

Neutrino telescopes and dark matter detection

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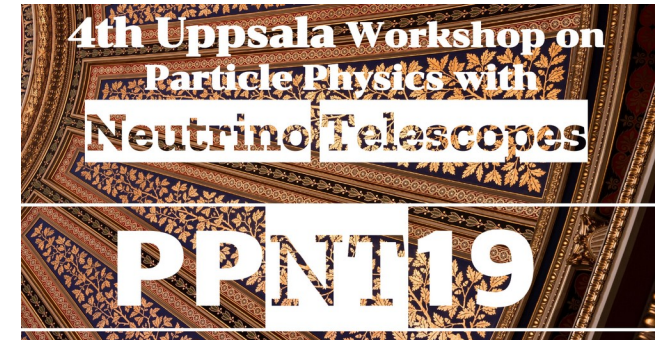


22-24 november 2021, LAPTh Annecy

Some material :

- *PPNT 2019*

<https://indico.uu.se/event/600/>



- *ICRC 2021*

<https://icrc2021.desy.de/>



Outline

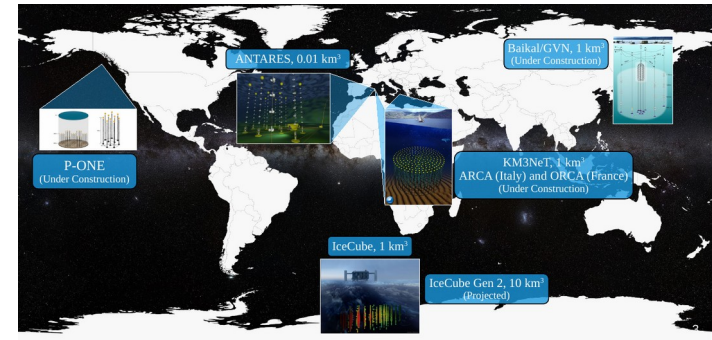
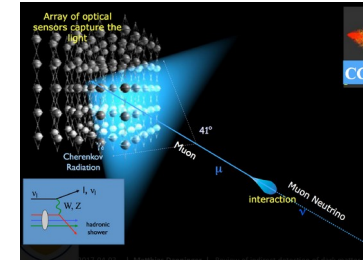
- *Detection principle*
- *Existing telescopes and projects*

IceCube – IceCube Gen 2

Antares - KM3Net

Baikal

P-ONE



- *Dark matter detection with neutrinos*

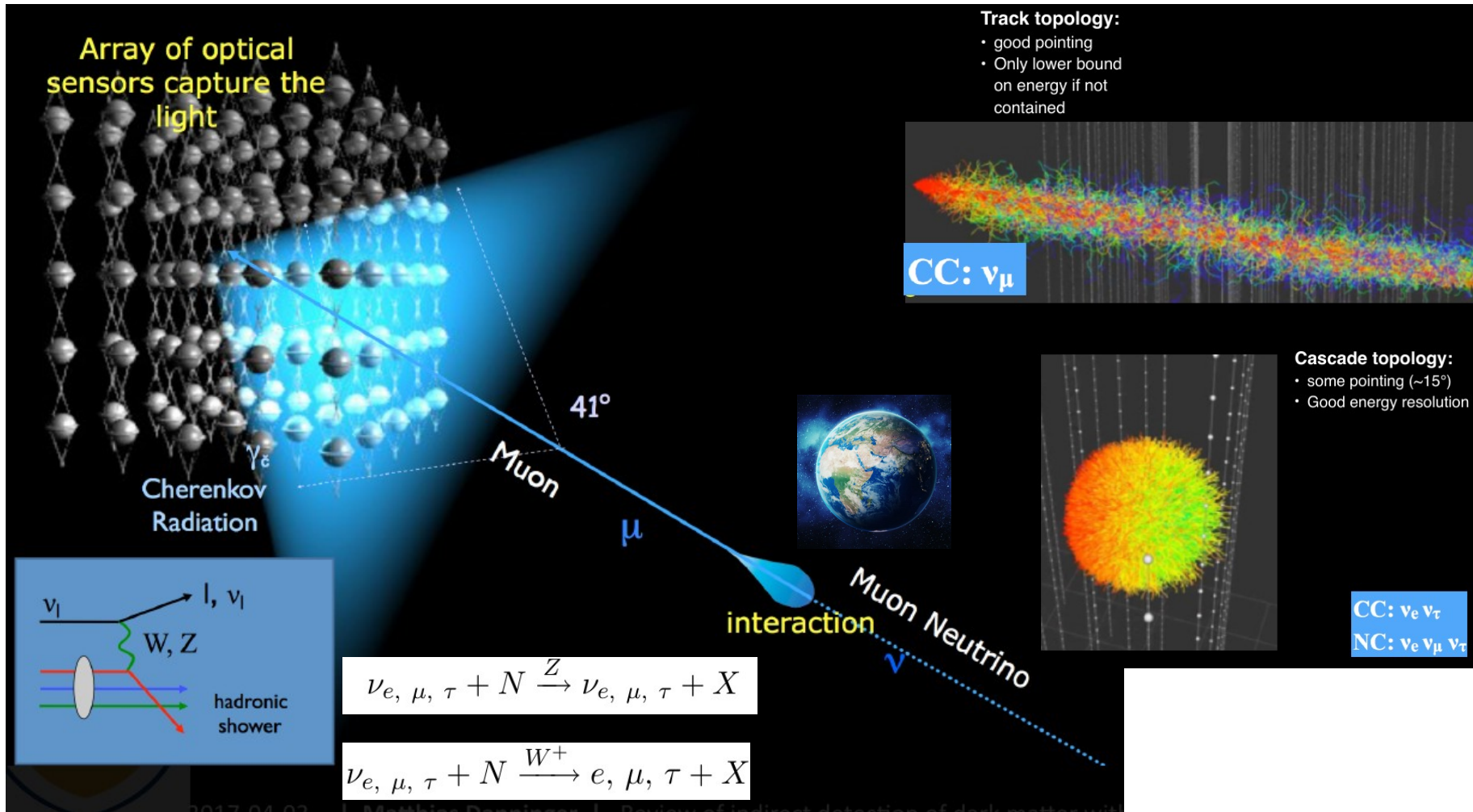
- *Targets:*

- *Dwarfs - Galaxy clusters*
- *Galactic center*
- *Sun*
- *Earth*

Specific studies:

- *DM annihilation into neutrino*
- *Angular Power Spectrum method*
- *Decaying DM*
- *Secluded DM*
- *Dark Matter neutrino scattering*
- *...*

Detection principle

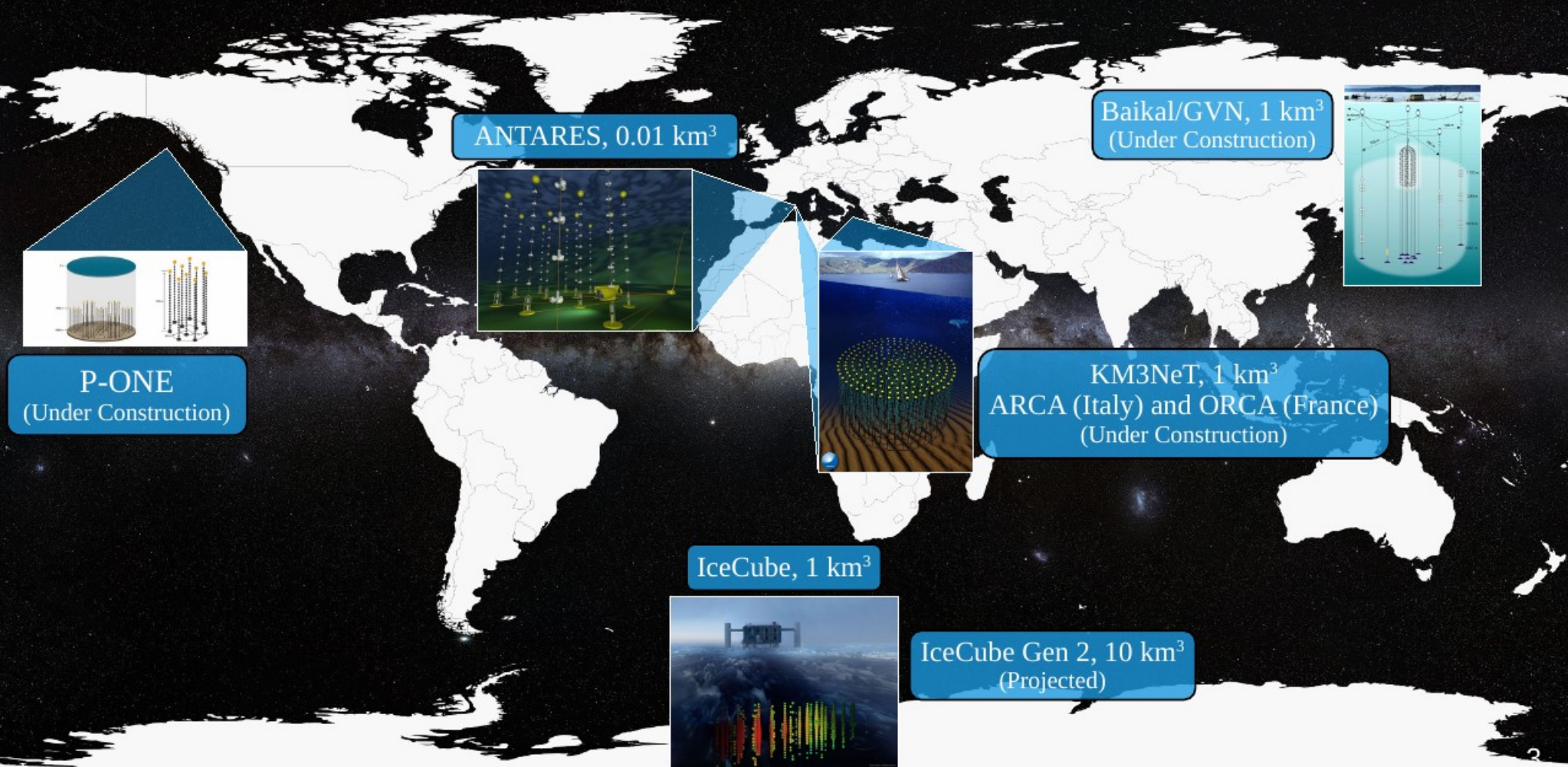


Different topologies depending on specy of the neutrinos and on energy (events inside/outside the instrumental volume)

Collect Cherenkov light of muon coming from muon neutrino interaction in the Earth through charged current

Muon track, typical events for DM searches

Neutrino Telescopes around the World



From Daniel Lopez Coto @ ICRC2021

Size evolution

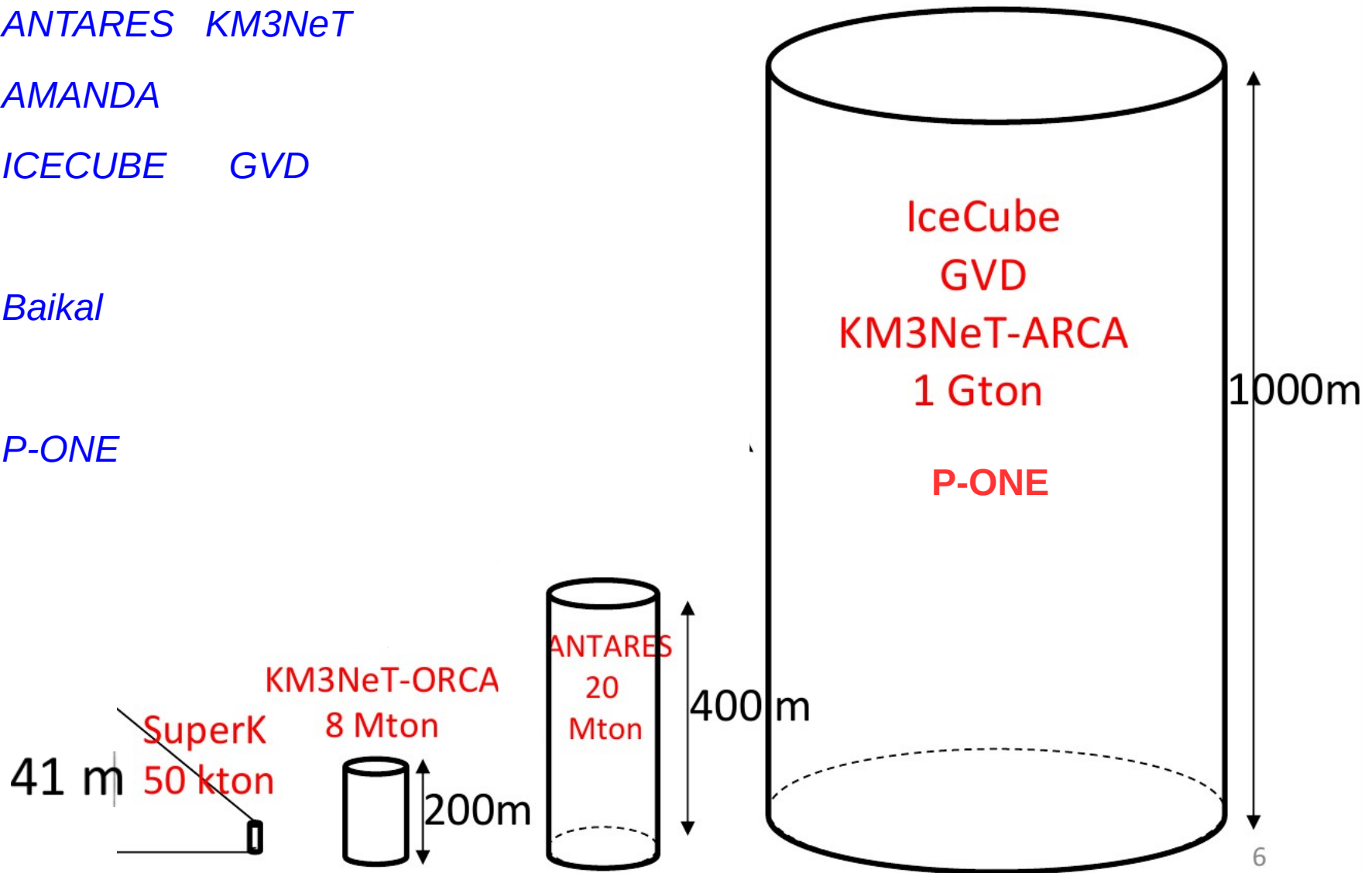
ANTARES KM3NeT

AMANDA

ICECUBE GVD

Baikal

P-ONE

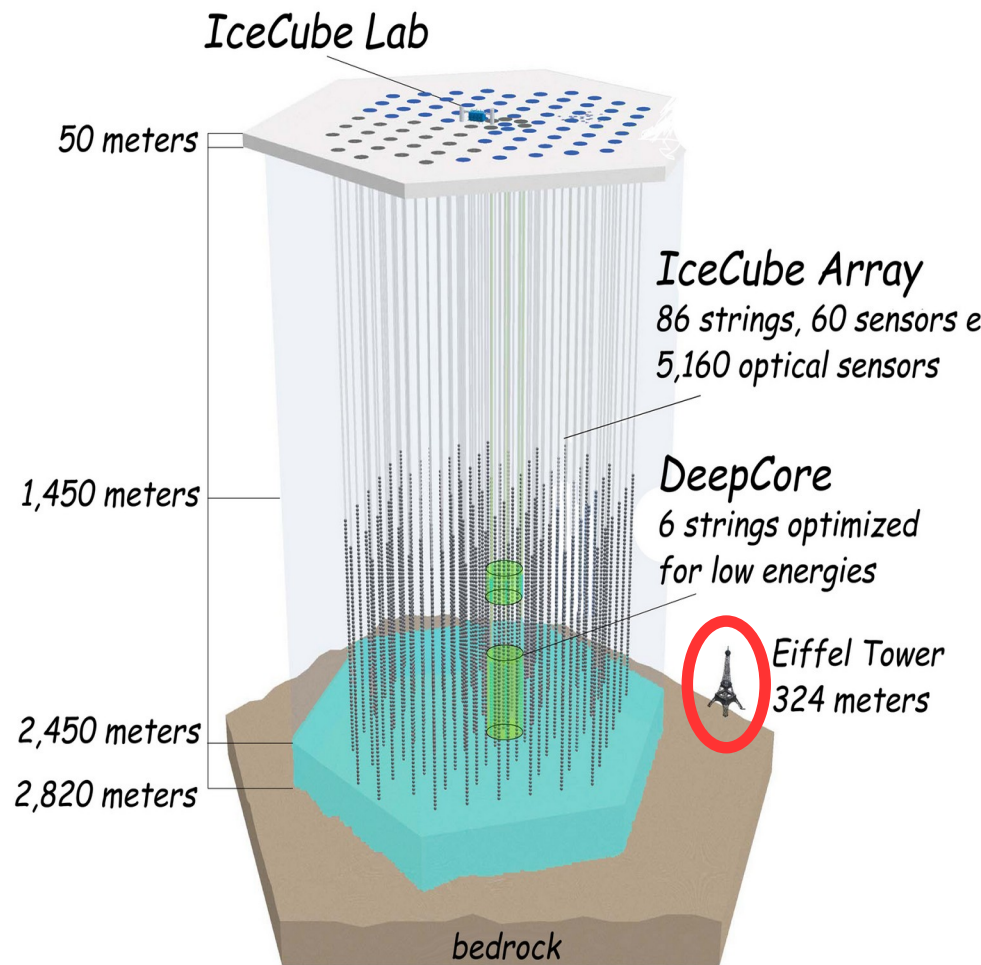
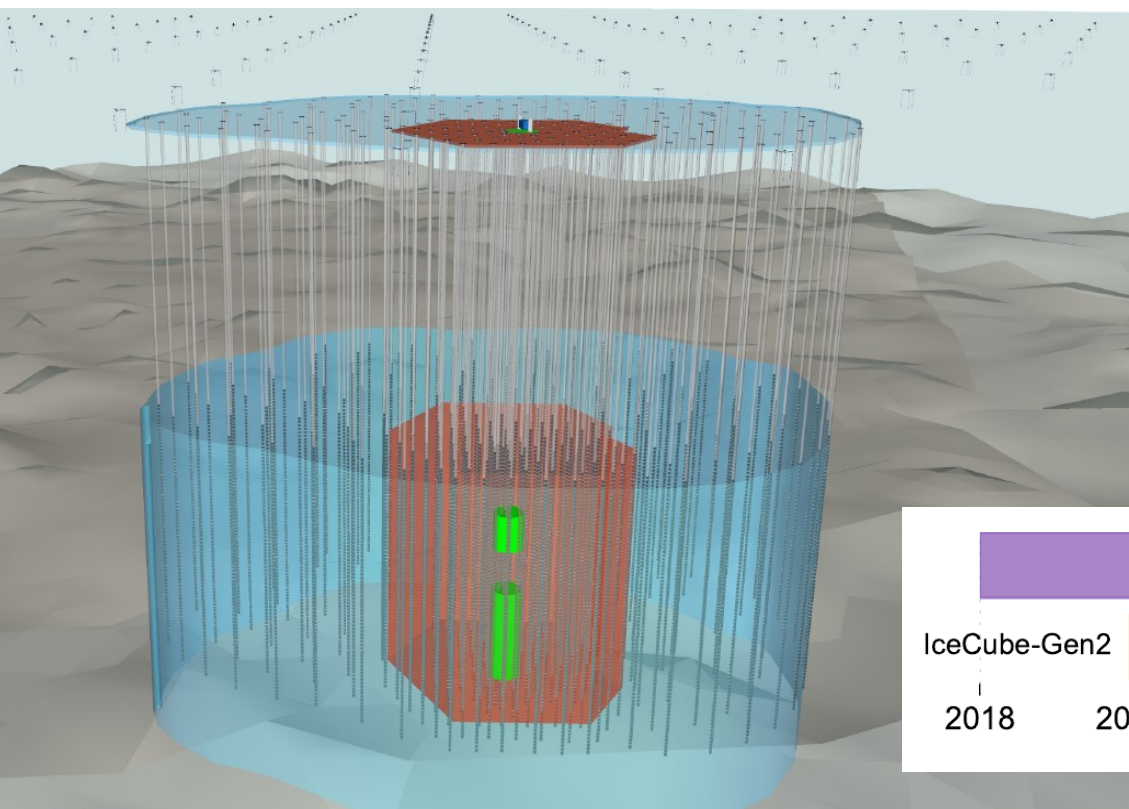


From Paschal Coyle @ ICRC2021

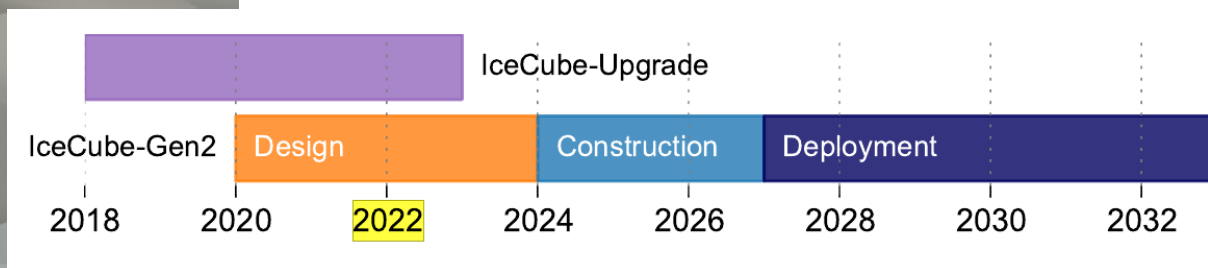
(Amanda) Icecube – Icecube GEN2



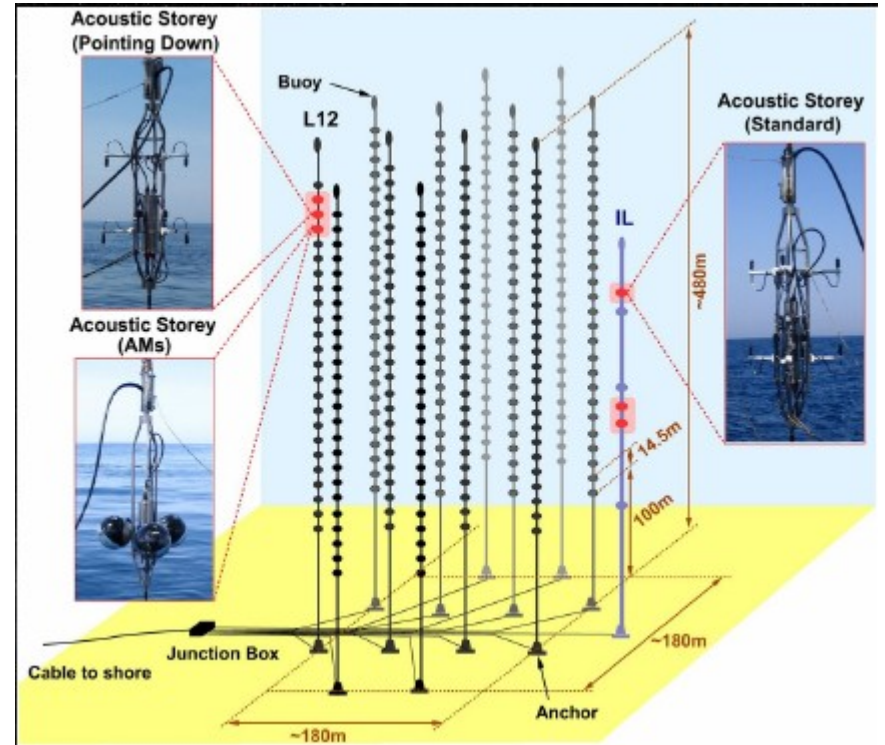
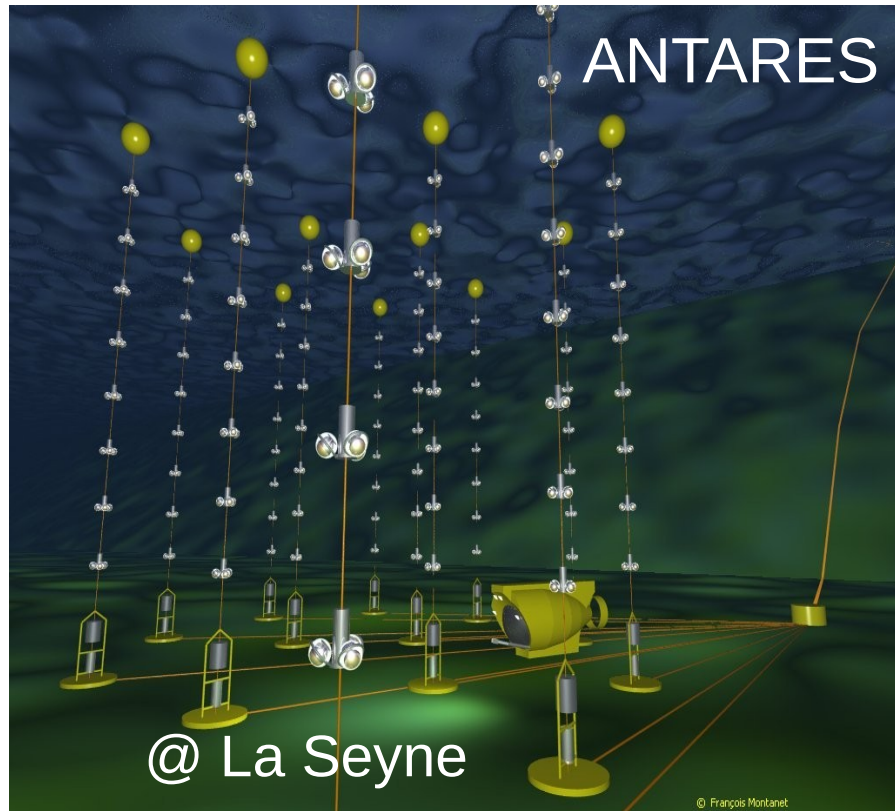
ICECUBE GEN 2 10 km³
arXiv:2008.04323



Schedule

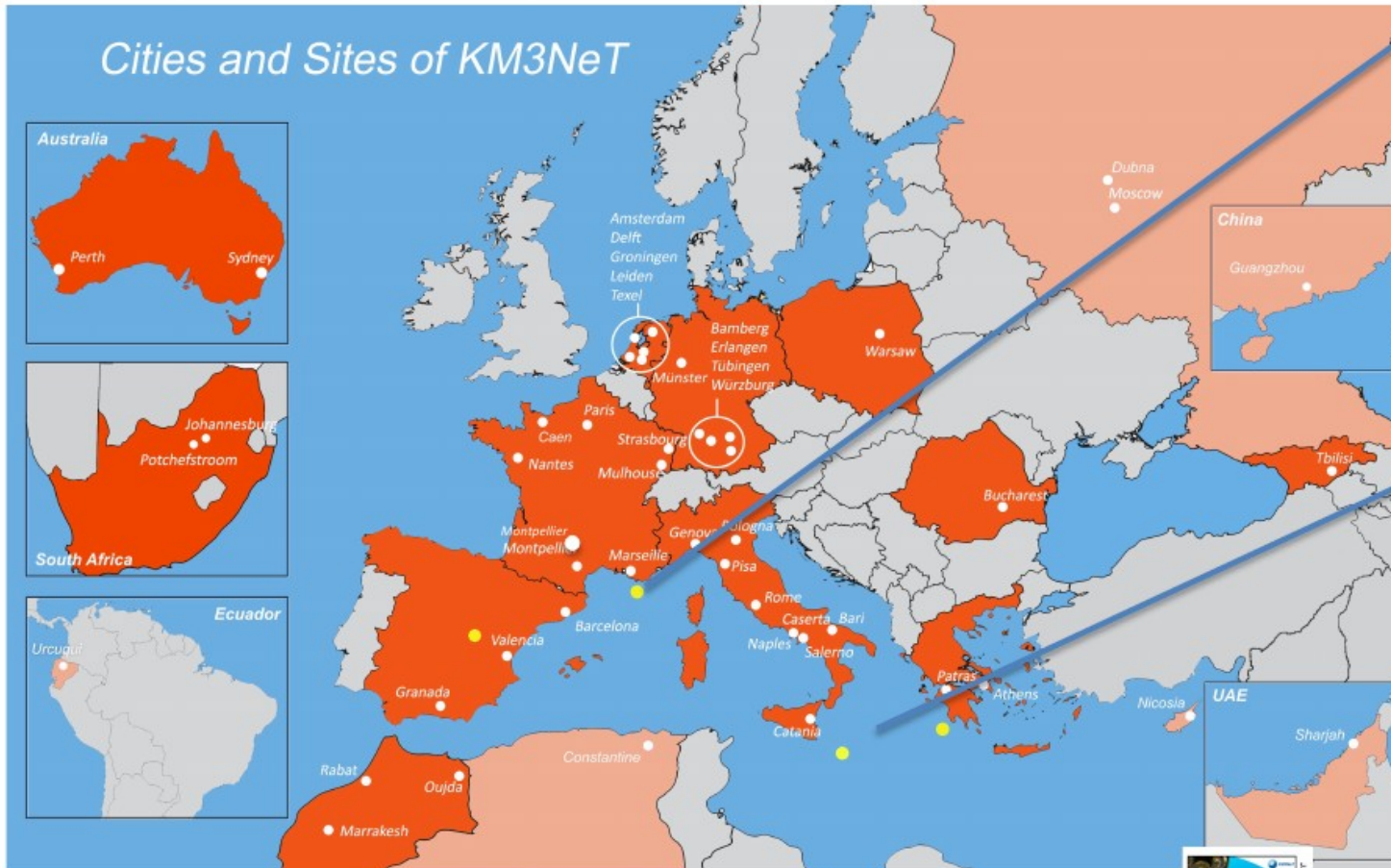


ANTARES



KM3NeT

Multi-site, deep-sea infrastructure
Selected for ESFRI roadmap
Single collaboration, Single technology



Cities and Sites of KM3NeT

[KM3NeT 2.0: Letter of Intent](http://dx.doi.org/10.1088/0954-3899/43/8/084001)

<http://dx.doi.org/10.1088/0954-3899/43/8/084001>

J. Phys. G: Nucl. Part. Phys. 43 (2016) 084001



Oscillation Research
with Cosmics In the Abyss



Astroparticle Research
with Cosmics In the Abyss

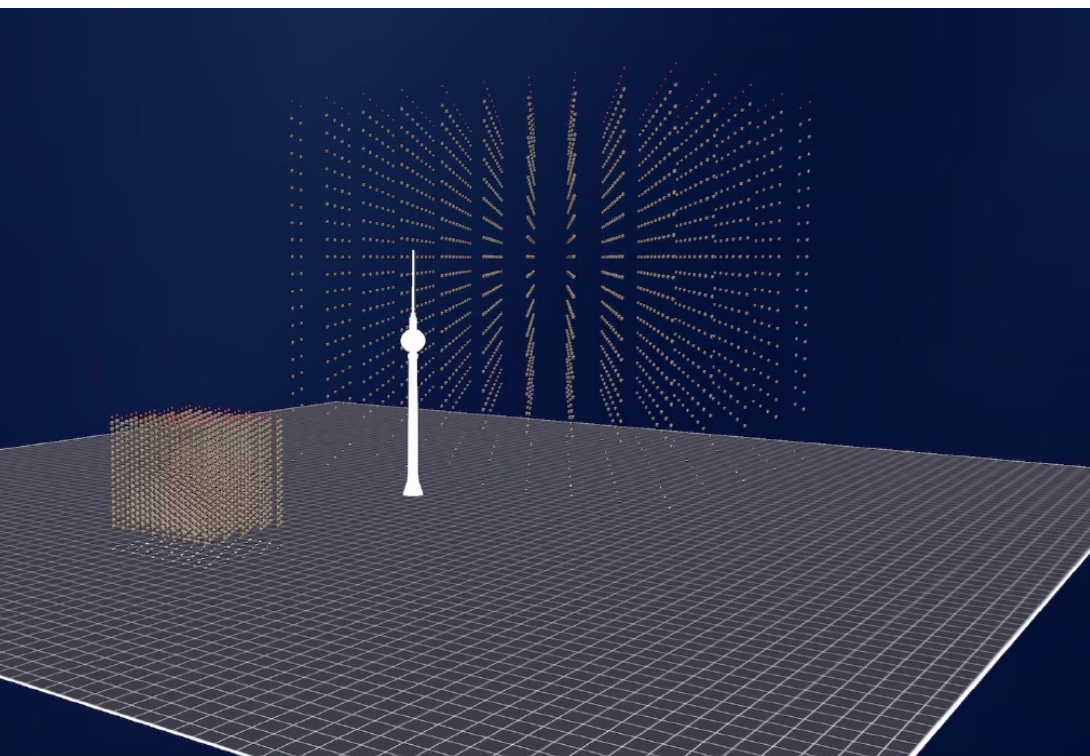
Connection nodes of

- European multidisciplinary seafloor & water column observatory

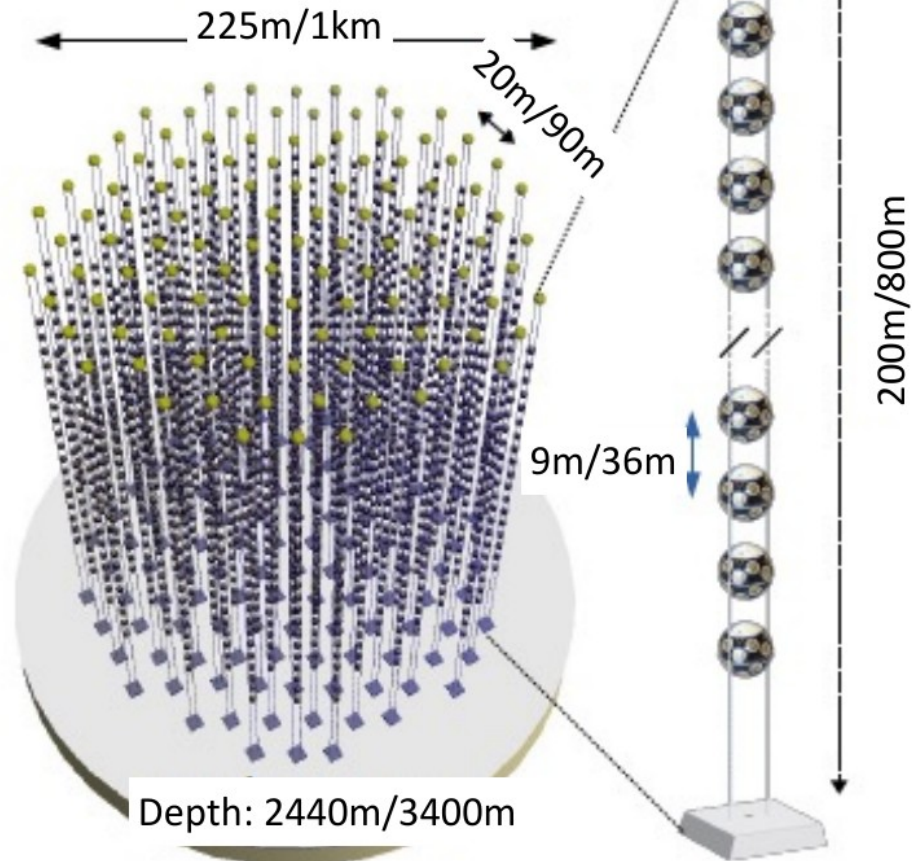


emso

KM3NeT



115 strings
18 DOMs / string



Instrumented mass	7 Mton	500*2 Mton
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Baikal

1980: Start of experiments at “106 km” site

1993: NT36 - 3 strings, 36 optical modules (OM)

1996: NT96 - 4 strings, 96 OM

1998: NT200 - 8 strings, 196 OM

2004-2005: NT200+ - three additional strings, 12 OM each

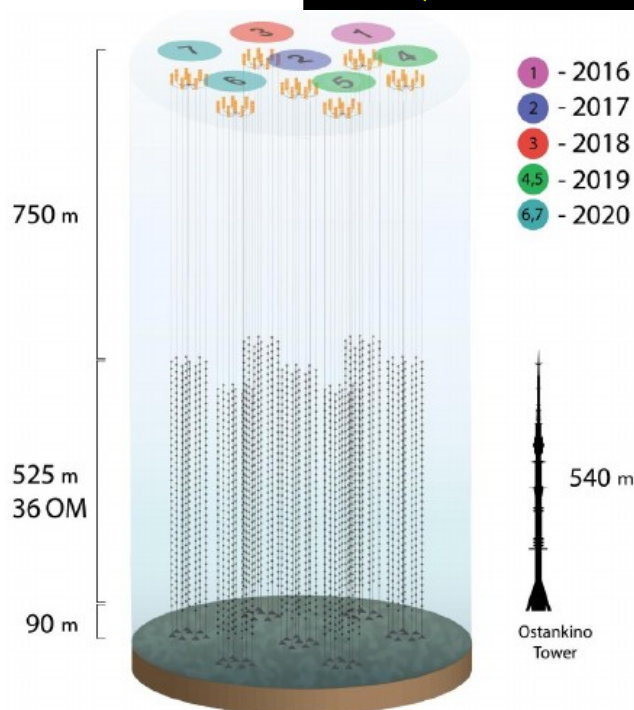
2015: Start of Baikal-GVD construction. Demonstration cluster “Dubna”, 8 strings, 192 OM

2016: First full-scale cluster of Baikal-GVD deployed

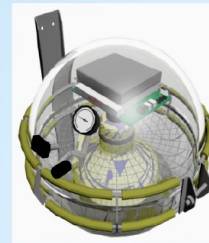
2020: Baikal-GVD operates 7 clusters, 2016 OM



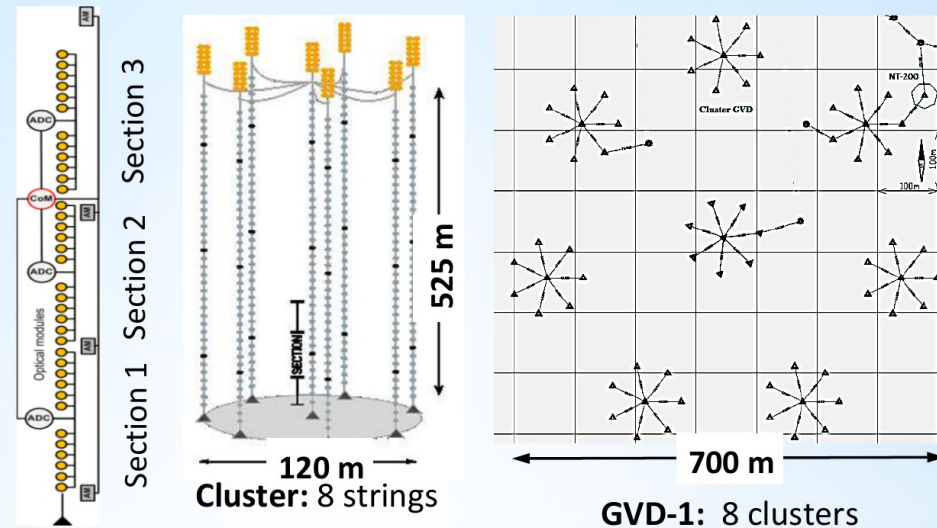
PoS (ICRC2021) 002



Baikal-GVD: phase I (2020-2021)



Optical module
PMT: R7081-100

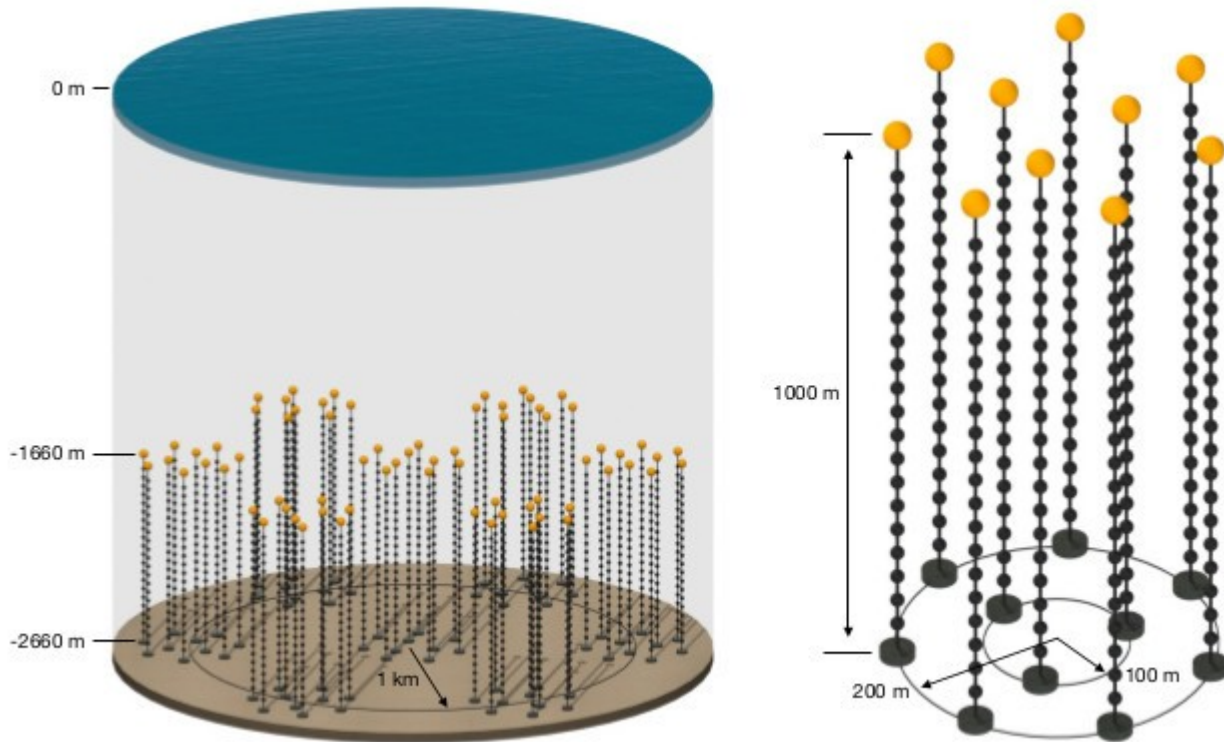


GVD-1	
OMs	2304
Clusters (8 Strings)	8
Depths, m	750 – 1275
Eff. Volume	0.4 km ³

Directional resolution	Energy resolution
Cascades: 3.5° – 5.5°	$\delta(E/E_{sh}) \sim 0.15$
Muons: 0.25° - 0.5°	$\delta(\lg E) \sim 0.4$

P-ONE *Pacific Ocean Neutrino Experiment*

arXiv:2005.09493



A KM3 size telescope installed within the deep Pacific Ocean underwater infrastructure of Ocean Networks Canada

10 first lines 2023-2024

+ 70 lines 2028-2030

From Paschal Coyle @ ICRC2021

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This talk

KM3NeT

THE LAKE BAIKAL NEUTRINO TELESCOPE

Zhan-Arys Dzhilkibaev

Mediterranean Sea
Saltwater: K40
Bioluminescence

Lake Baikal
Freshwater
Chemiluminescence

AMANDA

Marek Kowalski

ICECUBE

Antarctic
Ice
Dust, air bubbles

7

Water:

less diffusion, angular resolution

salt water: K40, Bioluminescence

freshwater: chemiluminescence

moving detector (waves and sea current)

need boat + ROV (remotely operated underwater vehicle)

Ice:

easier to install (but south pole)

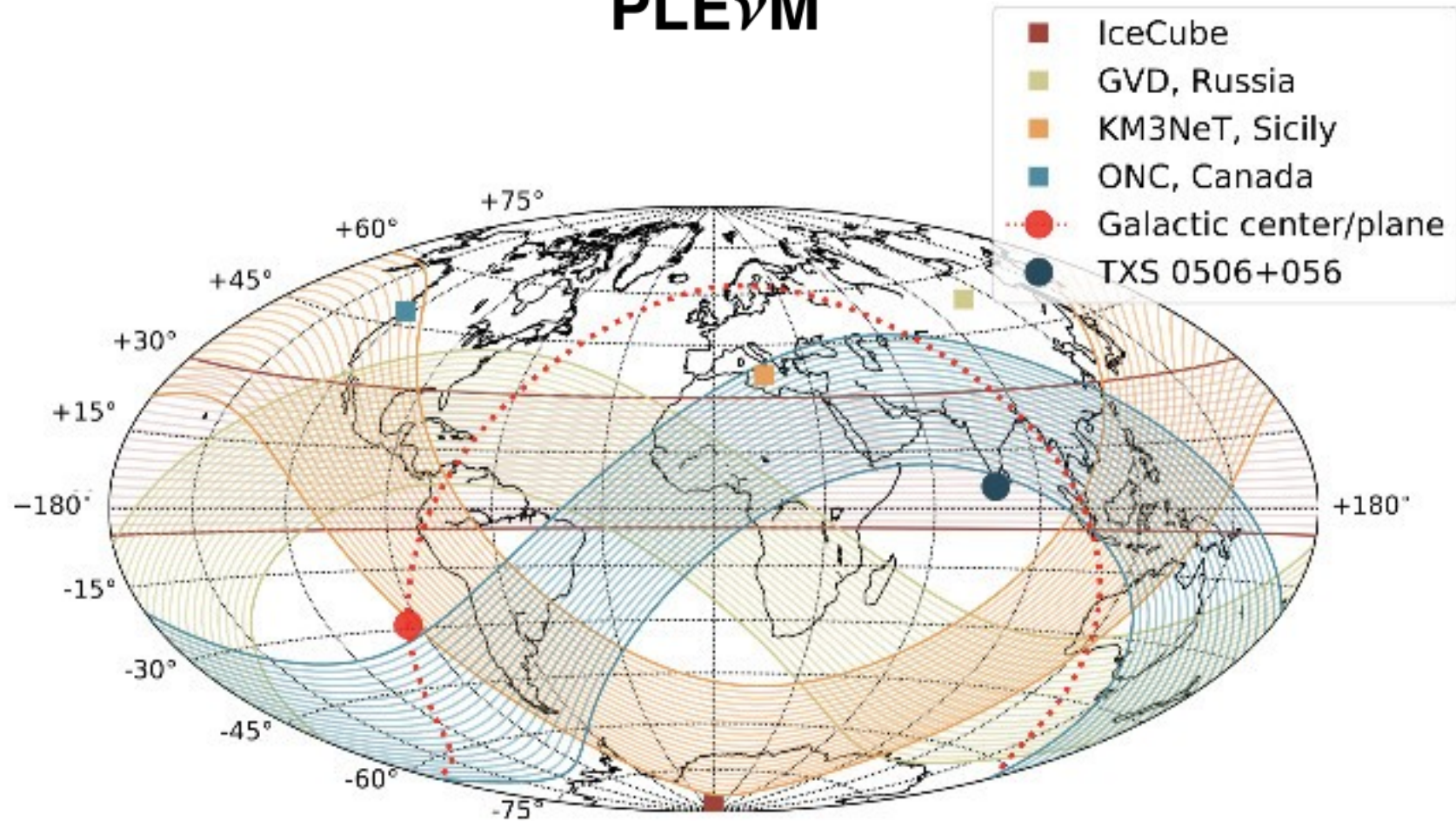
less constraints once installed,

more diffusion/angular resolution

Dust, air bubbles

Sky coverage

PLE ν M



Planetary Neutrino Monitoring System (PLE ν M)

A global and distributed monitoring system of high-energy astrophysical neutrinos

Lisa Schumacher@ICRC2021 and arXiv:2107.13534

Science scope

Neutrino and multimessenger astronomy

Neutrino oscillations

New physics, exotic searches

Indirect dark matter searches

Dark matter detection with neutrinos

Dark matter annihilation :

$$\chi\chi \rightarrow t\bar{t}, b\bar{b}, c\bar{c}, \tau^+\tau^-, W^+W^-, ZZ, \mu^+\mu^-, \nu\bar{\nu}...$$

Decay of annihilation products \rightarrow Neutrino spectrum = $\sum_i \frac{dN_\nu^i}{dE_\nu} BR_i$

$$\chi\chi \rightarrow X\bar{X} \rightarrow \nu Y$$

Typical spectra:

Pythia / WIMPSIM / PPC4DM

Typically use extremal cases:

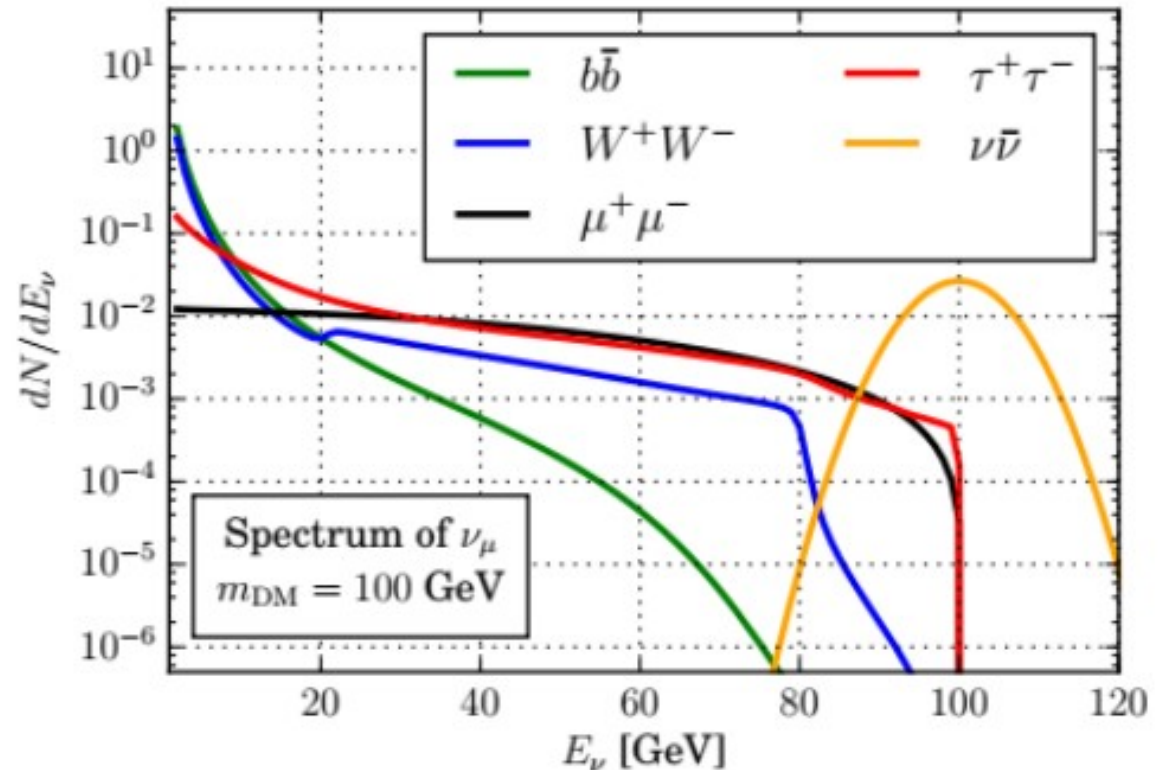
Hard spectrum $\tau^+\tau^- W^+W^- \mu^+\mu^-$

Soft spectrum $b\bar{b}$

(recent update see HDMspectra

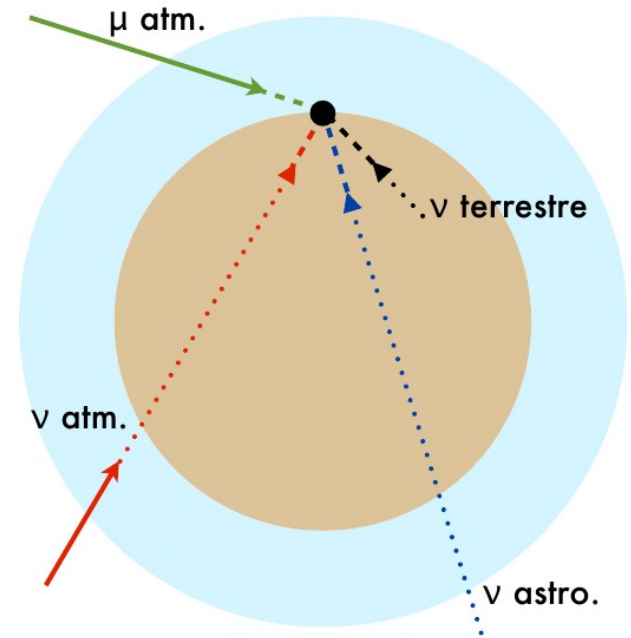
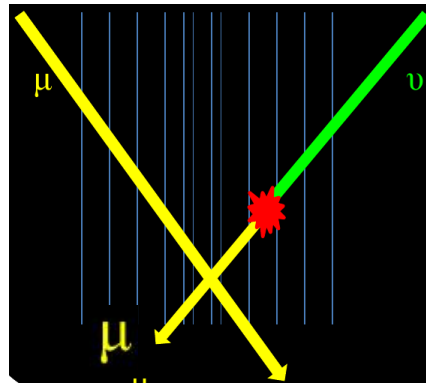
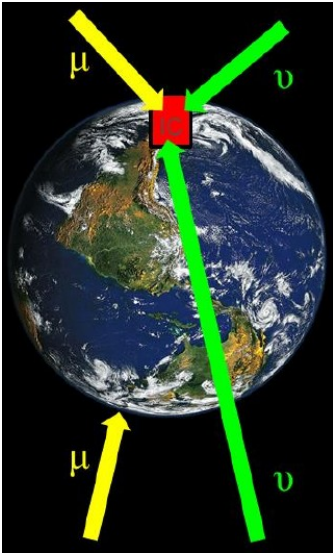
Bauer,Rodd,Webber arXiv:2007.15001)

Dark Matter Spectra from the Electroweak to the Planck Scale



Background

Atmospheric neutrinos/muons:



Select upgoing events to reduce atmospheric muons

Flux

Annihilation case

$$\frac{d\phi_\nu^{\text{ann}}}{dE_\nu} = \frac{\delta}{4\pi} \frac{\langle\sigma v\rangle}{m_{DM}^2} \sum_f b_f \frac{dN_\nu^f}{dE_\nu} \int_{res.} d\Omega \int_{l.o.s} \rho_{DM}^2(r) dl$$

Dark matter distribution ?

Clumps

Mas spectrum

Concentration

Spatial distribution

Streams

Density profile

Cusp/core

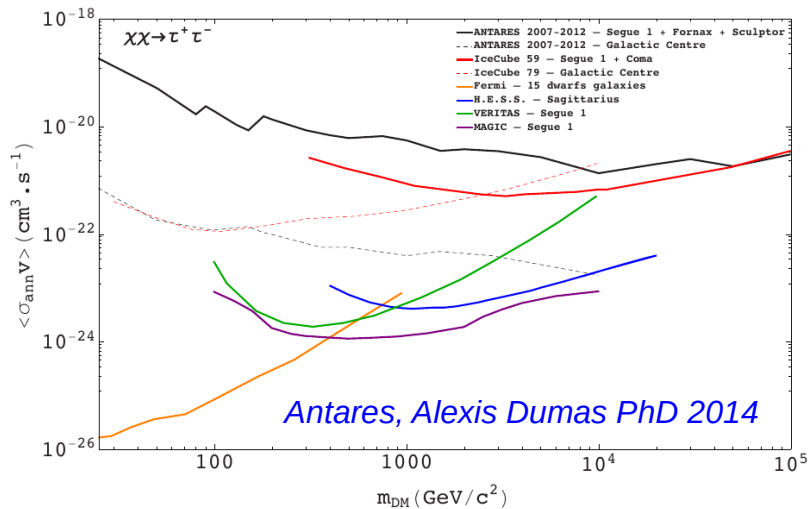
Baryons ?

...

Dsphs

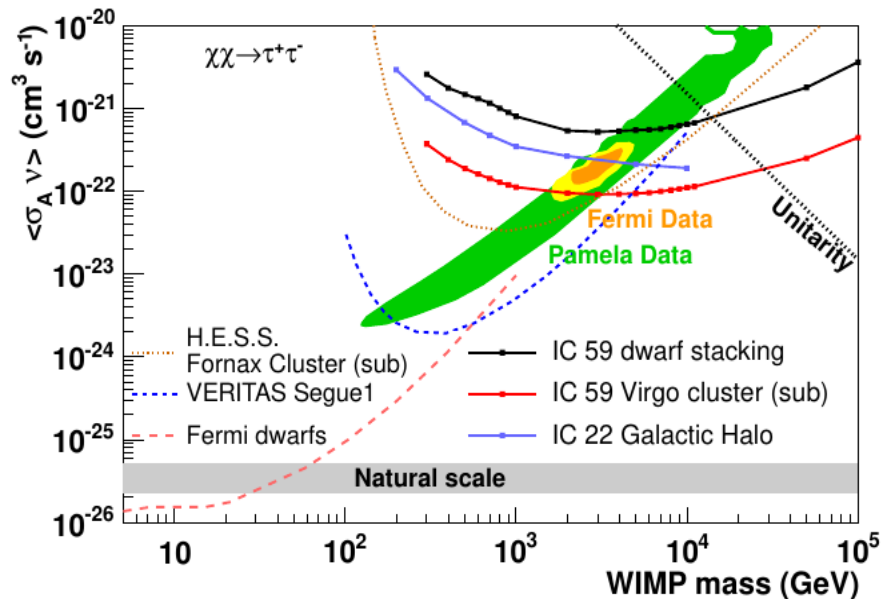
- Jeans equation to constrain the DM profile parameters

$$\sigma_p^2(R) = \frac{2}{I(R)} \int_R^\infty \left(1 - \beta_a \frac{R^2}{r^2}\right) \frac{v \sigma_r^2 r}{\sqrt{r^2 - R^2}} dr$$



Antares, Alexis Dumas PhD 2014

[Results from Baikal see O.Suvorova PPNT2019]



arXiv:1307.3473

ICECUBE

Clusters

- Derive profile parameters from X-ray data

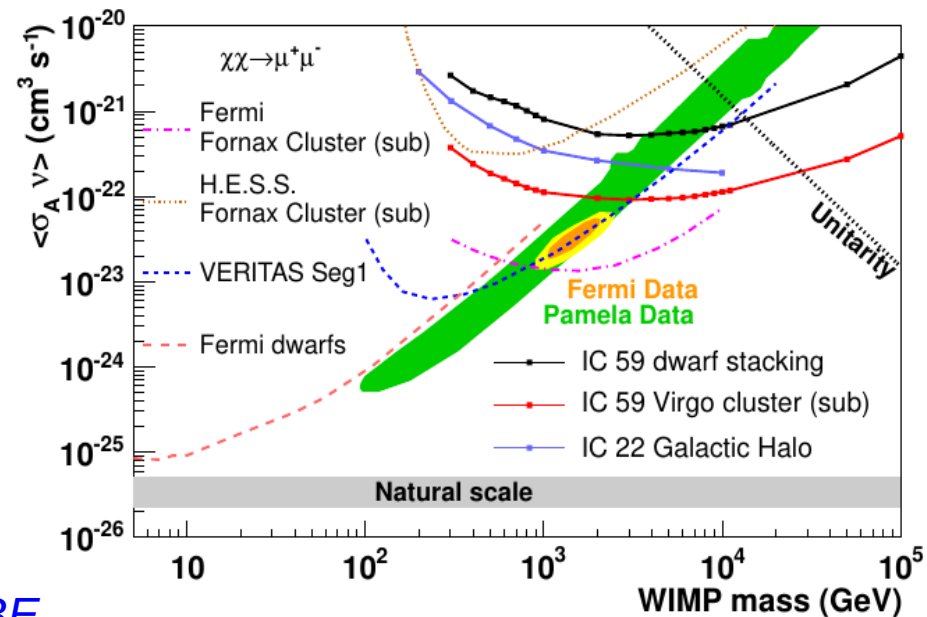
Use J factor from Fermi for comparison and

effective boost factor from Gao et al 2012

(Phoenix DMO simulation)

$$b(M_V) = \frac{J_{\text{sub-cluster}}}{J_{\text{NFW}}} = 1.6 \times 10^{-3} \left(\frac{M_V}{M_\odot}\right)^{0.39}$$

Discuss here angular size of objects vs resolution



Galactic center and MW halo

- Flux:

Annihilation case

$$\frac{d\phi_\nu^{\text{ann}}}{dE_\nu} = \frac{\delta}{4\pi} \frac{\langle\sigma v\rangle}{m_{DM}^2} \sum_f b_f \frac{dN_\nu^f}{dE_\nu} \int_{res.} d\Omega \int_{l.o.s} \rho_{DM}^2(r) dl$$

Dark matter density in the Milky Way ?

Clumps

Mas spectrum

Concentration

Spatial distribution

Streams

Density profile

Cusp/core

Baryons ?

Compression ?

Stellar formation/SN feedback ?

DM halo driven by the history of assembly of baryons. Steepening-Flattening ?

Galactic center and MW halo

- Flux:

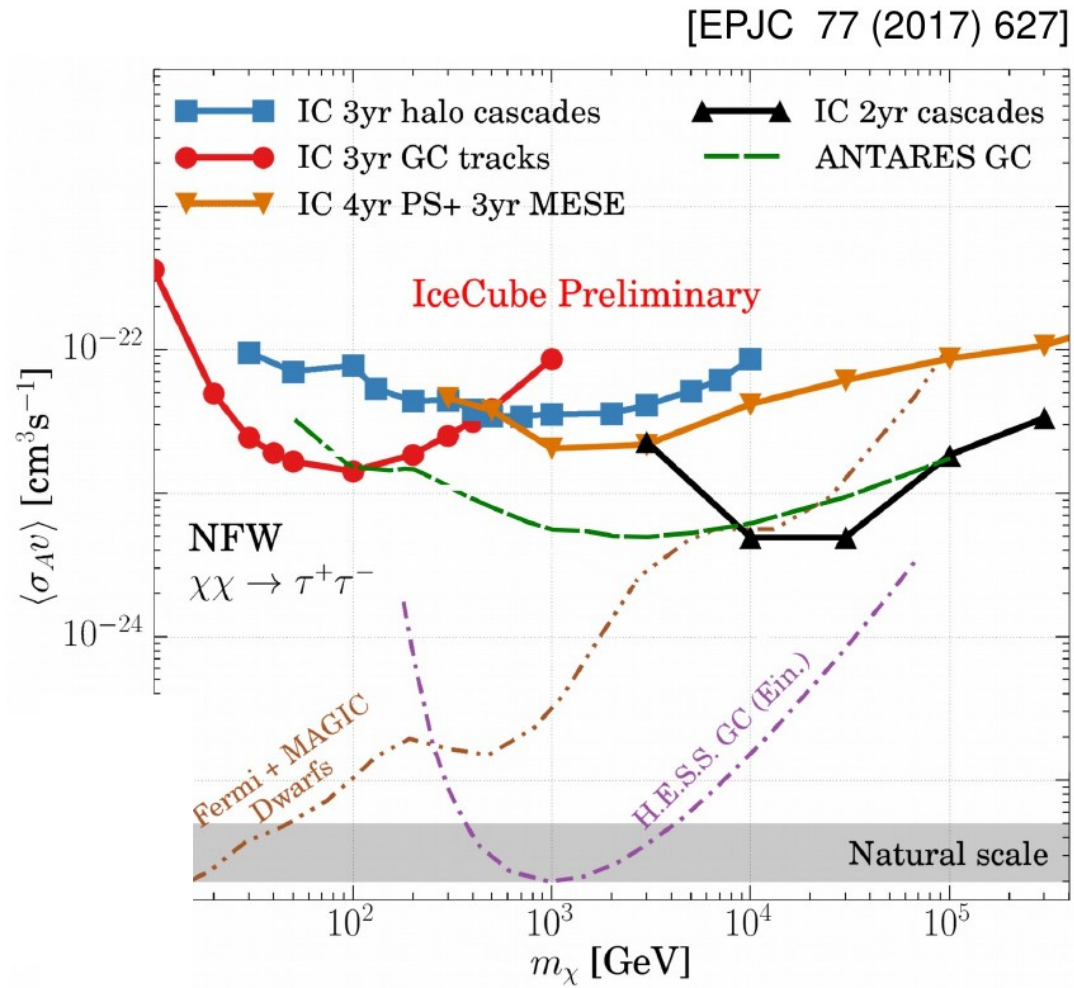
Annihilation case

$$\frac{d\phi_\nu^{\text{ann}}}{dE_\nu} = \frac{\delta}{4\pi} \frac{\langle\sigma v\rangle}{m_{DM}^2} \sum_f b_f \frac{dN_\nu^f}{dE_\nu} \int_{res.} d\Omega \int_{l.o.s} \rho_{DM}^2(r) dl$$

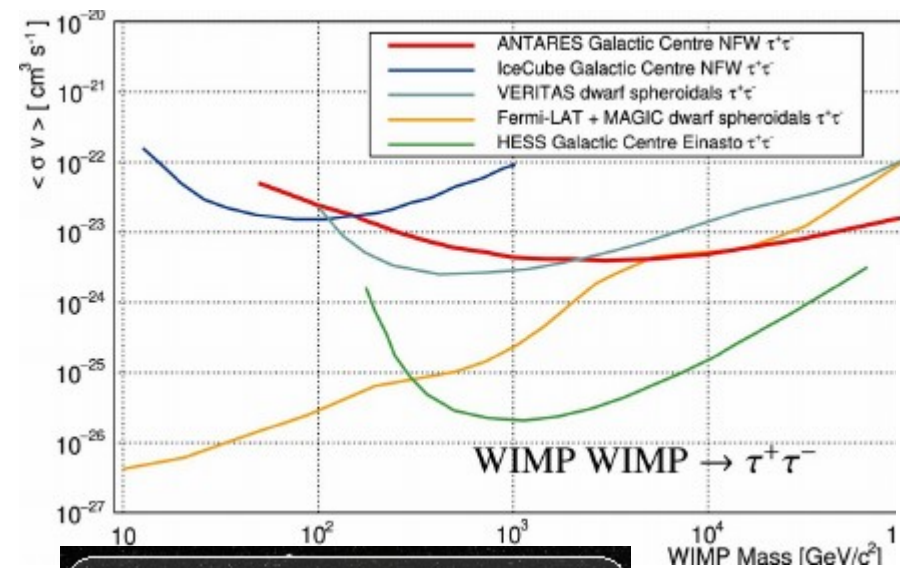
Dark matter density in the Milky Way ?

- Popular profile from (irrelevant) DMO simulations ? NFW, Einasto, Via Lactea, Aquarius ...
- (unrealistic but consistent) cosmo hydro simulations ? With strong cusps induced by stellar potential ? With cores induced by feedback ? Evaluate the diffuse emission ? (not only the DM emission)
- or (unrealistic) semi-analytic models ? (faster) Stref, Lavallo 2017, CLUMPY Hutten, Combet, Maurin 2019, Hiroshima, Ando, Ishiyama 2018 ...
- Cored profiles suggested by data ? (simple only smooth component)
MacMillan 2016, Portail 2016.

Galactic center

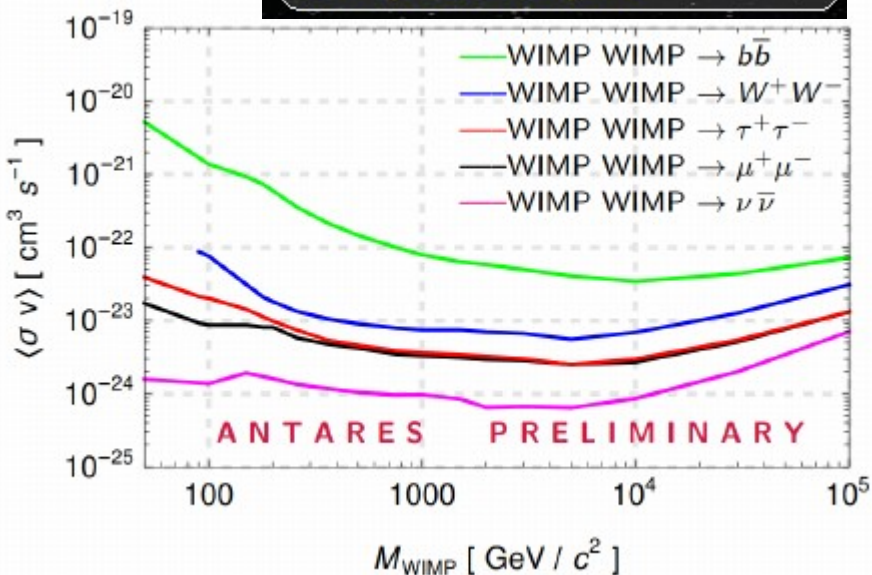


Galactic center

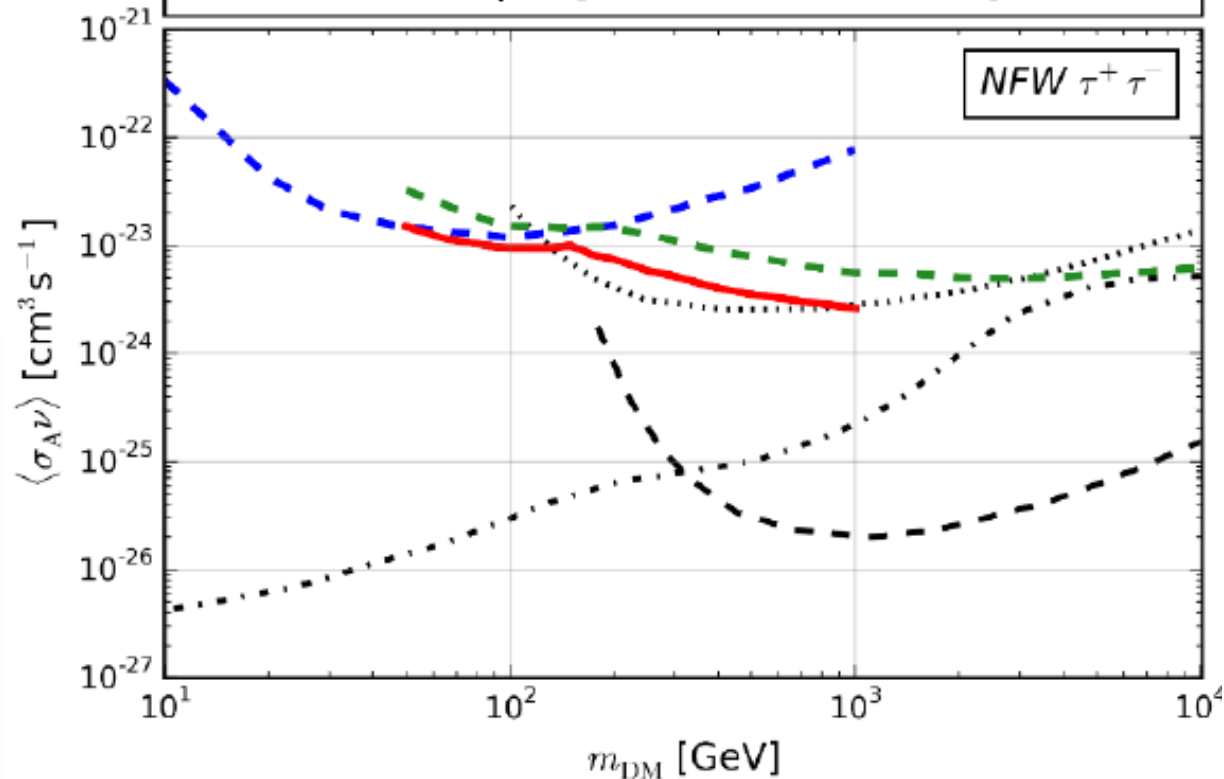


ANTARES GC,
11 years of Data (2007-2017)
Physics Letters B, Vol 805,2020

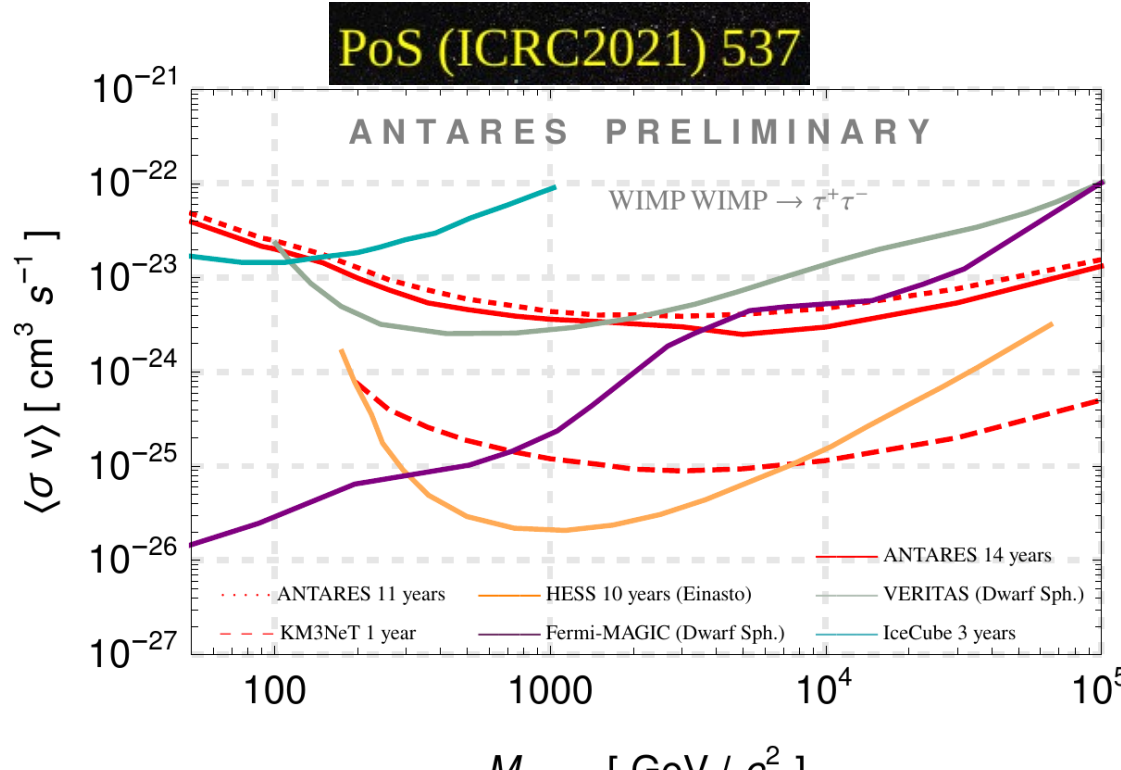
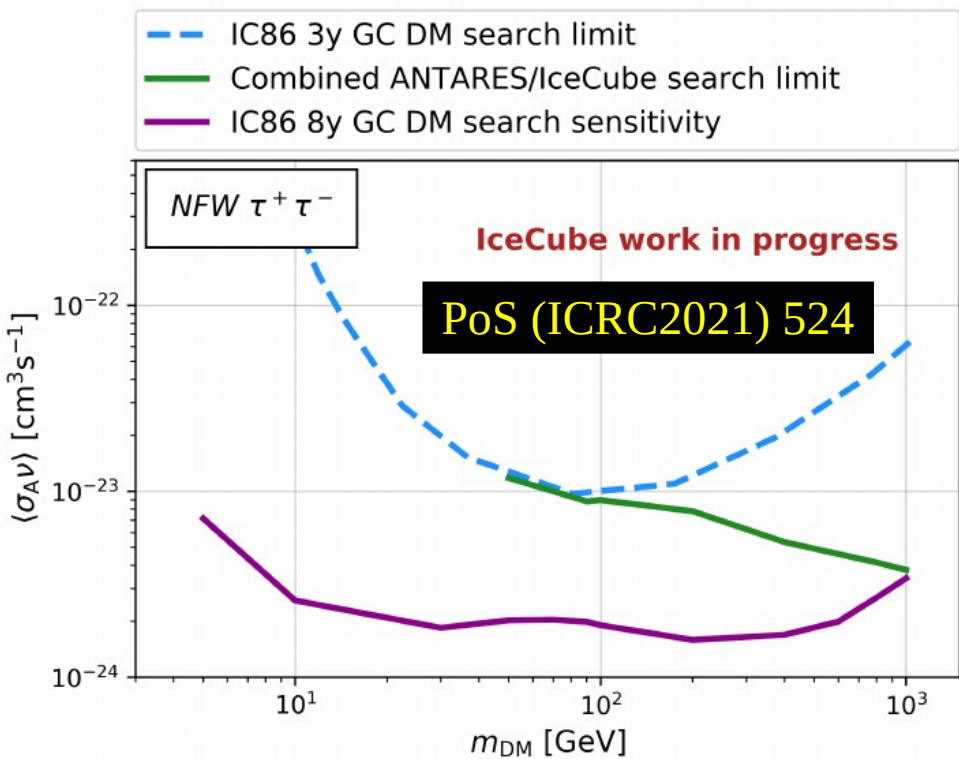
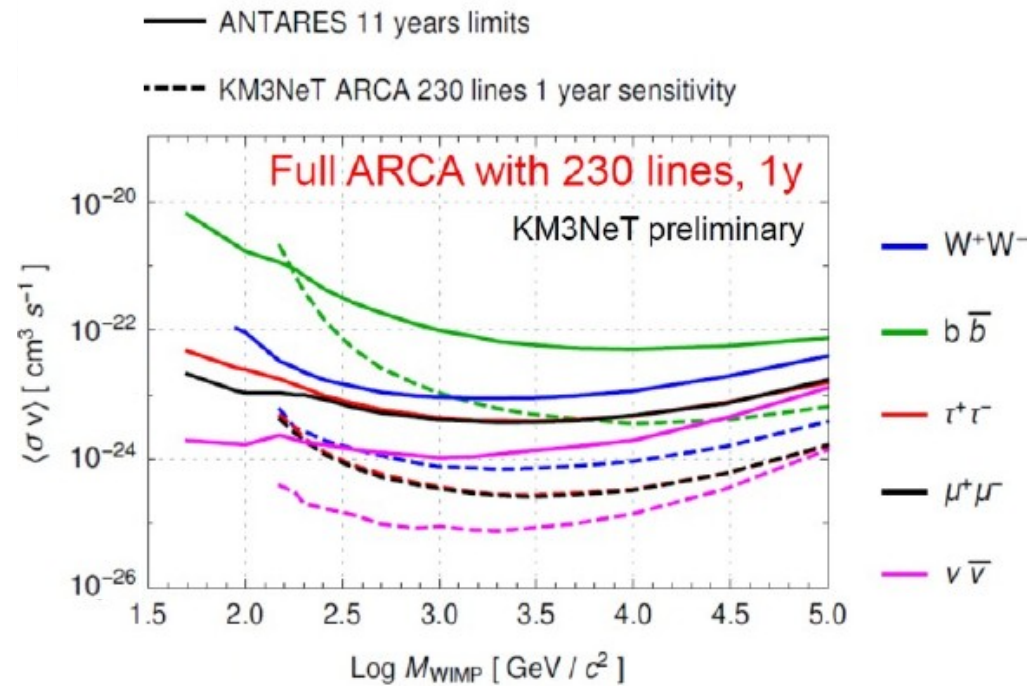
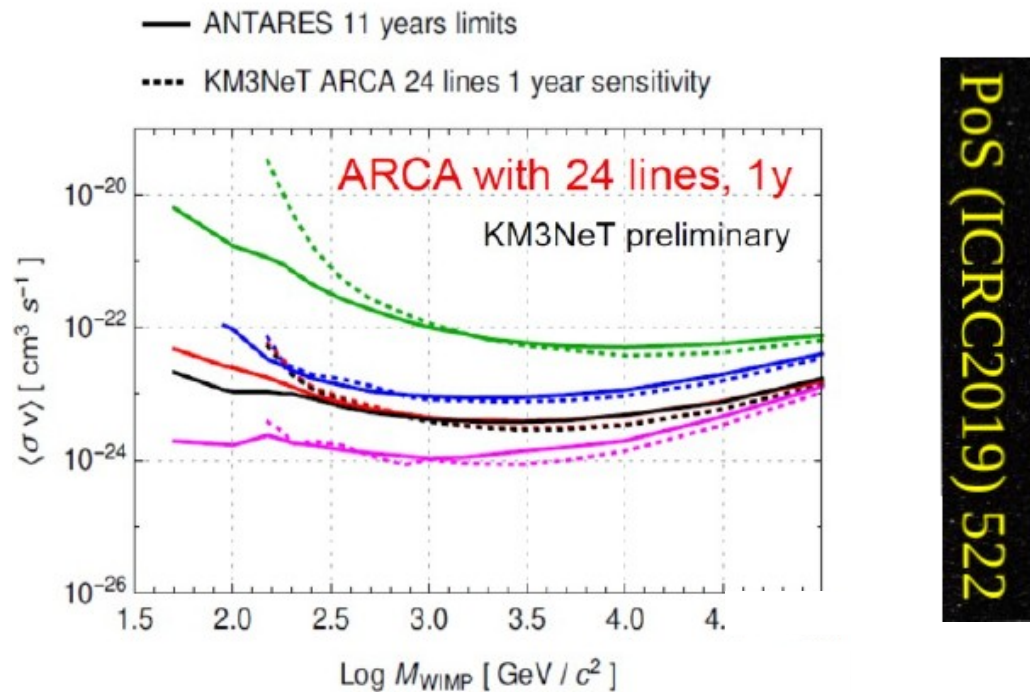
ANTARES GC,
13 years of Data (2007-2020)
PoS (ICRC2021) 537



ANTARES + IC combined GC,
11 years of Data (2007-2017)
PRD 102 (2020) 082002



Galactic center : Next



A. Gould, *Astrophys. J.* 321 (1987) 571
 A. Gould, *Astrophys. J.* 388 (1991) 338
 G. Jungman et al. / *Physics Reports* 267 (1996)

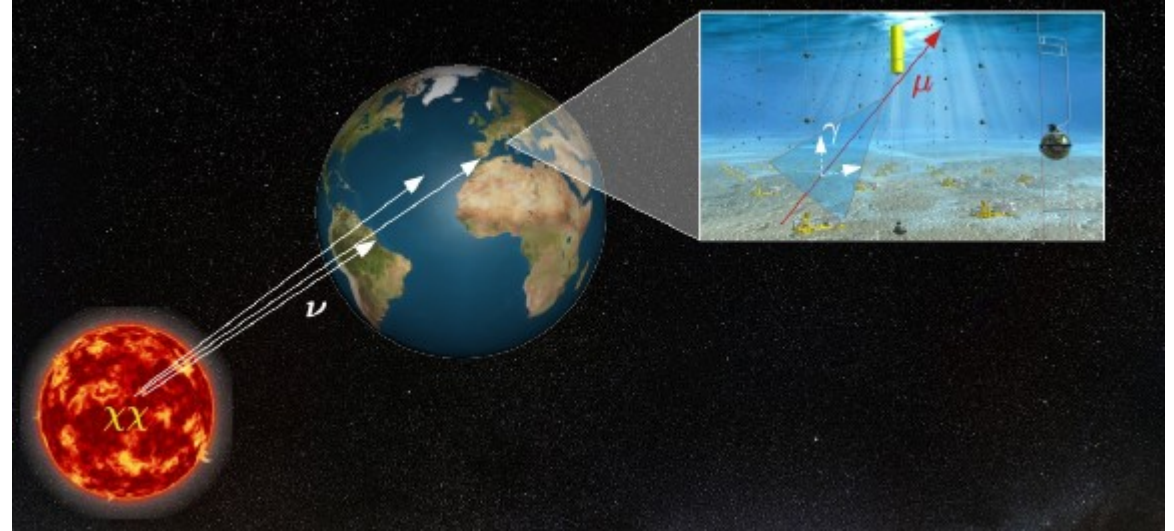
The Sun

Captured population

$$\dot{N}_\chi = C - C_A N_\chi^2$$

$$N_\chi = \left(\frac{C}{C_A} \right)^{1/2} \tanh(t\sqrt{CC_A})$$

Annihilation rate : $\Gamma_A = \frac{1}{2} C_A N_\chi^2$



Capture rate : $\frac{dC_i}{dV} = \frac{\rho_\odot}{m_\chi} \int_0^{u_{esc}^\odot} du \frac{f(u)}{u} \Omega_i(Q)$ *local DM density and velocity distribution*

$$C = \int_0^{R_\odot} 4\pi r^2 dr \sum_i \frac{dC_i}{dV} \quad \Omega_i = \sigma_i n_i \frac{M_i}{2\mu_i^2} \int_{Q_{min}}^{Q_{max}} F_i^2(Q) dQ$$

$$\frac{t_\odot}{\tau_\odot} = 330 \left(\frac{C}{s^{-1}} \right)^{1/2} \left(\frac{\langle \sigma_A v \rangle}{cm^3 s^{-1}} \right)^{1/2} \left(\frac{m_\chi}{10 \text{ GeV}} \right)^{3/4}$$

Annihilation rate at equilibrium driven by capture only

$$\sqrt{CC_A} t > 1, \Gamma_A \sim \frac{C}{2} = cste$$

The Sun

Captured population

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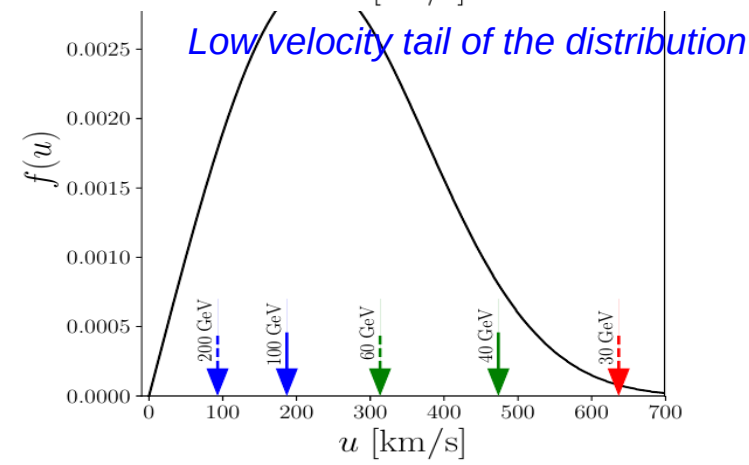
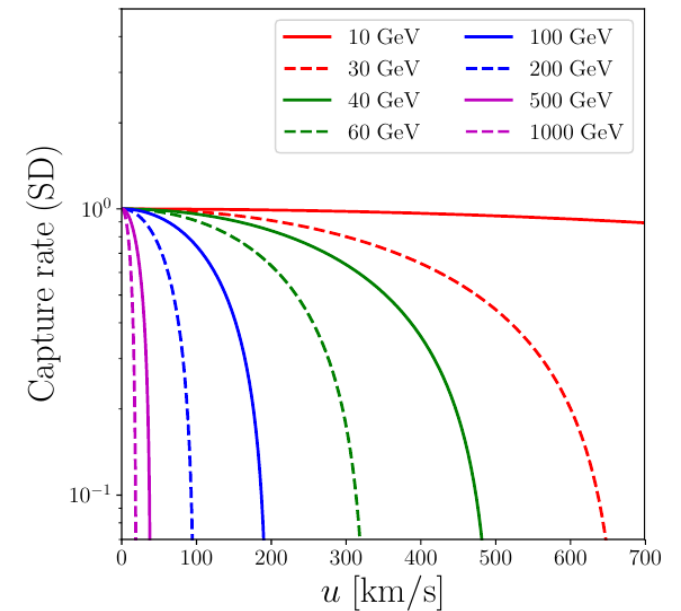
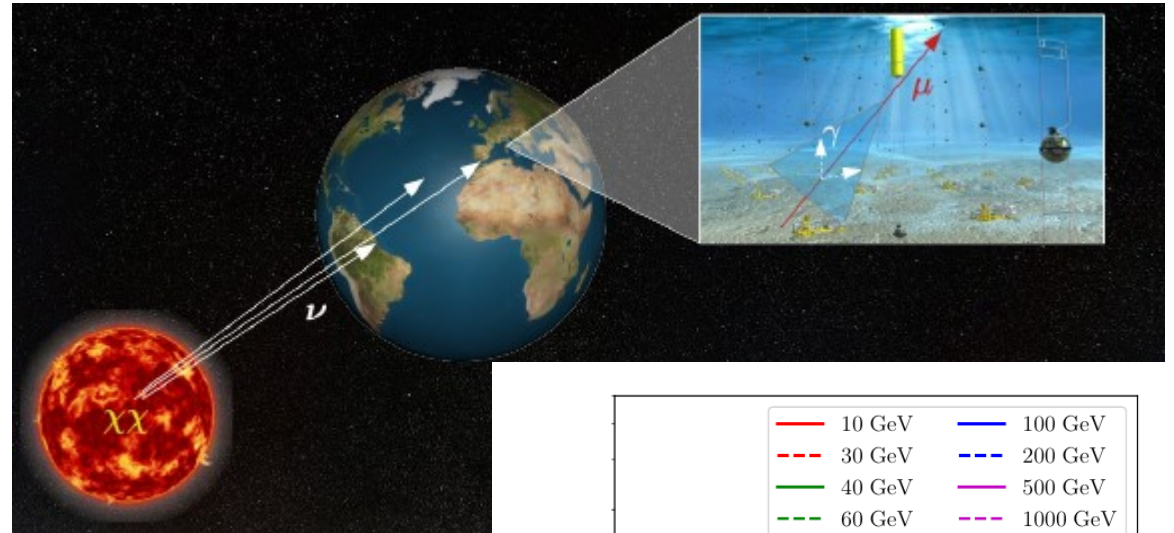
$$\frac{dC_i}{dV} = \frac{\rho_\odot}{m_\chi} \int_0^{u_{esc}^\odot} du \frac{f(u)}{u} \Omega_i(Q)$$

$$C = \int_0^{R_\odot} 4\pi r^2 dr \sum_i \frac{dC_i}{dV}$$

$$\frac{t_\odot}{\tau_\odot} = 330 \left(\frac{C}{s^{-1}}\right)^{1/2} \left(\frac{\langle\sigma_A v\rangle}{cm^3 s^{-1}}\right)^{1/2} \left(\frac{m_\chi}{10 GeV}\right)^{3/4}$$

Annihilation rate at equilibrium driven by capture only

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The Sun

Capture rate :

$$\frac{dC_i}{dV} = \frac{\rho_\odot}{m_\chi} \int_0^{u_{esc}^\odot} du \frac{f(u)}{u} \Omega_i(Q)$$

Beyond SHM :

- Cosmological simulations of spiral galaxies

- Other functions

Generalized Maxwellian, Tsallis. Mao+2013 ...

- Semi analytic methods:

Eddington inversion ...

Lacroix et al arXiv:1805.02403, arXiv:2005.03955

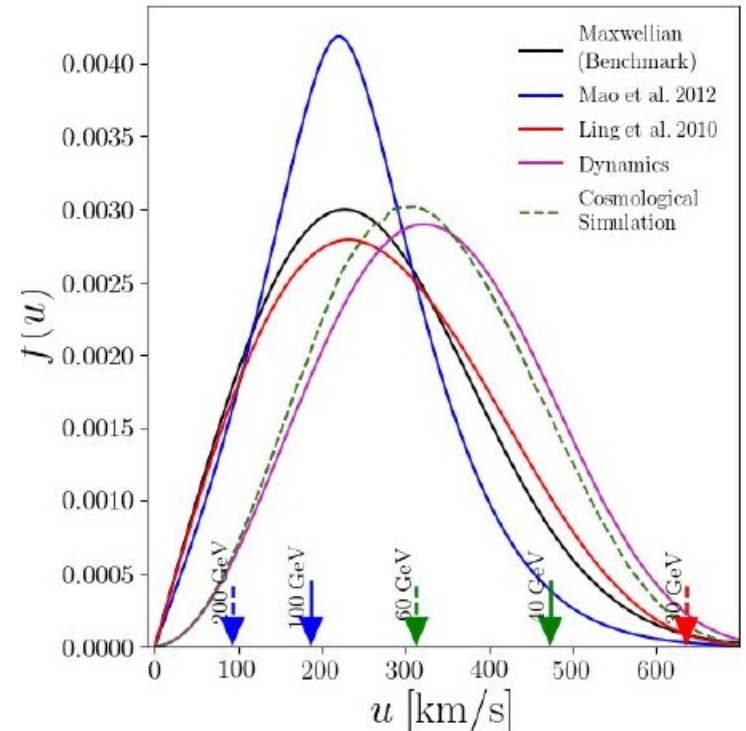
Petac et al arXiv:2106.01314

Usual assumptions : Standard Halo Model (SHM)
Maxwellian velocity distribution
(self-grav isothermal sphere)

$$f_{\vec{v}}(\vec{v}) = \frac{1}{v_0^3 \pi^{3/2}} \exp\left(-\frac{|\vec{v}|^2}{v_0^2}\right)$$

$$v_c = 220 \text{ km/s}, \quad v_0 = v_c$$

$$\rho_\odot = 0.3 \text{ GeV/cm}^3 \quad v_{esc} = 544 \text{ km/s}$$



The Sun

Capture rate :

$$\frac{dC_i}{dV} = \frac{\rho_\odot}{m_\chi} \int_0^{u_{esc}^\odot} du \frac{f(u)}{u} \Omega_i(Q)$$

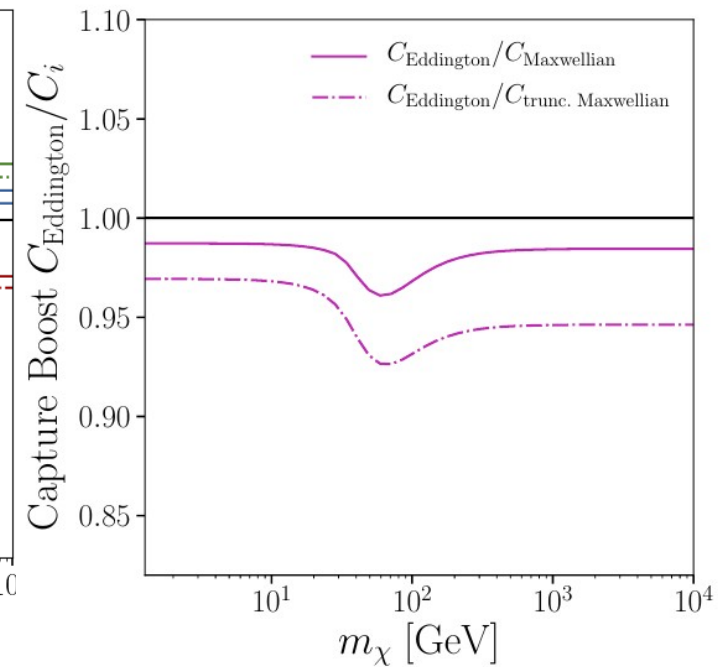
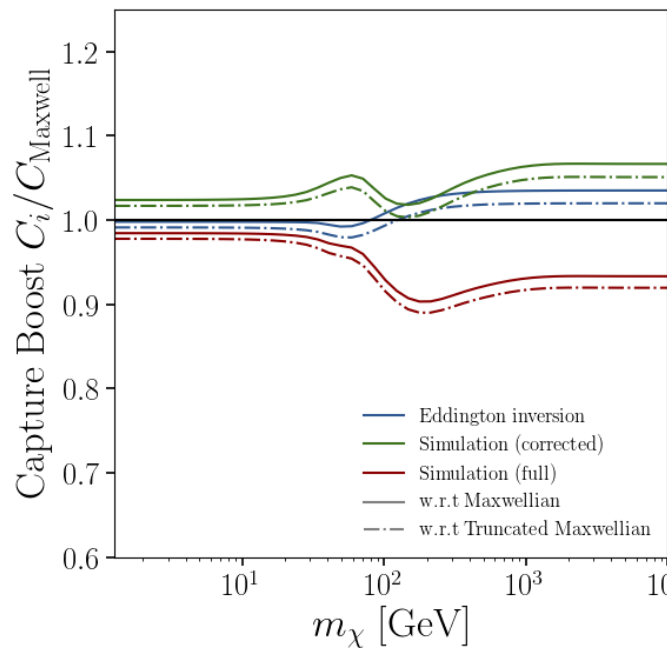
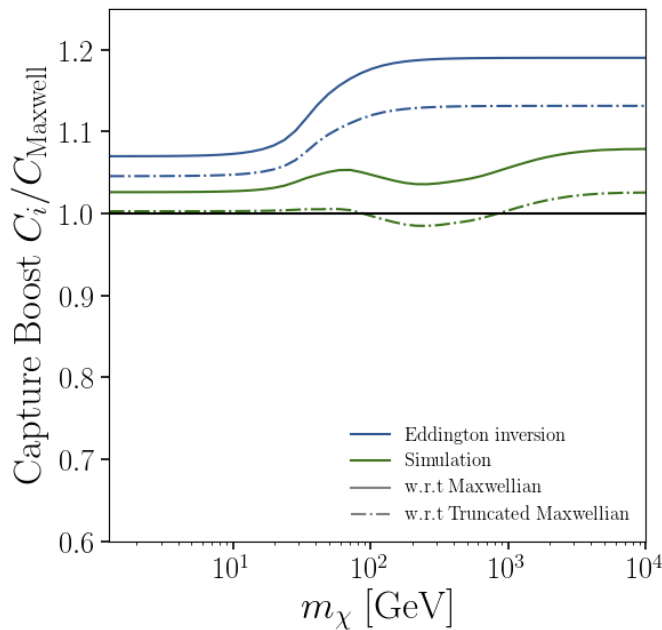
Usual assumptions : *Standard Halo Model (SHM)*
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$$\rho_\odot = 0.3 \text{ GeV/cm}^3 \quad v_{esc} = 544 \text{ km/s}$$

Beyond SHM :

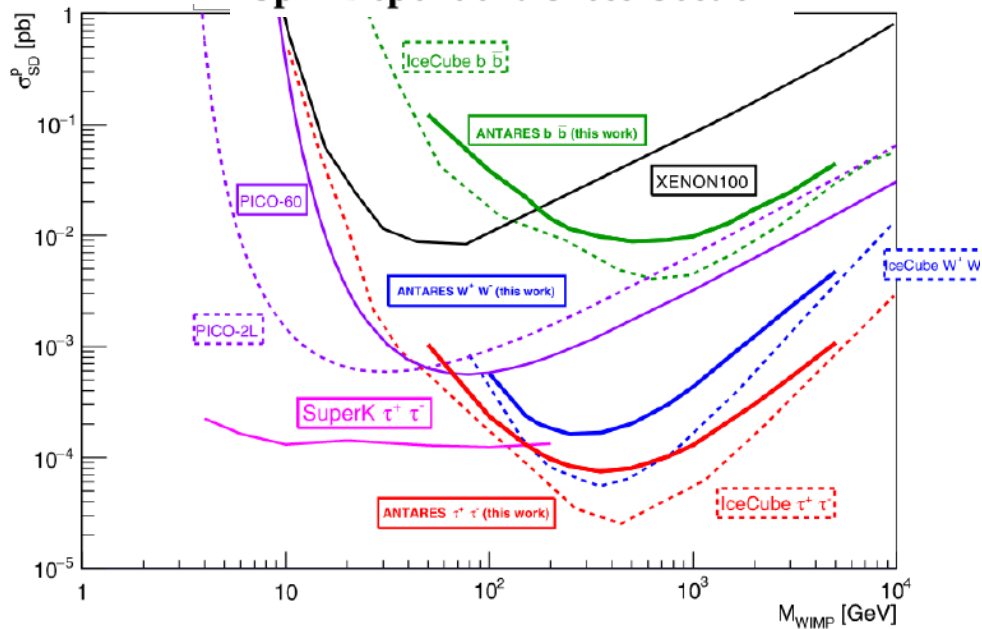


Nunez-Castineyra et al 2019, 20% uncertainties on capture
 Choi et al 2014

The Sun

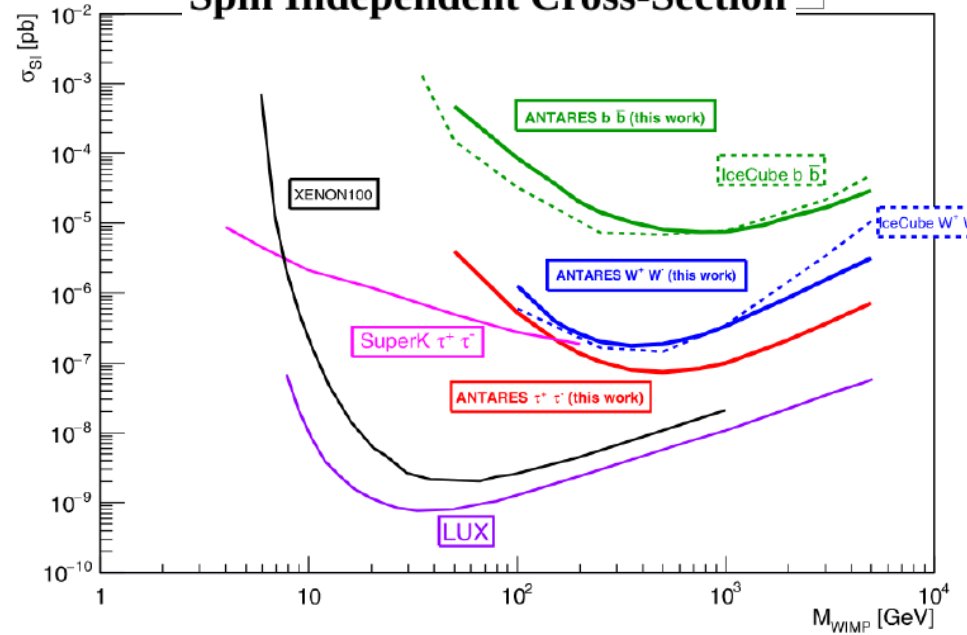
Limit on Spin Dependent Cross-Section

ANTARES

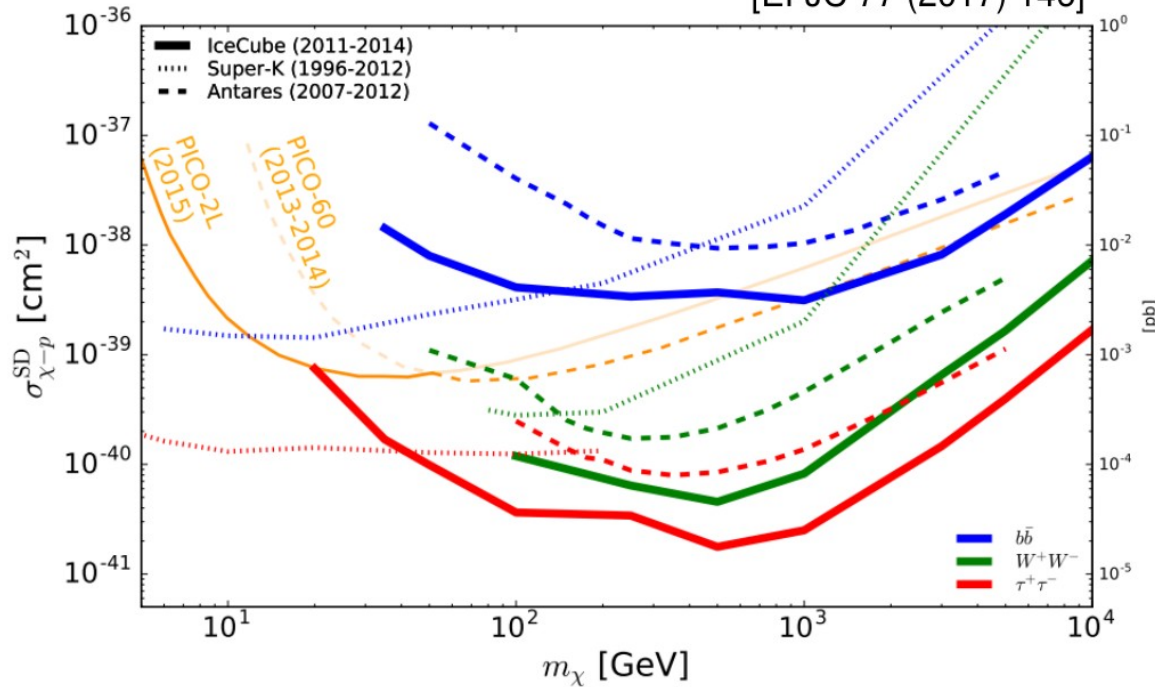


Phys. Lett. B 759 (2016) 69

Limit on Spin Independent Cross-Section



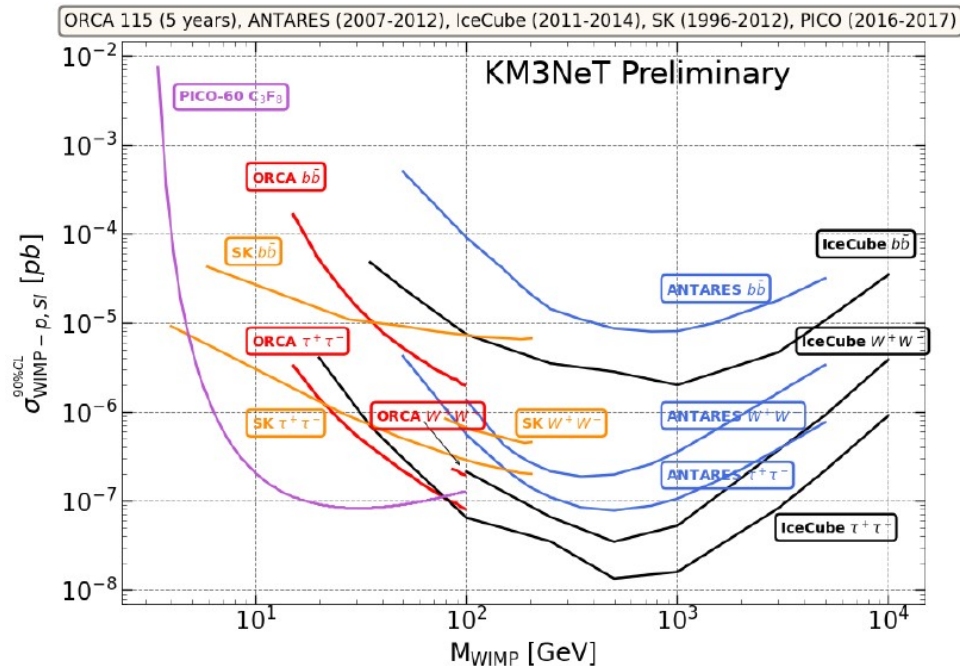
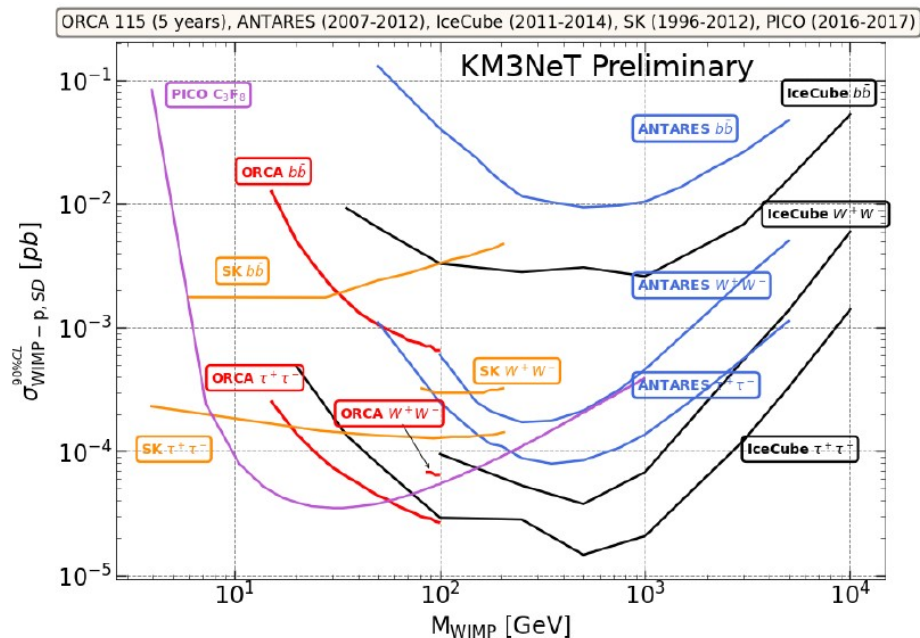
[EPJC 77 (2017) 146]



ICECUBE

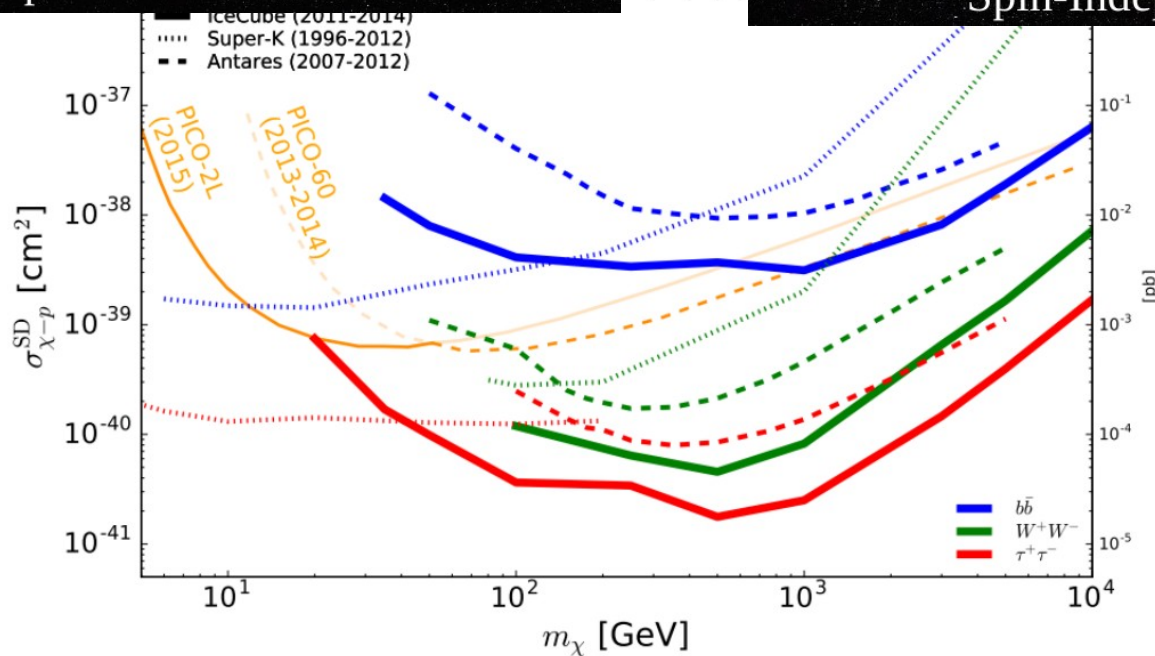
The Sun

KM3NeT



Spin-Dependent Cross section

Spin-Independent Cross section



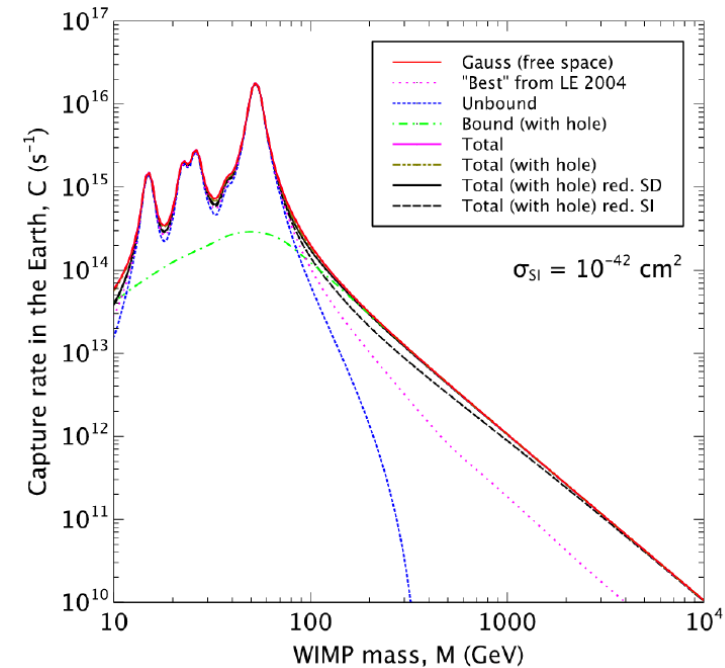
ICECUBE

The Earth

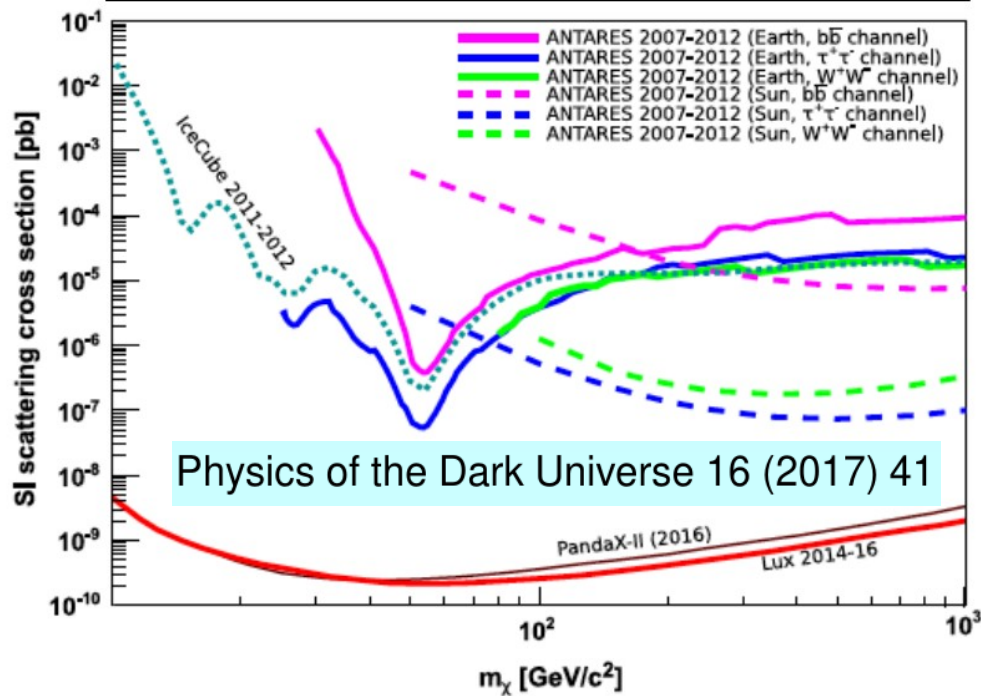
- Scalar coupling, Resonant capture with nuclei masses.

- Out of equilibrium

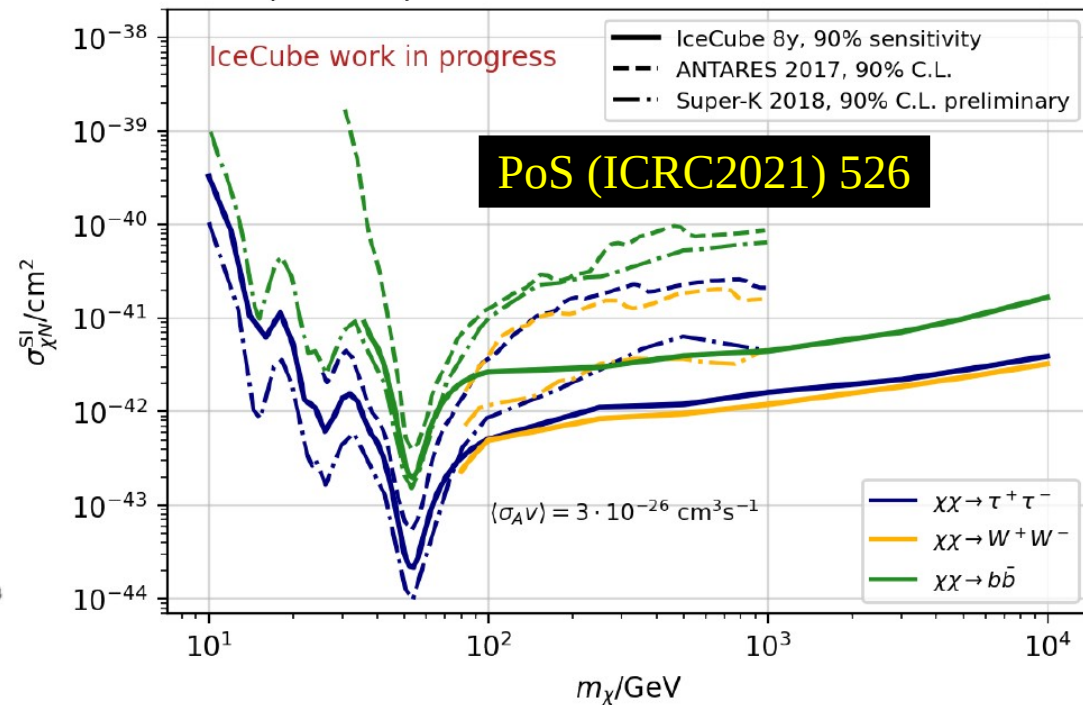
$$\sqrt{CC_A}t \ll 1, \Gamma_A \approx \frac{1}{2}C^2C_A t^2$$



Limit on WIMP-nucleon SI cross-section assuming 100% BR of annihilation into benchmark channel



Spin Independent WIMP-nucleon cross section



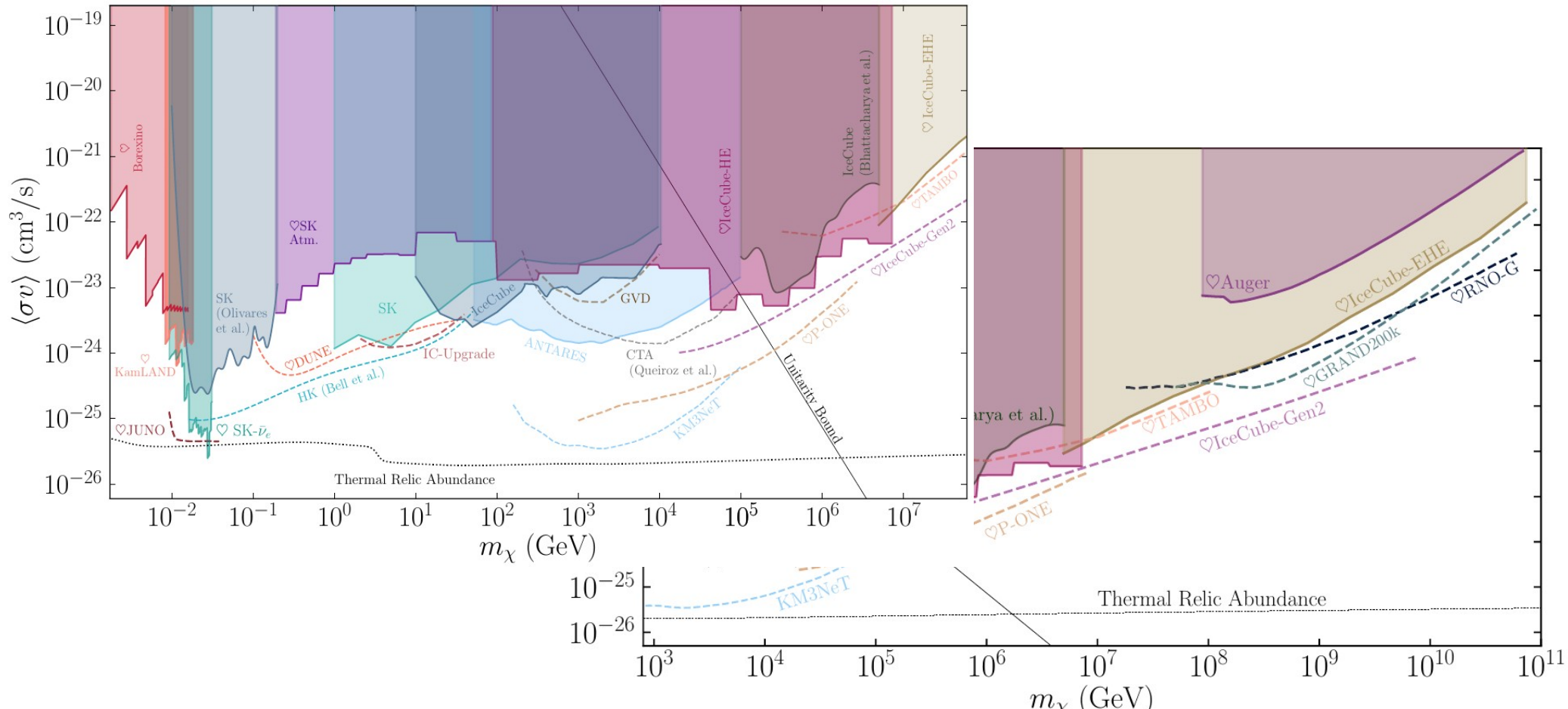
Dark Matter annihilation to Neutrinos

PoS (ICRC2021) 542

$$\chi\chi \rightarrow \nu\bar{\nu}$$

Galactic flux :
$$\frac{d\Phi_{\nu+\bar{\nu}}}{dE_\nu} = \frac{1}{4\pi} \frac{\sigma v}{\text{km}^2_\chi} \frac{1}{3} \frac{dN_\nu}{dE_\nu} \int d\Omega \int_{\text{l.o.s.}} \rho_\chi^2(x) dx$$

Extra galactic:
$$\frac{d\Phi_{\nu+\bar{\nu}}}{dE_\nu} = \frac{1}{4\pi} \frac{\Omega_{DM}^2 \rho_c^2 \sigma v}{\text{km}^2_\chi} \frac{1}{3} \int_0^{z_{up}} dz \frac{(1+G(z))(1+z)^3}{H(z)} \frac{dN_{\nu+\bar{\nu}}(E')}{dE'}$$



Angular Power Spectrum analysis

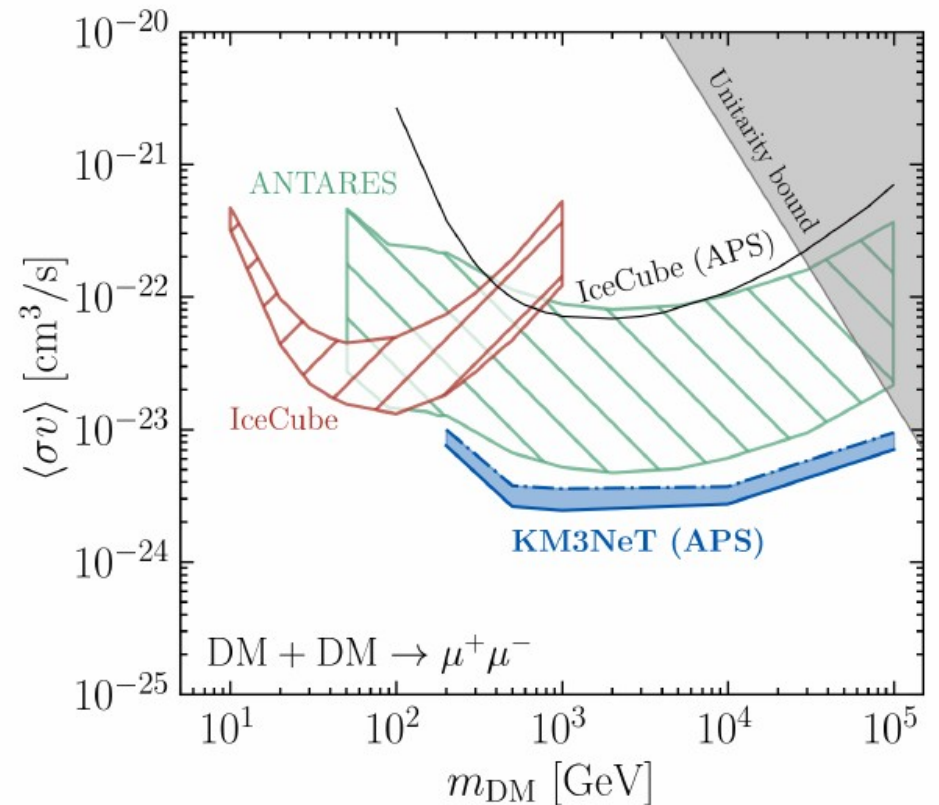
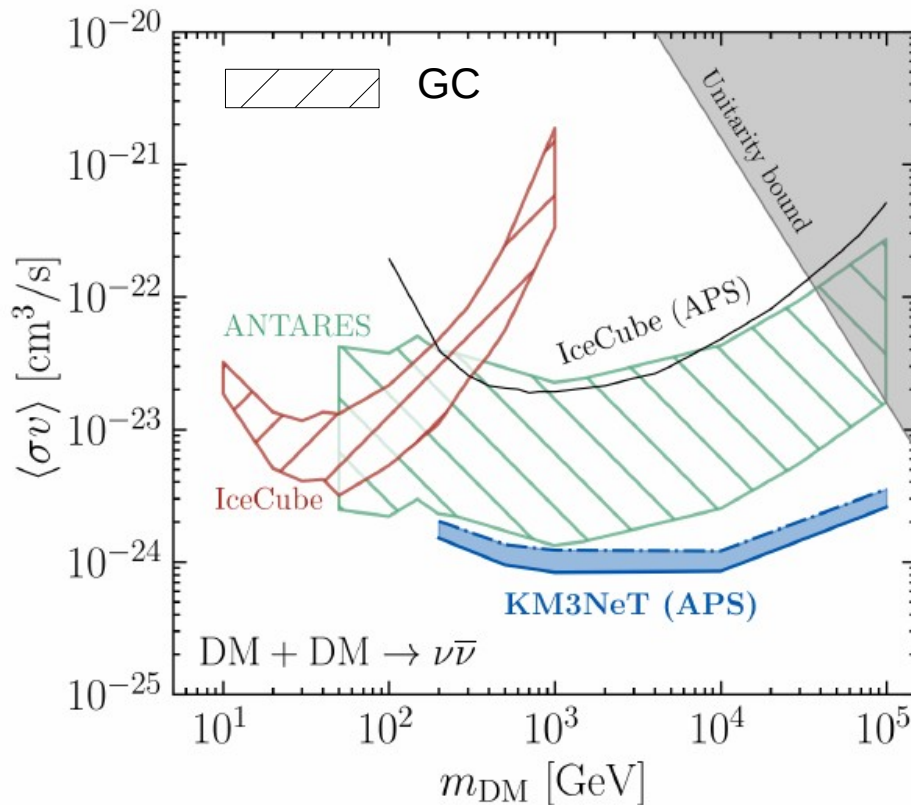
PoS (ICRC2021) 550

arXiv:2103.01237

Flux :

$$\frac{d\Phi_{\nu_\alpha + \bar{\nu}_\alpha}^{\text{DM}}}{dE_\nu d\Omega} = \sum_{\alpha\beta} P_{\alpha\beta} \left[\frac{d\Phi_{\nu_\beta + \bar{\nu}_\beta}^{\text{gal.}}}{dE_\nu d\Omega} + \frac{d\Phi_{\nu_\beta + \bar{\nu}_\beta}^{\text{ext.gal.}}}{dE_\nu d\Omega} \right]$$

$P_{\alpha\beta} = \sum_{i=3}^3 |U_{\alpha i}|^2 |U_{\beta i}|^2$ are the flavour-transition probabilities

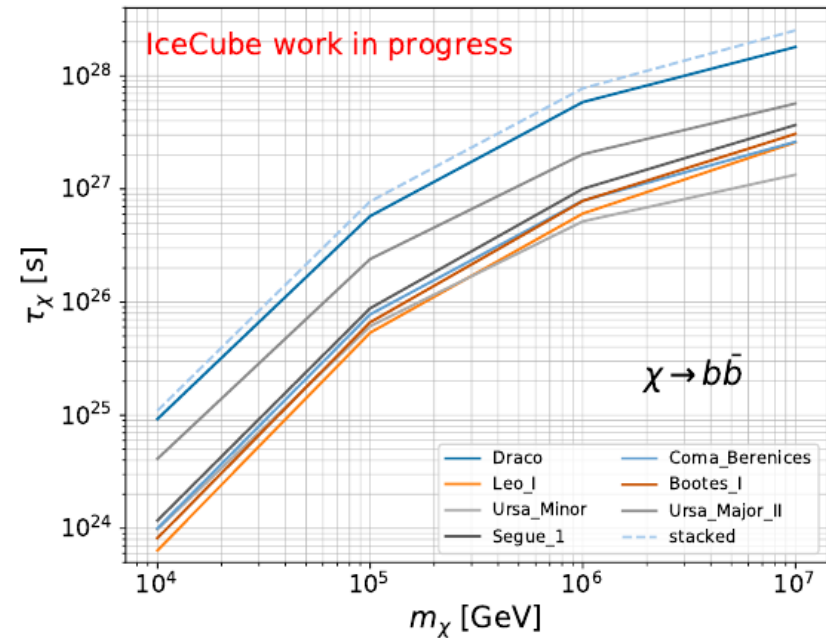
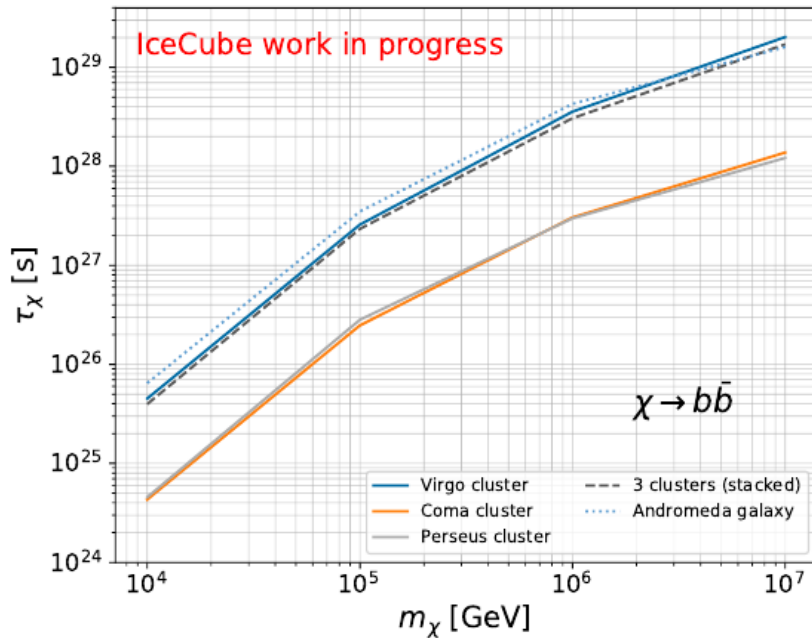
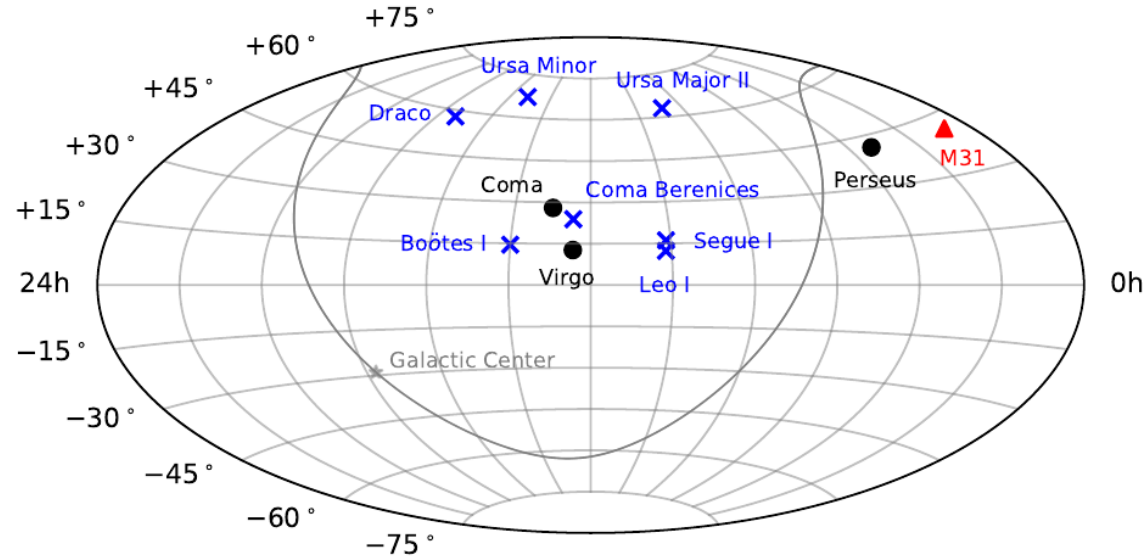


Decaying Dark Matter

PoS (ICRC2021) 506

Flux :

$$\frac{d\Phi_\nu}{dE_\nu}(E_\nu) = \frac{1}{4\pi m_\chi \tau_\chi} \frac{dN_\nu}{dE_\nu}(E_\nu) \int_0^{\Delta\Omega} d\Omega \int_0^\infty \rho_\chi(l\hat{n}) dl,$$

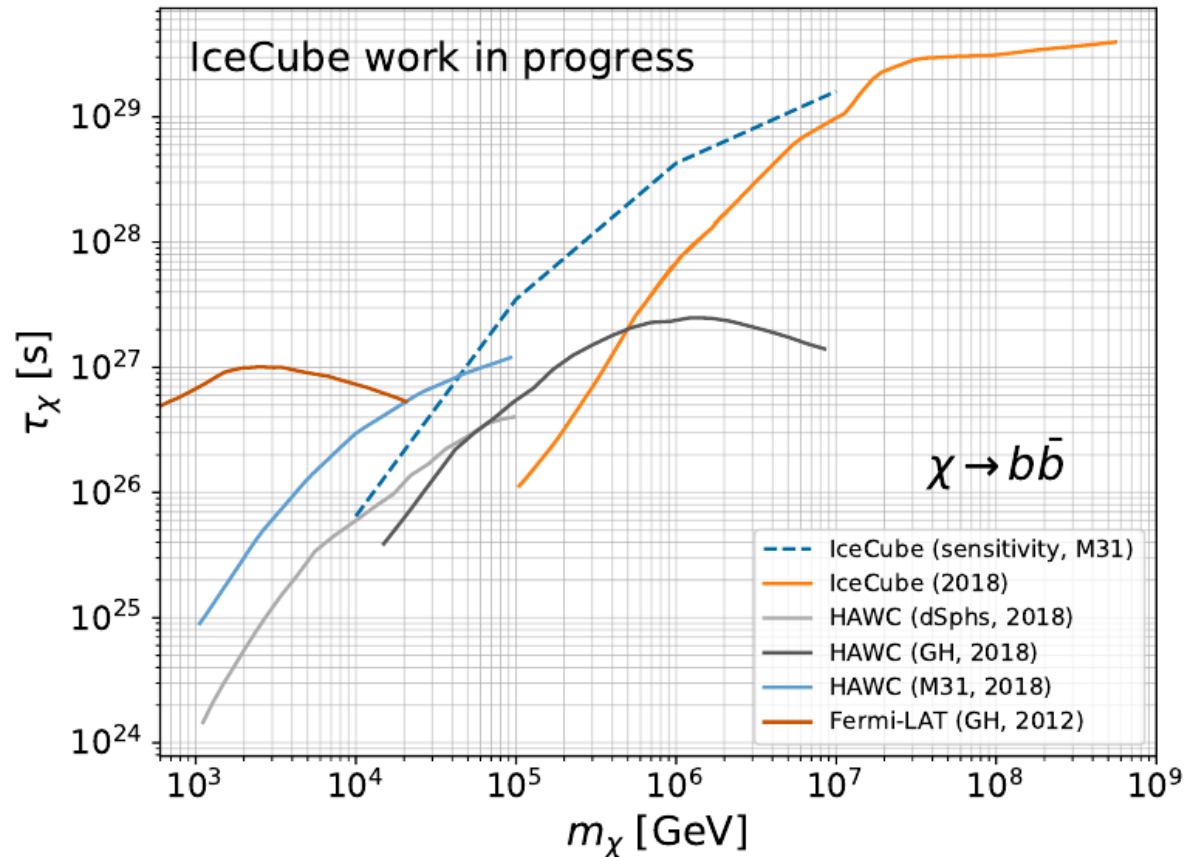


Decaying Dark Matter

PoS (ICRC2021) 506

Flux :

$$\frac{d\Phi_\nu}{dE_\nu}(E_\nu) = \frac{1}{4\pi m_\chi \tau_\chi} \frac{dN_\nu}{dE_\nu}(E_\nu) \int_0^{\Delta\Omega} d\Omega \int_0^\infty \rho_\chi(l\hat{n}) dl.$$



Secluded Dark Matter

JCAP 05 (2016) 016

JCAP04(2017) 010

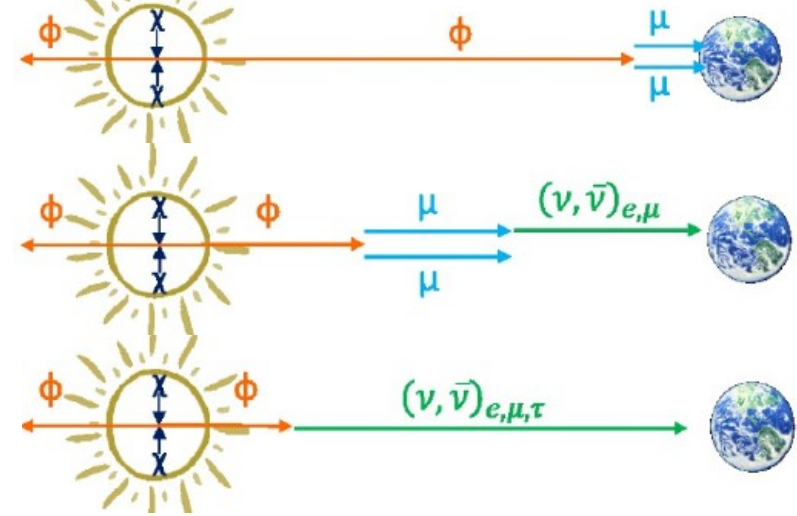
DM annihilates into **unstable mediator Φ** .
 Detectable particles: dimuons or neutrinos.

3 cases:

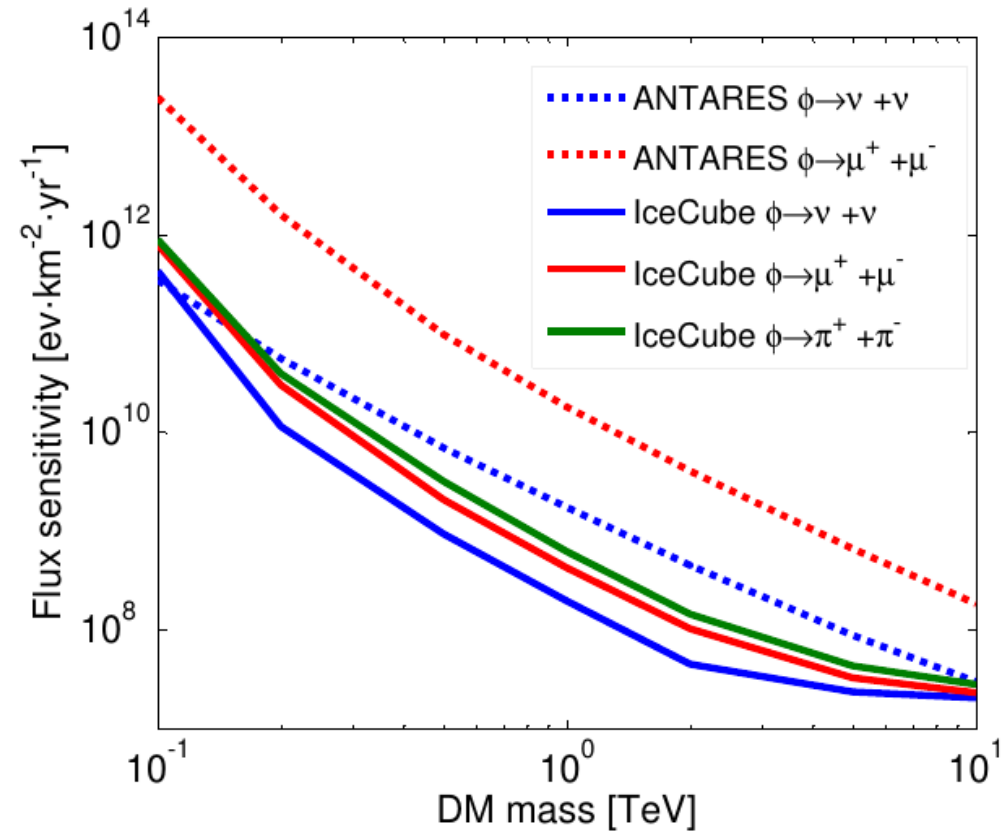
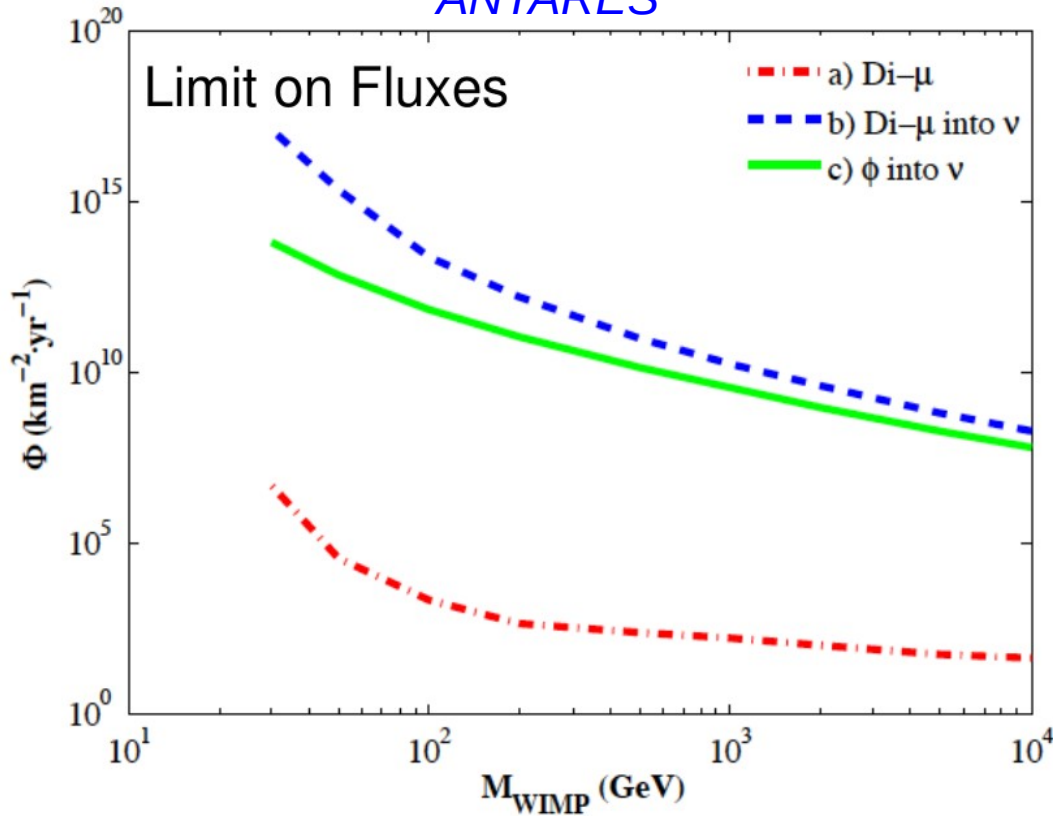
- ◆ $\Phi \rightarrow \mu\mu$.
- ◆ $\Phi \rightarrow \mu\mu \rightarrow \nu\nu$.
- ◆ $\Phi \rightarrow \nu\nu$.

Testing models from:

- Meade et al., JHEP06 (2010) 29
- Bell and Petraki, JCAP04 (2011) 003



ANTARES



Secluded Dark Matter

JCAP 05 (2016) 016

JCAP04(2017) 010

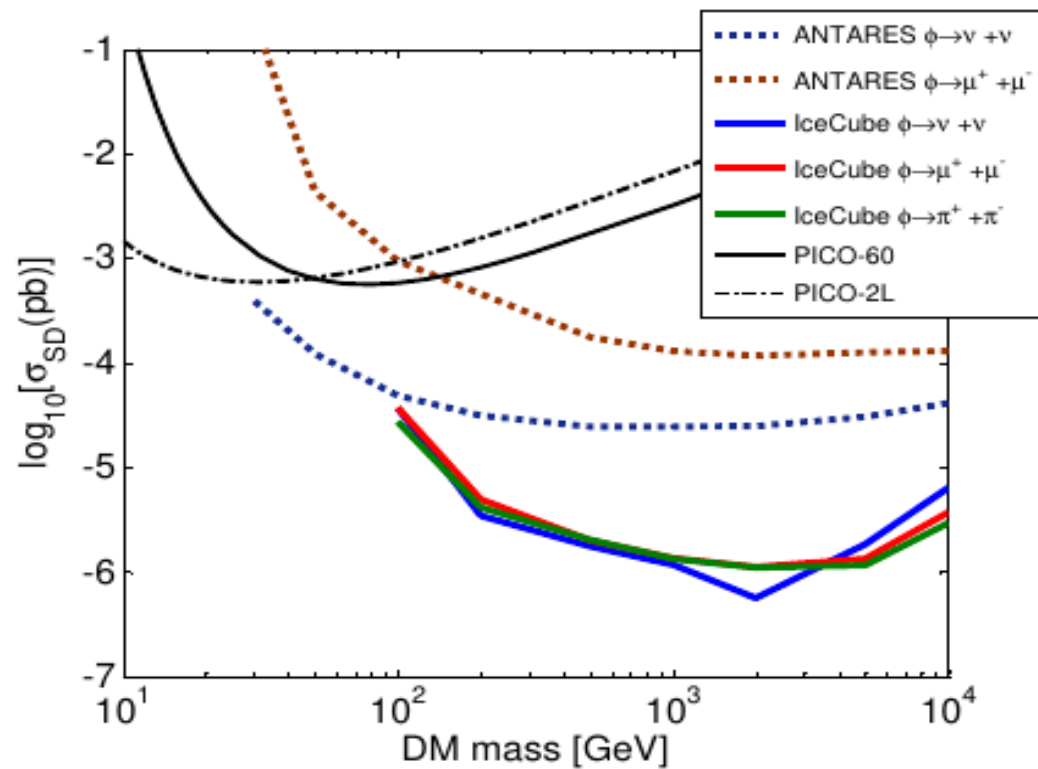
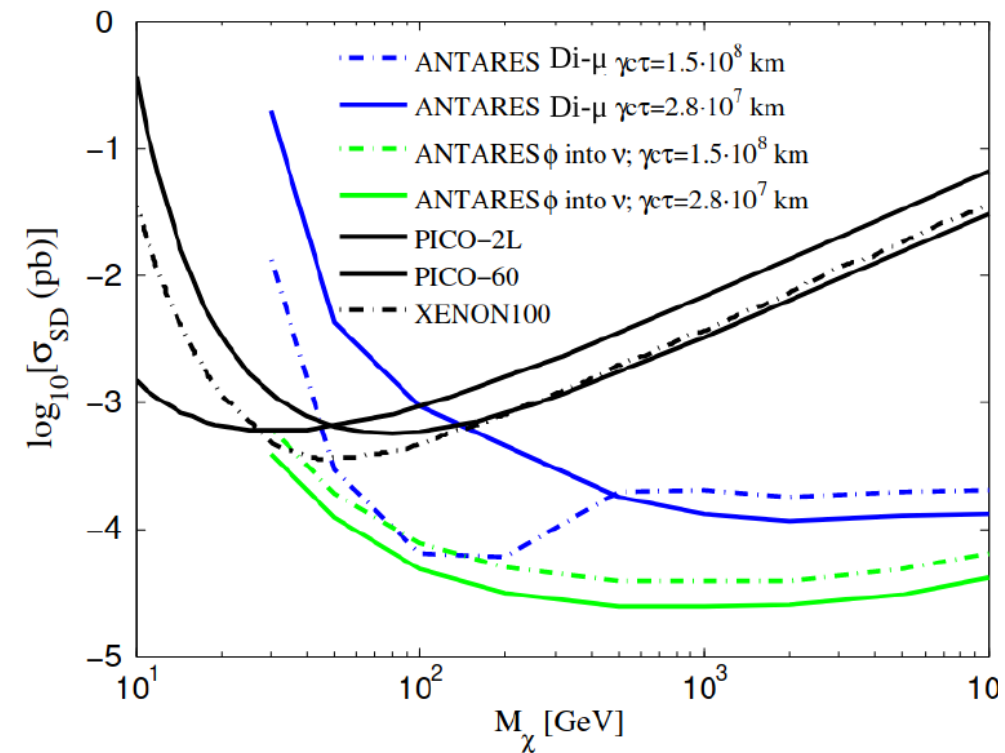
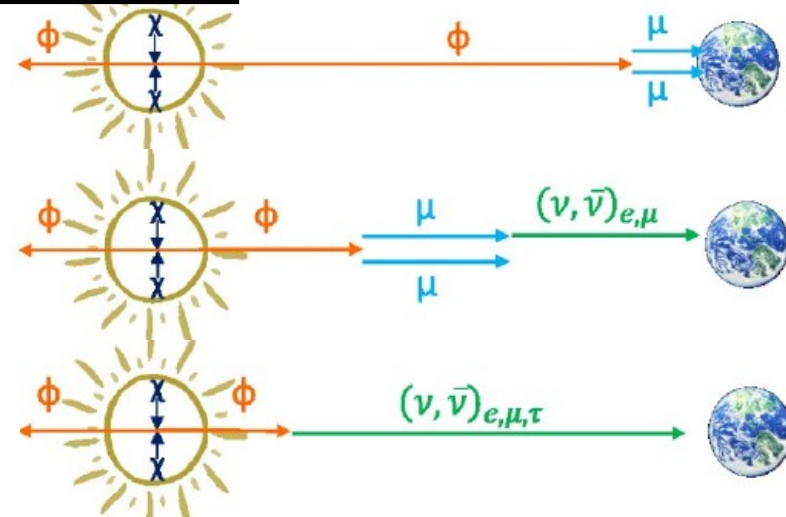
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Secluded Dark Matter

JCAP 05 (2016) 016

JCAP04(2017) 010

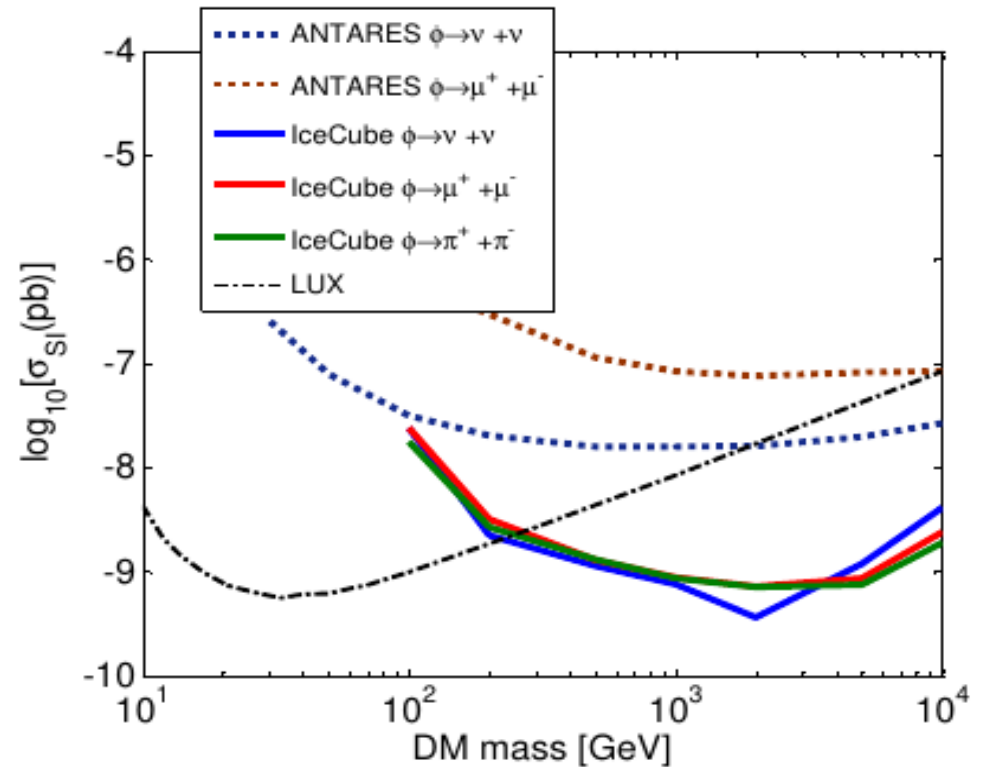
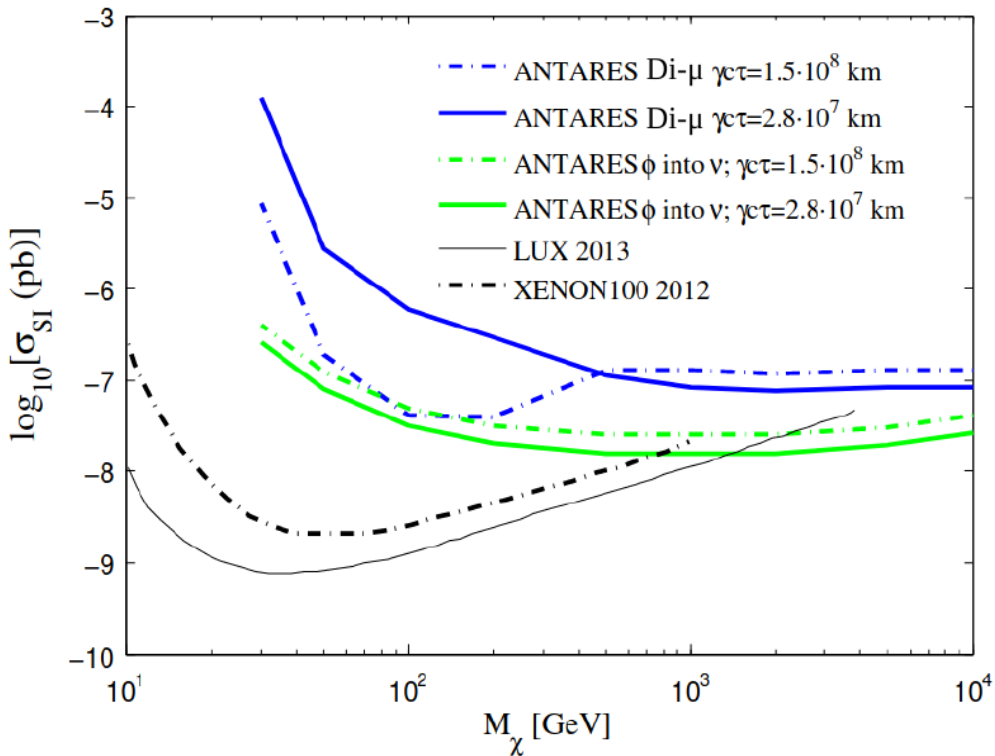
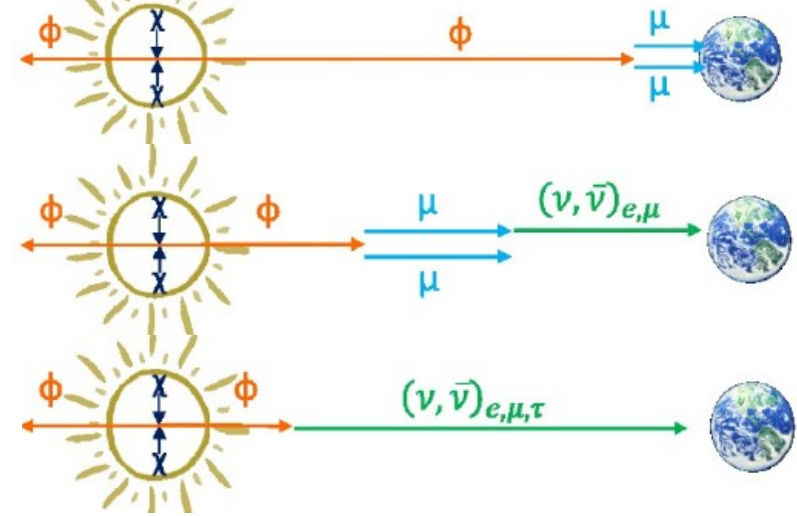
DM annihilates into **unstable mediator Φ** .
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3 cases:

- ◆ $\Phi \rightarrow \mu\mu$.
- ◆ $\Phi \rightarrow \mu\mu \rightarrow \nu\nu$.
- ◆ $\Phi \rightarrow \nu\nu$.

Testing models from:

- Meade et al., JHEP06 (2010) 29
- Bell and Petraki, JCAP04 (2011) 003



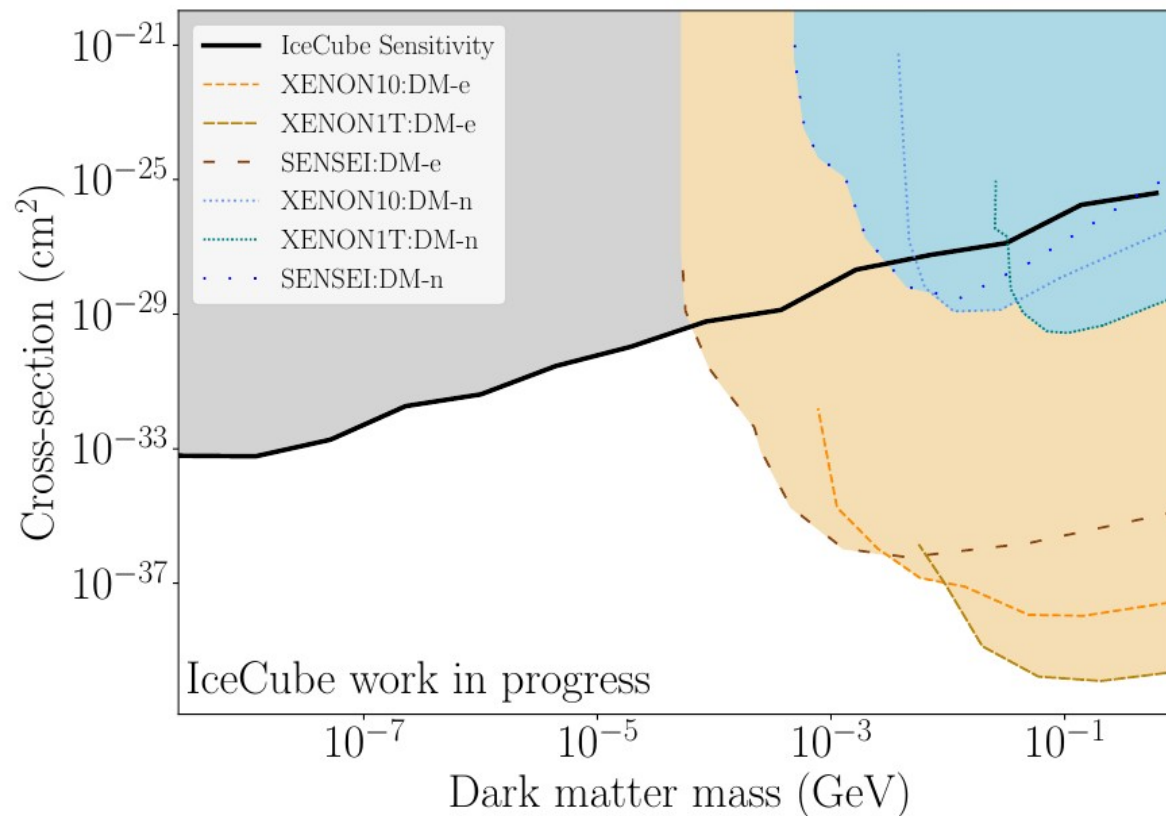
Dark matter neutrino scattering in the Galactic Centre

PoS (ICRC2021) 569

DM-neutrino scattering → Suppression of the high-energy astrophysical neutrino flux in the direction of the Galactic Centre ?

$$\frac{d\Phi(E, \tau)}{d\tau} = -\sigma(E)\Phi(E, \tau) + \int_E^\infty d\tilde{E} \frac{d\sigma(\tilde{E}, E)}{dE} \Phi(\tilde{E}, \tau)$$

$$\tau(\vec{x}) = \int_{l.o.s} n_\chi(\vec{x}) dx \quad n_\chi = \frac{\rho_\chi}{m_\chi}$$



Summary-Conclusion

- *Specific astronomy, interesting to look for dark matter*
Dsphs, galaxy clusters, Galactic Center, Sun, Earth
- *Bring info on DM nature, can test specific BSM scenarii/models*
- *(Non)Signal → Complementary researches with*
direct detection
gamma, CR indirect detection
- *Sun, golden signal*
- *Km3(s) size detector era already started*
Stay tuned



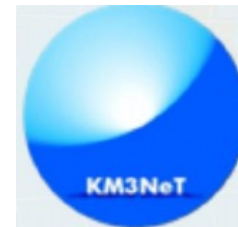
P-ONE
Deep water
1 km³
Planned 2023



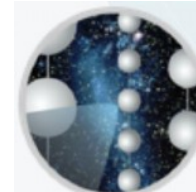
Baikal/GVD
Deep water
~1 km³
Construction



ANTARES
Deep water
0.01 km³
2008 –



KM3NeT
Deep water
1 + 0.006 km³
Construction



ICECUBE

<u>IceCube</u>	<u>IceCube-Gen2</u>
Deep ice	Deep ice
1 km ³	~10 km ³
2011 –	Projected, 1 st phase imminent

Thanks

Back-up

Test other assumptions for $f(v)$

Nunez-Castineyra, EN, Mollitor, Devriendt, Teyssier

In prep

Maxwellian

$$f(\vec{v}) = \frac{N}{2\pi v_0^2} \exp\left(-\frac{3|\vec{v}|^2}{2v_0^2}\right)$$

Generalized Maxwellian

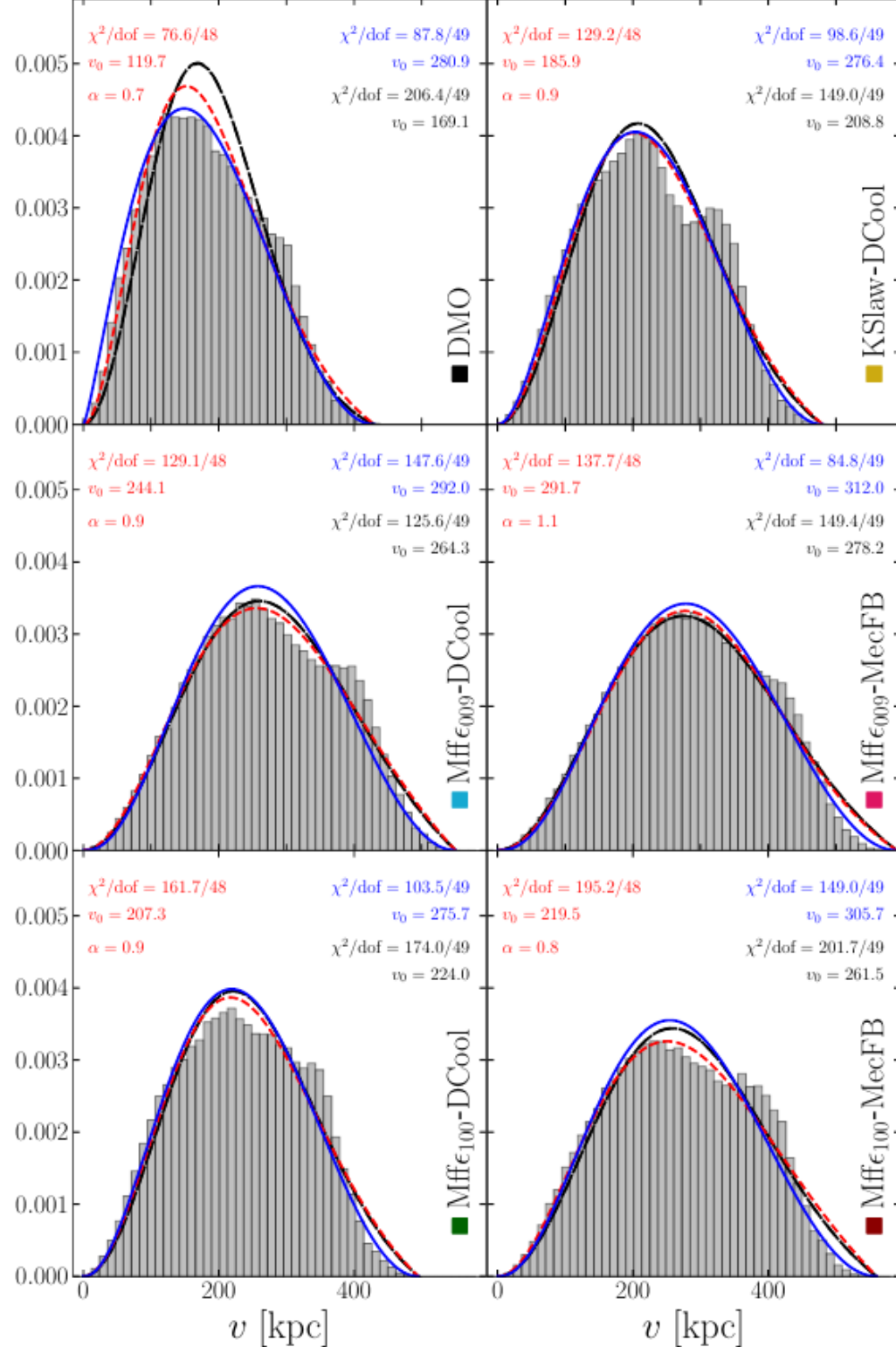
$$f(\vec{v}) = \frac{e^{-(\vec{v}^2/v_0^2)^\alpha}}{N(v_0, \alpha)}$$

Tsallis

$$f(\vec{v}) = \frac{1}{N(v_0, q)} \left(1 - (1 - q) \frac{\vec{v}^2}{v_0^2}\right)^{q/(1-q)}$$

Mao+ 2013

$$f(v, v_0, v_{\text{esc}}, p) = \frac{1}{N} v^2 \exp^{-\frac{v}{v_0}} (v_{\text{esc}}^2 - v^2)^p$$



The Sun

Orders of magnitude

$$\rho_\chi^0 \simeq 0.3 - 0.5 \text{ GeV/cm}^3 ; v_\chi^0 \simeq 220 - 300 \text{ km/sec}$$

$$\phi_\chi = \frac{\rho_\chi^0}{m_\chi} v_\chi^0 \simeq \frac{0.4 \text{ cm}^{-3}}{m_\chi [\text{GeV}]} \times (3 \times 10^7 \text{ cm/s}) \simeq \frac{1.2 \times 10^7}{m_\chi [\text{GeV}]} \text{ cm}^{-2} \text{ s}^{-1}$$

$$\sigma_{\chi-p} \simeq (G_F m_p^2)^2 \frac{1}{m_W^2} = 6 \times 10^{-42} \text{ cm}^2$$

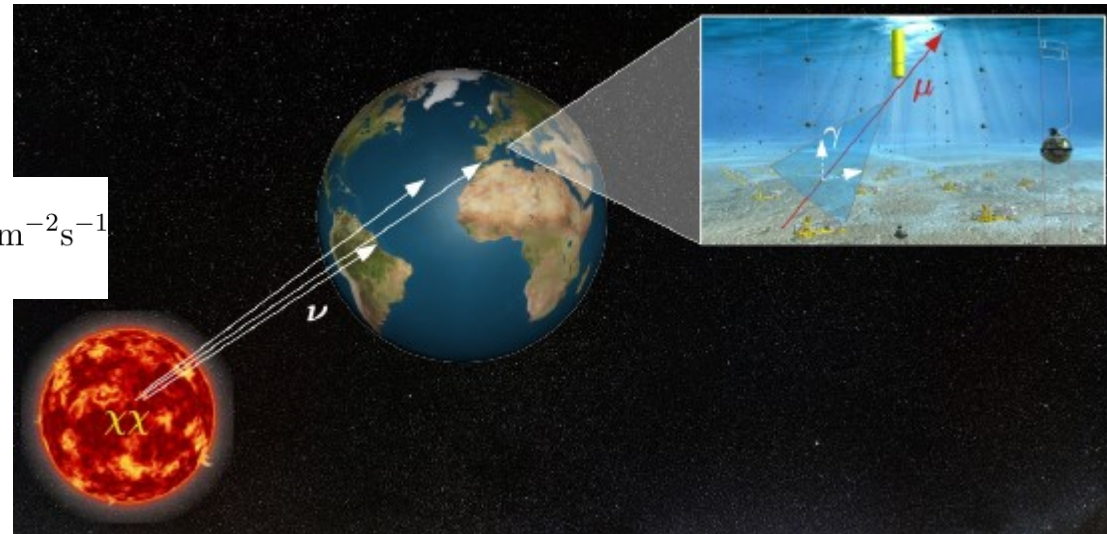
$$C_\odot = M_\odot N_A \sigma_{\chi-p} = 1.2 \times 10^{57} \sigma_{\chi-p}$$

$$\phi_\nu^\odot = \frac{\phi_\chi C_\odot}{4\pi d^2} = \frac{3. \times 10^{-5}}{m_\chi (\text{GeV})} \text{ cm}^{-2} \text{ s}^{-1} \simeq \frac{1 \times 10^{13}}{m_\chi [\text{GeV}]} \text{ km}^{-2} \text{ yr}^{-1}$$

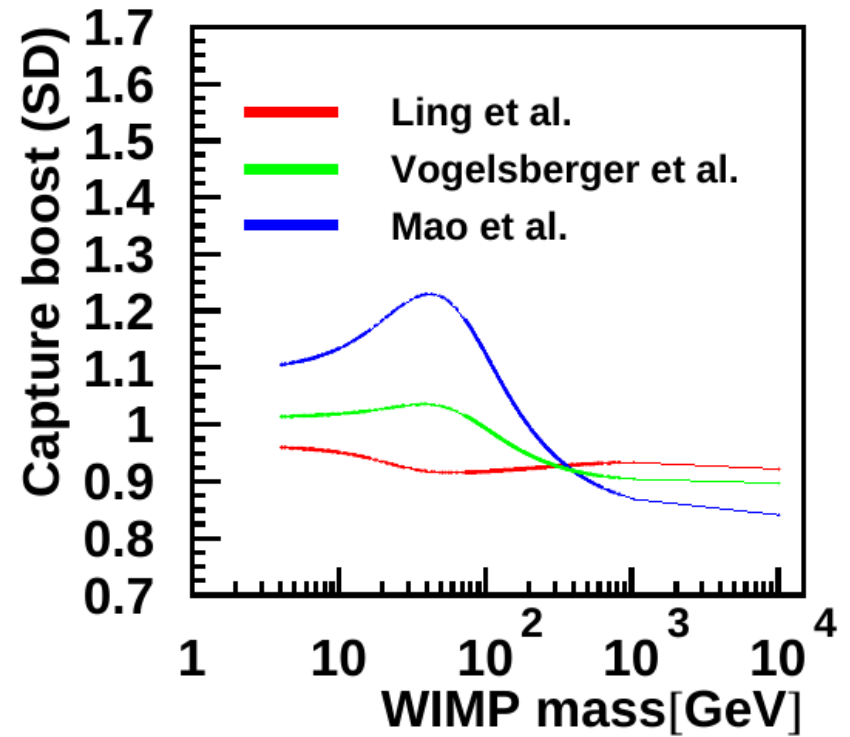
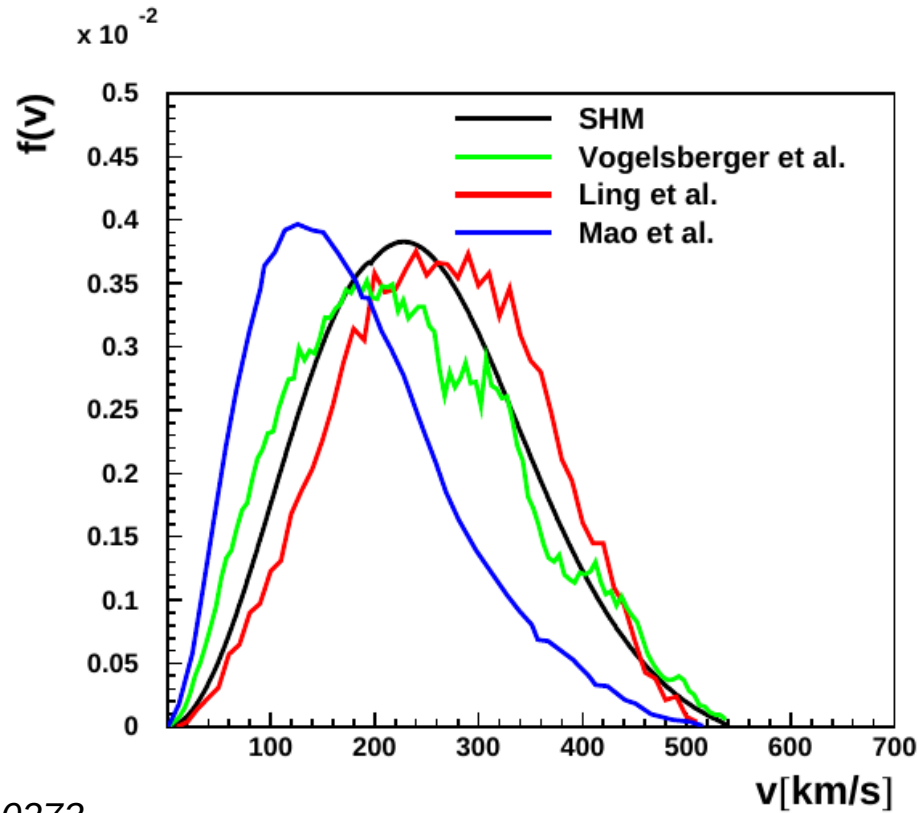
$$P = N_A \sigma_{\nu-N} R_\mu \simeq 1 - 2 \times 10^{-13} (m_\chi [\text{GeV}])^2$$

$$\phi_\mu^\odot = \phi_\nu^\odot P \simeq 10^2 - 10^3 \text{ km}^{-2} \text{ yr}^{-1}$$

→ *km3 detector*



Capture rate in the Sun



Choi+ 1312.0273

Dark disc :

Read+ 09
Brush+ 09
Ling 2010