Higgs-boson induced reheating and ultraviolet freeze-in dark matter

Anna Socha

University of Warsaw

based on: A. Ahmed, B. Grządkowski, AS 2111.06065 and 2206.XXXXX

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- Even in the case of non-instantaneous reheating models, it is usually assumed that the inflaton decay rate, Γ_{ϕ} , is constant.
- However, this widely used assumption of constant can be violated in generic models of perturbative reheating, e.g., when the inflaton has a non-trivial potential.
- The understanding of the reheating era is essential for the dark matter sector, especially in the context of the freeze-in DM production.

Reheating dynamics

The dynamics of the early Universe is captured by the following time-averaged Boltzmann equations for the inflaton field and the SM radiation ${\cal R}$

$$\dot{\rho}_{\phi} + 3(1+w)H\rho_{\phi} = -\Gamma_{\phi}\rho_{\phi},$$
$$\dot{\rho}_{\mathcal{R}} + 4H\rho_{\mathcal{R}} = +\Gamma_{\phi}\rho_{\phi},$$

where the Hubble rate is given by

$$\mathcal{H}^2 = \frac{1}{3M_{\rho l}^2} \left(\rho_\phi + \rho_\mathcal{R} \right),$$

whereas the time-dependence of the averaged inflaton decay width can be parametrized as

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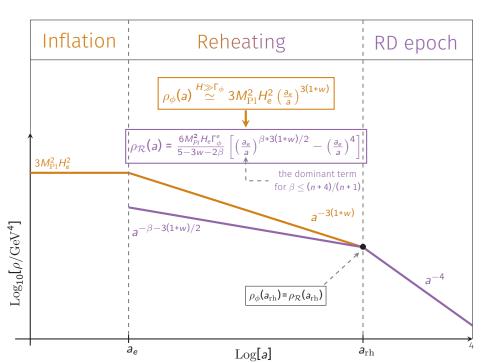
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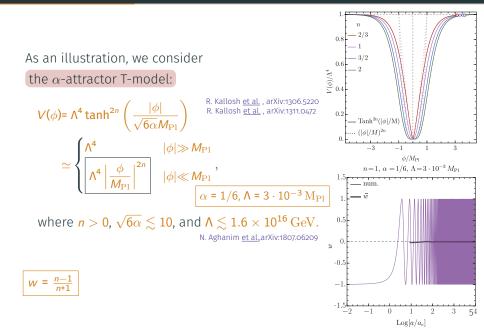
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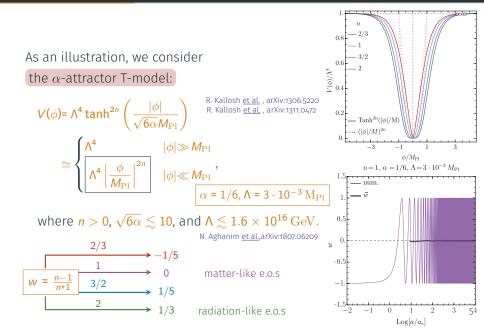
$$\Gamma_{\phi} = \Gamma_{\phi}^{e} \left(\frac{a_{e}}{a}\right)^{\beta}$$
initial value of
a scale factor
constant parameter



Example model



Example model



We assume that the inflaton couples to the SM sector through the Higgs portal

 $g_{h\phi}M_{\rm Pl}\phi(a)|\mathbf{h}|^2 = g_{h\phi}M_{\rm Pl}\varphi(a)\mathcal{P}(a)|\mathbf{h}|^2$

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$$\frac{1}{\sqrt{6\alpha}} \left(\frac{\Lambda^2}{\phi M_{\rm Pl}}\right)^2 \left(\frac{\phi}{M}\right) < g_{h\phi} < \frac{\Lambda^2}{\phi M_{\rm Pl}}$$

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Reheating

The energy gain of the radiation sector per volume and time is

$$\frac{1}{V}\frac{dE_g}{dt}=\rho_\phi \Gamma_\phi$$

with

$$\frac{1}{V}\frac{dE_g}{dt} = \frac{\varphi^2(t)}{8\pi} \sum_{i=0}^3 \sum_{k=1}^\infty k\omega |\mathcal{P}_k|^2$$
$$\times \sqrt{1 - \left(\frac{2m_{h_i}}{k\omega}\right)^2} |\mathcal{M}_{0 \to h_i h_i}(k)|^2$$

Inflaton-induced Higgs mass

$$m_{h_i}^2 = g_{h\phi} M_{\rm Pl} \varphi \begin{cases} |\mathcal{P}|, & \mathcal{P}(a) > 0, i = 0, 1, 2, 3\\ 2|\mathcal{P}|, & \mathcal{P}(a) < 0, i = 0\\ \infty, & \mathcal{P}(t) < 0, i = 1, 2, 3 \end{cases}$$

Due to the inflaton oscillations, the Higgs field goes through rapid phase transitions with ϕ -dependent vev:

$$v_{h} = \begin{cases} 0, & \mathcal{P}(a) > 0 \\ \sqrt{\frac{|m_{h_{0}}^{2}|}{2\lambda_{h}}}, & \mathcal{P}(a) < 0 \end{cases}$$

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K. Ichikawa <u>et al.</u> arXiv:0807.3988 $\frac{1}{V} \frac{dE_g}{dt} = \rho_{\phi} \Gamma_{\phi}$ With $\mathcal{P} = \sum_k \mathcal{P}_k e^{-ik\omega t} \ll --1$ $\frac{1}{V} \frac{dE_g}{dt} = \frac{\varphi^2(t)}{8\pi} \sum_{i=0}^3 \sum_{k=1}^\infty k\omega |\mathcal{P}_k|^2$ $\times \sqrt{1 - \left(\frac{2m_{h_i}}{k\omega}\right)^2} |\mathcal{M}_{0 \to h_i h_i}(k)|^2$ Inflaton-induced Higgs mass

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The inflaton decay rate can be written as

$$\Gamma_{\phi} = \frac{g_{h\phi}^2}{32\pi} \frac{M_{\rm Pl}^2}{m_{\phi}(a)} \gamma_h(a),$$

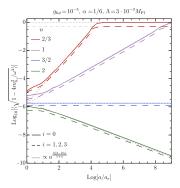
$$\gamma_h(a) \simeq \sum_{i=0}^3 \sum_{k=1}^\infty k |\mathcal{P}_k|^2 \left\langle \sqrt{1 - \left(\frac{2m_{h_i}(a)}{k\omega(a)}\right)^2} \right\rangle$$

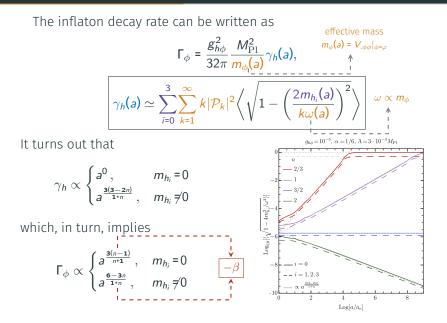
It turns out that

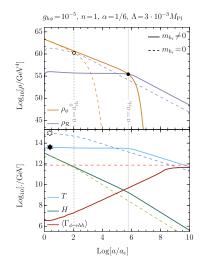
$$\gamma_h \propto \begin{cases} a^0, & m_{h_i} = 0\\ a^{\frac{3(3-2n)}{1+n}}, & m_{h_i} \neq 0 \end{cases}$$

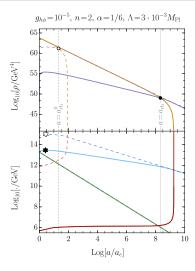
which, in turn, implies

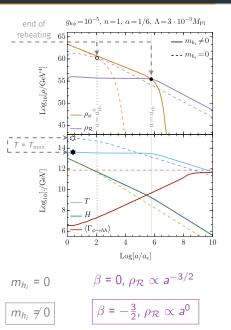
$$\Gamma_{\phi} \propto \begin{cases} a^{\frac{3(n-1)}{n+1}} \,, & m_{h_i} = 0 \\ a^{\frac{6-3n}{1+n}} \,, & m_{h_i} \neq 0 \end{cases}$$

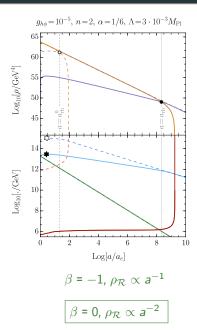












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Let us assume that the dark sector is composed of spin-1, massive particles X_{μ} , charged under a dark, abelian $U(1)_X$ symmetry, with the following Lagrangian density

$$\mathcal{L}_{\rm DM} = -\frac{1}{4} X_{\mu\nu} X^{\mu\nu} + \frac{1}{2} m_X^2 X_{\mu} X^{\mu} + \mathcal{L}_{\rm int}$$

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 the dark Higgs Φ

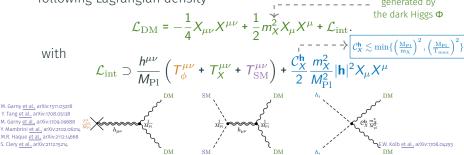
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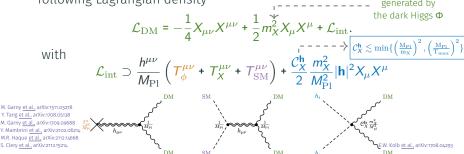
with

$$\mathcal{L}_{\rm int} \supset \frac{h^{\mu\nu}}{M_{\rm Pl}} \left(T^{\mu\nu}_{\phi} + T^{\mu\nu}_X + T^{\mu\nu}_{\rm SM} \right) + \frac{\mathcal{C}^{\sf h}_X}{2} \frac{m^2_X}{M^2_{\rm Pl}} |{\sf h}|^2 X_{\mu} X^{\mu}$$

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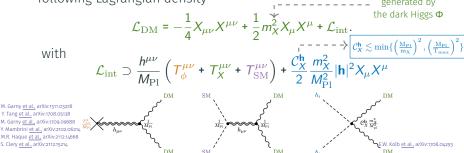
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Gravitational production

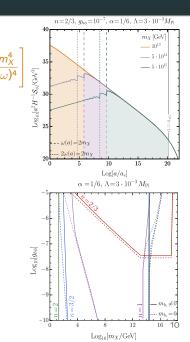
The source terms are

$$\begin{split} \mathcal{S}_{\phi} &= \frac{1}{8\pi} \left(\frac{\rho_{\phi}}{M_{\rm Pl}^2} \right)^2 \sum_{k=1}^{\infty} |\mathcal{P}_k^{2n}|^2 \left[\left(1 - \frac{2m_X^2}{(k\omega)^2} \right)^2 + \frac{8n}{(k\omega)^2} \right] \\ &\times \sqrt{1 - \frac{4m_X^2}{(k\omega)^2}} \\ \mathcal{S}_{\rm SM} &= n_0 \langle \sigma | v | \rangle_0 + n_{1/2} \langle \sigma | v | \rangle_{1/2} + n_1 \langle \sigma | v | \rangle_1 \\ n_1 \langle \sigma | v | \rangle_1 &\simeq \begin{cases} \frac{13}{20\pi^5} T^8 / M_{\rm Pl}^4, & m_X \ll T, \\ \frac{1}{16\pi^4} \frac{m_X^5 T^3}{M_{\rm Pl}^4} e^{-2m_X/T}, & m_X \gg T \end{cases} \end{split}$$

The DM relic abundance can be calculated as

$$\Omega_{\chi}^{
m grav} h^2 \simeq rac{m_{\chi}}{
ho_c} rac{N^{
m grav}(a_{
m rh})}{a_{
m rh}^3} rac{s_0}{s(a_{
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Successful DM model has to predict the correct amount of DM i.e., $\Omega_X^{\text{grav}} h^2 = \Omega_X^{(\text{obs})} h^2$



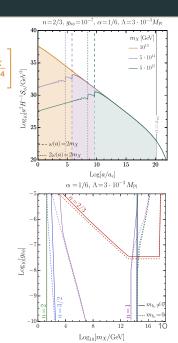
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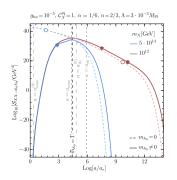
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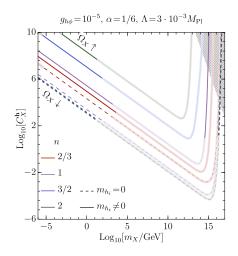
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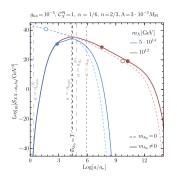
The DM freeze-in production is very sensitive to the dynamics of reheating.

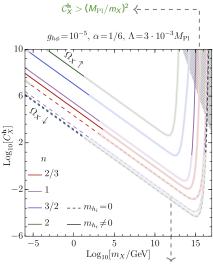




DM production through the contact operator

The DM freeze-in production is very sensitive to the dynamics of reheating.





Gravitational Overproduction

Summary

We have demonstrated that the non-standard $(n \neq 1)$ cosmologies and the kinematical suppression of radiation production significantly affect the thermal bath evolution and the DM production.

• In particular, we have shown that the duration of reheating and the evolution of the radiation energy density, ρ_R , are sensitive to the inflaton potential shape.

Summary

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- In particular, we have shown that the duration of reheating and the evolution of the radiation energy density, ρ_R , are sensitive to the inflaton potential shape.
- Moreover, we have discussed the role of kinematical suppression in the reheating dynamics. We have demonstrated that the non-zero mass of the Higgs boson leads to the elongation of the reheating period, changes the $\rho_{\mathcal{R}}(a)$ and $\mathcal{T}(a)$ evolution, and conduces to the decrease of \mathcal{T}_{max} .

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- Moreover, we have discussed the role of kinematical suppression in the reheating dynamics. We have demonstrated that the non-zero mass of the Higgs boson leads to the elongation of the reheating period, changes the $\rho_{\mathcal{R}}(a)$ and $\mathcal{T}(a)$ evolution, and conduces to the decrease of \mathcal{T}_{max} .
- Finally, we have pointed out that the DM freeze-in production is very sensitive to the reheating dynamics.

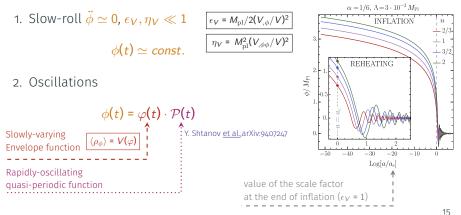
Thank you for your attention!

Back-up slides

The equation of motion (EoM) for the ϕ field is:

 $\ddot{\phi}+3H\dot{\phi}+V_{,\phi}(\phi)=0, \qquad H^2=\rho_\phi/(3M_{\rm Pl}). \label{eq:phi}$

We can distinguish two types of solutions to the ϕ 's EoM:



Analytical solutions to the inflaton EoM after the end of inflation

The EoM for the envelope function
$$\varphi$$
 is given by:
 $\dot{\varphi} = -\frac{3}{n+1}H\varphi, \Rightarrow \varphi(a) = \varphi(a_e) \left(\frac{a}{a_e}\right)^{-\frac{3}{n+1}},$

while \mathcal{P} satisfies the following approximate equation: M. A. G. Garcia <u>et al.</u> arXiv:2004.08404 M. A. G. Garcia <u>et al.</u> arXiv:2012.10756

$$\dot{\mathcal{P}}\simeq\pm\sqrt{rac{m_{\phi}^2(1-|\mathcal{P}|^{2n})}{n(2n-1)}}$$

$$r_{\phi}^{2} = 2n(2n-1)\Lambda^{2}\left(\frac{\Lambda}{\sqrt{6\alpha}M}\right)$$

 $\frac{1}{\Lambda_{\rm Pl}}\right)^2 \left(\frac{\rho_{\phi}}{\Lambda^4}\right)^{\frac{n-1}{n}} \cdots$

The solution to the above equation can be written as

Inverse of the regularized incomplete beta function $\mathcal{P}(t) = \left[I_z^{-1}\left(\frac{1}{2n}, \frac{1}{2}\right)\right]^{\frac{1}{2n}}, \quad z = 1 - \frac{4}{T}(t - t_0),$

where *T* denotes the period of the oscillations:

$$T = \frac{\sqrt{16\pi n(2n-1)}}{m_{\phi}} \frac{\Gamma\left(1 + \frac{1}{2n}\right)}{\Gamma\left(\frac{1}{2} + \frac{1}{2n}\right)}.$$
depend on time for $n \neq 1$

Particles production in a classical inflaton background

The inflaton field can be regarded as a homogeneous, classical field that coherently oscillates in time.

For the interactions linear in $\phi = \varphi \cdot \mathcal{P}$, the energy gain per unit volume per unit time due to the pair production of f particles with mass m can be calculated as

$$\frac{1}{V}\frac{dE_g}{dt} = \frac{\varphi^2(t)}{8\pi\,\delta_f} \sum_{k=1}^{\infty} k\omega |\mathcal{P}_k|^2 \left|\mathcal{M}_{0\to f}(k)\right|^2 \mathrm{Re}\left[\sqrt{1-\frac{4m^2}{k^2\omega^2}}\right],$$

where

$$\mathcal{P}(t) = \sum_{k=-\infty}^{\infty} \mathcal{P}_k e^{-ik\omega t}, \qquad \mathcal{P}_k = \frac{1}{\mathcal{T}(t_0)} \int_{t_0}^{t_0 + \mathcal{T}(t_0)} dt \, \mathcal{P}(t) e^{ik\omega t}.$$

The matrix element $\mathcal{M}_{0\to f}$ accounts for the quantum process of two particles production out of the vacuum.

Particles production in a classical inflaton background

For the interactions proportional to the $\phi = \varphi \cdot \mathcal{P}$ term, the lowest-order non-vanishing S-matrix element takes the form

$$S_{if}^{(1)} = \sum_{k} \mathcal{P}_{k} \langle f | \int d^{4} x \varphi(t) e^{-ik\omega t} \mathcal{L}_{int}(x) | i \rangle$$

where

$$\ket{i} \equiv \ket{0}, \qquad \qquad \ket{f} \equiv \hat{a}_{f}^{\dagger} \hat{a}_{f}^{\dagger} \ket{0}.$$

If the envelope $\varphi(t)$ varies on the time-scale much longer than the time-scale relevant for processes of particle creation, the S-matrix element can be written as

$$S_{if}^{(1)} = i\varphi(t)\sum_{k} \mathcal{P}_{k}\mathcal{M}_{0\to f}(k) \times (2\pi)^{4}\delta(k\omega - 2E_{f})\delta^{3}(p_{f_{1}} + p_{f_{2}}).$$