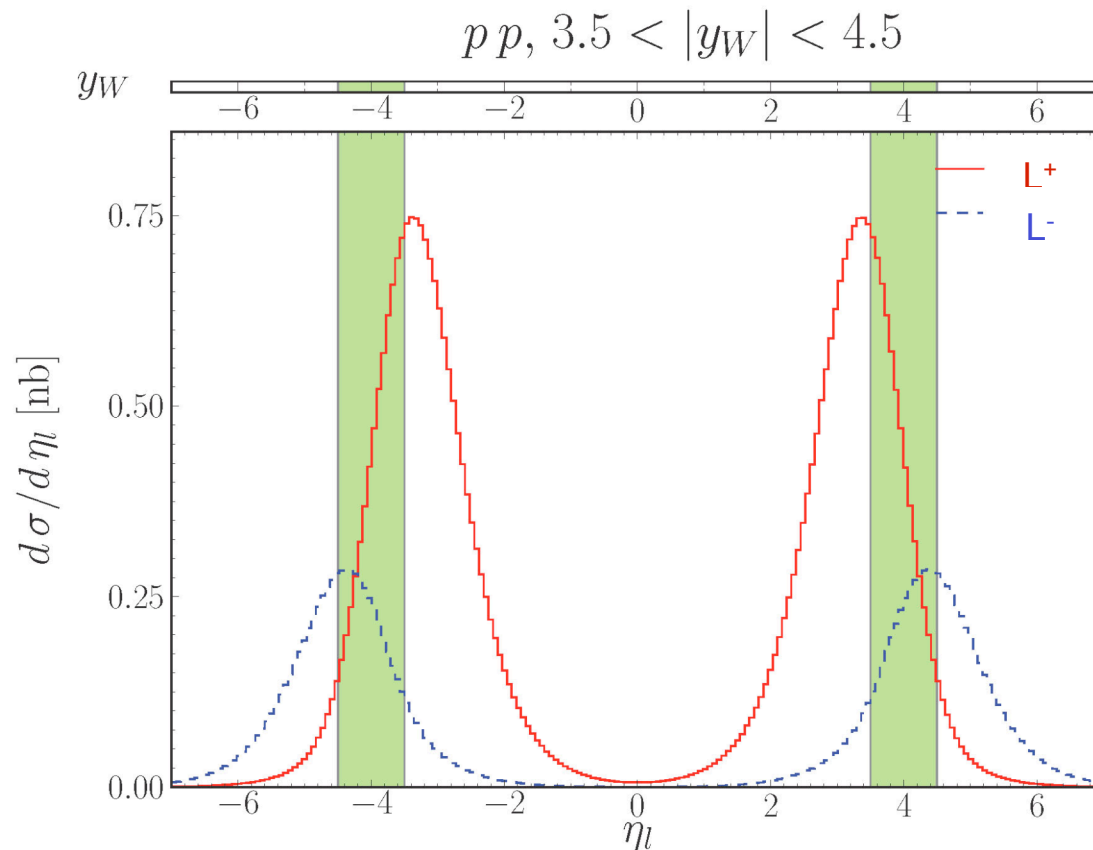
At the Tevatron symmetry relations at work:  $N_{W^+} = N_{W^-}$  and lepton angular distribution for  $Z$  almost the same as for  $W^+ + W^-$

# W production and decay pp collisions



Note:  $N_{W^+} > N_{W^-}$

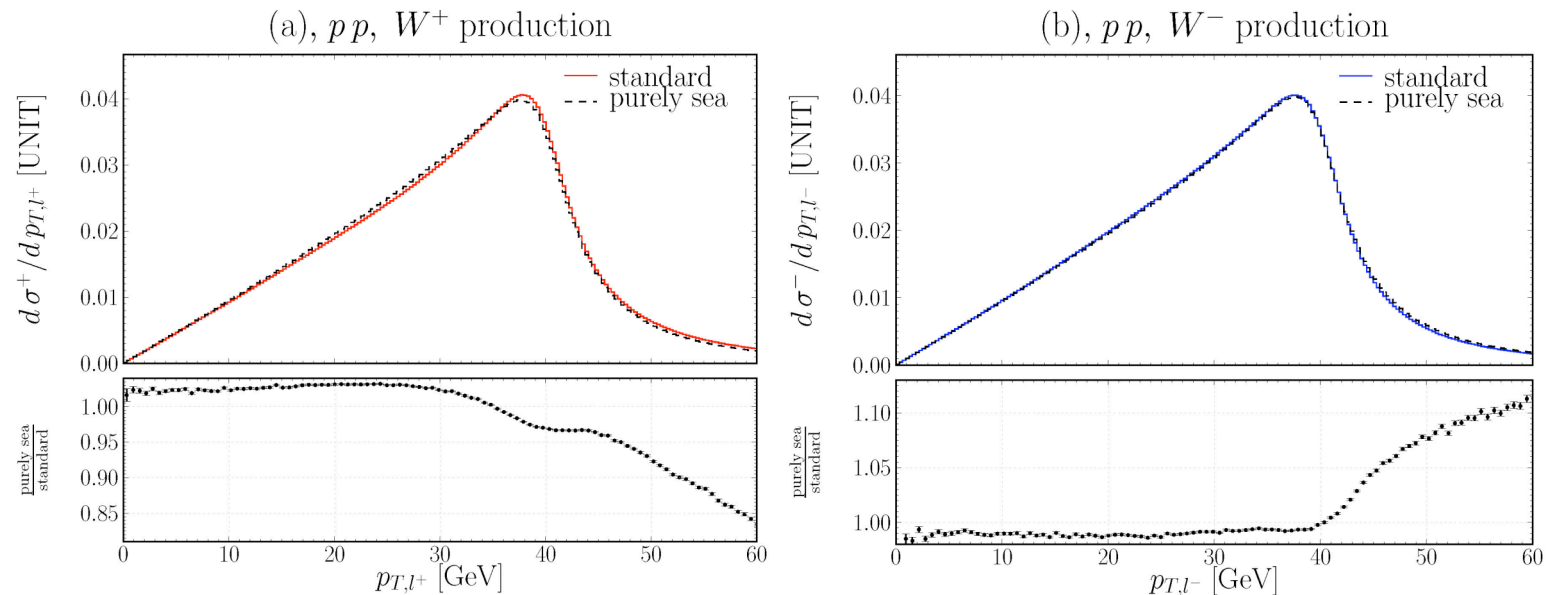
# W production and decay pp collisions



Note: opposite migration direction for  $L^+$  and  $L^-$

The asymmetry between  $W^+$  and  $W^-$  in pp collisions is driven by the asymmetry between quarks and antiquarks in the proton, generated by the valence quarks.

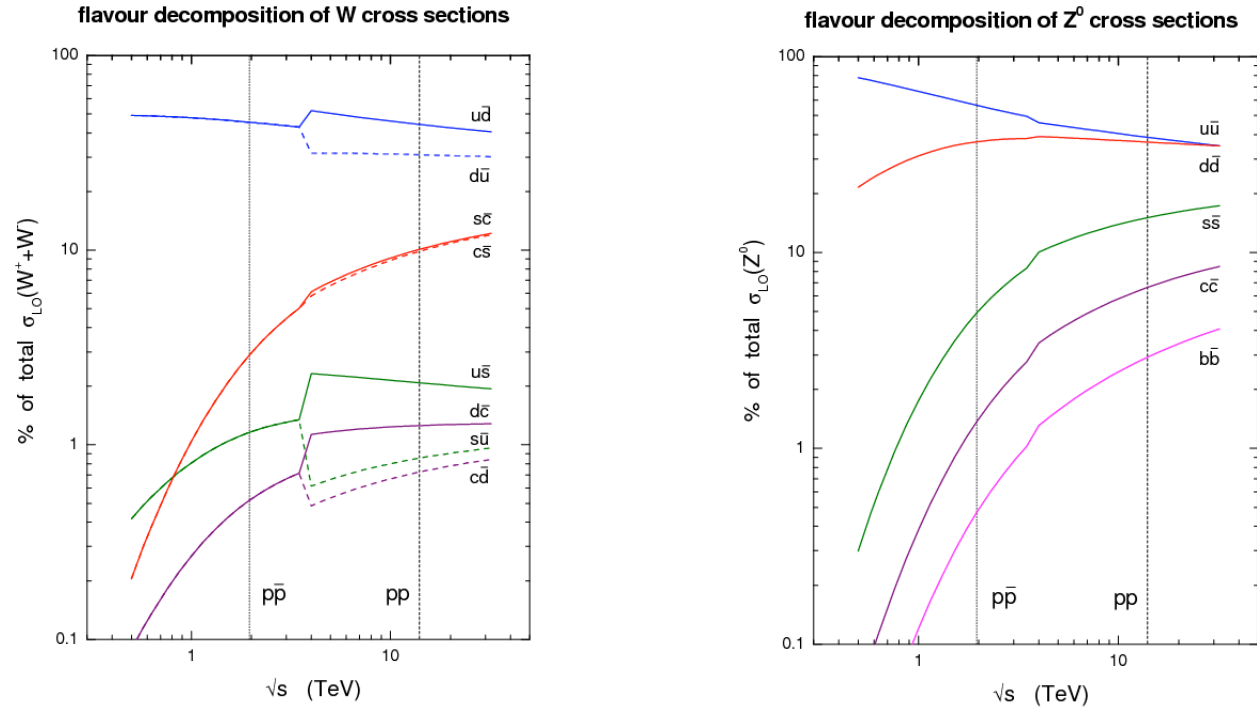
# Example: Valence quark effects in W mass measurement



estimated shifts of the peak position due to polarisation effects		
Fit range	Channel	$\varpi_{\text{standard}} - \varpi_{\text{sea}}$ [MeV]
$37 \text{ GeV} < p_{T,l} < 52 \text{ GeV}$	$W^+$	178.0
	$W^-$	-23.8

( $M_W$  biases at the level of  $\sim 400$  MeV ...at the Tevatron 0 MeV)

# Flavour asymmetries



BERGE, NADOLSKY, AND OLNESS

PHYSICAL REVIEW D **73**, 013002 (2006)

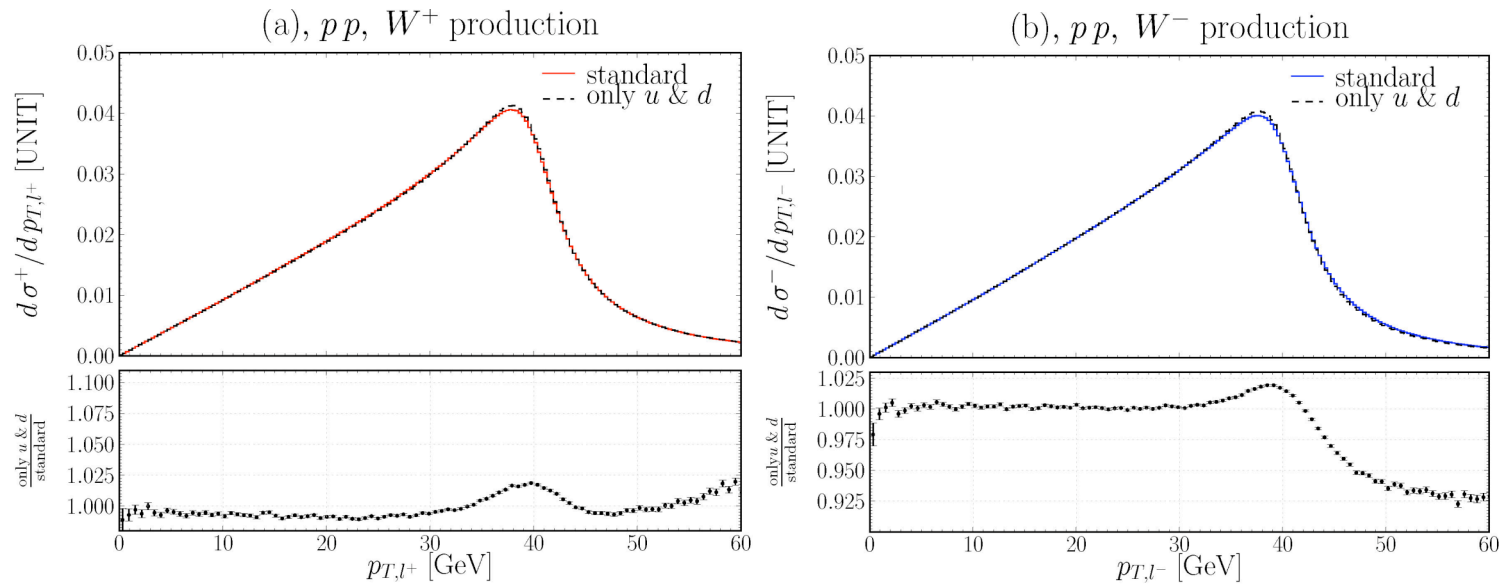
TABLE I. Partial contributions  $\sigma_{q\bar{q}}/\sigma_{\text{tot}}$  of quark-antiquark annihilation subprocesses to the total Born cross sections in  $W^+$  and  $Z^0$  boson production at the Tevatron and LHC (in percent).

Subprocesses	$W^+$					$W^-$					$Z^0$				
	$u\bar{d}$	$u\bar{s}$	$c\bar{d}$	$c\bar{s}$	$c\bar{b}$	$d\bar{u}$	$s\bar{u}$	$d\bar{c}$	$s\bar{c}$	$b\bar{c}$	$u\bar{u}$	$d\bar{d}$	$s\bar{s}$	$c\bar{c}$	$b\bar{b}$
Tevatron Run-2	90	2	1	7	0	90	2	1	7	0	57	35	5	2	1
LHC	74	4	1	21	0	67	2	3	28	0	36	34	15	9	6

Heavy flavour effects are driven by the asymmetries in the momentum distribution of heavy and light quarks - reflecting asymmetries in quark masses

(at the LHC the heavy quark effects are no longer small and must be experimentally controlled)

# Example: Heavy flavour effects in W mass measurement



estimated shifts of the peak position due to the presence of heavy quarks in the Wide Band Partonic Beam (WBPB)

Fit range	Channel	$\varpi_{\text{standard}} - \varpi_{\text{only } u, d}$ [MeV]
$37 \text{ GeV} < p_{T,l} < 52 \text{ GeV}$	$W^+$	-69.9
	$W^-$	-59.2

( $M_W$  biases at the level of  $\sim 150$  MeV ...at the Tevatron  $< 30$  MeV)



- $W^+$  from  $ud\bar{d} + us\bar{s} + ub\bar{b} + cd\bar{d} + cs\bar{s} + \dots$
- $W^-$  from  $d\bar{u} + d\bar{c} + s\bar{u} + s\bar{c} + \dots$
- $Z$  from  $u\bar{u} + d\bar{d} + s\bar{s} + c\bar{c} + b\bar{b} + \dots$

different pdf's  
 different couplings  
 different  $k_T$ 's  
 different masses

As a consequence, at the LHC:

- different  $p_{T,W^+}$ ,  $p_{T,W^-}$ , and  $p_{T,Z}$  spectra
- different polarizations
- different  $p_{T,l}$  spectra

Common root of the problems at the LHC:

## Interplay of the charge, polarization and flavour effects

- In all LHC studies ignored so far
- Improving the precision of the SM parameters at the LHC is not realistic unless...

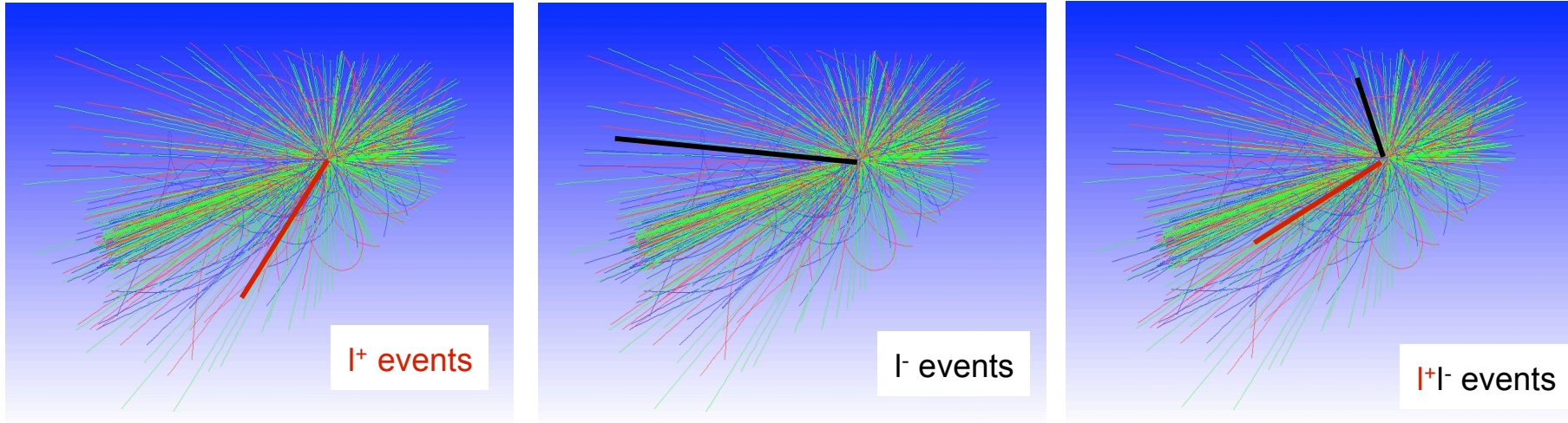
... dedicated LHC-specific measurement methods are developed...

the rest of my talk will be devoted to the presentation of a global, LHC-dedicated strategy to measure the standard model parameters...

# The measurement and the tools for its simulation

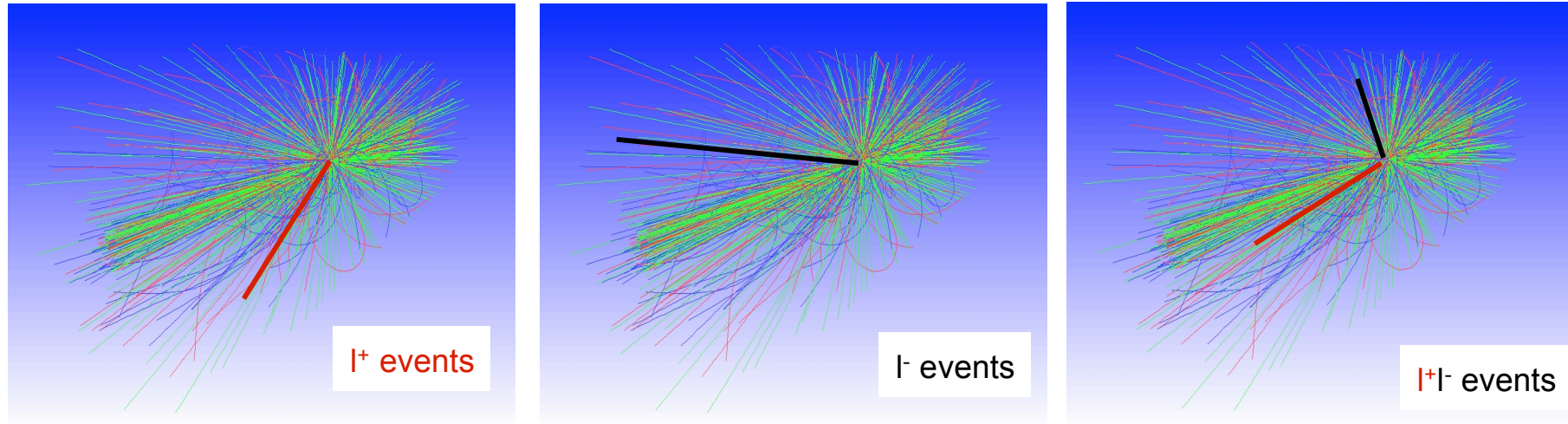
- Apparatus: **The ATLAS detector**
- Luminosity:  **$10 \text{ fb}^{-1}$**
- Trigger and Acceptance cuts:  **$p_{T,l} > 20 \text{ GeV}/c$ ,  $|\eta_l| < 2.5$**
- Dedicated event generators: **WINHAC/ZINHAC** (spin amplitudes)
- Simulation: parameterized response of the ATLAS detector
- Challenge: study based on  **$O(10^{10})$  simulated events**
- The team: **F. Fayette (PhD- 2009) now in Univ. Goetingen, W. Placzek, K. Rejzner (master-2009) now in Univ. Hamburg, A. Siodmok (PhD-2009) now in Univ. Karlsruhe, M.W. Krasny**  
- IN2P3-COPIN cooperation program 05-116

# Observables



- $O_{W^+}(p_{T,l}, \eta_l) = \frac{d^2\sigma}{dp_{T,l^+}d\eta_{l^+}}$  (“ $l^+$  events”),
- $O_{W^-}(p_{T,l}, \eta_l) = \frac{d^2\sigma}{dp_{T,l^-}d\eta_{l^-}}$  (“ $l^-$  events”),
- $O_{Z/\gamma}(M_{ll}, p_{T,ll}, y_{ll}) = \frac{d^3\sigma}{dM_{ll}dp_{T,ll}dy_{ll}}$  (“ $l^+l^-$  events”),
- $O_{(Z/\gamma)^+}(M_{ll}, p_{T,ll}, y_{ll}, p_{T,l}, \eta_l) = \frac{d^5\sigma}{dM_{ll}dp_{T,ll}dy_{ll}dp_{T,l^+}d\eta_{l^+}}$  (“ $l^+l^-$  events”),
- $O_{(Z/\gamma)^-}(M_{ll}, p_{T,ll}, y_{ll}, p_{T,l}, \eta_l) = \frac{d^5\sigma}{dM_{ll}dp_{T,ll}dy_{ll}dp_{T,l^-}d\eta_{l^-}}$  (“ $l^+l^-$  events”).

## ...and their interpretation



- $O_{W^+} = T_{W^+}(\epsilon_{l^+}, u, d, s, c, \bar{u}, \bar{d}, \bar{s}, \bar{c}, M_{W^+}, \Gamma_{W^+}),$
- $O_{W^-} = T_{W^-}(\epsilon_{l^-}, u, d, s, c, \bar{u}, \bar{d}, \bar{s}, \bar{c}, M_{W^-}, \Gamma_{W^-}),$
- $O_{Z/\gamma} = T_{Z/\gamma}(\epsilon_{l^-}, \epsilon_{l^+}, u, d, s, c, b, \bar{u}, \bar{d}, \bar{s}, \bar{c}, \bar{b}, M_Z, \Gamma_Z, \sin^2(\theta_W), \alpha_{EM}),$
- $O_{(Z/\gamma)^+} = T_{(Z/\gamma)^+}(\epsilon_{l^+}, u, d, s, c, b, \bar{u}, \bar{d}, \bar{s}, \bar{c}, \bar{b}, M_Z, \Gamma_Z, \sin^2(\theta_W), \alpha_{EM}),$
- $O_{(Z/\gamma)^-} = T_{(Z/\gamma)^-}(\epsilon_{l^+}, u, d, s, c, b, \bar{u}, \bar{d}, \bar{s}, \bar{c}, \bar{b}, M_Z, \Gamma_Z, \sin^2(\theta_W), \alpha_{EM}).$

$\epsilon$  -calibration scale of lepton momentum,  $\mathbf{k}_t$  -unintegrated partonic distributions:  $q(x, \mathbf{k}_t, M_{\text{scale}})$ , parameters of the Standard Model

# Precision observables

1. 
$$\text{Asym}_W^{(+,-)}(p_{T,l}, \eta) = \frac{O_{W^+}(p_{T,l}, \eta) - O_{W^-}(p_{T,l}, \eta)}{O_{W^+}(p_{T,l}, \eta) + O_{W^-}(p_{T,l}, \eta)},$$
  $\rightarrow$  sensitive to  $M_{W^+}$ -  $M_{W^-}$  and  $\Gamma_{W^+}$  -  $\Gamma_{W^-}$

2. 
$$\text{Asym}_Z^{(+,-)}(y_u, p_{T,u}, p_{T,l}, \eta) = \frac{O_{Z^+}(y_u, p_{T,u}, p_{T,l}, \eta) - O_{Z^-}(y_u, p_{T,u}, p_{T,l}, \eta)}{O_{Z^+}(y_u, p_{T,u}, p_{T,l}, \eta) + O_{Z^-}(y_u, p_{T,u}, p_{T,l}, \eta)},$$
  $\rightarrow$  sensitive to  $\sin^2(\theta_W)$

3. 
$$R_{WZ}(p_{T,l}, \eta) = \frac{O_{W^+}(p_{T,l}, \eta) + O_{W^-}(p_{T,l}, \eta)}{O_{Z^+}(p_{T,l}, \eta) + O_{Z^-}(p_{T,l}, \eta)},$$
  $\rightarrow$  sensitive to  $\alpha_s$ ,  $M_{W^+}$ +  $M_{W^-}$ , and  $\Gamma_{W^+}$  +  $\Gamma_{W^-}$

4. 
$$R_Z^{norm}(p_{T,u}, y_u) = \frac{O_Z(p_{T,u}, y_u)}{O_{l^+l^-}^{norm}},$$

$$O_Z(p_{T,u}, y_u) = \int_{M_Z - 3\Gamma_Z}^{M_Z + 3\Gamma_Z} O_{(Z/\gamma)}(M_u, p_{T,u}, y_u) dM_u,$$

$$O_{Z^{+(-)}}(y_u, p_{T,u}, p_{T,l}, \eta) = \int_{M_Z - 3\Gamma_Z}^{M_Z + 3\Gamma_Z} [O_{(Z/\gamma)^{+(-)}}(M_u, y_u, p_{T,u}, p_{T,l}, \eta)] dM_u,$$

$\rightarrow$  only Z-peak masses

$$O_{l^+l^-}^{norm} = \int \int \int O_{Z/\gamma}(M_u, y_u, p_{T,u}) dM_u dy_u dp_{T,u}.$$

$\rightarrow$  coplanar pairs - dedicated method of absolute normalization developed in parallel M.W. Krasny et al. NIM papers



# Making Z-boson (QCD)-identical to W-boson

1. Collect data at the two CM-energies:  $\sqrt{s_1}$  and  $\sqrt{s_2} = (M_Z/M_W) \times \sqrt{s_1}$ . These two settings allow to keep the momentum fractions of the partons producing the  $Z$  and  $W$ -bosons equal if the  $W$ -boson sample is collected at the CM-energy  $\sqrt{s_1}$  and the  $Z$ -boson sample at the CM-energy  $\sqrt{s_2}$ .
2. Rescale the solenoid current while running at the two CM-energies  $\sqrt{s_1}$  and  $\sqrt{s_2}$  by a factor  $i_2/i_1 = M_Z/M_W$  to equalize the distribution of the curvature radius  $\rho_l$  for charged leptons originating from the decays of the  $Z$  and  $W$ -bosons.
3. Redefine the  $RWZ$  observable as follows:

$$R_{WZ}^c(\rho_l, \eta_l) = \frac{O_{W^+}(\rho_l, \eta_l; s_1, i(s_1)) + O_{W^-}(\rho_l, \eta_l; s_1, i(s_1))}{O_{Z^+}(\rho_l, \eta_l; s_2, i(s_2)) + O_{Z^-}(\rho_l, \eta_l; s_2, i(s_2))}, \quad (9)$$

The remaining scale dependence of this observable is eliminated by modifying further the above observable :

$$R_{WZ}^c(\rho_l, \eta_l) = R_{WZ}^c(\rho_l, \eta_l) * \mathbf{C}_{\text{QCD}}$$

## Making Z boson “QCD-identical” to W boson

1. *Select events with opposite charge, same flavour lepton pairs*
2. *Determine the invariant mass of lepton pair  $M^{l+l-}$*
3. *Measure the QCD correction factor  $C_{QCD}$  defined as:*

$$C_{QCD} = \frac{\int_{M_Z-3\Gamma_Z}^{M_Z+3\Gamma_Z} N^{l+l-}(s_2, i(s_2), M^{l+l-}) dM^{l+l-}}{\int_{M_W-3\Gamma_W}^{M_W+3\Gamma_W} f_{BW}(M_W, \Gamma_W) \times w_{EW} \times N^{l+l-}(s_1, i(s_1), M^{l+l-}) dM^{l+l-}}$$

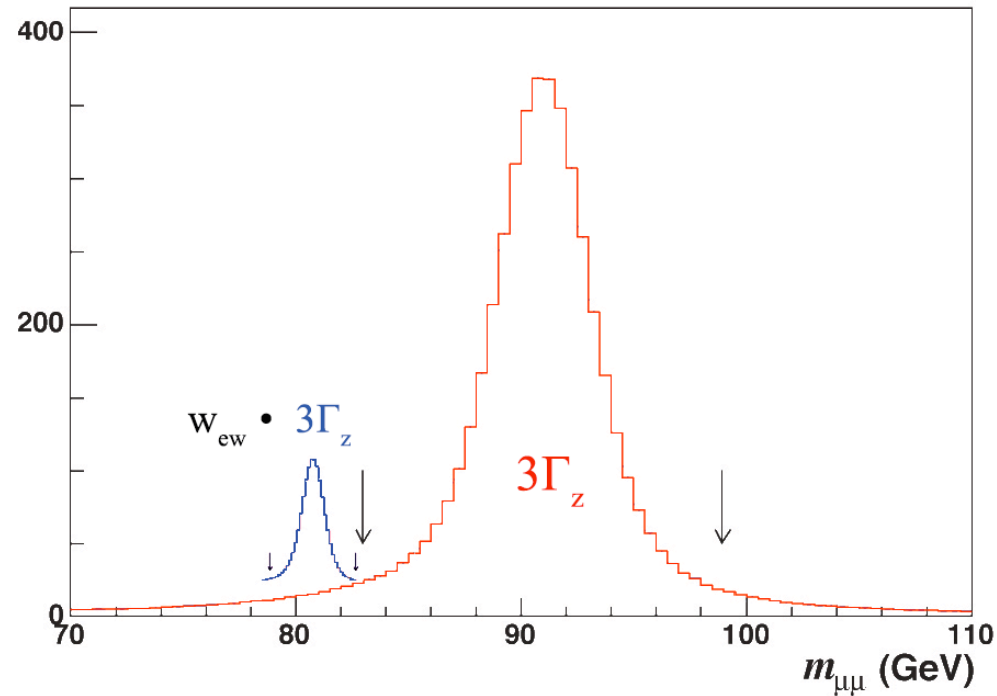
*Breit-Wigner weight*

*Electroweak weight correcting for asymmetries of angular distribution of leptons in the continuum and Z-peak region*

---

The scale dependence in the partonic distributions is eliminated - up to all orders of perturbative expansion !!! QCD- “eliminated” from the unfolding !!!

## Making Z boson “QCD-identical” to W boson



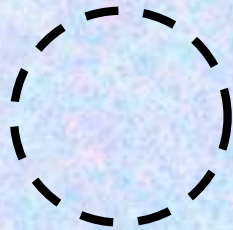
---

The scale dependence in the partonic distributions is eliminated - up to all orders of perturbative expansion !!! QCD- “eliminated” from the unfolding !!!

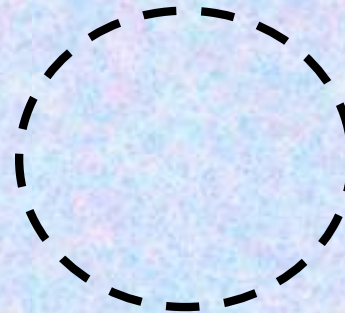
# Making Z boson “QCD-identical” to W boson

Cent. Exp.	Systematic $\xi$	$\Delta M$ [MeV]		
		$R_{WZ}$	$R_{WZ}^c$	$R_{WZ}^{QCD}$
	$\xi = 0$	$-1 \pm 6$	$0 \pm 7$	$-5 \pm 7$
	0	-180	-26	-8
	3	-68	-7	-3
$\sigma_{k_T}$ [GeV]	5	100	8	0
	6	206	12	4

QCD world of  
quark and gluons

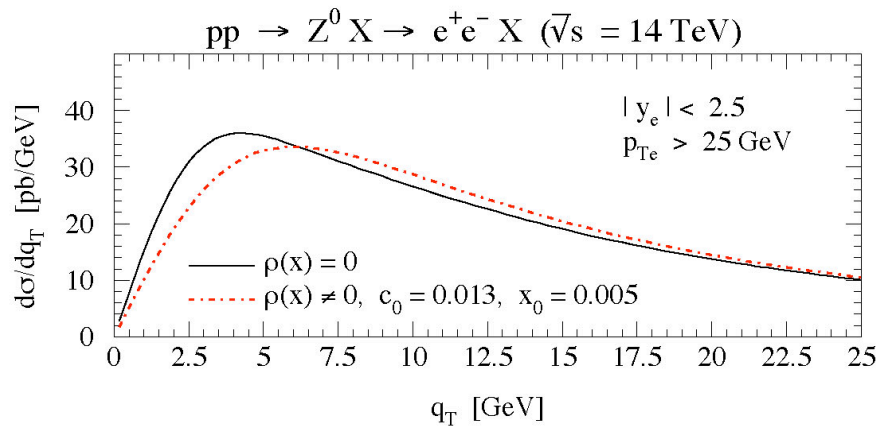


Observed with  
 $1/M_Z$  resolution

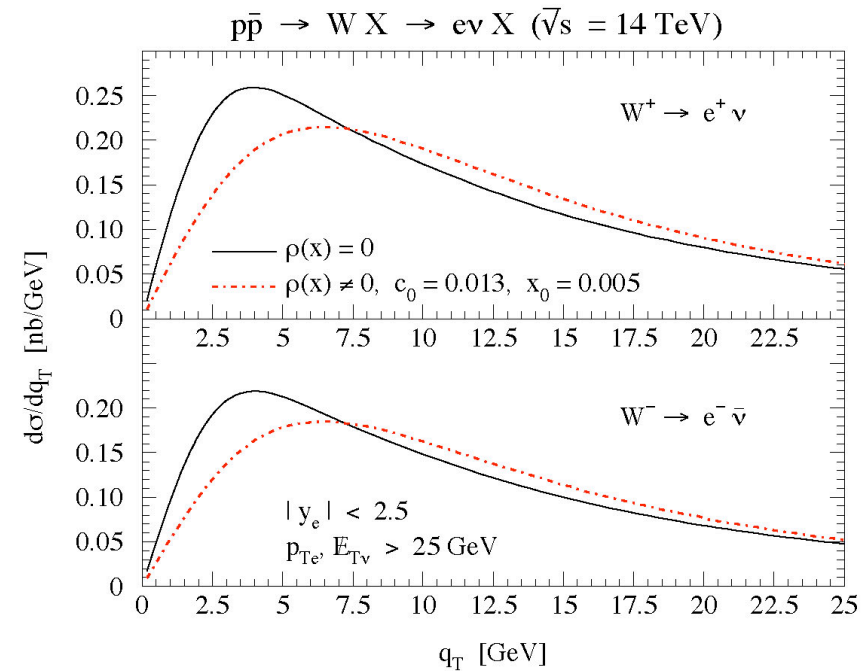


Observed with  
 $1/M_W$  resolution

# Making Z boson “QCD-identical” to W boson



S. Berge, et al., hep-ph/0410375.



- The relationship between the transverse momentum distributions of the Z-bosons and the W-bosons cannot be predicted and must be modelled. It involves a choice of: (1) the evolution scheme (DGLAP, BFKL, CCFM,...), (2) the parameters of the nonperturbative Sudakov form factors, (3) primordial  $k_T$  modelling
- The discussed above trick allows to get rid of all the flavour singlet aspects of modelling these distributions

... counting unknown partonic distributions

$$q_i(x, k_t, M_{\text{scale}})$$

$$5 \text{ flavours} \times 2 \text{ (q and } \bar{\text{q}}) \times 2 \text{ (scale)} = 20$$

The QCD scale degrees of freedom circumvented ...

$$q_i(x, k_t, M_{\text{scale}}) \longrightarrow q_i(x, k_t)$$

... unfolding confined to the polarization and flavour sectors: 10 unknown partonic distributions

# Unfolding $k_t$ -dependence of $q_i(x, k_t)$

## Ansatz:

$$1. k_t^{\text{quark}}(x) = k_t^{\text{antiquark}}(x)$$

(transverse momentum generated by gluon radiation (high energy limit))

$$2. k_t^u(x) = k_t^d(x) = k_t^s(x)$$

( $m_u, m_d, m_s \gg \Lambda_{\text{QCD}}$ )

## Remaining unknowns:

$$k_t^{u,d,s}(x), k_t^c(x), k_t^b(x)$$

They can be unfolded using observables 1(or 2), 3 and 4 provided that the  $x$  dependence of the quark distributions is known (the PDFs:  $q_i(x, M_W) = q_i(x)$ )

# Unconstrained PDF degrees of freedom at the LHC

Assume for a while:  $s(x)=\bar{s}(x)$ ,  $c(x)=\bar{c}(x)$ ,  $b(x)=\bar{b}(x)$  then:

- **5** sea-quark flavours (**u,d,s,c,b**) + **2** valence quark flavours ( **$u^{(v)}$ ,  $d^{(v)}$** ) **7** unknown PDFs:
- **4** constraints coming from the ( **$p_{T,i}$ ,  $\eta_i$** ) spectra for  **$W^+$ ,  $W^-$ , “ $Z^+$ ” and “ $Z^-$ ”** decays
- **7-4=3** degrees of freedom in the flavour-dependent pdf's remain unconstrained at the LHC

Important note:

At the Tevatron only the first quark family is relevant. In addition p collides with  $\bar{p}$ . This leaves only **2 (out of 7)** flavour dependent pdf's. They are over-constrained by the the  **$\eta_i$**  dependence of observables (1-4)



# A choice of 3 unconstrained degrees of freedom:

1.  $u^{(v)} - d^{(v)}$  - a missing constraint for the 1st family
2.  $s - c$  - a missing constraint for the 2nd family
3.  $b$  - a missing constraint for the 3rd family

Note:

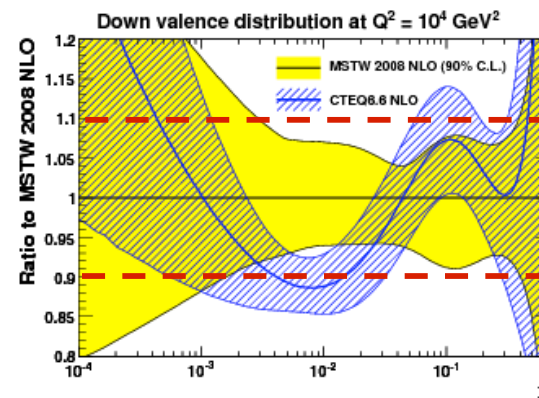
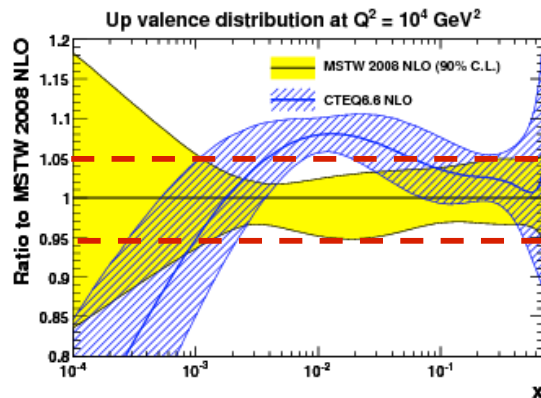
- $u^{(v)}$  can move up and  $d^{(v)}$  move down such that the rapidity distribution of Z-boson remain unchanged, the same for  $s$  and  $c$
- The non-singlet partonic distributions have only small scale dependence (they are robust with respect to the choice: (1) of QCD evolution scheme and (2) of order of perturbative expansion)

Can we constrain the PDFs using  
W and Z boson data collected at  
the LHC?

...No, we cannot. External constraints are  
needed. Is the precision of existing constraints  
sufficient?

# Present precision of: “ $u^{(v)} - d^{(v)}$ ” PDF and its impact on the $M_W$ measurement error

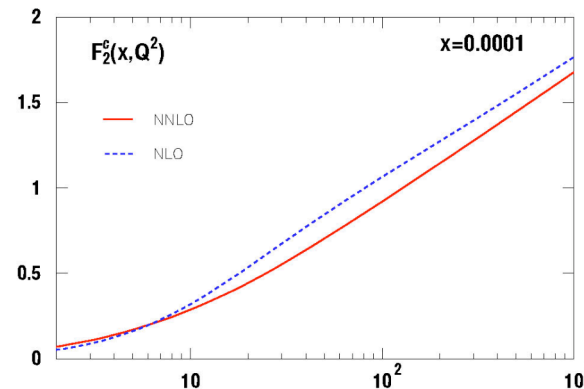
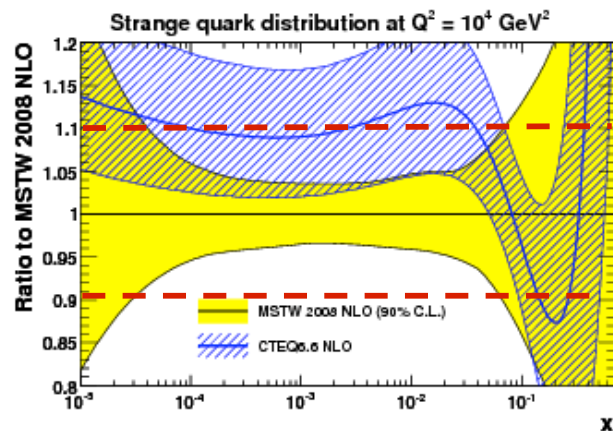
	$\Delta[(M_{W^+} + M_{W^-})/2]$	$\Delta[(M_{W^+} - M_{W^-})]$
$u_v^{\text{bias}} = 1.05 u_v$ $d_v^{\text{bias}} = d_v - 0.05 u_v$	79 MeV	115 MeV
$u_v^{\text{bias}} = 0.95 u_v$ $d_v^{\text{bias}} = d_v + 0.05 u_v$	-64 MeV	-139 MeV



Note: Only mutually compensating shifts leave the Z-boson rapidity distributions invariant

# Present precision of: “s - c” PDF and its impact on the $M_W$ measurement error

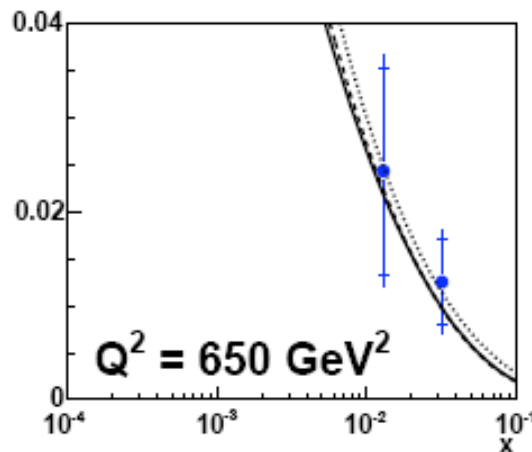
	$\Delta[(M_{W^+} + M_{W^-})/2]$	$\Delta[(M_{W^+} - M_{W^-})]$
$c^{\text{bias}} = 0.9 c$ $s^{\text{bias}} = s + 0.1 c$	148 MeV	17 MeV
$c^{\text{bias}} = 1.1 c$ $s^{\text{bias}} = s - 0.1 c$	-111 MeV	-11 MeV



Note: Only mutually compensating shifts leave the Z-boson rapidity distributions invariant

# Present precision of “b” PDF and its impact on the $M_W$ measurement error

	$\Delta[(M_{W^+} + M_{W^-})/2]$
$b^{\text{bias}} = 1.2 \text{ b}$	42 MeV
$b^{\text{bias}} = 0.8 \text{ b}$	-39 MeV



- H1 data
- ..... MSTW 2008 LO
- MSTW 2008 NLO
- MSTW 2008 NNLO

Note: b-quarks influence the biases while relating the spectra for W-bosons to the corresponding ones for Z-bosons

...The precision of  $M_W$   
cannot be improved at the  
LHC...

(...similar conclusion for  $\sin^2(\theta_W)$  and  $\Gamma_W$ )

...neither now nor at the  
completion phase of **the  
standard LHC programme...**

# The way forward

- A dedicated “precision-support” programme auxiliary to the standard LHC
- Note that neither the TJNAF programme (too low energy) nor the HERA programme (lack of deuteron data, too low statistics for CC processes, small statistics and large acceptance corrections for heavy quark sector) will improve the present experimental information

# Programme 1: Isoscalar beams at the LHC

- Isoscalar beams  $u^{(v)} = d^{(v)}$  cancel the majority of  $W^+$ ,  $W^-$  and  $Z$  production differences
- The measurement of the  $W$ -boson charge asymmetry constrain directly the  $s$ - $c$  distribution
- Analysis restricted to forward lepton pseudorapidities reduces errors due to  $b$  distribution uncertainty
- In addition, no need to assume  $s(x)=\bar{s}(x)$ ,  $c(x)=\bar{c}(x)$ ,  
 $b(x)=\bar{b}(x)$

elegant .. but unrealistic in the initial phase of the LHC operation



Programme 2: An “LHC-precision-support” DIS experiment with:

COMPASS

The Letter of Intent for such an experiment has been submitted a month ago to the SPSC and LHCC...

The measurement of the  $W$  mass at the LHC:  
shortcuts revisited

F. Dydak<sup>1</sup>, M.W. Krasny<sup>2\*</sup>, and R. Voss<sup>3</sup>

<sup>1</sup> CERN, Geneva, Switzerland; *Friedrich.Dydak@cern.ch*

<sup>2</sup> LPNHE, Universités Paris VI et VII; *Mieczyslaw.Krasny@cern.ch*

<sup>3</sup> CERN, Geneva, Switzerland; *Rudiger.Voss@cern.ch*

Abstract

The claim that the  $W$  mass will be measured at the LHC with a precision of  $\mathcal{O}(10)$  MeV is critically reviewed. It is argued that in order to achieve such precision, a considerably better knowledge of the  $u_v$ ,  $d_v$ ,  $s$ ,  $c$ , and  $b$  structure functions of the proton than available today is needed. This will permit to assess with adequate precision the production characteristics of the  $W$  and  $Z$  bosons in the proton-proton collisions at the LHC, and their effect on the  $p_T$  spectra of charged leptons from  $W$  and  $Z$  decays. An experimental programme is suggested that will deliver the missing information. The core of this programme is a dedicated muon scattering experiment at the CERN SPS, with simultaneous measurements on hydrogen and deuterium targets.

CERN-LHCC-2009-014 / LHCC-I-017  
17/09/2009



---

\* Contactperson

# Reminder: Unconstrained PDF degrees of freedom

- 5 sea-quark flavours (u,d,s,c,b) and 2 valence quark flavours ( $u^{(v)}$ ,  $d^{(v)}$ )
- 4 constraints coming from the  $(p_{T,l}, \eta_l)$  spectra for  $W^+$ ,  $W^-$ , “ $Z^+$ ” and “ $Z^-$ ” decays
- 3 degrees of freedom in the flavour-dependent pdf’s remain unconstrained at the LHC (external input needed)

# How to obtain the missing input?

1. **b-quark** distribution uncertainties can be assessed at the LHC by splitting the measurement domain  $0 < |\eta_{||}| < 2.5$  and  $2.0 < |\eta_{||}| < 2.5$
2. an assumption:  $s = s(u^{(s)}, d^{(s)} | \kappa_s)$  and  $\bar{s} = \bar{s}(\bar{u}^{(s)}, \bar{d}^{(s)} | \kappa_s)$   
Note:  $m_s \sim m_u, m_d < \Lambda_{\text{QCD}} \ll m_c, m_b$

---

Result: 7 unknown distributions constrained by 4 observables, 1 “large luminosity” observable and 1 “natural” assumption

→ only 1 high precision experimental constraint needed

...preferentially in the light quark sector, and of flavour non-singlet type

An optimal (in terms of its complementarities to the LHC measurements) constraint can be provided by a **COMPASS** high precision measurement of:

$$\text{Asym}_{\text{DIS}}^{(p,n)}(Q^2,x) = (d\sigma^p/dQ^2dx - d\sigma^n/dQ^2dx)/(d\sigma^p/dQ^2dx + d\sigma^n/dQ^2dx)$$

$$\dots \text{where } d\sigma^n/dQ^2dx = d\sigma^d/dQ^2dx - d\sigma^p/dQ^2dx$$

---

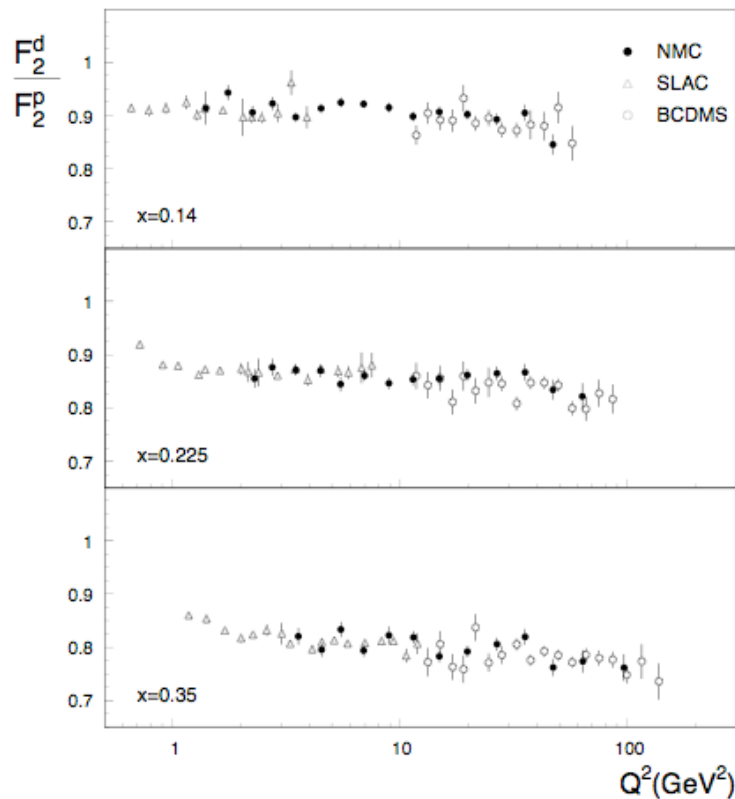
**Complementarities:**

$$\text{Asym}_{\text{DIS}}^{(p,n)} \sim 1/3 (u^{(v)} - d^{(v)}) + 2/3 (u^{(s)} - d^{(s)})$$

$$\text{Asym}_{\text{W}}^{(+,-)} \sim u^{(v)}d^{(s)} - u^{(s)}d^{(v)}$$

... asymmetry  $\text{Asym}_{\text{DIS}}^{(p,n)}$  provides a precious constraint for the valence/sea decomposition

# Experimental precision



## Achieved:

statistical precision: 1-3 %

systematic precision: 0.1- 0.3 %

## Required:

Increase of statistical precision by a factor of 5-10

... and, what is of extreme importance, reduced uncertainty, O(1%), of the extrapolation of the measured asymmetry to the  $Q^2$  domain of the LHC

# Steps from the measured asymmetries to their use at the LHC

1. Radiative corrections (small, better knowledge of quasi-elastic tails)
2. Corrections for nuclear effects: (1) Fermi motion in the deuterium nucleus, (2) off-shellness effect, (3) shadowing (better understanding of (1) and (2) (TJNAF), (3) HERA, ...in addition try to measure the proton spectator as a cross check)
3.  $p/n$  asymmetries of higher twists (significant progress in understanding both from theory side, S. Alekhin et al., and from exp. side (TJNAF), use two or three beam energies for a cross check)
4.  $p/n$  asymmetries of  $R = \sigma_L / \sigma_T$  (new NNLO QCD calculations)
5. QCD evolution of the asymmetry from the measured  $Q^2$  to  $M_W^2$  (better knowledge of  $\alpha_s$ , new dedicated NLO QCD tools linking time-like and space-like parton showers being prepared (S. Jadach et al.))

# Requirements

- 1) Highest possible flux:  $\sim 2 \times 10^8 \mu / \text{spill}$
- 2) Three months of data taking with 70% efficiency -  $8 \times 10^{13} \mu^+ / \text{target}$
- 3) The target length - 12 m, 5 cm radius segmented 4m H<sub>2</sub>, 2 m D<sub>2</sub>, 4m H<sub>2</sub>, 2 m D<sub>2</sub> (compression of the most downstream part of the beam-line? ... or compromise with the running time? )
- 4) Recoil proton detector?

Table 5: Number of  $\mu^+$  scatterings with  $1 < Q^2 < 100 \text{ GeV}/c^2$  and  $0.1 < x < 0.8$ .

80 GeV/c on hydrogen	$1.3 \times 10^8$
80 GeV/c on deuterium	$1.3 \times 10^8$
160 GeV/c on hydrogen	$1.4 \times 10^8$
160 GeV/c on deuterium	$1.4 \times 10^8$



# Programme 1: Isoscalar beams

example: expected precision of  $M_{W^+} - M_{W^-}$

- Isoscalar beams  $u^{(\nu)} = d^{(\nu)}$  up to a small  $\sim 0.2\%$  QED corrections

Expected biases in the measured values of  $M_{W^+} - M_{W^-}$  [MeV]

	Systematic $\xi$	$pp -  \eta  < 2.5$	$pp -  \eta  < 0.3$	$pp -  y_W  < 0.3$	$dd -  \eta  < 2.5$
$u^{(\nu)}, d^{(\nu)(*)}$	$u_{\max}^{(\nu)} = 1.05 u^{(\nu)}$ $d_{\min}^{(\nu)} = d^{(\nu)} - .05 u^{(\nu)}$	114.5	74.4	-38.1	2.4
	$u_{\min}^{(\nu)} = 0.95 u^{(\nu)}$ $d_{\max}^{(\nu)} = d^{(\nu)} + .05 u^{(\nu)}$	-138.5	-83.8	59.8	2.9
	$u_{\max}^{(\nu)} = 1.02 u^{(\nu)}$ $d_{\min}^{(\nu)} = 0.92 d^{(\nu)}$	85.2	51.2	-34.7	4.1
	$u_{\min}^{(\nu)} = 0.98 u^{(\nu)}$ $d_{\max}^{(\nu)} = 1.08 d^{(\nu)}$	-85.9	-53.2	47.2	-0.1

In addition the measurement of the W-bosons charge asymmetry constrain directly the s-c distribution...

# Programme 1: Isoscalar beams

example: expected precision of  $M_W = (M_{W^+} + M_{W^-})/2$

Expected biases\* in the measured values of  $M_W$

Systematic $\xi$	Expected precision [%]	$\Delta M$ [MeV]
" $\epsilon^+ - \epsilon^-$ "	0.5	< 5
" $u_v/d_v$ "	0.2	< 5
" $c - s$ " $\mathcal{L}_{int} = 10 fb^{-1}$	2	20
" $c - s$ " $\mathcal{L}_{int} = 100 fb^{-1}$	0.7	7
" $b$ "	20	7**

\* ...at this level of precision other systematic effects, not discussed in this presentation, may become dominant...

\*\* ...biases reflecting the uncertainties in the b-quark distributions reduced in a dedicated measurement in the restricted  $2.0 < |\eta_1| < 2.5$  region

# Programme 2: DIS experiment

example: expected precision of  $M_{W^+} - M_{W^-}$

Expected biases\* in the measured values of  $M_{W^+} - M_{W^-}$

Systematic $\xi$	Expected precision [%]	$M_{W^+} - M_{W^-}$ [MeV]
" $\epsilon^+ - \epsilon^-$ "	0.01	$\sim 10$ **
"s - c"	2	$< 5$
"u <sub>v</sub> /d <sub>v</sub> " $\mathcal{L}_{int} = 10 fb^{-1}$	1	$\sim 25$
"u <sub>v</sub> /d <sub>v</sub> " $\mathcal{L}_{int} = 100 fb^{-1}$	1	$\sim 10$ ***

\* ...at this level of precision other systematic effects, not discussed in this presentation, may become dominant...

\*\* change of polarisation of the solenoid current ... or use of unfolded  $u^{(v)}/d^{(v)}$  in the  $\epsilon^+ - \epsilon^-$  calibration

\*\*\* ...biases reduced in a dedicated measurement in the restricted  $0.3 < |\eta_{||}| < 0.3$  region

# Programme 2: DIS experiment

example: expected precision of  $M_W = (M_{W^+} + M_{W^-})/2$

Expected biases\* in the measured values of  $M_W$

Systematic $\xi$	Expected precision [%]	$\Delta M$ [MeV]
" $\epsilon^+ - \epsilon^-$ "	0.2	8
" $u_v/d_v$ "	1	12**
" $s - c$ "	1	10
" $b$ "	20	7***

\* ...at this level of precision other systematic effects, not discussed in this presentation, may become dominant...

\*\* the precision of unfolding the valence quark asymmetry is driven mainly by the precision of the measurement of  $\text{Asym}_{\text{DIS}}^{(p,n)}(Q^2, x)$  and by the uncertainty of its extrapolation to the  $M_W^2$  scale

\*\*\* ...biases reflecting the uncertainties in the b-quark distributions reduced in a dedicated measurement in the restricted  $2.0 < |\eta| < 2.5$  region

# Conclusions

- The electroweak precision measurements at the LHC require a dedicated measurement programme in order to improve the LEP and the Tevatron ones.
- Measurement of the proton/neutron  $\mu$ -DIS cross section asymmetry appears to be the simplest way of complementing the LHC electroweak precision measurement program (a complementary program involves running light isoscalar ions in the LHC machine)
- The proposed experiment could do this measurement with minor hardware modification of the COMPASS detector
- This experiment, to be performed, requires a recognition within the LHC community that the auxiliary, LHC-support programme is indispensable for a competitive EW-precision programme at the LHC