Exploring the Phase Diagram of Strongly Interacting Matter

from a wealth of experimental results my personal view of

- highlights
- physics insights
- perspectives





Johanna Stachel, Phys. Inst., Univ. Heidelberg International Symposium From Particles to the Universe Paris, December 10, 2021

the QCD phase diagram, as seen from a low energy nuclear physics viewpoint

the beginnings of research into the nuclear liquid gas phase transition: G. Bertsch and P. J. Siemens, Nuclear Fragmentation, PLB 126 (1983) 9

"we argue that fragmentation will occur when the nuclear matter has expanded adiabatically to the onset of hydrodynamic instability $\partial P/\partial V_{IS} = 0$ "



The caloric curve for the liquid gas phase transition

measurement with ALADiN

J. Pochodzalla, U. Lynen at al. Phys.Rev.Lett. 75 (1995) 1040



- temperatures from yield ratios He and Li
- excitation energies per nucleon of primary fragments from fragment and neutron distributions

Bi-modality and latent heat of liquid-gas phase transition

a major accomplishement by the INDRA and ALADiN collaborations, data obtained in Au-Au collisions at 60-100 MeV/nucleon at GSI

bi-modality as signal for phase transition in intermediate energy nuclear collisions

proposed by: P. Chomaz, M. Colonna, J. Randrup, Phys. Rep. 389 (2004) 263





size of largest fragment serves as order parameter of 1st oder phase transition between gas and liquid phase

 $\Delta E = E_g - E_l = 8.1(\pm 0.4)_{stat}(+1.2 - 0.9)_{syst}$ MeV/A

latent heat = energy difference between gas and liquid phase

E. Bonnet PRL 103 (2009) 072701

Equation of state of hot QCD matter in lattice QCD

computation of QCD EoS one of the major goals in IQCD community since 1980



consolidated results on EoS from different groups, extrapolated to continuum and chiral limit

rapid rise of energy density (normalized to T⁴ rise for relativistic gas)

- signals rapid increase in degrees of freedom due to transition from hadrons to quarks and gluons
- IQCD points to continuous cross over transition

Measure for chiral symmetry restoration in IQCD

order parameter: chiral condensate, its susceptibility peaks at T_c

S.Borsanyi et al. Wuppertal-Budapest Coll., PRL 125 (2020) 052001 A.Bazavov et al. HotQCD Coll., PLB795 (2019) 15



comparing different measures: pseudo-critical temperature for the chiral phase transition $T_c = 156.5 + 1.5 \text{ MeV}$

Experimental program

QGP and phase diagram studied in high energy collisions of nuclei

accelerator	years	√s _{NN}	large exp.
AGS	1986 - 2002	2.7 - 4.8 GeV	5
SPS	since 1986	6.2 - 19.3 GeV	7
RHIC	since 2000	7.0 – 200 GeV	4
LHC	since 2009	2.76 – 5.02 TeV	3 (4)



Space-time evolution of a relativistic nuclear collision at LHC energy



Charged particle production



increase in nuclear collisions much faster with \sqrt{s} than in pp

larger fractional energy loss in nuclear collision

Nuclear stopping power



AGS: nuclei stop each other completely $\Delta y = 1.7$ **SPS:** slight onset of transparency $\Delta y = 2.0$ **RHIC:** 'limiting fragmentation' $\Delta y = 2.0$ implying fraction 1-exp(- Δy) = 86% E_{loss} energy deposit in central fireball in pp (Fermilab data): $\Delta y = 0.95 \triangleq 60\%$ E_{loss}



Initial Energy Density

 $\epsilon_0 = dE_t/dy/A_t \times dy/dz = \langle m_t \rangle 1.5 dN_{\rm ch}/dy/A_t \times dy/dz$

Bjorken formula using Jacobian dy/dz=1/ τ_0 typically evaluated at τ_0 = 1 fm/c

	$\sqrt{s_{NN}}$	dE _t /dy	ϵ_0	Т
	(GeV)	(GeV)	(GeV/fm ³)	(GeV)
AGS	4.8	200	1.4	0.17
SPS	17.2	450	3.0	0.21
RHIC	200	600	5.5	0.30
at τ_0	$= 1/p_{sat} =$	40	0.49	
LHC	2760	1755	11.7	0.36
at τ_0	$= 1/p_{sat} =$	0.08 fm/c	146	0.68

all above IQCD result for pseudo-critical energy density and temperature

* these are lower bounds; if during expansion work is done (pdV) initial energy density higher (indications from hydrodynamics at LHC: factor 3)

Hadronization of the fireball

hadro-chemical freeze-out at phase boundary between QGP and hadronic matter

First measurement of a comprehensive set of hadrons at BNL AGS by 1993

14.6 A GeV/c central Si + Au collisions – combined data by E802, E810, E814



first successful application of statistical hadronization model (grand canonical ensemble) - 2 fit parameters dynamic range: 9 orders of magnitude! no deviation

P. Braun-Munzinger, J. Stachel, J.P. Wessels, N. Xu, PLB344 (1995) 43

Beam energy dependence of hadron yields in AuAu and PbPb collisions from AGS to LHC

fits work equally well at higher beam energies following the obtained T and μ_b evolution, features of proton/pion and kaon/pion ratios reproduced in detail

A. Andronic, P. Braun-Munzinger, J.Stachel, PLB 673 (2009) 142



Production of hadrons and (anti-)nuclei at LHC

1 free parameter: temperature T T = 156.5 ± 1.5 MeV

agreement over 9 orders of magnitude with QCD statistical operator prediction (- strong decays need to be added)

- matter and antimatter are formed in equal portions at LHC
- even large very fragile hypernuclei follow the same systematics



Biggest difference LHC compared to lower energies

- matter and anti-matter produced in equal proportions at LHC - consistent with net-baryon free central region, (μ_b < 1 MeV)

similar to early universe



Energy dependence of temperature and baryochem pot.



from pp to Pb-Pb collisions: smooth evolution with system size



universal hadronization can be described with few parameters in addition to T and $\mu_B \rightarrow transition$ from canonical to grand-canonical thermodynamics J. Cleymans, P.M. Lo, K. Redlich, N. Sharma, PRC 103 (2021) 014904

Hadron spectra and correlations

- reveal in addition to kinetic freeze-out temperature strong collective expansion
- survival of early fluctuations
- transport parameters of the QGP

Spectra of identified hadrons at SPS



Spectra of identified hadrons at RHIC and LHC



spectral shapes exhibit even stronger mass dependence

 characteristic for hydrodynamic expansion

indicate at LHC significantly larger expansion velocity than at RHIC

captured well by hydrodynamic expansion (EPOS, K. Werner et al. Subatech)

expansion velocity at surface: ³⁄₄ c

Azimuthal anisotropy of transverse spectra



Fourier decomposition of momentum distributions rel. to reaction plane:

$$\frac{dN}{dp_t dy d\phi} = N_0 \cdot \left[1 + \sum_{i=1}^{N} 2v_i (y, p_t) \cos(i\phi)\right]$$

quadrupole component v₂ "elliptic flow"

the v_n are the equivalent of the power spectrum of cosmic microwave rad.

Elliptic flow as function of collision energy



- effect of expansion (positive v_2) seen from top AGS energy upwards
- at lower energy: shadowing by fragments
- first discovered as tiny 2% effect by E877 in 1993

very much inspired by

Anisotropy as a signature of transverse collective flow

Jean-Yves Ollitrault (Saclay) (Mar 20, 1992)

Published in: Phys.Rev.D 46 (1992) 229-245

at top SPS energy, modelling with ideal relativistic hydrodynamics close to exp. data



Discovery of RHIC: paradigm of QGP as near ideal liquid



in hydro regime v₂ driven by
initial condition and
properties of the liquid as η/s
→ ambiguity between the two can be resolved by correlating observables

how perfect is the fluid observed at RHIC? very small ratio of shear viscosity to entropy density η /s describes data



Constraining initial condition and QGP medium properties

much higher precision can be obtained from cumulants defined in terms of multiparticle azimuthal correlations

N. Borghini, P.M. Dinh, J.Y. Ollitrault, PRC 64 (2001) 054901 → visionary paper guiding the way

LHC: global Bayesian analysis of such new collective flow observables in PbPb from ALICE

J. Parkkila et al., arXiv: 2111.08145



near T_c, shear viscosity/entropy density close to AdS/CFT lower bound $1/4\pi$ rising with temperature in QGP – bulk viscosity/entropy dens. peaks near T_c

Jet quenching – parton energy loss in QGP



Extracting the jet quenching parameter

prediction: H. Baier, Y.L. Dokshitzer, A.H. Mueller, S. Peigne, D. Schiff, NPB 483 (1997) 291 and 484 (1997) 265

 $dE/dx \propto \rho \sigma \langle k_t^2 \rangle L$

density of color charge carriers transport coefficient $\hat{q} \propto \rho \ \sigma \langle k_t^2 \rangle$





determine transport coefficient from comparing a combined model of splitting of high virtuality partons (MATTER) and scattering between jet partons and a thermal QGP (LBT) to inclusive hadron R_{AA} data for RHIC and LHC (Bayesian parameter estimation)

obtain

 $\hat{q} = 0.7 \pm 0.3 \text{ GeV}^2/\text{fm}$ at T = 400 MeV

factor 20-40 larger than in cold nuclear matter (from DIS)!

Charmonia as a probe of deconfinement

the original idea: implant charmonia into the QGP and observe their modification (Debye screening of QCD), in terms of suppressed production in nucleus-nucleus collisions – sequential melting

T. Matsui and H. Satz PLB 178 (1986) 416

"If high energy heavy-ion collisions lead to the formation of a hot quark-gluon-plasma, then color screening prevents $c\bar{c}$ binding in the deconfined interior of the interaction region. ... It is concluded that J/ψ suppression in nuclear collisions should provide an unambiguous signature of quark-gluon-plasma formation."

First J/ ψ suppression in nuclear collisions at SPS

key measurements by NA38 find suppression for O and S induced collisions QM 1991 conf.: data on photon, hadron, and nucleus-nucleus coll. described by nuclear absorption

C. Gerschel and J. Hűfner, Z.Physik C56 (1992) 171



finally observations NA50:

- in pp, pA and light nuclei, suppression pattern consistent with absorption on (cold) nuclear matter 4.3±0.5 mb

- in central collisions of PbPb much stronger suppression

data described by dissolution of J/ψ at critical density $n_c = 3.7/fm^2 - - -$ & including energy density fluct.

J.P. Blaizot, P.M. Dinh, J.Y. Ollitrault PRL 85 (2000) 4012

Charmonium formation at hadronization: extension of statistical model to include charmed hadrons

new insight:

QGP screens all charmonia, but charm quarks remain in the fireball charmonium production takes place at the phase boundary

- enhanced production at colliders signal for deconfinement
 - P. Braun-Munzinger, J. Stachel, PLB 490 (2000) 196

technically:

- assume: all charm quarks are produced in initial hard scattering number not changed in QGP
 N^{direct} from data (total charm cross section) or from pQCD
- hadronization at T_c following grand canonical statistical model used for hadrons with light valence quarks (canonical corr. if needed) technically number of charm quarks fixed by a charm-balance equation containing fugacity g_c (no free parameter)

$$N_{c\bar{c}}^{direct} = \frac{1}{2}g_c V(\sum_i n_{D_i}^{therm} + n_{\Lambda_i}^{therm}) + g_c^2 V(\sum_i n_{\psi_i}^{therm}) + \dots$$

J/ψ suppression at RHIC – 200 A GeV AuAu



PHENIX talk at QM2006:

suppression patterns are remarkably similar at SPS and RHIC!

cold matter suppression larger at SPS, hot matter suppression larger at RHIC, balance?

recombination cancels additional suppression at RHIC?

how did we get so "lucky"?

data could be indeed described by statistical hadronization using pQCD charm cross section A.Andronic, P.Braun-Munzinger, K.Redlich, J.Stachel, PLB 652 (2007)259

Expectations for LHC

2 possibilities:



Energy Density

J/ψ production in PbPb collisions: LHC relative to RHIC



melting scenario not observed rather: enhancement with increasing energy density! (from RHIC to LHC and from forward to mid-rapidity)



Energy Density

33

J/ψ overpopulation due to hard production of charm and statistical hadronization of deconfined quarks



J/ ψ enhanced compared to other M = 3 GeV hadrons by factor g_c^2 = 900 relative to purely thermal yield quantitative agreement with hadronization of deconfined thermalized charm quarks

Suppression of Upsilon states



Outlook – an incomplete, but maybe realistic wishlist for the coming decade

Important measurements to come:

- open charm cross section in PbPb down to pt=0, baseline for J/ψ
- higher charmonium states to determine T for deconfinement transition
- to what degree does beauty thermalize in QGP, baseline for Upsilon understanding
- direct photons (real and virtual) and their azimuthal asymmetries with larger significance, thermal evolution of QGP
- low mass dilepton pairs and rho spectral function, chiral symmetry restoration
- fluctuations of conserved charges as sign of critical behavior
 - at LHC due to proximity to O(4) critical region
 - at lower energies due to possible critical endpoint in phase diagram

Tasks for theory:

- the way to thermalization: from overpopulated gluon fields to hydrodynamics to hadronization
- determination of temperature dependent transport coefficients from exp. data
- first principles computation of transport coefficients
backup

Alternative for lattice QCD EoS



from Bazavov arXiv: 1407.6387

Measure of deconfinement in IQCD



rapid drop suggests: chiral cross over and deconfinement appear in the same narrow temperature range

Analysis of hadron yields: the statistical model – grand canonical

partition function: $\ln Z_i = \frac{Vg_i}{2\pi^2} \int_0^\infty \pm p^2 dp \ln(1 \pm \exp(-(E_i - \mu_i)/T))$

particle densities: $n_i = N/V = -\frac{T}{V} \frac{\partial \ln Z_i}{\partial \mu} = \frac{g_i}{2\pi^2} \int_0^\infty \frac{p^2 \, \mathrm{d}p}{\exp((E_i - \mu_i)/T) \pm 1}$

for every conserved quantum number there is a chemical potential:

$$\mu_i = \mu_B B_i + \mu_S S_i + \mu_{I_3} I_i^3$$

but can use conservation laws to constrain V, μ_S, μ_{I_3}



SPS Pb + Pb data and thermal model



J. Stachel, 50 years IN2P3

First phase diagram with experimental points



Production of light nuclei and antinuclei at the AGS



J. Stachel, 50 years IN2P3

Production of light anti-nuclei at LHC energy



penalty factor exp(-m/T) \approx 300 for nuclei and anti-nuclei as $\mu_b = 0$ at LHC compared to 24 for nuclei at top AGS energy and 140 000 for anti-nuclei with $\mu_b = 537$ and T=124 MeV

Propagation of sound in the quark-gluon plasma



long-range rapidity correlations <u>understanding</u>: higher harmonics (3,4,5,...) are due to initial inhomogeneities caused by granularity of binary parton-parton collisions survive the 10 fm/c hydrodynamic expansion phase

M. Luzum PLB 696 (2011) 499



Higher flow harmonics and their fluctuations

data: ATLAS JHEP 1311 (2013) 183 calc: B. Schenke, R. Venugopalan, Phys. Rev. Lett. 113 (2014) 102301



x [fm]

x [fm]

Elliptic Flow in PbPb Collisions at $\sqrt{s_{NN}} = 2.76 \text{ TeV}$



rapidly rising v_2 with p_t and mass ordering typical features of hydrodyn. expansion same hydrodynamics calc. with small eta/s reproduces data

Bose-Einstein correlations and space-time extent of fireball

stochastic emission from extended source consider 2 identical bosons (photons, pions, ...) 2 detectors in locations r_1 , r_2 observe identical bosons of momenta p_1 and p_2



cannot distinguish solid and dashed paths because of identical particles for plane waves, the probability amplitude for detection of the pair is

$$A_{12} = \frac{1}{\sqrt{2}} \left[e^{ip_1(r_1 - x)} e^{ip_2(r_2 - y)} + e^{ip_1(r_1 - y)} e^{ip_2(r_2 - x)} \right]$$

square of amplitude: intensity "intensity interferometry"

technique of intensity interferometry developed by Hanbury-Brown and Twiss in astrophysics as a means to determine size of distant objects

Hanbury-Brown/Twiss correlations to measure the spacetime extent of the fireball

Au + Au at 10.8 A GeV E877 data compared to RQMD



2-Pion Hanbury-Brown/Twiss correlations \rightarrow Radius Parameters as Function of Pair Transverse Momentum



Freeze-out volume and duration of expansion





pion HBT



Direct photons: give access to entire time evolution

WA98



 $\lambda_{mfp} \ge$ medium \rightarrow access to early QGP-phase

Direct photons: give access to entire time evolution



 $\lambda_{mfp} \ge$ medium \rightarrow access to early QGP-phase

first significant measurement in PbPb collisions: WA98 at SPS

- data consistent with QGP formation ($T_i = 200-270 \text{ MeV}$)
- but also purely hadronic scenario w. Cronin enhancement accounts for data

Direct photons at RHIC and LHC



J. Stachel, 50 years IN2P3

55

Direct photons at RHIC & LHC exhibit strong elliptic flow



Low and intermediate mass lepton pairs



- up to mass ≈1.0 GeV: radial flow of a hadronlike di-lepton source
- above: thermal component with $T = 205 \pm 12 \text{ MeV}$
- virtual photons vs real photons above

Low and intermediate mass lepton pairs



Low and intermediate mass lepton pairs at colliders



at colliders much more difficult
at RHIC after 15 years consolidated results between STAR and PHENIX described well by the same models as SPS data
for ALICE very challenging project for Run3/Run4



How does this modified ρ look like? integrate over spacetime evolution of spectral function for ee mass spectrum



Where does lost energy go?

Jet-hadron correlations in pp and PbPb collisions at 5.02 TeV



low momentum particles and at larger distance from jet core

in pA and light nucl. coll. J/ψ production suppressed (NA38)



RUPRECHT-KARLS-UNIVERSITÄT HEIDELBERG

Anomalous J/ ψ Suppression in PbPb Collisions



J/ψ and statistical hadronization



production in PbPb collisions at LHC consistent with deconfinement and subsequent statistical hadronization within present uncertainties main uncertainties for models: open charm cross section, shadowing in Pb

transverse momentum spectrum



softer in PbPb as compared to pp

a qualitatively new feature as compared to RHIC where the trend is opposite

in line with thermalized charm in QGP at LHC, forming charmonia

elliptic flow of J/ψ vs p_t



ALI-PREL-119005

first observation of significant $J/\psi v_2$ in line with expectation from statistical hadronization

ψ**(2S)**

in picture where psi is created from deconfined quarks in QGP or at hadronization, psi(2S) is suppressed more than J/psi



What about $\psi(2S)$?



also excited state population completely in line, suppressed by Boltzmann factor errors will decrease with more data in LHC Run3/4

Charmonium at LHC: peaks at mid-y and strong enhancement at low transverse momentum



nuclear modification factor:

J/ψ transverse momentum spectra from stat. hadr.



M. Köhler, A. Andronic, P. Braun-Munzinger, JS, arXiv:1807.01236

good agreement up to 5 GeV/c without any free parameters J/ψ formed at hadronization at T_c from thermalized charm quarks flowing with the rest of the medium

Ratios of charm hadron to D⁰ spectra



Spectra and R_{AA} of D^0 mesons and Λ_c baryons

for open heavy flavor hadrons strong contribution from resonance decays

- include all known charm hadron states as of PDG2020 in SHMc
- compute decay spectra with FastReso: 76 2-body and 10 3-body decays
- (A. Mazeliauskas, S. Floerchinger, E. Grossi, D. Teaney, EPJ C79 (2019) 284 arXiv: 1809.11049)


Feeding into Upsilon (1S)



Upsilon R_{AA} rapidity dependence



Indication: R_{AA} peaked at mid-y like for J/ ψ not in line with collisional damping in expanding medium

the Upsilon could also come from statistical hadronization

SHM/thermal model: Andronic et al.



in this picture, the entire Upsilon family is formed at hadronization but: need to know first – do b-quark thermalize at all? spectra of B - total b-cross section in PbPb