

Challenging the CDM paradigm: Constraining DM properties with CMB data

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In collaboration with
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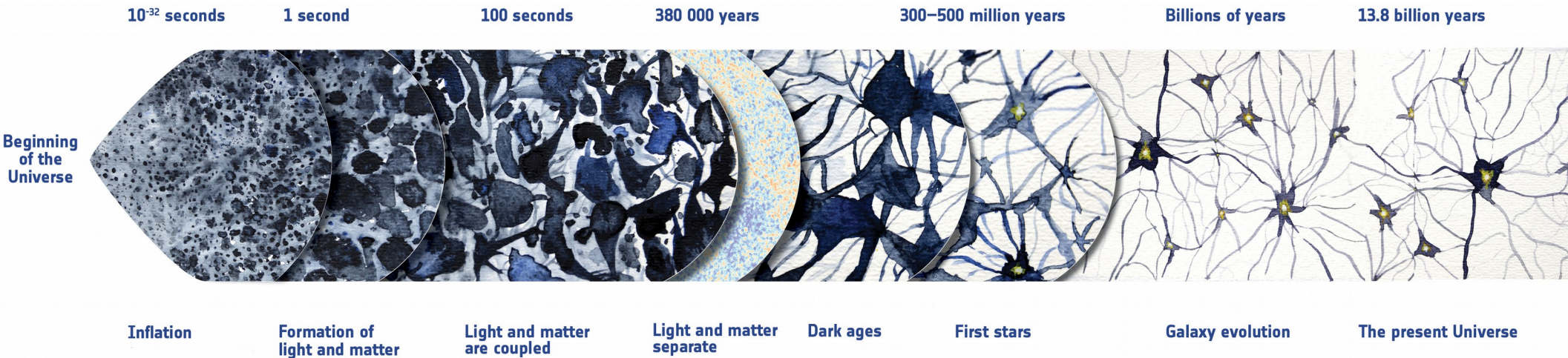
The research leading to these results has received funding from the European Research Council under the European Union's Seventh Framework Programme (FP7/2007–2013)/ERC Grant Agreement No. 617656 "Theories and Models of the Dark Sector: Dark Matter, Dark Energy and Gravity."



Atelier Théorie, Univers et Gravitation
@ IHP, 15/12/2021

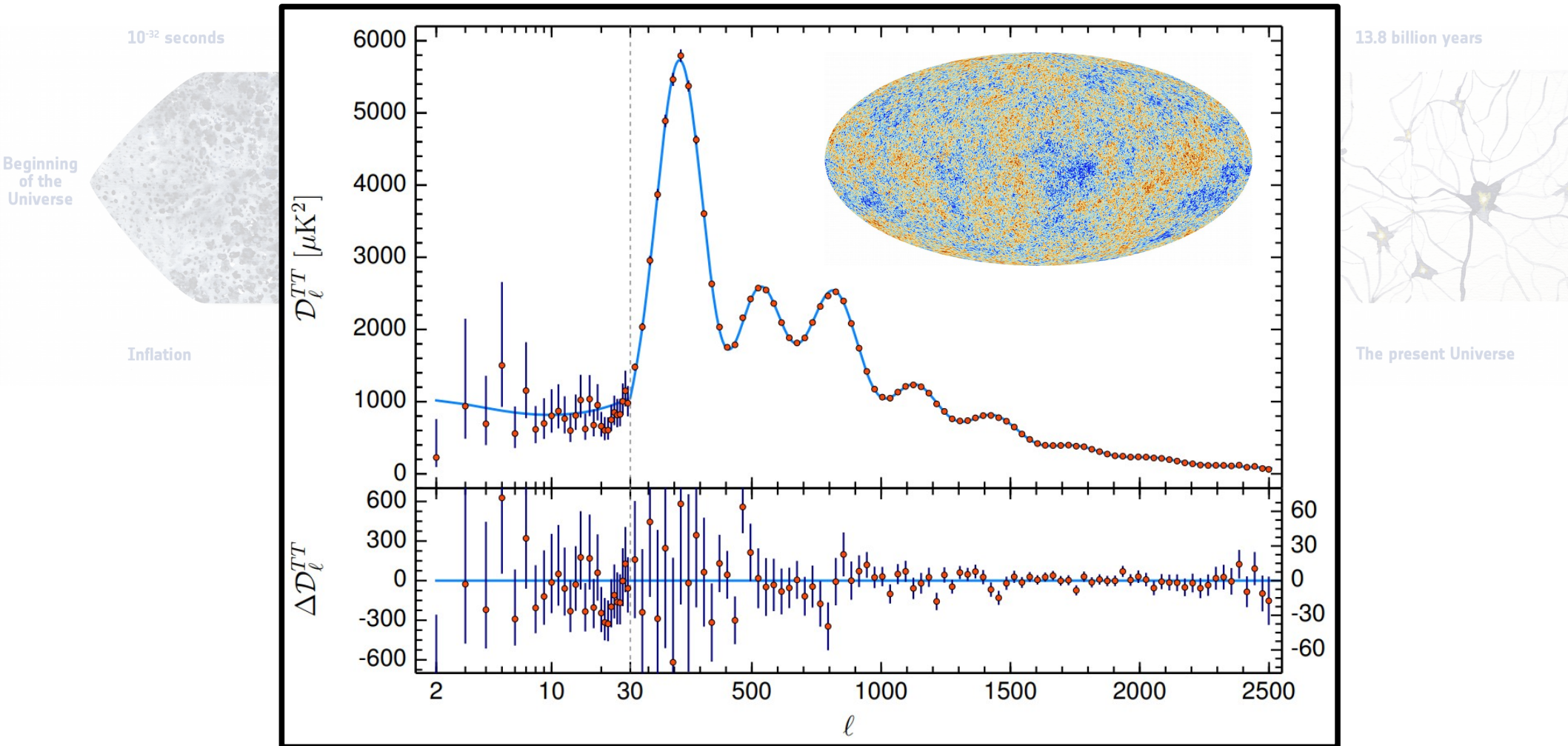
The standard model of cosmology

- The Λ CDM paradigm: a (relatively) simple model, with many successes...



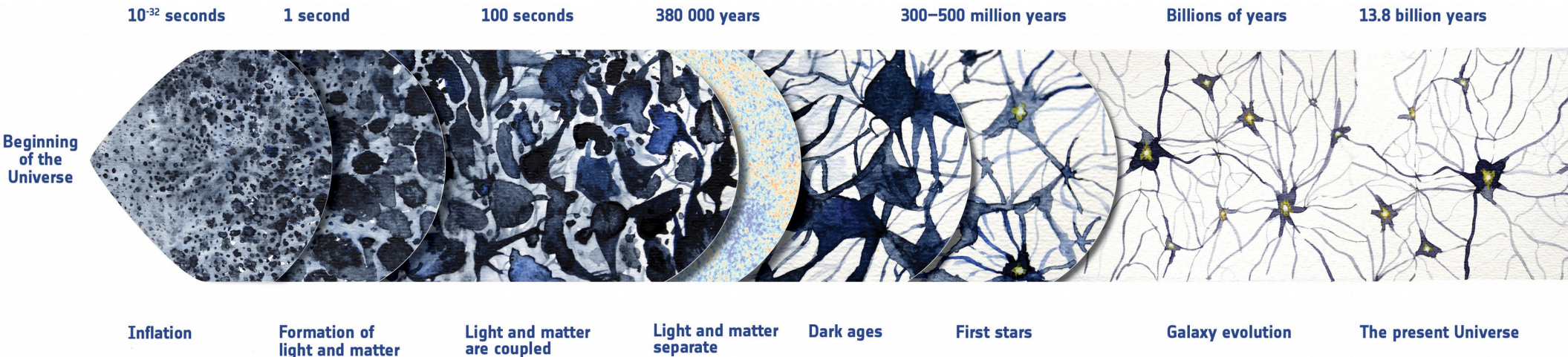
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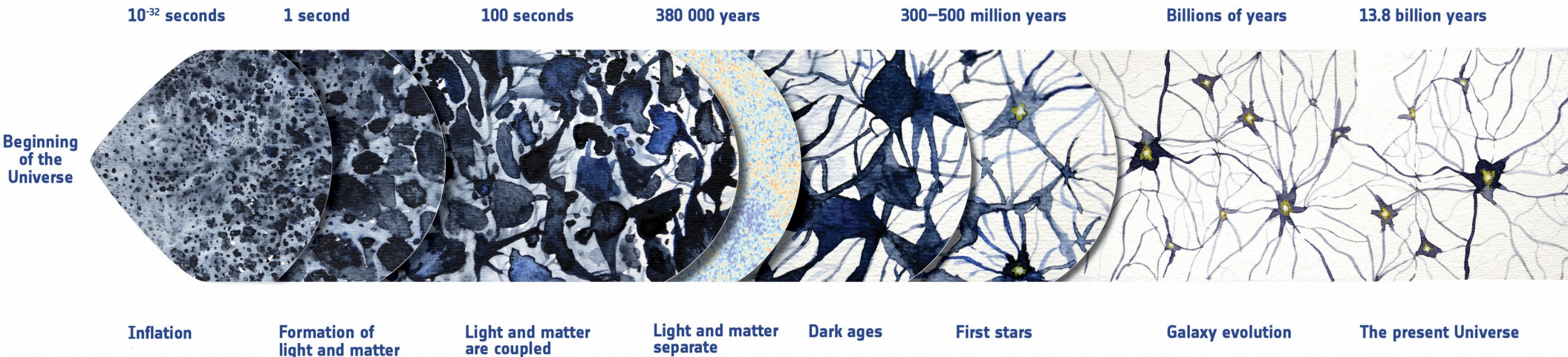
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- ... but rests on some pillars that are “shrouded in darkness”:
 - Primordial Universe, inflation
 - Dark matter (“CDM”)
 - Dark ages & reionisation
 - Dark energy (“ Λ ”)
- ... and is shaken by some persistent tensions :
 - H_0 discrepancies
 - σ_8 tensions
 - ISW excess
 - CMB “anomalies”

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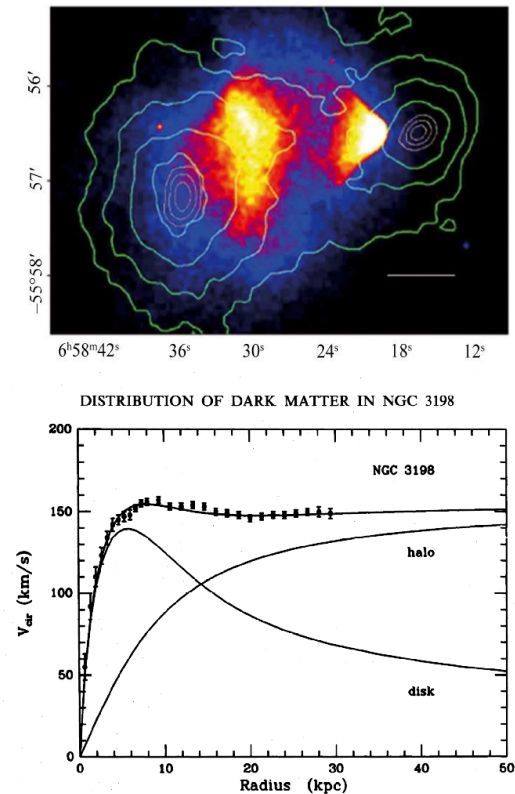
Cold dark matter, hot questions

- Is it really there ?

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- Direct detection:
 - Colliders
 - Nuclear recoils
 - Inconclusive so far
- Indirect detection:
 - Late gravitational effects (rot. curves, Bullet cluster)



Cold dark matter, hot questions

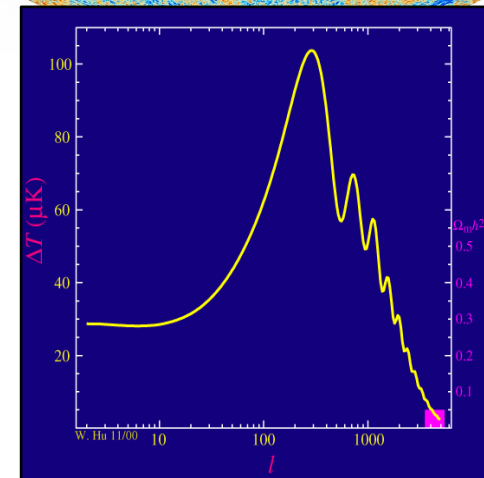
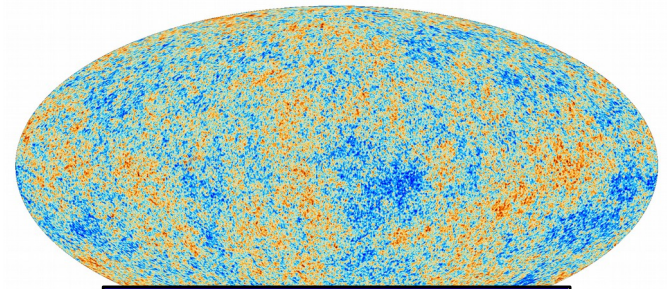
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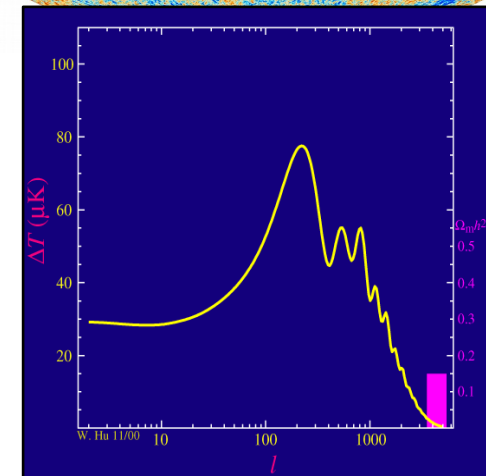
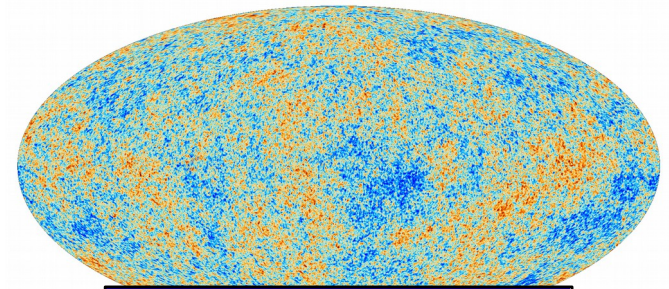
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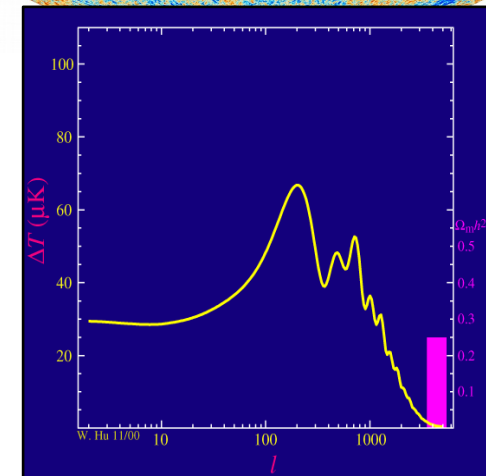
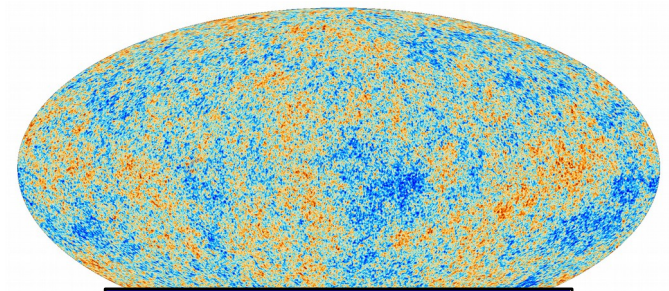
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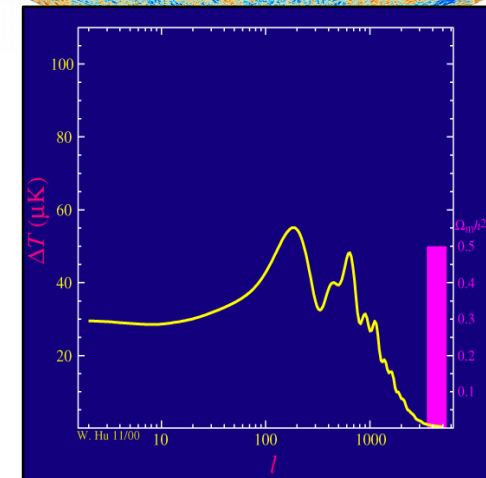
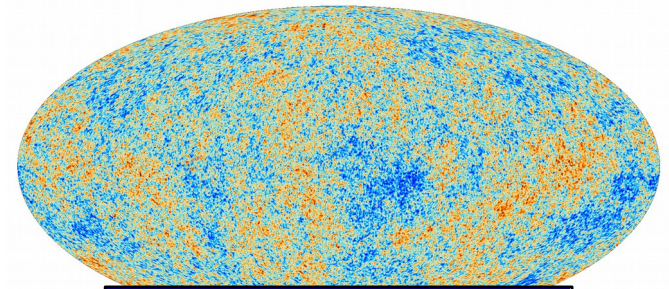
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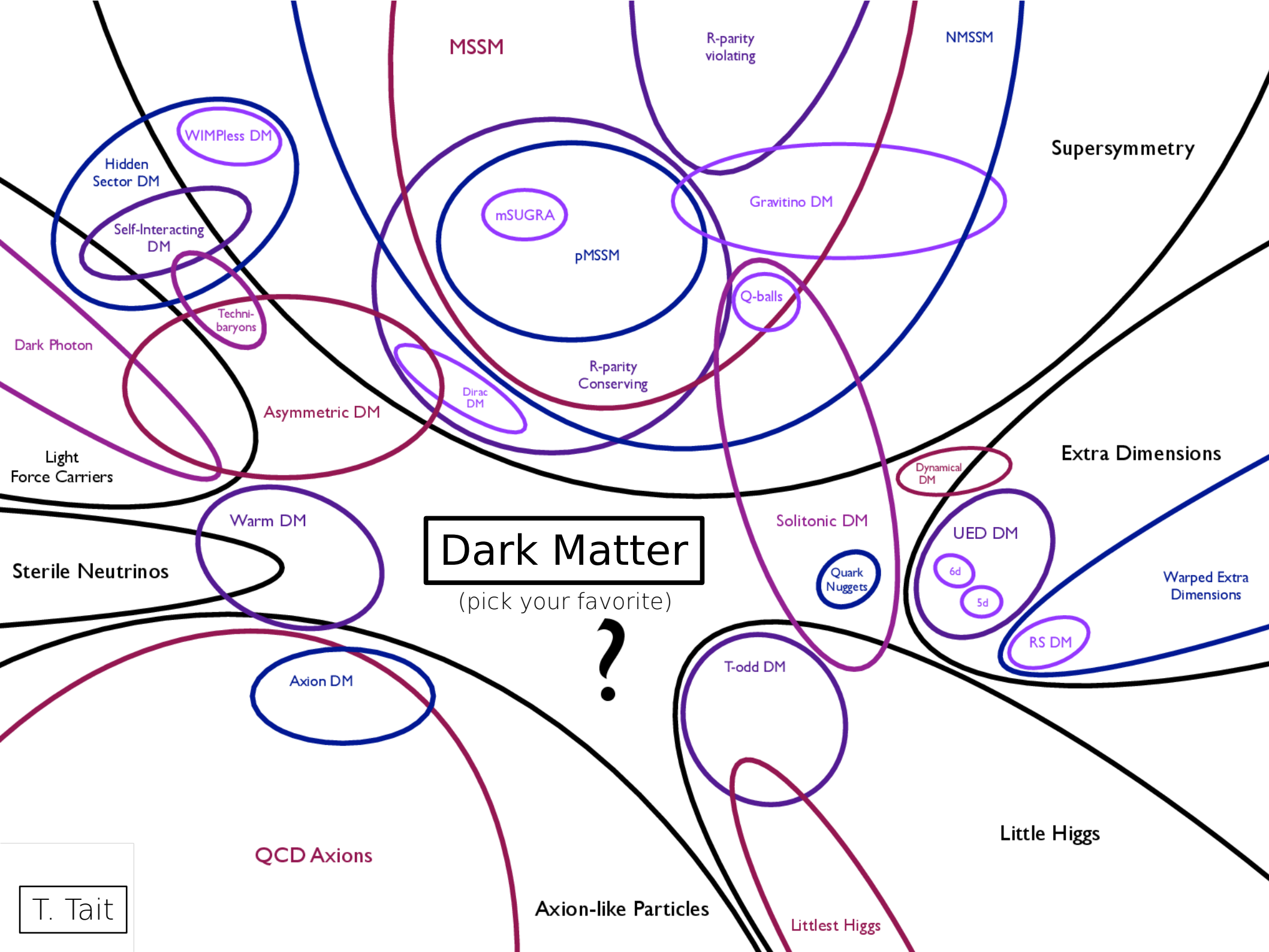
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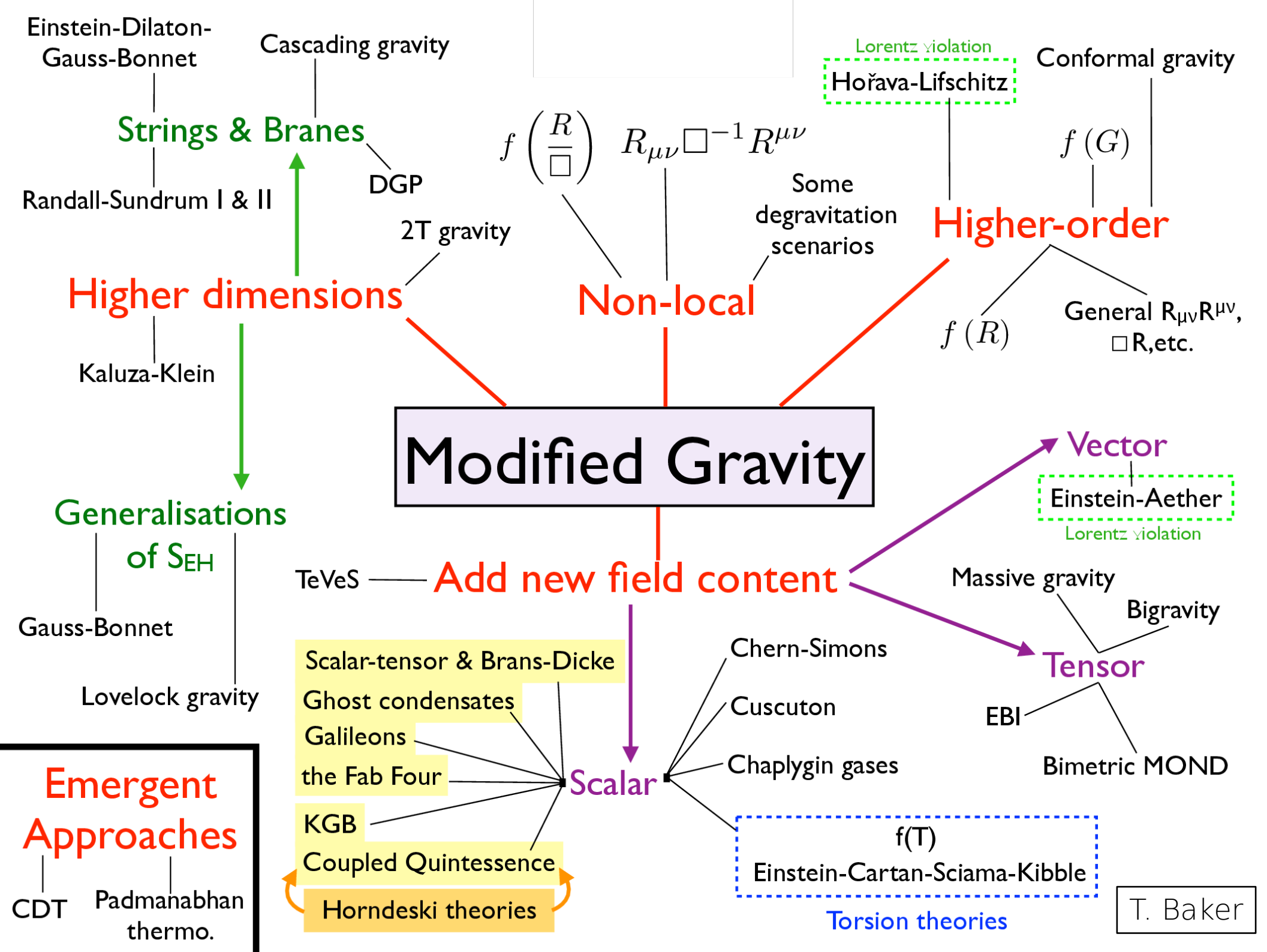
- Is it really there ?
- If yes, what it is made of ?

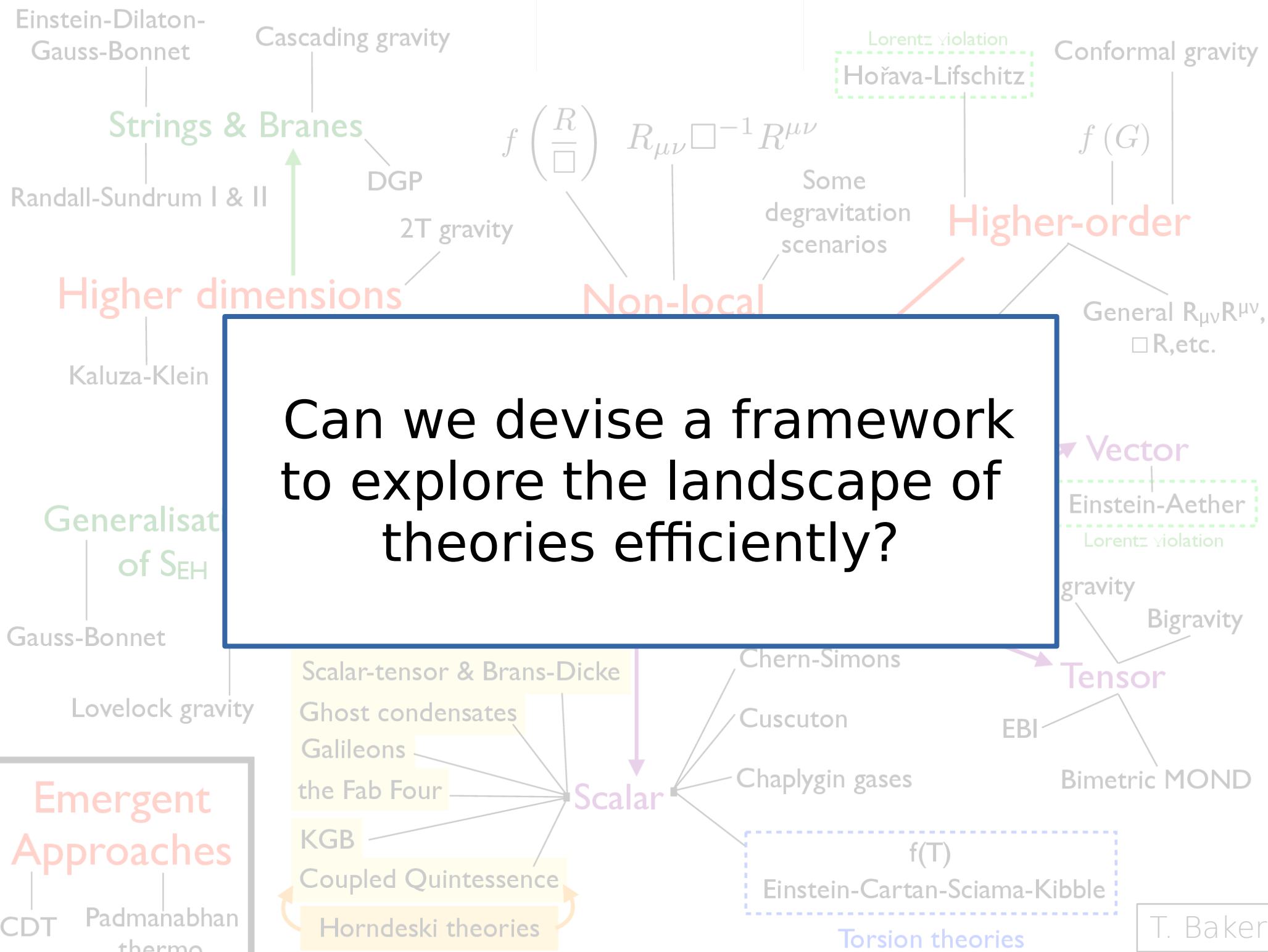


Dark Matter

(pick your favorite)







DM as a (more) general fluid

$$T_{\mu\nu} = \rho u_\mu u_\nu + P(g_{\mu\nu} + u_\mu u_\nu) + \Sigma_{\mu\nu}$$

- CDM: non-interacting, pressureless perfect fluid

$$\omega_c \equiv \Omega_c h^2 = 0.1200 \pm 0.0012 \quad (\text{Planck 2018 results. VI})$$

$$< 1.3\% \text{ isocurv. IC contribution} \quad (\text{Planck 2018 results. X})$$

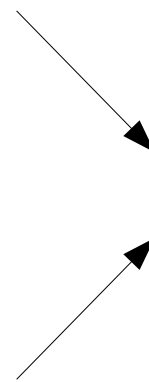
- But general fluid has **pressure**...

e.g. ultralight axions quantum pressure

- ...and non-zero **shear**

e.g. free-streaming warm dark matter
(sterile neutrinos, ...)

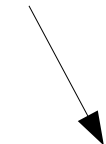
e.g. CDM + EFTofLSS



Generalized Dark Matter (GDM, Hu 1998)

- Defined for FLRW, linear perturbations
- Background: (non-zero) equation of state $w(\tau)$
- Perturbations: sound speed $c_s^2(\tau, k)$ & viscosity $c_{vis}^2(\tau, k)$
- Standard eqs. for density contrast & velocity divergence
- Continuity & Euler eqs. : requires closure equations (here by Hu):

$$\Pi_g \equiv \frac{\delta P_g}{\bar{\rho}_g} = c_a^2 \delta_g + (c_s^2 - c_a^2) \hat{\Delta}_g^{\text{rest frame}} \quad \dot{\Sigma}_g = -3\mathcal{H}\Sigma_g + \frac{4}{1+w} c_{vis}^2 \hat{\Theta}_g^{\text{Newt.}}$$


$$\left(c_a^2 = \frac{\dot{P}_g}{\dot{\rho}_g} = w - \frac{\dot{w}}{3\mathcal{H}(1+w)} \right)$$

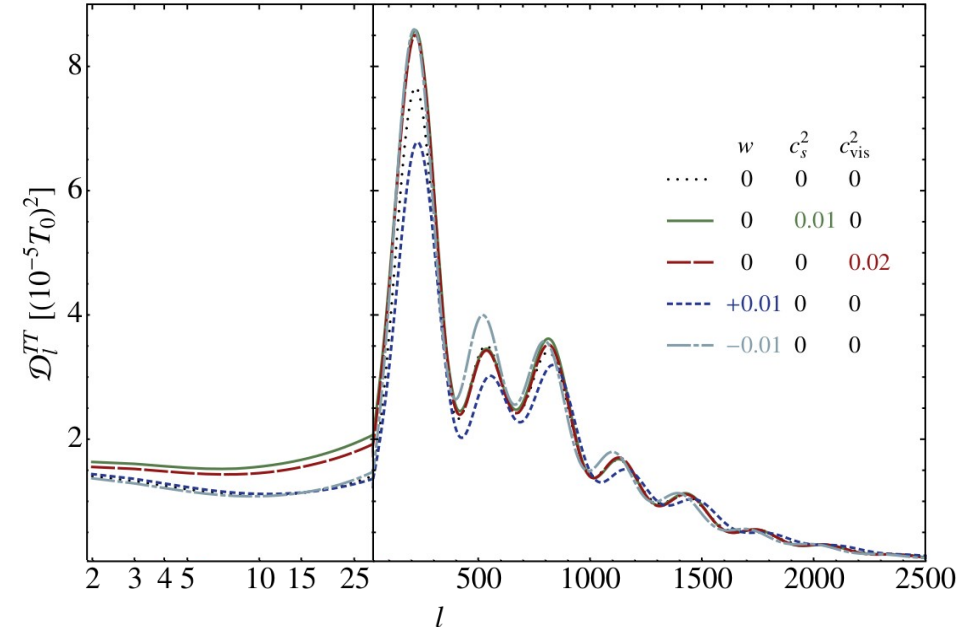
GDM phenomenology

- Equation of state:

$$\dot{\rho} = -3H\rho(1 + w)$$

$$a^3 \bar{\rho} \propto \omega_0 (1 + 3w \ln(1 + z)) \text{ for constant } w$$

- angular diam. dist., changes peak positions
- early rad/matter ratio, changes peak heights



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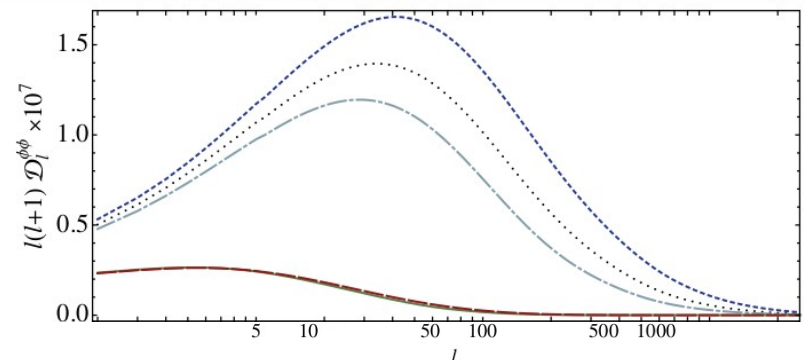
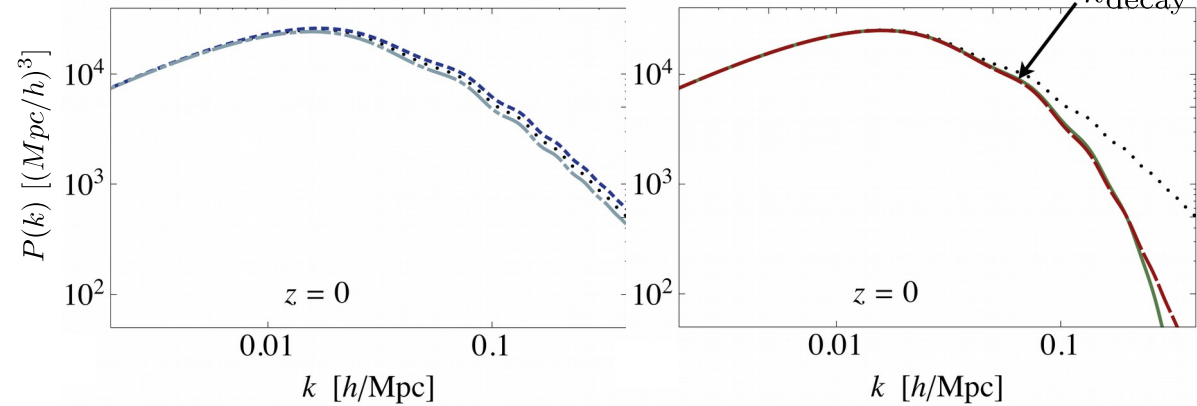
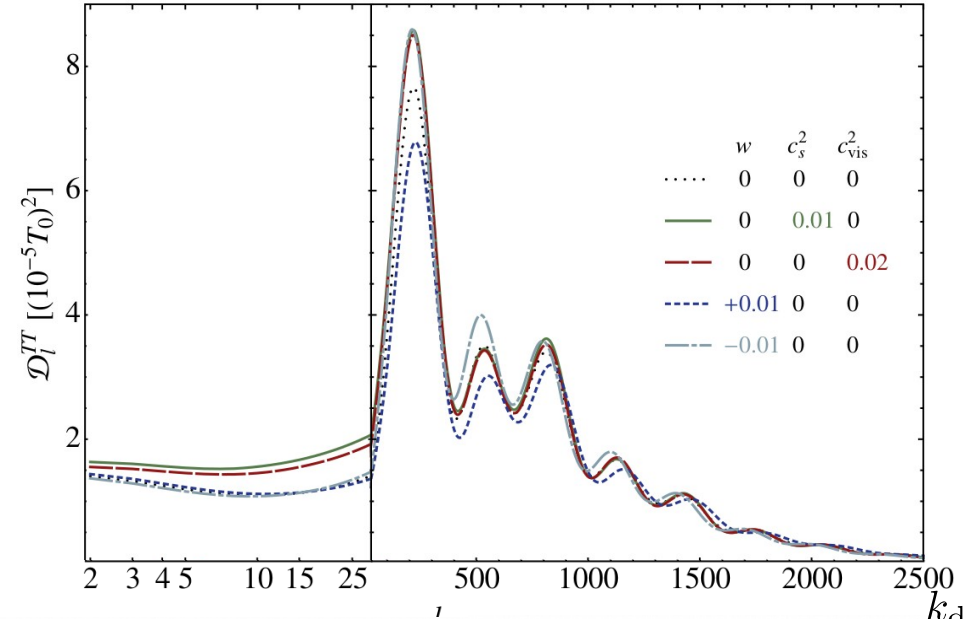
- angular diam. dist., changes peak positions
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- Sound speed & viscosity:

$$k_{decay}^{-1}(\tau) \equiv \tau \sqrt{c_s^2 + \frac{8}{15} c_v^2}$$

↑
(expected degeneracy)

- potentials decay below k_{decay}



Relating GDM to realistic theories

Particles (Boltzmann equation)

- Freely streaming **warm dark matter**

Armendariz-Picon, Neelakanta, JCAP 2014

- Specific models, like **self interacting massive neutrinos** and **dark atoms + dark photons**

Oldengott et al JCAP 2015
Cyr-Racine, Sigurdson, PRD 2013

Fields (effective or fundamental)

- **Axion condensates.**

Sikivie, Yang, PRL 2009
Hlozek, et al, PRD 2015

- **Effective theory of large scale structure:** Landau-Lifshitz type energy momentum tensor for **CDM** due to **small scale nonlinearities**

Baumann et al, JCAP 2012

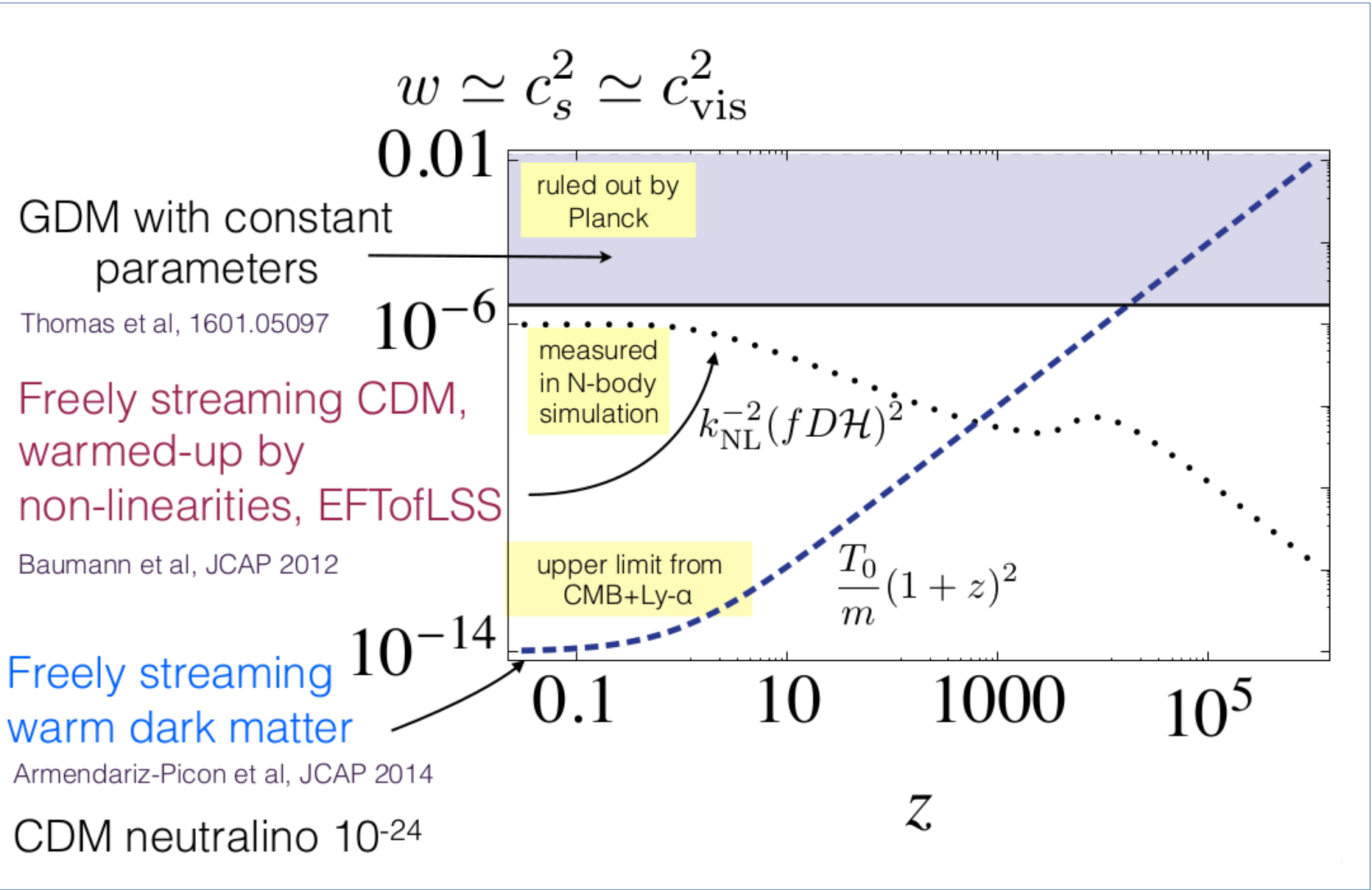
- **K-essence** and more general **constrained-norm scalar field theories.**

Scherrer, PRL 2004
Ballesteros, JCAP 2015

Fluids (imperfect, or coupled perfect)

Kopp et al, 1605.00649

Constant w , c_s^2 , and c_v^2 constraints



(courtesy of M. Kopp)²¹

Ingredients for constraining GDM

- Theoretical predictions:
custom modified version of public code CLASS,
solving for arbitrary w , c_s^2 , and c_v^2
- Datasets:
 - Planck 2015 low/high- l T/E/B data + lensing
 - H_0 (Riess) measurement
 - Assortment of BAO data
- Sampling:
Affine Invariant Markov chain Monte Carlo
Ensemble sampler

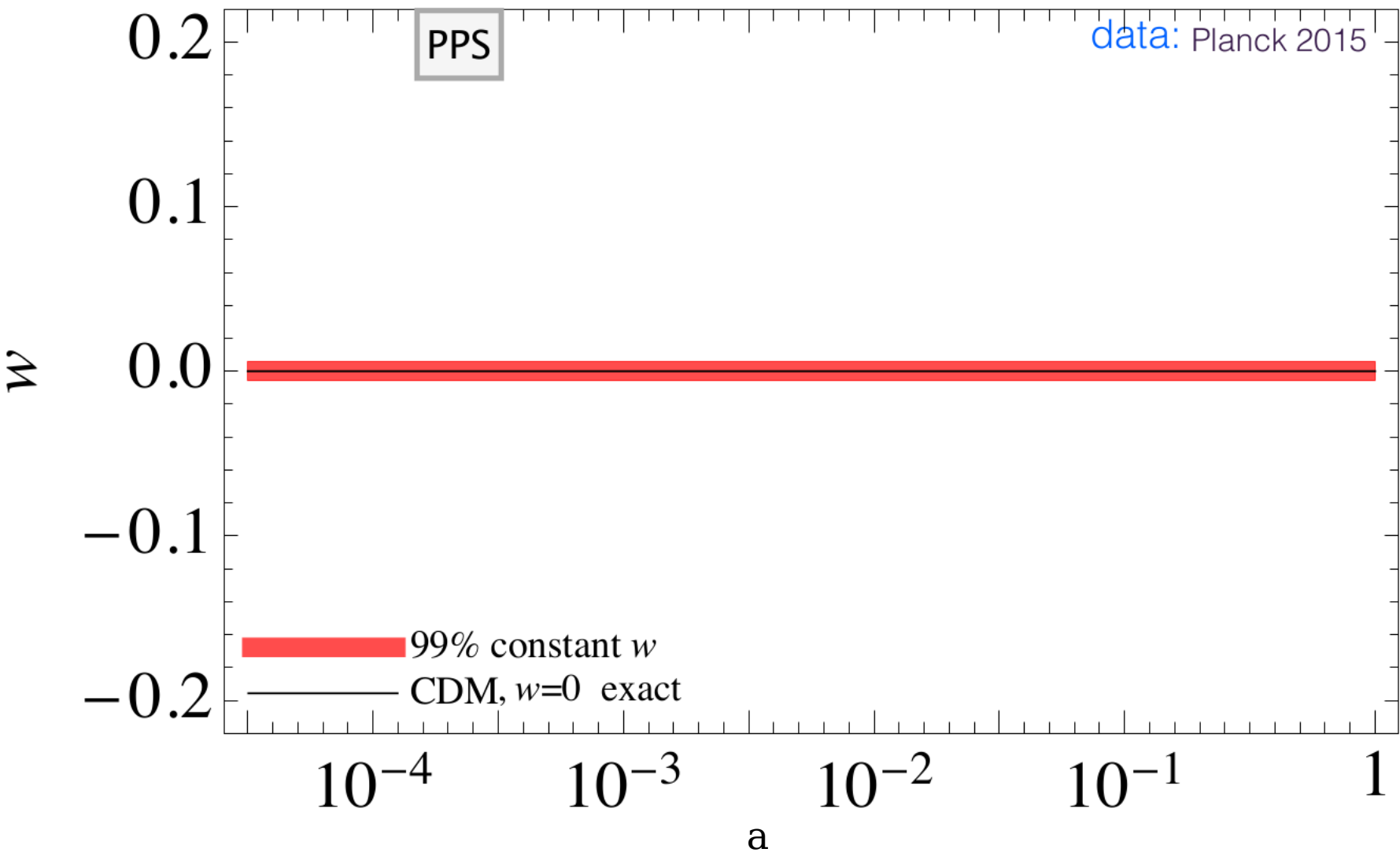
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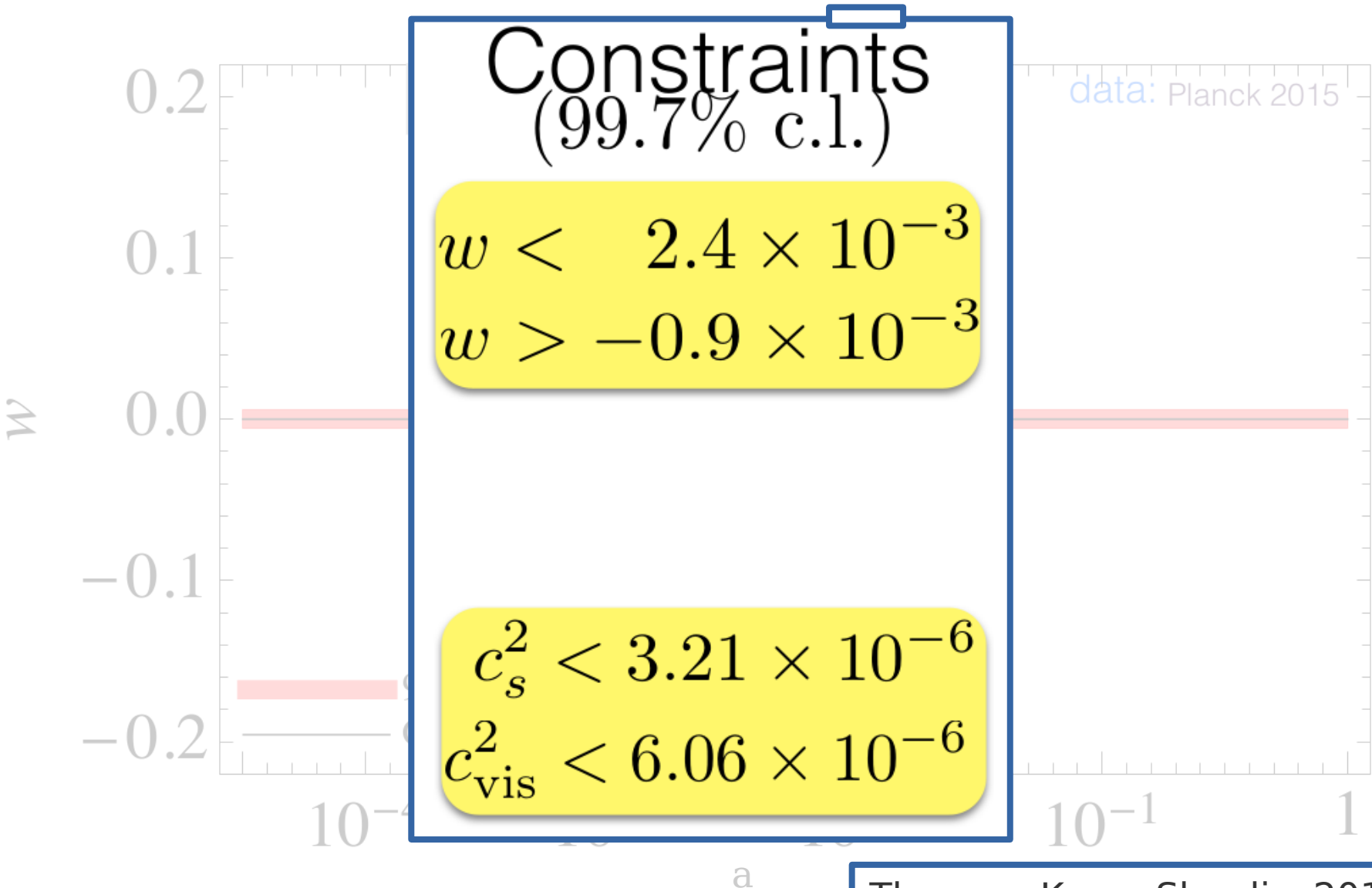
- Data
- Pla
- H₀
- Ass
- Sar

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Constant w , c_s^2 , and c_v^2 constraints

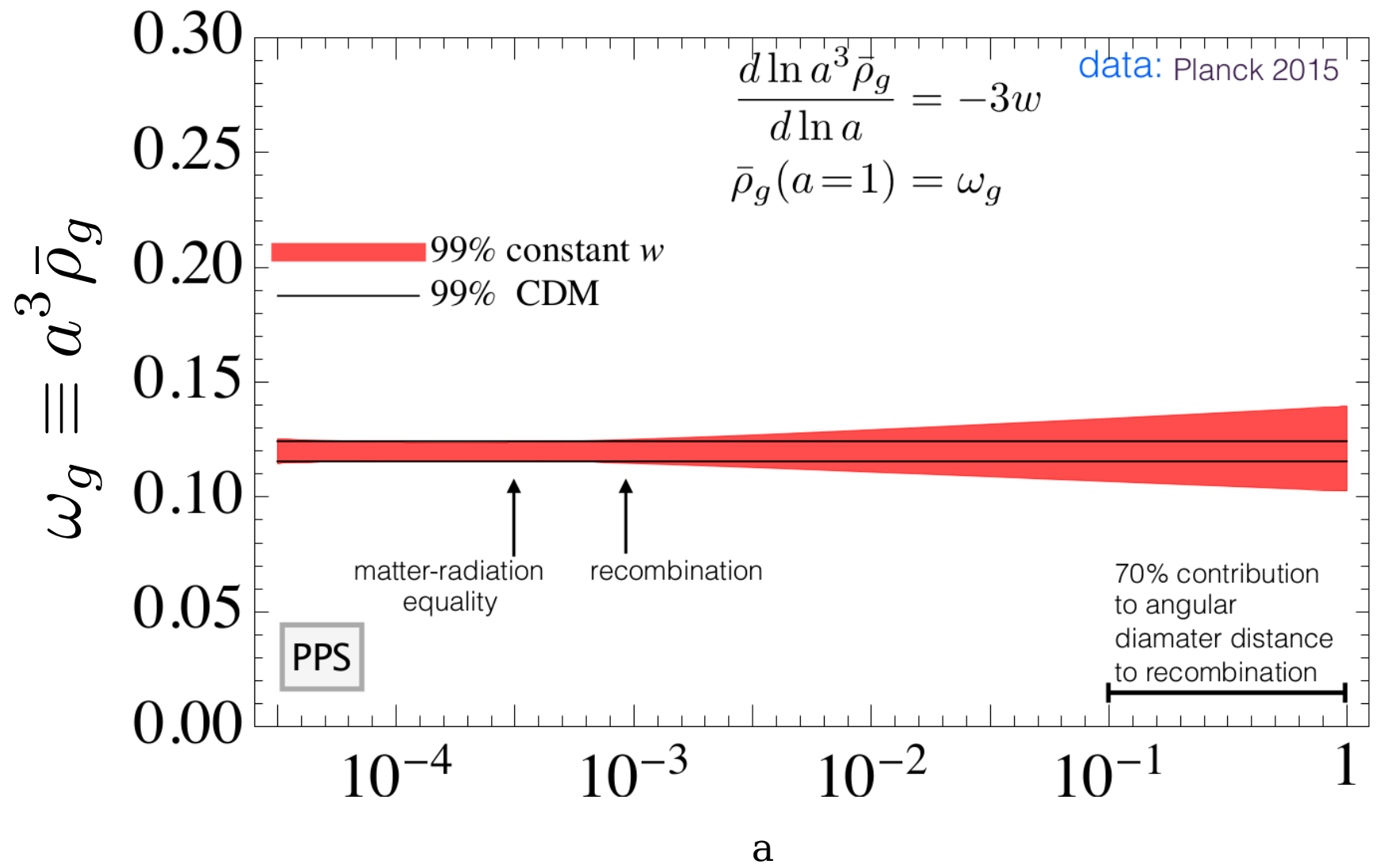


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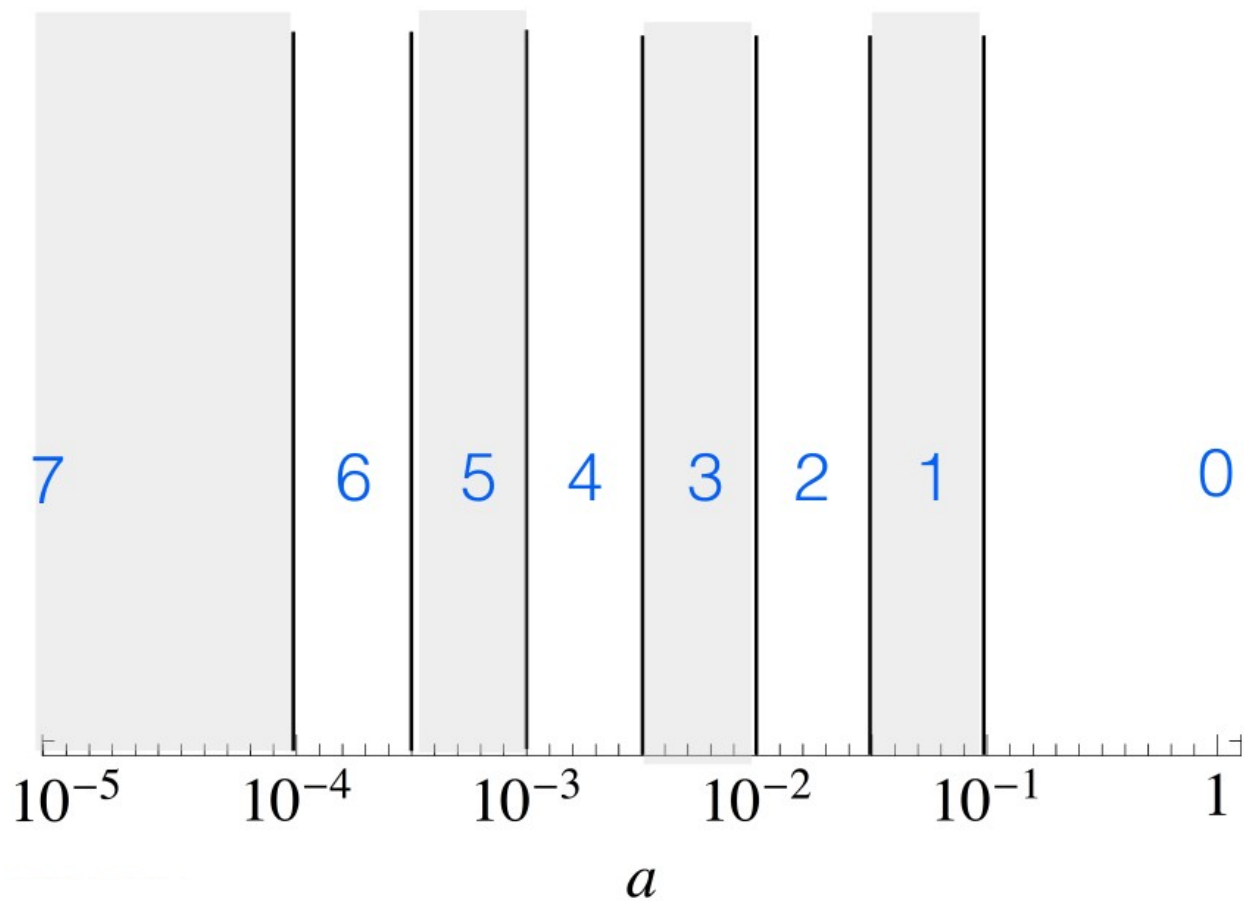
Thomas, Kopp, Skordis, 2016,
arXiv:1601.05097

Constant w , c_s^2 , and c_v^2 constraints



Binned $w(a)$, $c_s^2 = c_v^2 = 0$ constraints

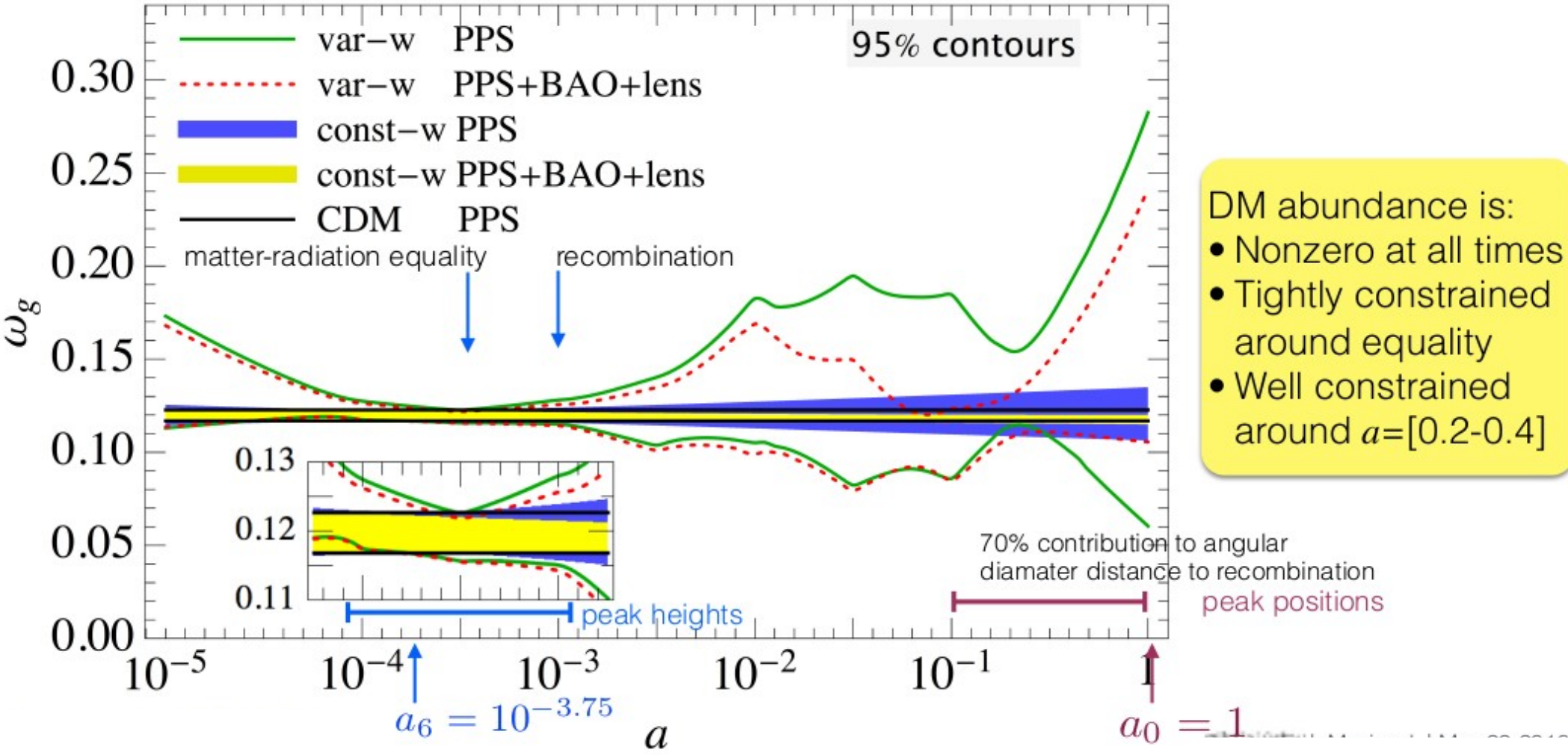
Kopp, Thomas, Skordis, Ilić, 2018, arXiv:1802.09541



8 w bins

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Kopp, Thomas, Skordis, Ilić, 2018, arXiv:1802.09541



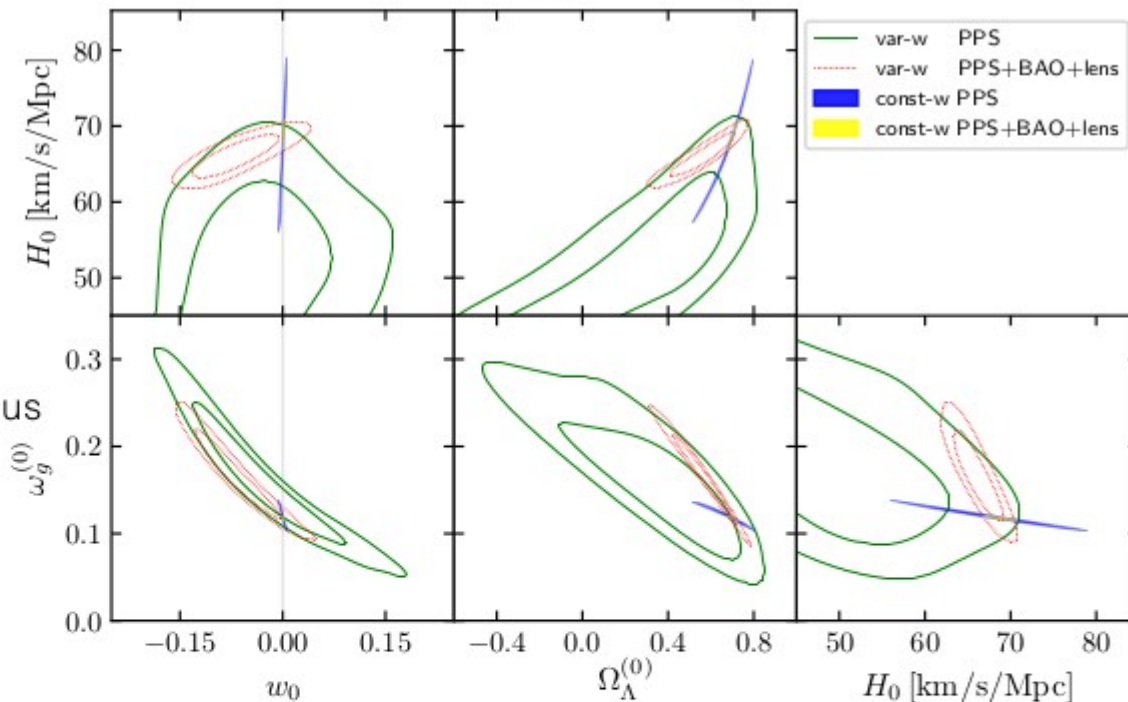
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68% and 95% contours of 2D marginalised posteriors

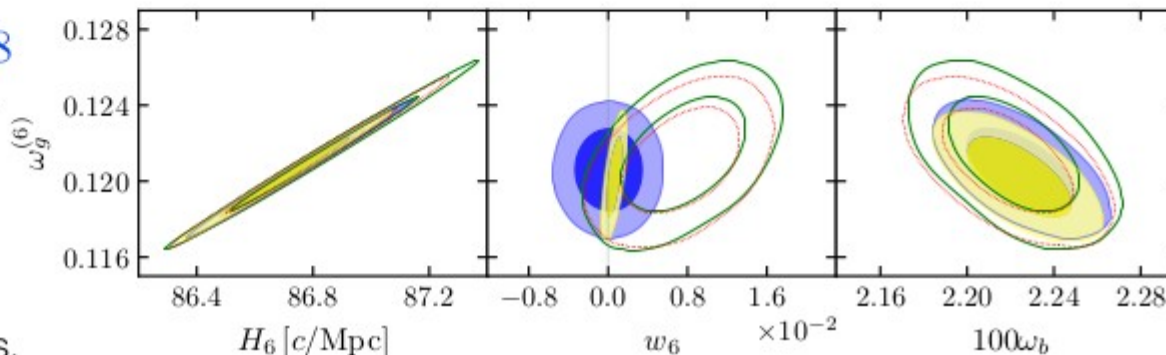
$a_0 = 1$

- Loss of constraining power at late times in the var-w model since the late Universe behaviour disassociates from the early Universe.
- Adding BAO or HST data thus strongly affects contours
- ω_g is anticorrelated with Ω_Λ since combination of CDM and Λ can be modeled by wDM.



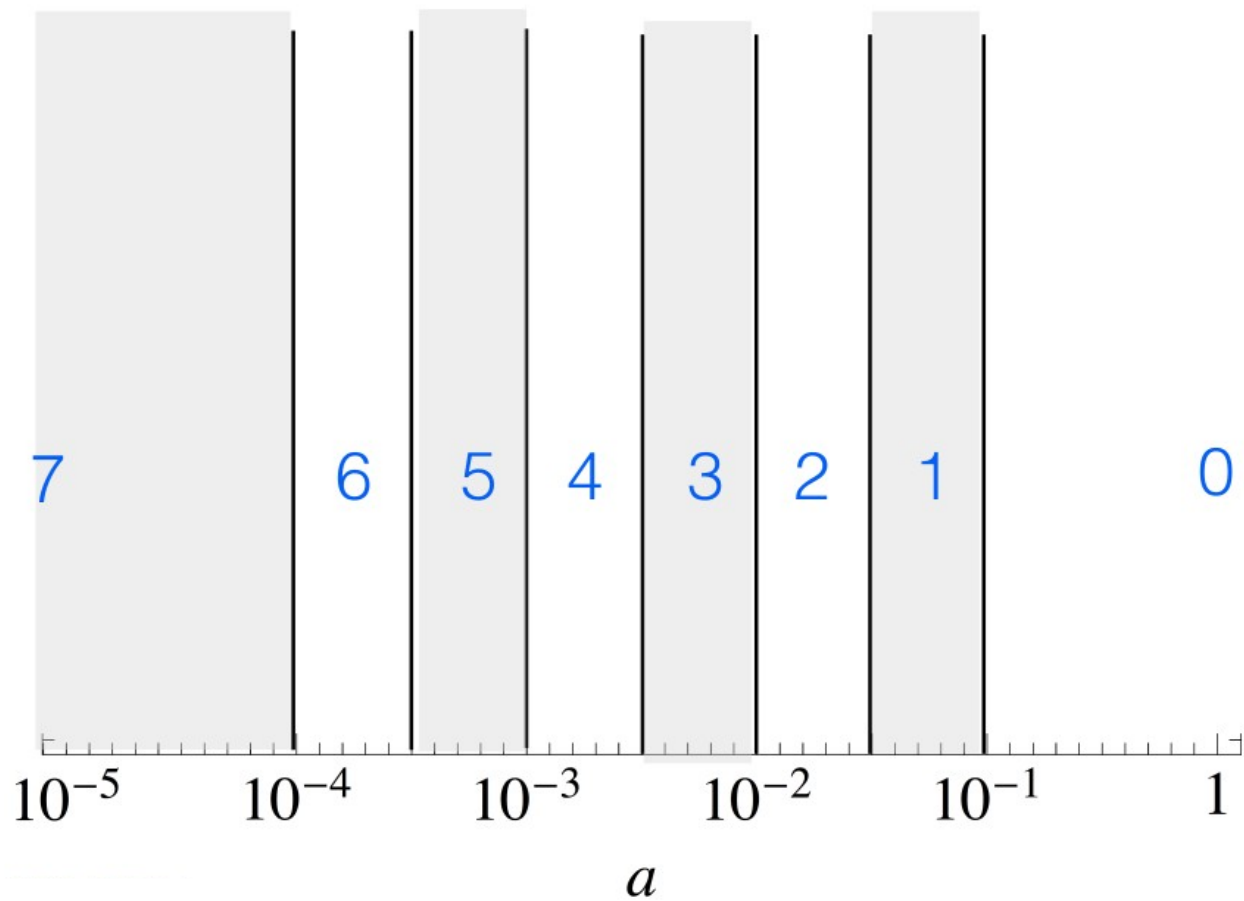
$a_6 = 10^{-3.75} = 0.00018$

- Strong constraining power at early times. Nearly as good as const w or CDM
- ω_g is better constrained than w . Causes correlations.



Binned $w(a)$, $c_s^2(a)$, and $c_v^2(a)$ constraints

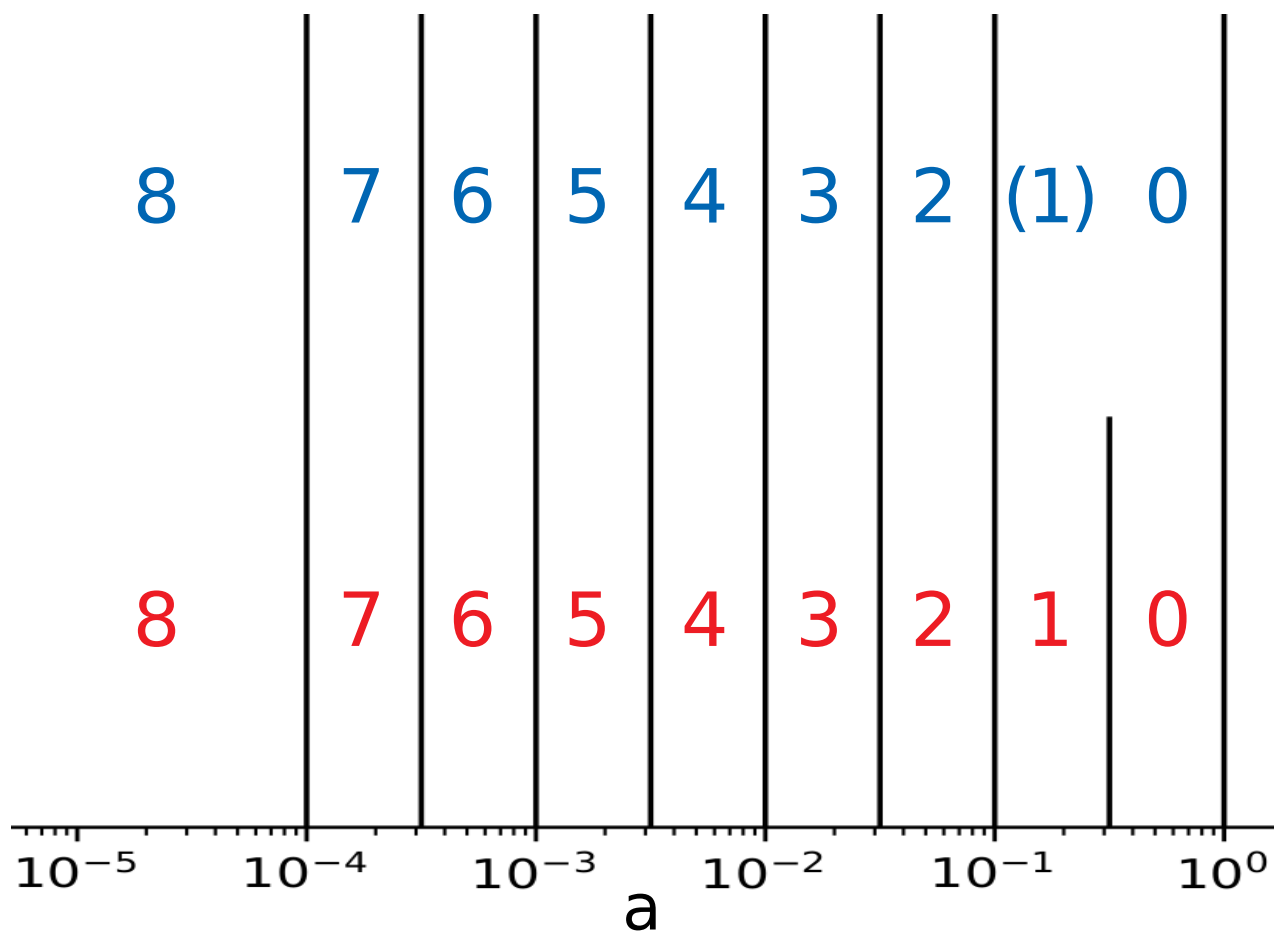
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Ilić et al., 2020, arXiv:2004.09572

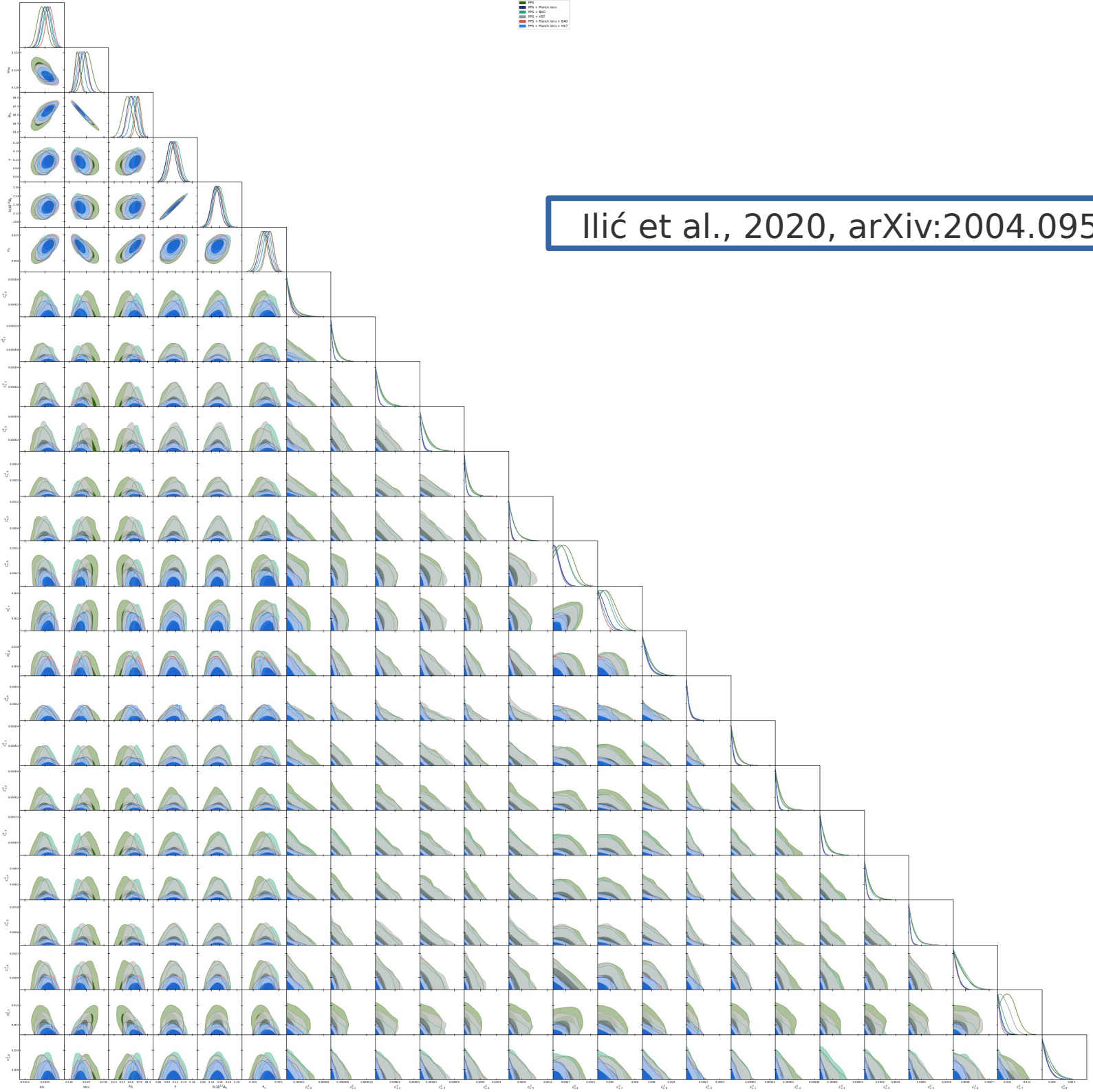


9 c_s^2 , and c_v^2 bins

+ 8 w bins

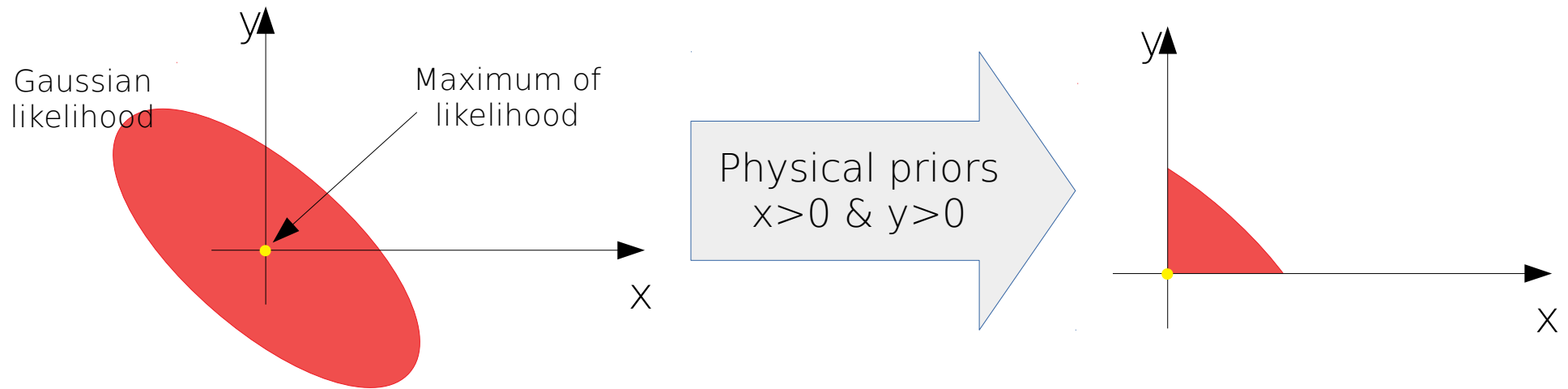
or

$w=0$

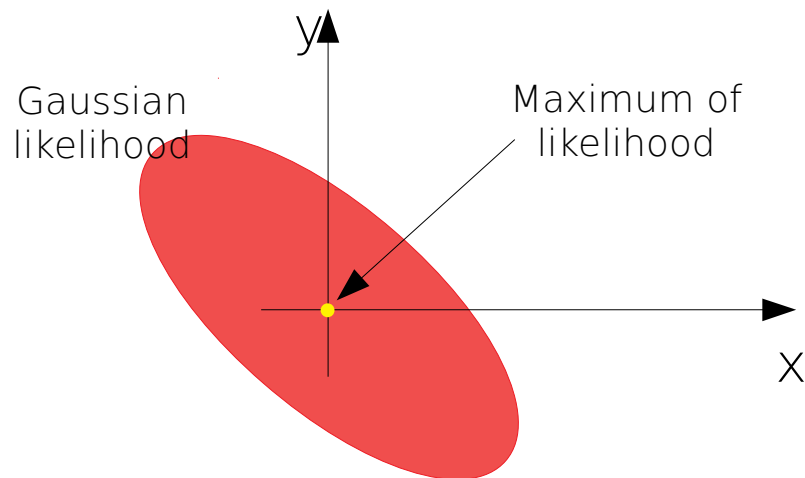


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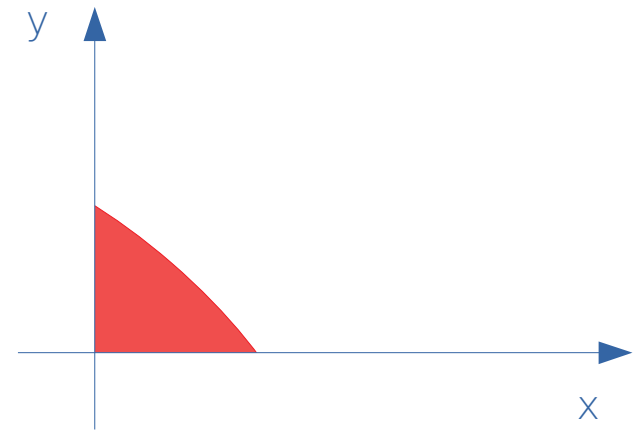
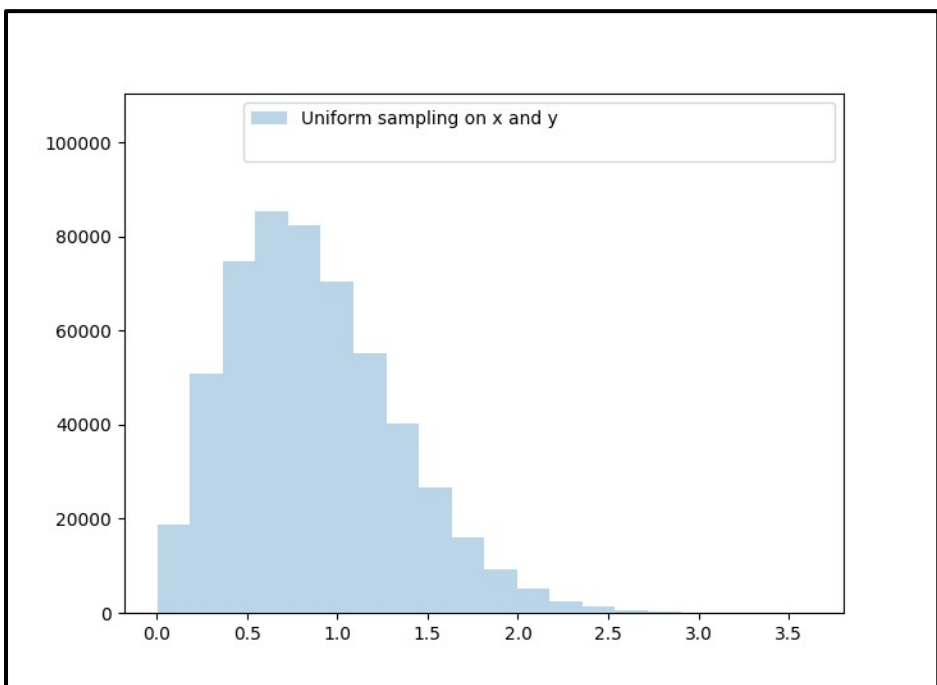
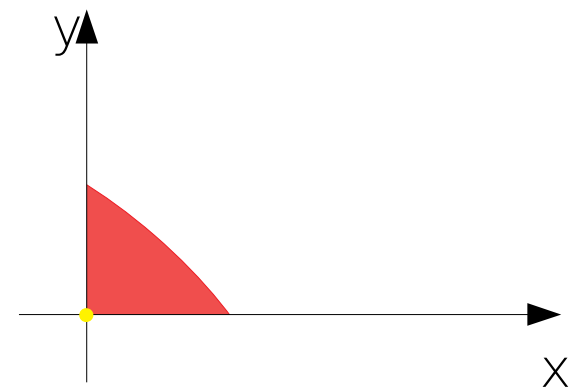
Effects of priors



Effects of priors



Physical priors
 $x > 0$ & $y > 0$

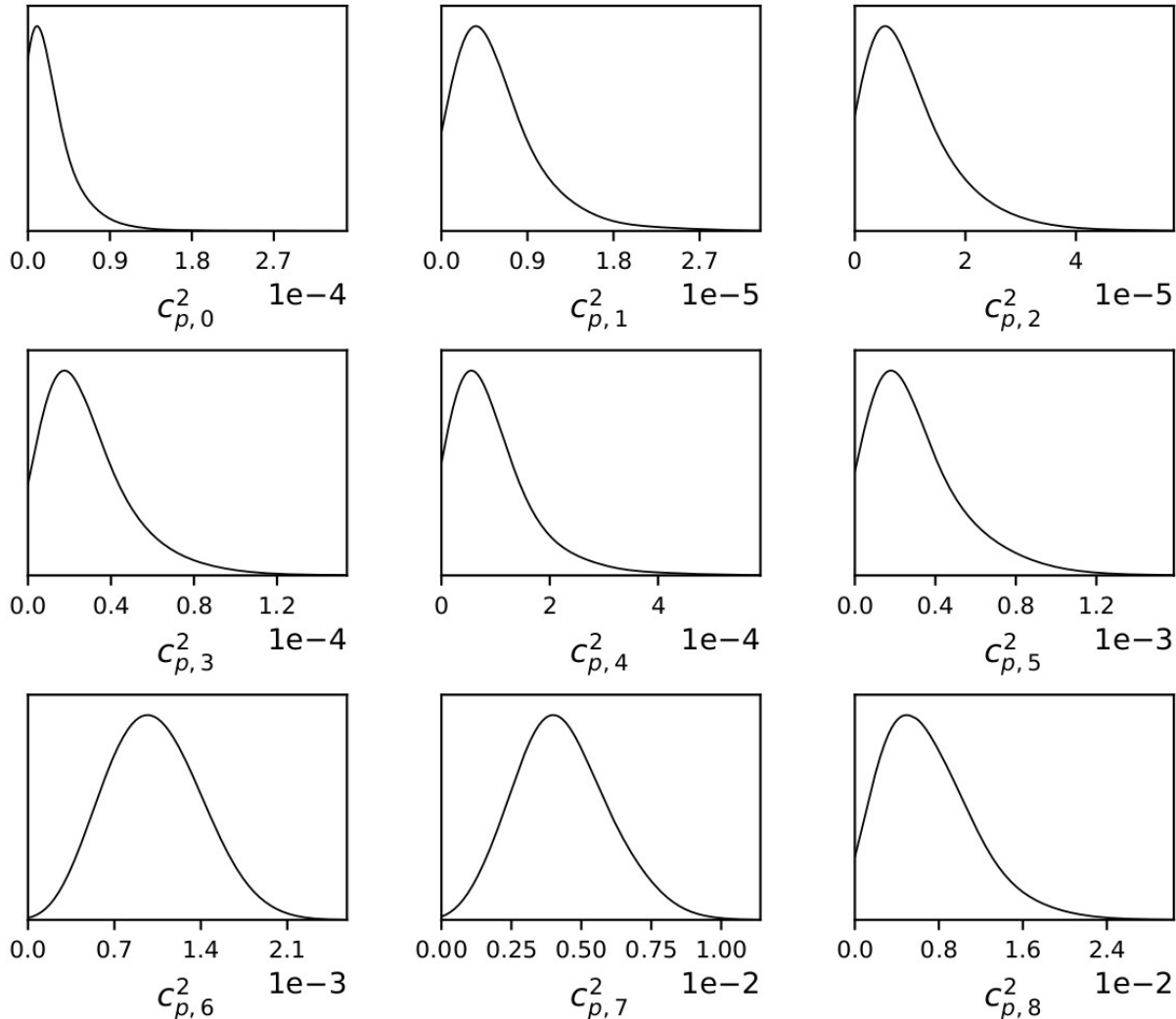


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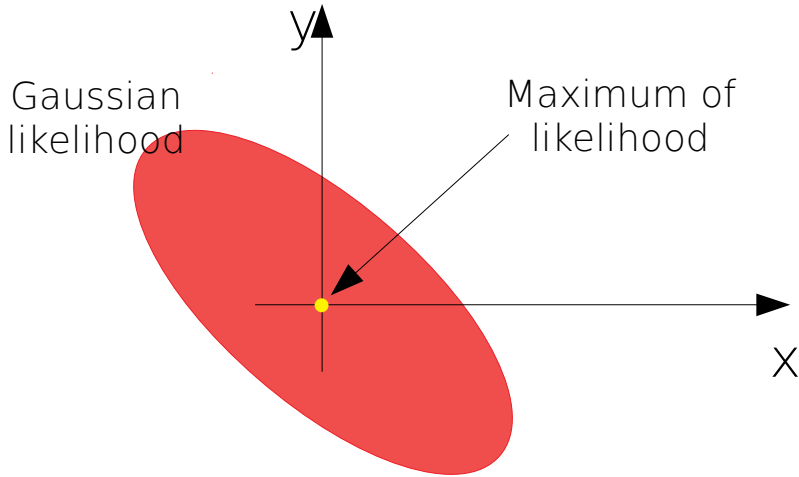
$$c_p^2 = c_s^2 + \frac{8}{15}c_v^2$$

— Uniform priors on c_s^2 and c_v^2

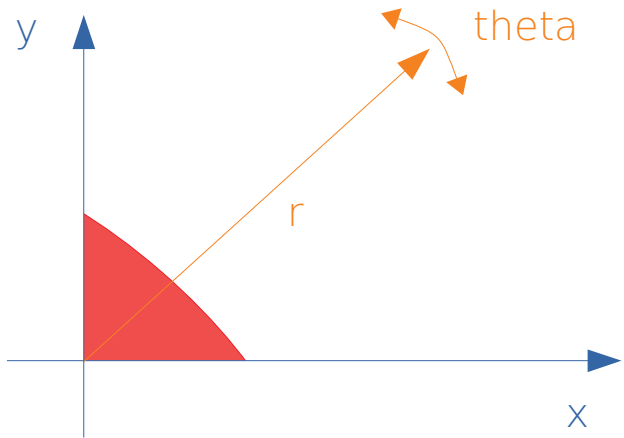
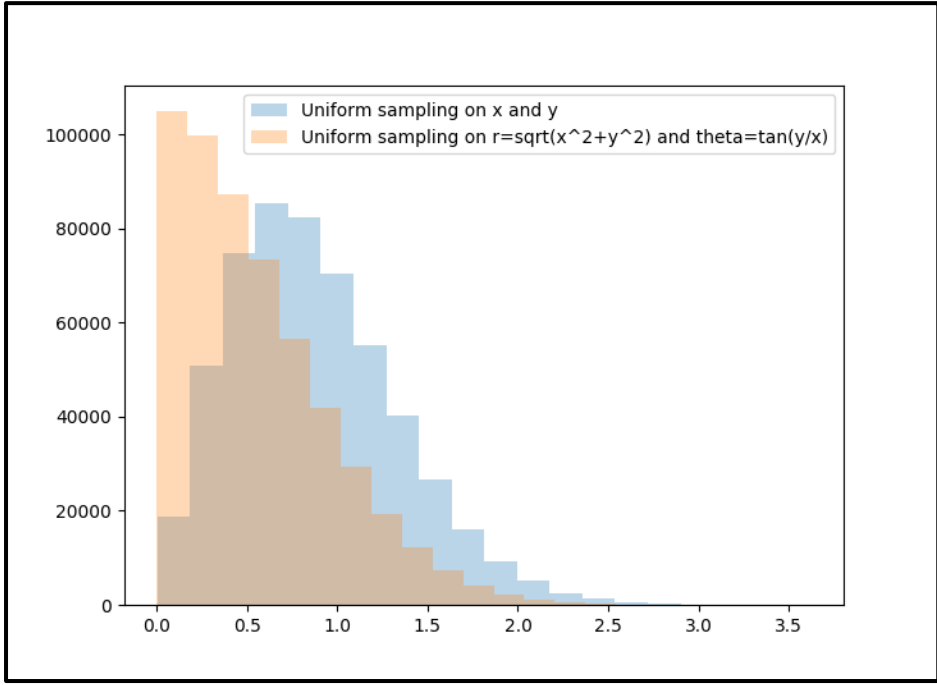
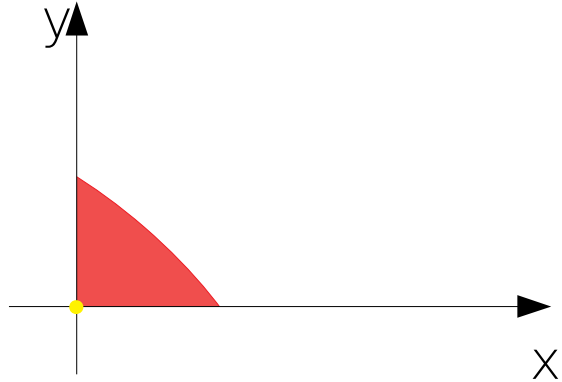
(c_s^2, c_v^2)



Effects of priors



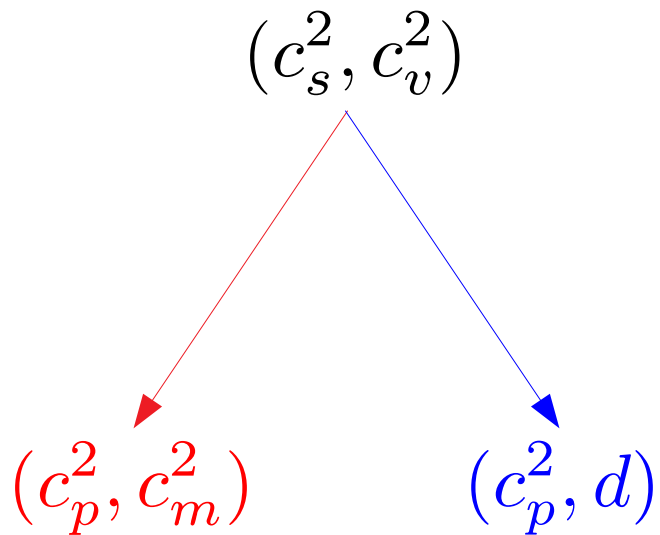
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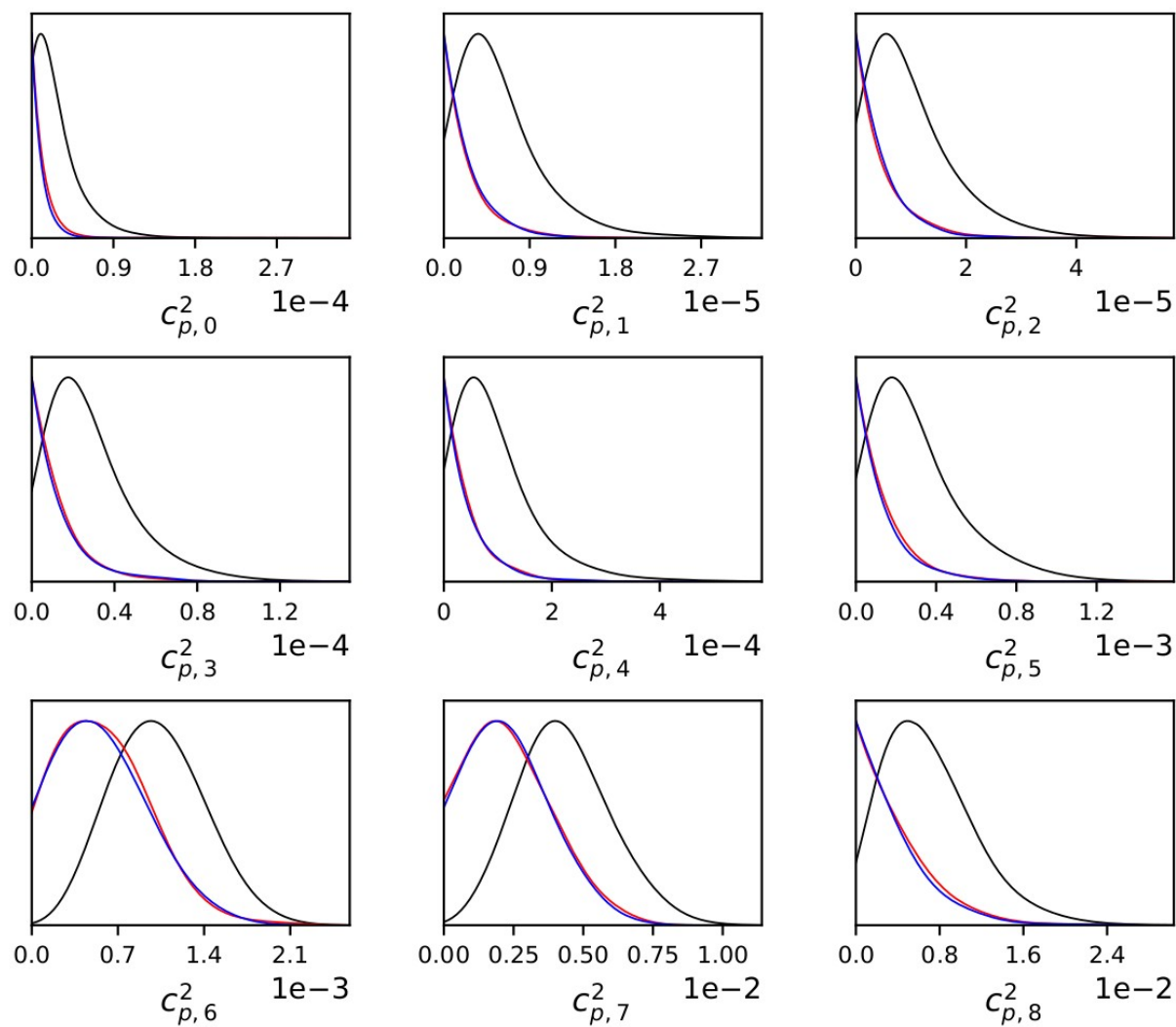
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- Uniform priors on c_s^2 and c_v^2
- Uniform priors on c_p^2 and c_m^2
- Uniform priors on c_p^2 and d



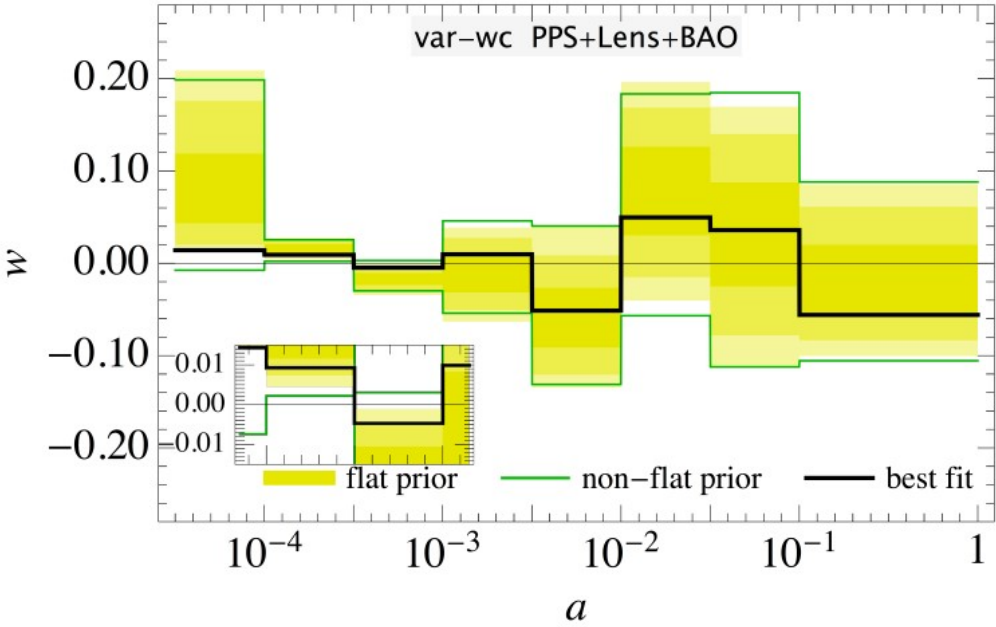
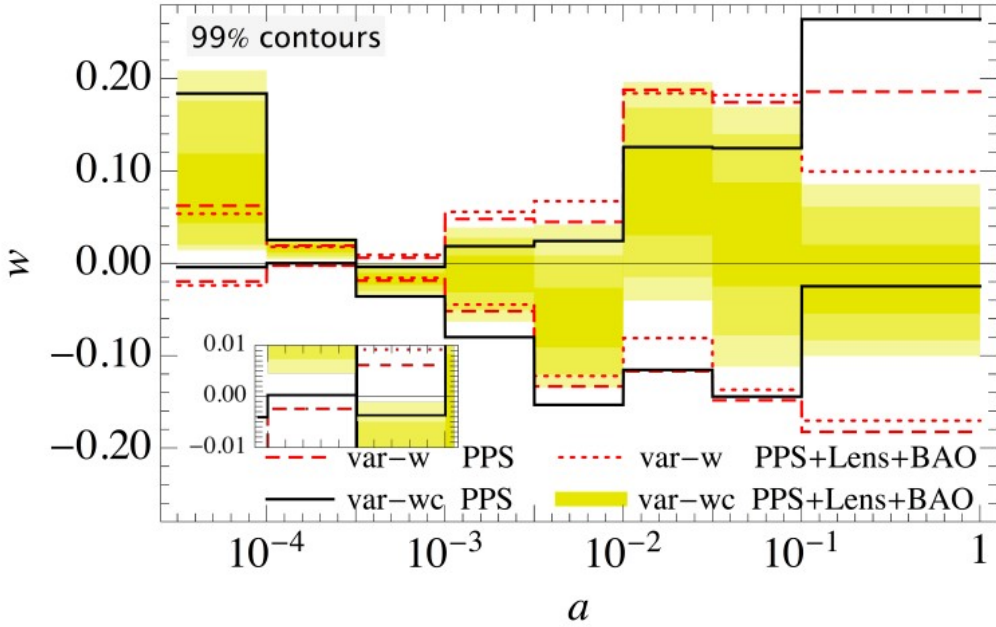
$$c_m^2 = \arctan\left(\frac{8}{15} \frac{c_v^2}{c_s^2}\right)$$

$$d = \frac{c_s^2}{c_p^2}$$



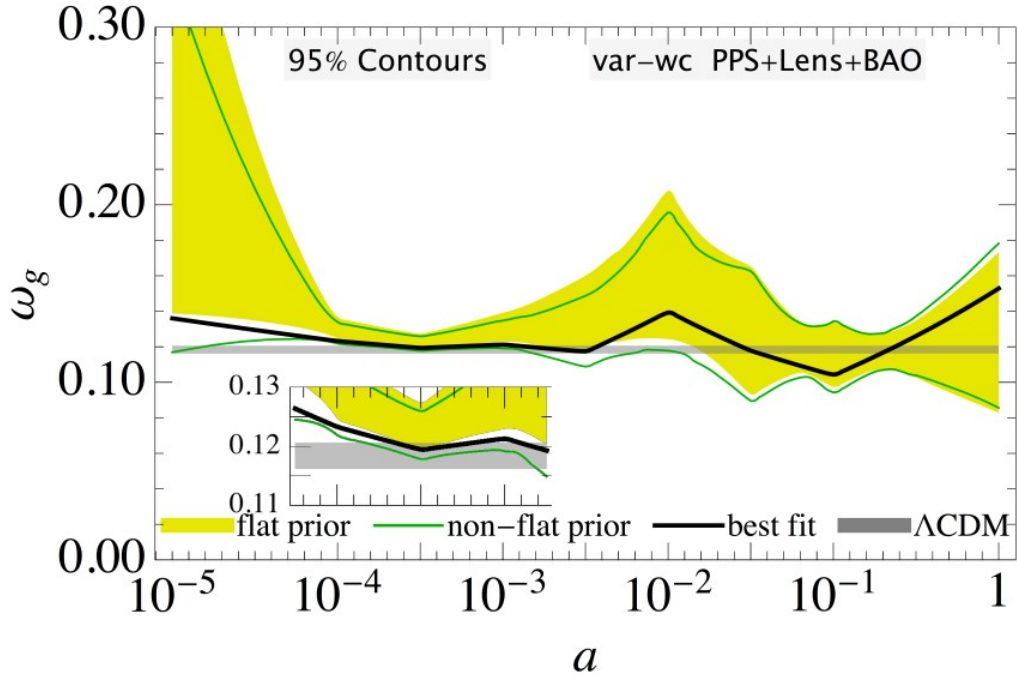
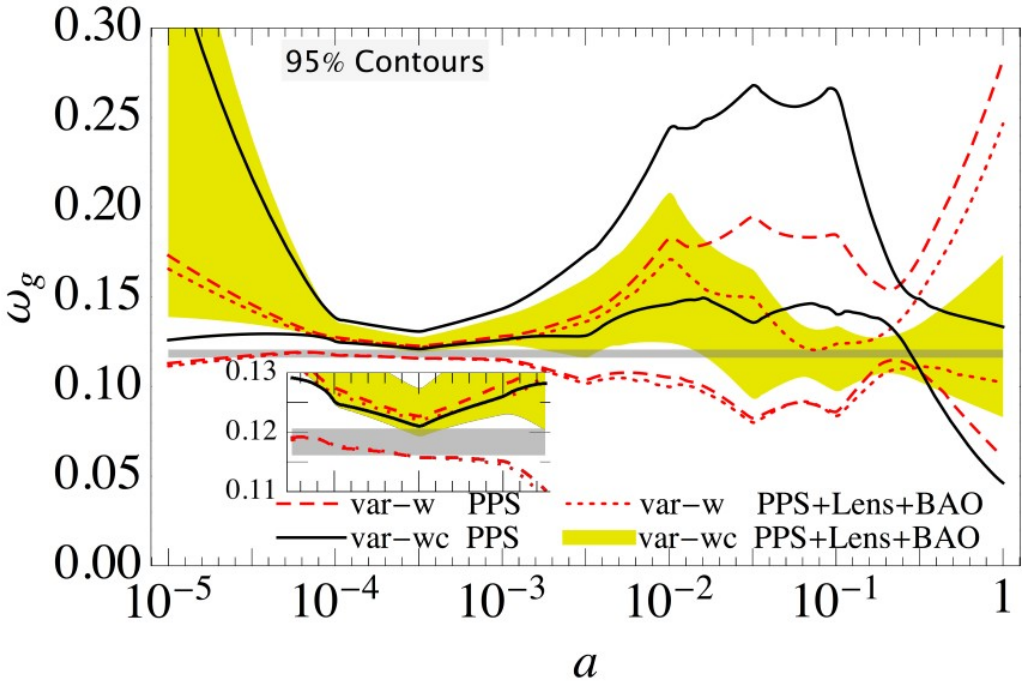
Binned $w(a)$, $c_s^2(a)$, and $c_v^2(a)$ constraints

Ilić et al., 2020, arXiv:2004.09572



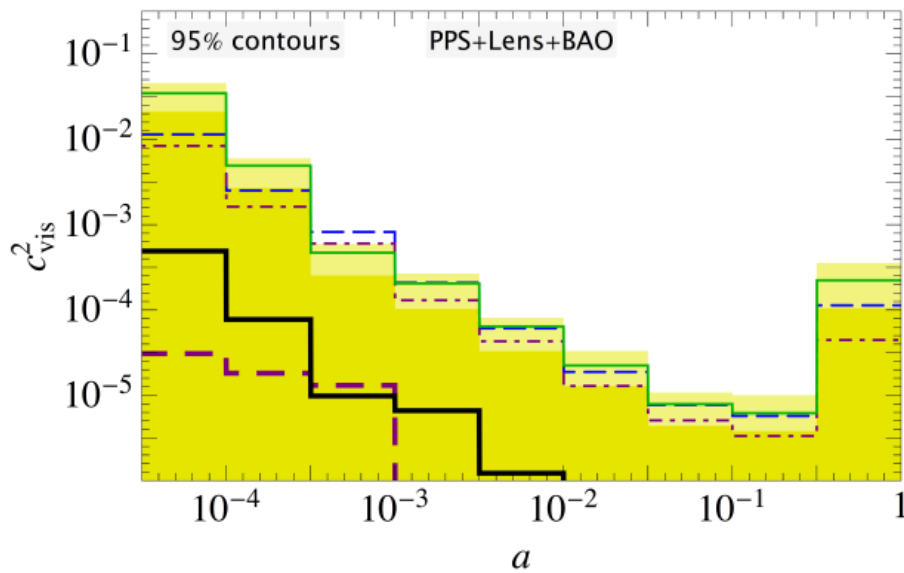
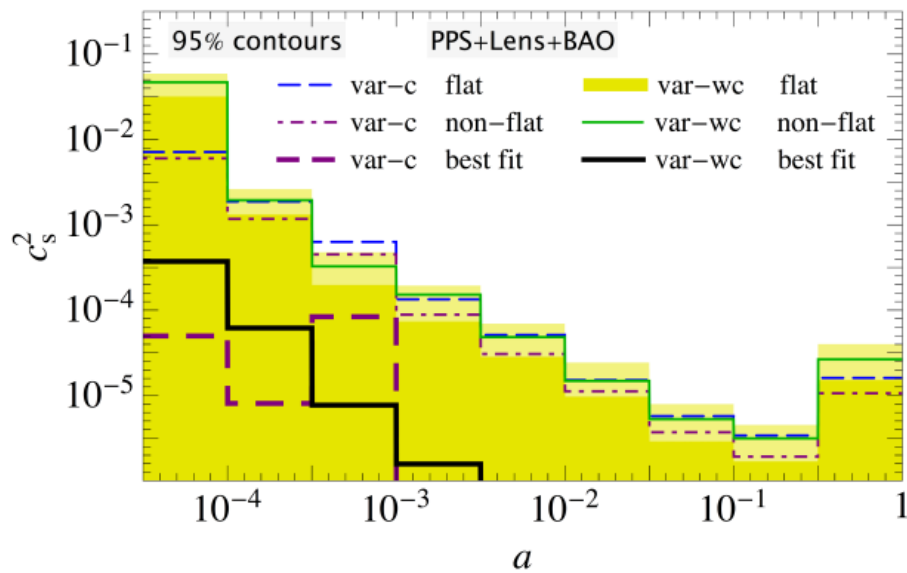
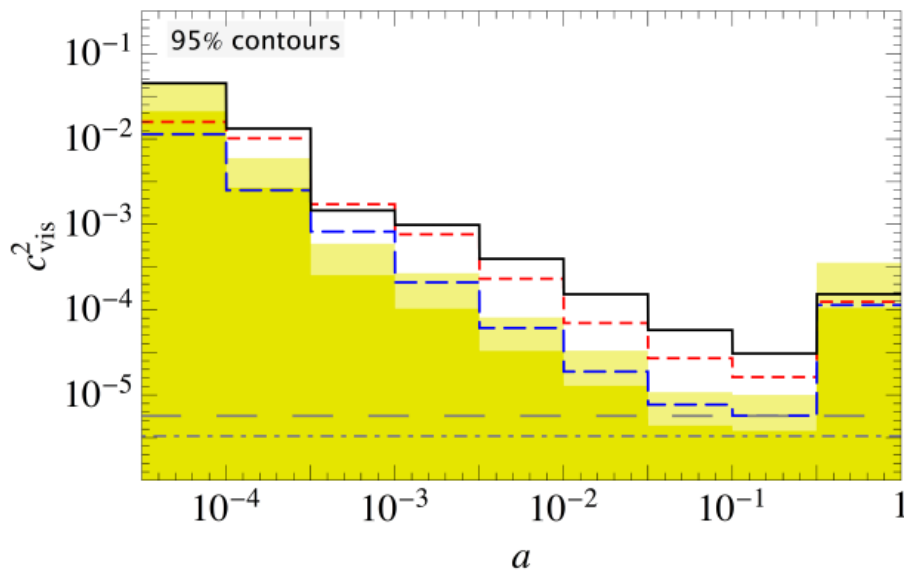
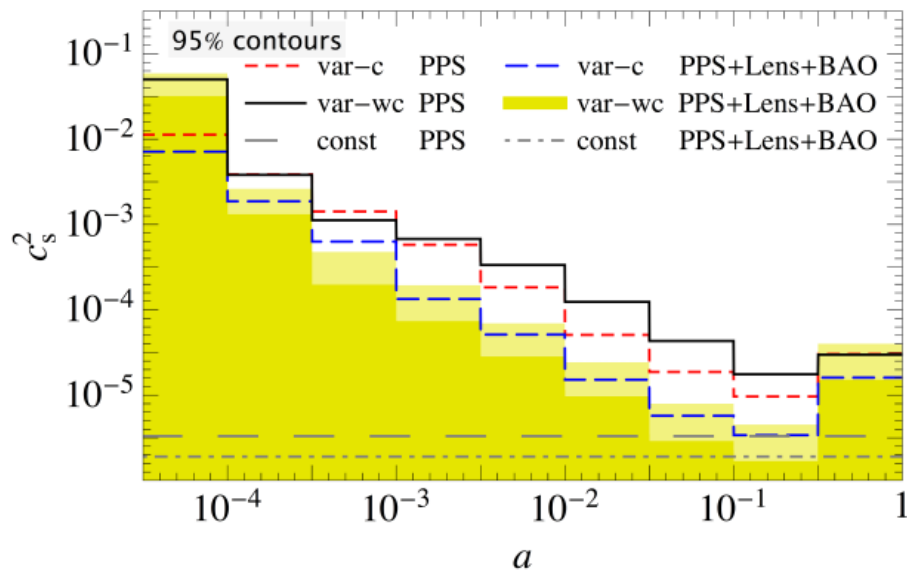
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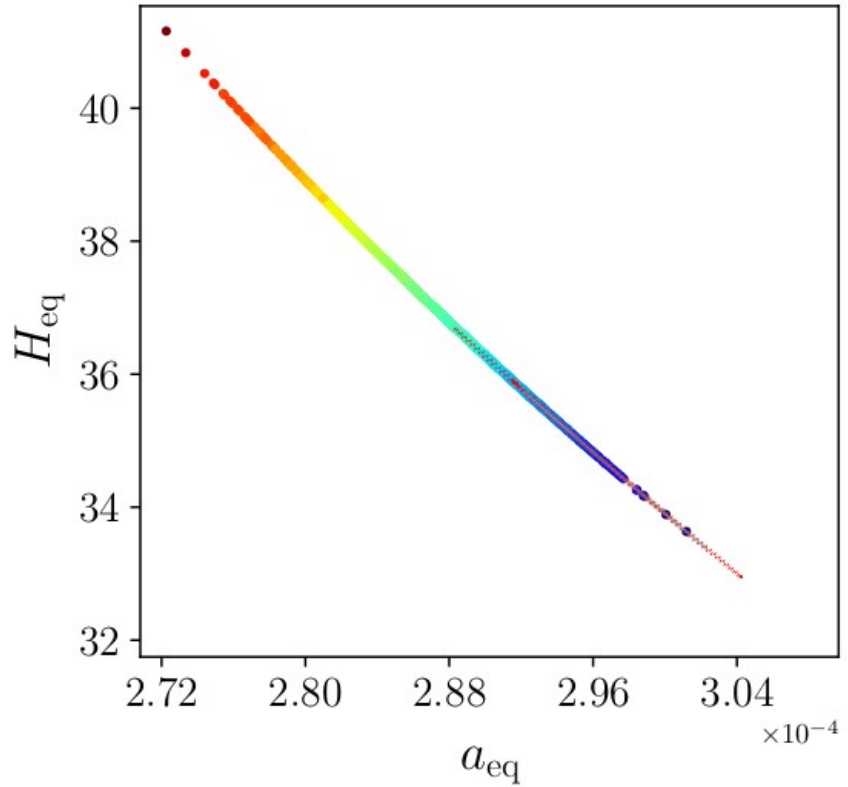
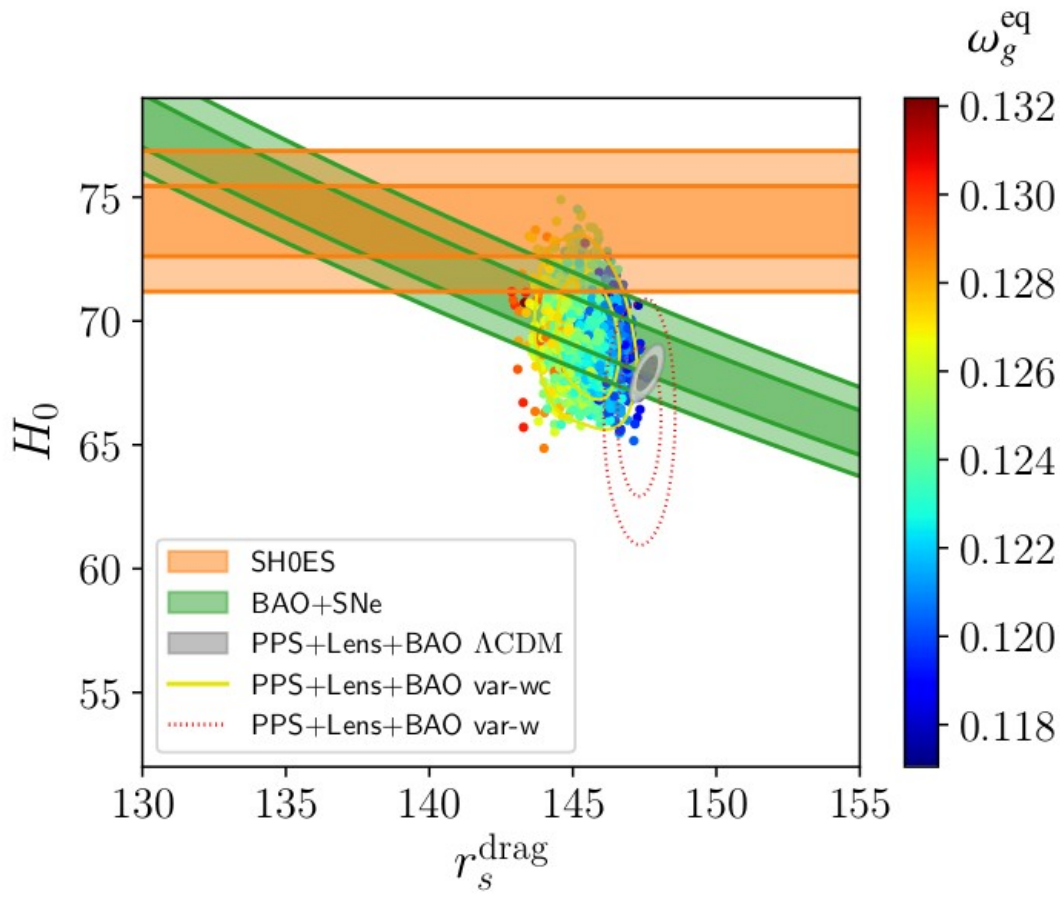
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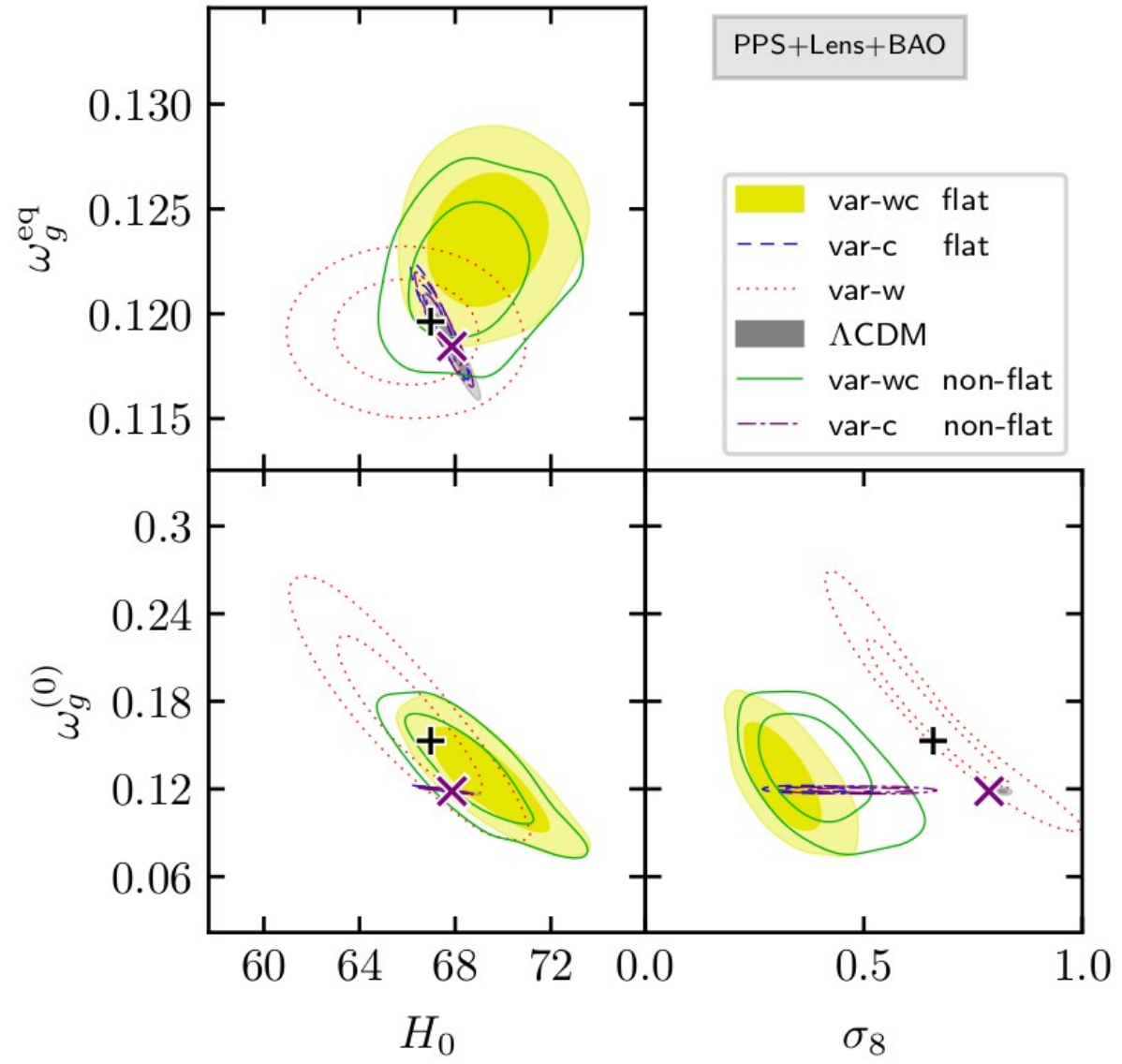
GDM and H0

Ilić et al., 2020, arXiv:2004.09572



Identifying prior effects with ECLAIR

Ilić et al., 2020, arXiv:2004.09572

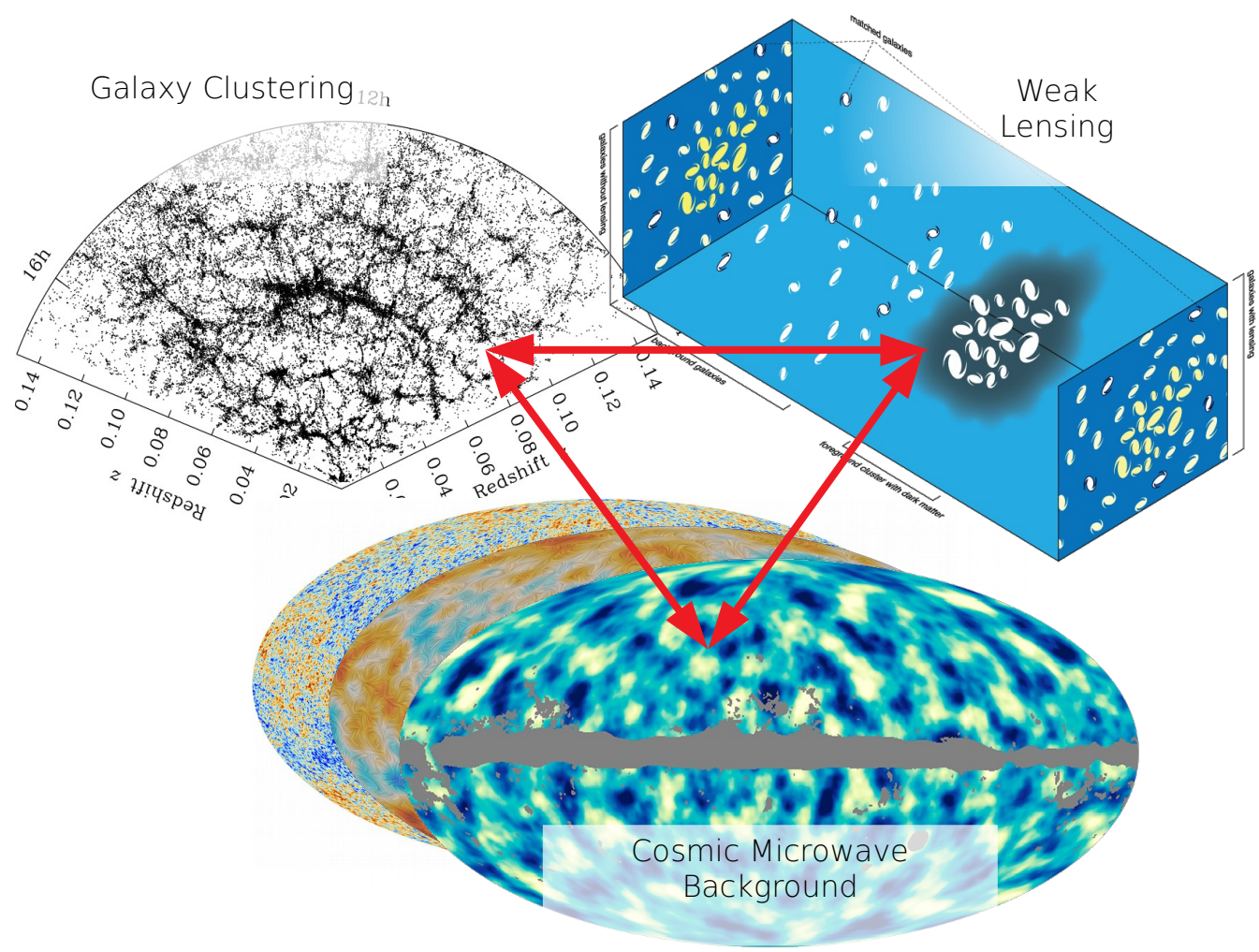


Summary

Ilić et al., 2020, arXiv:2004.09572

- No convincing evidence for w , $cs2$, $cv2$ to be nonzero
- Varying w improved fit marginally
- Only free $cs2$ and $cv2$ → virtually no improvement
- $w+cs2+cv2$ free: DM abundance around equality ++
while abundance today, $H0$, and $s8$ --
→ help in solving $s8$ and $H0$ tensions ?

Beyond CMB-only constraints

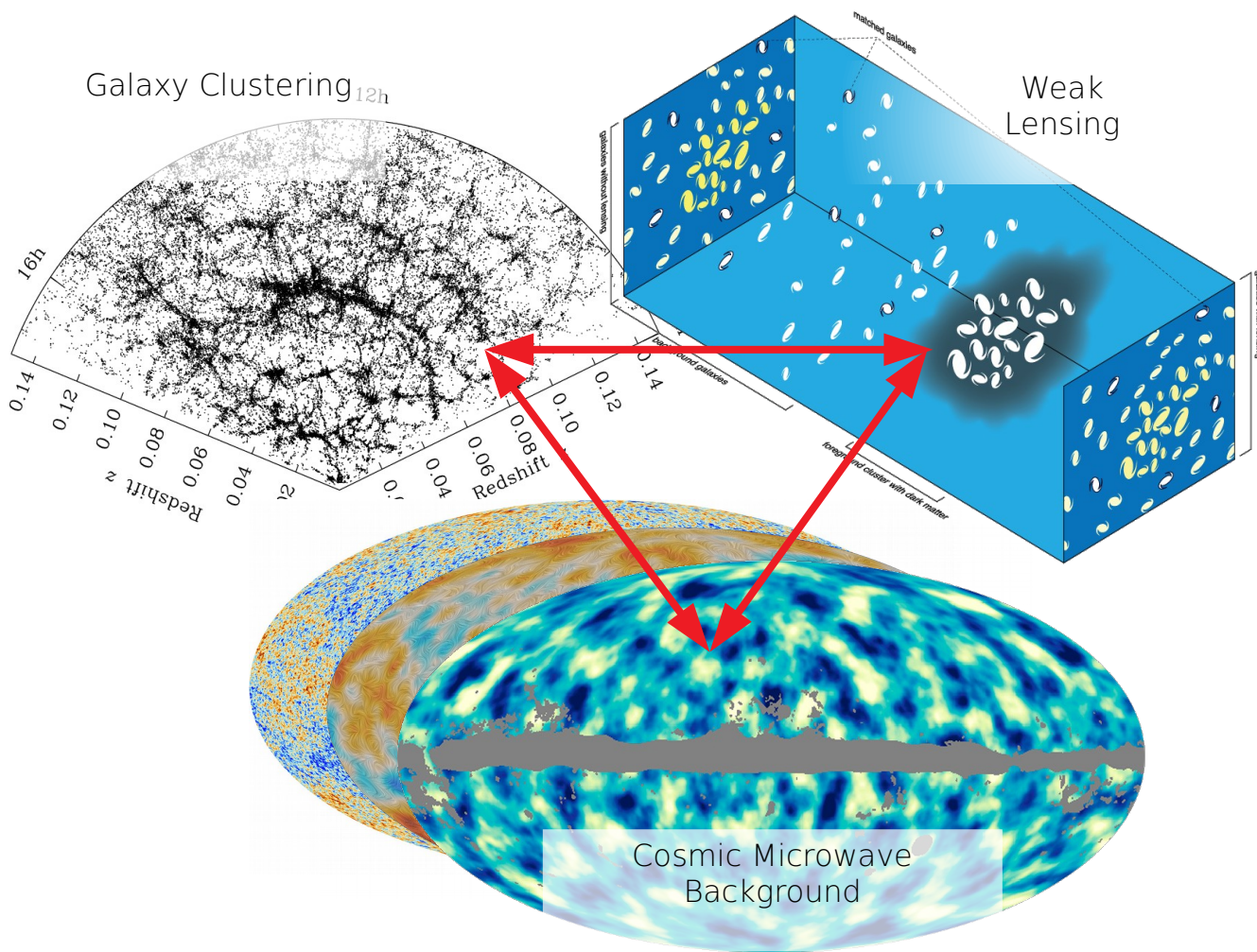


Take-away message(s)

- CDM remains (mostly) unchallenged
- Plethora of contenders
- GDM model : efficient way of pruning model space
- We put constraints on free, non-parametric functions describing GDM properties
- We applied GDM on current state-of-the-art data
- Ongoing preparation for new era of instruments, with some promising first results

Thank you
for your attention !

Beyond CMB-only constraints



GDM Halo model & LSS constraints

Thomas et al., 2019, arXiv:1905.02739

GDM cosmological constraints

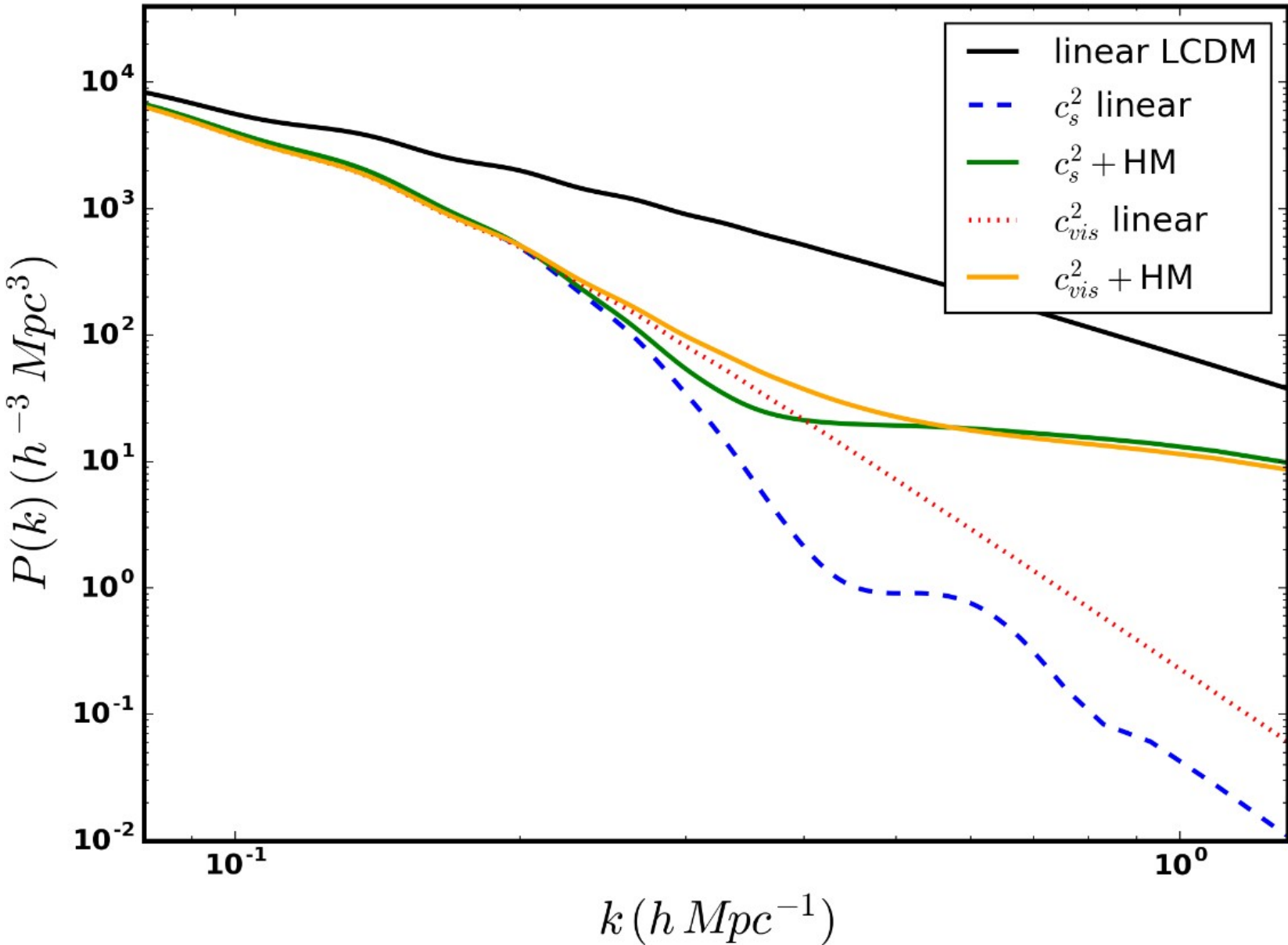
with free, constant w , c_s^2 , and c_v^2

+ New Halo model for non-linearities

+ LSS data : WiggleZ matter power spectrum

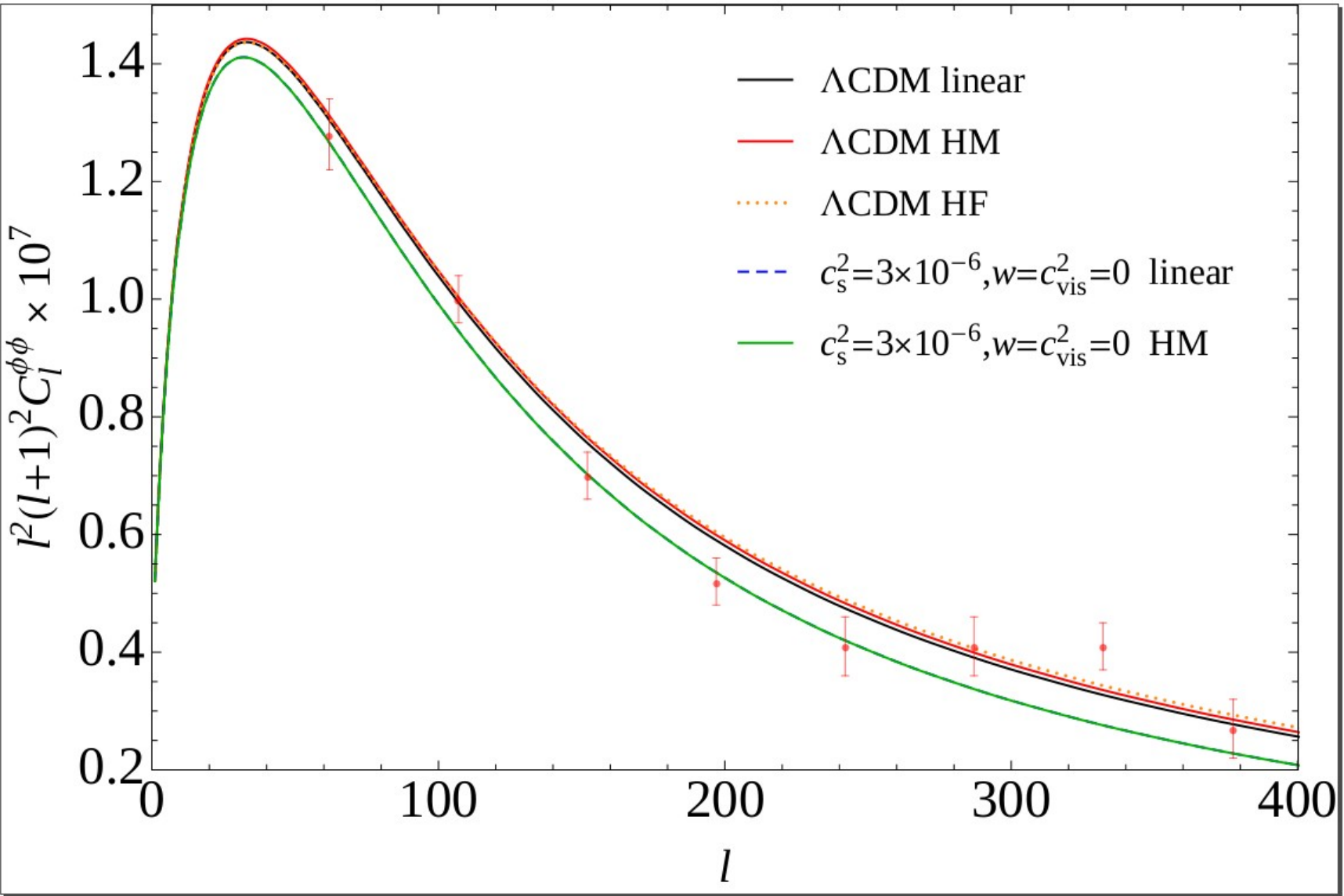
GDM Halo model & LSS constraints

Thomas et al., 2019, arXiv:1905.02739



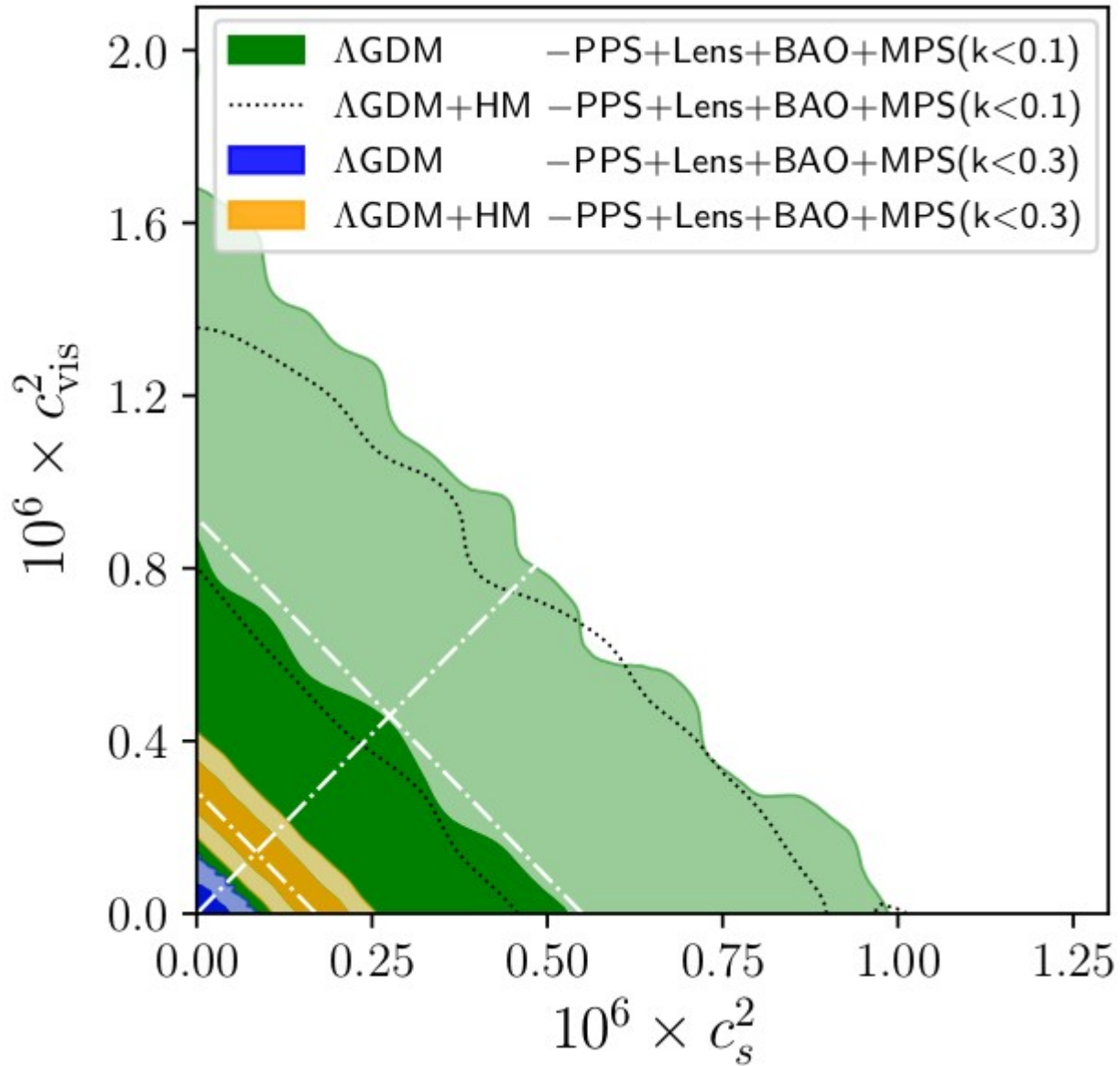
GDM Halo model & LSS constraints

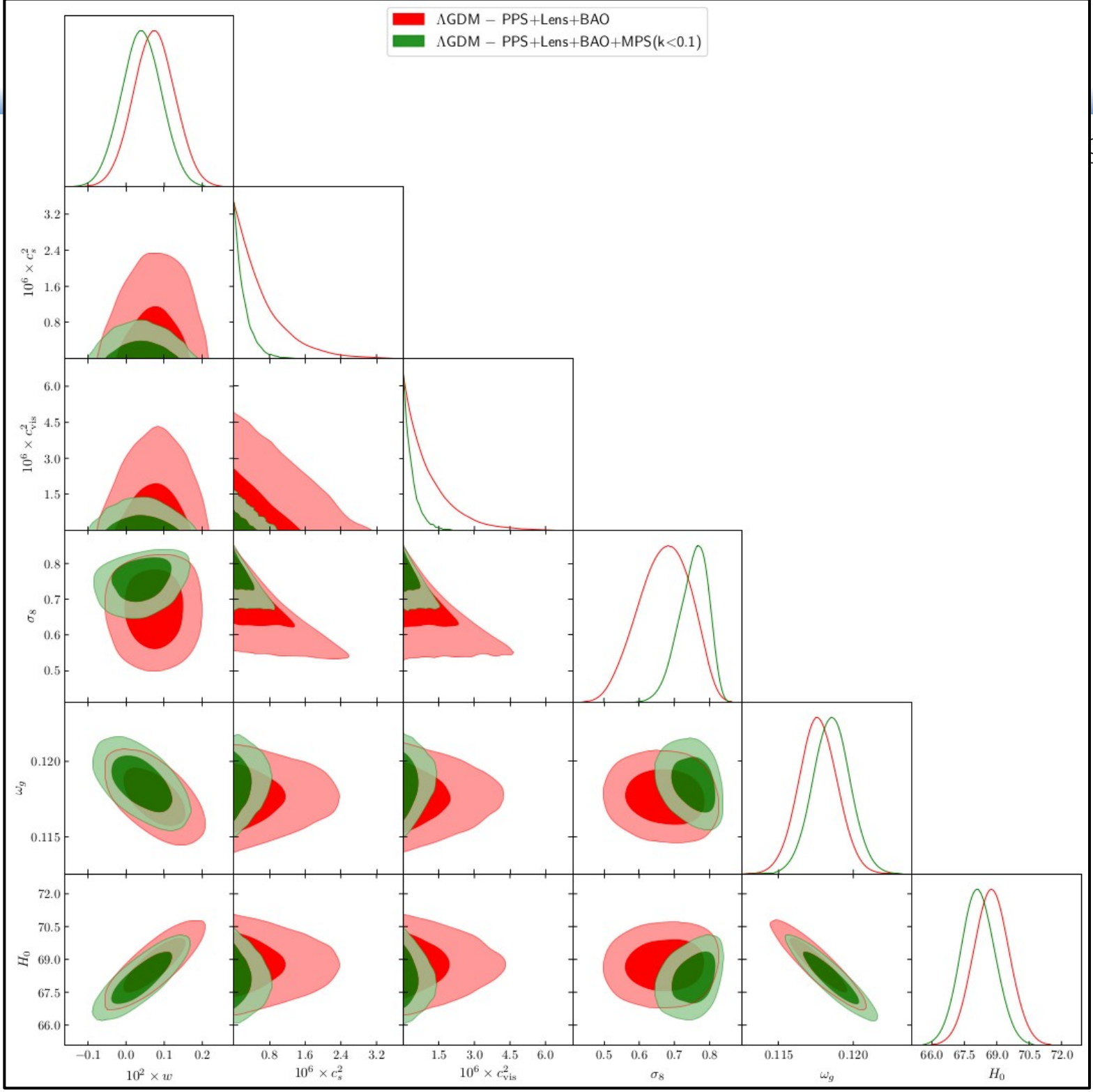
Thomas et al., 2019, arXiv:1905.02739



GDM Halo model & LSS constraints

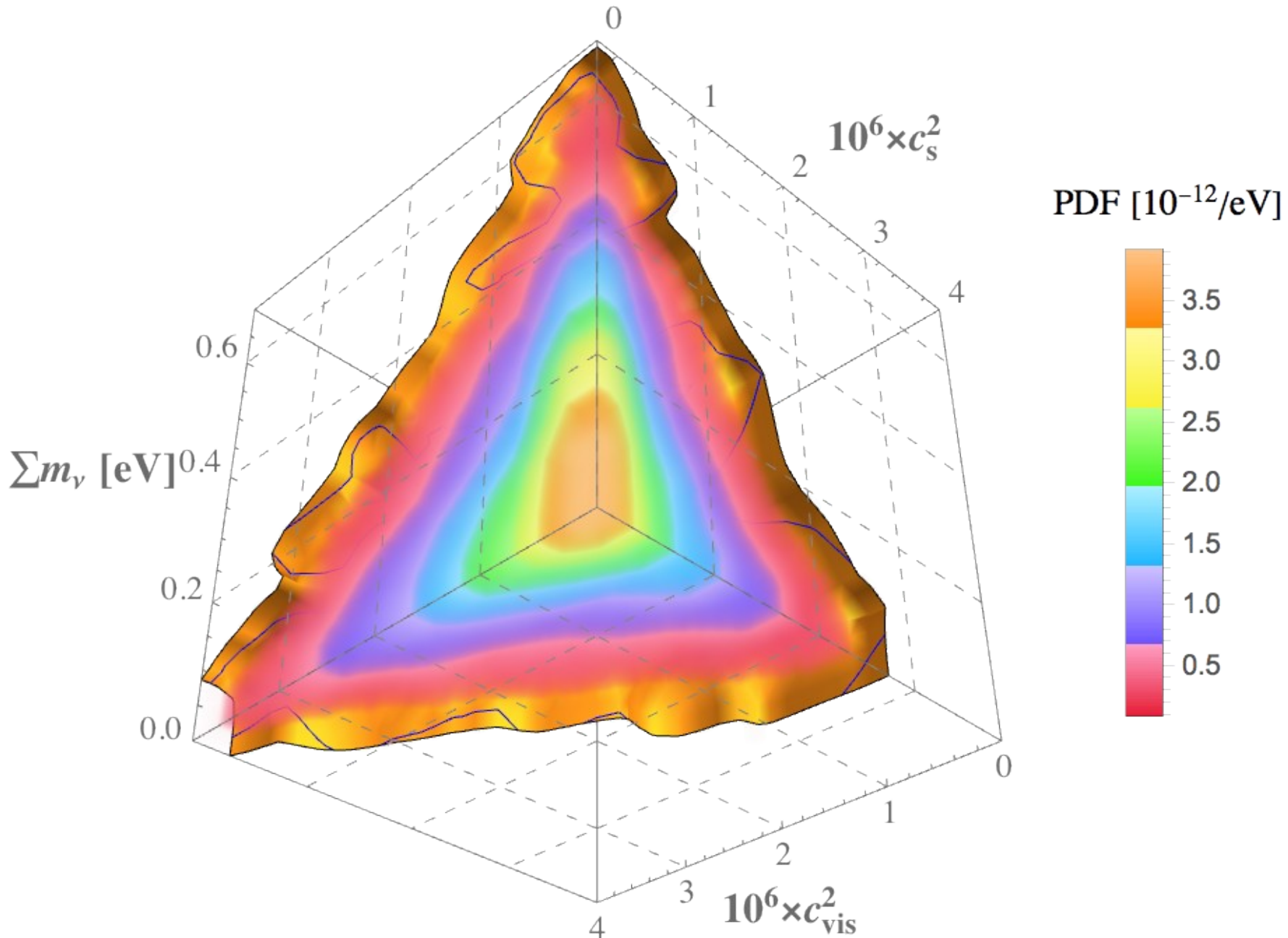
Thomas et al., 2019, arXiv:1905.02739





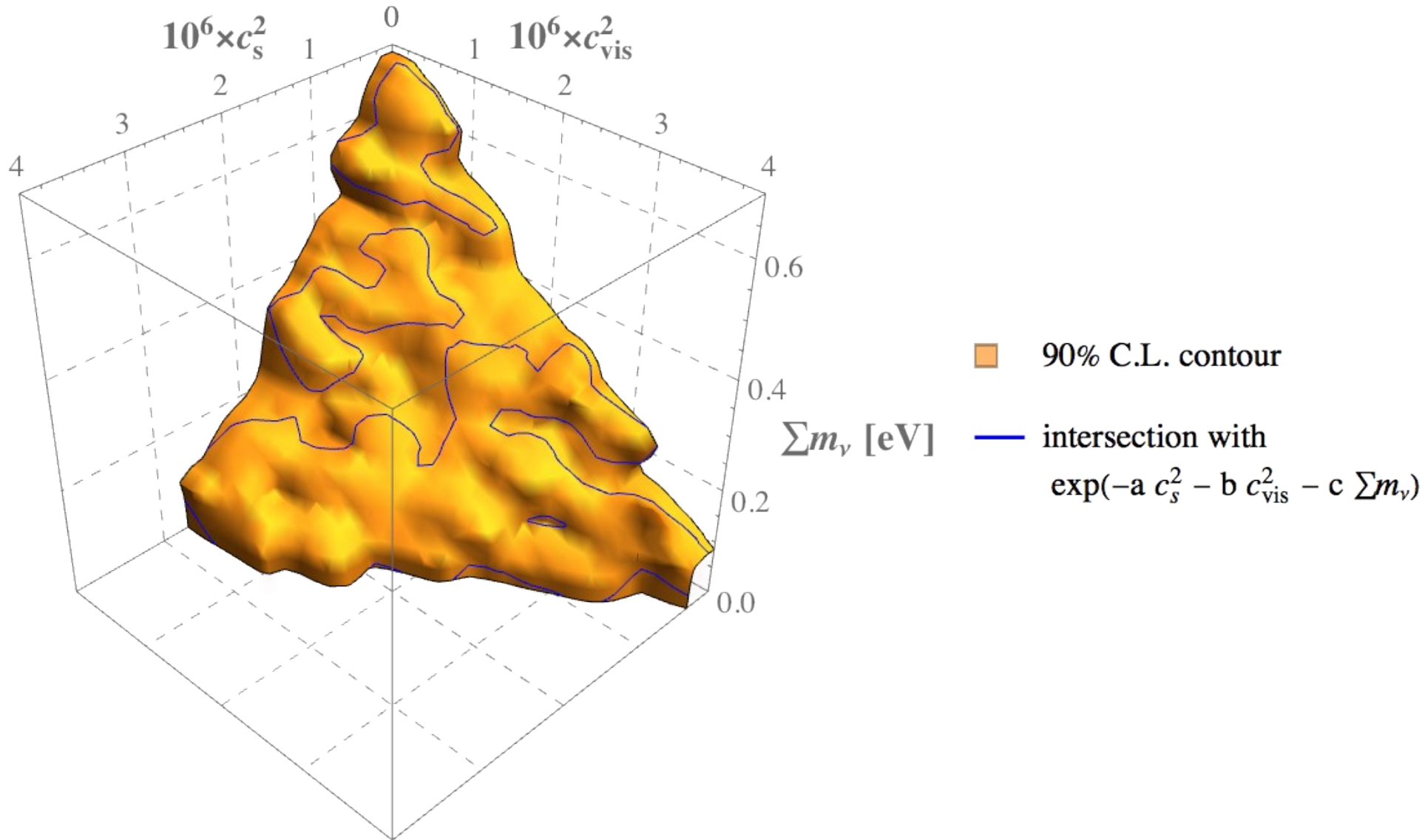
GDM and massive neutrinos

Thomas et al., 2019, arXiv:1905.02739



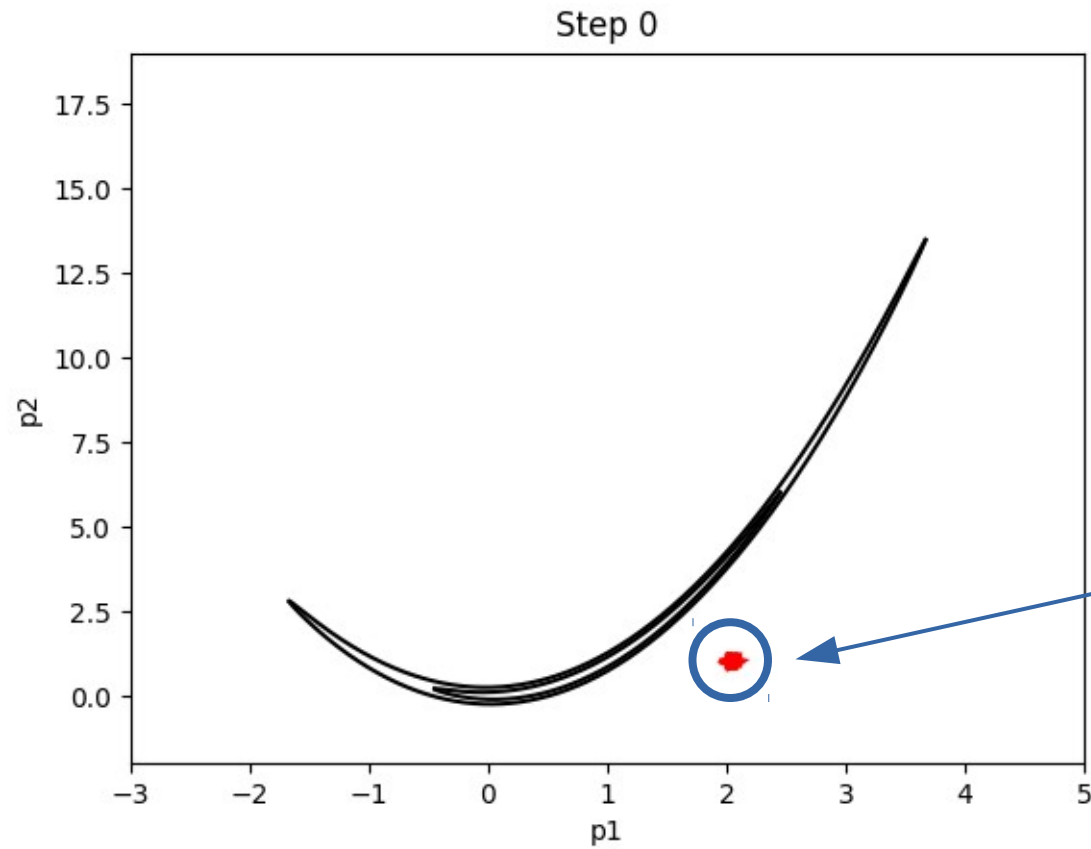
GDM and massive neutrinos

Thomas et al., 2019, arXiv:1905.02739



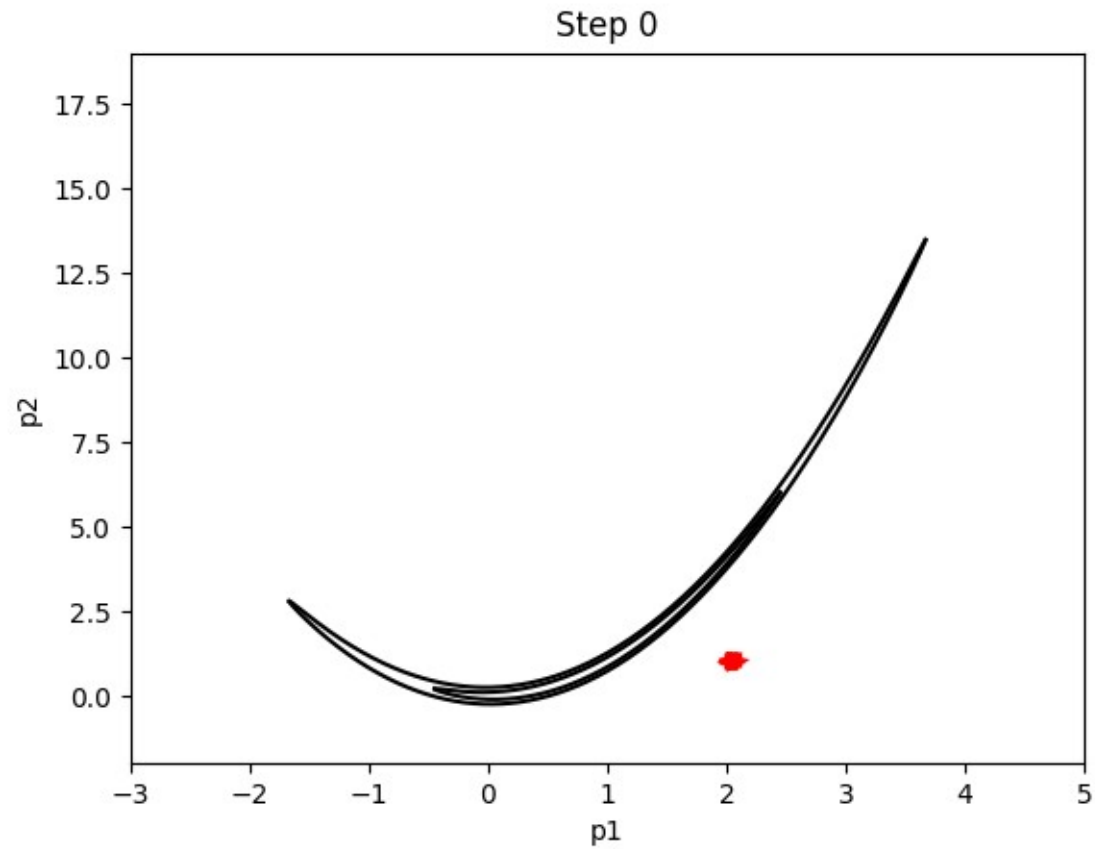
Ensemble sampling with ECLAIR

Ensemble sampling

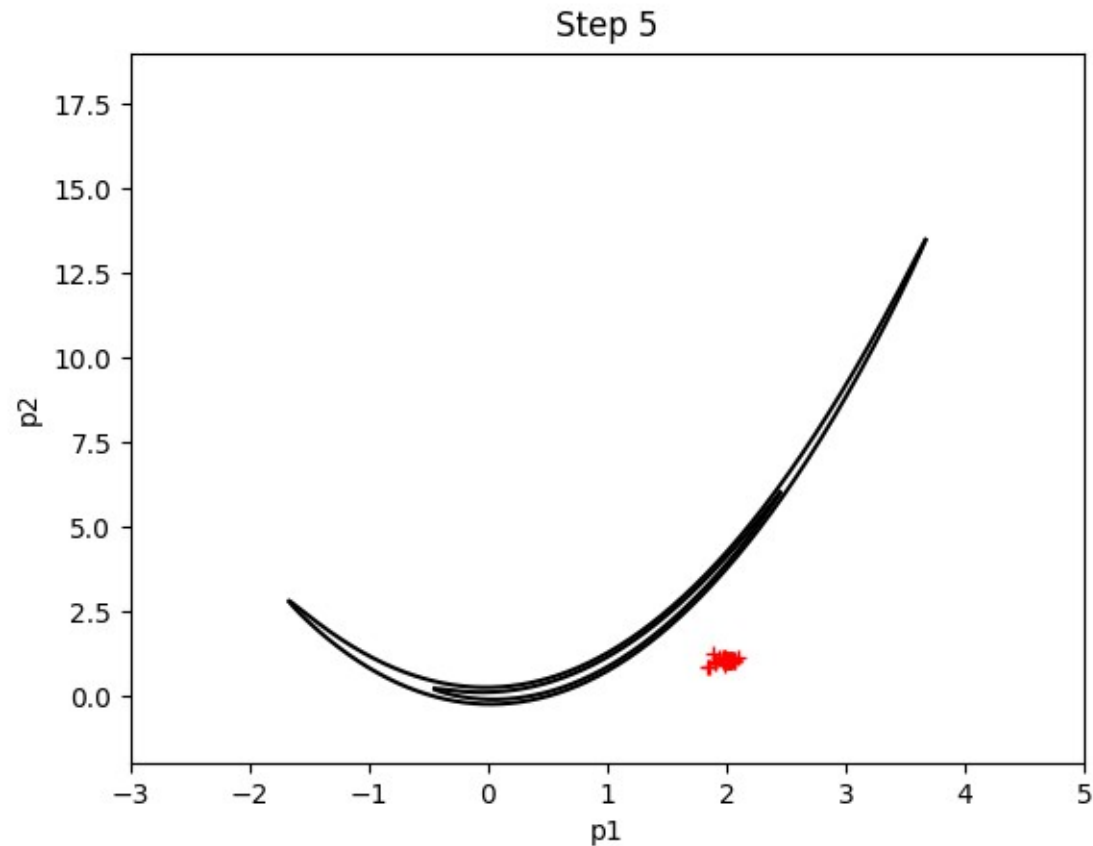


Collection of
"walkers"
initialized at
random
positions

Ensemble sampling

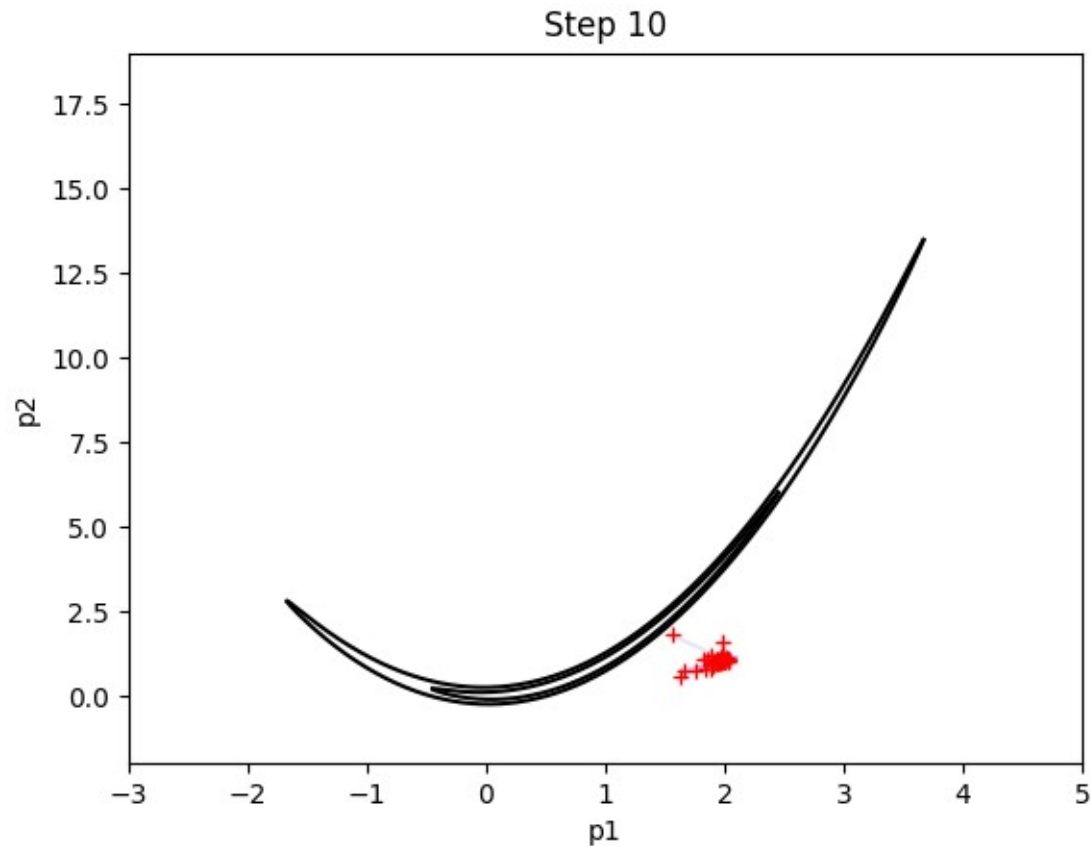


Ensemble sampling



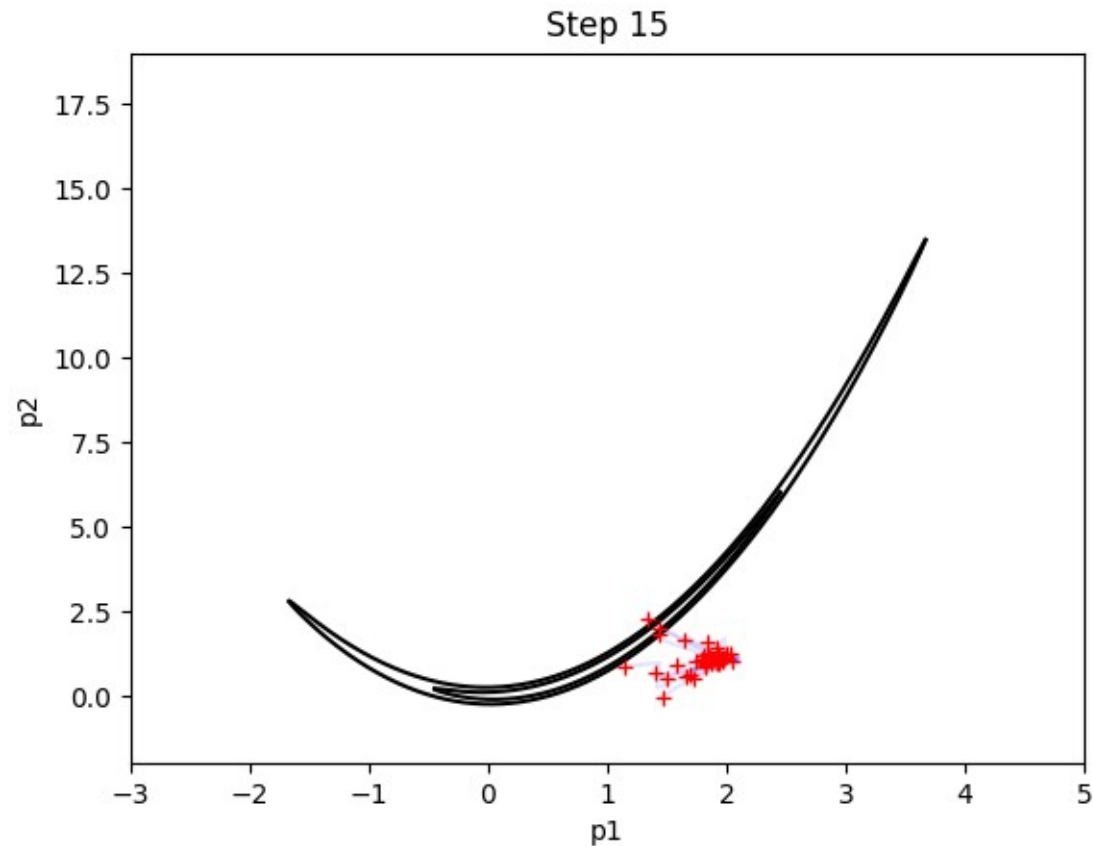
“Walkers”
quickly spread
throughout
parameter
space, using
each other’s
position to
propose jumps

Ensemble sampling



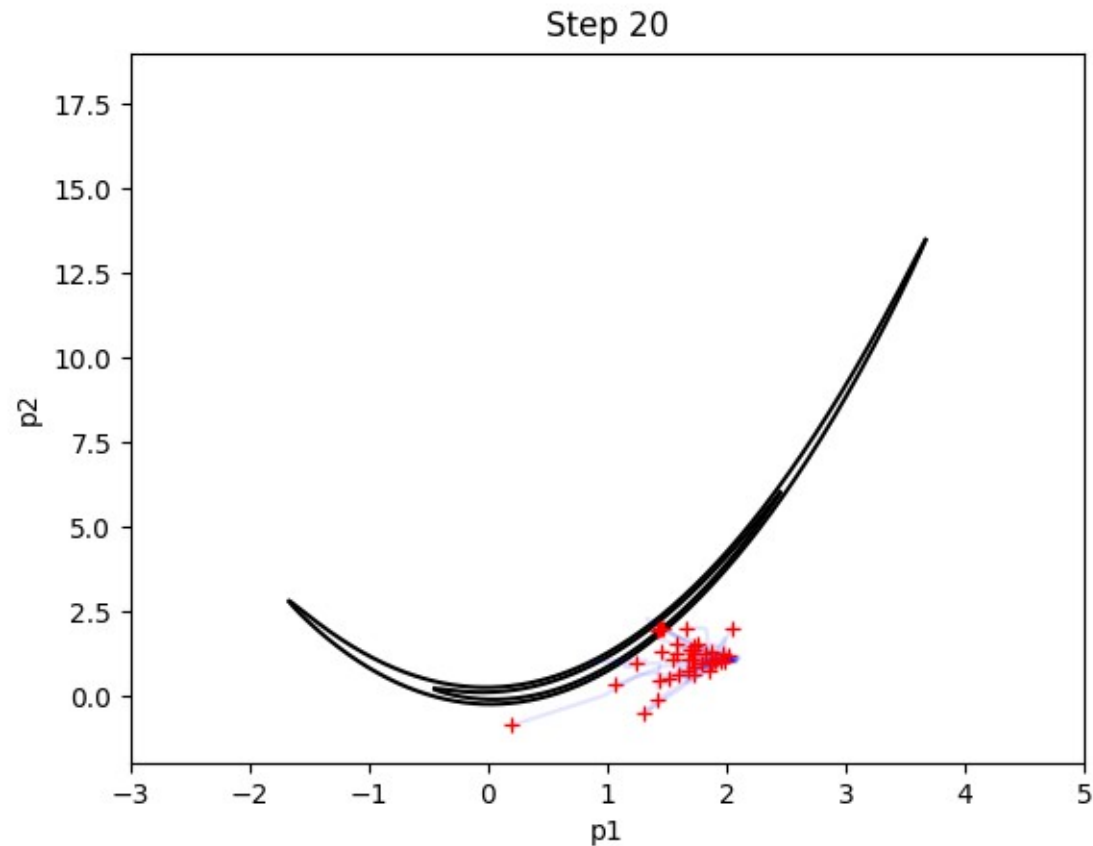
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Ensemble sampling



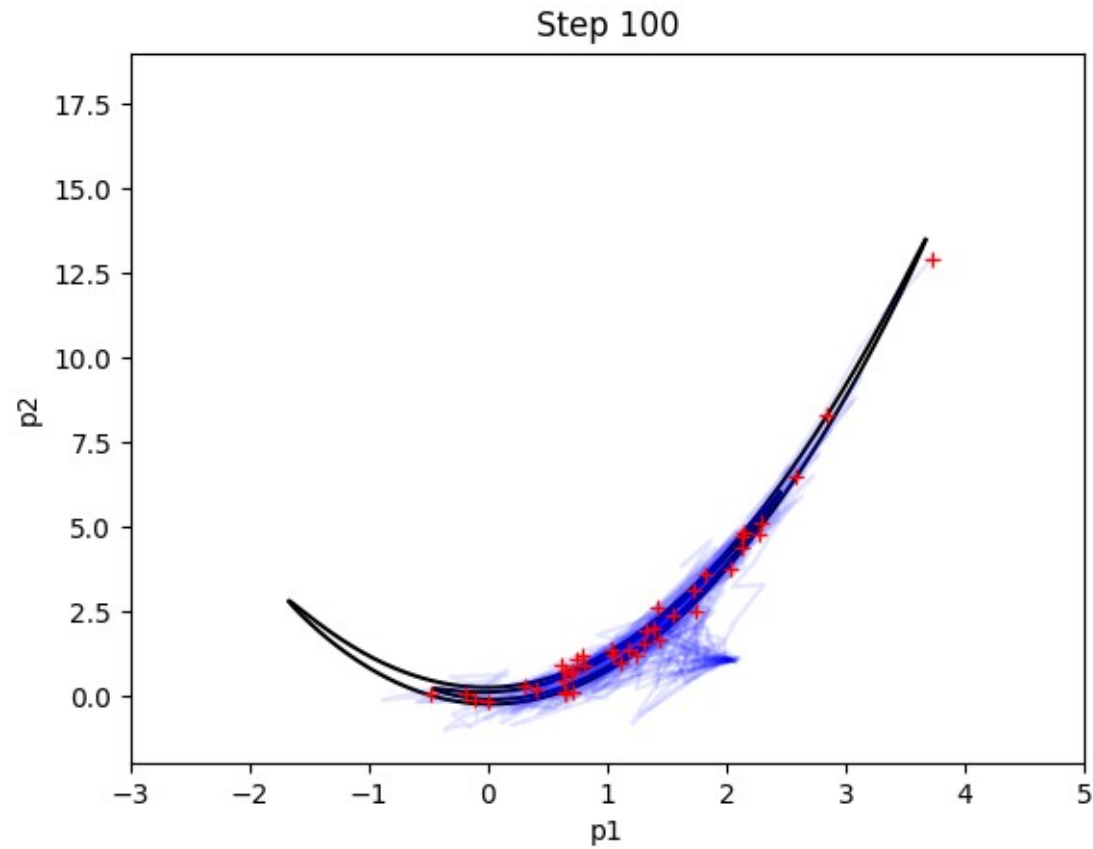
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Ensemble sampling



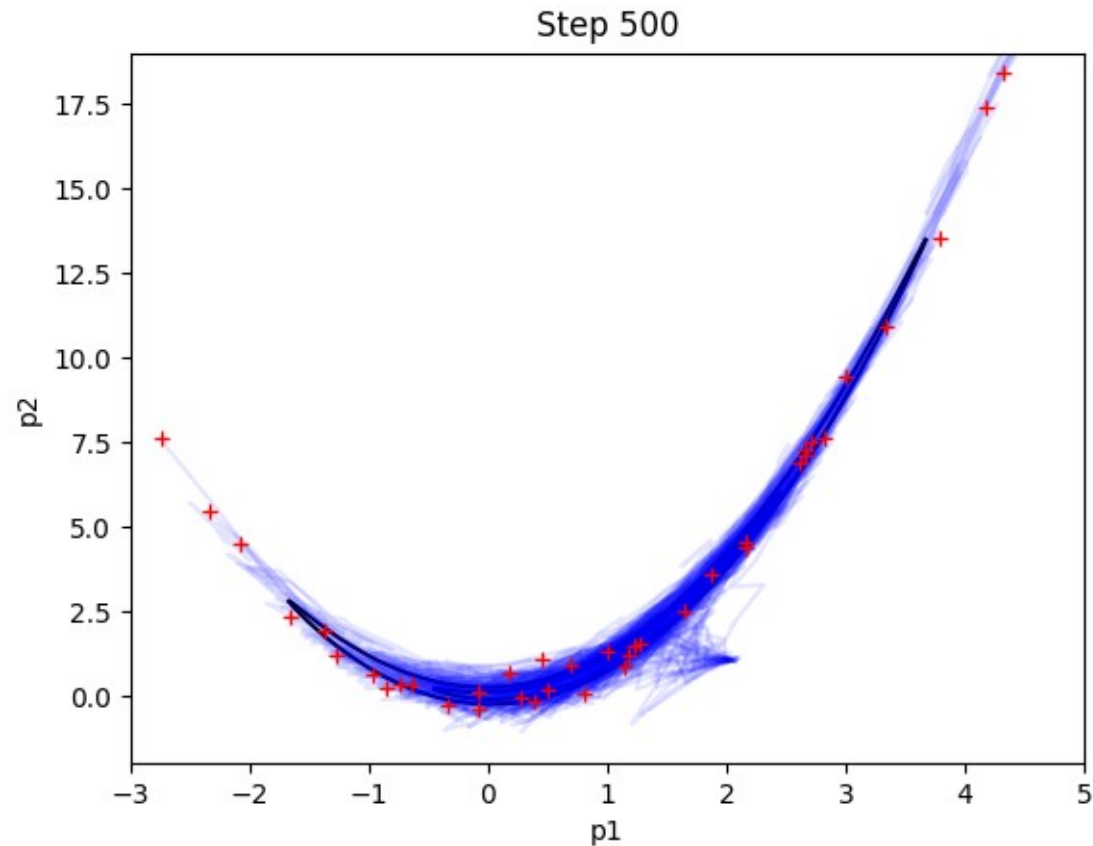
“Walkers”
quickly spread
throughout
parameter
space, using
each other’s
position to
propose jumps

Ensemble sampling



...and end up sitting in the “interesting” region of parameter space

Ensemble sampling

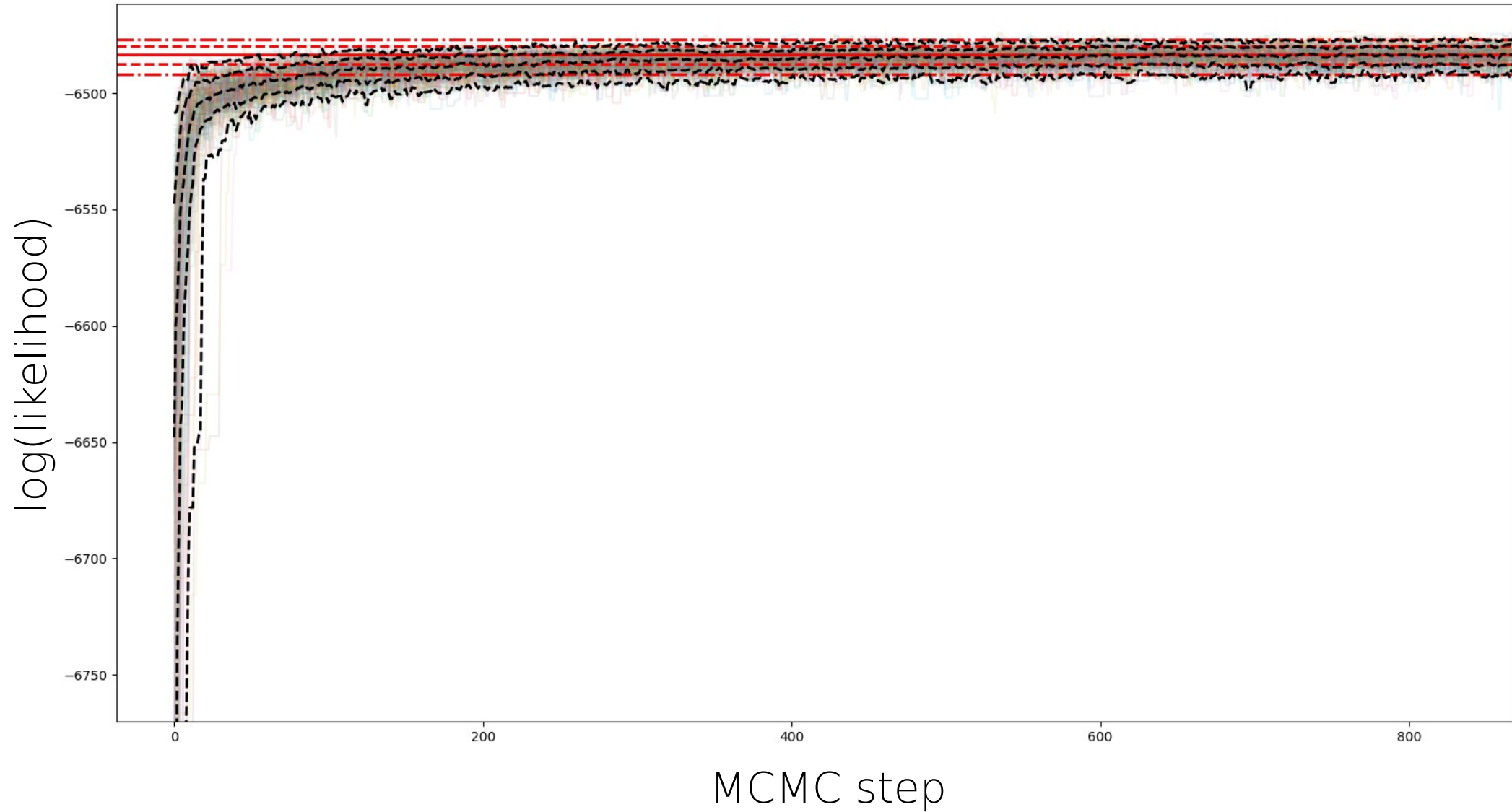


A single
snapshot of
walkers
positions
=
A representative
sample of the
posterior
distribution

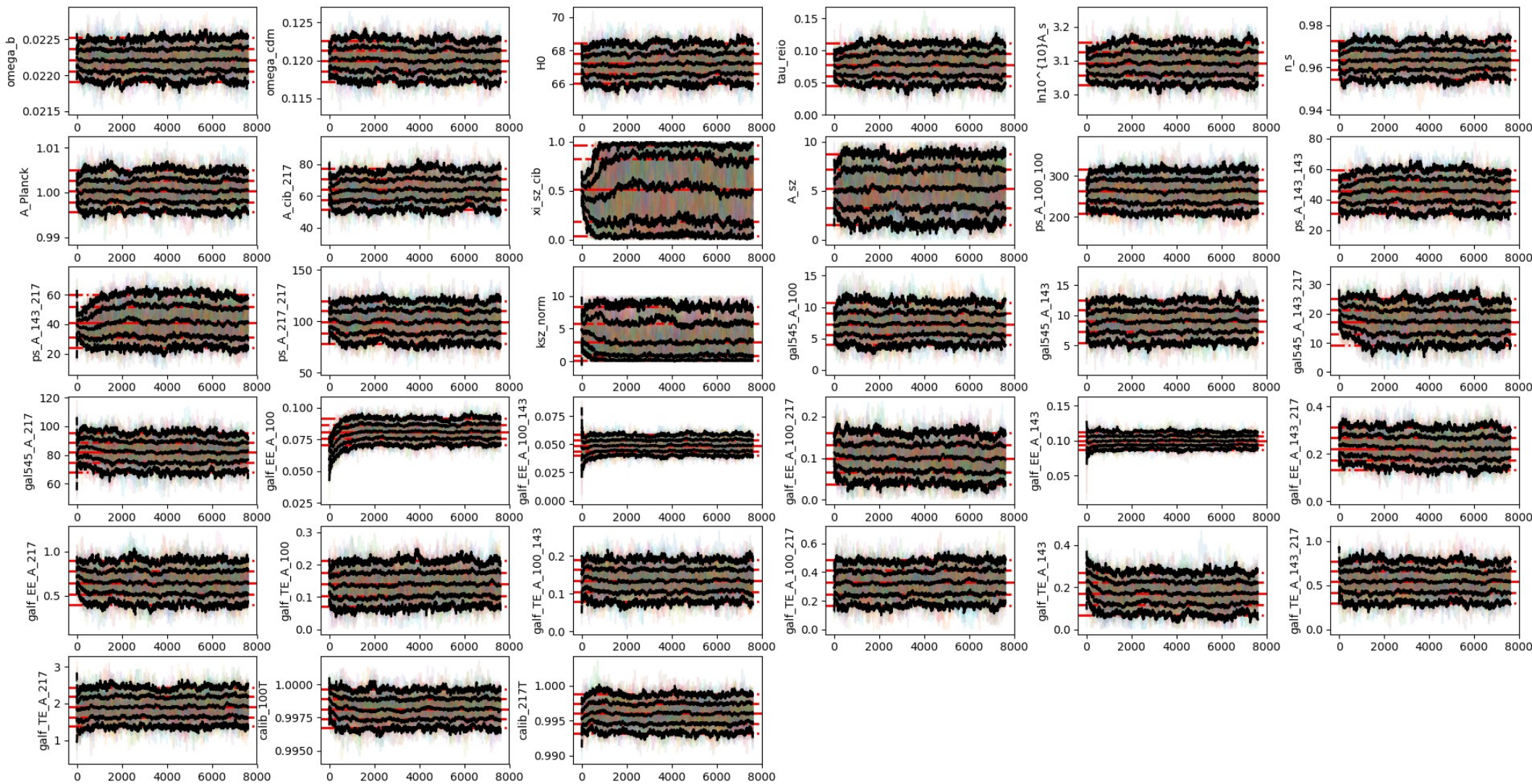
Introducing : ECLAIR

- Written in python (2 & 3 compatible)
- Two (fairly) short files : main (~200) & parser (~500)
- Human-readable/tweakable, well-commented
- Working with any CLASS variant, no modification required
- Growing number of likelihoods/datasets implemented (easy to add new ones)
- **Intuitive visualization scripts to assess convergence**

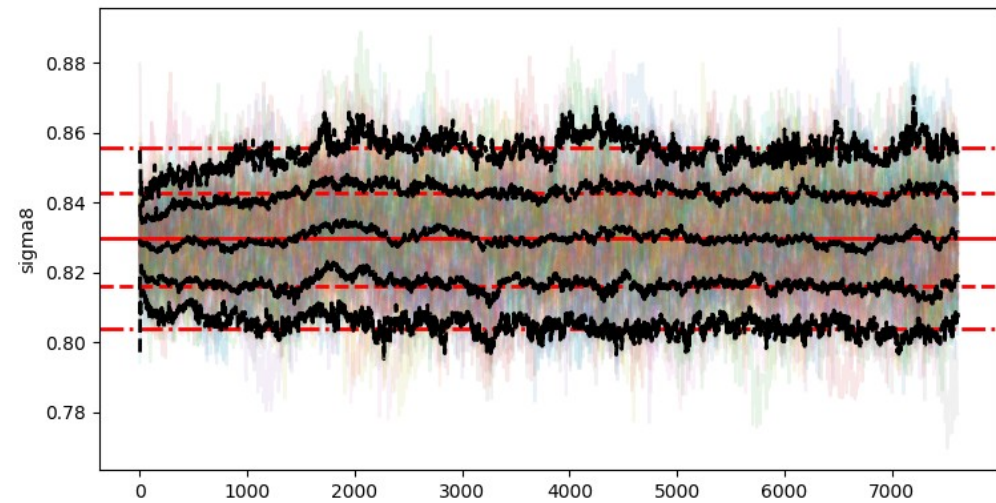
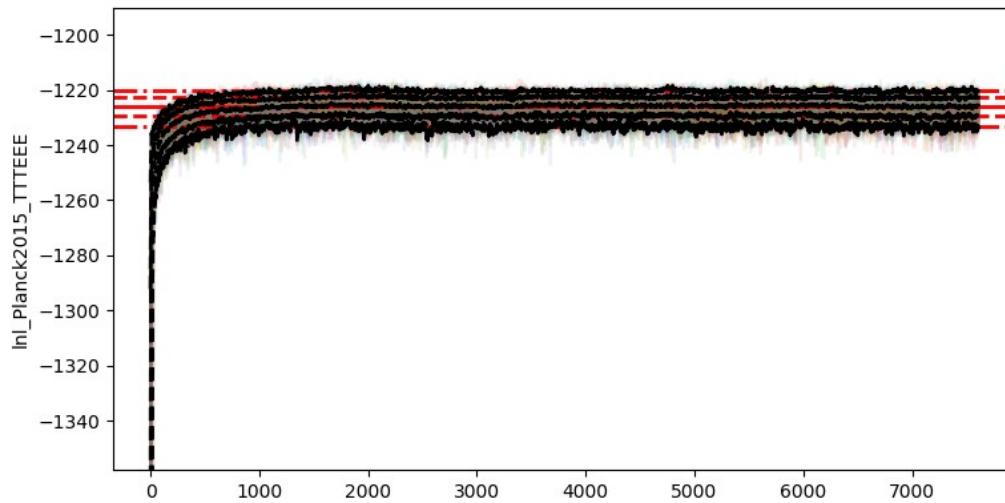
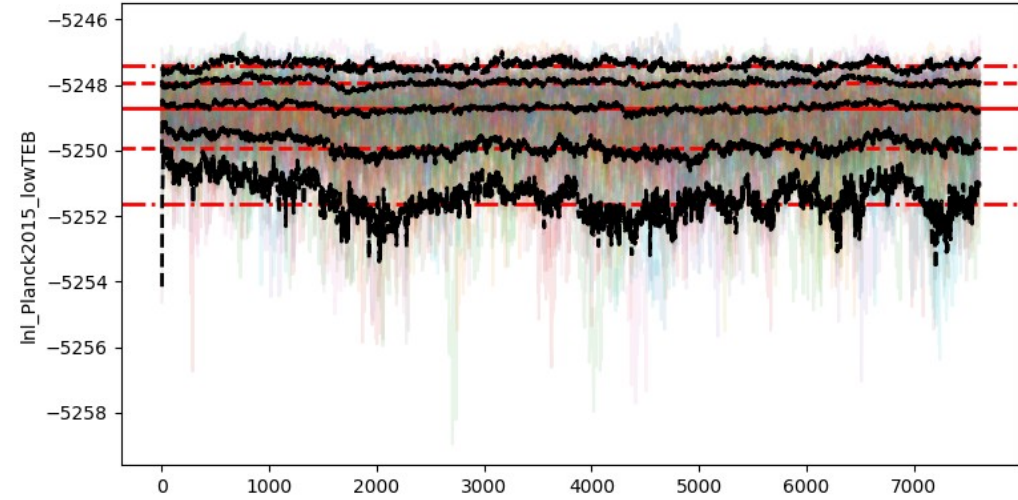
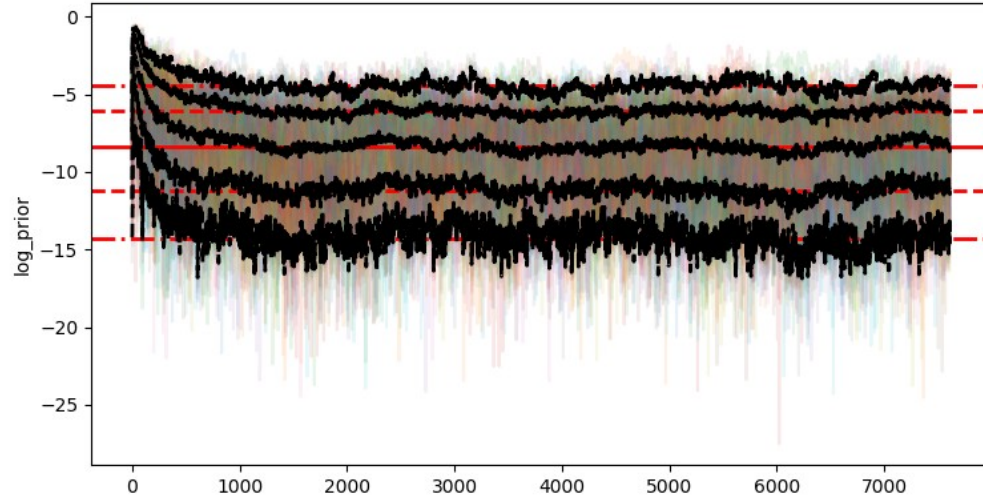
Visualization tools



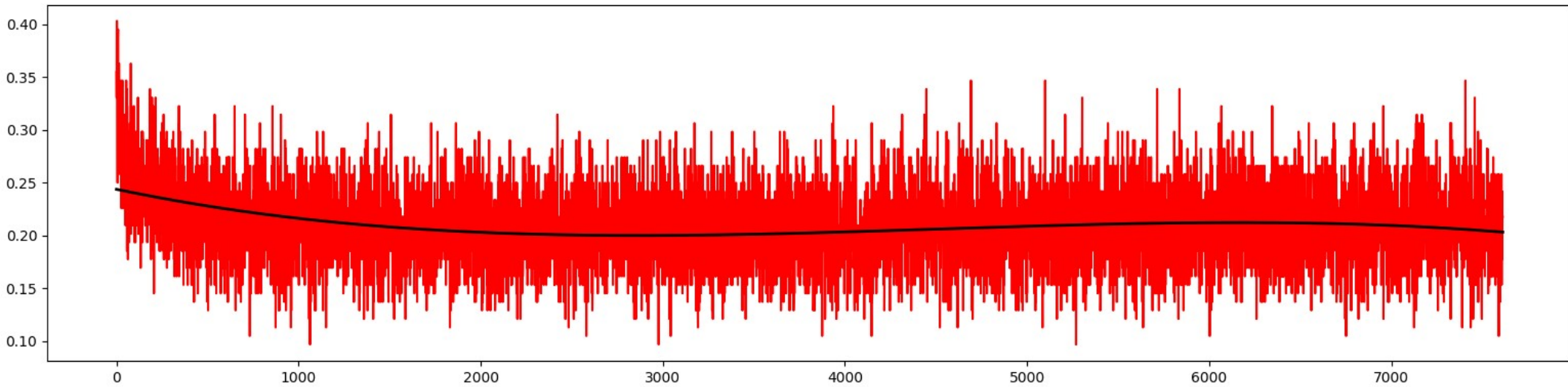
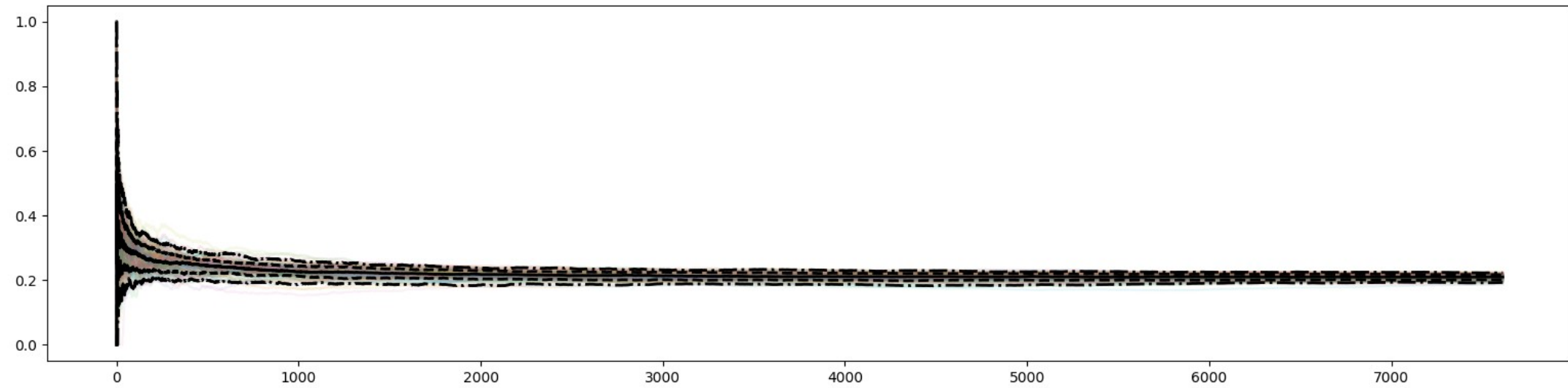
Visualization tools



Visualization tools



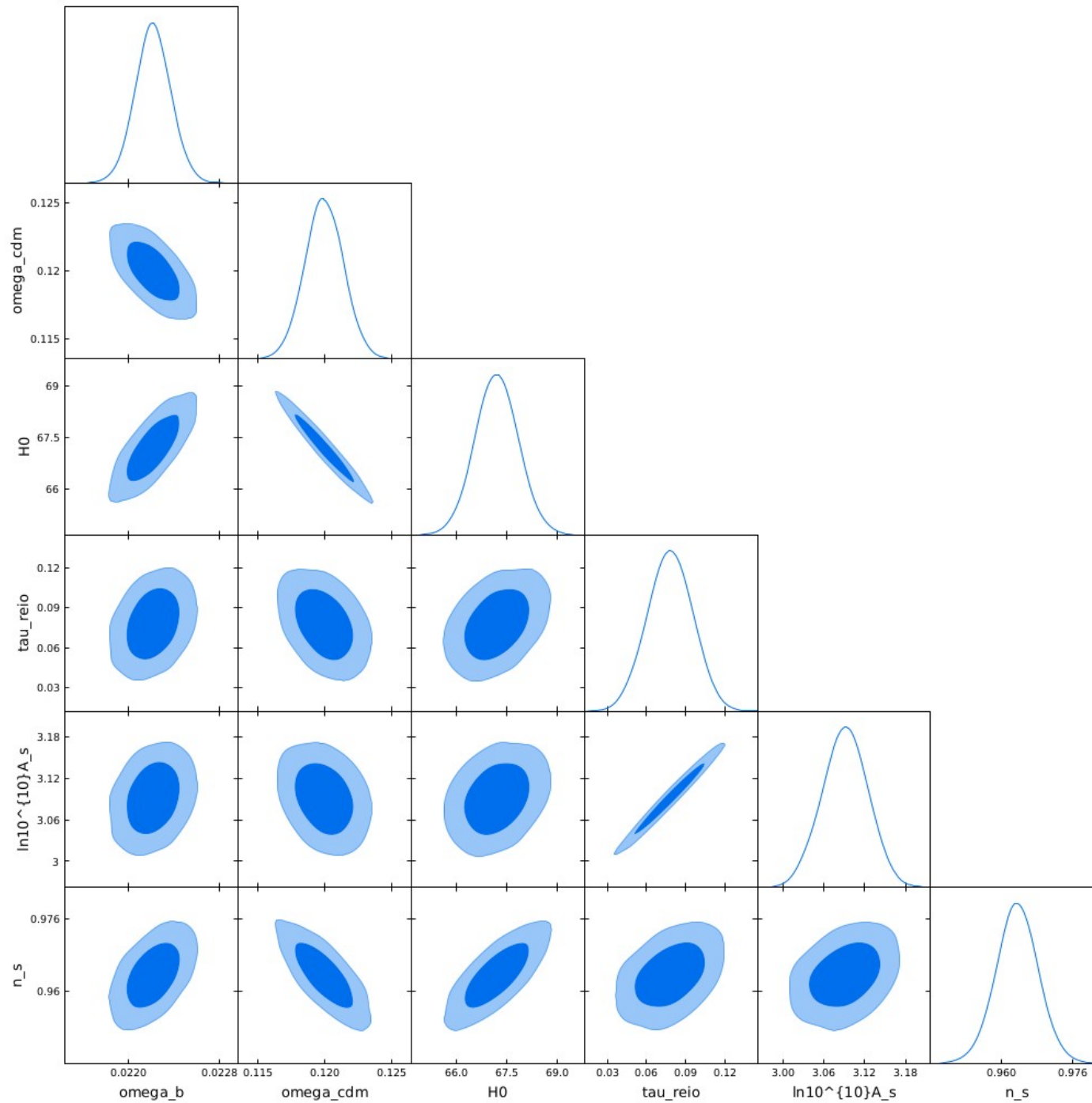
Visualization tools



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- Contour plot scripts (interfaced with getdist)

Contour plots



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- Contour plot scripts (interfaced with getdist)
- Convenient custom parser : “constraint” and “deriv” features

ECLAIR parsing features

```
File Edit Selection View Go Debug Terminal Help template.ini - Visual Studio Code
template.ini x
home > silic > Science > JAM > template.ini
309 #####
310
311 #-----#
312 # Put constraints on parameters #
313 #-----#-----#
314 # Syntax :-----#
315 # > constraint XXX = YYY-----#
316 # > where XXX is the parameter forced to be equal to YYY-----#
317 # Notes :-----#
318 # > YYY can be any fonction of any parameter-----#
319 # > in XXX and YYY, use syntax class[par_name] if class parameter #
320 # > in XXX and YYY, use syntax likes[par_name] otherwise-----#
321 # Examples :-----#
322 # > class[omega_b] = class[omega_cdm]-----#
323 #-----#
324 #constraint class[par_1] = class[par_2]+class[par_3]
325
326 #-----#
327 # Request some derived parameters in output #
328 #-----#-----#
329 # Syntax :-----#
330 # > deriv name quantity_requested-----#
331 # Notes :-----#
332 # > "name" == name of derived parameter in chain (should contain no space) #
333 # > "quantity_requested" can be any command one wants-----#
334 # > class wrapper accessible via "class_run" instance-----#
335 # > class background quantities accessible via "bg" dictionary-----#
336 # > class parameters accessible via "class_input" dictionary-----#
337 # > nuisance parameters accessible via "likes_input" dictionary-----#
338 # Examples :-----#
339 # > for H0 : deriv H0 bg['H [1/Mpc]'][-1]*299792.458-----#
340 # > for sigma_8 : deriv sigma_8 class_run.sigma8()-----#
341 # > for sum_nu : deriv sum_nu class_input['m_ncdm_val_0']+.-----#
342 #-----#
343 # deriv H0 bg['H [1/Mpc]'][-1]*299792.458
344
```


Introducing : ECLAIR

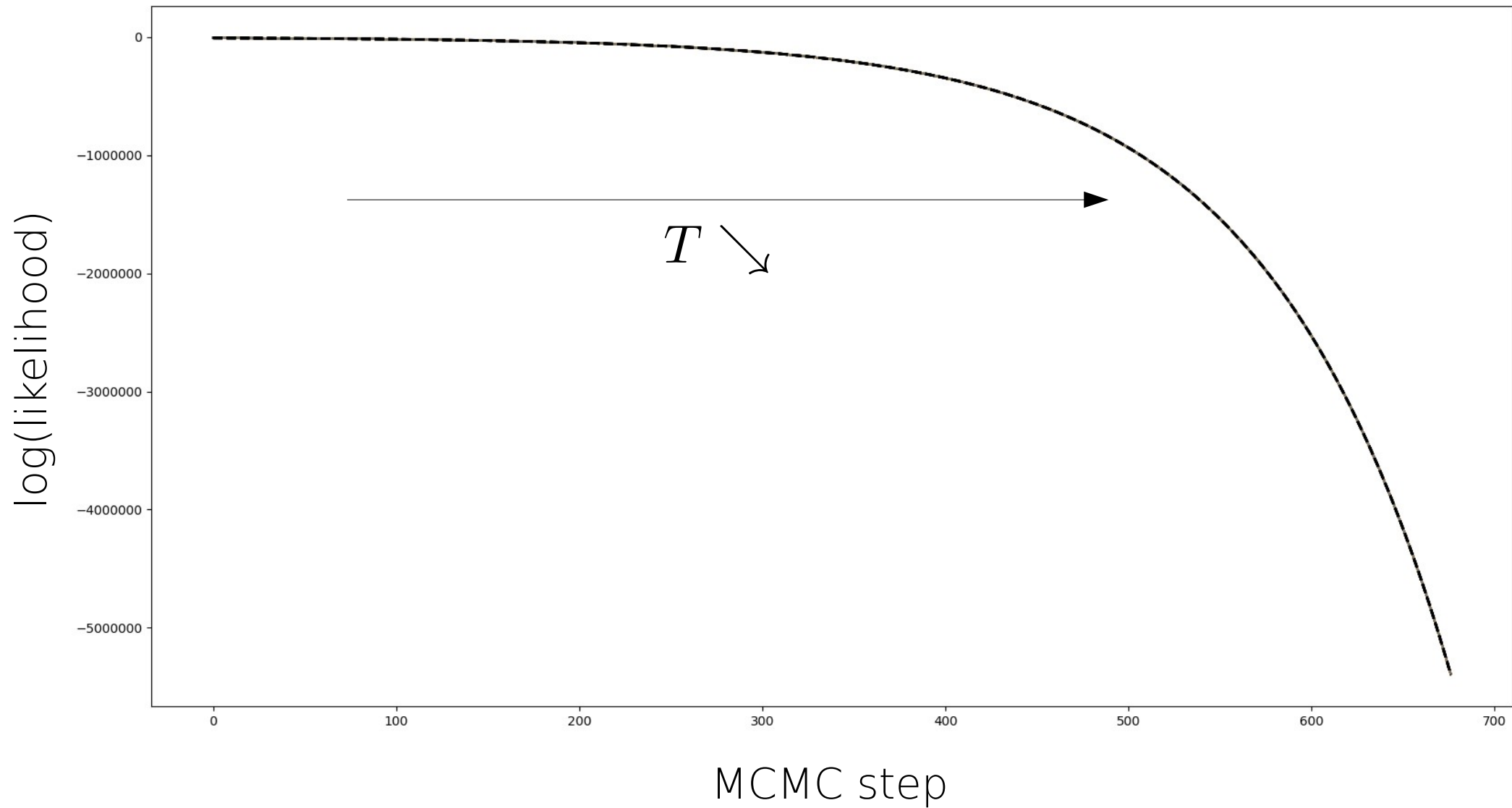
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- Contour plot scripts (interfaced with getdist)
- Convenient custom parser : “constraint” and “deriv” features
- Robust minimizer combining simulated annealing & ensemble sampling

Minimizing with ECLAIR

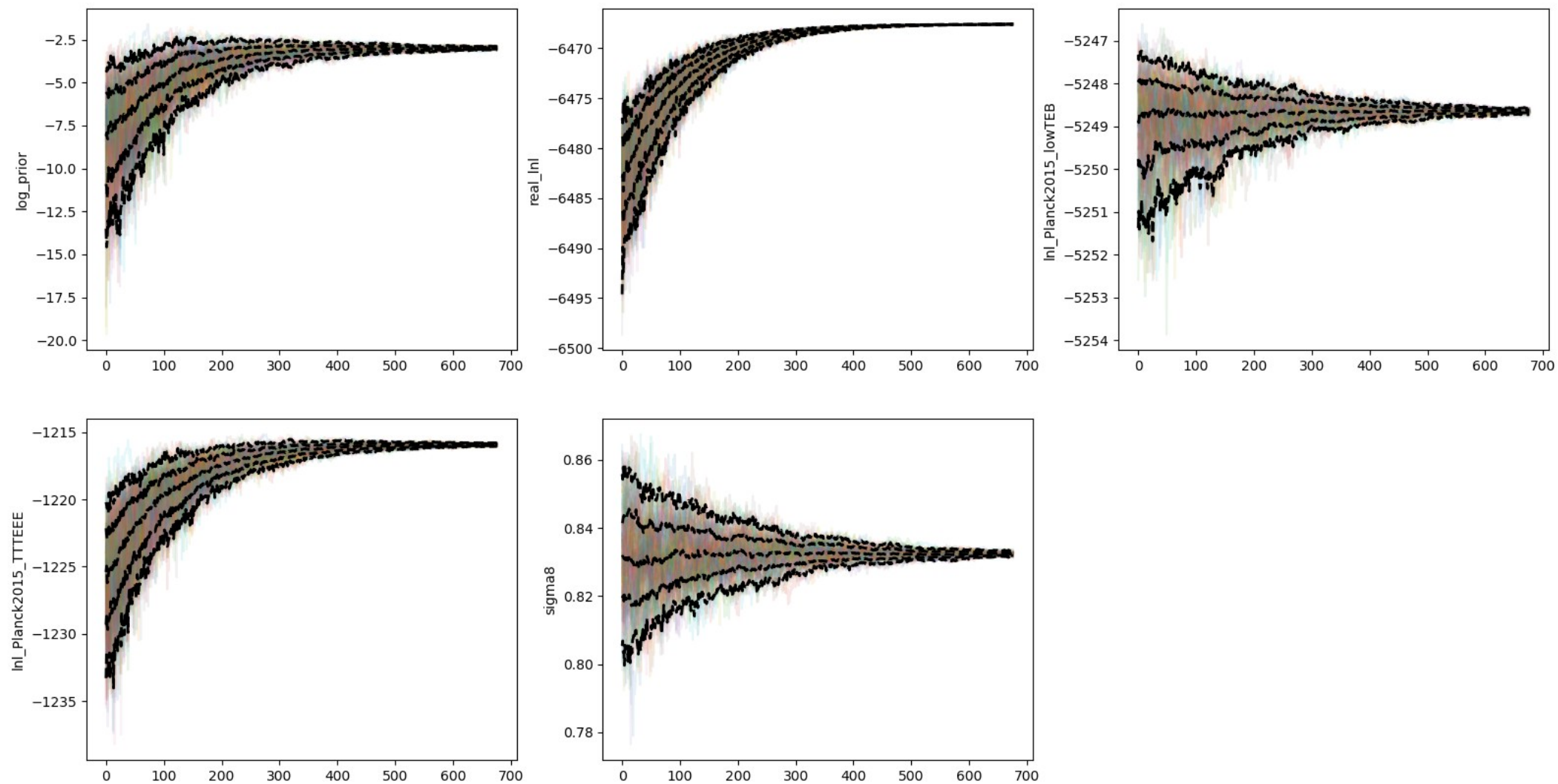
$$\mathcal{L} \longrightarrow \mathcal{L}^{1/T}$$

Minimizing with ECLAIR

$$\mathcal{L} \longrightarrow \mathcal{L}^{1/T}$$

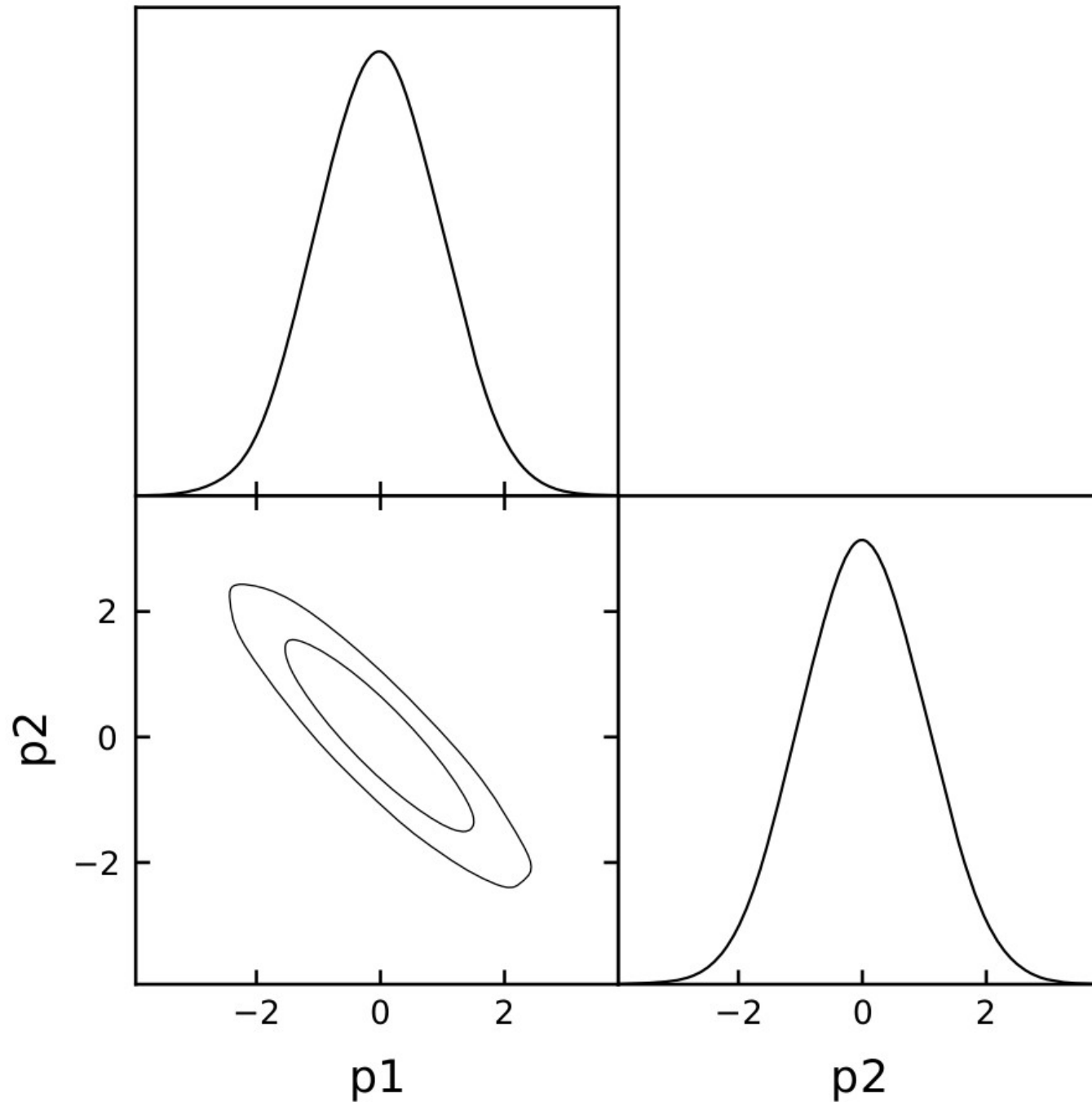


Minimizing with ECLAIR

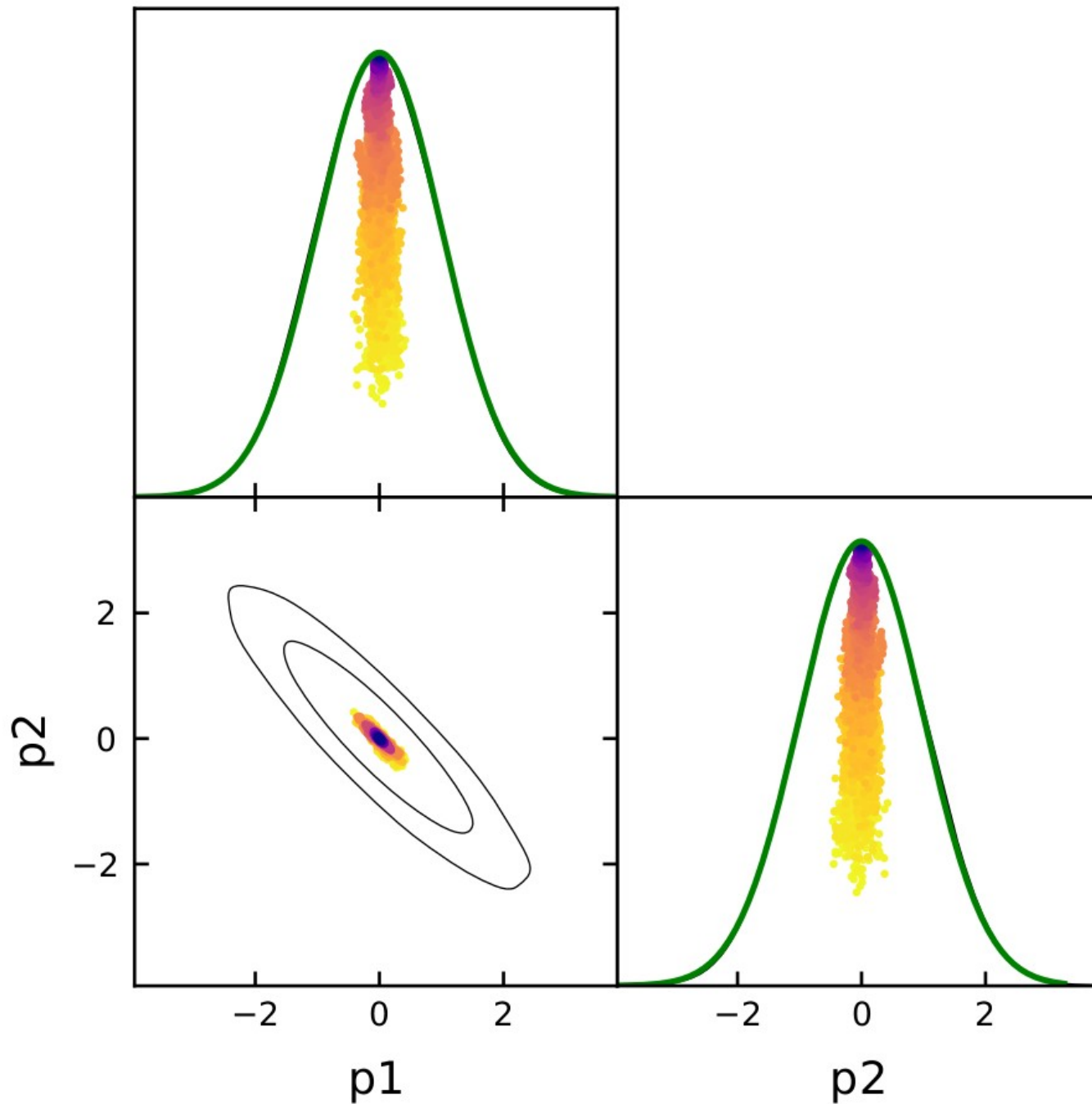


Identifying prior effects with ECLAIR

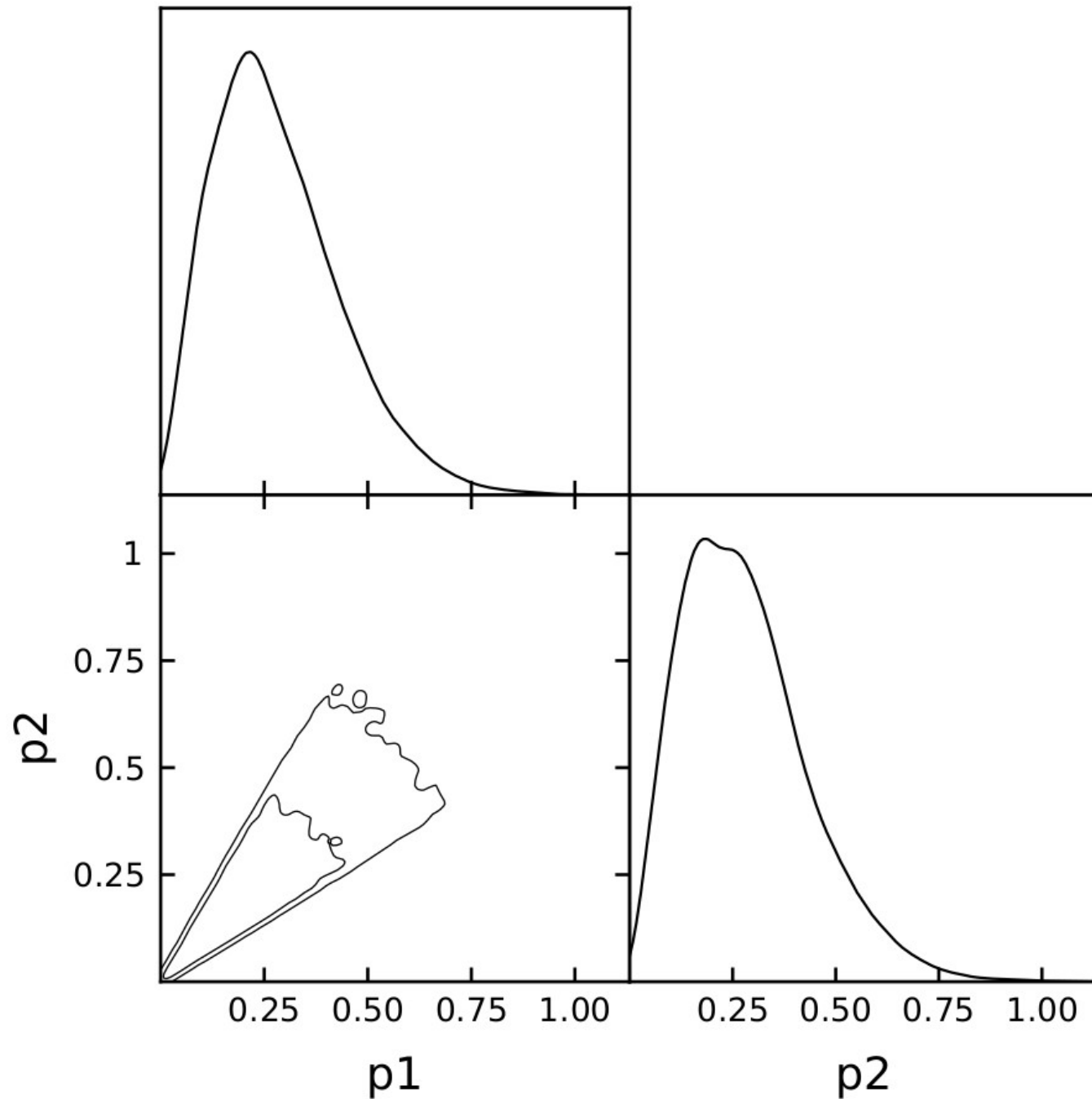
Identifying prior effects with ECLAIR



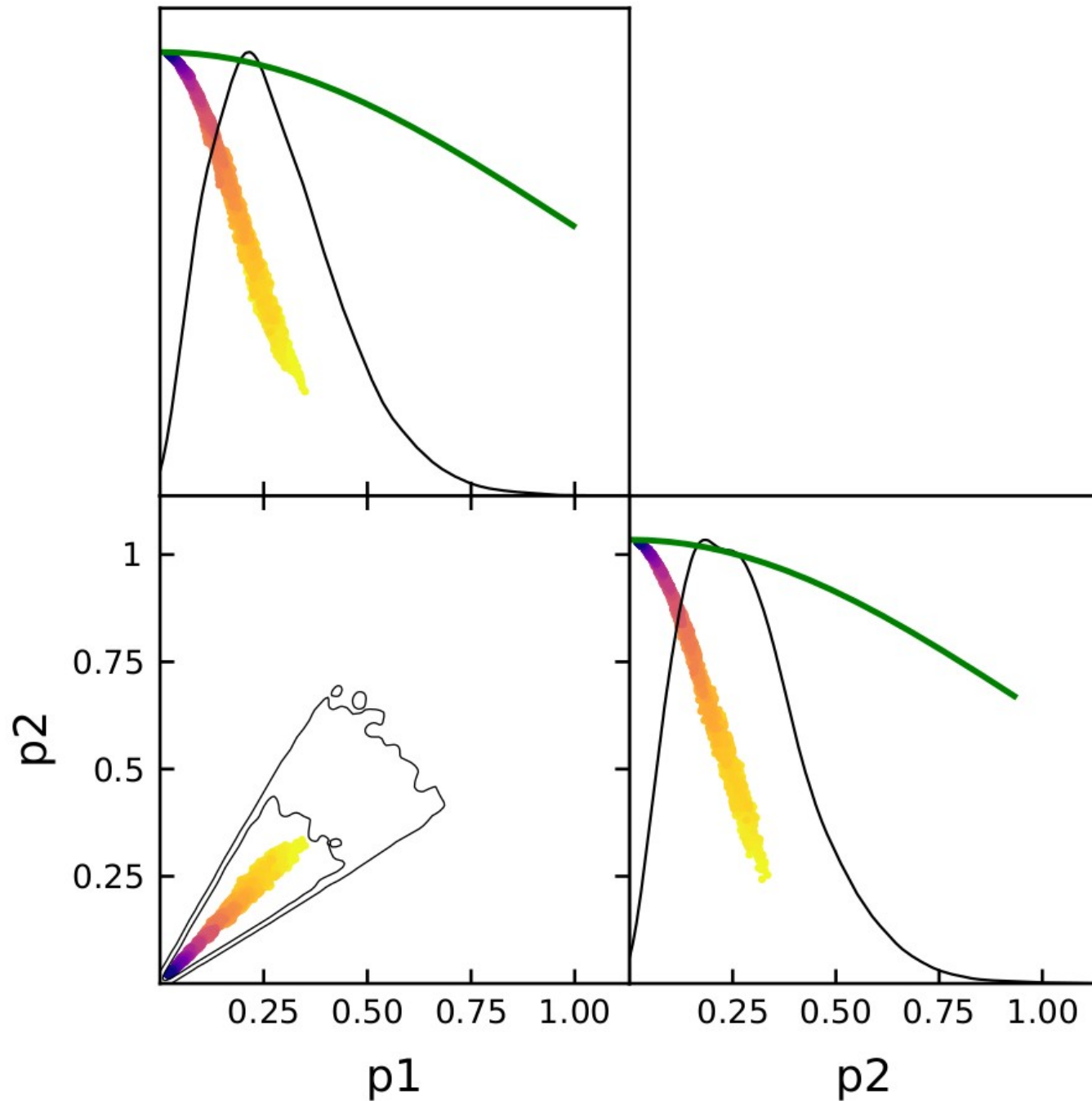
Identifying prior effects with ECLAIR



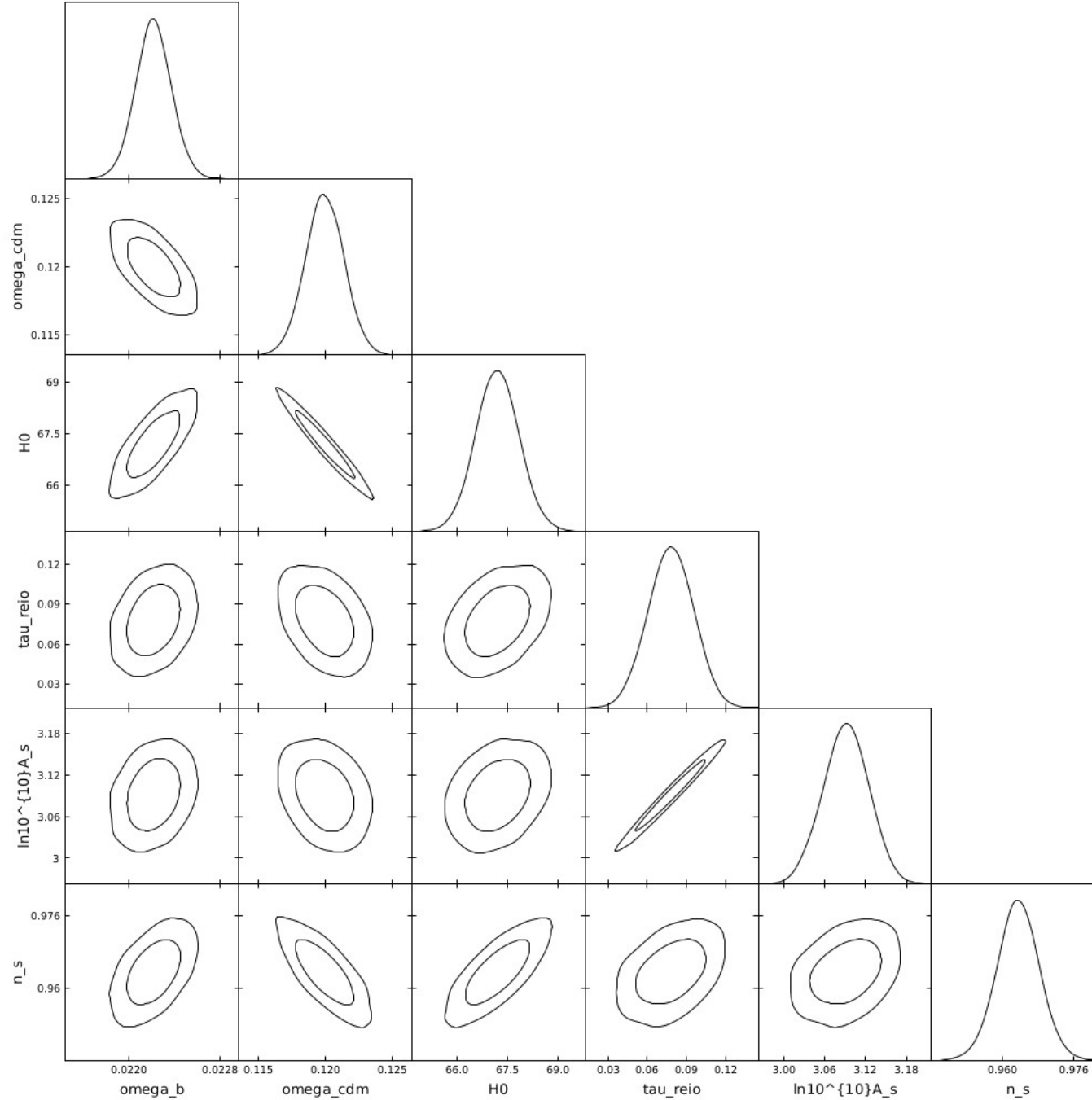
Identifying prior effects with ECLAIR



Identifying prior effects with ECLAIR



Identifying prior effects with ECLAIR



Identifying prior effects with ECLAIR

