

On the B -meson decay anomalies

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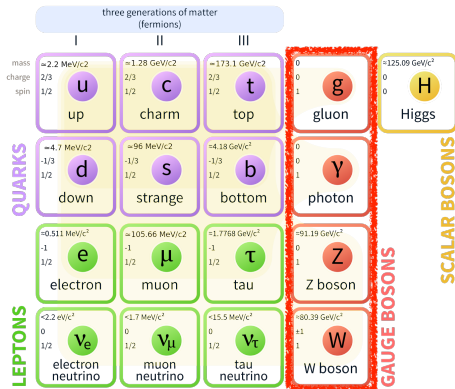
Based on: 2104.00015 with C. Hati, J. Orloff and A. M. Teixeira

22 October 2021

Flavour Physics

- In SM, force carriers

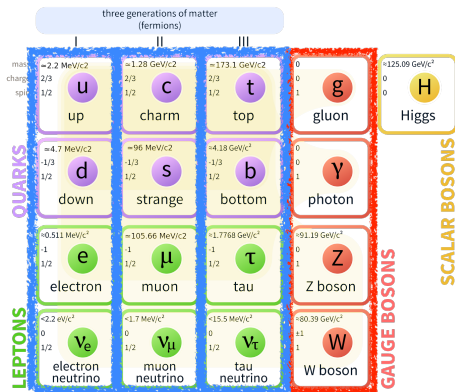
Standard Model of Elementary Particles



Flavour Physics

- In SM, force carriers and 3 generations of matter

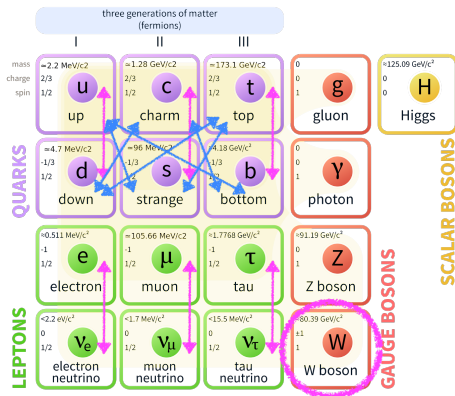
Standard Model of Elementary Particles



Flavour Physics

- In SM, force carriers and 3 generations of matter
- **Quark** sector: Higgs mechanism responsible for quark masses and **quark** flavour mixing

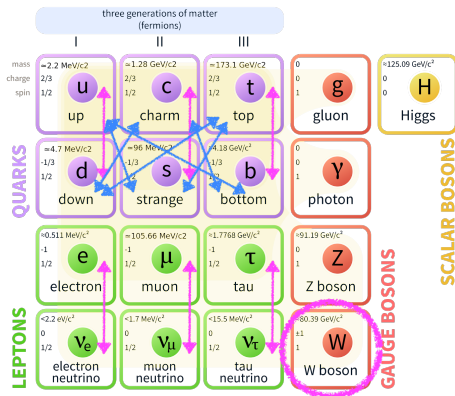
Standard Model of Elementary Particles



Flavour Physics

- In SM, force carriers and 3 generations of matter
- **Quark** sector: Higgs mechanism responsible for quark masses and **quark** flavour mixing
- Unitary **CKM** matrix \Rightarrow no flavour changing neutral current (**FCNC**) at *tree-level*
- **Lepton** sector: vanishing ν -masses \Rightarrow *accidental* lepton flavour conservation

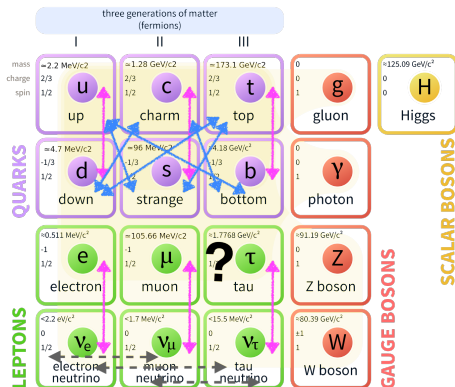
Standard Model of Elementary Particles



Flavour Physics

- In SM, force carriers and 3 generations of matter
- Quark** sector: Higgs mechanism responsible for quark masses and **quark** flavour mixing
- Unitary **CKM** matrix \Rightarrow no flavour changing neutral current (**FCNC**) at *tree*-level
- Lepton** sector: vanishing ν -masses \Rightarrow *accidental* lepton flavour conservation
- BUT**: ν oscillate, thus have (*tiny*) masses \Rightarrow explaining ν oscillations opens the door to lepton flavour violation (**LFV**)!

Standard Model of Elementary Particles

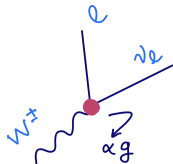


Lepton flavour universality

Only difference between leptons is their masses:

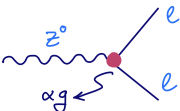
$$m_e \sim 511 \text{ keV}, \quad m_\mu \sim 105 \text{ MeV}, \quad m_\tau \sim 1.7 \text{ GeV}$$

Accidental “symmetry” in the SM: couplings of electroweak gauge bosons are “blind” to lepton **flavour** \Rightarrow **Lepton Flavour Universality (LFU)**



W^+ DECAY MODES

	Fraction (Γ_i/Γ)
$\ell^+ \nu$	[b] $(10.86 \pm 0.09) \%$
$e^+ \nu$	$(10.71 \pm 0.16) \%$
$\mu^+ \nu$	$(10.63 \pm 0.15) \%$
$\tau^+ \nu$	$(11.38 \pm 0.21) \%$
hadrons	$(67.41 \pm 0.27) \%$



Z DECAY MODES

	Fraction (Γ_i/Γ)
$e^+ e^-$	[h] $(3.3632 \pm 0.0042) \%$
$\mu^+ \mu^-$	[h] $(3.3662 \pm 0.0066) \%$
$\tau^+ \tau^-$	[h] $(3.3696 \pm 0.0083) \%$
$\ell^+ \ell^-$	[b,h] $(3.3658 \pm 0.0023) \%$

[PDG 2020]

\Rightarrow **BUT:** current measurements in semi-leptonic **B**-meson decays and low energy precision observables appear to tell a different story!

Hadrons

QCD bound states of quarks: Baryons ~ 3 quarks, Mesons ~ 1 quark, 1 anti-quark

mass	$\approx 2.2 \text{ MeV}/c^2$	$\approx 1.28 \text{ GeV}/c^2$	$\approx 173.1 \text{ GeV}/c^2$
charge	$2/3$	$2/3$	$2/3$
spin	$1/2$	$1/2$	$1/2$
	u up	c charm	t top
QUARKS	$\approx 4.7 \text{ MeV}/c^2$	$\approx 96 \text{ MeV}/c^2$	$\approx 4.18 \text{ GeV}/c^2$
	$-1/3$	$-1/3$	$-1/3$
	$1/2$	$1/2$	$1/2$
	d down	s strange	b bottom

Hadrons

QCD bound states of quarks: Baryons \sim 3 quarks, Mesons \sim 1 quark, 1 anti-quark

- Proton $|p\rangle \sim |uud\rangle$,
neutron $|n\rangle \sim |udd\rangle$,
pions $|\pi^0\rangle \sim \frac{|u\bar{u}\rangle + |d\bar{d}\rangle}{\sqrt{2}}$, $|\pi^+\rangle \sim |u\bar{d}\rangle$

QUARKS	mass charge spin	$\approx 2.7 \text{ MeV}/c^2$ $2/3$ $1/2$ u up	$\approx 1.28 \text{ GeV}/c^2$ $2/3$ $1/2$ c charm	$\approx 173.1 \text{ GeV}/c^2$ $2/3$ $1/2$ t top
		$\approx 4.7 \text{ MeV}/c^2$ $-1/3$ $1/2$ d down	$\approx 96 \text{ MeV}/c^2$ $-1/3$ $1/2$ s strange	$\approx 4.18 \text{ GeV}/c^2$ $-1/3$ $1/2$ b bottom

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\Rightarrow Kaons: $|K^0\rangle \sim |\bar{s}d\rangle$, $|K^+\rangle \sim |\bar{s}u\rangle$

QUARKS	mass charge spin	$\approx 2.2 \text{ MeV}/c^2$ 2/3 1/2	$\approx 1.28 \text{ GeV}/c^2$ 2/3 1/2	$\approx 173.1 \text{ GeV}/c^2$ 2/3 1/2
		u up	c charm	t top
		$\approx 4.7 \text{ MeV}/c^2$ -1/3 1/2	$\approx 96 \text{ MeV}/c^2$ -1/3 1/2	$\approx 4.18 \text{ GeV}/c^2$ -1/3 1/2
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\Rightarrow **K**aons: $|K^0\rangle \sim |\bar{s}d\rangle$, $|K^+\rangle \sim |\bar{s}u\rangle$

\Rightarrow **B** mesons: $|B^0\rangle \sim |\bar{b}d\rangle$, $|B^+\rangle \sim |\bar{b}u\rangle$

QUARKS	mass charge spin	$\approx 2.7 \text{ MeV}/c^2$ 2/3 1/2 u up	$\approx 1.28 \text{ GeV}/c^2$ 2/3 1/2 c charm	$\approx 173.1 \text{ GeV}/c^2$ 2/3 1/2 t top
		$\approx 4.7 \text{ MeV}/c^2$ -1/3 1/2 d down	$\approx 96 \text{ MeV}/c^2$ -1/3 1/2 s strange	$\approx 4.18 \text{ GeV}/c^2$ -1/3 1/2 b bottom

Hadrons

QCD bound states of quarks: Baryons \sim 3 quarks, Mesons \sim 1 quark, 1 anti-quark

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- \Rightarrow **K**aons: $|K^0\rangle \sim |\bar{s}d\rangle$, $|K^+\rangle \sim |\bar{s}u\rangle$
- \Rightarrow **B** mesons: $|B^0\rangle \sim |\bar{b}d\rangle$, $|B^+\rangle \sim |\bar{b}u\rangle$
- \Rightarrow **D** mesons: $|D^0\rangle \sim |\bar{c}u\rangle$, $|D^-\rangle \sim |\bar{c}d\rangle$
- Heavy flavours: hadrons involving **b** or **c** quarks
- (**top** quark does not hadronise, it decays before a bound state can be formed)

QUARKS	mass charge spin	$\approx 2.7 \text{ MeV}/c^2$ 2/3 1/2 u up	$\approx 1.28 \text{ GeV}/c^2$ 2/3 1/2 c charm	$\approx 173.1 \text{ GeV}/c^2$ 2/3 1/2 t top
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B -meson decays

B -mesons offer powerful **probes of the SM** and hints of **new physics**:

- **Theoretically** “clean(ish)” - due to large mass of b -quark, certain theoretical approximations apply and precise predictions are possible (thanks to non-pert. QCD methods)
- **Experimentally** accessible - mostly produced in forward region (design of LHCb), hundreds of decay channels to explore
- Exciting **future programme** (LHCb, Belle II, ...)
- **Charged** current B -decays used to measure **CKM** parameters ($|V_{cb}|, |V_{ub}|, \gamma, \delta_{CP}$)
- B and B_s -meson oscillations offer insight on **CP** violation in the SM
- Due to extremely low SM background, rare **FCNC** B -meson decays are powerful **probes of new physics**

B-meson decays

B-mesons offer powerful

- **Theoretically** “clean” (few hadronic approximations apply to methods)
- **Experimentally** accessible (hundreds of decay channels)
- Exciting future programs
- **Charged** current B-decays
- **B** and **B_s**-meson oscillations
- Due to extremely low backgrounds, B-decays are powerful probes of new physics

B ⁺ DECAY MODES	Fraction (Γ_i/Γ)	Scale factor/ Confidence level (MeV/c)	p
Semileptonic and leptonic modes			
$\ell^+ \nu_\ell X$	[III] (10.99 ± 0.28) %	—	—
$e^+ \nu_e X_c$	(10.8 ± 0.4) %	—	—
$D \ell^+ \nu_\ell X$	(9.7 ± 0.7) %	—	—
$\bar{D}^0 \ell^+ \nu_\ell$	[III] (2.35 ± 0.09) %	2310	—
$\bar{D}^0 \tau^+ \nu_\tau$	(7.7 ± 2.5) × 10 ⁻³	1911	—
$\bar{D}^*(2007)^0 \ell^+ \nu_\ell$	[III] (5.66 ± 0.22) %	2258	—
$\bar{D}^*(2007)^0 \tau^+ \nu_\tau$	(1.88 ± 0.20) %	1839	—
$D^- \pi^+ \ell^+ \nu_\ell$	(4.4 ± 0.4) × 10 ⁻³	2306	—
$\bar{D}_0^*(2420)^0 \ell^+ \nu_\ell, \bar{D}_0^{*0} \rightarrow D^- \pi^+$	(2.5 ± 0.5) × 10 ⁻³	—	—
$\bar{D}_2^{*0}(2460)^0 \ell^+ \nu_\ell, \bar{D}_2^{*0} \rightarrow D^- \pi^+$	(1.53 ± 0.16) × 10 ⁻³	2065	—
$D^{(*)} n \pi^+ \ell^+ \nu_\ell (n \geq 1)$	(1.88 ± 0.25) %	—	—
$D^{*-} \pi^+ \ell^+ \nu_\ell$	(6.0 ± 0.4) × 10 ⁻³	2254	—
$\bar{D}_1^-(2420)^0 \ell^+ \nu_\ell, \bar{D}_1^- \rightarrow D^{*-} \pi^+$	(3.03 ± 0.20) × 10 ⁻³	2084	—
$\bar{D}_1^{\prime-}(2430)^0 \ell^+ \nu_\ell, \bar{D}_1^{\prime0} \rightarrow D^{*-} \pi^+$	(2.7 ± 0.6) × 10 ⁻³	—	—
$\bar{D}_2^{*-}(2460)^0 \ell^+ \nu_\ell, \bar{D}_2^{*0} \rightarrow D^{*-} \pi^+$	(1.01 ± 0.24) × 10 ⁻³	S=2.0 2065	—
$\bar{D}_2^{*0} \rightarrow D^{*-} \pi^+$	(1.7 ± 0.4) × 10 ⁻³	2301	—
$\bar{D}^{*0} \pi^+ \pi^- \ell^+ \nu_\ell$	(8 ± 5) × 10 ⁻⁴	2248	—
$D_s^{(*)-} K^+ \ell^+ \nu_\ell$	(6.1 ± 1.0) × 10 ⁻⁴	—	—
$D_s^- K^+ \ell^+ \nu_\ell$	(3.0 ± 1.4 / 1.2) × 10 ⁻⁴	2242	—

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to non-pert. QCD
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SM
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B-meson decays

B-mesons offer powerful

B ⁺ DECAY MODES		Fraction (Γ_i/Γ)	Scale factor/ Confidence level (MeV/c)	p
Semileptonic and leptonic modes				
$\ell^+ \nu_\ell X$				
$D_s^{*-} K^+ \ell^+ \nu_\ell$	(2.9 ± 1.9) × 10 ⁻⁴	2185	[III] (10.99 ± 0.28) %	—
$\pi^0 \ell^+ \nu_\ell$	(7.80 ± 0.27) × 10 ⁻⁵	2638	(10.8 ± 0.4) %	—
$\eta \ell^+ \nu_\ell$	(3.9 ± 0.5) × 10 ⁻⁵	2611	(9.7 ± 0.7) %	—
$\eta' \ell^+ \nu_\ell$	(2.3 ± 0.8) × 10 ⁻⁵	2553	[III] (2.35 ± 0.09) %	2310
$\omega \ell^+ \nu_\ell$	[III] (1.19 ± 0.09) × 10 ⁻⁴	2582	(7.7 ± 2.5) × 10 ⁻³	1911
$\rho^0 \ell^+ \nu_\ell$	[III] (1.58 ± 0.11) × 10 ⁻⁴	2583	[III] (5.66 ± 0.22) %	2258
$p \bar{p} \ell^+ \nu_\ell$	(5.8 ± 2.6 / 2.3) × 10 ⁻⁶	2467	(1.88 ± 0.20) %	1839
$p \bar{p} \mu^+ \nu_\mu$	< 8.5 × 10 ⁻⁶ CL=90%	2446	(4.4 ± 0.4) × 10 ⁻³	2306
$p \bar{p} e^+ \nu_e$	(8.2 ± 4.0 / 3.3) × 10 ⁻⁶	2467	(2.5 ± 0.5) × 10 ⁻³	—
$e^+ \nu_e$	< 9.8 × 10 ⁻⁷ CL=90%	2640	(1.53 ± 0.16) × 10 ⁻³	2065
$\mu^+ \nu_\mu$	2.90 × 10 ⁻⁰⁷ to 1.07 × 10 ⁻⁰⁶ CL=90%	2639	(1.88 ± 0.25) %	—
$\tau^+ \nu_\tau$	(1.09 ± 0.24) × 10 ⁻⁴ S=1.2	2341	(6.0 ± 0.4) × 10 ⁻³	2254
$\ell^+ \nu_\ell \gamma$	< 3.0 × 10 ⁻⁶ CL=90%	2640	(3.03 ± 0.20) × 10 ⁻³	2084
$e^+ \nu_e \gamma$	< 4.3 × 10 ⁻⁶ CL=90%	2640	(2.7 ± 0.6) × 10 ⁻³	—
$\mu^+ \nu_\mu \gamma$	< 3.4 × 10 ⁻⁶ CL=90%	2639	(1.01 ± 0.24) × 10 ⁻³ S=2.0	2065
$\mu^+ \mu^- \mu^+ \nu_\mu$	< 1.6 × 10 ⁻⁸ CL=95%	2634		
Inclusive modes				
$D^0 X$	(8.6 ± 0.7) %	—	(1.7 ± 0.4) × 10 ⁻³	2301
$\bar{D}^0 X$	(79 ± 4) %	—	(8 ± 5) × 10 ⁻⁴	2248
$D^+ X$	(2.5 ± 0.5) %	—	(6.1 ± 1.0) × 10 ⁻⁴	—
$D^- X$	(9.9 ± 1.2) %	—	(3.0 ± 1.4 / 1.2) × 10 ⁻⁴	2242
$D_s^+ X$	(7.9 ± 1.4 / 1.3) %	—		
$D_s^- X$	(1.10 ± 0.40 / 0.32) %	—		
$\Lambda_c^+ X$	(2.1 ± 0.9 / 0.6) %	—		
$\bar{\Lambda}_c^- X$	(2.8 ± 1.1 / 0.9) %	—		
$\bar{c} X$	(97 ± 4) %	—		

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B^+ DECAY MODES		Fraction (Γ_i/Γ)	Scale factor/ Confidence level (MeV/c)	p	
Semileptonic and leptonic modes					
$\ell^+ \nu_\ell X$		[III] (10.99 \pm 0.28) %	—	—	cs:
		(10.8 \pm 0.4) %	—	—	n theoretical
		(9.7 \pm 0.7) %	—	—	
		[III] (2.35 \pm 0.09) %	2310	—	
± 1.9) $\times 10^{-4}$	2185	$\pi^+ \ell^+ \ell^-$	$B1$	< 4.9	$\times 10^{-8}$ CL=90% 2638
± 0.27) $\times 10^{-5}$	2638	$\pi^+ e^+ e^-$	$B1$	< 8.0	$\times 10^{-8}$ CL=90% 2638
± 0.5) $\times 10^{-5}$	2611	$\pi^+ \mu^+ \mu^-$	$B1$	(1.75 \pm 0.22)	$\times 10^{-8}$ 2634
± 0.8) $\times 10^{-5}$	2553	$\pi^+ \nu \bar{\nu}$	$B1$	< 1.4	$\times 10^{-5}$ CL=90% 2638
± 0.09) $\times 10^{-4}$	2582	$K^+ \ell^+ \ell^-$	$B1$	[III] (4.51 \pm 0.23)	$\times 10^{-7}$ S=1.1 2617
± 0.11) $\times 10^{-4}$	2583	$K^+ e^+ e^-$	$B1$	(5.5 \pm 0.7)	$\times 10^{-7}$ 2617
$+ 2.6$) $\times 10^{-6}$	2467	$K^+ \mu^+ \mu^-$	$B1$	(4.41 \pm 0.22)	$\times 10^{-7}$ S=1.2 2612
$- 2.3$) $\times 10^{-6}$	2446	$K^+ \mu^+ \mu^-$ nonreso-	$B1$	(4.37 \pm 0.27)	$\times 10^{-7}$ 2612
$+ 4.0$) $\times 10^{-6}$	2467	nant			
$- 3.3$) $\times 10^{-6}$	2640	$K^+ \tau^+ \tau^-$	$B1$	< 2.25	$\times 10^{-3}$ CL=90% 1687
$\times 10^{-7}$ CL=90%	2639	$K^+ \bar{\nu} \nu$	$B1$	< 1.6	$\times 10^{-5}$ CL=90% 2617
07 to 1.07×10^{-6} CL=90%	2640	$\rho^+ \nu \bar{\nu}$	$B1$	< 3.0	$\times 10^{-5}$ CL=90% 2583
± 0.24) $\times 10^{-4}$	2341	$K^*(892)^+ \ell^+ \ell^-$	$B1$	[III] (1.01 \pm 0.11)	$\times 10^{-6}$ S=1.1 2564
$\times 10^{-6}$ CL=90%	2640	$K^*(892)^+ e^+ e^-$	$B1$	(1.55 \pm 0.40)	$\times 10^{-6}$ 2564
$\times 10^{-6}$ CL=90%	2639	$K^*(892)^+ \mu^+ \mu^-$	$B1$	(9.6 \pm 1.0)	$\times 10^{-7}$ 2560
$\times 10^{-8}$ CL=95%	2634	$K^*(892)^+ \nu \bar{\nu}$	$B1$	< 4.0	$\times 10^{-5}$ CL=90% 2564
		$K^+ \pi^+ \pi^- \mu^+ \mu^-$	$B1$	(4.3 \pm 0.4)	$\times 10^{-7}$ 2593
		$\phi K^+ \mu^+ \mu^-$	$B1$	(7.9 \pm 2.1)	$\times 10^{-8}$ 2490
		$\bar{\Lambda} p \nu \bar{\nu}$		< 3.0	$\times 10^{-5}$ CL=90% 2430
± 0.7) %	—	$\pi^+ e^+ \mu^-$	LF	< 6.4	$\times 10^{-3}$ CL=90% 2637
± 4) %	—	$\pi^+ e^- \mu^+$	LF	< 6.4	$\times 10^{-3}$ CL=90% 2637
± 0.5) %	—	$\pi^+ e^\pm \mu^\mp$	LF	< 1.7	$\times 10^{-7}$ CL=90% 2637
± 1.2) %	—	$\pi^+ e^+ \tau^-$	LF	< 7.4	$\times 10^{-5}$ CL=90% 2338
$+ 1.4$) %	—	$\pi^+ e^- \tau^+$	LF	< 2.0	$\times 10^{-5}$ CL=90% 2338
$- 1.3$) %	—	$\pi^+ e^\pm \tau^\mp$	LF	< 7.5	$\times 10^{-5}$ CL=90% 2338
$+ 0.40$) %	—	$\pi^+ \mu^+ \tau^-$	LF	< 6.2	$\times 10^{-5}$ CL=90% 2333
$- 0.32$) %	—	$\pi^+ \mu^- \tau^+$	LF	< 4.5	$\times 10^{-5}$ CL=90% 2333
$+ 0.9$) %	—	$\pi^+ \mu^\pm \tau^\mp$	LF	< 7.2	$\times 10^{-5}$ CL=90% 2333
$- 0.6$) %	—				
$+ 1.1$) %	—				
$- 0.9$) %	—				
± 4) %	—				

B -mesons offer powerful

... and hundreds more, most in excellent agreement with SM!

B-mesons offer powerful

		(10.8 ± 0.4) %	-			n theoretical	
± 1.9) × 10 ⁻⁴	2185	(9.7 ± 0.7) %		2310			
± 0.27) × 10 ⁻⁵	2638	[III] (2.35 ± 0.09) %					
± 0.5) × 10 ⁻⁵	2611						
± 0.8) × 10 ⁻⁵	2553	$\pi^+ \ell^+ \ell^-$	B1	< 4.9	× 10 ⁻⁸	CL=90%	2638
± 0.09) × 10 ⁻⁴	2582	$\pi^+ e^+ e^-$	B1	< 8.0	× 10 ⁻⁸	CL=90%	2638
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+ 2.6 - 2.3) × 10 ⁻⁶	2467	$\pi^+ \nu \bar{\nu}$	B1	< 1.4	× 10 ⁻⁵	CL=90%	2638
	2446	$K^+ \ell^+ \ell^-$	B1	[III] (4.51 ± 0.23)	× 10 ⁻⁷	S=1.1	2617
		$K^+ e^+ e^-$	B1	(5.5 ± 0.7)	× 10 ⁻⁷		2617
				(7.2 ± 0.7)	× 10 ⁻⁷	S=1.2	2612
					× 10 ⁻³	CL=90%	1687
					× 10 ⁻⁵	CL=90%	2617
					× 10 ⁻⁵	CL=90%	2583
					1) × 10 ⁻⁶	S=1.1	2564
					0 1) × 10 ⁻⁶		2564
					(9.0 ± 1.0) × 10 ⁻⁷		2560
		$K^*(892)^+ \nu \bar{\nu}$	B1	< 4.0	× 10 ⁻⁵	CL=90%	2564
		$K^+ \pi^+ \pi^- \mu^+ \mu^-$	B1	(4.3 ± 0.4)	× 10 ⁻⁷		2593
		$\phi K^+ \mu^+ \mu^-$	B1	(7.9 + 2.1 - 1.7)	× 10 ⁻⁸		2490
		$\Lambda p \nu \bar{\nu}$		< 3.0	× 10 ⁻⁵	CL=90%	2430
		$\pi^+ e^+ \mu^-$	LF	< 6.4	× 10 ⁻³	CL=90%	2637
		$\pi^+ e^- \mu^+$	LF	< 6.4	× 10 ⁻³	CL=90%	2637
		$\pi^+ e^\pm \mu^\mp$	LF	< 1.7	× 10 ⁻⁷	CL=90%	2637
		$\pi^+ e^+ \tau^-$	LF	< 7.4	× 10 ⁻⁵	CL=90%	2338
		$\pi^+ e^- \tau^+$	LF	< 2.0	× 10 ⁻⁵	CL=90%	2338
		$\pi^+ e^\pm \tau^\mp$	LF	< 7.5	× 10 ⁻⁵	CL=90%	2338
		$\pi^+ \mu^+ \tau^-$	LF	< 6.2	× 10 ⁻⁵	CL=90%	2333
		$\pi^+ \mu^- \tau^+$	LF	< 4.5	× 10 ⁻⁵	CL=90%	2333
		$\pi^+ \mu^\pm \tau^\mp$	LF	< 7.2	× 10 ⁻⁵	CL=90%	2333

$D^0 X$	(8.6 \pm 0.7) %
$\bar{D}^0 X$	(79 \pm 4) %
$D^+ X$	(2.5 \pm 0.5) %
$D^- X$	(9.9 \pm 1.2) %
$D_s^+ X$	(7.9 \pm 1.4 \pm 1.3) %
$D_s^- X$	(1.10 \pm 0.40 \pm 0.32) %
$\Lambda_c^+ X$	(2.1 \pm 0.9 \pm 0.6) %
$\bar{\Lambda}_c^- X$	(2.8 \pm 1.1 \pm 0.9) %
$\bar{c} X$	(97 \pm 4) %

Observables in $b \rightarrow cl\nu$

$$R_{D^{(*)}} = \frac{\text{BR}(B \rightarrow D^{(*)} \tau \nu)}{\text{BR}(B \rightarrow D^{(*)} \ell \nu)}$$

- **Charged current** tree-level decay
- Theoretically clean: hadronic uncertainties cancel in the ratio

- **SM:** $R_D = 0.299 \pm 0.003$

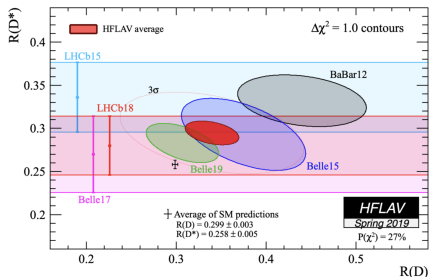
$$R_{D^*} = 0.258 \pm 0.005$$

- **Exp.:** $R_D = 0.340 \pm 0.030$

$$R_{D^*} = 0.295 \pm 0.014$$

⇒ **SM** predictions are **significantly smaller** than experimental results,
(combined) deviation from SM $\sim 3.1\sigma$!

⇒ Violation of **LFU**? New physics coupled to τ ?



Observables in $b \rightarrow sll$

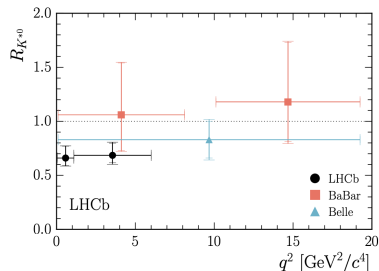
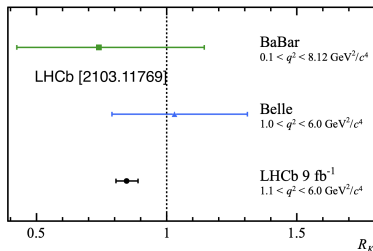
$$R_{K^{(*)}} = \frac{\text{BR}(B \rightarrow K^{(*)} \mu \mu)}{\text{BR}(B \rightarrow K^{(*)} e e)}$$

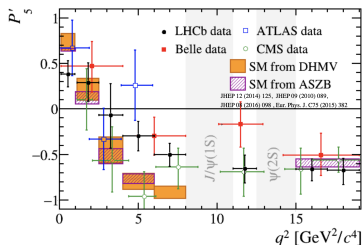
- FCNC penguin decay
- Theoretically clean: hadronic uncertainties cancel in the ratio
- SM: $R_K = R_{K^*} \simeq 1$
- Exp.: $R_K = 0.846^{+0.044}_{-0.041}$ (NEW!)
 $R_{K^*} = 0.69 \pm 0.12$

⇒ First **evidence** for violation of **LFU** @ **3.1 σ** !

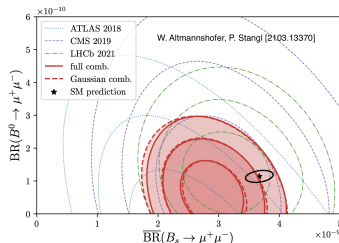
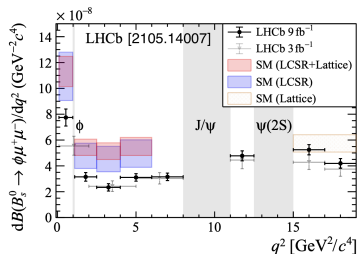
⇒ Strong hint on **new physics** coupled to μ ! (and/or to e)

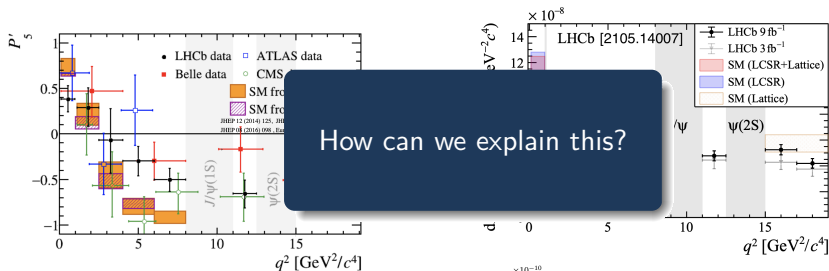
- (Recent measurements of $R_{K_S^0}$ and $R_{K^{*+}}$ corroborate the picture, but too low statistics)



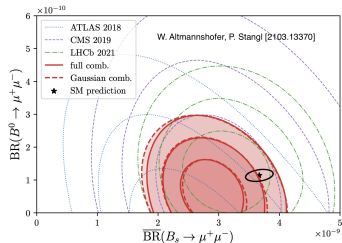
Observables in $b \rightarrow s\mu\mu$ 

- Angular observables and BRs in $B^{+,0} \rightarrow K^* \mu^+ \mu^-$ and $B_s \rightarrow \phi \mu^+ \mu^-$, (local) deviations $2-3\sigma$!
- ATLAS, CMS and LHCb measurements of $\text{BR}(B_{(s)} \rightarrow \mu^+ \mu^-)$ consistent with SM



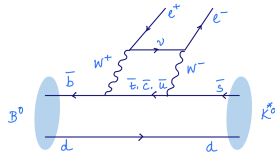
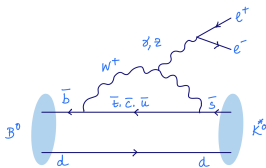
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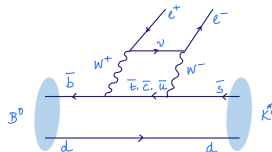
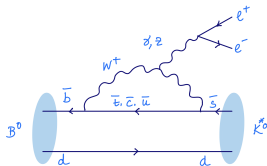
Electroweak penguins in $b \rightarrow sll$

FCNC transitions in the SM are “loop-suppressed”: (e.g. $B^0 \rightarrow K^{0*} \ell^+ \ell^-$)

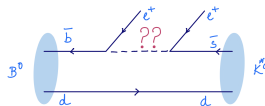
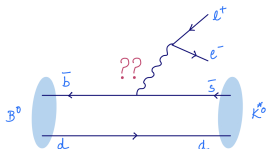


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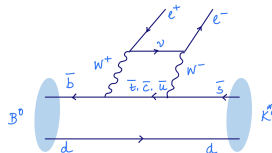
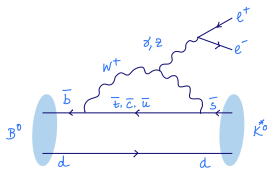


Heavy **BSM** contributions are “mass suppressed” \Rightarrow If required to be large, must be present at *tree-level*:

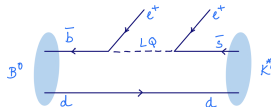
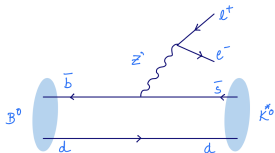


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Z': BSM “cousin” of SM Z -boson

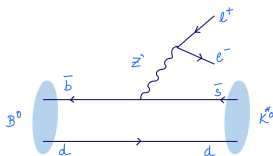
Leptoquarks: scalar or vector fields coupling
leptons to quarks

Electroweak penguins in $b \rightarrow sll$

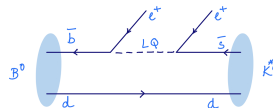
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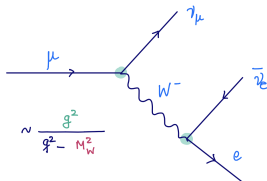


Leptoquarks: scalar or vector fields coupling
leptons to quarks

EFT *intermezzo* I

Effective Field Theory \simeq SM Lagrangian + non-renormalisable operators

Heavy fields are “*integrated out*”: only valid in certain energy regime



EFT *intermezzo* I

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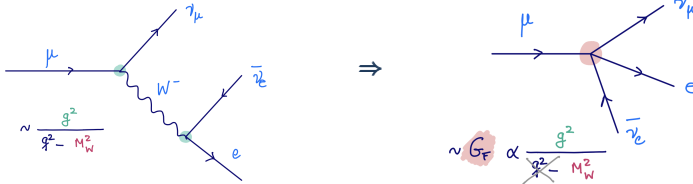


\Rightarrow **Fermi** constant G_F is an *effective* coupling constant

EFT *intermezzo* I

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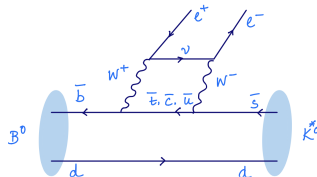
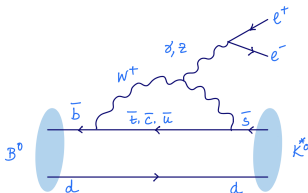
EFT Lagrangian for $b \rightarrow s\ell\ell$: $\mathcal{L}_{\text{eff}} \propto \frac{4G_F}{\sqrt{2}} \sum_k C_k(\mu) \mathcal{O}_k(\mu)$

- Effective operators \mathcal{O}_k are accompanied by **effective coupling constants** C_k (**Wilson coefficients**)
- Couplings run! (depend on energy scale μ)

$$\begin{aligned} \mathcal{O}_7^{ij} &= \frac{e m_{d_j}}{(4\pi)^2} (\bar{d}_i \sigma_{\mu\nu} P_R d_j) F^{\mu\nu}, & \mathcal{O}_9^{ij;\ell\ell'} &= \frac{e^2}{(4\pi)^2} (\bar{d}_i \gamma^\mu P_L d_j) (\bar{\ell} \gamma_\mu \ell'), \\ \mathcal{O}_{10}^{ij;\ell\ell'} &= \frac{e^2}{(4\pi)^2} (\bar{d}_i \gamma^\mu P_L d_j) (\bar{\ell} \gamma_\mu \gamma_5 \ell'), & \mathcal{O}_S^{ij;\ell\ell'} &= \frac{e^2}{(4\pi)^2} (\bar{d}_i P_R d_j) (\bar{\ell} \ell'), \\ \mathcal{O}_P^{ij;\ell\ell'} &= \frac{e^2}{(4\pi)^2} (\bar{d}_i P_R d_j) (\bar{\ell} \gamma_5 \ell'), & \mathcal{O}_T^{ij;\ell\ell'} &= \frac{e^2}{(4\pi)^2} (\bar{d}_i \sigma_{\mu\nu} d_j) (\bar{\ell} \sigma^{\mu\nu} \ell'), \\ \mathcal{O}_{T5}^{ij;\ell\ell'} &= \frac{e^2}{(4\pi)^2} (\bar{d}_i \sigma_{\mu\nu} d_j) (\bar{\ell} \sigma^{\mu\nu} \gamma_5 \ell') \end{aligned}$$

EFT
Effective

He



$$O_7^{ij} = \frac{e m_{d_j}}{(4\pi)^2} (\bar{d}_i \sigma_{\mu\nu} P_R d_j) F^{\mu\nu},$$

$$O_{10}^{ij;\ell\ell'} = \frac{e^2}{(4\pi)^2} (\bar{d}_i \gamma^\mu P_L d_j) (\bar{\ell} \gamma_\mu \gamma_5 \ell')$$

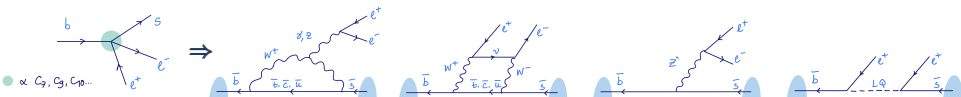
$$O_P^{ij;\ell\ell'} = \frac{e^2}{(4\pi)^2} (\bar{d}_i P_R d_j) (\bar{\ell} \gamma_5 \ell'),$$

$$O_{T5}^{ij;\ell\ell'} = \frac{e^2}{(4\pi)^2} (\bar{d}_i \sigma_{\mu\nu} d_j) (\bar{\ell} \sigma^{\mu\nu} \gamma_5 \ell')$$

$$O_9^{ij;\ell\ell'} = \frac{e^2}{(4\pi)^2} (\bar{d}_i \gamma^\mu P_L d_j) (\bar{\ell} \gamma_\mu \ell')$$

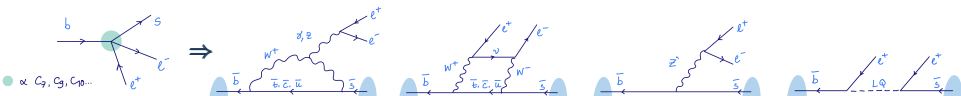
$$O_S^{ij;\ell\ell'} = \frac{e^2}{(4\pi)^2} (\bar{d}_i P_R d_j) (\bar{\ell} \ell'),$$

$$O_T^{ij;\ell\ell'} = \frac{e^2}{(4\pi)^2} (\bar{d}_i \sigma_{\mu\nu} d_j) (\bar{\ell} \sigma^{\mu\nu} \ell'),$$

EFT *intermezzo* II

\Rightarrow All diagrams contribute to the **Wilson** coefficients!

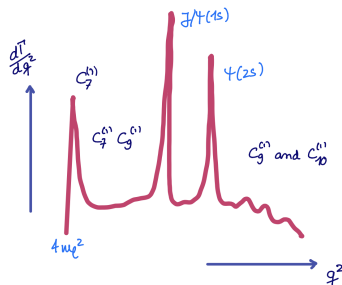
EFT intermezzo II



⇒ All diagrams contribute to the **Wilson** coefficients!

- Different kinematical bins are sensitive on different **Wilson** coefficients

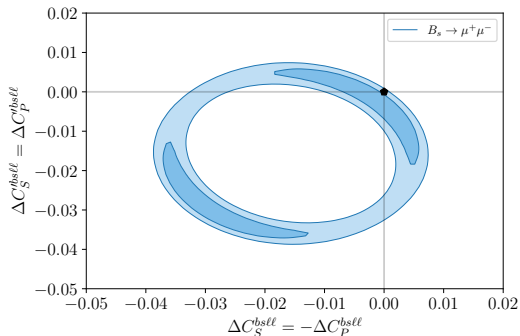
⇒ **Fit** Wilson coefficients on **data** to **discriminate** between new physics scenarios!



Constraints on (pseudo-) scalar operators

Weak effective theory fit @ 4.8 GeV for all $b \rightarrow s\ell\ell$ data:

$C_9^{bs\mu\mu}$	$C_{10}^{bs\mu\mu}$	$C_9^{bs\mu\mu}$	$C_{10}^{bs\mu\mu}$	C_7^{bs}
-1.17 ± 0.16	0.09 ± 0.14	0.41 ± 0.34	-0.19 ± 0.20	0.002 ± 0.014
C_7^{bs}	$C_S^{bs\mu\mu} = -C_P^{bs\mu\mu}$	$C_S^{bs\mu\mu} = C_P^{bs\mu\mu}$	Pull _{SM}	p-value
0.006 ± 0.017	-0.001 ± 0.025	-0.001 ± 0.025	5.8	49.7%

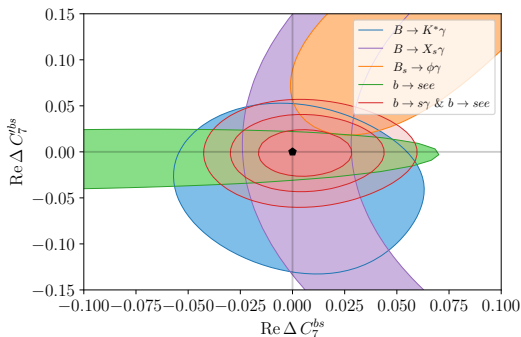


- Primed operators:
right-handed quark current, vanishing in SM
- Scalar and pseudo-scalar operators tightly constrained by $B_s \rightarrow \mu^+ \mu^-$ and effective lifetime, consistent with 0

Constraints on dipoles

Weak effective theory fit @ 4.8 GeV for all $b \rightarrow sll$ data:

C_9	C_{10}	C'_9	C'_{10}	C_7	C'_7	Pull _{SM}
$1.18^{+0.17}_{-0.16}$	$0.11^{+0.15}_{-0.14}$	$0.34^{+0.33}_{-0.33}$	$-0.25^{+0.18}_{-0.17}$	$0.001^{+0.014}_{-0.014}$	$0.005^{+0.014}_{-0.014}$	6.1



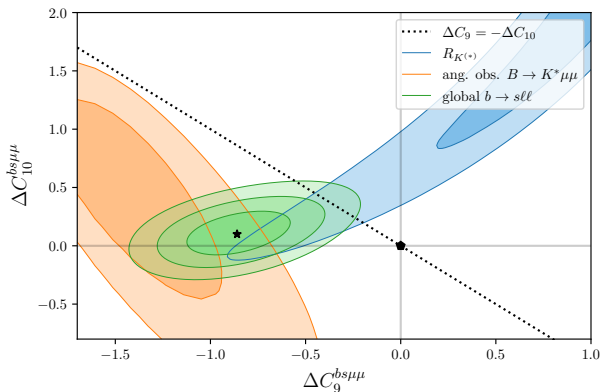
- Primed operators: **right-handed** quark current, vanishing in SM
- Dipole coefficients tightly constrained by $b \rightarrow s\gamma$ and $b \rightarrow see$, consistent with 0

DISCLAIMER: take pulls with a grain of salt, only a taste of how things are moving qualitatively...

C_9 vs C_{10}

Add **BSM** to **SM** contribution in LH **V** and **A** currents (SM: $C_9 \approx -C_{10} \rightsquigarrow V - A$)

\Rightarrow best fit: $\Delta C_9^{bs\mu\mu} = -0.86^{+0.18}_{-0.17}$, $\Delta C_{10}^{bs\mu\mu} = 0.10^{+0.12}_{-0.12}$, $\text{Pull}_{\text{SM}} = 5.8$



◇: SM

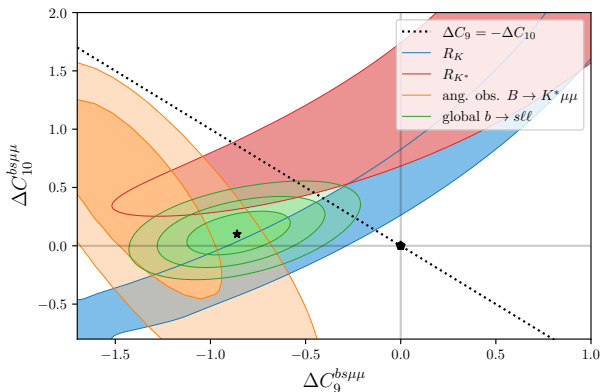
★: best fit
small tension between
 R_K and R_{K^*} with ang.
obs.

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◇: SM

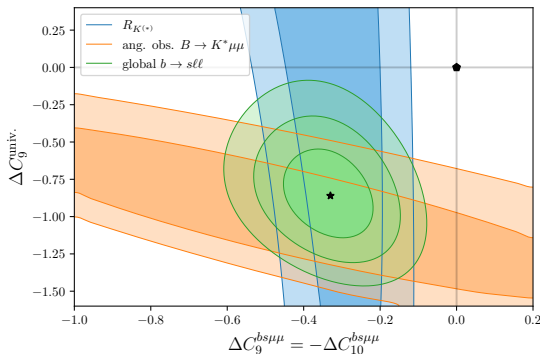
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$$C_9 \equiv -C_{10} \text{ vs } C_9^{\text{univ.}}$$

First considered in Alguéro et.al. [1809.08447]: $C_9^{b\text{see}} = \Delta C_9^{\text{univ.}}$, $C_9^{bs\mu\mu} = \Delta C_9^{bs\mu\mu} + \Delta C_9^{\text{univ.}}$.

\Rightarrow best fit: $\Delta C_9^{bs\mu\mu} = -\Delta C_{10}^{bs\mu\mu} = -0.33^{+0.08}_{-0.08}$, $\Delta C_9^{\text{univ.}} = -0.86^{+0.19}_{-0.17}$, $\text{Pull}_{\text{SM}} = 6.4$



◇: SM

★: best fit



$C_9^{\text{univ.}}$ can be **RG**
running induced
(e.g. from large $C_9^{bst\tau\tau}$)
 $\leadsto R_{D^{(*)}}?$

Unknown $c\bar{c}$ corr. can mimic $C_9^{\text{univ.}} \Rightarrow$ Lancerini et. al. [2104.05631]: **4.3σ** significance (with LEE)

DISCLAIMER: take pulls with a grain of salt, only a taste of how things are moving qualitatively...

RG tales from the SMEFT

Consider Standard Model EFT (**SMEFT**) at $\Lambda_{\text{NP}} \sim \mathcal{O}(\text{TeV}) \gg \Lambda_{\text{EW}}$

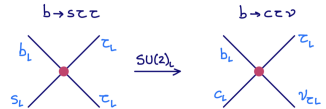
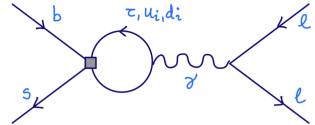
Semileptonic operators:

$SU(2)_L$ -**singlet**: $(C_1)_{\ell q}^{ijmn} (\bar{L}_i \gamma_\mu L_j) (\bar{Q}_m \gamma^\mu Q_n)$

$SU(2)_L$ -**triplet**: $(C_3)_{\ell q}^{ijmn} (\bar{L}_i \gamma_\mu \tau_a L_j) (\bar{Q}_m \gamma^\mu \tau_a Q_n)$

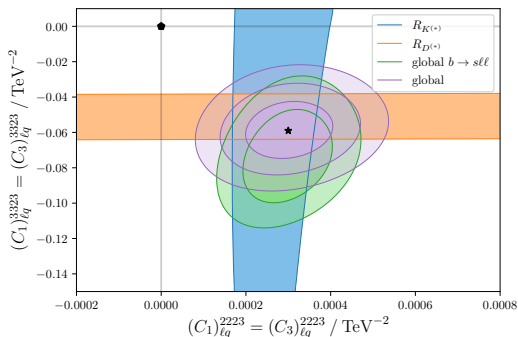
Tree-level matching SMEFT \rightarrow WET:

- $C_9^{bs\mu\mu} = -C_{10}^{bs\mu\mu} \propto (C_1)_{\ell q}^{2223} + (C_3)_{\ell q}^{2223}$
- $R_{D^{(*)}} \propto (C_3)_{\ell q}^{3323}$; also leads to $C_9^{bs\tau\tau} = -C_{10}^{bs\tau\tau}$ and under RG running to $C_9^{\text{univ.}}$
- Require $(C_1)_{\ell q}^{\ell\ell 23} = (C_3)_{\ell q}^{\ell\ell 23}$ to evade constraints from $B \rightarrow K^{(*)} \nu \bar{\nu}$!



SMEFT @ 2 TeV: $(C_1)_{\ell q}^{2223} = (C_3)_{\ell q}^{2223}$ vs $(C_1)_{\ell q}^{3323} = (C_3)_{\ell q}^{3323}$
 $(C_1)_{\ell q}^{3323} = (C_3)_{\ell q}^{3323} \Rightarrow$ large $C_9^{b s \tau \tau}$ via $SU(2)_L$ invariance \Rightarrow RGE induced $C_9^{\text{univ.}}$

best fit: $(C_{1,3})_{\ell q}^{2223} = (3.0_{-0.6}^{+0.7}) \times 10^{-4} \text{ TeV}^{-2}$, $(C_{1,3})_{\ell q}^{3323} = -0.059_{-0.01}^{+0.01} \text{ TeV}^{-2}$, $\text{Pull}_{\text{SM}} = 7.4$



☆: SM

★: best fit

Massive enhancement of
 $b \rightarrow s \tau \tau$ processes; for example:
 $\text{BR}(B_s \rightarrow \tau^+ \tau^-)_{\text{SMEFT}} \simeq 10^3 \times \text{SM}$
 Capdevila et. al. [1712.01919]

Candidate model: $V_1 \sim (\mathbf{3}, \mathbf{1}, 2/3)$ vector **leptoquark** (e.g. Buttazzo et. al. [1706.07808])

Global likelihood now also contains $R_{D^{(*)}}$ and binned data for $\text{BR}(B \rightarrow D^{(*)} \ell \nu)$!

Requirements on (minimal) single-particle BSM explanations

- $b \rightarrow s\ell\ell$ requires **FCNC** at *tree*-level (competing with SM at 1-loop)
- $b \rightarrow c\ell\nu$ requires **charged** current at *tree*-level (competing with SM at *tree*-level)
- ⇒ Single particle explanations need very different couplings,
for $b \rightarrow c\ell\nu$ a low mass is required $\mathcal{O}(\text{TeV})$
- ⇒ Expect stringent constraints from **cLFV** observables (e.g. $B \rightarrow K\tau\mu$)
- Heavy Z' can explain **only** $b \rightarrow s\ell\ell$, most models ruled out by $B_s - \bar{B}_s$ mixing
- Scalar $SU(2)_L$ -singlet leptoquark S_1 : **only** $b \rightarrow c\ell\nu$
- Scalar $SU(2)_L$ -triplet leptoquark S_3 : **only** $b \rightarrow s\ell\ell$
- Vector $SU(2)_L$ -triplet leptoquark V_3 : ruled out by $B \rightarrow K\nu\bar{\nu}$
- ⇒ **Vector $SU(2)_L$ -singlet leptoquark V_1** : explains **both** anomalies,
but heavily constrained from **cLFV**!

Extensive list of dedicated analyses, $\mathcal{O}(10^{23})$ relevant contributions...

Other approaches rely on more non-minimal field content (e.g. “4321”-models [EPJC 79(2019)4, 334], PS³ [PLB 779(2018)317], RPV SUSY [PRD 102(2020)1, 015031] ...)

Conclusions and outlook

First **evidence** for **LFUV** in R_K !

- Waiting for R_{K^*} updates...
 - Patterns of deviations in several $b \rightarrow s\mu\mu$ draw a more and more clear (and consistent) picture
 - Slight tension between $R_{K^*} < R_K$ and $b \rightarrow s\mu\mu$ can be reduced by considering $C_9^{\text{univ.}}$
- ⇒ $C_9^{\text{univ.}}$ can be RG running induced; connection to $R_{D^{(*)}}$?
- ⇒ “Combined explanation” implies large $b \rightarrow s\tau\tau$
- SM extensions via V_1 -leptoquark offer viable explanations for both B -decay anomalies
 - Large region of the **parameter space** to be probed in the near **future!**



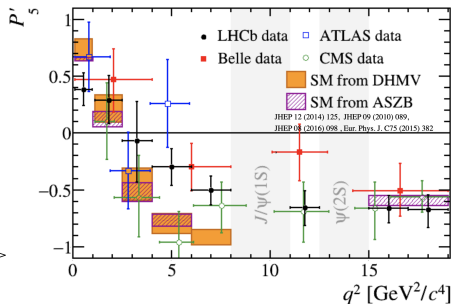
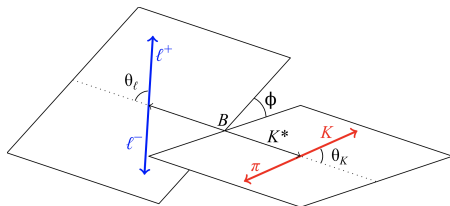
Thank you!!!



Bonus slides



Angular observables

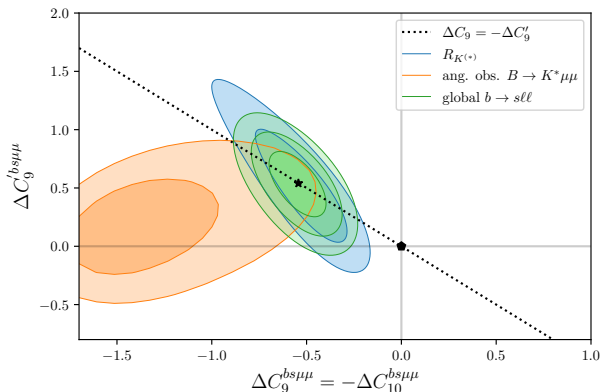


Statistical setup

Likelihoods: $-2\Delta \log \mathcal{L} \approx \mathcal{O}^T (\mathcal{C}_{\text{exp}} + \mathcal{C}_{\text{theo}})^{-1} \mathcal{O}$ (see e.g. [smelli \[arXiv:1810.07698\]](#))
all observables (and their uncertainties) calculated with **flavio**

- **New/updated measurements:**
 - $R_K, q^2 \in [1.1, 6.0] \text{ GeV}^2$
 - $\text{BR}(B^+ \rightarrow K^+ e^+ e^-), q^2 \in [1.1, 6.0] \text{ GeV}^2$
 - Updated measurement of $\text{BR}(B_{(s)} \rightarrow \mu^+ \mu^-)$
 - Angular data and binned BRs in $B_s \rightarrow \phi \mu^+ \mu^-$
- Other **observables** included:
 - $R_{K^{(*)}}$ measurements by LHCb, BaBar and Belle
 - Angular LFU Q_4, Q_5 measured by Belle
 - Angular data in $B^{+,0} \rightarrow K^* \mu^+ \mu^-$
 - Angular data in $B^0 \rightarrow K^* e^+ e^-$
 - (Binned) BR's of $B \rightarrow K^{(*)} \mu^+ \mu^-$
 - $\text{BR}(B \rightarrow K^* \gamma), \text{BR}(B_s \rightarrow \phi \gamma), \text{BR}(B \rightarrow X_s \gamma)$

DISCLAIMER: take absolute values of pulls with a grain of salt, only a taste of how things are moving qualitatively...

$C_9 = -C_{10}$ vs C_9' Add RH (quark) V current C_9' to $C_9 = -C_{10}$ \Rightarrow best fit: $\Delta C_9^{bs\mu\mu} = -\Delta C_{10}^{bs\mu\mu} = -0.54_{-0.10}^{+0.10}$, $\Delta C_9'^{bs\mu\mu} = 0.53_{-0.18}^{+0.18}$, $\text{Pull}_{\text{SM}} = 6.0$ 

◇: SM

★: best fit

Better, but ang. obs. vs.

 $R_{K^{(*)}}$ still not fully
reconciled...

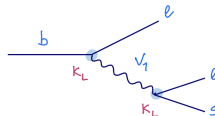
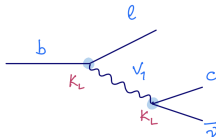
DISCLAIMER: take pulls with a grain of salt, only a taste of how things are moving qualitatively...

V_1 vector leptoquark

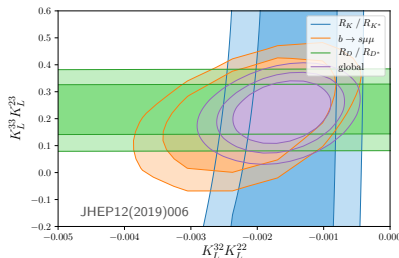
Leptoquarks: scalar or vector fields coupling **leptons** to **quarks** (typically arise in GUTs)

$$\text{Leptoquark Lagrangian: } \mathcal{L} \supset V_1^\mu \left(\bar{d}_L^i \gamma_\mu K_L^{ik} \ell_L^k + \bar{u}_L^j V_{ji}^\dagger \gamma_\mu K_L^{ik} U_{kj}^P \nu_L^j \right)$$

Both $b \rightarrow c \ell \nu$ and $b \rightarrow s \ell \ell$ at *tree-level*:



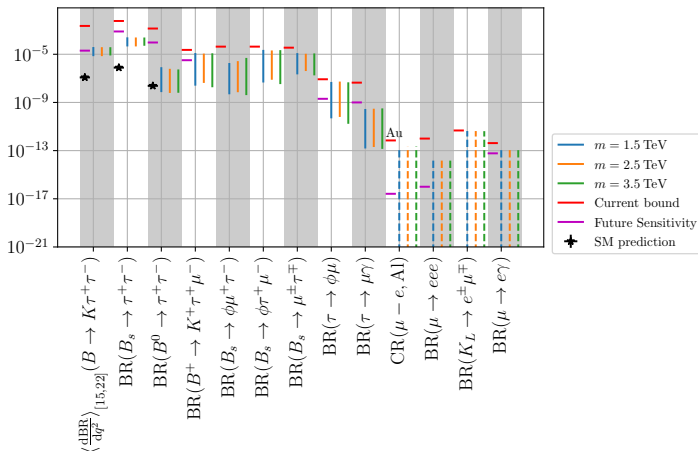
- $K_L^{23} K_L^{33}$ contributes to $b \rightarrow c \ell \nu$ and $b \rightarrow s \tau \tau$
- (Large) $C_9^{bs\tau\tau}$ feeds universally into $C_9^{bs\mu\mu}$ and C_9^{bsee} (RG running)
 $\Rightarrow \Delta C_9^{\text{univ.}}$



LFV Prospects

What does the future hold?

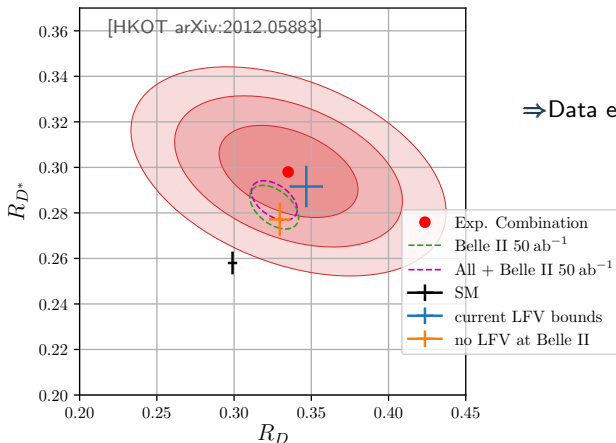
⇒ Fit of 9 **LQ** couplings ⇒ MCMC posterior distributions:



Prospects for $R_{D(*)}$

BELLE II will improve sensitivities in several b and τ decay channels!

Fit of 9 LQ couplings:



⇒ Data evolution of $R_{D(*)}$ is crucial!

Non-universality from universal gauge interactions

Gauge couplings are strictly universal; how to explain **LFU Violation**?

⇒ Only unitary **$q\ell$** mass misalignment is ruled out by **LFV**

► Add **n vector-like (VL) leptons** mixing with (left-handed) SM leptons

effective LQ- $q\ell$ couplings $K_L^{q\ell}$ parametrised via **non-unitary matrix**
(from mixing with heavy states)

⇒ Induce **LFUV structure** in $C_{9,10}^{ij;\ell\ell'}$ **Wilson coefficients** (*tree-level*)

$$C_{9,10}^{ij;\ell\ell'} = \mp \frac{\pi}{\sqrt{2}G_F \alpha V_{3j} V_{3i}^*} \frac{1}{m_{V_1}^2} K_L^{i\ell'} K_L^{j\ell'*}$$

⇒ Required mixing pattern: induce non-universal $Z \rightarrow \ell\ell^{(\prime)}$ (*at tree-level*)

↪ VL leptons have to be **$SU(2)_L$ -doublets!!**

⇒ **$R_{K^{(*)}}$** and **$R_{D^{(*)}}$** can be explained, tight constraints from **cLFV**, **EWPO**, colliders...

Non-unitary parametrisation

In analogy to neutrino physics, the mixing matrices get enlarged:

$$U_L^\ell = \begin{pmatrix} A & R \\ B & S \end{pmatrix} \begin{pmatrix} V_0 & \mathbf{0} \\ \mathbf{0} & 1 \end{pmatrix}$$

In case of $n = 3$ generations:

$$\begin{pmatrix} A & R \\ B & S \end{pmatrix} = \mathcal{R}_{56} \mathcal{R}_{46} \mathcal{R}_{36} \mathcal{R}_{26} \mathcal{R}_{16} \mathcal{R}_{45} \mathcal{R}_{35} \mathcal{R}_{25} \mathcal{R}_{15} \mathcal{R}_{34} \mathcal{R}_{24} \mathcal{R}_{14}$$

$$\begin{pmatrix} V_0 & \mathbf{0} \\ \mathbf{0} & 1 \end{pmatrix} = \mathcal{R}_{23} \mathcal{R}_{13} \mathcal{R}_{12}$$

Defining **semi-unitary** rectangular matrix:

$$K_L^{q\ell} = (K_1, K_2) = \frac{\kappa_L}{\sqrt{2}} (A V_0, R)$$