

Charting new particle physics with primordial GWs

Planck 2022
01.06.2022

based on
[1912.02569 Cosmic-string GW](#) (model-independent)
[1912.03245 Cosmic-string GW probes heavy & unstable particles](#)
[2108.10328, 2111.01150](#)
Primordial GWs probe [kination era and axion physics](#).



Yann Gouttenoire (Tel Aviv university)
with
Peera Simakachorn (DESY & U.Hamburg),
Géraldine Servant (DESY & U.Hamburg)

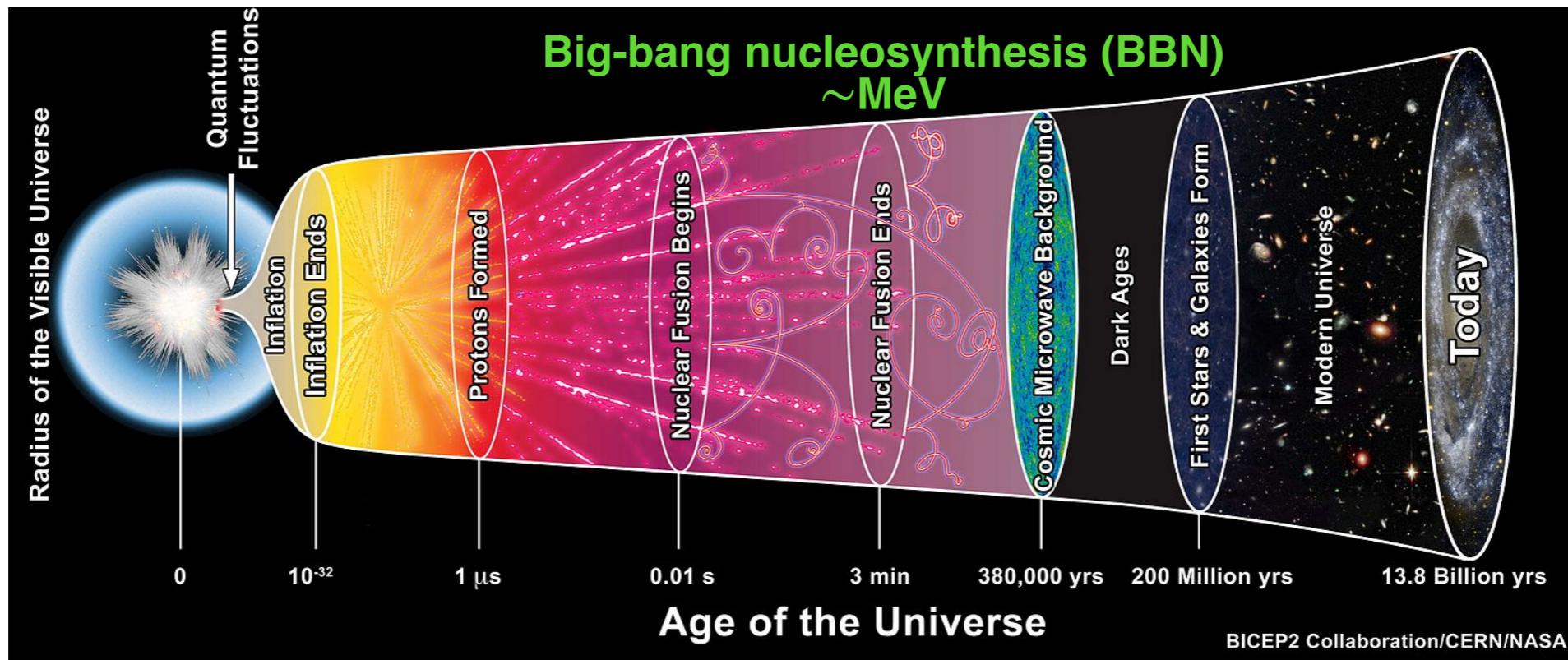


Funded by



History of the Universe

high energies ← → low energies



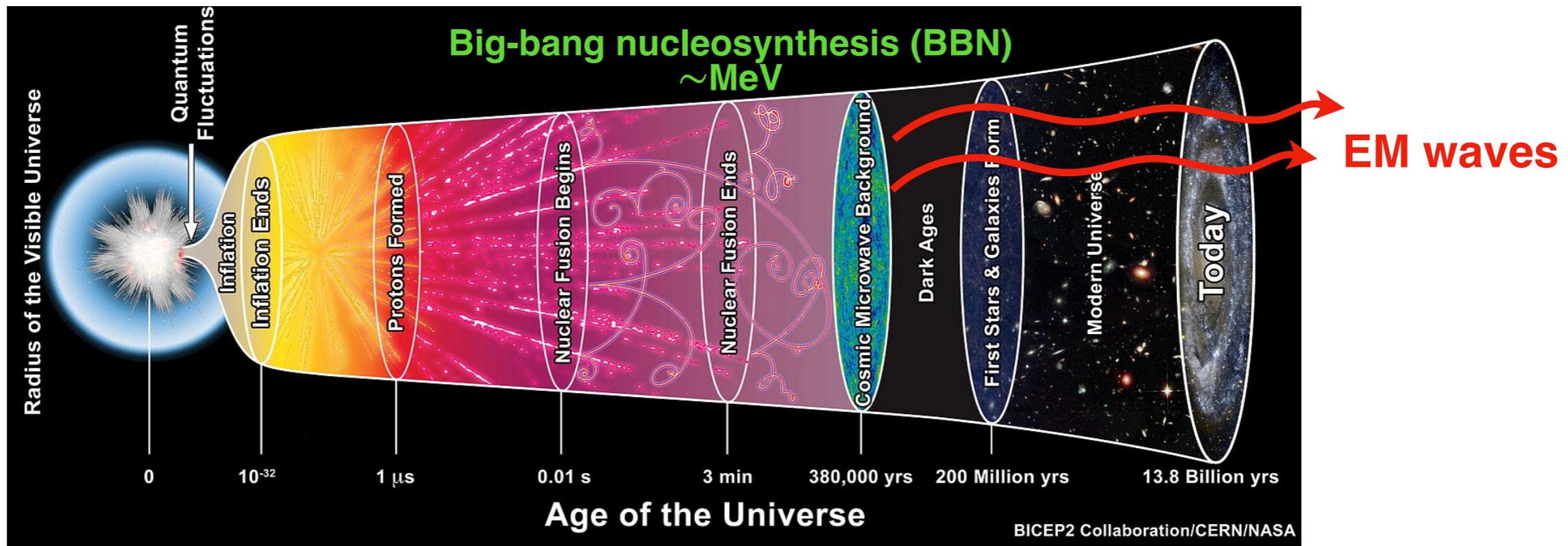
History of the Universe

high energies



low energies

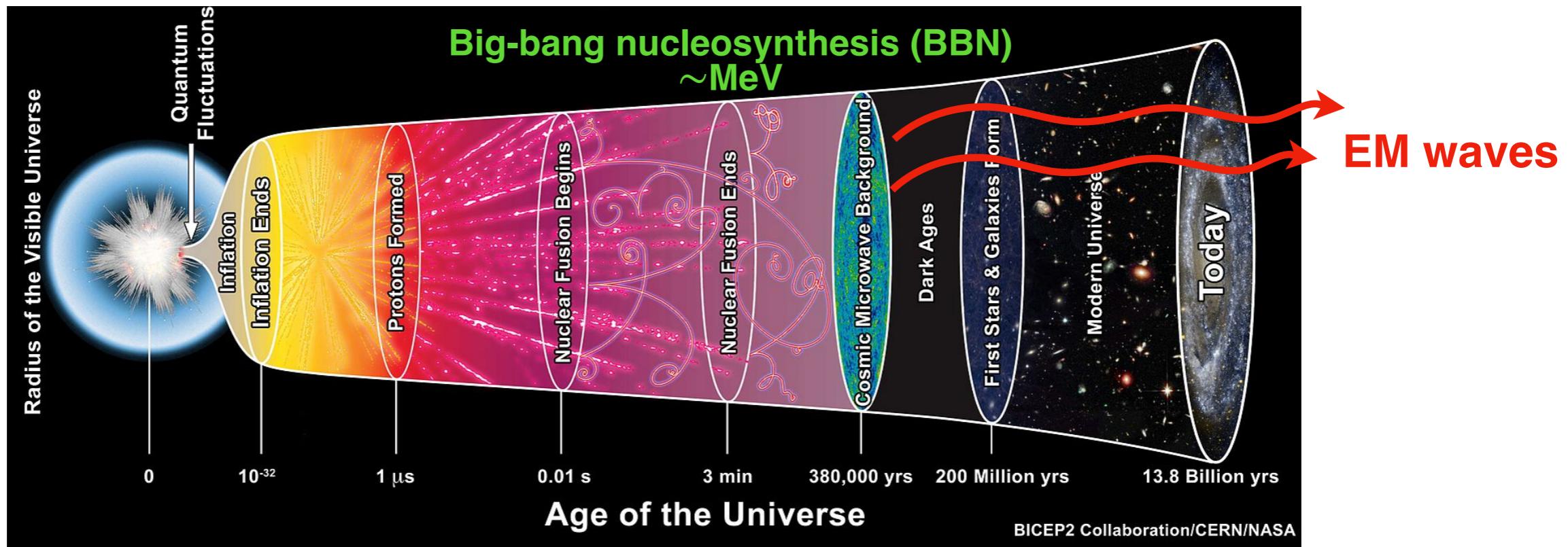
→ well-tested



History of the Universe

high energies ← → low energies

unconstrained ← → well-tested



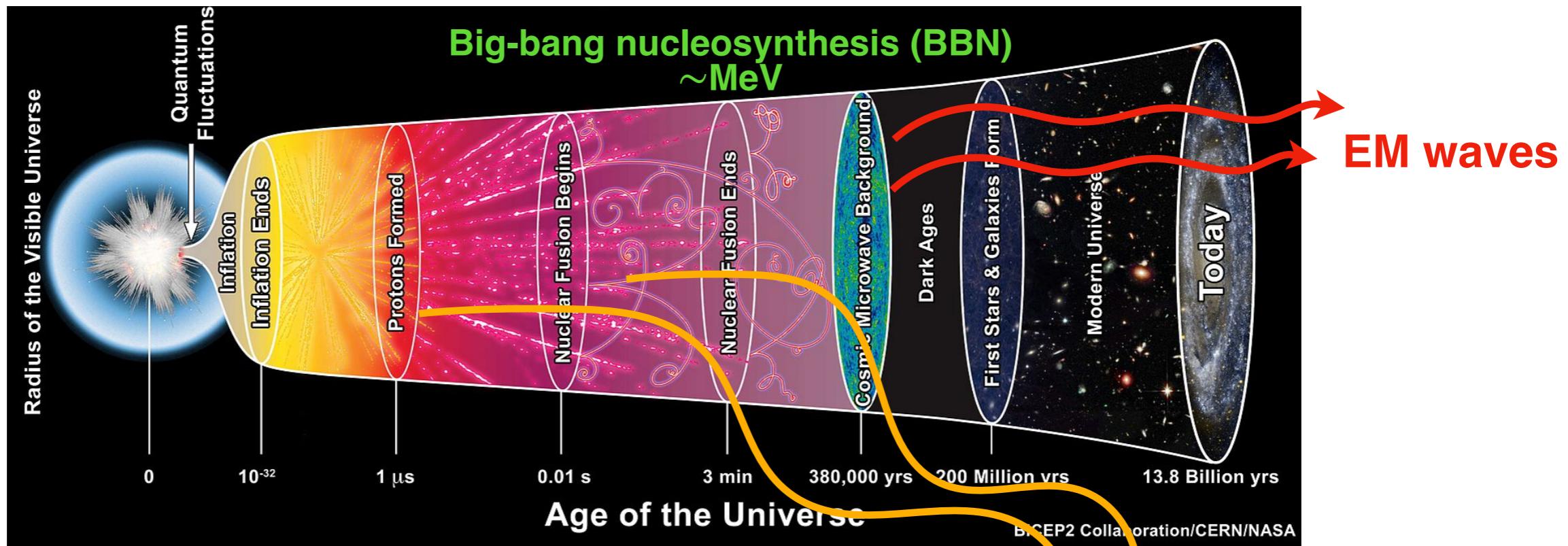
Cosmological dark age

inflation, reheating, phase transitions,
baryogenesis, dark matter,...

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Cosmological dark age

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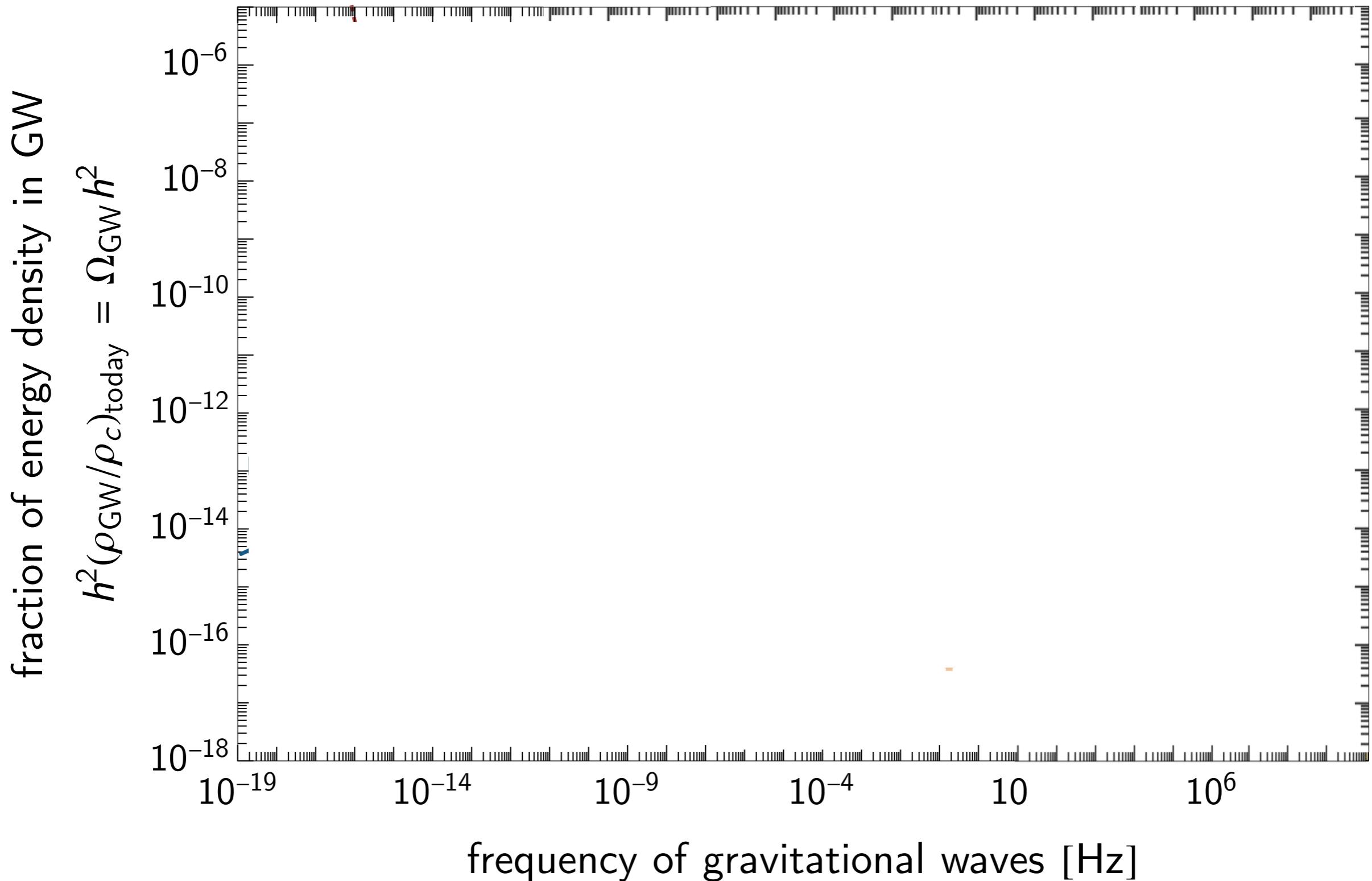
Primordial GW

(propagates freely after production)

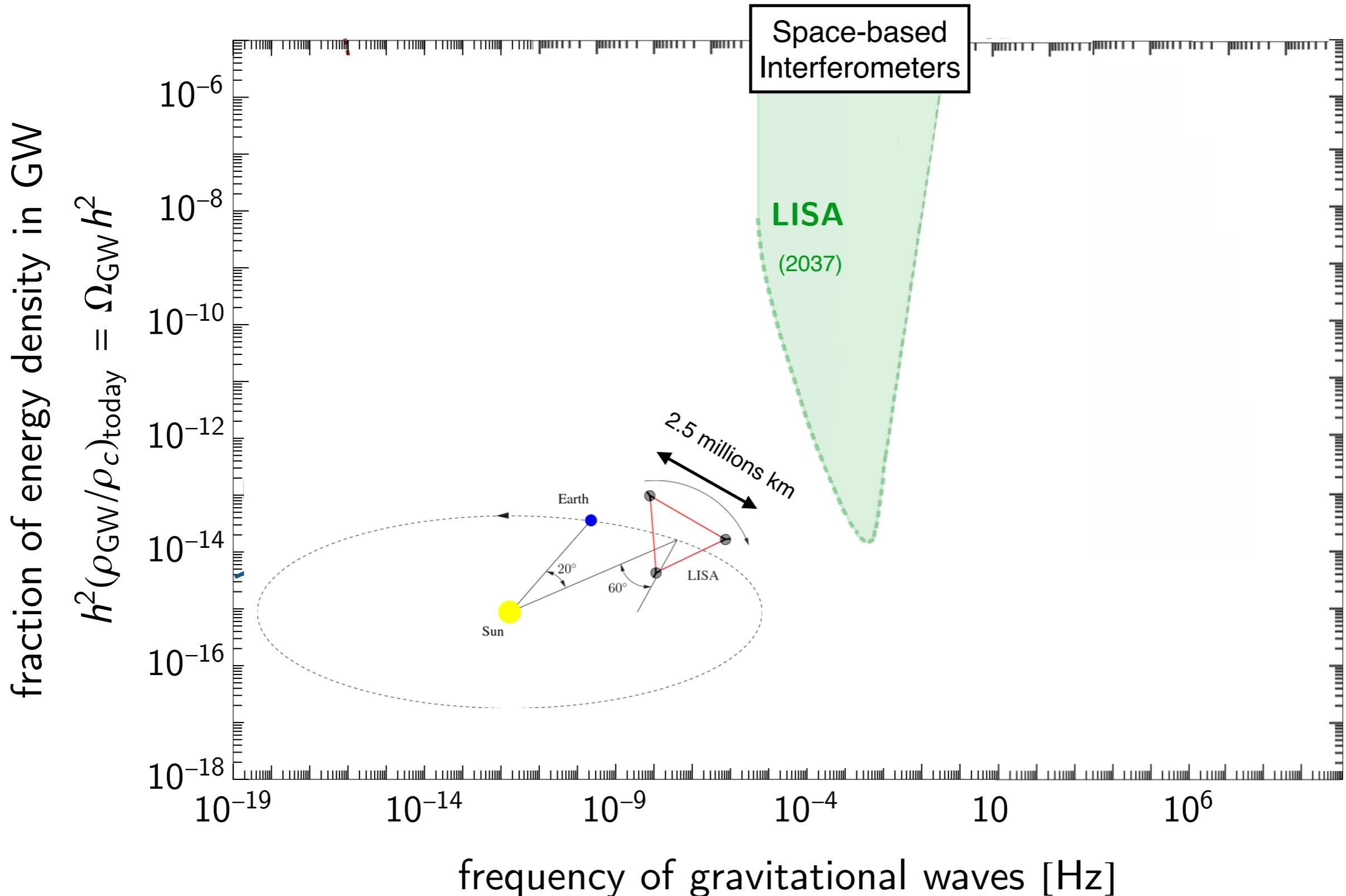
$$\frac{\Gamma_{\text{GW}}(T)}{H(T)} \sim \frac{G^2 T^5}{T^2 / M_{\text{pl}}} = \left(\frac{T}{M_{\text{pl}}}\right)^3$$

GW as probes of pre-BBN Universe ($T \gtrsim \text{MeV}$).

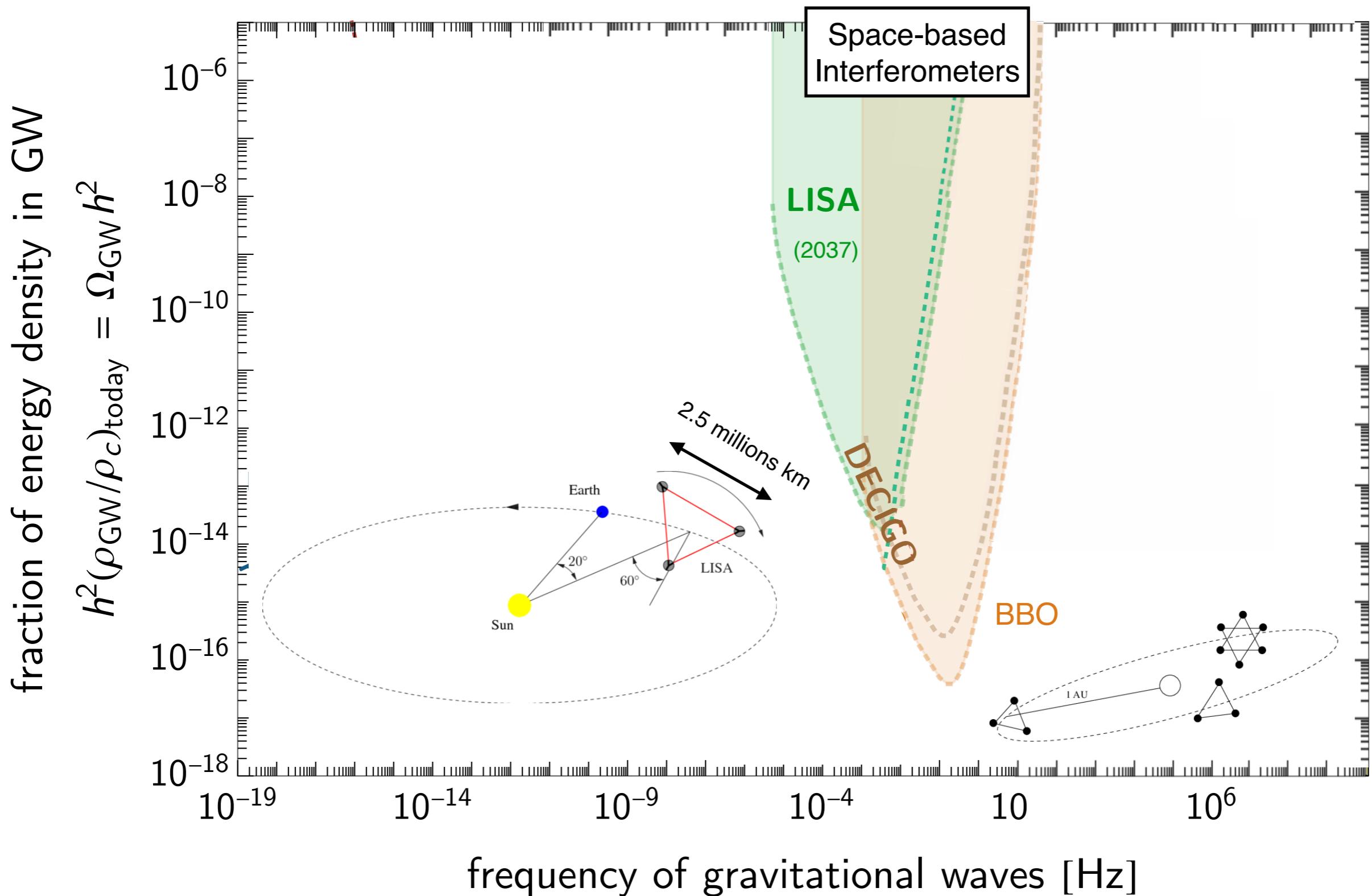
Future prospects of **GW** experiments



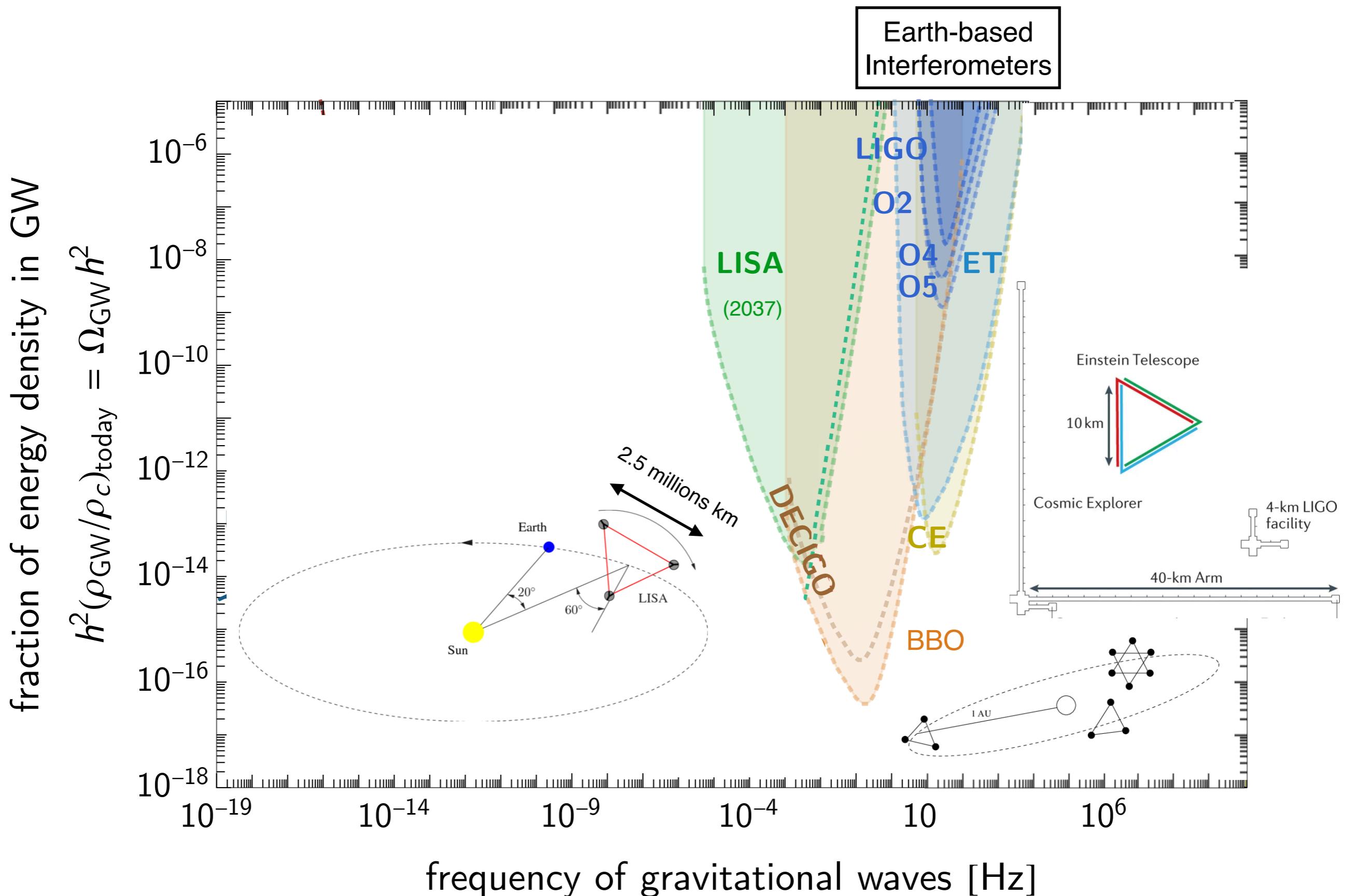
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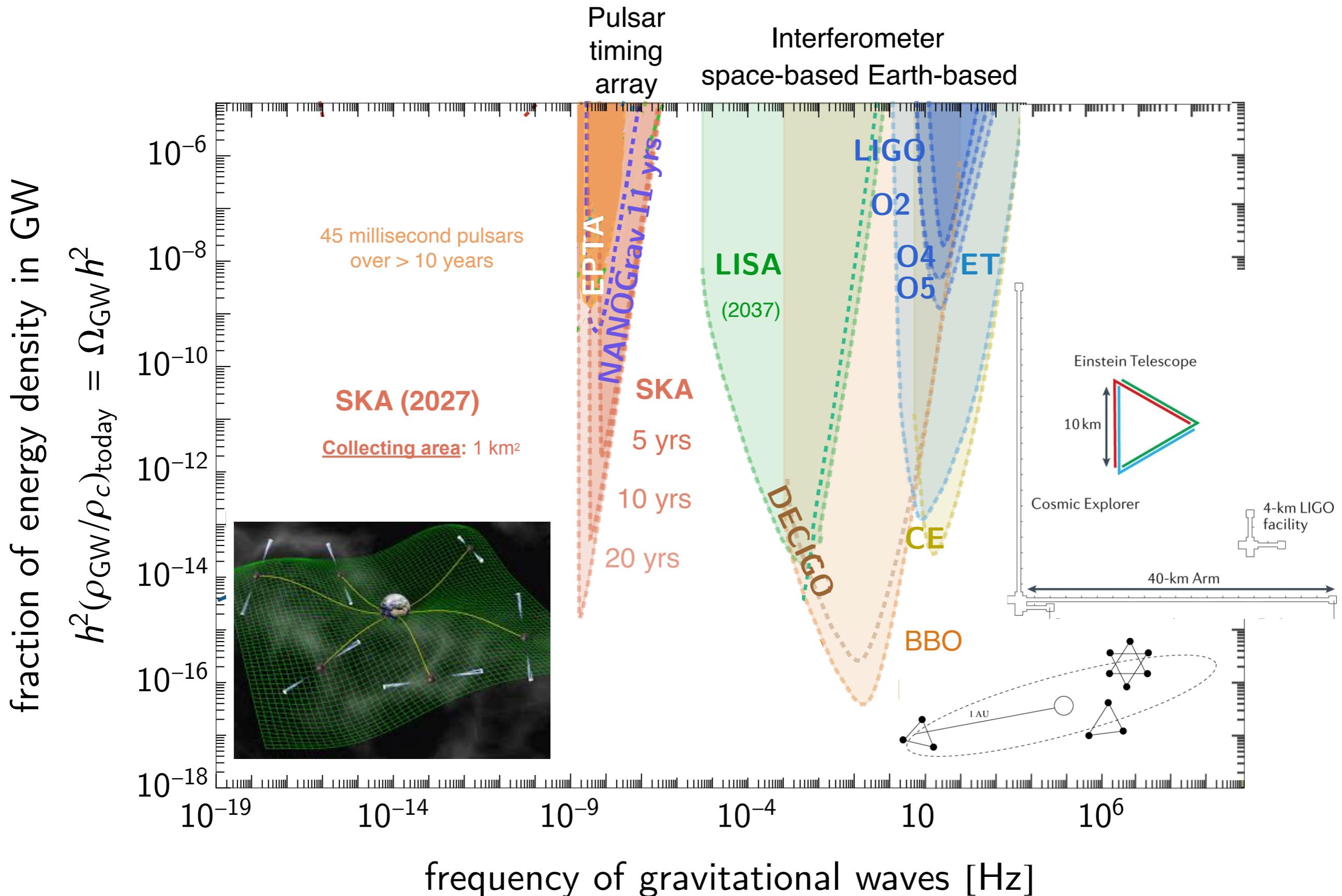
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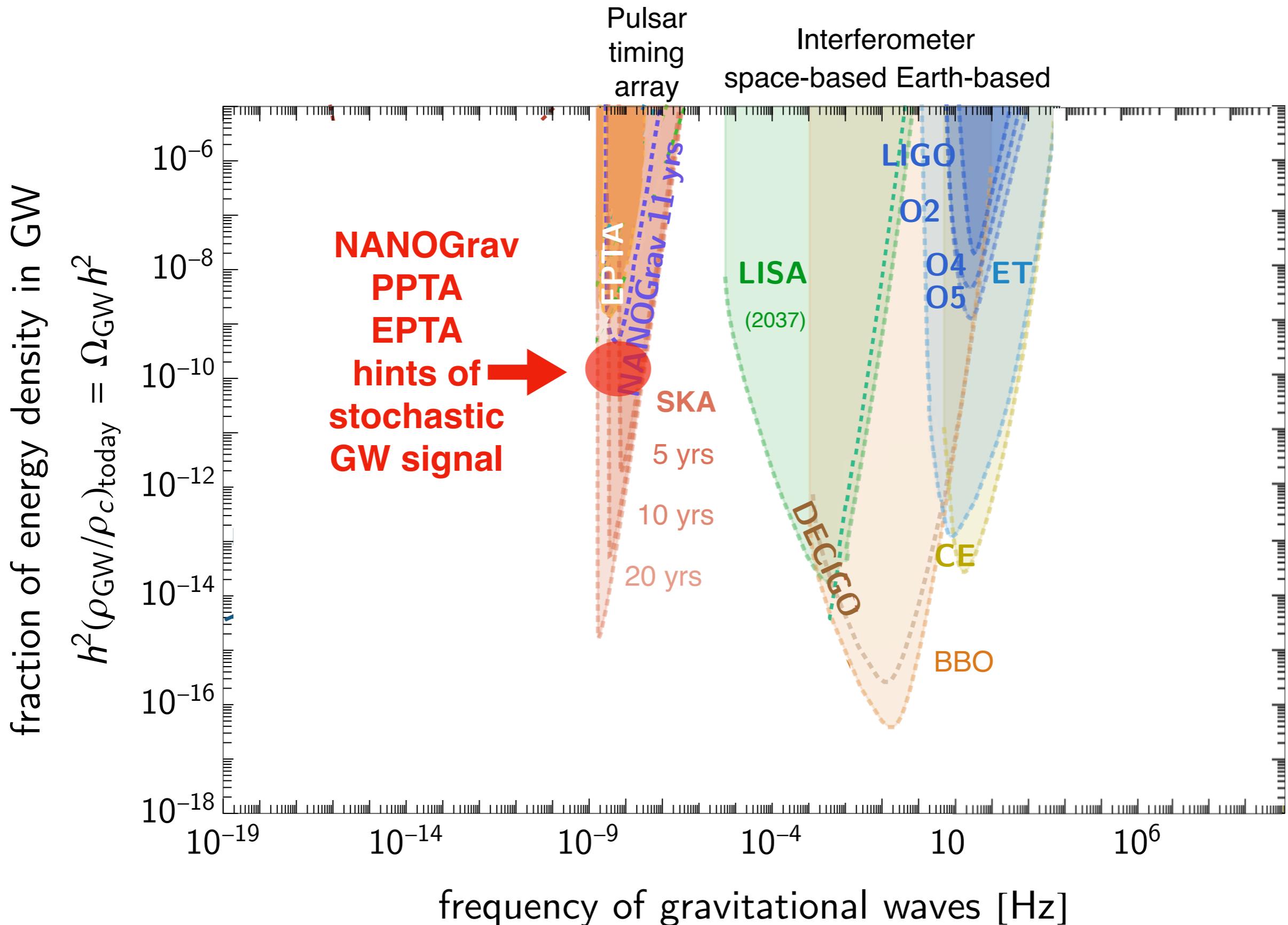
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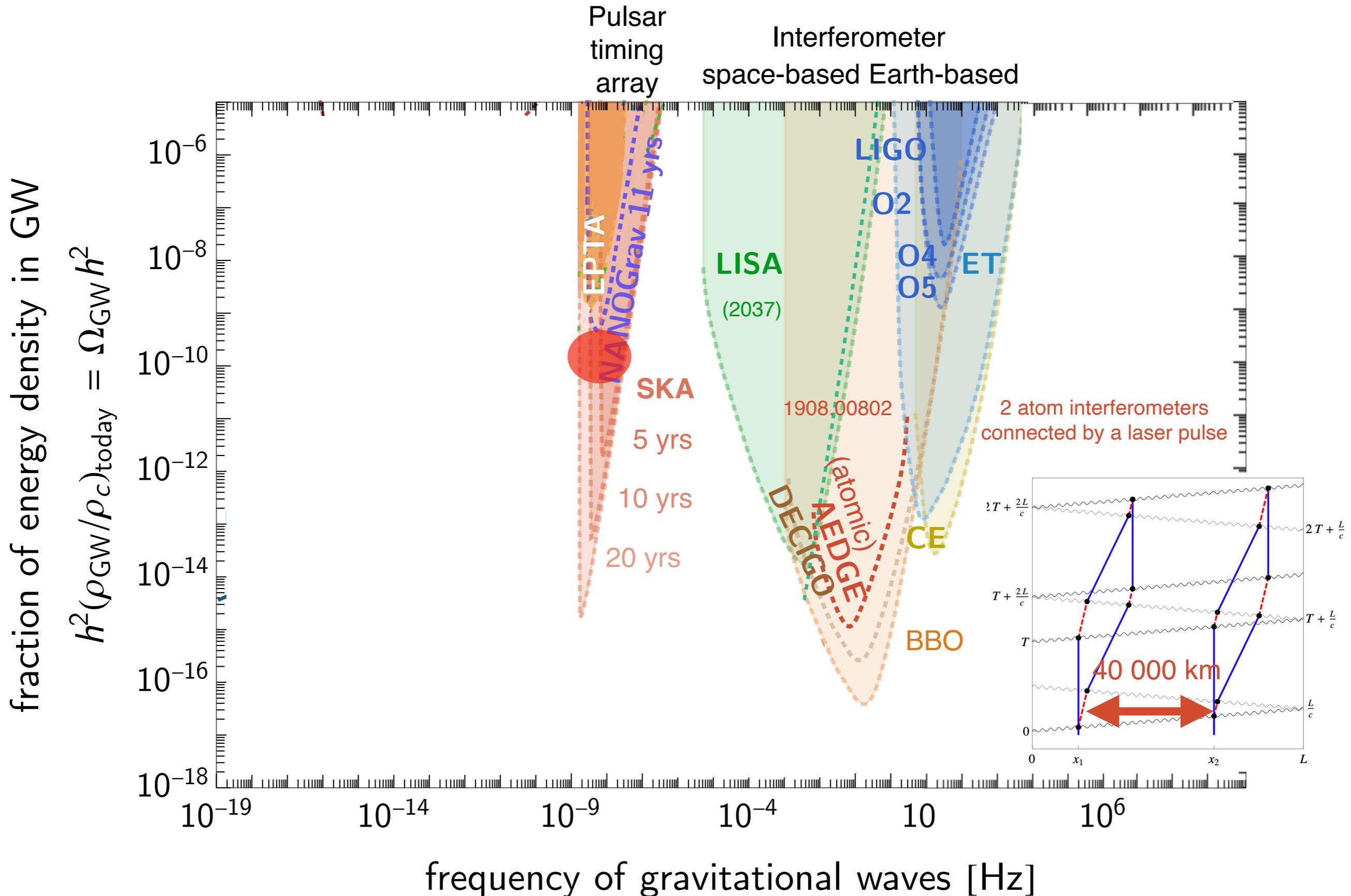
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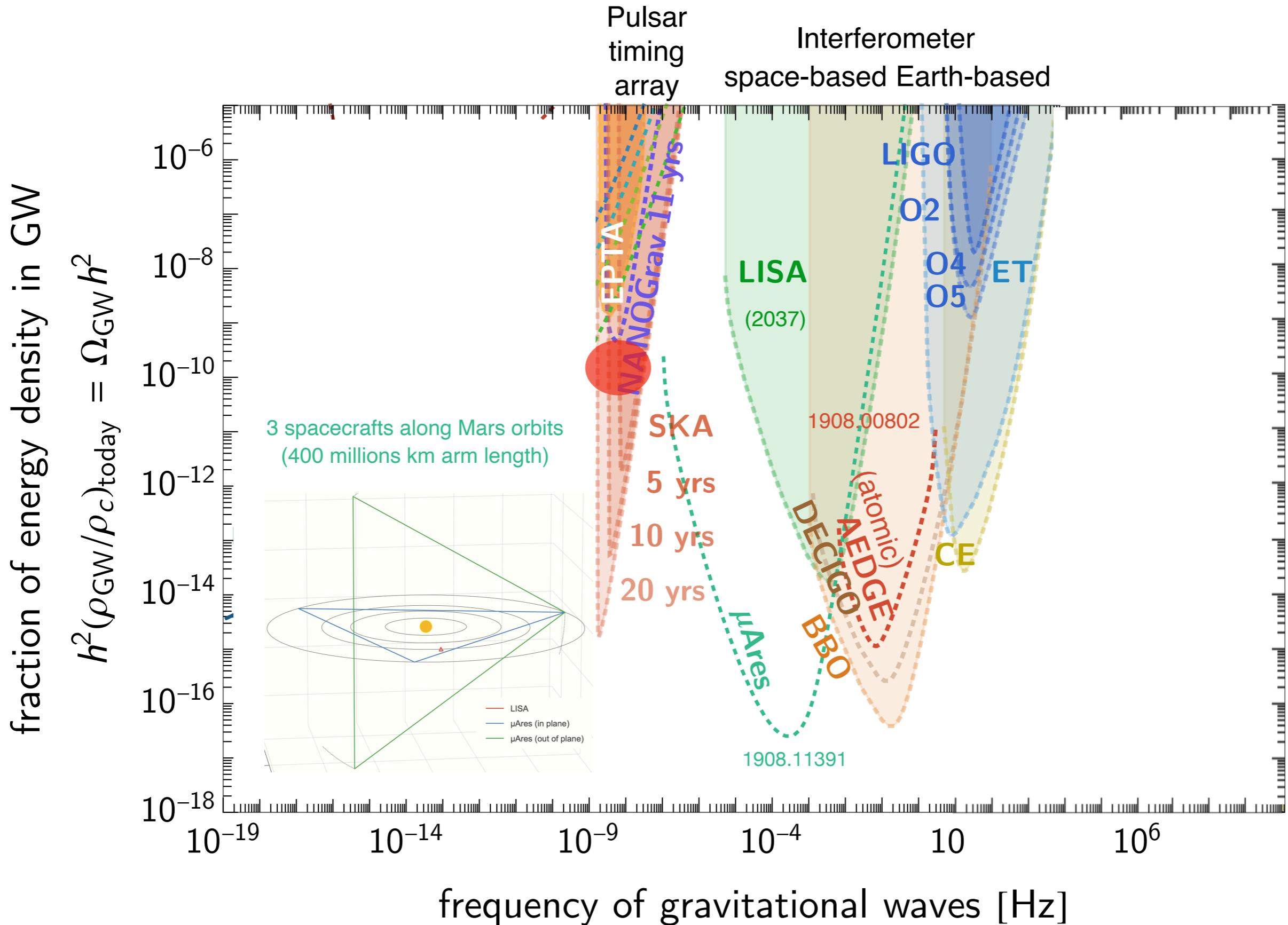
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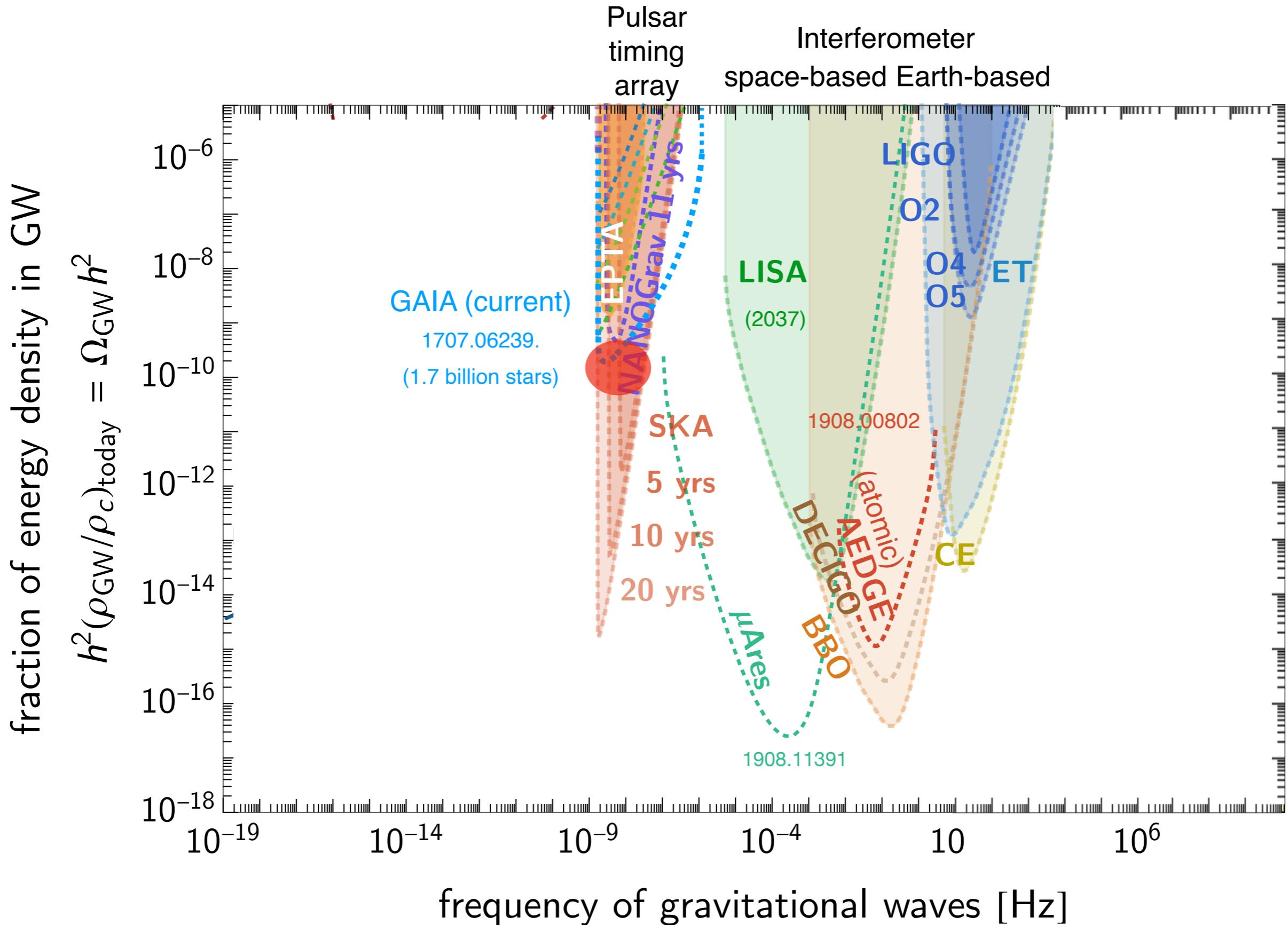
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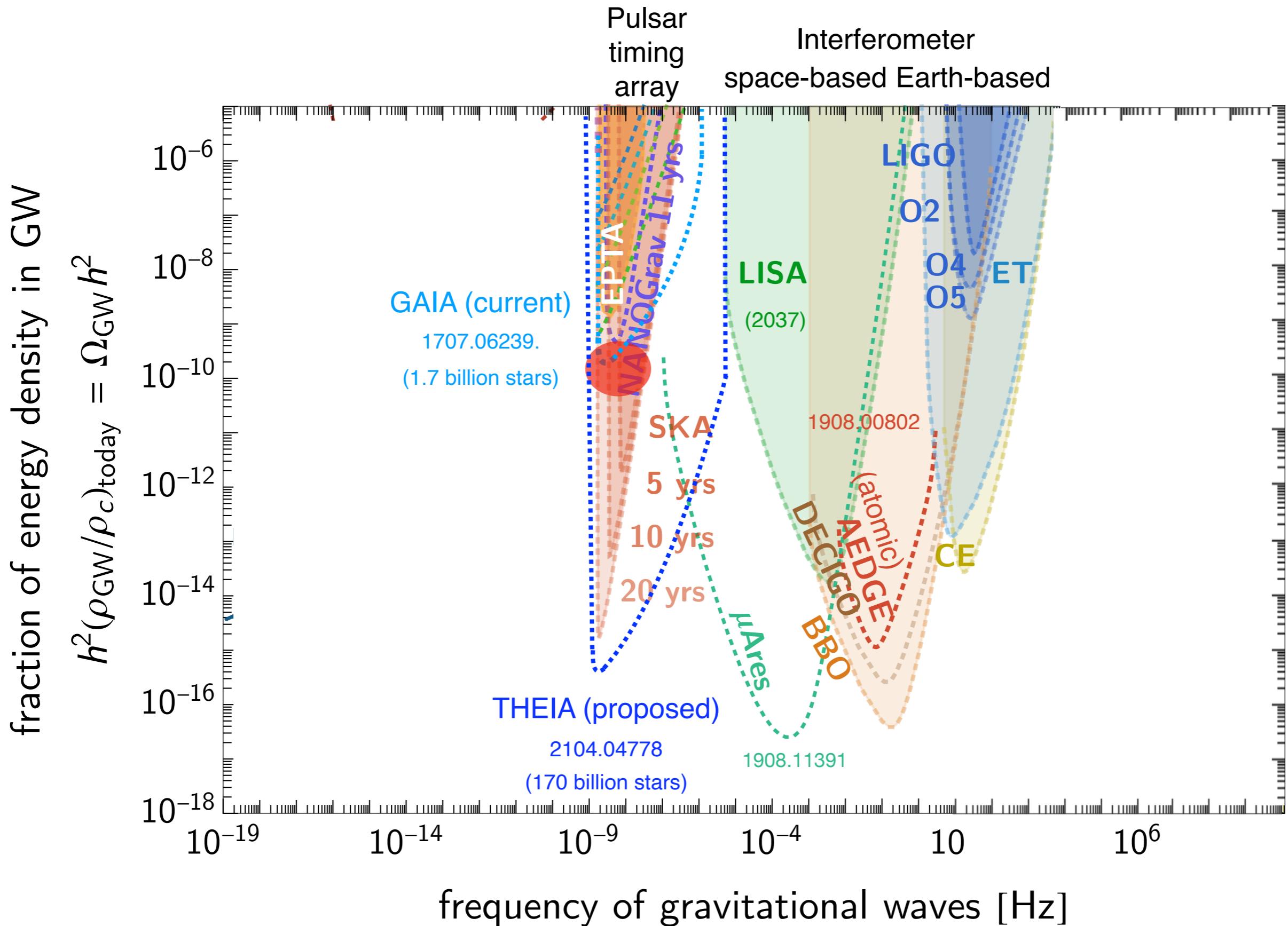
Future prospects of GW experiments



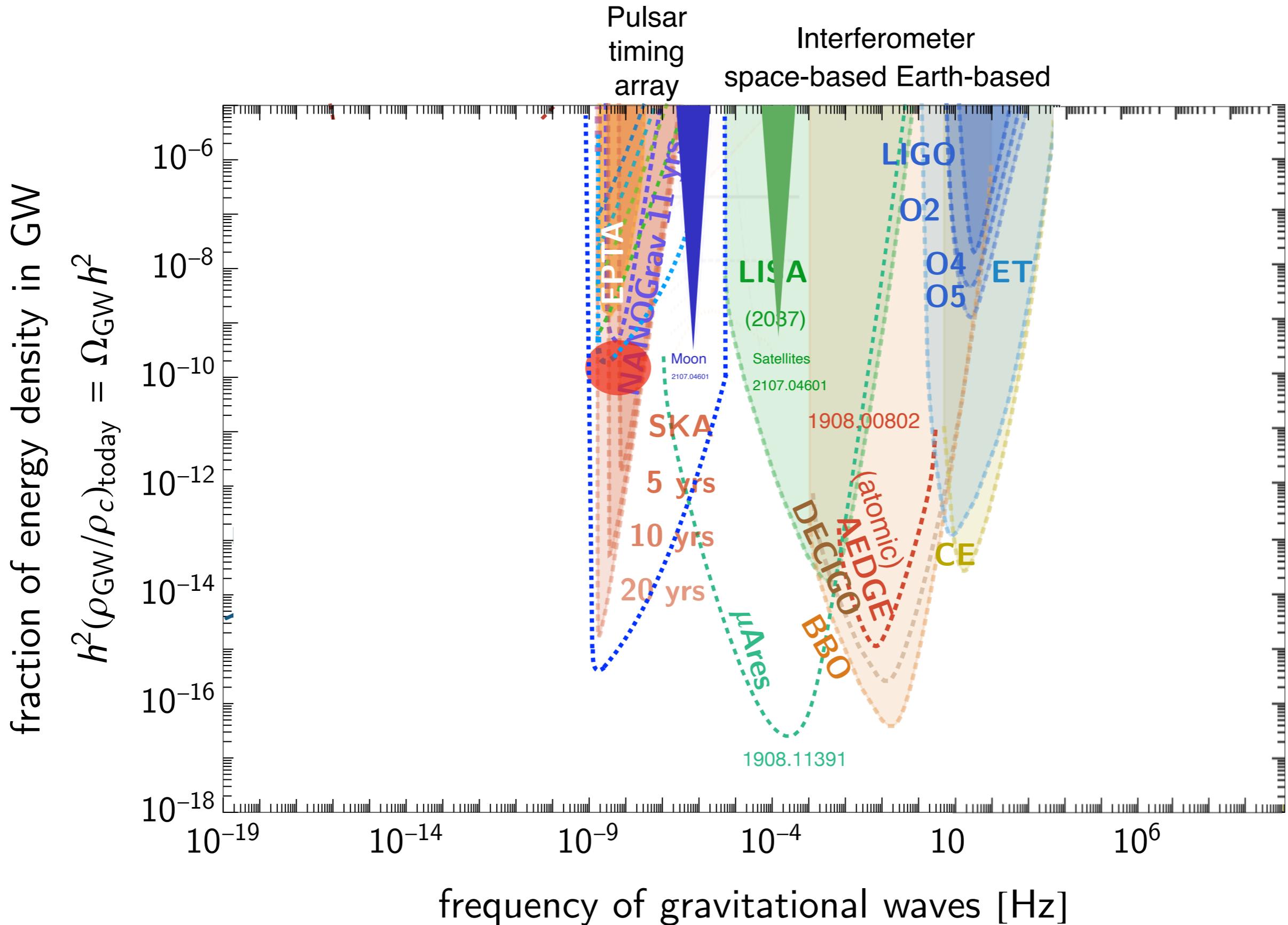
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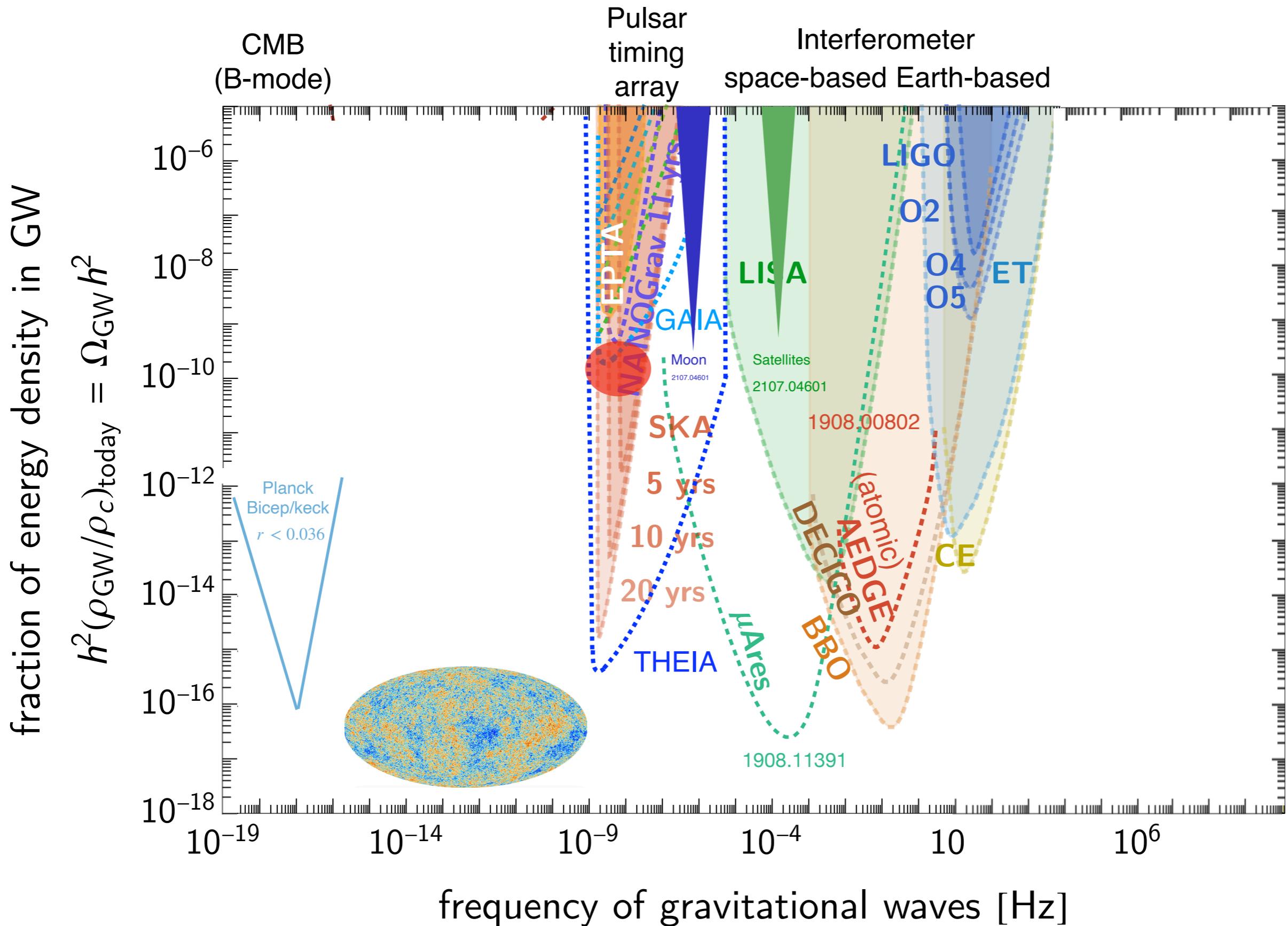
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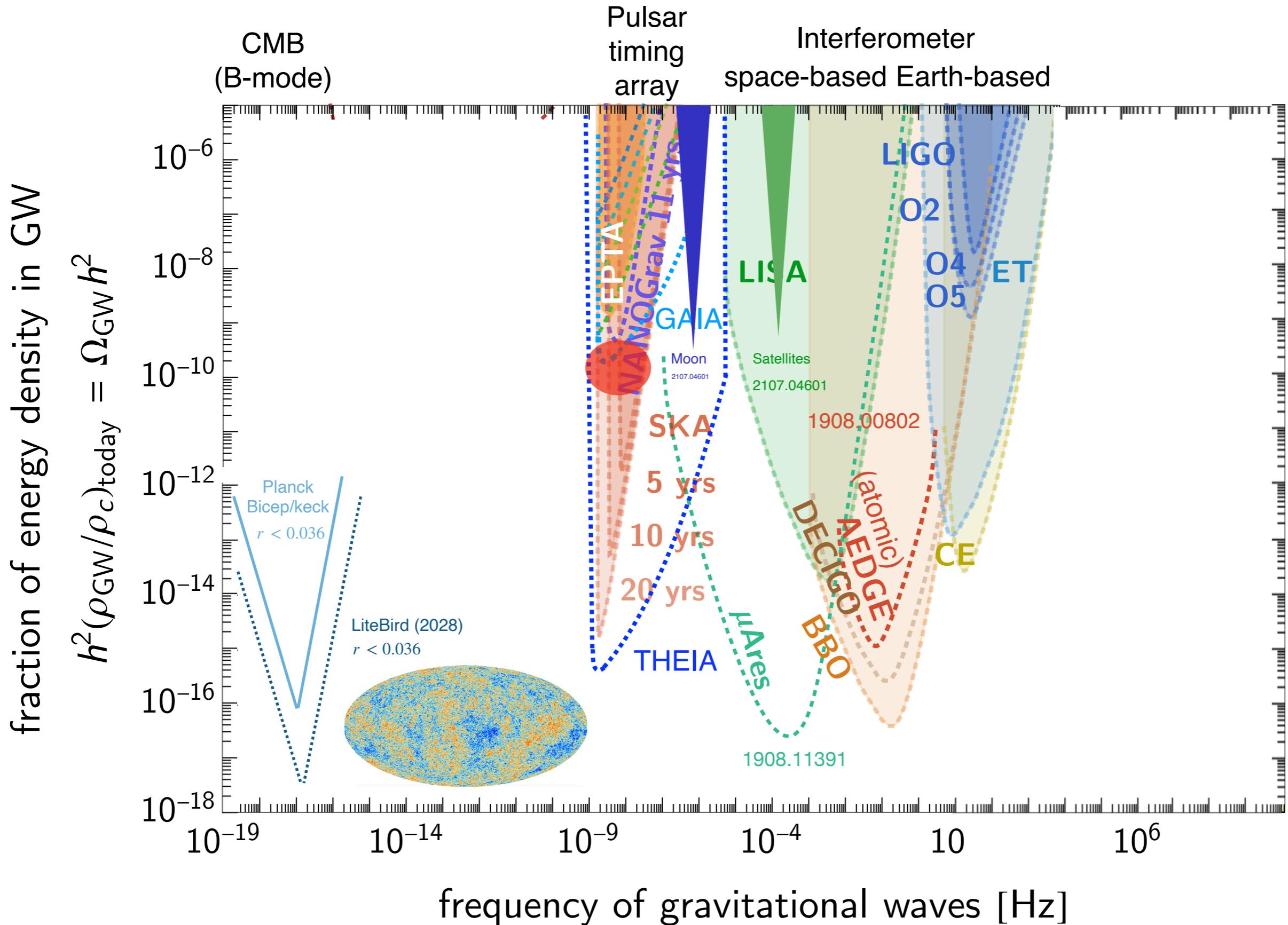
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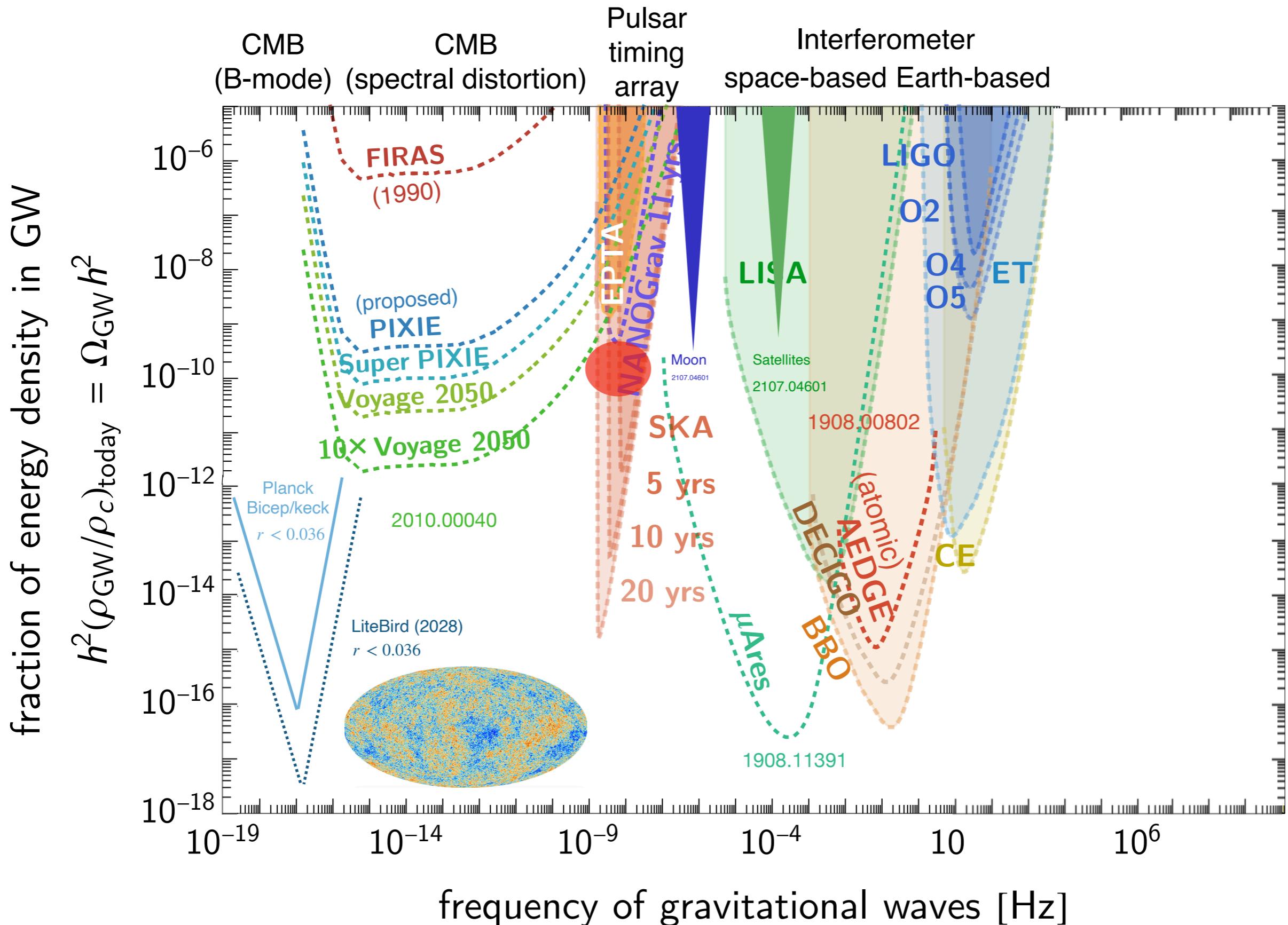
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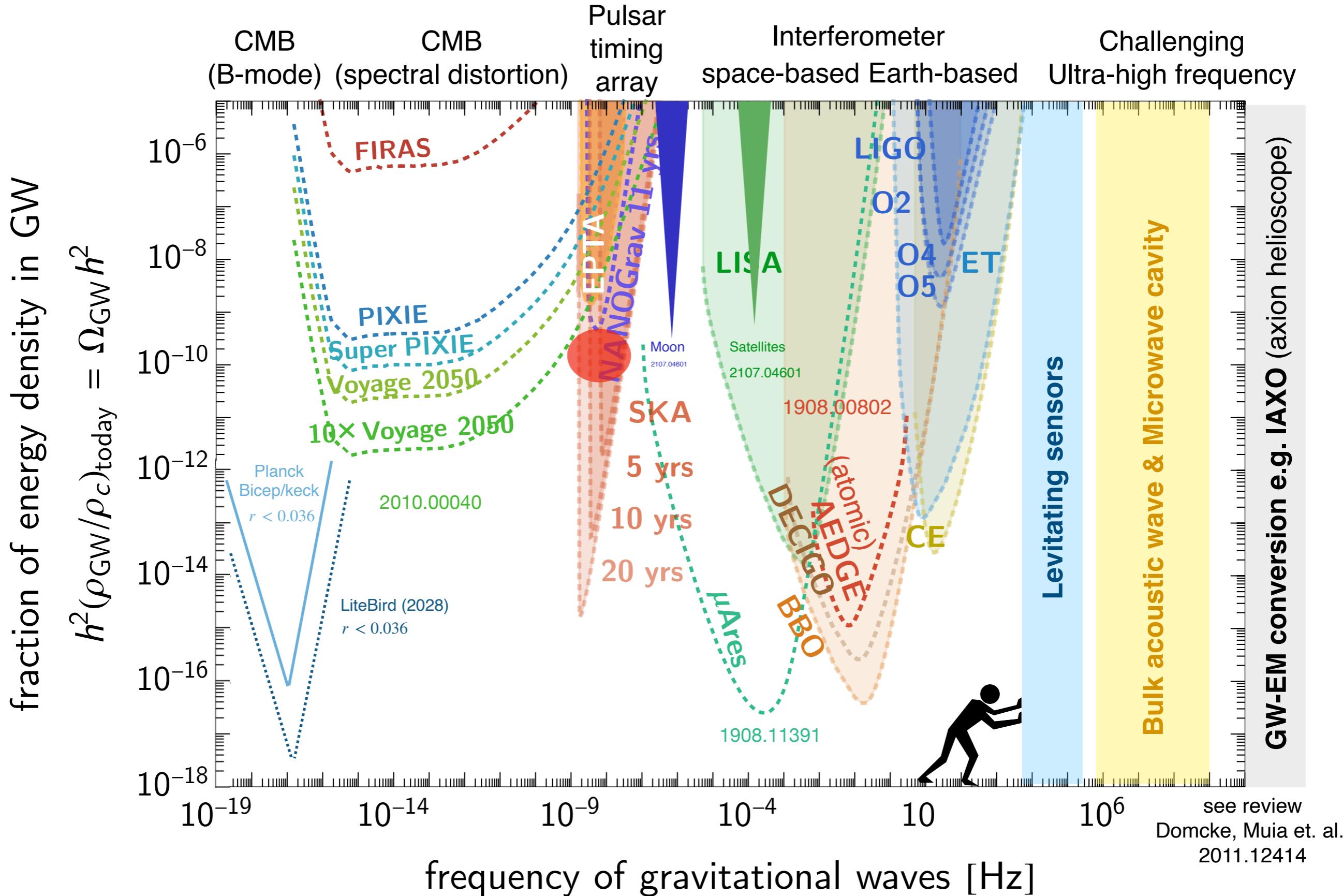
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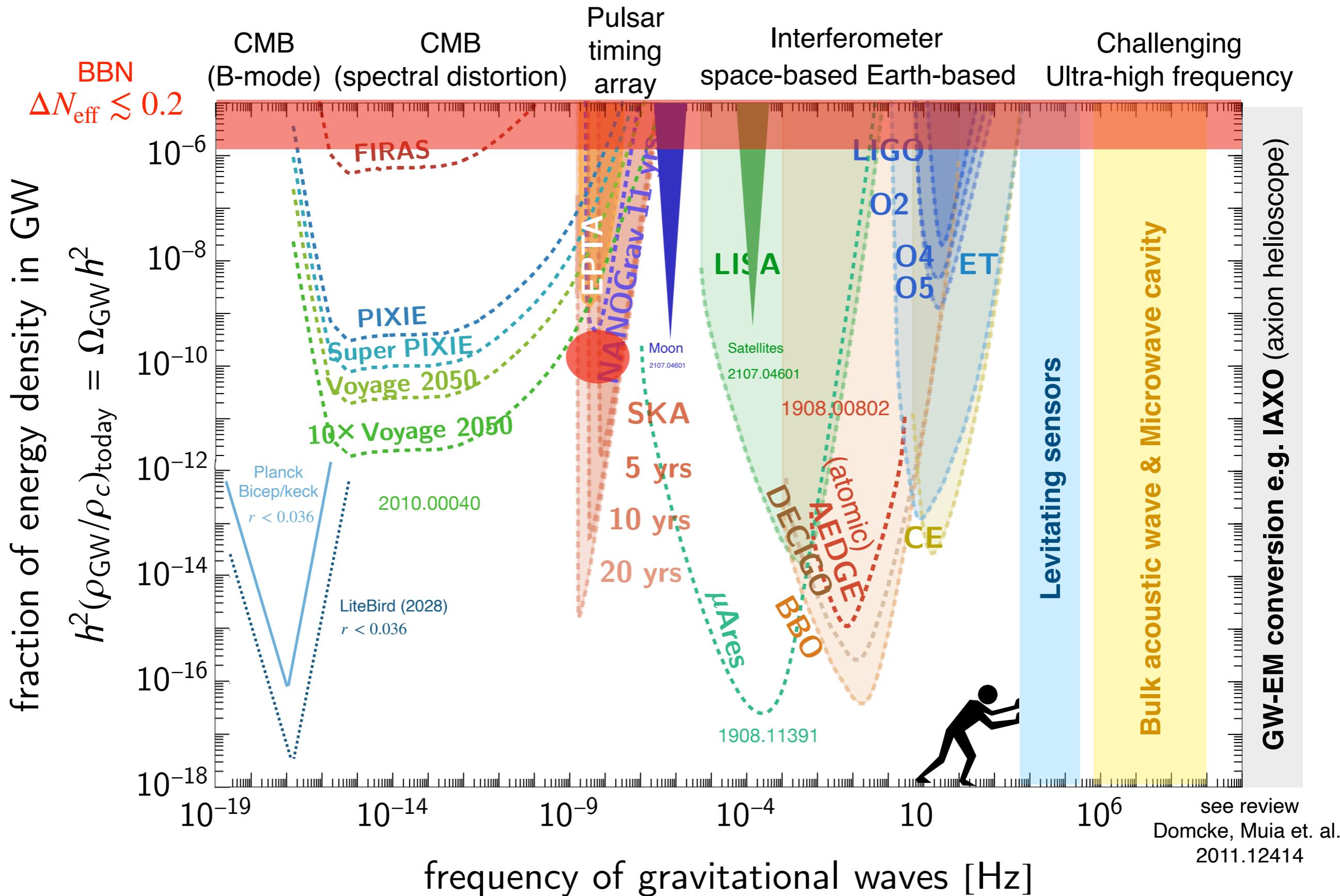
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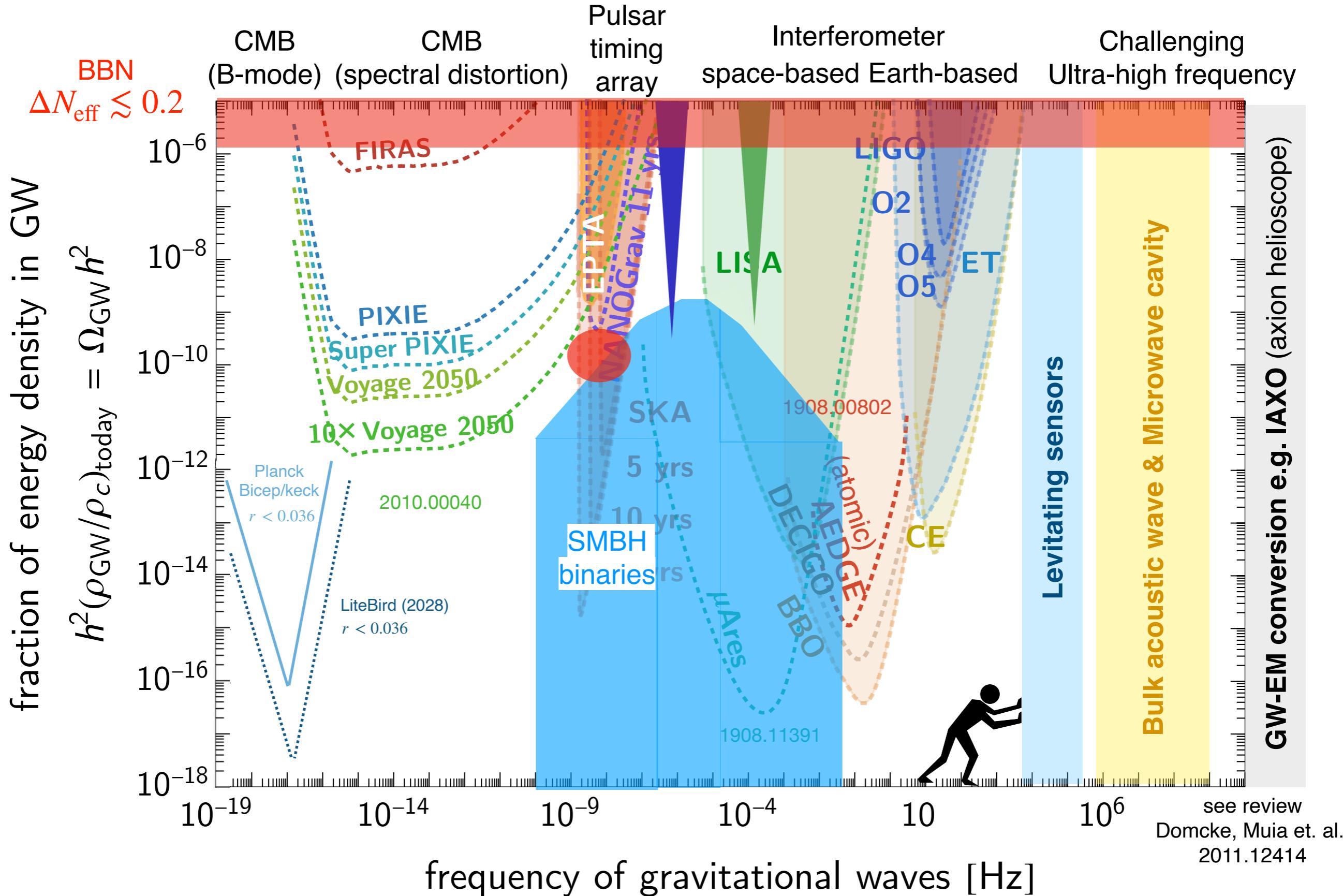
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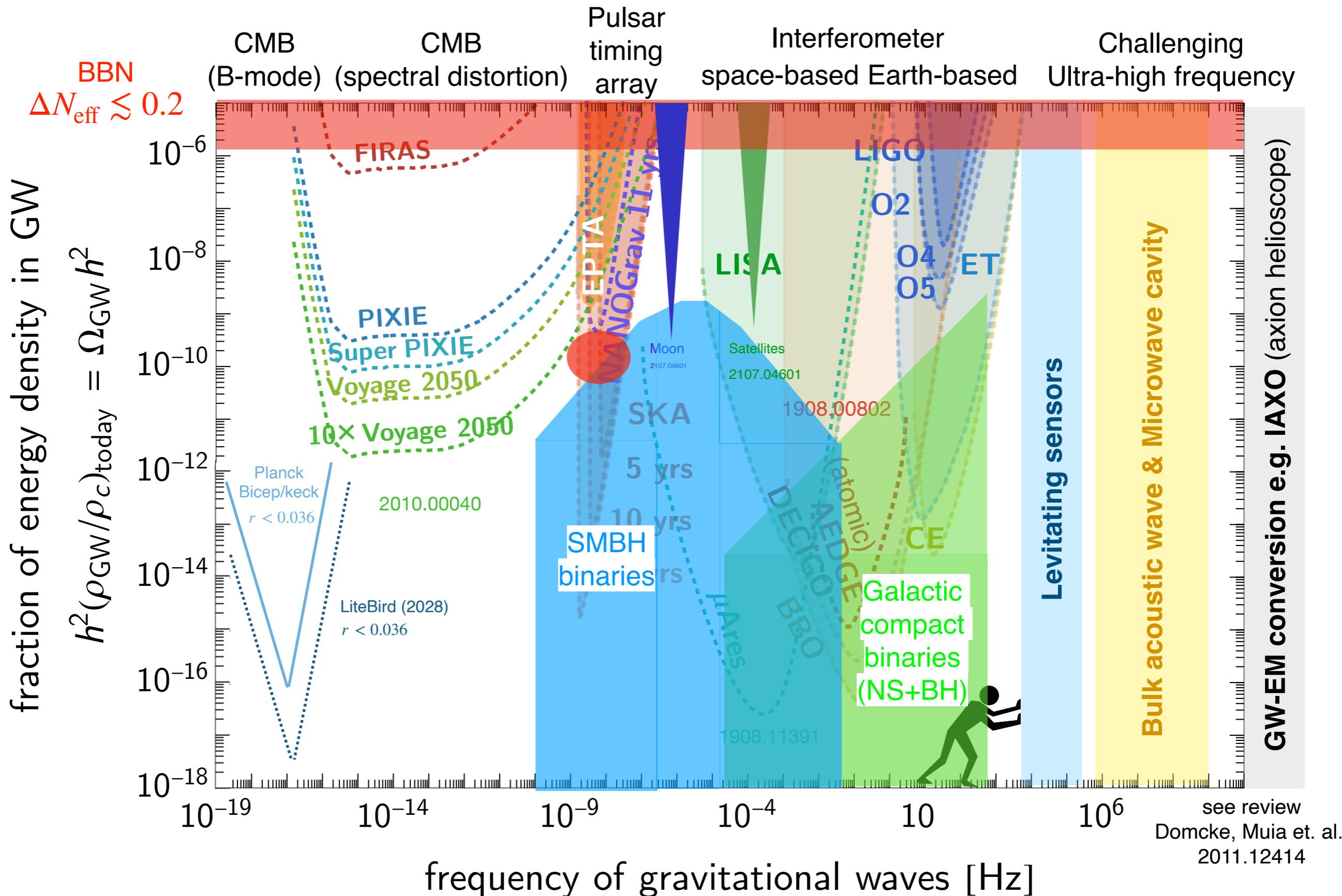
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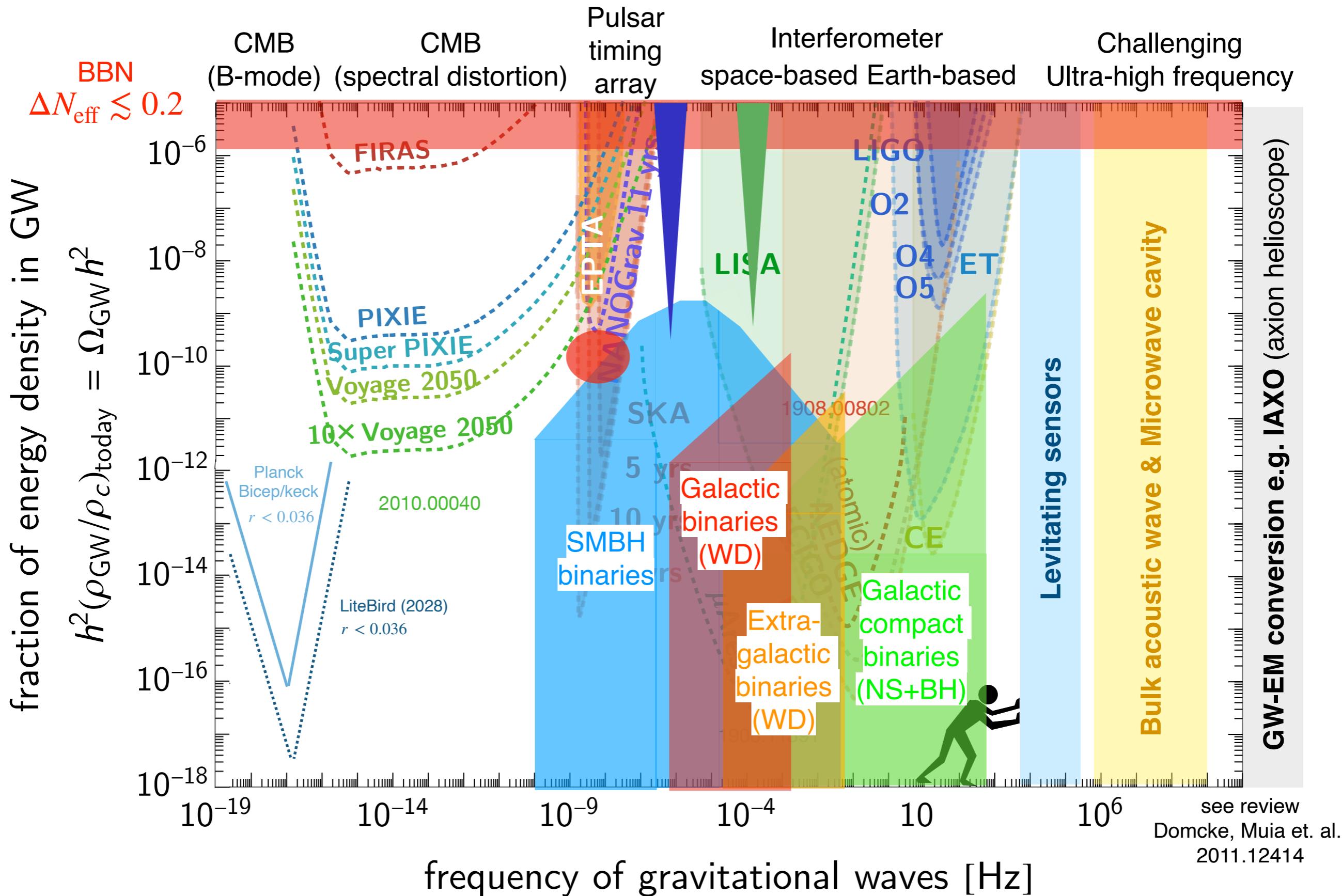
Astrophysical foreground



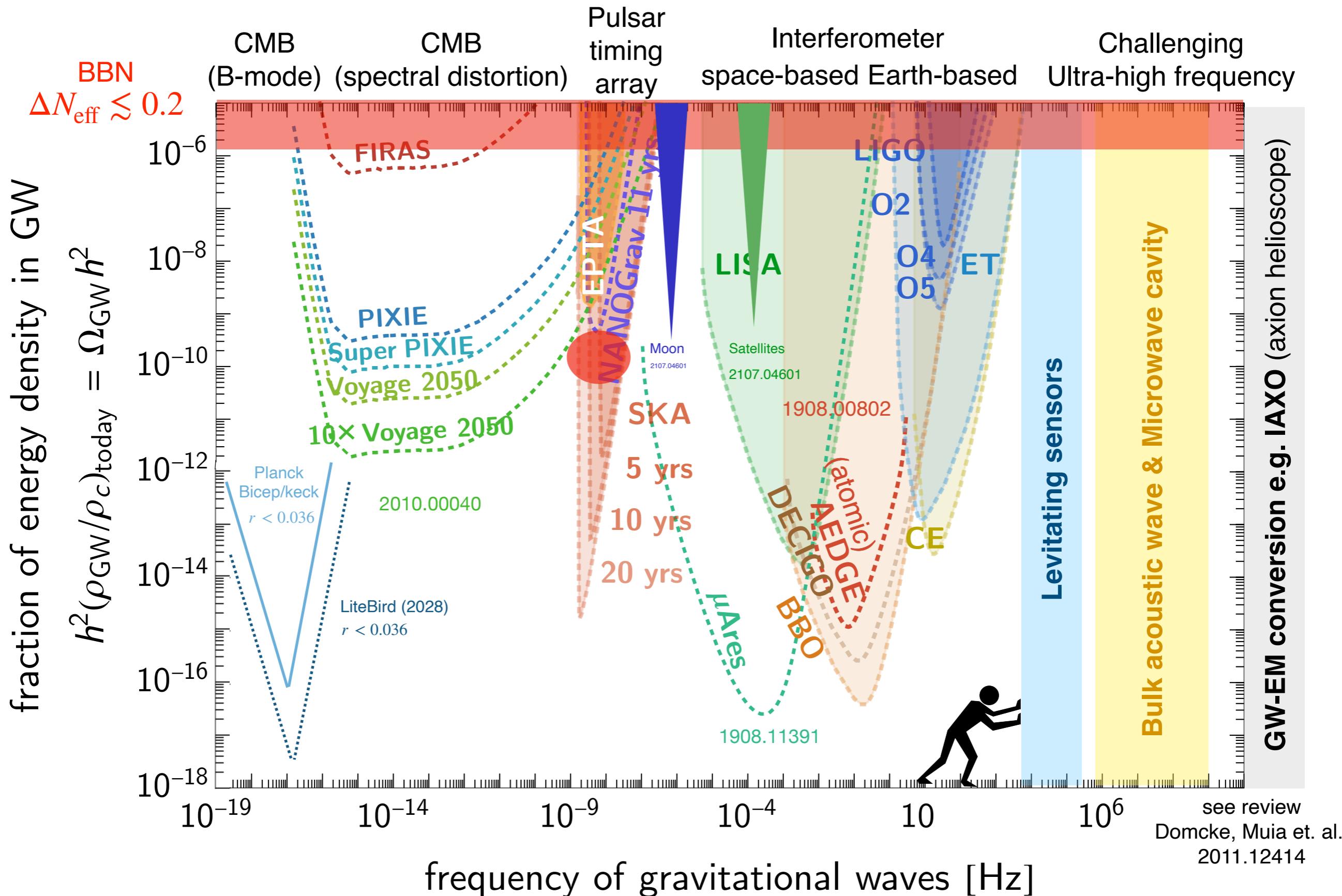
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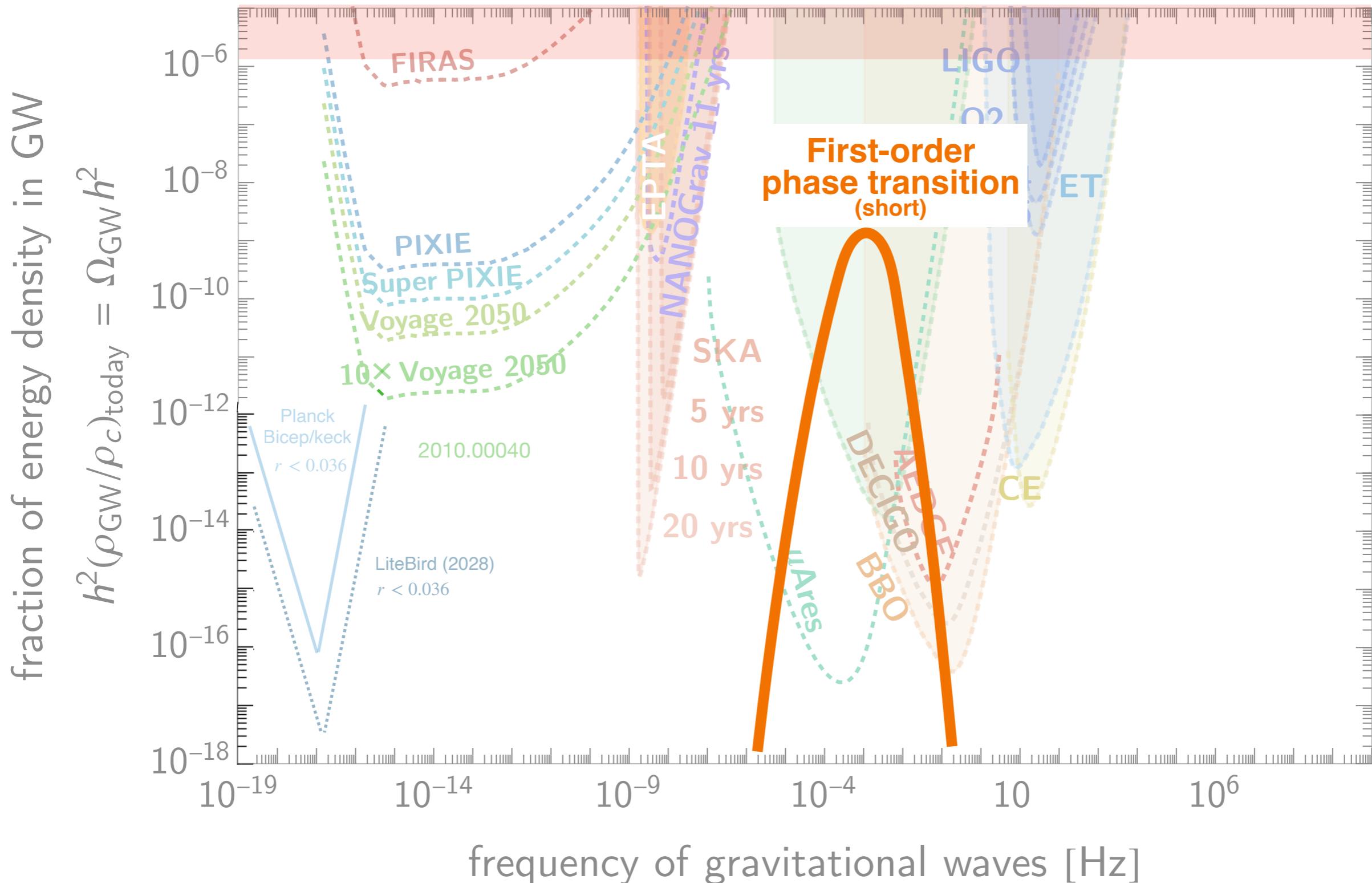
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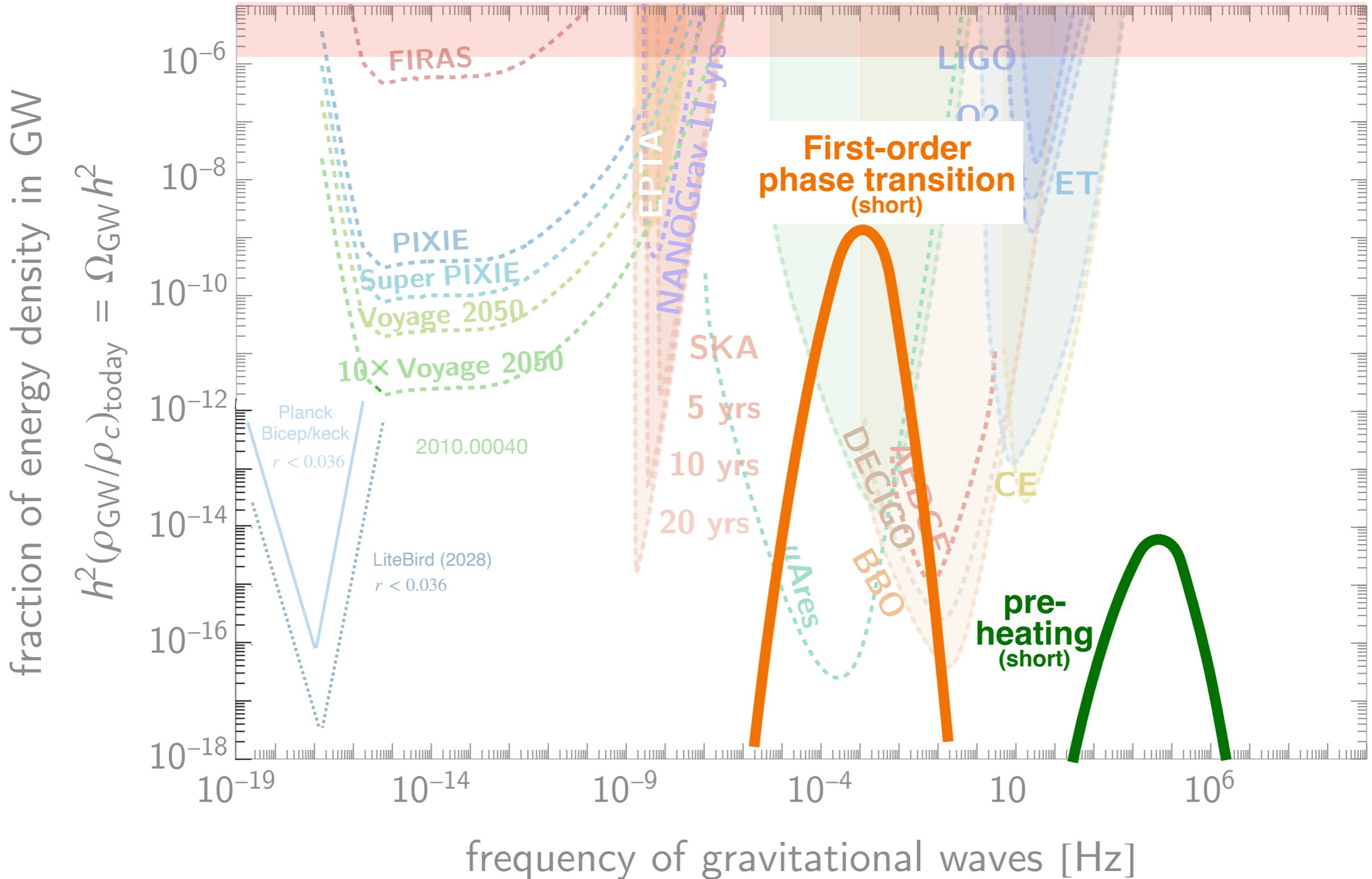
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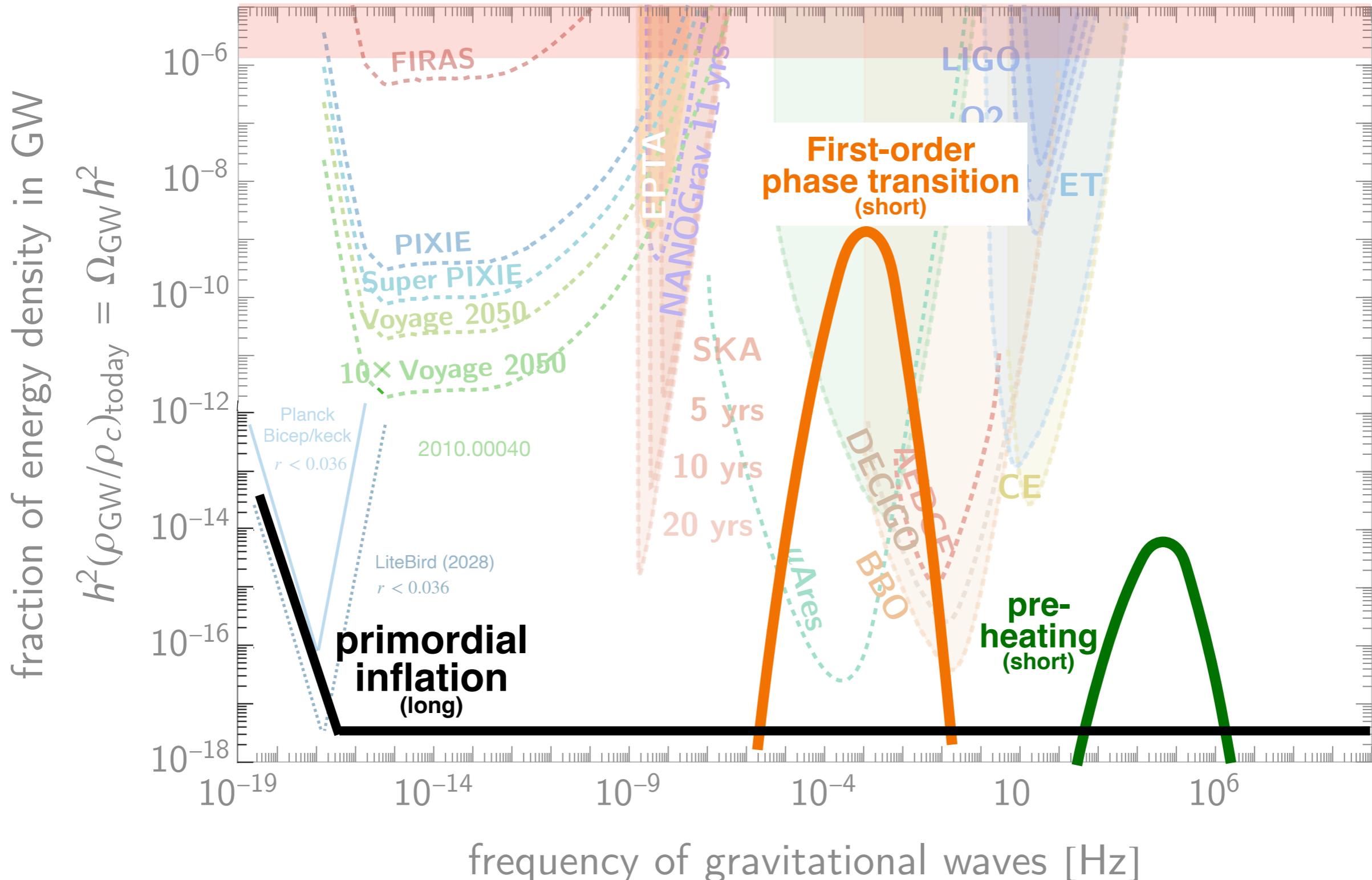
GW of primordial origins



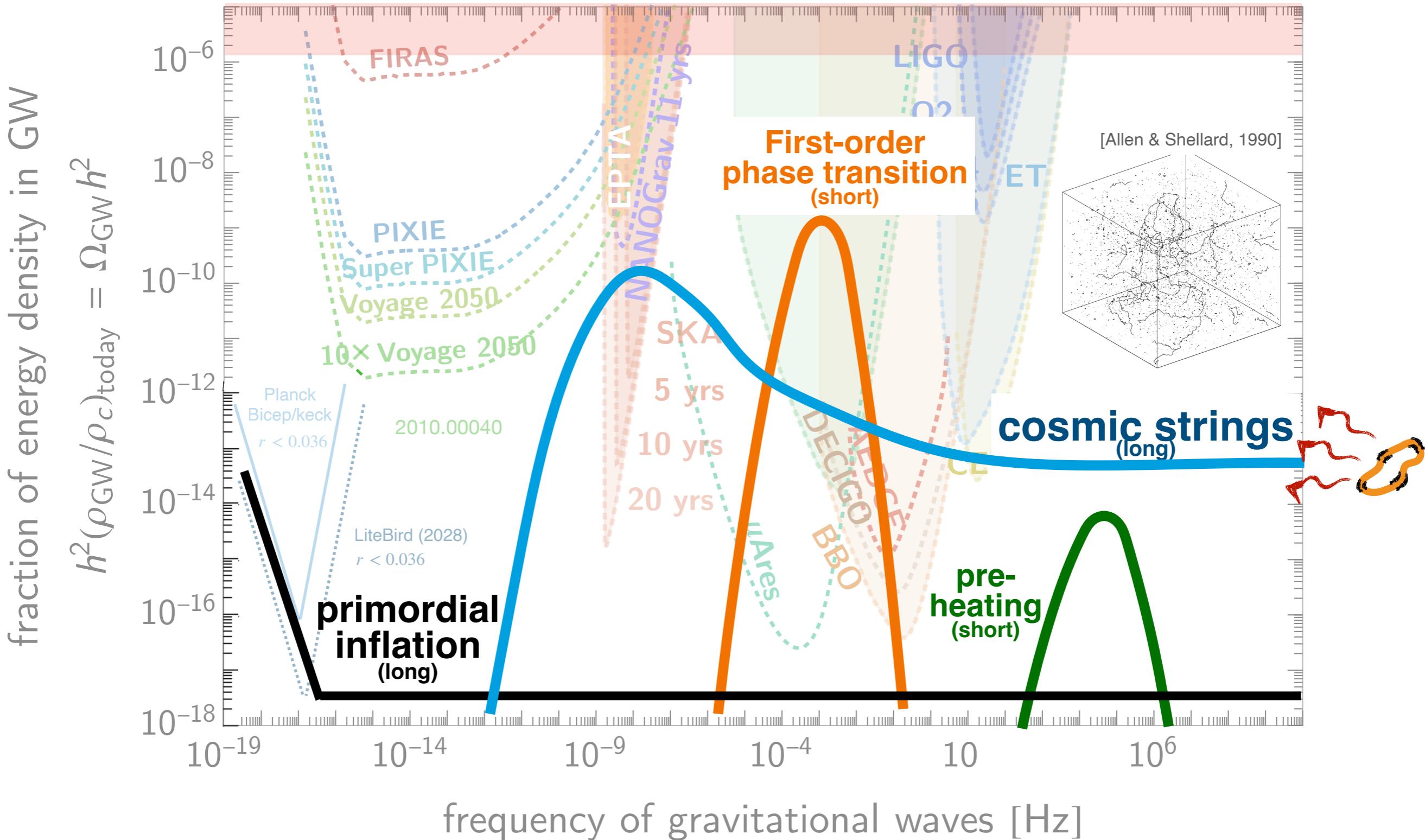
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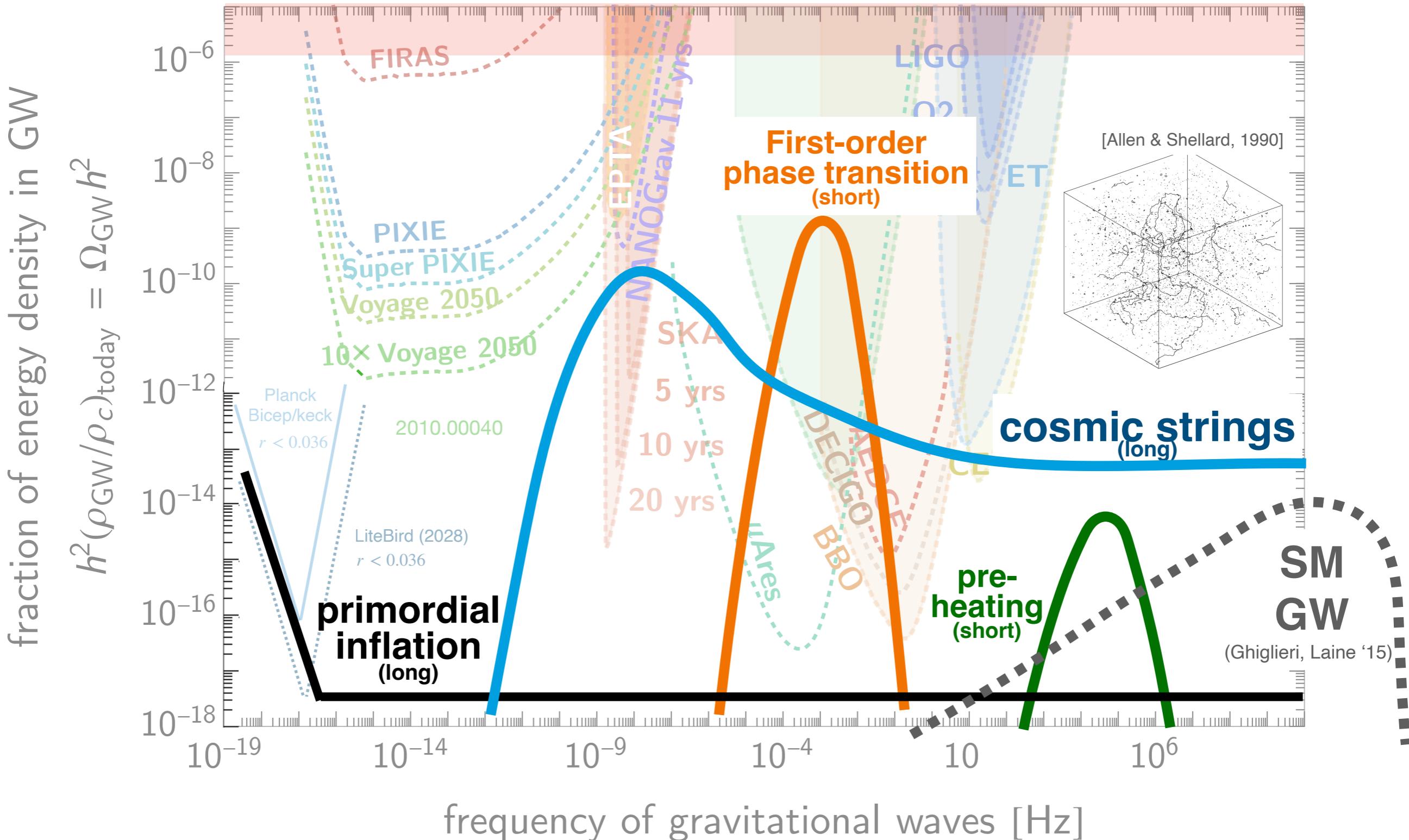
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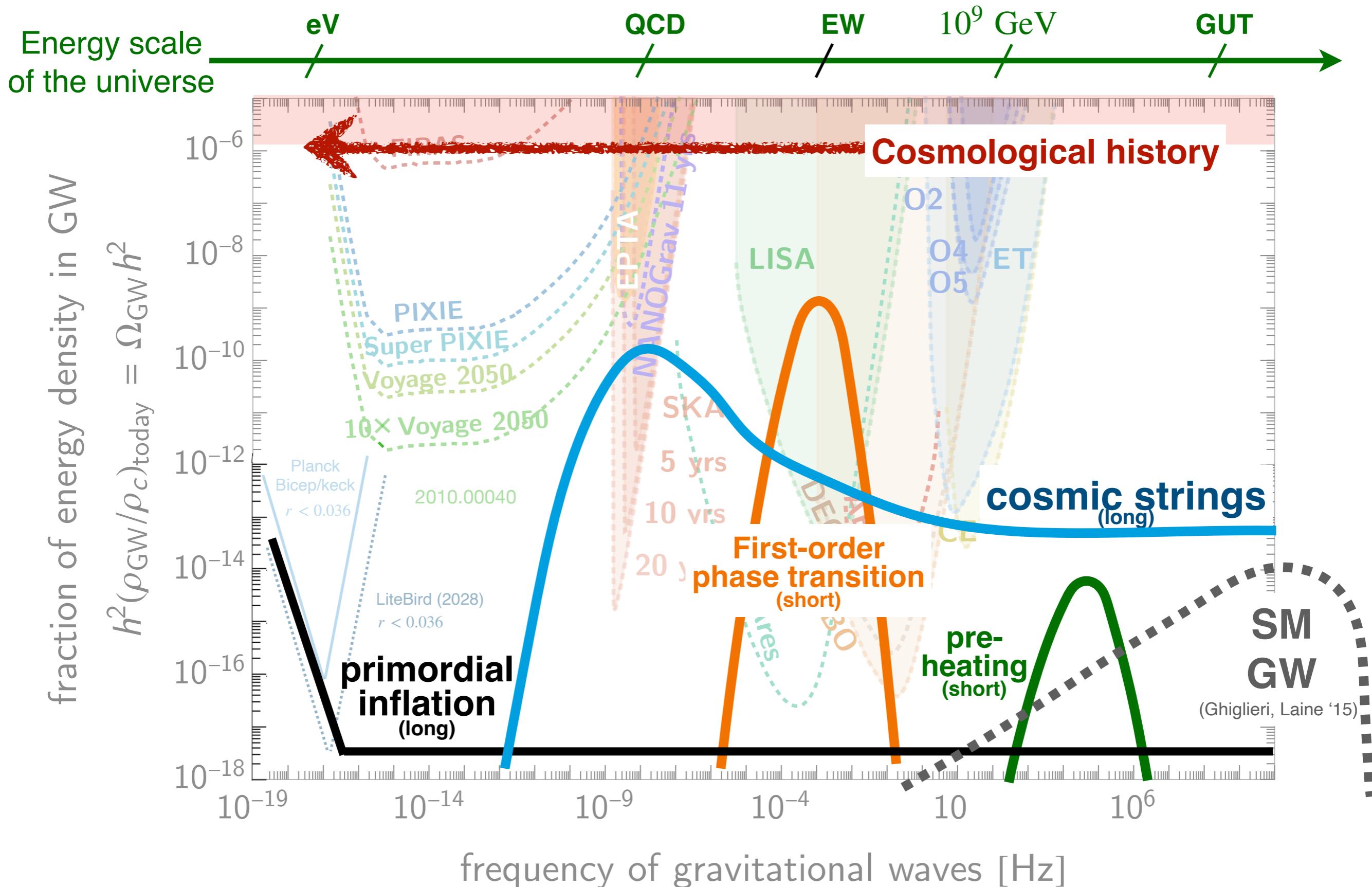
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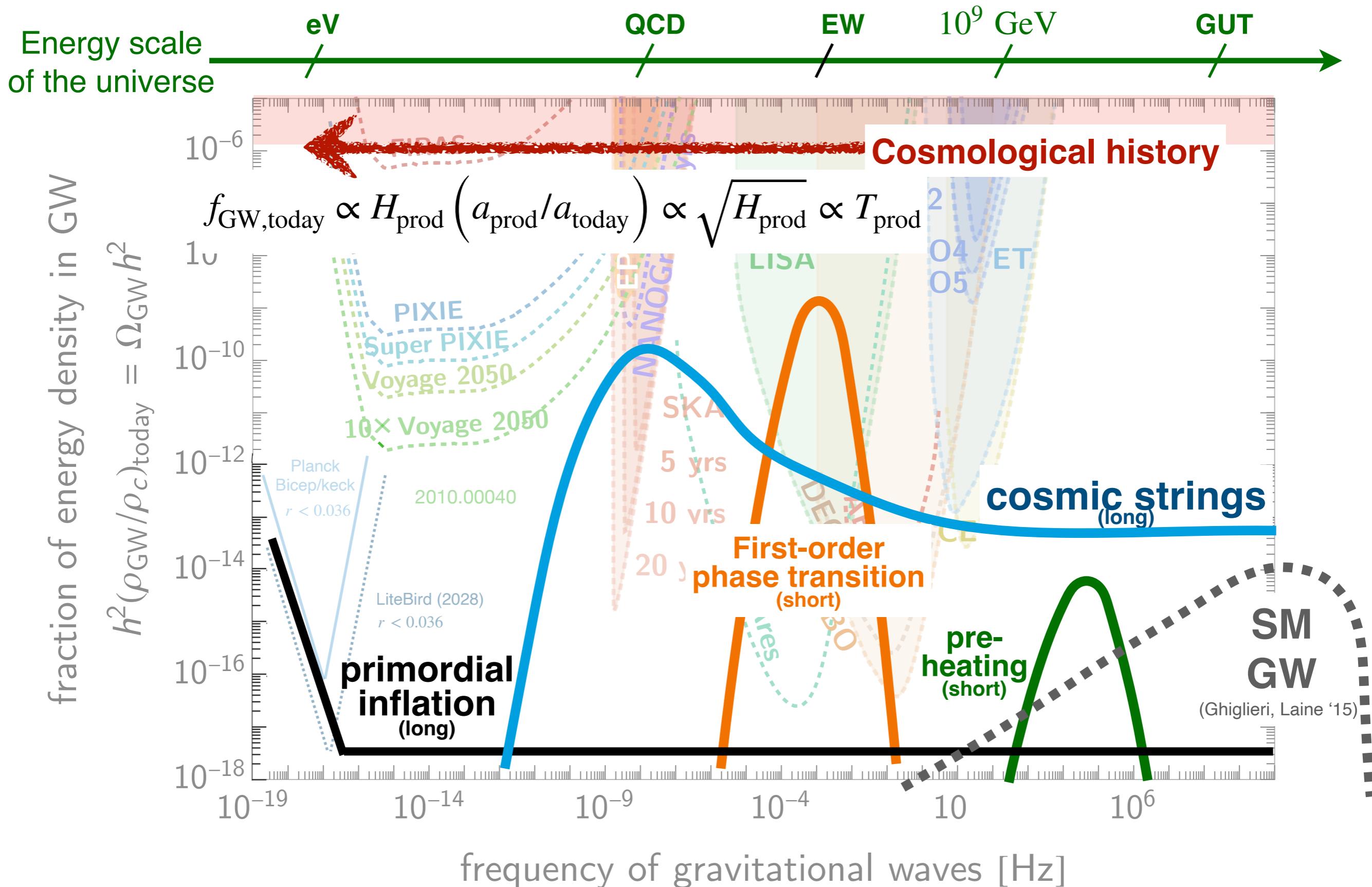
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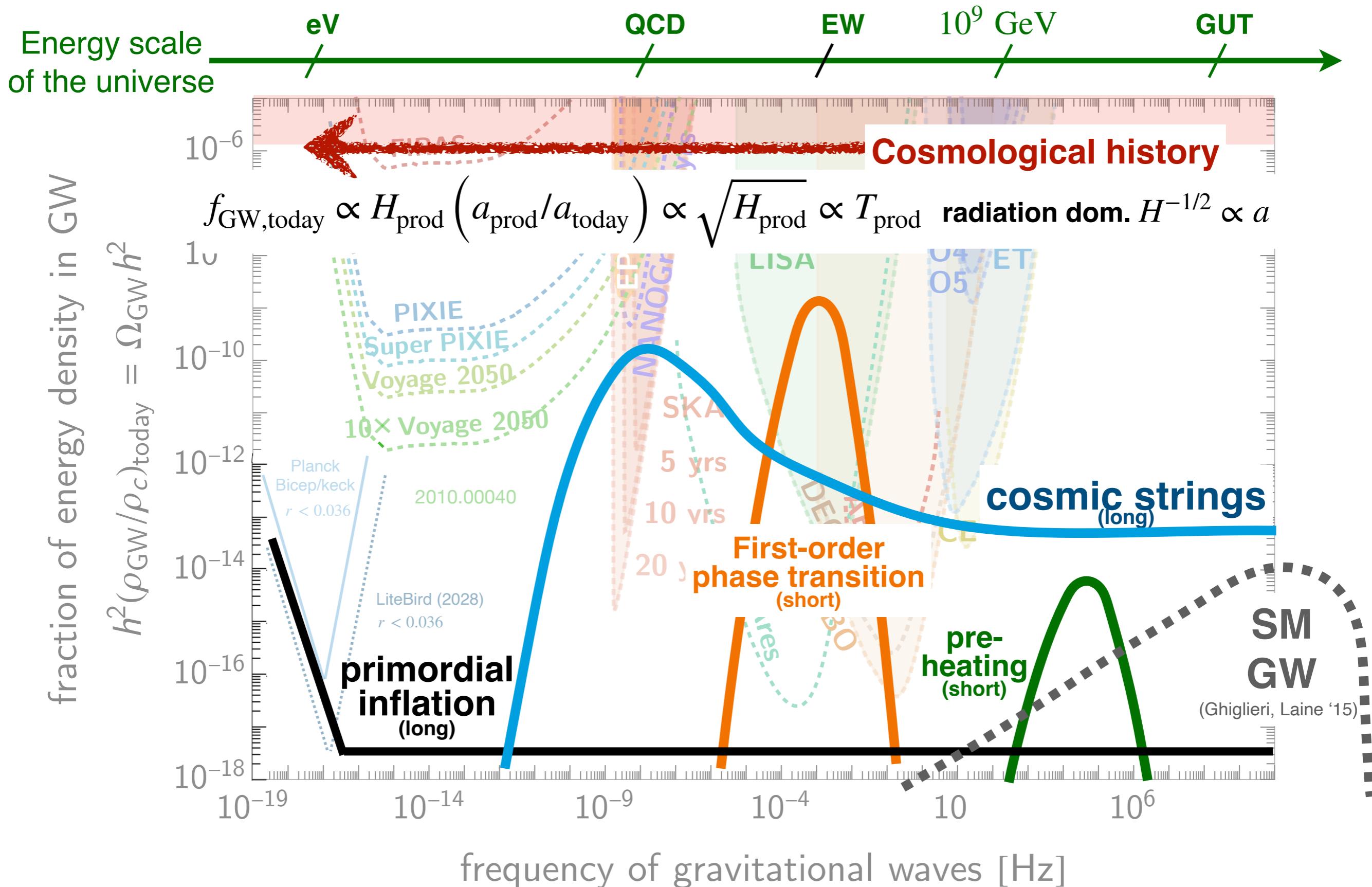
Cosmic Archeology



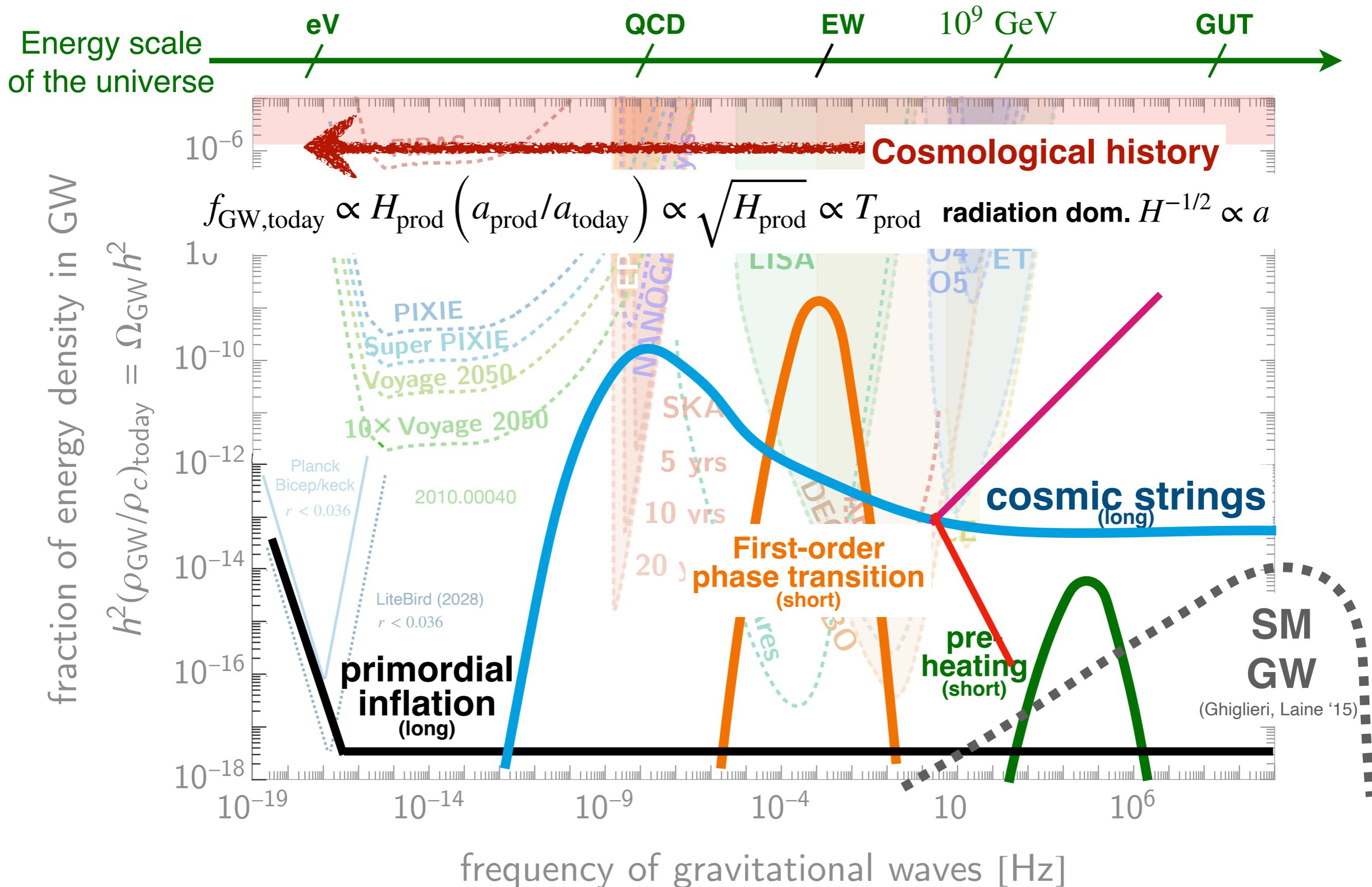
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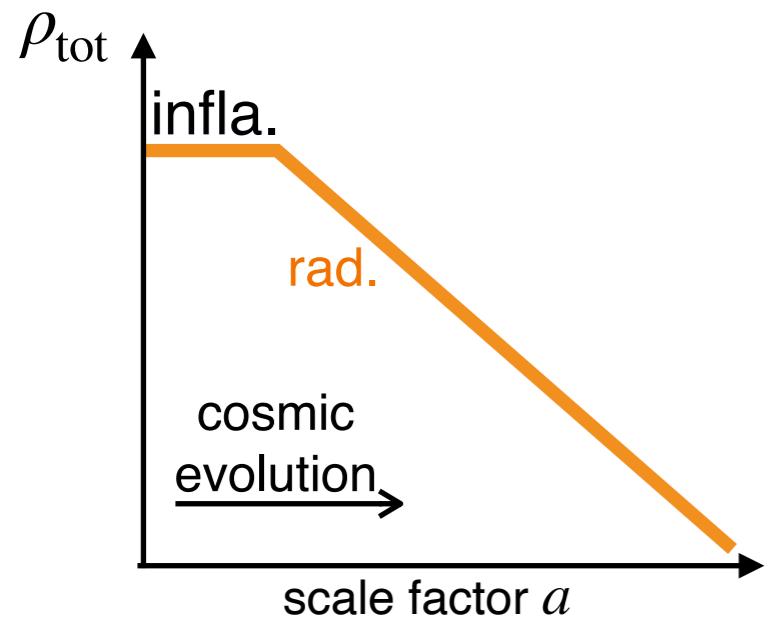


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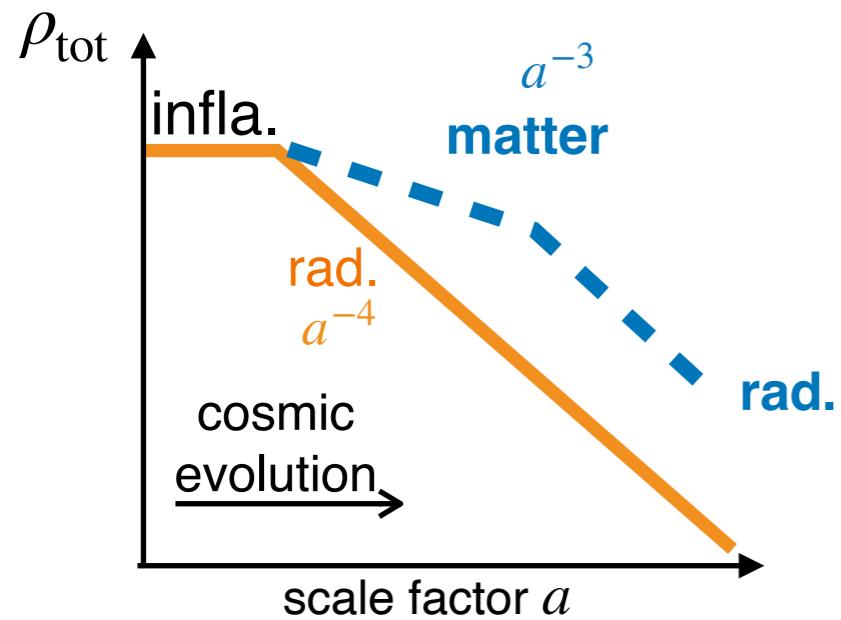


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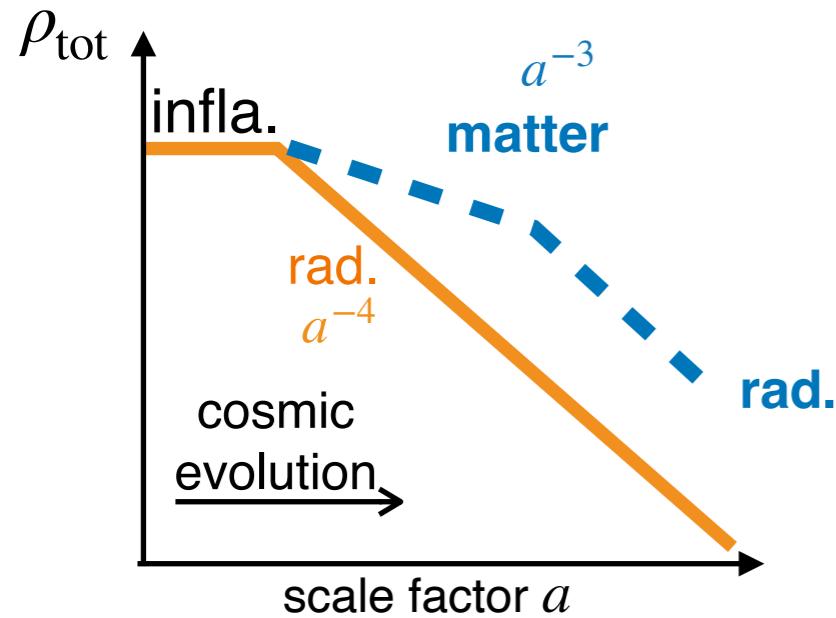


A) Post-inflationary dynamics

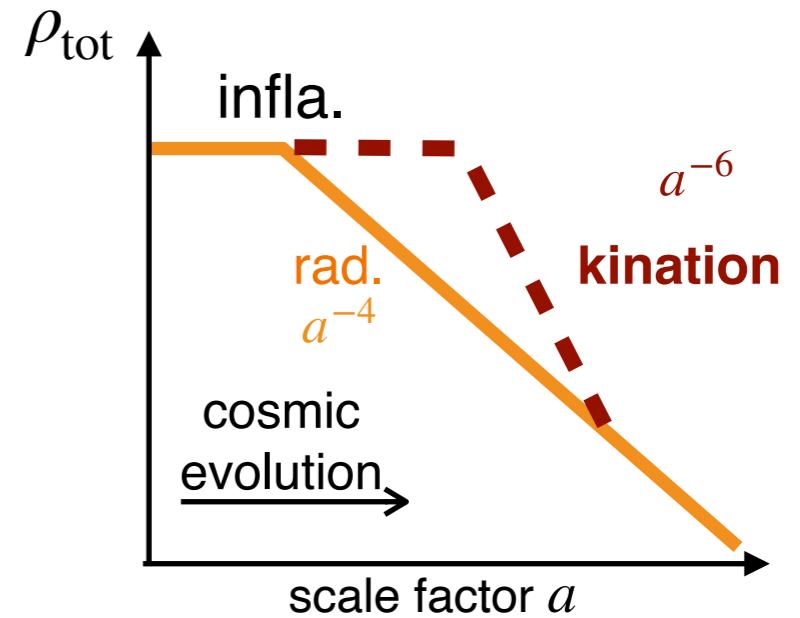


Inflation oscillation

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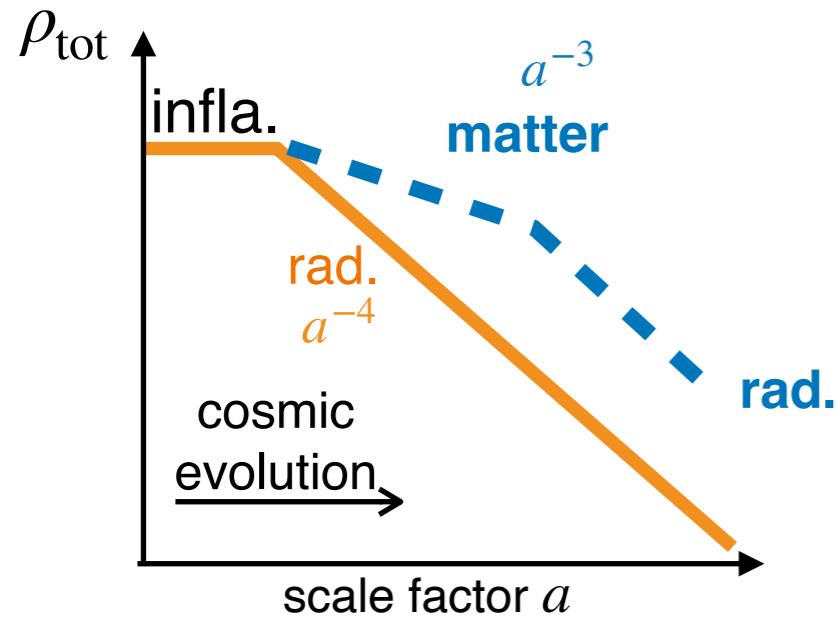


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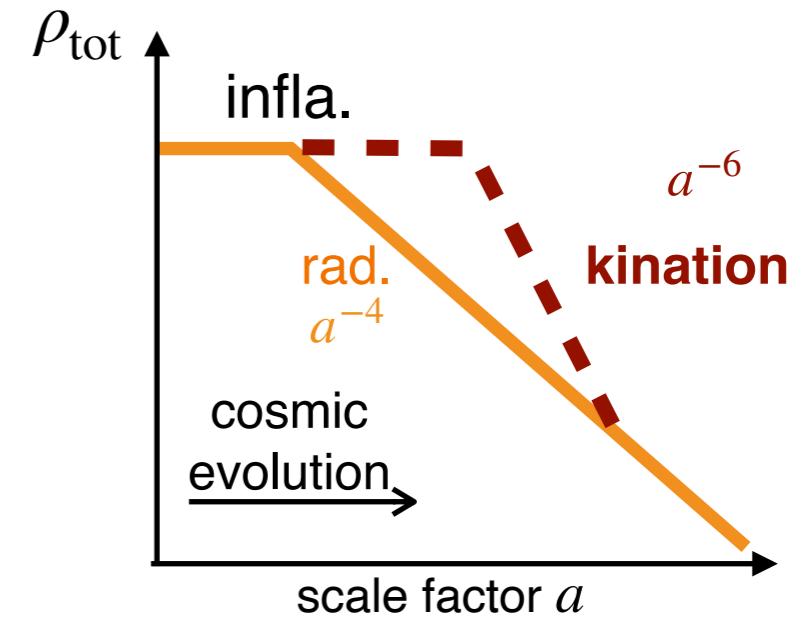


Quintessence inflation

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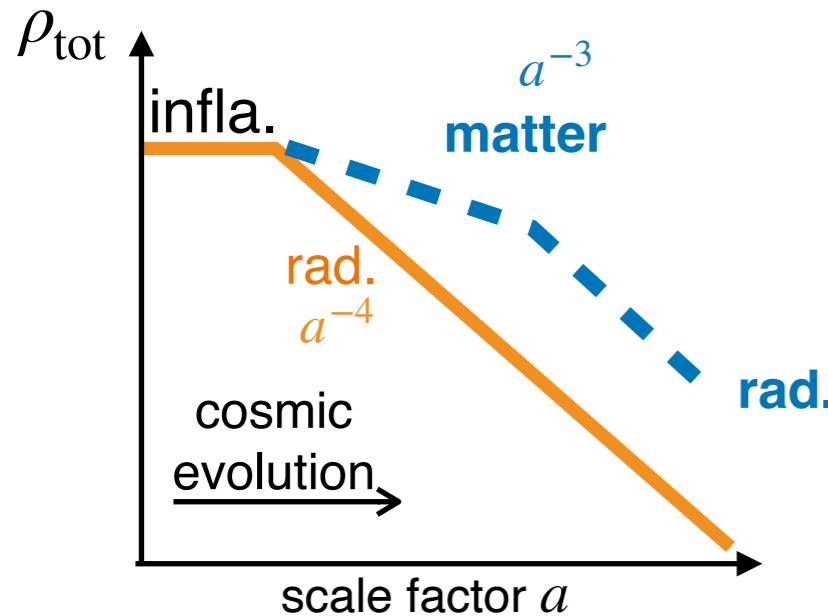
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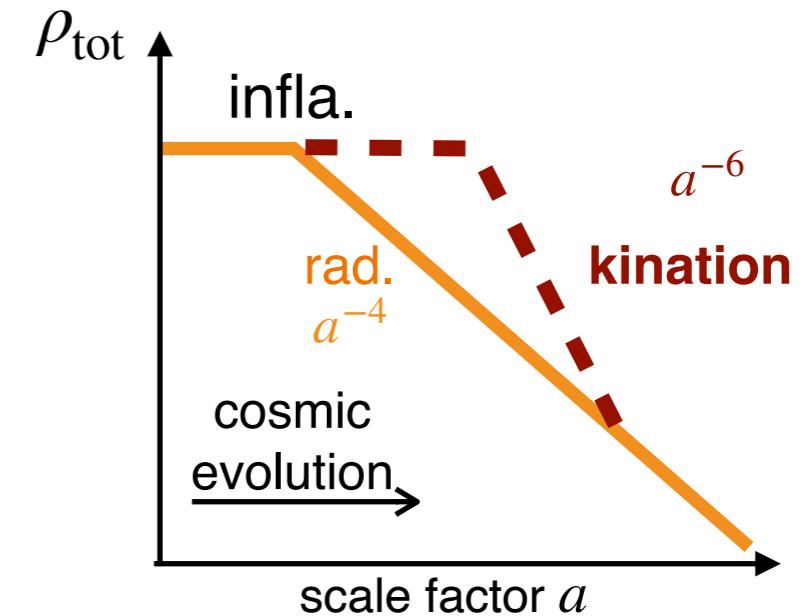
Quintessence inflation

B) Disconnected from inflation sector (this talk)

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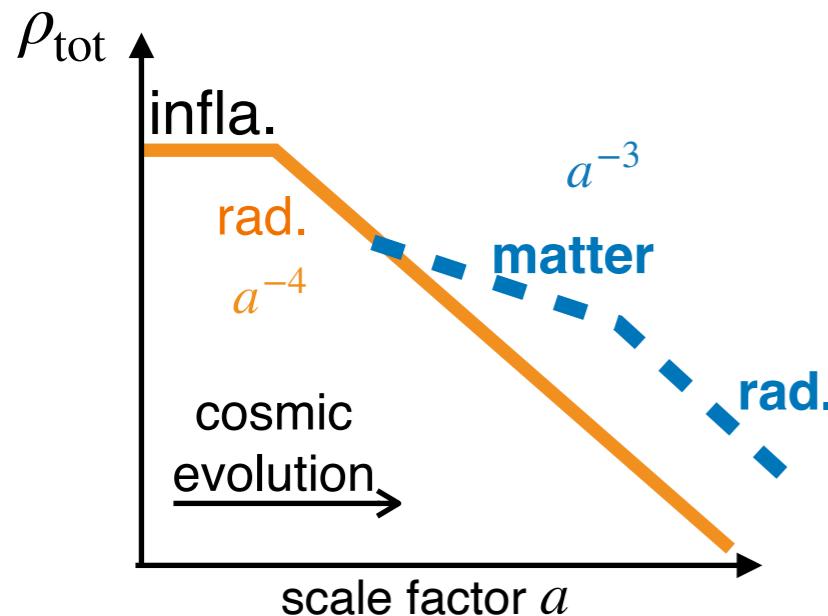


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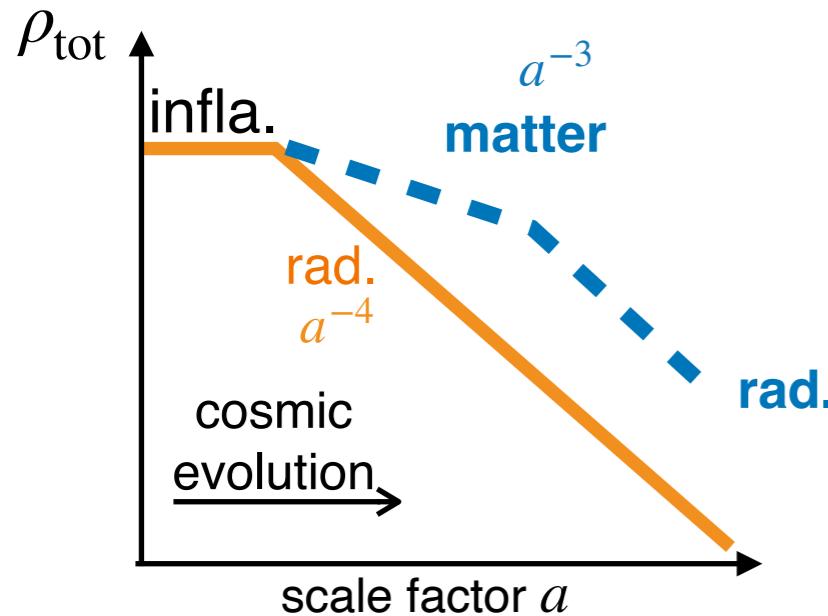
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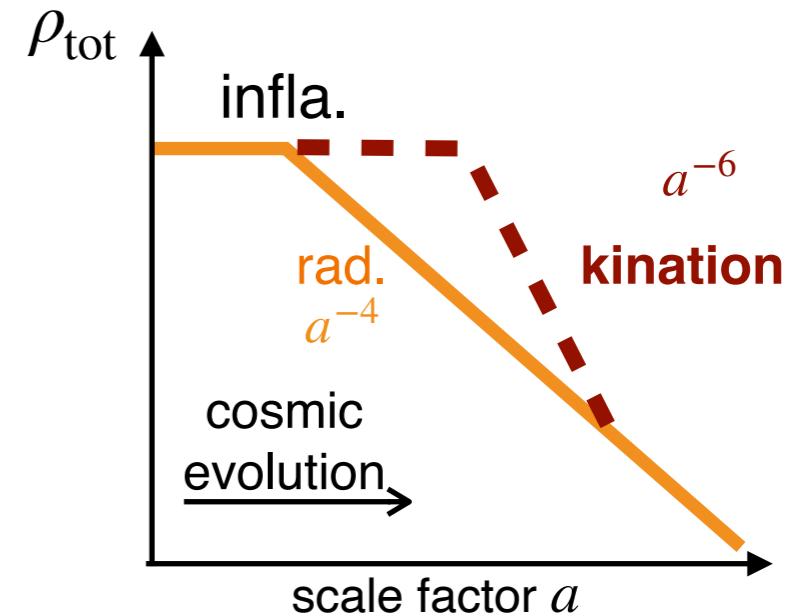


Heavy & unstable
particles

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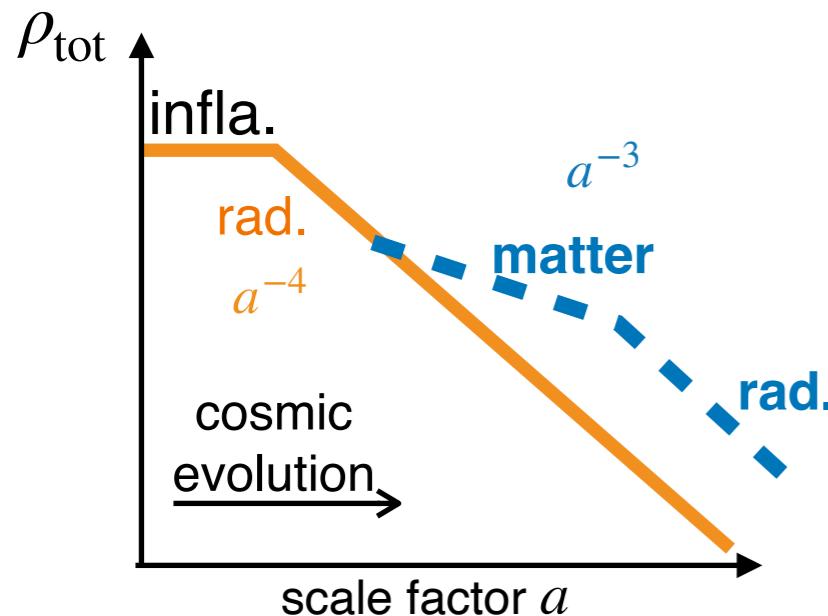


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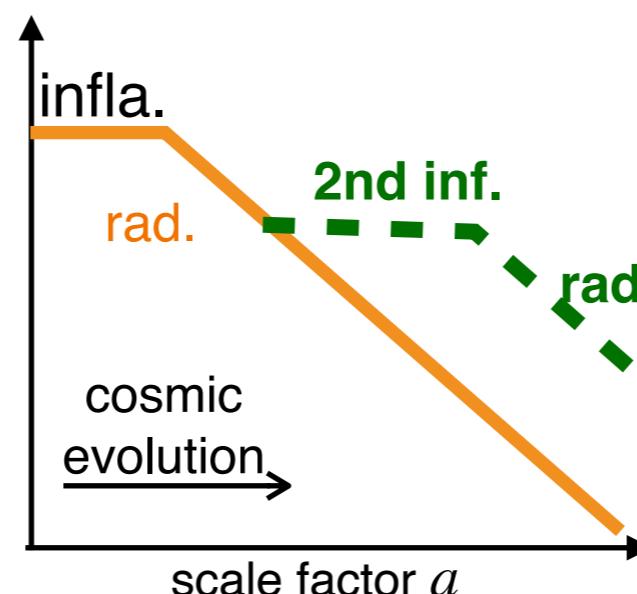


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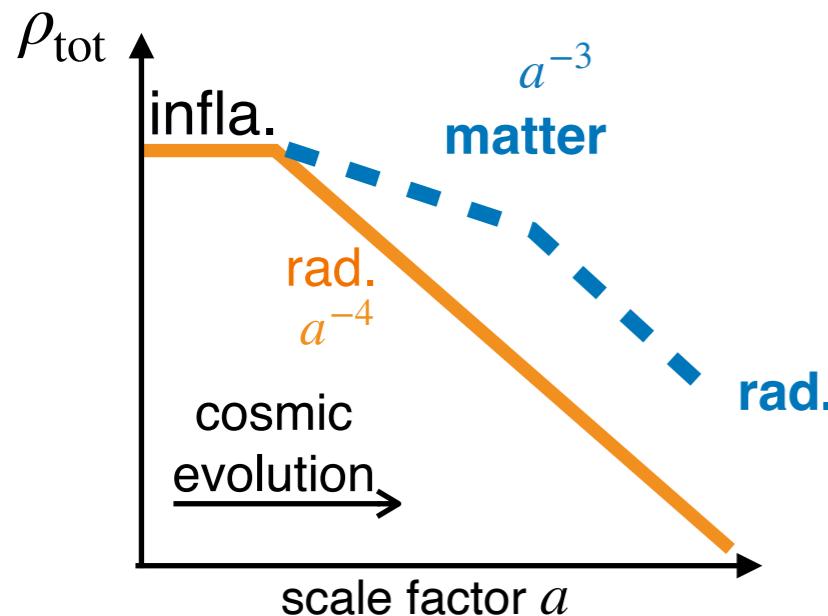


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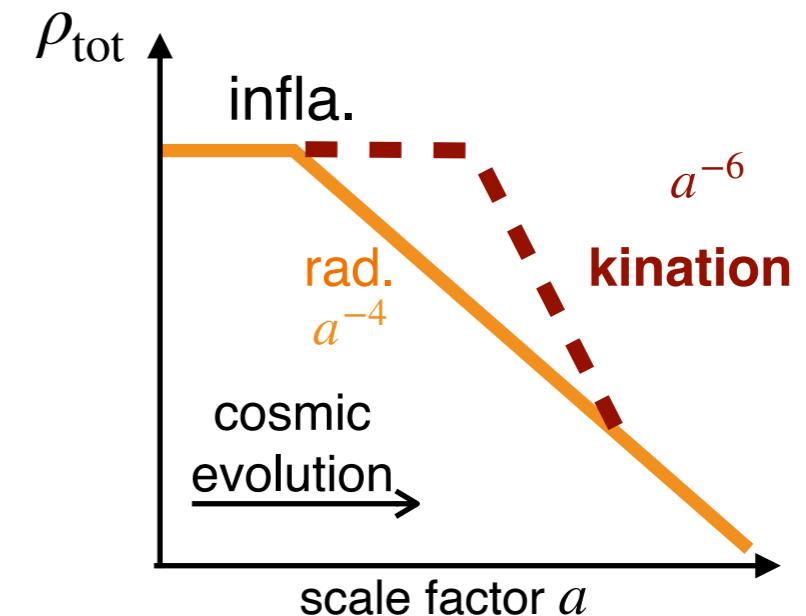


Supercool 1st-order
phase transition

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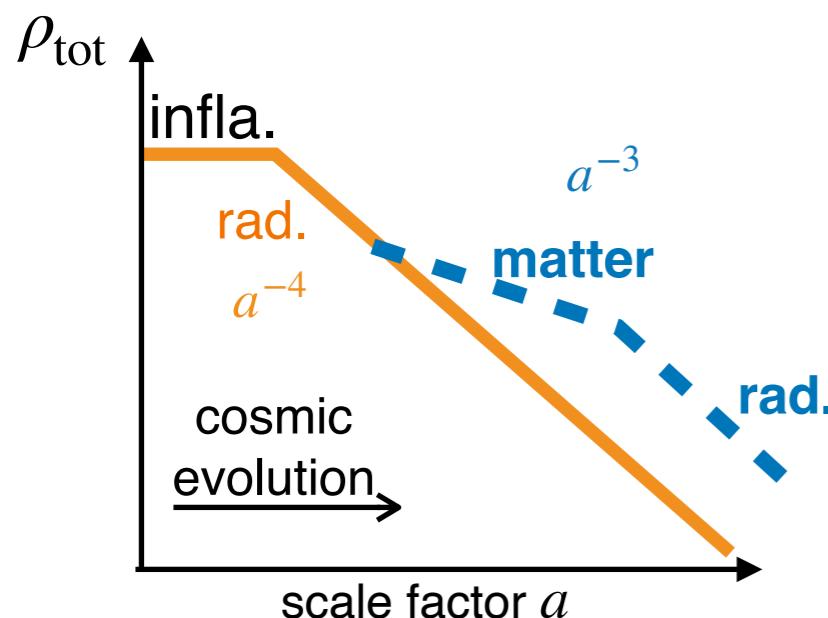


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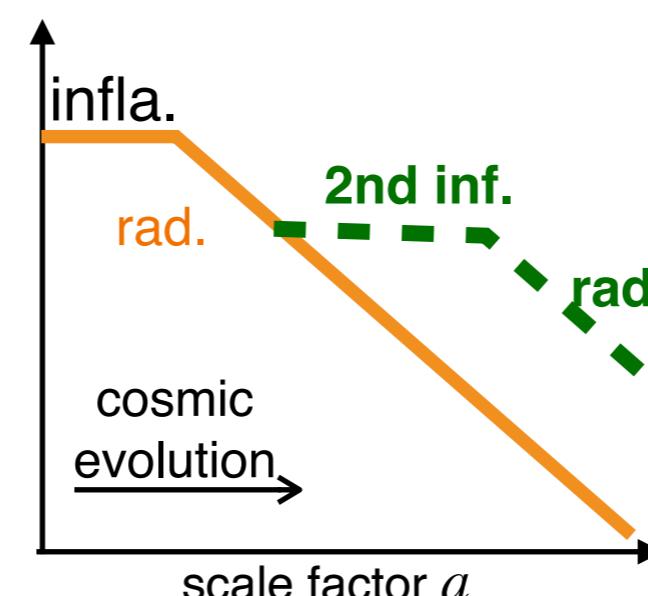


Quintessence inflation

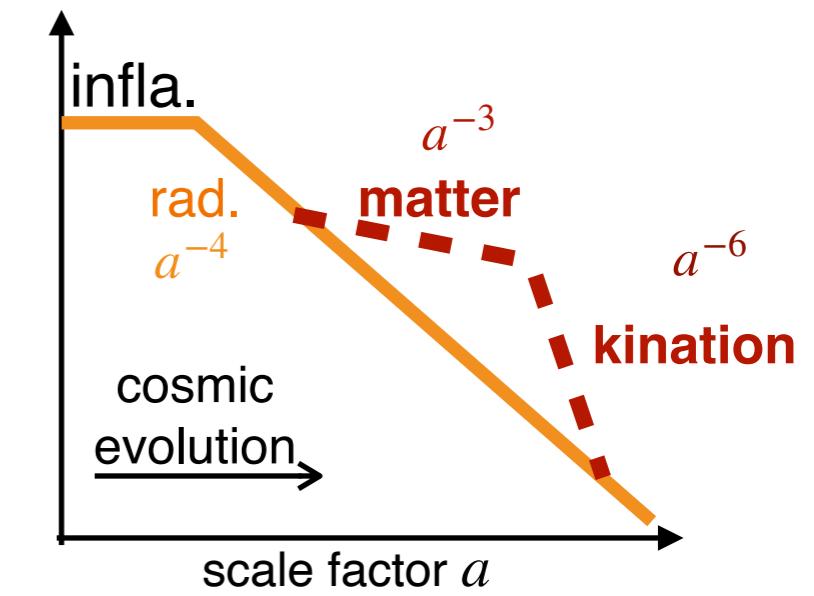
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**Heavy & unstable
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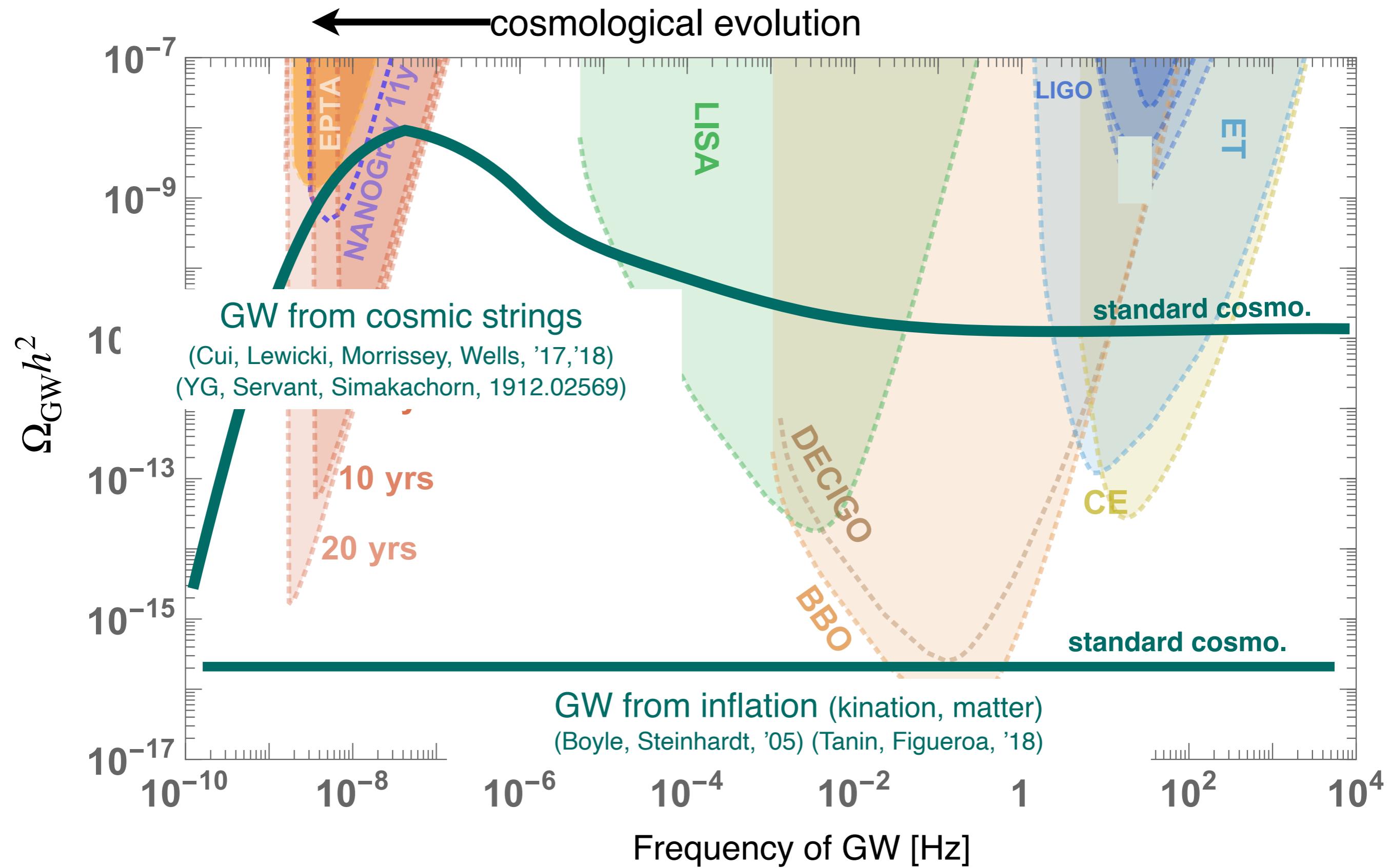


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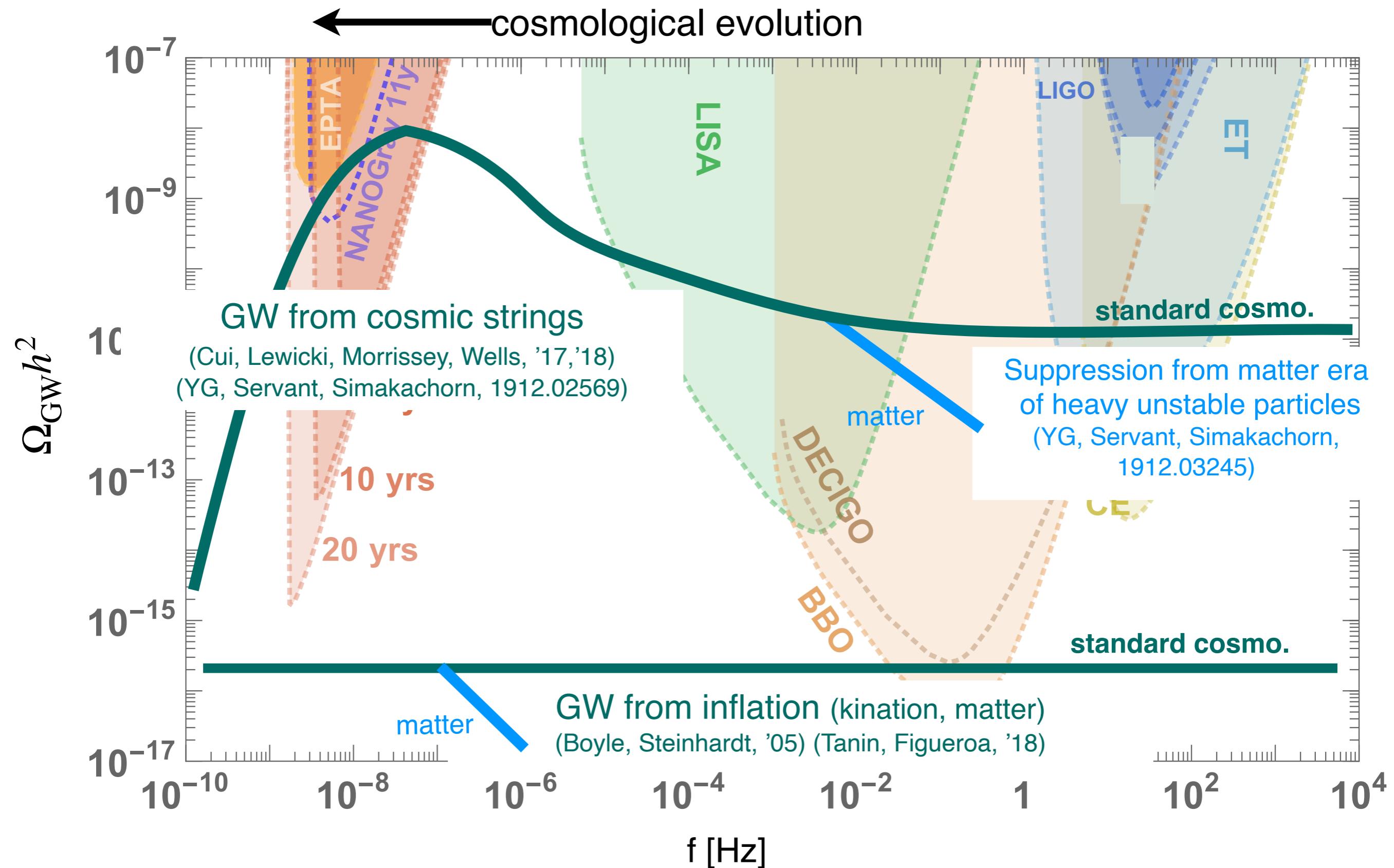


**Rotating field
(Affleck-Dine)**

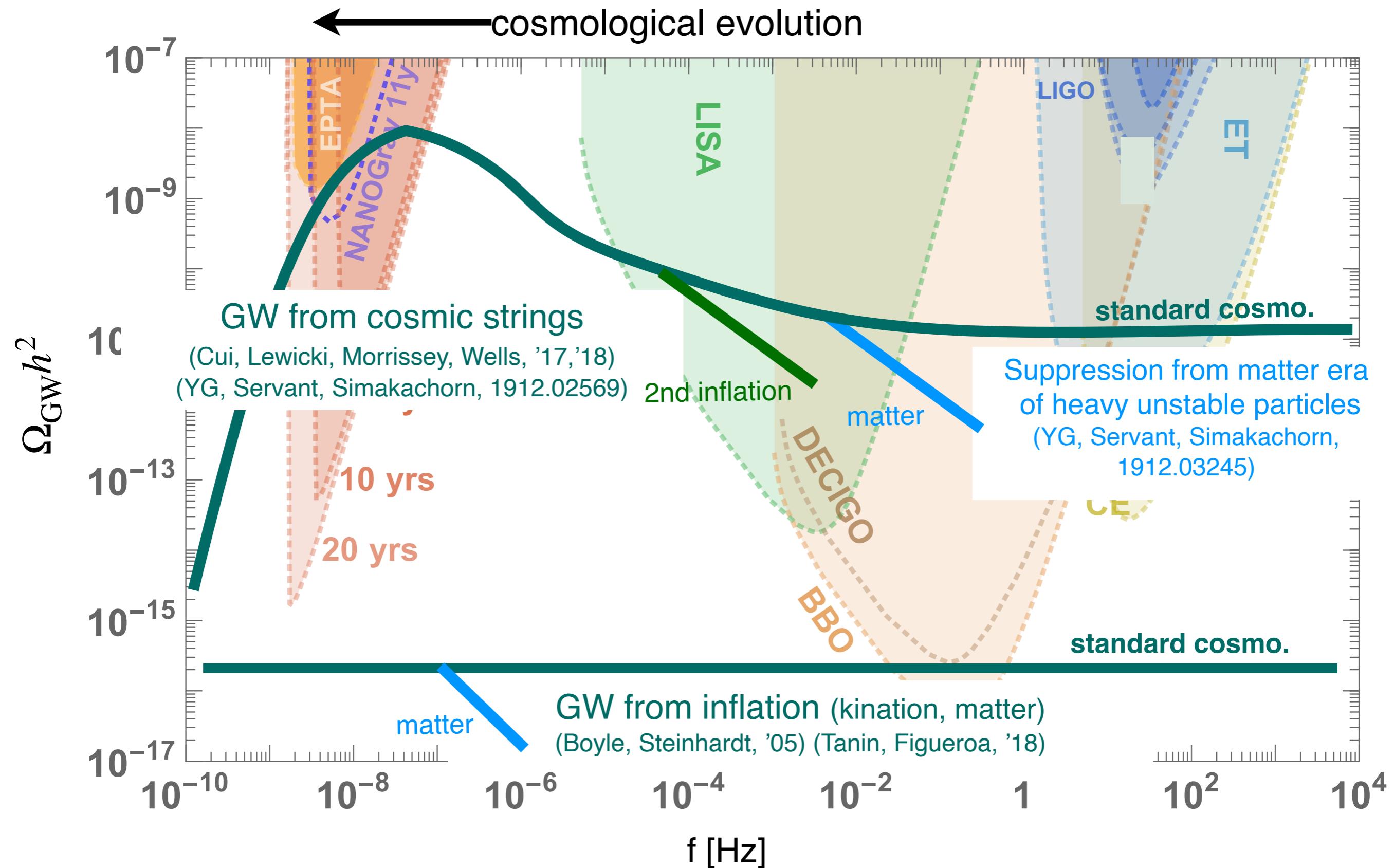
Overview: Cosmic archeology with GW



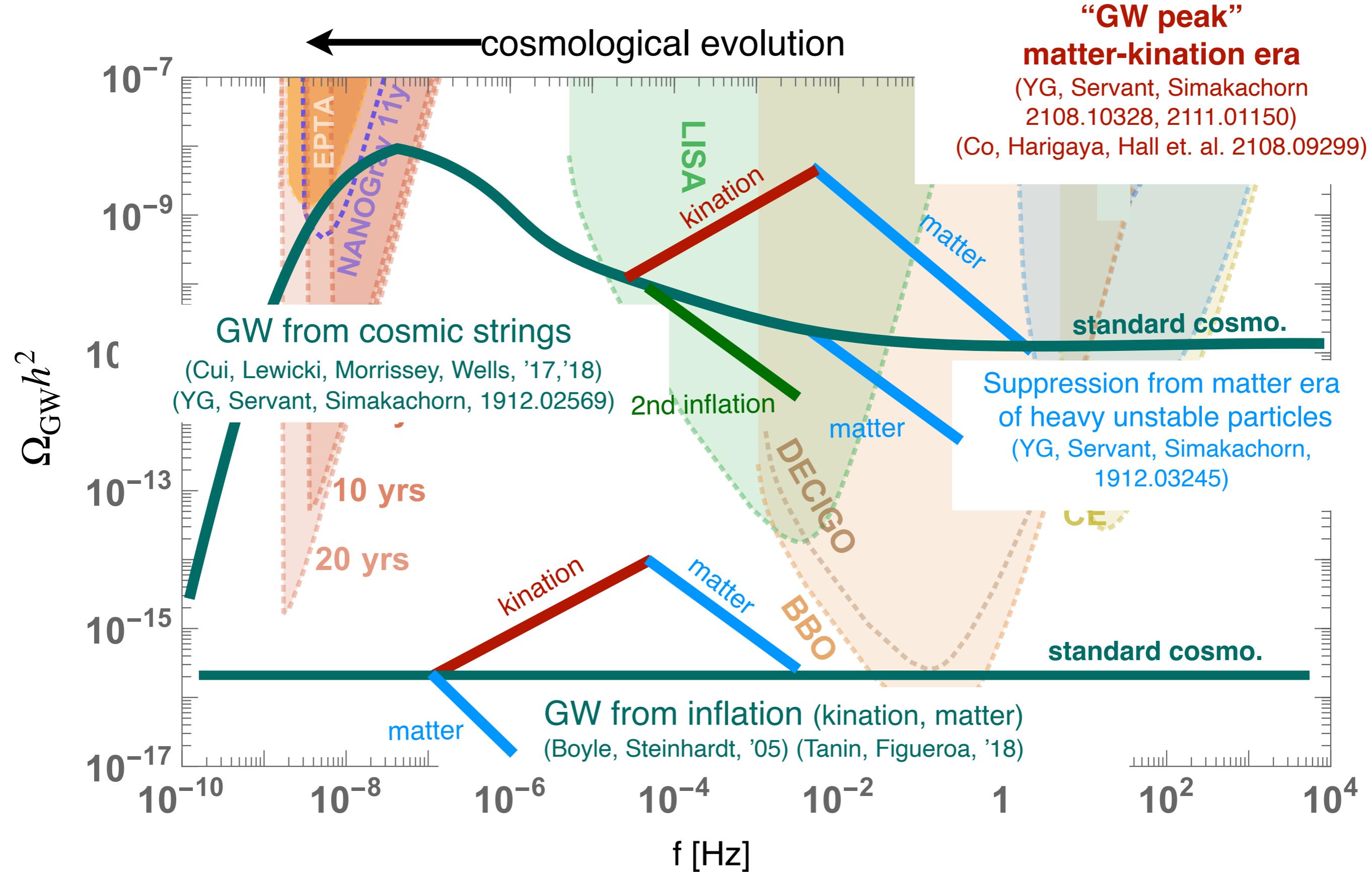
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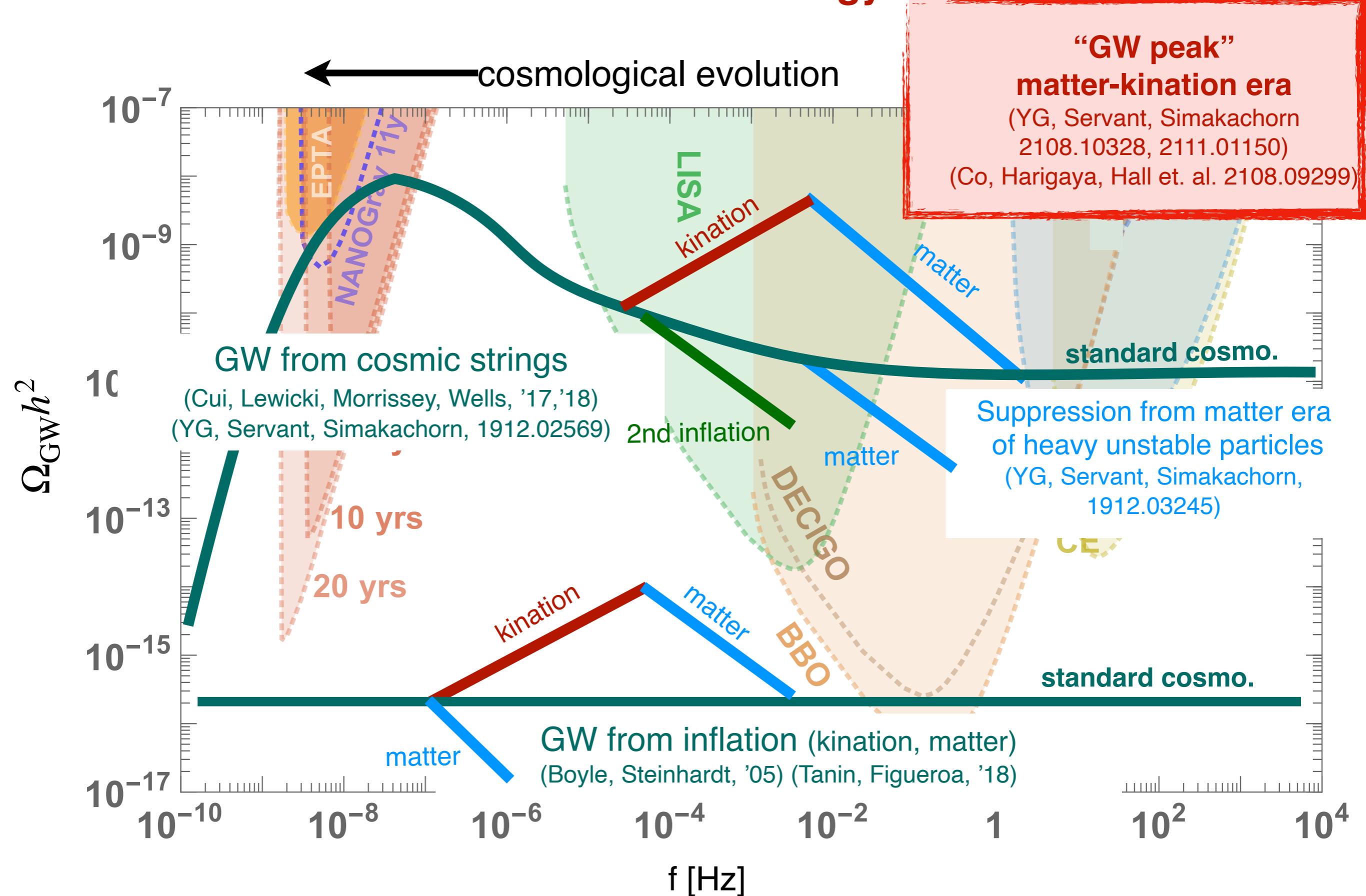
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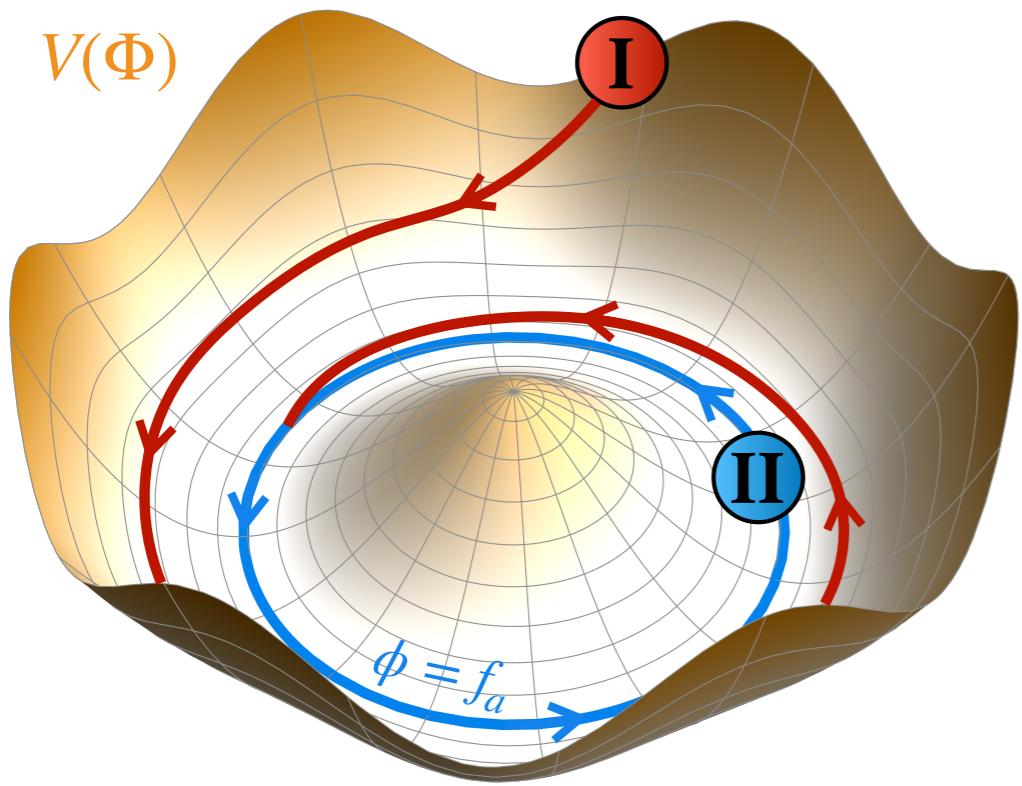


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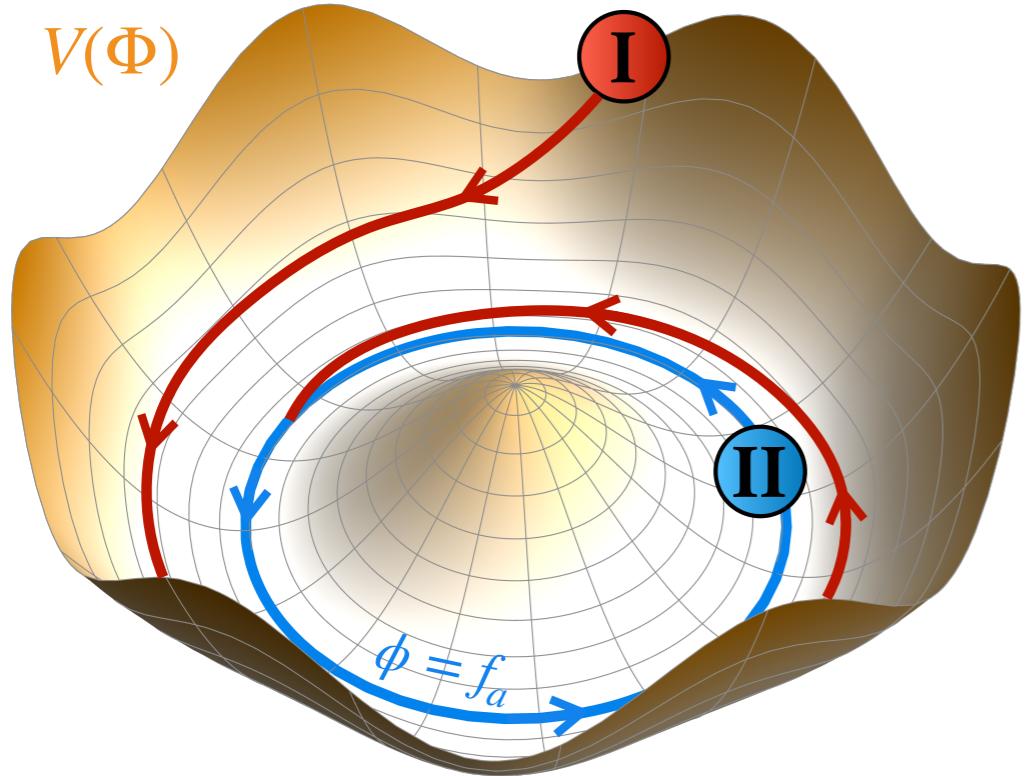




Rotating complex scalar field

“Affleck-Dine Baryogenesis” (Affleck, Dine, 1985)

“Axiogenesis” (Co, Hall, Harigaya, et. al., '19)

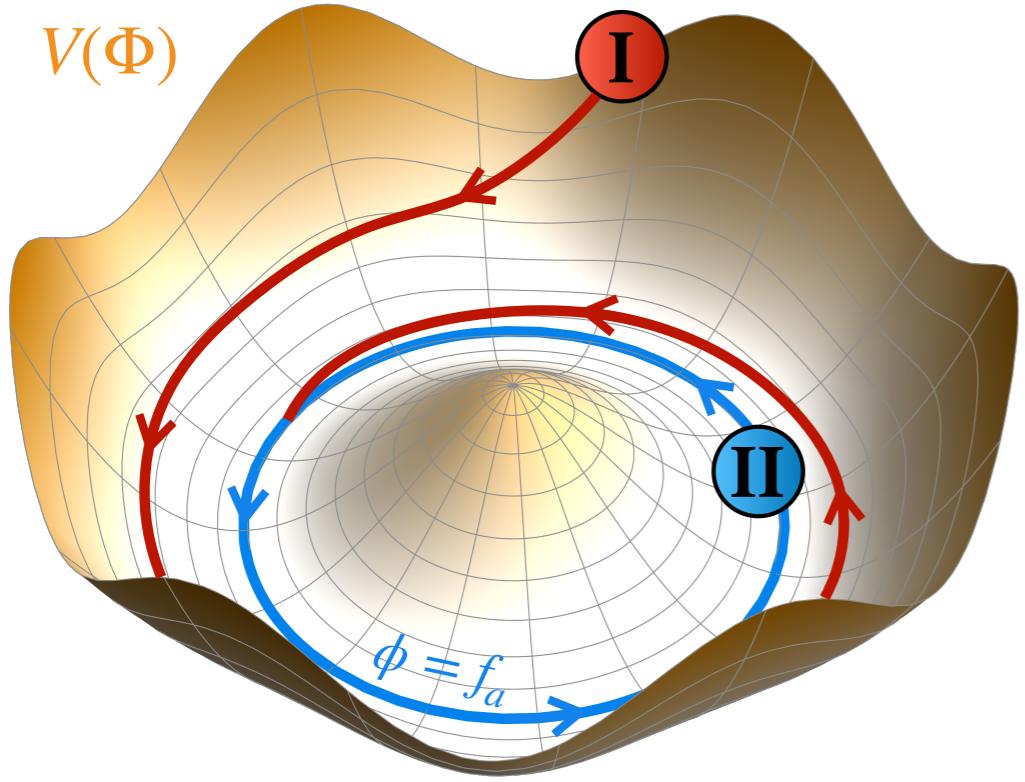


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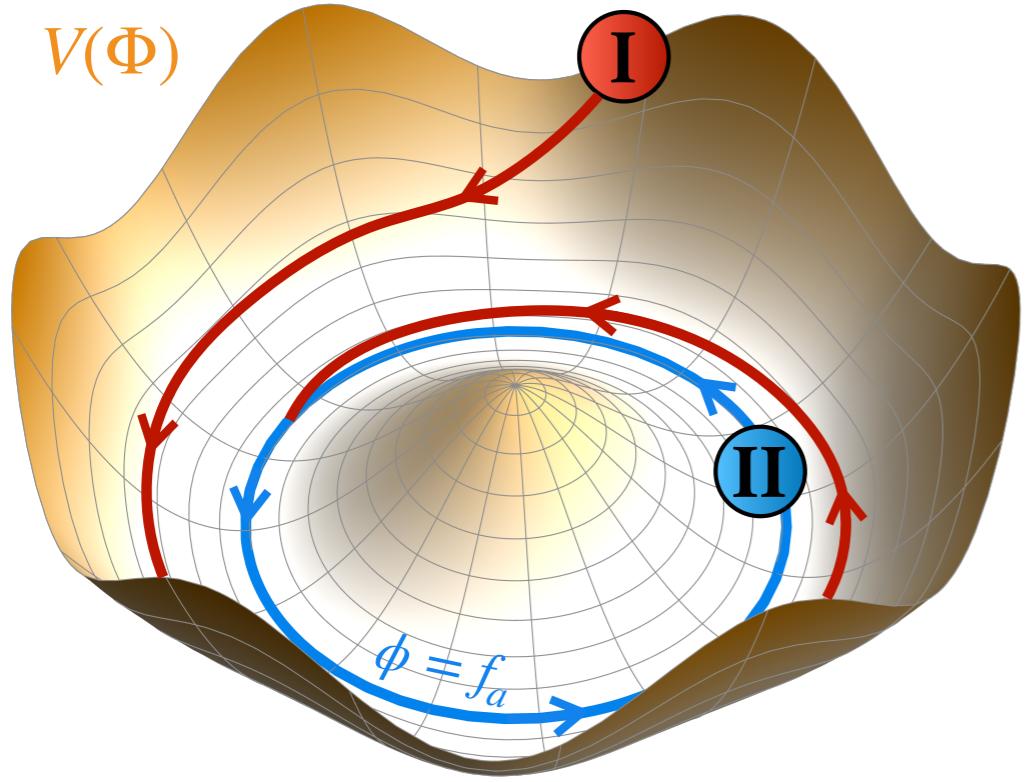
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Ingredients for successful kination era:

- I. $U(1)$ -symmetric (**quadratic**) potential with spontaneous symmetry-breaking minimum

$$V(\Phi) = m_r^2 |\Phi|^2 \left[\log\left(\frac{|\Phi|^2}{f_a^2}\right) - 1 \right]$$

(generic in SUSY)



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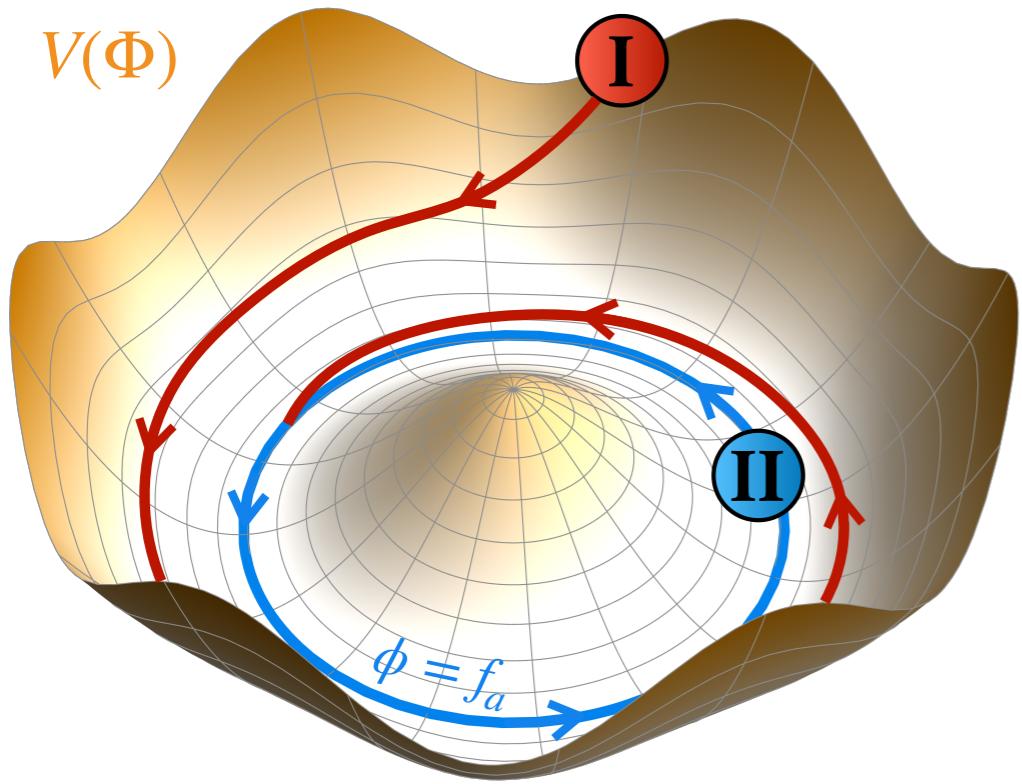
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$$V_H = -H^2 |\Phi|^2$$

(Dine, Randall, Thomas, 1995) (SUSY again)



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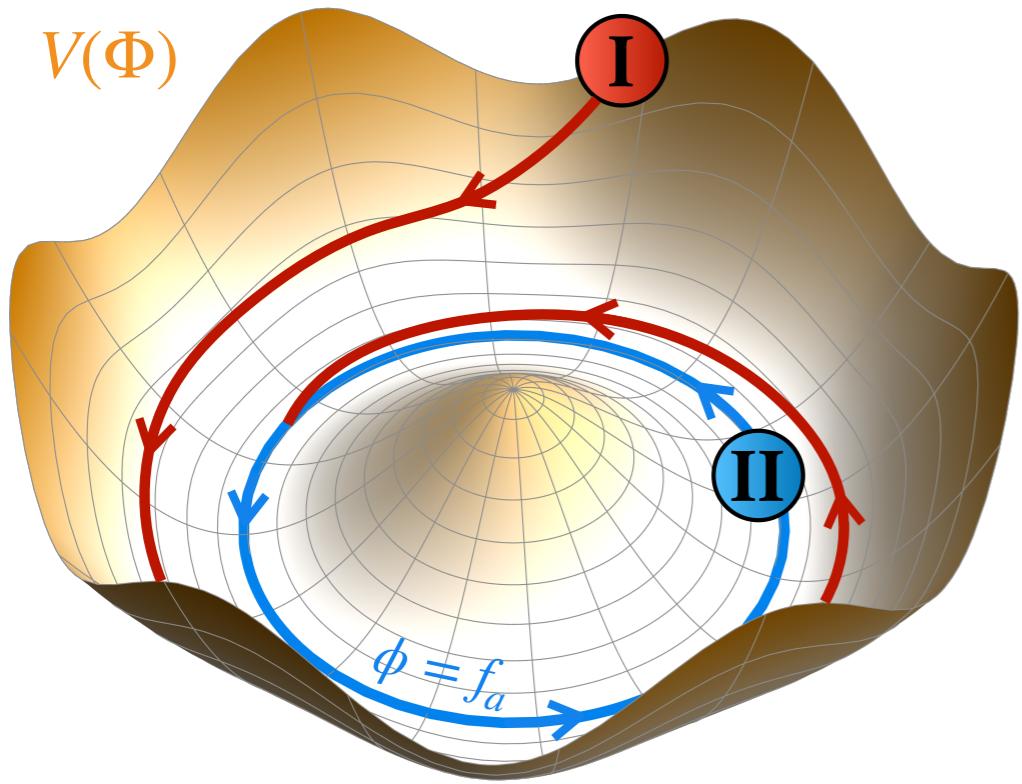
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$$V(\Phi) = \Lambda_b^4 \left[\left(\frac{\Phi}{M_{Pl}} \right)^l + \left(\frac{\Phi^\dagger}{M_{Pl}} \right)^l \right]$$

(Neutron EDM bound $l \gtrsim 10$)



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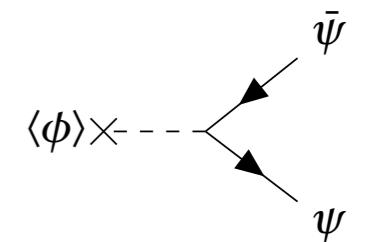
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- IV. Damping of radial motion

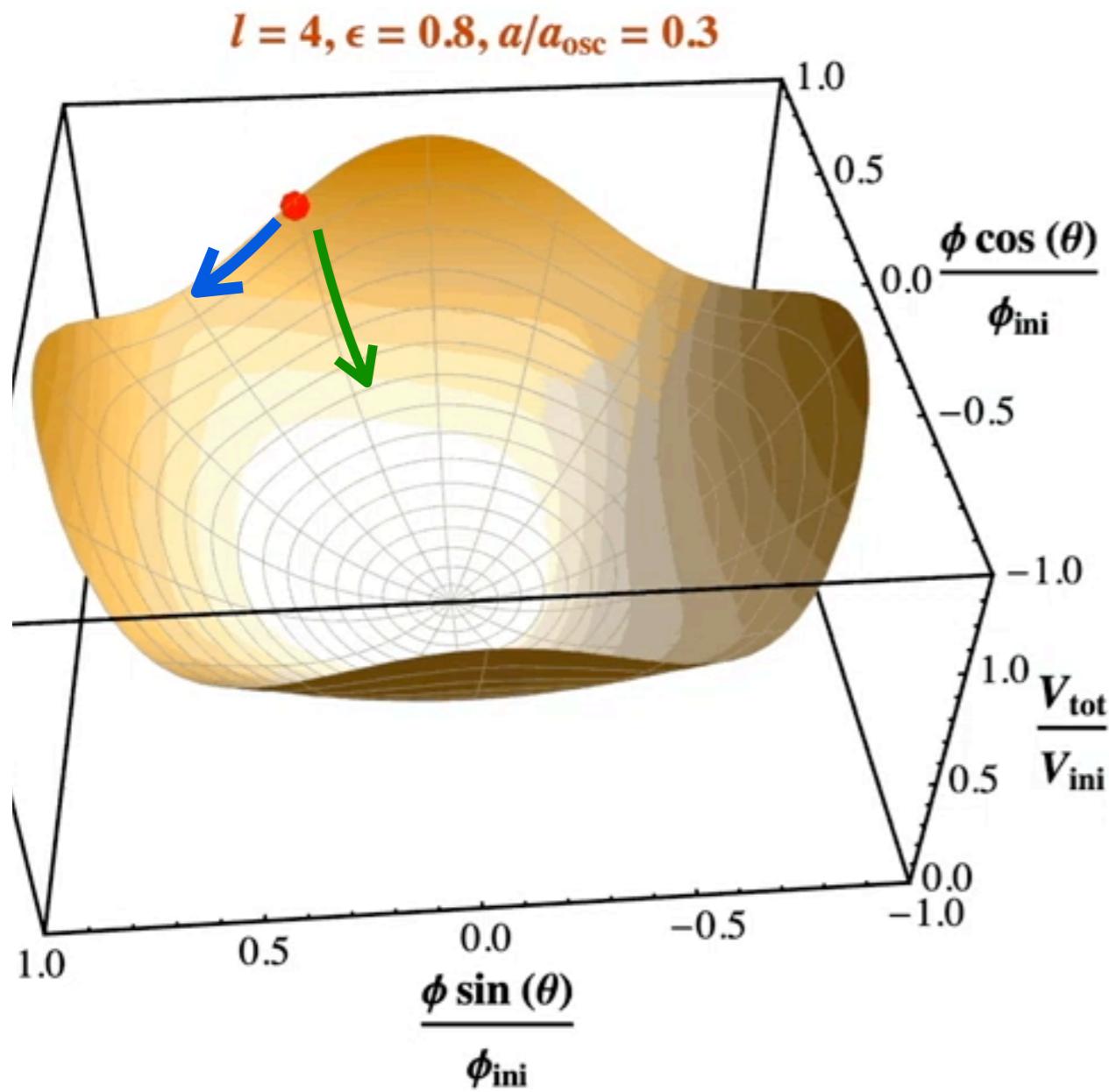
$$V_{int} = \lambda_\psi \phi \bar{\psi} \psi$$



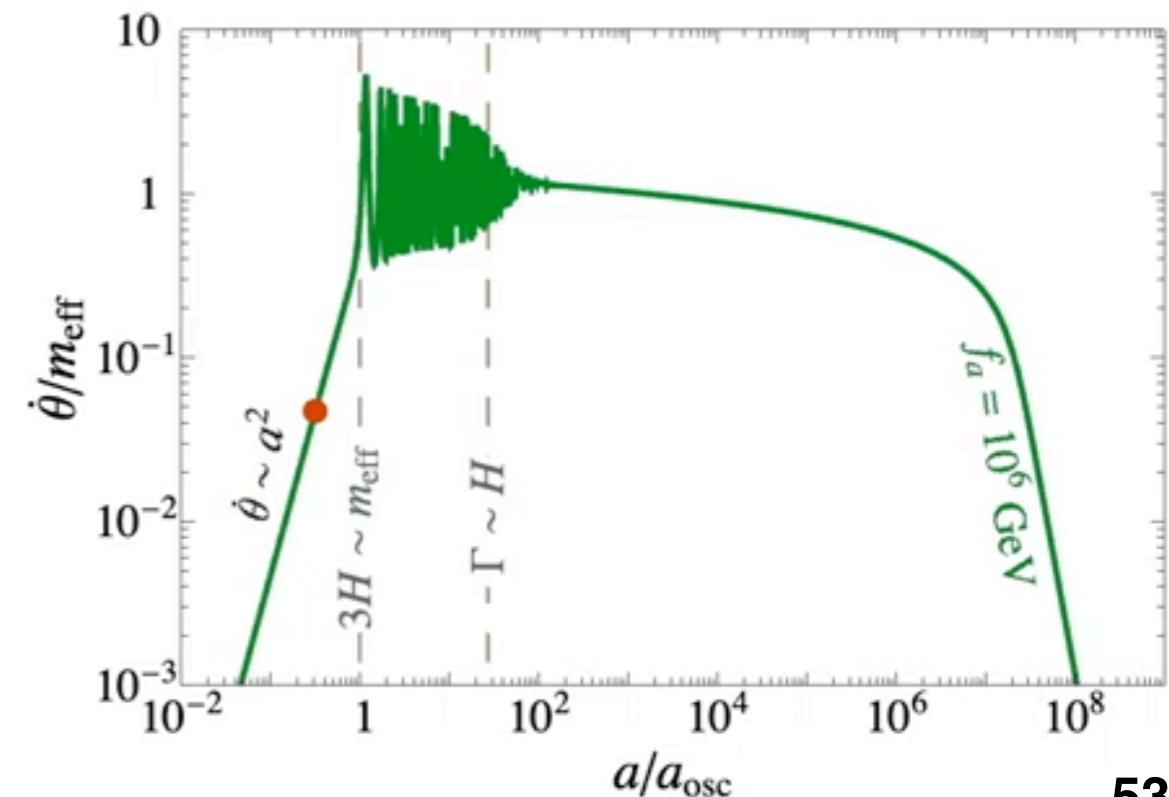
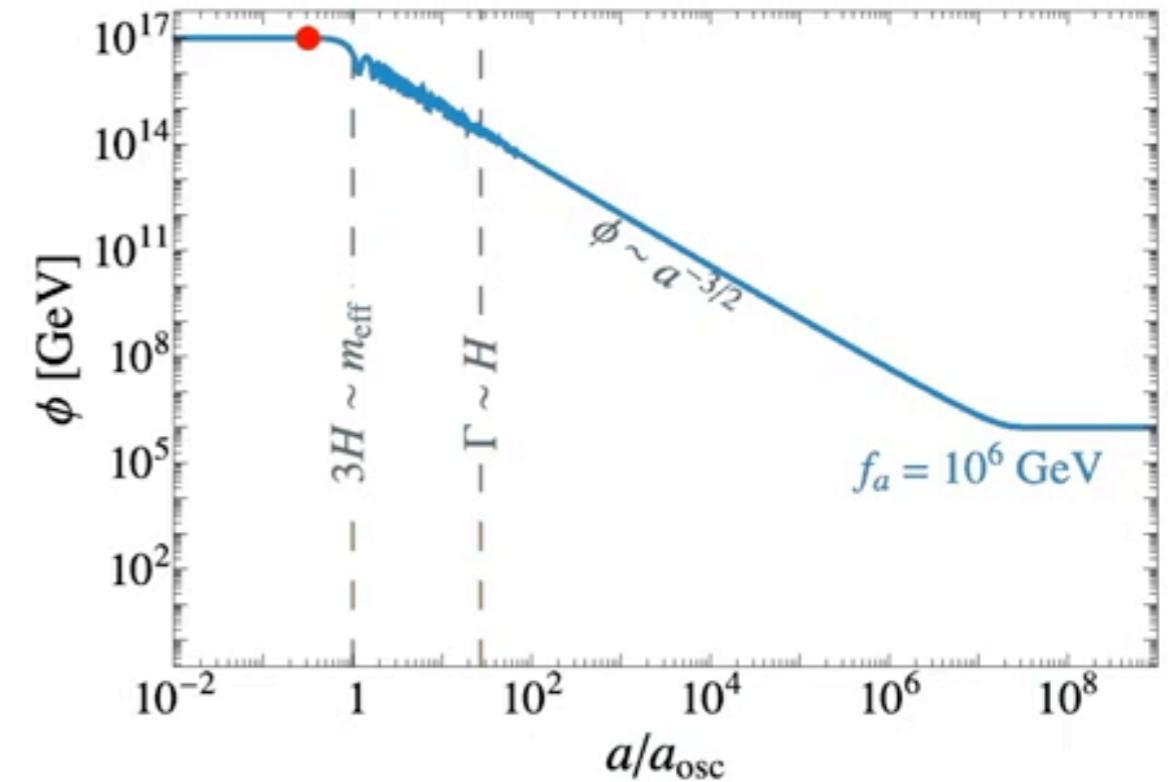
[Mukaida, Nakayama, '12 '13]

Ingredients I & II & III: scalar potential and large initial VEV

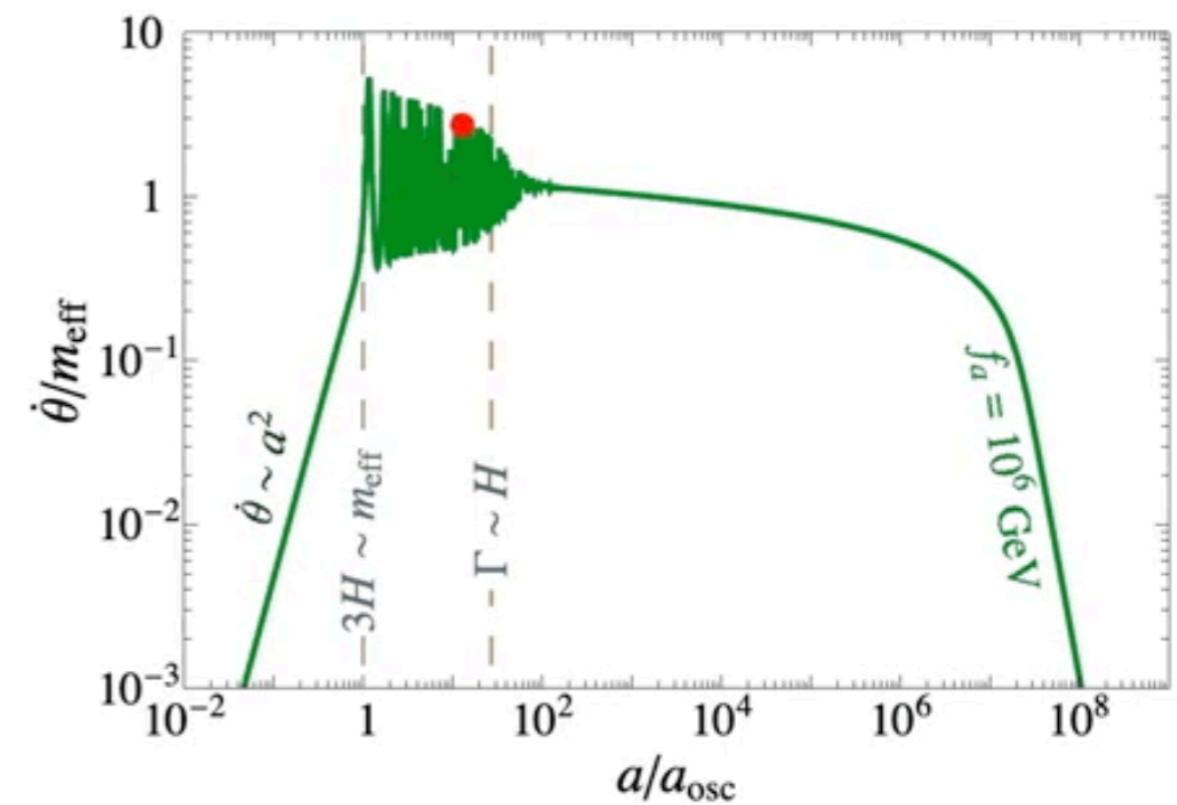
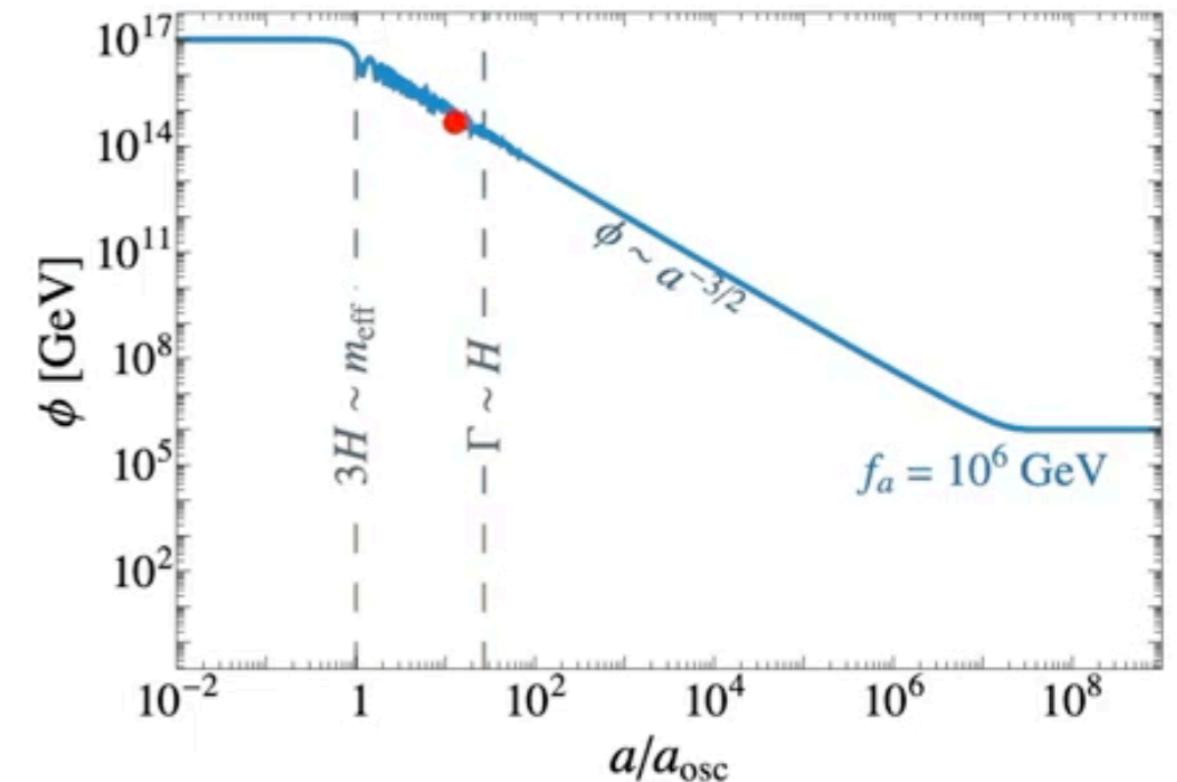
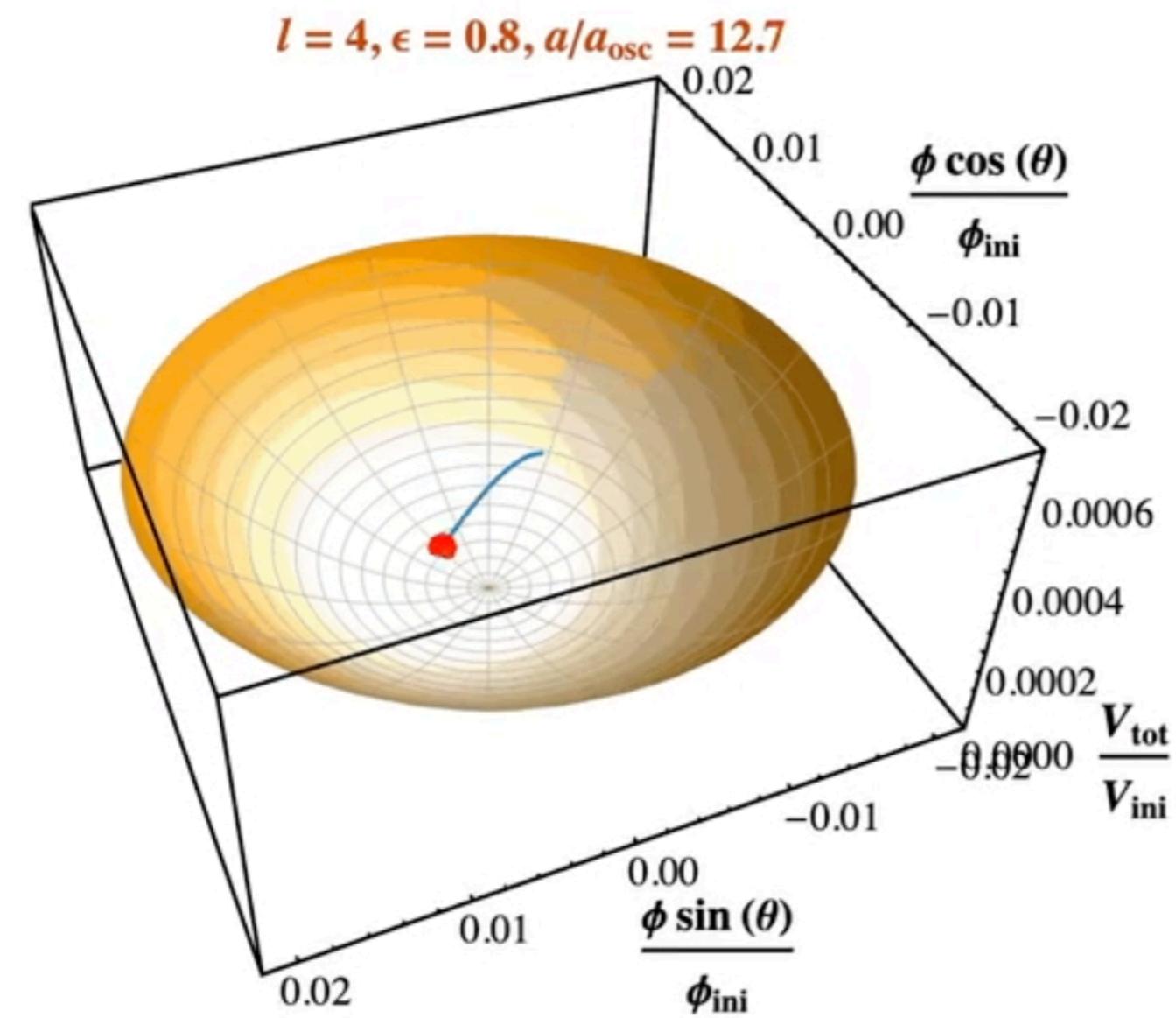
[YG, Servant, Simakachorn, 2111.01150]



$$V(\Phi) = m_r^2 |\Phi|^2 \left[\log \left(\frac{|\Phi|^2}{f_a^2} \right) - 1 \right] + \Lambda_b^4 \left[\left(\frac{\Phi}{M_{\text{Pl}}} \right)^l + \left(\frac{\Phi^\dagger}{M_{\text{Pl}}} \right)^l \right] - H^2 |\Phi|^2$$

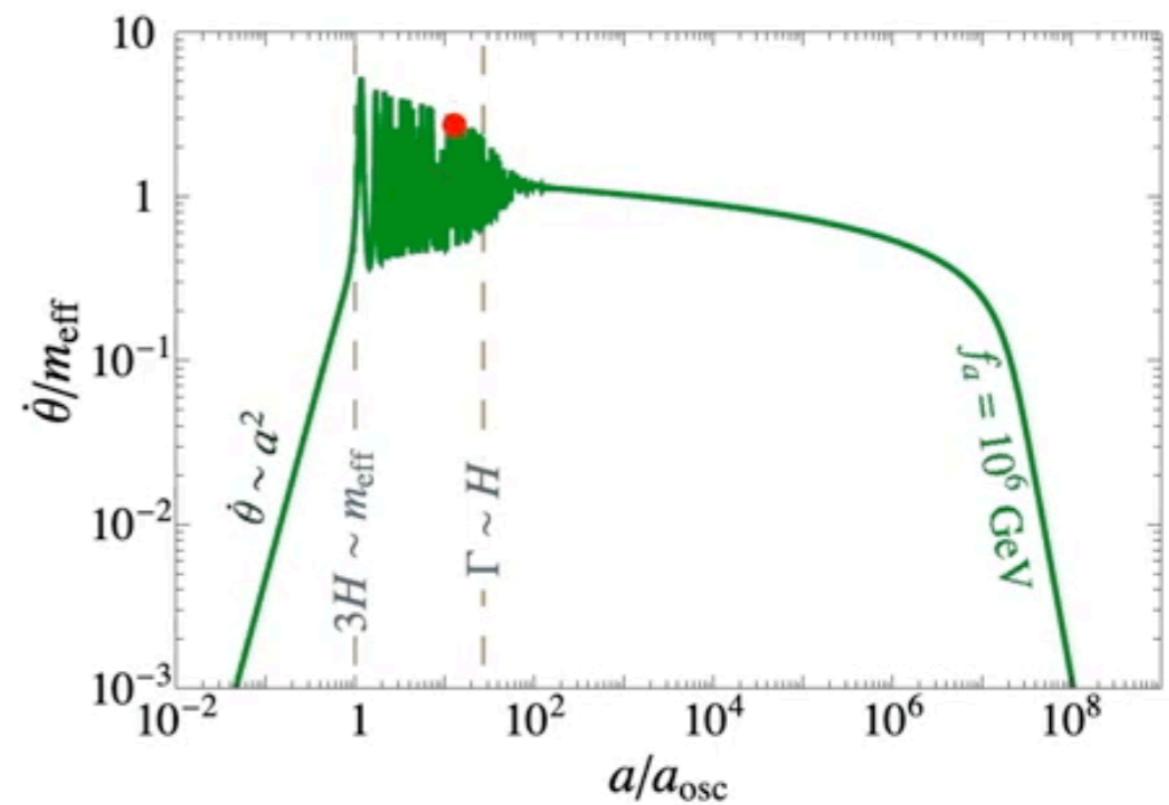
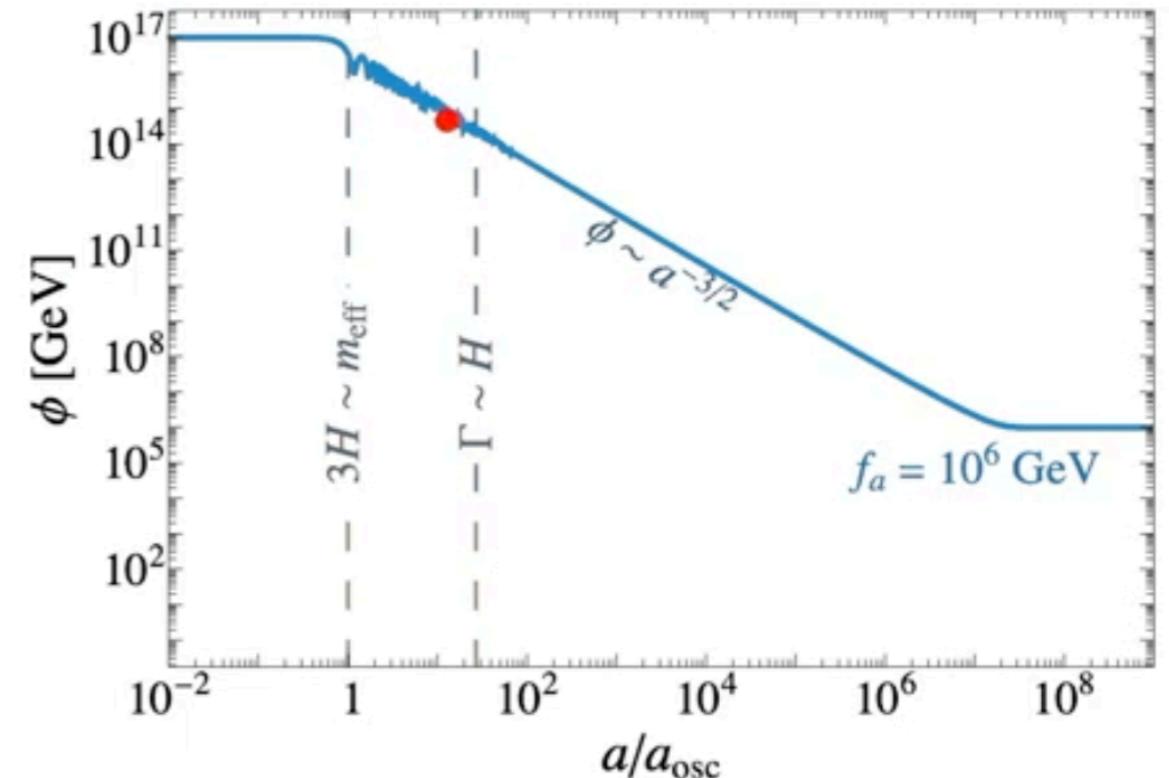
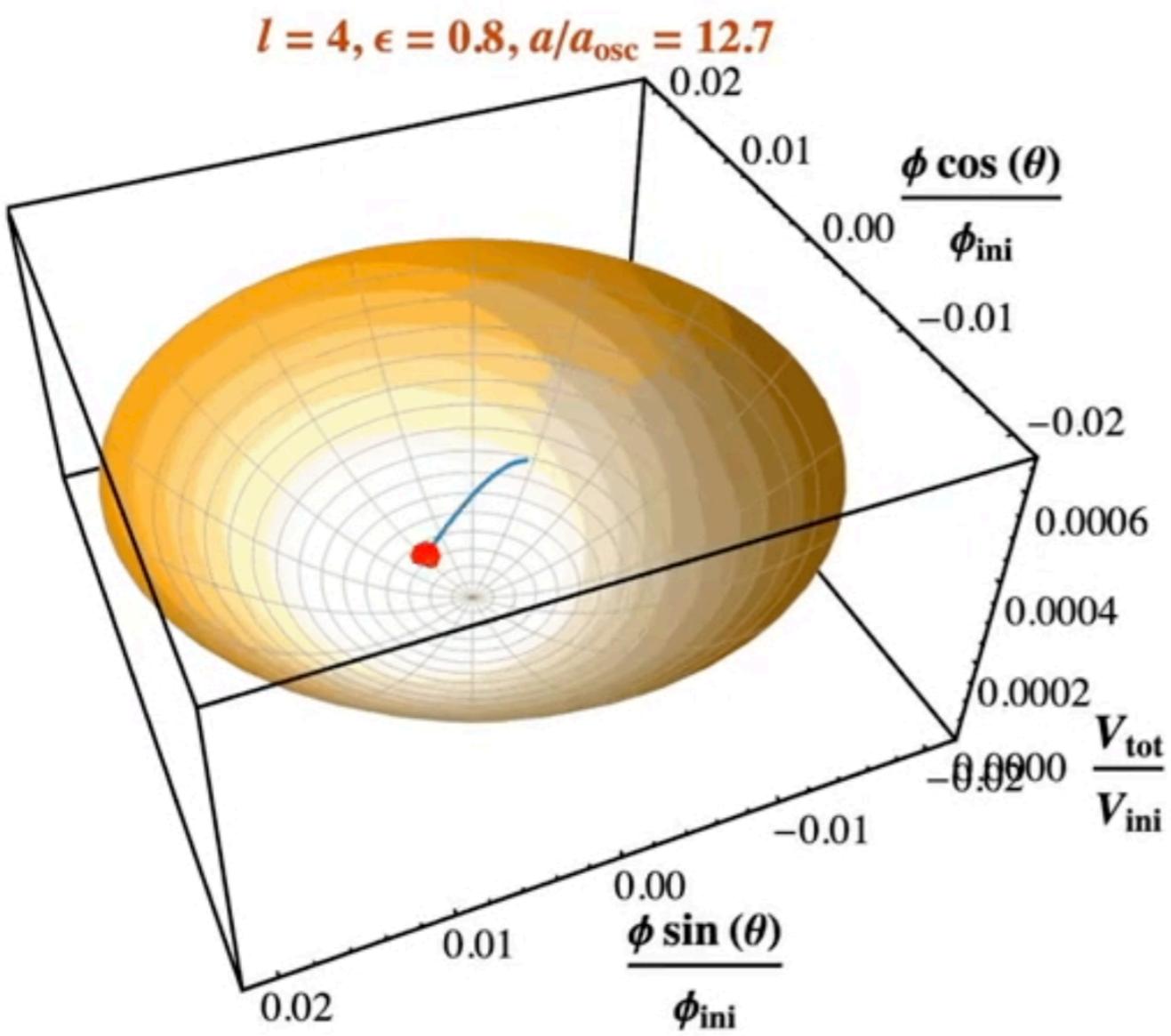


Ingredients IV: radial-motion damping



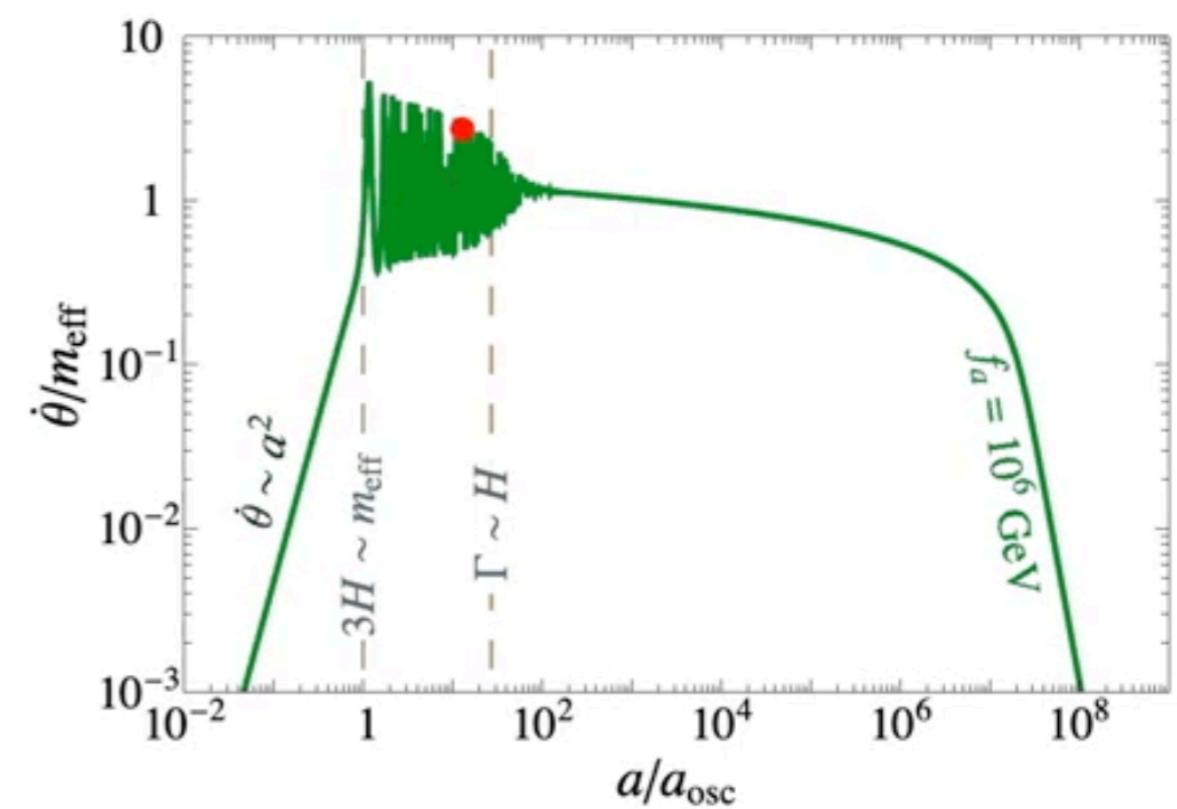
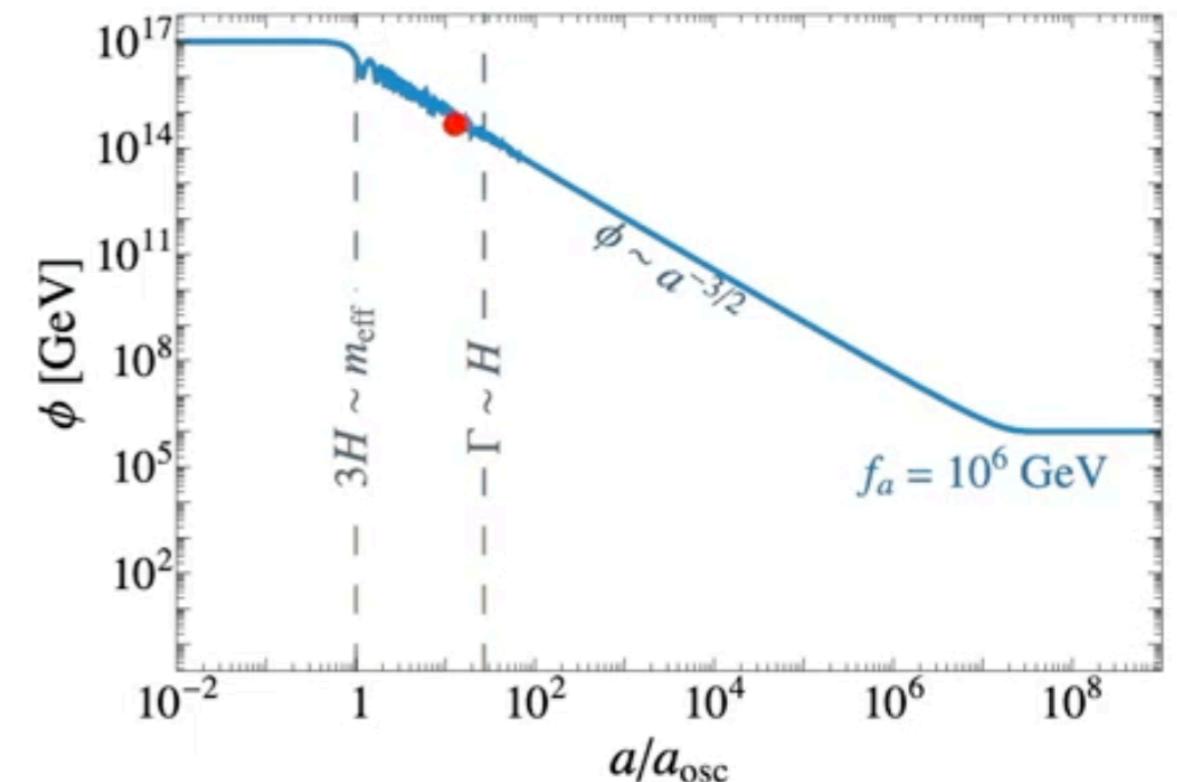
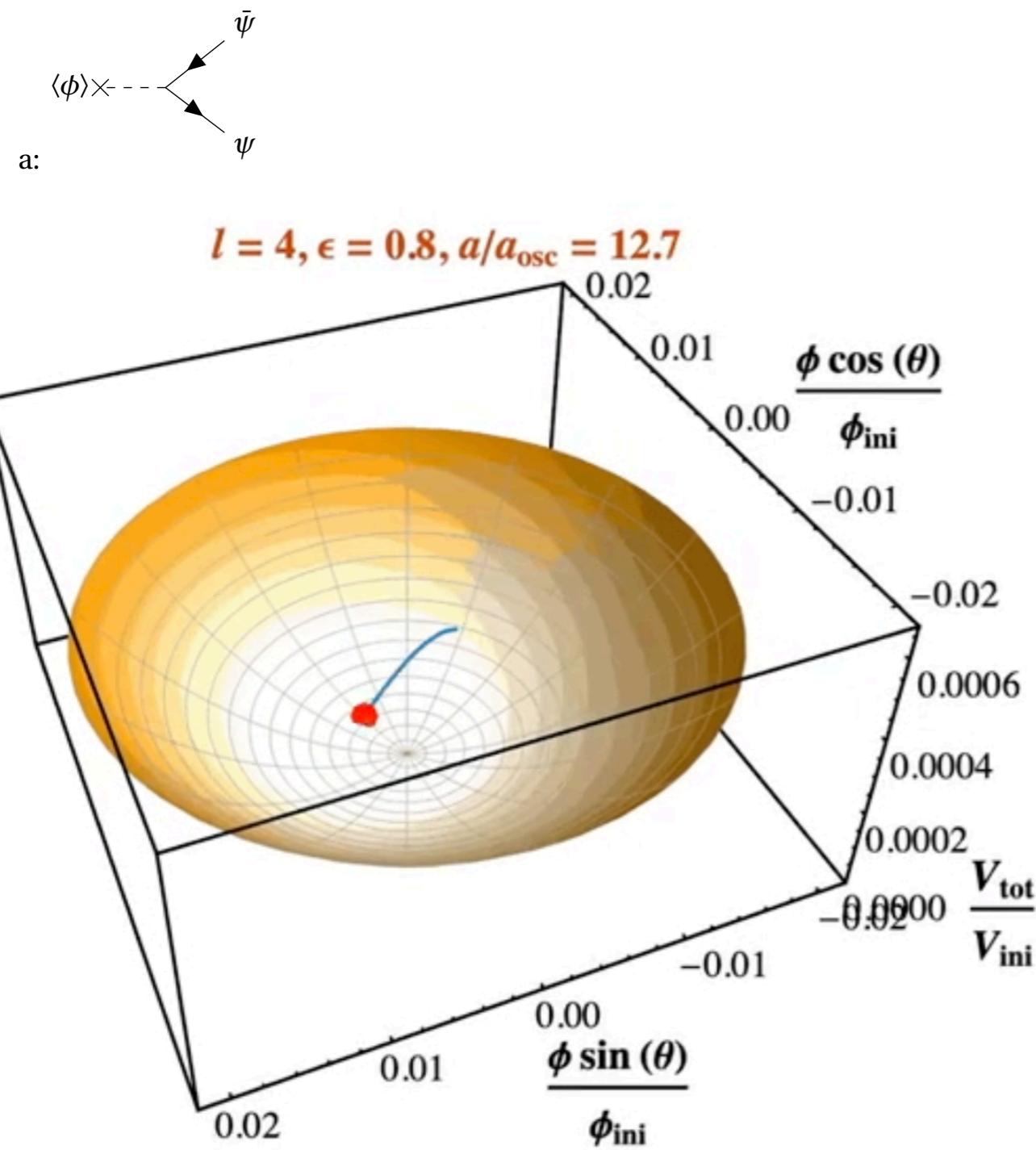
$$V_{\text{int}} = \lambda_\psi \phi \bar{\psi} \psi$$

Ingredients IV: radial-motion damping



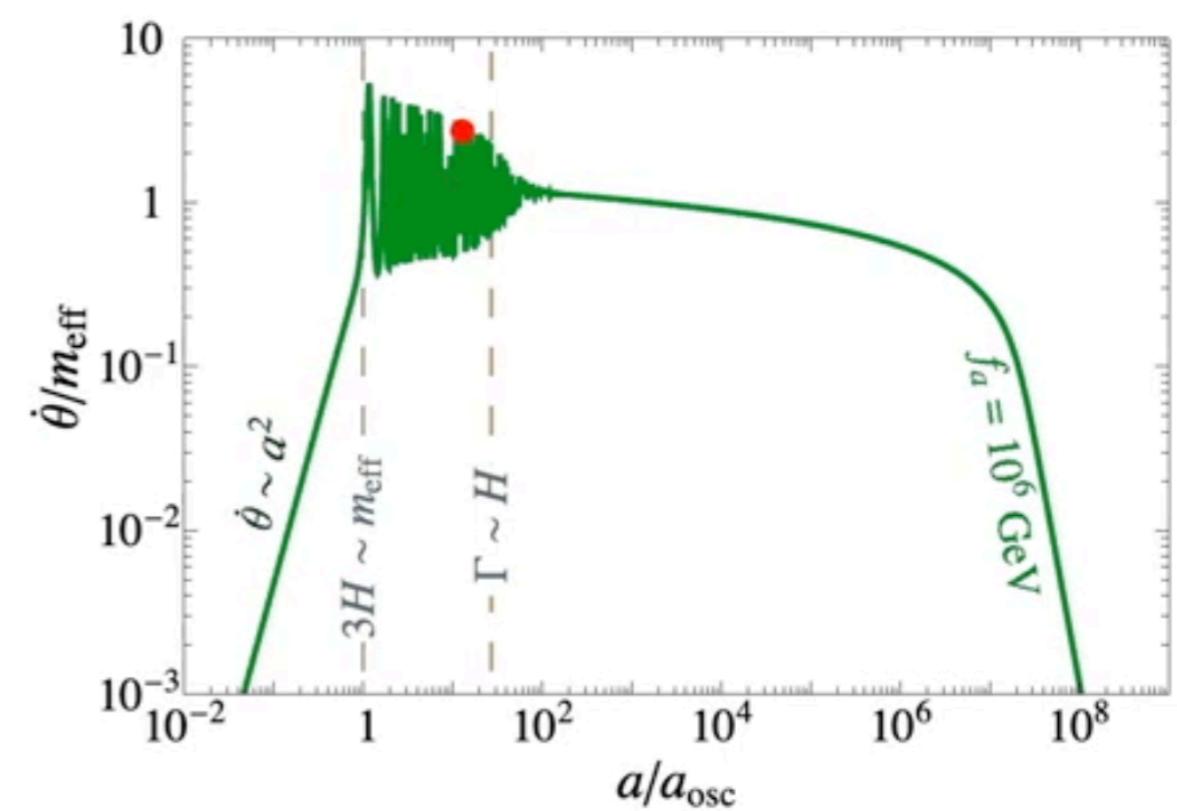
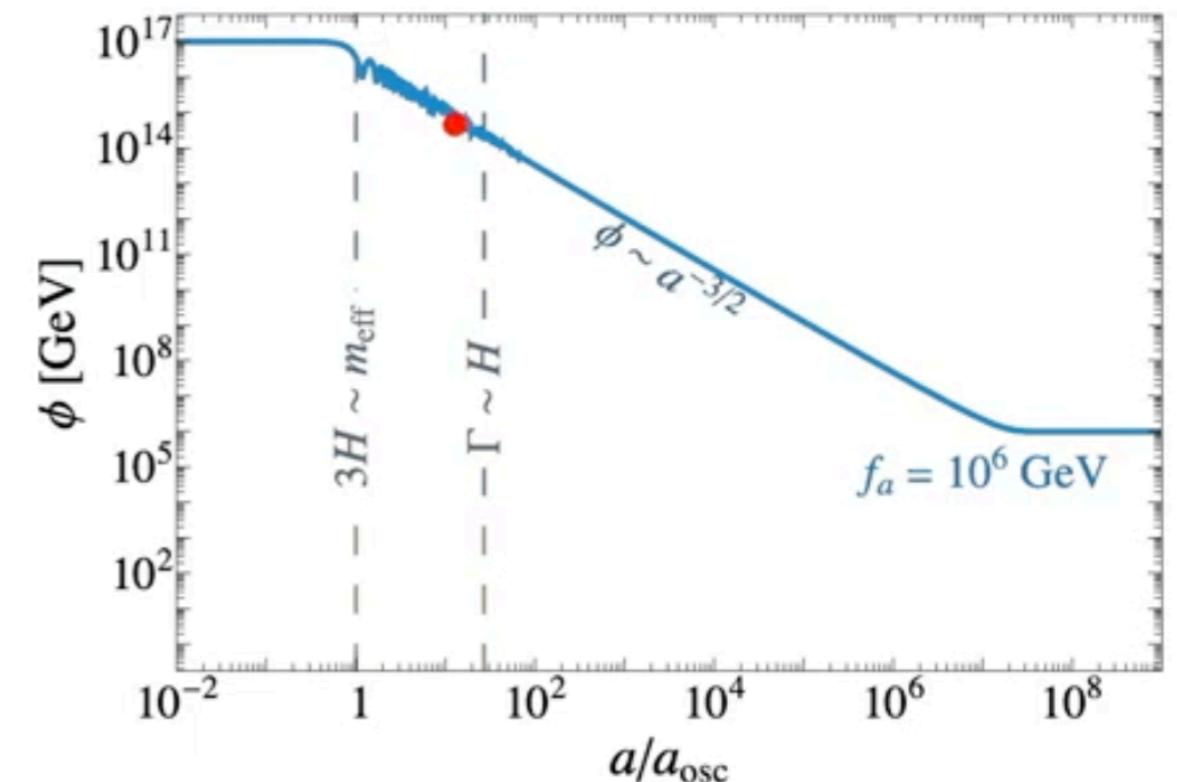
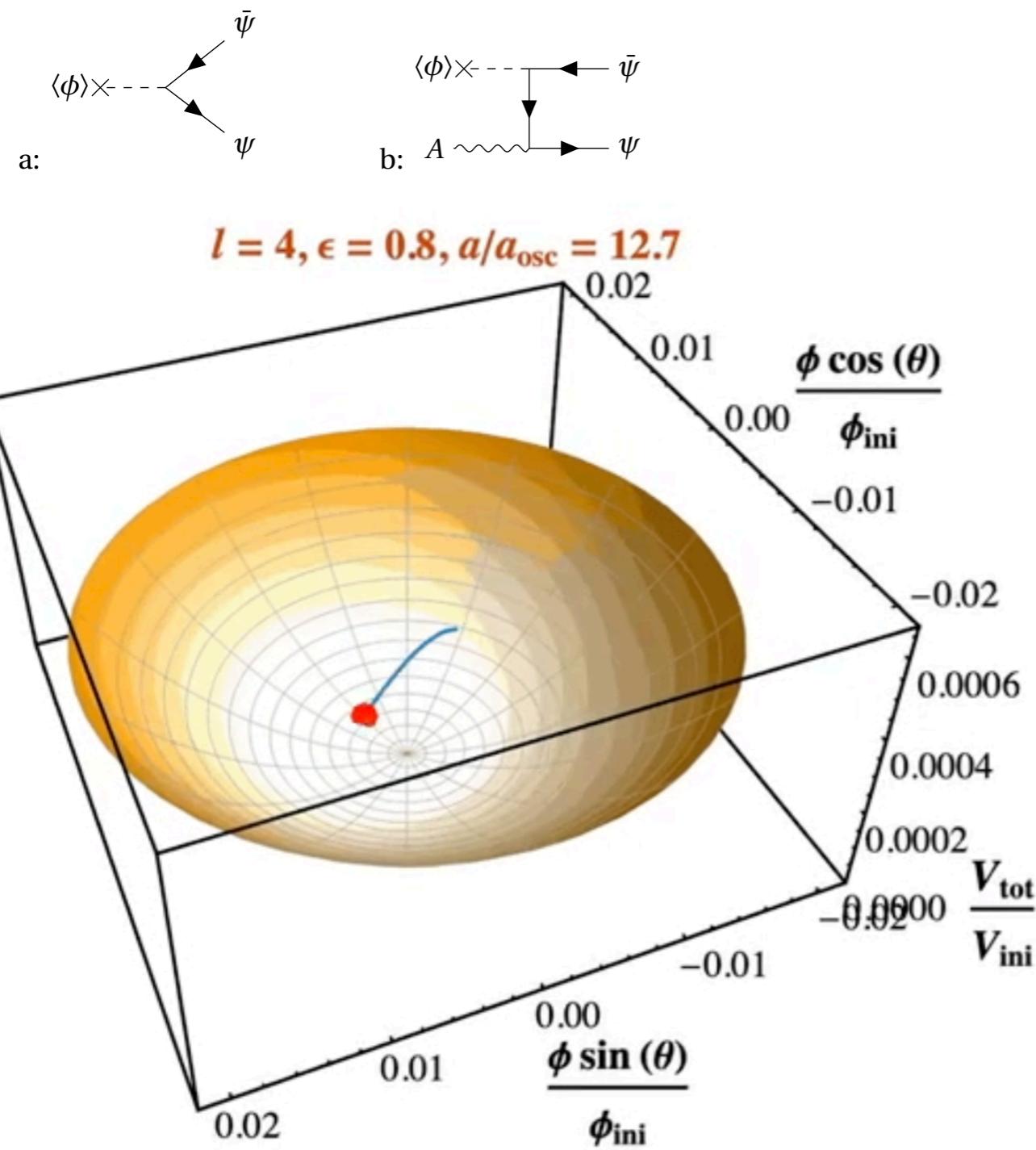
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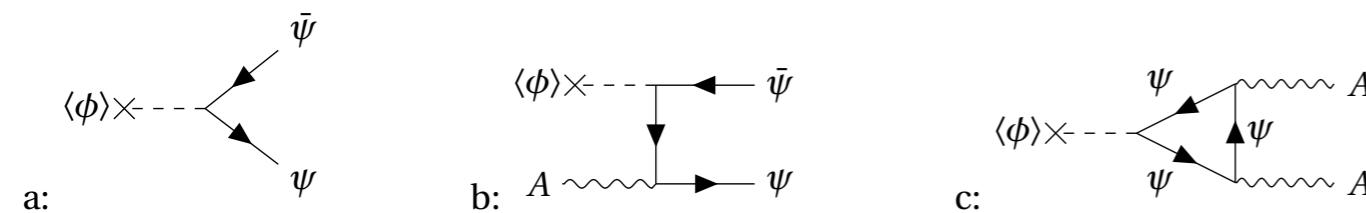
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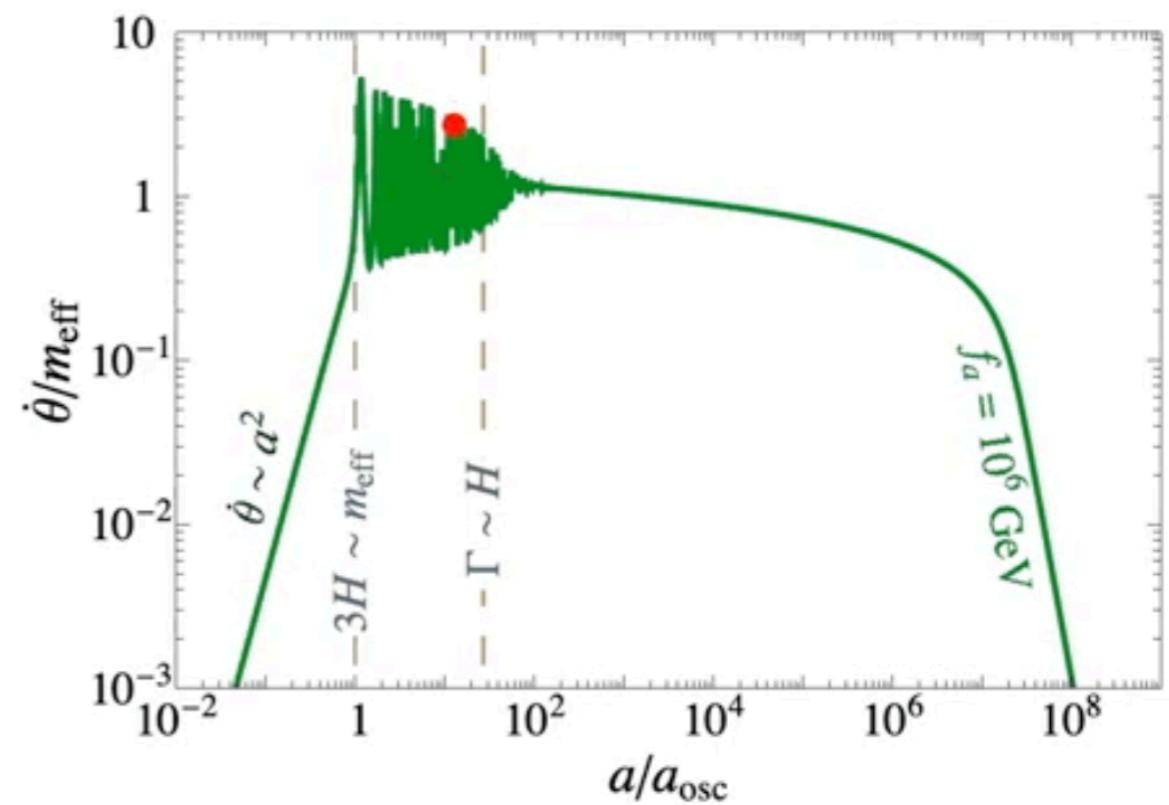
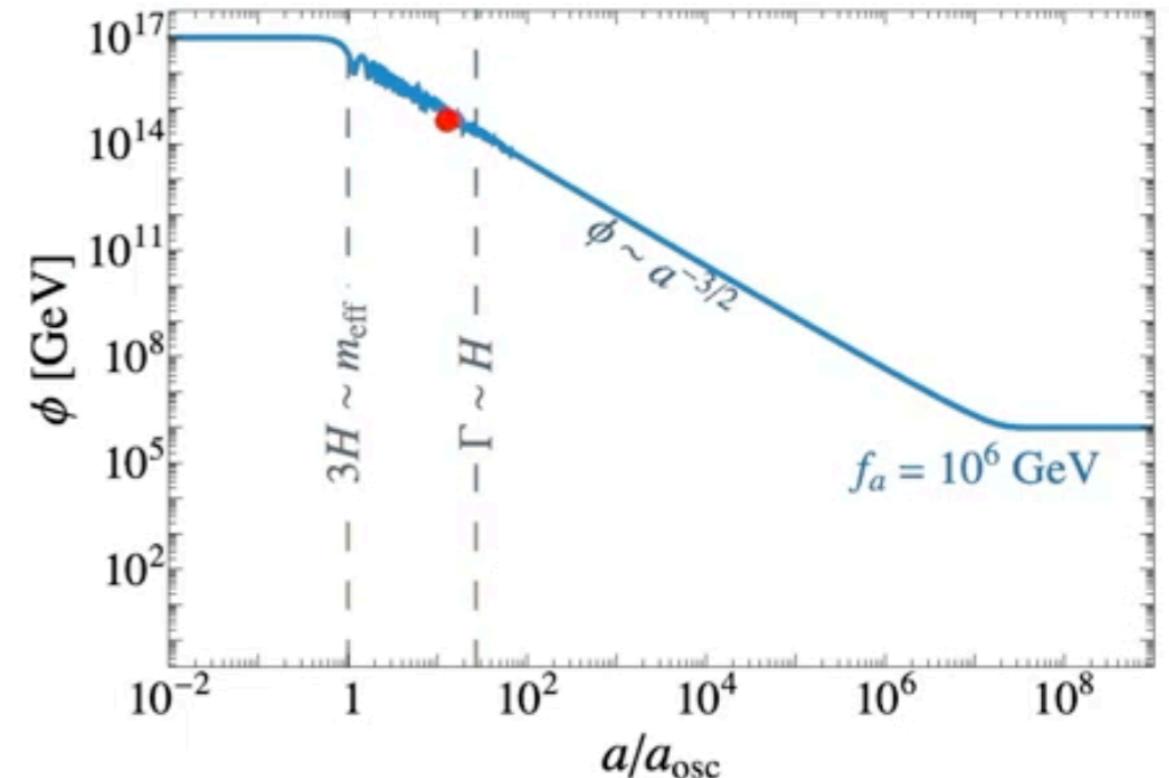
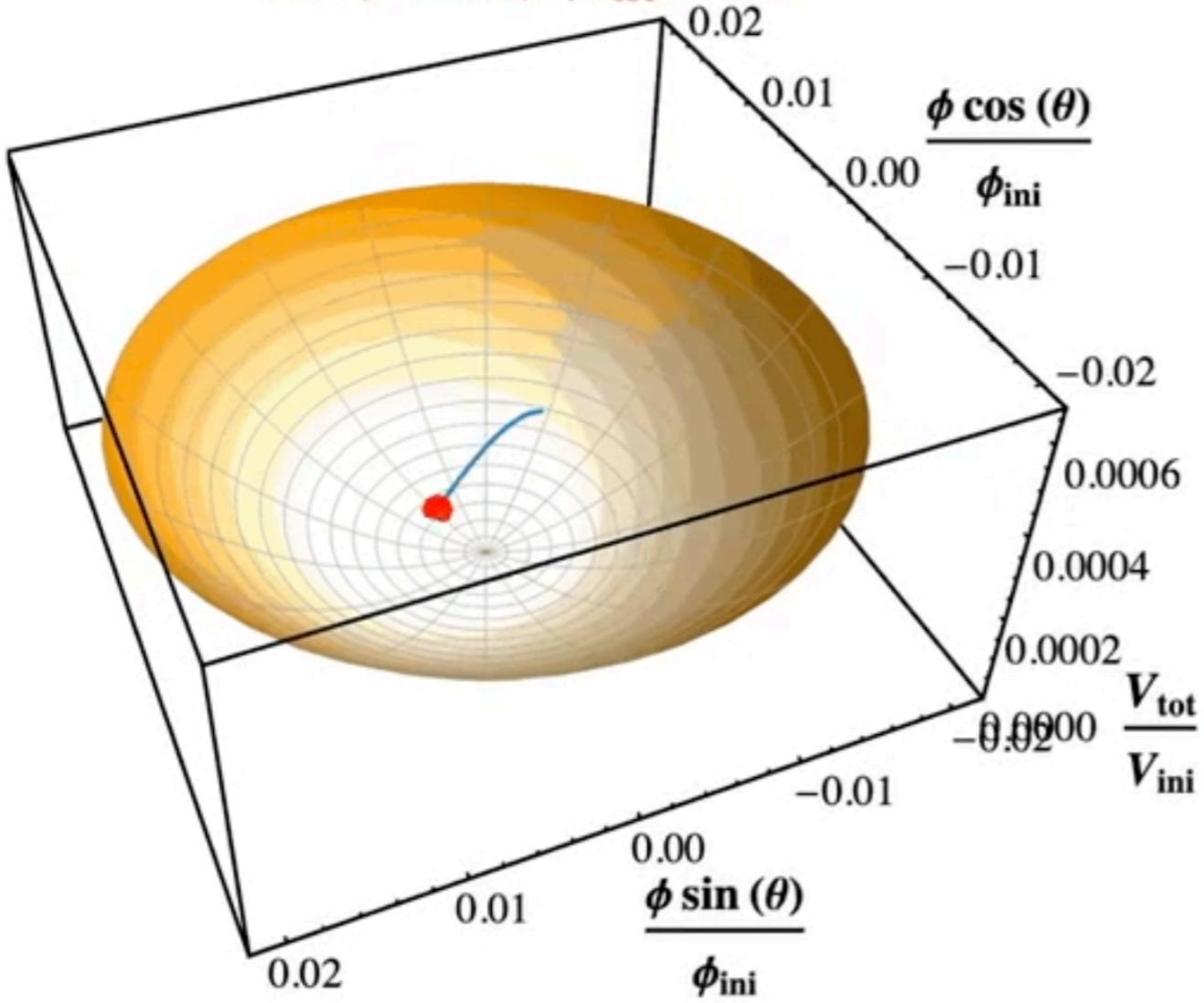


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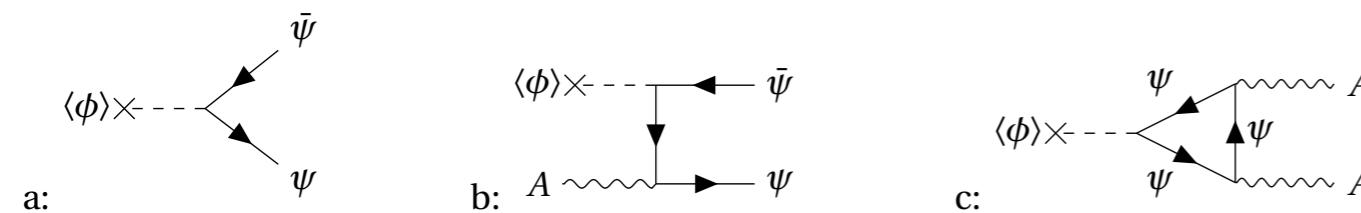


$$l = 4, \epsilon = 0.8, a/a_{\text{osc}} = 12.7$$

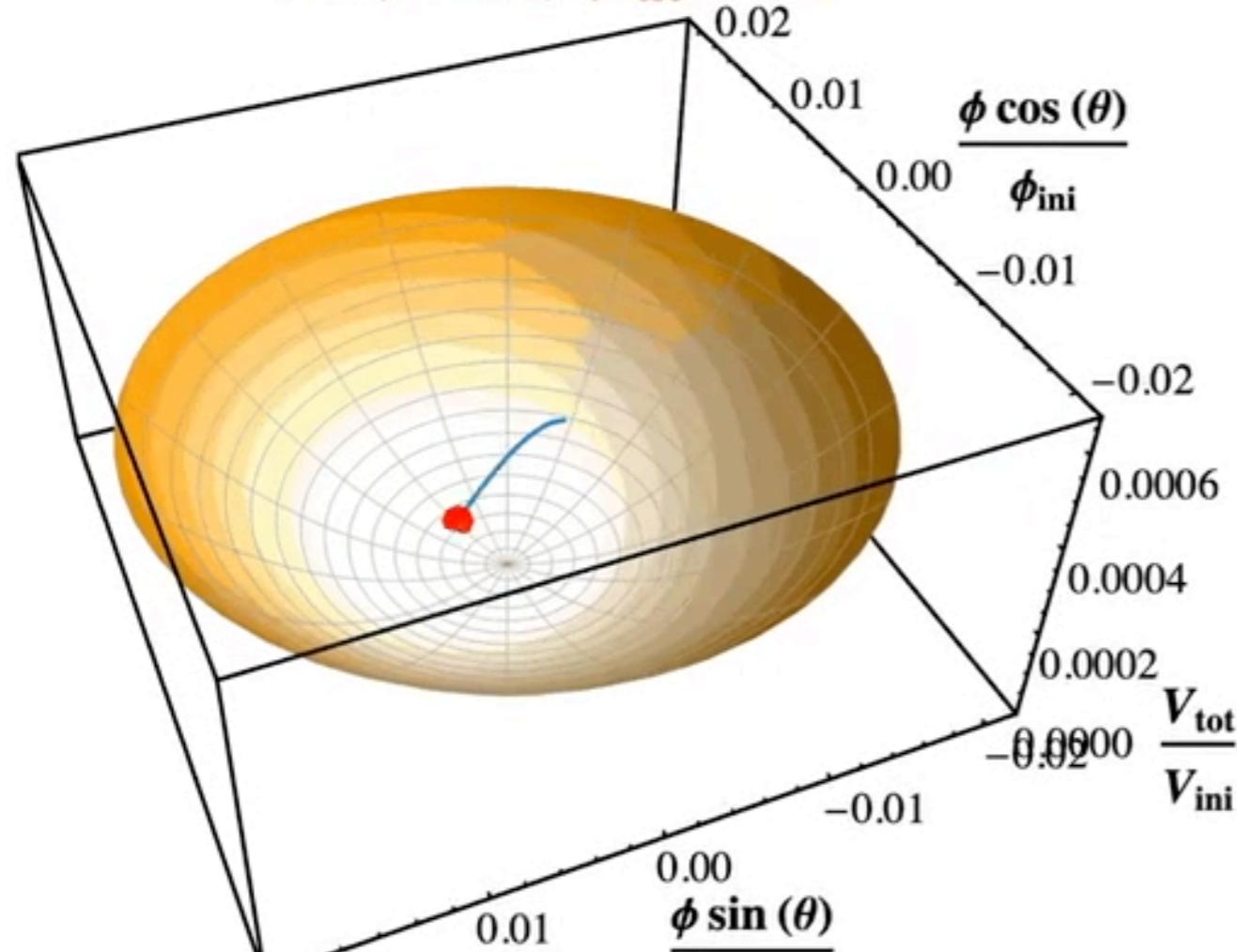


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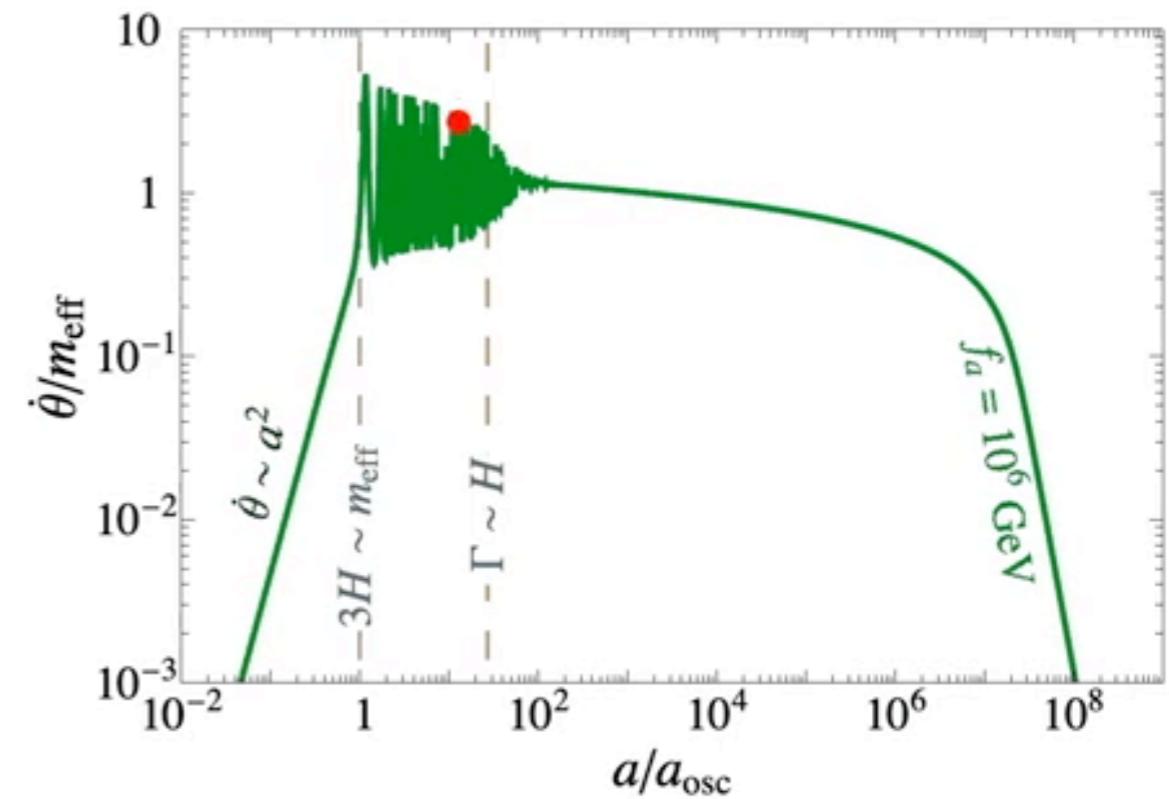
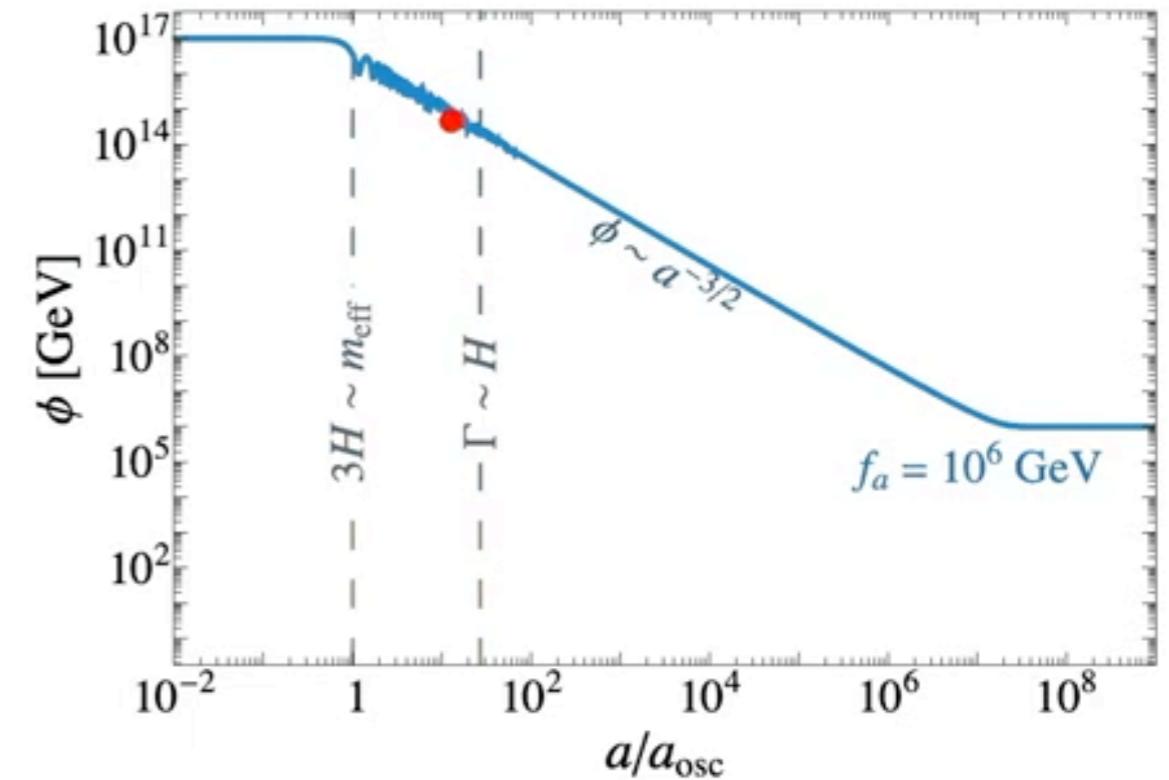


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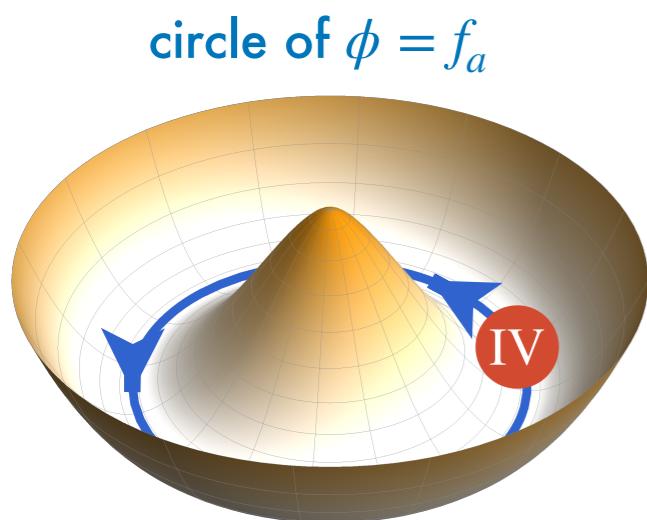


$$\frac{F}{V} = \rho - Ts = \begin{cases} \frac{1}{2}\phi^2\dot{\theta}^2 - \#T^4, & (\text{U(1) charge remains in the condensate}) \\ \#\frac{\phi^4\dot{\theta}^2}{T^2} - \#T^4, & (\text{U(1) charge transferred to the plasma}) \\ (\rho \supset \mu n \text{ with } \mu = n/T^2 \text{ and } n = \phi^2\dot{\theta}) \end{cases}$$

If $\phi \gg T \implies \text{U(1) charge remains in the condensate}$



After reaching the bottom \Rightarrow kination era



Axion speed $\dot{\theta} \sim m_r$ (from $V''(\phi) \sim \dot{\theta}^2 \phi$)

$$\frac{d}{dt}(a^3 \phi^2 \dot{\theta}) = 0 \Rightarrow \dot{\theta} \propto a^{-3}$$

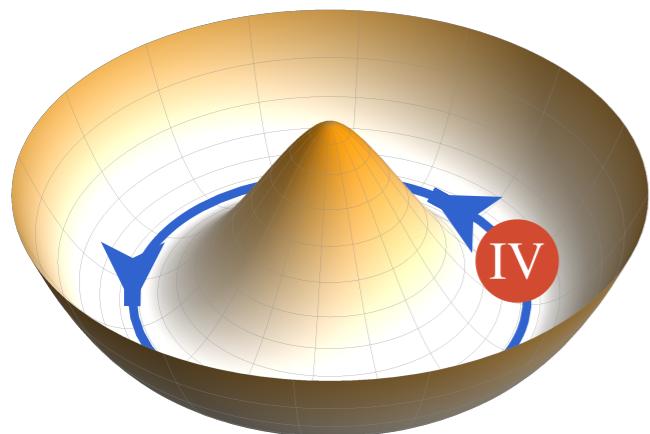
Kinetic energy dominates

$$\rho_\Phi = KE \propto \dot{\theta}^2 \propto a^{-6}$$

and behaves as **kination**.

After reaching the bottom \Rightarrow kination era

circle of $\phi = f_a$



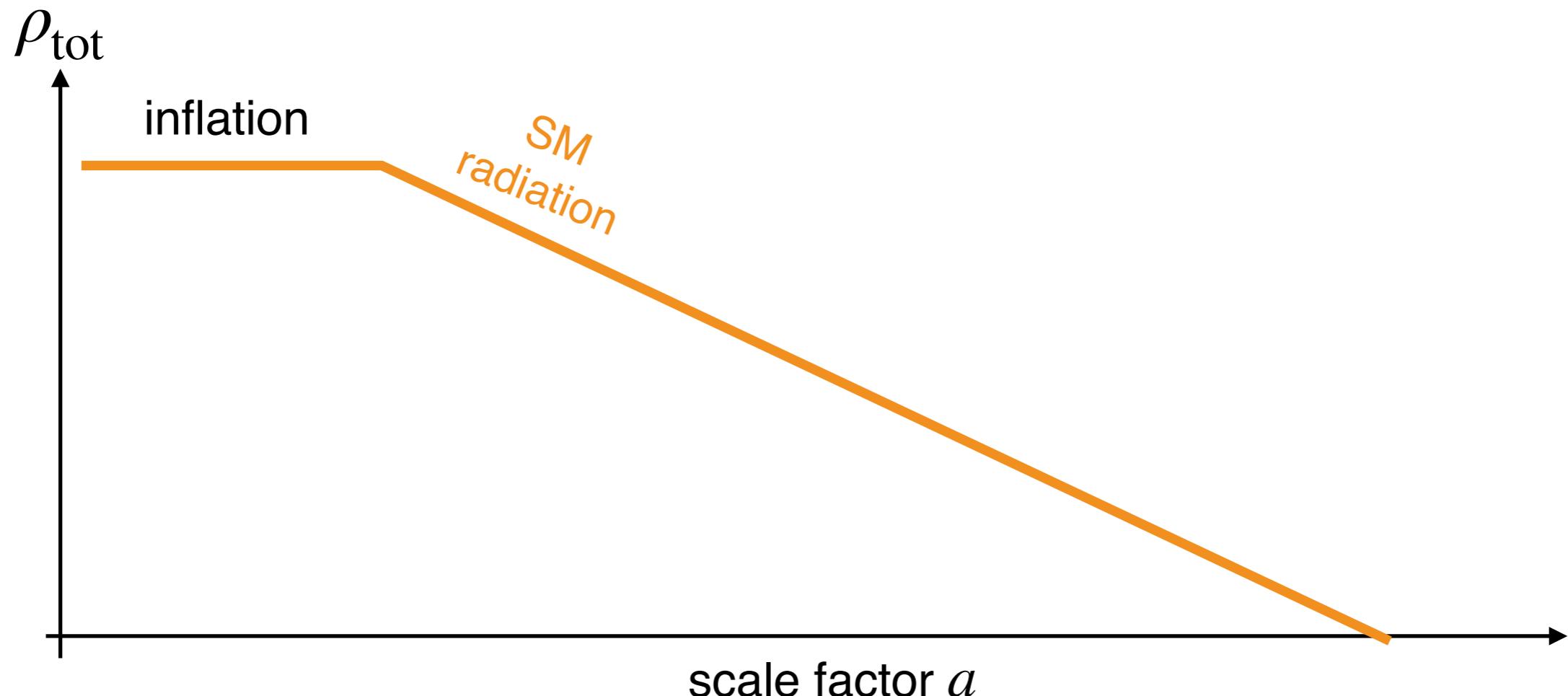
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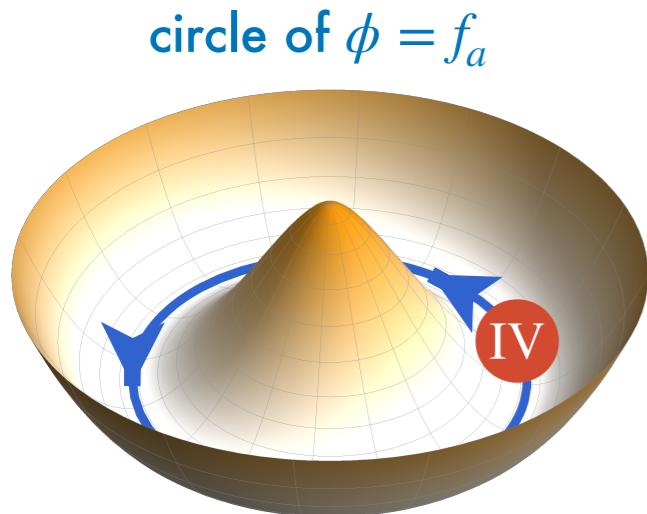
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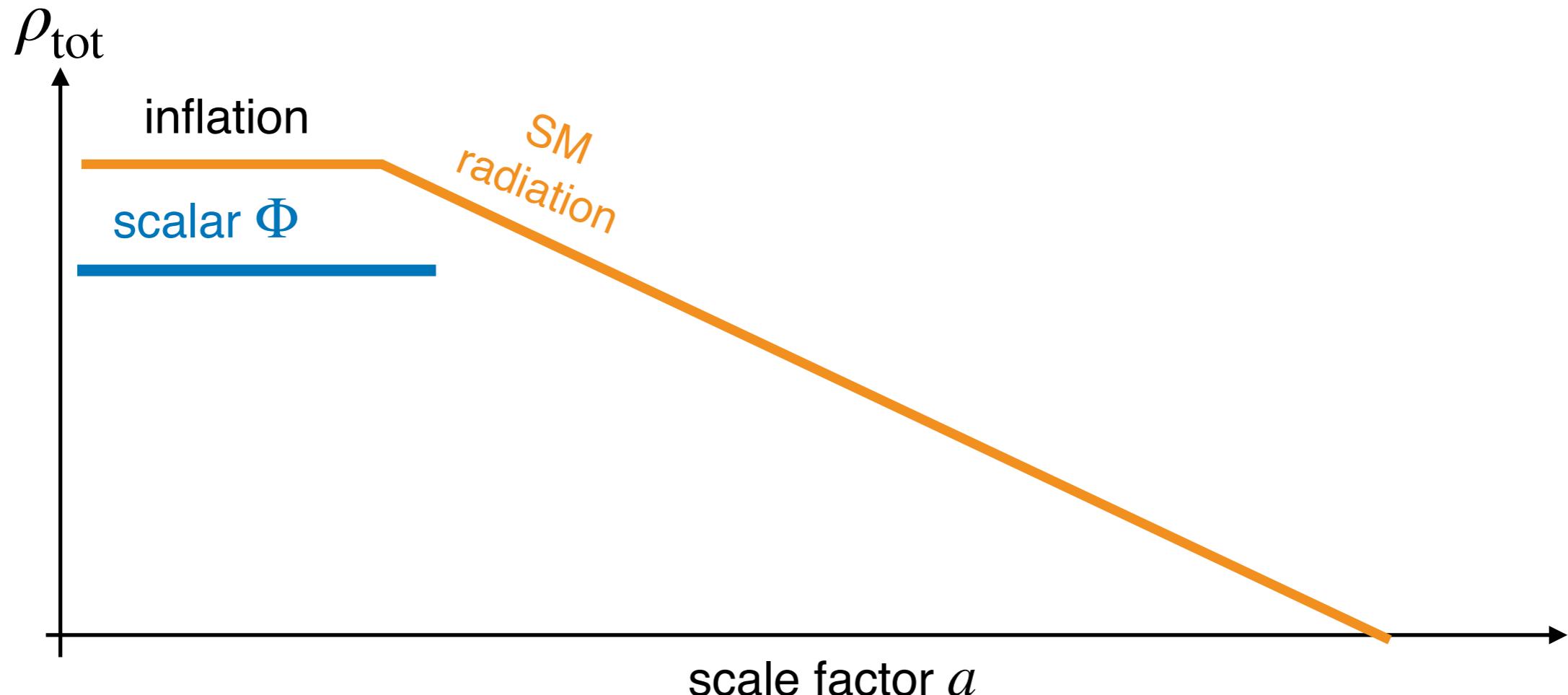
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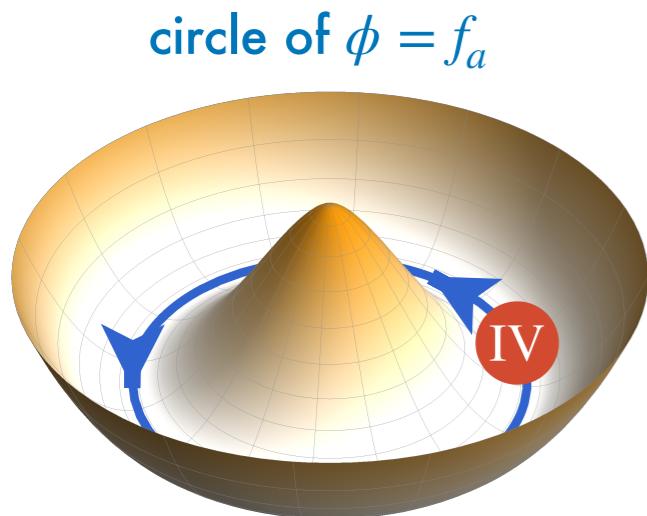
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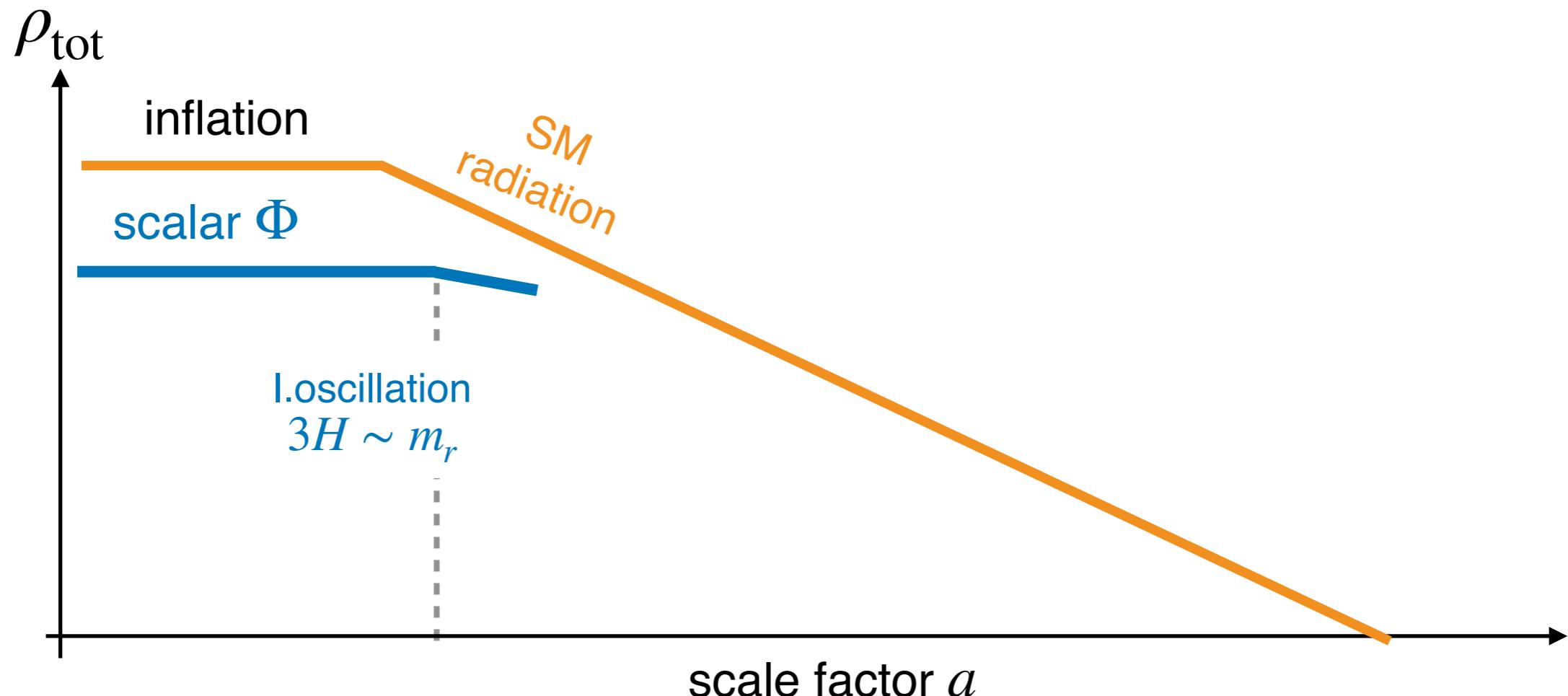
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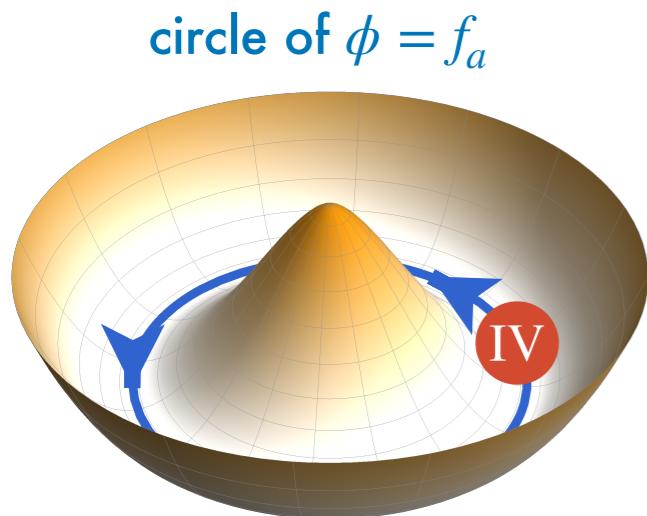
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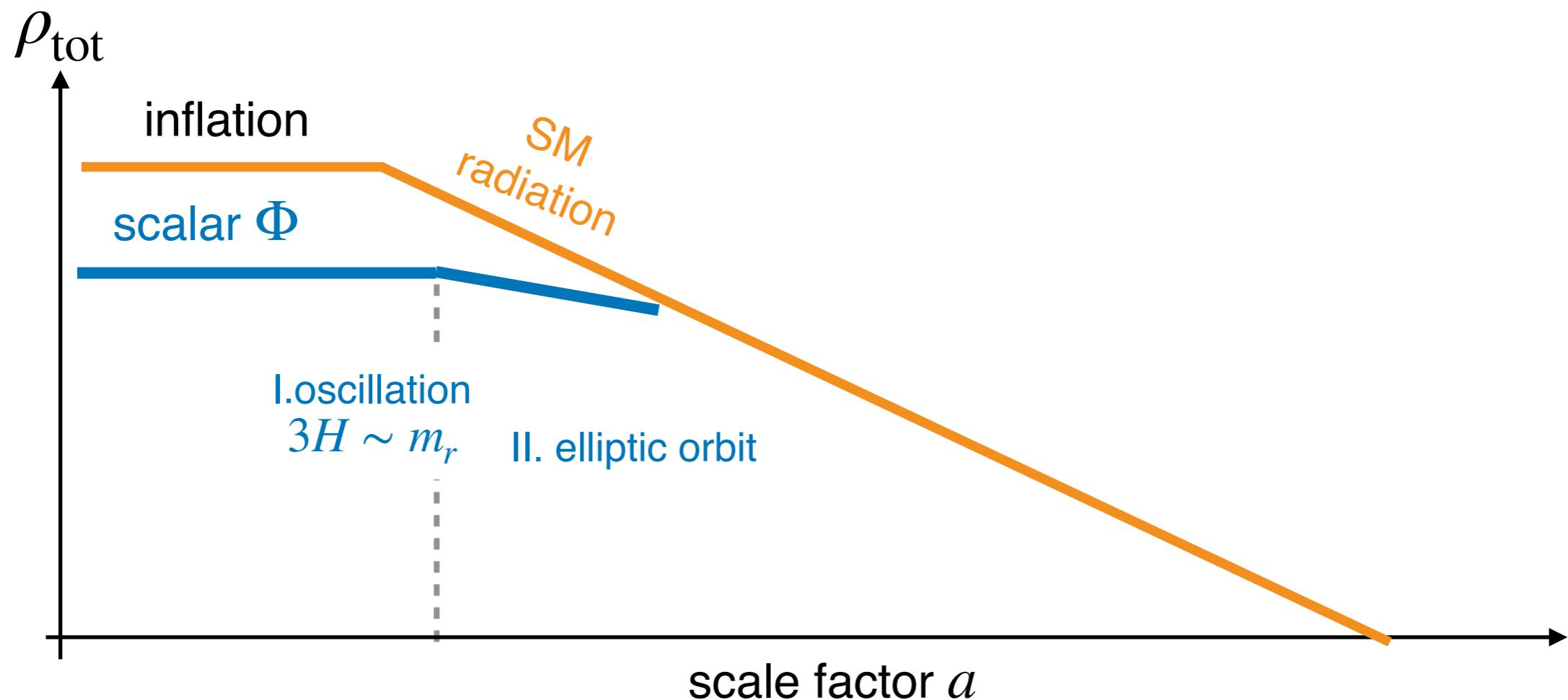
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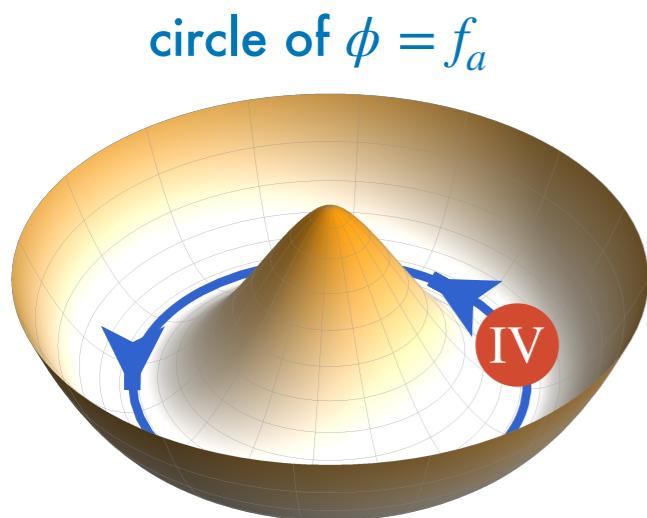
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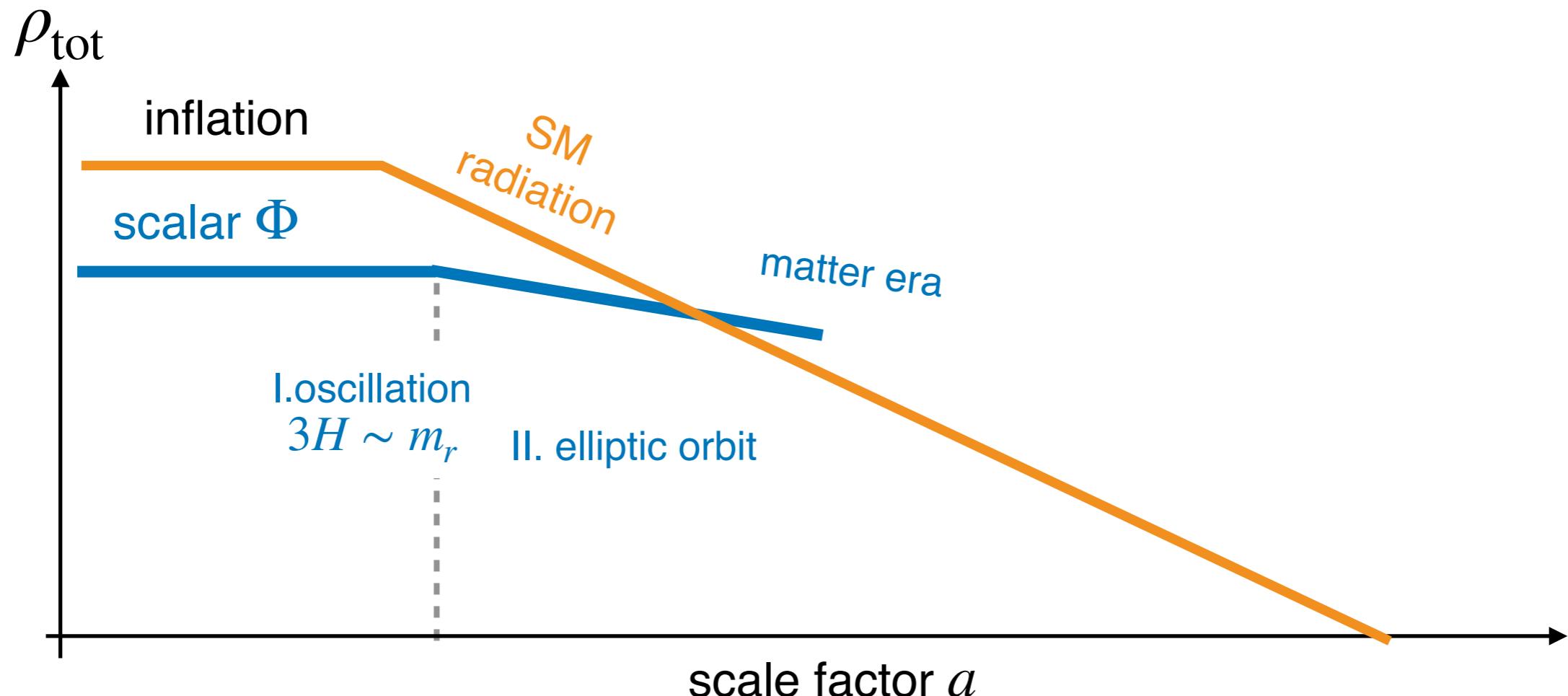
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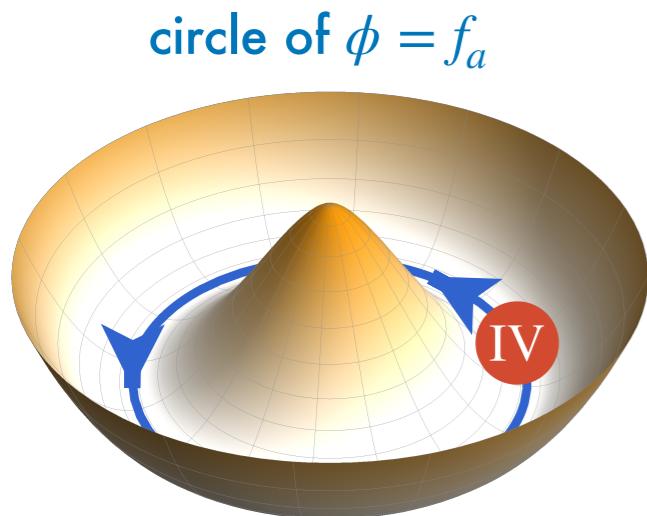
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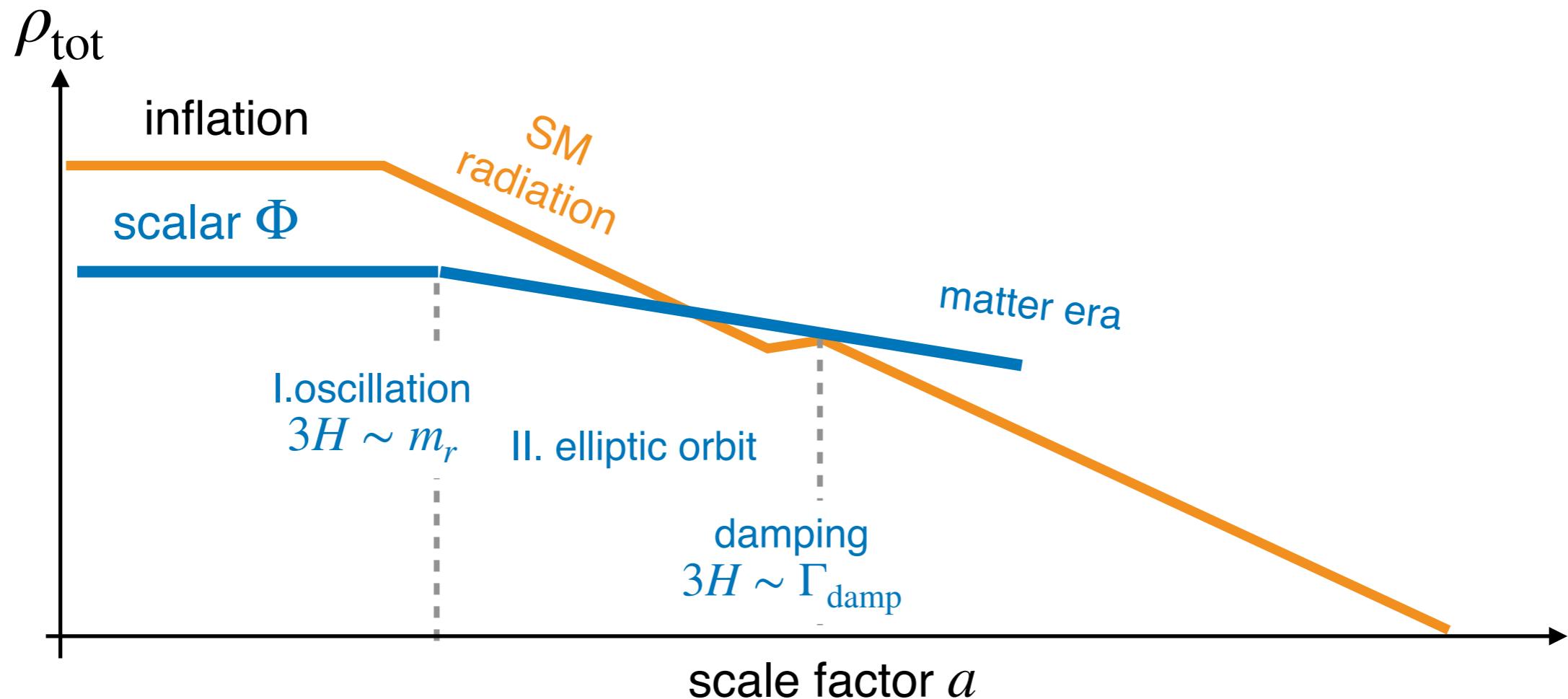
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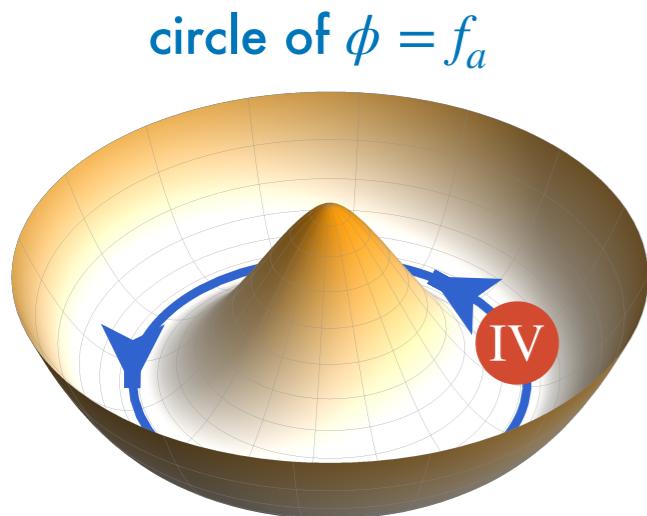
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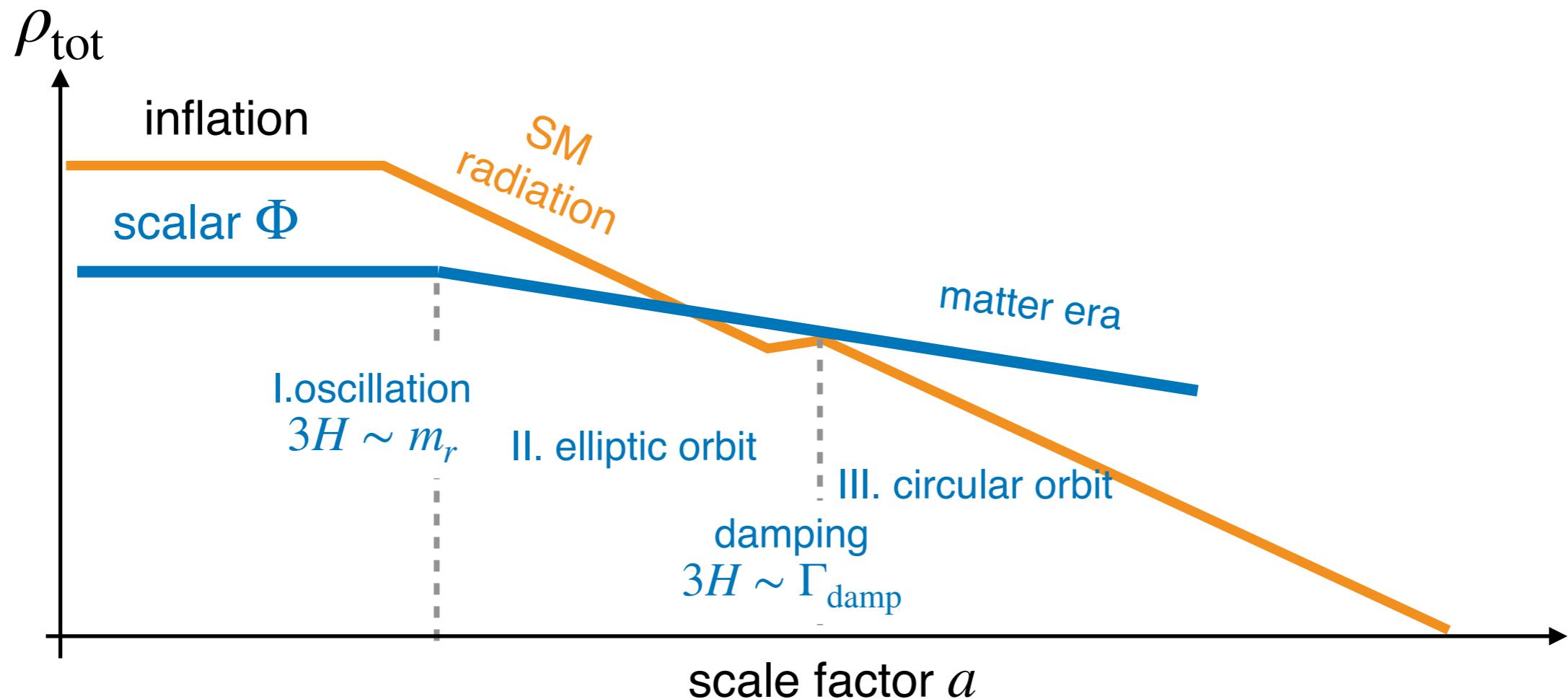
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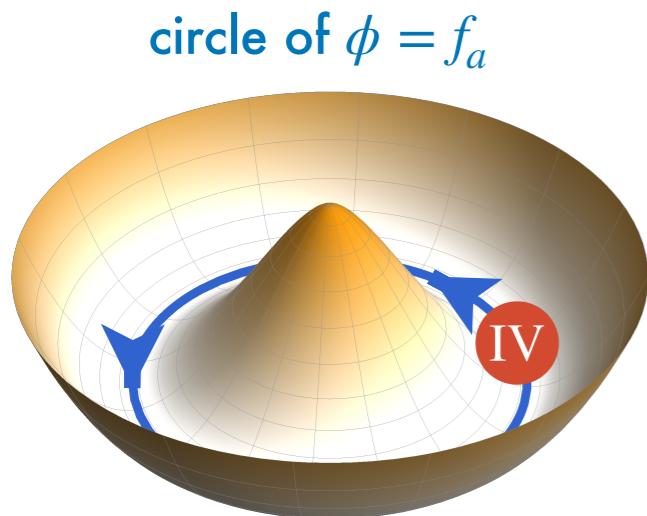
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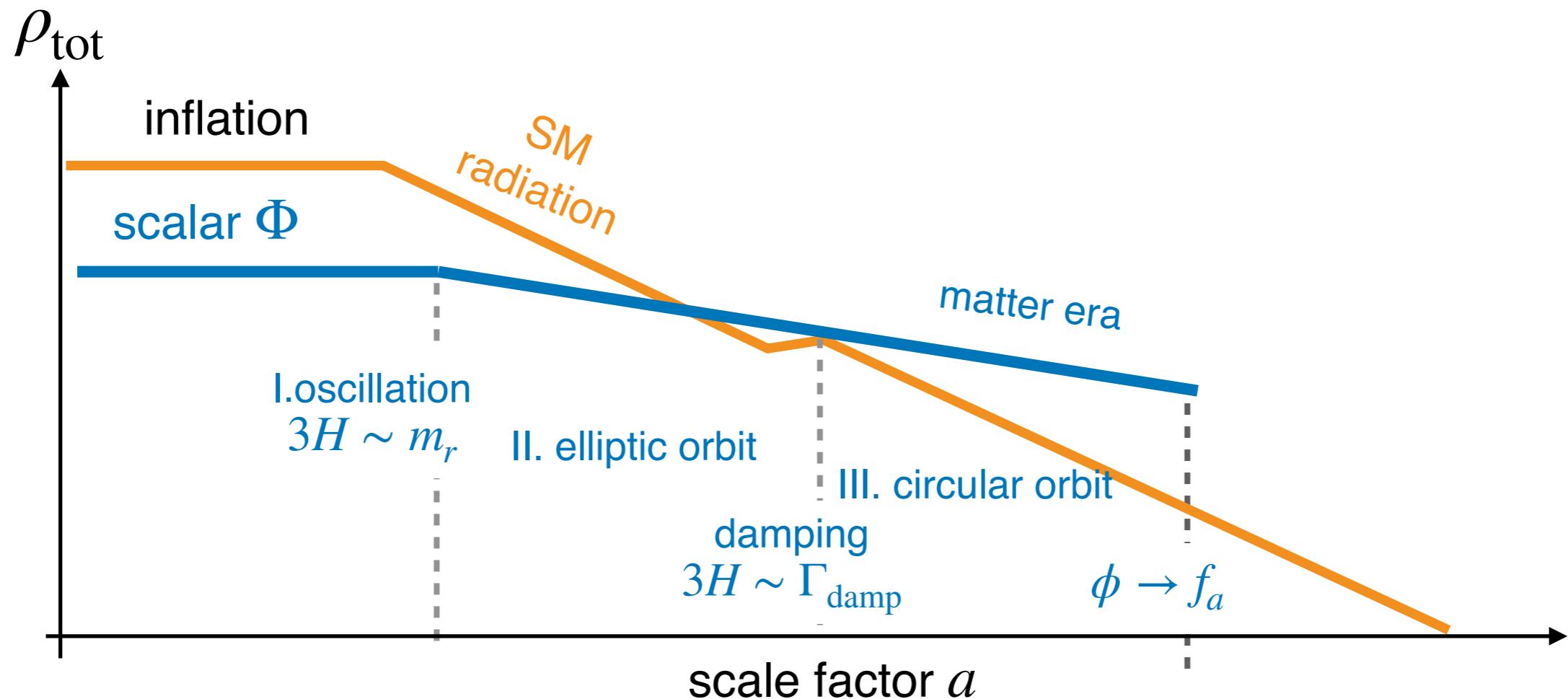
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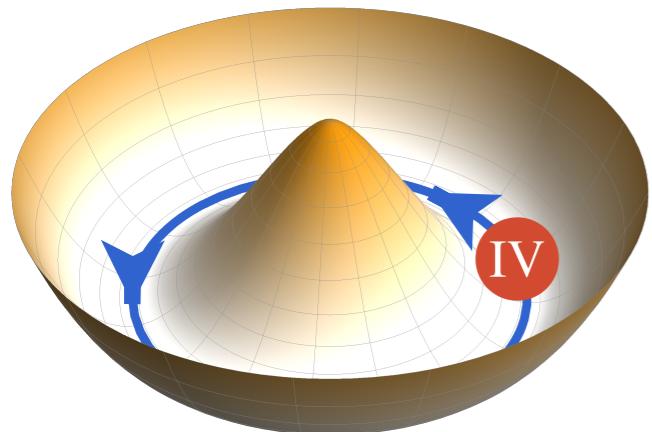
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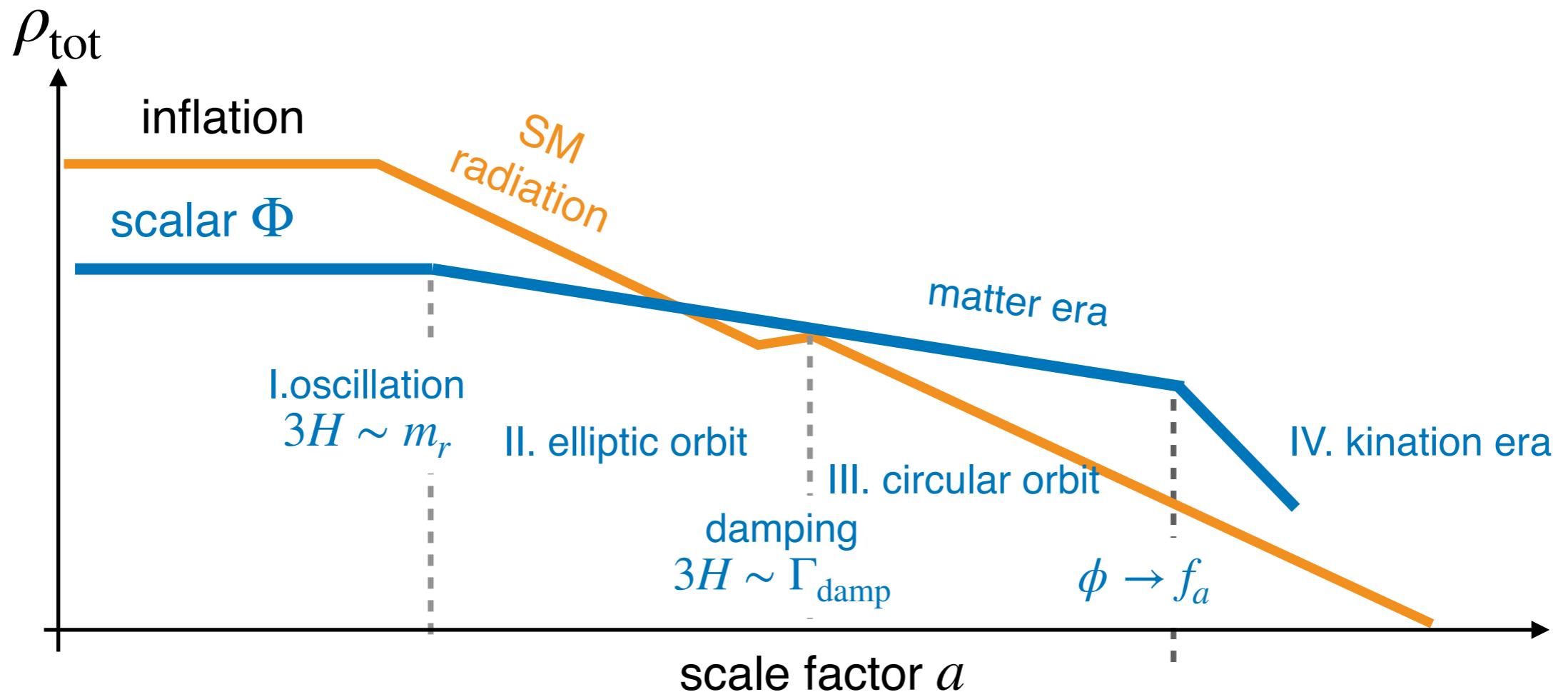
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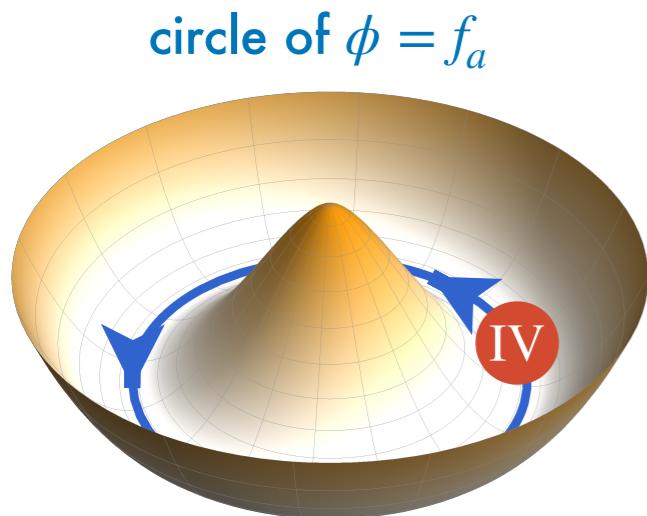
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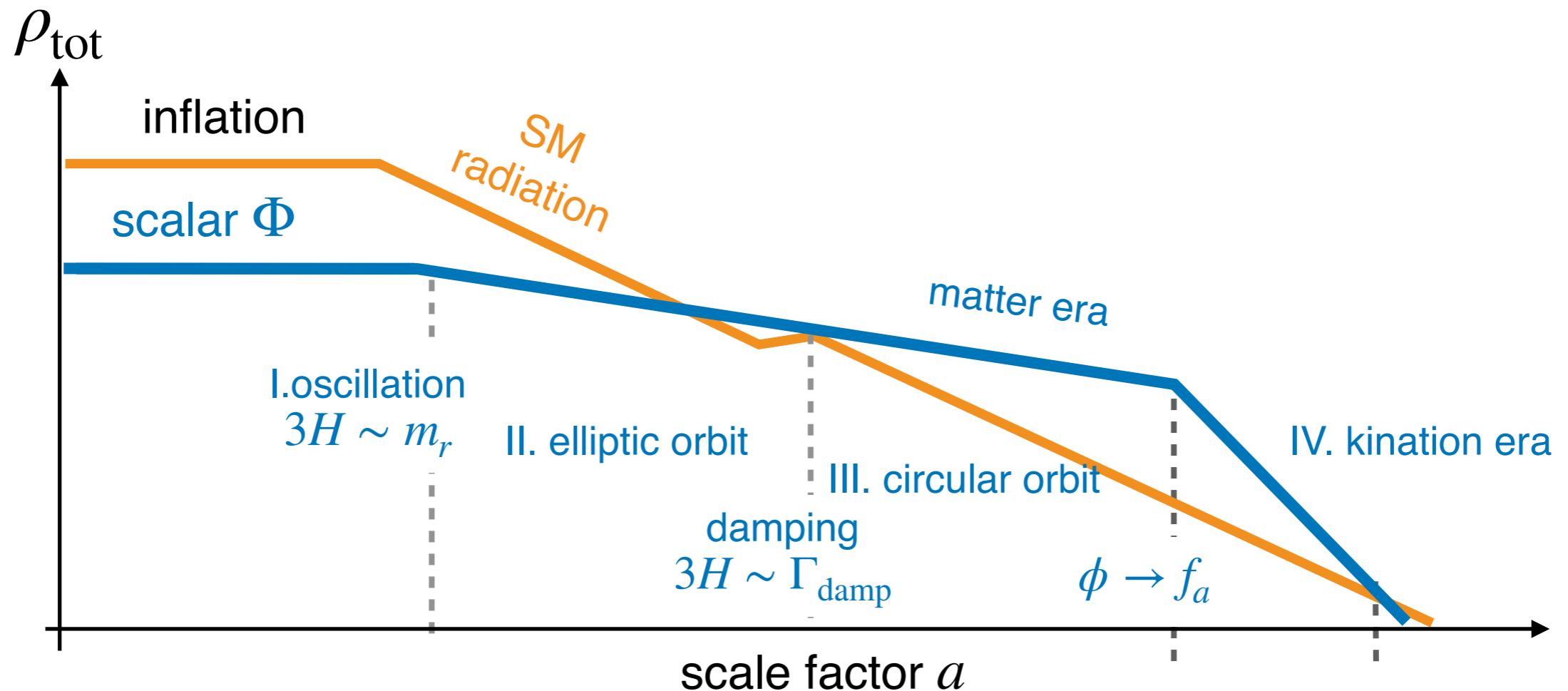
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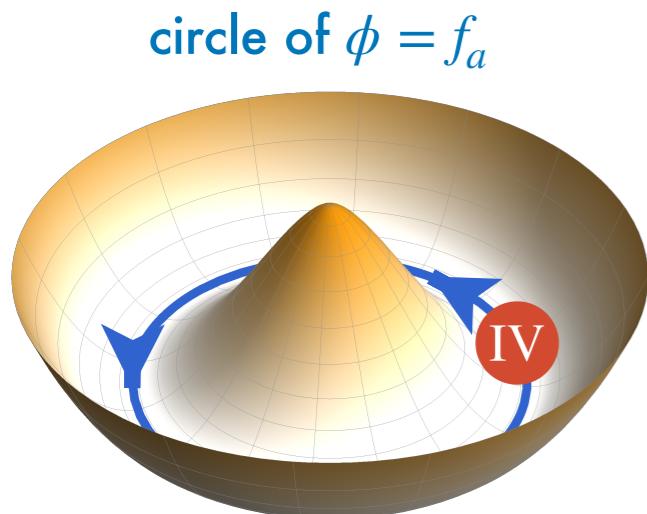
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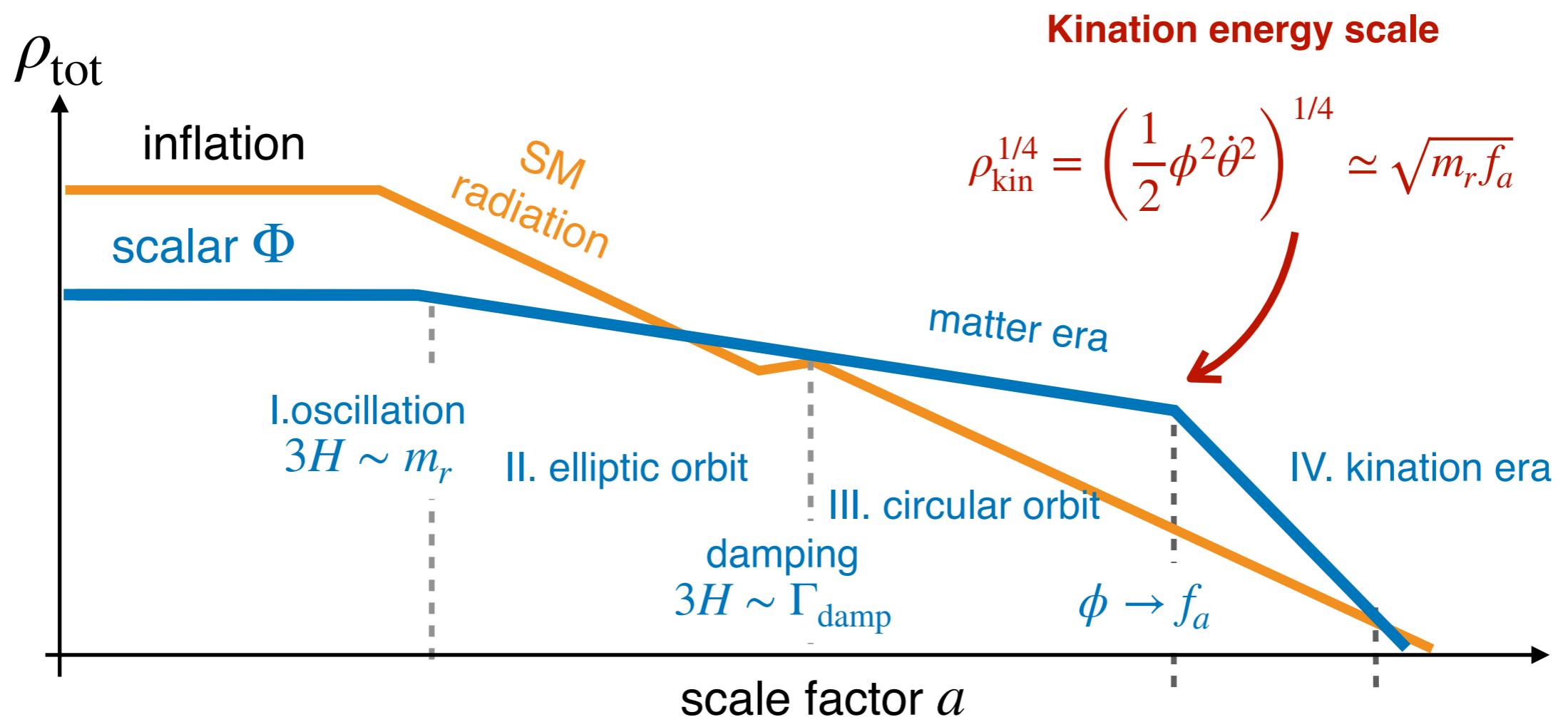
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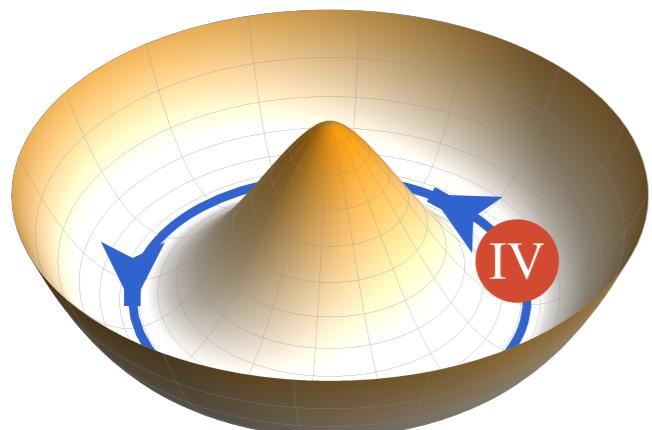
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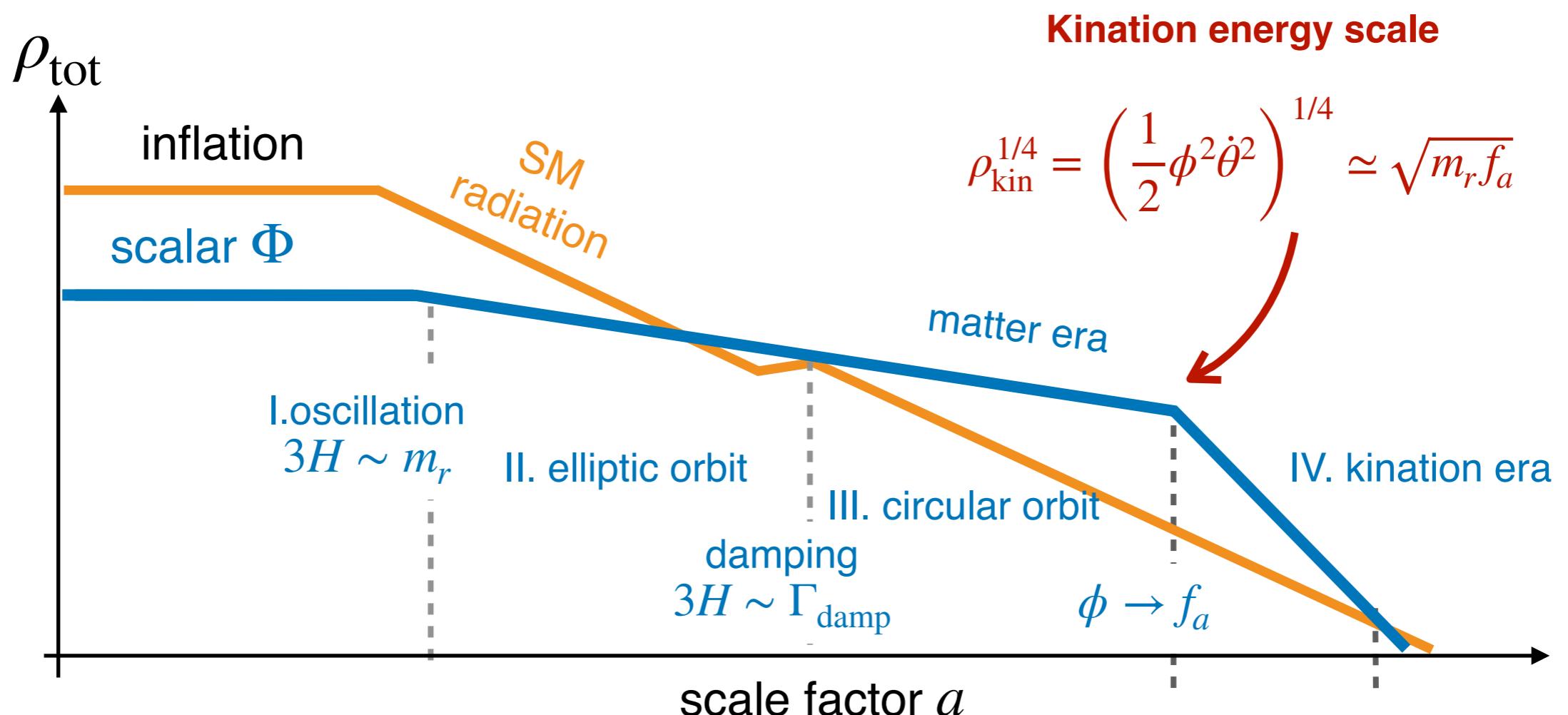
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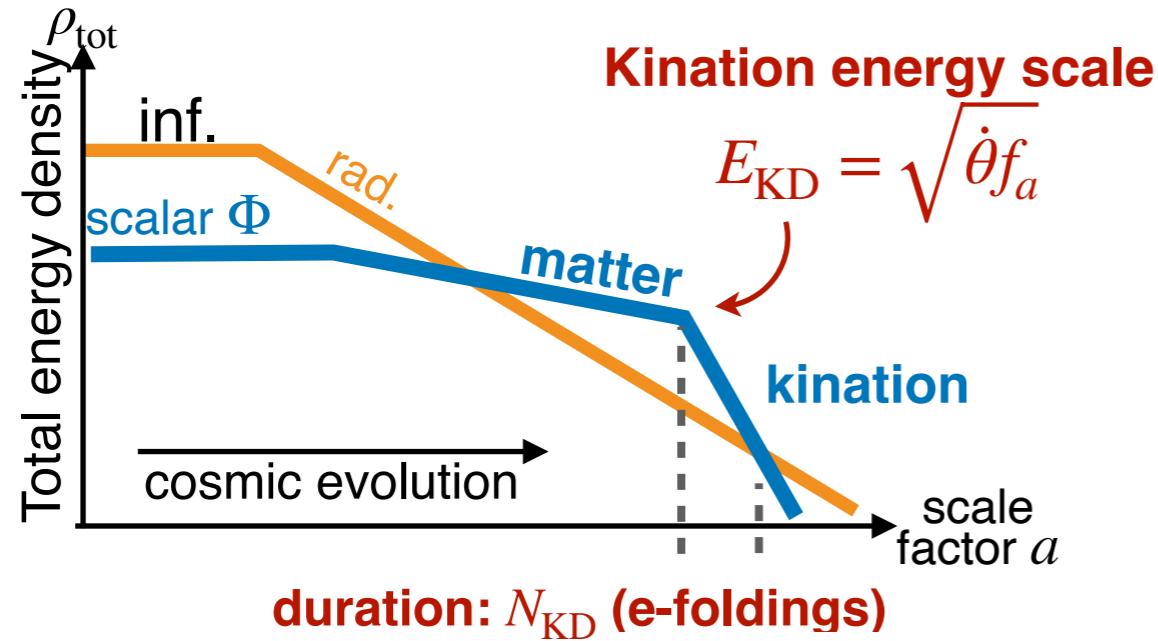
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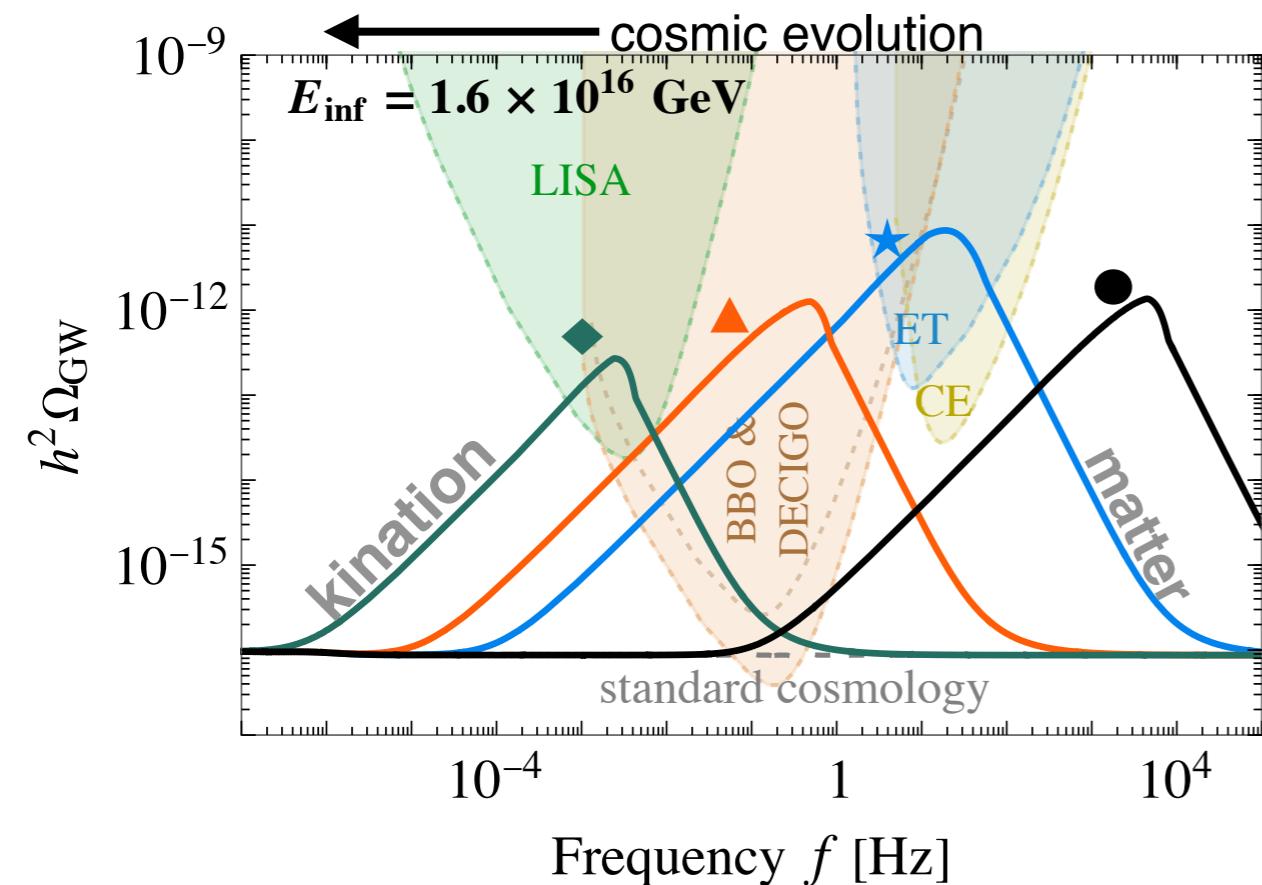
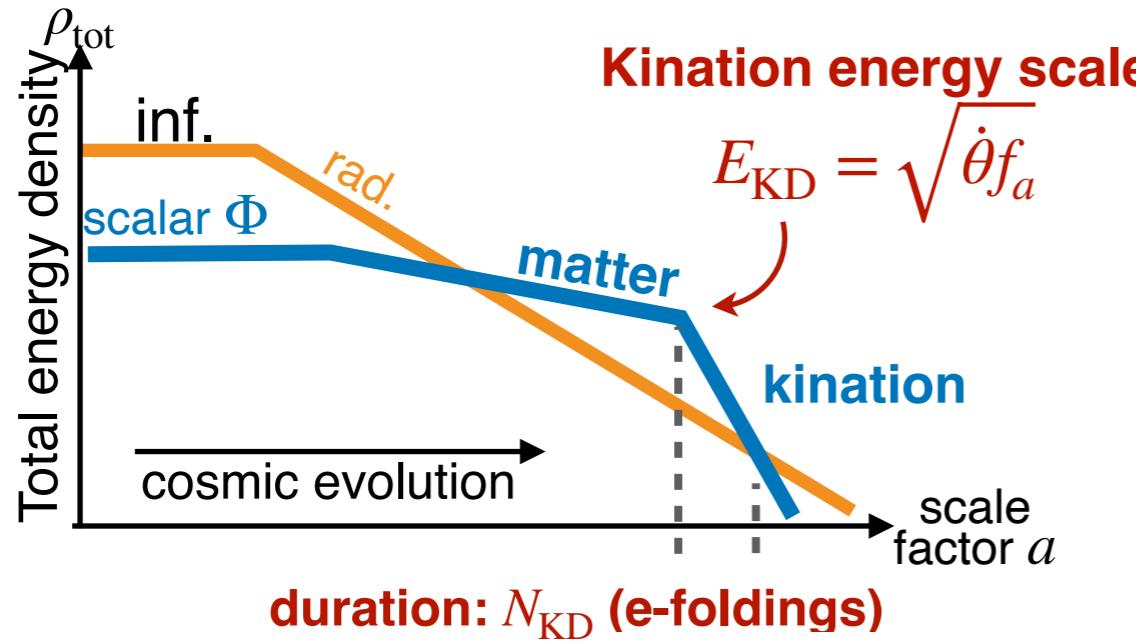
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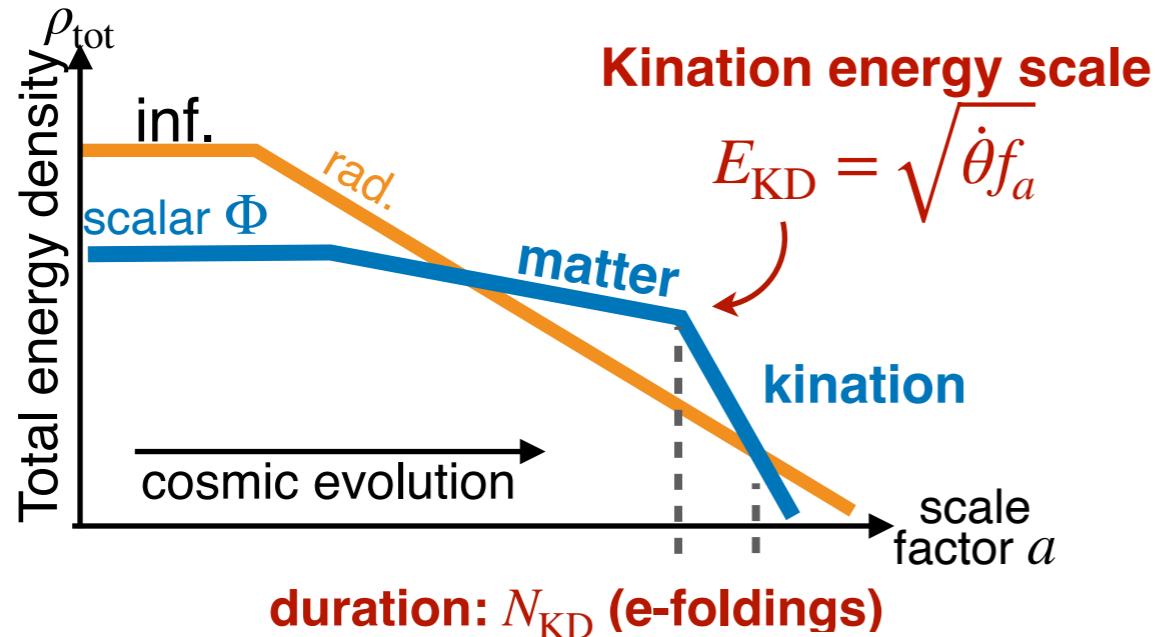
GW signature: a “Peak”



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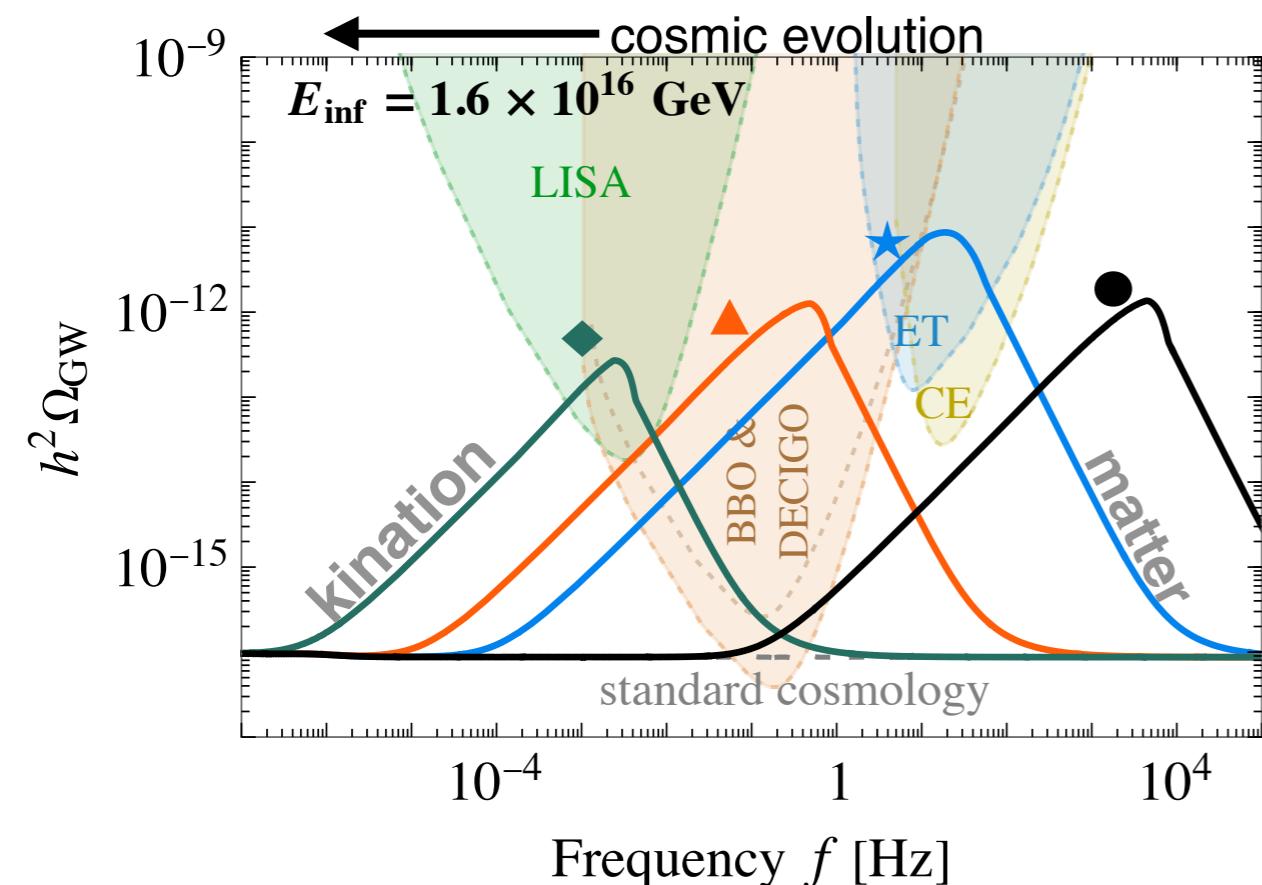
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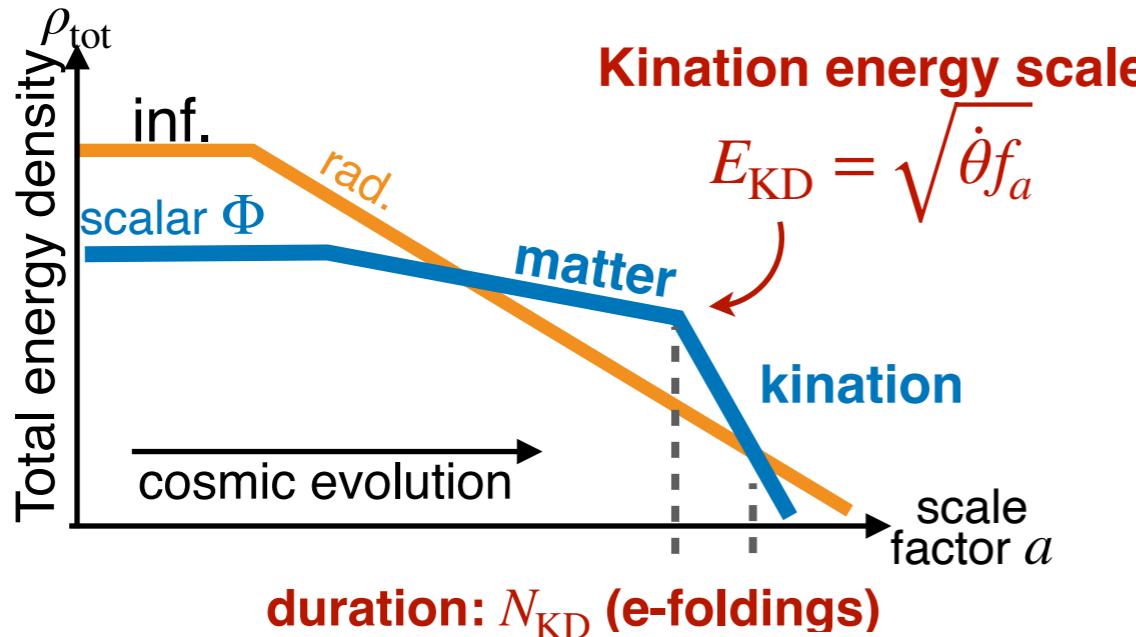
Peak position for GW from inflation.

$$f_{\text{peak}} \approx 10 \text{ Hz} \left(\frac{E_{\text{KD}}}{10^8 \text{ GeV}} \right) \left[\frac{\exp(N_{\text{KD}}/2)}{10} \right]$$

$$\Omega_{\text{peak}} h^2 \approx 10^{-12} \left(\frac{E_{\text{inf}}}{1.6 \times 10^{16} \text{ GeV}} \right)^4 \left[\frac{\exp(2N_{\text{KD}})}{10^4} \right]$$



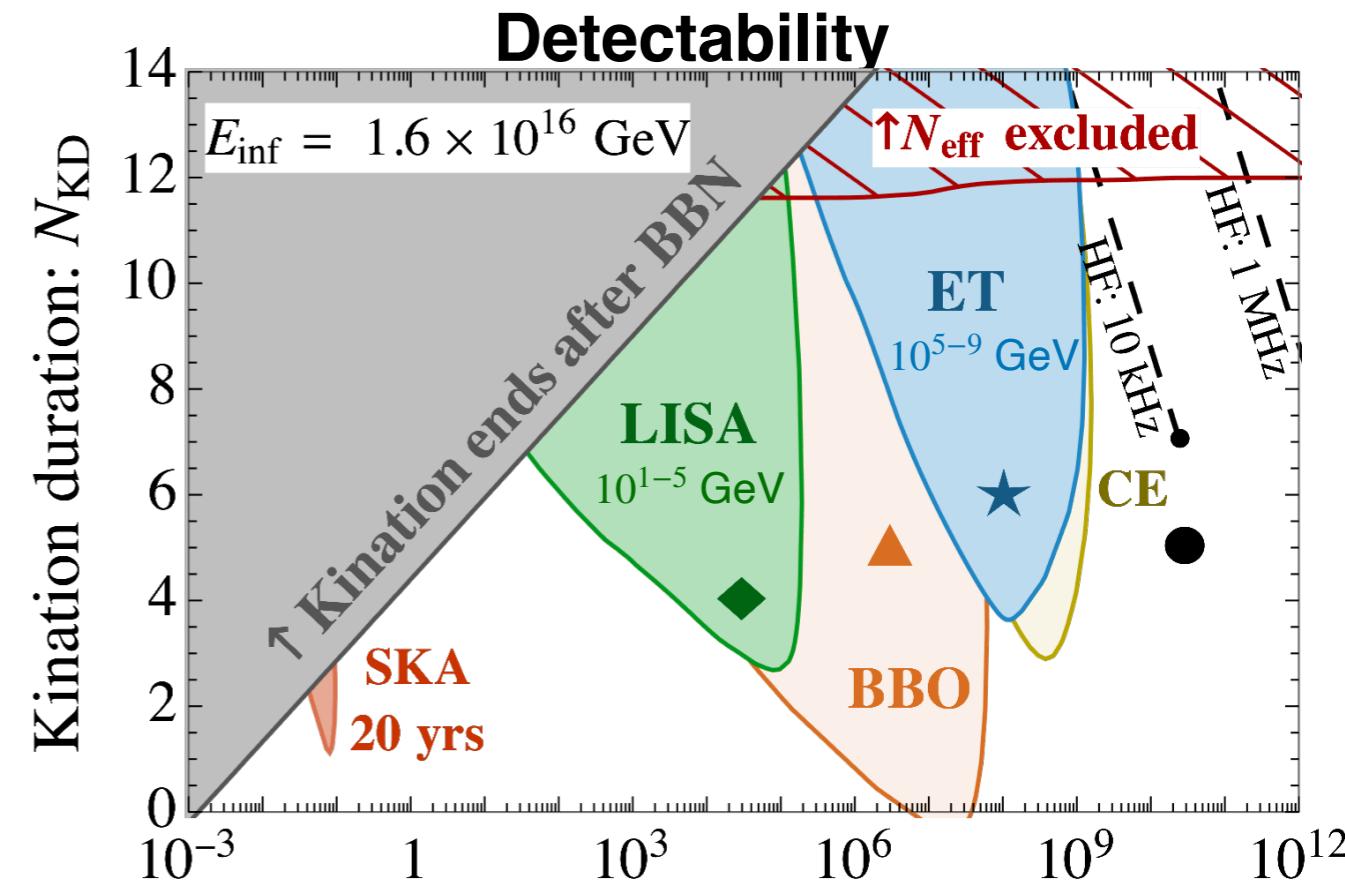
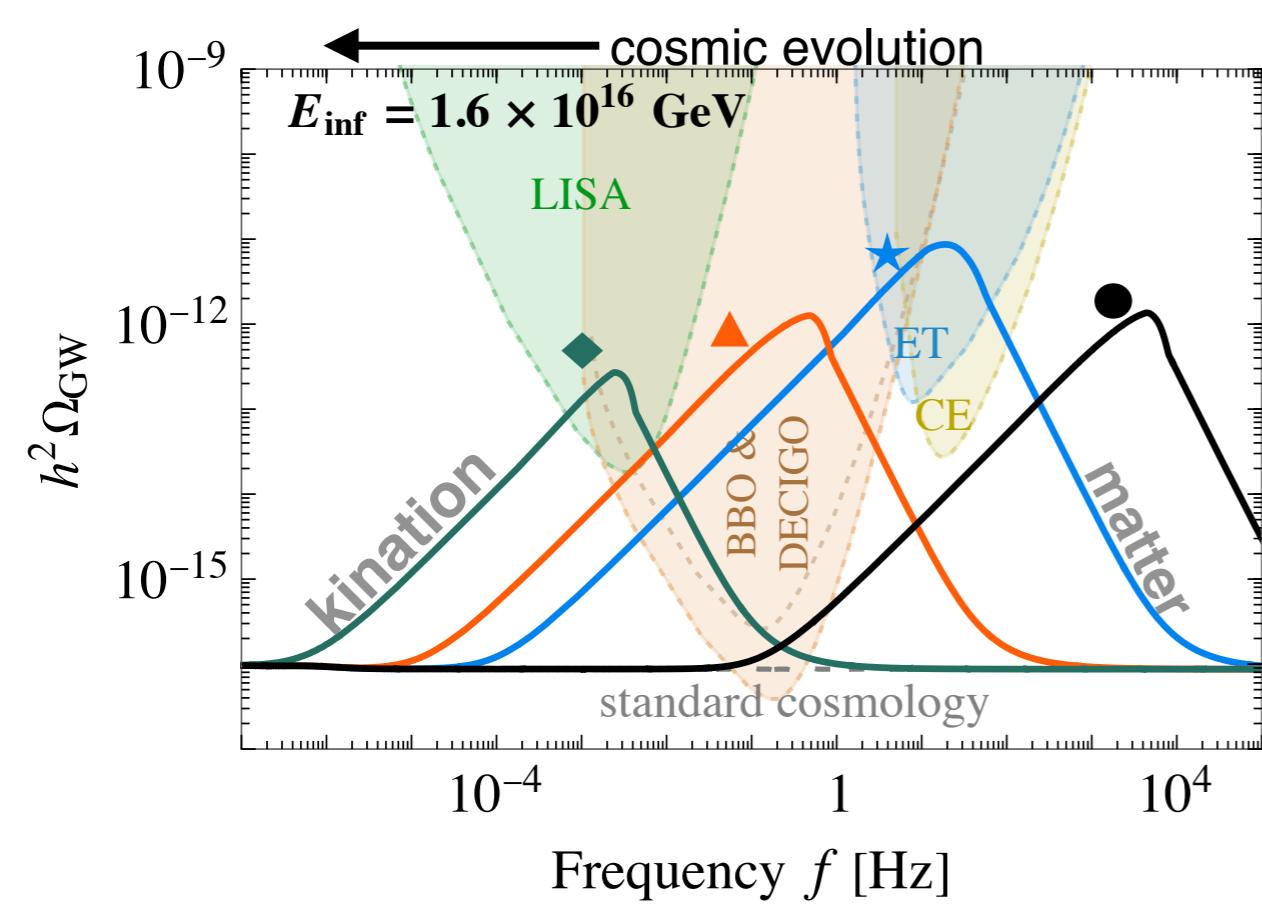
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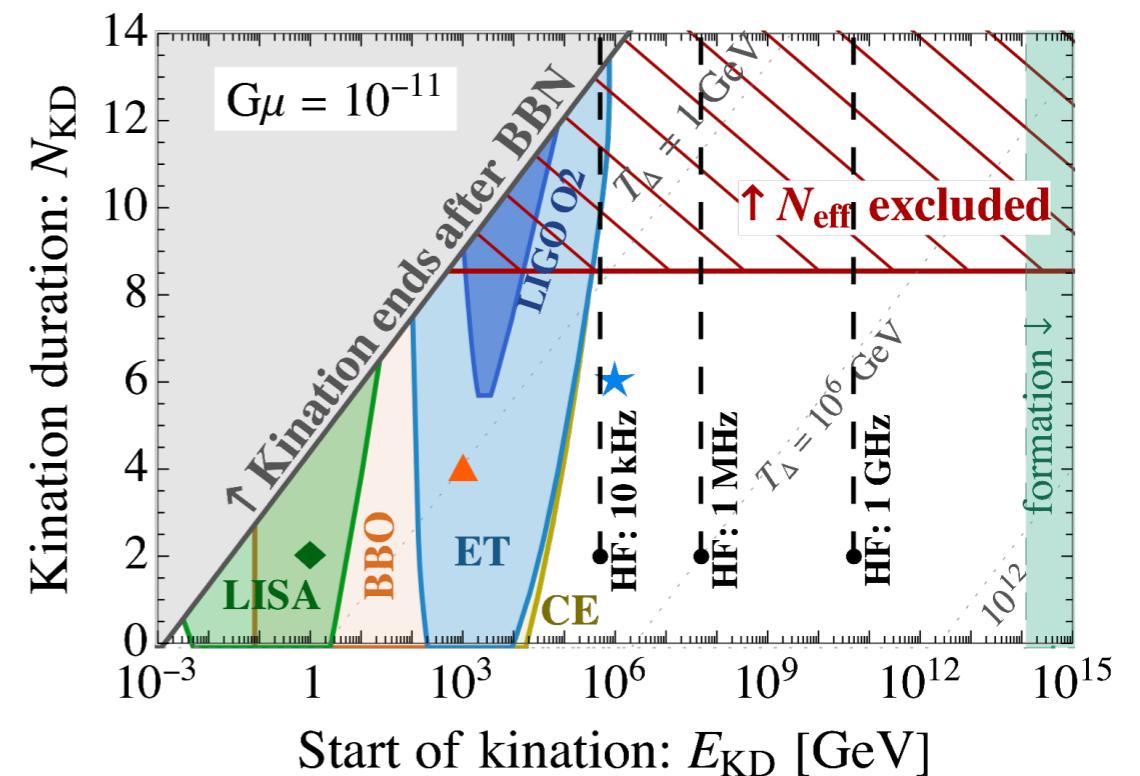
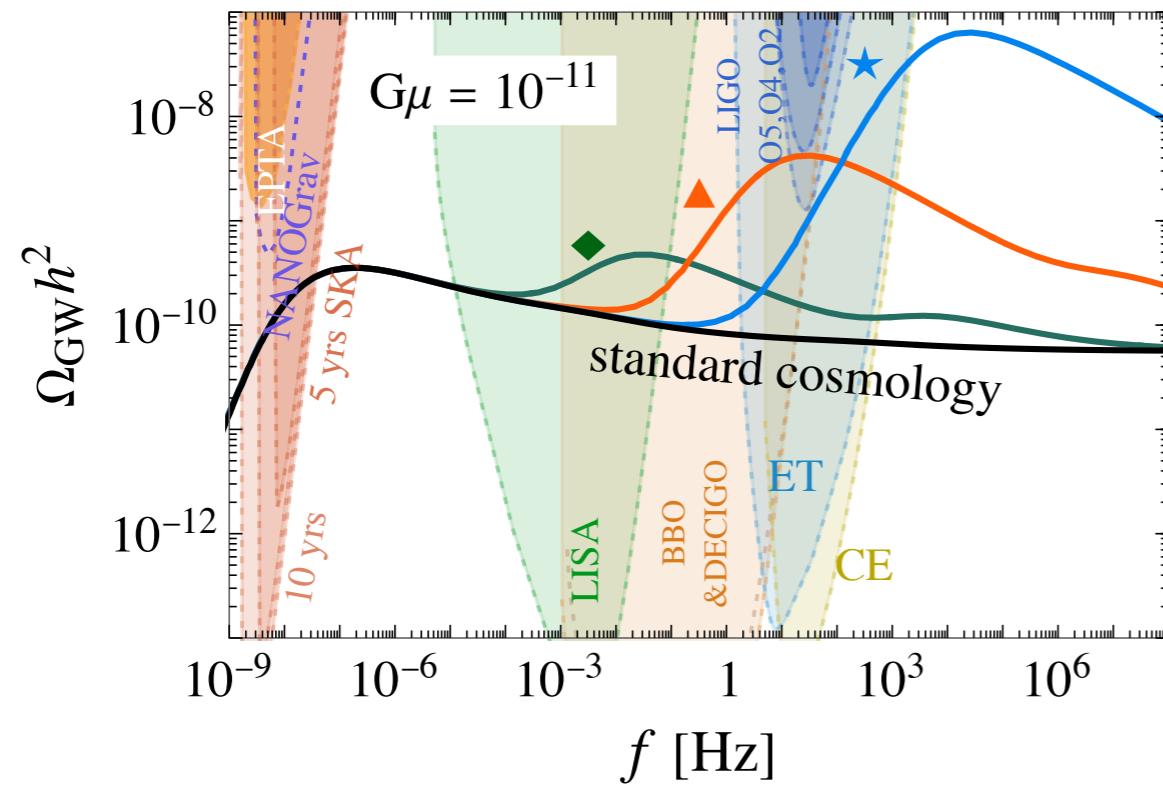
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$$\text{Kination starts: } E_{\text{KD}} \simeq \sqrt{f_a \dot{\theta}} \text{ [GeV]}$$

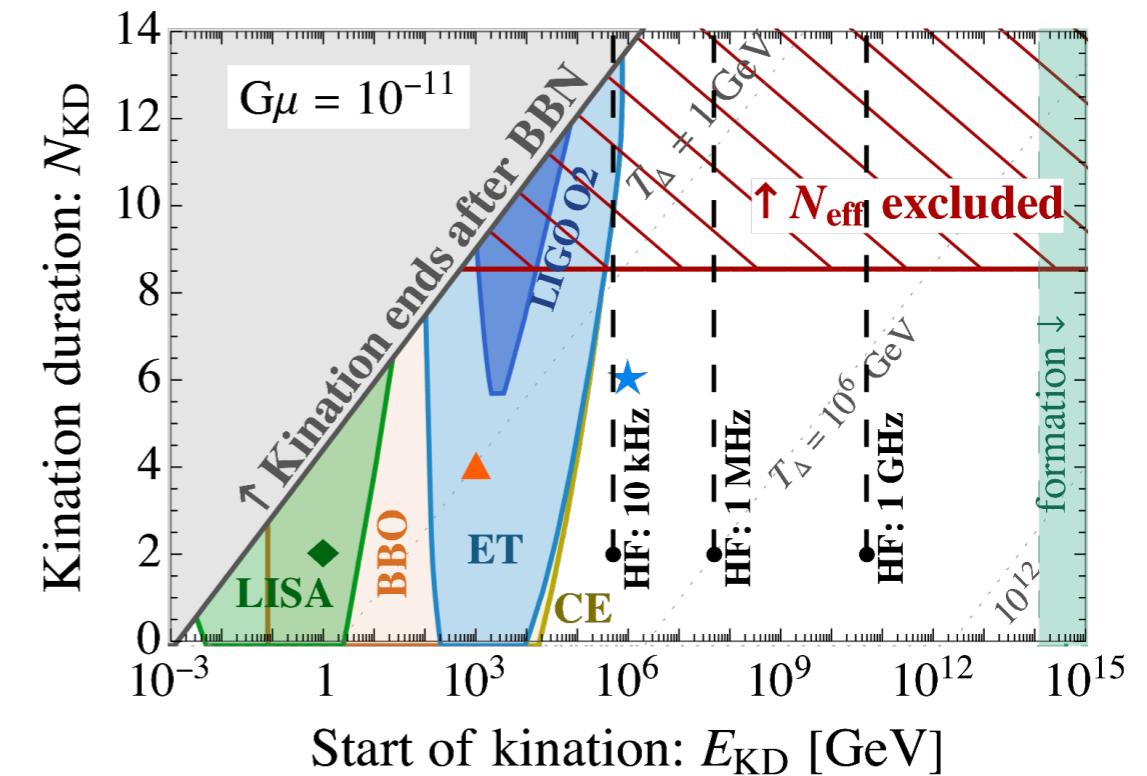
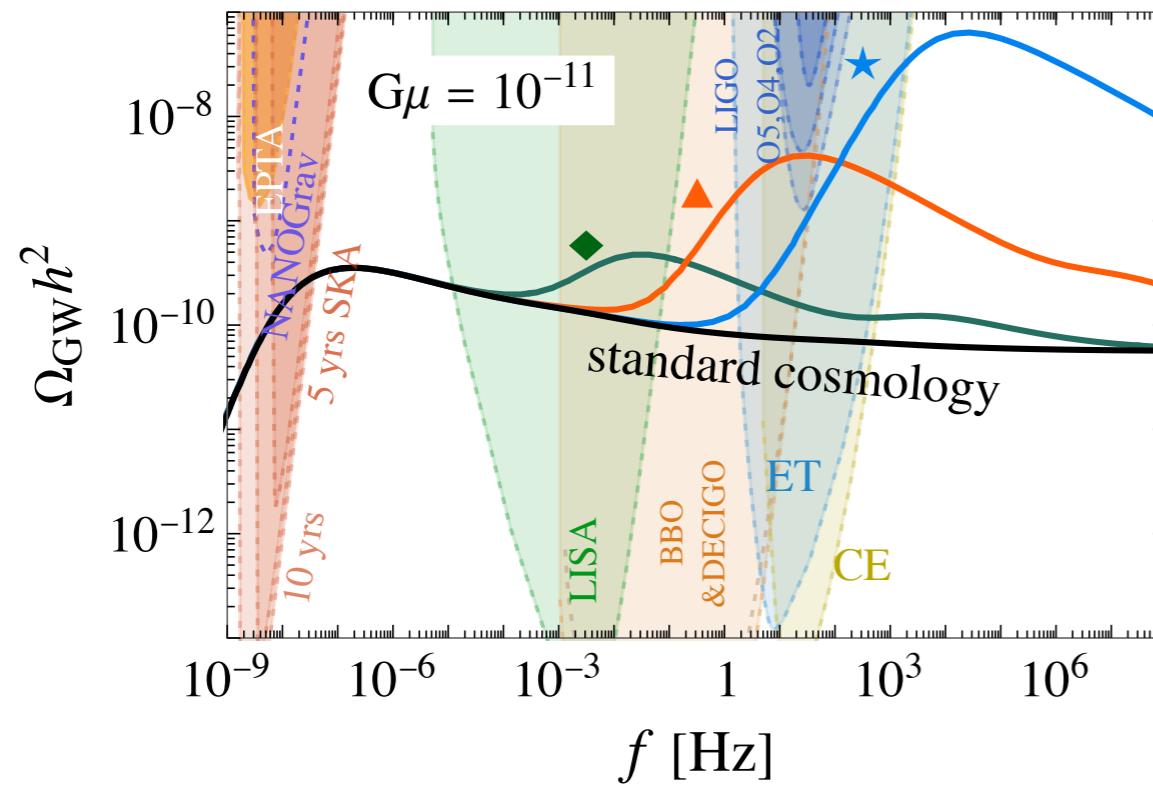
Local cosmic strings symmetry breaking scale $\simeq M_{\text{pl}} \sqrt{G\mu}$

YG, Servant, Simakachorn, 2111.01150

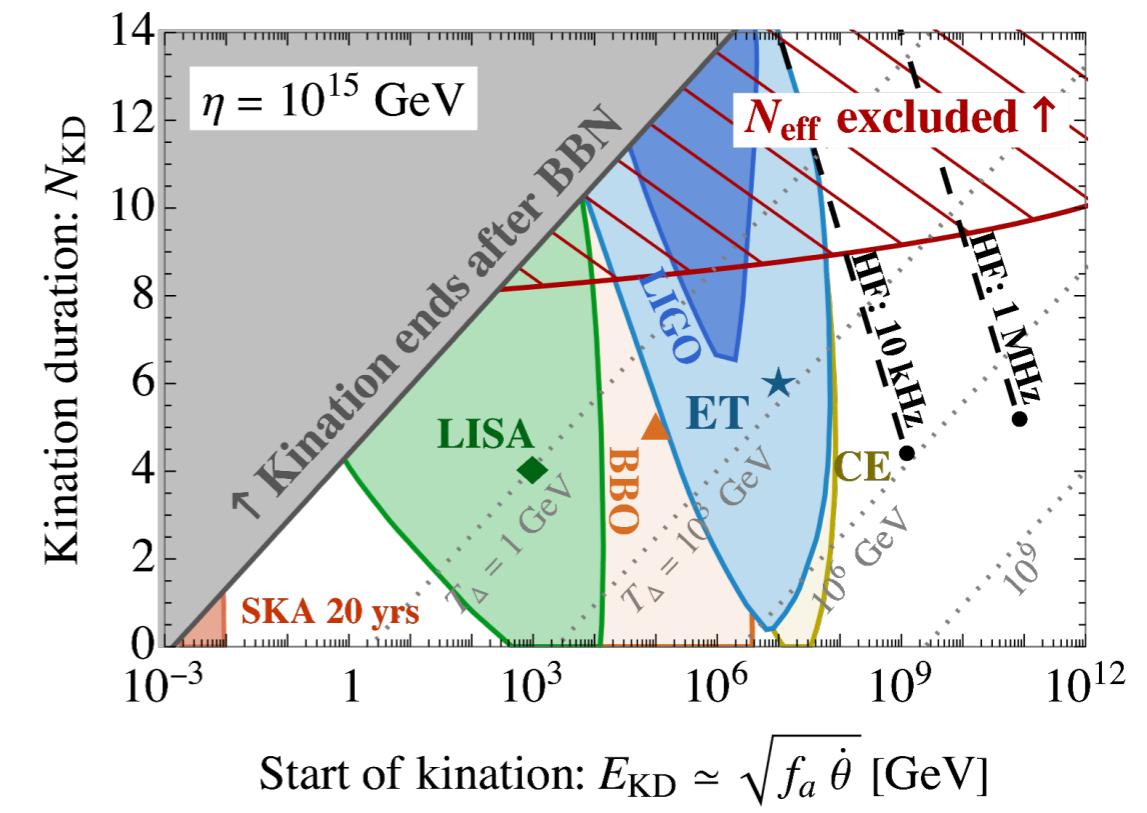
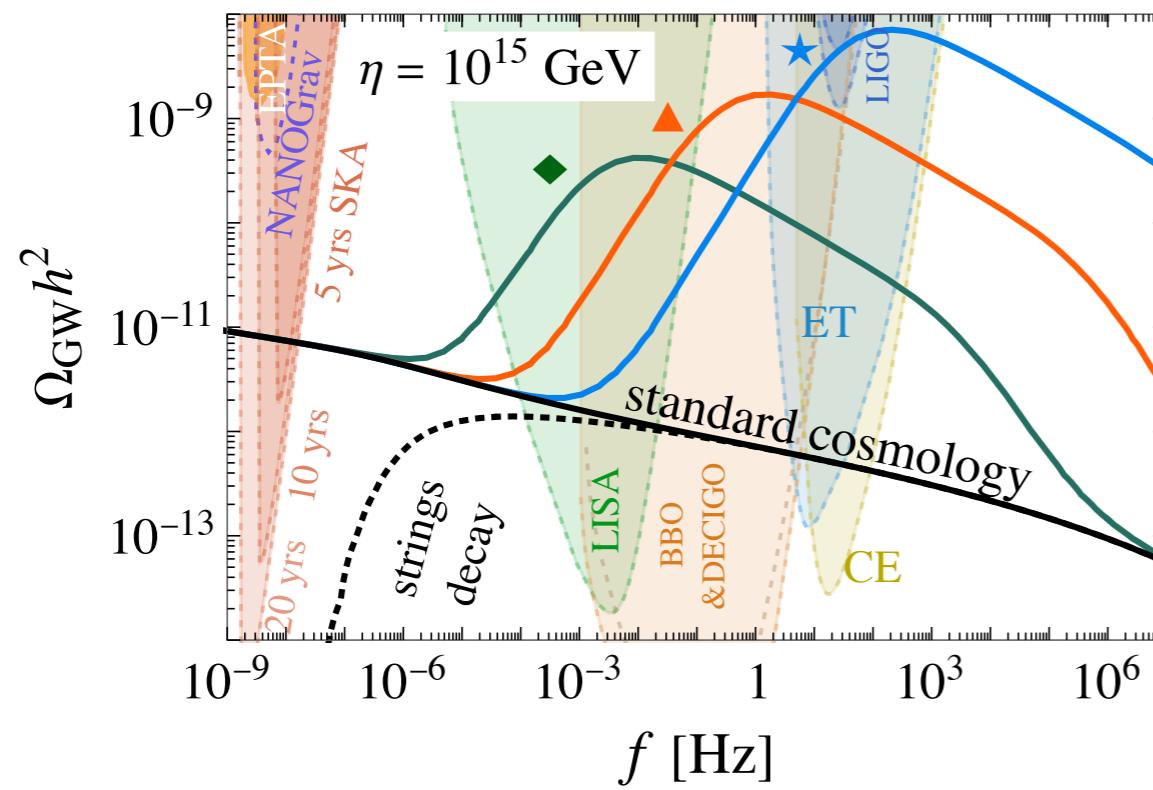


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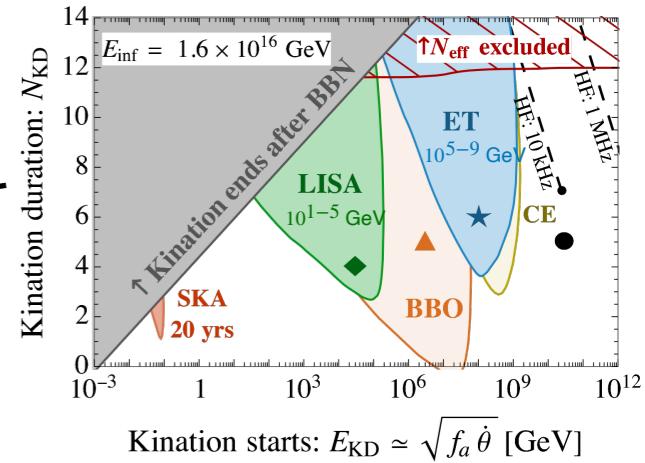
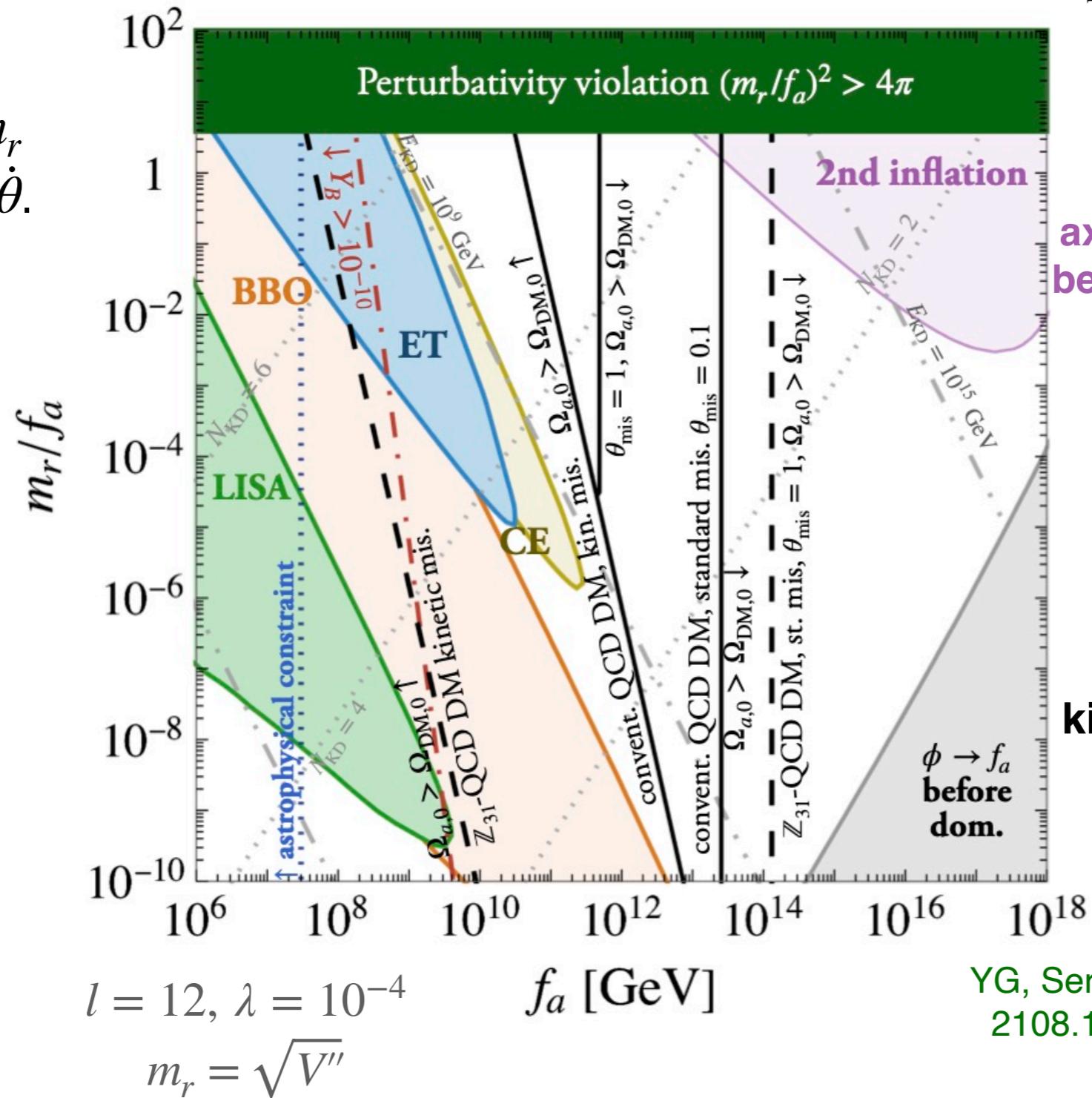


Global cosmic strings symmetry breaking scale $\simeq \eta$



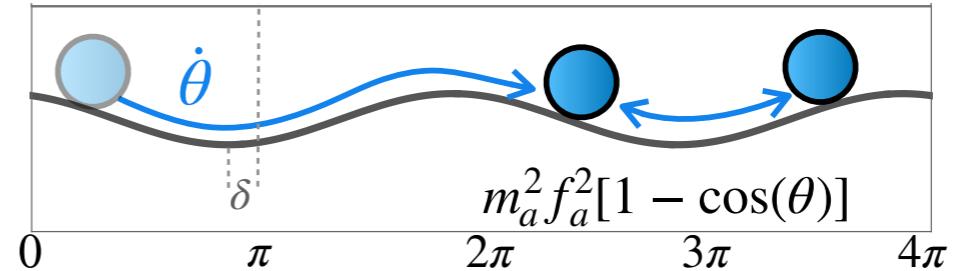
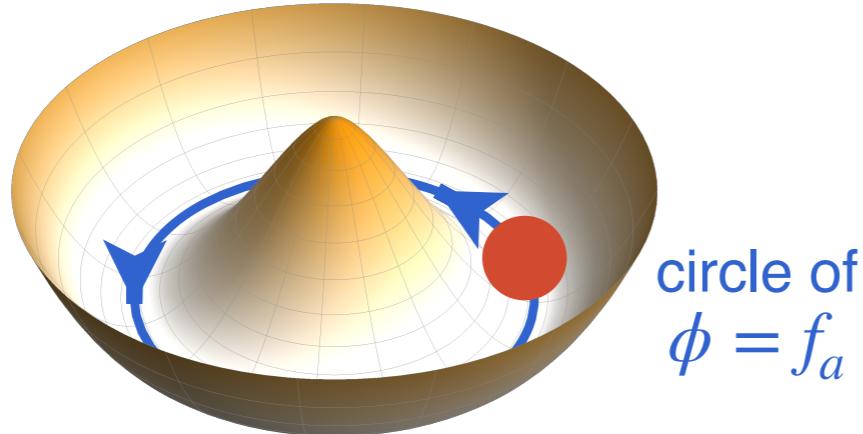
In terms of model parameters

Radial mode mass m_r
controls axion speed $\dot{\theta}$.



YG, Servant, Simakachorn,
2108.10328, 2111.01150

Axion Dark Matter



Kinetic energy red-shifts $\dot{\theta}^2 f_a^2 \propto a^{-6}$ **until** $\dot{\theta}^2 f_a^2 \simeq m_a^2 f_a^2$.

PQ charge in the spinning axion transfers to the axion number density via kinetic misalignment & axion fragmentation

[Co, Harigaya, Hall, '19]
[Chang, Cui, '19]

[Fonseca, Morgante, Sato, Servant, '19]
[Morgante, Ratzinger, Sato, Stefanek, '21]

$$\left. \frac{n_a}{s} \right|_0 \simeq \left. \frac{n_\theta}{s} \right|_{\text{KD}} \equiv \frac{f_a^2 \dot{\theta}_{\text{KD}}}{s_{\text{KD}}}$$

QCD Axion Dark Matter

via kinetic misalignment & axion fragmentation

[Co, Harigaya, Hall, '19]
[Chang, Cui, '19]

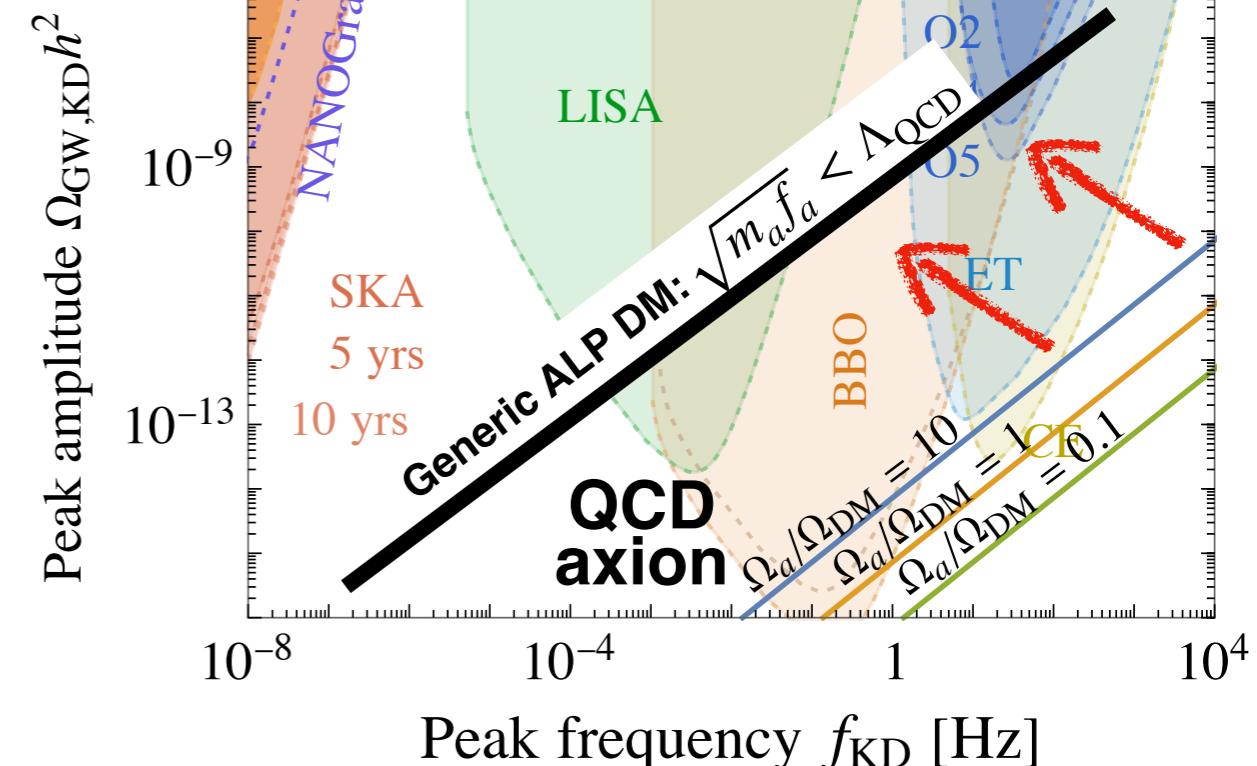
[Fonseca, Morgante, Sato, Servant, '19]
[Morgante, Ratzinger, Sato, Stefanek, '21]

$$\left| \frac{n_a}{s} \right|_0 \sim \left| \frac{n_\theta}{s} \right|_{\text{KD}} \equiv \frac{f_a^2 \dot{\theta}}{s_{\text{KD}}}$$

GW peak & Axion abundance

$$f_{\text{peak}} \approx 10 \text{ kHz} \left(\frac{\sqrt{m_a f_a}}{100 \text{ MeV}} \right)^2 \left(\frac{E_{\text{KD}}}{10^9 \text{ GeV}} \right)^{4/3} \left(\frac{\Omega_{a,0}}{\Omega_{\text{DM},0}} \right)^{1/3}$$

$$\Omega_{\text{peak}} h^2 \approx 10^{-15} \left(\frac{f_{\text{KD}}}{\text{Hz}} \right) \left(\frac{E_{\text{inf}}}{10^{16} \text{ GeV}} \right)^4 \left(\frac{100 \text{ MeV}}{\sqrt{m_a f_a}} \right)^2 \left(\frac{\Omega_{a,0}}{\Omega_{\text{DM},0}} \right)$$



The conventional QCD axion DM has no observable peak,
except BBO or HF experiments.

Observable signals for generic ALP DM and
QCD axion DM with lighter mass, e.g., from the \mathbb{Z}_N -axion.

[Hook, '18] & [Di Luzio, Gavela, Quilez, Ringwald, '21]

Conclusion

Cosmic archeology with GW from primordial inflation and cosmic strings

Early matter era

Heavy & unstable particles

$$1 \text{ s} \gtrsim \tau_X \gtrsim 10^{-17} \text{ s}$$

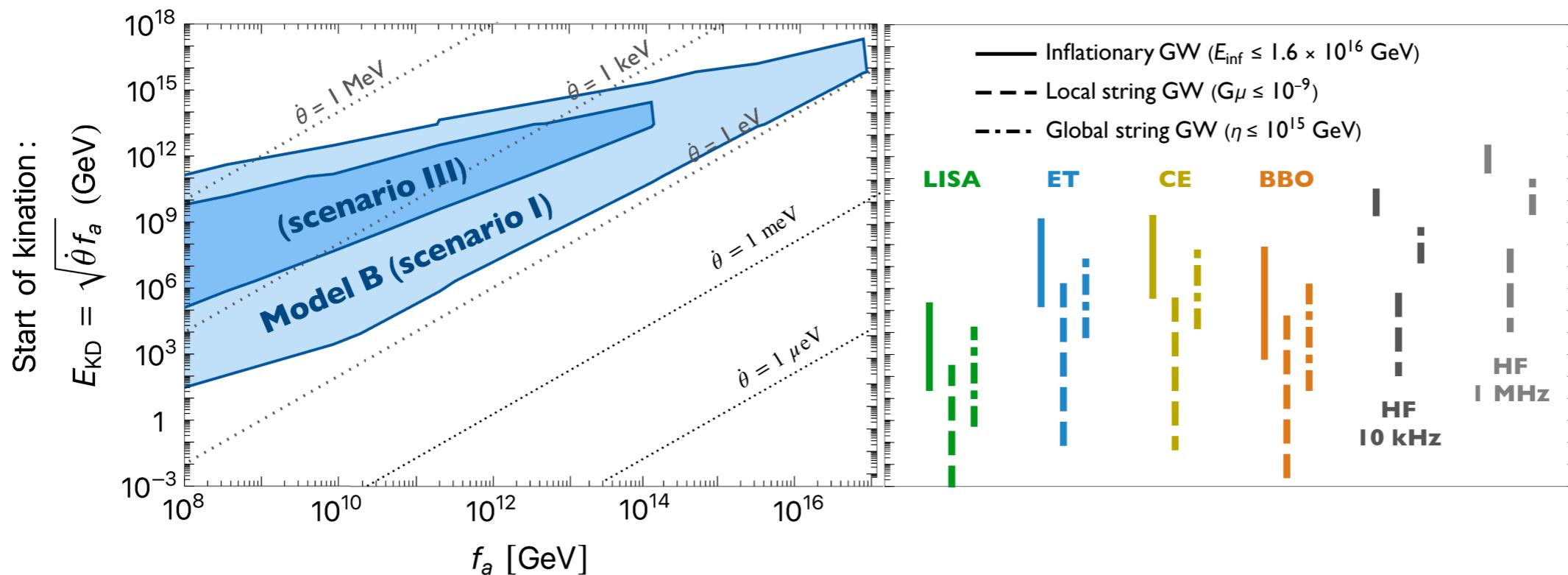
2nd inflation era

Supercool 1st-order phase transition

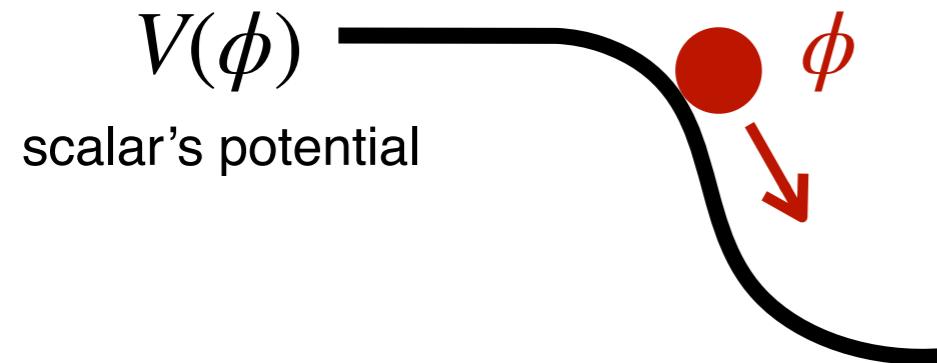
$$10^{-2} \text{ GeV} \lesssim E_{\text{inf}} \lesssim 10^{13} \text{ GeV}$$

Intermediate kination era

Spinning axion



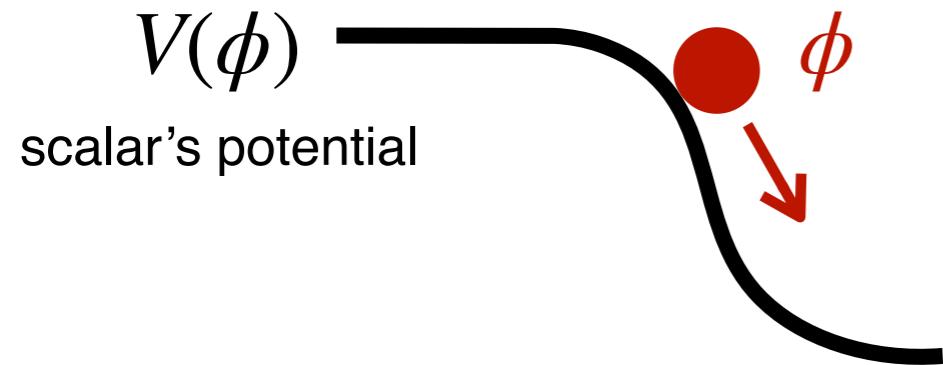
The simplest **kination** era



equation-of-state: $\omega_\phi = \frac{E_{\text{kinetic}} - E_{\text{potential}}}{E_{\text{kinetic}} + E_{\text{potential}}}$

Maximum $\omega_\phi = 1$, when $E_{\text{kinetic}} \gg E_{\text{potential}}$

The simplest **kination** era



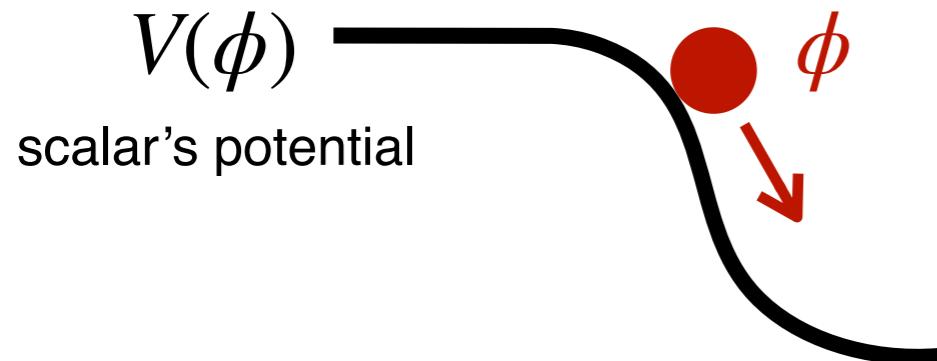
equation-of-state: $\omega_\phi = \frac{E_{\text{kinetic}} - E_{\text{potential}}}{E_{\text{kinetic}} + E_{\text{potential}}}$

Maximum $\omega_\phi = 1$, when $E_{\text{kinetic}} \gg E_{\text{potential}}$

**A scalar field dominates the universe with large kinetic energy,
“Kination” era. ($\rho_\phi \propto a^{-6}$)**

[Spokoiny 1993, Joyce, 1997]

The simplest **kination** era



$$\text{equation-of-state: } \omega_\phi = \frac{E_{\text{kinetic}} - E_{\text{potential}}}{E_{\text{kinetic}} + E_{\text{potential}}}$$

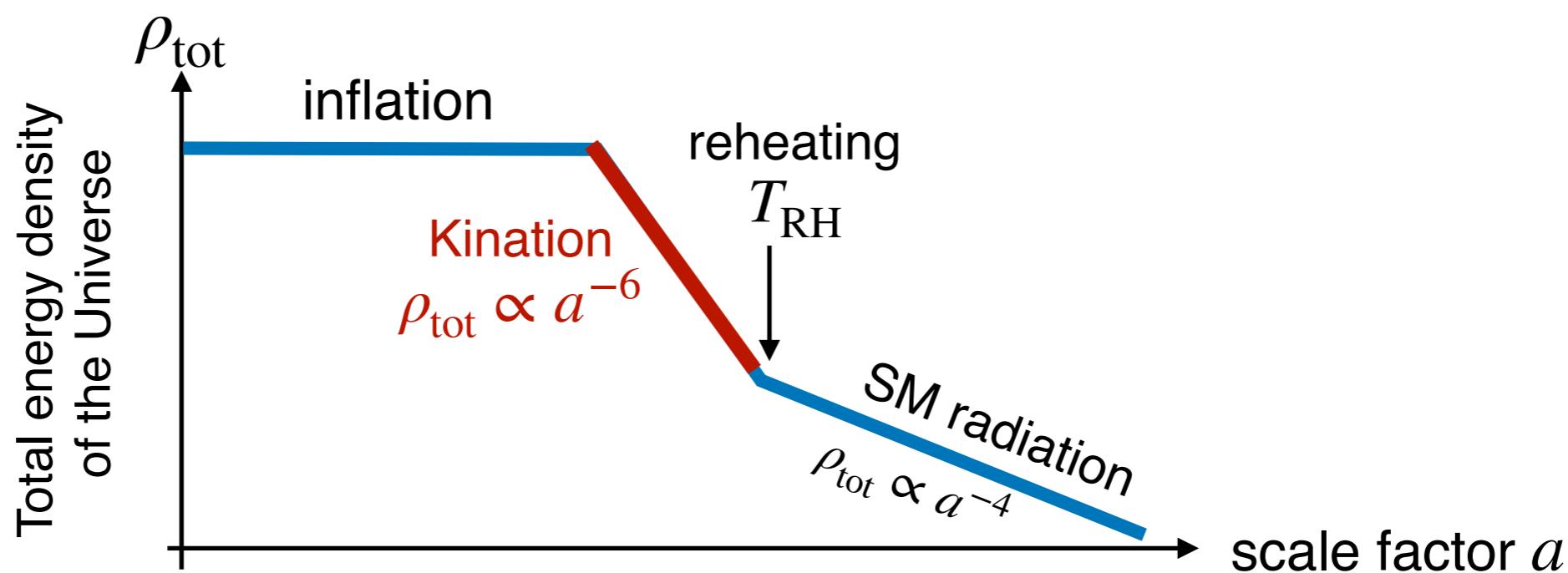
Maximum $\omega_\phi = 1$, when $E_{\text{kinetic}} \gg E_{\text{potential}}$

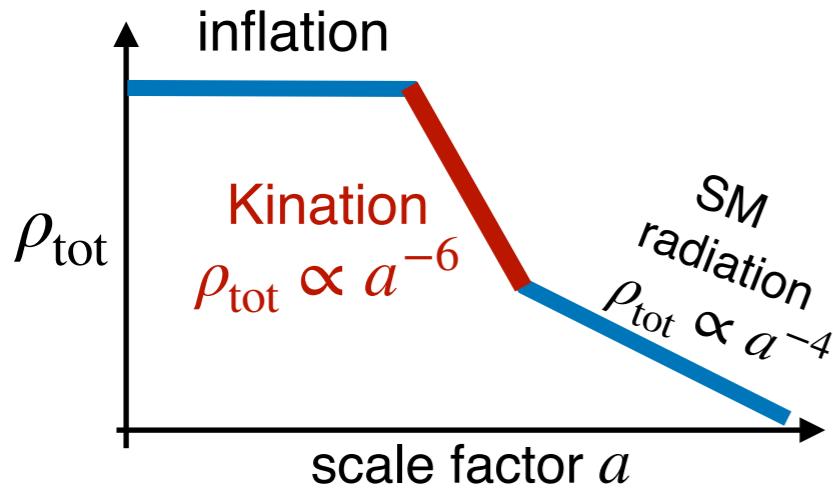
A scalar field dominates the universe with large kinetic energy,
“Kination” era. ($\rho_\phi \propto a^{-6}$)

[Spokoiny 1993, Joyce, 1997]

Example: **quintessential inflation**

Peebles and Vilenkin 1998



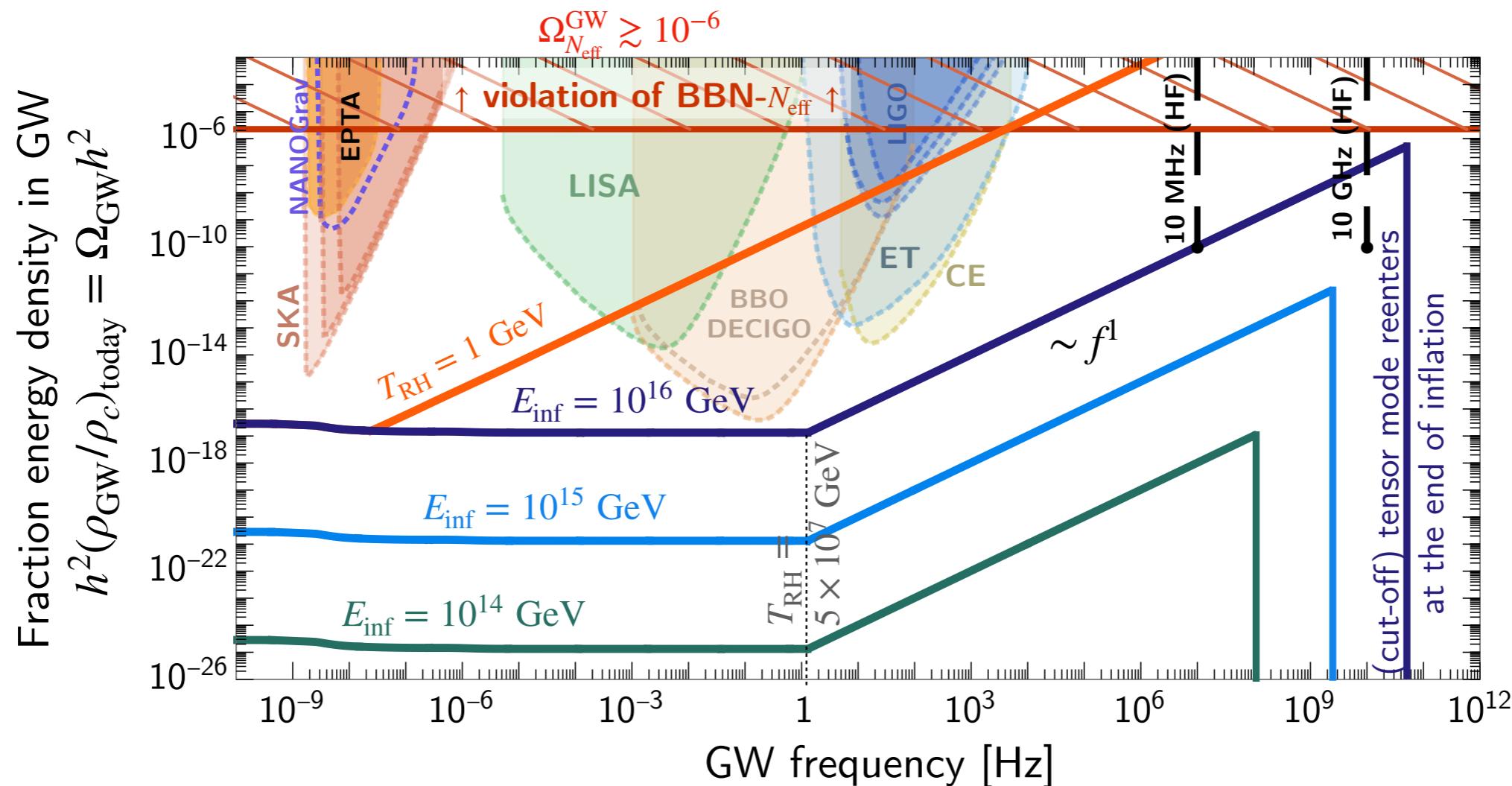


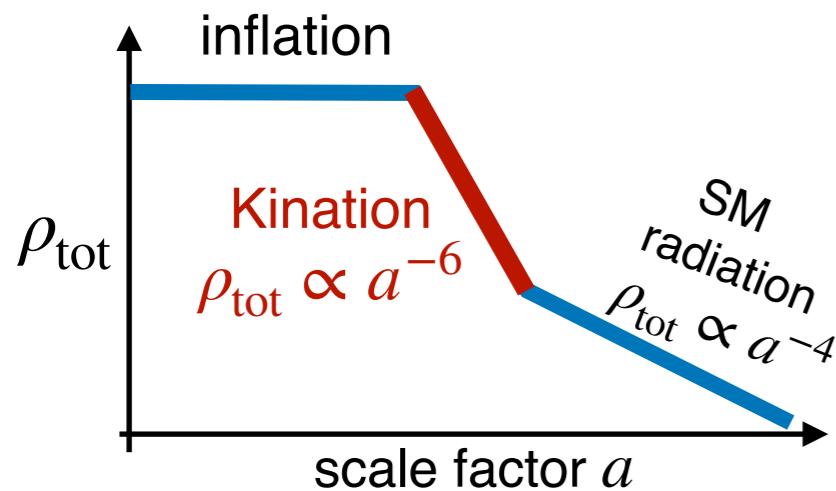
GW is an extra radiation.

Too much GW violate BBN/CMB bound:

$$\Delta N_{\text{eff}} \lesssim 0.2$$

A long kination after inflation cannot have observable signal.



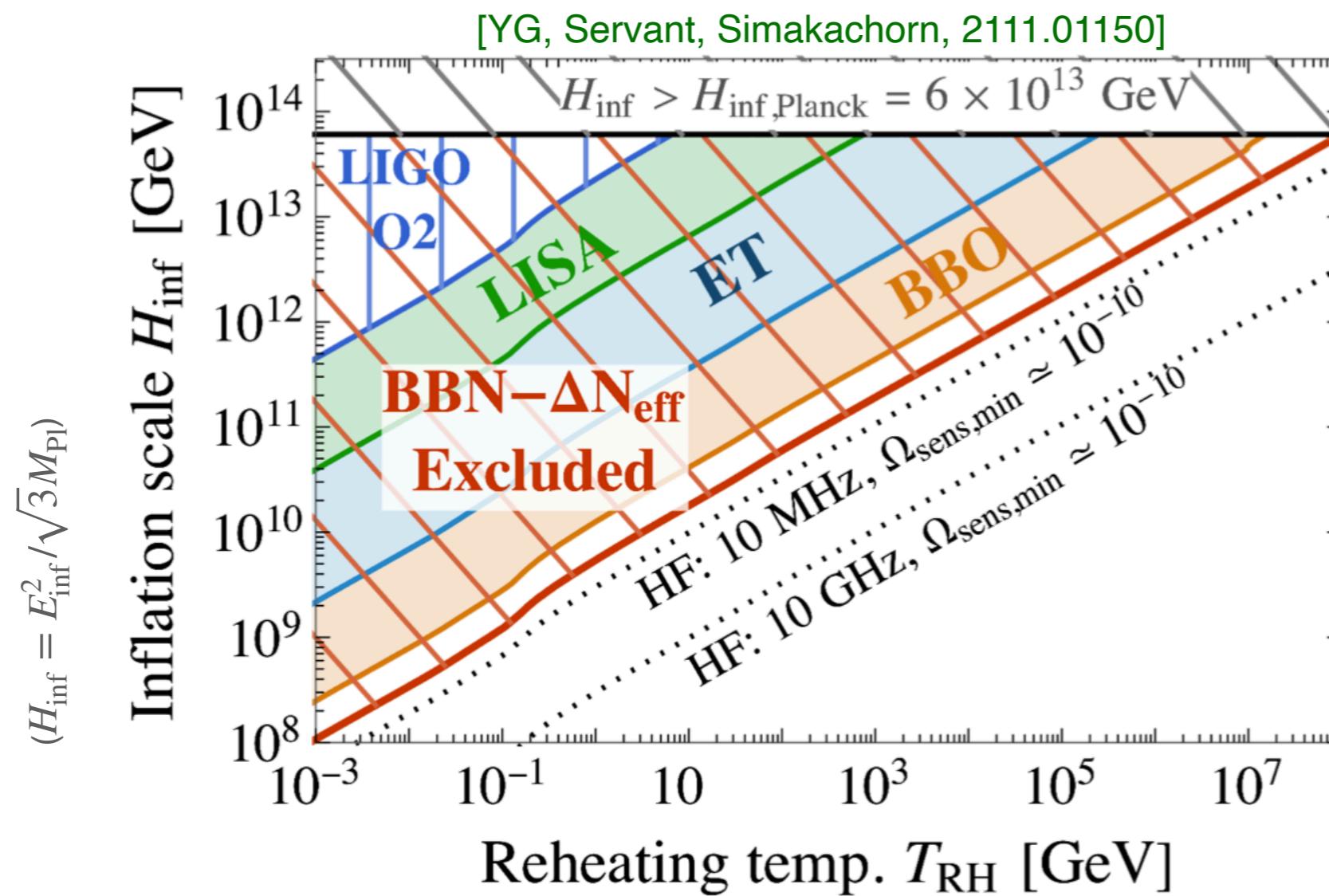


GW is an extra radiation.

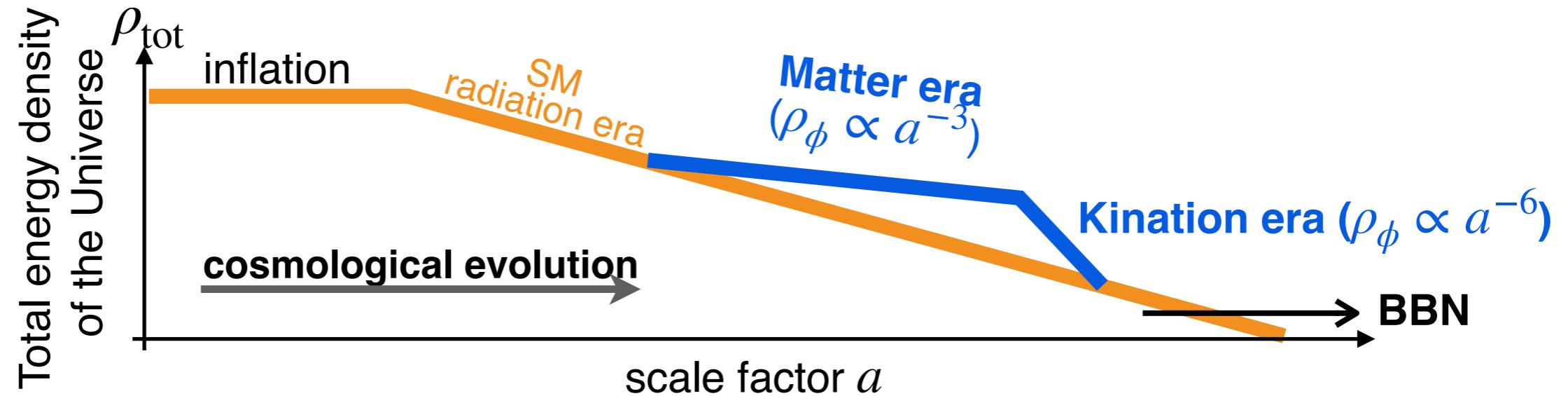
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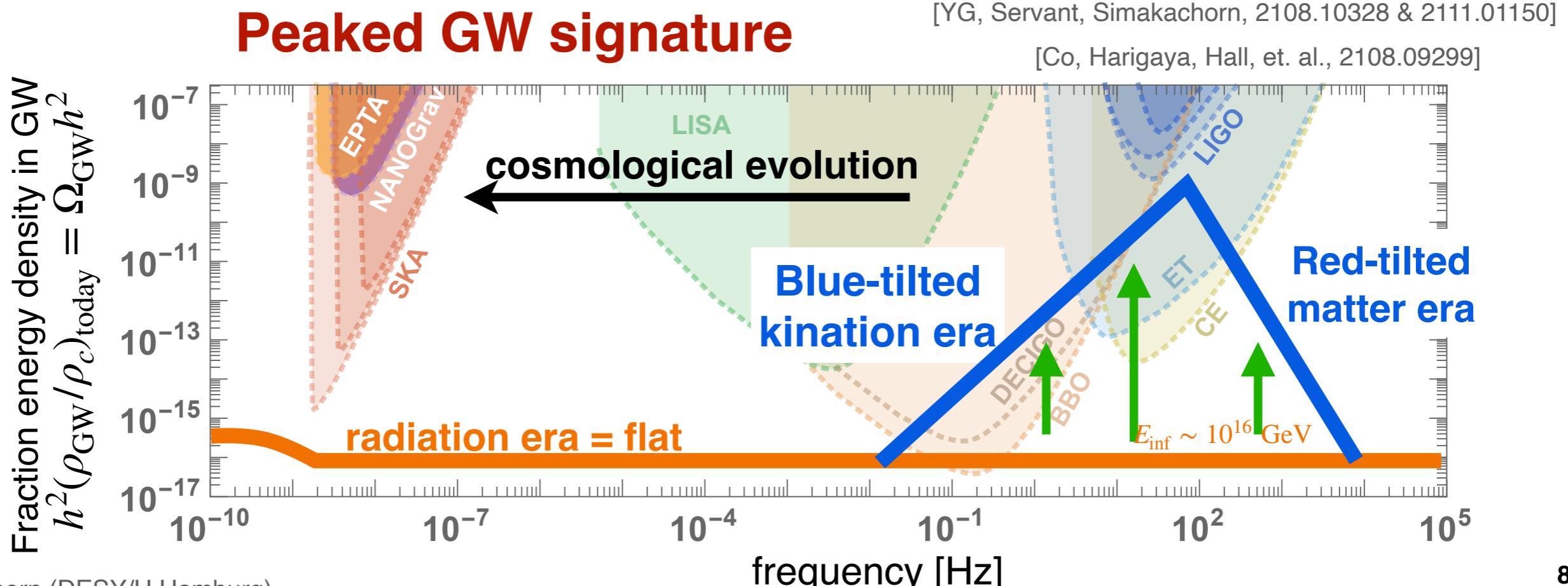
A long kination after inflation cannot have observable signal.



What if instead **kination** occurs long after inflation ?



Spinning axion!

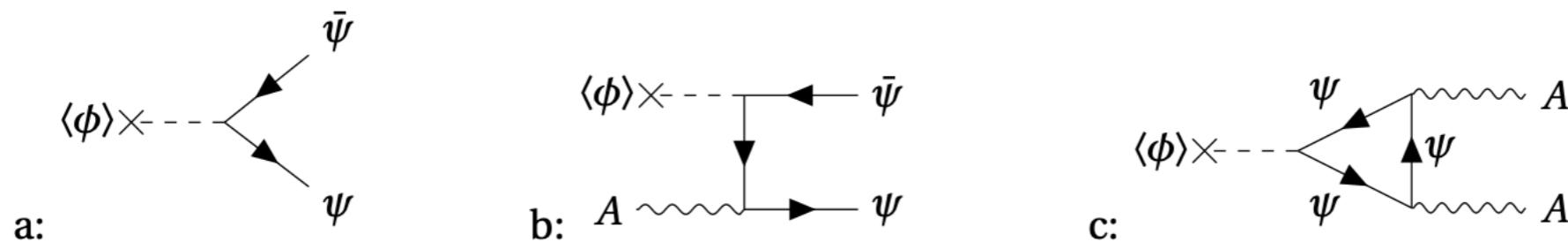


Number of e-folds of kination

$$\epsilon = \begin{cases} \frac{1}{\sqrt{2}} \frac{m_{r,\text{eff}}(f_a)}{m_{r,\text{eff}}(\phi_{\text{ini}})} l \sin l\theta_{\text{ini}}, & \text{if } c > l-1, \\ \frac{1}{\sqrt{2}} \sqrt{\frac{c}{l-1}} \frac{m_{r,\text{eff}}(f_a)}{m_{r,\text{eff}}(\phi_{\text{ini}})} l \sin l\theta_{\text{ini}}, & \text{otherwise.} \end{cases}$$

$$\phi_{\text{ini}} = M_{\text{pl}} \left(\sqrt{c} \frac{m_{r,\text{eff}}(\phi_{\text{ini}})}{\lambda \sqrt{2l-2} M_{\text{pl}}} \right)^{\frac{1}{l-2}}.$$

$$\Gamma_\phi \simeq \begin{cases} \text{for } y_\psi \phi < T : \begin{cases} \text{for } m_{\psi,\text{th}} = g T > m_\phi/2, & \frac{y_\psi^2 \alpha T}{2\pi^2}, \\ \text{for } m_{\psi,\text{th}} = g T < m_\phi/2, & \frac{y_\psi^2 m_\phi}{8\pi}, \end{cases} \\ \text{for } y_\psi \phi > T : \quad b \alpha^2 \frac{\text{Max}[T, m_\phi]^3}{\phi^2} + \frac{y_\psi^2 m_\phi}{8\pi} \Theta(2m_\phi - y_\psi \phi). \end{cases} \quad (\text{F.5})$$



$$e^{N_{\text{KD}}} = \left(\frac{\min(\rho_{\text{dom}}, \rho_{\text{damp}})}{\rho_{\text{KD},i}} \right)^{1/6} = \begin{cases} \sqrt{\frac{3}{2}} \left(\frac{m_{r,\text{eff}}(\phi_{\text{ini}})}{m_{r,\text{eff}}(f_a)} \frac{M_{\text{pl}}}{f_a} \right)^{1/3} \left(\frac{\phi_{\text{ini}}}{M_{\text{pl}}} \right)^{4/3} \epsilon^{2/3}, & \text{if } \rho_{\text{damp}} > \rho_{\text{dom}}, \\ \left(\frac{6M_{\text{pl}}^2 \Gamma_{\text{damp}}^2}{f_a^2 m_{r,\text{eff}}^2(f_a)} \right)^{1/6} \epsilon^{2/3}, & \text{if } \rho_{\text{damp}} < \rho_{\text{dom}}. \end{cases} \quad (8.28)$$

$$\rho_{\text{damp}} > \rho_{\text{dom}} \quad \Rightarrow \quad e^{N_{\text{KD}}} \simeq e^{8.2} \epsilon^{2/3} \left(\frac{10^9 \text{ GeV}}{f_a} \right)^{1/3} \left(\frac{m_{r,\text{eff}}(\phi_{\text{ini}})}{5m_{r,\text{eff}}(f_a)} \right)^{1/3} \left(\frac{\phi_{\text{ini}}}{M_{\text{pl}}} \right)^{4/3},$$

Baryogenesis from a spinning axion

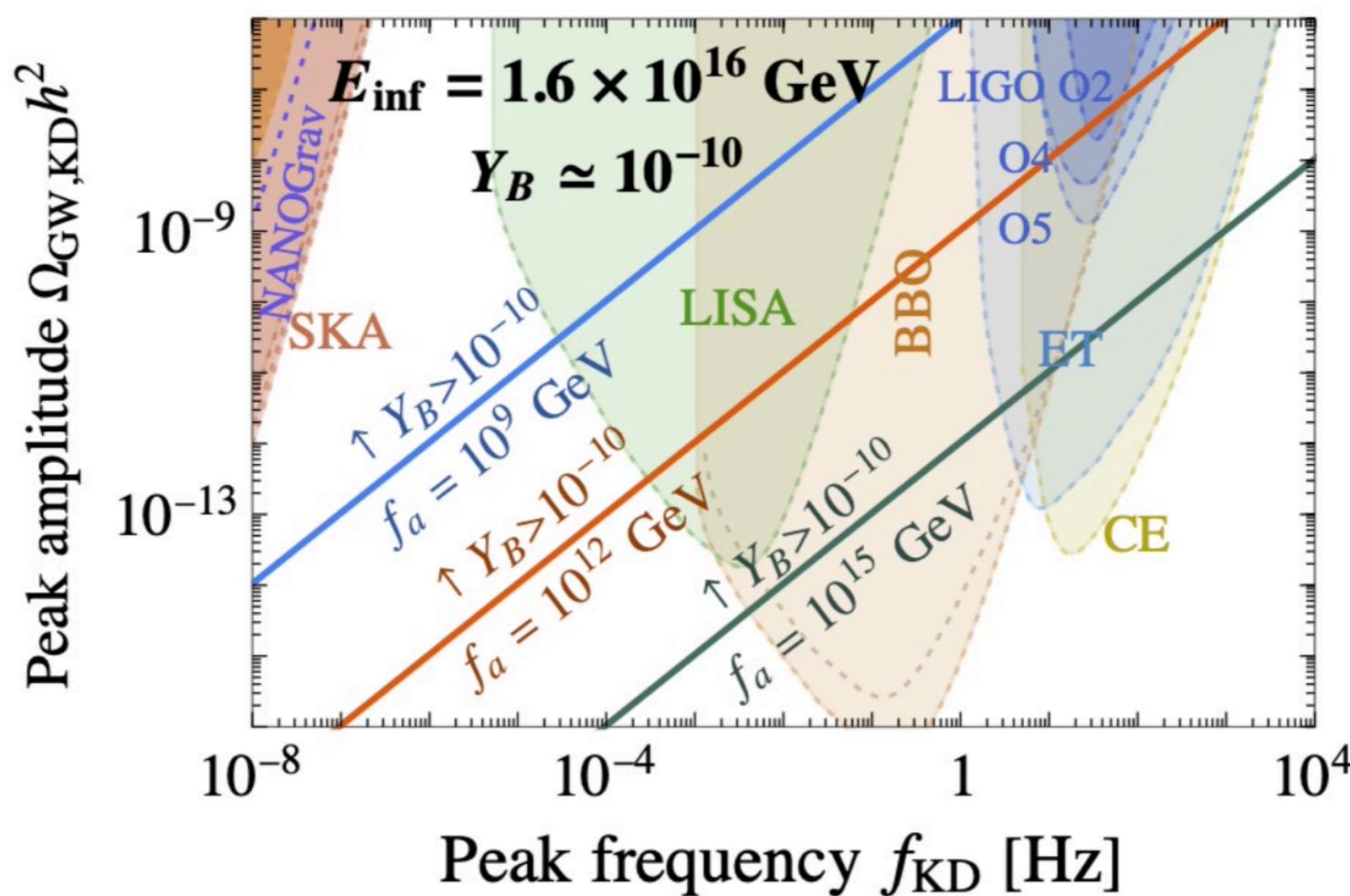
Standard “Axiogenesis” [Co, Harigaya, ’19]

$U(1)_{\text{PQ}}$ -charge transfers to baryon number via $SU(3)_c$ and $SU(2)_L$ sphaleron.

$$Y_\theta = 692 \left(\frac{0.1}{c_B} \right) \left(\frac{130 \text{ GeV}}{T_{\text{ws}}} \right)^2 \left(\frac{f_a}{10^8 \text{ GeV}} \right)^2 \left(\frac{Y_B}{10^{-10}} \right).$$

$$E_{\text{KD}} = (74 \text{ TeV}) G^{3/4} (T_{\text{KD}}) \left(\frac{c_B}{0.1} \right) \left(\frac{T_{\text{ws}}}{130 \text{ GeV}} \right)^2 \left(\frac{10^8 \text{ GeV}}{f_a} \right) \left(\frac{10^{-10}}{Y_B} \right) \exp \left(\frac{3N_{\text{KD}}}{2} \right).$$

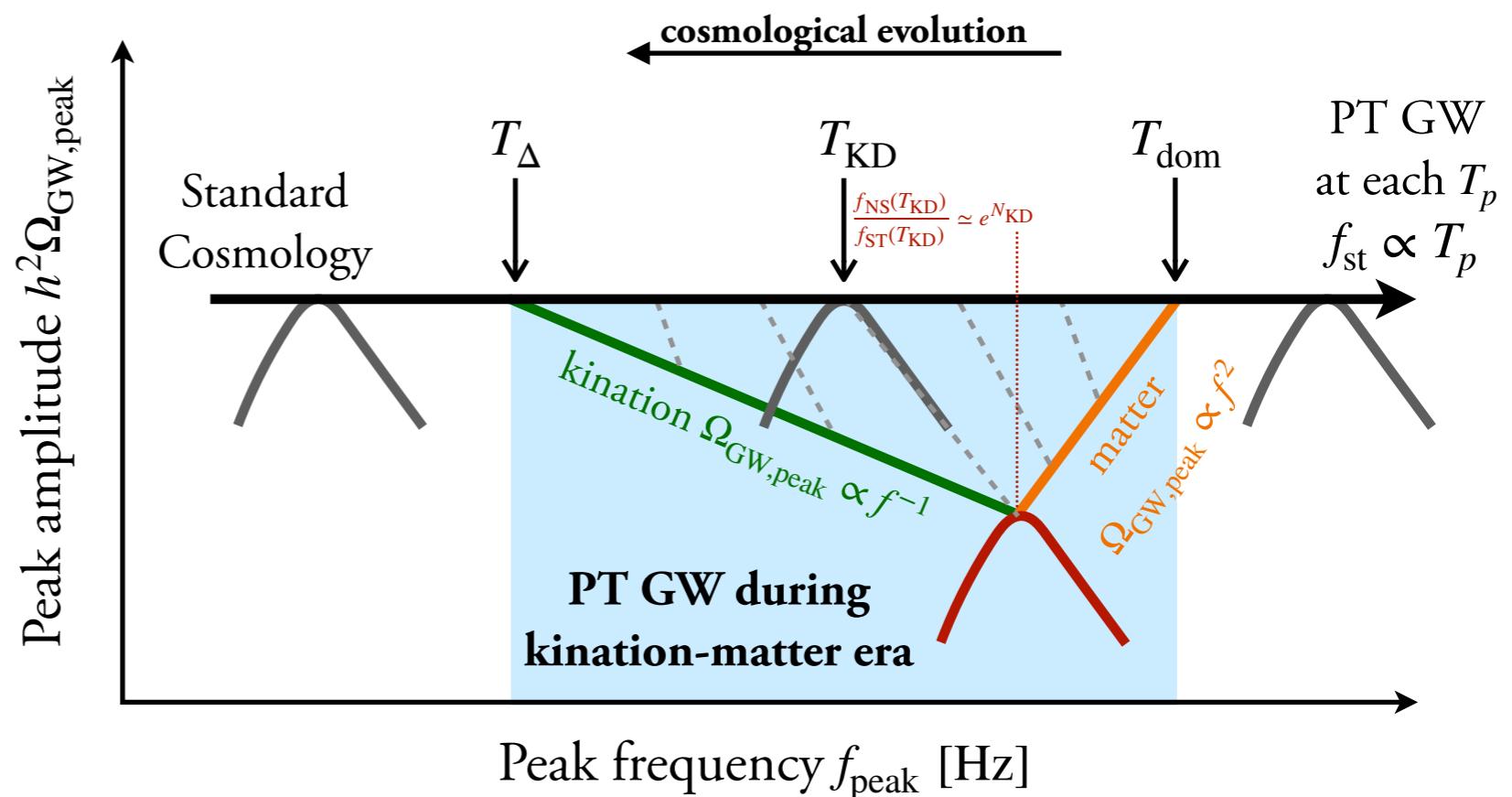
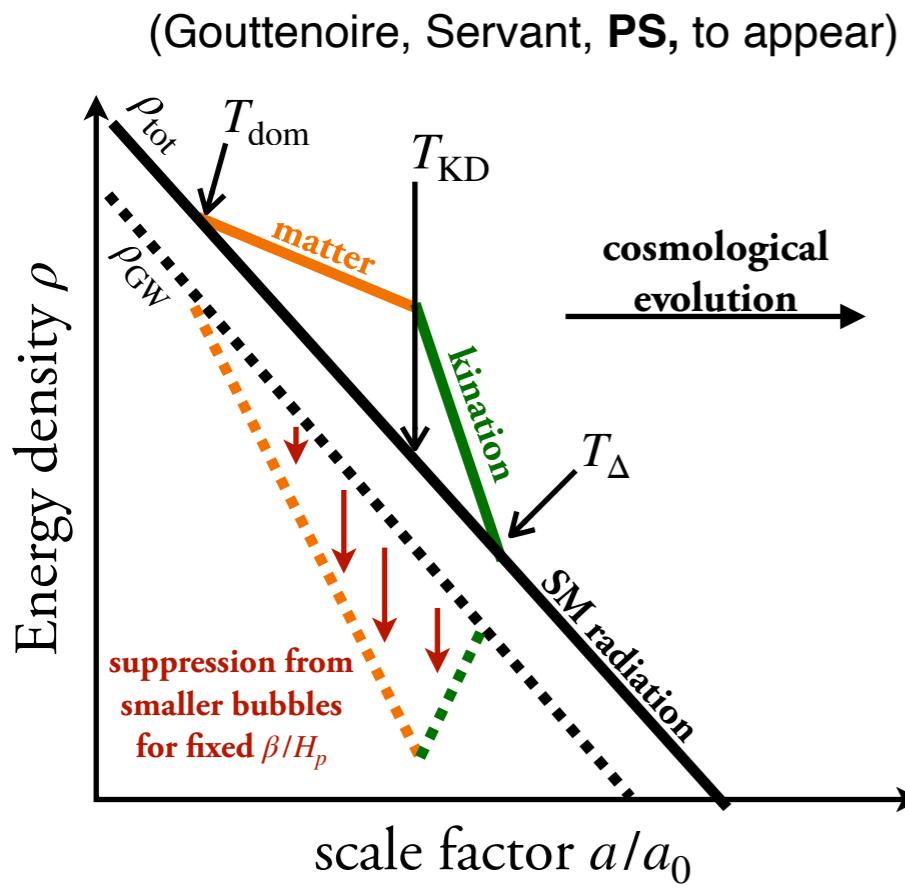
Gravitational waves from primordial inflation



Effect on short-lasting GW

e.g. first-order phase transition

Thermal phase transition where the source of GW is the thermal plasma cannot have the enhancement.



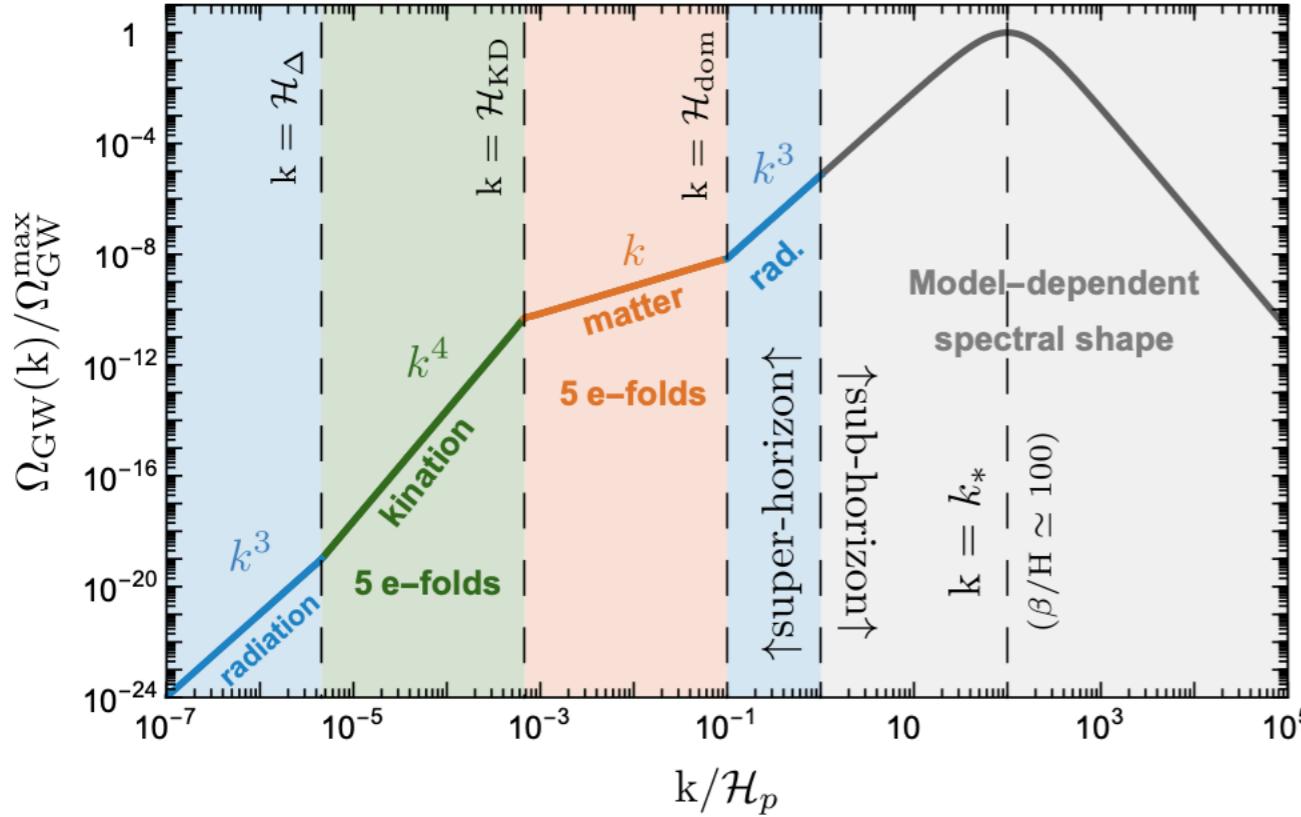
Super simplified argument: For fixed β/H_p ,

the bubble size is fixed to be some fraction of Hubble horizon.

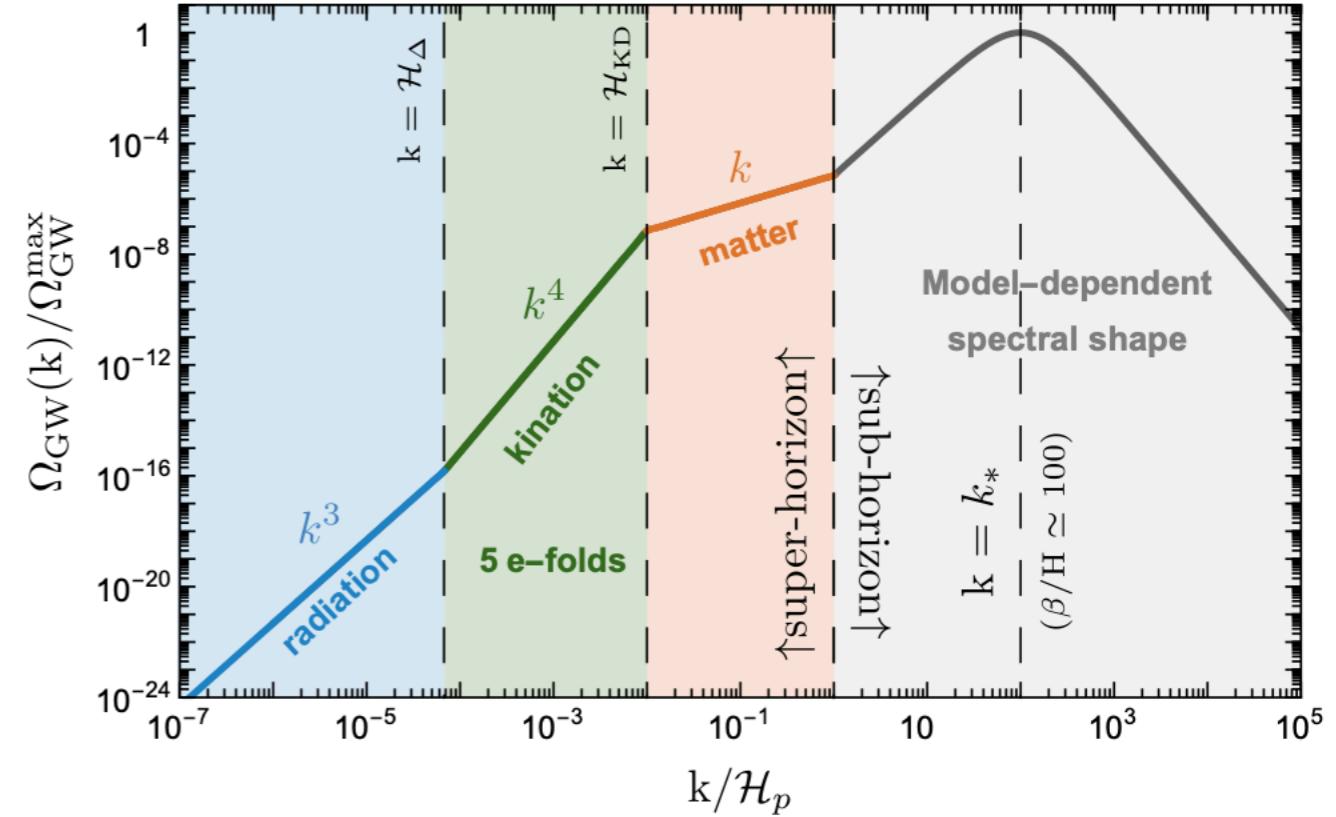
During the matter-kination era, Universe has smaller size, smaller bubbles, and thus weaker GW.

GW from phase transition

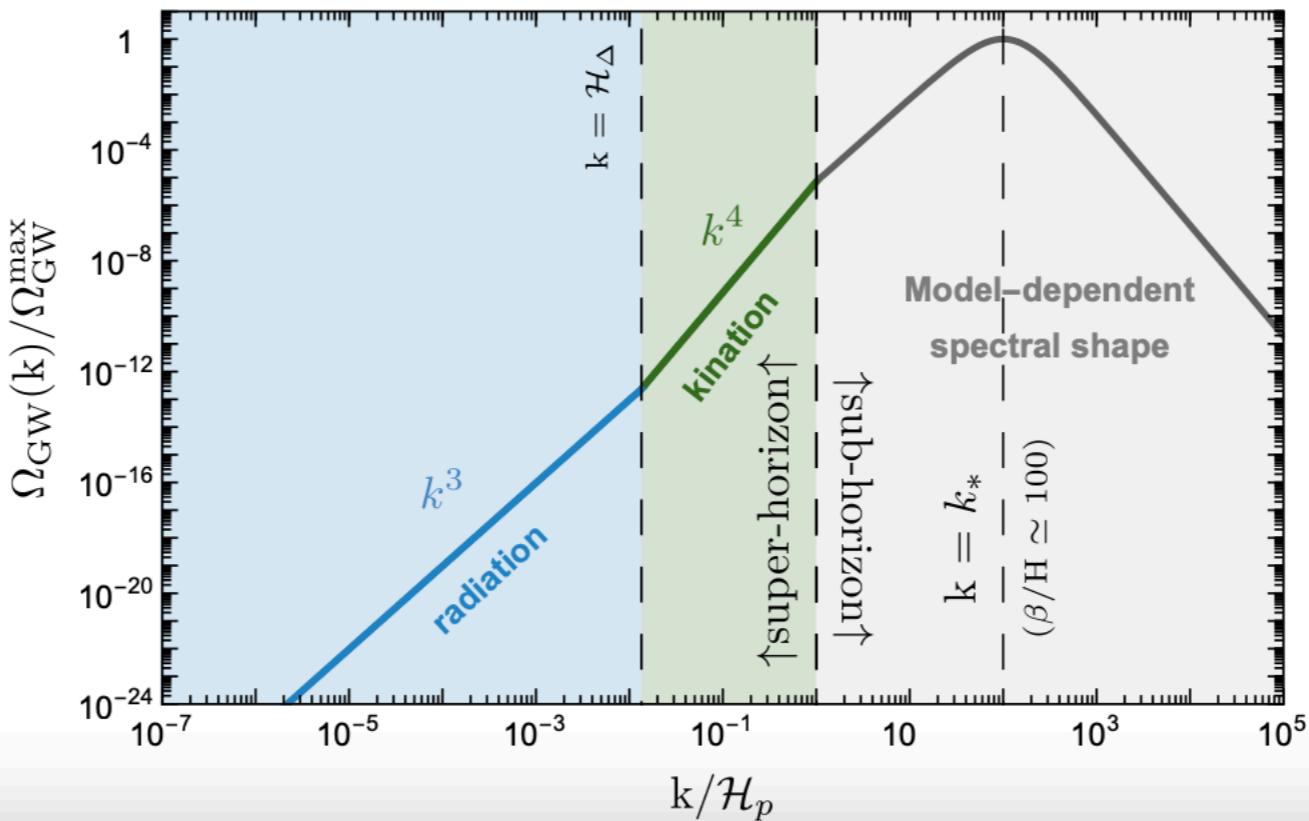
PT occurring before matter-kination era



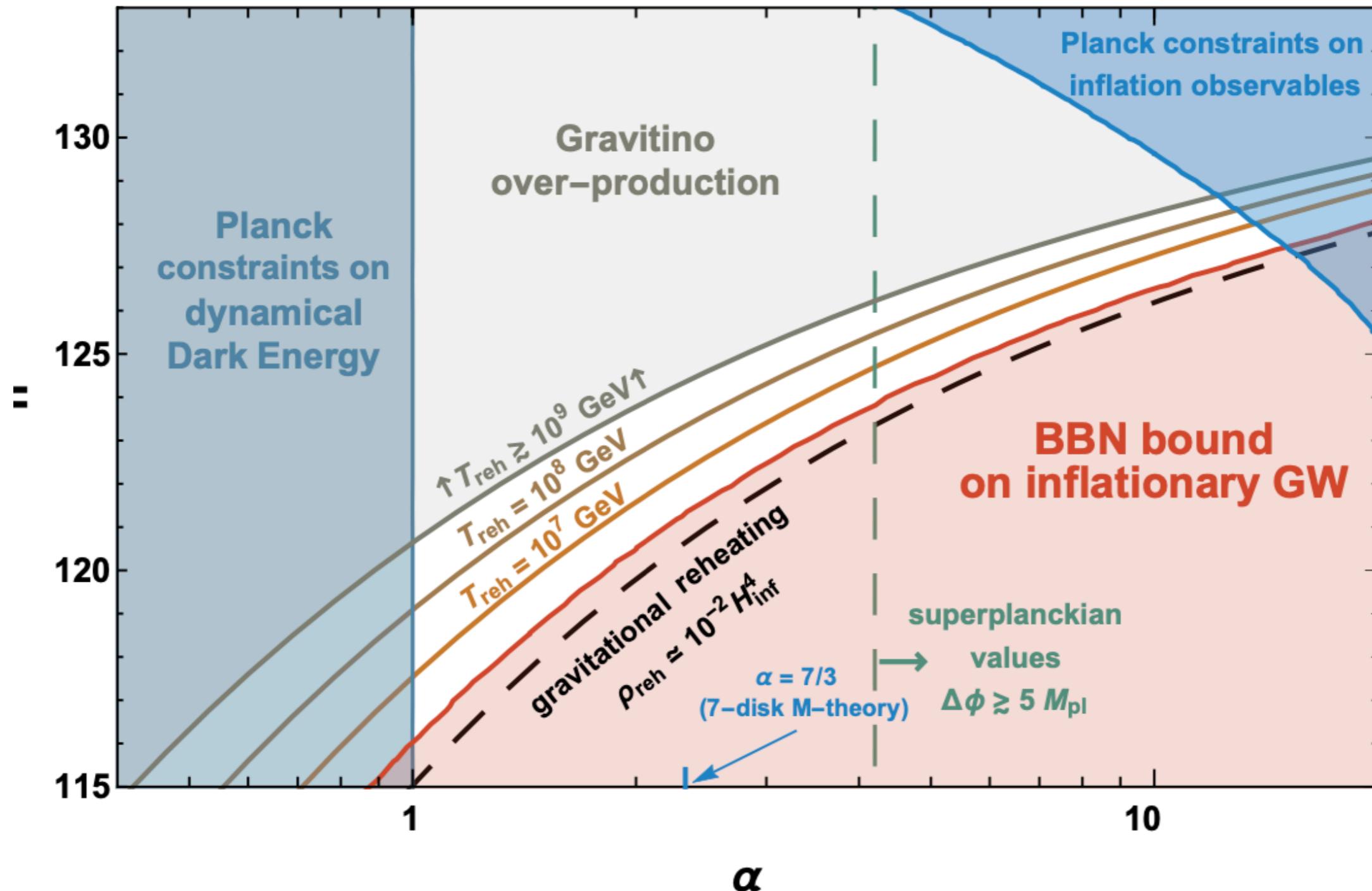
PT occurring during matter era



PT occurring during kination era



Quintessencial inflation with α -attractor

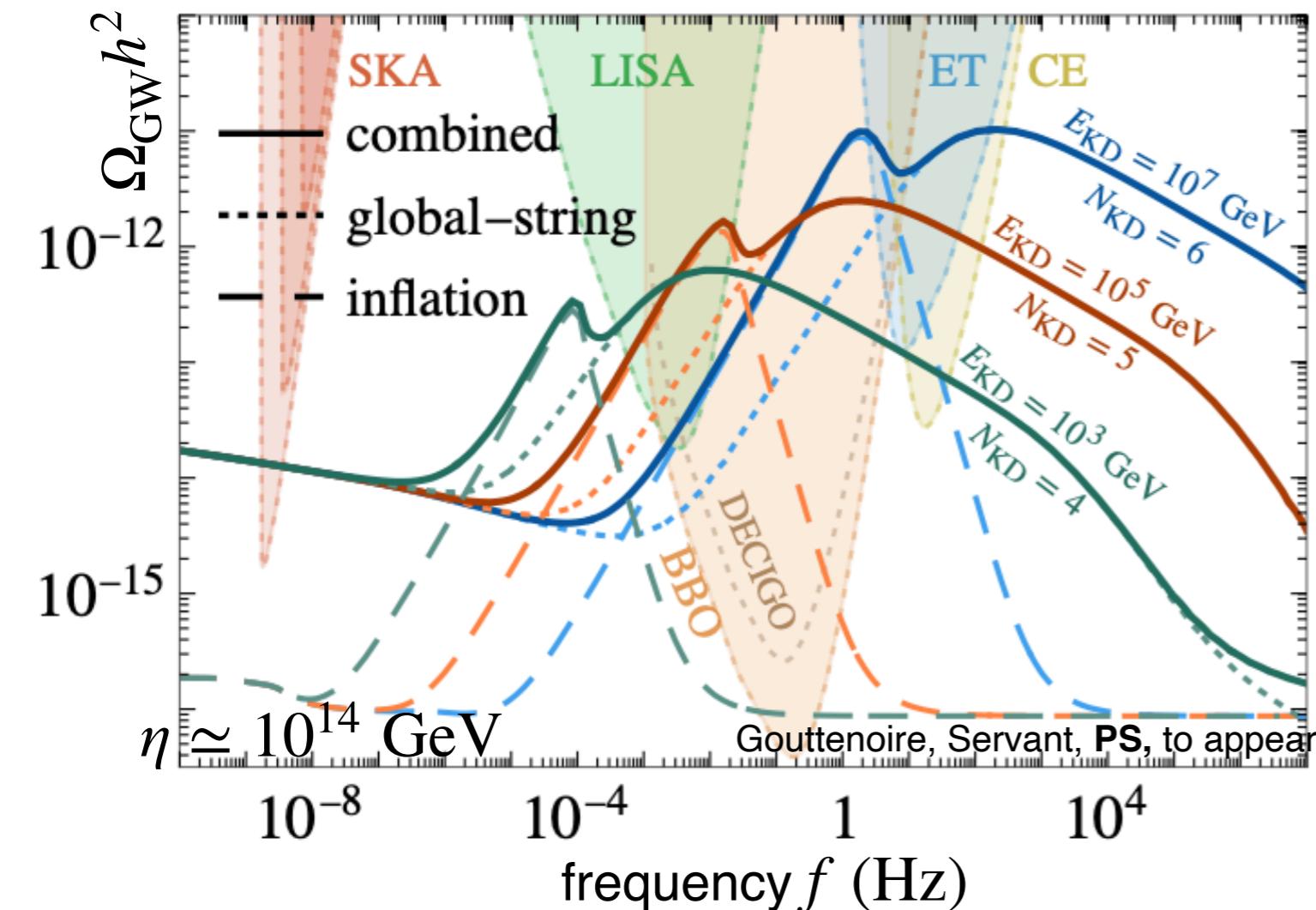


Inflation + global cosmic strings

String network formed at energy scale η
 continuously produces loops which decay into GW (and also particles.)

E.g. Axionic strings from PQ symmetry breaking with $\eta \sim f_a$.

peak amplitude from global strings: $\Omega_{\text{peak}}^{\text{glob}} h^2 \approx 10^{-14} \left(\frac{\eta}{10^{15} \text{ GeV}} \right)^4 \left[\frac{\exp(2N_{\text{KD}})}{10^4} \right] \log^3(\dots)$



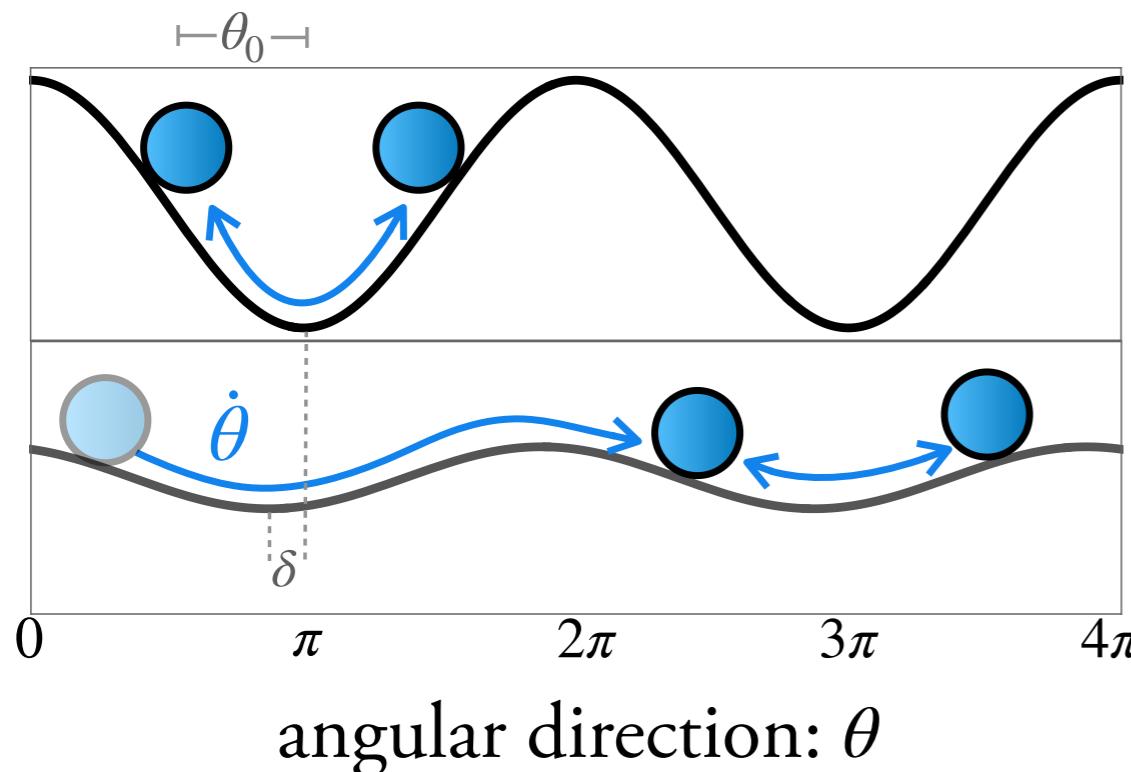
Fixed peak separation
 $f_{\text{inf}}/f_{\text{glob}} = \mathcal{O}(10^{-2})$
 [for loops' size: $(0.1)H^{-1}$]

With $E_{\text{inf}} \sim 10^{16} \text{ GeV}$,
two-peak signature
 for $10^{12} \lesssim \frac{\eta}{\text{GeV}} \lesssim 10^{15}$.

Model A: trapped misalignment

Model A: Trapped misalignment

[Di Luzio, Gavela, Quilez, Ringwald, '21]

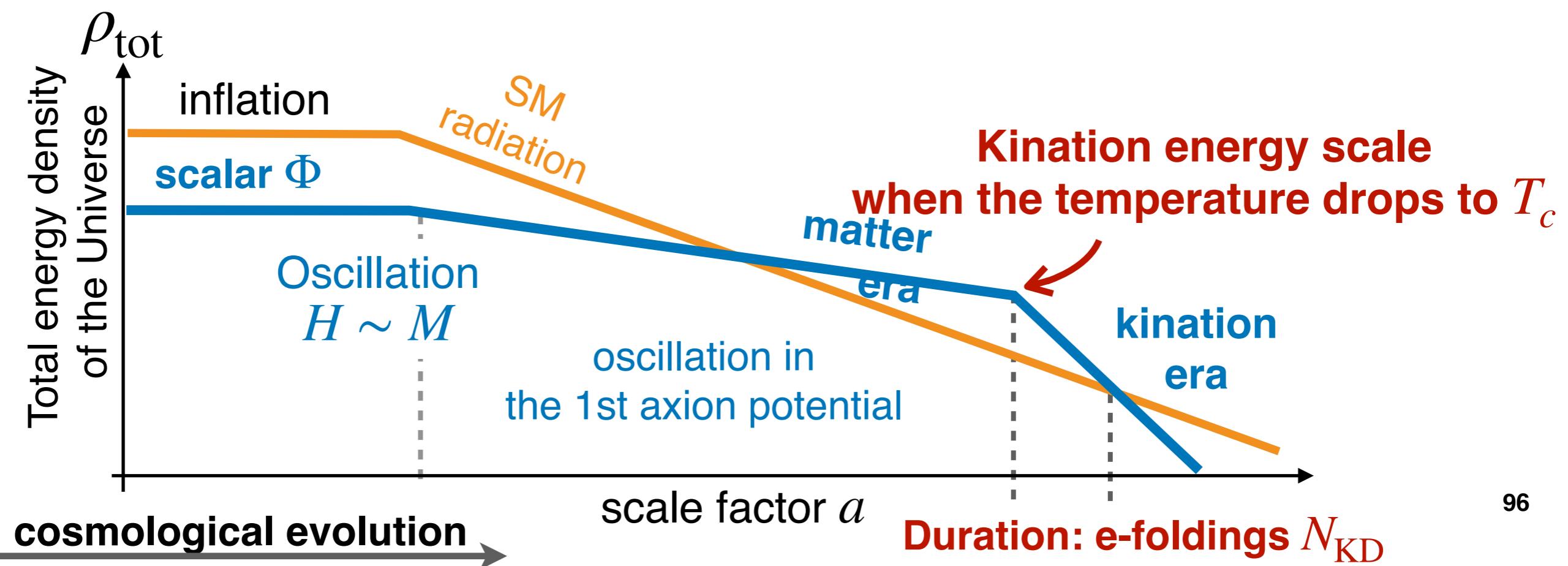


For $T \gtrsim T_c$, $V_{\text{high}} \sim M^2 f_a^2 \cos(\theta)$
axion oscillates and behaves as **matter**.

For $T \lesssim T_c$, $V_{\text{low}} \sim m_a^2 f_a^2 \cos(\theta)$ with $M \gg m_a$

Axion rolls freely with **large initial speed** at T_c

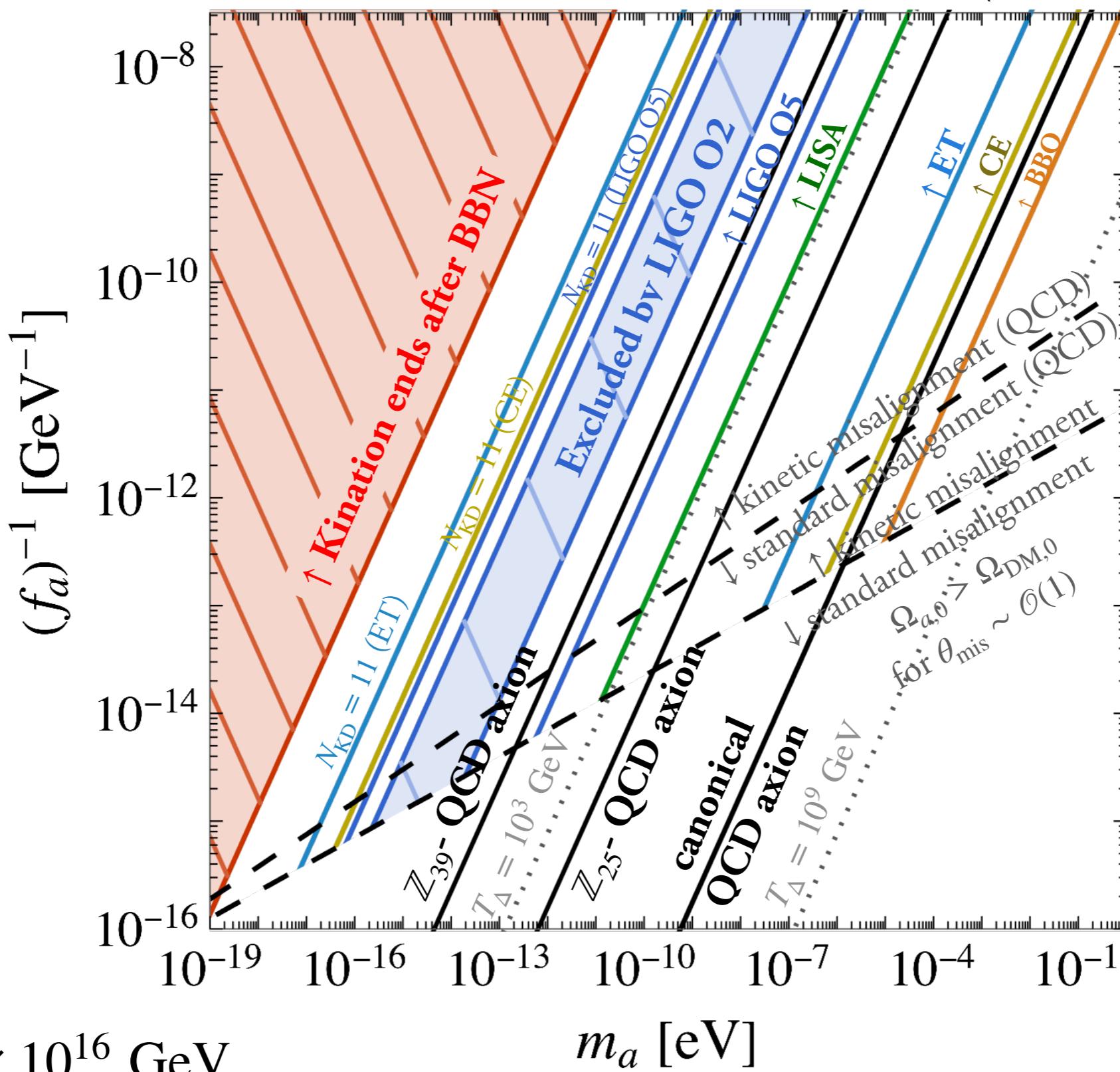
$$\dot{\theta}_c \sim \frac{T_c^{3/2} M^{1/4}}{M_{\text{Pl}}^{3/4}} \text{ and generates kination era.}$$



Detectability in axion parameter spaces

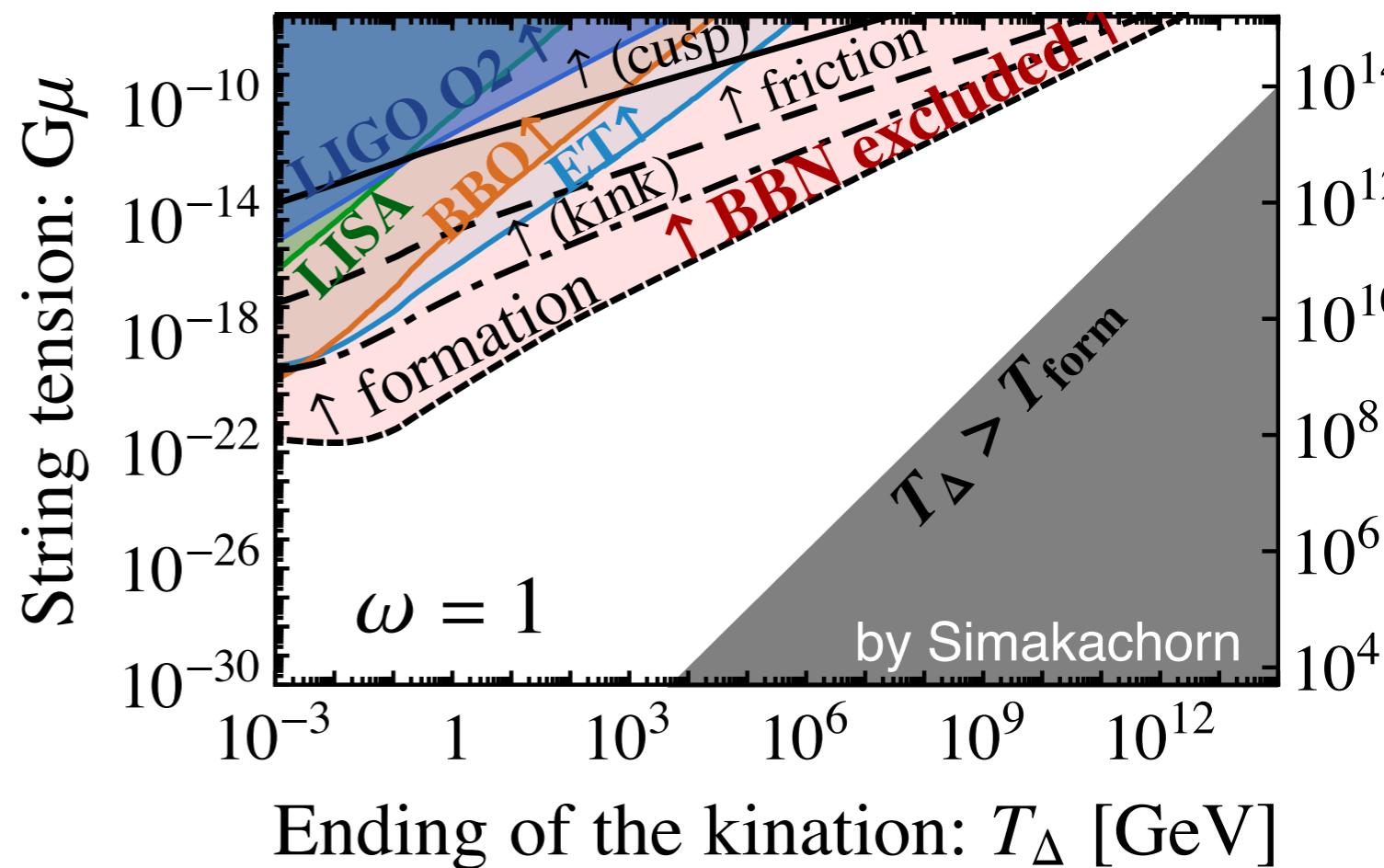
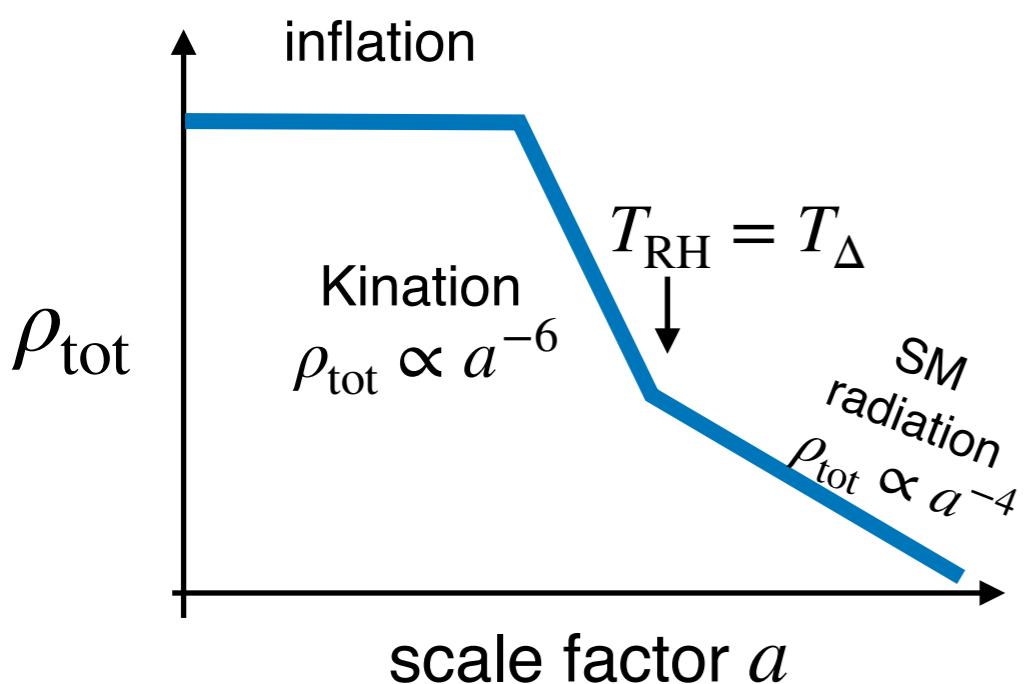
$$\Omega_{a,0} = \Omega_{\text{DM},0}$$

(Gouttenoire, Servant, PS, to appear)



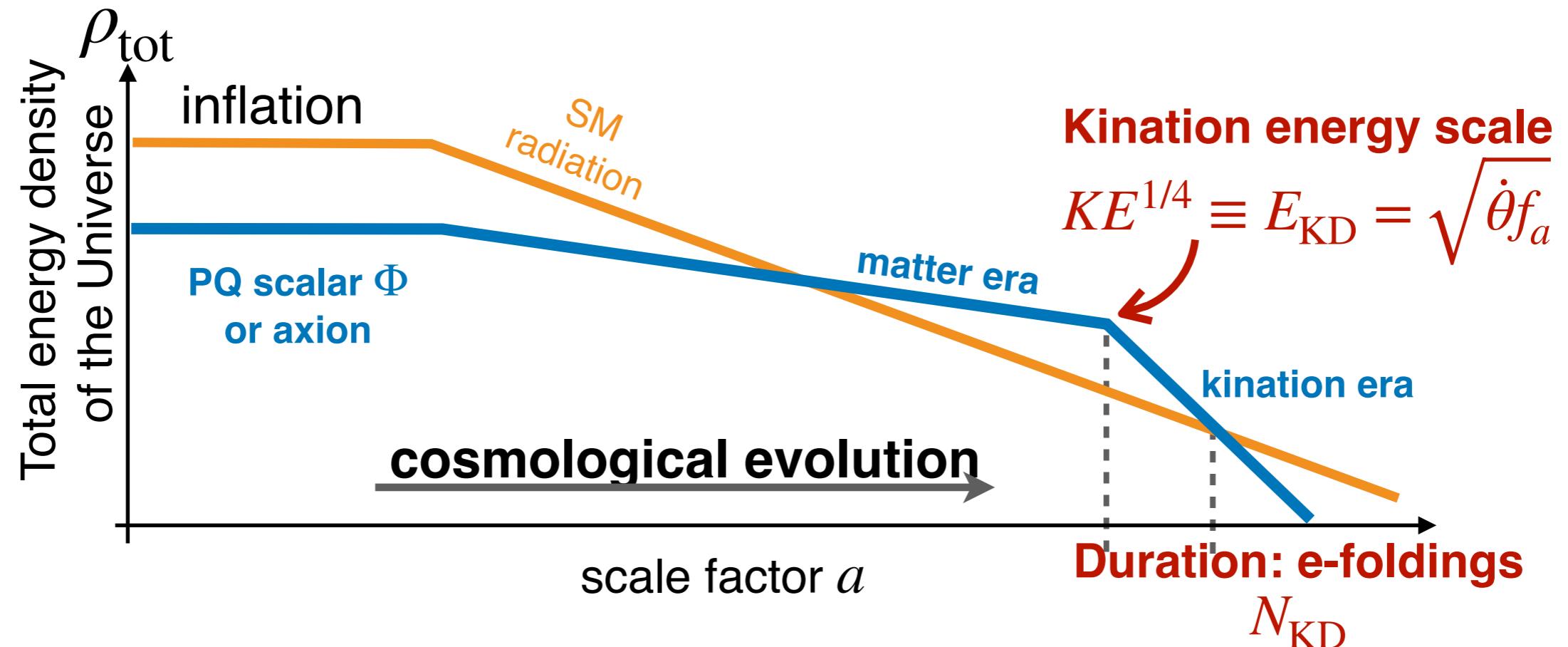
Long Kination \Rightarrow too much GW

GW from local cosmic strings



The cut-off of the cosmic-string GW is crucial for the BBN constraint.
No well-motivated model that generates cosmic strings during
kination ?

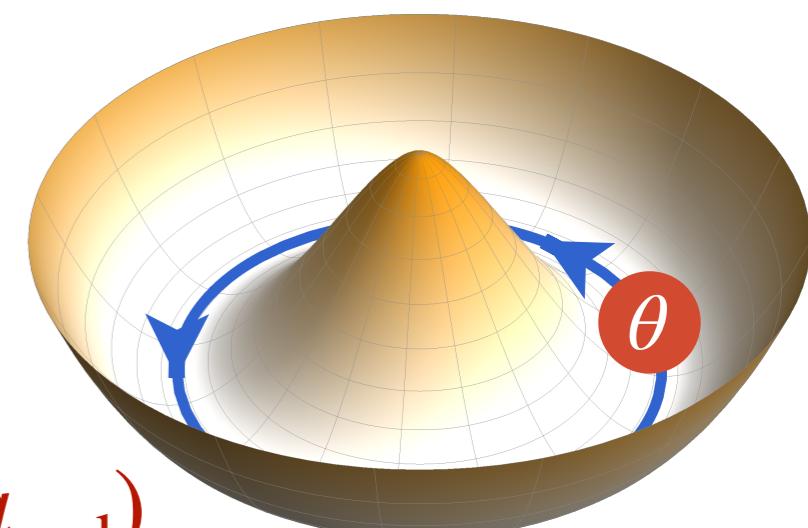
Model-independent kination from spinning axion



are characterized by
(given the spontaneous symmetry-breaking scale f_a)

1. **kination energy scale** $E_{\text{KD}} = \sqrt{\dot{\theta} f_a}$

(the **spinning speed** of axion $\dot{\theta}$ when kination starts)



2. **the duration of kination era** $N_{\text{KD}} = \log(a_{\text{start}}/a_{\text{end}})$
(related to the beginning of the matter era)