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Gluodynamics

Intermediate mass dileptons as pre-equilibrium probes in heavy ion collisions

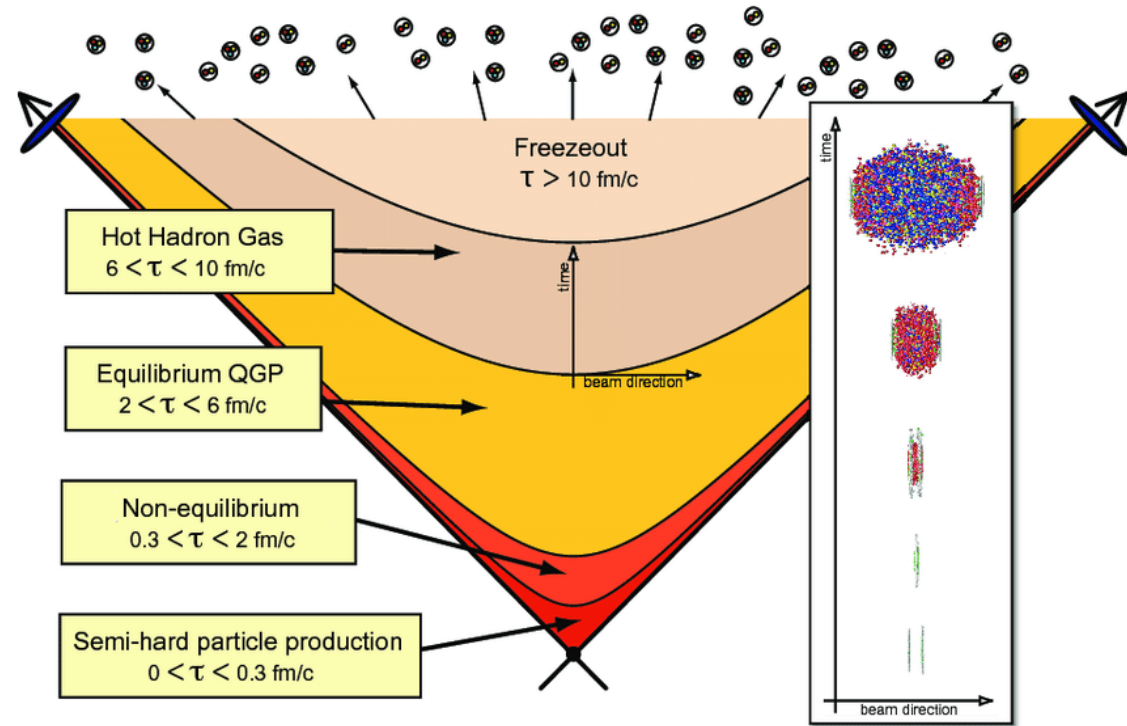
GDR QCD, 25th November 2021, Maurice Coquet

MC, Xiaojian Du, Jean-Yves Ollitrault, Sören Schlichting, Michael Winn

Phys.Lett.B 821 (2021) 136626

Space-time evolution of heavy-ion collisions

- A+A collisions: **different time scales** described by different effective theories
- Late stages very accurately modeled by hydrodynamic descriptions of expanding near-equilibrium QGP
- A challenge : matching between far-from-equilibrium **initial state** and **viscous hydrodynamics**



M.Strickland, Acta Physica Polonica B 45, 2355 (2014)

Dilepton production as a probe

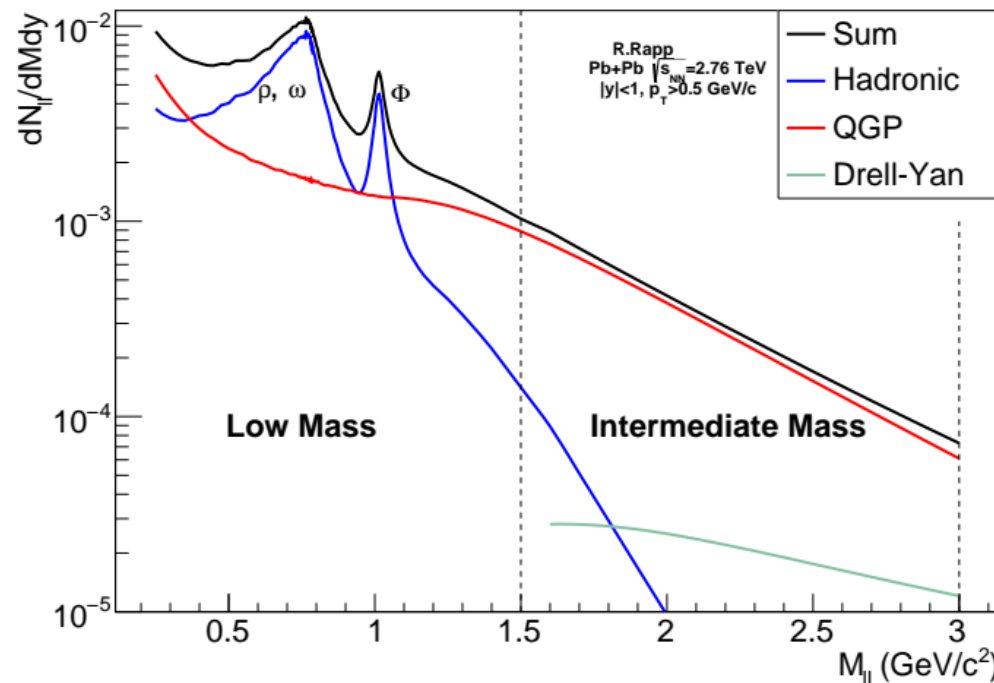
- Electromagnetic interactions with the QGP have a small cross section
- Produced during all stages of the collision
- Dilepton carry extra information : invariant mass
→ not affected by blue-shift

→ Intermediate mass region ($M > 1.5$ GeV)
→ Characterized by quarks and gluons degrees of freedom

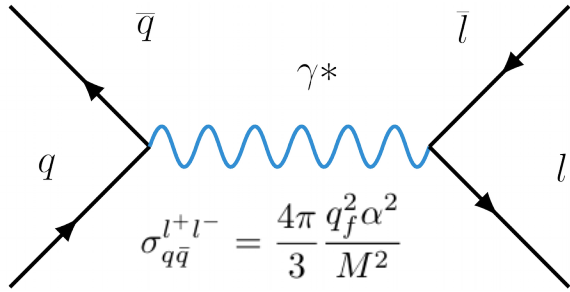
→ High mass ↔ High T ↔ early times

$$\frac{dN}{d^4x dM} \propto (MT)^{3/2} \exp\left(-\frac{M}{T}\right)$$

→ Highly sensitive to early-times/pre-equilibrium emission



Production rate calculation



Production rate for dileptons from cross section calculated at LO (quark-anti-quark annihilation)

Cf: Strickland PRD 99 (2019) 3, 034015, Phys. Rev. C 103, 024904 (2021), Ryblewski, Strickland PRD 92, 025026 (2015)

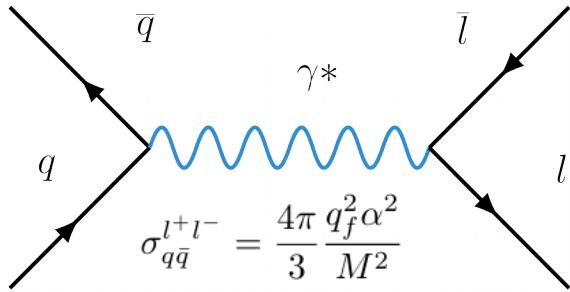
$$\frac{dN^{l^+l^-}}{d^4x d^4K} = \int \frac{d^3\mathbf{p}_1}{(2\pi)^3} \frac{d^3\mathbf{p}_2}{(2\pi)^3} 4N_c \sum_f f_q(x, \mathbf{p}_1) f_{\bar{q}}(x, \mathbf{p}_2) v_{q\bar{q}} \sigma_{q\bar{q}}^{l^+l^-} \delta^{(4)}(K - P_1 - P_2)$$

→ Integrate over space-time evolution of the medium to calculate the dilepton yield

$$\frac{dN}{dM dy} = \int \tau d\tau \int d\eta \int d^2x_T \frac{dN}{d^4x dM dy}$$

- Assume **one dimensional Bjorken** expansion :
 - boost invariant along the longitudinal direction
 - **homogeneous** in the transverse plane
 - Transverse flow neglected (high T ↔ early times)

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Pre-equilibrium dynamics

- **Universality in pre-equilibrium** dynamics (attractor solutions) as a function of scaling variable :

$$\tilde{w} = \frac{\tau T_{eff}}{4\pi\eta/s}$$

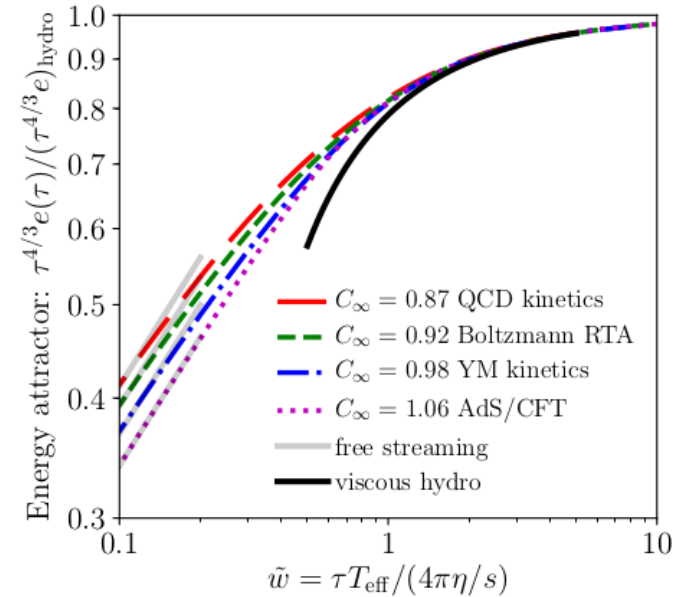
→ Can choose a specific calculation (QCD kinetics) to determine **evolution of energy density** and constrain pre-equilibrium dynamics

- For this, need final condition at late times ($w \gg 1$):

$$\frac{e(\tau)\tau^{4/3}}{e_{hydro}\tau_{hydro}^{4/3}} = \mathcal{E}(\tilde{w})$$

- Fixed by charged particle multiplicity in the final state

→ final state entropy density $\frac{dS}{d\eta} \propto \frac{dN_{ch}}{d\eta} \approx 1900$ (For $\eta=2$ at 5.02 TeV)

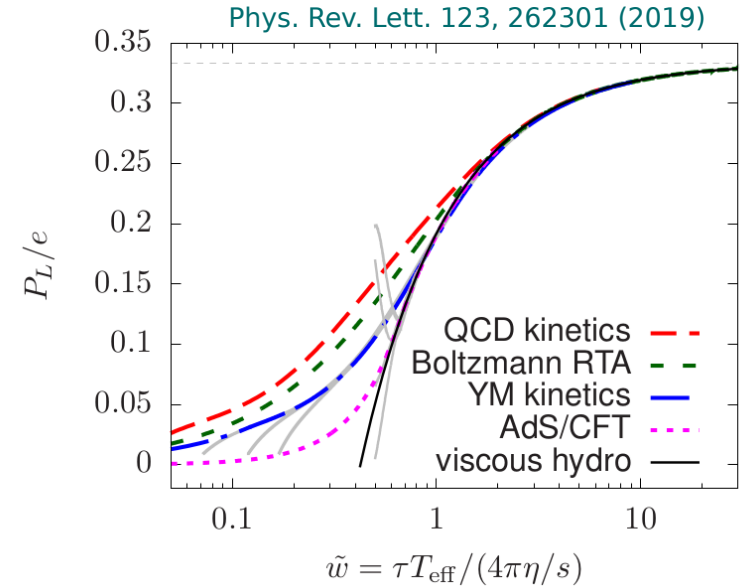
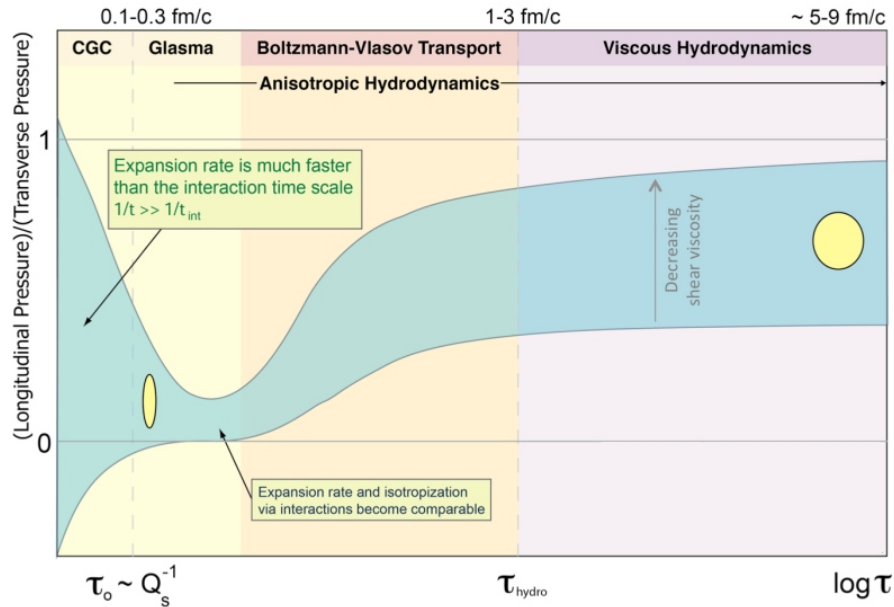


Giacalone, Mazeliauskas, Schlichting, Phys. Rev. Lett. 123, 262301 (2019)

$$e(\tau) \equiv \frac{\pi^2}{30} \nu_{eff} T_{eff}^4(\tau)$$

Features of pre-equilibrium: pressure asymmetry

- At early times, rapid longitudinal expansion $\rightarrow P_L \ll P_T$
 \rightarrow Anisotropy of distributions in momentum space



For typical parameters (e.g. $\eta/s=0.32$):
 $w=1 \rightarrow \tau=3 \text{ fm/c} \rightarrow p_L/e=0.2$

- Local pressure isotropy occurs at late times, but applicability of viscous hydro better than anticipated $\rightarrow \tau_{hydro} \ll \tau_{eq}$

M.Strickland, Acta Physica Polonica B 45, 2355 (2014)

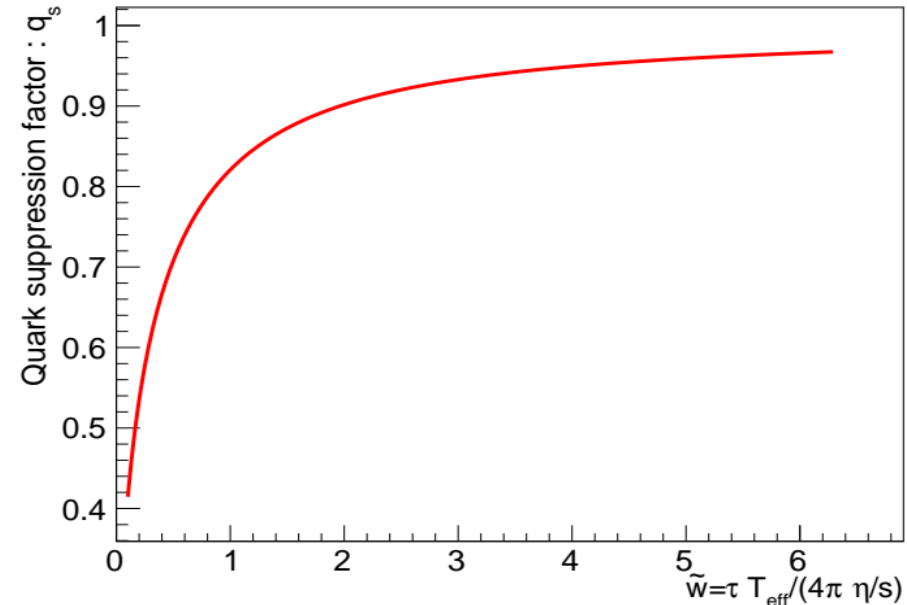
Features of pre-equilibrium: quark suppression

- Initial state theories (e.g. CGC) predict a gluon-dominated medium at early times
 - quark suppression factor, defined as the ratio between quark and gluon energy density :

$$q_s(\tau) \propto \frac{e^{(q)}}{e^{(g)}} \left(T(\tau) \right)$$

- Transition of highly gluon-dominated system towards a chemically equilibrated medium

X. Du, S. Schlichting: Phys. Rev. D 104, 054011 (2021)
Phys. Rev. Lett. 127, 122301 (2021)



→ Calculated in the weak coupling regime with QCD kinetics

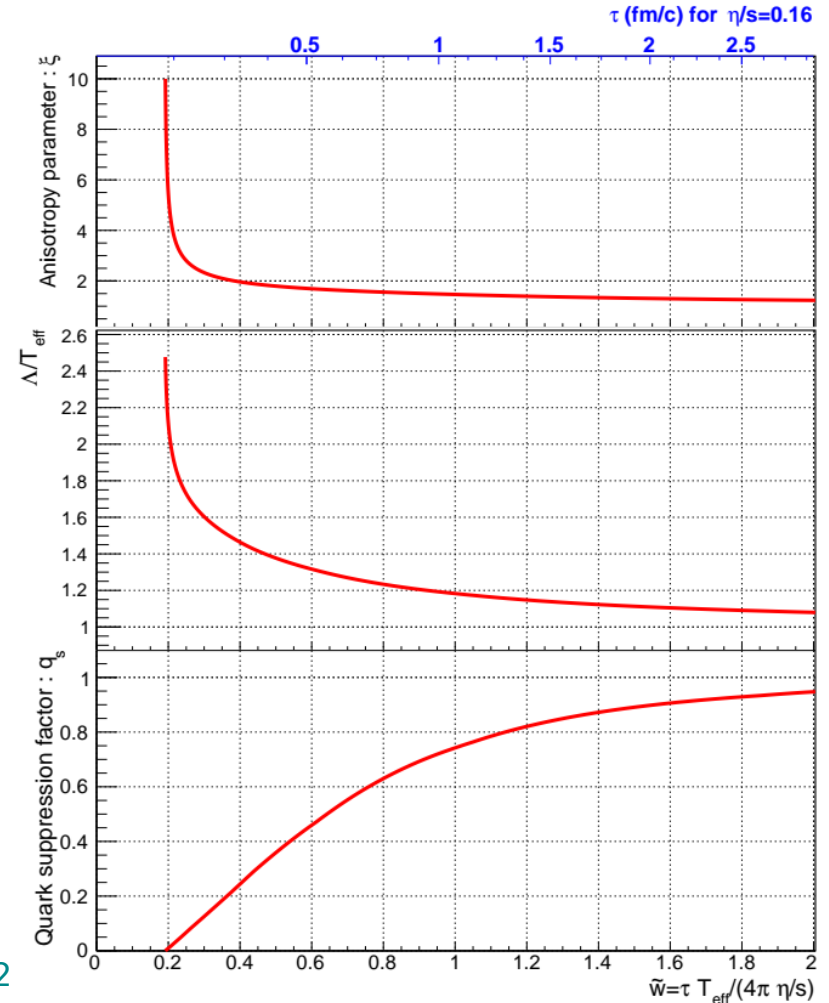
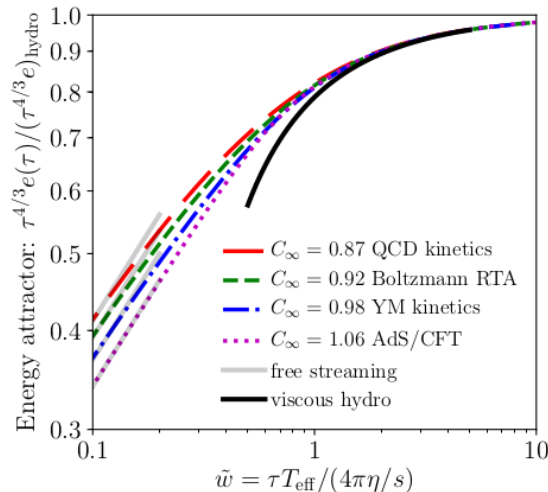
Out-of-equilibrium quark distributions

Distribution for quarks anisotropic in momentum space :

$$f_q(\tau, p_T, p_L) = q_s(\tau) f_{FD} \left(- \sqrt{p_T^2 + \xi^2(\tau) p_L^2} / \Lambda(\tau) \right)$$

→ Depend on Λ (anisotropic effective temperature), anisotropy parameter ξ calculated w/ P_L/e , and quark suppression factor q_s

→ Evolution of non-equilibrium parameters constrained by the evolution of energy density :



Results: mass spectra

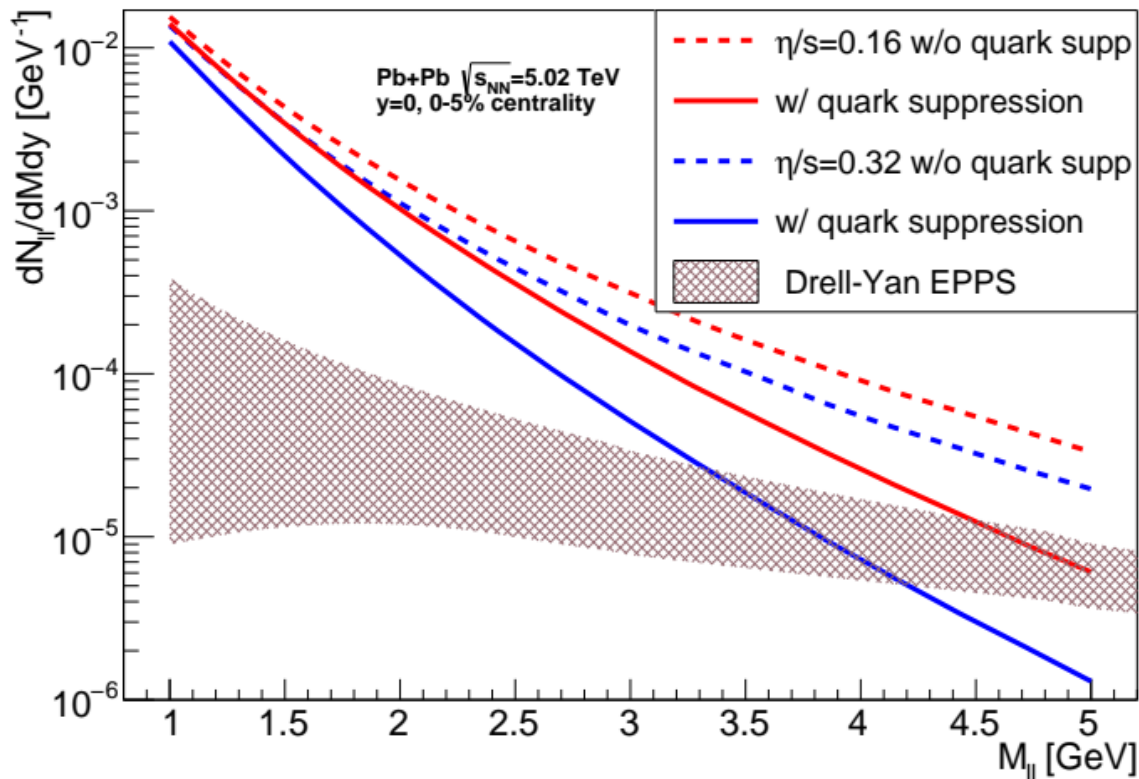
- Yields can be fitted by the formula :

$$\frac{dN^{l+l-}}{dMdy} = C \left(1 + \frac{M}{nT_0}\right)^{-n}$$

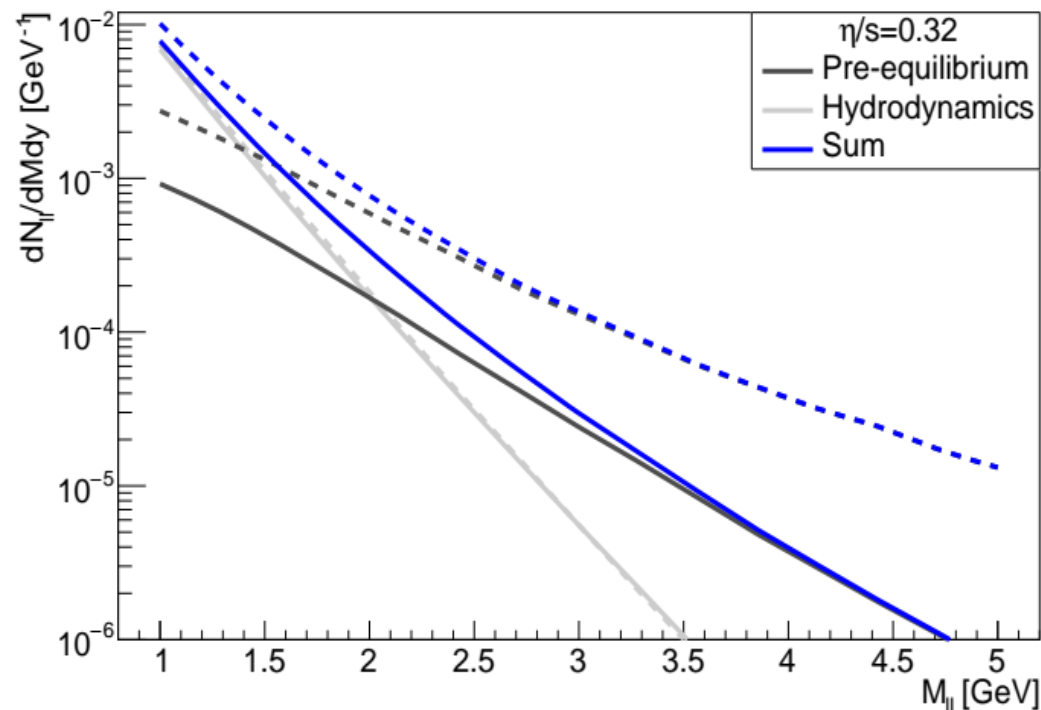
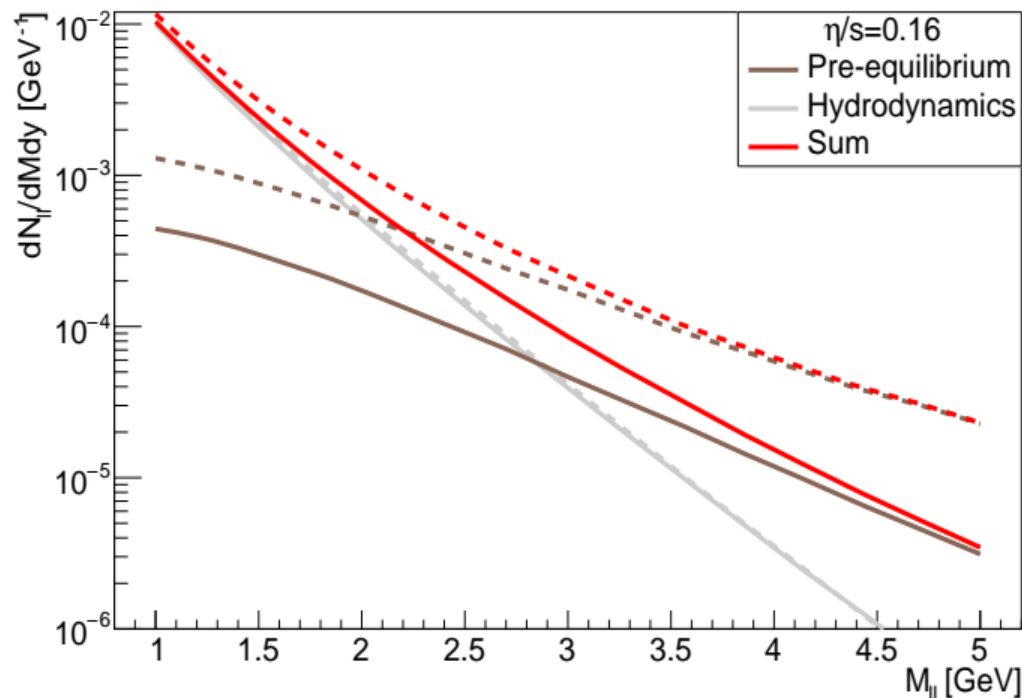
with $C = 0.5 \text{ GeV}^{-1}$ $T_0 = 0.2 \text{ GeV}$ and

$$n \simeq 5.3 \left(1 + 4\frac{\eta}{s}\right)$$

- η/s is not the viscosity in the hydro regime but **viscosity at high temperature** : controls time scale for applicability of hydrodynamics
- Drell-Yan process calculated at NLO \rightarrow dominates dilepton production at high mass
- Pre-equilibrium+hydro production is very sensitive to quark suppression
 \rightarrow [access to early-stage chemistry](#)



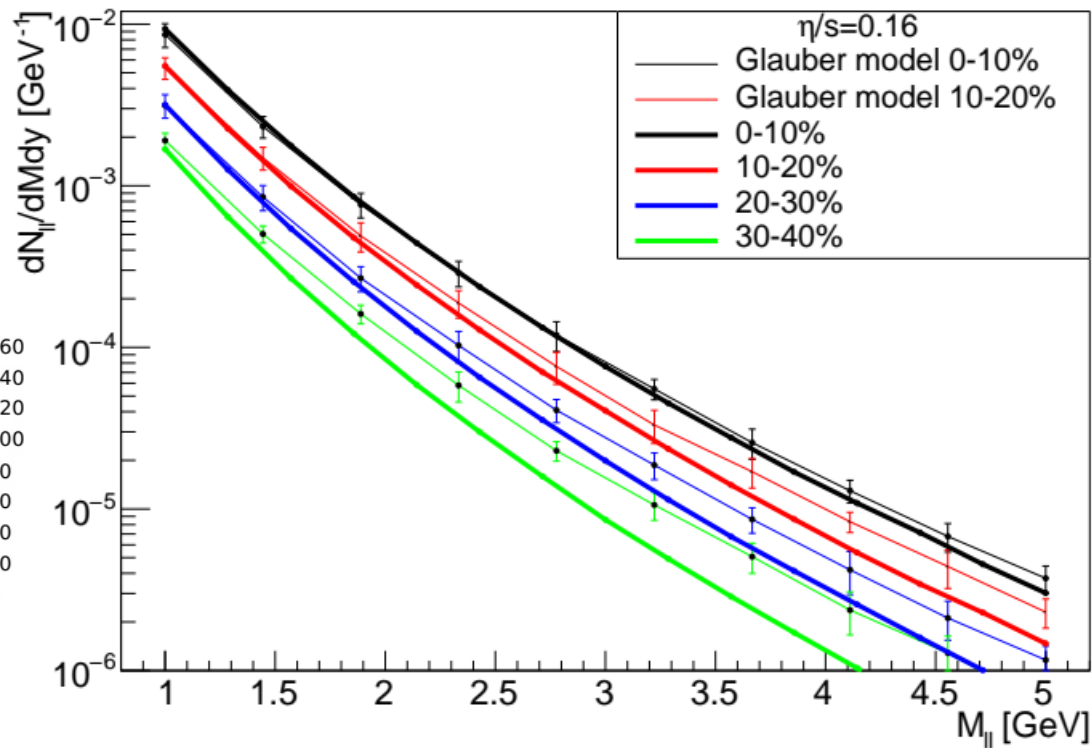
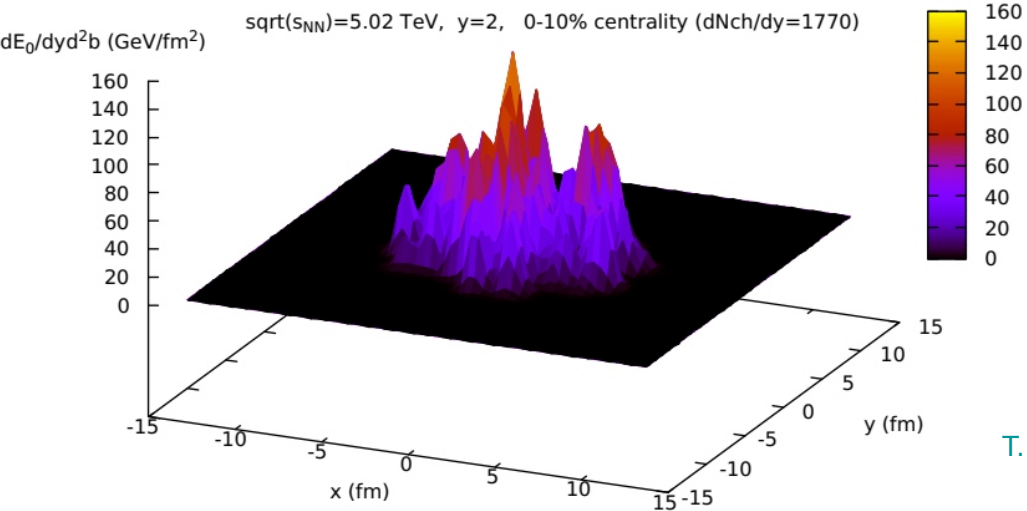
Results: time decomposition



- Since η/s controls time scale for applicability of hydrodynamics; depending on value of η/s **considerable contributions from pre-equilibrium regime** ($w < 1$)
- \rightarrow larger viscosity \rightarrow later thermalization \rightarrow more contribution from pre-equilibrium

Estimating the transverse fluctuations

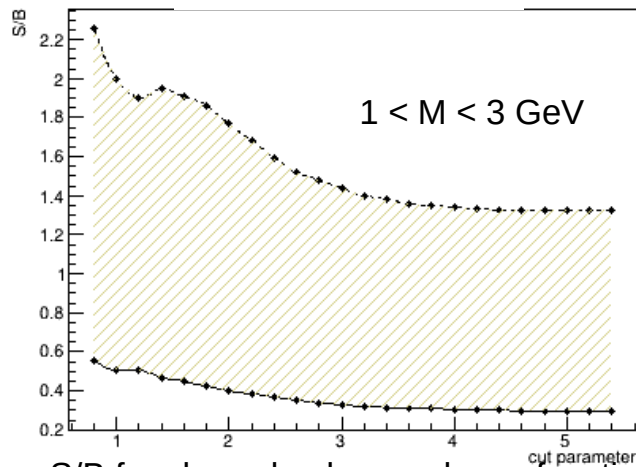
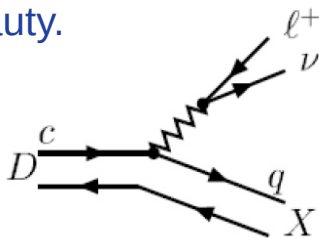
- modelling of event-by-event fluctuations (hot spots) using a TMD-Glauber model : parametrization of gluon distributions in nucleons + Glauber
 - parameters tuned to reproduce ALICE data for $dN_{ch}/d\eta$
- important for **large invariant mass** region in more **peripheral events**



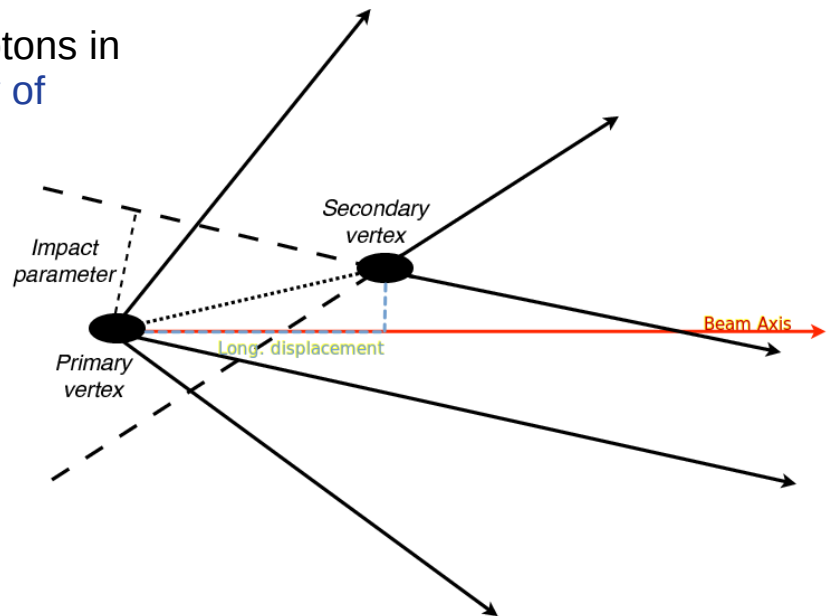
T. Lappi and S. Schlichting, Phys. Rev. D 97 (2018) no.3, 034034
S. Schlichting, X. Du, private communication

Background suppression with LHCb

→ Dominant background for intermediate mass dileptons in heavy ion collisions at 5.02 TeV : **semileptonic decay of charm and beauty.**



S/B for charm background as a function of IP cut, with $0.5 < R_{AA} < 1$ for D and Λ_c



Rejection of background:

- impact parameter of the single-track muons
- longitudinal displacement of the **secondary vertex**
- LHCb upgrade 2 setup for heavy ion collisions would provide appropriate secondary vertexing

Conclusion and outlook

- Pre-equilibrium dynamics essential to the high mass spectrum
 - insight into quark suppression & matter properties at early stage
 - extract from the mass spectrum a measure of the thermalization time, i.e. of η/s at early times
- Background suppression : secondary vertexing
 - LHCb gives good performance: small distance between instrument and primary vertex, and longitudinal boost
- Investigating m_T spectrum : m_T scaling as a signature of thermal emission, with small breaking due to pre-equilibrium dynamics



Thank you !



Backup

M_T scaling of dilepton production

In the fluid rest frame :

$$\frac{dN^{l^+l^-}}{d^4x d^4K} = C \exp\left(-\frac{k_0}{T}\right)$$

For leading-order production, explicit calculation gives :

$$C = \frac{N_c \alpha^2}{12\pi^4} \sum_f q_f^2$$

We assume :

- boost invariance and neglect transverse flow
- that the temperature profile is uniform within a transverse area A_\perp
- Local thermal equilibrium holds at all times, hence the expansion is ruled by ideal hydro, with the scaling $\tau T^3 = \text{const.}$

Then, after intergration over space-time :

$$\left(\frac{dN^{l^+l^-}}{d^4K}\right)_{\text{ideal}} = \frac{32N_c \alpha^2 \sum_f q_f^2 A_\perp (\tau T^3)^2}{\pi^4 M_t^6}$$

L. D. McLerran and T. Toimela, Phys. Rev. D31(1985), 545

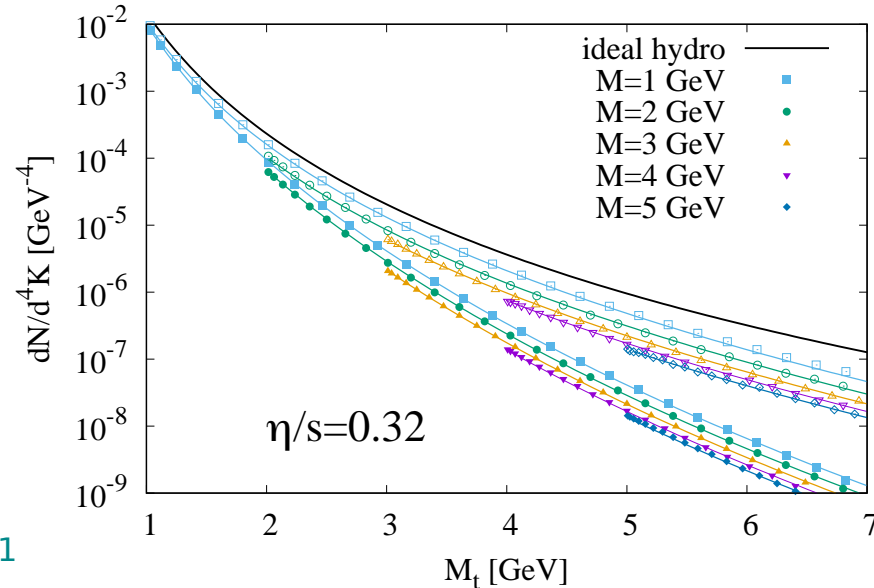
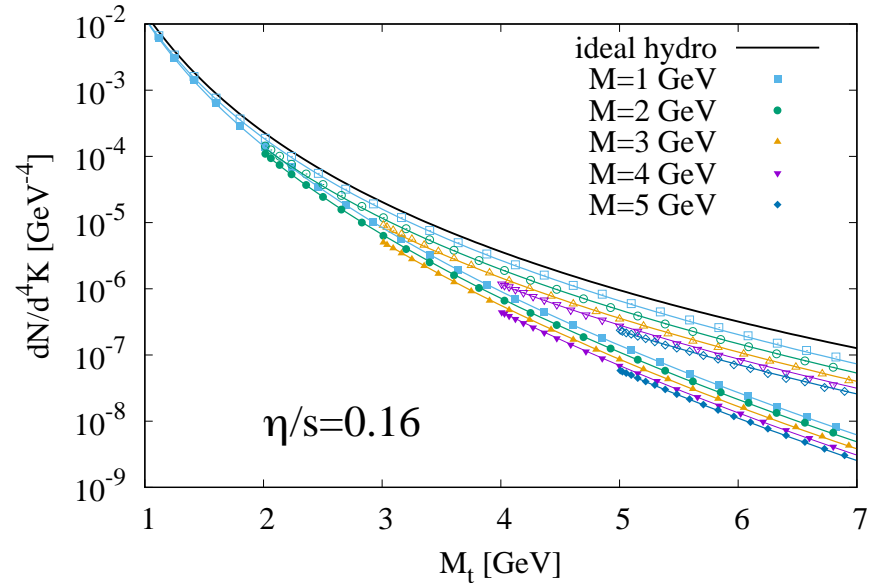
M_T scaling violation

Out of equilibrium, two important effects appear :

- quark suppression implies a suppression of dilepton production, which is a global factor, i.e. no impact on M_T scaling, but deviation from ideal case, more pronounced at high mass (\leftrightarrow early times \leftrightarrow more quark suppression)
- Fast longitudinal expansion \rightarrow pressure asymmetry \rightarrow momentum anisotropy which violates M_T scaling,
- favouring small masses over large masses for a given M_T value

$$\frac{dN^{l+l^-}}{d^4K} \simeq \left(\frac{dN^{l+l^-}}{d^4K} \right)_{\text{ideal}} \frac{\left(1 + a \frac{\eta}{s} M_t^2 / n \right)^{-n}}{\sqrt{1 + b \frac{\eta}{s} M^2}}$$

With : $a = 0.61 \text{ GeV}^{-2}$, $b = 1.6 \text{ GeV}^{-2}$, $n = 3.1$



TMD-Glauber model

T. Lappi and S. Schlichting, Phys. Rev. D 97 (2018) no.3, 034034
S. Schlichting, X. Du, private communication

- K_T factorization for gluon number density is assumed :

$$\frac{dN_g}{d^2\mathbf{b}d^2\mathbf{P}dy} = \frac{\alpha_s N_c}{\pi^4 \mathbf{P}^2 (N_c^2 - 1)} \int \frac{d^2\mathbf{k}}{(2\pi)^2} \Phi_A(x, \mathbf{b} + \mathbf{b}_0/2, \mathbf{k}) \Phi_B(x, \mathbf{b} - \mathbf{b}_0/2, \mathbf{P} - \mathbf{k})$$

- The gluon distributions are assumed to be adjoint dipole distribution and the GBW saturation model is used :

$$\Phi_{A,B}(x, \mathbf{b}, \mathbf{k}) = 4\pi^2 \frac{(N_c^2 - 1)}{N_c} \frac{\mathbf{k}^2}{Q_{s,A,B}^2(x, \mathbf{b})} \exp \left\{ -\frac{\mathbf{k}^2}{Q_{s,A,B}^2(x, \mathbf{b})} \right\}$$

With : $Q_{s,A,B}^2(x_{A,B}, \mathbf{b}) = Q_{s,p}^2(x_{A,B}) \sigma_0 T_{A,B}(\mathbf{b})$ And $Q_{s,p,avg}^2 \approx \sqrt{s_{NN}} x_0 \left(\frac{C_A}{C_F} \left(\frac{Q_0}{\sqrt{s_{NN}} x_0} \right) \right)^{1/(2+\lambda)}$

- Integrating the gluon number density yields the initial energy density :

$$(e\tau)_0 = \frac{\alpha_s (N_c - 1) \sqrt{\pi}}{N_c} \frac{Q_A^2 Q_B^2}{(Q_A^2 + Q_B^2)^{5/2}} [2Q_A^4 + 7Q_A^2 Q_B^2 + 2Q_B^4]$$