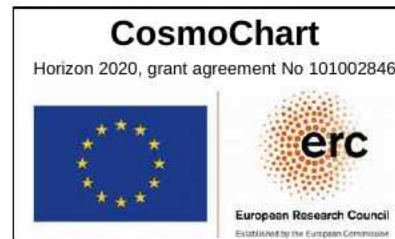


# Perspectives on dark matter

Kallia Petraki

Sorbonne University, LPTHE, Paris and Nikhef, Amsterdam



Planck conference  
Paris, 31 May 2022

# Classification schemes of dark matter candidates

## Interaction with the SM

### Portal operators

$$\epsilon F_Y^{\mu\nu} F_{D\mu\nu}$$

$$(\mu\phi + \lambda\phi^2)|H|^2$$

$$yLHN$$

### SM interactions

WIMPs

### Heavy mediators

EFTs

## (Self-) interaction type

### Long-range

Light mediators

$$m_{\text{med}} \ll m_{\text{DM}}$$

### Contact type

Heavy mediators

$$m_{\text{med}} \gtrsim m_{\text{DM}}$$

## Production mechanism

### Scalar condensates

Q-balls  
Axions

### Collapse of density perturbations

Primordial black holes

### Freeze-in

Sterile neutrinos  
Gravitinos

### Asymmetric freeze-out

Hidden sector models, e.g.  
dark U(1),  
dark QCD

### Symmetric freeze-out

WIMPs,  
Hidden sectors

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Talk by Alex Kusenko

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Talk by Keith Olive

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# Frontiers in dark matter searches

- **Heavy DM**

Particles with  $m \gtrsim \text{TeV}$  coupled to SM via the Weak or other interactions not constrained by collider experiments

→ existing and upcoming telescopes observing multi-TeV sky with increasing sensitivity, e.g. HESS, IceCube, CTA, Antares

- **Light DM**

Particles with  $m \lesssim \text{few GeV}$ , possibly coupled to SM via a portal interaction, not constrained by older direct detection experiments

→ development of new generation of direct detection experiments

# Frontiers in dark matter searches

- **Heavy DM**

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- **Light DM**

Partic

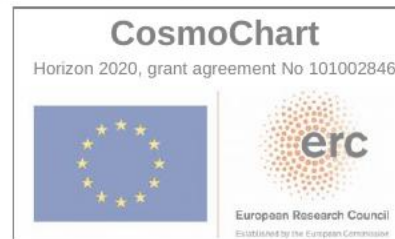
- Simple thermal-relic WIMP models live in the (multi-)TeV scale.
- Thermal-relic DM can be as heavy as  $\text{few} \times 100 \text{ TeV}$ .

**How heavy can thermal-relic DM be, and what are the underlying dynamics of heavy ( $\gtrsim \text{TeV}$ ) thermal-relic DM?**

# Perspectives on dark matter <sup>heavy</sup>

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# Long-range interactions

If dark matter is very heavy, then:

$$\lambda_B \sim \frac{1}{\mu v_{\text{rel}}}, \frac{1}{\mu \alpha} \lesssim \frac{1}{m_{\text{mediator}}} \sim \text{interaction range}$$

$\mu$ : reduced mass ( $m_{\text{DM}}/2$ )



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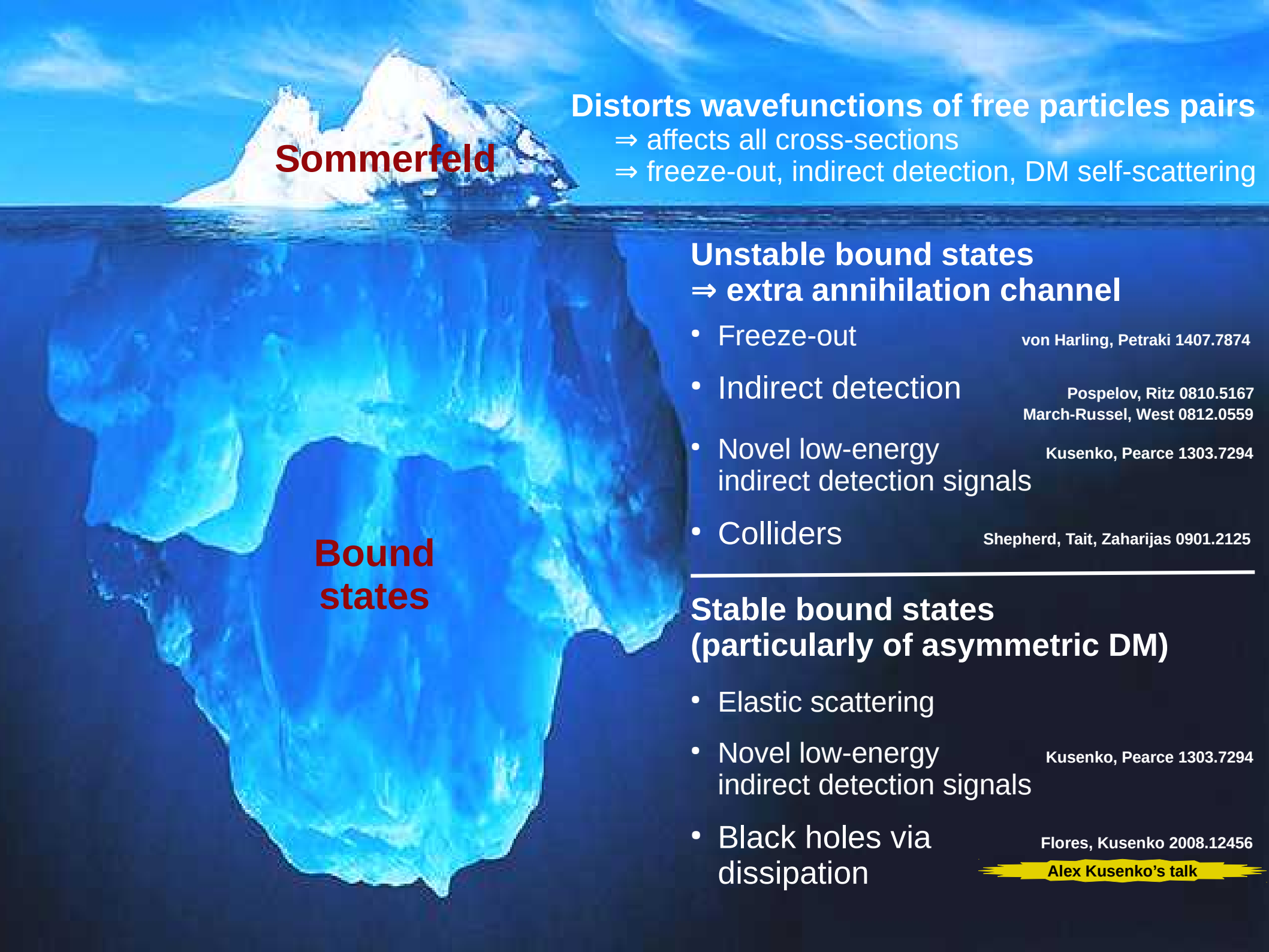
$\mu$ : reduced mass ( $m_{\text{DM}}/2$ )

## Relevant for various models

- Self-interacting DM
- WIMP DM with  $m_{\text{DM}} > \text{few TeV}$ .
- WIMP DM with  $m_{\text{DM}} < \text{TeV}$ ,  
in scenarios of DM co-annihilation with coloured partners.

**+ other models with dark forces**

**What's different about  
long-range interactions?**



**Sommerfeld**

**Distorts wavefunctions of free particles pairs**

⇒ affects all cross-sections

⇒ freeze-out, indirect detection, DM self-scattering

**Unstable bound states**

⇒ **extra annihilation channel**

- Freeze-out

von Harling, Petraki 1407.7874

- Indirect detection

Pospelov, Ritz 0810.5167

March-Russel, West 0812.0559

- Novel low-energy indirect detection signals

Kusenko, Pearce 1303.7294

- Colliders

Shepherd, Tait, Zaharijas 0901.2125

**Bound states**

**Stable bound states (particularly of asymmetric DM)**

- Elastic scattering

- Novel low-energy indirect detection signals

Kusenko, Pearce 1303.7294

- Black holes via dissipation

Flores, Kusenko 2008.12456

**Alex Kusenko's talk**

An iceberg floating in the ocean. The tip of the iceberg is above the water surface and is labeled 'Sommerfeld'. The much larger part of the iceberg is submerged below the surface and is labeled 'Bound states'. The sky is blue with some clouds, and the water is a deep blue.

**Sommerfeld**

**Distorts wavefunctions of free particles pairs**  
⇒ affects all cross-sections  
⇒ freeze-out, indirect detection, DM self-scattering

**Unstable bound states**  
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# Freeze-out with bound states

- Dark U(1) sector
- Neutralino-squark coannihilation
- The role of the Higgs

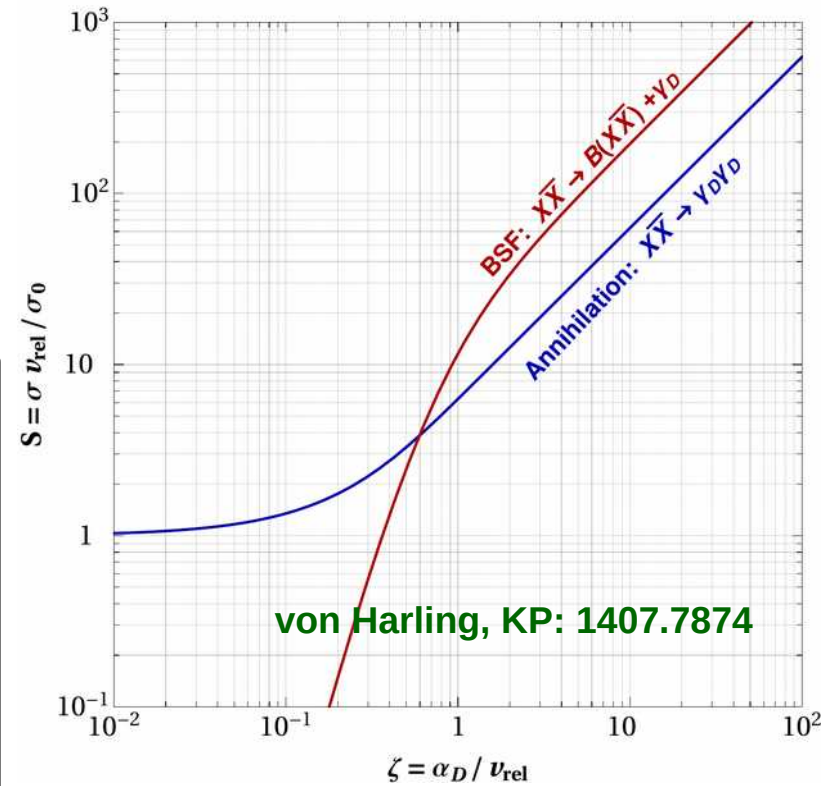
# Dark U(1) model: Dirac DM $X, \bar{X}$ coupled to $\gamma_D$

**Direct annihilation**  
 $X + \bar{X} \rightarrow 2\gamma_D$

$$\sigma_{\text{ann}} v_{\text{rel}} = \frac{\pi \alpha_D^2}{m_X^2} \times S_{\text{ann}}(\alpha_D / v_{\text{rel}})$$

**Bound-state formation and decay**

$$\sigma_{\text{BSF}} v_{\text{rel}} = \frac{\pi \alpha_D^2}{m_X^2} \times S_{\text{BSF}}(\alpha_D / v_{\text{rel}})$$



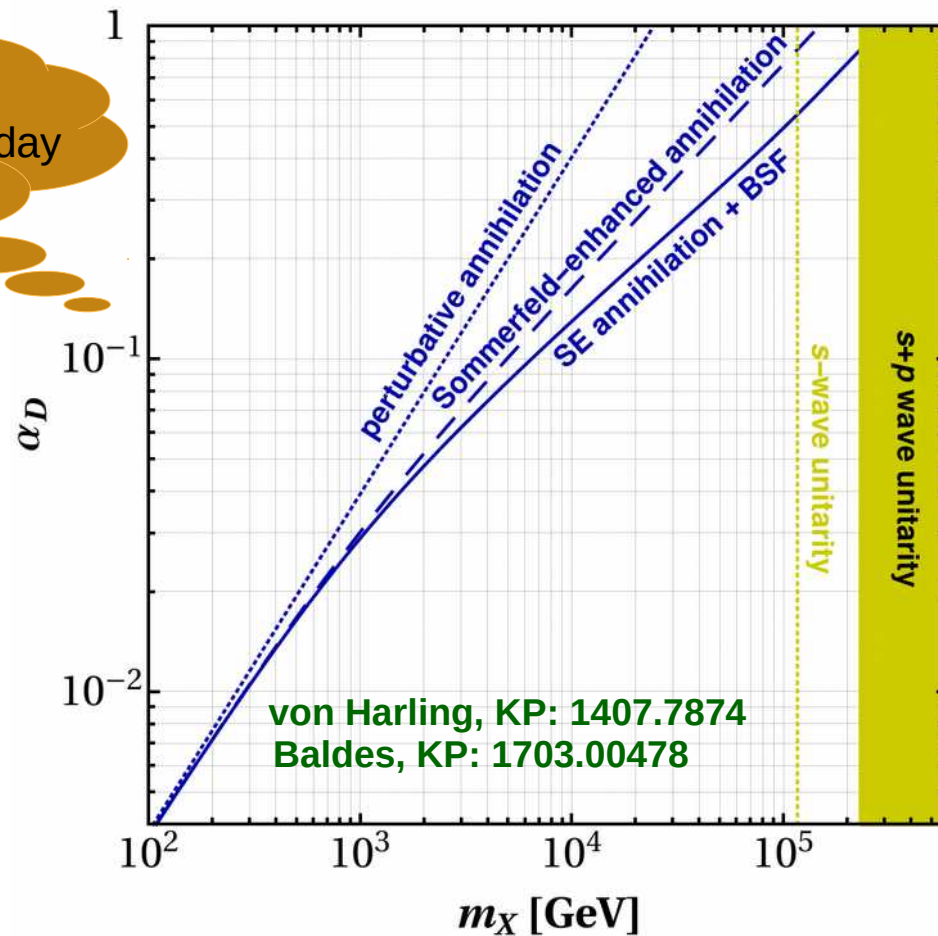
$$S_{\text{ann}} \simeq \left( \frac{2\pi\zeta}{1 - e^{-2\pi\zeta}} \right) \xrightarrow{\zeta \gg 1} 2\pi\zeta$$

$$S_{\text{BSF}} \simeq \left( \frac{2\pi\zeta}{1 - e^{-2\pi\zeta}} \right) \frac{2^9 \zeta^4 e^{-4\zeta \text{arccot} \zeta}}{3(1 + \zeta^2)^2} \xrightarrow{\zeta \gg 1} 3.13 \times 2\pi\zeta$$

# Thermal freeze-out with long-range interactions

Dark U(1) model: Dirac DM  $X, \bar{X}$  coupled to  $\gamma_D$

Important because it determines DM interactions today (direct, indirect detection)



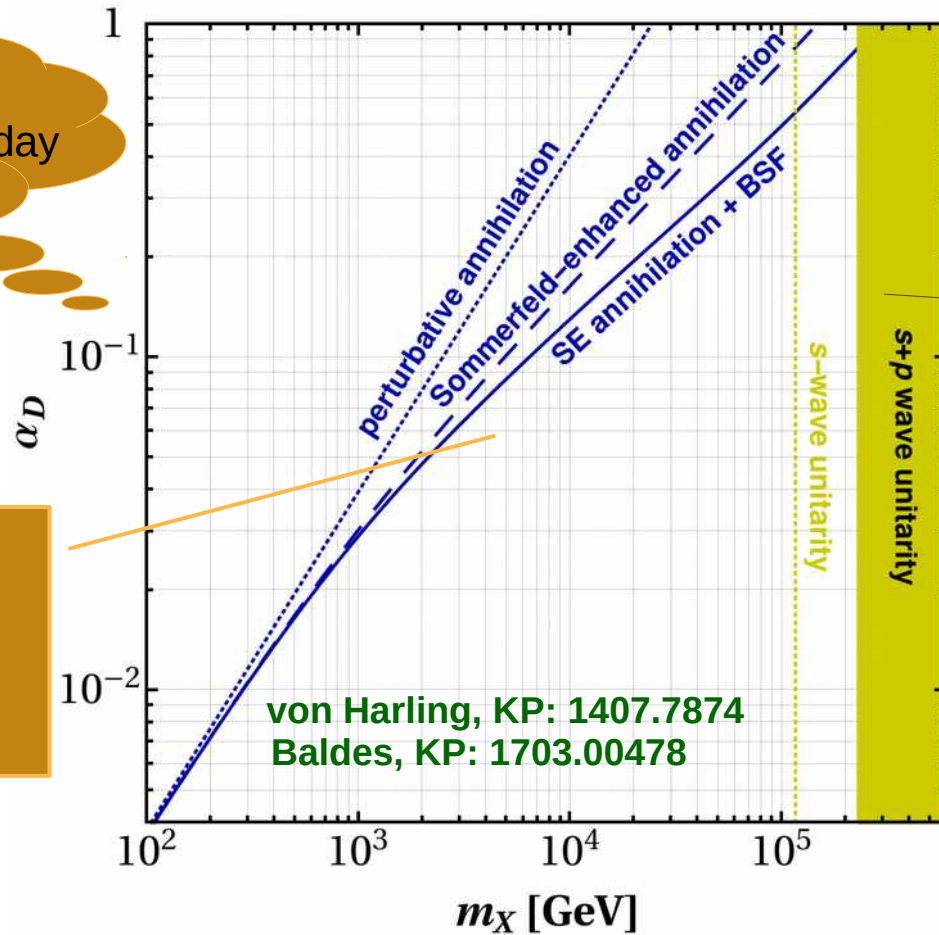


# Thermal freeze-out with long-range interactions

Dark U(1) model: Dirac DM  $X, \bar{X}$  coupled to  $\gamma_D$

Important because it determines DM interactions today (direct, indirect detection)

Long-range effects indeed become at  $m_{DM} \gtrsim$  few TeV.  
Verifies expectation from unitarity arguments!



Dominant annihilation mode: **s-wave**.  
Dominant BSF mode: **p-wave**  
Same order!  
Higher partial waves Important / dominant in multi-TeV regime.  
**DM may be even heavier!**



# Neutralino in SUSY models

## Squark-neutralino co-annihilation scenarios

- Degenerate spectrum  $\rightarrow$  soft jets  $\rightarrow$  evade LHC constraints
- Large stop-Higgs coupling reproduces measured Higgs mass and brings the lightest stop close in mass with the LSP

$\Rightarrow$  DM density determined by “effective” Boltzmann equation

$$n_{\text{tot}} = n_{\text{LSP}} + n_{\text{NLSP}}$$

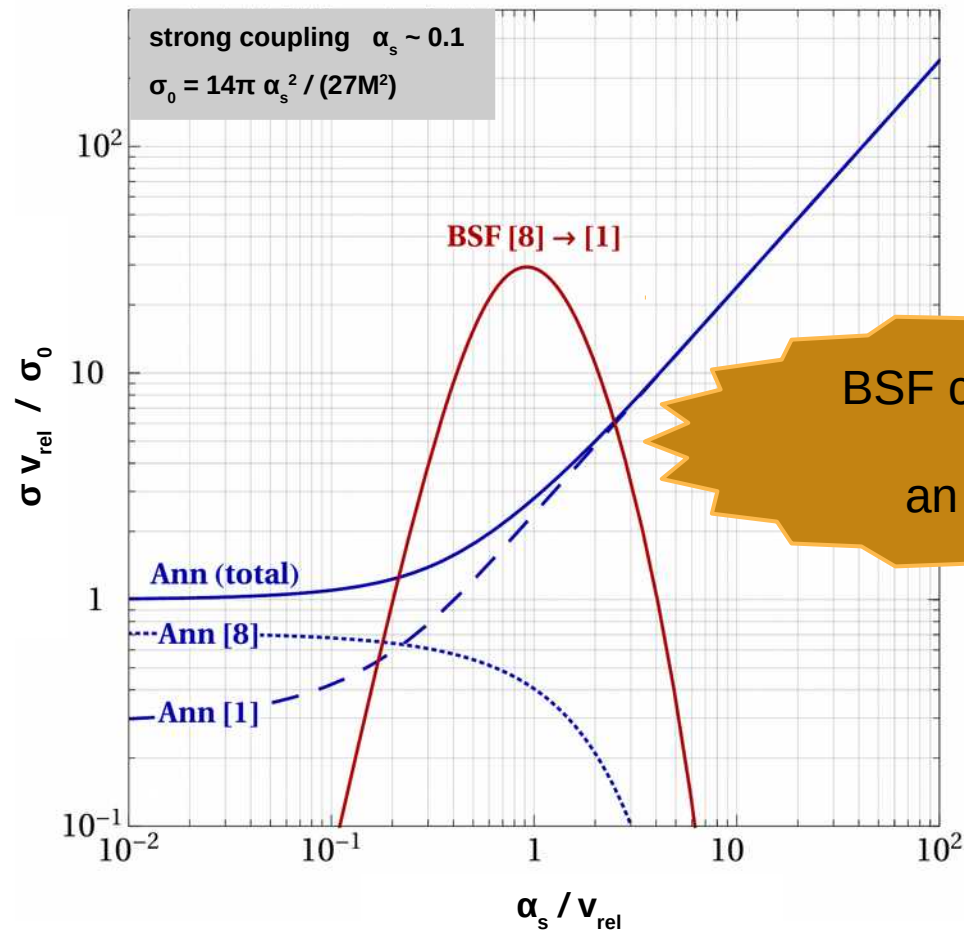
$$\sigma_{\text{ann}}^{\text{eff}} = [n_{\text{LSP}}^2 \sigma_{\text{ann}}^{\text{LSP}} + n_{\text{NLSP}}^2 \sigma_{\text{ann}}^{\text{NLSP}} + n_{\text{LSP}} n_{\text{NLSP}} \sigma_{\text{ann}}^{\text{LSP-NLSP}}] / n_{\text{tot}}^2$$

Scenario probed in colliders.  
 Important to compute DM density accurately!  
 $\rightarrow$  QCD corrections

# DM coannihilation with scalar colour triplet

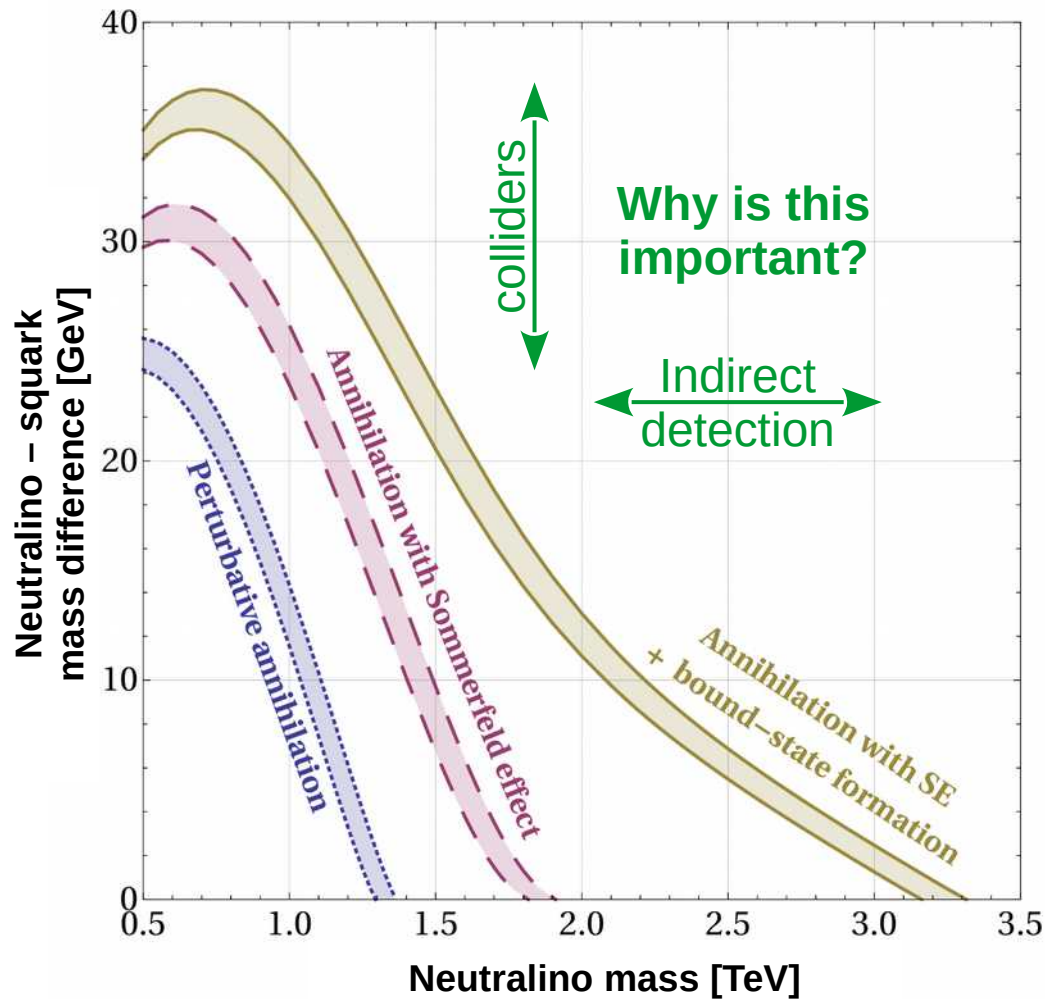
## MSSM-inspired toy model

### Bound-state formation vs Annihilation



BSF can exceed Annihilation  
by more than  
an order of magnitude!

# DM coannihilation with scalar colour triplet MSSM-inspired toy model



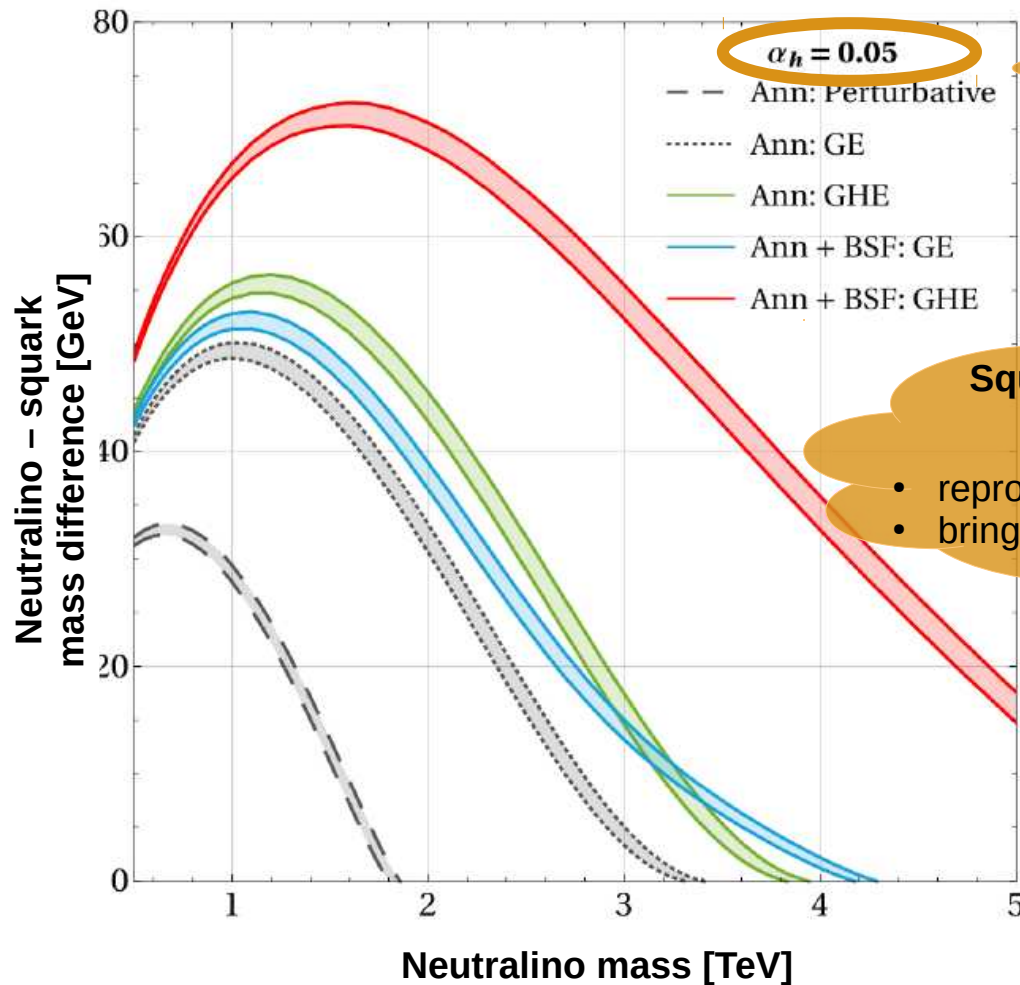
Effect on relic density:  
much much larger than  
obs uncertainty in  $\Omega_{\text{DM}}$

Not the  
final picture!

# DM coannihilation with scalar colour triplet

## MSSM-inspired toy model

### The effect of the Higgs-mediated potential



Squark-antisquark-Higgs coupling

Large  $\alpha_h$

- reproduces measured Higgs mass
- brings lightest stop close in mass with LSP

Not the final picture!

# The Higgs as a light mediator

- Sommerfeld enhancement of direct annihilation
- Binding of bound states

Harz, KP: 1711.03552

Harz, KP: 1901.10030

# The Higgs as a light mediator

- Sommerfeld enhancement of direct annihilation
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## • Formation of bound states via Higgs (*doublet*) emission ?

Capture via emission of neutral scalar suppressed,  
due to selection rules: quadruple transitions

March-Russel, West 0812.0559  
KP, Postma, Wiechers: 1505.00109  
An, Wise, Zhang: 1606.02305  
KP, Postma, de Vries: 1611.01394

Capture via emission of charged scalar [or its Goldstone mode]  
very very rapid: monopole transitions !

Ko, Matsui, Tang: 1910.04311  
Oncala, KP: 1911.02605  
Oncala, KP: 2101.08666  
Oncala, KP: 2101.08667

Sudden change in effective Hamiltonian precipitates transitions.  
Akin to atomic transitions precipitated by  $\beta$  decay of nucleus.

# Renormalisable WIMP models with coupling to the Higgs

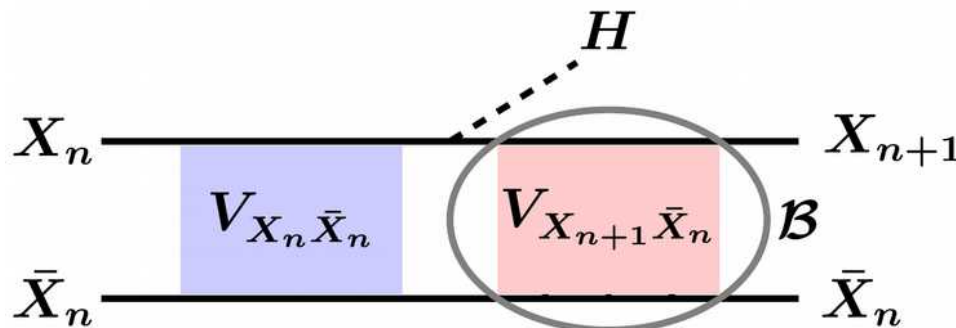
In some prototypical WIMP models, DM is the lightest linear combination of the neutral components of SU(2) multiplets that couple to the Higgs

$$\delta\mathcal{L} \supset -y\bar{X}_n H X_{n+1} + \text{h.c.}$$

Includes many SUSY scenarios, e.g. Wino-Higgsino, coloured coannihilation

If  $m > 5$  TeV, DM freeze-out begins before electroweak phase transition.

⇒ **Bound-state formation via Higgs-doublet emission!**



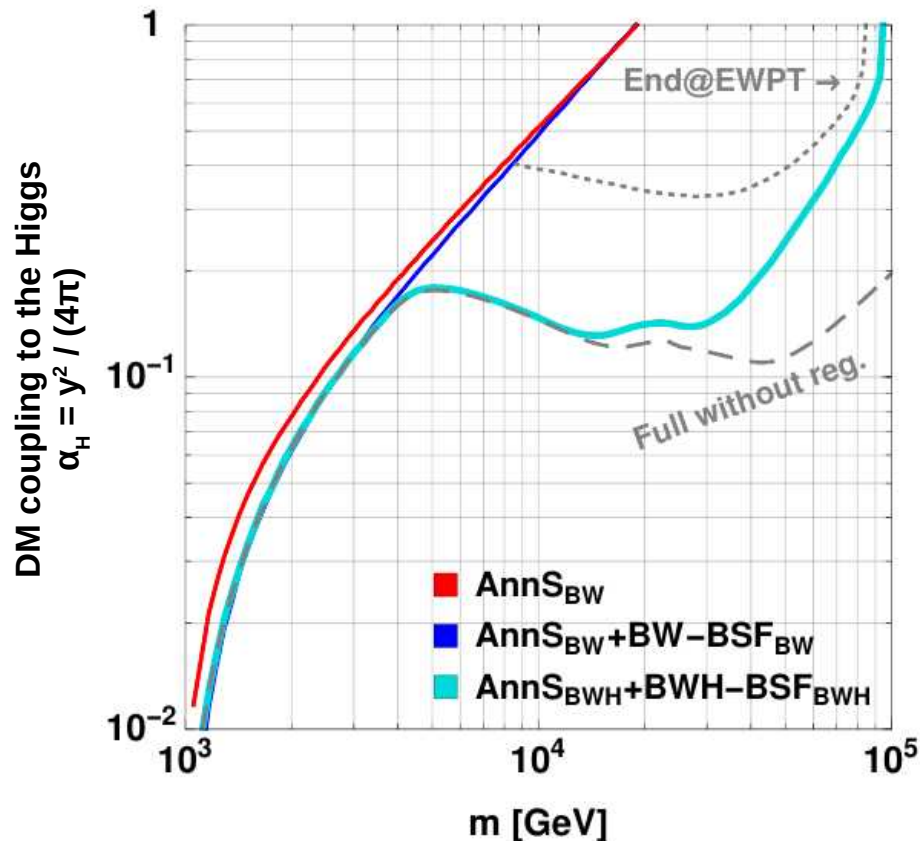
Change in potential  
⇒ monopole transition!

# Renormalisable WIMP models with coupling to the Higgs

Singlet-Doublet coupled to the Higgs:  $L \supset -y \bar{D} H S$

$m_D \approx m_S \rightarrow D$  and  $S$  co-annihilate.

Freeze-out begins before the EWPT if  $m_{DM} > 5\text{TeV}$



**Huge effect!**

**$\sim 10^2$  in relic density!**

**Impels reconsideration  
of Higgs-portal models  
(incl. neutralino-squark  
coann scenarios)**



## Many studies of bound-state effects on DM freeze-out

In this conference

- **“Closing the window on WIMP dark matter models”**, Salvatore BOTTARO (Monday 30/05)
- **“Sommerfeld Effect and Bound State Formation in Simplified Dark Matter Models”**, Emanuele COPELLO (Wednesday 01/06)

Is it random that non-perturbative effects arise  
in all these models at multi-TeV?

Or is there a model-independent way  
to understand and *predict* it?

If so, what else can we learn from it?

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in all these models at multi-TeV?

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to understand and *predict* it?

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# Partial-wave unitarity limit

$$S^\dagger S = 1 \quad \xrightarrow{S=1+iT} \quad -i(T - T^\dagger) = T^\dagger T$$

Project on a partial wave and  
insert complete set of states on RHS

↓

$$\sigma_{\text{inel}}^{(\ell)} \leq \frac{\pi(2\ell + 1)}{k_{\text{cm}}^2} \xrightarrow{\text{non-rel}} \frac{\pi(2\ell + 1)}{\mu^2 v_{\text{rel}}^2} \xrightarrow{\mu=M_{\text{DM}}/2} \frac{4\pi(2\ell + 1)}{M_{\text{DM}}^2 v_{\text{rel}}^2}$$

[Griest, Kamionkowski (1990); Hui (2001)]

**Physical meaning:**  
saturation of probability for inelastic scattering

# Partial-wave unitarity limit in non-relativistic regime

$$\sigma_{\text{inel}}^{(\ell)} v_{\text{rel}} \leq \sigma_{\text{uni}}^{(\ell)} v_{\text{rel}} = \frac{4\pi(2\ell + 1)}{M_{\text{DM}}^2 v_{\text{rel}}}$$

Implies upper bound on the mass of thermal-relic DM

Griest, Kamionkowski (1990)

$$\sigma_{\text{ann}} v_{\text{rel}} \simeq 2.2 \times 10^{-26} \text{ cm}^3/\text{s} \leq \frac{4\pi}{M_{\text{DM}}^2 v_{\text{rel}}}$$

$$\langle v_{\text{rel}}^2 \rangle^{1/2} = (6T/M_{\text{DM}})^{1/2} \xrightarrow[M_{\text{DM}}/T \approx 25]{\text{freeze-out}} 0.49$$

$$\Rightarrow M_{\text{uni}} \simeq \begin{cases} 117 \text{ TeV,} & \text{self-conjugate DM} \\ 83 \text{ TeV,} & \text{non-self-conjugate DM} \end{cases}$$

- Assumes contact-type interactions,  $\sigma v_{\text{rel}} = \text{constant}$
- Considers only s-wave annihilation

# Partial-wave unitarity limit in non-relativistic regime



What interactions can realise the unitarity limit?

$$\sigma_{\text{inel}}^{(\ell)} v_{\text{rel}} \leq \sigma_{\text{uni}}^{(\ell)} v_{\text{rel}} = \frac{4\pi(2\ell + 1)}{M_{\text{DM}}^2 v_{\text{rel}}}$$

Parametric dependence on mass and velocity implies that  $\sigma_{\text{uni}}$  can be approached or attained only by long-range interactions

Long-range interactions imply **bound states**, which may form by **higher partial waves** of the scattering state that contribute at the same order.

- Thermal relic DM can be much heavier than anticipated.
- In viable thermal scenarios, expect long-range behavior at  $m_{\text{DM}} \gtrsim \text{few TeV}$  (important for exps)
- No model-independent unitarity limit on mass of thermal relic DM!

Baldes, KP: 1703.00478

# Conclusions

- **Bound states impel complete reconsideration of thermal decoupling at / above the TeV scale: *emergence of a new type of inelasticity***

Unitarity limit can be approached / realised only by long-range interactions  
⇒ bound states play very important role!

Baldes, KP: 1703.00478

**There is no unitarity limit on the mass of thermal relic DM!**

- **Experimental implications:**
  - **DM heavier than anticipated:** multi-TeV probes very important.
  - **Indirect detection:**
    - Enhanced rates due to BSF
    - Novel signals: low-energy radiation emitted in BSF
    - Indirect detection of asymmetric DM
  - **Colliders:** improved detection prospects due increased mass gap in coannihilation scenarios
- **Effects not limited to the thermal-relic scenario...**