



High-energy Landau levels in graphene beyond first nearest-hopping processes: Corrections to the effective Dirac Hamiltonian

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Abstract

We study the Landau level spectrum of bulk graphene monolayers beyond the Dirac Hamiltonian with linear dispersion. We consider an effective Wannier-like tight-binding model obtained from *ab initio* calculations, that includes long-range electronic hopping integral terms [1, 2]. We employ the Haydock-Heine-Kelly (HHK) recursive method [3-5] to numerically compute the Landau level spectrum of bulk graphene in the quantum Hall regime, circumventing the need of using large supercells and the corresponding restriction on the magnetic field [6], and demonstrate that this method is both accurate and computationally much faster than the standard numerical approaches used for this kind of study. The Landau level energies are also obtained analytically for an effective Hamiltonian that accounts for up to third nearest neighbor hopping processes. Our analytical approach is based, as standard, in expanding the electronic dispersion relation around the Dirac points, the K and K'-points, in powers of the canonical momentum [7]. We find an excellent agreement between both approaches. We also study the effect of disorder on the electronic spectrum. Our analysis helps to elucidate the discrepancy between the high-energy Landau levels measured using infrared transmission spectroscopy [8] and theory.

References

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