

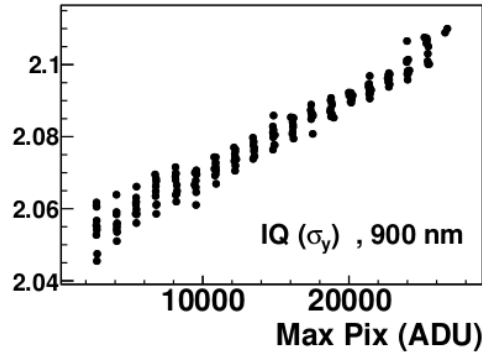
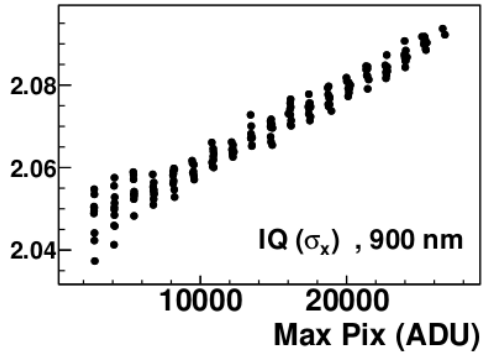
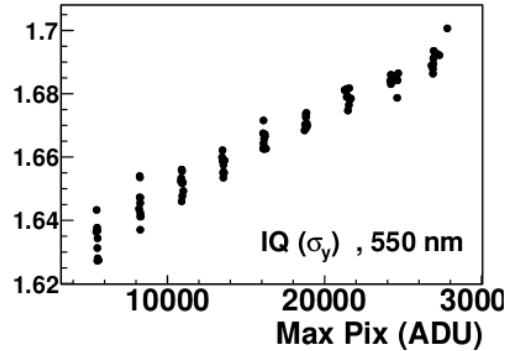
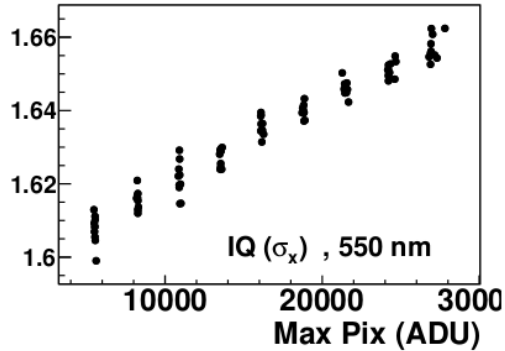
# Brighter-Fatter effect on HyperSuprimeCam

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(Rubin/LSST-France, nov. 2021)

# Brighter-fatter ?



The size of a spot a few pixels across increases by a few % from 0 to saturation.

This is a genuine non-linearity unrelated to electronics.

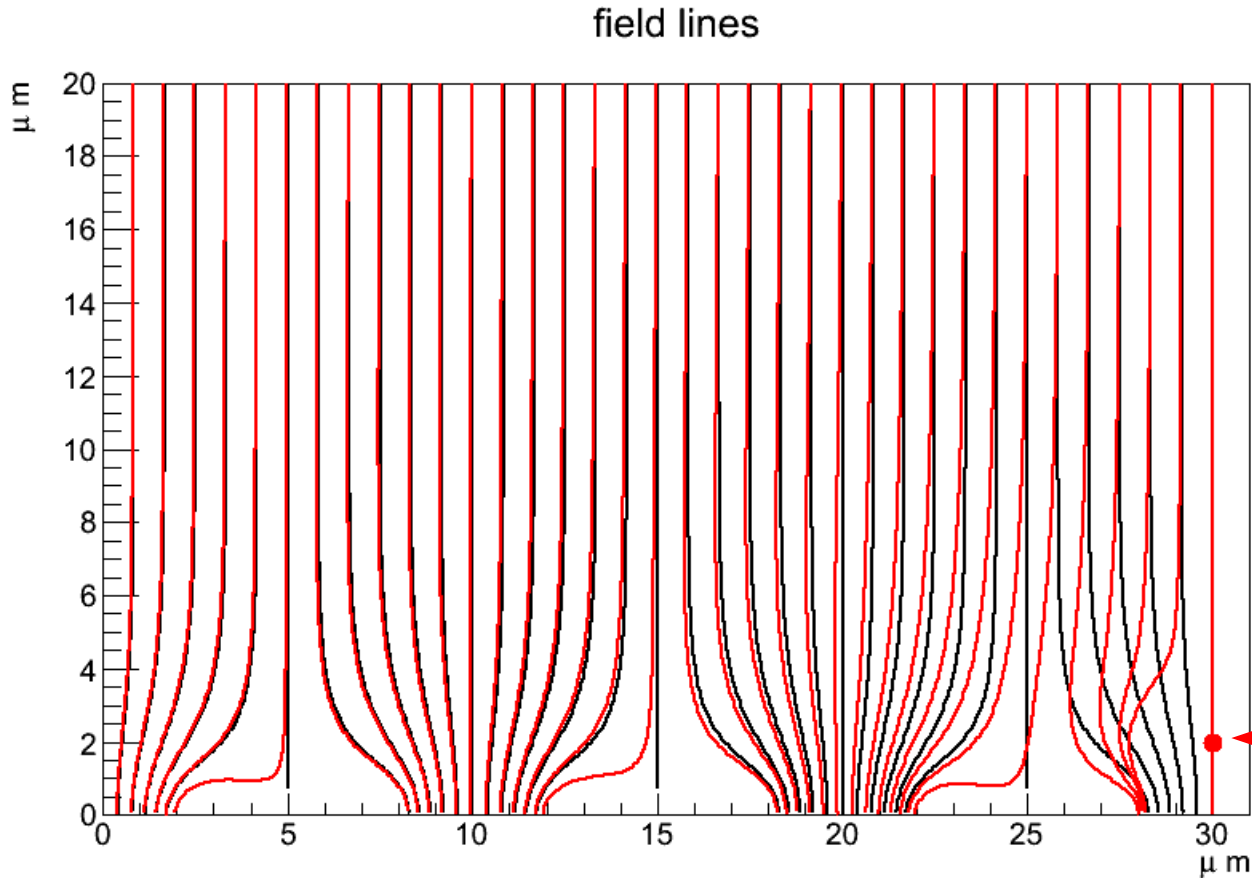
Name :  
« brighter-fatter effect »

1402.0725 : sizes of (lab) star as a function of its max (flux), in both directions and for two wavelengths.

# Why bother ?

- The PSF is measured from bright stars, and is hence biased when used to describe the system response to faint astronomical objects.
- This bias potentially messes up measurements of galaxy shapes and distant supernova fluxes.
- The effect is due to electrostatics in the CCD (Guyonnet et al 2015).
- The standard (and so far unchallenged) way to cope with is to constrain the CCD electrostatics using the correlation function of flatfields, and derive a correction to be applied to raw science images.

# Dynamical image distortions



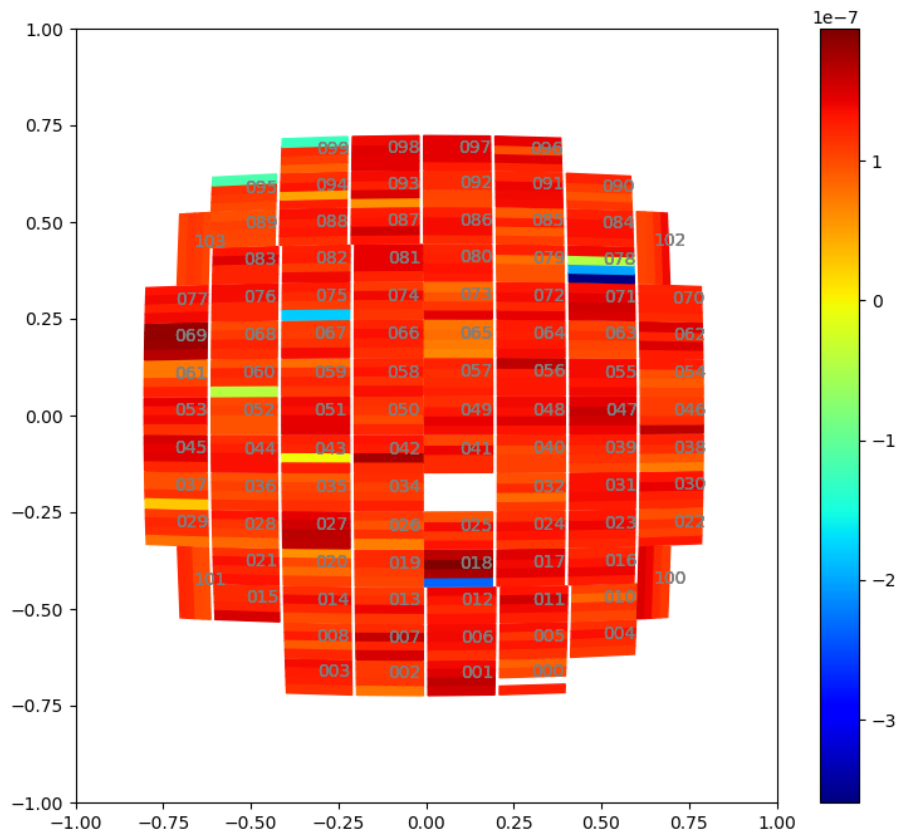
Charges stored in the CCD distort the drift lines of the forthcoming electrons.

50 k electrons

# What is new w.r.t the first HSC science papers

- New series of flat fields acquired at fall 2019
  - firstly to measure non-linearity
  - but can be used also measure the 2-point function
- These flat fields are much more stable than the legacy data, and allow to disentangle the lamp intensity variation from non-linearity.
- They allow to actually measure non-linearity
  - The average non-linearity on HSC is sizable and affects the PTC curvature ( $\sim 10\%$ ).
- Revisiting the BF effect on HSC is worth it.

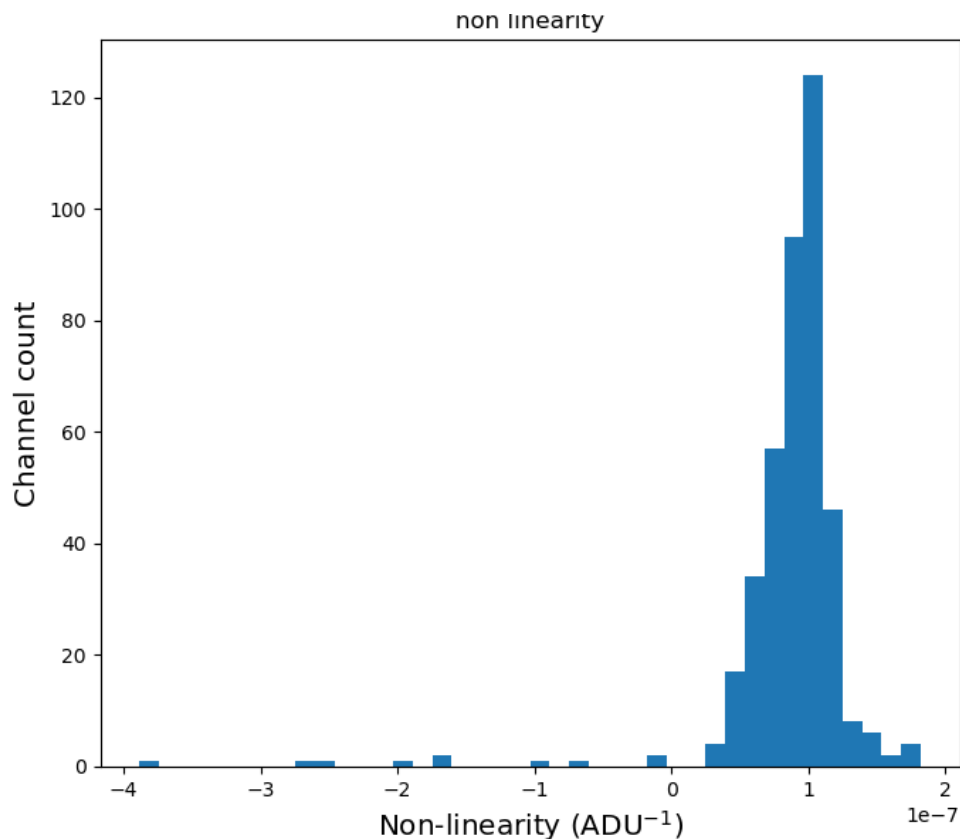
# All channels nonlinearity map



$$I_{\text{corr}} = I_{\text{raw}} + k I_{\text{raw}}^2$$

Fairly homogeneous  
over the focal plane,  
with some odd chips.

# All channels non linearity



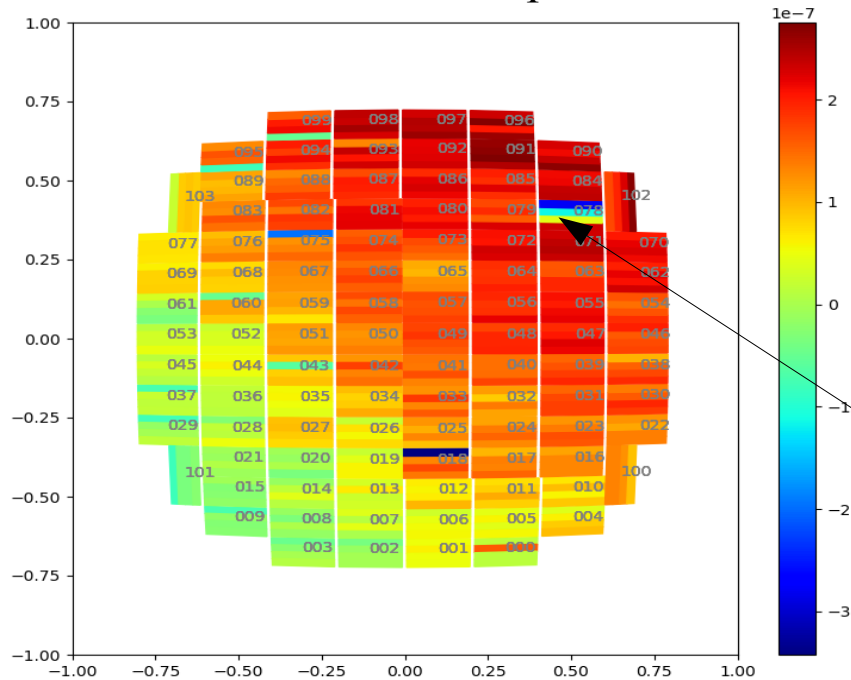
$$I_{\text{corr}} = I_{\text{raw}} + k I_{\text{raw}}^2$$

k is expressed  
in ADU<sup>-1</sup>

Amounts to ~0.4%  
at full scale  
(~ 40 kADUs).

# DM non-linearity corrections

k values in the focal plane



$$I_{true} = I_{obs} + k I_{obs}^2$$

This may be due to lamps varying differently as the sequence goes.

Chip 78 covers the whole range

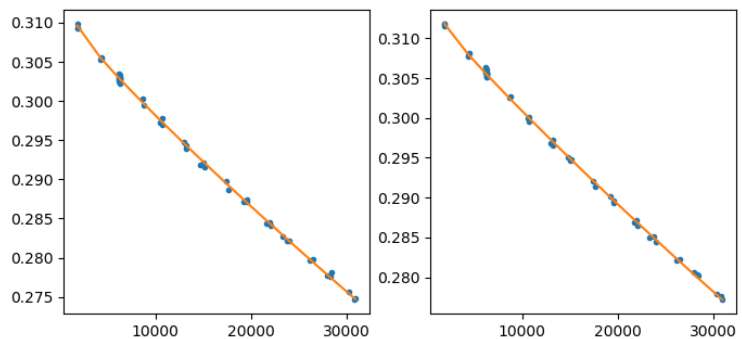
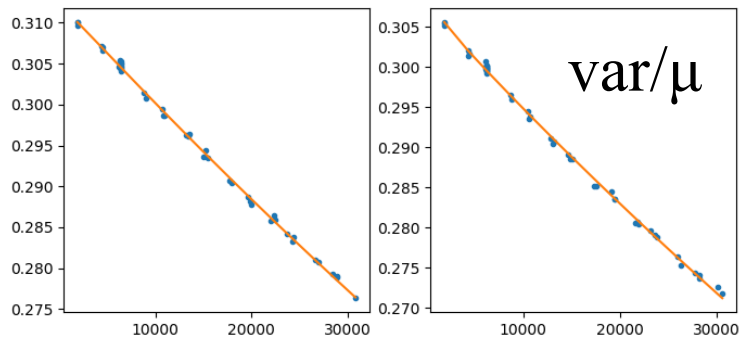


# Two-point function of flats

- This is the core ingredient to the brighter-fatter correction.
- 104 CCDs, 4 channels/chip, with a handful of dead channels
- All calculations are done at the video channel level.
- Evaluate  $10 \times 10$  co-variances
- 62 flat pairs in total in this 2019 data.
- g band.

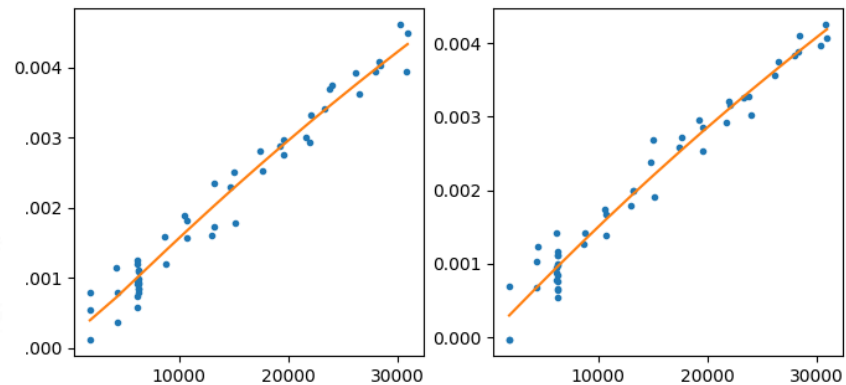
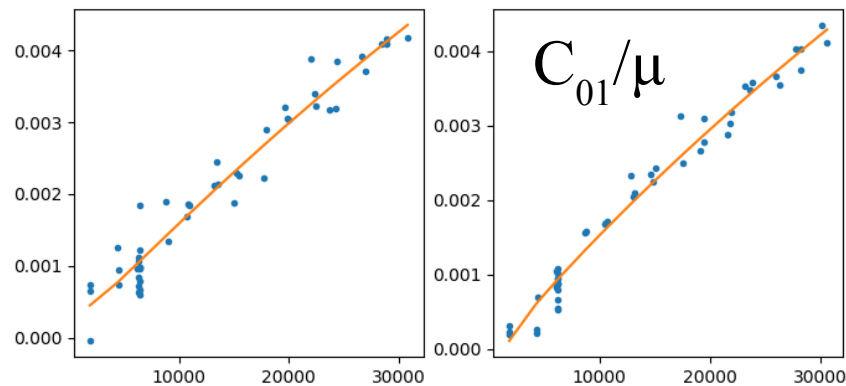
# What determines the flat-field co-variances?

- The pixel area change due to a (1 electron) charge put in a pixel
- The area is changed by  $(1+a_{ij})$  for a pixel located  $i$  columns and  $j$  rows away from the source.
- $a_{00}$  is negative (“self interaction” shrinks a pixel)
- For almost all reasonable configurations all the other  $a_{ij}$  are positive.
- because of area conservation, 
$$\sum_{-\infty < i, j < \infty} a_{ij} = 0$$
- See 1905.08677 for details



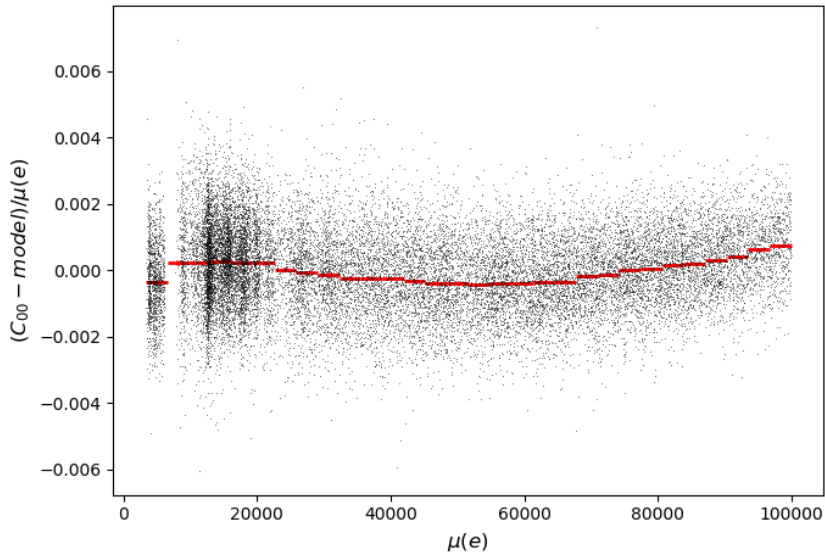
$$C_{ij}(\mu) = \frac{\mu}{g} \left[ \delta_{i0}\delta_{j0} + a_{ij}\mu g + \frac{2}{3}[\mathbf{a} \otimes \mathbf{a}]_{ij}(\mu g)^2 + \frac{1}{3}[\mathbf{a} \otimes \mathbf{a} \otimes \mathbf{a}]_{ij}(\mu g)^3 + \dots \right] + n_{ij}/g^2, \quad (15)$$

# Data and fits

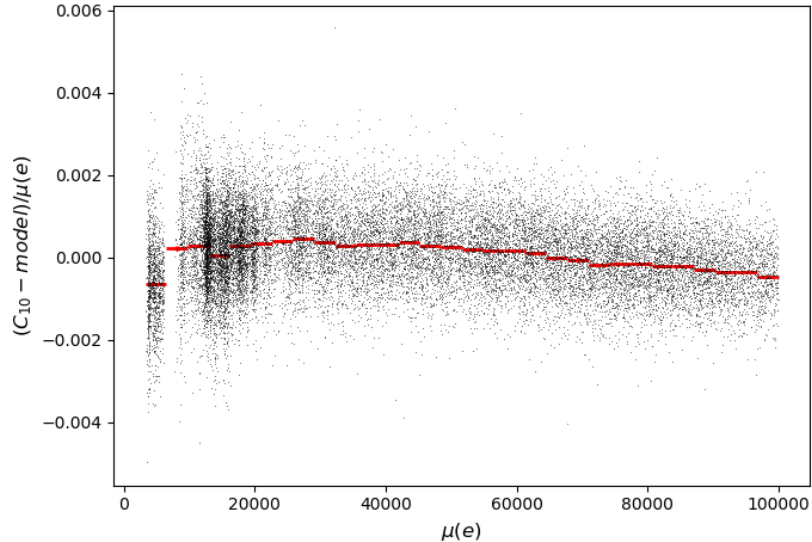
042  $C_{01}/\mu$ 

# PTC fits residuals

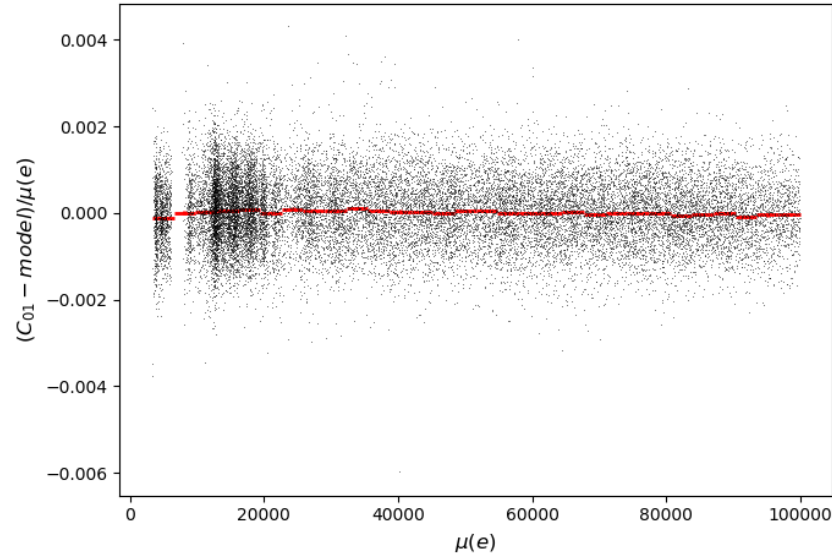
fit residuals (all HSC channels)  $i,j=0,0$



fit residuals (all HSC channels)  $i,j=1,0$

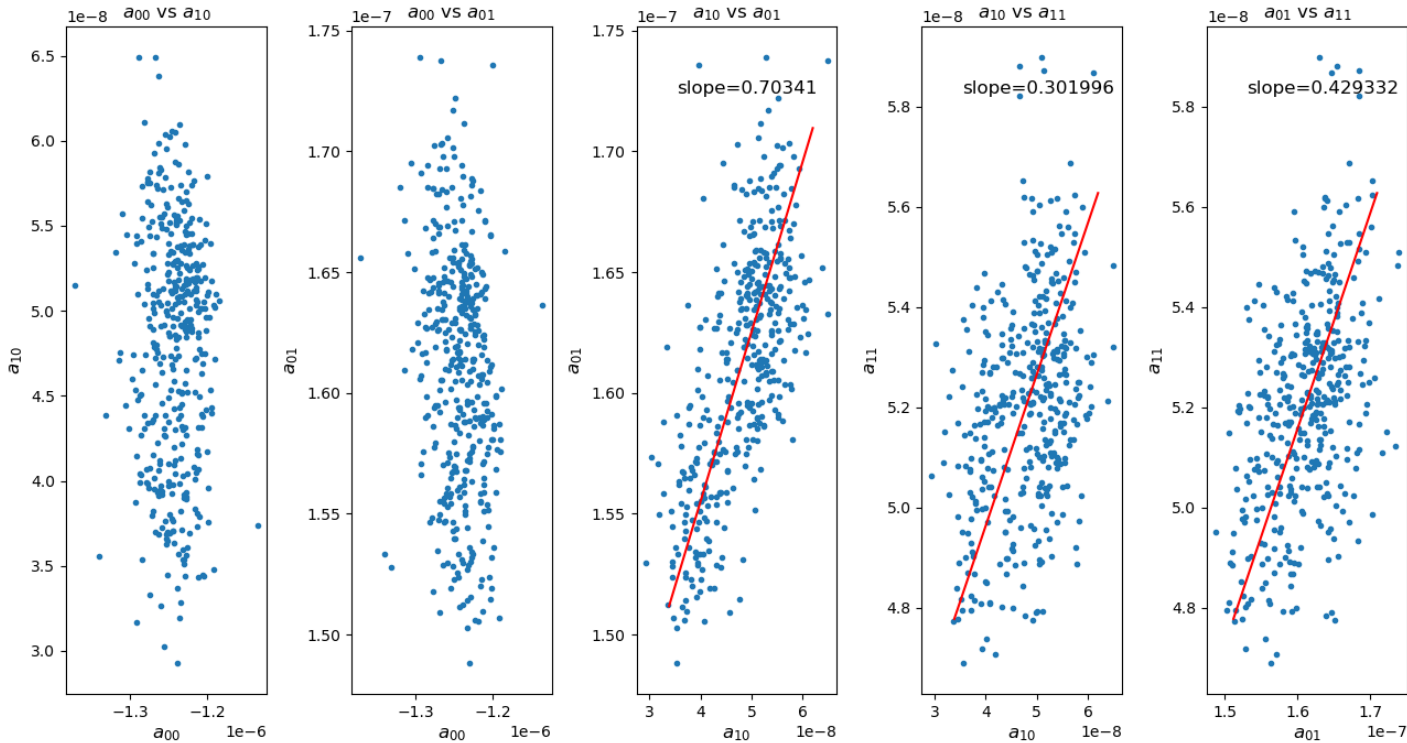


fit residuals (all HSC channels)  $i,j=0,1$



- There is some sort of next-to-leading order effect.
- An imperfect non-linear correction is an unlikely explanation because
  - non-linearity does not affect covariances
  - the non-linearity residuals are too small to accommodate the size of the effect.
- There are strange problems at low flux.
- Size is significant: about 10% of covariances.

# Distributions of $a_{ij}$ over ( $\sim 400$ ) channels



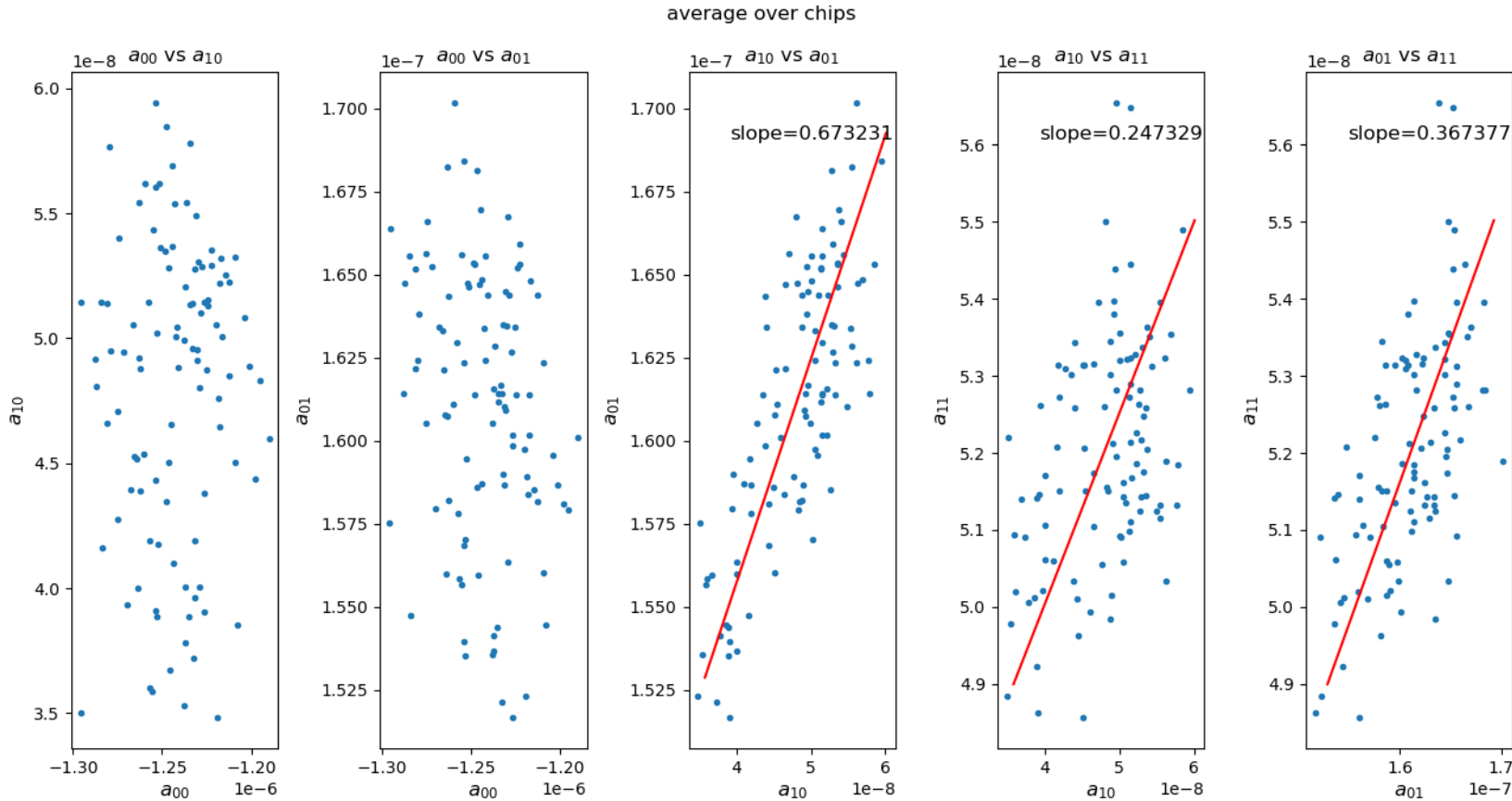
The  $a_{ij}$  are independent of the gain.

Spreads are larger than expected from shot noise

Covariances expected from fits are expected to go the other way

Variability is probably real.

# Average over chips

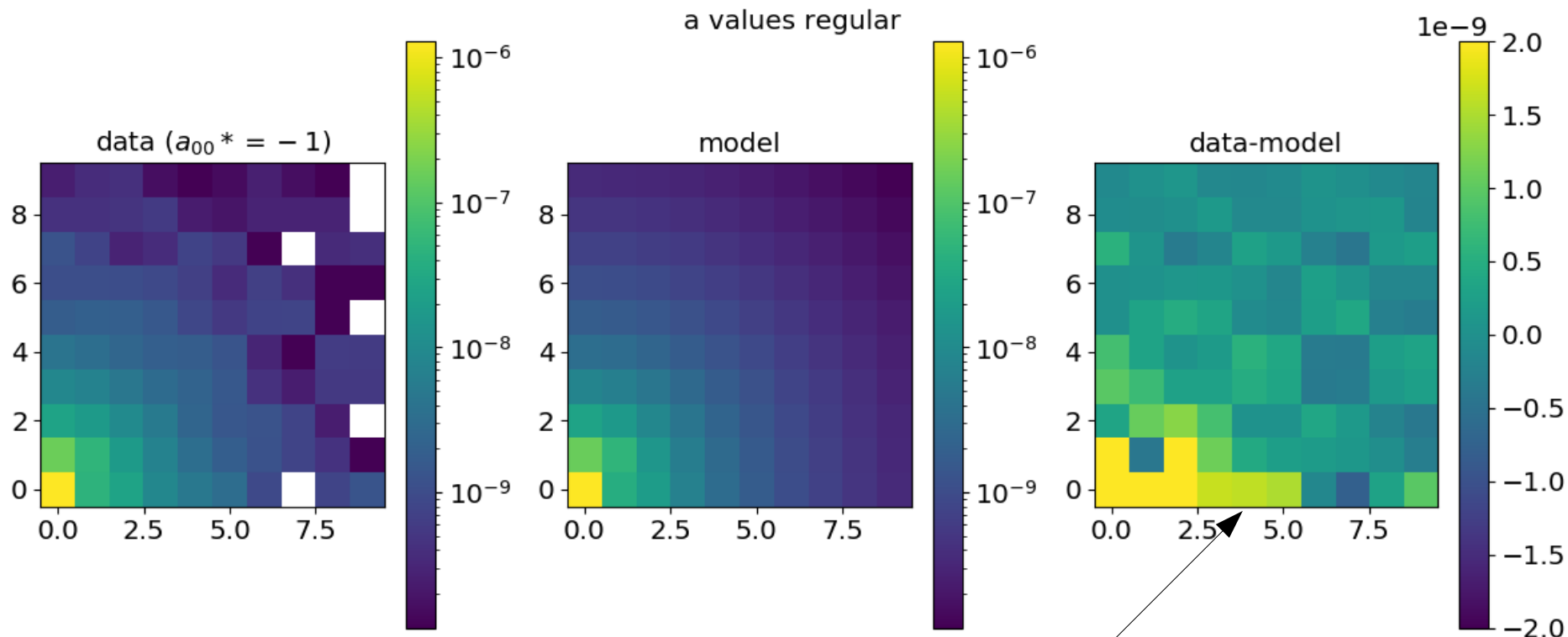


Both trends and ranges are similar to the amp-level data

# Average over all channels

- The spread over channels is at most 5 to 10% rms
- We decide to average the  $a_{ij}$  over all channels in order to get a significant measurement at a distance of a few pixels.
- We perform an electrostatic fit to the (average) data.
- The sum rule of the fitted  $a_{ij}$  coefficients is enforced  $\sum_{i,j} a_{ij} = 0$
- We measure :  $a_{00} = -1.26 \cdot 10^{-6}$  and  $\text{sum}(|i,j| < 10) = 7 \cdot 10^{-8}$
- Since we evaluate that  $\sum_{|i,j| > 9} a_{ij} \simeq 7 \cdot 10^{-8}$ , we have an excess of  $\sim 10\%$  of  $|a_{00}|$  in the data

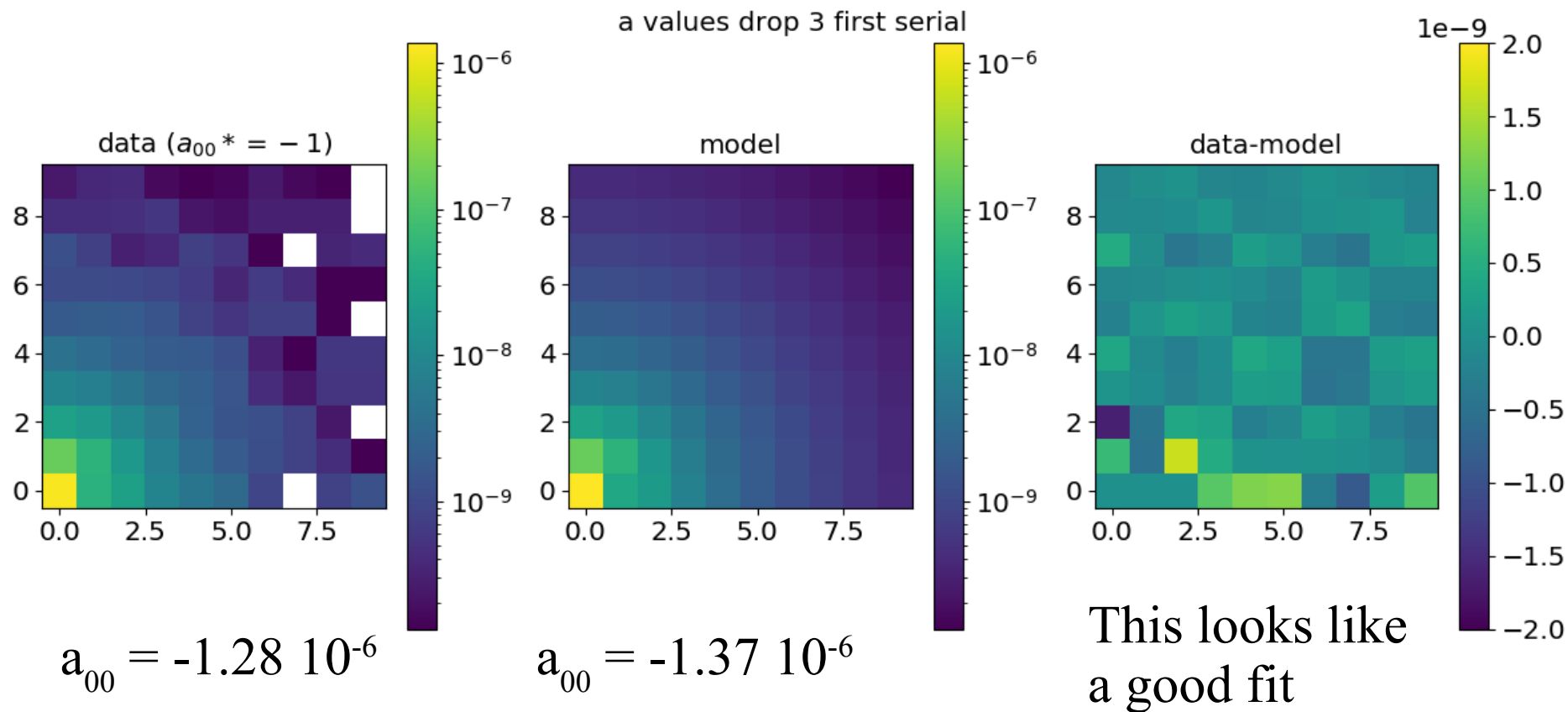
# Electrostatic fit

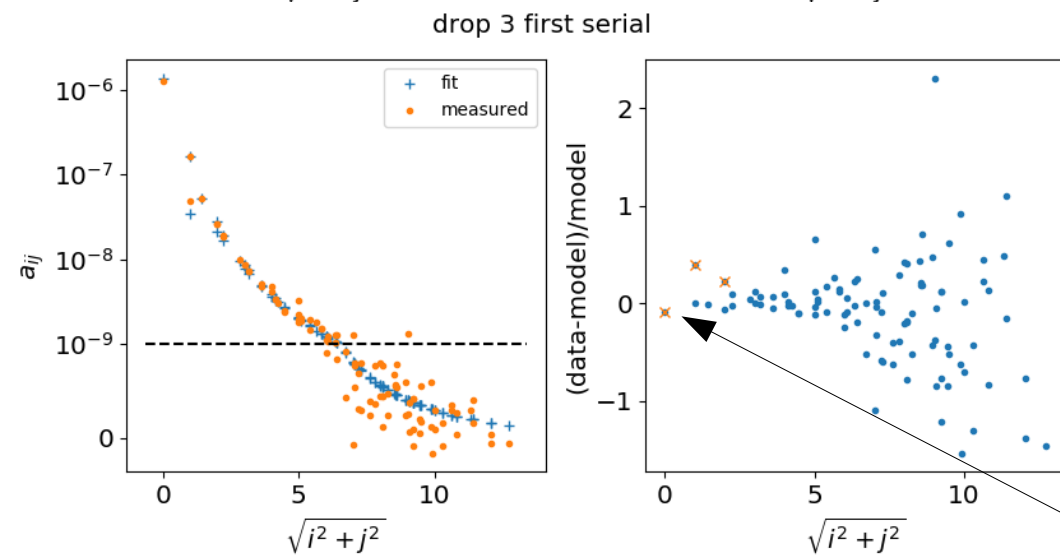
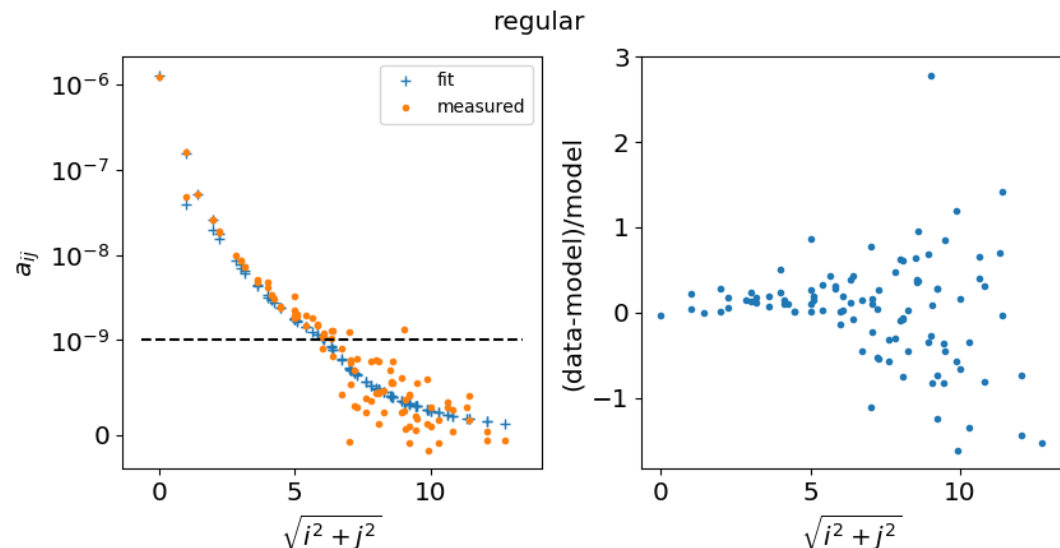


Electrostatics cannot accommodate the x/y asymmetry of data.



# Electrostatic fit without the first 3 serial pixels



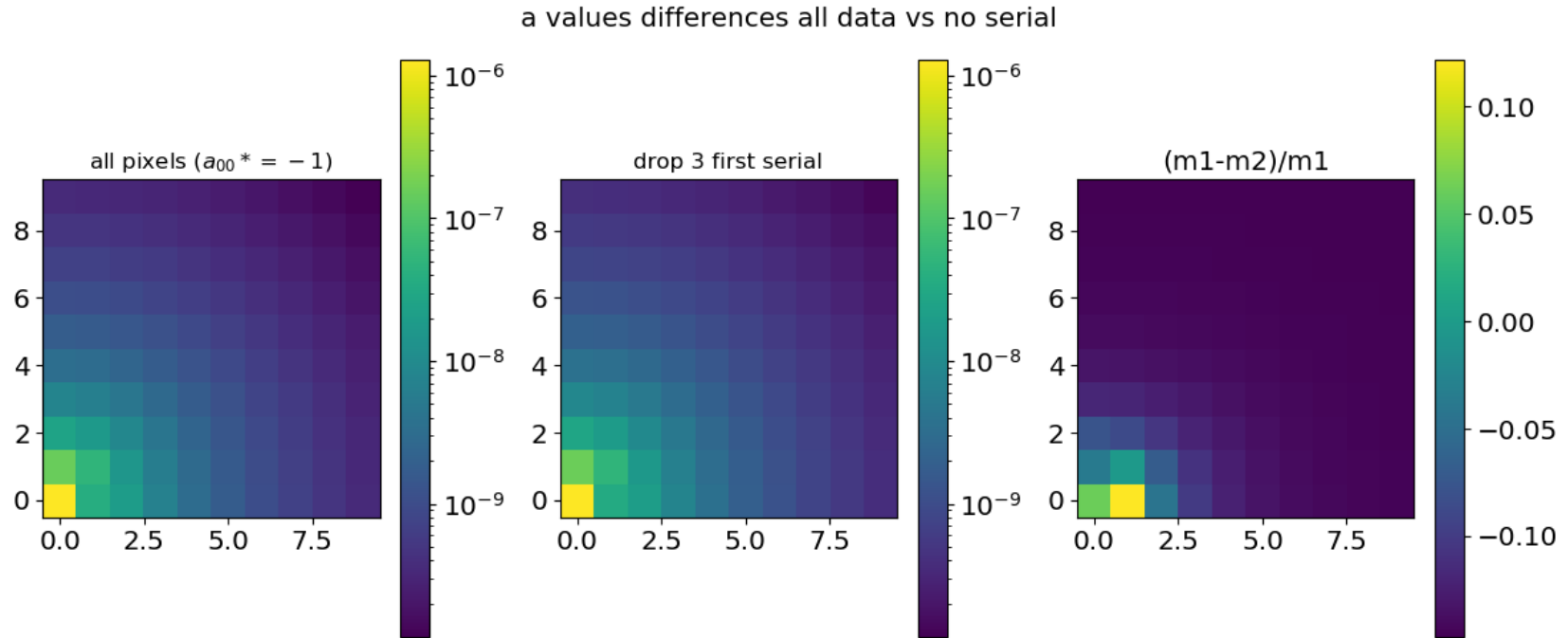


# Comparison

- All data points carry roughly the same uncertainty
- The bottom fit is much better than the top one

flipped sign

# Comparing the two models



The large-distance scale difference is about 15%

## Serial noise excess : which source ?

- The first covariance measurements along the serial direction cannot be described by an electrostatic model, because they are too large w.r.t their neighbor (same  $i$ ,  $j=1$ ) and their X/Y symmetric ( $i \leftrightarrow j$ )
- This can be the explanation for the “sum rule excess”.
- Since the HSC electronics uses Dual Slope Integration, (correlated) clock noise could be the culprit. But there are absolutely no cross-amp covariances ?!
- The dominant (variance) gain fluctuation would be  $\sim 3 \cdot 10^{-4}$  and decaying with distance.
- There is a lab measurement of this noise ([Miyake et al](#)),

# Gain noise on HSC front end, measured in the lab

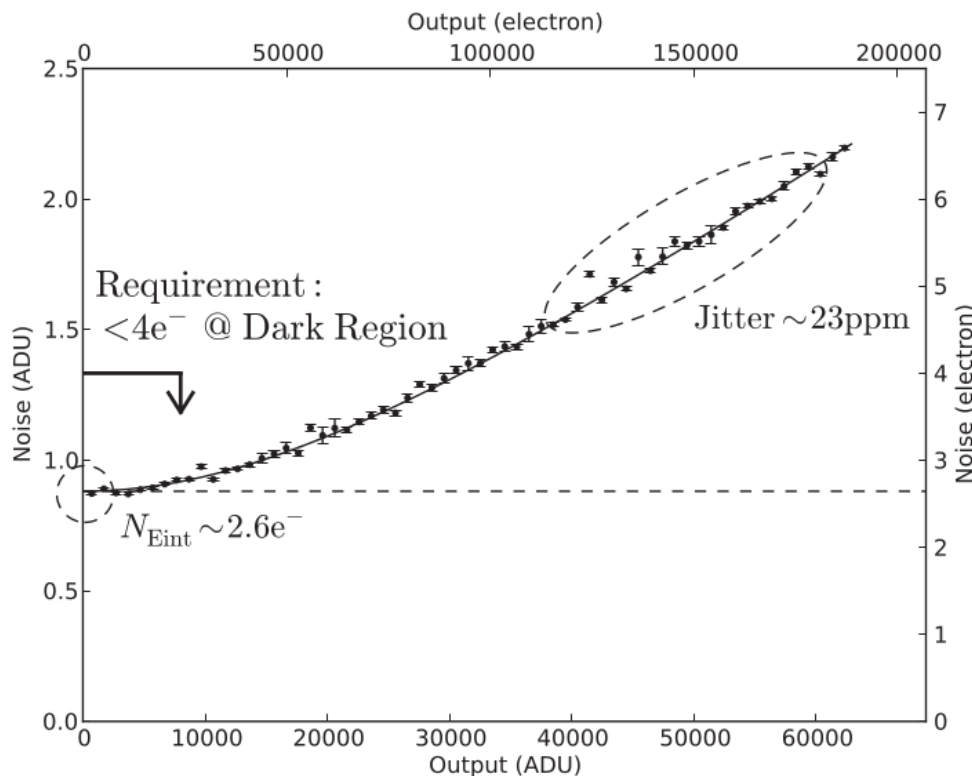


Fig. 8. Result of noise measurement.

“gain noise”:  
 $\sim 2 \cdot 10^{-5}$

It could be larger  
in the actual instrument,  
with probably different  
power supplies and  
environment.

No channels  
cross-correlations  
in this test.

## Chapter 2 : stars in science data.

- We have reduced (mostly Nicolas...) all the Ultra Deep data from the Subaru Strategic Program. This means Cosmos and SXDS (~1 pointing each), in 5 bands (grizy) over a few seasons, in order to detect and measure high-z SNe Ia. There are a few 100s events in this data, and (host) redshifts are being collected.
- The data covers a huge range in observing conditions.
- We use the code developed for SNLS, with a few modifications.
- What follows only depends on very simple algorithms, mostly the “Gaussian moments measurement”, similar if not identical to Galsim and DM.

# Gaussian moments measurements

- This is an unweighted least-squares fit of a Gaussian to a “spot”, with 6 parameters (flux, position, moments). There is a (large) speed-up trick for the Gaussian shape that we use (as Galsim).
- This is called “SDSS moments in DM”, adaptive moments in Galsim.
- Should be independent of flux if star images are free of BF...
- ... but because color and brightness are not independent (generally) in star samples, and because star sizes depend on color, I am using color measurements averaged in order to correct for the PSF chromaticity.

# Three processings

- No BF correction
- With BF correction from “fit 1” (all separations): model1
- With BF correction from “fit 2” (uses all separations but the 3 first serials): model2
- All corrections evaluate “charge on pixel frontiers” using a quadratic interpolator.
- There are  $\sim 20$  millions star measurements in each processing.



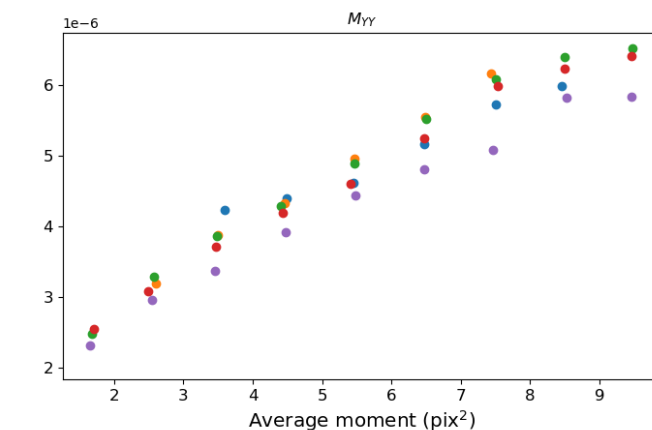
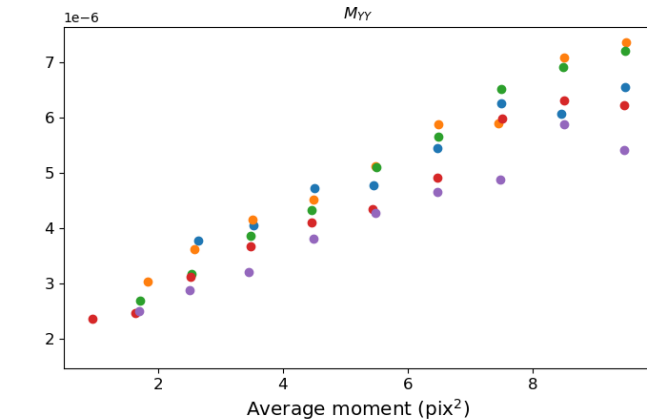
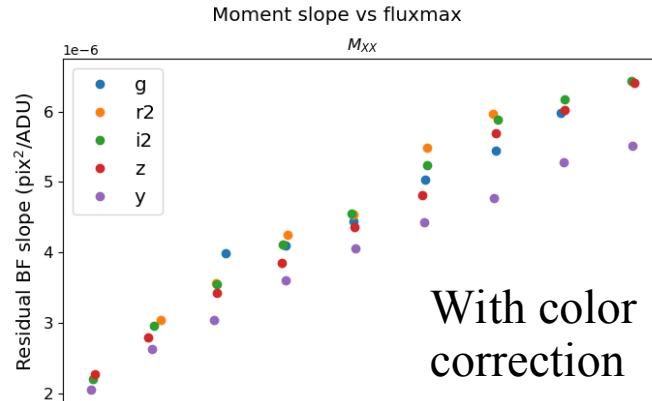
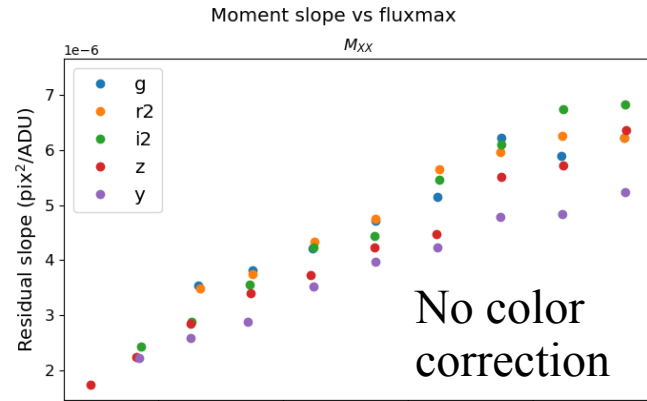
# Analysis

- For each CCD, we fit a 2D quadratic interpolator of the measured moments as a function of position in CCD, with outlier rejection.
- We then analyze the difference of the measurement to the smoothing, as a function of  $f_{\max}$  and color:

$$M_{ab} - \hat{M}_{ab} = \alpha f_{max} + \beta c + \gamma$$

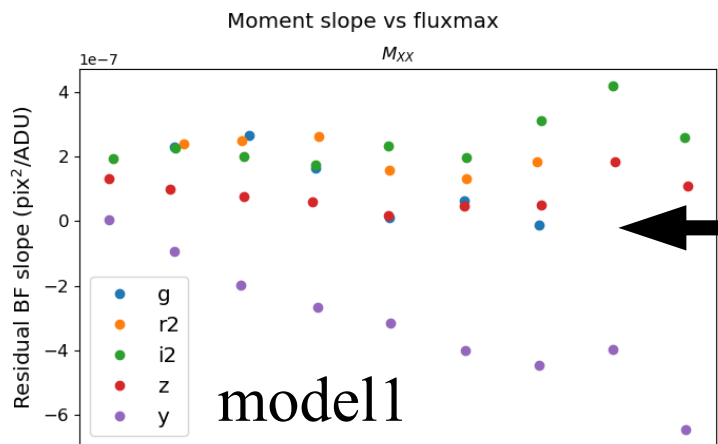
- We consider separately  $M_{xx}$  and  $M_{yy}$
- $f_{\max}$  is measured on flat-fielded images and the flats vary by  $\sim 30\%$  on HSC from chip to chip. Since we have to average over chips, this smears the BF relation.

# BF slopes on uncorrected data



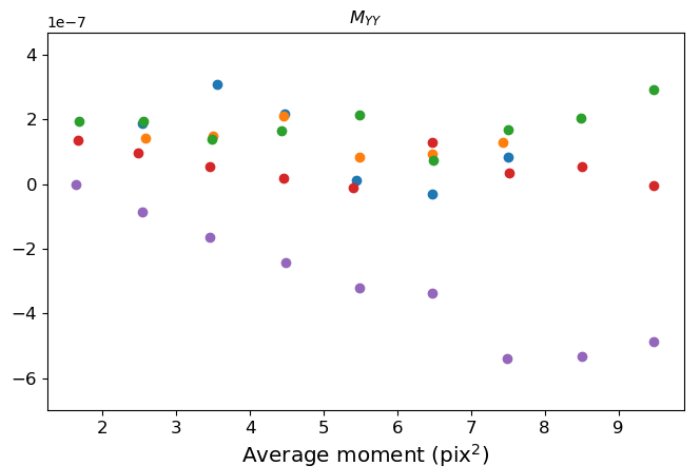
- At full scale ( $\sim 35\text{k ADUs}$ ), the second moment increase is  $\sim 3\%$
- The slope increases  $\sim$ linearly with moment
- X/Y asymmetry 10 to 20%
- Almost achromatic except for y and perhaps z bands.
- Color correction reduces the apparent slopes by  $\sim 10\%$

# Corrected data: BF slopes

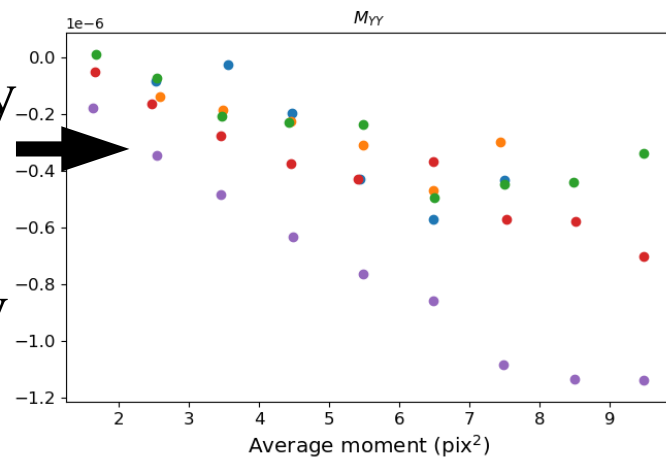
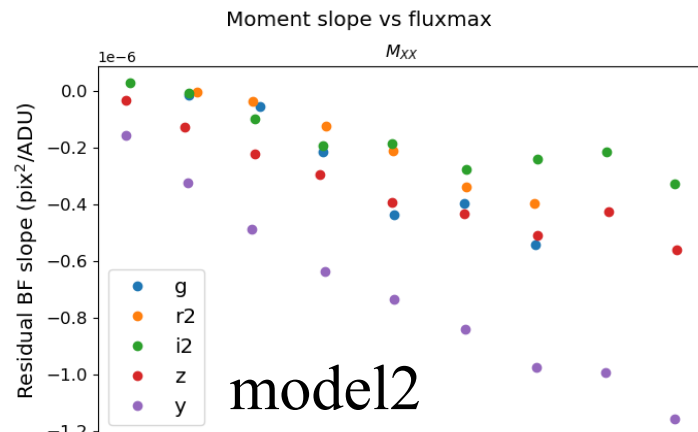


Let us ignore y for the time being.

- Effect reduced by much more than 10
- Residual slope independent of IQ (?!)

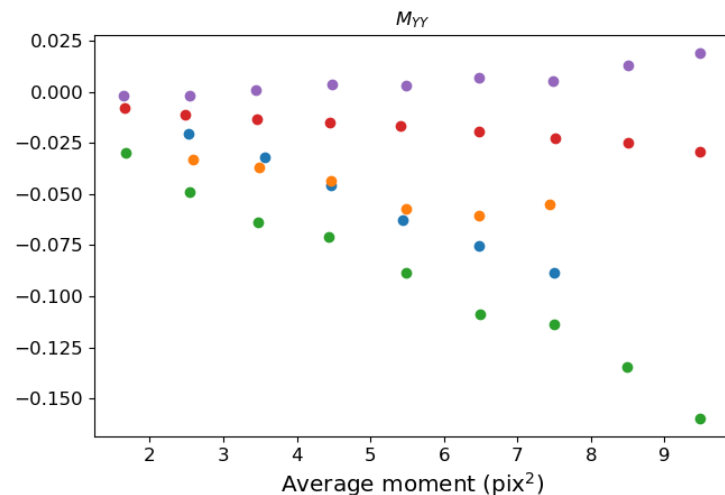
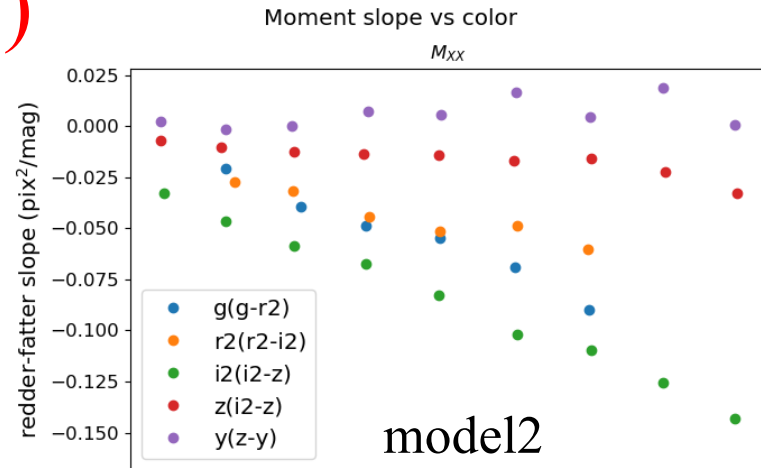
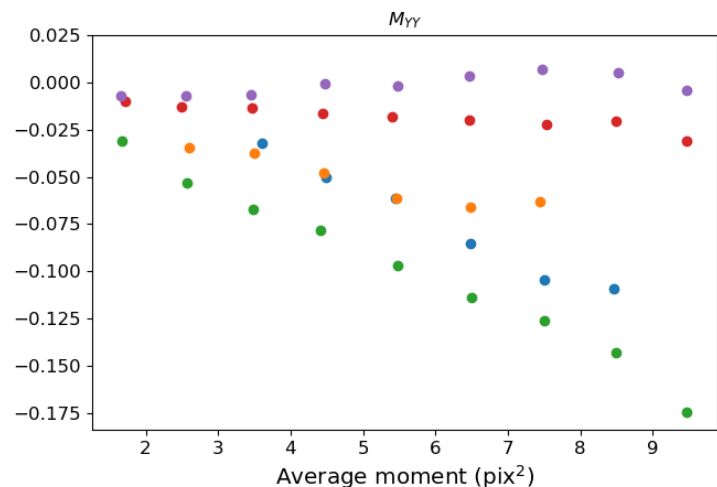
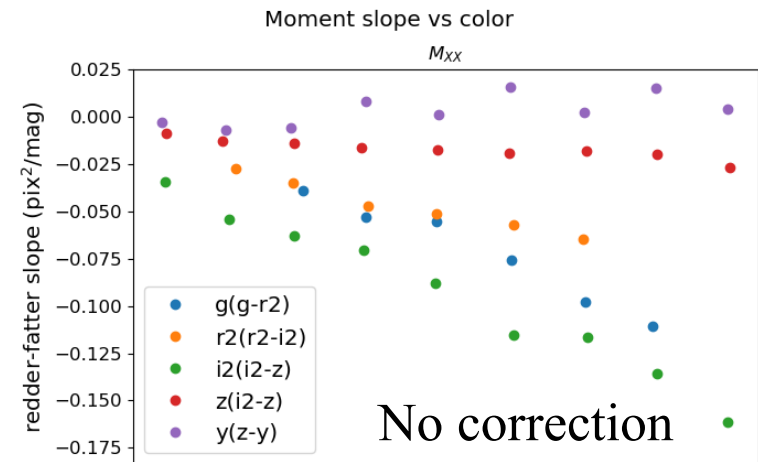


- Effect also reduced by much more than 10
- Looks like a slight over correction, mildly better than model1 (best IQs in particular)



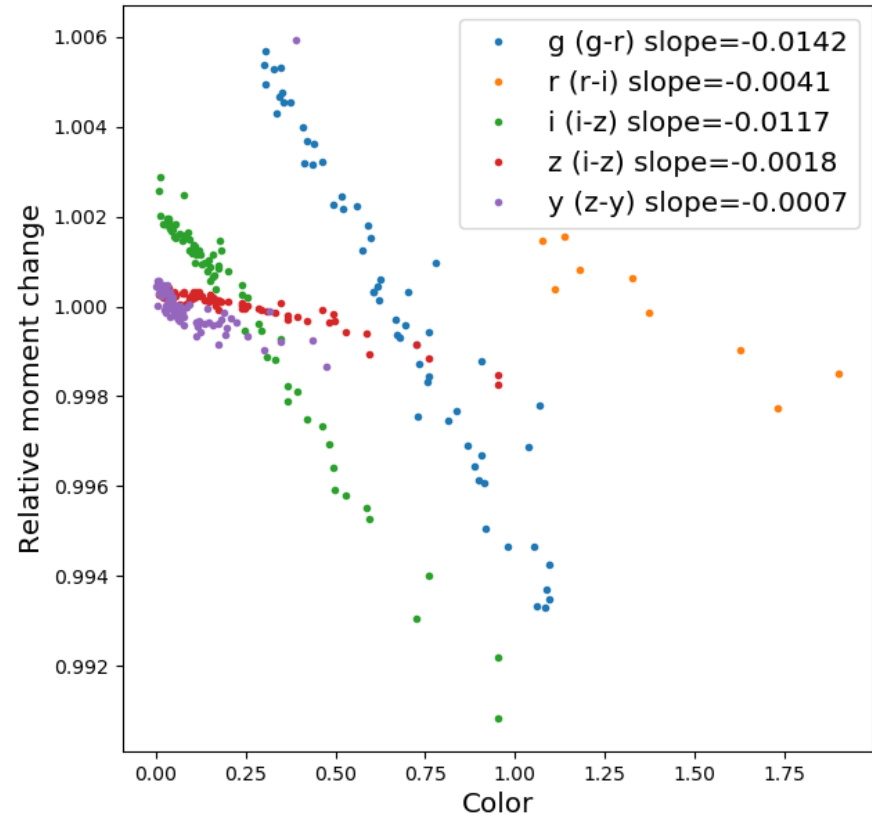
# Color slopes (1)

- The two plots are extremely similar
- Beware: the color index varies from band to band
- Surprised by the largest effect in i2
- No effect in y: compensating CCD effect ?
- The  $\sim$ linear increase with  $\text{size}^2$  is compatible with an atmospheric origin.



## Color slopes(2)

- On real data, the measured color slopes in g and i are of the order of 1 to 1.5% variations of second moments per unit color.
- Assuming the variation of PSF size\*\*2 goes as  $\lambda^{-0.4}$  provides the right order of magnitude, and essentially the same band ordering as observed.
- Need r2 and i2 bandpasses.

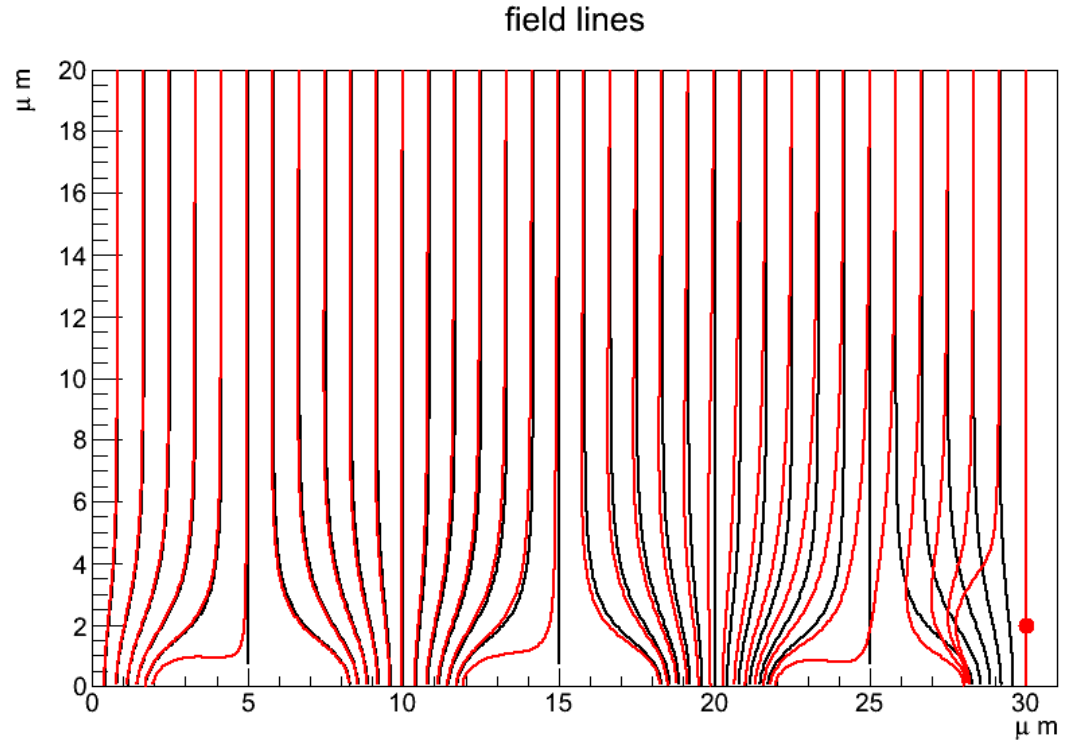


## Color slopes(3)

- The range of moment variation due to color is one half or less of the one due to BF.
- Regarding the measurement of BF effect on stars, the chromaticity of PSF acts as a sizable correction to the BF slope, because of a small covariance between flux and color in practical star samples.
- On BF-corrected data, the moments variations with color have become larger than the ones with flux.

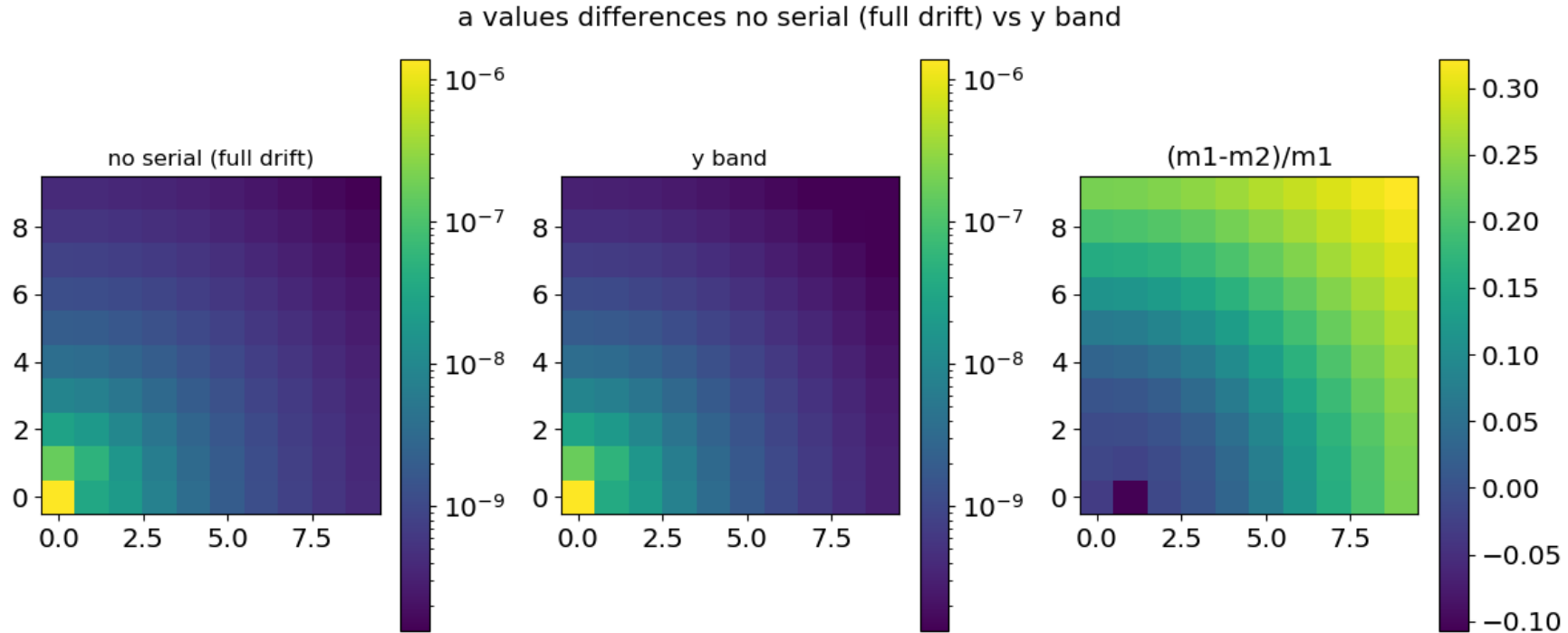
# Chromaticity of brighter-fatter ?

- The achromaticity of BF is more a principle than a fact.
- There are very few chromatic comparisons, if any.
- The physics indicates that it should be achromatic...
- ...but perhaps for large distances.



All the action happens near the bottom, so how could the conversion depth matter?

# Differences due to conversions in the bulk



Differences actually increase with distance.



## What's next?

- The quality of the correction is good enough to measure distant SNe.
- The full scale variation of star sizes is  $\sim 0.14\%$  after correction, which presumably allows one to measure a PSF size accurate to the  $10^{-3}$  level.
- Apply this reduced correction to y data and see if it explains the difference of y data as compared to other bands.
- Having to ignore variance and serial covariances is a concern. I am not sure that LSST is immune to this “gain noise” problem.
- I am starting to think that deriving the correction from the correlation function of flats is perhaps not the best way to go.