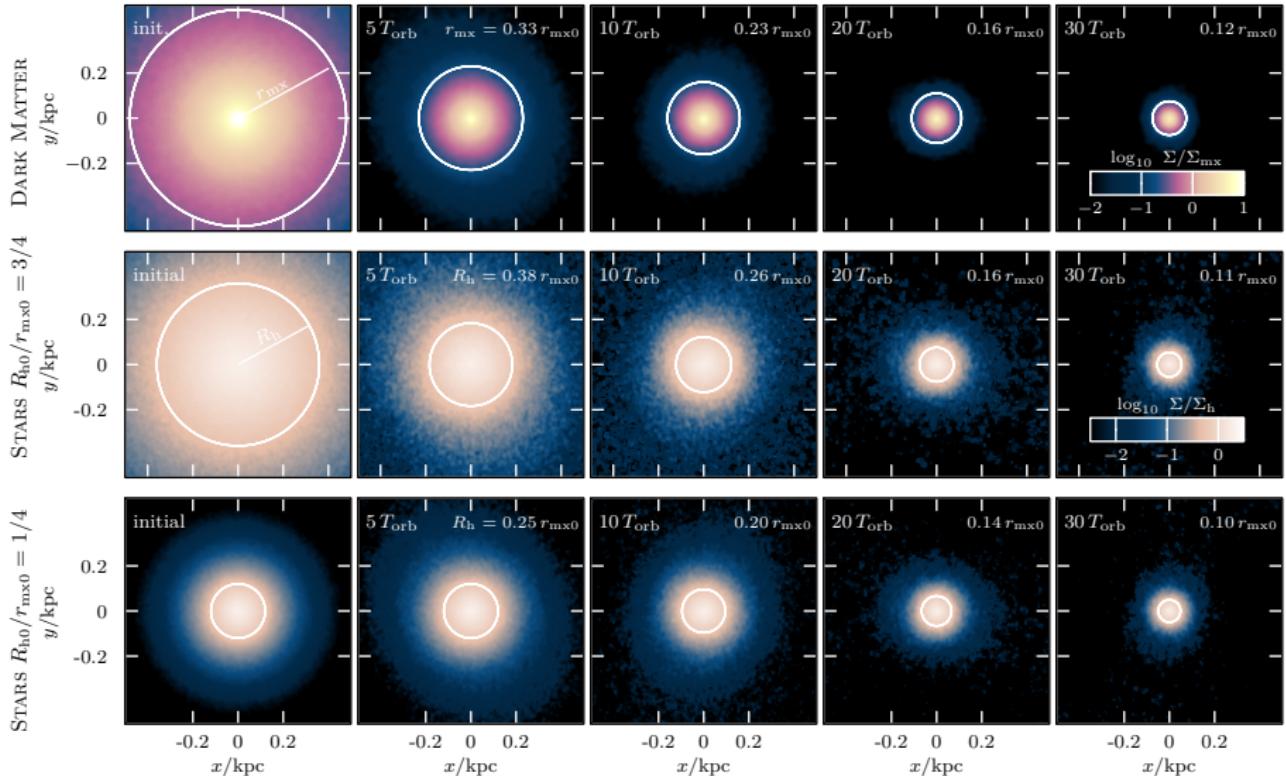


# Structure and kinematics of tidally limited satellite galaxies in LCDM

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with Julio Navarro, Rodrigo Ibata, Jorge Peñarrubia  
arXiv:2111.05866



# Tidal stripping of stellar tracers in NFW subhalo

Numerical setup:

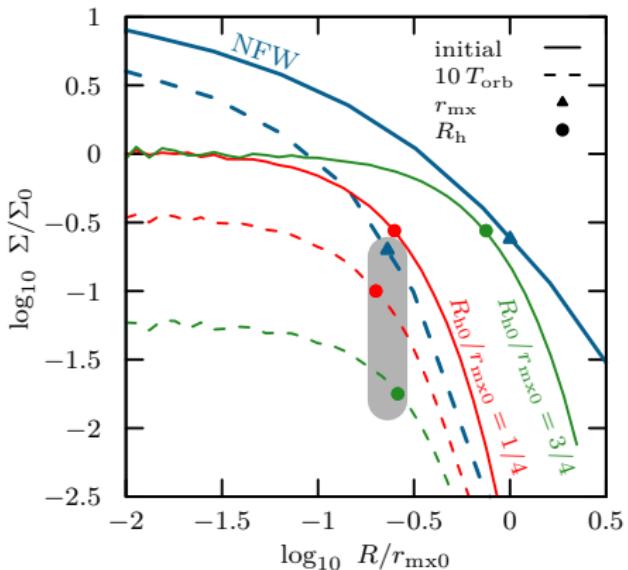
- NFW subhalo, orbiting in an isothermal  $220 \text{ km s}^{-1}$  host halo
- mass-less stellar tracers,  
 $\rho_\star \propto e^{-r/r_\star}$
- stellar probability tagging:  
 $\mathcal{P}_\star(E) = (\mathrm{d}N_\star/\mathrm{d}E)/( \mathrm{d}N_{\mathrm{DM}}/\mathrm{d}E)$

Initial conditions:

- two tracers with initial 2D half-light radii of  
tracer a:  $R_{h0}/r_{\mathrm{mx0}} = 3/4$   
tracer b:  $R_{h0}/r_{\mathrm{mx0}} = 1/4$

Evolved system:

- $R_h \sim r_{\mathrm{mx}}$
- dark matter:  $M_{\mathrm{mx}}/M_{\mathrm{mx0}} = 6\%$
- tracer a:  $L/L_0 = 1\%$
- tracer b:  $L/L_0 = 23\%$



# Stripping of the dark matter: circular velocity

## Circular velocity profiles

- $V_c = \sqrt{GM(< r)/r}$

Convergence of the density profile towards an exponentially truncated cusp

- $\rho_{\text{asy}}(r) = \rho_s \frac{e^{-r/r_s}}{r/r_s}$

Tidal evolution stalls once the subhalo crossing time

- $T_{\text{mx}} = 2\pi r_{\text{mx}}/V_{\text{mx}}$

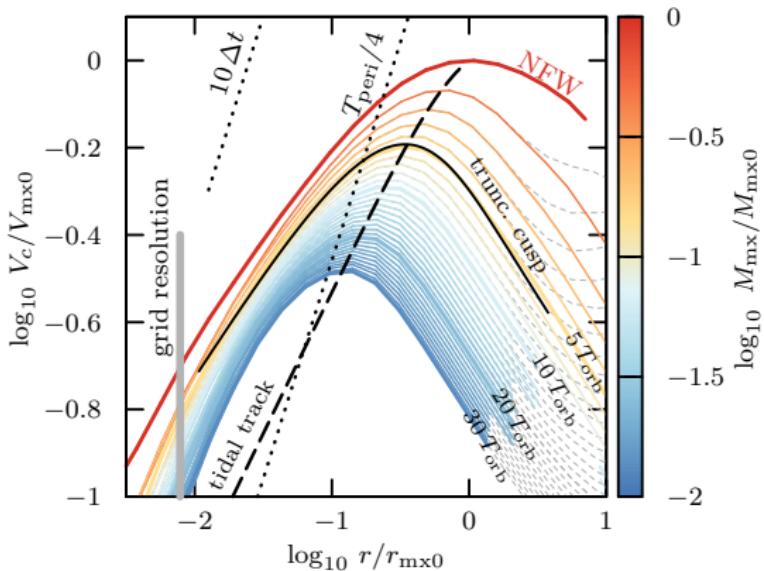
equals 1/4 of the host crossing time at pericentre

- $T_{\text{peri}} = 2\pi r_{\text{peri}}/V_c(r_{\text{peri}})$

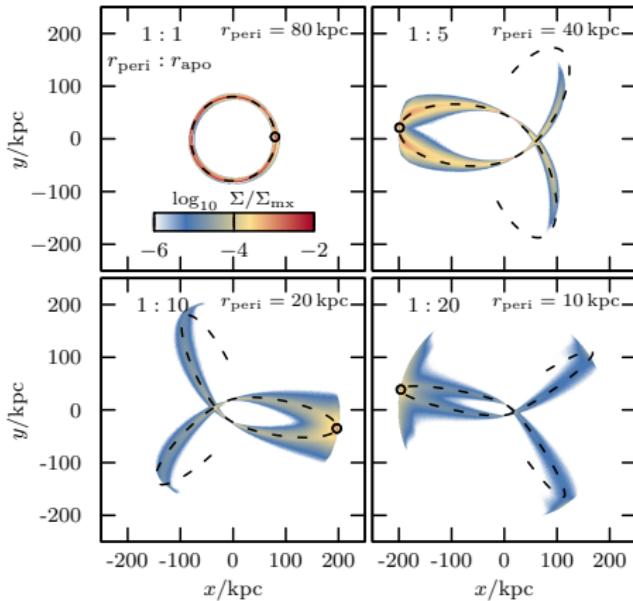
- $T_{\text{mx,asy}} = T_{\text{peri}}/4$

Structural parameters follow *tidal track*

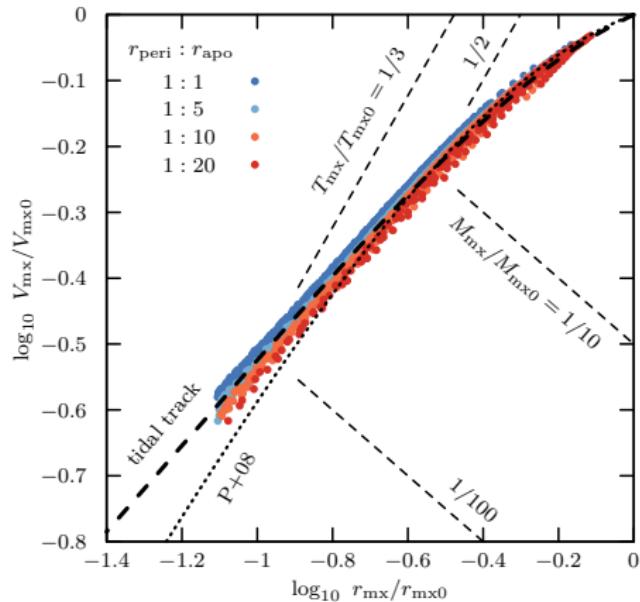
- $\frac{V_{\text{mx}}}{V_{\text{mx}0}} = \frac{2^\alpha (r_{\text{mx}}/r_{\text{mx}0})^\beta}{[1 + (r_{\text{mx}}/r_{\text{mx}0})^2]^\alpha}$



# Stripping of the dark matter: tidal tracks



(EN21, arXiv:2011.07077)



# Stripping of the dark matter: initial conditions

Energies referred to potential minimum  
(ground state)

- $\mathcal{E} \equiv 1 - E/\Phi_0$

Most bound:  $\mathcal{E} = 0$ . Unbound:  $\mathcal{E} \geq 1$ .

Potential minimum correlates with  $V_{\text{mx}}$

- NFW:  $\Phi_0 \approx -4.63 V_{\text{mx}}^2$

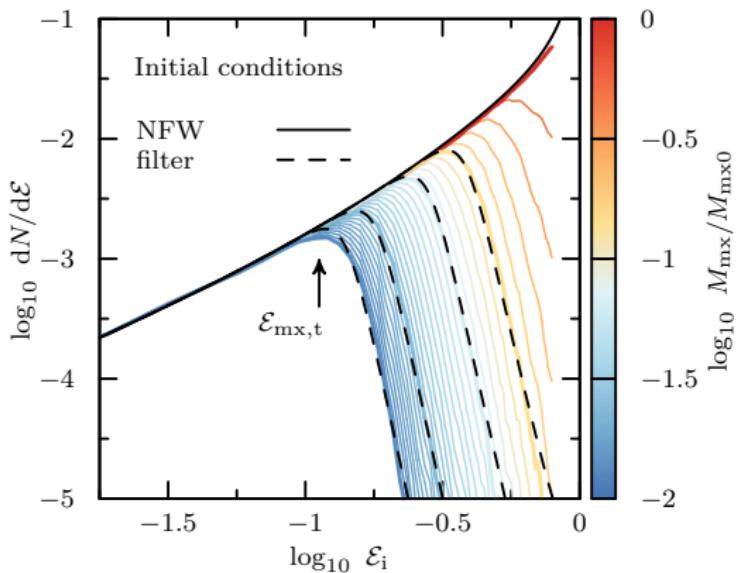
- truncated cusp:  $\Phi_0 \approx -3.35 V_{\text{mx}}^2$

Tides truncate sharply in  $\mathcal{E}$ . Those particles with smallest  $\mathcal{E}$  form the bound remnant.

- $$\frac{dN}{d\mathcal{E}} \Big|_{i,t} = \frac{dN}{d\mathcal{E}} \Big|_i \left[ 1 + (a \mathcal{E}/\mathcal{E}_{\text{mx},t})^k \right]^{-1}$$

(with  $k \approx 12$ ,  $a \approx 0.85$ )

Tidal truncation energy  $\mathcal{E}_{\text{mx},t}$  correlates with remnant mass  $M_{\text{mx}}/M_{\text{mx}0}$



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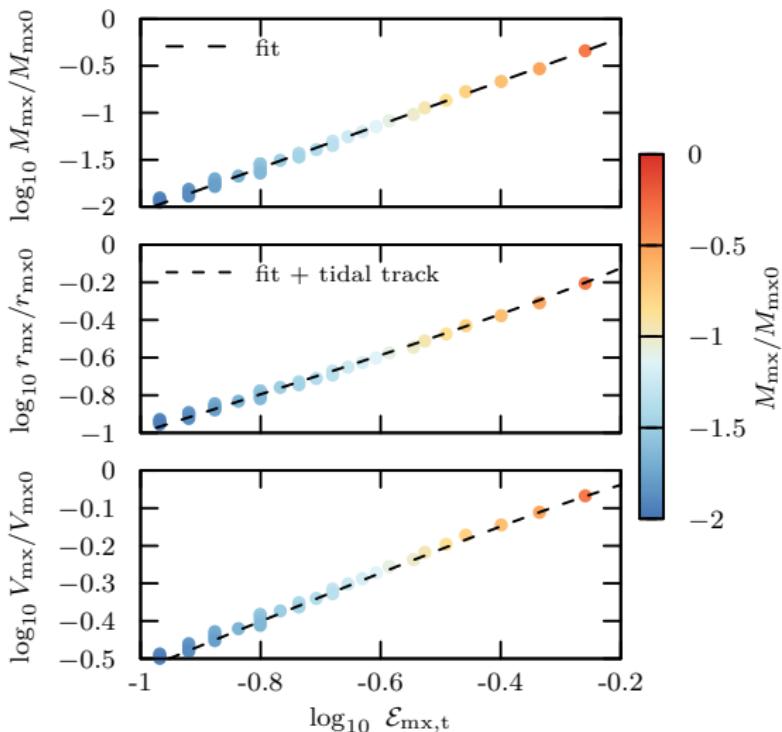
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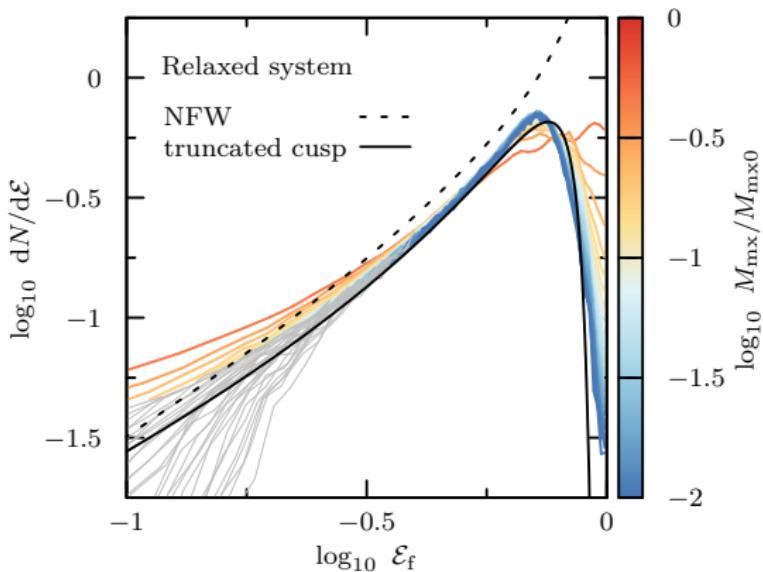
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# Stripping of the dark matter: relaxed system

Convergence of the density profile towards an exponentially truncated cusp

- $\rho_{\text{asy}}(r) = \rho_s \frac{e^{-r/r_s}}{r/r_s}$
- energy distribution has well-defined maximum
- profile converged once  $M_{\text{mx}}/M_{\text{mx0}} \lesssim 1/10$



# Stripping of the dark matter: Initial-to-final energy mapping

Energy: normalised to instantaneous potential minimum

- $\mathcal{E}_i = 1 - E/\Phi_{0,i}$
- $\mathcal{E}_f = 1 - E/\Phi_{0,f}$

Universal energy mapping, form independent of  $M_{\text{mx}}/M_{\text{mx0}}$

- $\bar{\mathcal{E}}_f = \left[ 1 + a (\mathcal{E}_i / \mathcal{E}_{\text{mx,t}})^{-b} \right]^{-1/b}$

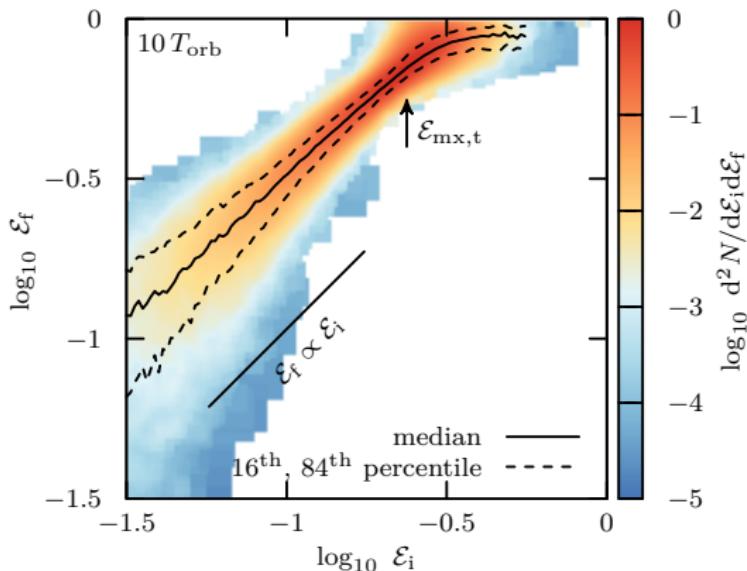
Energy map preserves most-bound energy distribution

- $\mathcal{E}_i < \mathcal{E}_{\text{mx,t}}$ :  $\bar{\mathcal{E}}_f \propto \mathcal{E}_i$

The final energy distribution may be empirically constructed through

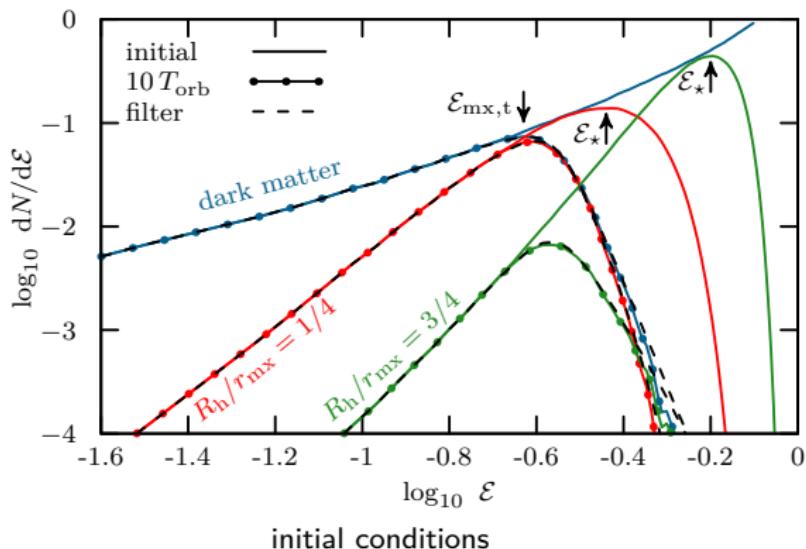
- $$\frac{dN}{d\mathcal{E}} \Big|_f = \frac{dN \left( \bar{\mathcal{E}}_f^{-1}(\mathcal{E}_f) \right)}{d\mathcal{E}} \Big|_{i,t} \left| \frac{d\bar{\mathcal{E}}_f^{-1}}{d\mathcal{E}_f} \right|,$$

or, to take into account the scatter, through a convolution.

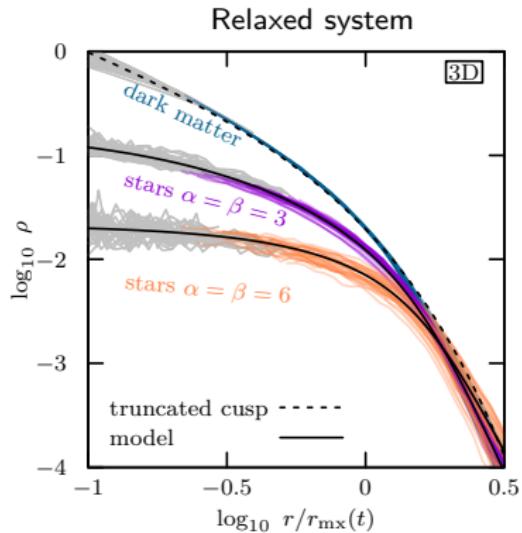
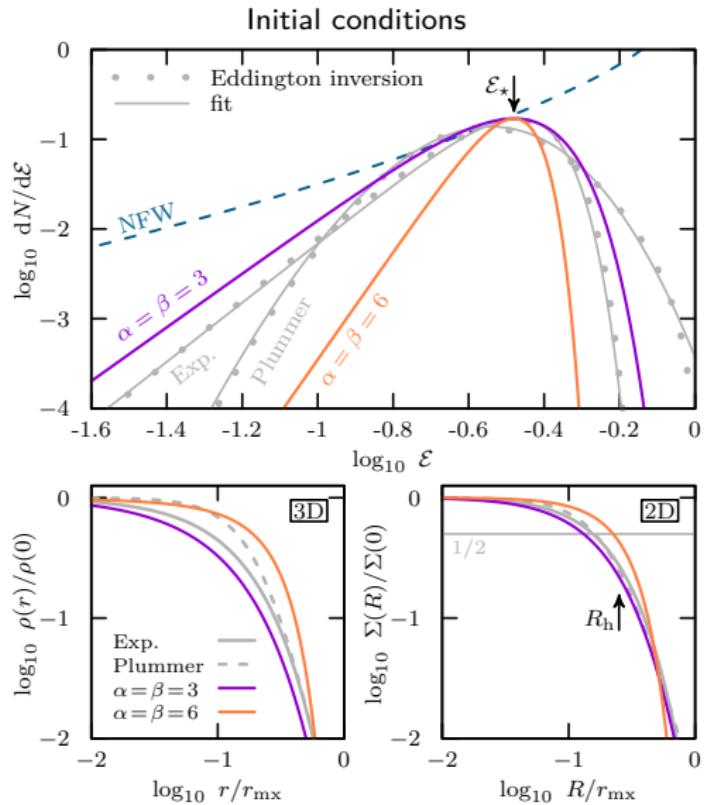


## Stripping of stars: energy cut imposed by tides

- same filter function as for dark matter
- luminosity only affected if tidal truncation within stellar energy range
- *tidally limited regime*: peak energy  $\mathcal{E}_{\text{mx,t}}$  similar for dark matter and stars



# Stripping of stars: tidally limited regime

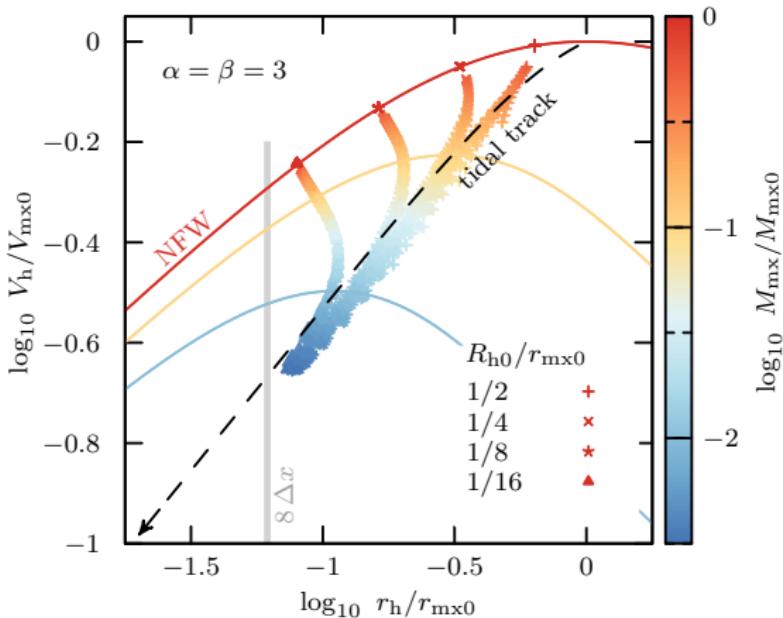


initial  $dN_*/d\mathcal{E} =$

$$\begin{cases} \mathcal{E}^\alpha \exp \left[ -(\mathcal{E}/\mathcal{E}_*)^\beta \right] & \text{if } 0 \leq \mathcal{E} < 1 \\ 0 & \text{otherwise} \end{cases}$$

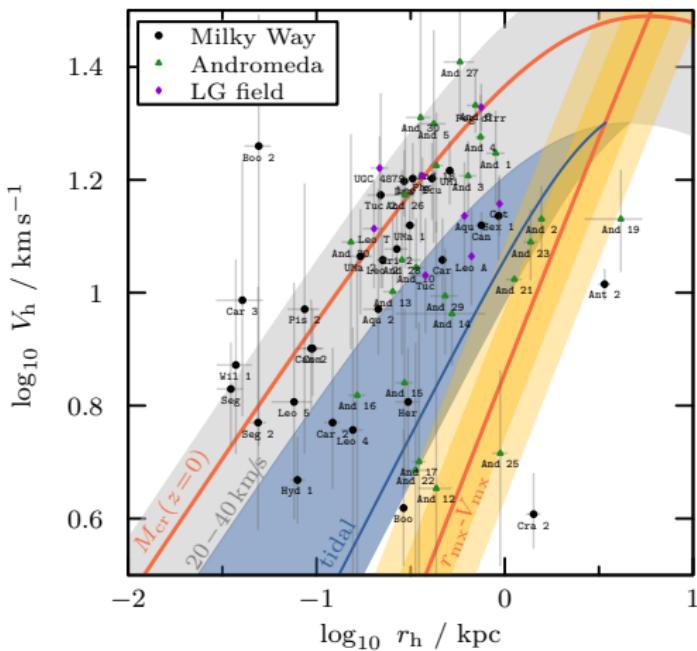
## Stripping of stars: tidal tracks

- 3D half-light radius  $r_h$  vs. circular velocity  $V_h$  at that radius
- four stellar tracers with different initial segregation:  $R_{h0}/r_{mx0} = 1/2, 1/4, 1/8, 1/16$
- no unique track: deeply segregated systems expand first, more extended ones get trimmed down immediately
- evolution asymptotic to dark matter  $r_{mx}, V_{mx}$  - track



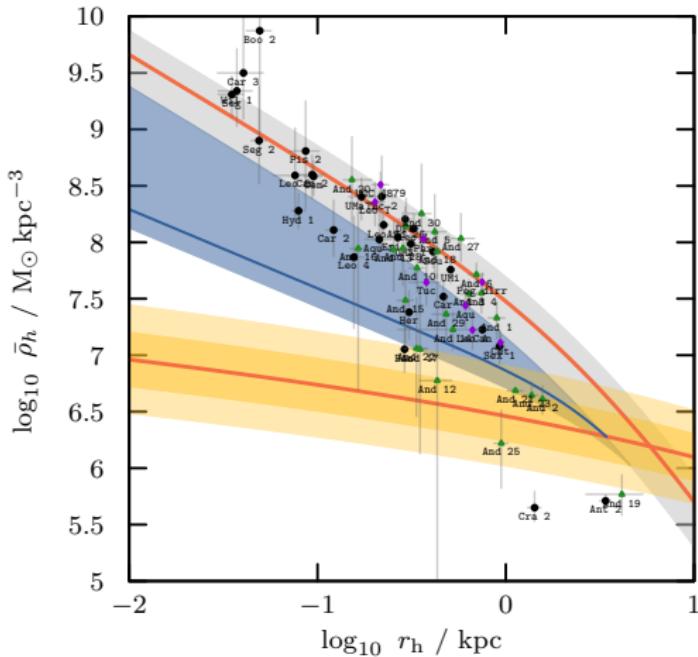
# Cosmological context: comparison against Local Group dwarfs

- Shown are LG dwarfs with  $L < 10^7 L_\odot$
- grey band:  $20 < V_{\text{max}}/\text{km s}^{-1} < 40$   
NFW: subhalos massive enough to form stars
- yellow band: cosmological mass-concentration relation
- blue area (this work): region accessible through tides
- structure of low-density dwarfs like Ant 2 and Cra 2 can't be explained by tides alone
- **to be submitted soon:**  
**Asya's detailed analysis of Cra 2**  
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