

Gyroscopic Gravitational Memory

Blagoje Oblak

LPTHE (Sorbonne) & CPHT (Polytechnique)

arXiv 2112.04535 with A. Seraj



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Intro

(How a top sees gravitational waves)

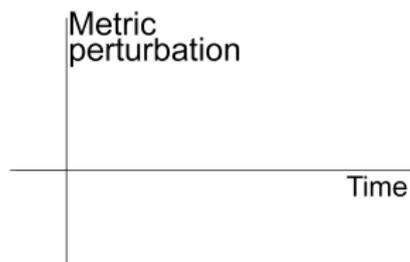
TWO MOTIVATIONS

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1. Observable **gravitational waves** !

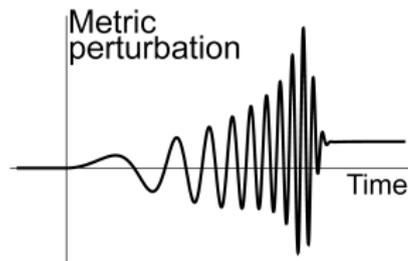
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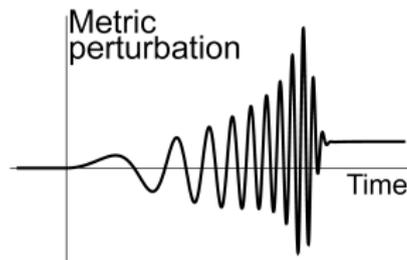
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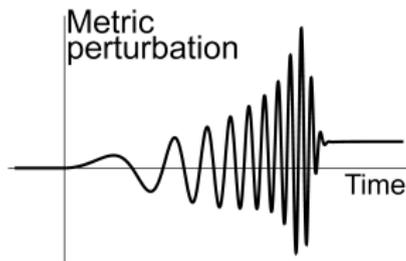
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 - ▶ Measurable implications ?



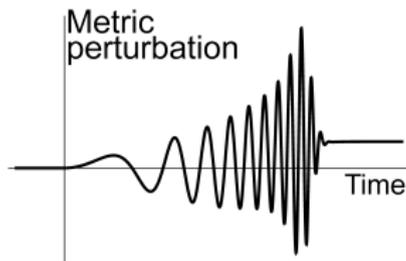
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 - ▶ **Memory effect** :



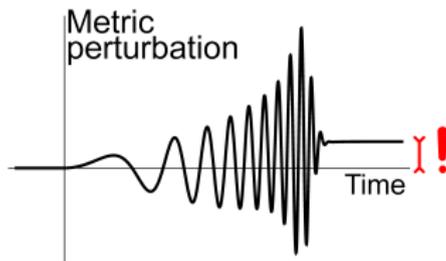
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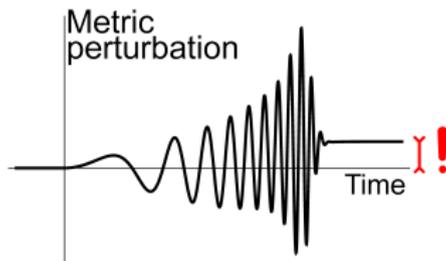
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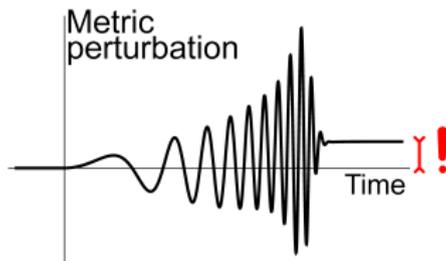


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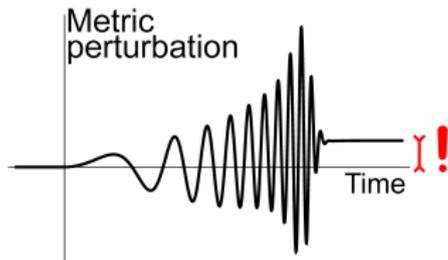
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- ▶ Large distance **asymptotic symmetries**

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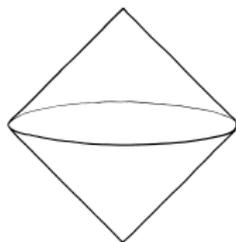
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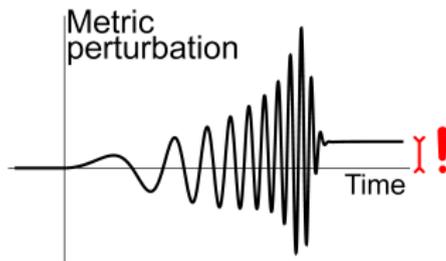
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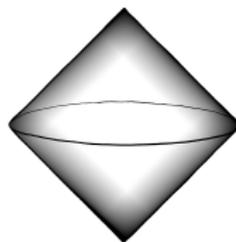
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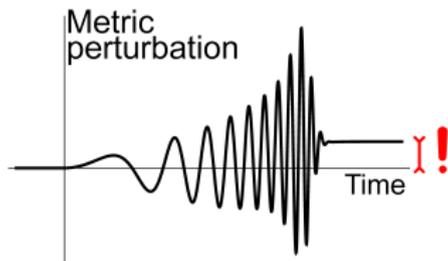
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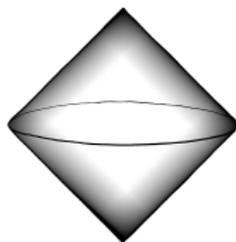
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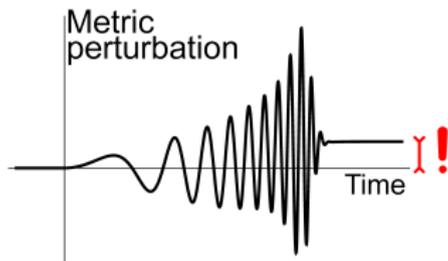
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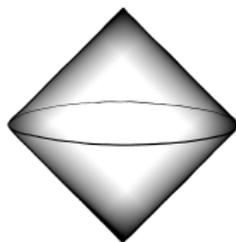
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Memory = **observable** effect of gravitational **symmetries**

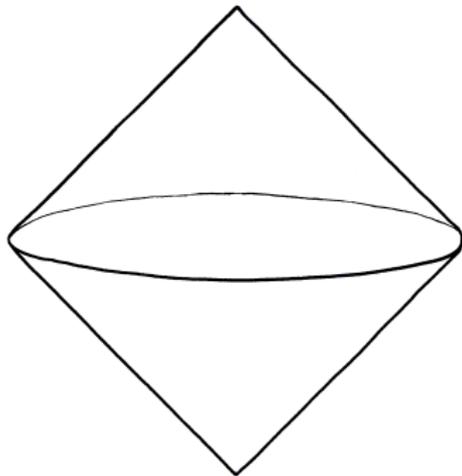
THIS TALK IN A NUTSHELL

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Gravitational **memory** seen with freely falling **gyroscope**

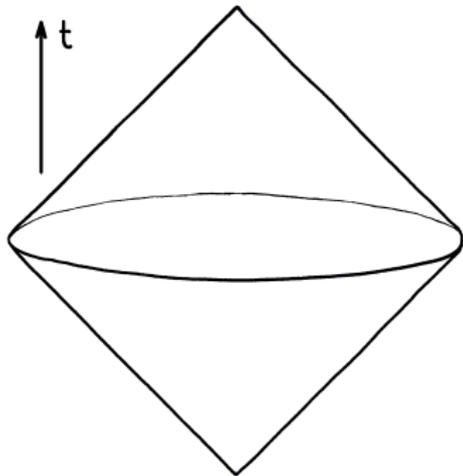
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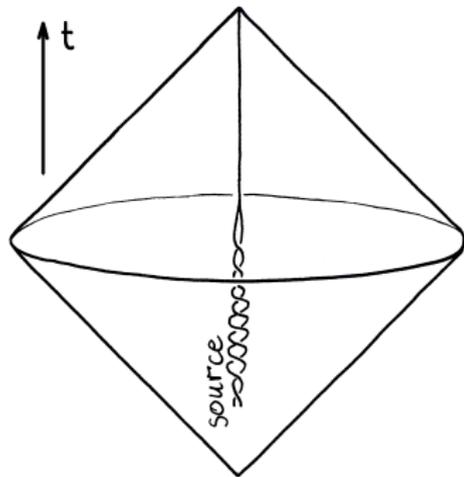
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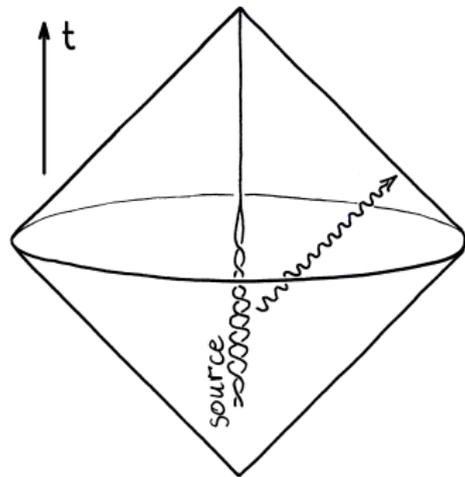
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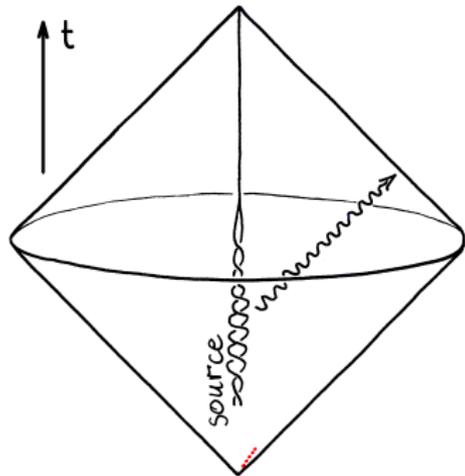
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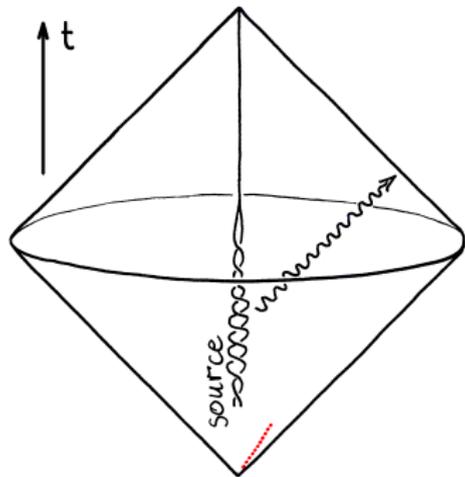
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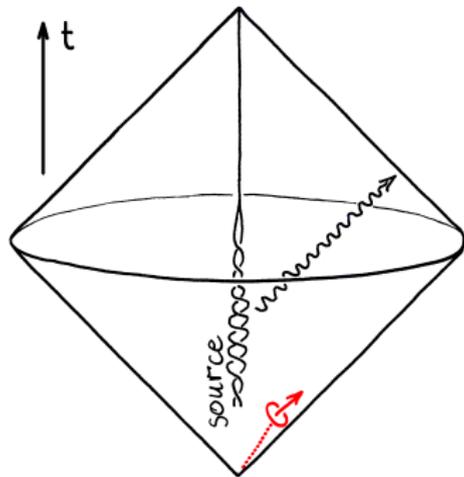
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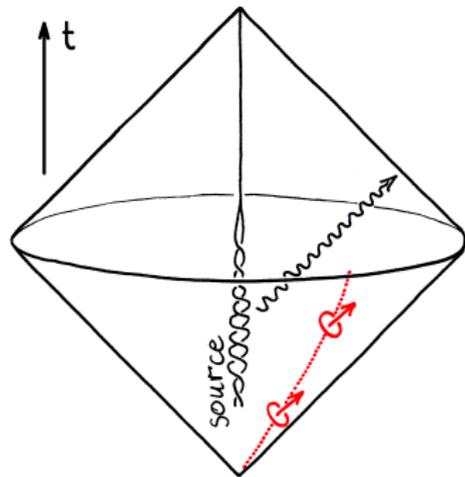
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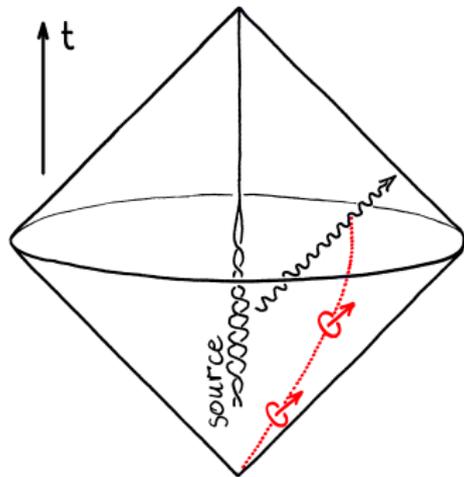
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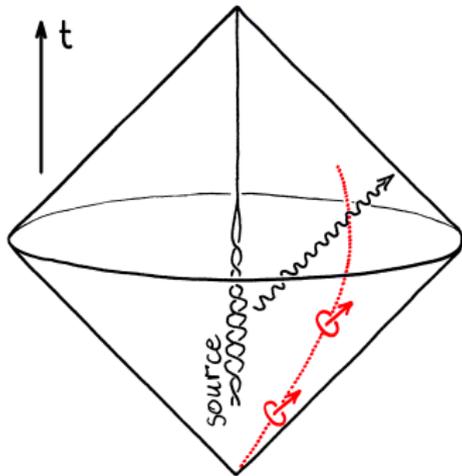
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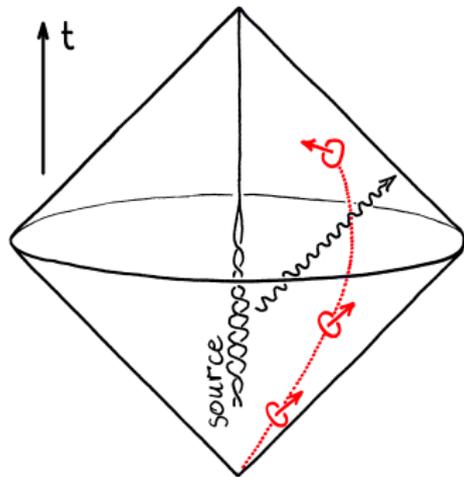
Waves cause precession



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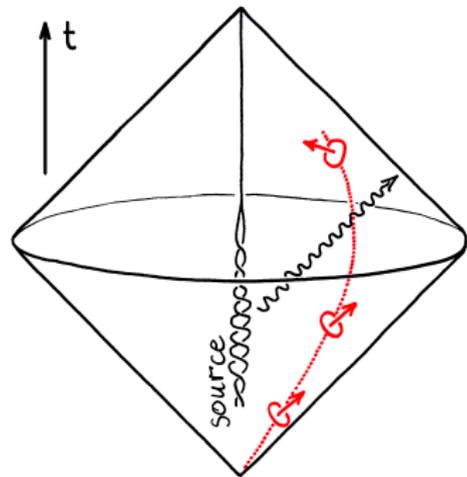
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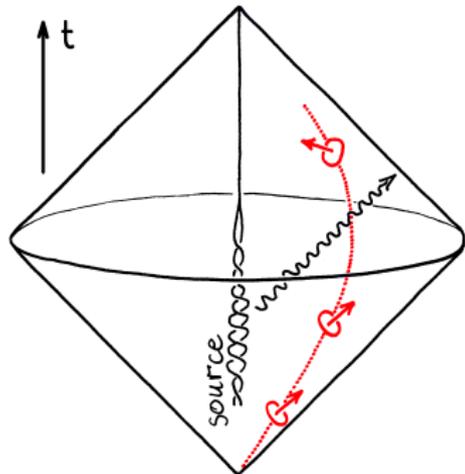
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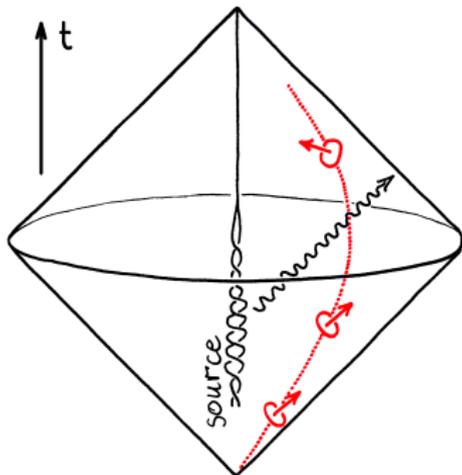
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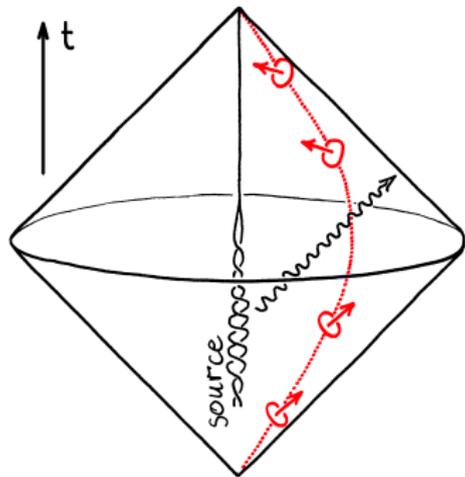
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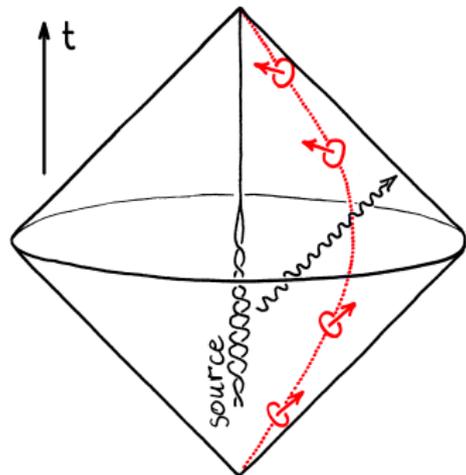


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Gravitational **memory** seen with freely falling **gyroscope** :

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- ▶ Orientation memory !



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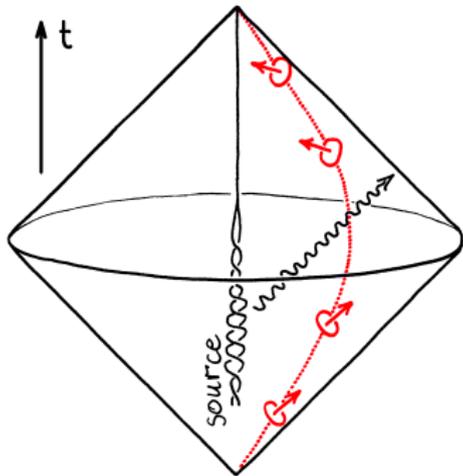
Gravitational **memory** seen with freely falling **gyroscope** :

Waves cause precession

- ▶ Orientation memory !

Underlying symmetries :

- ▶ Precession rate = current of **dual supertranslations**
- ▶ Memory involves **electric-magnetic duality**



PLAN

PLAN

1. Method

PLAN

1. Method : Build a frame tied to distant stars

PLAN

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2. Result

PLAN

1. Method : Build a frame tied to distant stars

2. Result : Gyroscopic precession and memory

1. Method

(Stargazing in wobbly space-times)

SPACE-TIME METRIC

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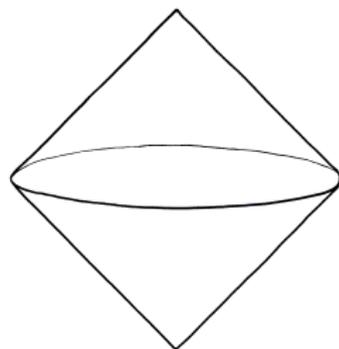
Minkowski in polar coordinates :

$$ds^2 = -dt^2 + dr^2 + r^2 h_{ab} d\theta^a d\theta^b$$

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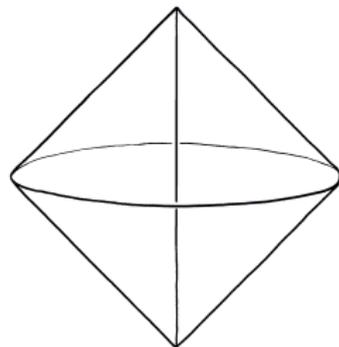
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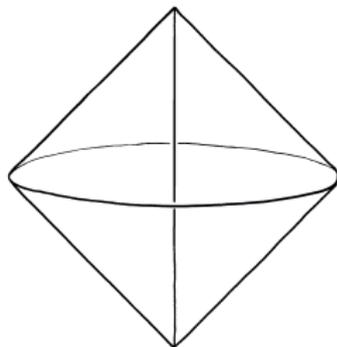
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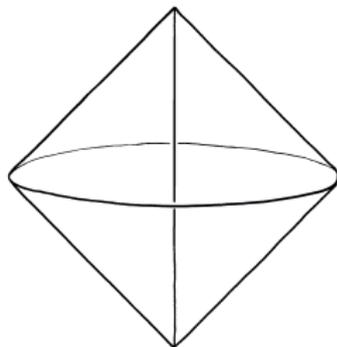
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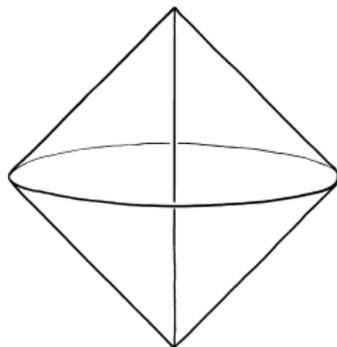
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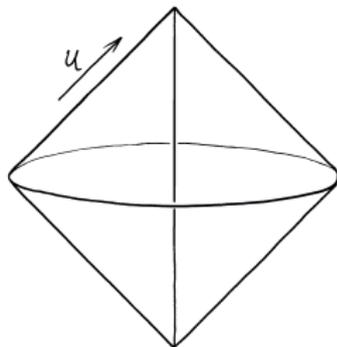
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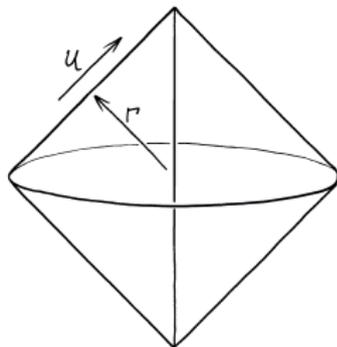
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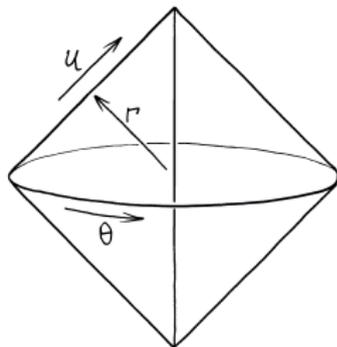
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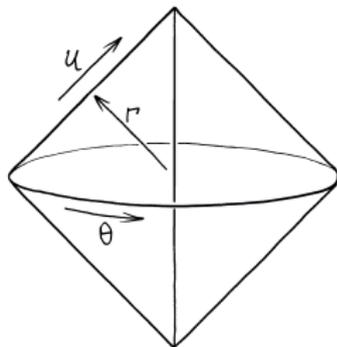


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- ▶ Null infity at $r \rightarrow \infty$

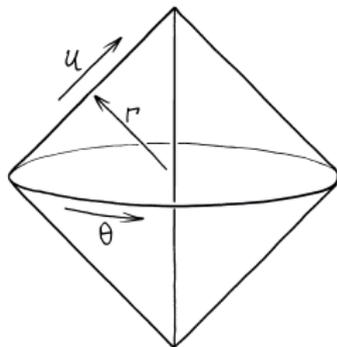


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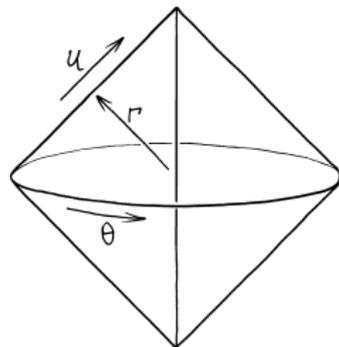
Observer sees **asymptotically flat** metric :

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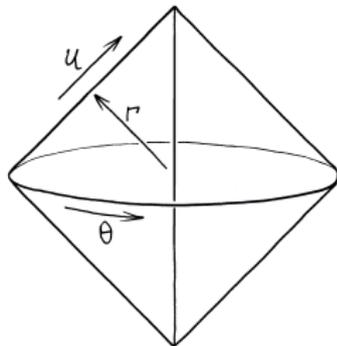
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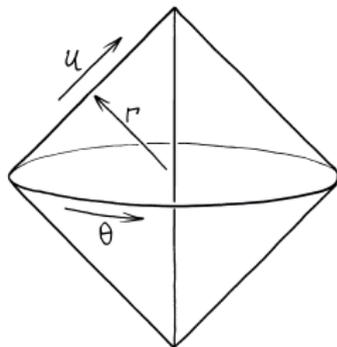
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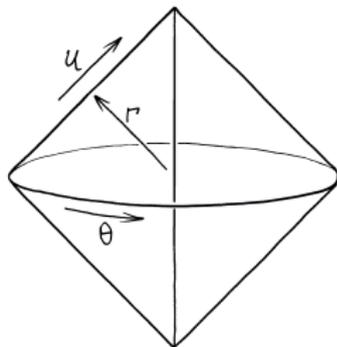
$$ds^2 \sim -\left(1 + \dots^{\text{mass}}\right) du^2 - \left(2 + \dots\right) du dr$$

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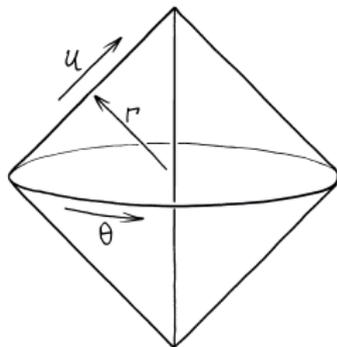
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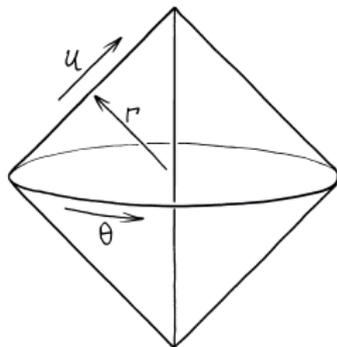
mass
angular mom

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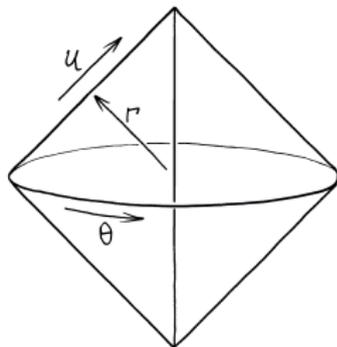
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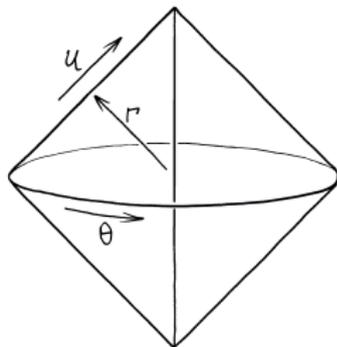
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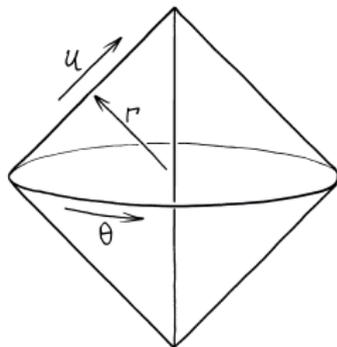
- $C_{ab}(u, \theta)$

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$$ds^2 \sim -\overset{\text{mass}}{(1 + \dots)} du^2 - \overset{\text{angular mom}}{(2 + \dots)} du dr + (\dots) du d\theta^a + (r^2 h_{ab} + r C_{ab} + \dots) d\theta^a d\theta^b$$

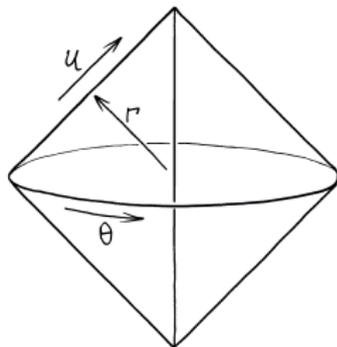
- $C_{ab}(u, \theta) =$ aspt **shear** of null rays

SPACE-TIME METRIC

Minkowski in **Bondi** coordinates ($u = t - r$):

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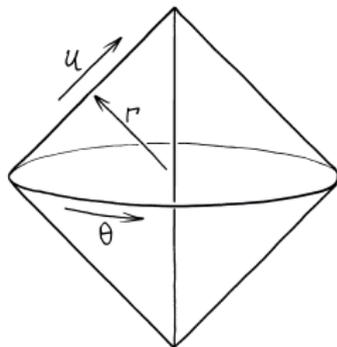
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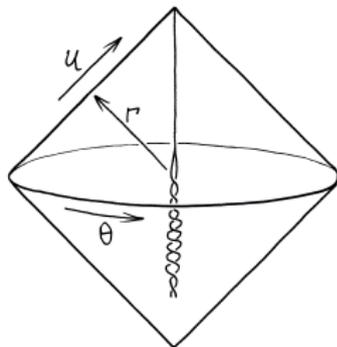
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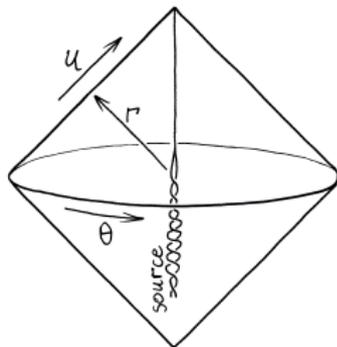
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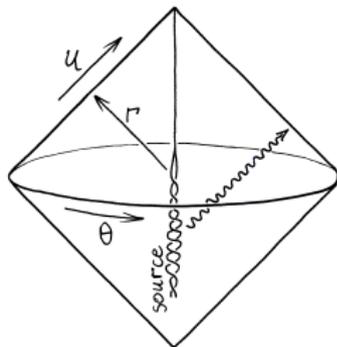
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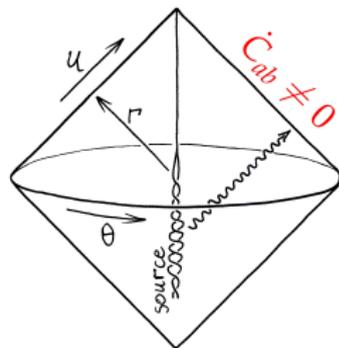
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LOCAL FRAME

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Freely falling observer

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LOCAL FRAME

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LOCAL FRAME

Freely falling observer



LOCAL FRAME

Freely falling observer with gyroscope



LOCAL FRAME

Freely falling observer with gyroscope



LOCAL FRAME

Freely falling observer with gyroscope

Measure orientation ?



LOCAL FRAME

Freely falling observer with gyroscope

Measure orientation :

- ▶ Build **source-oriented frame**



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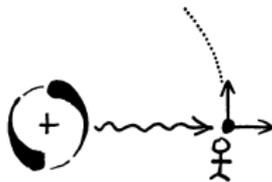


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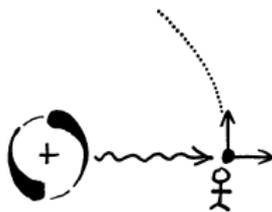


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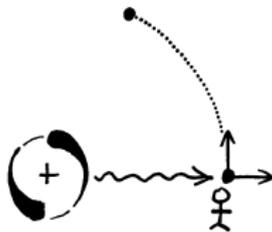


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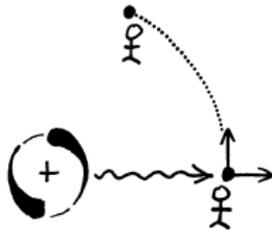


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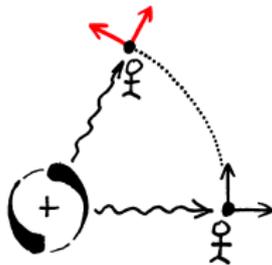


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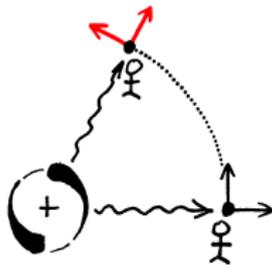


LOCAL FRAME

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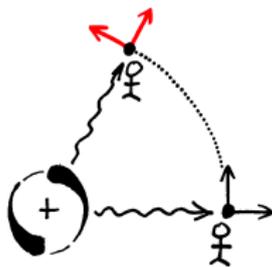
LOCAL FRAME

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Choose **distant stars** instead



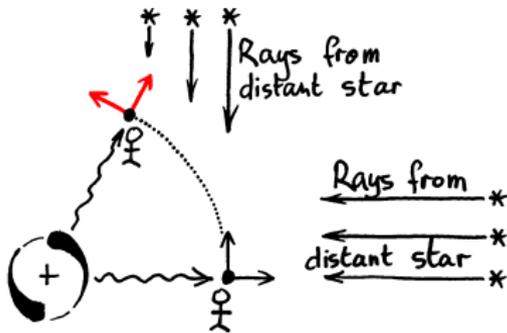
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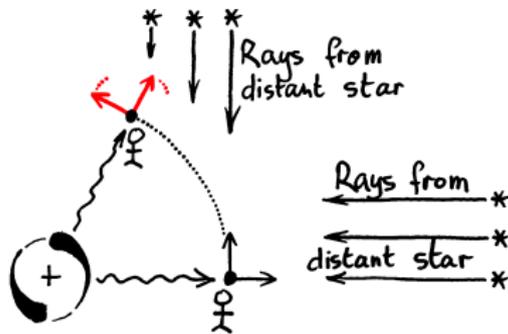
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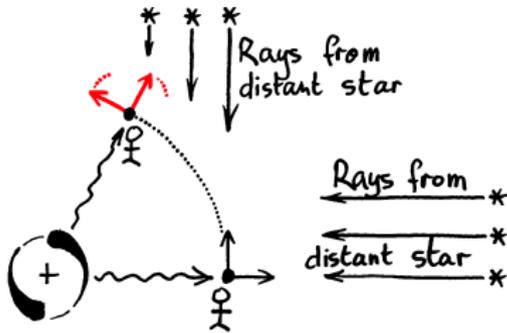
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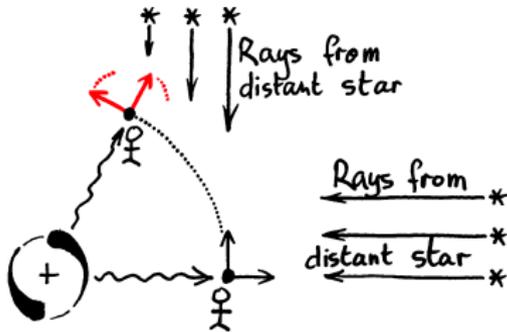
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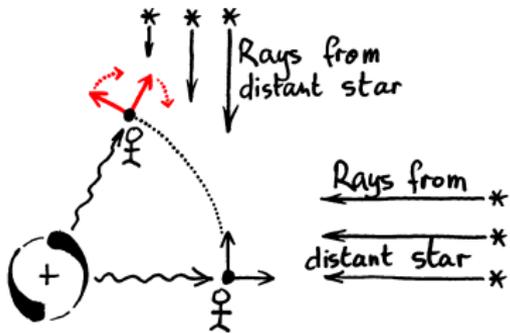
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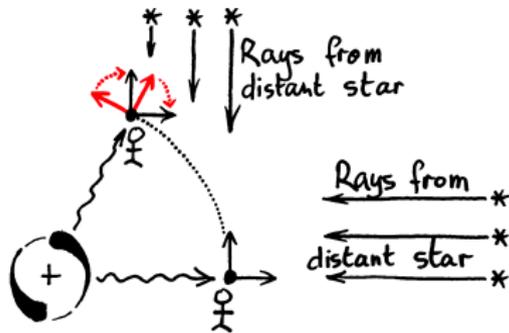
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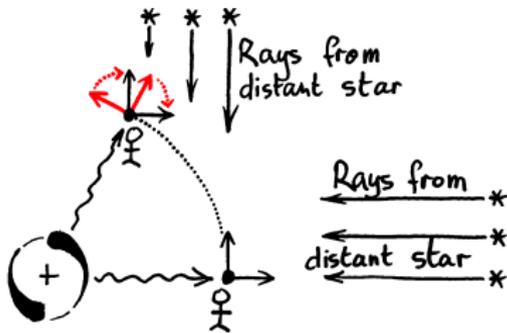
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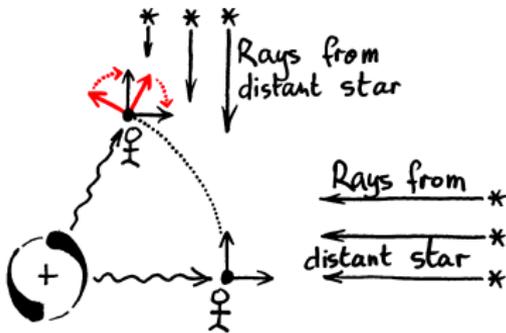
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- ▶ Frame e_1, e_2, e_3



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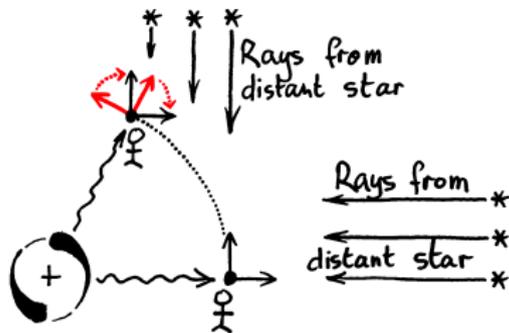
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- ▶ Gyroscope's spin $\mathbf{S} = S^i e_i$



Parallel transport \leftrightarrow **precession** $\dot{\mathbf{S}} = \boldsymbol{\Omega} \times \mathbf{S}$

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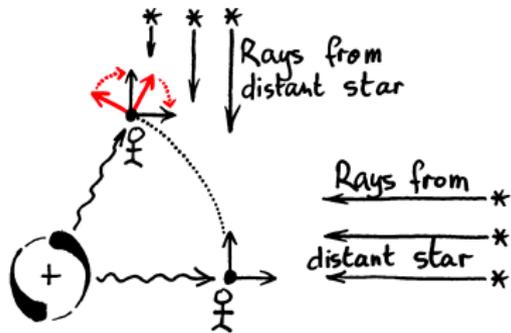
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- ▶ **Find $\boldsymbol{\Omega}$!**

2. Results

Precession and orientation memory

RADIATION CAUSES PRECESSION

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$$DD\tilde{C} - \frac{1}{2}\dot{C}\tilde{C} = \text{dual mass aspect} \quad [\text{Porrati+, Godazgar+, Freidel+,...}]$$

ORIENTATION MEMORY

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Precession $\dot{\mathbf{S}} = \boldsymbol{\Omega} \times \mathbf{S}$ during radiation burst

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Change of
charge due
to S^2 diffeo

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(superrotation)

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\swarrow \downarrow
 Change of Flux
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Change of charge due to S^2 diffeo
(**superrotation**)

Flux

Duality generator on radiative phase space

