

# Form Factors in Higgs Couplings from BSM Physics

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# Outline

- 1. Higgs Form Factors**
- 2. Form Factor Examples**
- 3. Signals at the LHC**
- 4. Conclusions**

# The Higgs at the LHC

**Hierarchy problem** → Resonances at the TeVs

**Future of the LHC:** First **precision** then **Energy**

BSM → Deviations in the Higgs couplings

- κ framework
- EFTs (SMEFT ,...)

 **Constant shifts**

# Higgs Form Factors

**Higgs Form Factors** = (Non-local) BSM momentum dependence in the Higgs couplings

Examples → Model dependent approach to momentum effects

→ Complementary to the EFT program

# Higgs Form Factors

- Heavy BSM physics  $\sim \mathcal{O}\left(\frac{v^2}{M^2}\right)$  (On-shell) i.e. CHMs with  $\xi = \frac{v^2}{f^2}$ ,  
2HDM with  $\tan \alpha \simeq \frac{v^2}{M_\pm^2}$ , etc...
- Off-shell effects  $\sim \mathcal{O}\left(\frac{q^2}{M^2}\right)$

$$c_{h,X}(q_h, p) = c_{h,X}^{\text{SM}} \kappa_X F(q_h, p)$$

**On-shell normalization:**  $F(0, m_X) = 1$



**Off-shellness to disentangle  $q^2$  effects**

# Example: Composite Higgs

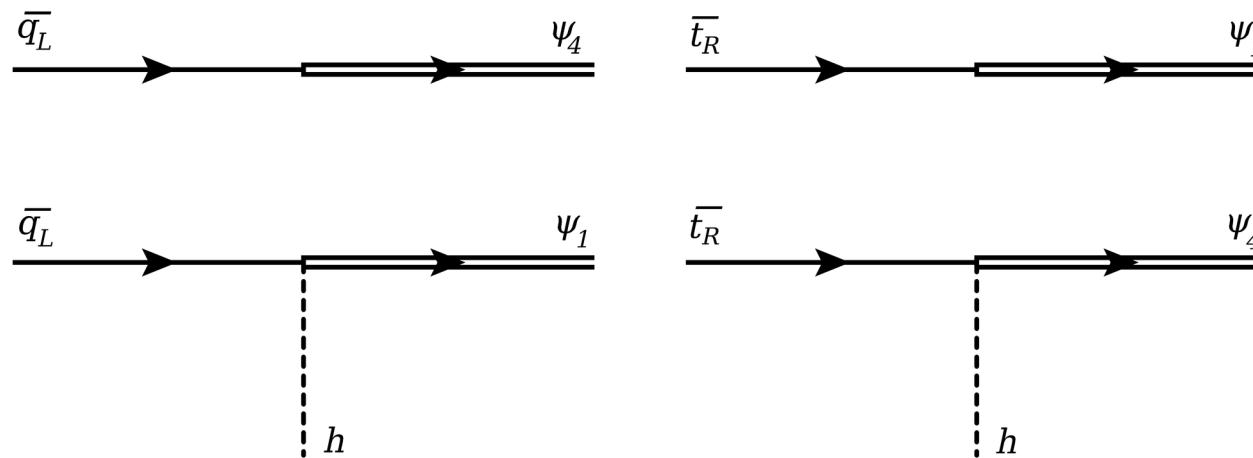
Composite Higgs: **pNGB** from a new strongly interacting sector

EWSB is triggered by explicit breakings that generate the Higgs couplings and its potential

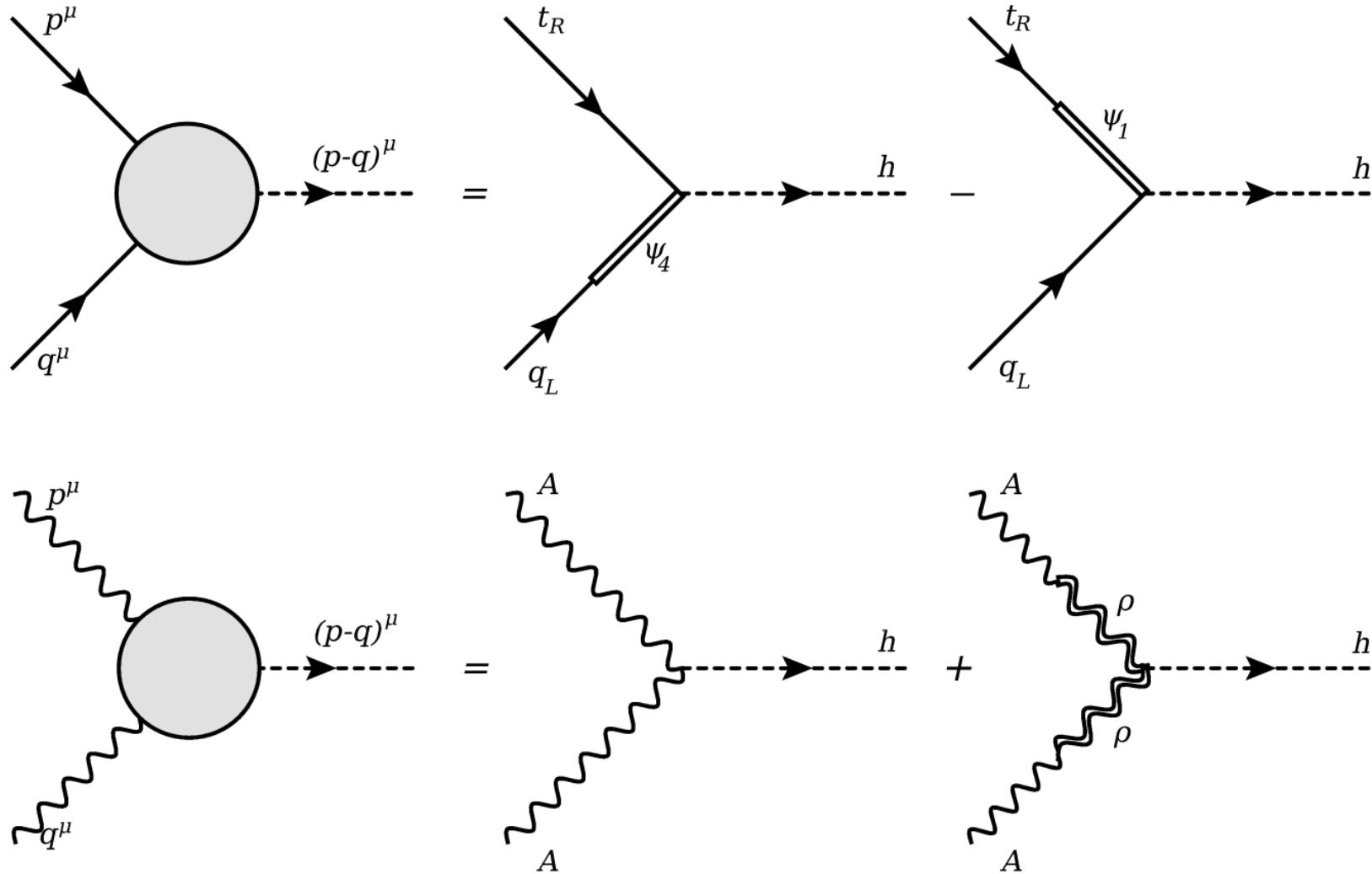
**Not any breaking:**

Top and the gauge bosons mix with their composite partners

**MCHM<sub>5</sub> partial compositeness:**



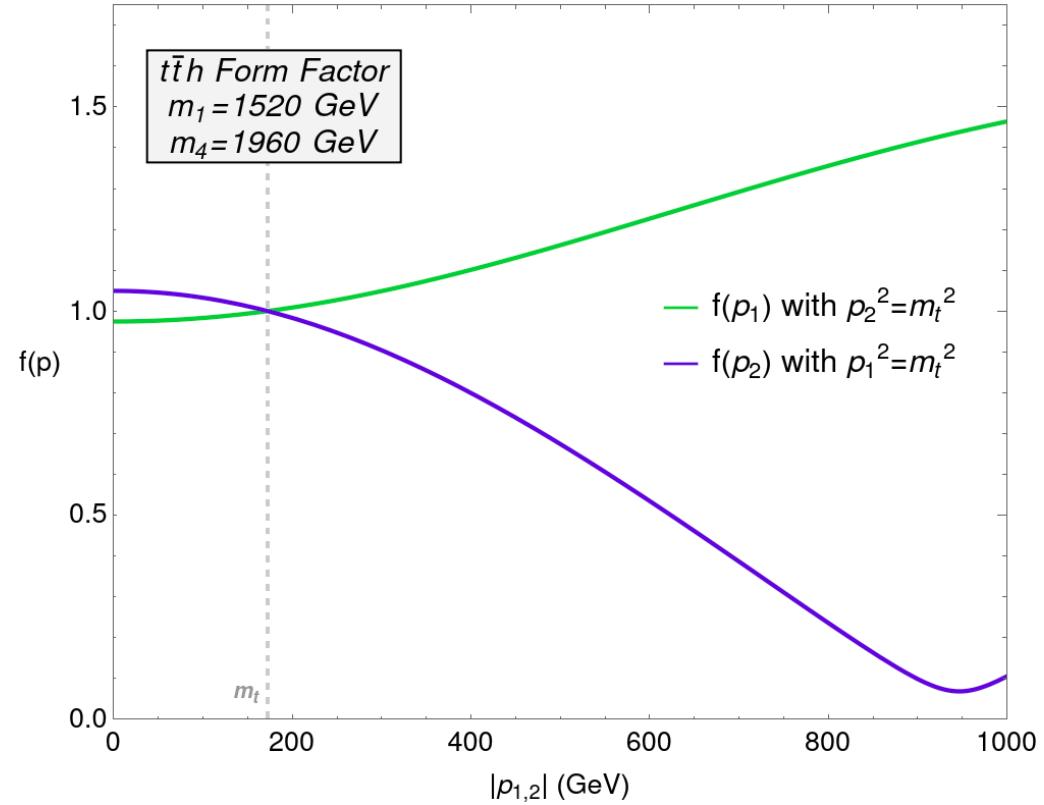
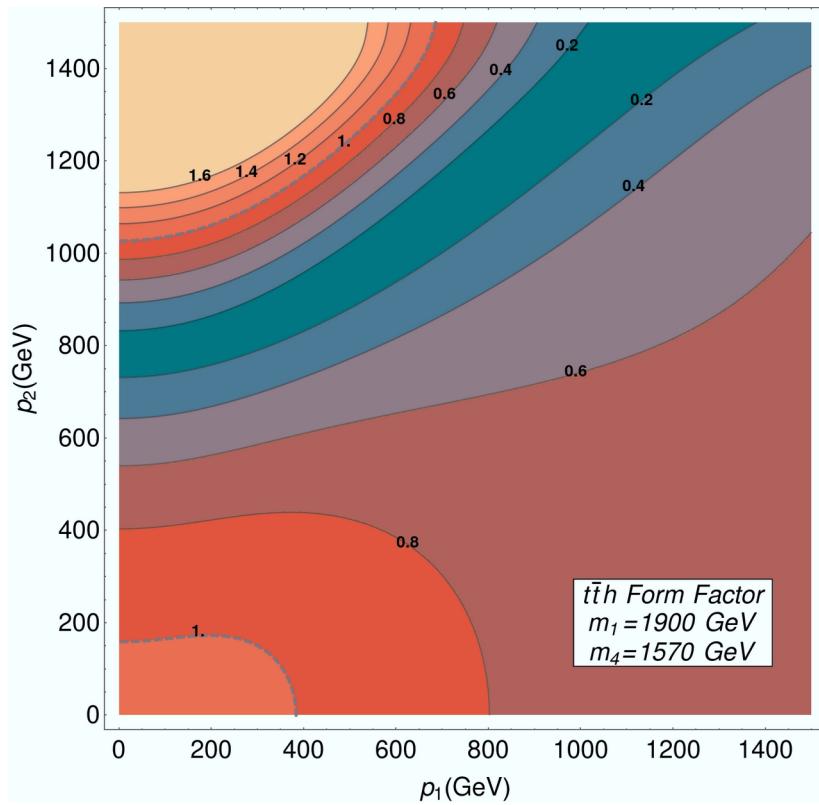
# Example: Composite Higgs



# Example: Composite Higgs

$$\frac{f_{t\bar{t}h}(p_1, p_2)}{y_t} = \left(1 - \frac{M_L(p_1) - m_t}{p_1 - m_t}\right)^{-1} \left(1 - \frac{M_R(p_2) - m_t}{p_2 - m_t}\right)^{-1}$$

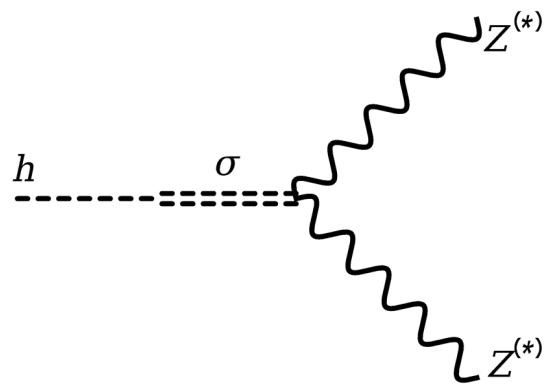
$$\frac{M(p_1, p_2) (1 - 2\xi) / \sqrt{2}}{\left(\Pi_0^L(p) + \Pi_1^L(p) \frac{1}{2} \langle S_h^2 \rangle\right) \left(\Pi_0^R(q) + \Pi_1^R(q) \langle C_h^2 \rangle\right)}.$$



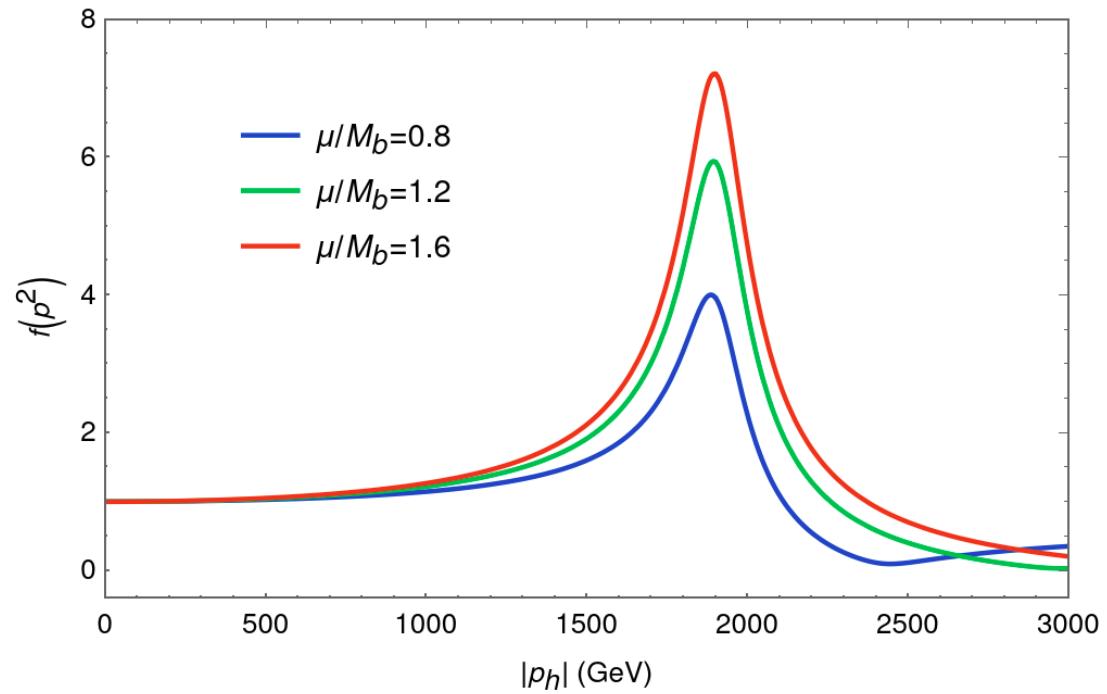
# Example: Scalar Form Factor

CHMs → Illustrative but not exhaustive

Mixing with a Scalar to generate the Higgs couplings:  $- \mu^2 (H_a^\dagger H_b + h.c.)$



$$f_{hVV}(q^2) = \frac{g_V^2 v}{2} \left( 1 - \frac{\mu^4}{M_b^2} \frac{1}{q^2 - M_b^2} \right)$$



# Example: Unparticle Form Factor

No resonances in the LHC so far

- Form factor examples presented so far have **poles**
- Explore effects from the continuum part of the amplitude → **Branch cuts**

Assume a **new conformal sector**

CFT is broken at a scale  $\mu$

Scalar unparticle operator:  $\phi(x), d$

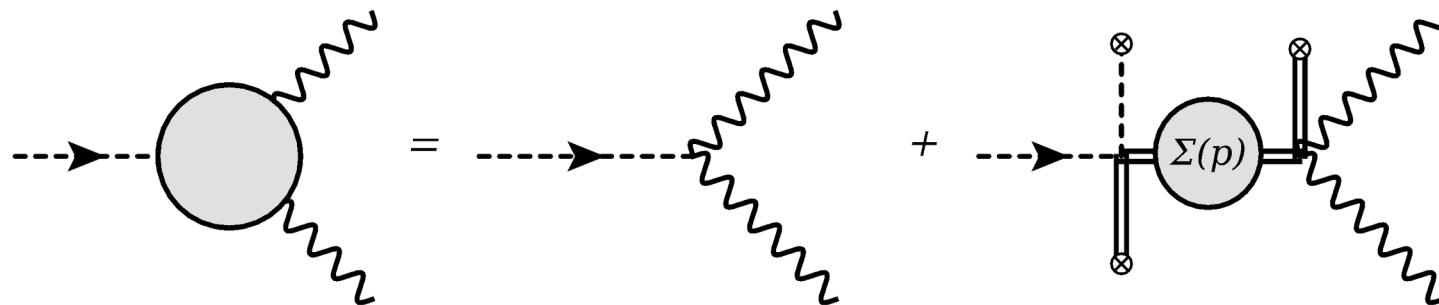
**Unparticle scalar 2-point function:**  $\Delta(p, \mu, d) = \frac{A_d}{2 \sin d\pi} \frac{i}{(\mu^2 - p^2 - i\epsilon)^{2-d}}$

Unscalar with the same quantum numbers as the Higgs.

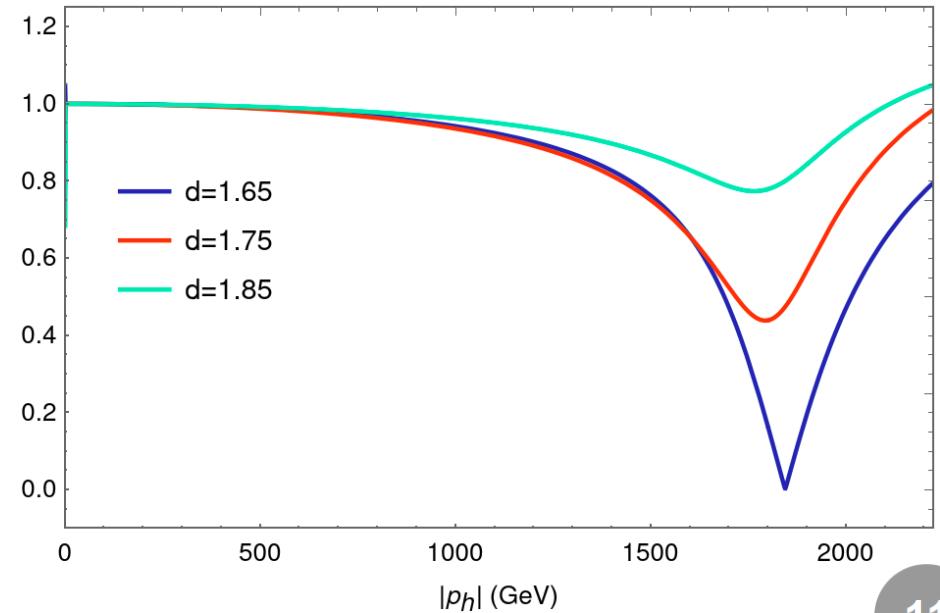
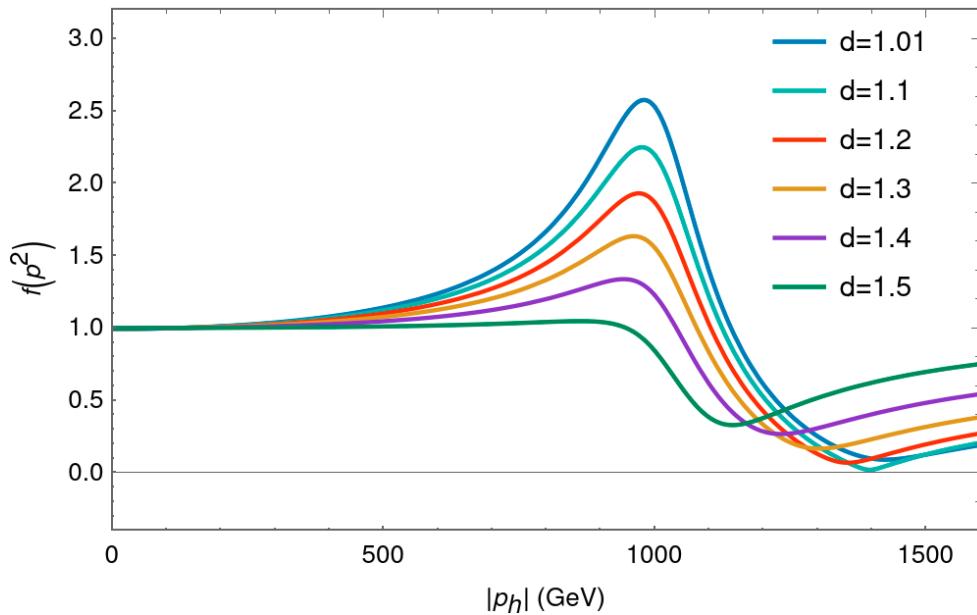
$$S_{NL} = \int d^4x \left\{ \phi^\dagger (D^2 - m^2)^{2-d} \phi - \lambda_t \bar{u}_R \frac{\phi^\dagger}{\Lambda^{d-1}} q_L + h.c. + \alpha |H|^2 \frac{|\phi|^2}{\Lambda^{2(d-1)}} \right\}$$

(Mandelstam's Method)

# Example: Unparticle Form Factor

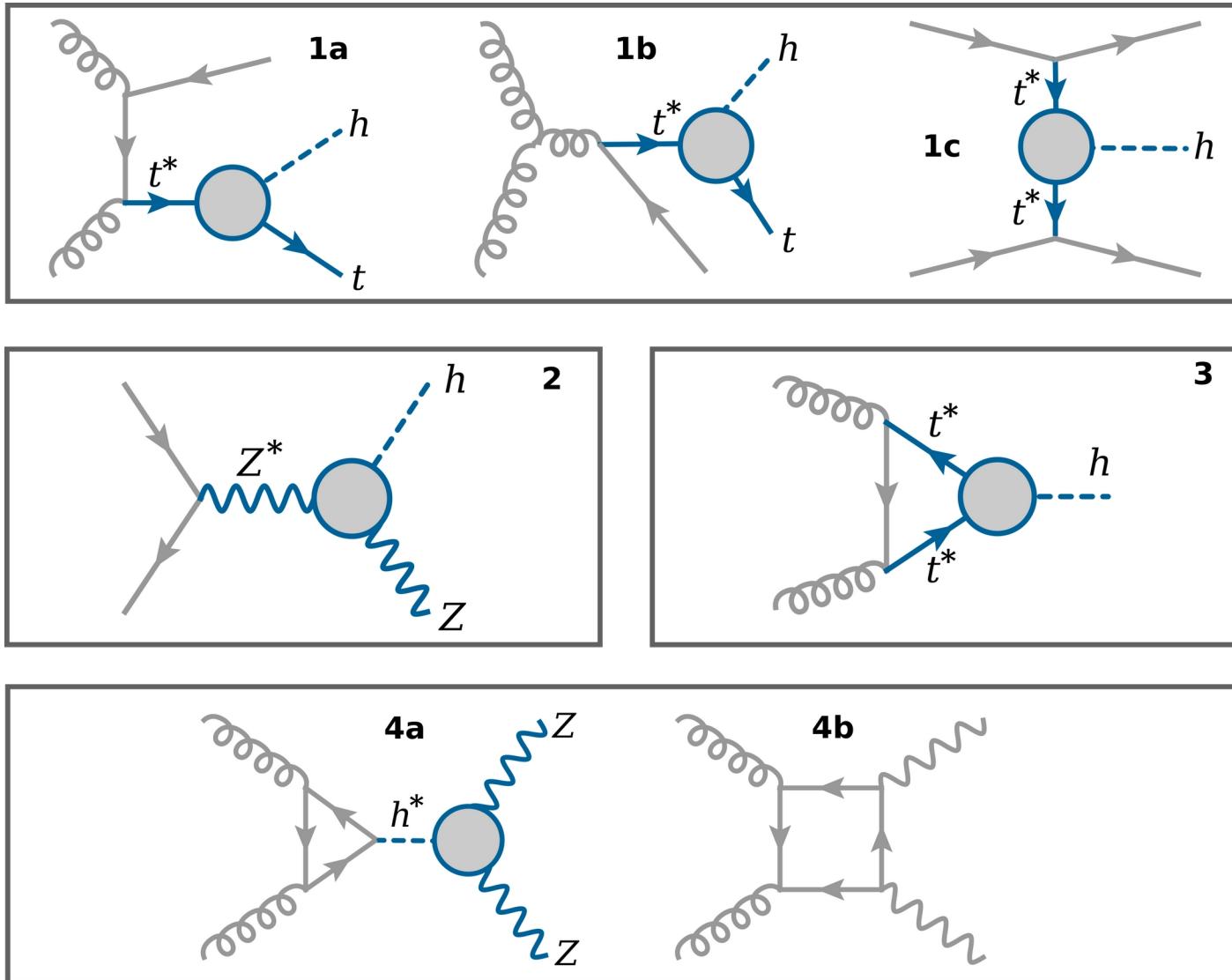


$$f_{unp}(p, q_1, q_2) = \frac{g^2 v}{2c_w^2} + \frac{\alpha v f^{2d}}{\Lambda^{2(d-1)}} \frac{g_*^2}{2} \frac{A_d}{2 \sin d\pi} \frac{i\mathcal{F}(0, q_1 + q_2)}{(p_h^2 - m^2)^{2-d}}$$



# Signals at the LHC

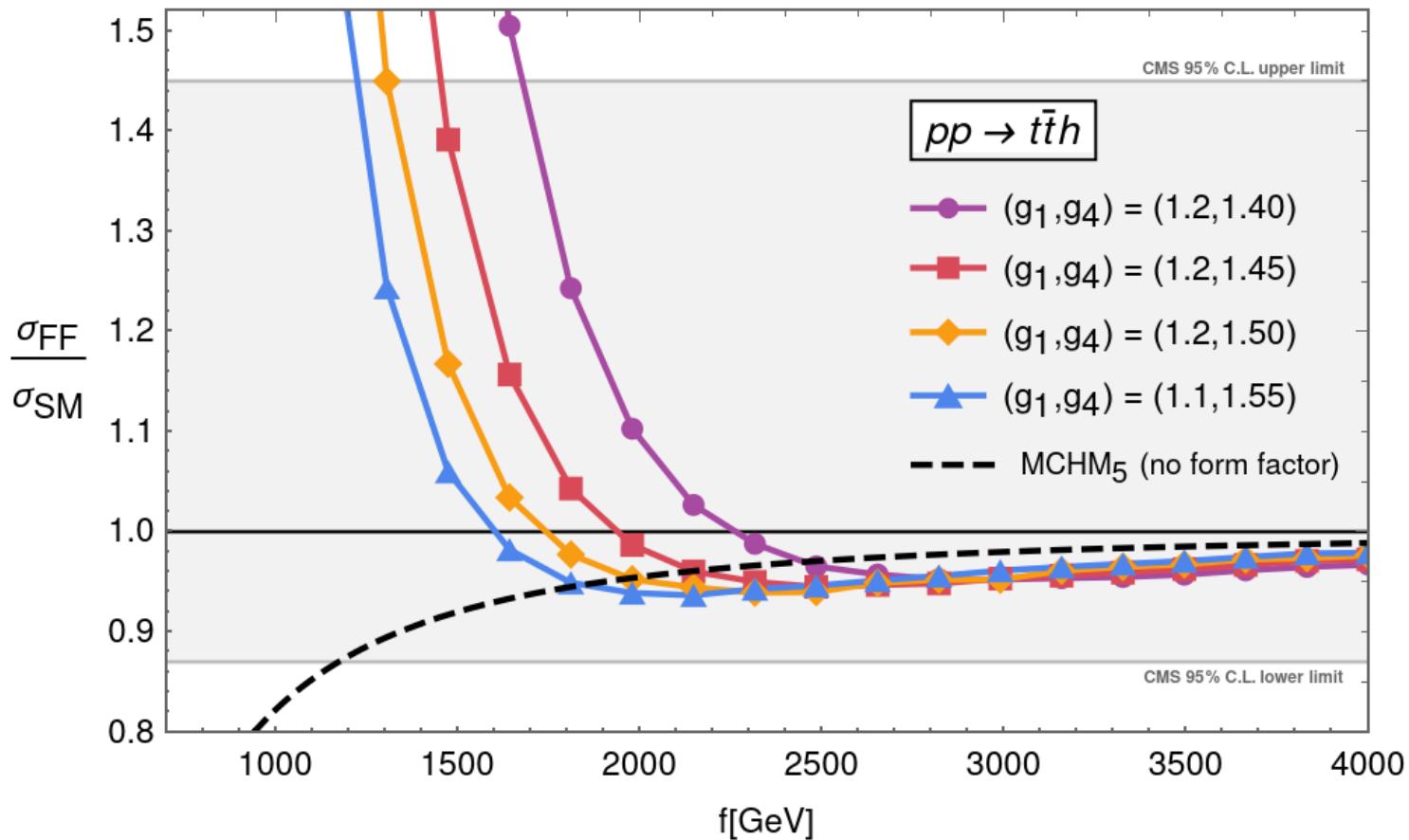
## Off-shell probes to the form factors



# Signals at the LHC

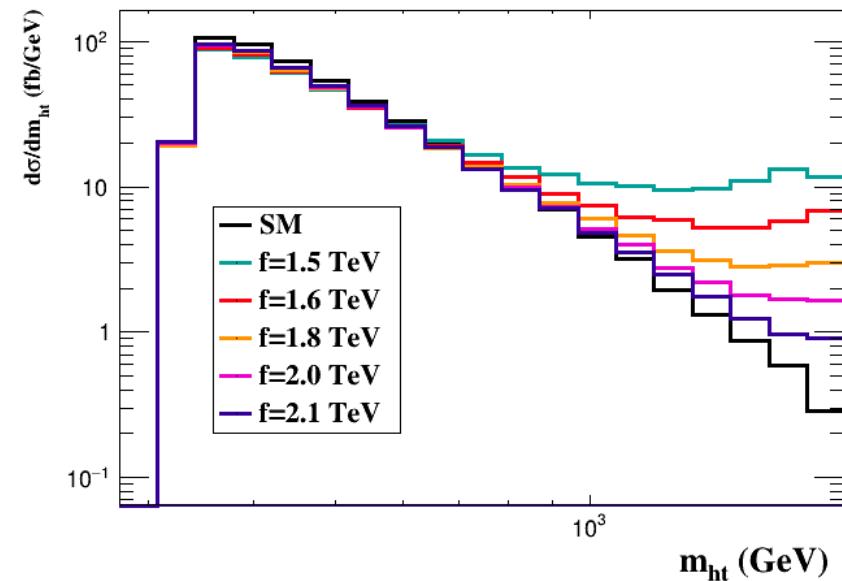
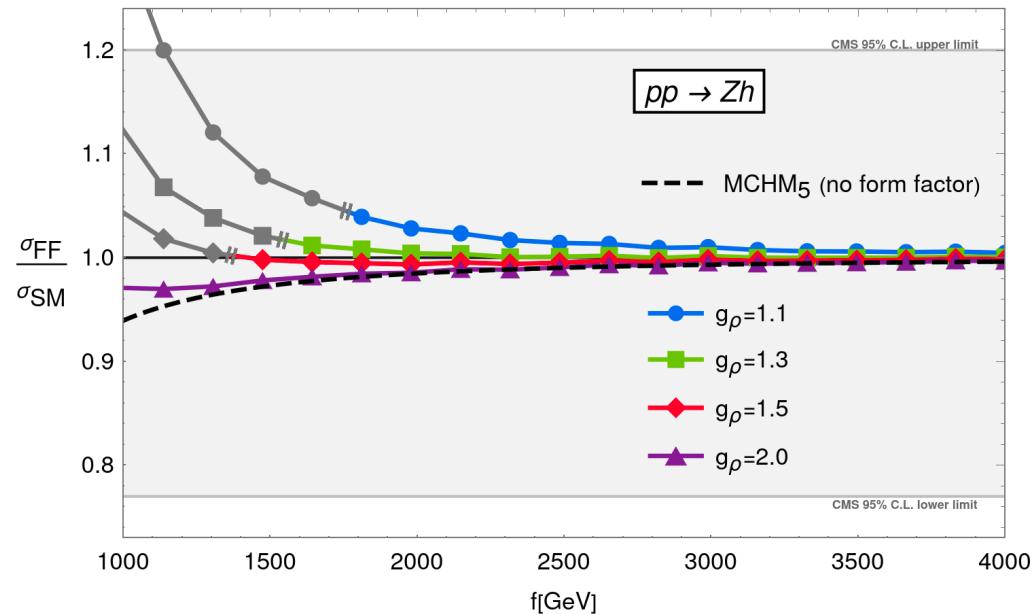
- Implementation of form factors in MadGraph5\_aMC@NLO
- Signal modification: Reach of LHC will be left for future work

## MCHM<sub>5</sub> tth Signal

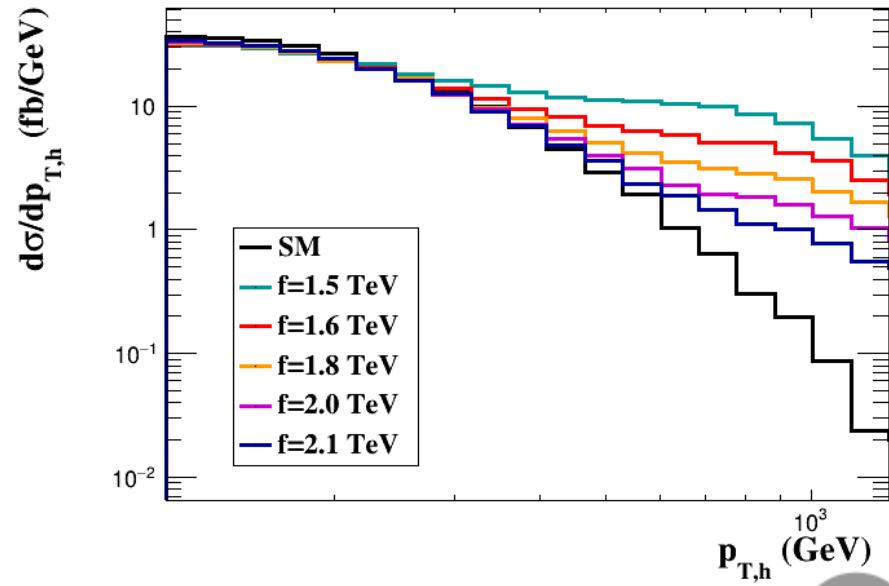


$$\kappa_\xi^5 = \frac{1 - 2\xi}{\sqrt{1 - \xi}}$$
$$\xi = v^2/f^2$$

# Signals at the LHC

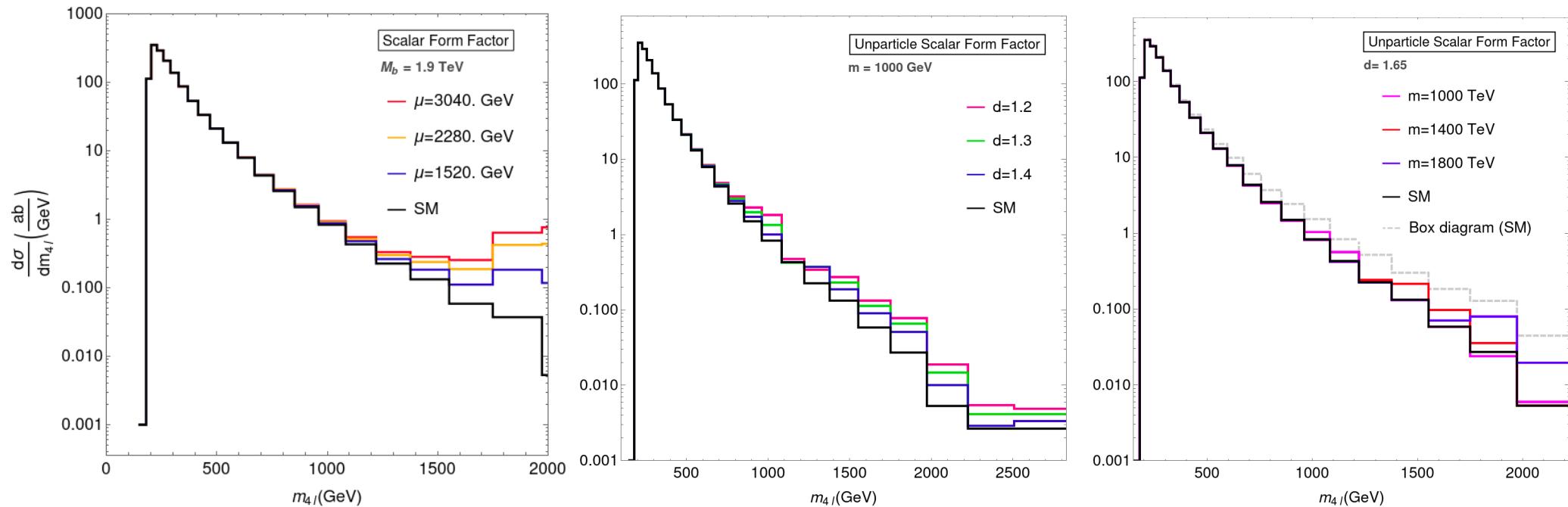


- Momentum effects do not decouple from the on-shell modifications
- Shape modification of Kinematic distributions: Trademark of composite objects



# Example: Composite Higgs

**pp → 4l:**  $\frac{d\sigma}{dm_{4l}} = |F(m_{4l})|^2 \frac{d\sigma_{h^*}}{dm_{4l}} + |F(m_{4l})| \frac{d\sigma_{int}}{dm_{4l}} + \frac{d\sigma_{box}}{dm_{4l}}$



**Interference:**

Both an enhancement and a suppression in the form factor lead to an enhanced signal

# Conclusions

- Precision at **future LHC**
- Form Factors as a **model dependent approach** to pinpoint momentum effects
- Need **off-shell channels** (off-shell top, W, Z and h)
- CHM momentum effects do **not decouple at low energies**
- Framework for **non-resonant phenomena**. Continuum effects, CFTs and unparticles

# Thank you!

A night photograph of the Eiffel Tower and the Pont Alexandre III in Paris. In the foreground, a modern boat with a curved glass roof is illuminated from within, reflecting light on the water. The Eiffel Tower stands tall in the background, its lights visible against the dark sky. The Pont Alexandre III bridge is also visible, with its ornate pillars and golden statues. The overall atmosphere is romantic and atmospheric.

**PLANCK 2022**

*Paris, May 30 - June 3, 2022*

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*Photo By Karim Benakli*

# References

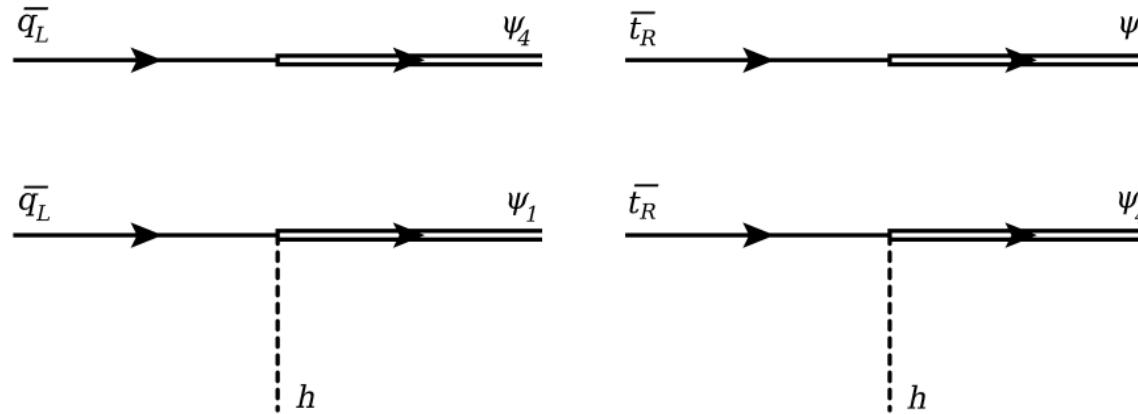
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# Backup: MCHM<sub>5</sub> Form Factors

$$U[h] = \exp \left( \frac{i\sqrt{2}}{f} h^{\hat{a}} T^{\hat{a}} \right) \quad q_L^5 = \begin{pmatrix} -ib_l \\ -b_l \\ -it_l \\ t_l \\ 0 \end{pmatrix} \quad t_r^5 = \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ t_r \end{pmatrix} \quad b_r^5 = \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ b_r \end{pmatrix}.$$

Partial Compositeness:

$$\begin{aligned} \mathcal{L}_{int}^F &= f \left[ y_{L1} (\overline{q}_L^5 U[\pi])_5 \psi_1 + y_{L4} (\overline{q}_L^5 U[\pi])_j \psi_{4,j} \right] + h.c. \\ &+ f \left[ y_{R1} (\overline{t}_r^5 U[\pi])_5 \psi_1 + y_{R4} (\overline{t}_r^5 U[\pi])_j \psi_{4,j} \right] + h.c. \end{aligned}$$



# Backup: MCHM<sub>5</sub> Form Factors

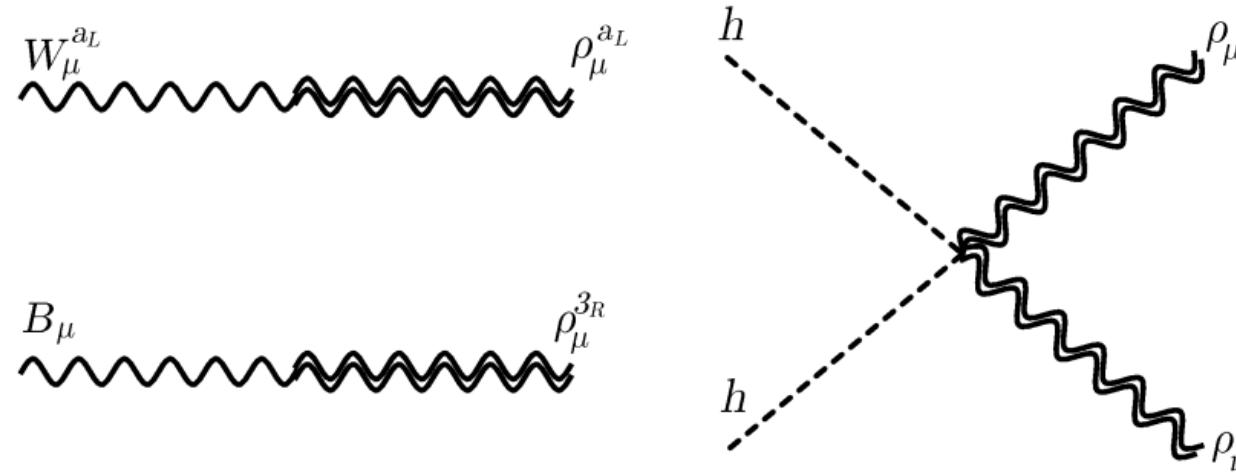
## Form Factor Effective Lagrangian

$$\begin{aligned}\mathcal{L}_{eff}^F = & \overline{q_L} p_1 \left( \Pi_0^L(p_1) + \Pi_1^L(p_1) \frac{S_h^2}{2} \right) q_L + \overline{t_R} p_2 \left( \Pi_0^R(p_2) + \Pi_1^R(p_2) C_h^2 \right) t_R + \\ & + \overline{t_R} \left( M_1(p_1, p_2) \frac{S_h C_h}{\sqrt{2}} \right) q_L,\end{aligned}$$

$$\begin{aligned}\Pi_0^L(p) = 1 + \Pi_{\mathbf{4}}^L(p) &= 1 + \frac{f^2 |y_L|^2}{p^2 - m_4^2}, & \Pi_0^R(p) = 1 + \Pi_{\mathbf{1}}^L(p) &= 1 + \frac{f^2 |y_L|^2}{p^2 - m_1^2} \\ \Pi_1^L(p_1, p_2) = \Pi_{\mathbf{1}}^L(p_1) - \Pi_{\mathbf{4}}^L(p_2) &= f^2 |y_L|^2 \left( \frac{1}{p_1^2 - m_1^2} - \frac{1}{p_2^2 - m_4^2} \right), & L \leftrightarrow R \\ M(p_1, p_2) = M_{\mathbf{4}}(p_1) - M_{\mathbf{1}}(p_2) &= f^2 y_L y_R \left( \frac{m_4}{p_1^2 - m_4^2} - \frac{m_1}{p_2^2 - m_1^2} \right),\end{aligned}$$

# Backup: Hidden Local Symmetry

$$\begin{aligned}\mathcal{L}_{CS}^V &= -\frac{1}{4}\rho_{\mu\nu}^a\rho^{a,\mu\nu} + \frac{m_\rho^2}{2}\rho_\mu^a\rho^{a,\mu} + g_\rho\rho_\mu^a J^{a,\mu} + \frac{g_\rho^2}{2}\rho_\mu^a\rho^{a,\mu}h^2, \\ \mathcal{L}_{ES}^V &= -\frac{1}{4}W_{\mu\nu}^{a_L}W^{a_L,\mu\nu} + g_0W_\mu^{a_L}J^{a_L,\mu} + \frac{g_0^2}{2}W_\mu^{a_L}W^{a_L,\mu}h^2 \\ &\quad -\frac{1}{4}B_{\mu\nu}B^{\mu\nu} + g'_0B_\mu J^{3_R,\mu} + \frac{g'_0^2}{2}B_\mu B^\mu h^2, \\ \mathcal{L}_{int}^V &= \frac{1}{2}\frac{g_0}{g_\rho}W_{\mu\nu}^{a_L}\rho^{a_L,\mu\nu} + \frac{1}{2}\frac{g_0}{g_\rho}B_{\mu\nu}\rho^{3_R,\mu\nu}.\end{aligned}$$



# Backup: Mandelstam's Method

Gauge symmetry in the non-local effective Action → Mandelstam's Method

Introduces a wilson line between two unparticle fields. Then, compute the fourth functional derivative to obtain the Higgs-Gauge vertex

$$ig^2 \Gamma^{ab\alpha\beta}(p, q_1, q_2) = \frac{\delta^4 S_{\text{NL}}}{\delta A^{a\alpha}(q_1)\delta A^{b\beta}(q_2)\delta\phi^\dagger(p+q_1+q_2)\delta\phi(p)}$$
$$\begin{aligned} & ig^2 \left\{ \left( T^a T^b + T^b T^a \right) g^{\alpha\beta} \mathcal{F}(p, q_1 + q_2) \right. \\ & + T^a T^b \frac{(2p + q_2)^\beta (2p + 2q_2 + q_1)^\alpha}{q_1^2 + 2(p + q_2) \cdot q_1} [\mathcal{F}(p, q_1 + q_2) - \mathcal{F}(p, q_2)] \\ & \left. + T^b T^a \frac{(2p + q_1)^\alpha (2p + 2q_1 + q_2)^\beta}{q_2^2 + 2(p + q_1) \cdot q_2} [\mathcal{F}(p, q_1 + q_2) - \mathcal{F}(p, q_1)] \right\} \end{aligned}$$

$$\mathcal{F}(p, q) = - \frac{(m^2 - (p+q)^2)^{2-d} - (m^2 - p^2)^{2-d}}{q^2 + 2p \cdot q}$$

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