



SCUOLA
NORMALE
SUPERIORE



EW WIMPs at future lepton colliders

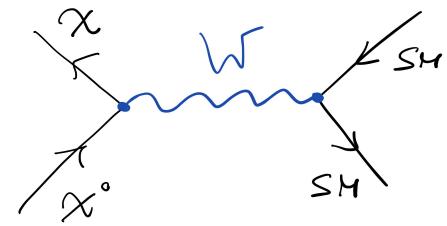
Marco Costa
(Scuola Normale Superiore, INFN Pisa)

based on 2107.09688, 2205.04486

In collaboration with S. Bottaro, D. Buttazzo, R. Franceschini, P.
Panci, D. Redigolo, and L. Vittorio

Which WIMP?

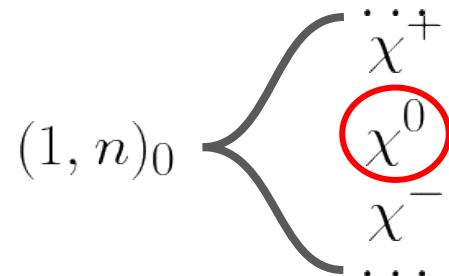
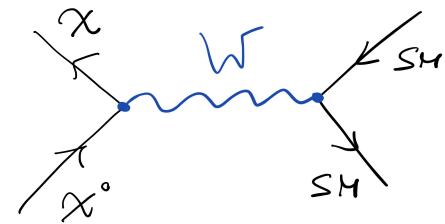
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$$T_3 + Y = 0$$

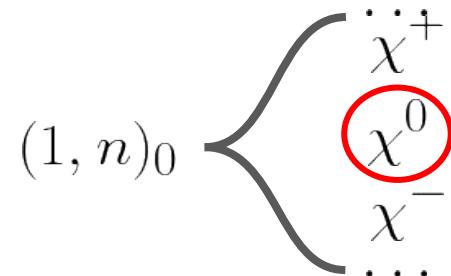
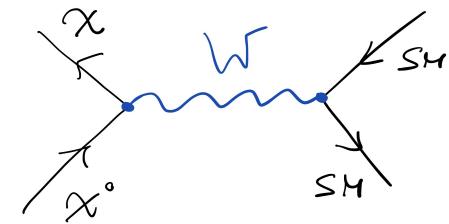


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 - odd n: **Y=0 (real)**
 - even n, **Y=½ , 1** : needs UV physics (mixing partner)

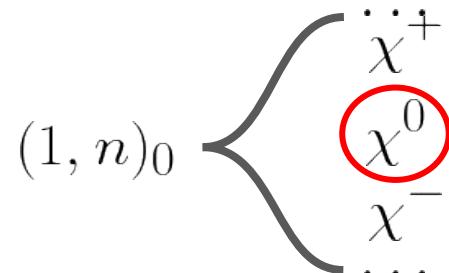
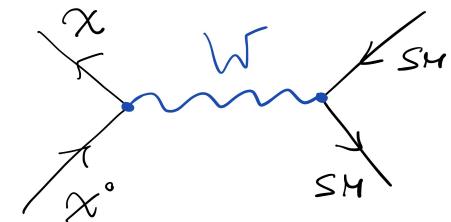


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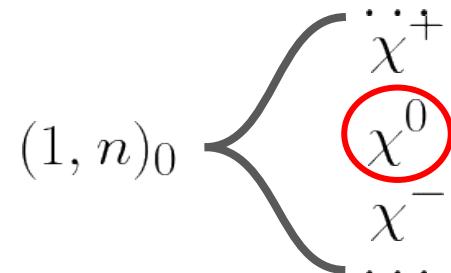
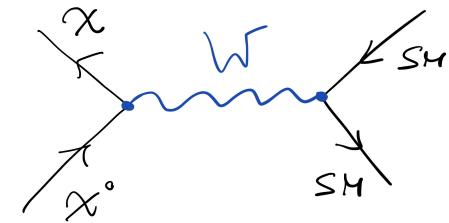


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- **Computability**: (perturbative unitarity) $\Rightarrow \mathbf{n \leq 13}$



Thermal target results

DM spin	EW n-plet	M_χ (TeV)
Real scalar $Y = 0$	3	2.53 ± 0.01
	5	15.4 ± 0.7
	7	54.2 ± 3.1
	9	117.8 ± 15.4
	11	199 ± 42
	13	338 ± 102
Majorana fermion $Y = 0$	3	2.86 ± 0.01
	5	13.6 ± 0.8
	7	48.8 ± 3.3
	9	113 ± 15
	11	202 ± 43
	13	324.6 ± 94

30-ish TeV
collider might
probe them

DM spin	n_Y	M_{DM} (TeV)
Dirac fermion	$2_{1/2}$	1.08 ± 0.02
	3_1	2.85 ± 0.14
	$4_{1/2}$	4.8 ± 0.3
	5_1	9.9 ± 0.7
	$6_{1/2}$	31.8 ± 5.2
	$8_{1/2}$	82 ± 8
Complex scalar	$10_{1/2}$	158 ± 12
	$12_{1/2}$	253 ± 20
	$2_{1/2}$	0.58 ± 0.01
	3_1	2.1 ± 0.1
	$4_{1/2}$	4.98 ± 0.25
	5_1	11.5 ± 0.8
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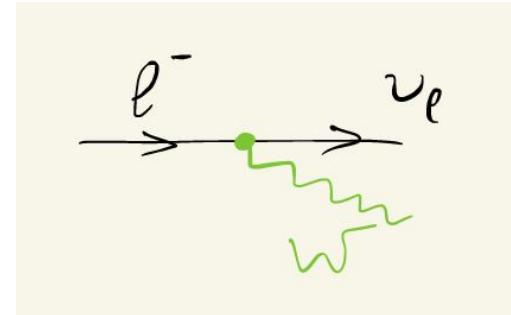
Need > 60
TeV
collider!

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WIMPs @ high energy lepton colliders

Why high energy lepton colliders?

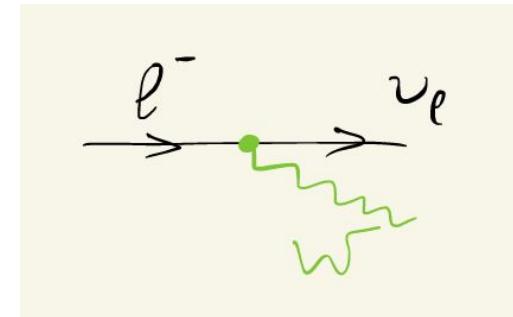
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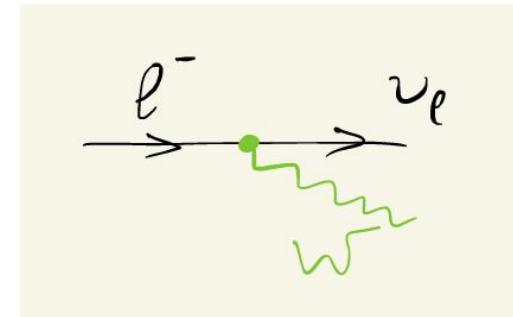
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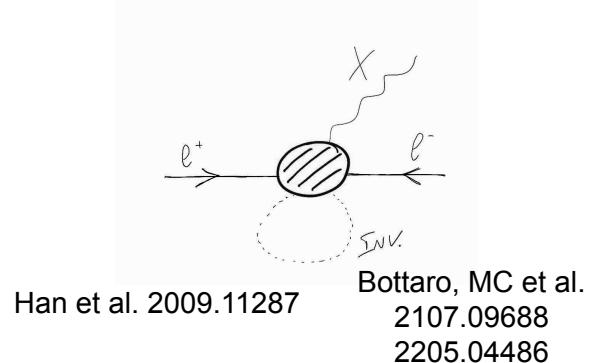
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- **Clean environment**: full event reconstruction
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- **More energy in hard cross section**: needed since WIMPs are heavy



How to detect WIMPs @ Muon Collider?

- **Recoils** against invisible objects: **Mono-X,Di-X**
(mono γ , monoW, monoZ, Di γ , DiW, mono μ , Di μ)

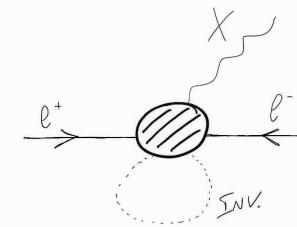


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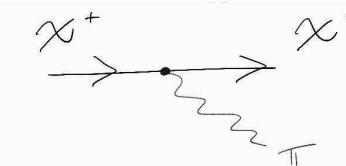
Han et al. 2009.11287



Bottaro, MC et al.
2107.09688
2205.04486

- **Tracks**: (1 or 2 “stub” tracks, “long” tracks)

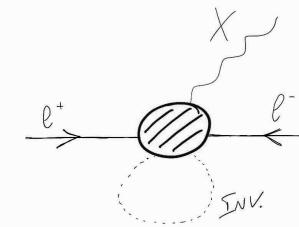
Recast of Capdevilla et al.
2102.11292



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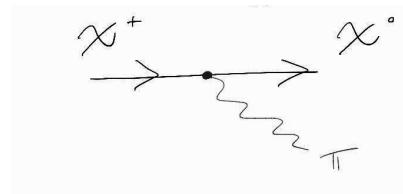


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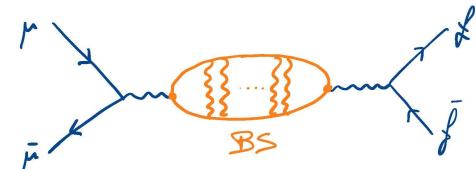
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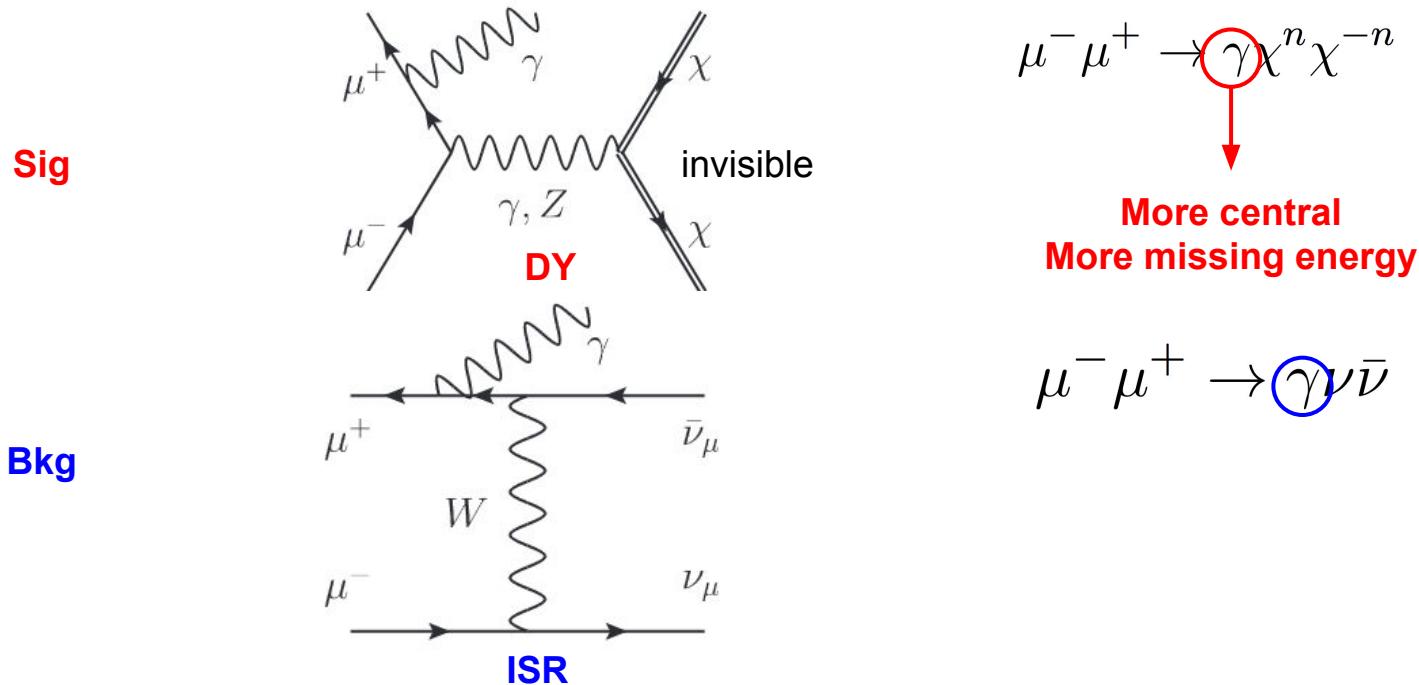


- **Resonances: Bound States**

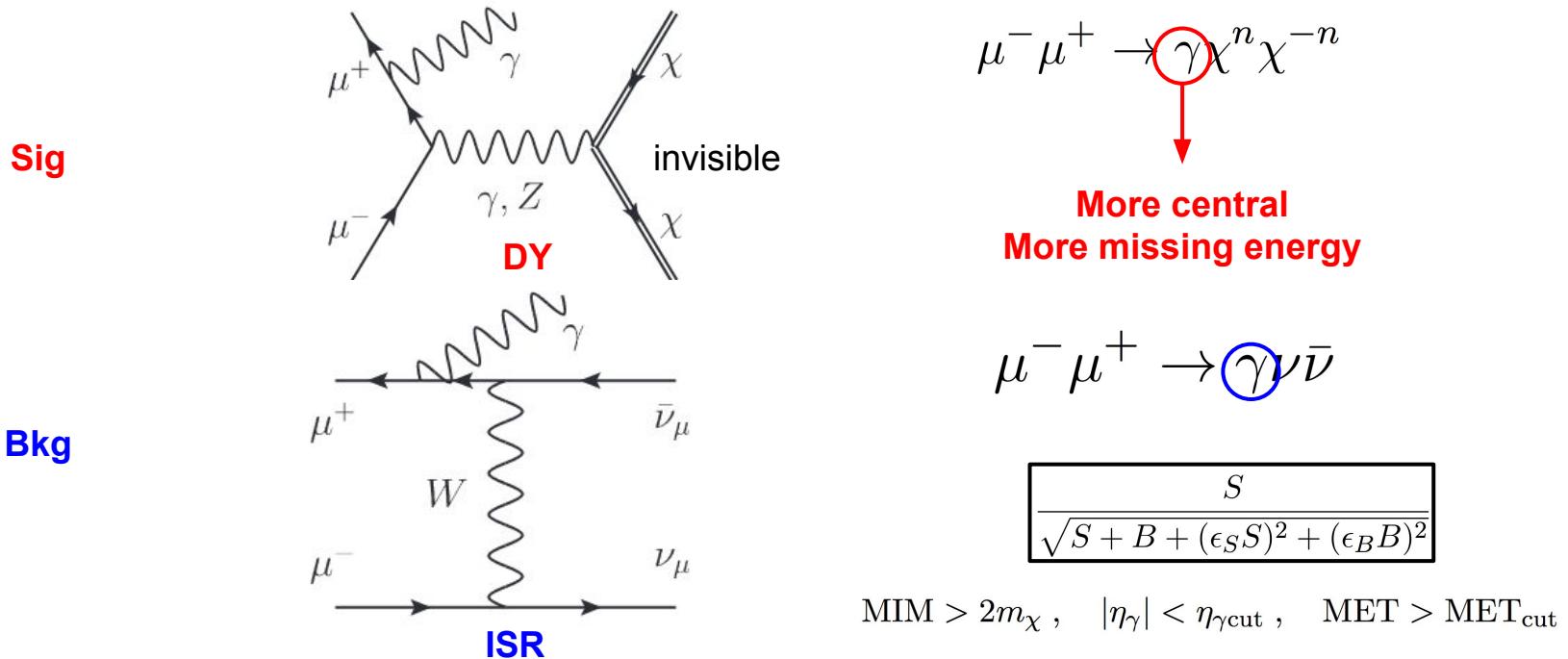
Bottaro et al. 2103.12766



Missing Mass search example: mono- γ

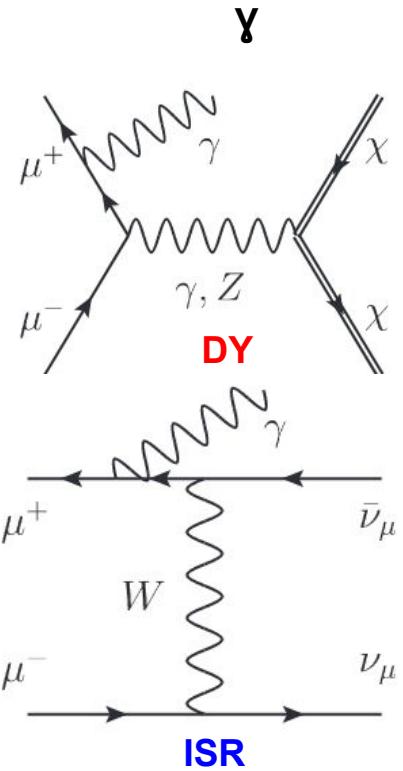


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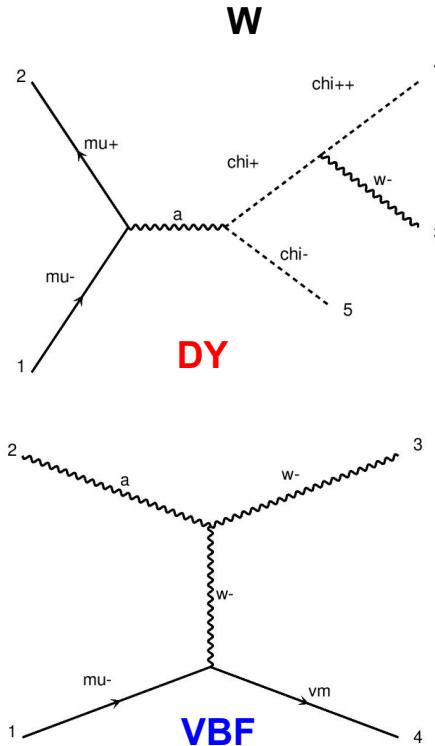


Mono-V

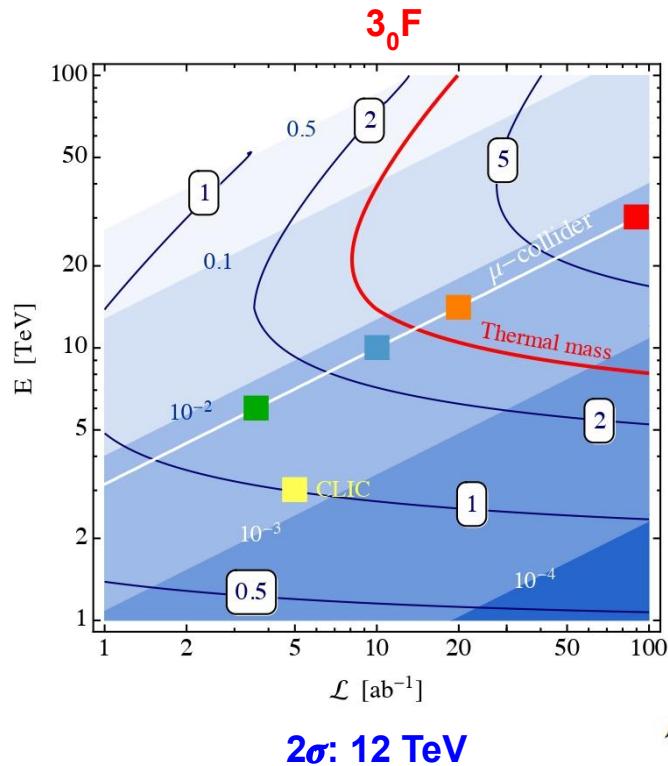
Sig



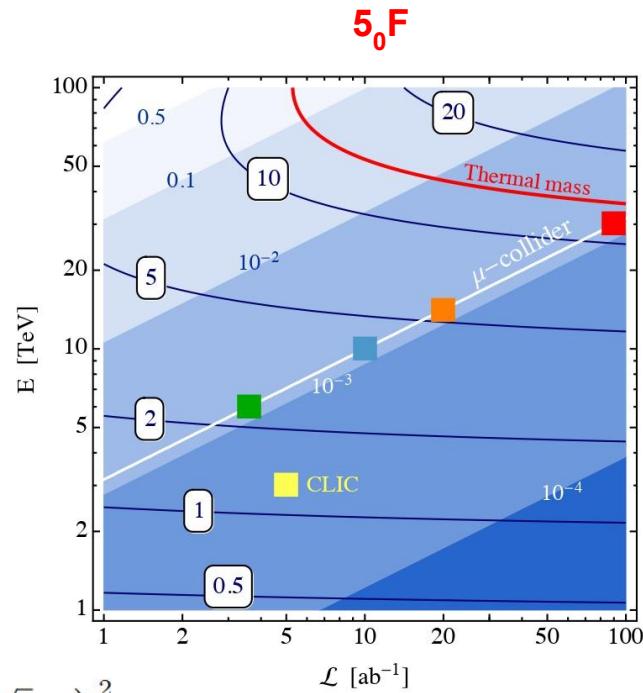
Bkg



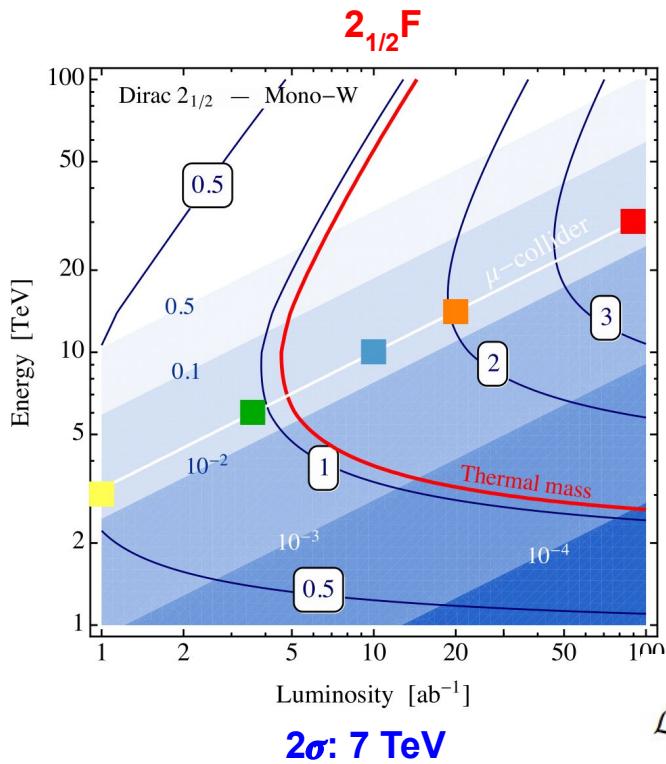
Lumi vs Energy (Mono-W)



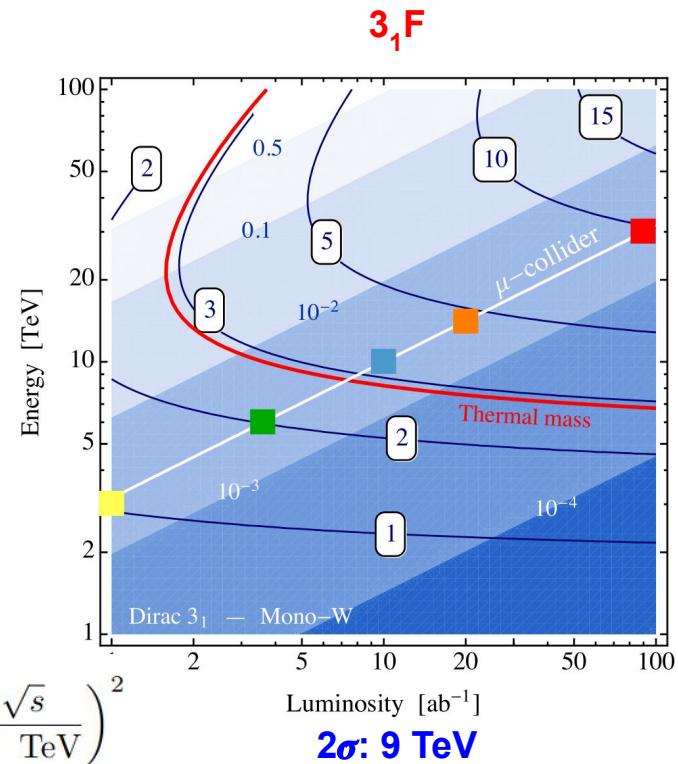
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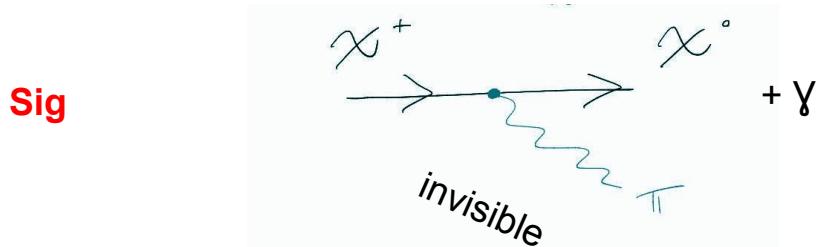
$\epsilon=0\%$



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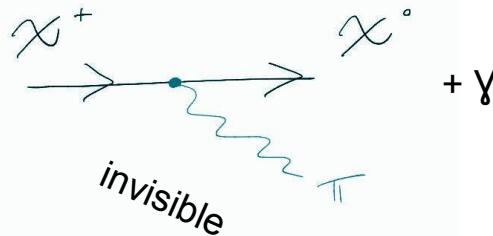
Bkg BIB hits reconstructed as tracks + γ

Disappearing condition:
decay between 5 cm and 12.7 cm

Tracks

1 or 2 Disappearing (“stub”)

Sig



Charged (“long”)



Bkg

BIB hits reconstructed as tracks + γ

??

Disappearing condition:
decay between 5 cm and 12.7 cm

Long Track condition:
decay after 1m

Understanding Lifetimes

$$\Gamma_{\pi^\pm} = g(n, Y, \pm 1) \frac{G_F^2 f_\pi^2 |V_{ud}|^2 \delta m_\pm^3}{4\pi} \sqrt{1 - \frac{m_\pi^2}{\delta m_\pm^2}}$$

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gauge

$$\Delta M_Q^{\text{EW}} = \delta_g \left(Q^2 + \frac{2YQ}{\cos \theta_W} \right)$$

$$\delta_g = \alpha_2 M_W \sin^2 \frac{\theta_W}{2} \approx 167 \text{ MeV}$$



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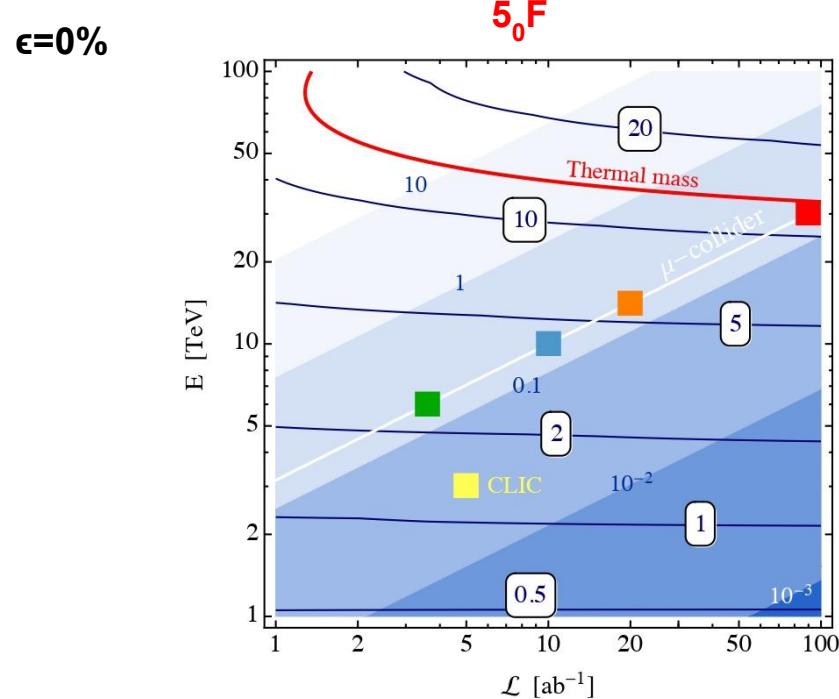
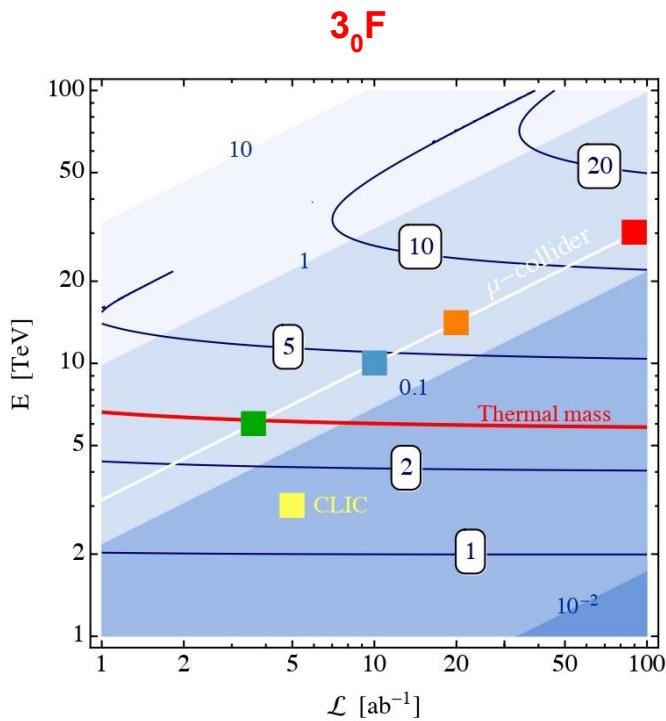
$$\mathcal{O}_+ = -\bar{\chi} T^a \chi H^\dagger \frac{\sigma^a}{2} H$$

Vanishes for real candidates

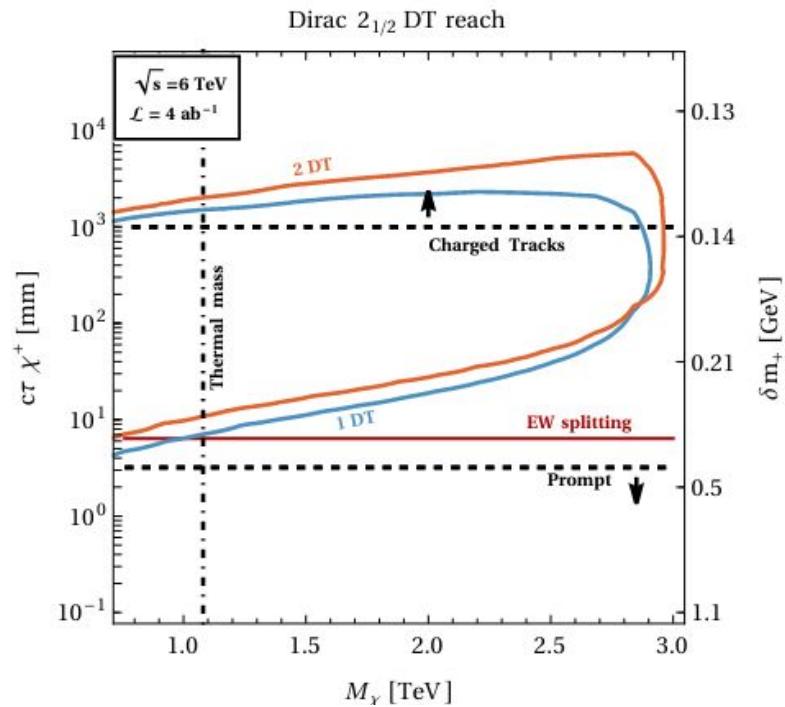
$$c\tau_{\chi^+} \simeq \frac{120 \text{ mm}}{T(T+1)}$$

6 cm n=3
2 cm n=5

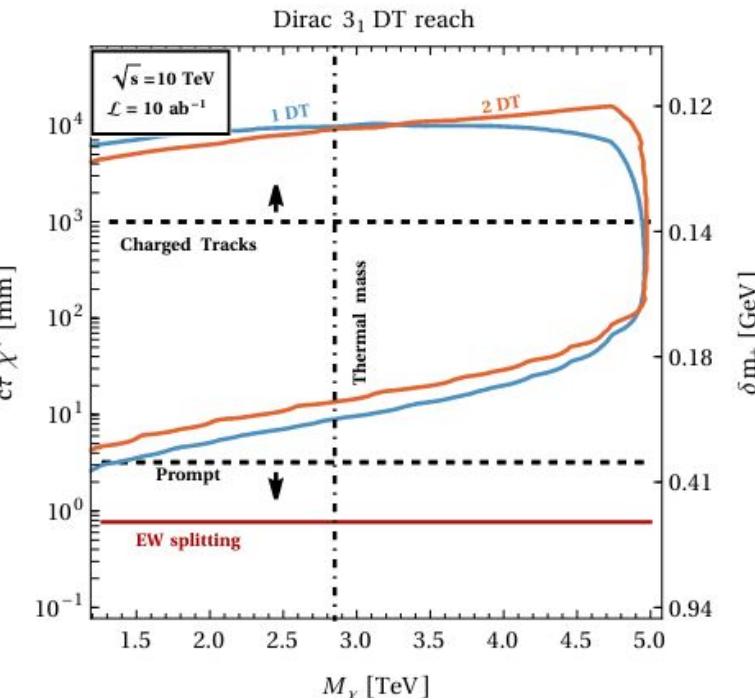
DT Real WIMPs



Complex DT: $2_{1/2}, 3_1$

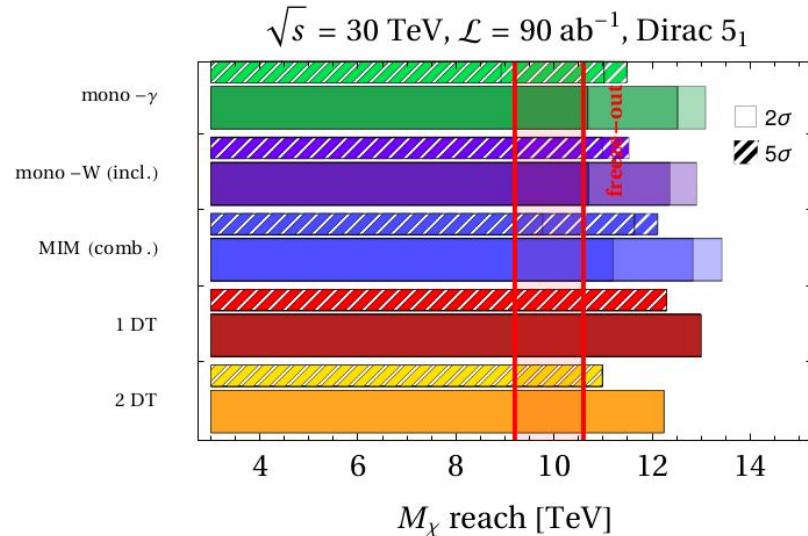
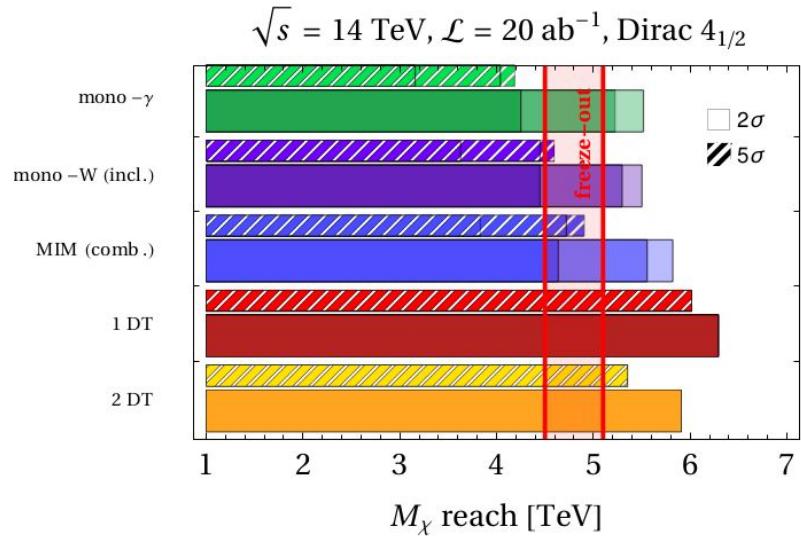


(neglecting δm_0)



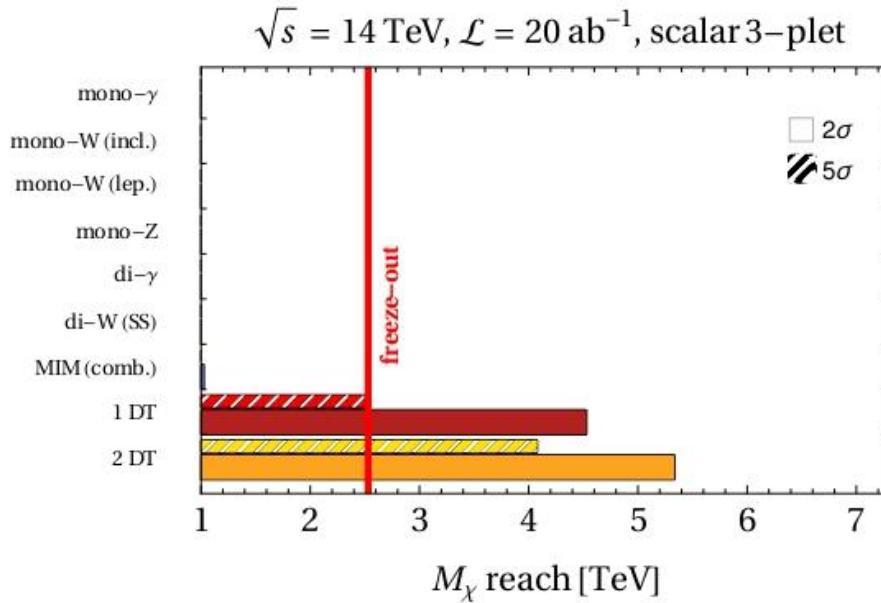
Complex WIMPs: $4_{1/2}, 5_1$

$\epsilon = 0\%, 0.1\%, 1\%$

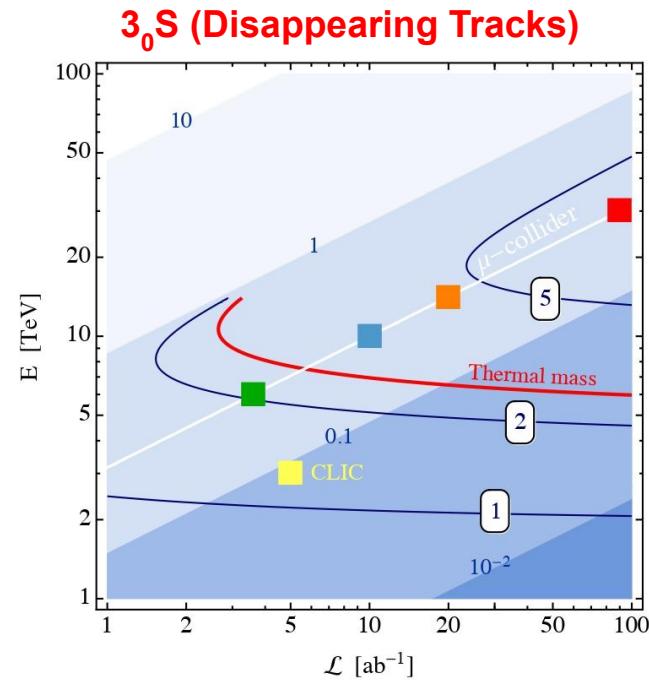


MIM: $4_{1/2}$ @ \square 12 TeV, 5_1 needs < 30 TeV. DT (EW) as good

Scalar Real WIMPs

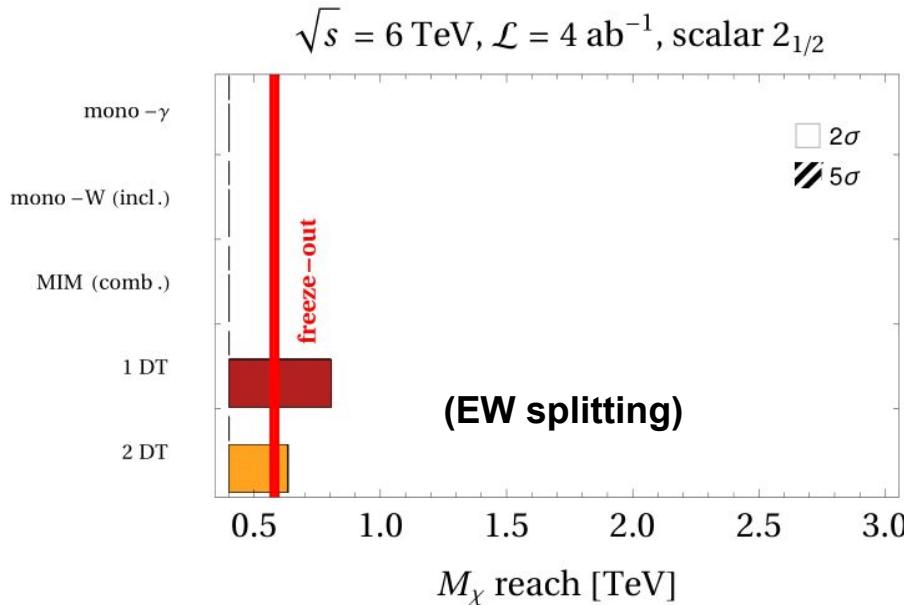


3S: DTs only hope

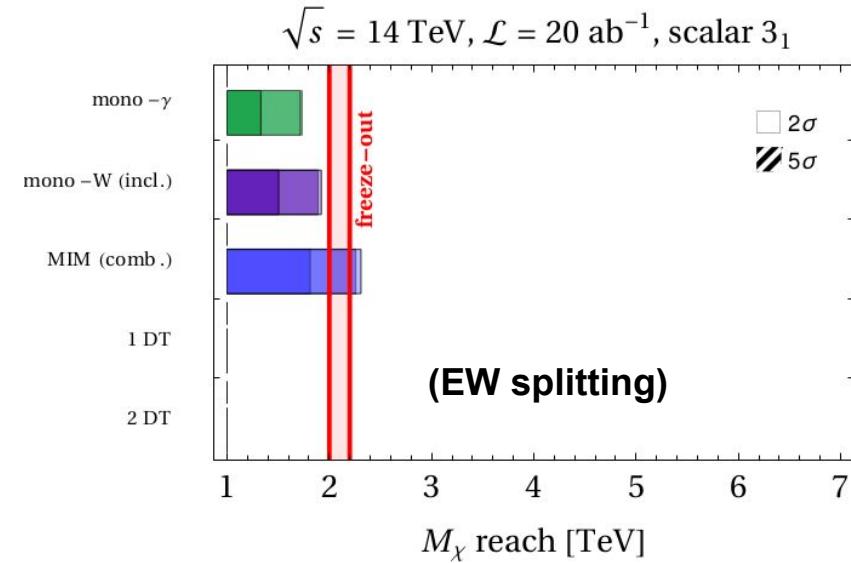


2 σ : 8 TeV

Scalar Complex WIMPs



$2_{1/2}\text{S}$: DT only hope, 6 TeV (but MODEL DEPENDENT)



3_1S : MIM 2σ 14 TeV
 $4_{1/2}\text{S}$: MIM 2σ 30 TeV, DT 14 TeV

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- Only **$2_{1/2}, 4_{1/2}, 3_0, 5_{0,1}$ (F,S)** kinematically allowed if $\sqrt{s} < 30$ TeV
- mono-X 2σ : **$2_{1/2}F$ 6 TeV, 3_0F 12 TeV, 3_1F 8 TeV, $4_{1/2}F$ 12 TeV, 3_1S 14 TeV**
- **DT**: robust for reals. **3_0F 2σ @ 6 TeV, 3_0S @ 8 TeV** (only chance)
- **DT**: model dependent for complex. Best channel for **$2_{1/2}S$: 2σ @ 6 TeV** (EW)

Conclusions

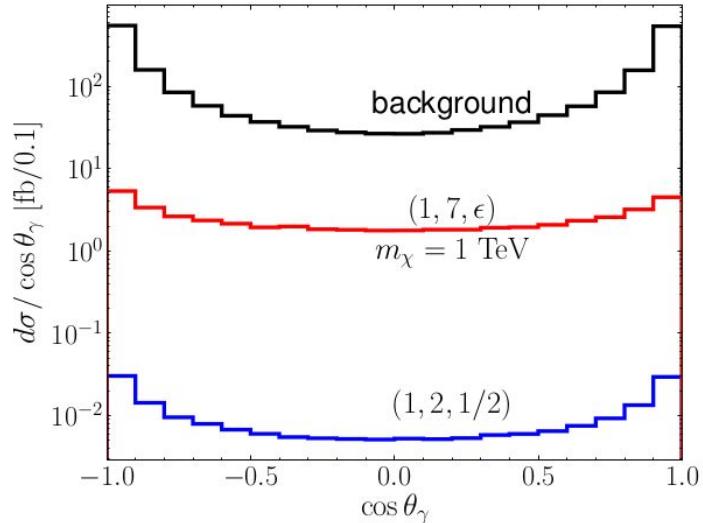
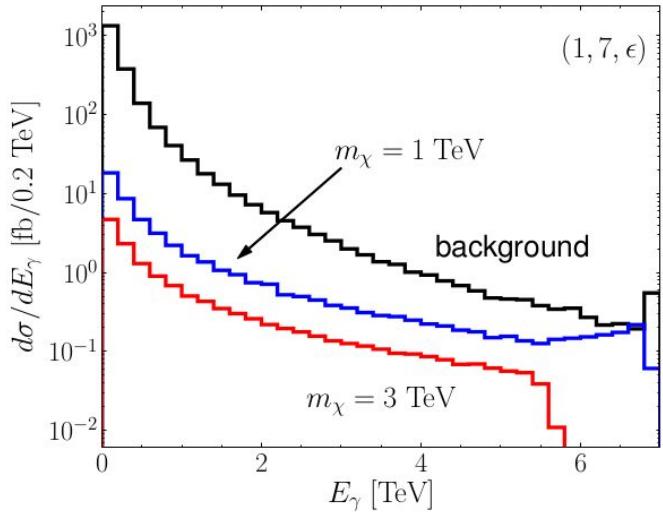
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- **DT**: model dependent for complex. Best channel for **$2_{1/2}S$: 2σ @ 6 TeV** (EW)
- **Other**: **30 TeV** or more

Thanks for the attention!

Backup

Missing Mass search example: mono- γ

Han et al.2009.11287



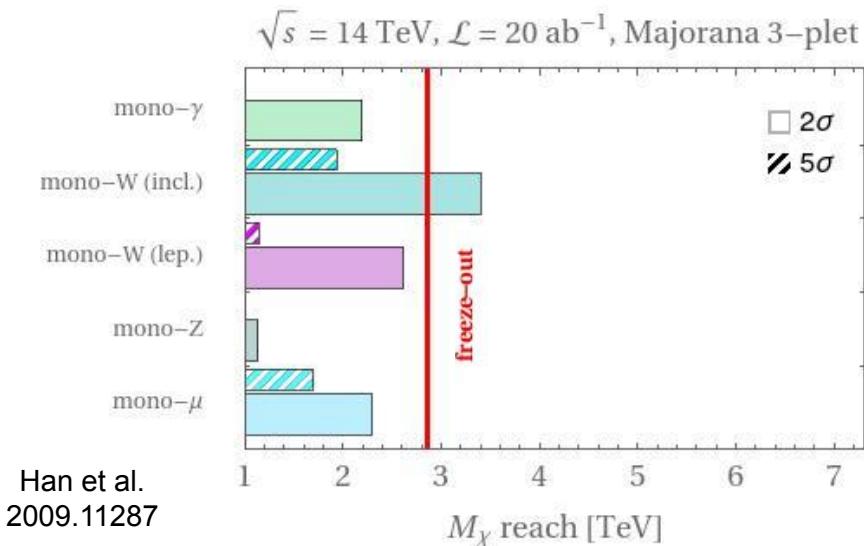
S/B<0.1% LOW!

$$\text{MIM} > 2m_\chi, \quad |\eta_\gamma| < \eta_{\gamma\text{cut}}, \quad \text{MET} > \text{MET}_{\text{cut}}$$

$$\frac{S}{\sqrt{S + B + (\epsilon_S S)^2 + (\epsilon_B B)^2}}$$

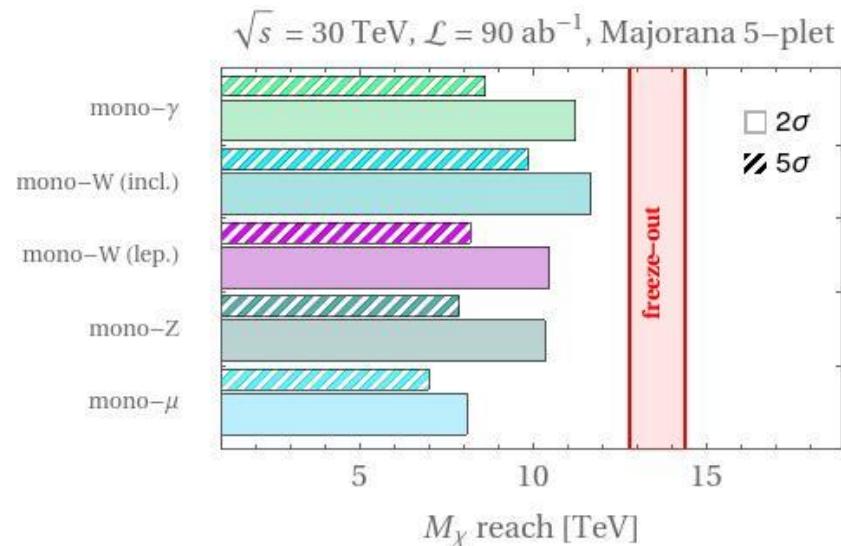
Mono-X

Bottaro, MC et al. 2107.09688

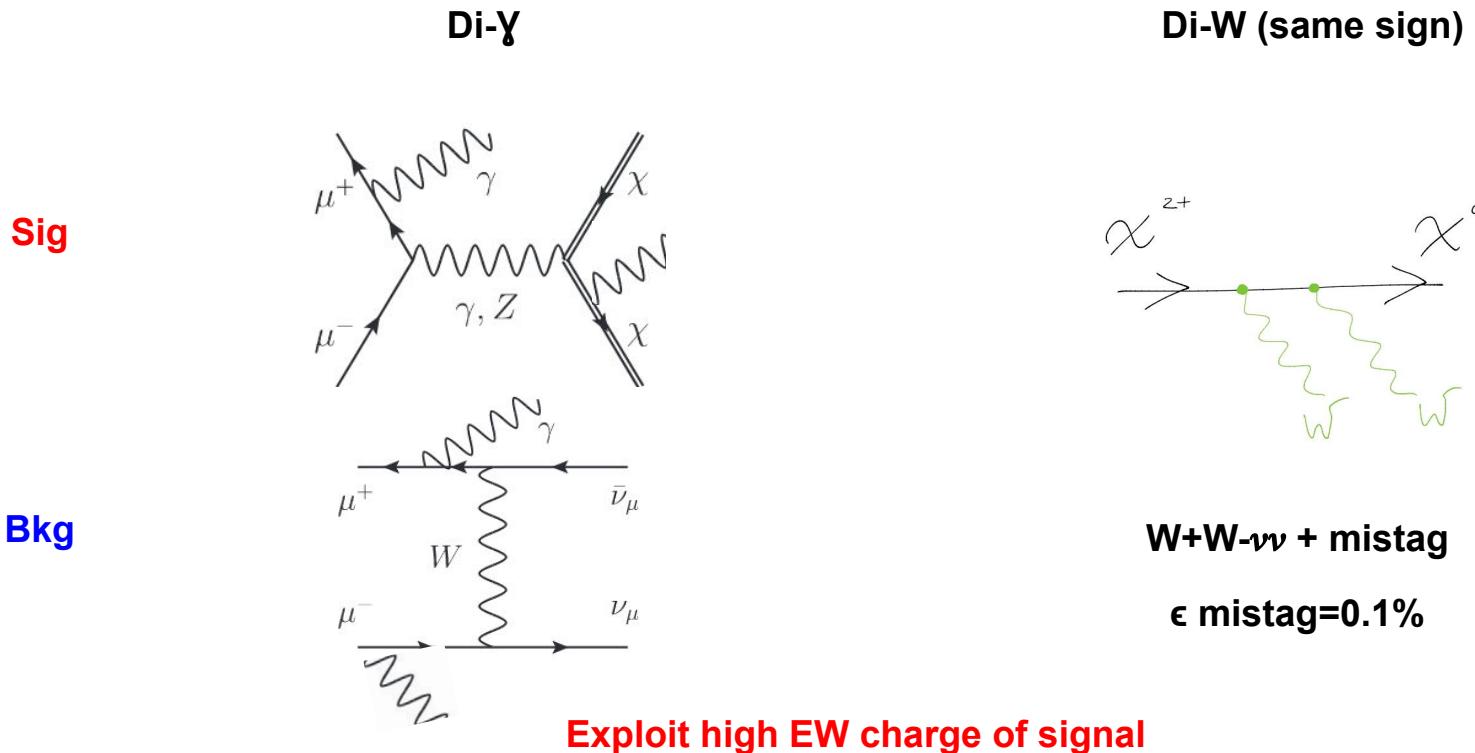


Han et al.
2009.11287

$\epsilon=0\%$

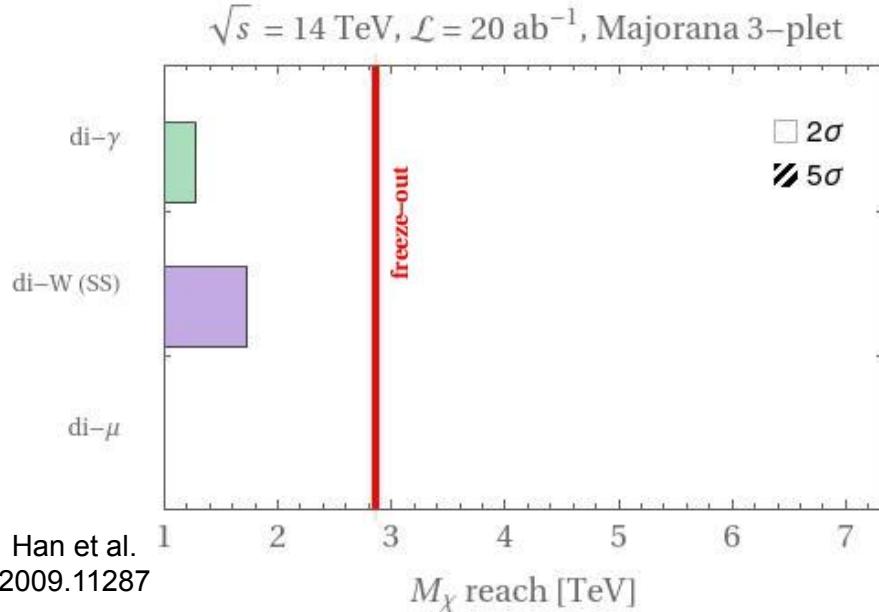


Di-V

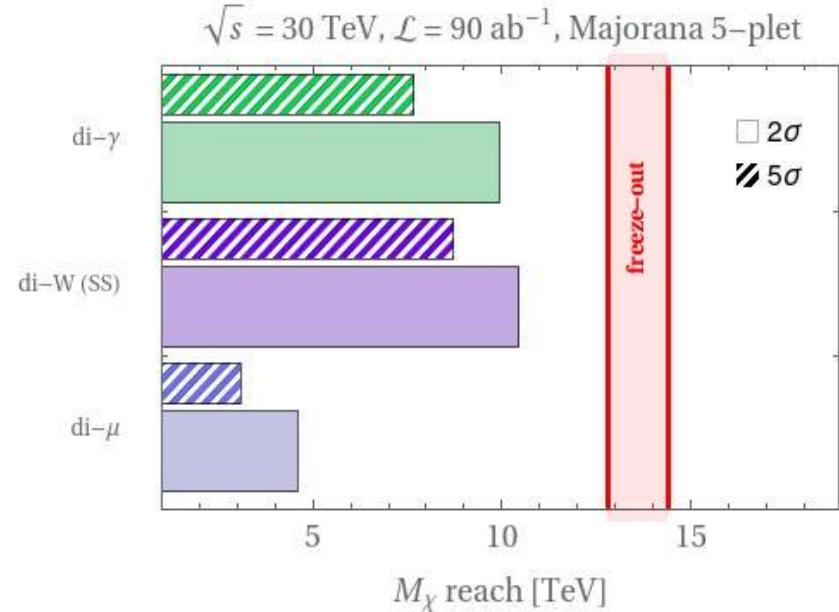


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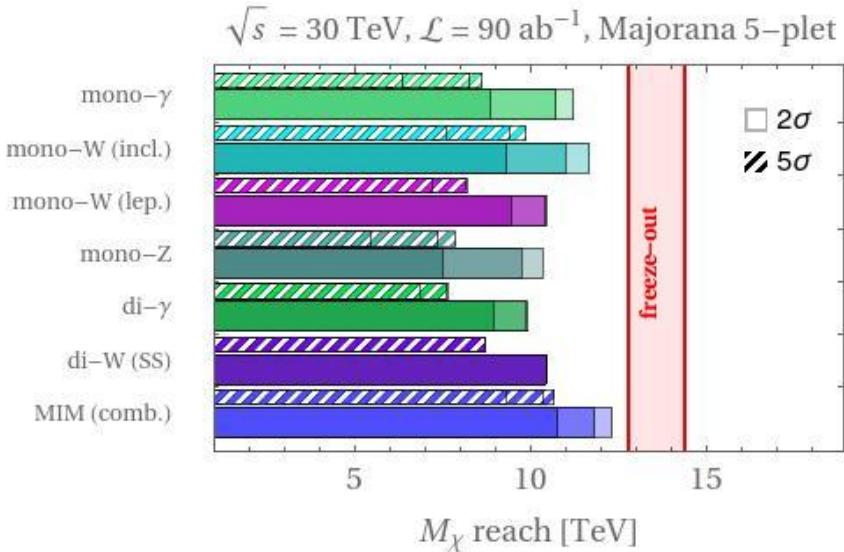
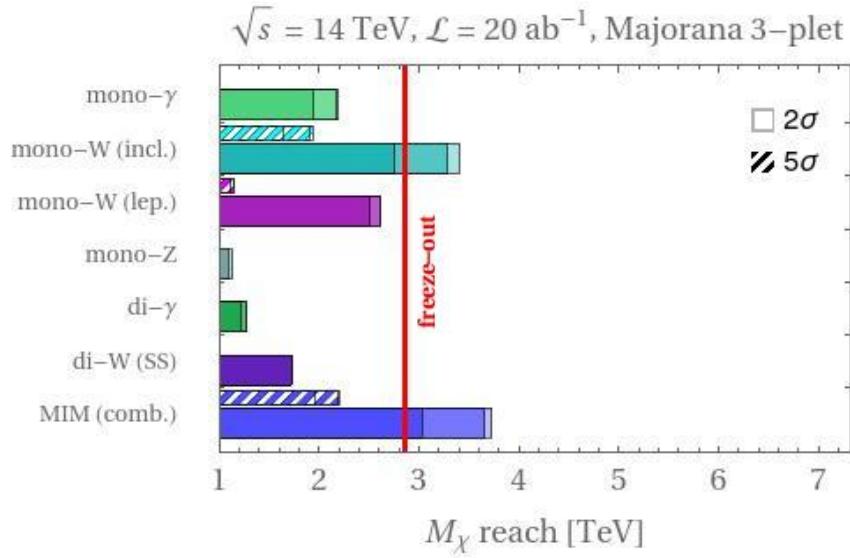


$\epsilon=0\%$



Mono-X & Di-X Real results

$\epsilon = 0\%, 0.1\%, 1\%$



Mono-X: Mono-W best; S/B<0.1%: need strong pT cuts (E/4-ish)

Di-X: Good for 5; S/B up to 1; robust to ϵ

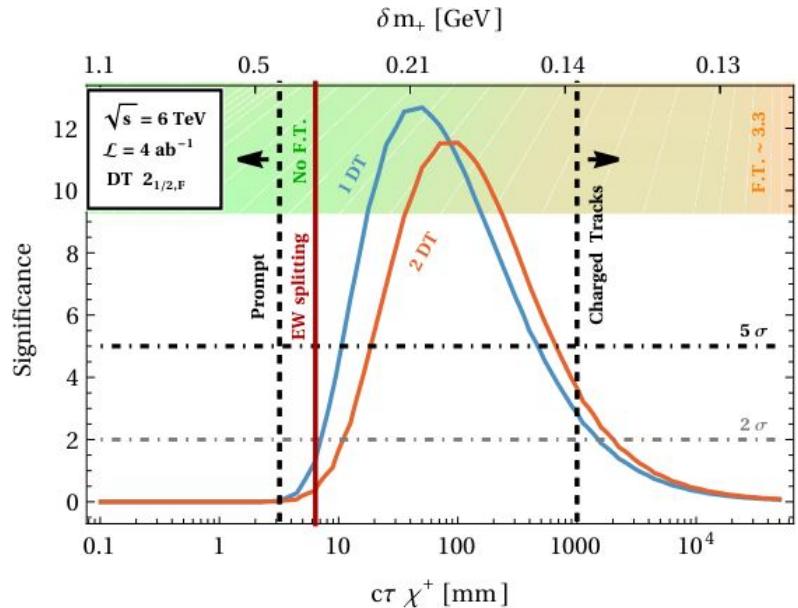
DT recast

$$P(\theta, r_{\min}, r_{\max}) = \int_{r_{\min}}^{r_{\max}} \frac{dr}{c\tau\beta\gamma \sin\theta} \epsilon_{\text{rec}}(r, \theta) e^{-r/(c\tau\beta\gamma \sin\theta)},$$

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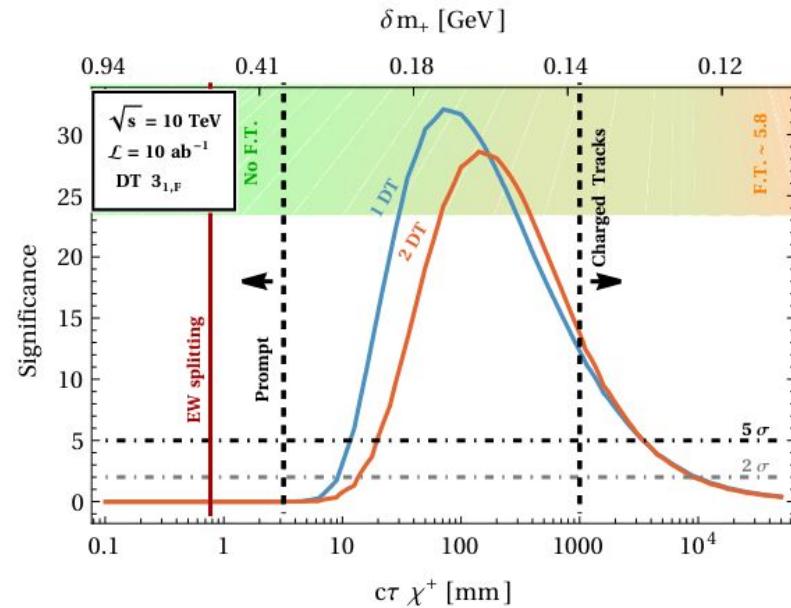
Requirement / Region	SR _{1t} ^γ	SR _{2t} ^γ
Veto	leptons and jets	
Leading tracklet p_T [GeV]	> 300	> 20
Leading tracklet θ [rad]	[2/9π, 7/9π]	
Subleading tracklet p_T [GeV]	-	> 10
Tracklet pair Δz [mm]	-	< 0.1
Photon energy [GeV]	> 25	> 25

DT Complex WIMPs



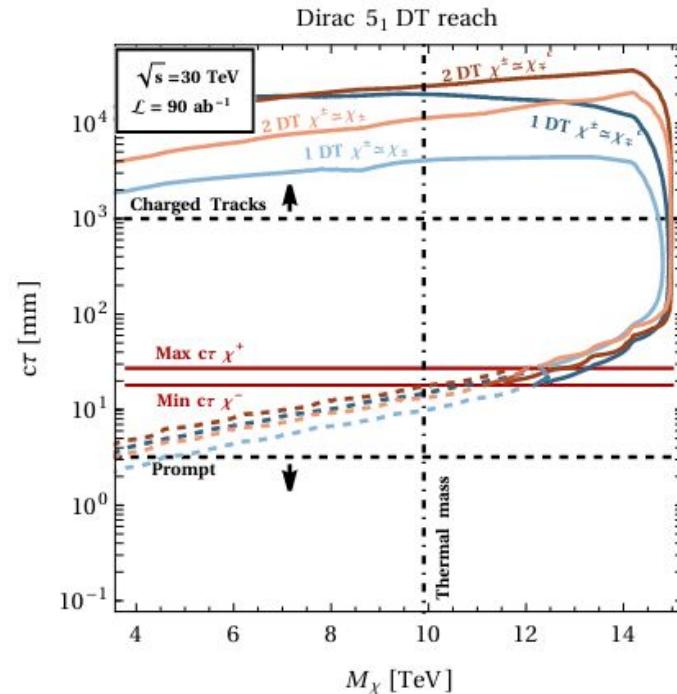
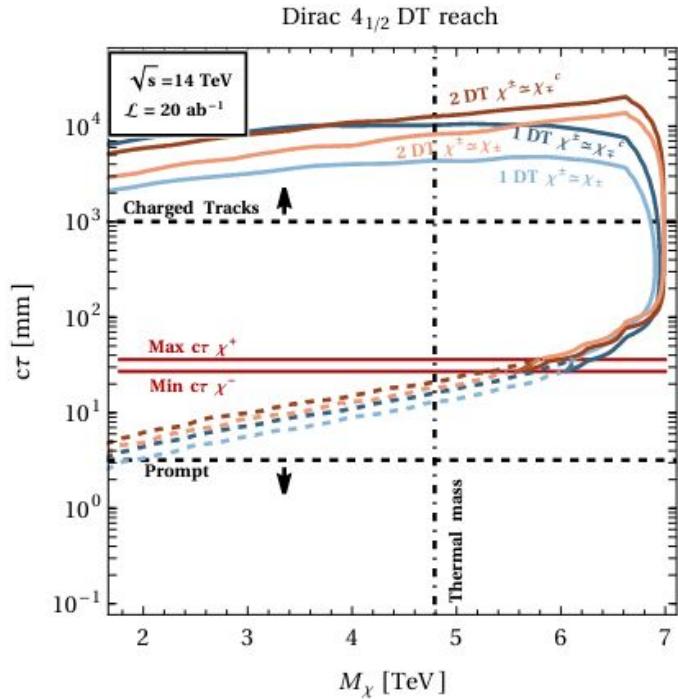
**2 σ : 6 TeV probe
EW splitting**

(neglecting δm_0)



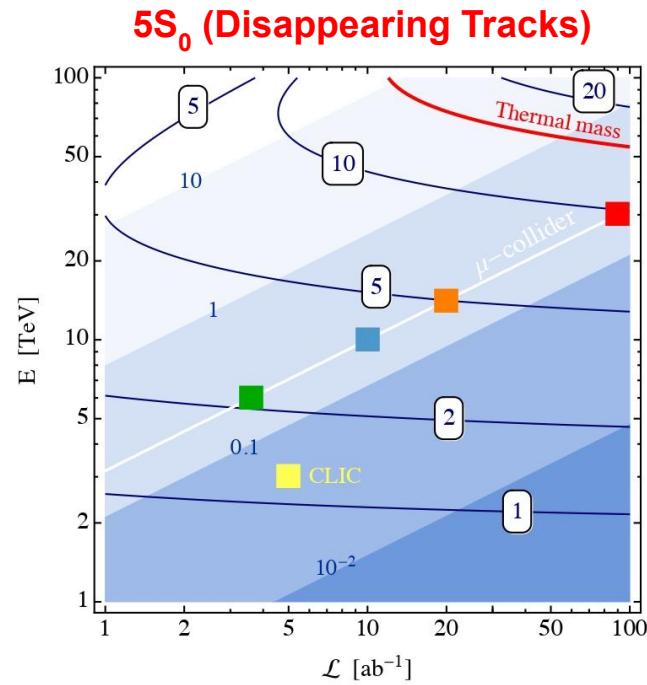
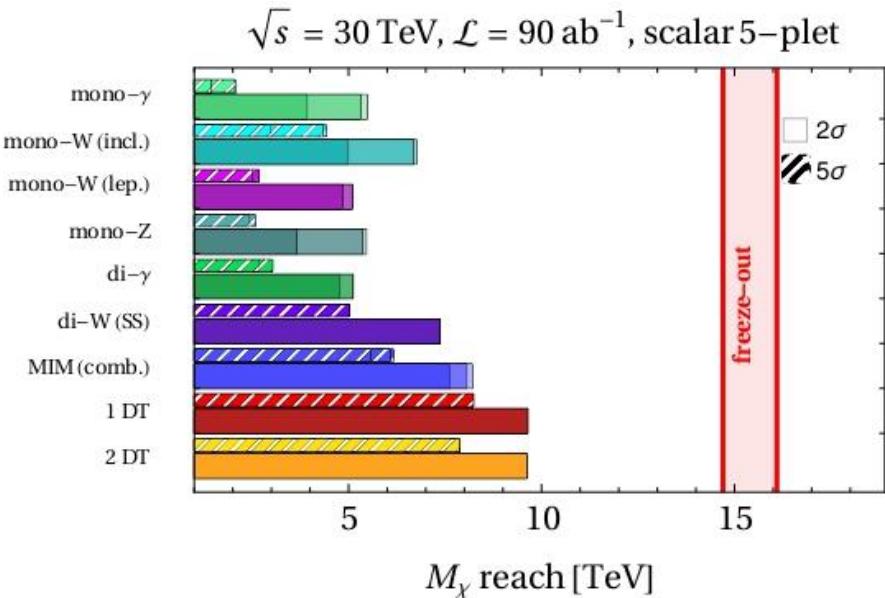
**EW splitting
TOO PROMPT**

Complex DT full reach



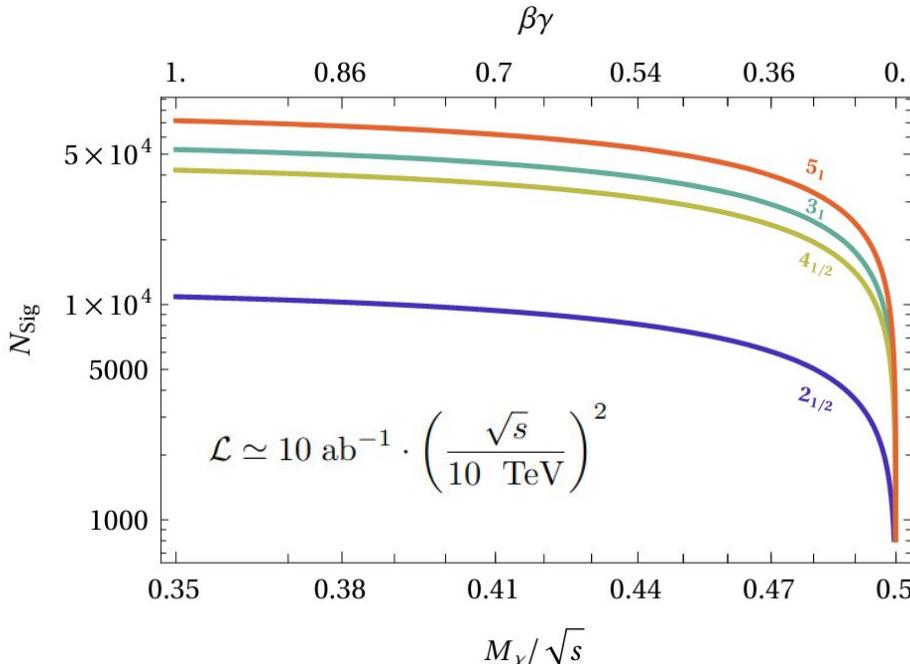
2 charged particles: long lived (solid), short lived (dashed)

5₀S



2σ: hopeless

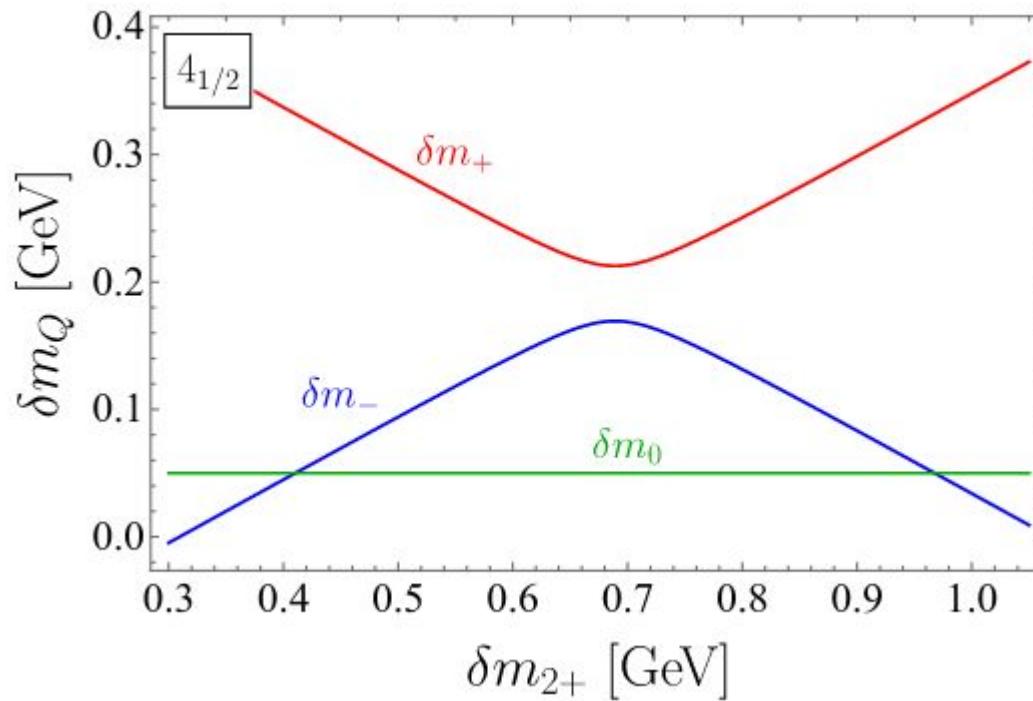
Charged Tracks



$$\mu^- \mu^+ \rightarrow \chi^n \chi^{-n}$$

- **Signal:** energy deposition
- Energy loss β dependent
- Need careful bkg estimation
- Longest lived charged particle depends on spectrum, which depends also on neutral splitting

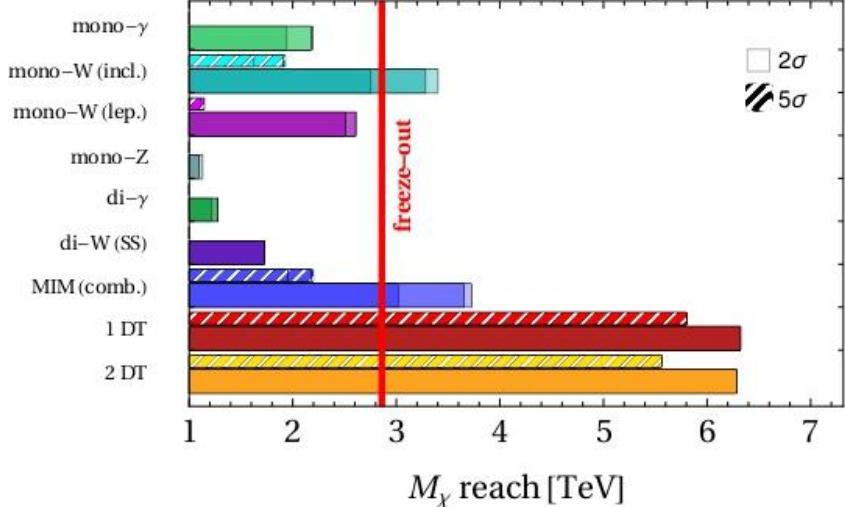
Mixing: $4_{1/2}, 5_1$



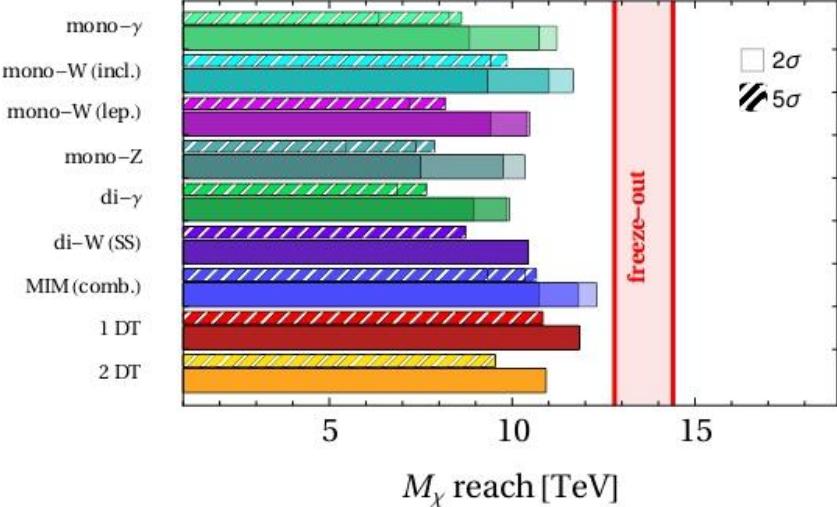
Results: Real WIMPs

$\epsilon = 0\%, 0.1\%, 1\%$

$\sqrt{s} = 14 \text{ TeV}, \mathcal{L} = 20 \text{ ab}^{-1}$, Majorana3-plet



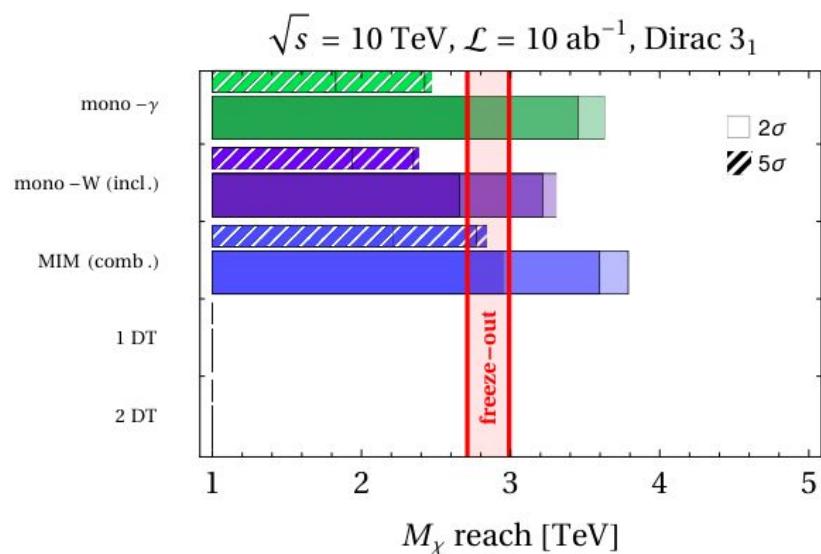
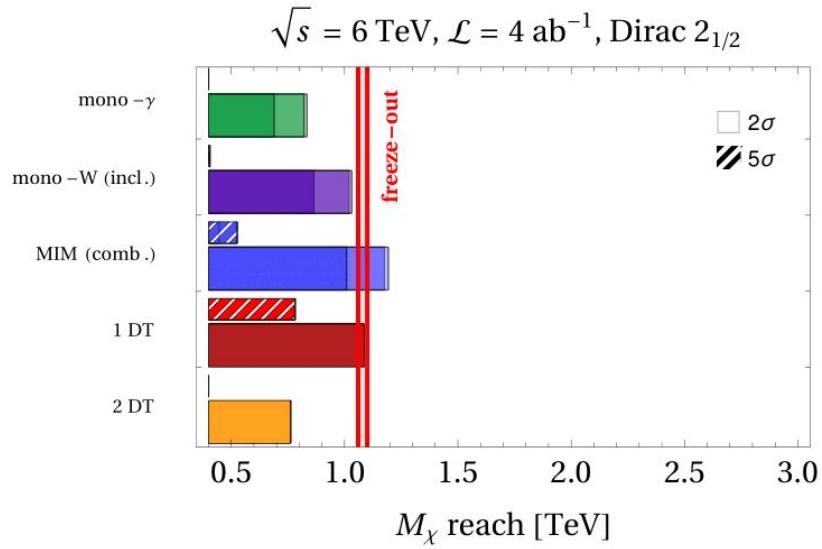
$\sqrt{s} = 30 \text{ TeV}, \mathcal{L} = 90 \text{ ab}^{-1}$, Majorana5-plet



1DT: Good for 3_0 ; For 5_0 comparable to MIM

Complex WIMPs: $2_{1/2}$, 3_1

$\epsilon = 0\%, 0.1\%, 1\%$



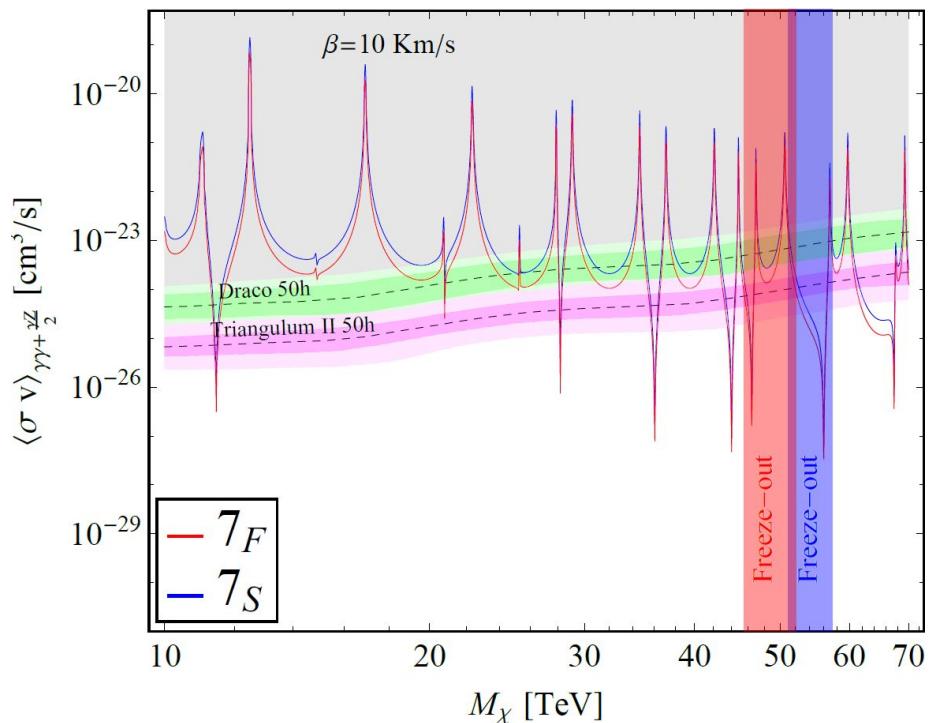
$2_{1/2}$: @6 TeV with MIM and DT (EW)

3_1 : 10 TeV only MIM more than enough

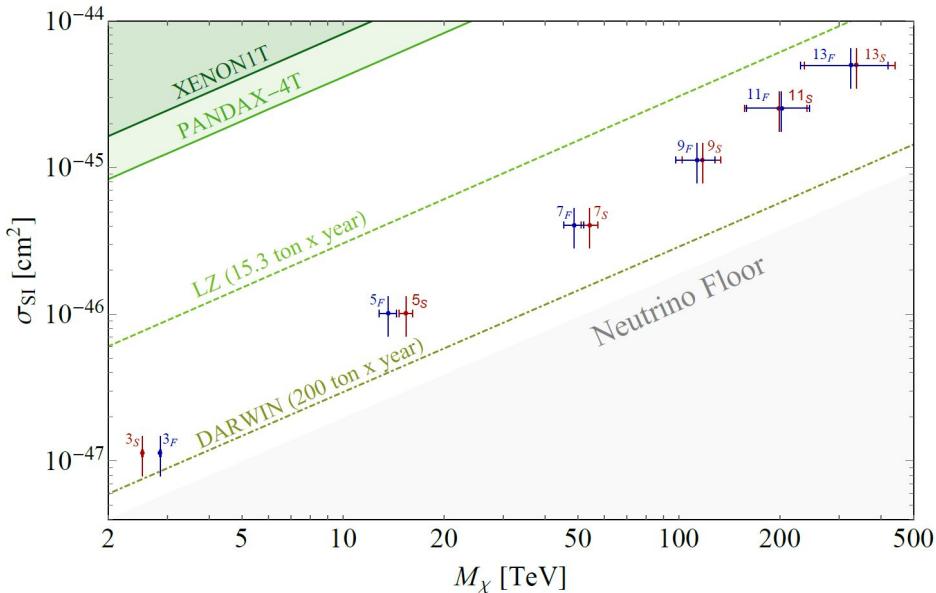
Cuts (Reals)

		Majorana 3-plet						Majorana 5-plet					
		\sqrt{s}	ϵ_{sys}	η_X^{cut}	$p_{T,X}^{\text{cut}}$ [TeV]	$S_{95\%}$	$S_{95\%}/B$	$M_{95\%}$ [TeV]	η_X^{cut}	$p_{T,X}^{\text{cut}}$ [TeV]	$S_{95\%}$	$S_{95\%}/B$	$M_{95\%}$ [TeV]
Mono- γ	3 TeV	0	2.4	0.18	1007	0.004	0.72	2.4	0.0	3038	0.001	1.4	
		1%	2.2	0.24	746	0.006	0.67	1.2	0.0	3683	0.003	1.3	
		1%	1.2	0.78	107	0.05	0.58	0.6	0.3	639	0.02	1.1	
	14 TeV	0	1.6	2.5	360	0.01	2.2	2.2	0.28	3693	0.001	5.5	
		1%	1.6	2.8	323	0.01	2.2	1.2	0.84	1300	0.004	5.2	
		1%	1.0	4.5	108	0.05	1.9	0.8	2.8	331	0.03	4.4	
	30 TeV	0	1.2	7.8	174	0.02	4.4	1.6	1.8	1795	0.002	11	
		1%	1.2	7.8	175	0.02	4.4	1.0	2.4	1312	0.004	11	
		1%	1.2	8.4	190	0.03	4.0	0.8	6.0	455	0.03	8.8	
Mono-W (inclusive)	3 TeV	0	1.6	0.36	842	0.005	0.79	2.2	0.06	5625	0.0007	1.2	
		1%	1.4	0.48	534	0.008	0.78	1.0	0.24	1649	0.004	1.2	
		1%	1.0	0.84	172	0.04	0.64	0.6	0.54	515	0.02	1.0	
	14 TeV	0	1.6	2.0	819	0.005	3.4	1.8	0.56	5325	0.0008	5.5	
		1%	1.6	2.2	665	0.007	3.3	1.0	1.4	1342	0.004	5.2	
		1%	0.8	4.2	155	0.04	2.8	1.2	2.5	635	0.03	4.4	
	30 TeV	0	1.4	5.4	696	0.006	6.7	1.8	1.8	3946	0.001	12	
		1%	1.4	5.4	606	0.007	6.7	1.4	2.4	2771	0.003	11	
		1%	1.0	9.0	211	0.03	5.2	0.8	5.4	813	0.02	9.3	

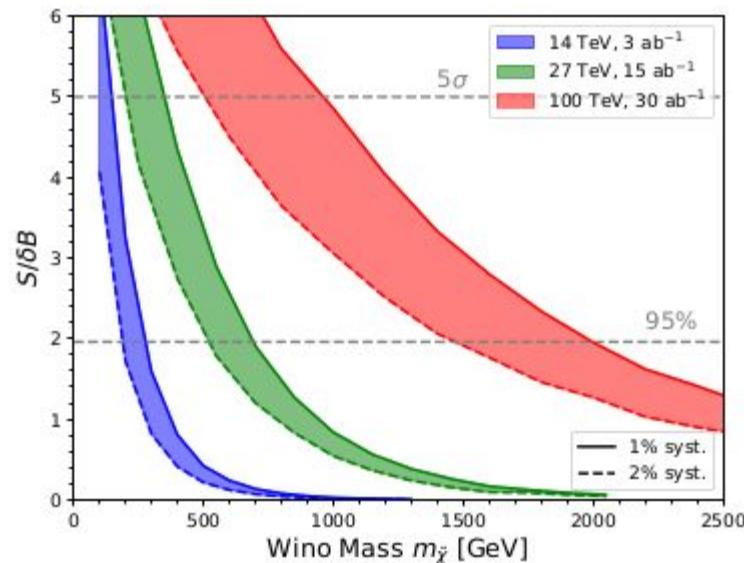
Collider vs ID/DD



recast from Panci et al. 1608.00786

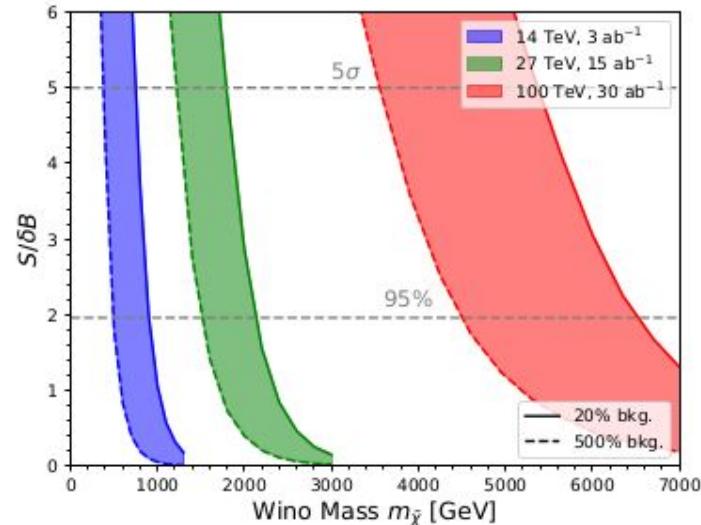


FCC-hh prospects



mono-jet

Han et al.
1805.00015

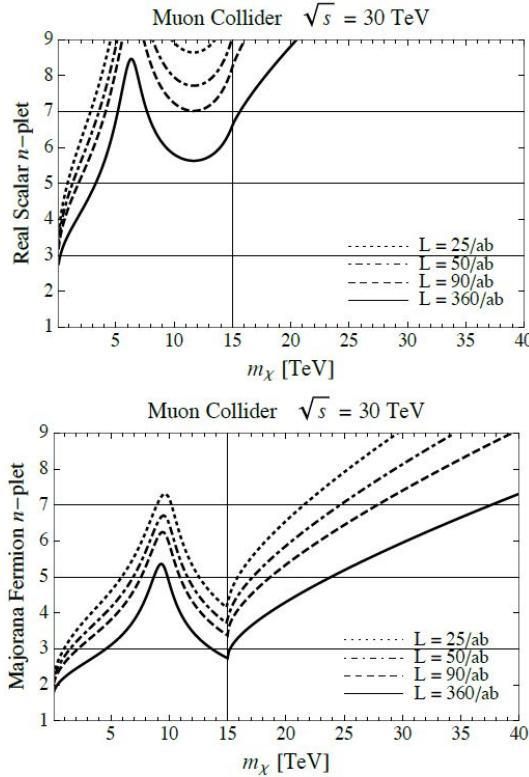
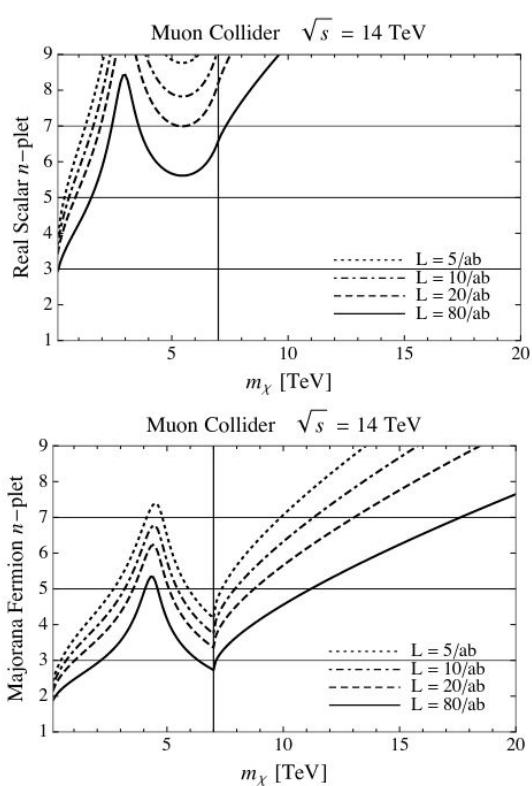


DT

Indirect collider prospects

$\mu\mu \rightarrow ff$
corrections

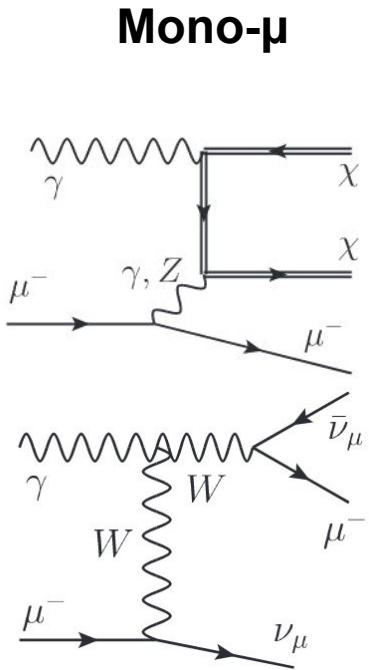
Expected 95% CL exclusion limits



Di Luzio et al.
1810.10993

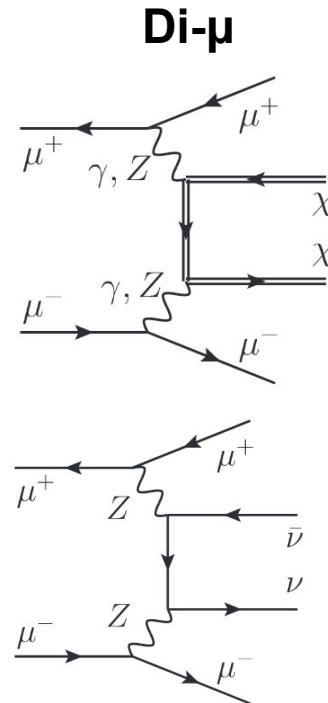
Muon channels

Sig



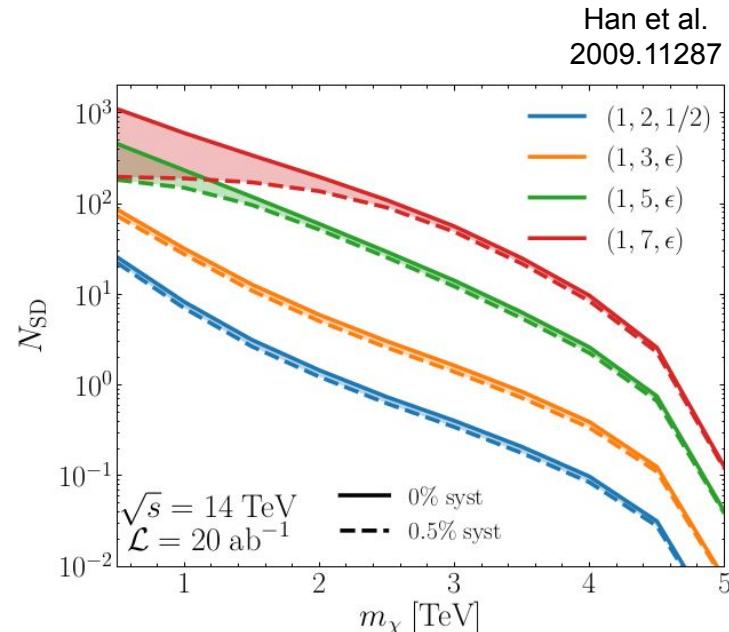
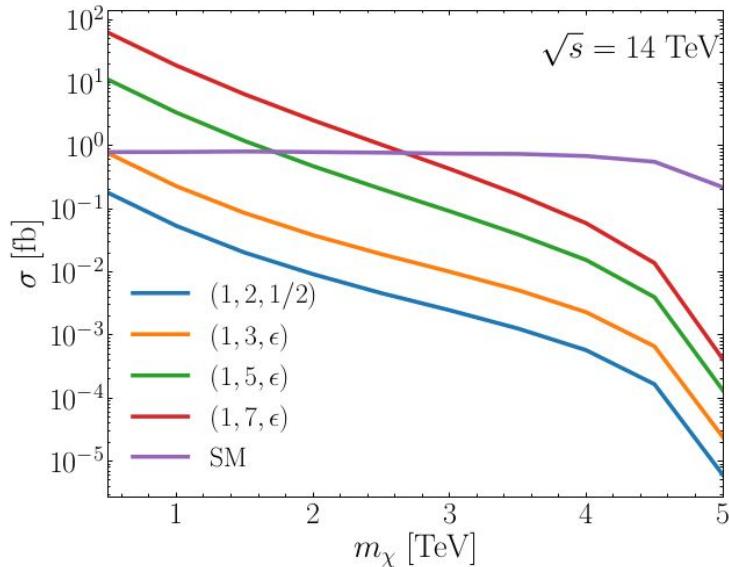
Bkg

VBF channels



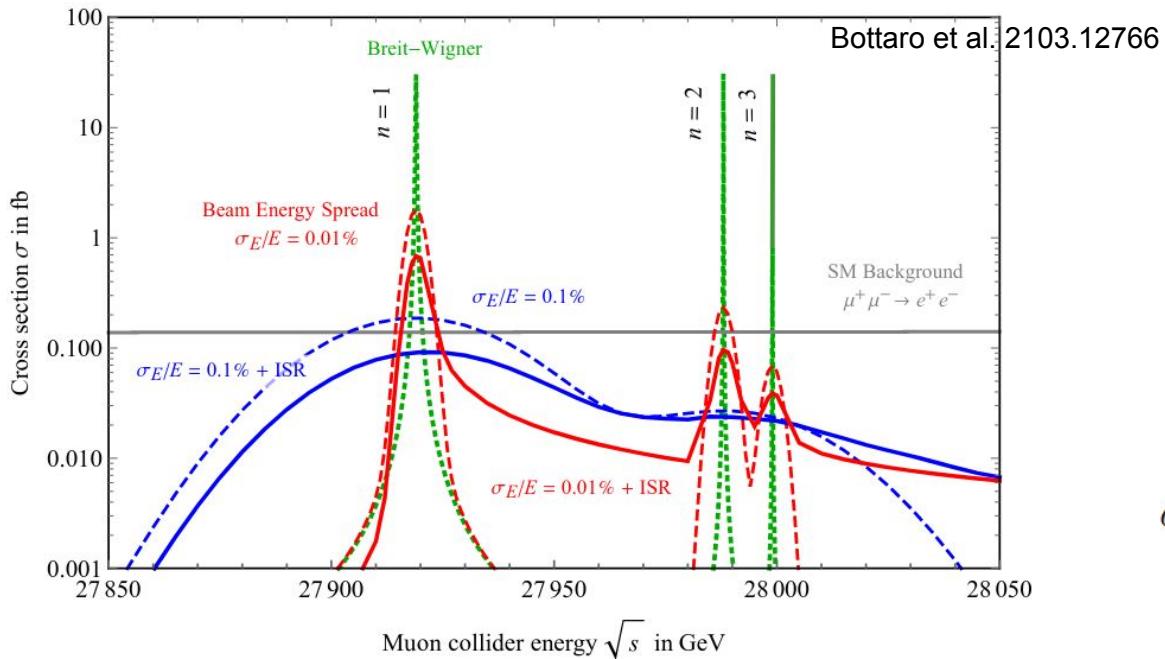
Han et al.
2009.11287

Mono- μ results



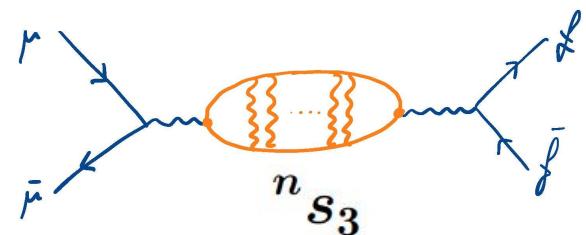
Good at low mass

Bound States (5_0^F only)



Peaks in ee cross section

same QN as W's!
s-channel mixing



$$\sigma(i_1 i_2 \rightarrow B \rightarrow f) \approx \text{BW}(s) \sigma_{\text{peak}}$$

Convoluted with Gaussian beam
Energy spread
 $O(1\text{-}10 \text{ GeV})$ vs $O(0.1\text{-}1 \text{ GeV})$ widths