COSMOLOGICAL SELECTION OF THE WEAK SCALE

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TUG 2021

Higgs Mass
Squared

$$m_h^2|H|^2$$

WEAK FORCE, STRUCTURE OF NUCLEI, COMPLEX CHEMISTRY, …

SYMMETRY

$$m_h^2 \sim y_t^2 M_{\rm Pl}^2$$

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Selection Rules of
Spacetime Dilations

(assuming masses at
the Planck scale)

SYMMETRY

$$m_h^2 \sim y_t^2 M_{\rm Pl}^2$$

Selection Rules of the
Higher-Spin Symmetry
of Free Scalars

See R. Rattazzi @ GGI: https://www.ggi.infn.it/talkfiles/slides/slides5297.pdf

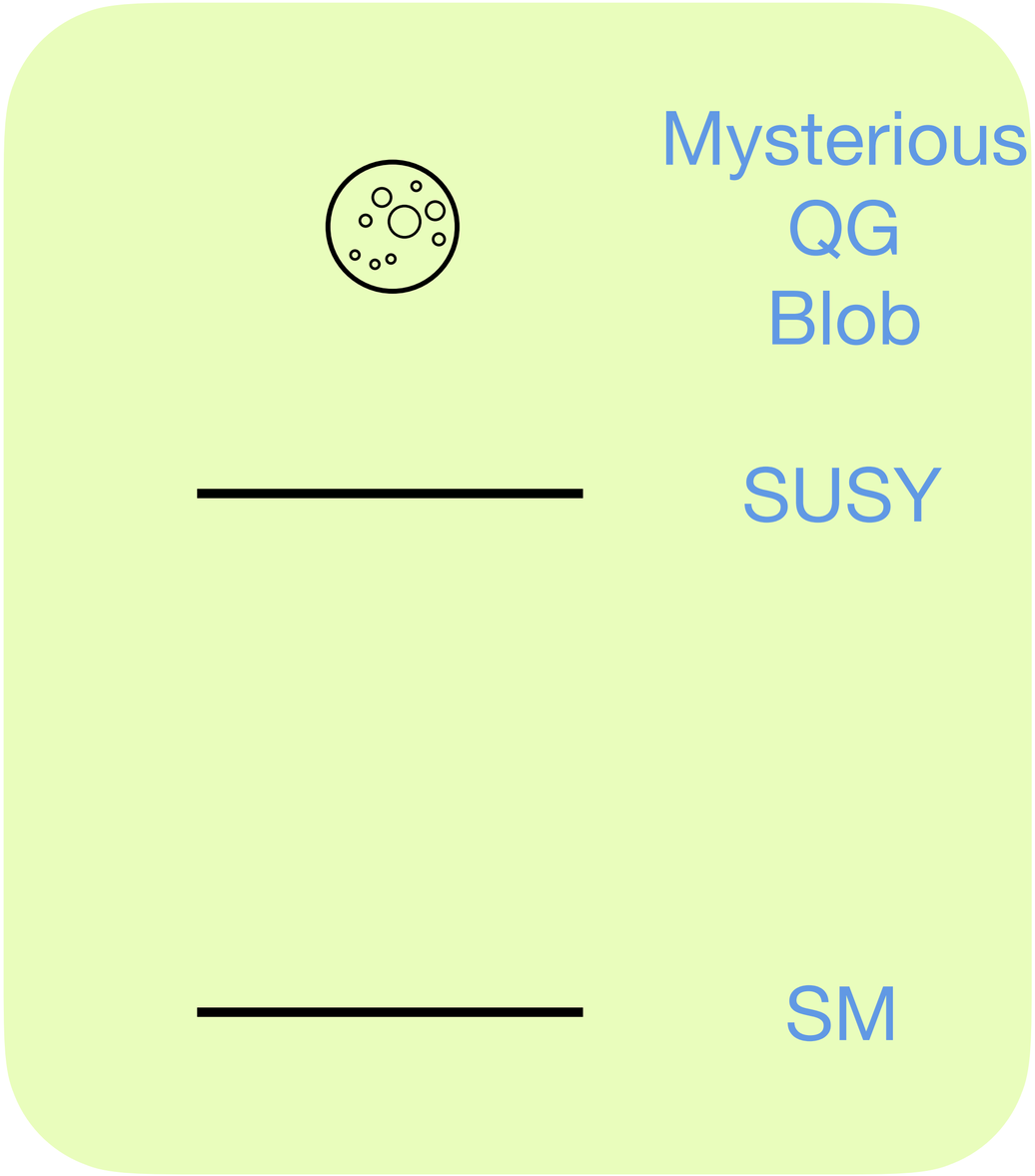
SYMMETRY

$$m_h^2 \sim y_t^2 M_{\rm Pl}^2$$

Symmetry~10^{34}Experiment

Precious clue about fundamental physics in the UV

Is there a new symmetry?


Mysterious
QG
Blob
SUSY
SM

EXAMPLE: HIGGS VEV IN THE MSSM

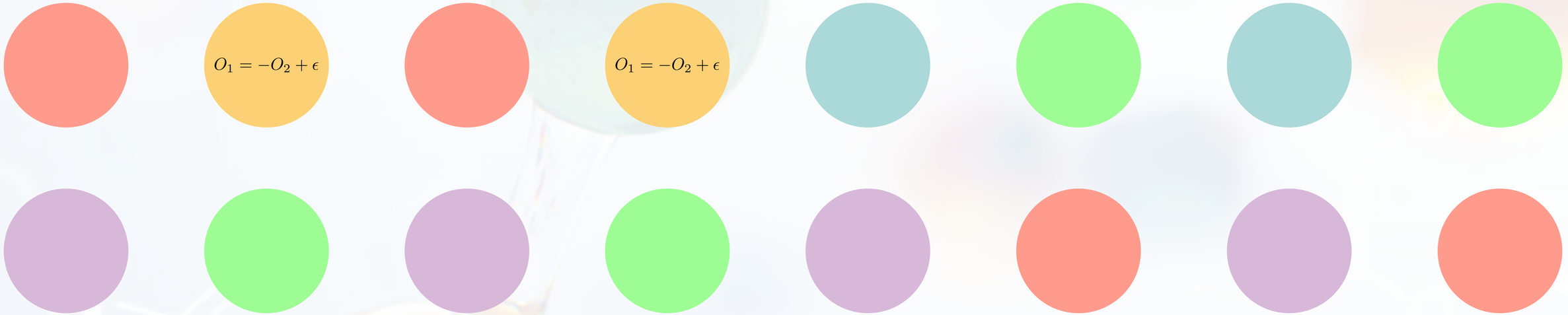
$$v^2 = \frac{2}{g^2 + g'^2}\left(\frac{|m_{H_d}^2 - m_{H_u}^2|}{\sqrt{1-\sin(2\beta)^2}} - m_{H_u}^2 - m_{H_d}^2 - 2|\mu|^2 + \frac{y_t^2}{16\pi^2} m_{\widetilde{t}}^2 f\left(\frac{m_{\widetilde{t}_1}^2}{m_{\widetilde{t}}^2}, \frac{m_{\widetilde{t}_2}^2}{m_{\widetilde{t}}^2}\right)\right) + \ldots$$

$$\left(m_h^2 |H|^2 \right)$$

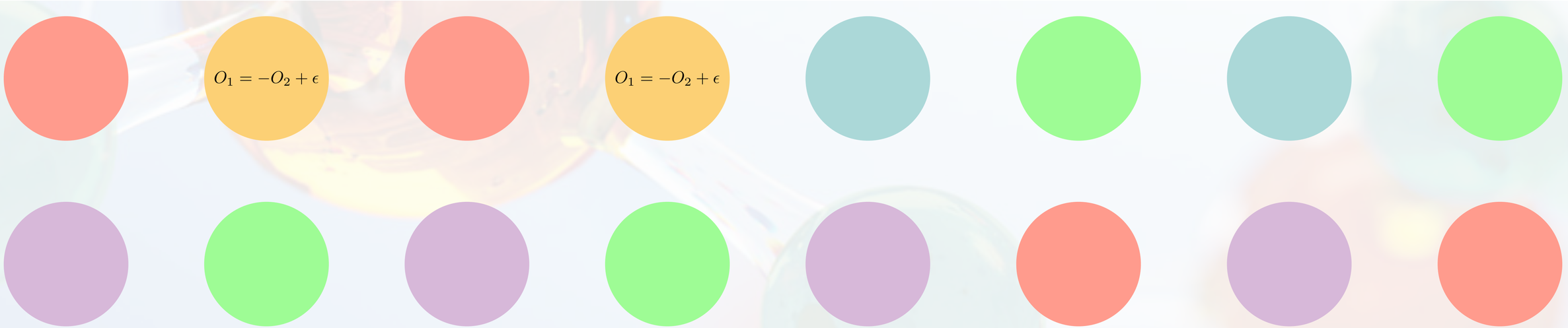
We have been looking
for answers
here **for more than 40 years**

Higgs Boson

and we have not found them



Is there a landscape?



Change of perspective:

Can we find the origin of the weak scale early in the history of the Universe?

Historically:

Multiverse
+Anthropic selection

Recently:

New class of ideas that can be tested in the laboratory in the near future

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Multiverse
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Recently:

New class of ideas that can be tested in the laboratory in the near future

[Agrawal, Barr, Donoghue, Seckel ’97],

[Arvanitaki, Dimopoulos, Gorbenko, Huang, Van Tilburg ’16],

[Arkani-Hamed, **RTD**, Kim, ‘20],

[Giudice, Kehagias, Riotto, ’20],

…

[Dvali, Vilenkin ’03],

[Dvali ’04],

[Geller, Hochberg, Kuflik,’18],

[Giudice, McCullough, You, ’21],

…

[Graham, Rajendran, Kaplan, ’15],

[Arkani-Hamed, Cohen, **RTD**, Kim, Pinner, ’16],

[Csaki, **RTD**, Geller, Ismail, ’20],

[Strumia, Teresi, ’20],

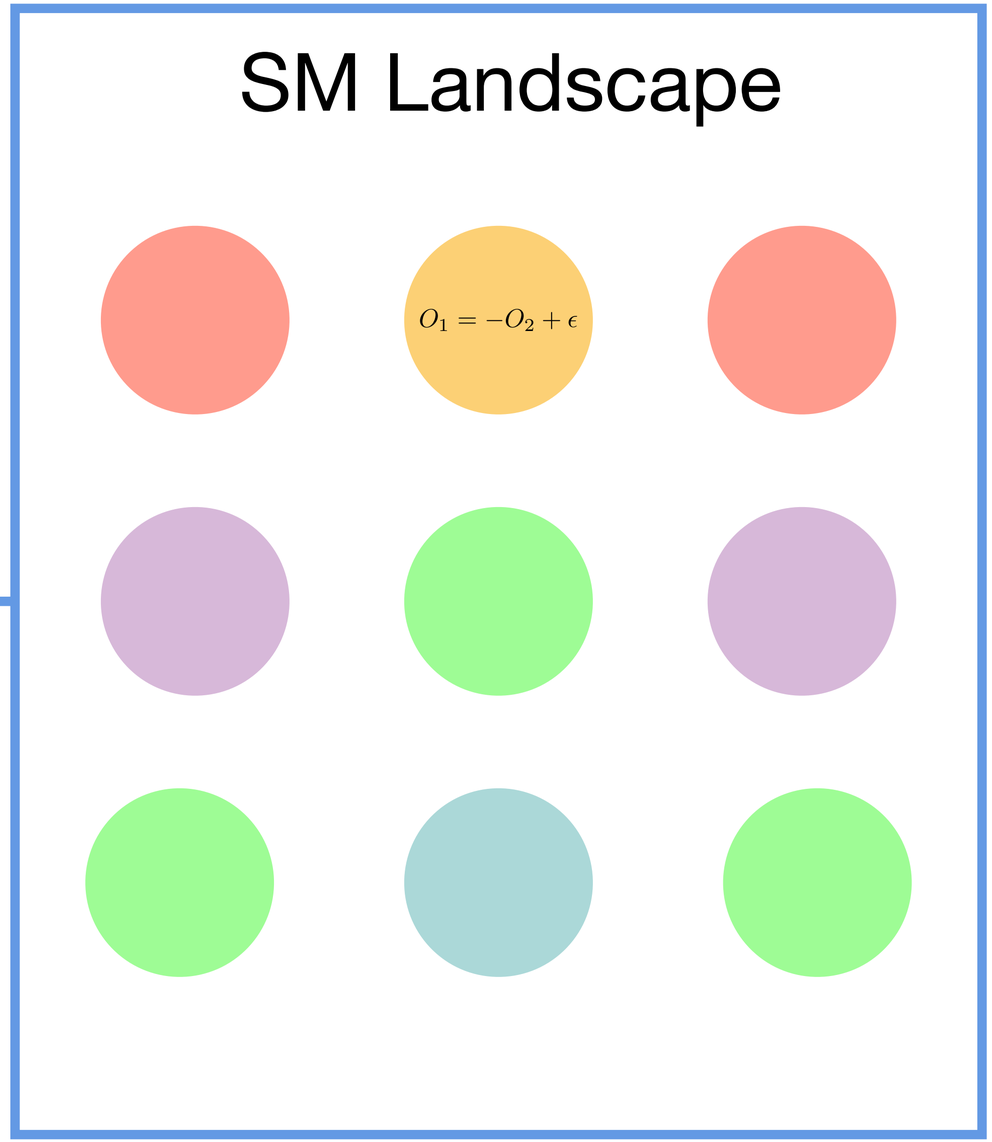
[**RTD**, Teresi, ’21],

…

Early History of the Universe

Symmetric Sector

$$\Lambda_S \ll M_{\rm Pl}$$

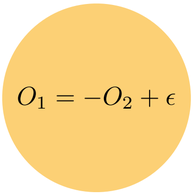


Late times

Symmetric Sector

$$\Lambda_S \ll M_{\rm Pl}$$

SM Landscape



An event triggered by the symmetric sector selects the observed

$$m_h^2$$

EXAMPLE: STATISTICAL

[Dvali, Vilenkin ’03], [Dvali ’04]

$$F_4 = dA_3$$

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EXAMPLE: STATISTICAL

[Dvali, Vilenkin ’03], [Dvali ’04]

$$q(\phi) = \frac{\phi^N}{M_{\rm Pl}^{N-2}}$$

$$\Delta\langle\phi\rangle^2/\langle\phi\rangle^2 \sim \langle\phi\rangle^{N-2}$$

At every step the brane charge is smaller -> most vacua are at small vev

EXAMPLE: STATISTICAL

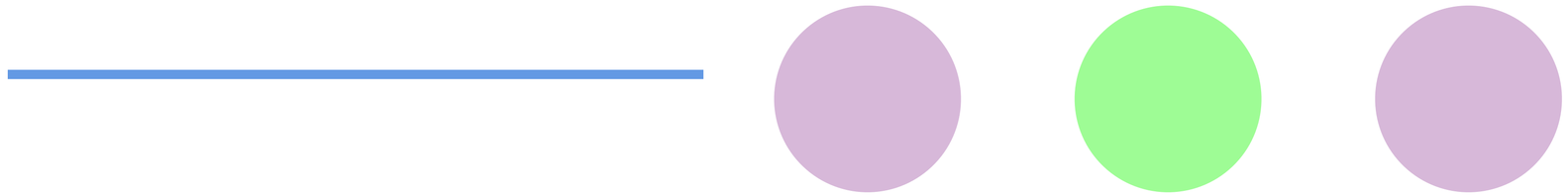
[Dvali, Vilenkin ’03], [Dvali ’04]

$$F_4 = dA_3$$

Symmetric Sector

$$q(\phi) \lesssim M_{\rm Pl}^2$$

SM Landscape



A_3

$$\frac{\phi^N}{M_{\rm Pl}^{N-2}} \int_{2+1} A_3$$

$$\frac{F_4^2}{M_{\rm Pl}^2} |\phi|^2$$

EXAMPLE: RELAXION

[Graham, Kaplan, Rajendran ’15],

$$V(\phi) = g\phi + ... + (M^2 + g\phi + ...)|H|^2 + \frac{\phi}{f} G\tilde{G}$$

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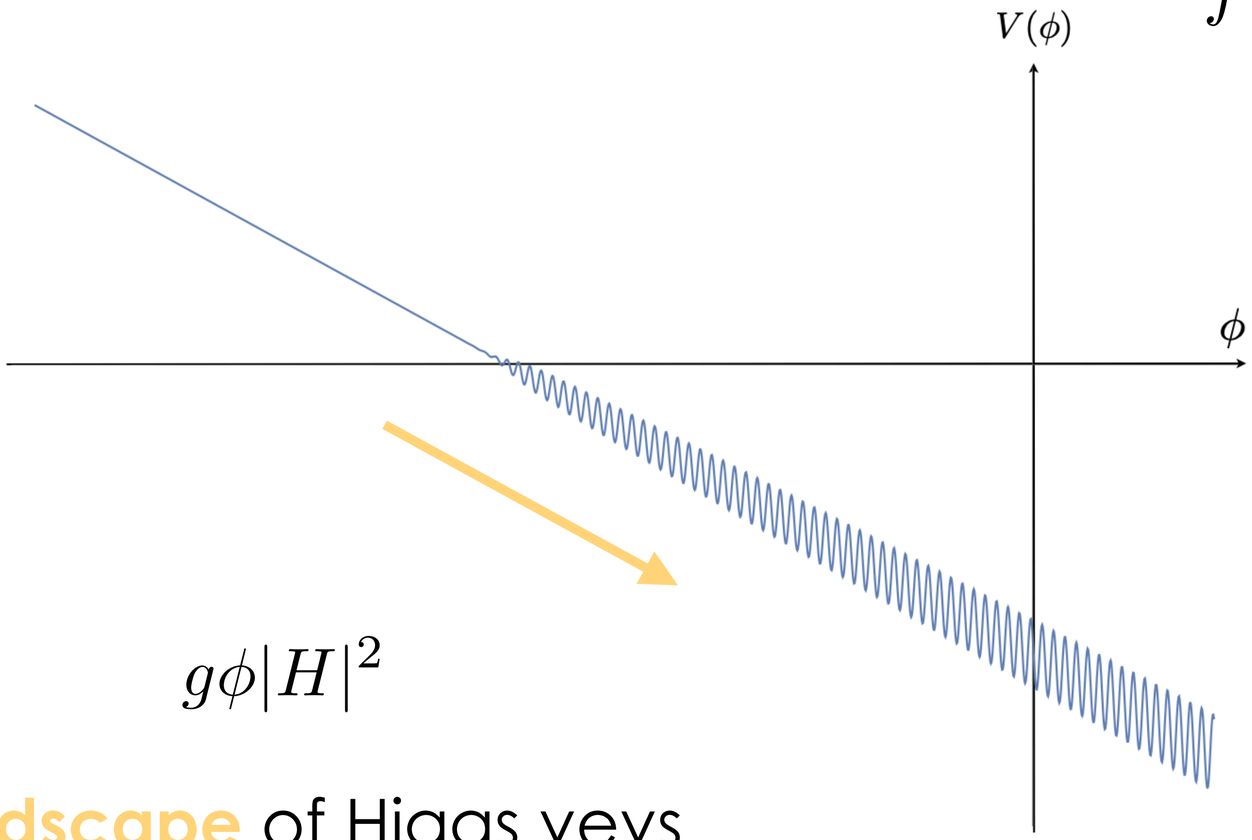

$g\phi|H|^2$

Landscape of Higgs vevs

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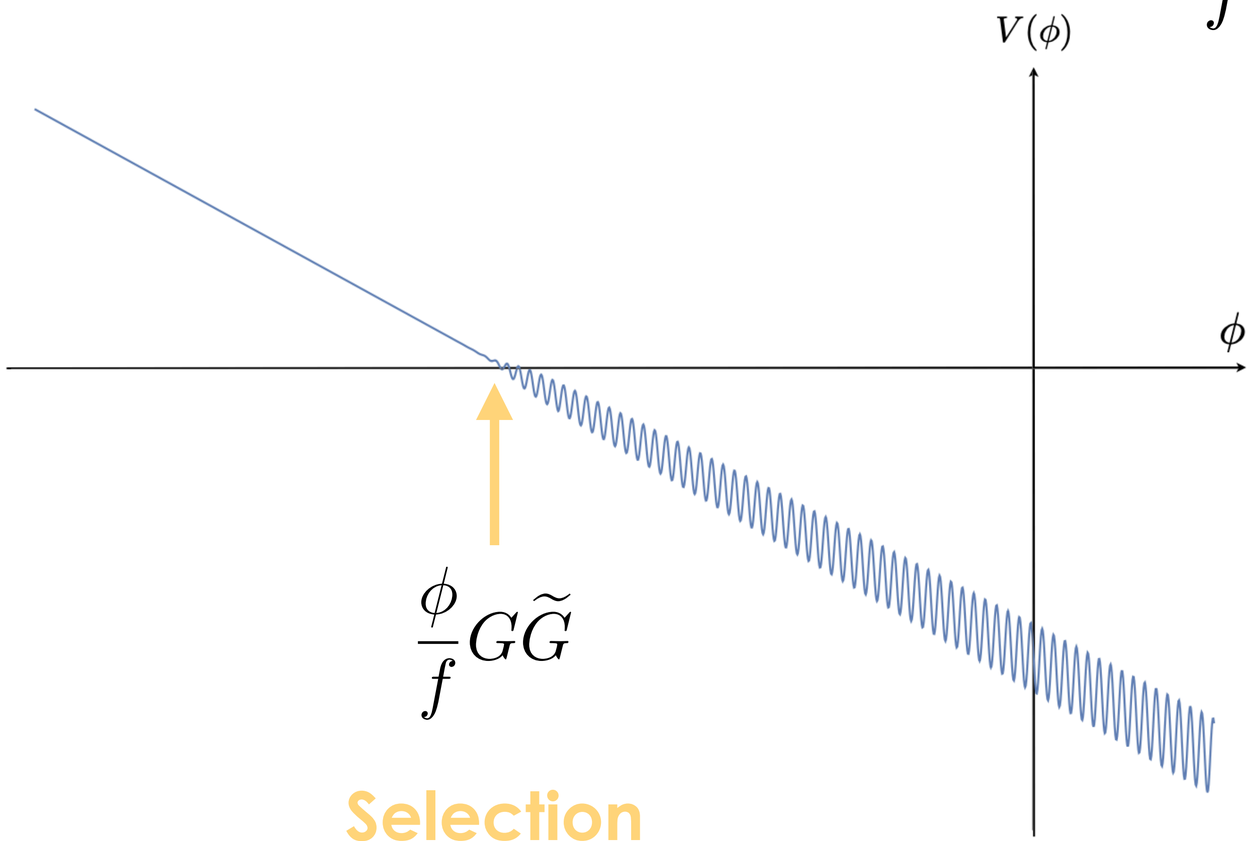

Selection

EXAMPLE: RELAXION

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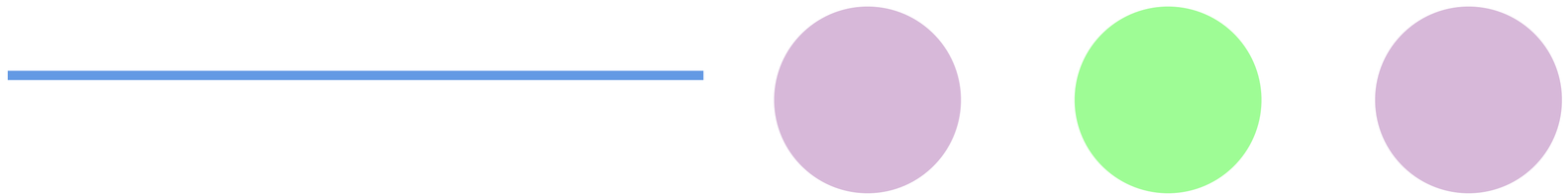
Symmetric Sector

$$g \ll M_{\rm Pl}^3$$

SM Landscape



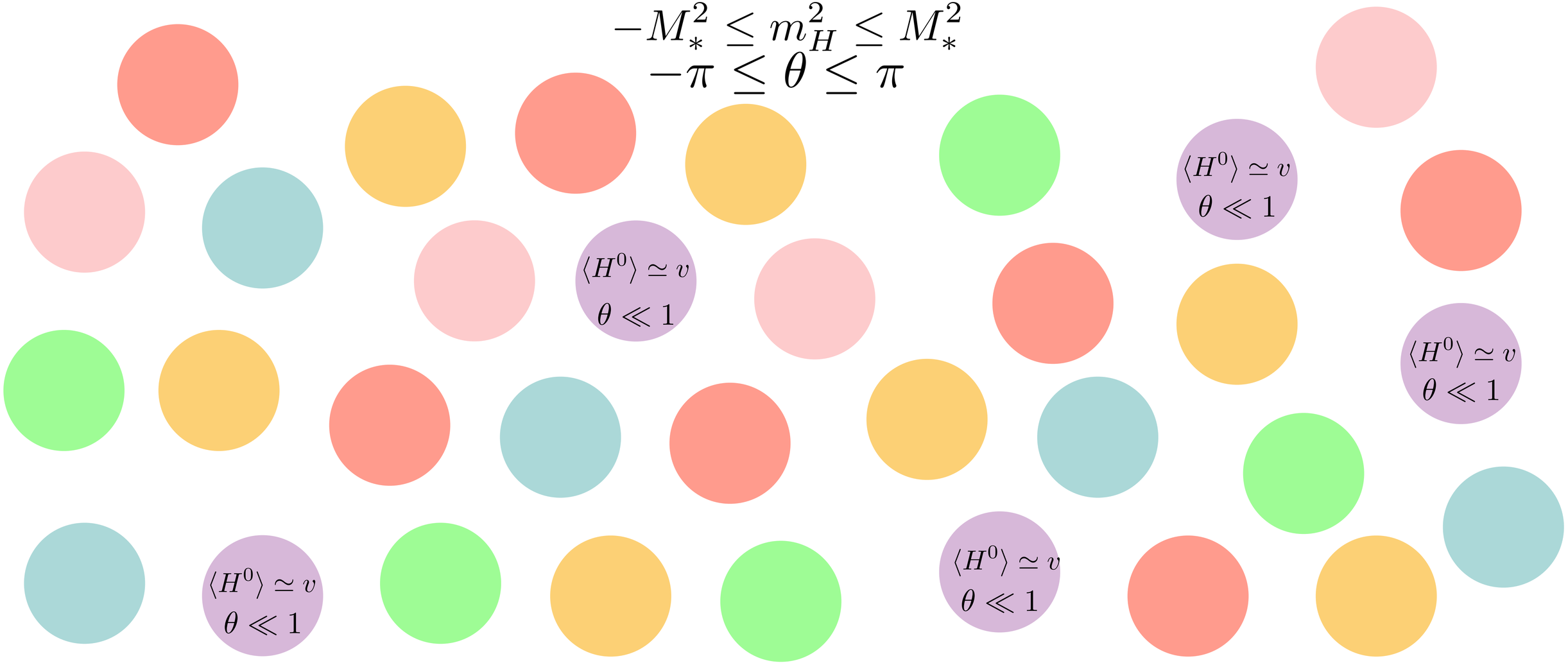
ϕ $\phi G\tilde{G}$ $g\phi|H|^2$

EXAMPLE: CRUNCHING

[Bloch, Csaki, Geller ,Volansky ’19], [Csaki, Geller, RTD, Ismail, ‘20], [RTD, Teresi ’21]

Landscape of Higgs Masses and theta-angles populated by inflation

$$-M_*^2 \leq m_H^2 \leq M_*^2$$
$$-\pi \leq \theta \leq \pi$$



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[Bloch, Csaki, Geller ,Volansky ’19], [Csaki, Geller, RTD, Ismail, ‘20], [RTD, Teresi ’21]

After reheating and a time

$$t_c \sim 1/H(\Lambda_{\rm QCD}) \sim 10^{-5}\ s$$

All patches where the Higgs vev

$$\langle H^0 \rangle \equiv h$$

Is outside of a certain range

$$h_{\rm min} \lesssim h \leq h_{\rm crit}$$

And theta is large

$$\theta \leq \theta_{\rm max}$$

crunch

$\langle H^0 \rangle \simeq v$
$\theta \ll 1$

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Only universes with the observed value of the weak scale can live longer than EW time. **Today the multiverse looks like**:

$$\langle H^0 \rangle \simeq v$$
$$\theta \ll 1$$

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EXAMPLE: SLIDING NATURALNESS

[RTD, Teresi ’21]

$$V = \mp m_{\pm}^2 \phi_{\pm}^2 - \lambda_{\pm} \phi_{\pm}^4 + \frac{\alpha_s}{8\pi} \left(\theta + \frac{\phi_+}{F_+} + \frac{\phi_-}{F_-} \right) G\tilde{G}$$

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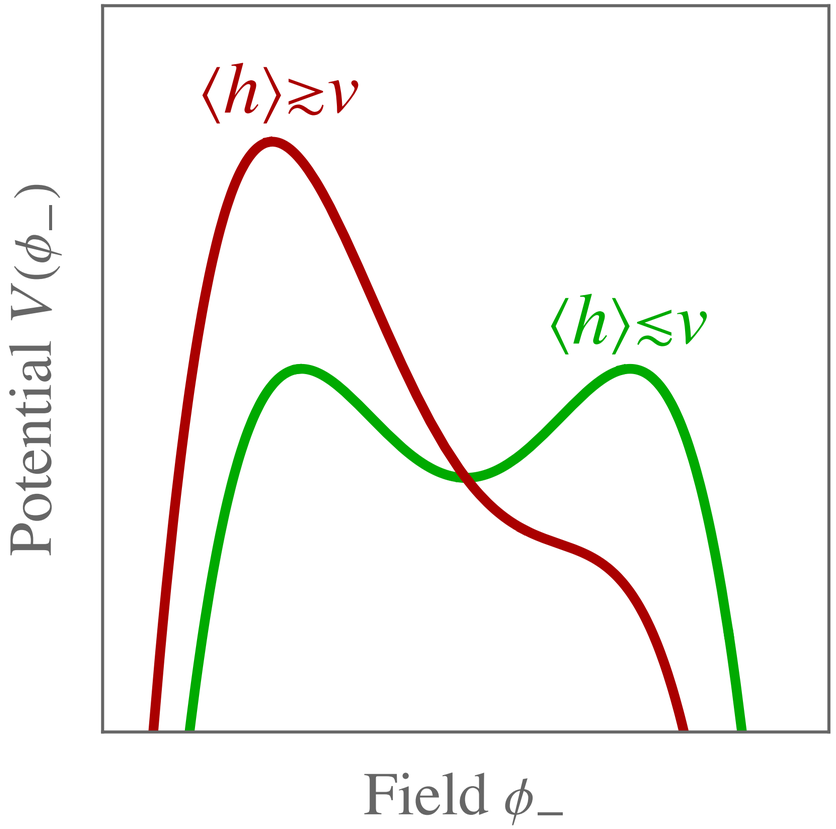

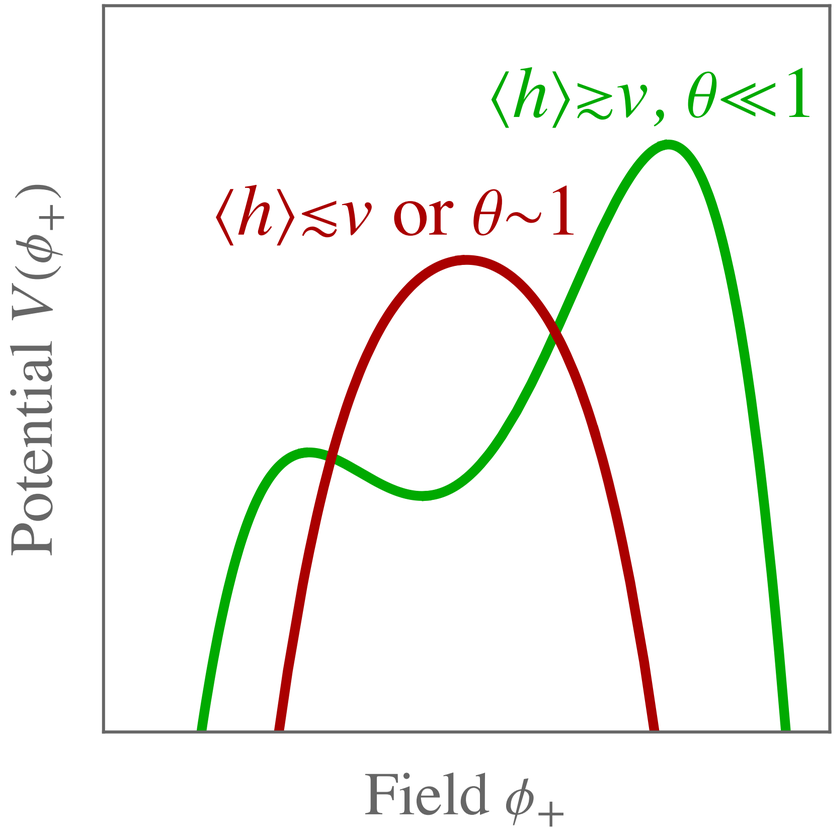

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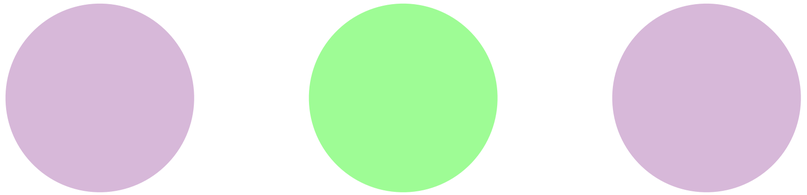
Symmetric Sector

$$m_\pm \ll M_{\rm Pl}$$

SM Landscape

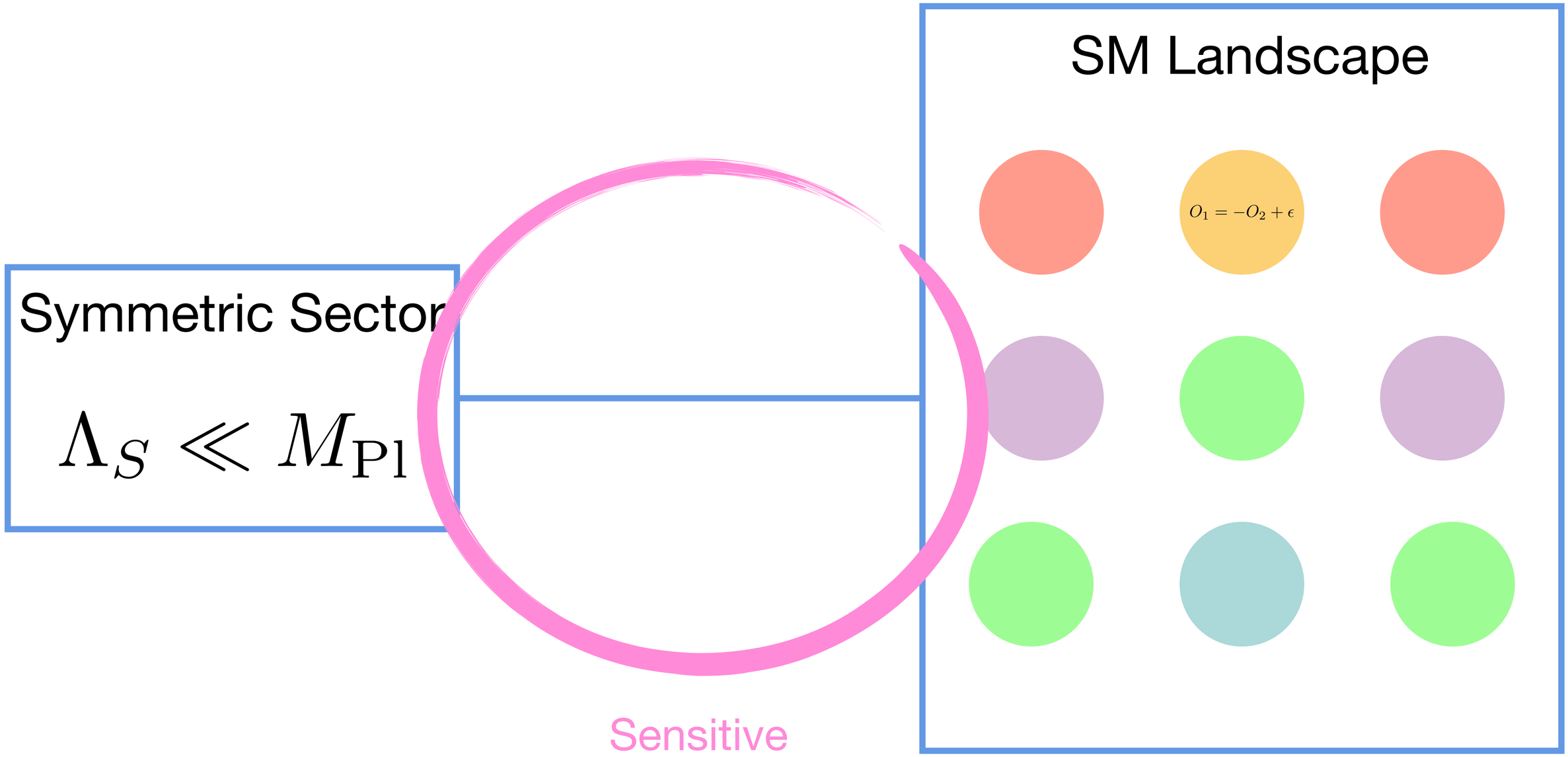


$\phi_\pm$

$\phi_\pm G\tilde{G}$

“Friendly”
String Landscape?

[Arakni-Hamed, Dimopoulos, Kachru, ‘05]


SM Landscape
$O_1 = -O_2 + \epsilon$
Symmetric Sector
$\Lambda_S \ll M_{\rm Pl}$
Sensitive
to the Higgs vev

HIERARCHY 102

[Arkani-Hamed, RTD, Kim '20]

Does anything change in the SM as we vary $\langle h \rangle$?

1. Obviously the spectrum

2. If we look at local operators we discover the hierarchy problem:

$$\langle h^\dagger h \rangle \sim \Lambda_H^2$$

HIERARCHY 102

Does anything change in the SM as we vary $\langle h \rangle$?

$$\frac{\alpha_s}{8\pi}(\xi\phi + \theta)\mathrm{Tr}\left[G\tilde{G}\right]$$

$$m_\pi^2 f_\pi^2 \sqrt{1 - \frac{4m_u m_d}{(m_u + m_d)^2}\sin^2\left(\xi\phi + \theta\right)}$$

$$(y_u + y_d) v f_\pi^3 \left(\theta\xi\phi + \xi^2\phi^2 + ...\right)$$

HIERARCHY 102

Does anything change in the SM as we vary $\langle h \rangle$?

$$\xi \phi \mathrm{Tr}\left[G\widetilde{G}\right]$$

Important Pheno Message:

Axion-Like phenomenology can be related to the hierarchy problem

TRIGGER PHENOMENOLOGY

$G\tilde{G}$

ALPs

TRIGGER PHENOMENOLOGY

$G\widetilde{G}$

ALPs

$F\widetilde{F} + yLHE^c$

Vector-like Leptons

TRIGGER PHENOMENOLOGY

$G\tilde{G}$ — ALPs

$F\tilde{F} + yLHE^c$ — Vector-like Leptons

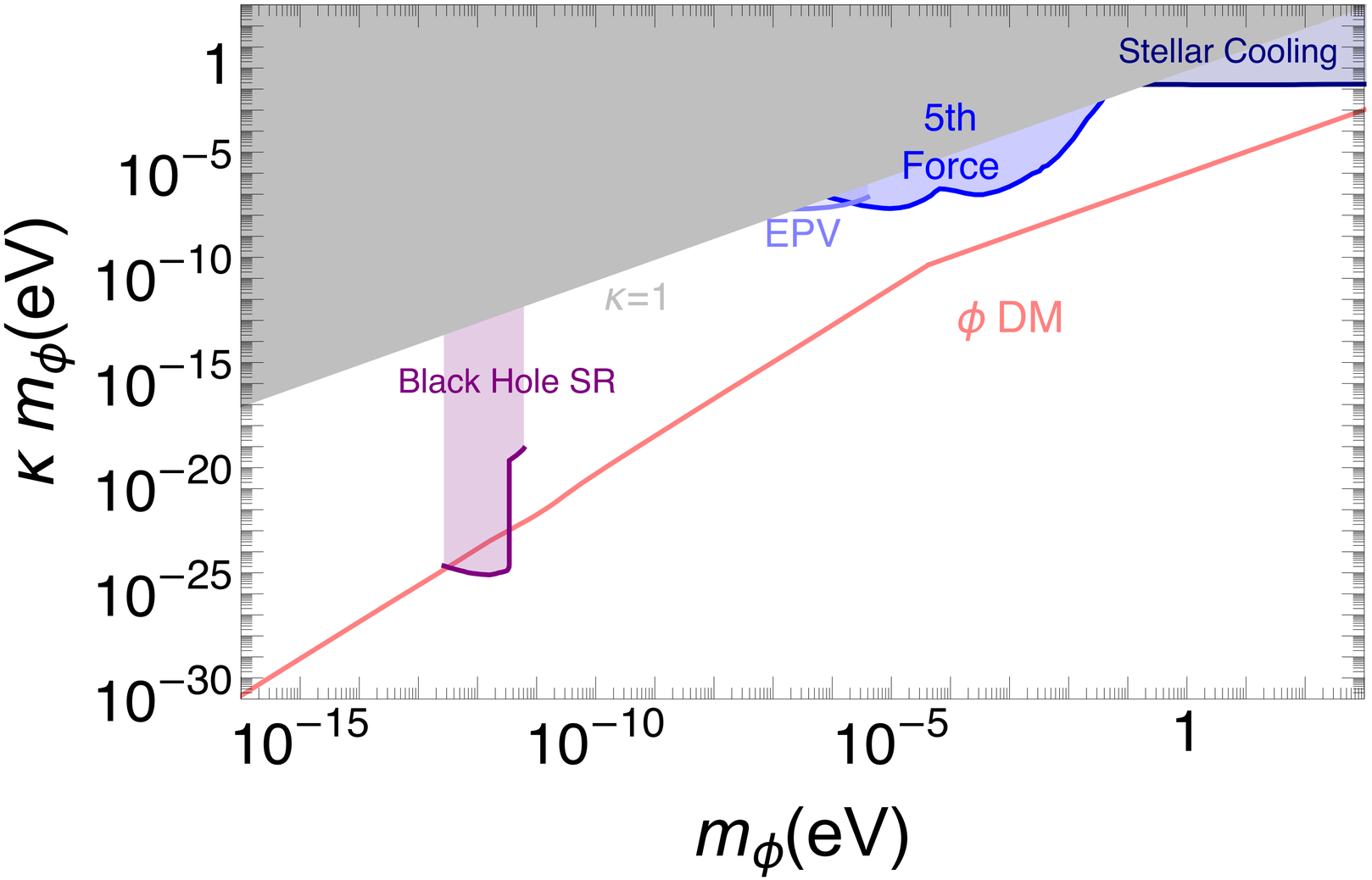
$H_1 H_2$ — Type-0 2HDM

See [Arkani-Hamed, RTD, Kim, ‘20]

[Arkani-Hamed, RTD, Kim, ‘20], [Dvali, Vilenkin ’03], [Geller, Hochberg, Kuflik,’18], [Graham, Rajendran, Kaplan, ’15], [Strumia, Teresi, ’20], [Espinosa, Grojean, Panico, Pomarol, Pujolas, ’15], …

A ULTRALIGHT WIMP MIRACLE

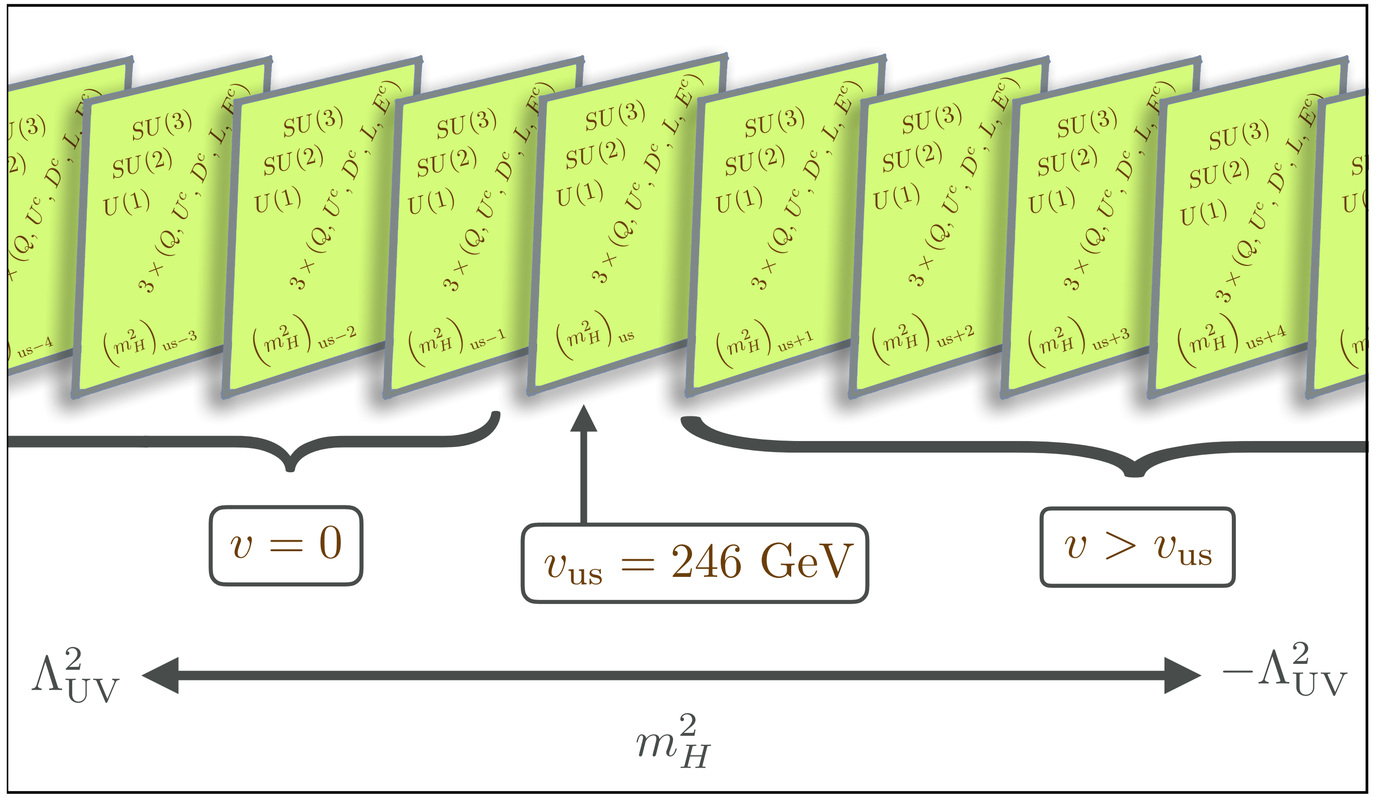
$$V_\phi / V_{\phi H} \sim 1$$



[Arkani-Hamed, **RTD**, Kim] '20 = [**RTD**, Teresi] '21

AN EXCEPTION: NNATURALNESS

[Arkani-Hamed, Cohen, **RTD**, Hook, Kim, Pinner] '16



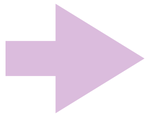
$$\mathcal{L} \supset m_\phi \phi |H_i|^2$$

$$\Gamma_\phi \sim \frac{1}{m_{h_i}^n}$$

Change of perspective:

Can we find the origin of the weak scale early in the history of the Universe?

Completely new
perspectives
on key “classic” questions



New Experimental Targets

Tuning

Cosmological Selection

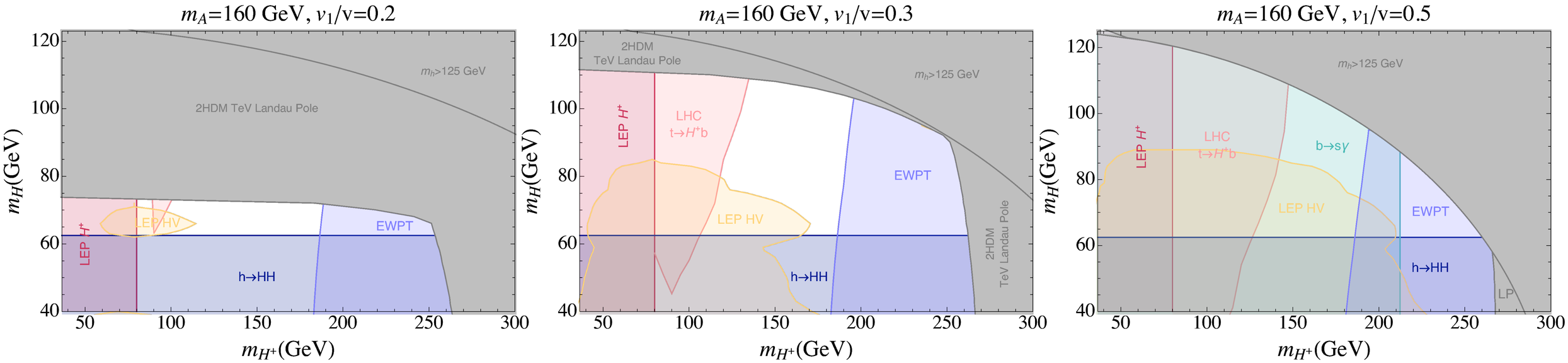
UV/IR? Calculability?

BACKUP

EXAMPLE: TYPE-0 2HDM

[Arkani-Hamed, RTD, Kim '20]

N.B. It is extremely hard to find a viable BSM trigger

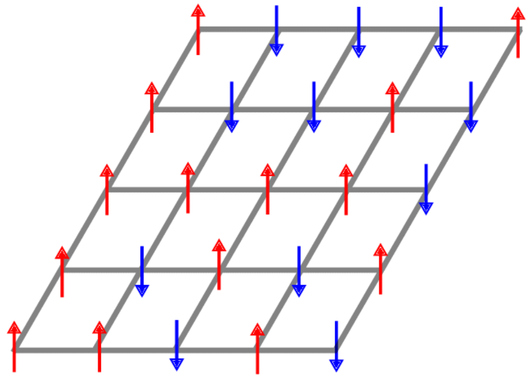


Sharp target which **can't be decoupled**!

$$m_{\rm NP} \lesssim m_h$$

A LANDSCAPE IN THE LAB

Prepare Ising Model



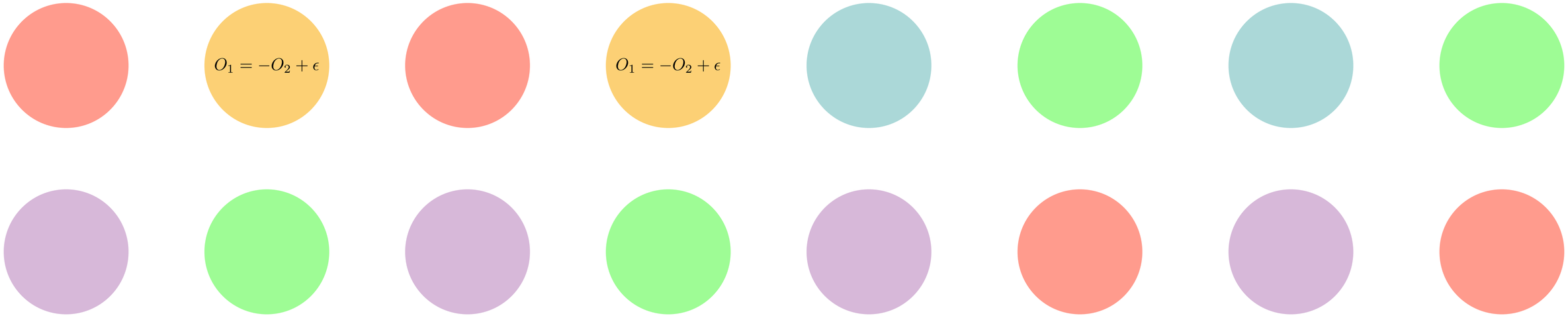
Scan Temperature

$$T - T_c \simeq 10^{-30}$$

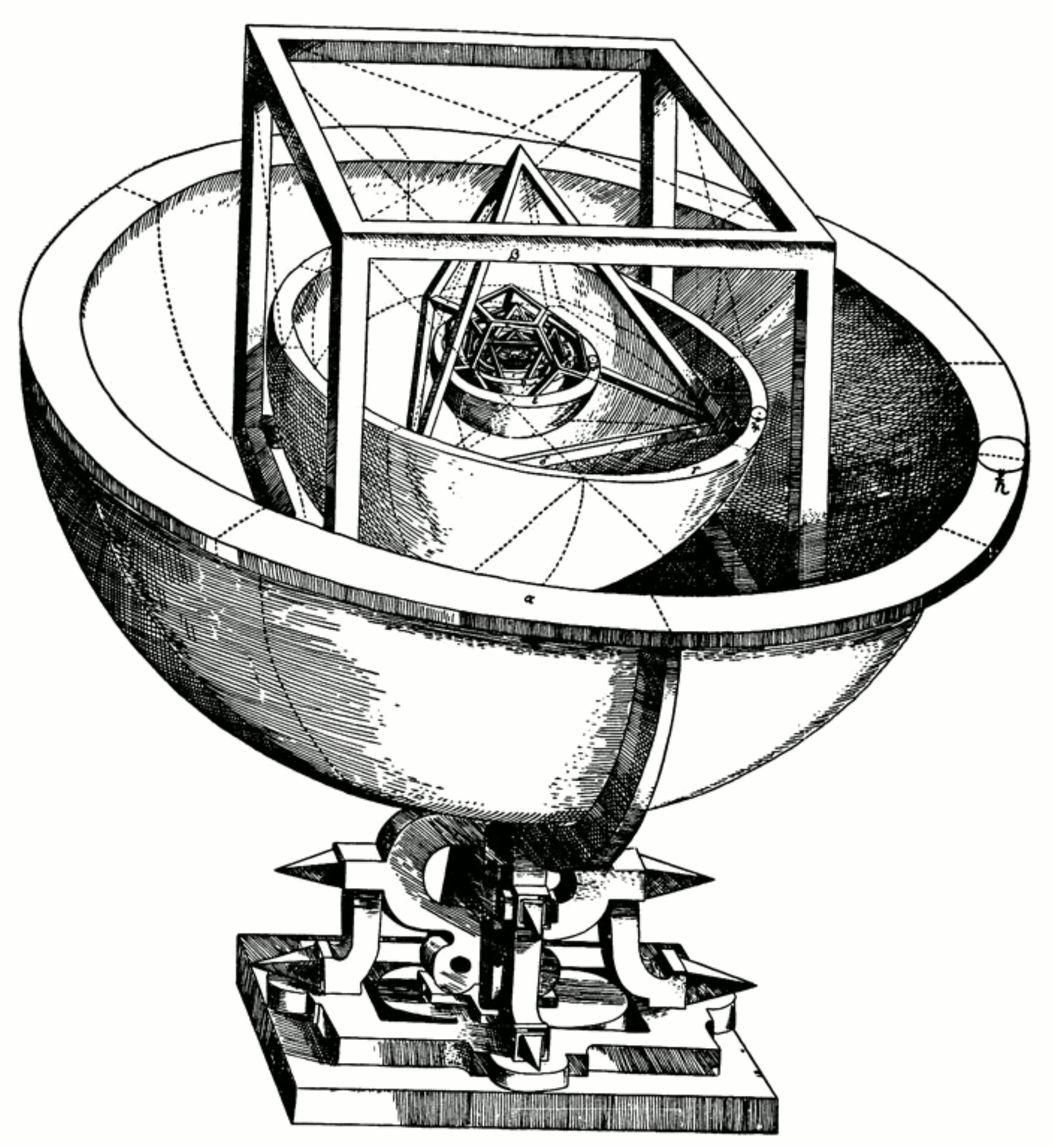
The scalar is
much lighter
than the lattice spacing

A LANDSCAPE

1. One day it can be tested experimentally
2. Currently our most concrete explanation for the CC
3. It probably exists independently of the two problems



Mysterium Cosmographicum



Why $M_{\rm Pl}^4 \gg m_h^4, \Lambda_{\rm CC}^4$?

Mysterious QG Blob

SM

1. Cosmological Constant and Higgs mass are inputs (can not be calculated, only measured)

2. UV/IR Mixing

3. IR constraints from UV consistency (swampland, …)

EXAMPLE: ANTHROPIC

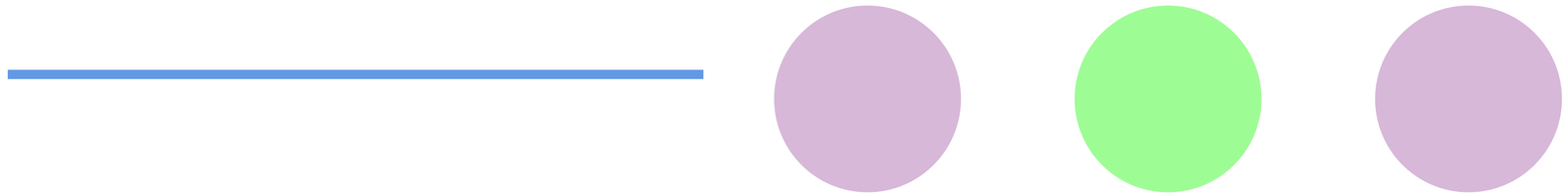
[Agrawal, Barr, Donoghue, Seckel ’97]

For complex chemistry we need a Higgs vev not too far from the QCD scale

Symmetric Sector

$$\Lambda_{\rm QCD} \ll M_{\rm Pl}$$

SM Landscape



QCD

$$Y_q Q H q^c$$

“Friendly”
String Landscape?

[Arakni-Hamed, Dimopoulos, Kachru, ‘05]

Anthropic Selection

Does not require new physics with couplings to the SM stronger than gravitational

Statistical Selection

Does not require new physics with couplings to the SM stronger than gravitational

Dynamical Selection

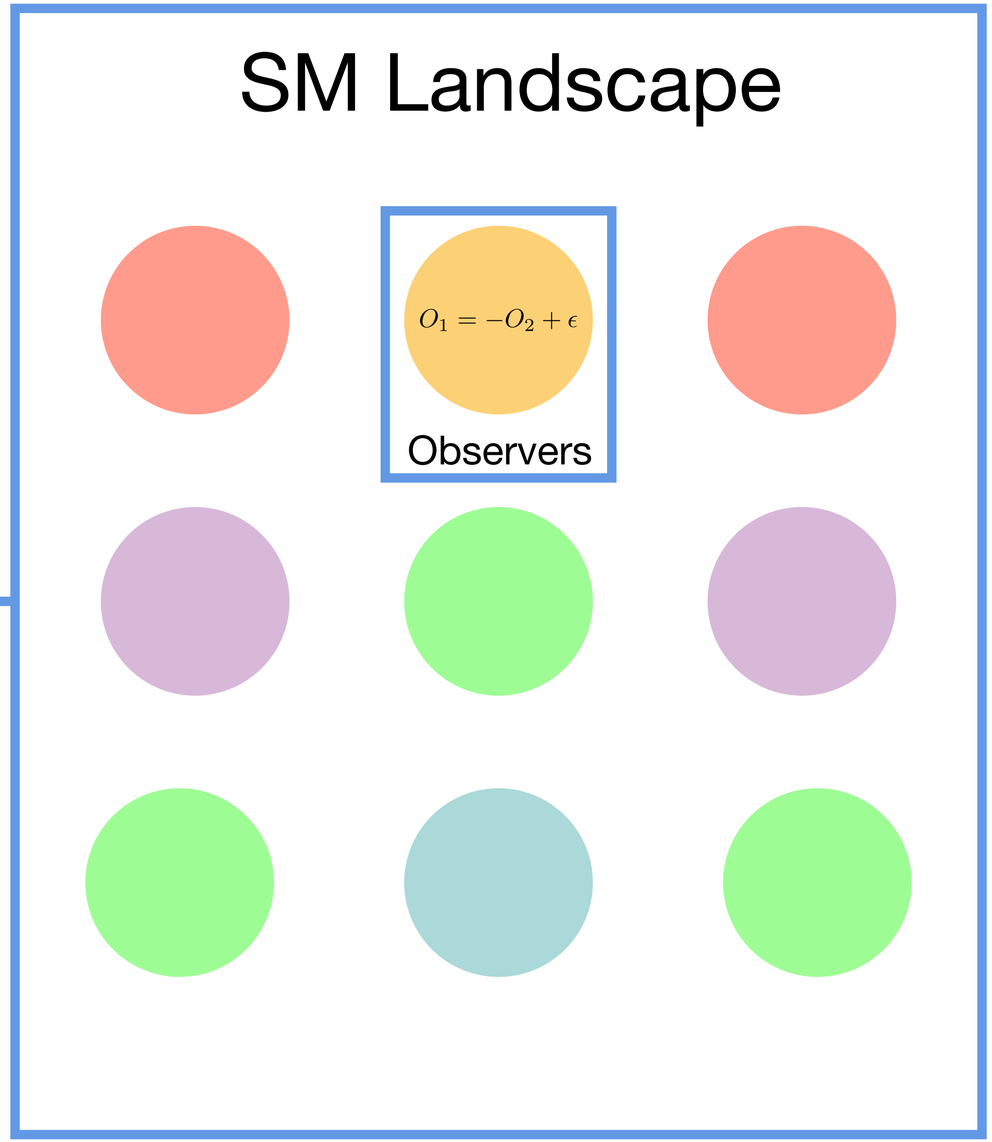
Typically visible!

From now on: **focus on the Higgs vev**

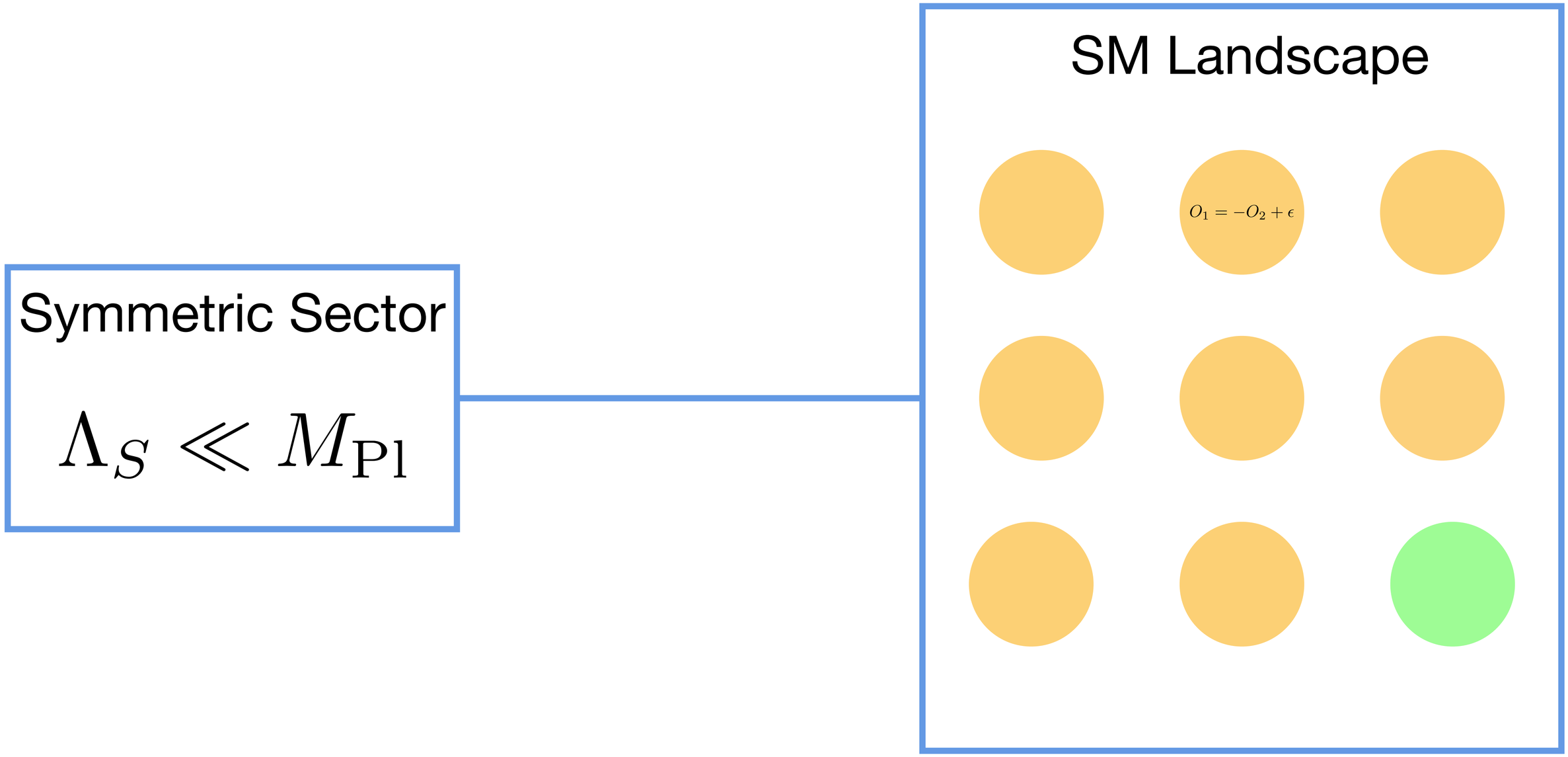
“Anthropic” Selection

Symmetric Sector

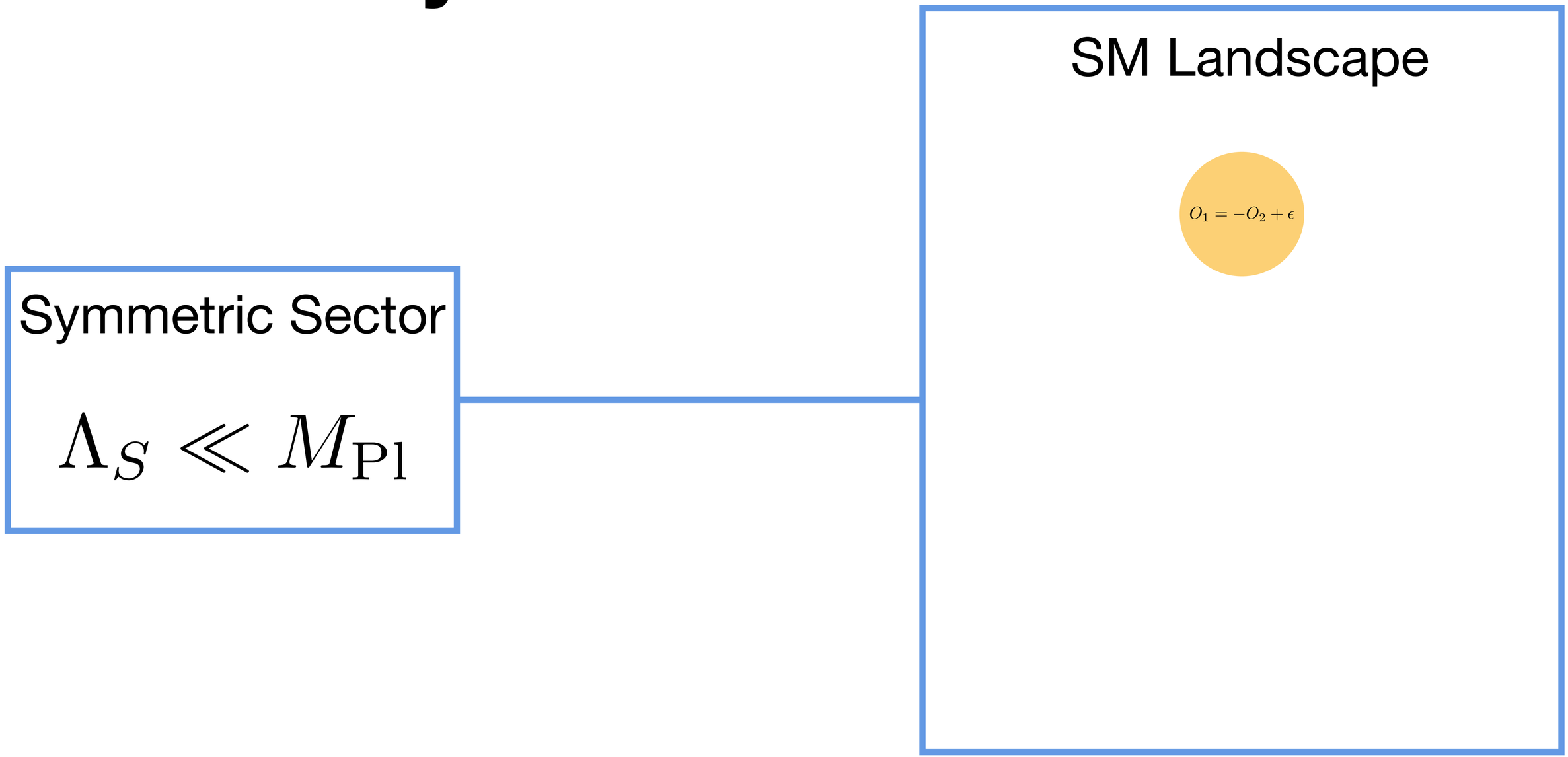
$$\Lambda_S \ll M_{\rm Pl}$$



“Statistical” Selection



“Dynamical” Selection



Historically:

Multiverse
+Anthropic selection

Recently:

New class of ideas that can be tested in the laboratory in the near future

EXAMPLE: ANTHROPICS

Anthropic Arguments: **a symmetry and a landscape**

$$\Lambda_{\rm CC} \leftrightarrow \rho_{\rm MR} \left(\frac{\delta\rho}{\rho}\right)^3 \ll M_{\rm Pl}^4$$ [Weinberg '87]

$$v \leftrightarrow \Lambda_{\rm QCD} \ll M_{\rm Pl}$$ [Agrawal, Barr, Donoghue, Seckel '97]

EXAMPLE: ANTHROPICS

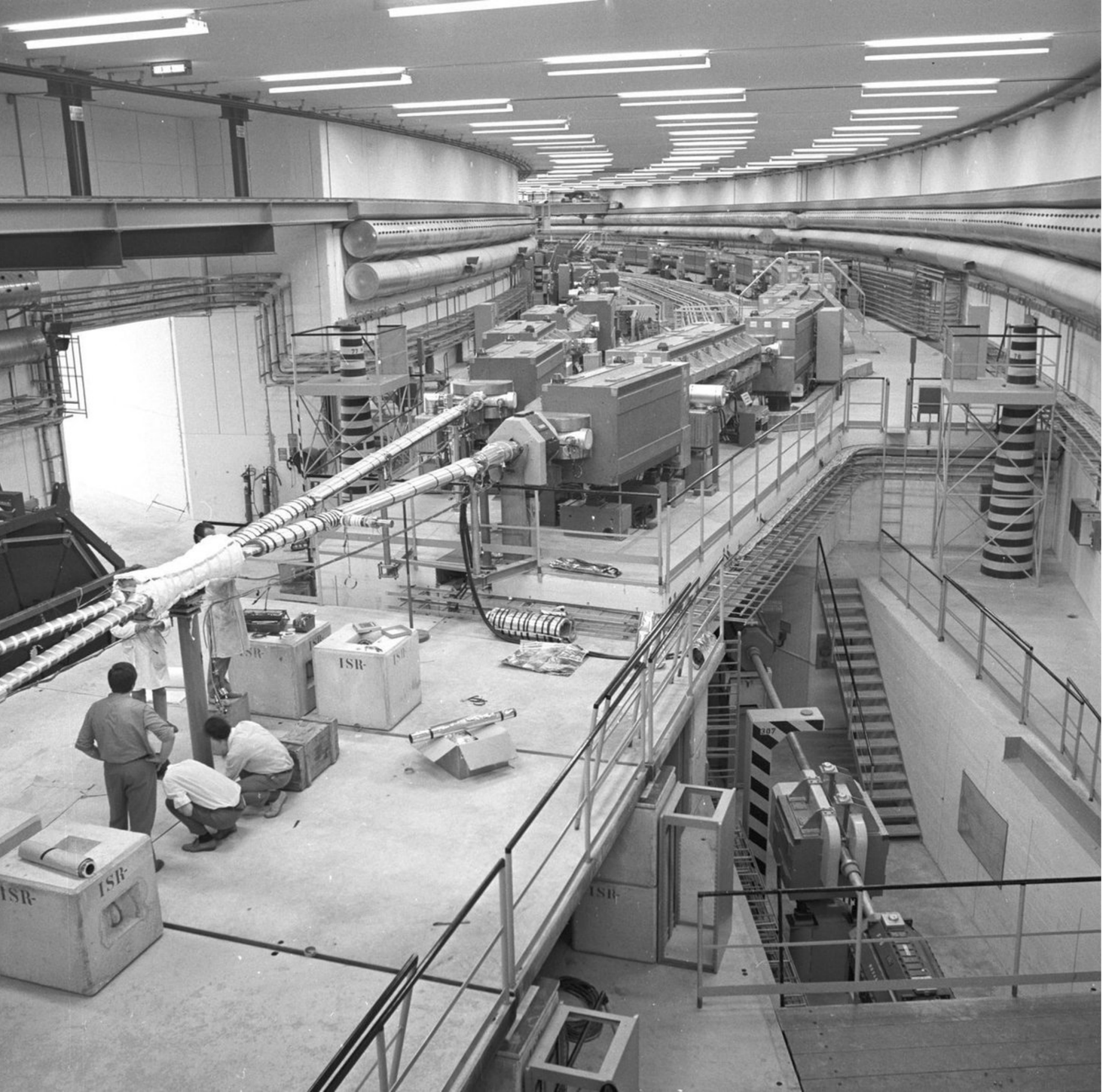
Anthropic Arguments: **a symmetry and a landscape**

$$\Lambda_{\rm CC} \leftrightarrow \rho_{\rm MR} \left(\frac{\delta\rho}{\rho}\right)^3 \ll M_{\rm Pl}^4$$

We do not know yet, but
easy to achieve

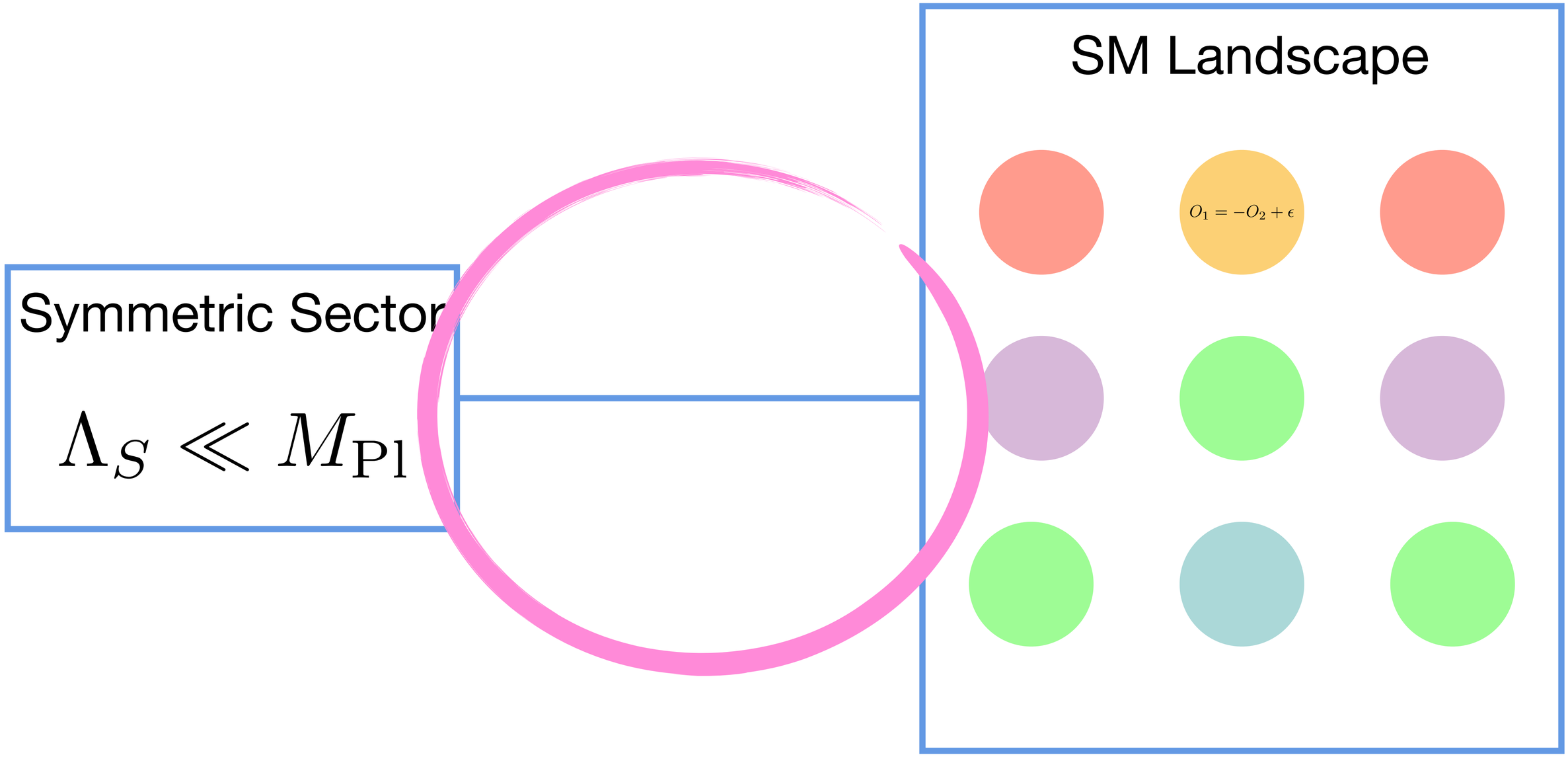
$$v \leftrightarrow \Lambda_{\rm QCD} \ll M_{\rm Pl}$$

Approximate scale invariance



CERN
1971

A change in theoretical perspective
can win (or lose) you
two Nobel Prizes


SM Landscape
Symmetric Sector
$\Lambda_S \ll M_{\rm Pl}$
$O_1 = -O_2 + \epsilon$

EXAMPLE: STATISTICAL

[Dvali, Vilenkin ’03], [Dvali ’04]

$$F_4 = dA_3$$

$$S \supset \int d^4x\sqrt{-g}\left(\frac{F_4^2}{48} + M_{\rm Pl}^2(-1 + \frac{F_4^2}{M_{\rm Pl}^2} + ...)|\phi|^2 + ...\right) + q(\phi)\int d^3\xi A_{\mu\nu\rho}\frac{\partial x^\mu}{\partial\xi^a}\frac{\partial x^\nu}{\partial\xi^b}\frac{\partial x^\rho}{\partial\xi^c}\epsilon^{abc}$$

Large initial “Electric Field”
(Brown-Teitelboim)

$$F_4^2 \sim M_{\rm Pl}^4$$

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Very slow process: requires eternal inflation!

Branes can be spontaneously nucleated (tunnelling)

EXAMPLE: STATISTICAL

[Dvali, Vilenkin ’03], [Dvali ’04]

$$F_4 = dA_3$$

$$S \supset \int d^4x\sqrt{-g}\left(\frac{F_4^2}{48} + M_{\rm Pl}^2(-1 + \frac{F_4^2}{M_{\rm Pl}^2} + ...)|\phi|^2 + ...\right) + q(\phi)\int d^3\xi A_{\mu\nu\rho}\frac{\partial x^\mu}{\partial\xi^a}\frac{\partial x^\nu}{\partial\xi^b}\frac{\partial x^\rho}{\partial\xi^c}\epsilon^{abc}$$

$$\Delta F_4 = q(\phi)$$

Branes can be spontaneously nucleated (tunnelling)

EXAMPLE: STATISTICAL

[Dvali, Vilenkin ’03], [Dvali ’04]

$$F_4 = dA_3$$

$$S \supset \int d^4x\sqrt{-g}\left(\frac{F_4^2}{48} + M_{\rm Pl}^2(-1+\frac{F_4^2}{M_{\rm Pl}^2}+...)|\phi|^2+...\right) + q(\phi)\int d^3\xi A_{\mu\nu\rho}\frac{\partial x^\mu}{\partial\xi^a}\frac{\partial x^\nu}{\partial\xi^b}\frac{\partial x^\rho}{\partial\xi^c}\epsilon^{abc}$$

The scalar mass is scanned

$$\Delta F_4 = q(\phi)$$

Cosmological Constant

Higgs Mass Squared

1. The two quantities are not calculable

2. Scale of gravity?

Theory ~ 10^{120} Experiment

Theory~10^{34} Experiment

Cosmological Constant

Higgs Mass Squared

1. The two quantities are not calculable

2. Scale of gravity?

3. Planck Scale = QFT Mass Scale?

Theory ~ 10^{120} Experiment

Theory~10^{34} Experiment

HIERARCHY 102

[Arkani-Hamed, RTD, Kim ’20]

Does anything change in the SM as we vary $\langle h \rangle$?

HIERARCHY 102

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1. Obviously the spectrum

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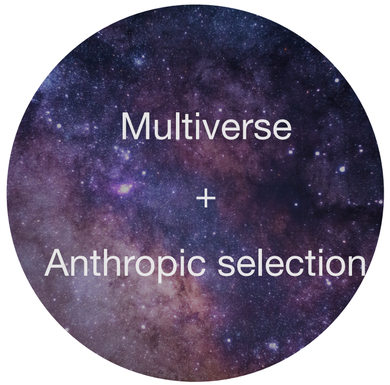


HIERARCHY 102

Does anything change in the SM as we vary $\langle h \rangle$?

$$\xi \phi \mathrm{Tr}\left[G\widetilde{G}\right]$$

Dvali, Vilenkin ‘01
Graham, Kaplan, Rajendran ‘15
Geller, Hochberg, Kuflik ’18
…

EXAMPLE: STATISTICAL

[Giudice, McCullough, You ’21]

Scalar dominated by quantum dynamics during inflation

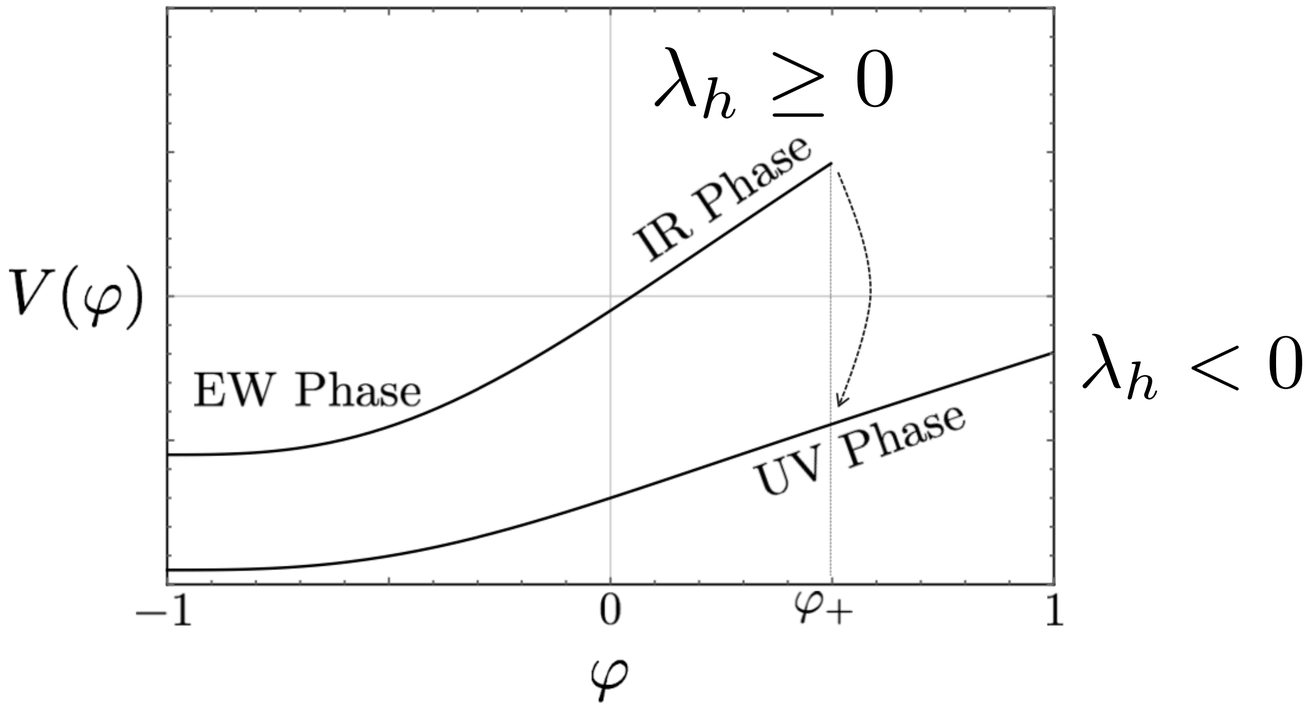
Solve Fokker-Planck Equation

In most gauges you will find that the volume is dominated by quantum dynamics for critical points of some potentials

(measure problem)

EXAMPLE: STATISTICAL

[Giudice, McCullough, You ’21]



Can select Higgs vev corresponding to zero quartic

EXAMPLE: DYNAMICAL

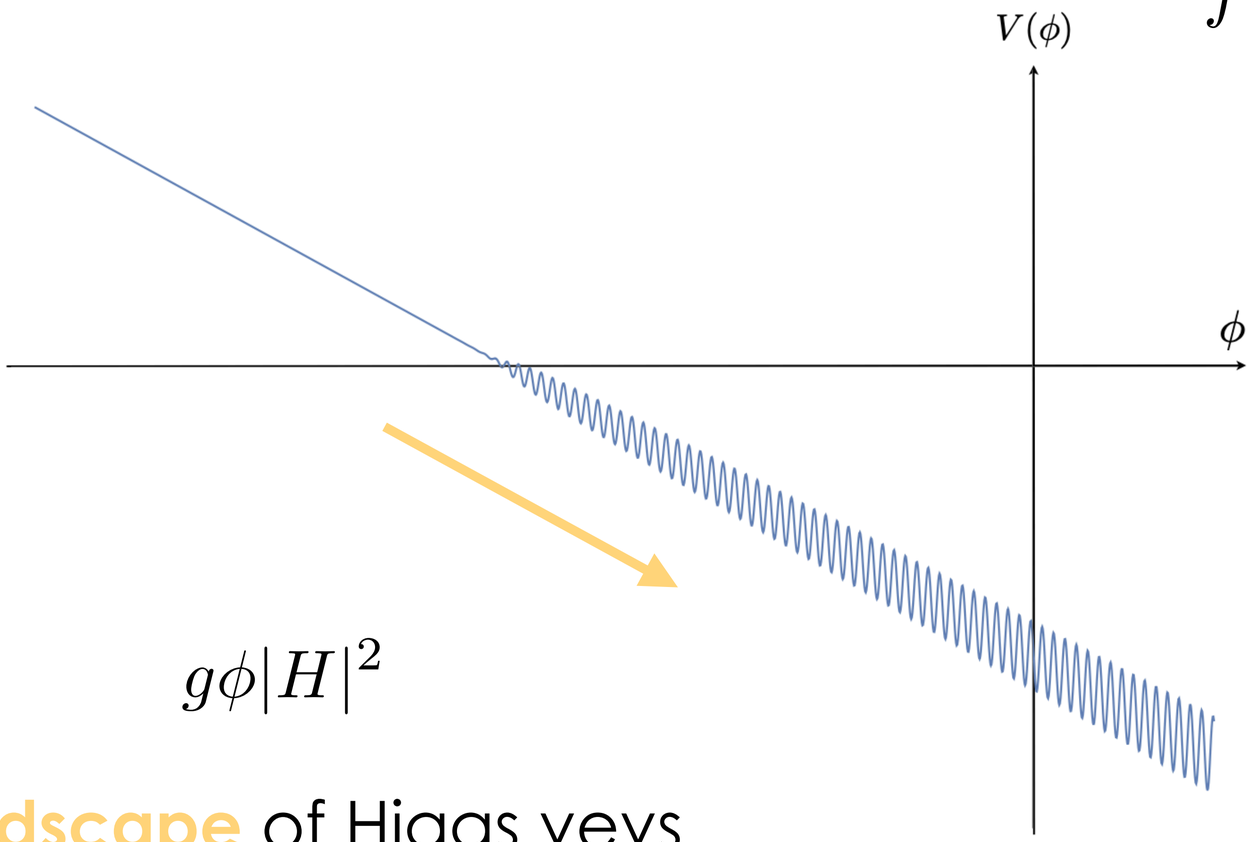
[Graham, Kaplan, Rajendran ’15],

$$V(\phi) = g\phi + ... + (M^2 + g\phi + ...)|H|^2 + \frac{\phi}{f} G\tilde{G}$$

EXAMPLE: DYNAMICAL

[Graham, Kaplan, Rajendran '15],

$$V(\phi) = g\phi + ... + (M^2 + g\phi + ...)|H|^2 + \frac{\phi}{f} G\tilde{G}$$



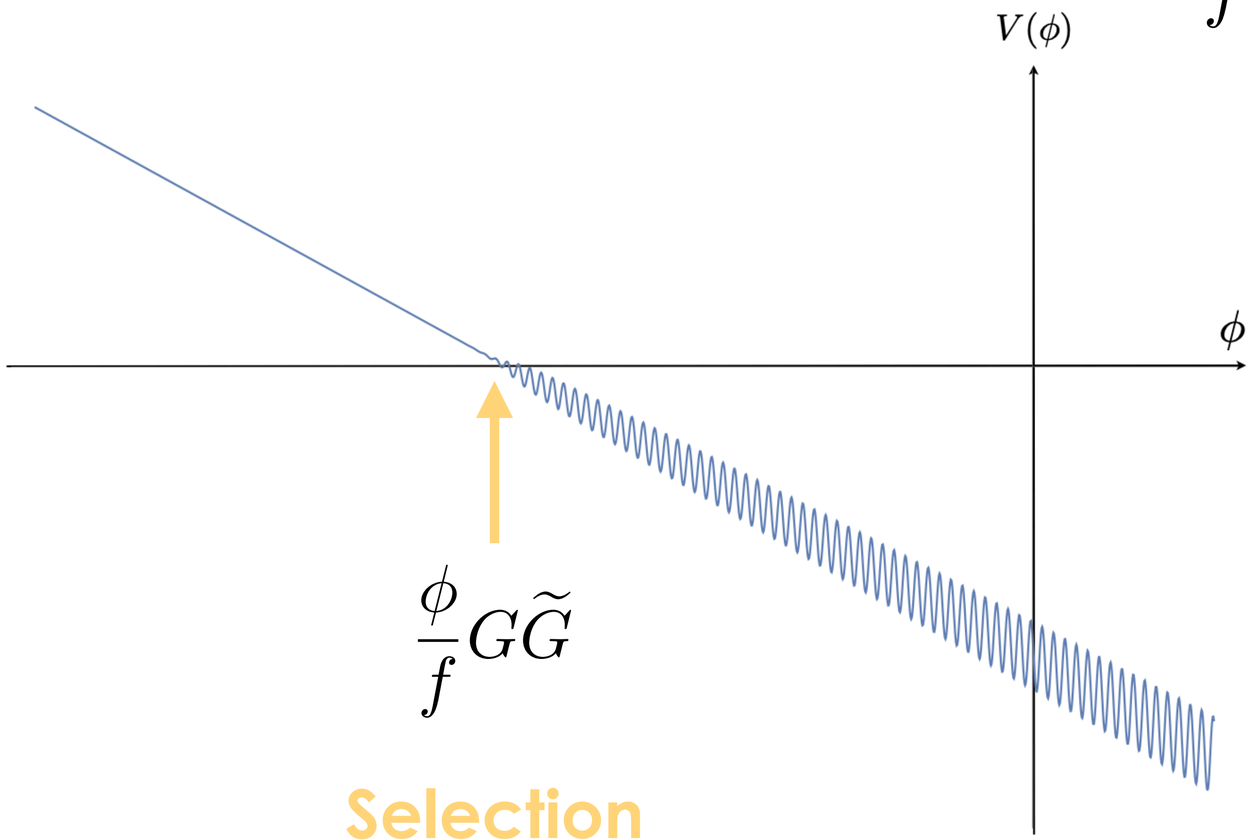
$g\phi|H|^2$

Landscape of Higgs vevs

EXAMPLE: DYNAMICAL

[Graham, Kaplan, Rajendran ’15],

$$V(\phi) = g\phi + ... + (M^2 + g\phi + ...)|H|^2 + \frac{\phi}{f} G\tilde{G}$$



Selection

EXAMPLE: DYNAMICAL

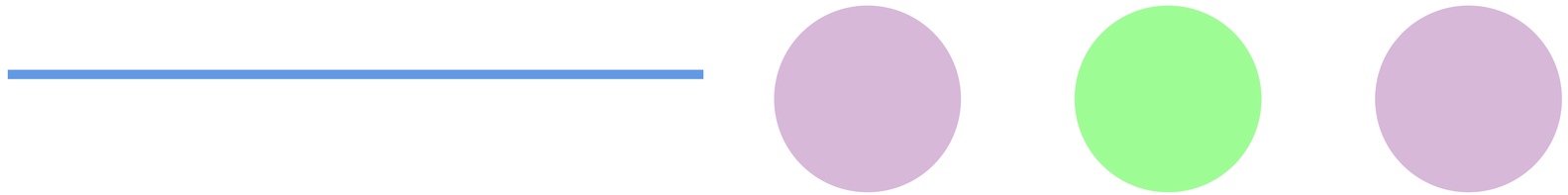
[Graham, Kaplan, Rajendran '15],

$$V(\phi) = g\phi + ... + (M^2 + g\phi + ...)|H|^2 + \frac{\phi}{f} G\tilde{G}$$

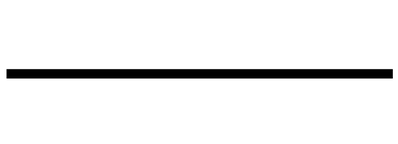
Symmetric Sector

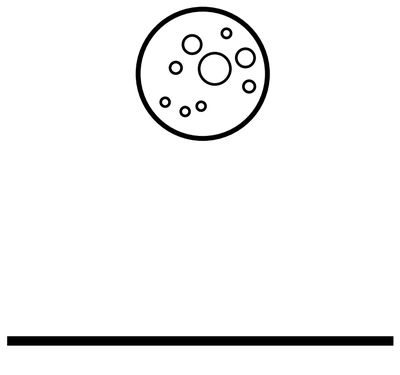
$$g \ll M_{\rm Pl}^3$$

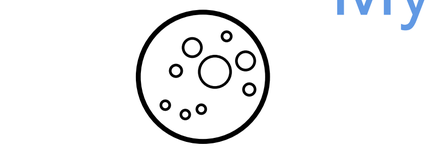
SM Landscape



ϕ $\phi G\tilde{G}$ $g\phi|H|^2$


Planck
String
SUSY
SM


Mysterious
QG
Blob
SUSY
SM


Mysterious
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