

Origin of matter in a black hole-cosmic string landscape

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Operational Programme Research,
Development and Education



Presentation take away

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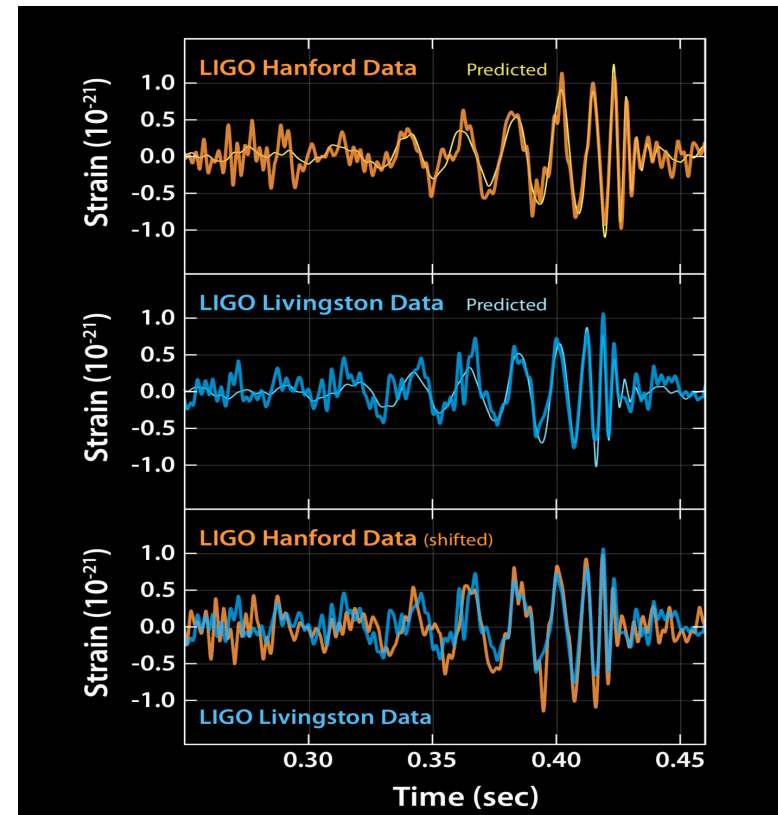
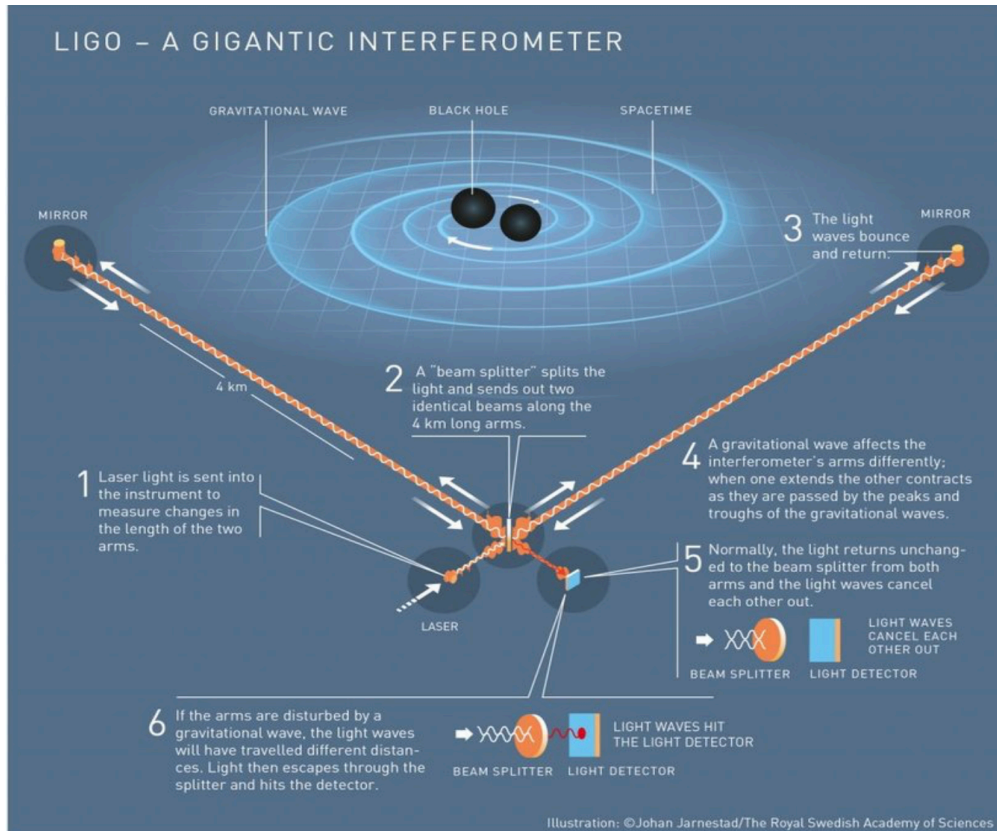
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1. Ultralight primordial black hole can produce super heavy dark matter. **If the dark matter gets its mass with a gauged U(1)-breaking**, gravitational waves and their spectral features could be a unique way to probe dark matter above 10^9 GeV.
2. **If the recent finding by the pulsar timing arrays** corresponds to an existence of super heavy dark matter, high frequency detectors like LISA, DECIGO should be able to find a break in the GW spectrum.
3. **When implemented in seesaw**, one of the right-handed neutrinos could be super heavy dark matter and other two lead to thermal leptogenesis.

References

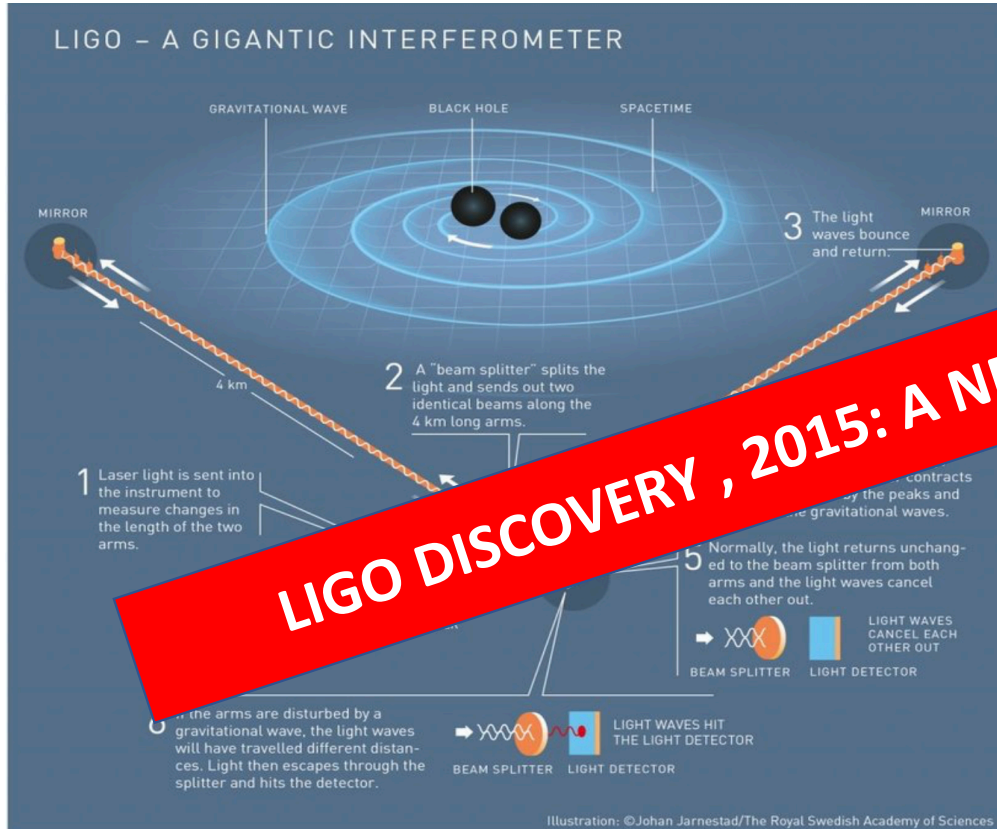
- R. Samanta and F. Urban, JCAP**(2022)*** .
- R. Samanta, D. Borah, S.Das, A Saha, 2202.10474
- R. Samanta and F. Urban, to appear soon.

Hearing from the early universe

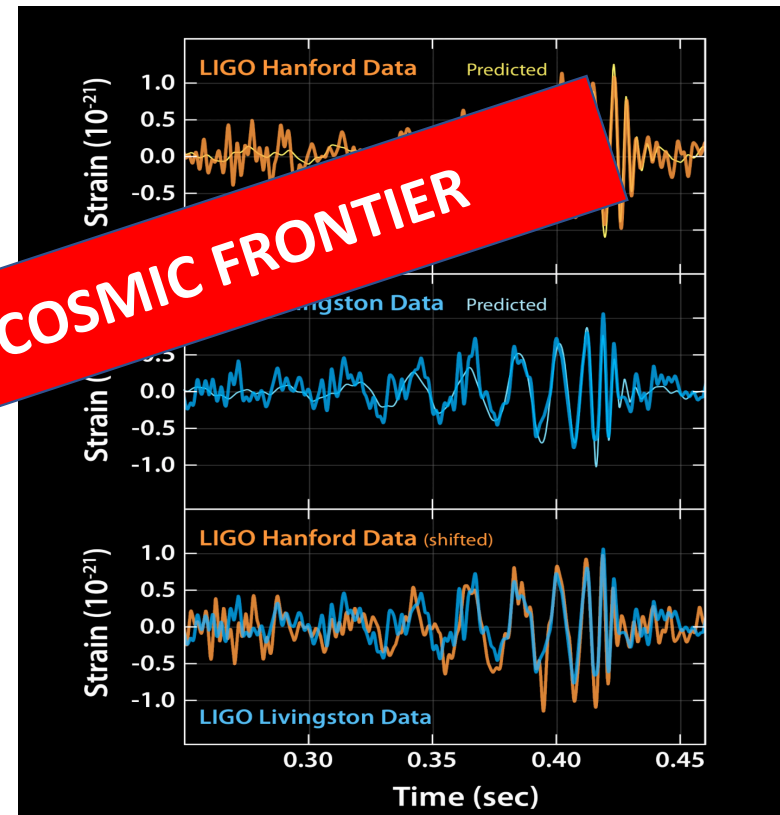


CREDIT: <https://phys.org/news/2019-05-ligo-virgo-neutron-star-smash-ups.html>

Hearing from the early universe



LIGO DISCOVERY, 2015: A NEW COSMIC FRONTIER

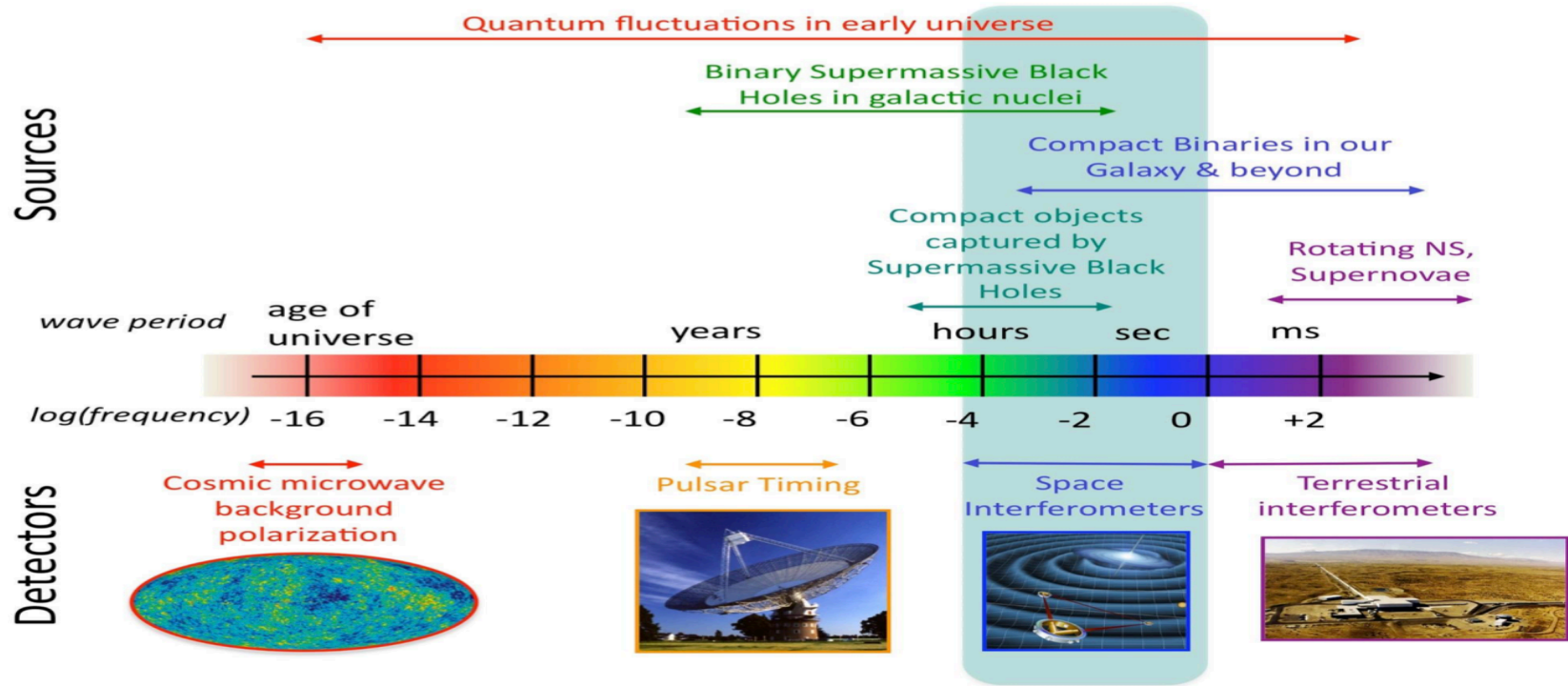


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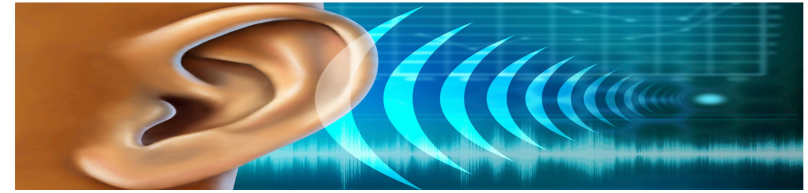


The Gravitational Wave Spectrum

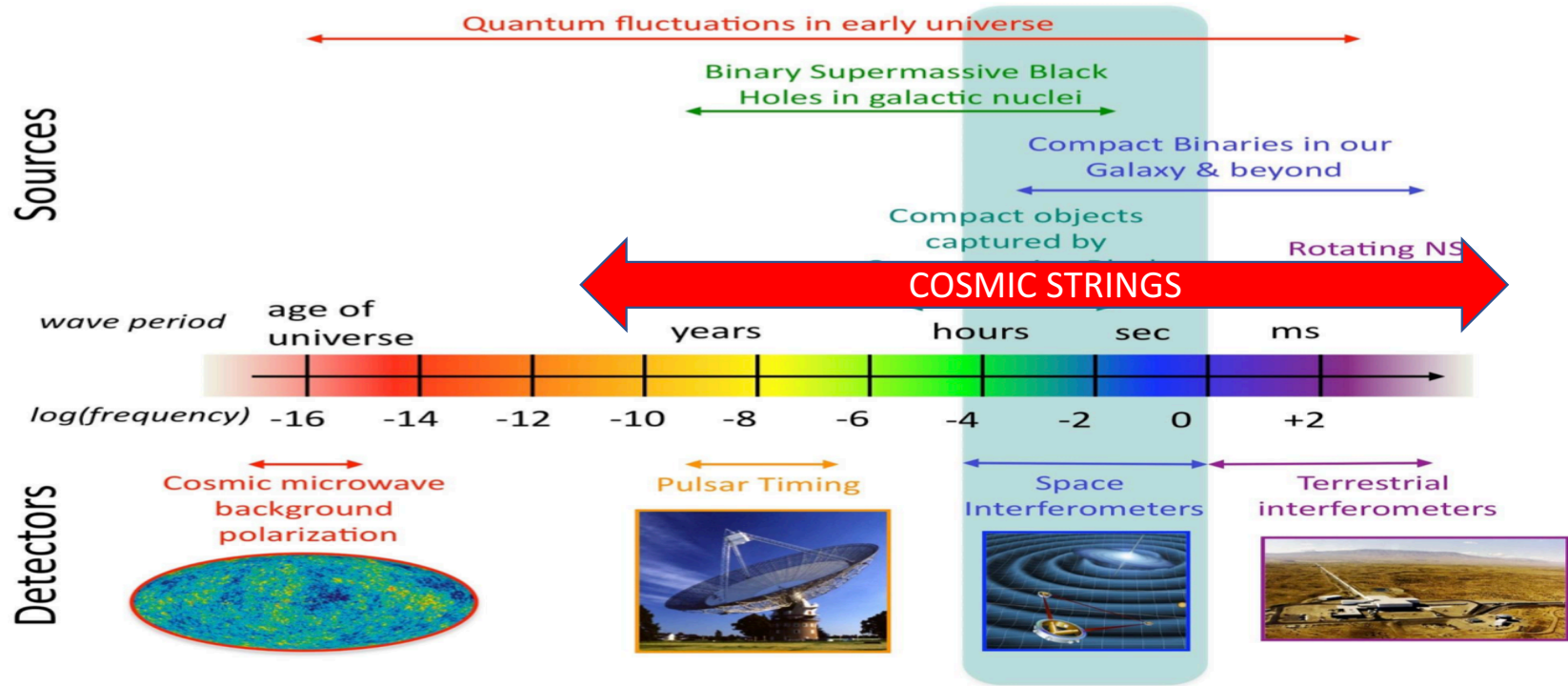


Credit: NASA Goddard Space Flight Center

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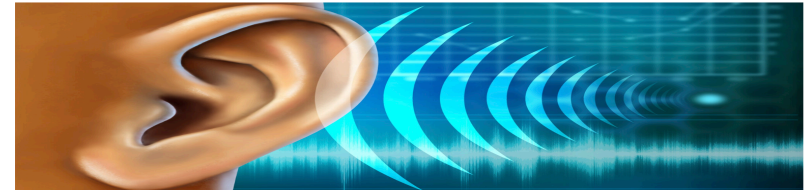


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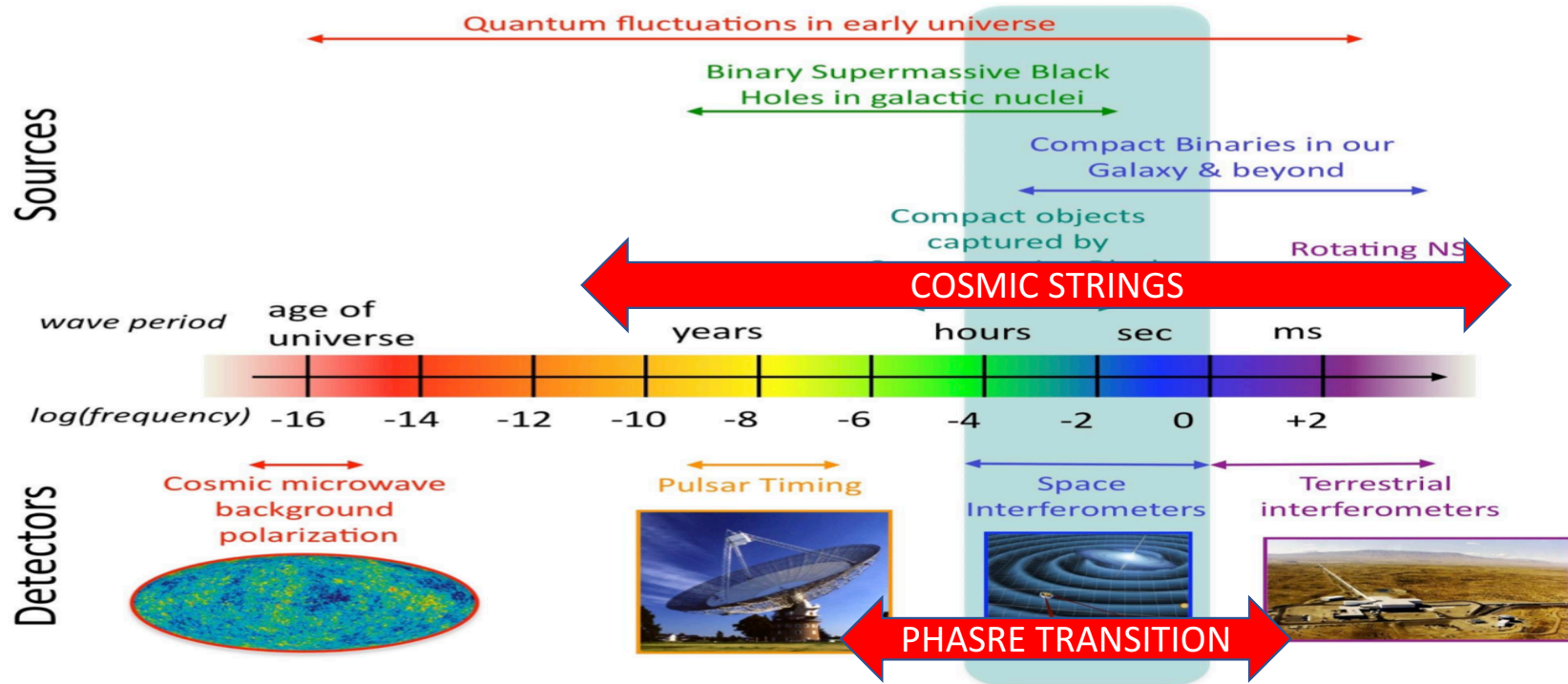


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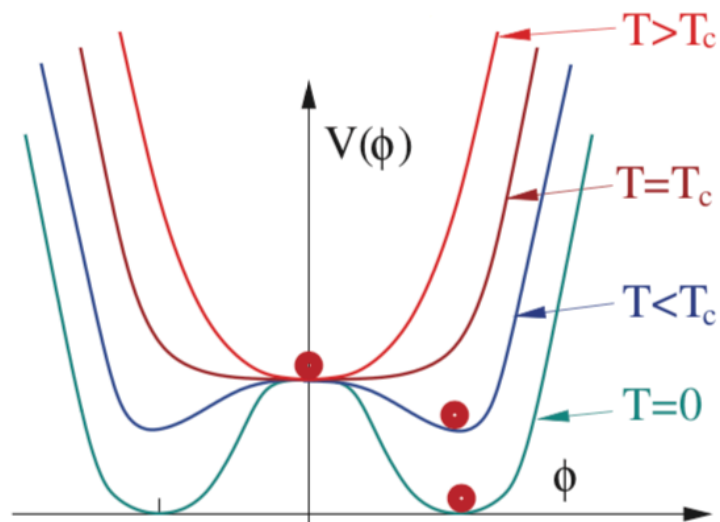
The Gravitational Wave Spectrum



Credit: NASA Goddard Space Flight Center

Dynamics of phase transition

Second order Transition



Rolling of the field

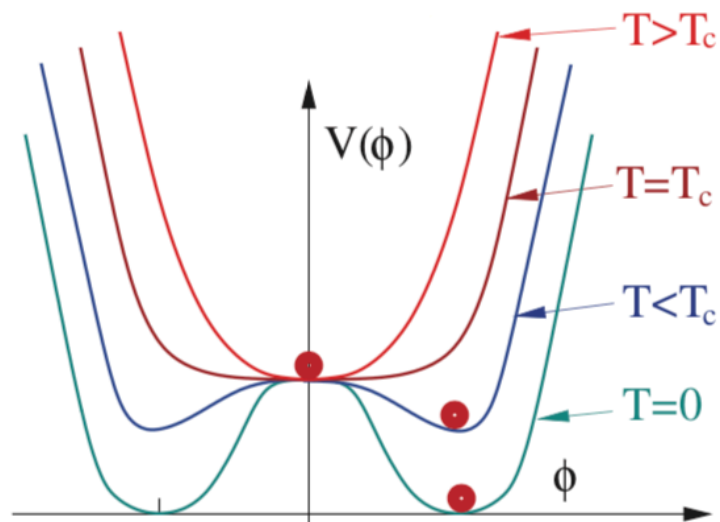
$$V(\Phi, 0) = -\frac{\mu^2}{2}\Phi^2 + \frac{\lambda}{4}\Phi^4$$

$$V(\Phi, T) = V(\Phi, 0) + D(T^2 - T_0^2)\Phi^2 - ET\Phi^3$$

$$D = \frac{3g^2 + 4\lambda}{24}, \quad E = \frac{3g^3 + g\lambda + 3\lambda^{3/2}}{24\pi} \quad \text{and} \quad T_0 = \frac{\sqrt{12\lambda}v_\Phi}{\sqrt{3g^2 + 4\lambda}}$$

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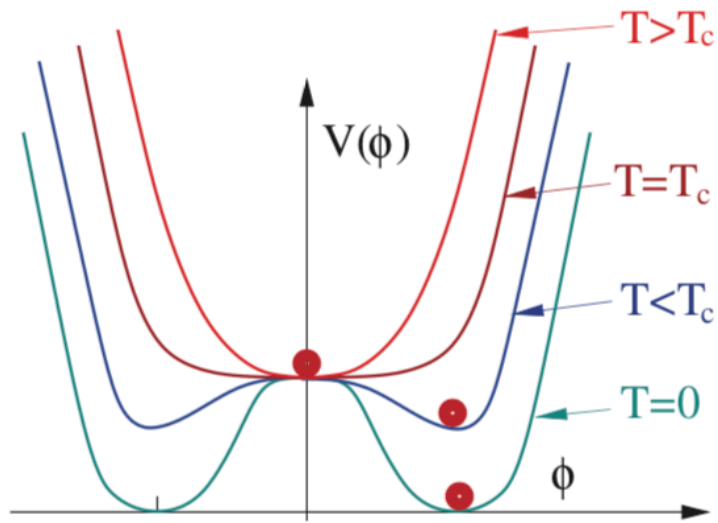
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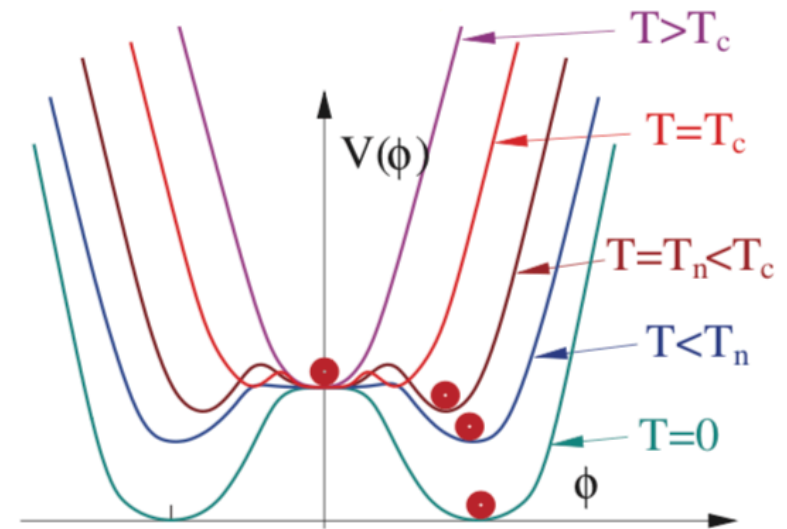
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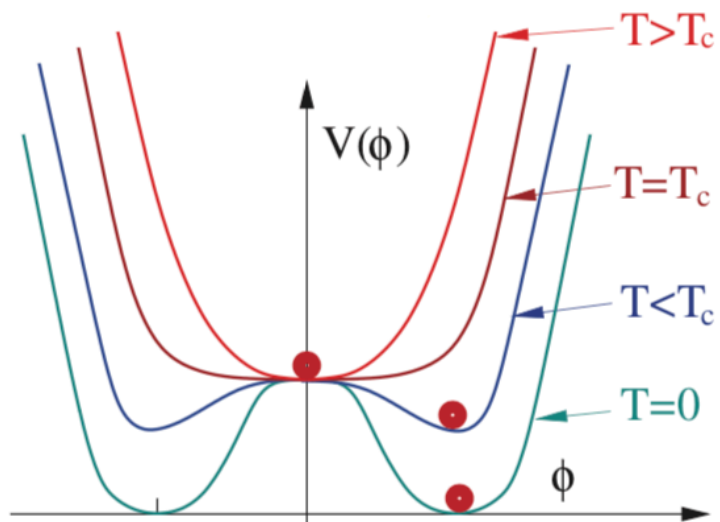


Tunneling

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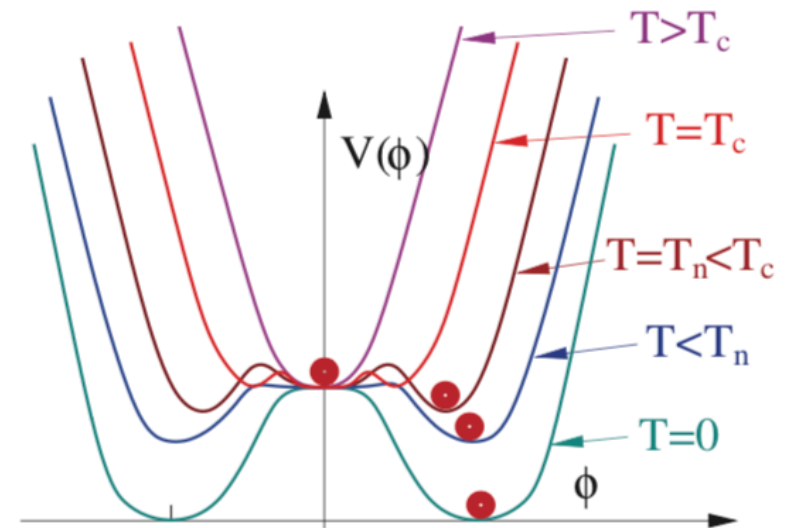
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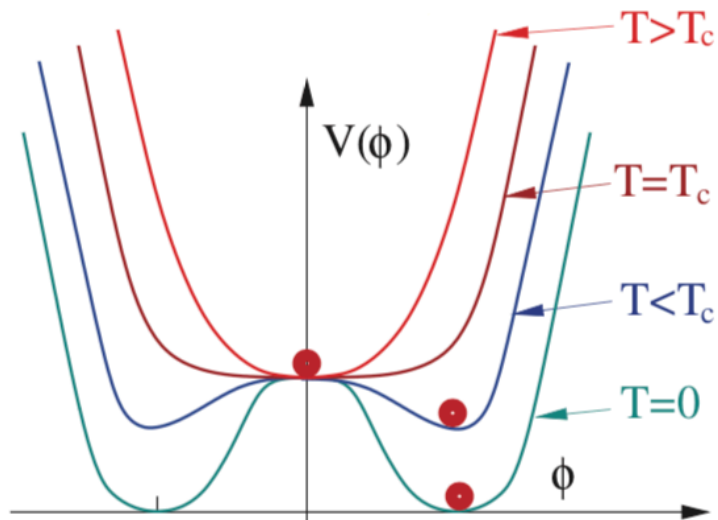


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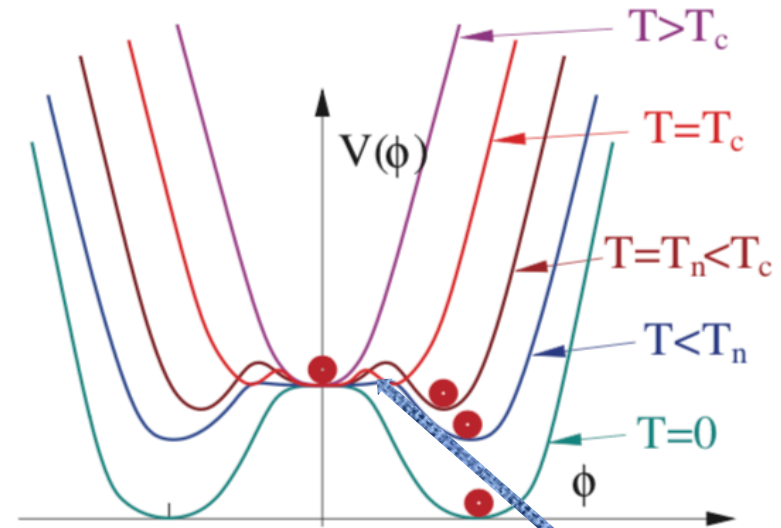
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Gravitational waves

E.g., Hindmarsh et al, SciPost (2021)

First order Transition



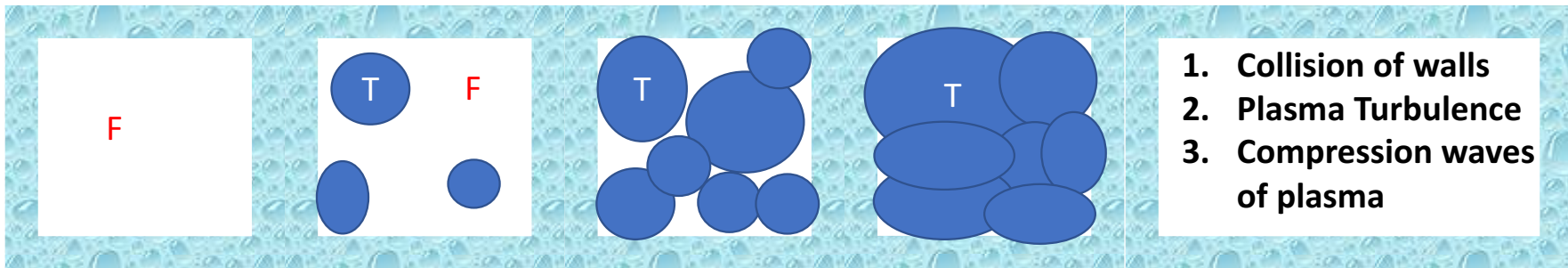
direct contribution (Dynamics of vacuum bubbles)

T_c

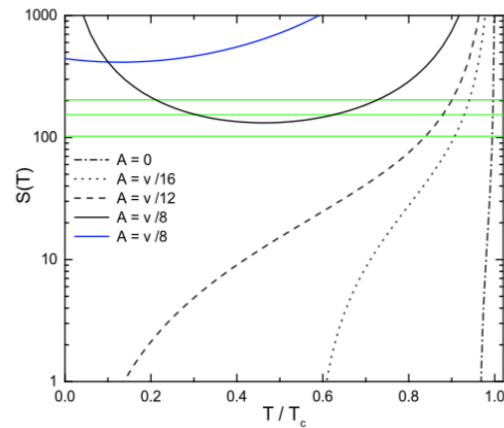
T_t

$T_p: f+=0.71$

T_0



$$\frac{\beta}{H_*} = \left[T \frac{d}{dT} \left(\frac{S_3(T)}{T} \right) \right] \Big|_{T=T_*}$$



$$h^2 \Omega_{sw}(f) = 2.59 \times 10^{-6} \frac{v_w(\alpha)}{\beta/H_*} \left[\frac{\kappa(\alpha)\alpha}{1+\alpha} \right]^2 \left(\frac{106.75}{g_\rho^*} \right)^{1/3} S_{sw}(f),$$

where the spectral shape function is

$$S_{sw}(f) = \left(\frac{f}{f_{sw}} \right)^3 \left[\frac{7}{4 + 3(f/f_{sw})^2} \right]^{7/2},$$

Gravitational waves

First order Transition



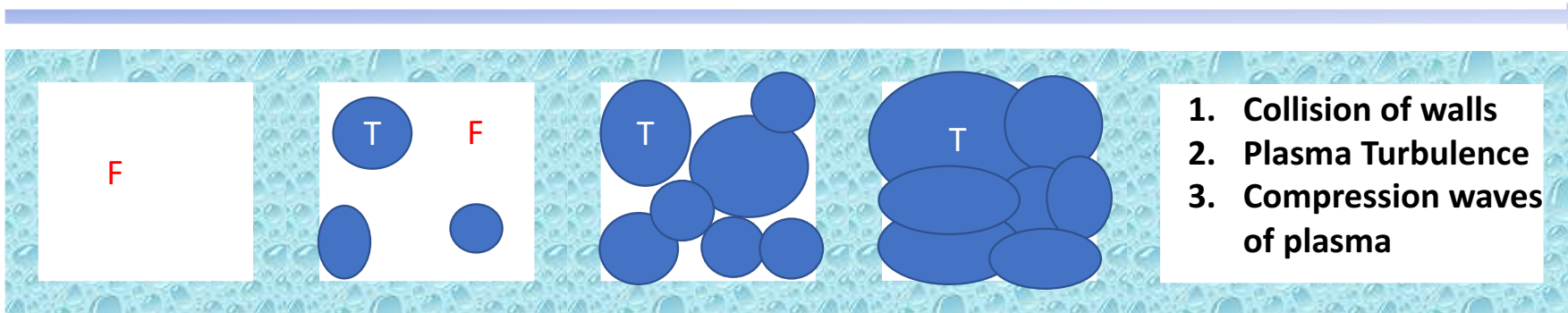
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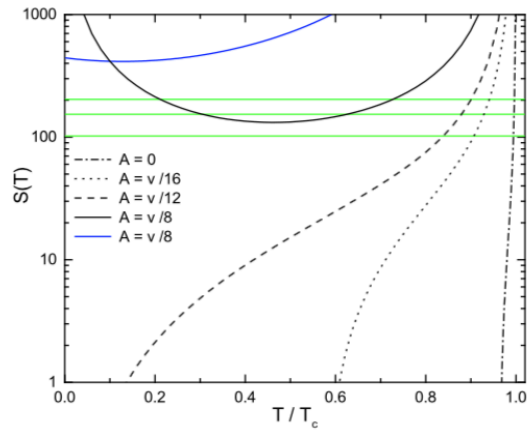
T_t

$T_p: f_{\pm}=0.71$

T_0

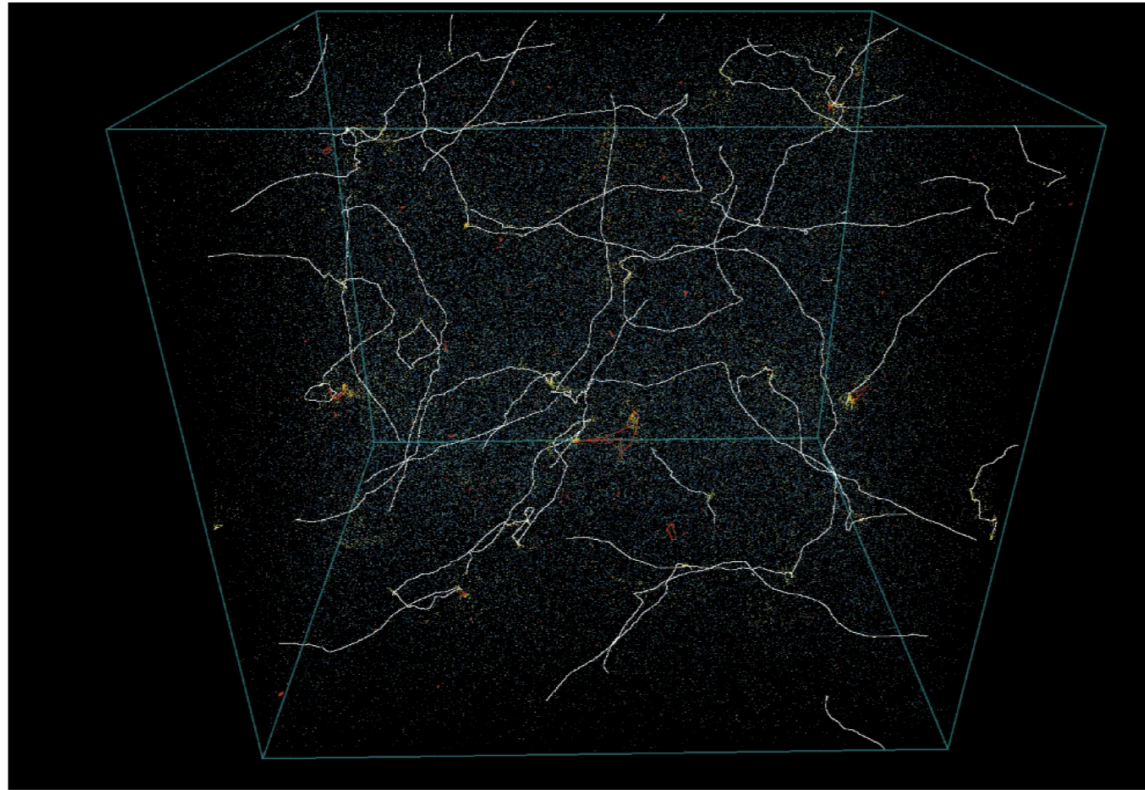


$$\frac{\beta}{H_*} = \left[T \frac{d}{dT} \left(\frac{S_3(T)}{T} \right) \right] \Big|_{T=T_*}$$



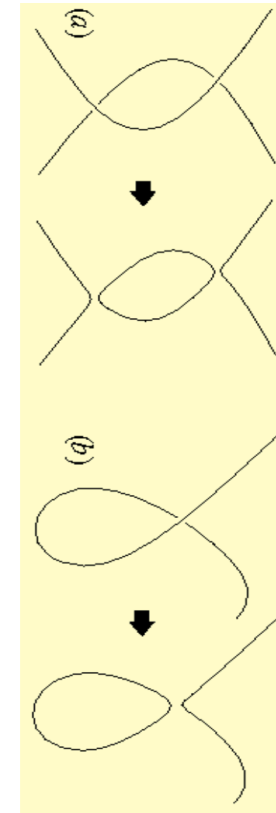
$$f_{sw} = 1.92 \times 10^{-2} \text{ mHz} \frac{1}{v_w} \frac{\beta}{H_*} \frac{T_*}{100 \text{ GeV}} \left(\frac{g_\rho^*}{106.75} \right)^{1/6}$$

String inter-commutation



T. Vachaspati et al 1506.04039

U(1) theory



These loops radiate to GWs

Cosmic string scaling

Long strings evolution is a random walk problem in the early universe (**velocity-dependent-one-scale model**)

Long-string correlation length $L^2 = \mu/\rho_L$, $L \approx t \Rightarrow \rho_L \approx \mu t^{-2}$

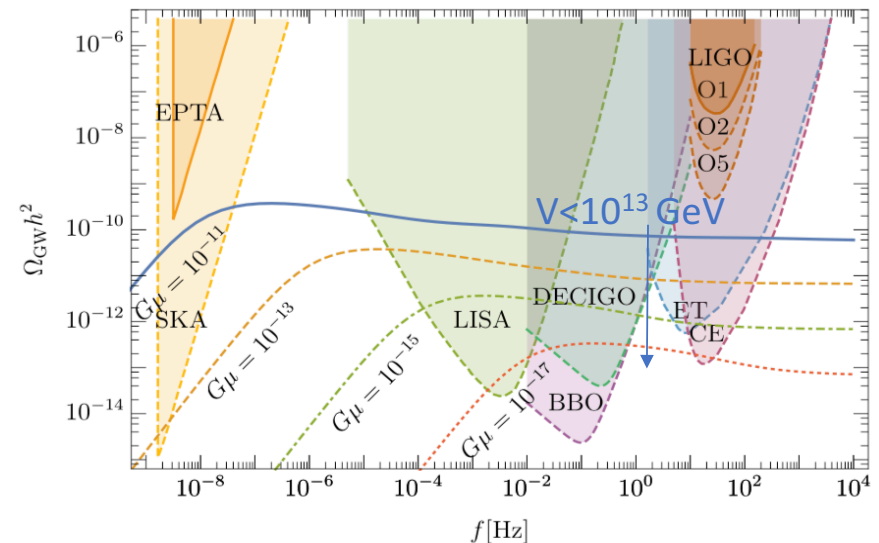
Friedmann equation: $t^2 G^{-1} \approx \rho_{bg}$

$$\rho_L \approx \rho_{bg} G\mu$$

$V = 10^{15} \Rightarrow \mu = 10^{30}, \Rightarrow G\mu \approx 10^{-8}$

$$\mu = V(\text{vev})^2$$

CS never dominates the energy density of the universe



Gravitational waves power spectrum and loop number density

Amplitude/energy density $\Omega_{GW}(t_0, f) = \frac{f}{\rho_c} \frac{d\rho_{GW}}{df} = \sum_k \Omega_{GW}^{(k)}(t_0, f)$. Summing over all the modes

Differential energy density $\frac{d\rho_{GW}^{(k)}}{df} = \int_{t_F}^{t_0} \left[\frac{a(\tilde{t})}{a(t_0)} \right]^4 P_{GW}(\tilde{t}, f_k) \frac{dF}{df} d\tilde{t}$,

Power spectrum

Amplitude/energy density

$$P_{GW}(\tilde{t}, f_k) = \frac{2kG\mu^2\Gamma_k}{f_k^2} n(\tilde{t}, f_k) = \frac{2kG\mu^2\Gamma_k}{f^2 \left[\frac{a(t_0)}{a(\tilde{t})} \right]^2} n\left(\tilde{t}, \frac{2k}{f} \left[\frac{a(\tilde{t})}{a(t_0)} \right]\right).$$

$$\Omega_{GW}^{(k)}(t_0, f) = \frac{2kG\mu^2\Gamma_k}{f\rho_c} \int_{t_{osc}}^{t_0} \left[\frac{a(\tilde{t})}{a(t_0)} \right]^5 n\left(\tilde{t}, \frac{2k}{f} \left[\frac{a(\tilde{t})}{a(t_0)} \right]\right) d\tilde{t}.$$

Loop number density

μ^2/M_{pl}

Numerical simulation: $n(\tilde{t}, l_k(\tilde{t})) = \frac{0.18}{[l_k(\tilde{t}) + \Gamma G\mu\tilde{t}]^{5/2} \tilde{t}^{3/2}}$. Analytical $n(l, t) = \frac{A_\beta C_\beta(\alpha)}{t^{3\beta} (l + \Gamma G\mu t)^{4-3\beta}}$,

Cosmic archeology, GW spectral shapes and Leptogenesis

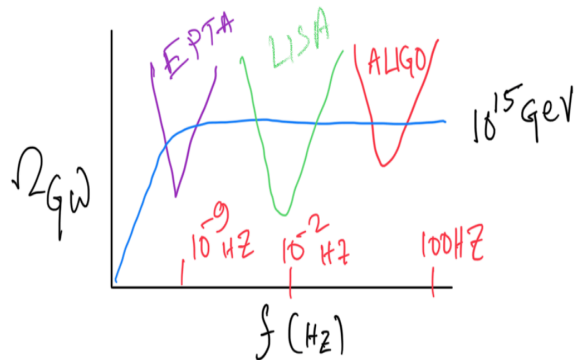
Amplitude sensitivity

Amplitude + spectral shape sensitivity

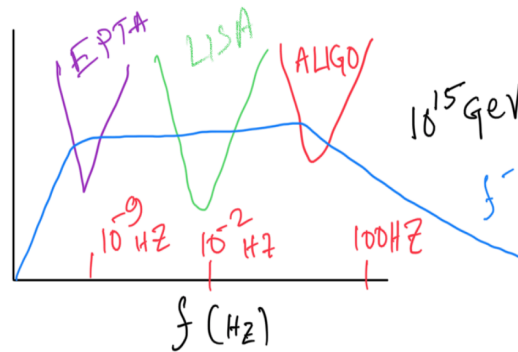
Standard Cosmology ($w=1/3$)

Early Matter domination ($w=0$)

Fundamental mode ($k=1$):



A spectral break



Turning point frequency

$$f_{\Delta} = \sqrt{\frac{8}{z_{\text{eq}} \alpha \Gamma G \mu}} \left[\frac{g_*(T_{\Delta})}{g_*(T_0)} \right]^{1/4} \left(\frac{T_{\Delta}}{T_0} \right) t_0^{-1},$$

Standard cosmology

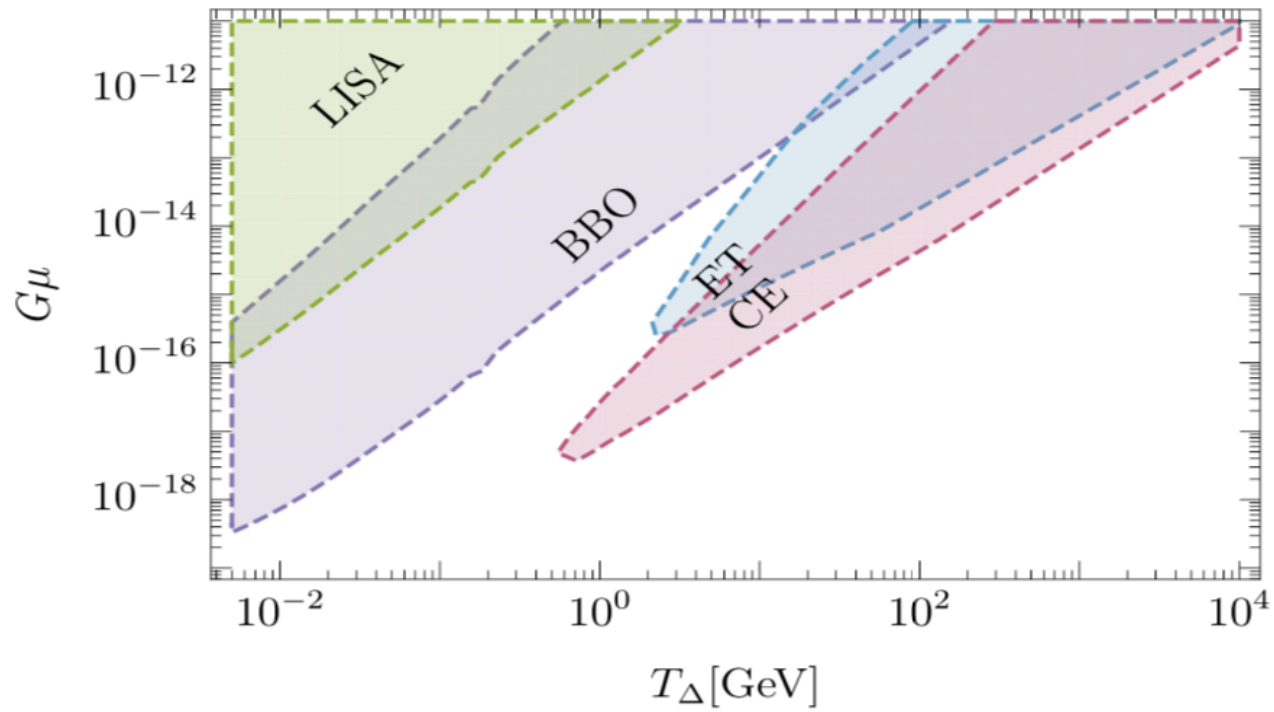
Matter/Black holes dominated universe

Murayama et al PRL(2020)

Samanta et al JHEP(2020)

Samanta et al JCAP(2021)

Sensitivity

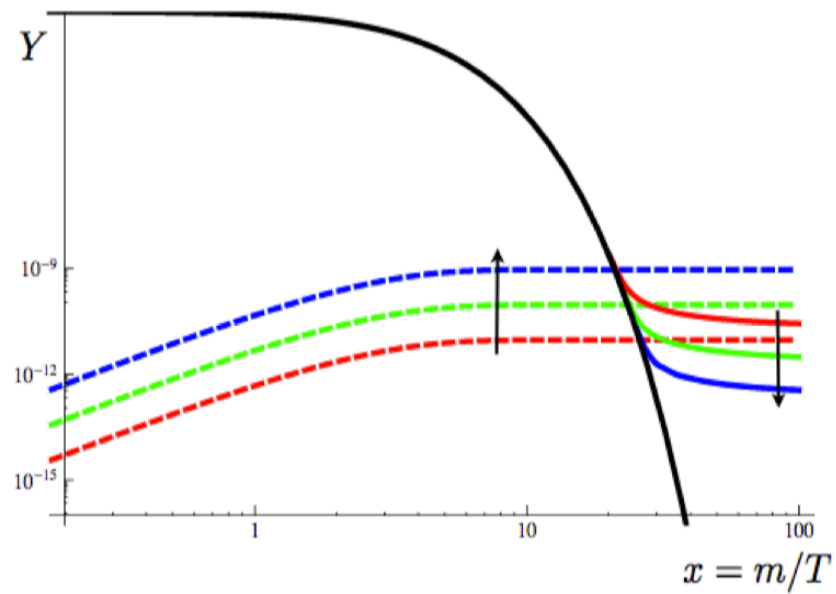


e.g, Y. Cui et al, JHEP (2020)

Miracle-less WIMP: A new class of DM

Samanta et al, 2202.10474

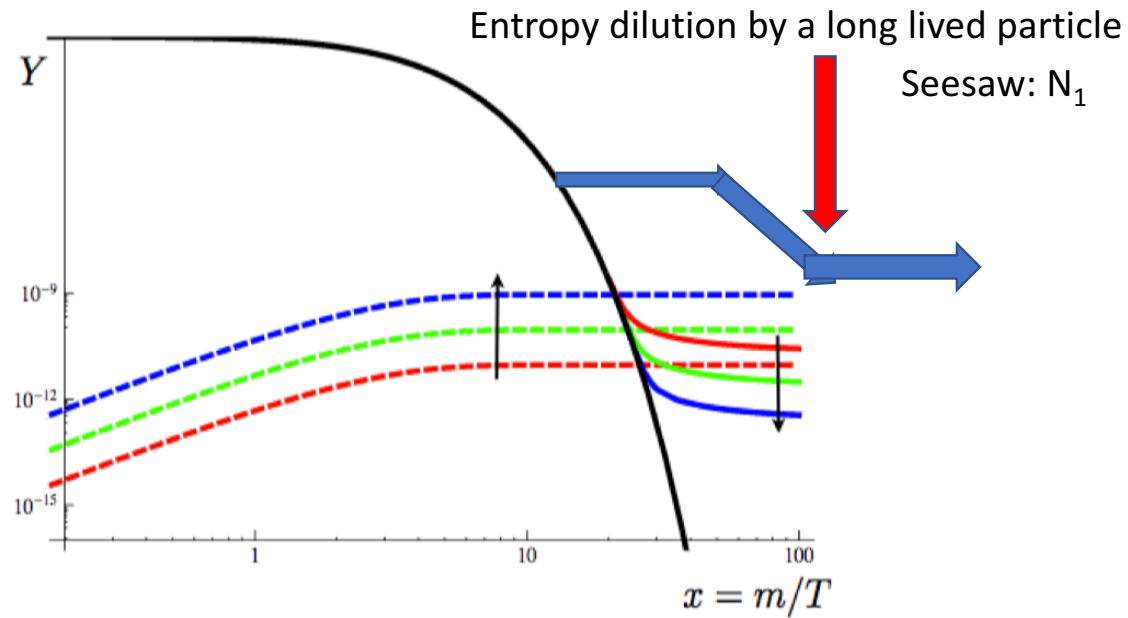
DM has u(1) charge



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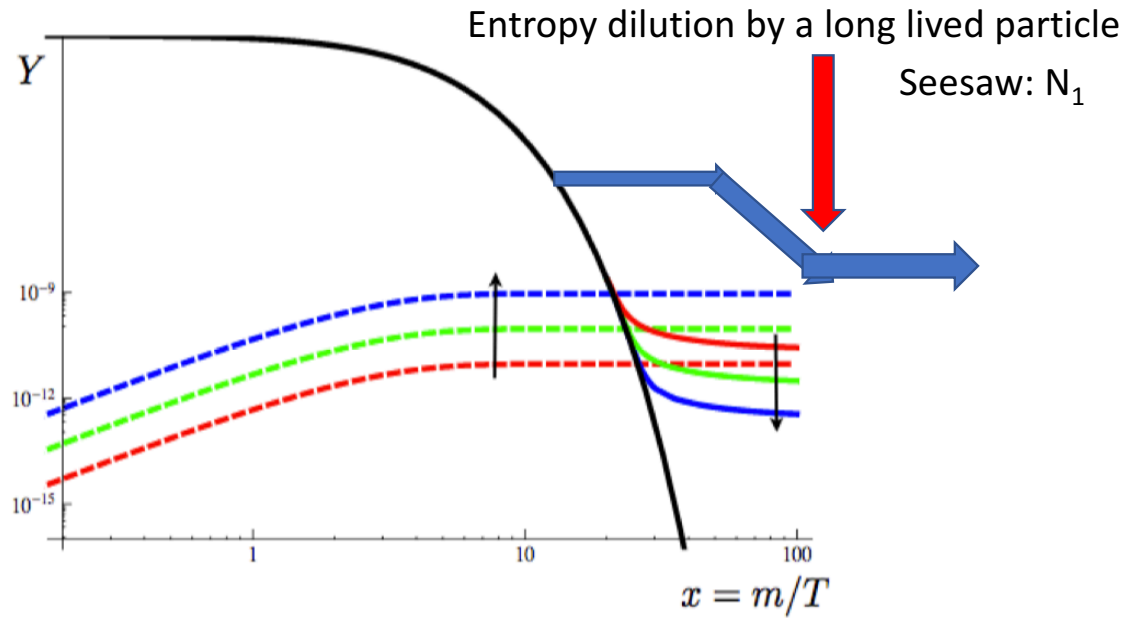
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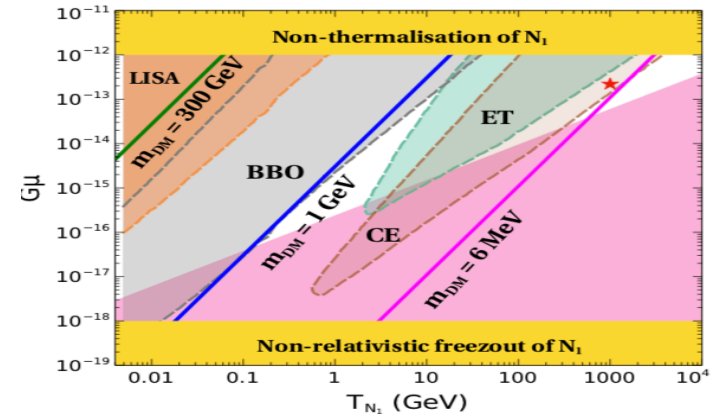
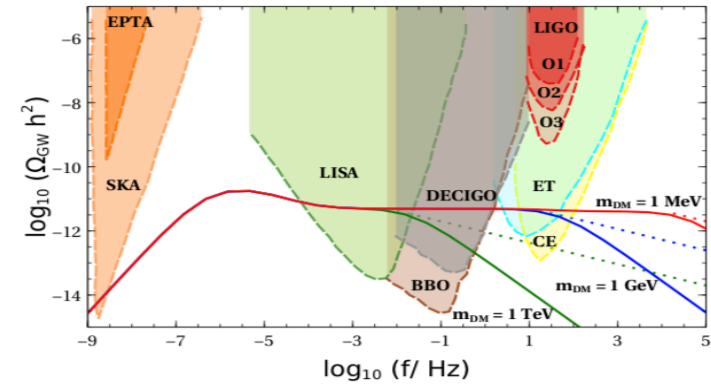
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Otherwise Diluter mess with BBN predictions



Ultralight primordial black holes as diluters

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Constraints on black hole masses masses Free parameter: $\beta = \rho_{\text{BH}}/\rho_{\text{rad}}$

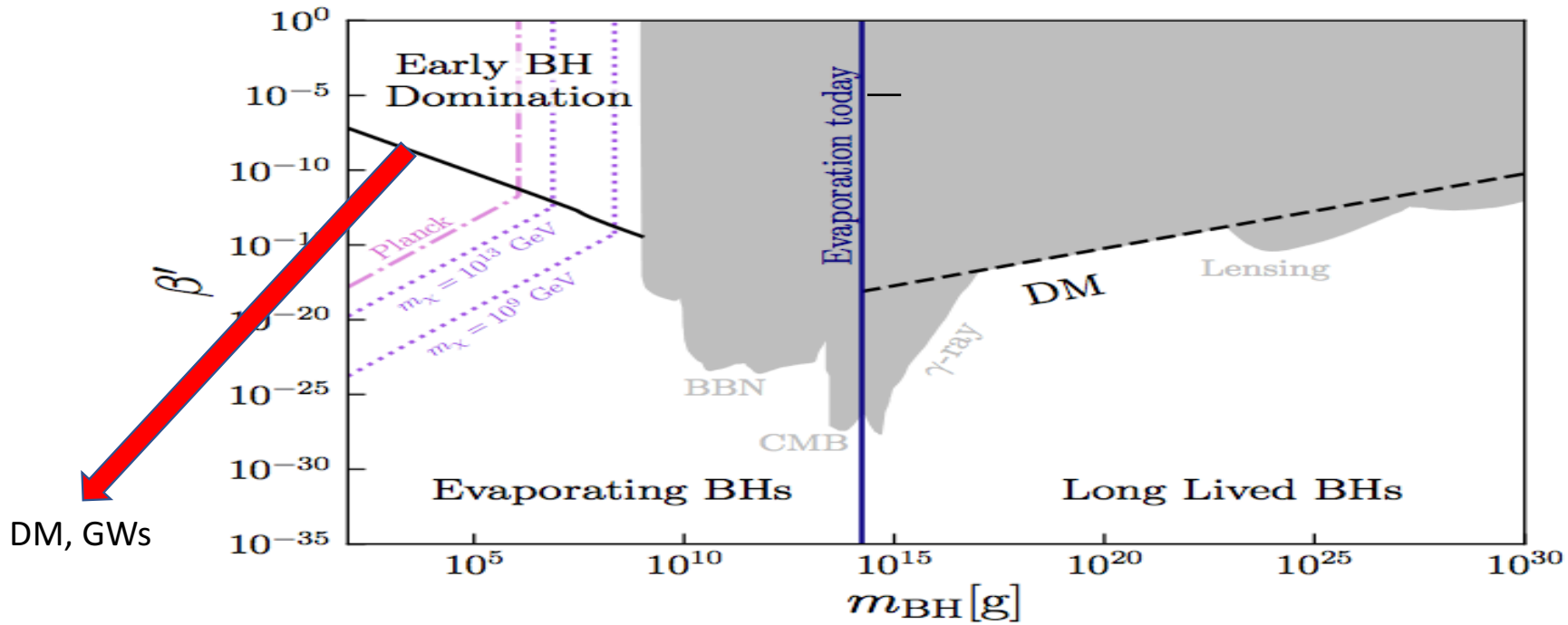
PBH Mass



< 0.1 g (CMB) produce Dark matter

>10⁹ g (constrained by BBN T~5MeV)

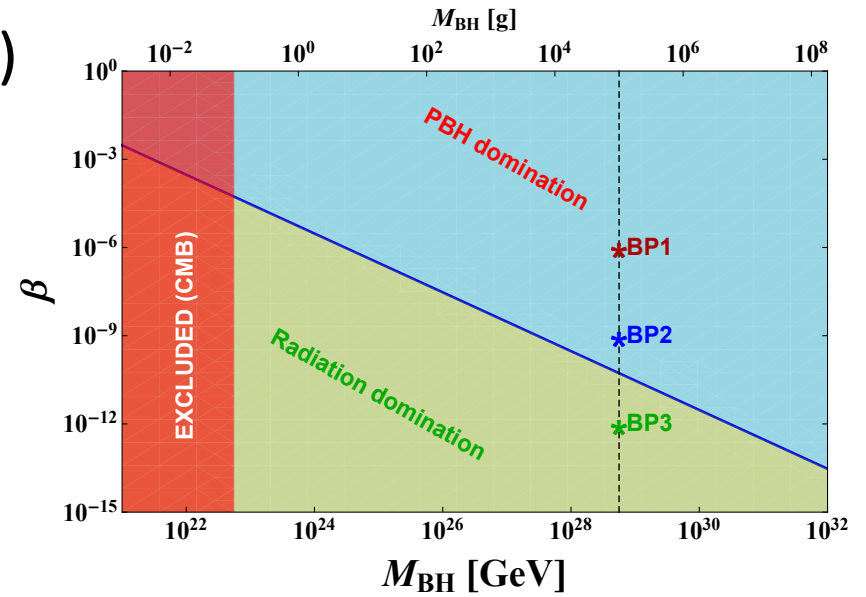
> 10¹⁵ g (it self Dark matter)



Ultralight PBH dynamics (only non-rotating)

e.g., Samanta, Datta JCAP (2021)

Black holes not to dominate:
$$\beta < \gamma^{-1/2} \left(\frac{\mathcal{G}g_{*B}(T_{BH})}{10240\pi} \right)^{1/2} \frac{M_{Pl}}{M_{BH}}.$$



Ultralight PBH dynamics (only non-rotating)

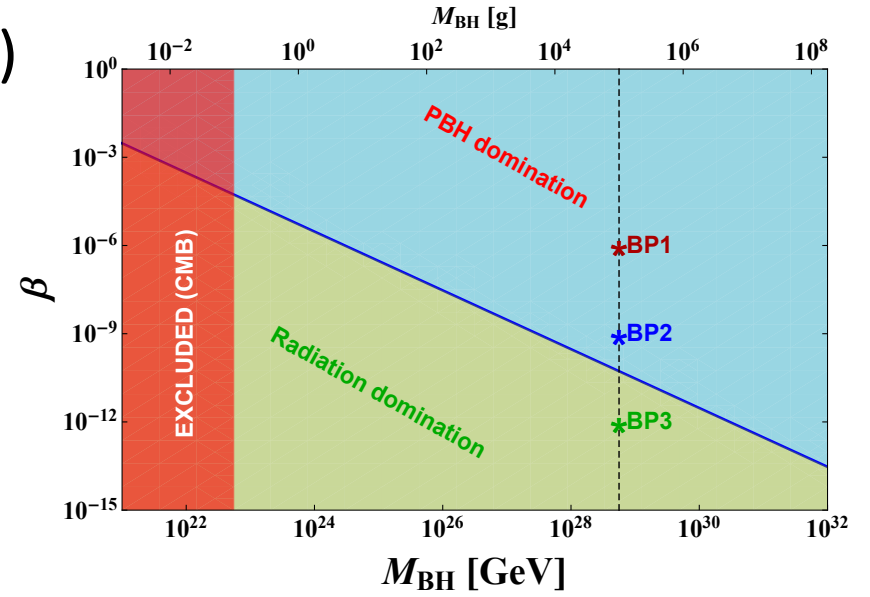
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Kintetic equations:

$$\frac{d\rho_R}{dt} + 4H\rho_R = -\frac{\dot{M}_{BH}}{M_{BH}}\rho_{BH},$$

$$\frac{d\rho_{BH}}{dt} + 3H\rho_{BH} = +\frac{\dot{M}_{BH}}{M_{BH}}\rho_{BH},$$

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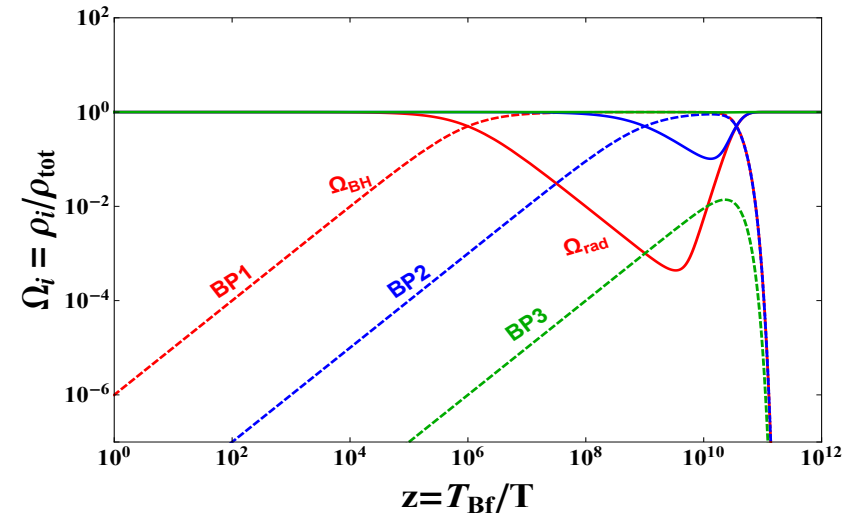
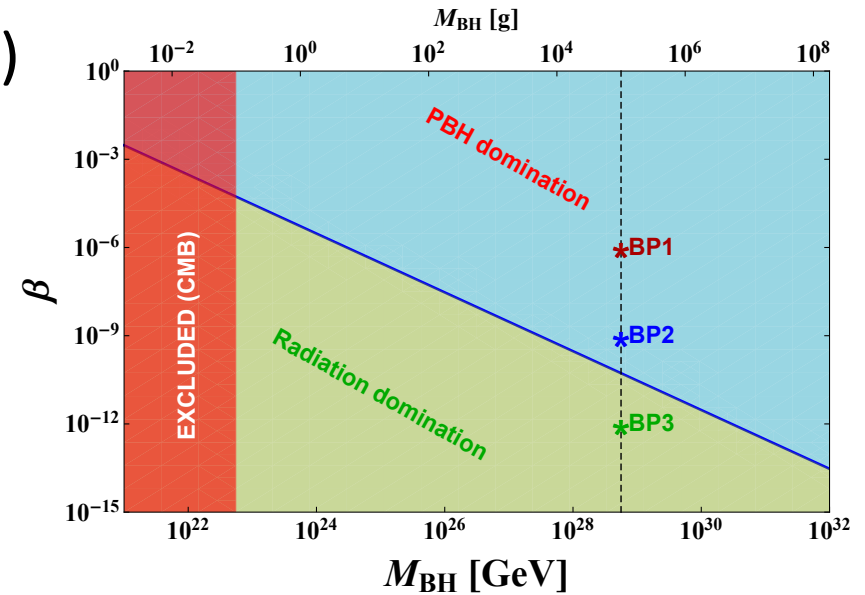


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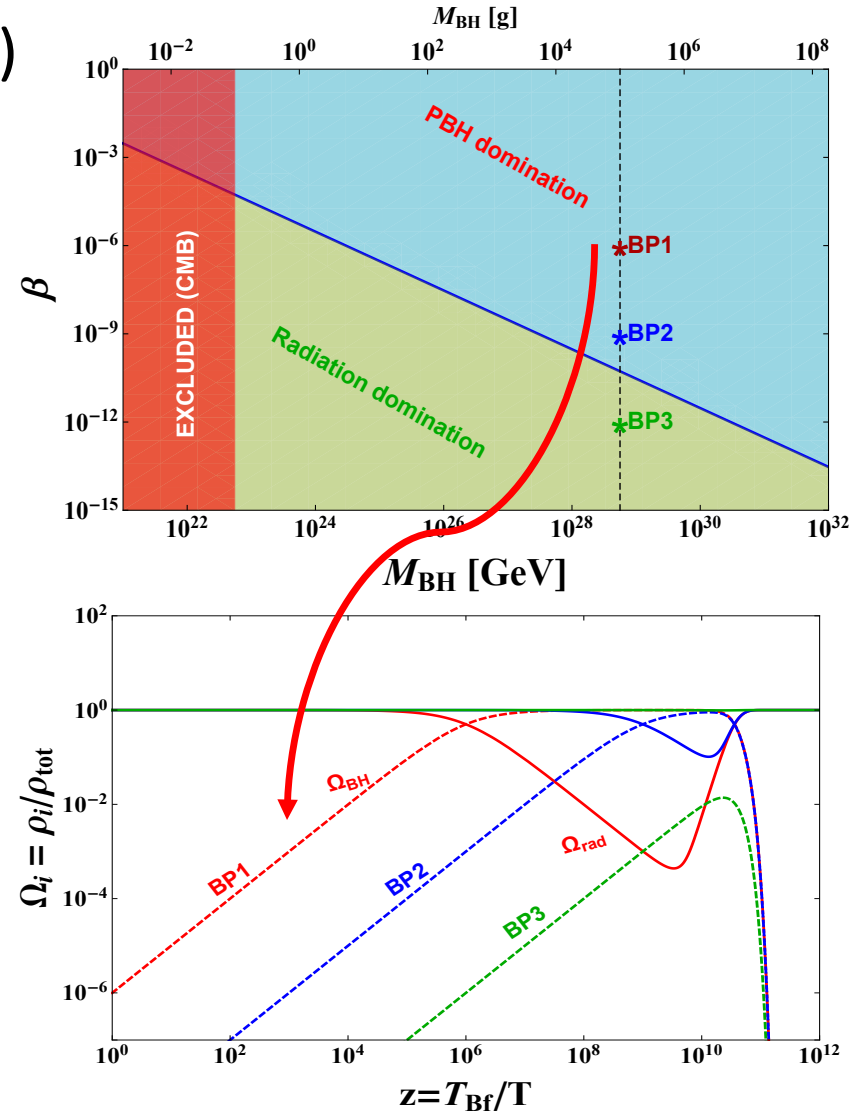


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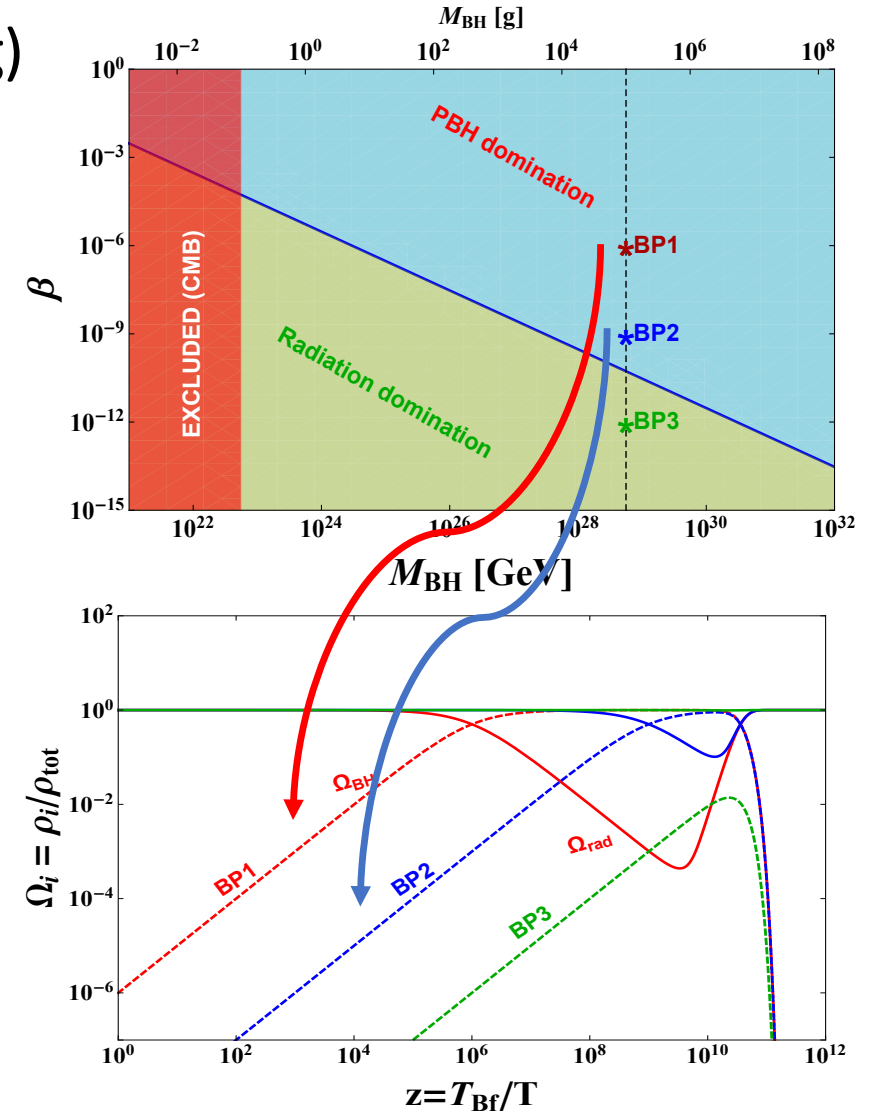


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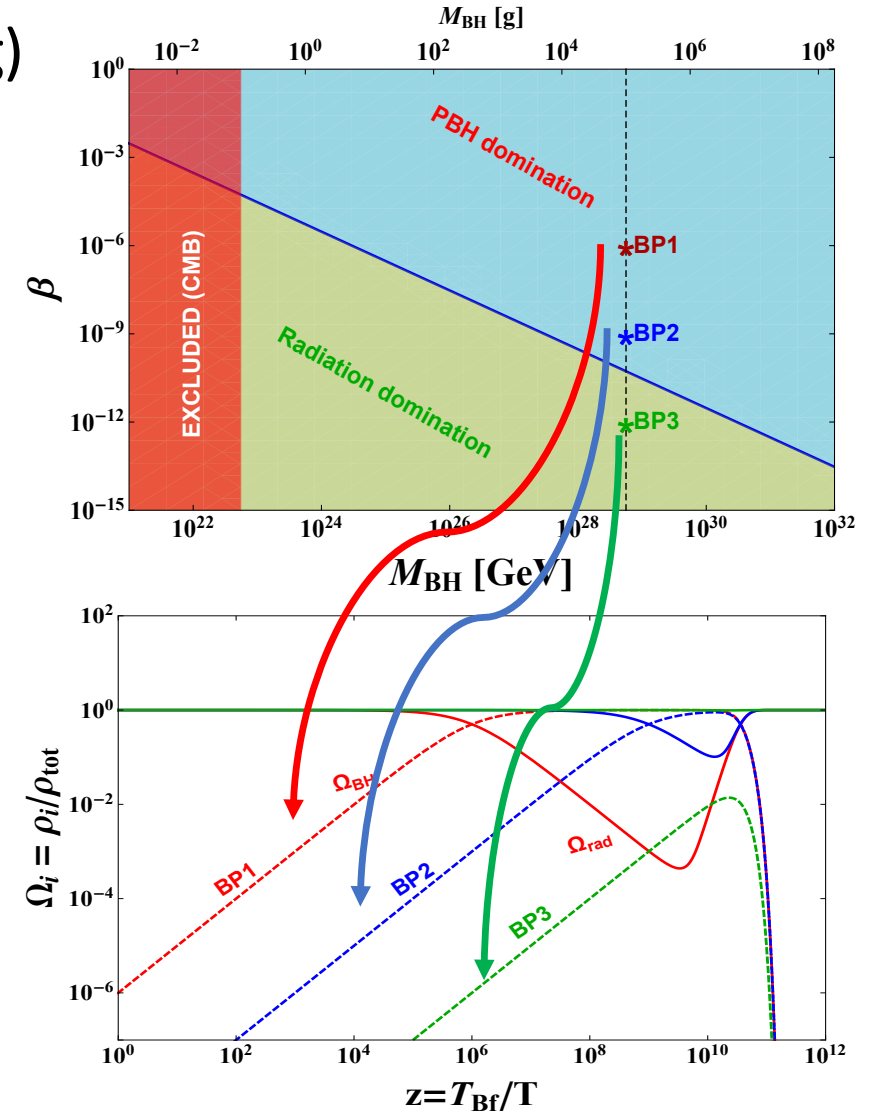


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Ultralight PBH dynamics (only non-rotating)

Consider formation in the radiation domination

Mass:
$$M_{BH} = \gamma \frac{4}{3} \pi (H_{Bf}^{-1})^3 \rho_{Bf} \quad \text{with} \quad \rho_{Bf} = \frac{3H_{Bf}^2 M_{Pl}^2}{8\pi}, \quad H_{Bf} = \frac{1}{2t_{Bf}}.$$

Mass loss:
$$-\frac{dM_{BH}}{dt} = f_{ev} (4\pi r_{BH}^2) \frac{dE}{dt},$$

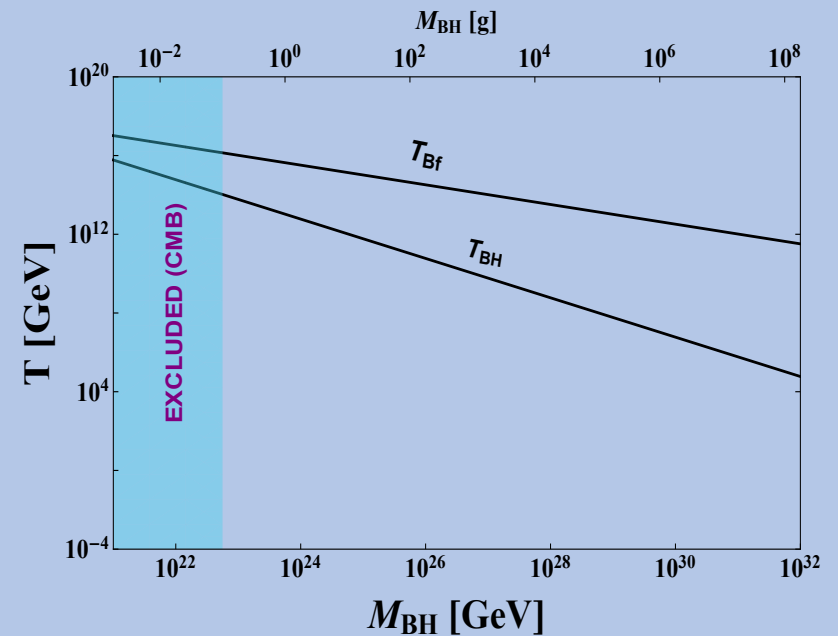
$$\frac{dM_{BH}}{dt} = -\frac{\mathcal{G} g_{*B}(T_{BH})}{30720\pi} \frac{M_{Pl}^4}{M_{BH}^2},$$

Life-time:
$$\tau = \int_{t_{Bf}}^{t_{ev}} dt = -\int_{M_{BH}}^0 dM_{BH} \frac{30720\pi M_{BH}^2}{\mathcal{G} g_{*B}(T_{BH}) M_{Pl}^4} = \frac{10240\pi M_{BH}^3}{\mathcal{G} g_{*B}(T_{BH}) M_{Pl}^4}.$$

Evaporation
$$T_{ev} = \left(\frac{45 M_{Pl}^2}{16\pi^3 g_*(T_{ev}) \tau^2} \right)^{1/4}.$$

Formation temperature

$$T_{Bf} = \left(\frac{45\gamma^2}{16\pi^3 g_*(T_{Bf})} \right)^{1/4} \left(\frac{M_{Pl}}{M_{BH}} \right)^{1/2} M_{Pl}.$$



Super heavy Dark Matter (SHDM) from PBH

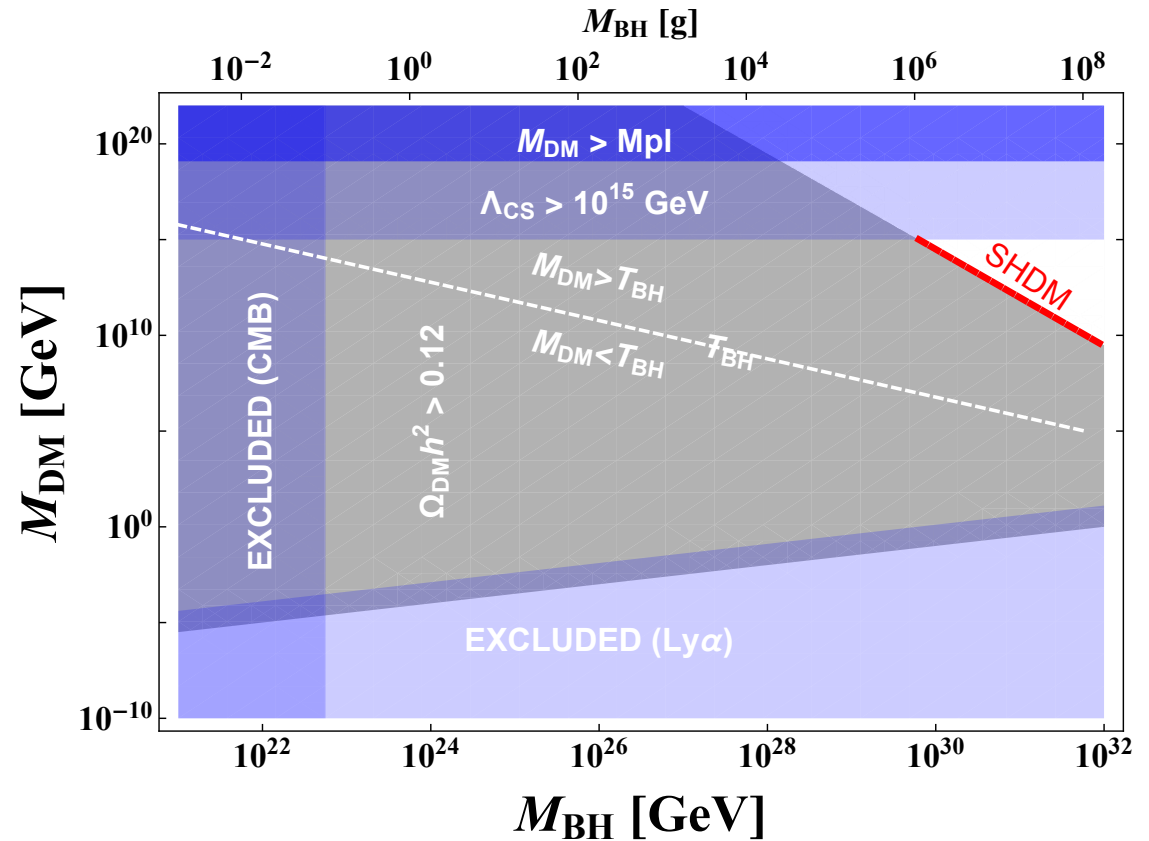
Can not save $M_{DM} < T_{BH}$

free streaming length

$$\lambda_{FS} = \int_{t_i}^{t_{\text{dec}}} \frac{v(t)}{a(t)} dt \lesssim 0.1 \text{ Mpc}$$

$$\Rightarrow v_{DM} \text{ at } z_{\text{dec}} \gtrsim 2 \times 10^{-8}$$

$$\Rightarrow M_{DM} \gtrsim 2 \times 10^3 (M_{BH})^{1/2}$$



Super heavy Dark Matter (SHDM) from PBH

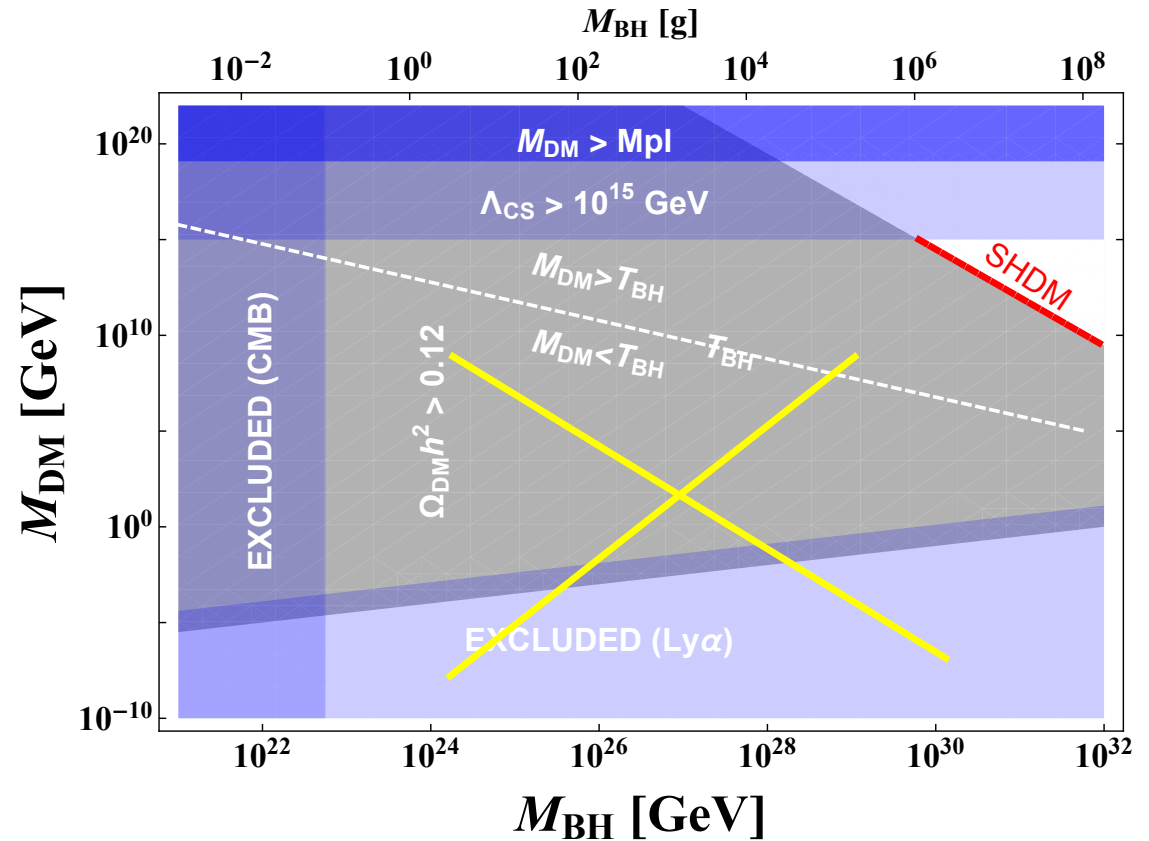
Can not save $M_{DM} < T_{BH}$

free streaming length

$$\lambda_{FS} = \int_{t_i}^{t_{\text{dec}}} \frac{v(t)}{a(t)} dt \lesssim 0.1 \text{ Mpc}$$

$$\Rightarrow v_{DM} \text{ at } z_{\text{dec}} \gtrsim 2 \times 10^{-8}$$

$$\Rightarrow M_{DM} \gtrsim 2 \times 10^3 (M_{BH})^{1/2}$$



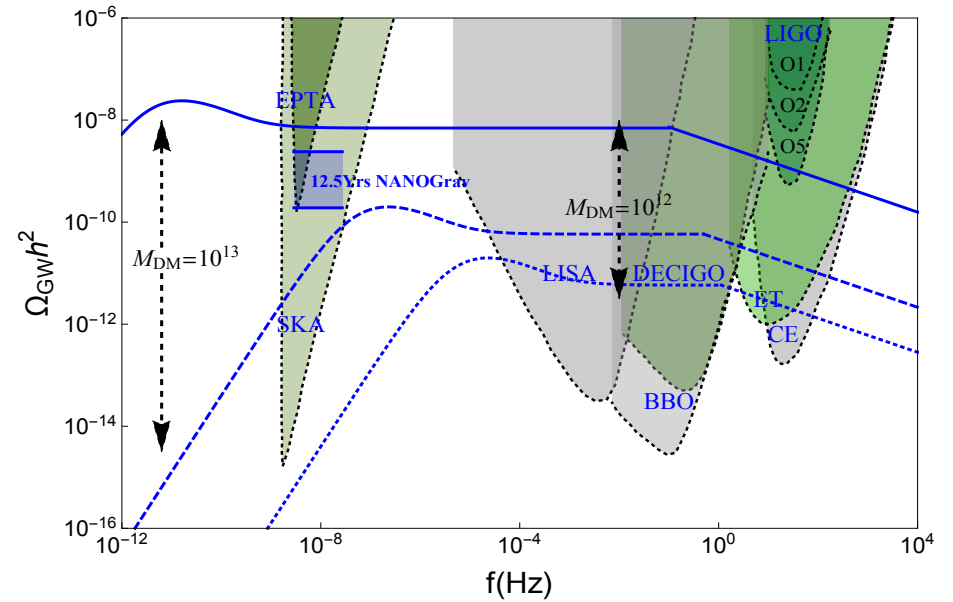
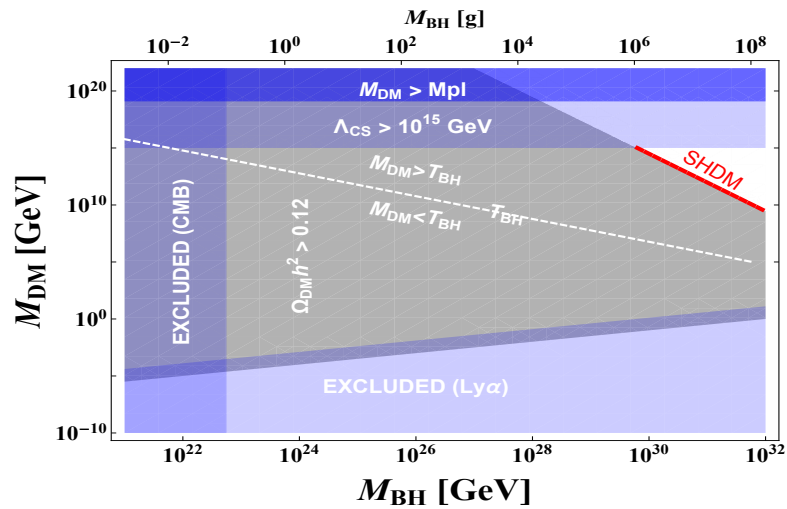
The turning point frequency

Samanta, Urban JCAP(2022)

$$T_{ev} = \left(\frac{45 M_{Pl}^2}{16 \pi^3 g_*(T_{ev}) \tau^2} \right)^{1/4}$$

$$f_* \simeq 2.1 \times 10^{-8} \sqrt{\frac{50}{z_{eq} \alpha \Gamma G \mu}} \left(\frac{M_{DM}}{T_0} \right)^{3/5} T_0^{-2/5} t_0^{-1}$$

$$\tau = \int_{t_{Bf}}^{t_{ev}} dt = - \int_{M_{BH}} dM_{BH} \frac{30720 \pi M_{BH}^2}{\mathcal{G} g_{*B}(T_{BH}) M_{Pl}^4} = \frac{10240 \pi M_{BH}^3}{\mathcal{G} g_{*B}(T_{BH}) M_{Pl}^4}$$



Why strong amplitude GWs are of interest? PTAs and LIGO

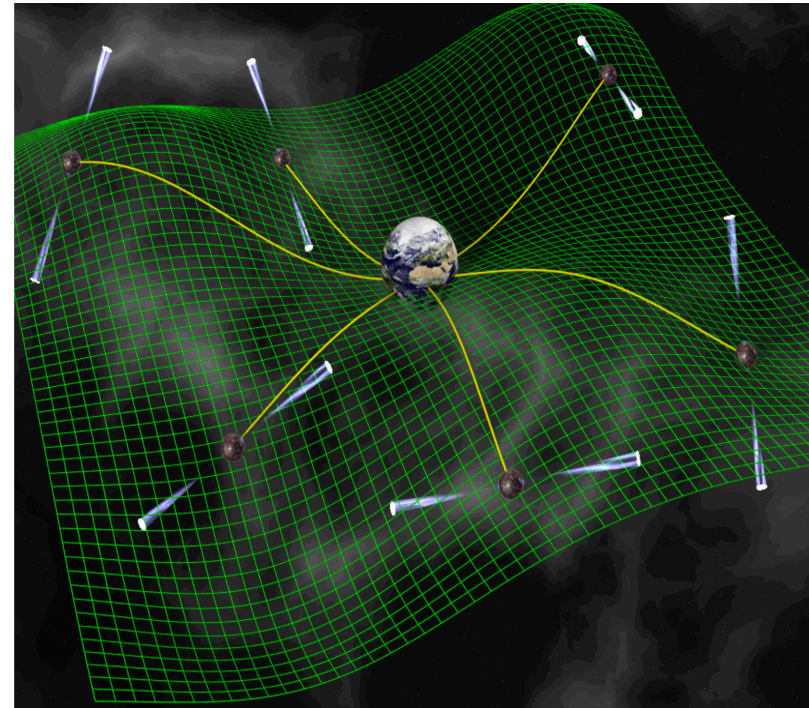
Millisecond pulsars (spins ~100 times a second) produce most stable pulses and are used by the PTAs

When a gravitational wave (a disturbance) passes between the earth and pulsar system, the time of arrival of the signal from the pulsars changes. This induces a change in frequency due to the gravitational wave.

Time residual:

$$R(t) = - \int_0^t \frac{\delta v}{v} dt$$

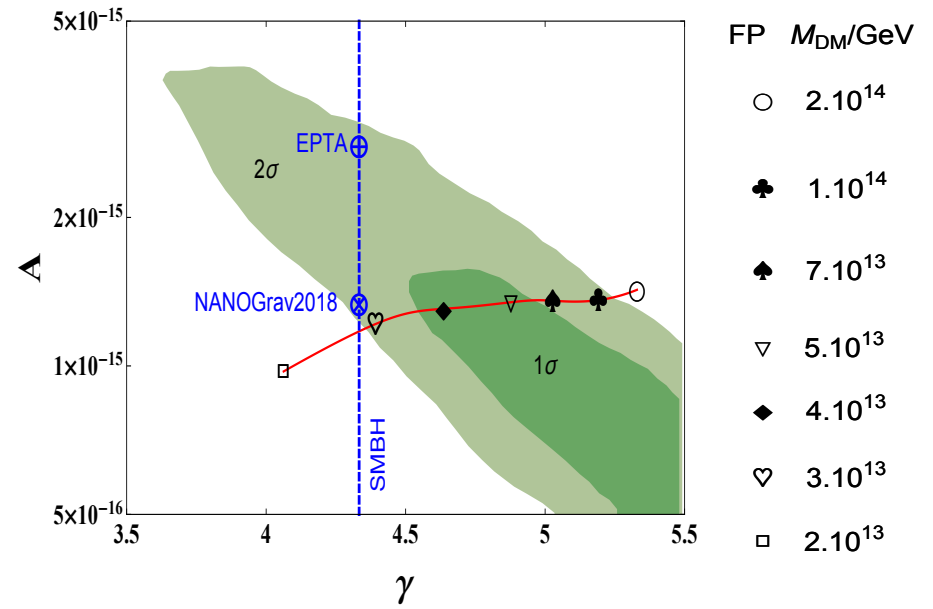
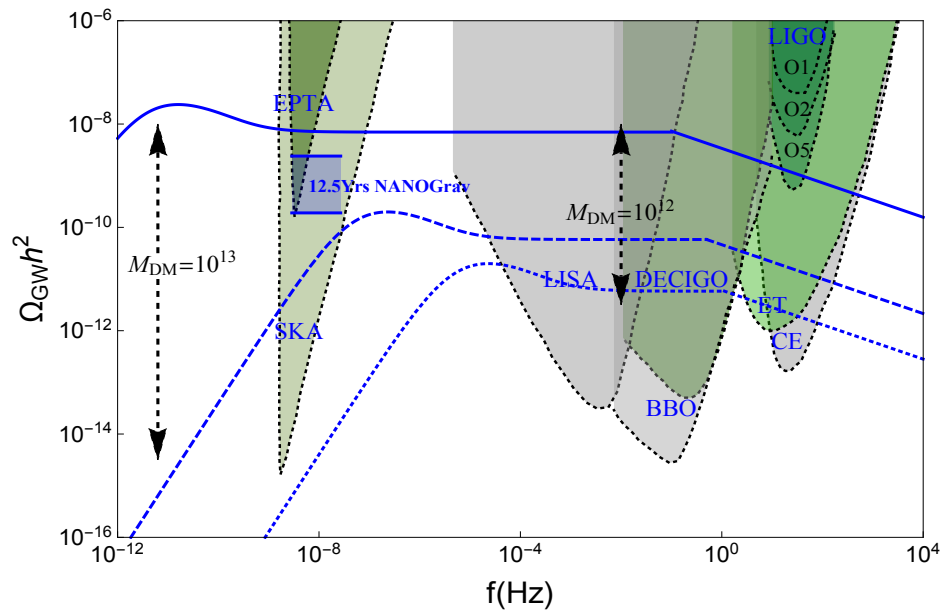
Pulsar-Timing-Arrays typically work with high amplitude GWs => Could be a Detector of High Scale Symmetry breaking theories



PTA results (2020)

NANOGrav-fit

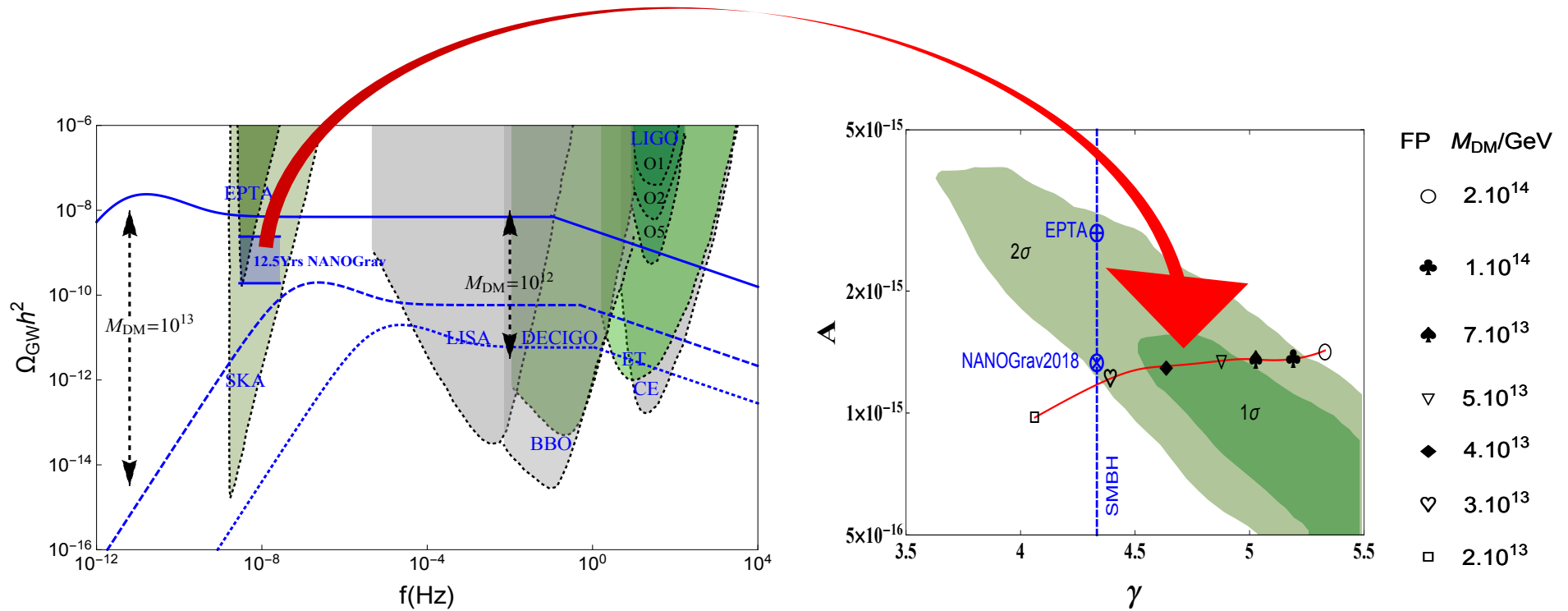
$$\Omega_{GW}(f) = \frac{2\pi^2}{3H_0^2} f^2 h_c(f)^2 = \Omega_{yr} \left(\frac{f}{f_{yr}} \right)^{5-\gamma}, \quad \text{with} \quad \Omega_{yr} = \frac{2\pi^2}{3H_0^2} A^2 f_{yr}^2.$$



Samanta, Urban JCAP (2022)

NANOGrav-fit

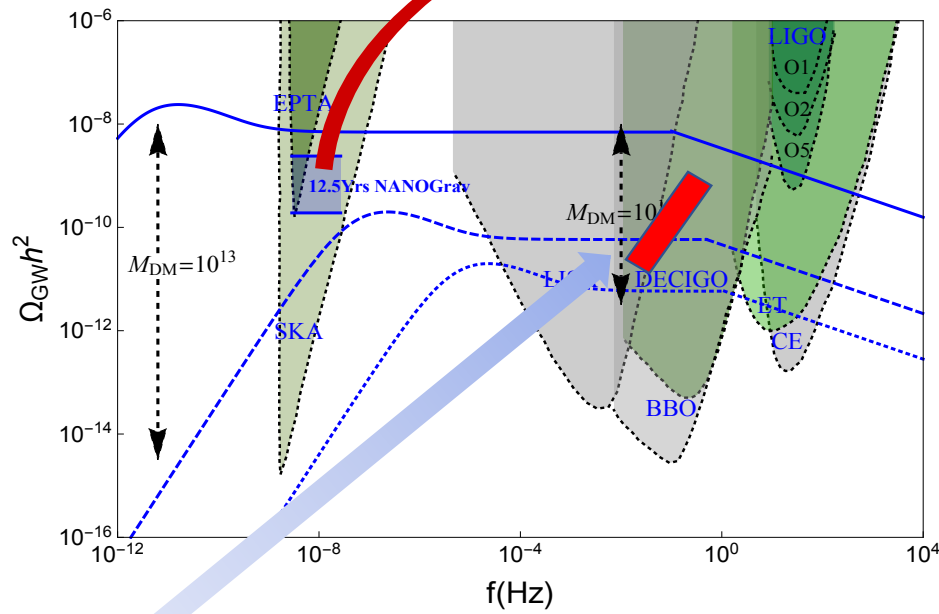
$$\Omega_{GW}(f) = \frac{2\pi^2}{3H_0^2} f^2 h_c(f)^2 = \Omega_{yr} \left(\frac{f}{f_{yr}} \right)^{5-\gamma}, \quad \text{with} \quad \Omega_{yr} = \frac{2\pi^2}{3H_0^2} A^2 f_{yr}^2.$$



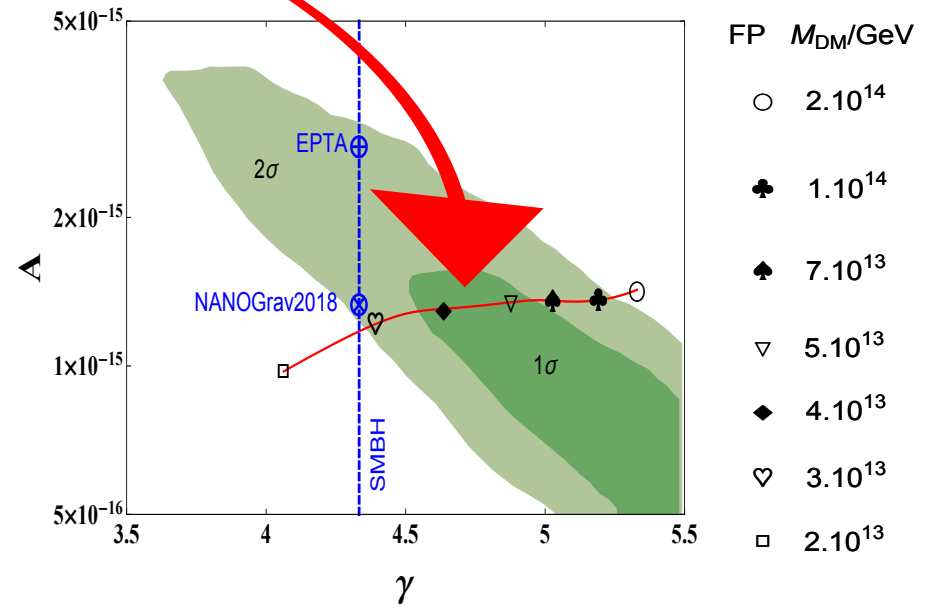
Samanta, Urban JCAP (2022)

NANOGrav-fit

$$\Omega_{GW}(f) = \frac{2\pi^2}{3H_0^2} f^2 h_c(f)^2 = \Omega_{yr} \left(\frac{f}{f_{yr}} \right)^{5-\gamma}, \quad \text{with} \quad \Omega_{yr} = \frac{2\pi^2}{3H_0^2} A^2 f_{yr}^2.$$



Turning point freq.



Samanta, Urban JCAP (2022)

Implementing in seesaw

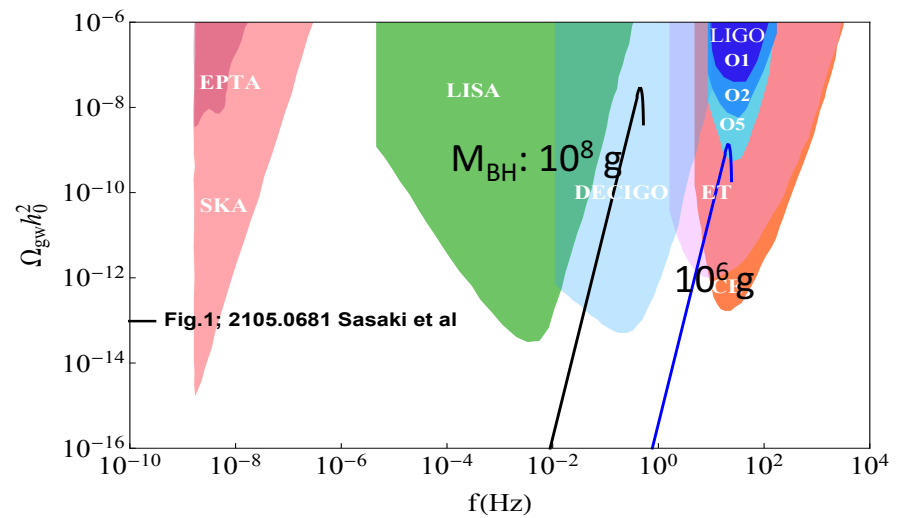
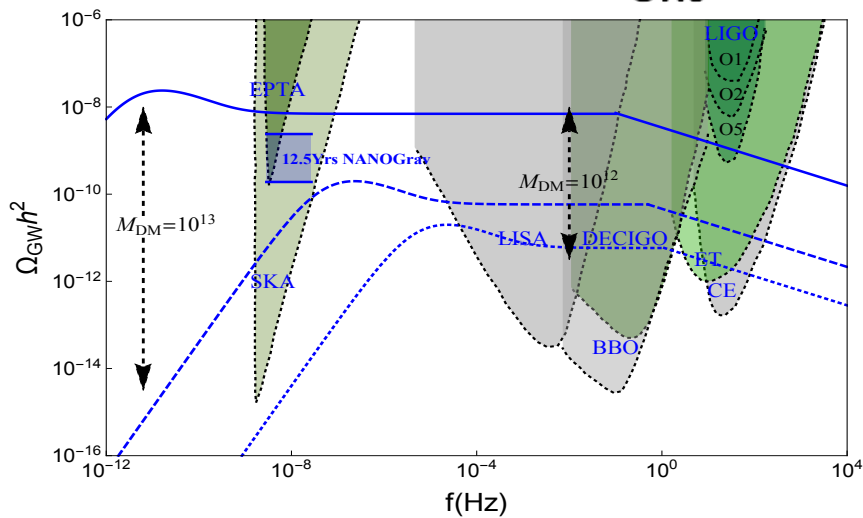
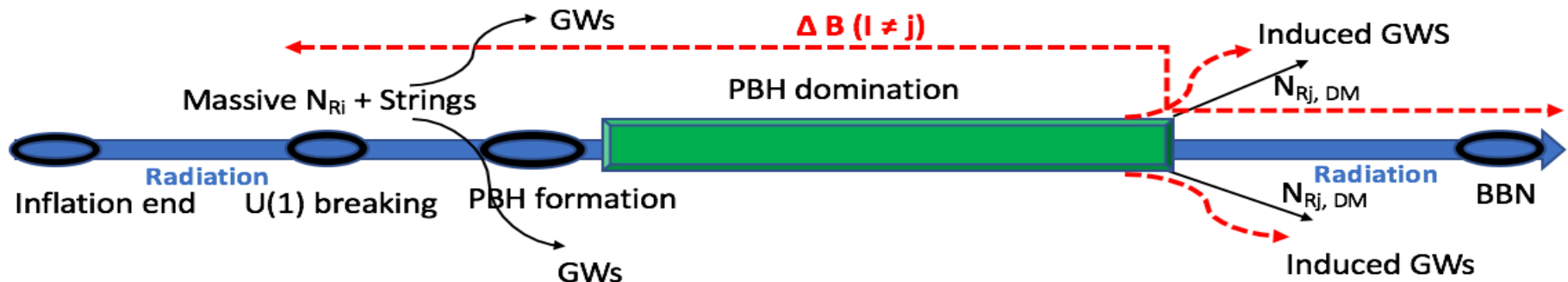
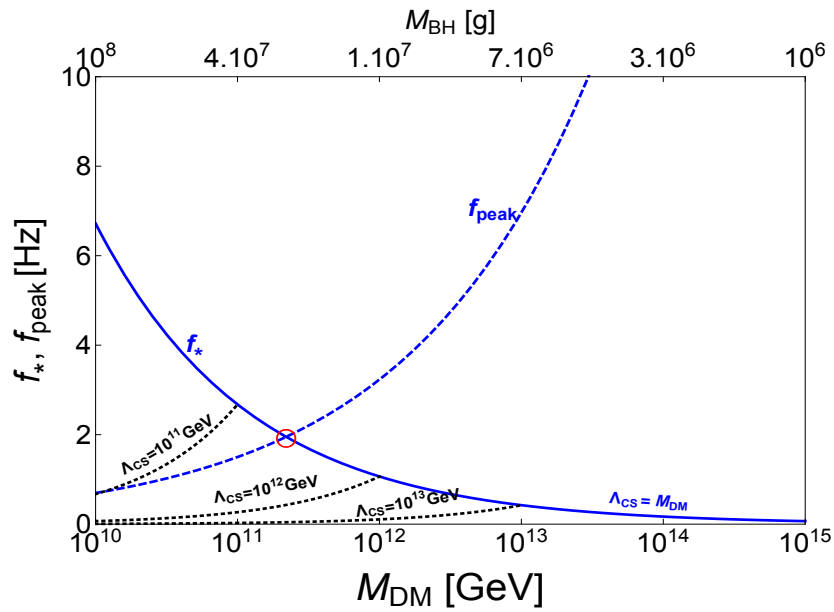
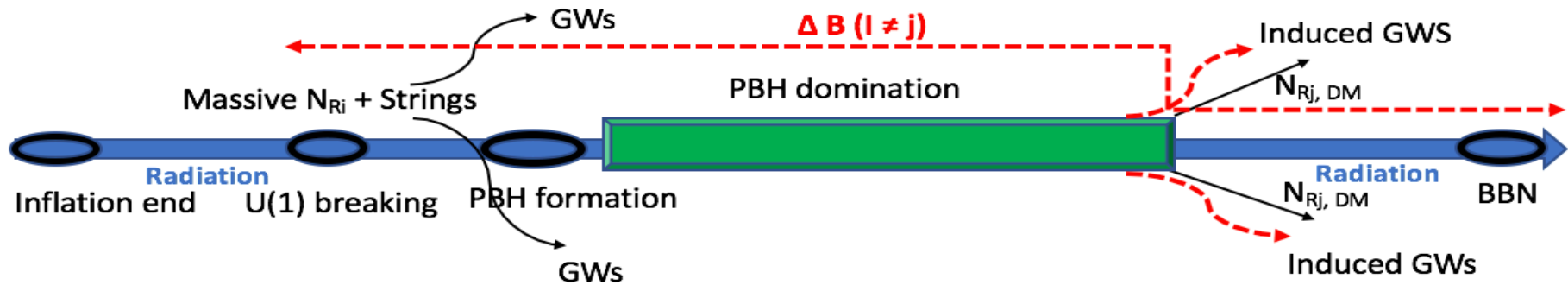


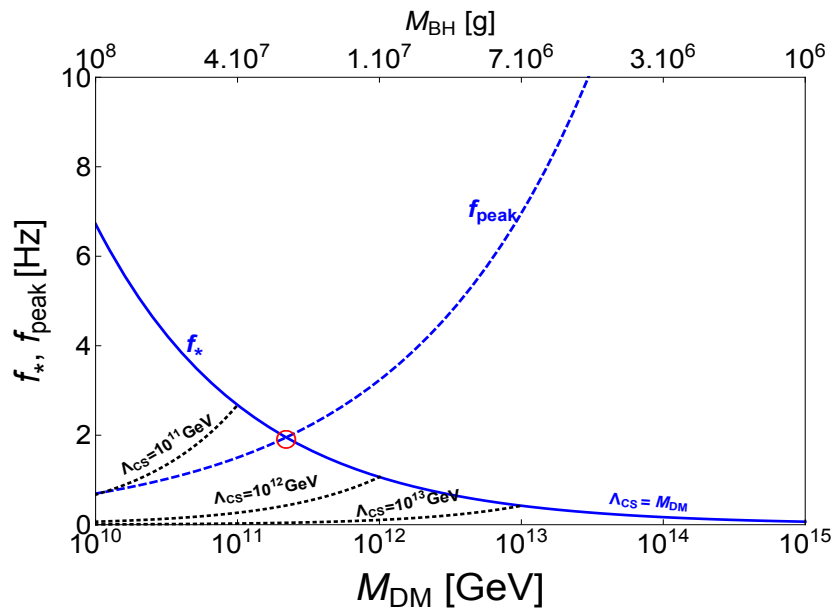
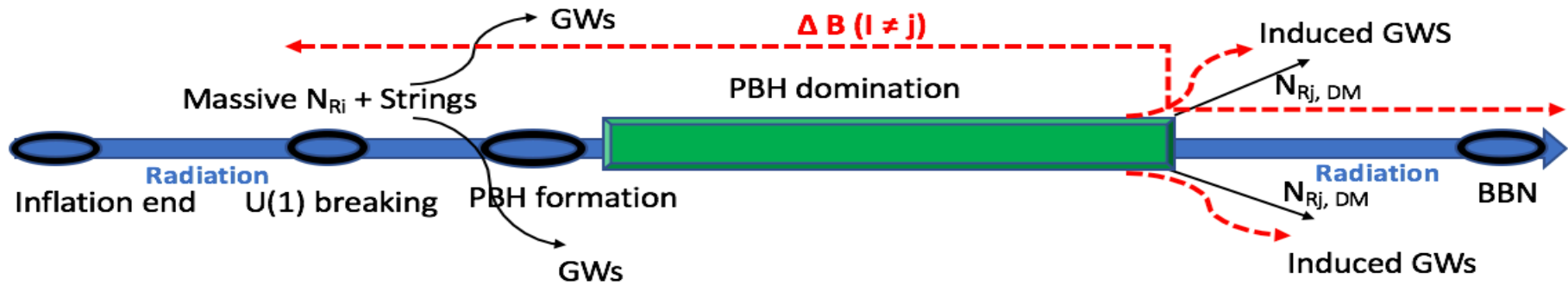
Fig.1; 2105.0681 Sasaki et al

$$\Omega_{GW}^{\text{peak}} \simeq 2 \times 10^{-6} \left(\frac{\beta}{10^{-8}} \right)^{16/3} \left(\frac{M_{BH}}{10^7 \text{ g}} \right)^{34/9}$$

Implementing in seesaw



Implementing in seesaw



Seesaw: all the N_i s are super heavy $\sim M \sim M_{DM} > 10^9$ GeV

Presentation take away

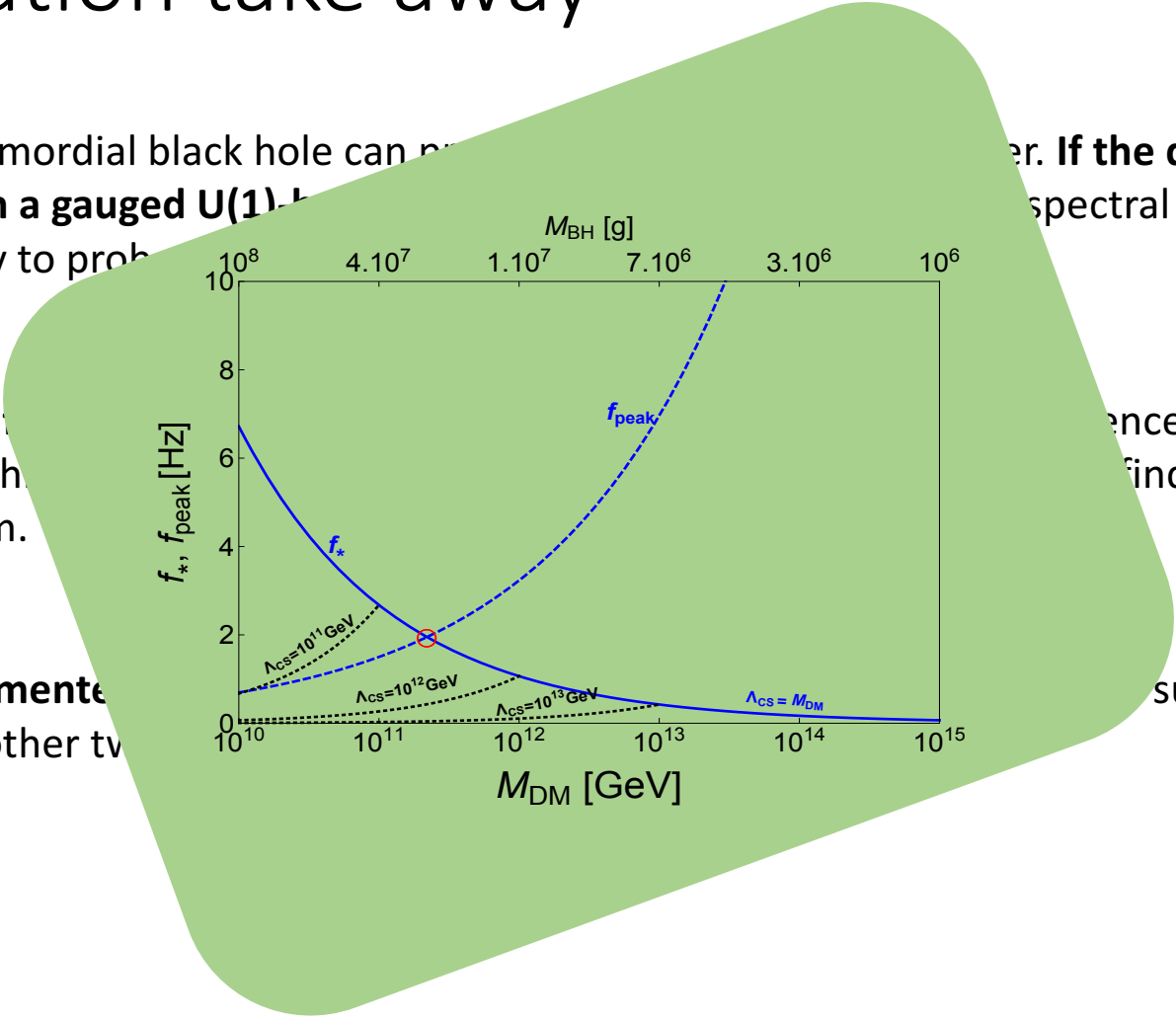
1. Ultralight primordial black hole can produce super heavy dark matter. **If the dark matter gets its mass with a gauged U(1)-breaking**, gravitational waves and their spectral features could be a unique way to probe dark matter above 10^9 GeV.
2. **If the recent finding by the pulsar timing arrays** corresponds to an existence of super heavy dark matter, high frequency detectors like LISA, DECIGO should be able to find a break in the GW spectrum.
3. **When implemented in seesaw**, one of the right-handed neutrinos could be super heavy dark matter and other two lead to thermal leptogenesis.

Presentation take away

1. Ultralight primordial black hole can produce a peak in the GW spectrum. **If the dark matter gets its mass with a gauged U(1) symmetry**, the peak frequency could be a unique way to probe the dark matter mass.

2. If the recent LIGO/Virgo observations find a peak in the GW spectrum, the presence of super heavy dark matter could be a good candidate to find a break in the spectrum.

3. When implemented in the context of super heavy dark matter and other theories, the peak frequency could be a unique way to probe the dark matter mass.



U(1) saga

S.F King, S Pascoli, J. Turner, YL Zhou, PRL (2021)

